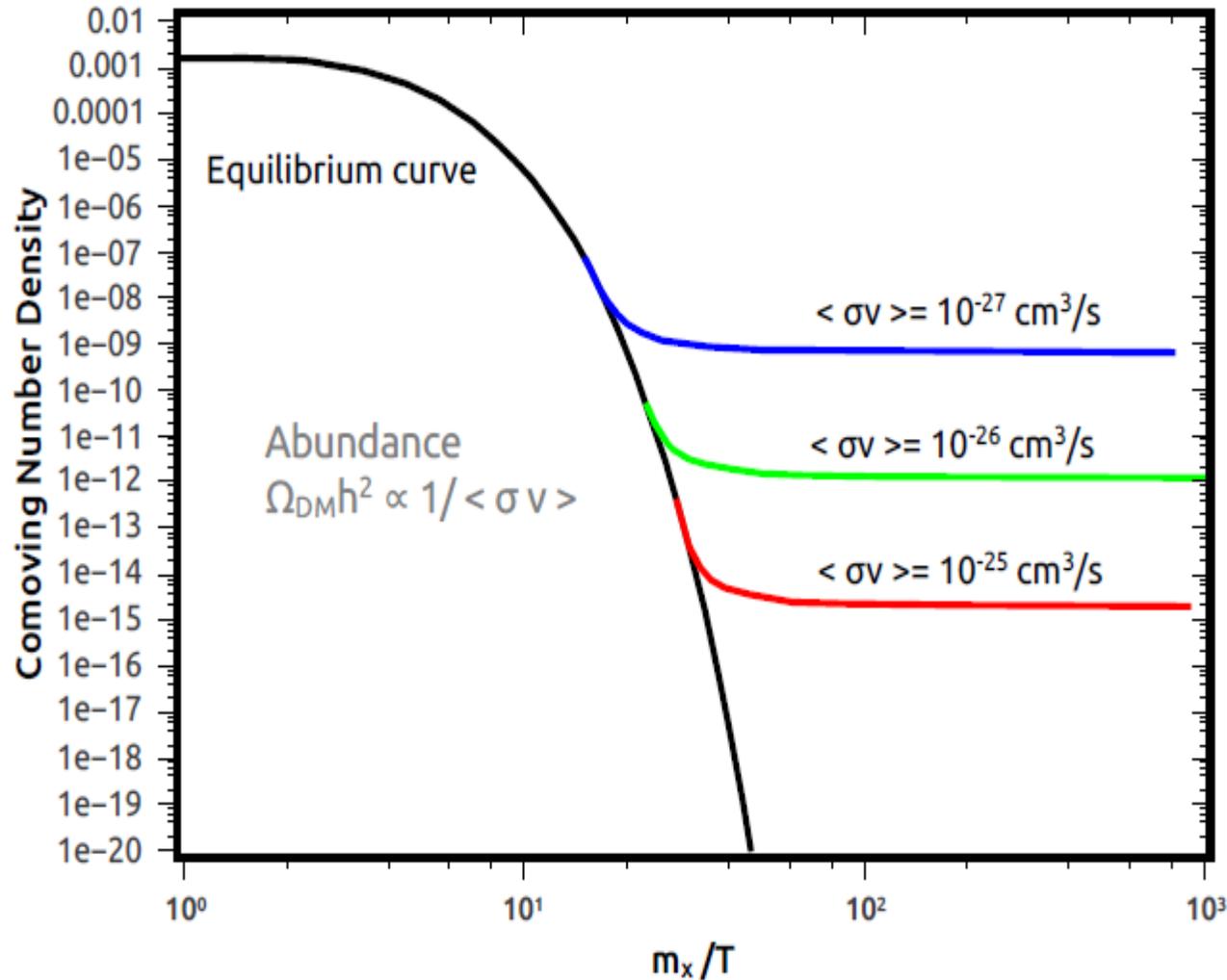


From Simplified to Gauge Invariant Realizations of a Light Pseudoscalar Portal

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WIMP Paradigm

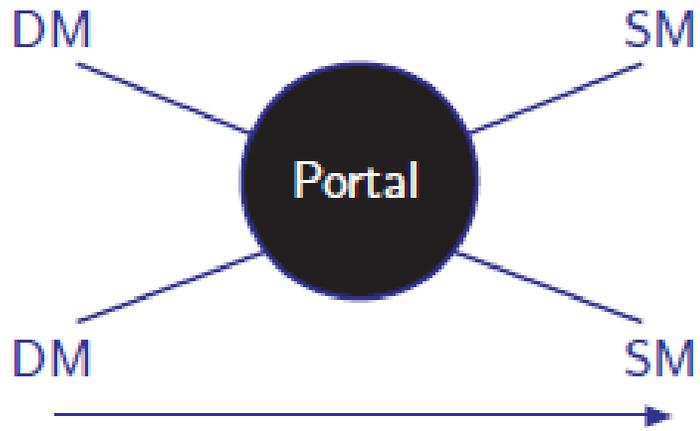


$$\frac{dn}{dt} = -3Hn - \langle \sigma_{\text{ann}} v \rangle (n^2 - n_{\text{eq}}^2)$$

$$\frac{dY}{dx} = \frac{1}{3H} \frac{ds}{dx} \langle \sigma v \rangle (Y^2 - Y_{\text{eq}}^2)$$

$$\Omega h^2 \theta^{-3} \approx 8.7661 \times 10^{-11} \text{ GeV}^{-2} \left[\frac{1}{g_{\text{eff}}}^{1/2} \int_{T_0}^{T_f} \langle \sigma v_{\text{Mol}} \rangle \frac{dT}{m} \right]^{-1}$$

$$\langle \sigma v \rangle = a + bv^2$$



Relic Density

$$\langle \sigma v \rangle \approx \frac{\lambda_f^2 \lambda_\chi^2 m_\chi^2}{(4m_\chi^2 - m_{\text{med}}^2)^2} (a + bv_{\text{f.o}}^2)$$

$$v_{\text{f.o}} \sim 0.3$$

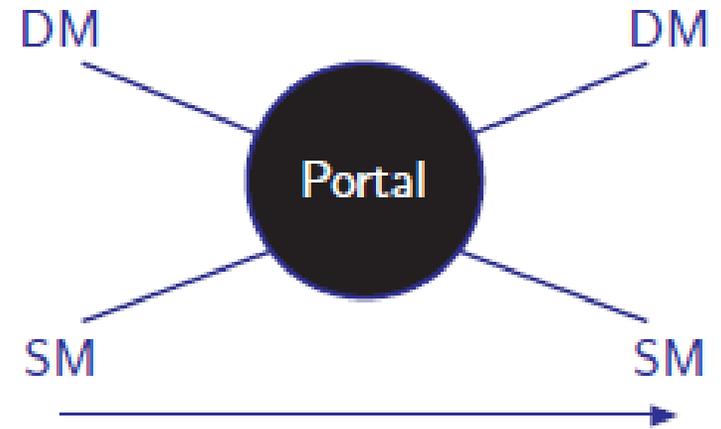
Indirect Detection

$$\langle \sigma v \rangle \approx \frac{\lambda_f^2 \lambda_\chi^2 m_\chi^2}{(4m_\chi^2 - m_{\text{med}}^2)^2} (a + bv_{\text{now}}^2)$$

$$v_{\text{now}} \sim 10^{-3}$$

s-wave

p-wave



$$\sigma_{\chi N} = \frac{\mu_{\chi N}^2 \lambda_\chi^2}{\pi m_{\text{med}}^4} f(\lambda_q)$$

Dark portal examples

$$\mathcal{L} = \xi \mu_\chi^S \chi \chi S + \xi \lambda_\chi^{S^2} |\chi|^2 |S|^2 + \frac{c_S}{\sqrt{2}} \frac{m_f}{v_h} \bar{f} f S$$

$$\mathcal{L} = \xi g_\psi \bar{\psi} \psi S + \frac{c_S}{\sqrt{2}} \frac{m_f}{v_h} \bar{f} f S$$

← Spin-0 mediator

$$\mathcal{L} = -i \lambda_\psi^a \bar{\psi} \gamma_5 \psi a - i \sum_f \frac{c_a}{\sqrt{2}} \frac{m_f}{v_h} \bar{f} \gamma_5 f a$$

Spin-1 mediator

$$\mathcal{L} = m_V \eta_V^S V^\mu V_\mu S + \frac{1}{2} \eta_S^{V^2} V^\mu V_\mu S S + \frac{c_S}{\sqrt{2}} \frac{m_f}{v_h} S \bar{f} f$$

$$\mathcal{L} = i g' \lambda_\chi^{Z'} (\chi^* \partial_\mu \chi - \chi \partial_\mu \chi^*) Z'^\mu + g'^2 \lambda_\chi^{Z'^2} \chi \chi^* Z'_\mu Z'^\mu + g' \sum_f \bar{f} \gamma^\mu (V_f^{Z'} - A_f^{Z'} \gamma_5) f Z'_\mu$$

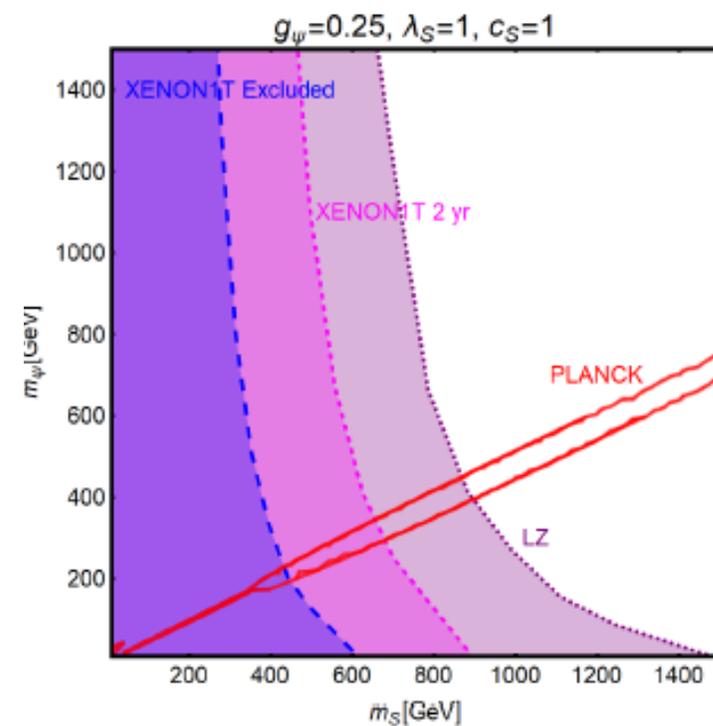
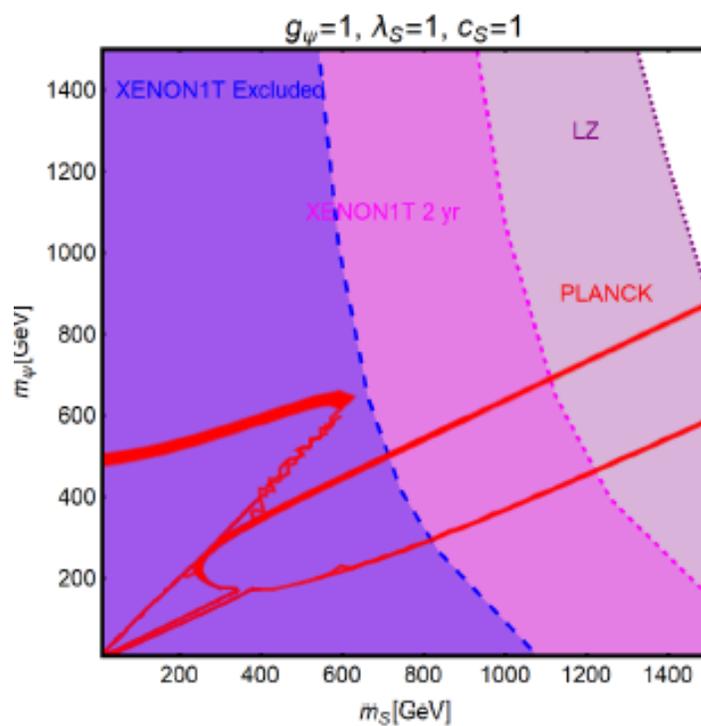
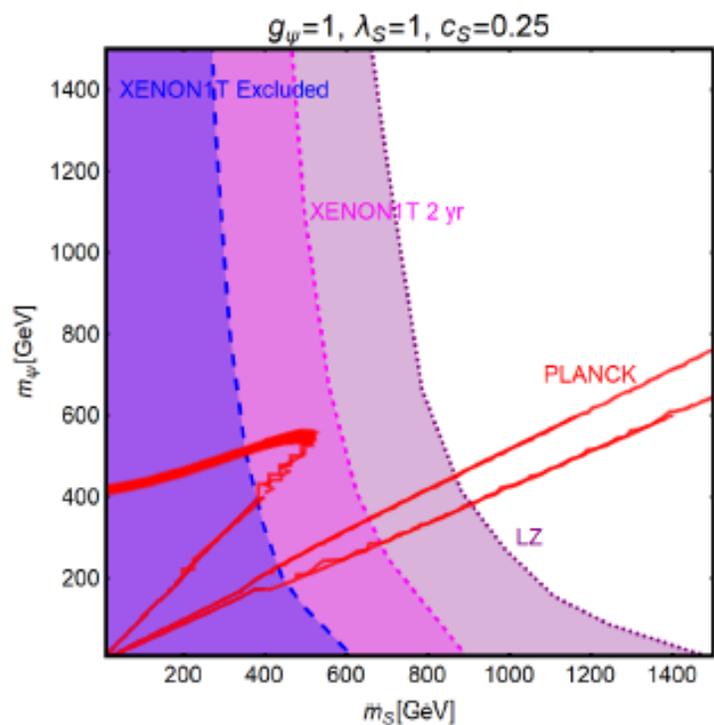
$$\mathcal{L} = g' \xi \bar{\psi} \left(\boxed{V_\psi^{Z'}} - A_\psi^{Z'} \gamma_5 \right) \psi Z'^\mu + g' \sum_f \bar{f} \gamma^\mu (V_f^{Z'} - A_f^{Z'} \gamma_5) f Z'_\mu$$

→ Not present for Majorana fermions

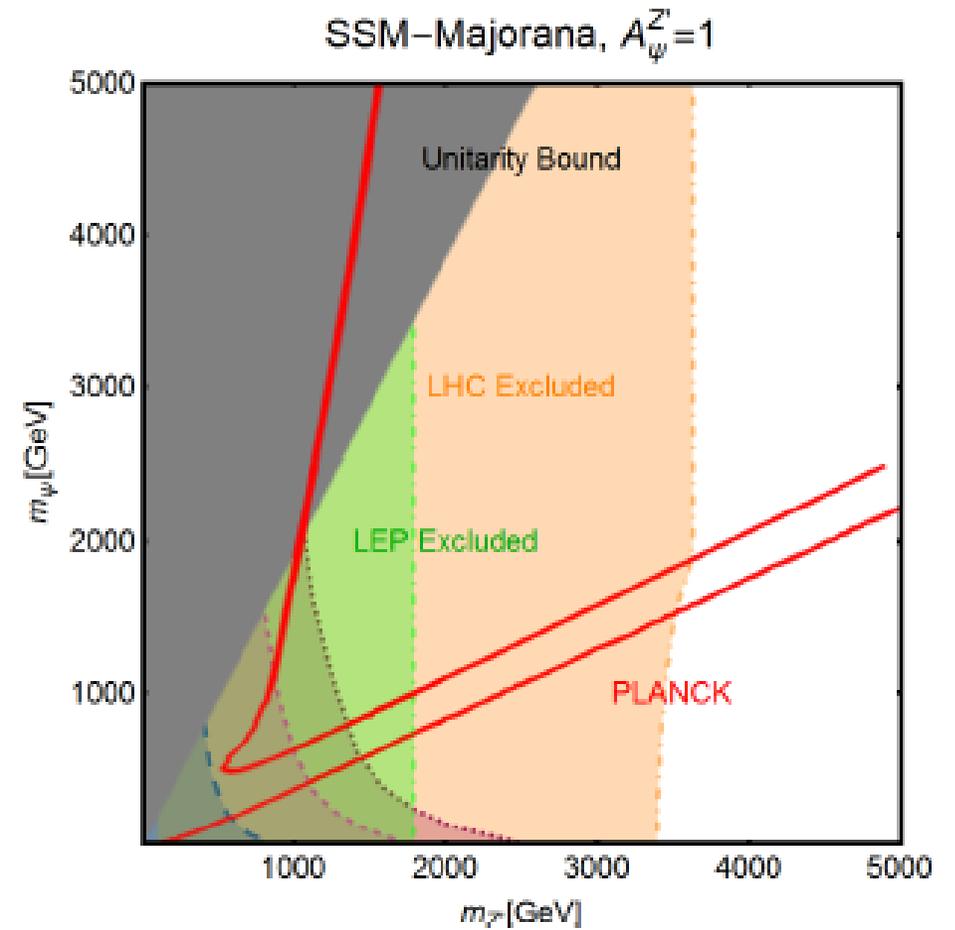
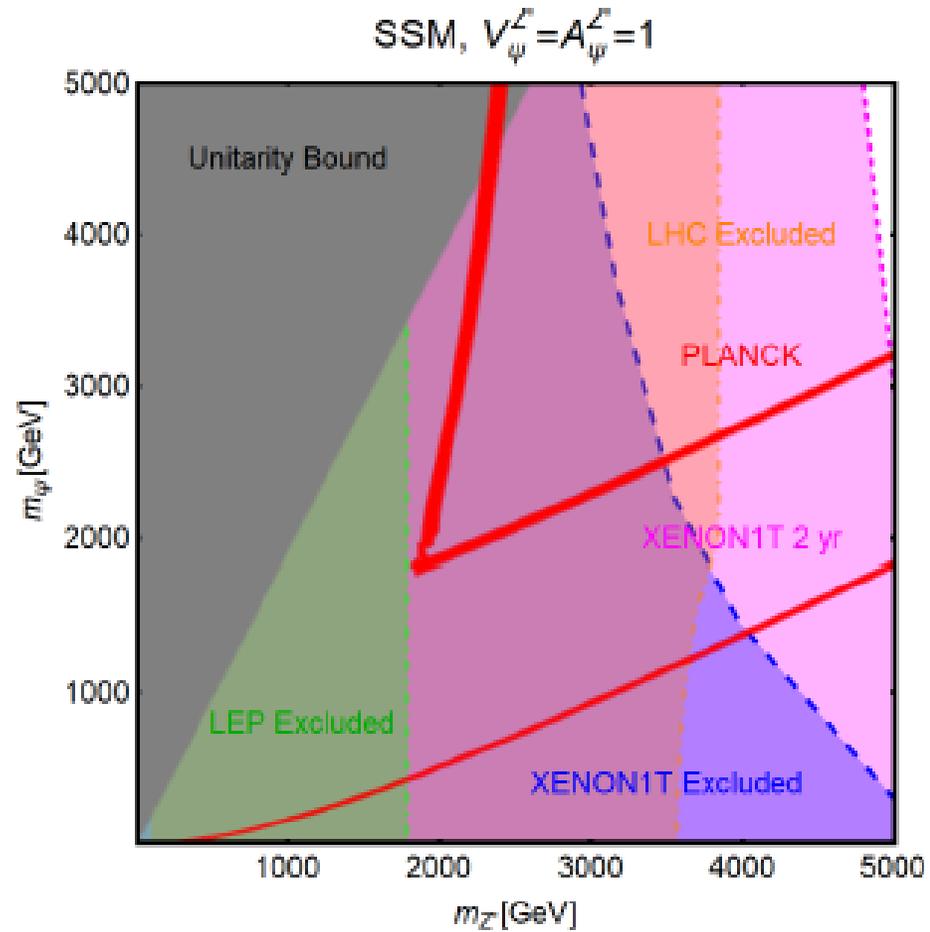
$$\mathcal{L} = g \eta_V^{Z'} [[V V Z]] + \bar{f} \gamma^\mu (V_f^{Z'} - A_f^{Z'} \gamma_5) f Z'_\mu$$

(Real) Scalar mediator

Arcadi et al. 1703.07364



Vector mediator



Achieve sizable DM annihilation cross-section with suppressed scattering cross-section on nuclei (not exhaustive list):

- **Accidental** cancellations (“Blind Spots”)
- “Natural” suppression of the scattering cross-section, e.g. dependence on the momentum transfer (radiative corrections can be relevant though)
- Break of the correlation between Direct Detection and relic density, i.e. presence of additional annihilation channels do not influencing Direct Detection.

CP-violation is required

<i>DM bilinear</i>	<i>SM fermion bilinear</i>			
<i>fermion DM</i>	$\bar{f}f$	$\bar{f}\gamma^5 f$	$\bar{f}\gamma^\mu f$	$\bar{f}\gamma^\mu\gamma^5 f$
$\bar{\chi}\chi$	$\sigma v \sim v^2, \sigma_{\text{SI}} \sim 1$	$\sigma v \sim v^2, \sigma_{\text{SD}} \sim q^2$	–	–
$\bar{\chi}\gamma^5\chi$	$\sigma v \sim 1, \sigma_{\text{SI}} \sim q^2$	$\sigma v \sim 1, \sigma_{\text{SD}} \sim q^4$	–	–
$\bar{\chi}\gamma^\mu\chi$ (Dirac only)	–	–	$\sigma v \sim 1, \sigma_{\text{SI}} \sim 1$	$\sigma v \sim 1, \sigma_{\text{SD}} \sim v_\perp^2$
$\bar{\chi}\gamma^\mu\gamma^5\chi$	–	–	$\sigma v \sim v^2, \sigma_{\text{SI}} \sim v_\perp^2$	$\sigma v \sim 1, \sigma_{\text{SD}} \sim 1$

Radiative corrections relevant

<i>DM bilinear</i>	<i>SM fermion bilinear</i>			
<i>scalar DM</i>	$\bar{f}f$	$\bar{f}\gamma^5 f$	$\bar{f}\gamma^\mu f$	$\bar{f}\gamma^\mu\gamma^5 f$
$\phi^\dagger\phi$	$\sigma v \sim 1, \sigma_{\text{SI}} \sim 1$	$\sigma v \sim 1, \sigma_{\text{SD}} \sim q^2$	–	–
$\phi^\dagger\overleftrightarrow{\partial}_\mu\phi$ (complex only)	–	–	$\sigma v \sim v^2, \sigma_{\text{SI}} \sim 1$	$\sigma v \sim v^2, \sigma_{\text{SD}} \sim v_\perp^2$
<i>vector DM</i>	$\bar{f}f$	$\bar{f}\gamma^5 f$	$\bar{f}\gamma^\mu f$	$\bar{f}\gamma^\mu\gamma^5 f$
$X^\mu X_\mu^\dagger$	$\sigma v \sim 1, \sigma_{\text{SI}} \sim 1$	$\sigma v \sim 1, \sigma_{\text{SD}} \sim q^2$	–	–
$X^\nu\partial_\nu X_\mu^\dagger$	–	–	$\sigma v \sim v^2, \sigma_{\text{SI}} \sim q^2 \cdot v_\perp^2$	$\sigma v \sim v^2, \sigma_{\text{SD}} \sim q^2$

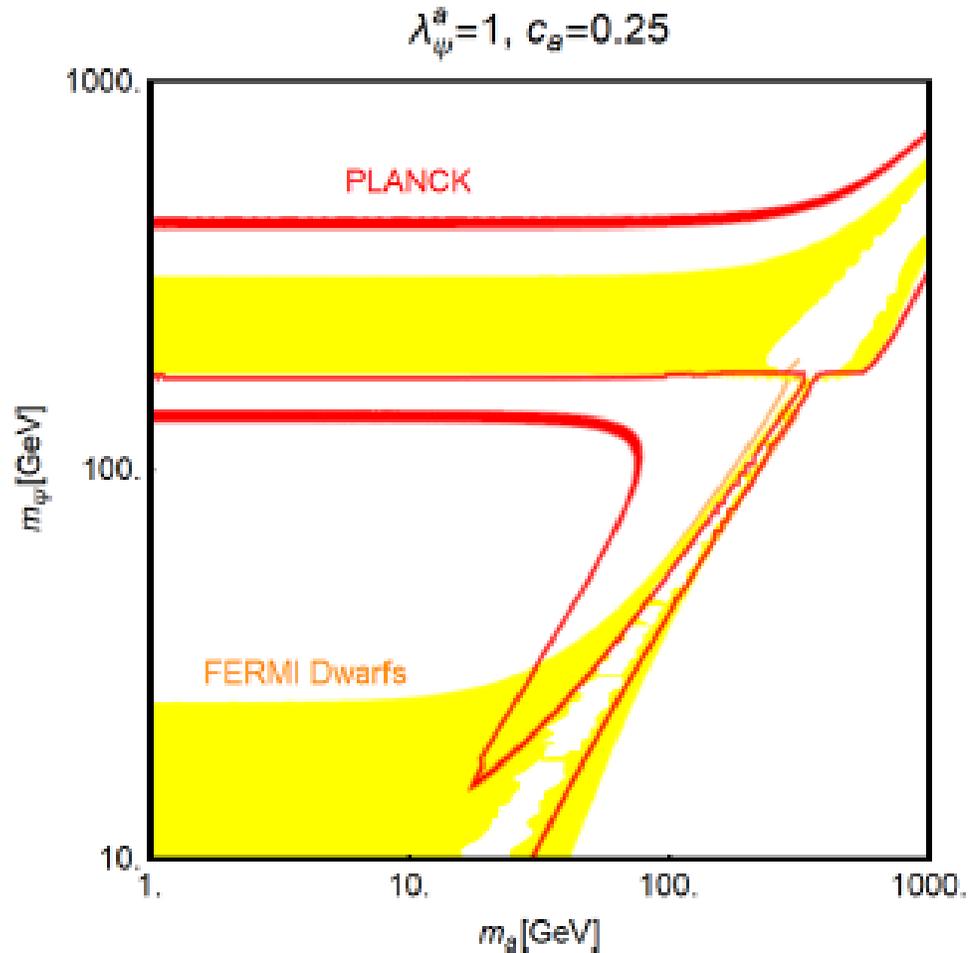
(Berlin et al 1404.0022)

(Light) Pseudoscalar mediator

$$\mathcal{L} = -i\lambda_\psi^a \bar{\psi} \gamma_5 \psi a - i \sum_f \frac{c_a}{\sqrt{2}} \frac{m_f}{v_h} \bar{f} \gamma_5 f a.$$

(see also Arina et al 1406.5542, Bauer et al. 1701.07427,1712.06597)

s-wave cross-section into SM fermions



$$\langle \sigma v \rangle (\bar{\psi} \psi \rightarrow \bar{f} f) \approx \sum_f \frac{n_c^f c_a^2 (\lambda_\psi^a)^2 m_f^2}{2\pi v_h^2} \times \begin{cases} \frac{m_\psi^2}{m_a^4} & \text{for } m_\psi < m_a \\ \frac{1}{16m_\psi^2} & \text{for } m_\psi > m_a \end{cases}$$

$$\langle \sigma v \rangle (\bar{\psi} \psi \rightarrow a a) \approx \frac{(\lambda_\psi^a)^2}{192\pi m_\psi^2} v^2$$

Scattering cross-section on nuclei suppressed (at tree level) by the fourth power of momentum transfer.

Tree level DM scattering cross-section suppressed

For a review Cirelli et al arXiv:1307.5955

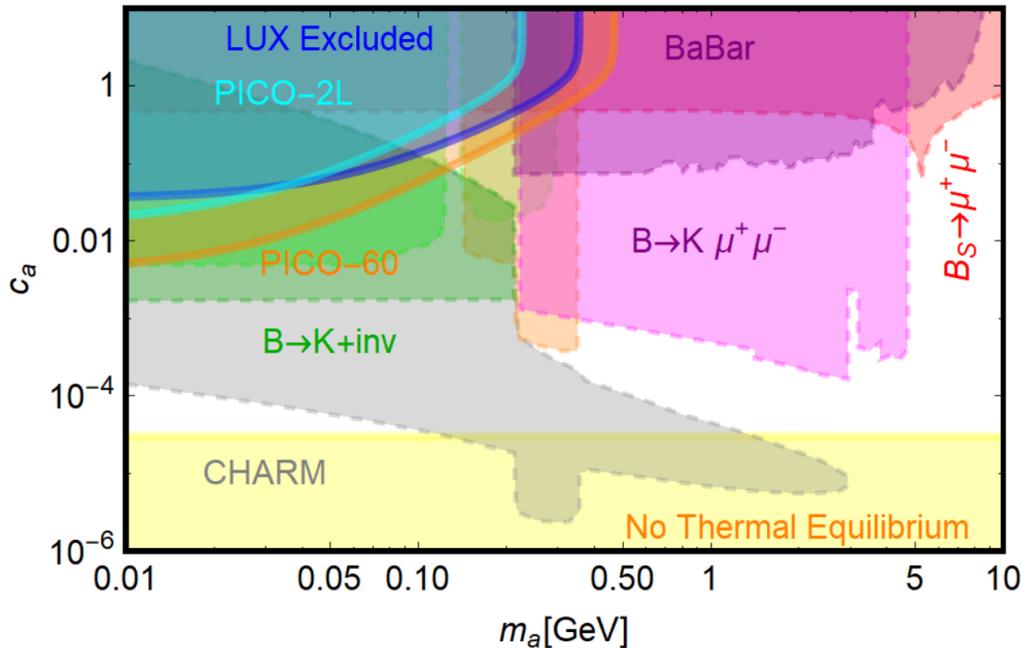
$$\mathcal{L} = g_\chi \bar{\chi} \gamma_5 \chi a + c_a \frac{m_q}{v_h} \bar{q} \gamma_5 q a \longrightarrow \frac{4g_\chi c_a g_N}{m_a^2} \mathcal{O}_6^{\text{NR}}$$

$$\mathcal{O}_6^{\text{NR}} = (\vec{s}_\chi \cdot \vec{q})(\vec{s}_N \cdot \vec{q})$$

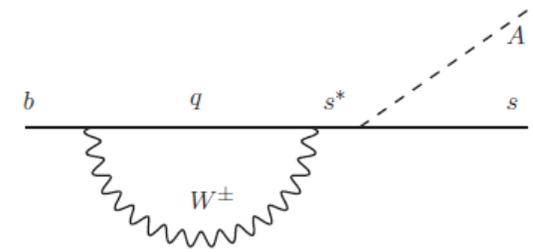
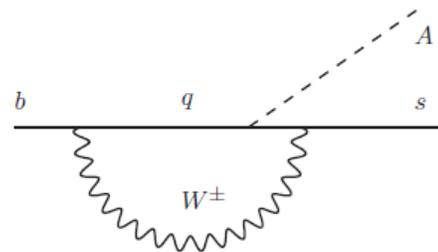
$$\frac{d\sigma}{dE_T} = \frac{g_\chi^2 c_a^2}{128\pi} \frac{q^2}{m_a^2} \frac{m_T^2}{m_\chi m_N} \frac{1}{v_E^2} \sum_{N,N'} F_{\Sigma''}^{NN'}(q^2)$$

$$g_N = \sum_{q=u,d,s} \frac{m_N}{v_h} \left(1 - \frac{\bar{m}}{m_q}\right) \Delta_q^N$$

$m_\chi = 35 \text{ GeV}$



$$\bar{m} = (1/m_u + 1/m_d + 1/m_s)^{-1}$$

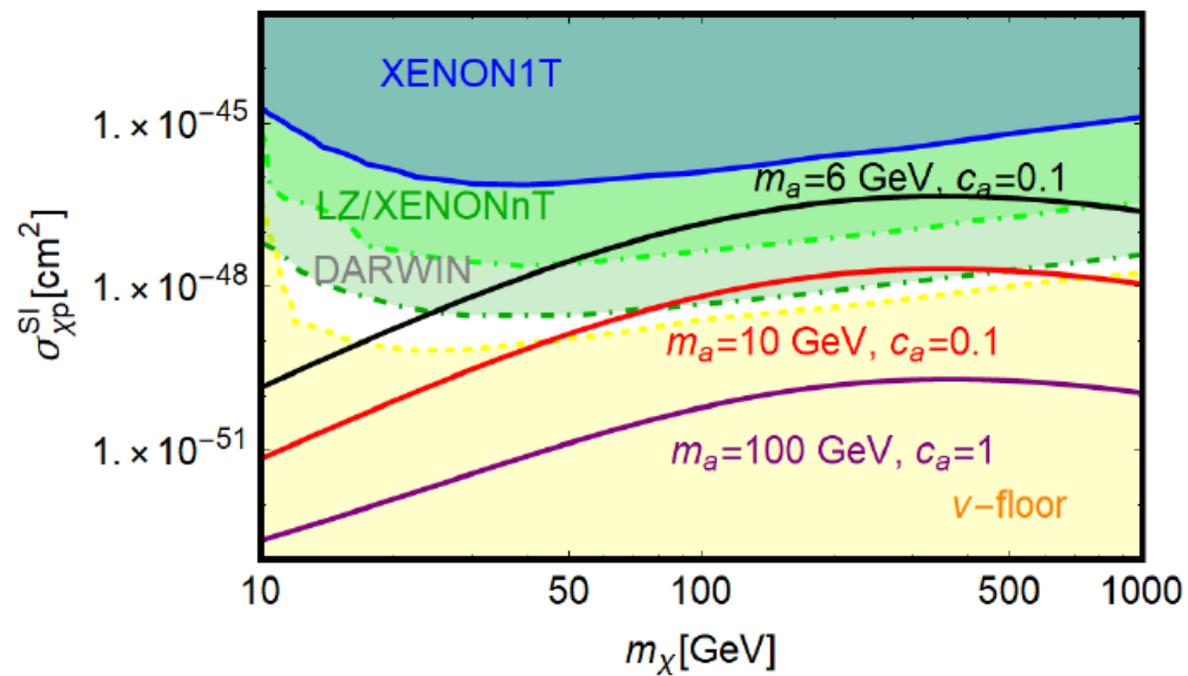
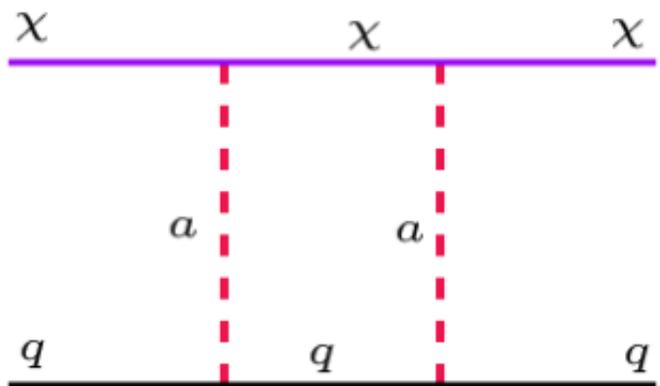


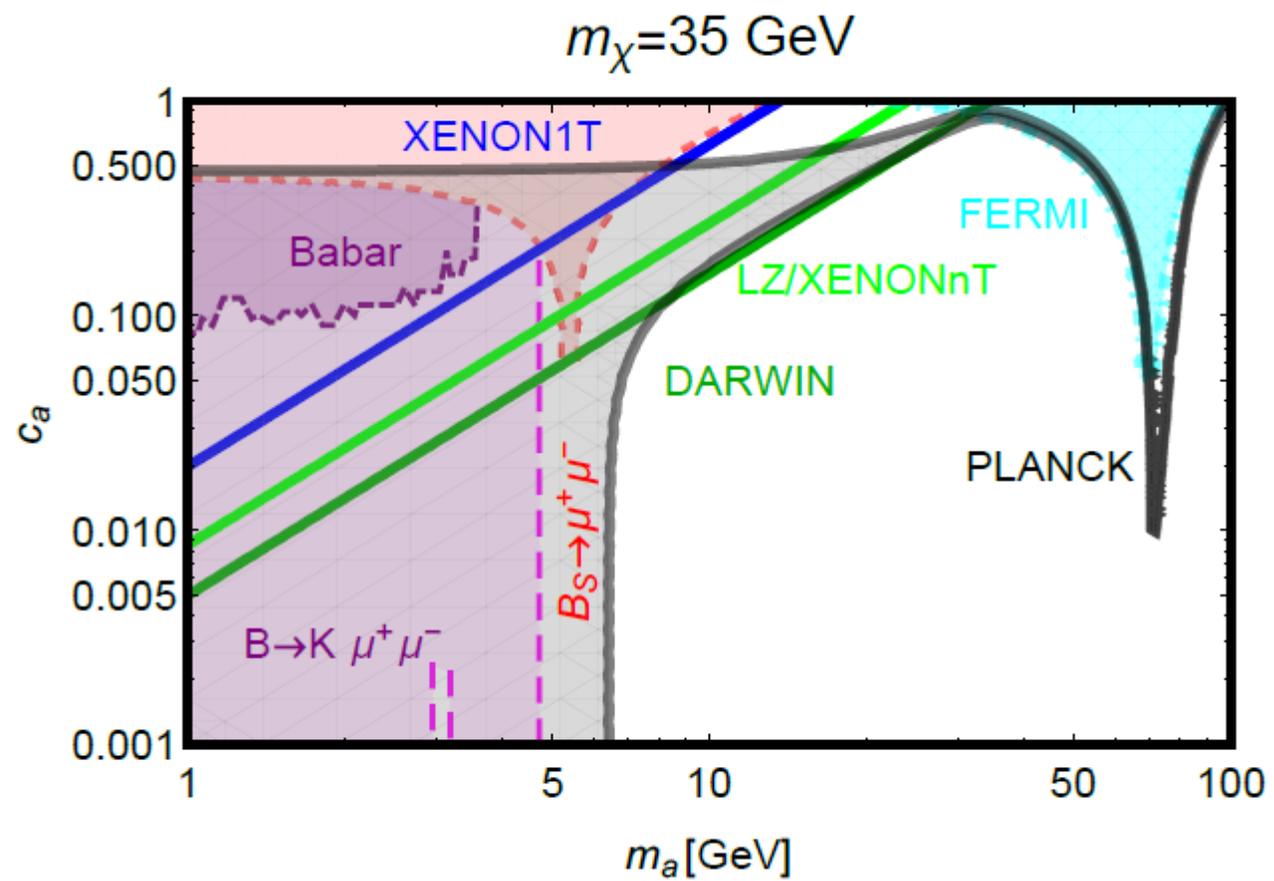
Dolan et al. arXiv:1412.5174
Döbrich et al. arXiv:1810.11336

Table from Dolan et al.
arXiv:1412.5174

Channel	Experiment	Mass range [MeV]	Ref.	Relevant for
$K^+ \rightarrow \pi^+ + \text{inv}$	E949	0–110	[70]	Long lifetime*
		150–260	[71]	Long lifetime*
	E787	0–110 & 150–260	[72]	Long lifetime
$K^+ \rightarrow \pi^+ \pi^0 \rightarrow \pi^+ \nu \bar{\nu}$	E949	130–140	[73]	Long lifetime*
$K^+ \rightarrow \pi^+ e^+ e^-$	NA48/2	140–350	[74]	Leptonic decays
$K_L \rightarrow \pi^0 e^+ e^-$	KTeV/E799	140–350	[75]	Leptonic decays*
$K^+ \rightarrow \pi^+ \mu^+ \mu^-$	NA48/2	210–350	[76]	Leptonic decays
$K_L \rightarrow \pi^0 \mu^+ \mu^-$	KTeV/E799	210–350	[77]	Leptonic decays*
$K_L \rightarrow \pi^0 \gamma \gamma$	KTeV	40–100 & 160–350	[78]	Photonic decays*
$K_L \rightarrow \pi^0 \pi^0 \rightarrow 4\gamma$	KTeV	130–140	[79]	Photonic decays*
$K^+ \rightarrow \pi^+ A$	$K_{\mu 2}$	10–130 & 140–300	[80]	All decay modes*
$B^0 \rightarrow K_S^0 + \text{inv}$	CLEO	0–1100	[81]	Long lifetime*
$B \rightarrow K \ell^+ \ell^-$	BaBar	30–3000	[82]	Leptonic decays
	BELLE	140–3000	[83]	Leptonic decays
	LHCb	220–4690	[84]	Leptonic decays*
$B \rightarrow X_s \mu^+ \mu^-$	BELLE	210–3000	[85]	Leptonic decays
$b \rightarrow s g$	CLEO	$m_A < m_B - m_K$	[86]	Hadronic decays*
$B_s \rightarrow \mu^+ \mu^-$	LHCb/CMS	all masses	[87, 88]	Lepton couplings*
$\Upsilon \rightarrow \gamma \tau^+ \tau^-$	BaBar	3500–9200	[89]	Leptonic decays*
$\Upsilon \rightarrow \gamma \mu^+ \mu^-$	BaBar	212–9200	[90]	Leptonic decays*
$\Upsilon \rightarrow \gamma + \text{hadrons}$	BaBar	300–7000	[91]	Hadronic decays*
$K, B \rightarrow A + X$	CHARM	0–4000	[92]	Leptonic and photonic decays*

SI cross-section induced at the loop level





2HDM

Can a light pseudoscalar be accommodated in the 2HDM ?

$$V(H_1, H_2) = m_{11}^2 H_1^\dagger H_1 + m_{22}^2 H_2^\dagger H_2 - m_{12}^2 (H_1^\dagger H_2 + \text{h.c.}) + \frac{\lambda_1}{2} (H_1^\dagger H_1)^2 \\ + \frac{\lambda_2}{2} (H_2^\dagger H_2)^2 + \lambda_3 (H_1^\dagger H_1) (H_2^\dagger H_2) + \lambda_4 (H_1^\dagger H_2) (H_2^\dagger H_1) \\ + \frac{\lambda_5}{2} \left[(H_1^\dagger H_2)^2 + \text{h.c.} \right]$$

$$H_i = \begin{pmatrix} \phi_i^+ \\ (v_i + \rho_i + i\eta_i)/\sqrt{2} \end{pmatrix}$$

$$\lambda_1 = \frac{1}{v^2} \left[-\tan^2 \beta M^2 + \frac{\sin^2 \alpha}{\cos^2 \beta} m_h^2 + \frac{\cos^2 \alpha}{\cos^2 \beta} m_H^2 \right],$$

$$\lambda_2 = \frac{1}{v^2} \left[-\frac{1}{\tan^2 \beta} M^2 + \frac{\cos^2 \alpha}{\sin^2 \beta} m_h^2 + \frac{\sin^2 \alpha}{\sin^2 \beta} m_H^2 \right],$$

$$\lambda_3 = \frac{1}{v^2} \left[-M^2 + 2m_{H^\pm}^2 + \frac{\sin 2\alpha}{\sin 2\beta} (m_H^2 - m_h^2) \right],$$

$$\lambda_4 = \frac{1}{v^2} [M^2 + m_A^2 - 2m_{H^\pm}^2],$$

$$\lambda_5 = \frac{1}{v^2} [M^2 - m_A^2],$$

$$\begin{pmatrix} \phi_1^+ \\ \phi_2^+ \end{pmatrix} = \begin{pmatrix} \cos \beta & -\sin \beta \\ \sin \beta & \cos \beta \end{pmatrix} \begin{pmatrix} G^+ \\ H^+ \end{pmatrix}$$

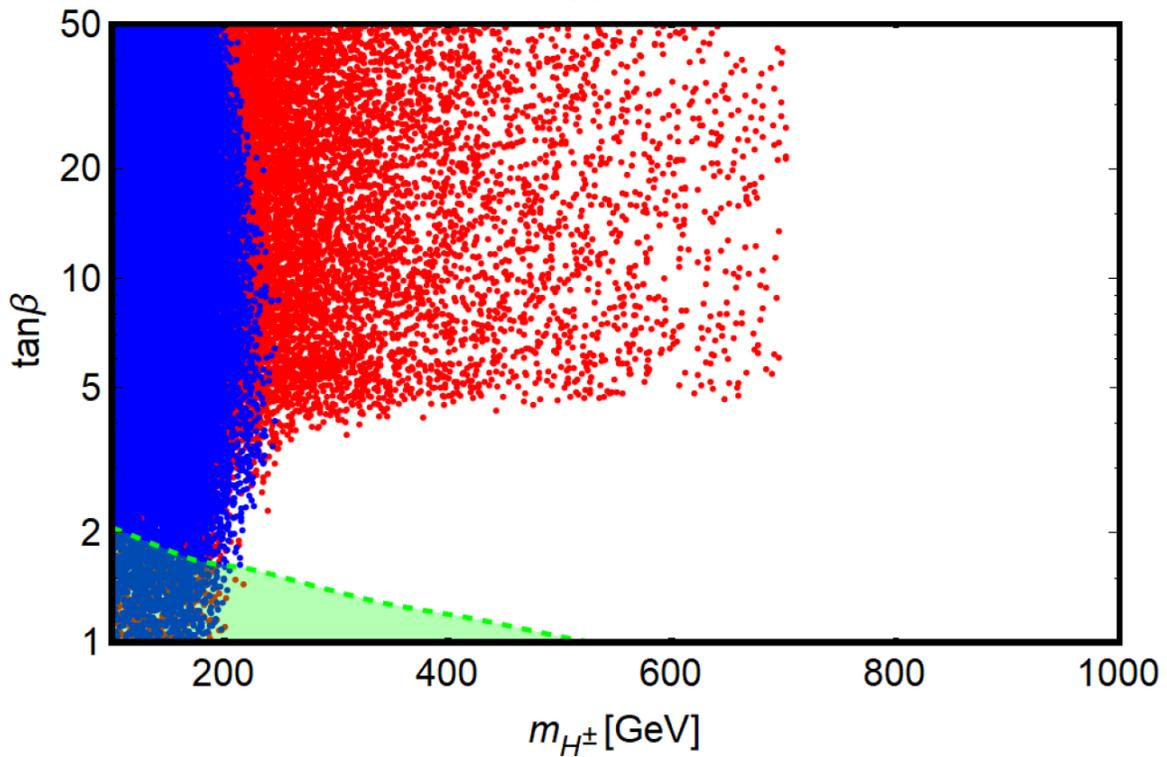
$$\begin{pmatrix} \eta_1 \\ \eta_2 \end{pmatrix} = \begin{pmatrix} \cos \beta & -\sin \beta \\ \sin \beta & \cos \beta \end{pmatrix} \begin{pmatrix} G^0 \\ A \end{pmatrix}$$

$$\begin{pmatrix} \rho_1 \\ \rho_2 \end{pmatrix} = \begin{pmatrix} \cos \alpha & -\sin \alpha \\ \sin \alpha & \cos \alpha \end{pmatrix} \begin{pmatrix} H \\ h \end{pmatrix}$$

$$\begin{aligned}
-\mathcal{L}_{yuk}^{SM} = & \sum_{f=u,d,l} \frac{m_f}{v} \left[\xi_h^f \bar{f} f h + \xi_H^f \bar{f} f H - i \xi_A^f \bar{f} \gamma_5 f A \right] \\
& - \left[\frac{\sqrt{2}}{v} \bar{u} (m_u \xi_A^u P_L + m_d \xi_A^d P_R) d H^+ + \frac{\sqrt{2}}{v} m_l \xi_A^l \bar{\nu}_L l_R H^+ + \text{h.c.} \right],
\end{aligned}$$

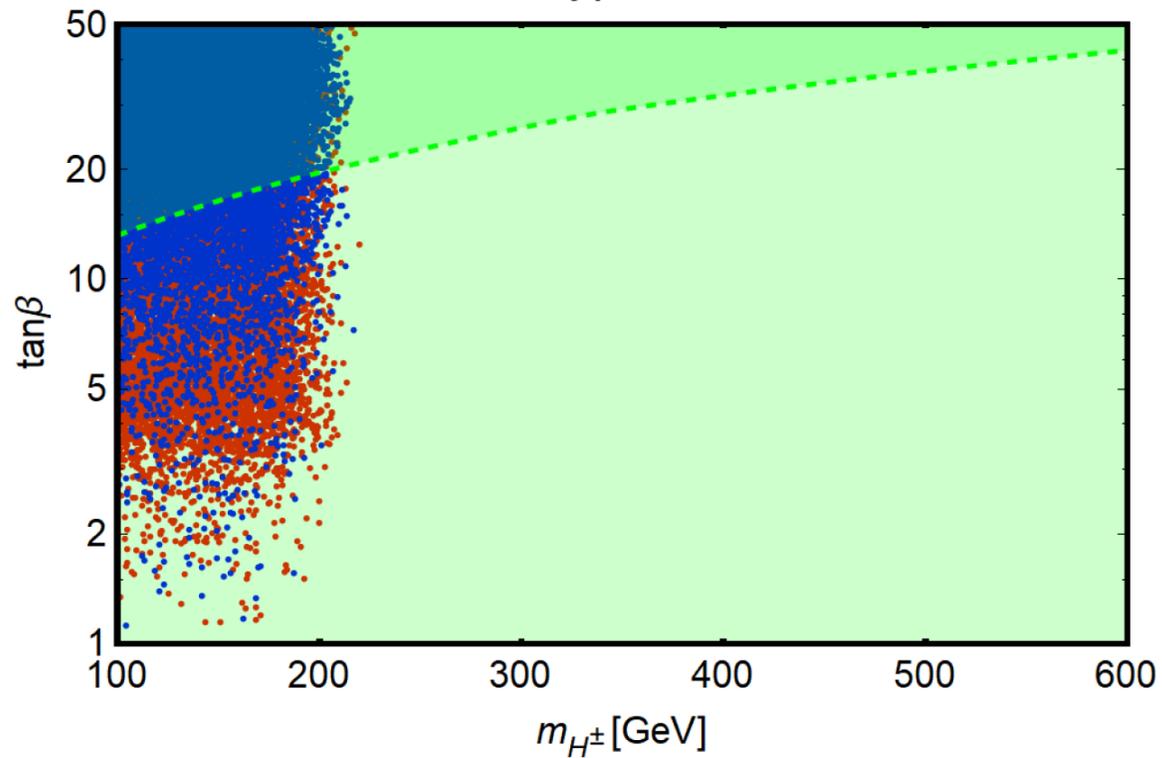
	Type I	Type II	Lepton-specific	Flipped
ξ_h^u	c_α/s_β	$c_\alpha/s_\beta \rightarrow 1$	$c_\alpha/s_\beta \rightarrow 1$	$c_\alpha/s_\beta \rightarrow 1$
ξ_h^d	$c_\alpha/s_\beta \rightarrow 1$	$-s_\alpha/c_\beta \rightarrow 1$	$c_\alpha/s_\beta \rightarrow 1$	$-s_\alpha/c_\beta \rightarrow 1$
ξ_h^l	$c_\alpha/s_\beta \rightarrow 1$	$-s_\alpha/c_\beta \rightarrow 1$	$-s_\alpha/c_\beta \rightarrow 1$	$c_\alpha/s_\beta \rightarrow 1$
ξ_H^u	$s_\alpha/s_\beta \rightarrow -t_\beta^{-1}$	$s_\alpha/s_\beta \rightarrow -t_\beta^{-1}$	$s_\alpha/s_\beta \rightarrow -t_\beta^{-1}$	$s_\alpha/s_\beta \rightarrow -t_\beta^{-1}$
ξ_H^d	$s_\alpha/s_\beta \rightarrow -t_\beta^{-1}$	$c_\alpha/c_\beta \rightarrow t_\beta$	$s_\alpha/s_\beta \rightarrow -t_\beta^{-1}$	$c_\alpha/c_\beta \rightarrow t_\beta$
ξ_H^l	$s_\alpha/s_\beta \rightarrow -t_\beta^{-1}$	$c_\alpha/c_\beta \rightarrow t_\beta$	$c_\alpha/c_\beta \rightarrow t_\beta$	$s_\alpha/s_\beta \rightarrow -t_\beta^{-1}$
ξ_A^u	t_β^{-1}	t_β^{-1}	t_β^{-1}	t_β^{-1}
ξ_A^d	$-t_\beta^{-1}$	t_β	$-t_\beta^{-1}$	t_β
ξ_A^l	$-t_\beta^{-1}$	t_β	t_β	$-t_\beta^{-1}$

Type-I



$60 \text{ GeV} < m_A < m_h$

Type-II



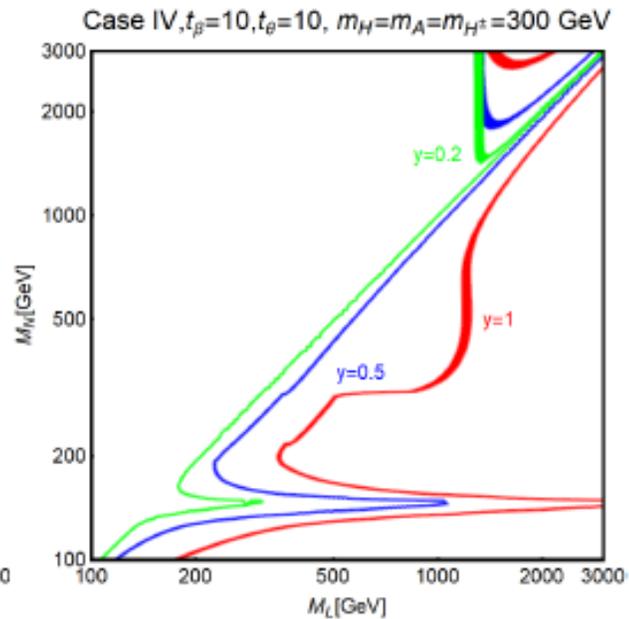
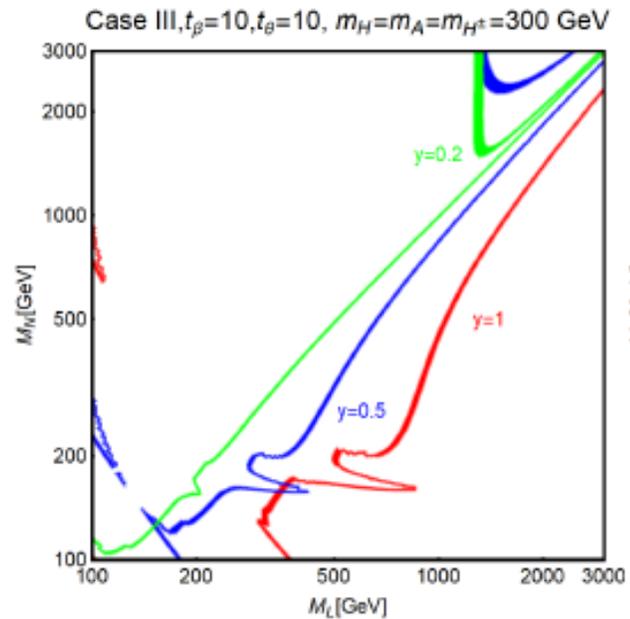
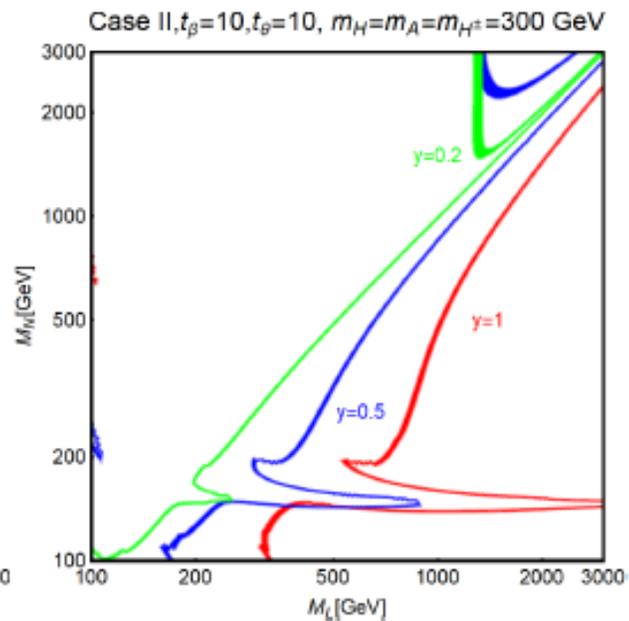
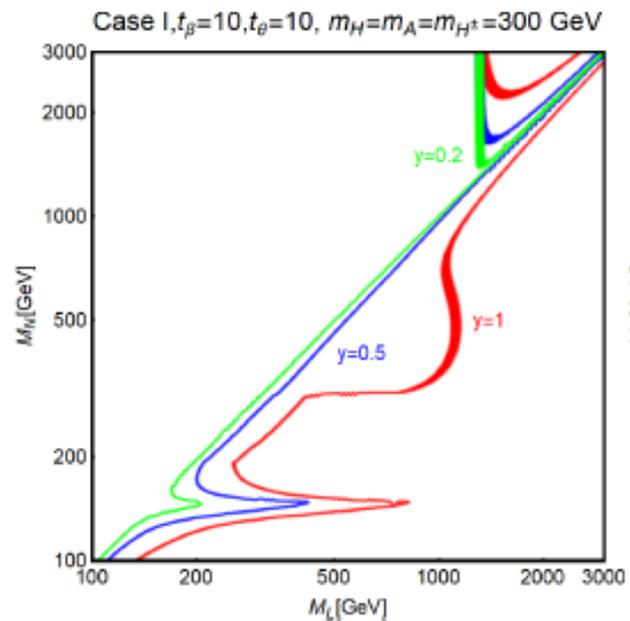
The Dark Matter is a mixture of a SM singlet and two (Weyl) fermions doublets under SU(2)

$$\mathcal{L} = -\frac{1}{2}M_N N'^2 - M_L L_L L_R - y_i^L L_L H_i N' - y_i^R \bar{N}' \tilde{H}_i^\dagger L_R + \text{h.c.}, \quad i = 1, 2$$

$$y_1 = y \cos \theta \quad y_2 = y \sin \theta$$

$$M = \begin{pmatrix} M_N & \frac{y_1 v_1}{\sqrt{2}} & \frac{y_2 v_2}{\sqrt{2}} \\ \frac{y_1 v_1}{\sqrt{2}} & 0 & M_L \\ \frac{y_2 v_2}{\sqrt{2}} & M_L & 0 \end{pmatrix} \longrightarrow \psi_i = N' U_{i1} + N_L U_{i2} + N_R U_{i3}$$

$$\begin{aligned} \mathcal{L} = & \bar{\psi}^- \gamma^\mu (g_{W\chi_i}^V - g_{W\chi_i}^A \gamma_5) \psi_i W_\mu^- + \text{h.c.} + \frac{1}{2} \sum_{i,j=1}^3 \bar{\psi}_i \gamma^\mu (g_{Z\psi_i\psi_j}^V - g_{Z\psi_i\psi_j}^A \gamma_5) Z_\mu \psi_j \\ & + \frac{1}{2} \sum_{i,j=1}^3 \bar{\psi}_i (y_{h\psi_i\psi_j} h + y_{H\psi_i\psi_j} H + y_{A\psi_i\psi_j} \gamma_5 A) \psi_j + \text{h.c.} + \bar{\psi}^- (g_{H^\pm\psi_i}^S - g_{H^\pm\psi_i}^P \gamma_5) \psi_i H^- + \text{h.c.} \\ & - e A_\mu \bar{\psi}^- \gamma^\mu \psi^- - \frac{g}{2 \cos \theta_W} (1 - 2 \sin^2 \theta_W) Z_\mu \bar{\psi}^- \gamma^\mu \psi^- + \text{h.c.} \end{aligned}$$



Exchange of CP-even Higgses induces SI cross-section.

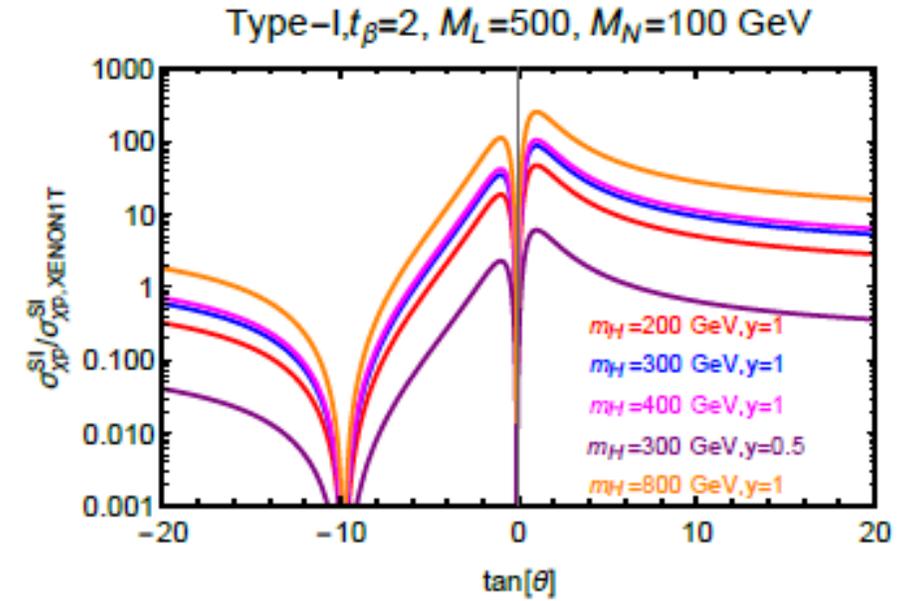
Limits can be avoided in presence of the so called Blind Spots.

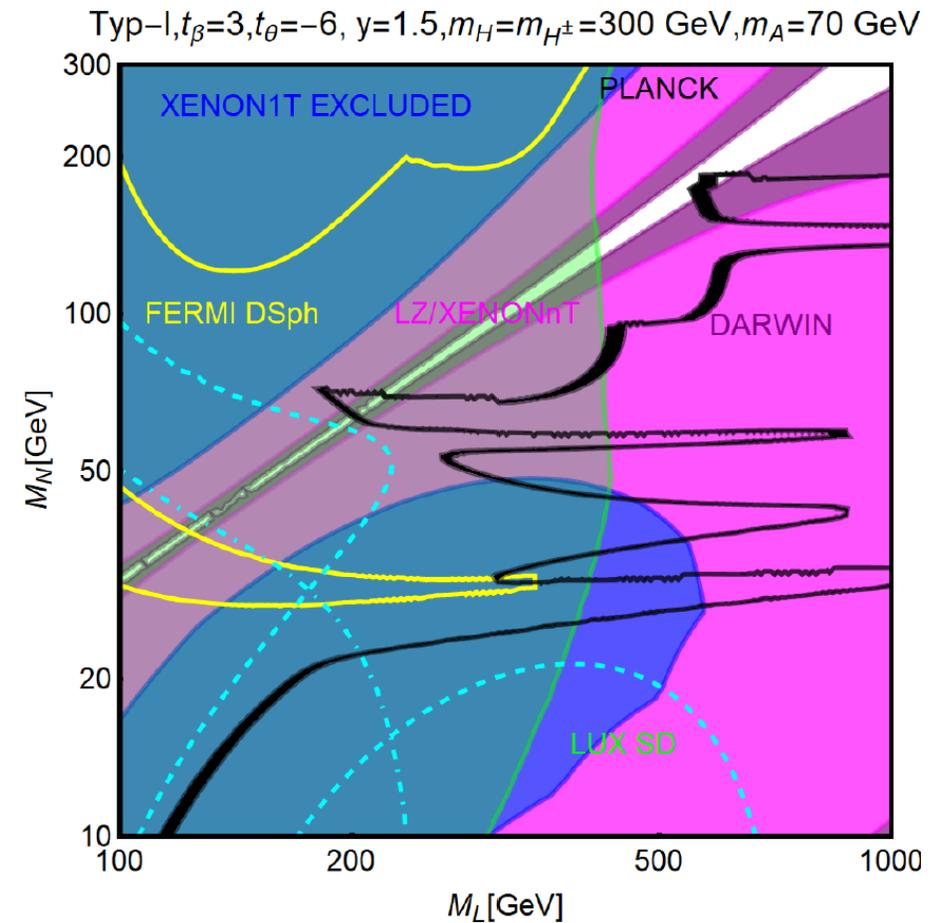
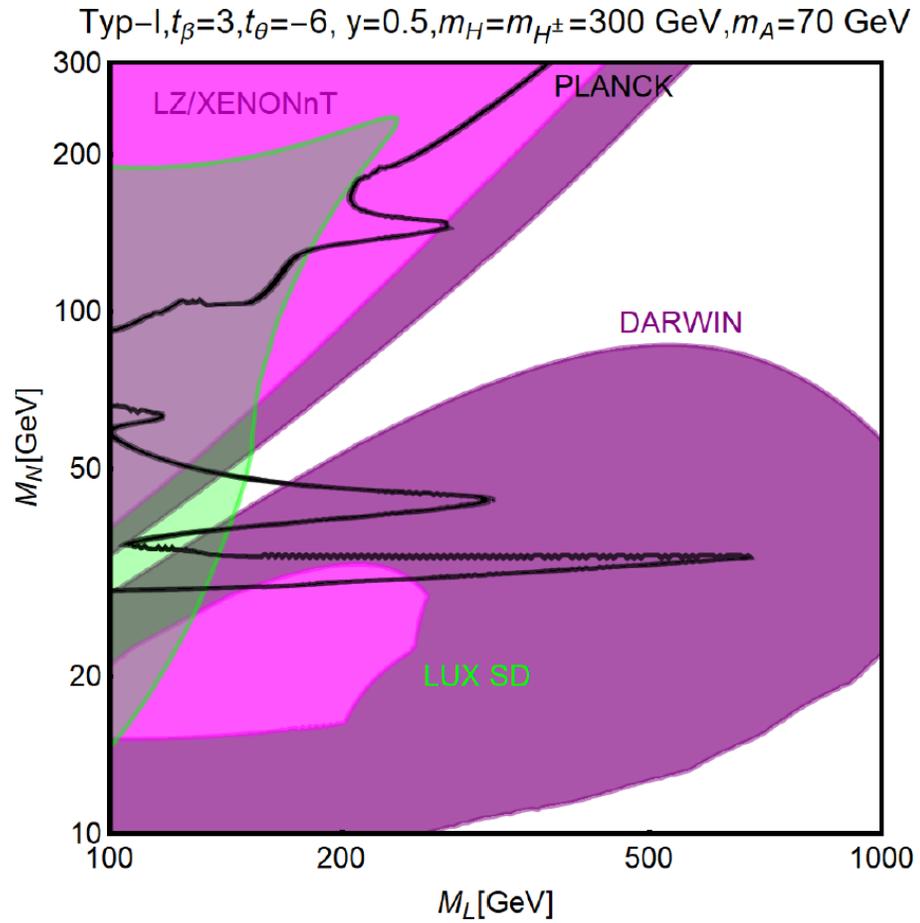
$$\sigma_{\chi p}^{\text{SI}} = \frac{\mu_{\chi}^2}{\pi} \frac{m_p^2}{v^2} \left| \sum_q f_q \left(\frac{g_{h\psi_1\psi_1} \xi_h^q}{m_h^2} + \frac{g_{H\psi_1\psi_1} \xi_H^q}{m_H^2} \right) \right|^2$$

In case the new fermions couple with only one doublet

$$g_{h\psi_1\psi_1} = y^2 v \cos^2 \beta \frac{m_{\psi_1} + M_L \sin 2\theta}{2M_L^2 + 4M_N m_{\psi_1} - 6m_{\psi_1}^2 + y^2 v^2 \cos^2 \beta}$$

$$g_{H\psi_1\psi_1} = \frac{1}{2} y^2 v \sin 2\beta \frac{m_{\psi_1} + M_L \sin 2\theta}{2M_L^2 + 4M_N m_{\psi_1} - 6m_{\psi_1}^2 + y^2 v^2 \cos^2 \beta}$$





2HDM+Light Pseudoscalar

- DM can be a pure SM singlet.
- Higher hierarchy between the lighter pseudoscalar and the other new boson (not arbitrary because of unitarity bound).

$$V = V_{2\text{HDM}} + \frac{1}{2}m_{a_0}a_0^2 + \frac{\lambda_a}{4}a_0^4 + (i\kappa a_0 H_1^\dagger H_2 + \text{h.c.})$$

$$\mathcal{L} = ig_\chi a_0 \bar{\chi} i\gamma^5 \chi$$

$$\begin{pmatrix} A_0 \\ a_0 \end{pmatrix} = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} A \\ a \end{pmatrix}$$

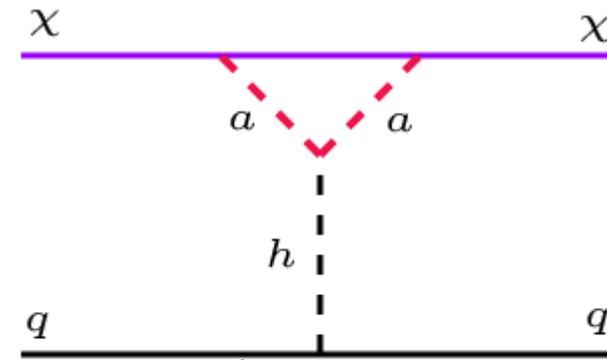
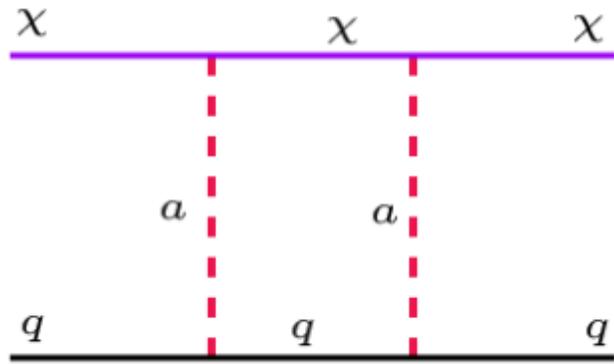
$$\tan 2\theta = \frac{2\kappa v_h}{m_{A_0}^2 - m_{a_0}^2}$$

$$\mathcal{L}_{\text{DM}} = g_\chi (\cos \theta a + \sin \theta A) \bar{\chi} i \gamma_5 \chi$$

$$\mathcal{L}_{\text{scalar}} = \frac{1}{2v_h} (m_A^2 - m_a^2) [\sin 4\theta a A + \sin^2 2\theta (A^2 - a^2)] (\sin(\beta - \alpha)h + \cos(\beta - \alpha)H)$$

$$\mathcal{L}_{\text{Yuk}} = \sum_f \frac{m_f}{v_h} \left(\xi_f^h h \bar{f} f + \xi_f^H H \bar{f} f - i\xi_f^A A \bar{f} \gamma_5 f - i\xi_f^a a \bar{f} \gamma_5 a \right)$$

SI cross-section induced at the loop level



(see also 1803.01574)

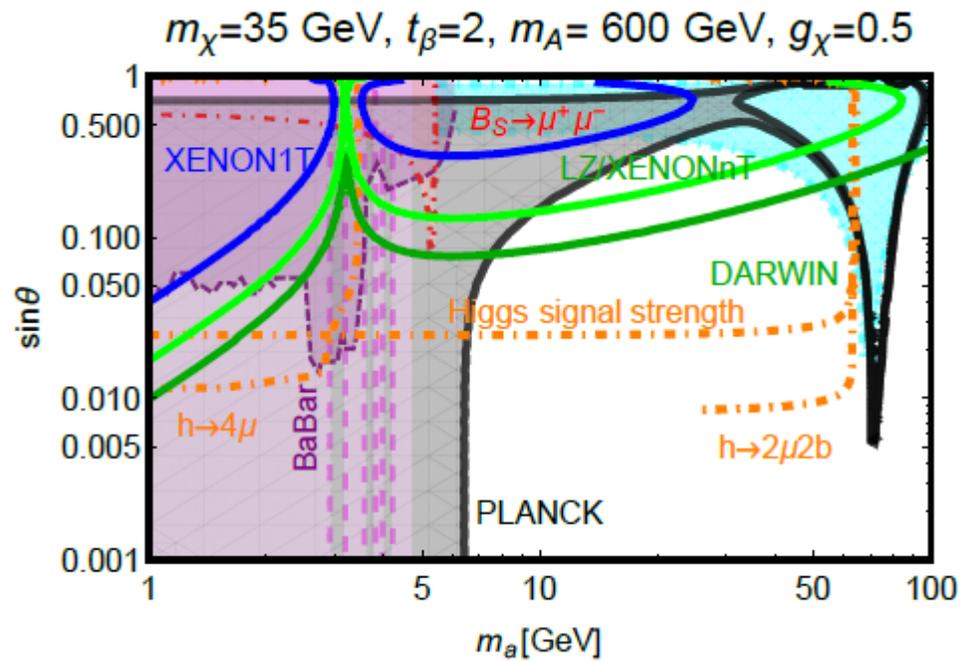
Computation recently superseded by Abe et al
arXiv:1810.01039

$$\mathcal{L} = g_\chi^2 \sum_q C_{V,q} \bar{\chi} \gamma^\mu \chi \bar{q} \gamma_\mu q + C_{S,q} \bar{\chi} \chi \bar{q} q$$

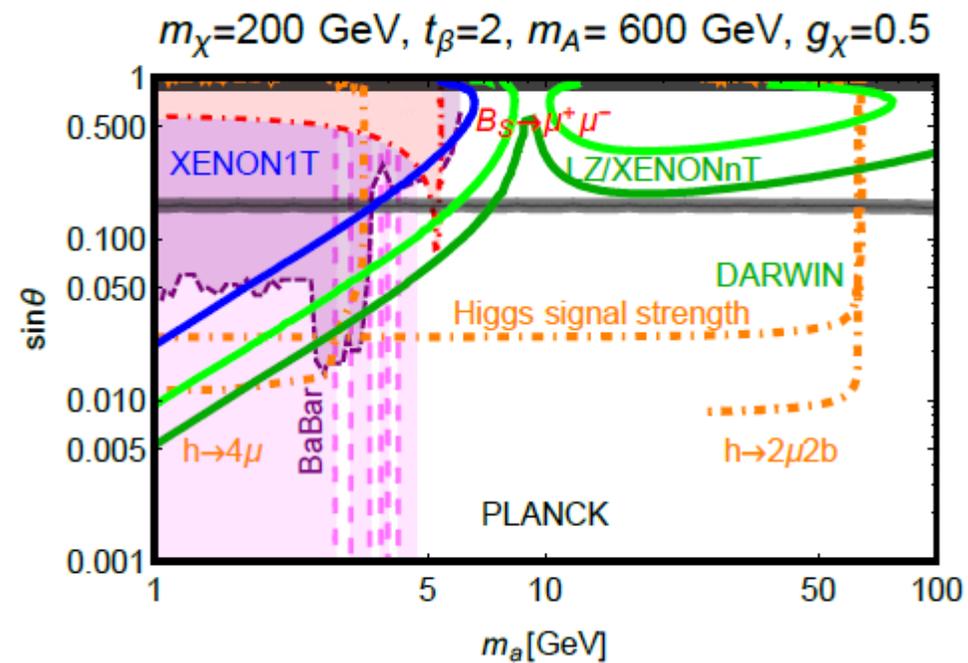
Negligible for yukawa like interactions

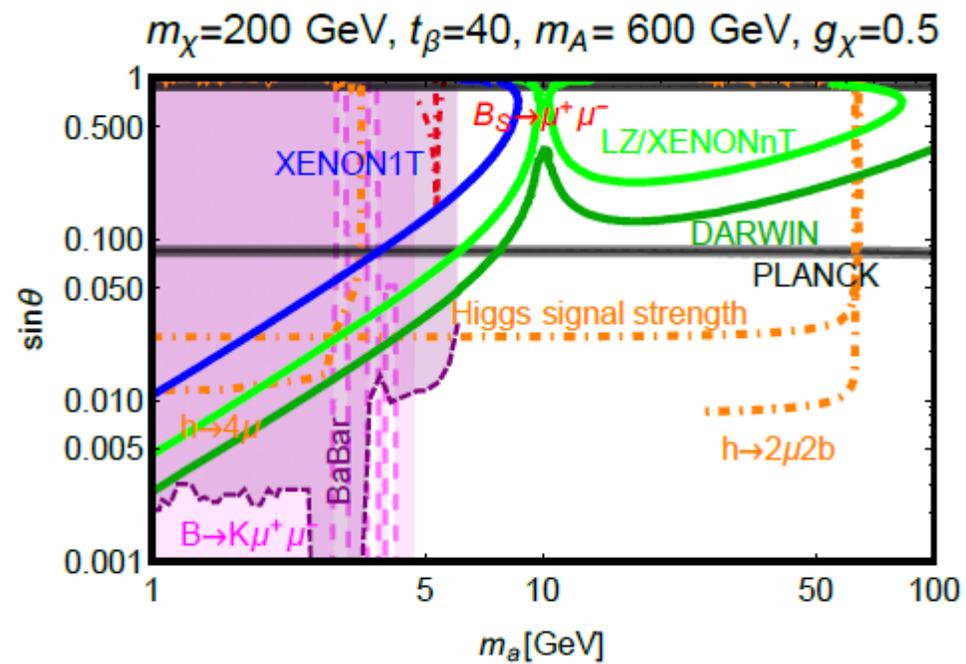
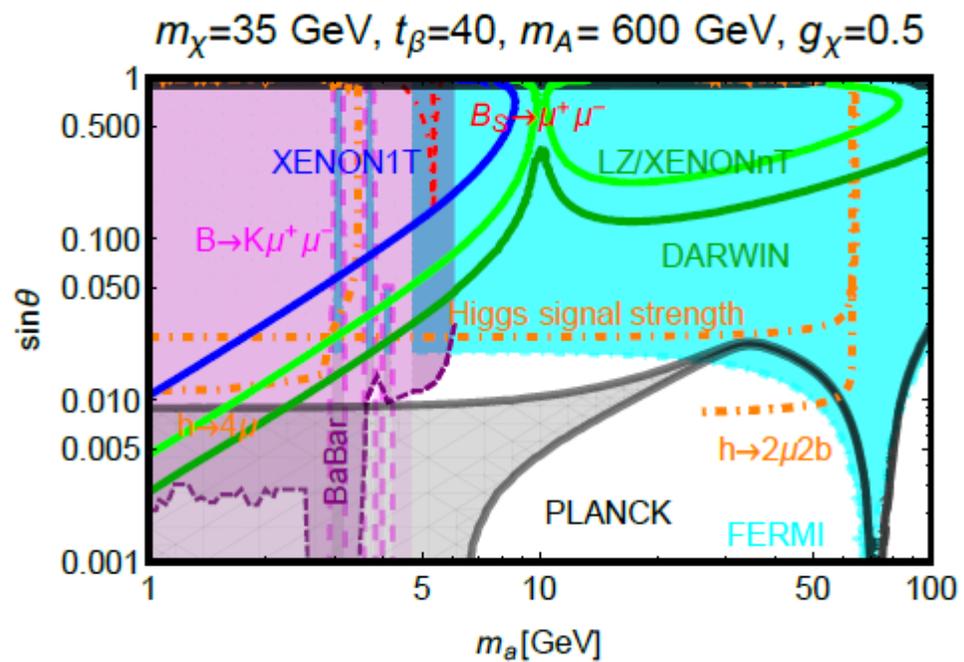
$$\sigma_{\chi p}^{\text{SI}} = \frac{\mu_{\chi p}^2}{\pi} g_\chi^4 |F_l(m_\chi, m_a, m_h, m_q)|^2$$

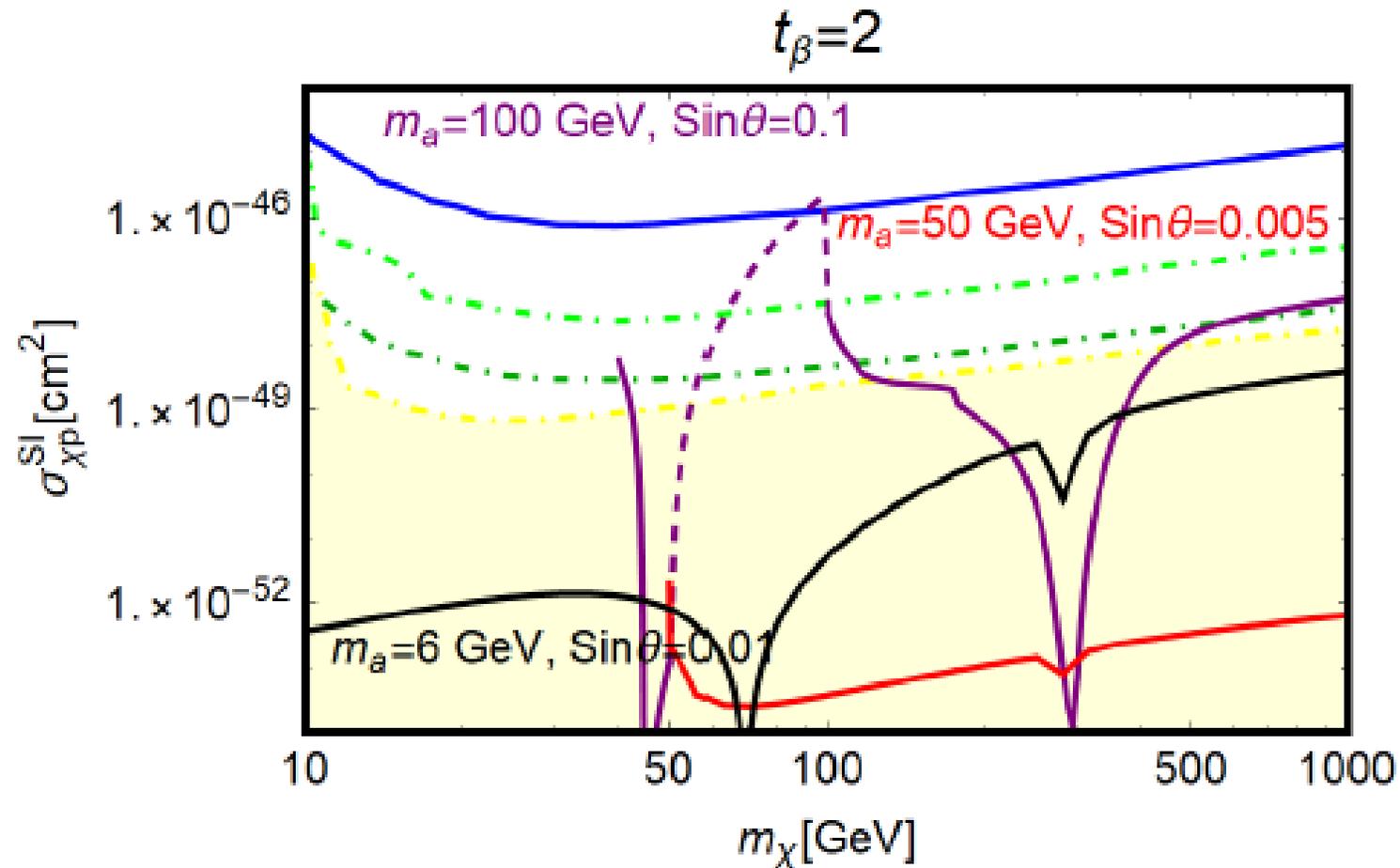
$$F_l(m_\chi, m_a, m_h, m_q) = \frac{2}{27} f_{\text{TG}} \sum_{q \in \text{heavy}} \frac{m_q m_p}{v_h^2} (C_{S,q,\text{triangle}} + C_{S,q,\text{box}})$$



G.A., M. Lindner, F. Queiroz, W. Rodejohann, S. Vogl
 arXiv:1711.02110







It is possible to have a WIMP model with typical scattering cross-section lying in the so-called 'neutrino floor'

Conclusions

A particularly interesting scenario is the case in which WIMP interactions are mostly mediated by a (possibly light) pseudoscalar field.

We have proposed an overview of possible implementations of this scenario from a simple portal to more refined models.