

RECENT PROGRESS IN NUCLEAR INTERACTIONS FROM CHIRAL EFFECTIVE FIELD THEORY



R. Machleidt

University of Idaho

THE
NUCLEAR FORCE
IN THE

III. MILLENIUM

AFTER JESUS CHRIST :

a PREVIEW

R. MACHLEIDT
U. of IDAHO

ECBA
JUNE 26-30, 2000

HISTORY



1990

RECENT PROGRESS



2000

FUTURE

ACCURATE NN POT
(PHENOMENOLOGY)

THEORY

HJ
REID
PARIS

HISTORY

ORFÈRE'S
PARIS
BONN

V₁₄

1990

Nijmegen I, II, 93
REID 93

V₁₈

RECENT

LATTICE QCD
QUARK MODELS
SKYRME MOD.
PROGRESS

CD-BONN

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Nijmegen I, II, 93
REID 93

RECENT

PROGRESS

If you want accuracy,
Forget about theory.

CD-BONN

If you use real theory,
Don't expect accuracy.

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**Accuracy AND
Theory**

THE PROGRAM FOR THE NEW MILLENIUM

For a reliable derivation of
nuclear forces, we need

- a basic theory
- that is amenable to calculations
- yields quantitative results.

THE PROGRAM FOR THE NEW MILLENNIUM

For a reliable derivation of
nuclear forces, we need

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 χ eff. field theory
- that is amenable to calculations

χ PTh

- yields quantitative results.

let's hope for it!

2N Force

3N Force

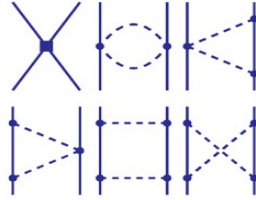
4N Force

5N Force

LO
 $(Q/\Lambda_\chi)^0$



NLO
 $(Q/\Lambda_\chi)^2$



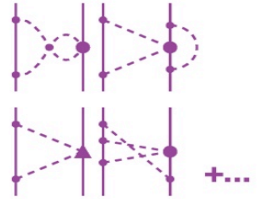
NNLO
 $(Q/\Lambda_\chi)^3$



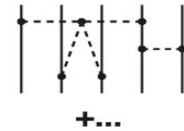
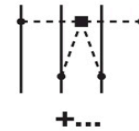
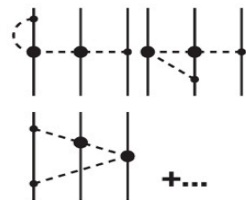
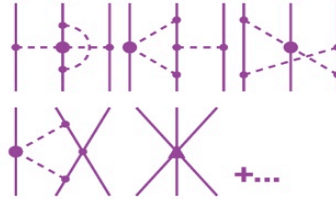
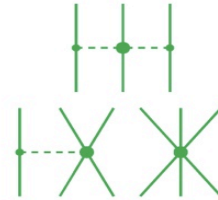
N³LO
 $(Q/\Lambda_\chi)^4$



N⁴LO
 $(Q/\Lambda_\chi)^5$



N⁵LO
 $(Q/\Lambda_\chi)^6$



2N Force

3N Force

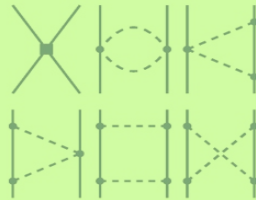
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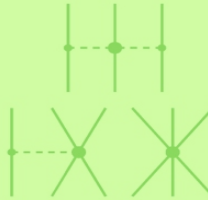
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 $(Q/\Lambda_\chi)^2$

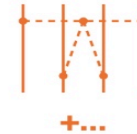


NNLO
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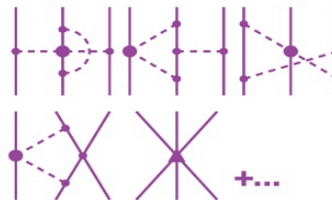
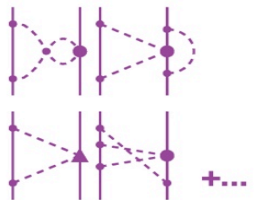


**Status
 A.D.
 2000**

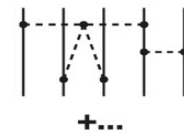
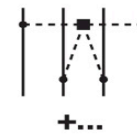
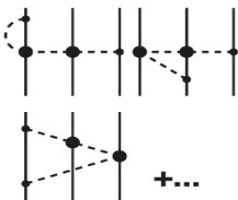
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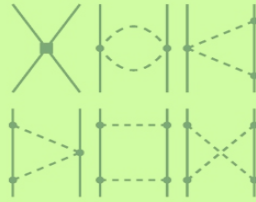
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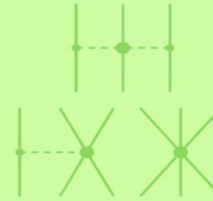
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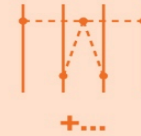
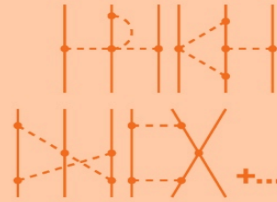
NLO
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NNLO
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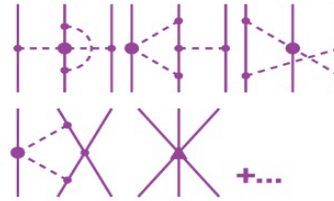
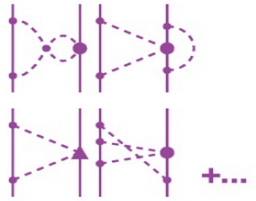


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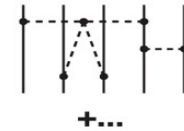
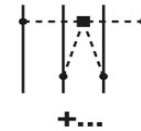
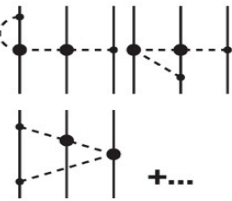
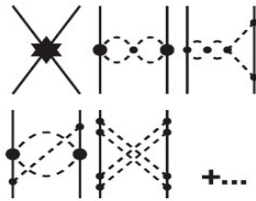


**Status
 A.D.
 2010**

N⁴LO
 $(Q/\Lambda_\chi)^5$



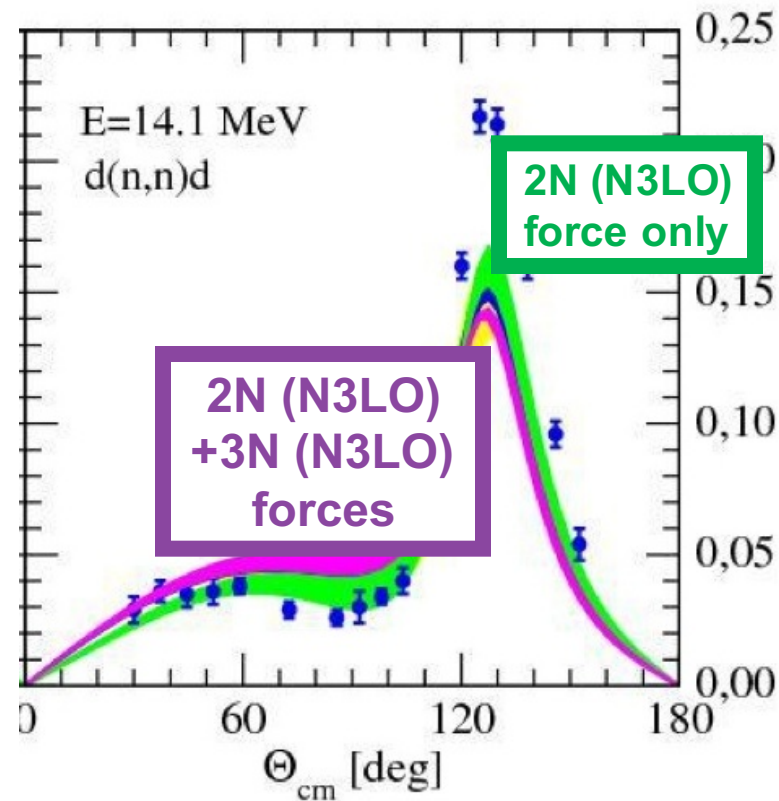
N⁵LO
 $(Q/\Lambda_\chi)^6$



WHAT HAVE WE ACHIEVED WITH THOSE FORCES?

- **There has been some success (ground state of 10B, drip lines, nuclear matter saturation, orbit evolution, etc.), but some persistent problems remain.**
- **In the few-body sector: A_y puzzle, N-d break-up, ...**

N-d A_y calculations by Witala et al.



- chiral $N^3\text{LO}$ + 3NF $N^3\text{LO}$ ($\pi\pi$ +D+E)
- chiral $N^3\text{LO}$ + 3NF $N^3\text{LO}$ ($\pi\pi$ + $2\pi 1\pi$ +D+E)
- chiral $N^3\text{LO}$
- TUNL nd data
- chiral $N^3\text{LO}$ + 3NF $N^3\text{LO}$ ($\pi\pi$ + $2\pi 1\pi$ +ring+D+E)

CURRENT STATUS AND OPEN ISSUES

- **Current status: 2NFs and 3NFs up to N3LO are applied in nuclear few- and many-body systems.**
- **In general, quite a bit of success, but some persistent problems remain.**
- **In the few-body sector: A_y puzzle, N-d break-up, ...**
- **Light nuclei: Spectra not perfect.**

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- **The radii of nuclei**



Radii and Binding Energies in Oxygen Isotopes: A Challenge for Nuclear Forces

V. Lapoux,^{1,*} V. Somà,¹ C. Barbieri,² H. Hergert,³ J.D. Holt,⁴ and S.R. Stroberg⁴

¹CEA, Centre de Saclay, IRFU, Service de Physique Nucléaire, 91191 Gif-sur-Yvette, France

²Department of Physics, University of Surrey, Guildford GU2 7XH, United Kingdom

³National Superconducting Cyclotron Laboratory and Department of Physics and Astronomy, Michigan State University, East Lansing, Michigan 48824, USA

⁴TRIUMF, 4004 Wesbrook Mall, Vancouver, British Columbia, Canada V6T 2A3

(Received 29 April 2016; published 27 July 2016)

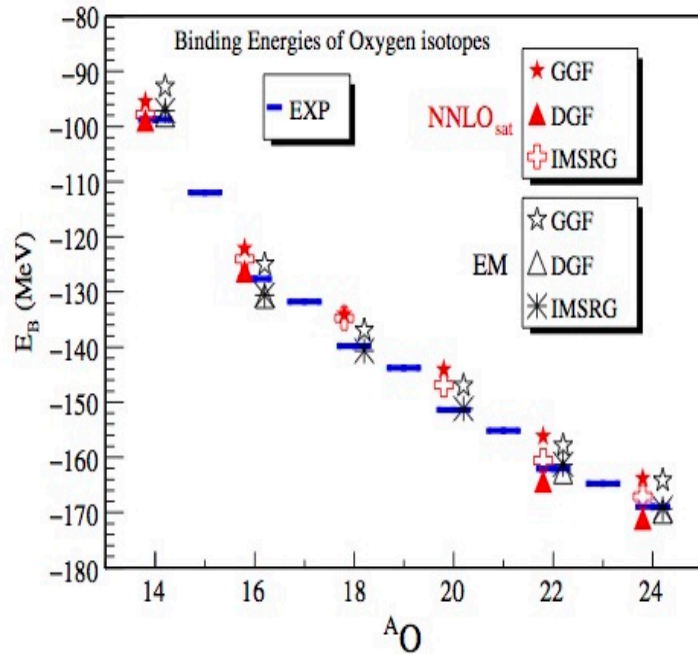


FIG. 1. Oxygen binding energies. Results from SCGF (DGF and GGF) and IMSRG calculations with EM and NNLO_{sat} are displayed along with experimental data.

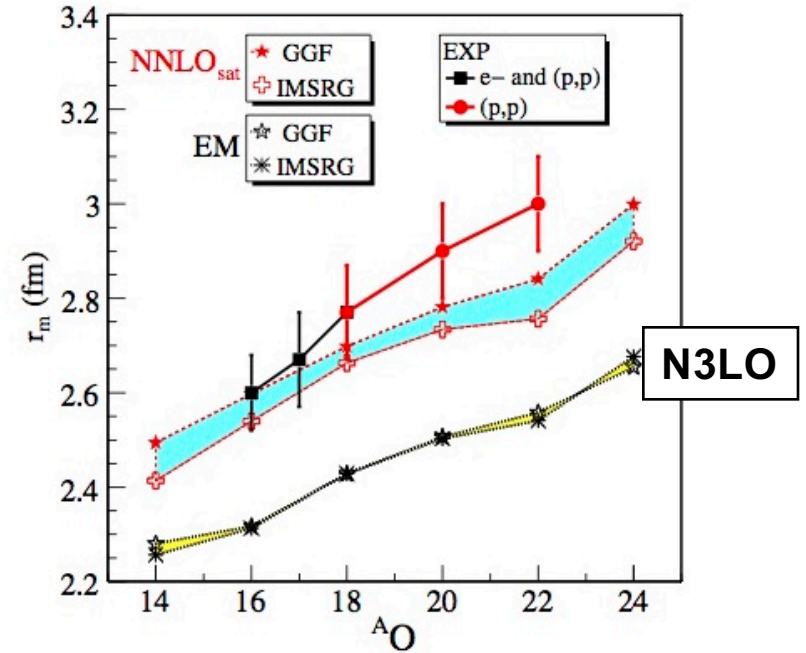


FIG. 5. Matter radii from our analysis and given in Table I, compared to calculations with EM [27–29] and NNLO_{sat} [36]. Bands span results from GGF and MR-IMSRG schemes.

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- **Overbinding of intermediate-mass nuclei**

Overbinding of intermediate-mass nuclei

Oxygen

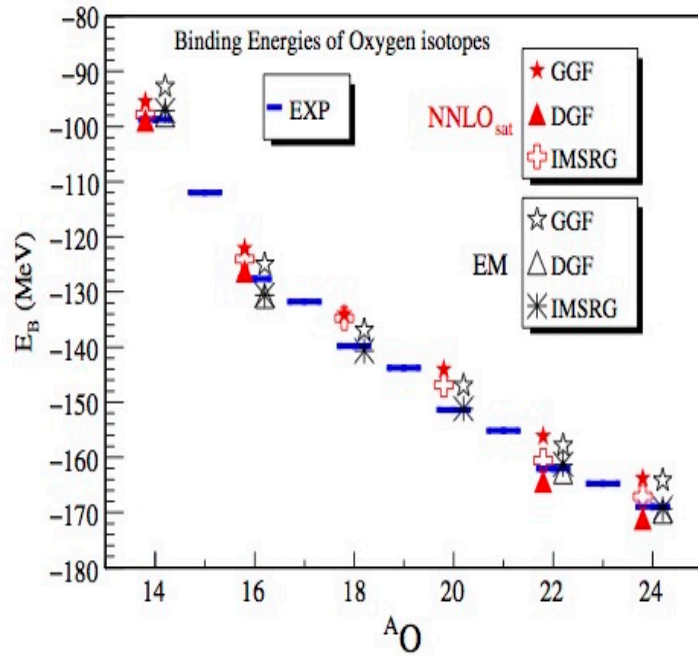
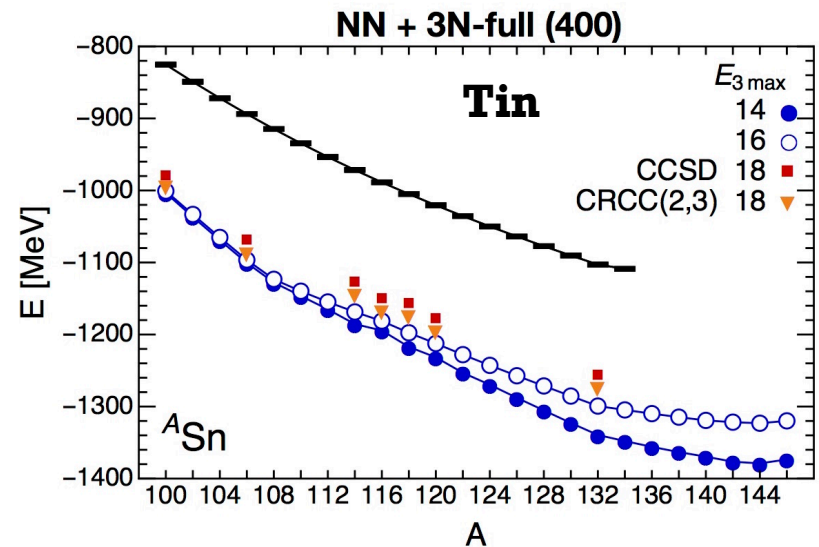
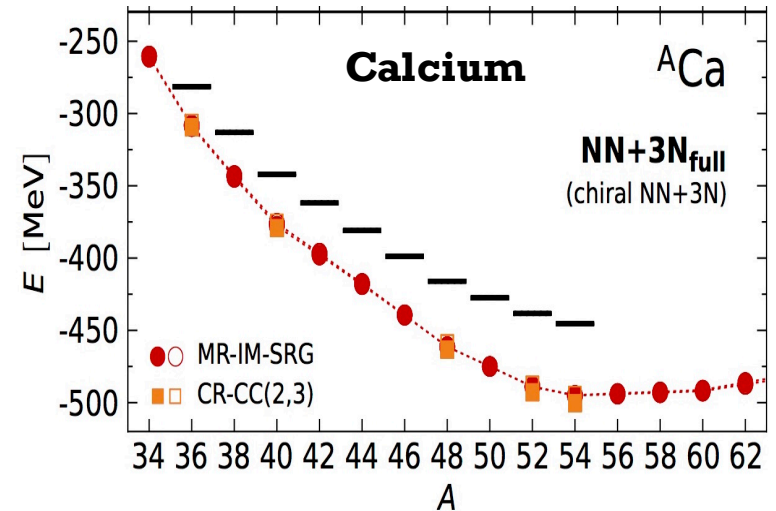


FIG. 1. Oxygen binding energies. Results from SCGF (DGF and GGF) and IMSRG calculations with EM and NNLO_{sat} are displayed along with experimental data.



From Hergert et al., PRC 90, 041302 (2014).

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**BECAUSE OF THE PROBLEMS JUST POINTED OUT,
IMPROVEMENT OF CURRENT NUCLEAR FORCES IS
CALLED FOR.**

- **How?**
- **Revisit the lower orders**
- **Move on to higher orders**

2N Force

3N Force

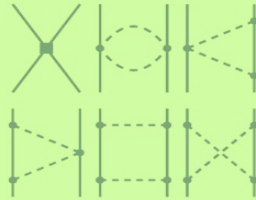
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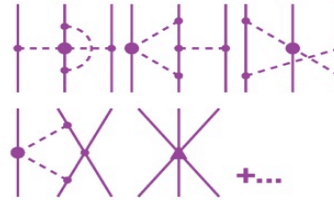
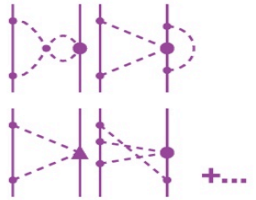


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 $(Q/\Lambda_\chi)^4$

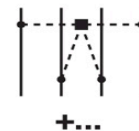
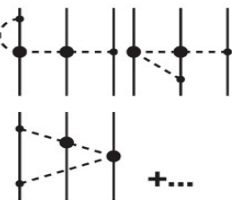


**Status
 A.D.
 2010**

N⁴LO
 $(Q/\Lambda_\chi)^5$



N⁵LO
 $(Q/\Lambda_\chi)^6$



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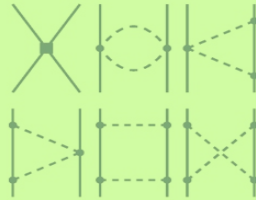
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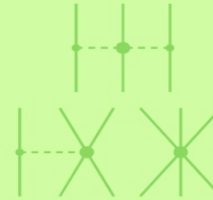
LO
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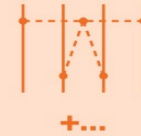
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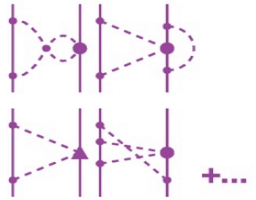
NNLO
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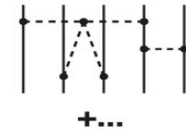
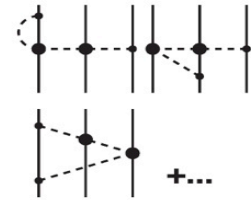
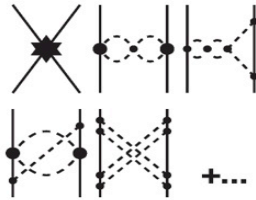
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 $(Q/\Lambda_\chi)^6$



Chiral Nuclear Interactions

Elba, 25 June 2019

R. Machleidt

All possible 20 isospin-spin-momentum/position structures occur in the 3NF at N4LO!

Epelbaum et al., Eur. Phys. J. A51, 26 (2015)

Generators \mathcal{G} in momentum space	Generators $\tilde{\mathcal{G}}$ in coordinate space
$\mathcal{G}_1 = 1$	$\tilde{\mathcal{G}}_1 = 1$
$\mathcal{G}_2 = \boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_3$	$\tilde{\mathcal{G}}_2 = \boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_3$
$\mathcal{G}_3 = \vec{\sigma}_1 \cdot \vec{\sigma}_3$	$\tilde{\mathcal{G}}_3 = \vec{\sigma}_1 \cdot \vec{\sigma}_3$
$\mathcal{G}_4 = \boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_3 \vec{\sigma}_1 \cdot \vec{\sigma}_3$	$\tilde{\mathcal{G}}_4 = \boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_3 \vec{\sigma}_1 \cdot \vec{\sigma}_3$
$\mathcal{G}_5 = \boldsymbol{\tau}_2 \cdot \boldsymbol{\tau}_3 \vec{\sigma}_1 \cdot \vec{\sigma}_2$	$\tilde{\mathcal{G}}_5 = \boldsymbol{\tau}_2 \cdot \boldsymbol{\tau}_3 \vec{\sigma}_1 \cdot \vec{\sigma}_2$
$\mathcal{G}_6 = \boldsymbol{\tau}_1 \cdot (\boldsymbol{\tau}_2 \times \boldsymbol{\tau}_3) \vec{\sigma}_1 \cdot (\vec{\sigma}_2 \times \vec{\sigma}_3)$	$\tilde{\mathcal{G}}_6 = \boldsymbol{\tau}_1 \cdot (\boldsymbol{\tau}_2 \times \boldsymbol{\tau}_3) \vec{\sigma}_1 \cdot (\vec{\sigma}_2 \times \vec{\sigma}_3)$
$\mathcal{G}_7 = \boldsymbol{\tau}_1 \cdot (\boldsymbol{\tau}_2 \times \boldsymbol{\tau}_3) \vec{\sigma}_2 \cdot (\vec{q}_1 \times \vec{q}_3)$	$\tilde{\mathcal{G}}_7 = \boldsymbol{\tau}_1 \cdot (\boldsymbol{\tau}_2 \times \boldsymbol{\tau}_3) \vec{\sigma}_2 \cdot (\hat{r}_{12} \times \hat{r}_{23})$
$\mathcal{G}_8 = \vec{q}_1 \cdot \vec{\sigma}_1 \vec{q}_1 \cdot \vec{\sigma}_3$	$\tilde{\mathcal{G}}_8 = \hat{r}_{23} \cdot \vec{\sigma}_1 \hat{r}_{23} \cdot \vec{\sigma}_3$
$\mathcal{G}_9 = \vec{q}_1 \cdot \vec{\sigma}_3 \vec{q}_3 \cdot \vec{\sigma}_1$	$\tilde{\mathcal{G}}_9 = \hat{r}_{23} \cdot \vec{\sigma}_3 \hat{r}_{12} \cdot \vec{\sigma}_1$
$\mathcal{G}_{10} = \vec{q}_1 \cdot \vec{\sigma}_1 \vec{q}_3 \cdot \vec{\sigma}_3$	$\tilde{\mathcal{G}}_{10} = \hat{r}_{23} \cdot \vec{\sigma}_1 \hat{r}_{12} \cdot \vec{\sigma}_3$
$\mathcal{G}_{11} = \boldsymbol{\tau}_2 \cdot \boldsymbol{\tau}_3 \vec{q}_1 \cdot \vec{\sigma}_1 \vec{q}_1 \cdot \vec{\sigma}_2$	$\tilde{\mathcal{G}}_{11} = \boldsymbol{\tau}_2 \cdot \boldsymbol{\tau}_3 \hat{r}_{23} \cdot \vec{\sigma}_1 \hat{r}_{23} \cdot \vec{\sigma}_2$
$\mathcal{G}_{12} = \boldsymbol{\tau}_2 \cdot \boldsymbol{\tau}_3 \vec{q}_1 \cdot \vec{\sigma}_1 \vec{q}_3 \cdot \vec{\sigma}_2$	$\tilde{\mathcal{G}}_{12} = \boldsymbol{\tau}_2 \cdot \boldsymbol{\tau}_3 \hat{r}_{23} \cdot \vec{\sigma}_1 \hat{r}_{12} \cdot \vec{\sigma}_2$
$\mathcal{G}_{13} = \boldsymbol{\tau}_2 \cdot \boldsymbol{\tau}_3 \vec{q}_3 \cdot \vec{\sigma}_1 \vec{q}_1 \cdot \vec{\sigma}_2$	$\tilde{\mathcal{G}}_{13} = \boldsymbol{\tau}_2 \cdot \boldsymbol{\tau}_3 \hat{r}_{12} \cdot \vec{\sigma}_1 \hat{r}_{23} \cdot \vec{\sigma}_2$
$\mathcal{G}_{14} = \boldsymbol{\tau}_2 \cdot \boldsymbol{\tau}_3 \vec{q}_3 \cdot \vec{\sigma}_1 \vec{q}_3 \cdot \vec{\sigma}_2$	$\tilde{\mathcal{G}}_{14} = \boldsymbol{\tau}_2 \cdot \boldsymbol{\tau}_3 \hat{r}_{12} \cdot \vec{\sigma}_1 \hat{r}_{12} \cdot \vec{\sigma}_2$
$\mathcal{G}_{15} = \boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_3 \vec{q}_2 \cdot \vec{\sigma}_1 \vec{q}_2 \cdot \vec{\sigma}_3$	$\tilde{\mathcal{G}}_{15} = \boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_3 \hat{r}_{13} \cdot \vec{\sigma}_1 \hat{r}_{13} \cdot \vec{\sigma}_3$
$\mathcal{G}_{16} = \boldsymbol{\tau}_2 \cdot \boldsymbol{\tau}_3 \vec{q}_3 \cdot \vec{\sigma}_2 \vec{q}_3 \cdot \vec{\sigma}_3$	$\tilde{\mathcal{G}}_{16} = \boldsymbol{\tau}_2 \cdot \boldsymbol{\tau}_3 \hat{r}_{12} \cdot \vec{\sigma}_2 \hat{r}_{12} \cdot \vec{\sigma}_3$
$\mathcal{G}_{17} = \boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_3 \vec{q}_1 \cdot \vec{\sigma}_1 \vec{q}_3 \cdot \vec{\sigma}_3$	$\tilde{\mathcal{G}}_{17} = \boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_3 \hat{r}_{23} \cdot \vec{\sigma}_1 \hat{r}_{12} \cdot \vec{\sigma}_3$
$\mathcal{G}_{18} = \boldsymbol{\tau}_1 \cdot (\boldsymbol{\tau}_2 \times \boldsymbol{\tau}_3) \vec{\sigma}_1 \cdot \vec{\sigma}_3 \vec{\sigma}_2 \cdot (\vec{q}_1 \times \vec{q}_3)$	$\tilde{\mathcal{G}}_{18} = \boldsymbol{\tau}_1 \cdot (\boldsymbol{\tau}_2 \times \boldsymbol{\tau}_3) \vec{\sigma}_1 \cdot \vec{\sigma}_3 \vec{\sigma}_2 \cdot (\hat{r}_{12} \times \hat{r}_{23})$
$\mathcal{G}_{19} = \boldsymbol{\tau}_1 \cdot (\boldsymbol{\tau}_2 \times \boldsymbol{\tau}_3) \vec{\sigma}_3 \cdot \vec{q}_1 \vec{q}_1 \cdot (\vec{\sigma}_1 \times \vec{\sigma}_2)$	$\tilde{\mathcal{G}}_{19} = \boldsymbol{\tau}_1 \cdot (\boldsymbol{\tau}_2 \times \boldsymbol{\tau}_3) \vec{\sigma}_3 \cdot \hat{r}_{23} \hat{r}_{23} \cdot (\vec{\sigma}_1 \times \vec{\sigma}_2)$
$\mathcal{G}_{20} = \boldsymbol{\tau}_1 \cdot (\boldsymbol{\tau}_2 \times \boldsymbol{\tau}_3) \vec{\sigma}_1 \cdot \vec{q}_1 \vec{\sigma}_3 \cdot \vec{q}_3 \vec{\sigma}_2 \cdot (\vec{q}_1 \times \vec{q}_3)$	$\tilde{\mathcal{G}}_{20} = \boldsymbol{\tau}_1 \cdot (\boldsymbol{\tau}_2 \times \boldsymbol{\tau}_3) \vec{\sigma}_1 \cdot \hat{r}_{23} \vec{\sigma}_3 \cdot \hat{r}_{12} \vec{\sigma}_2 \cdot (\hat{r}_{12} \times \hat{r}_{23})$

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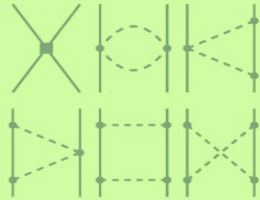
4N Force

5N Force

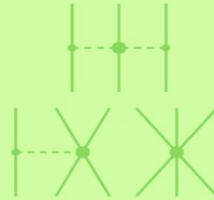
LO
 $(Q/\Lambda_\chi)^0$



NLO
 $(Q/\Lambda_\chi)^2$



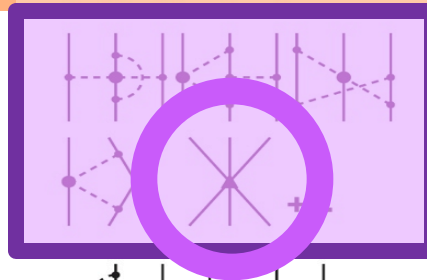
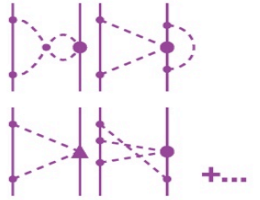
NNLO
 $(Q/\Lambda_\chi)^3$



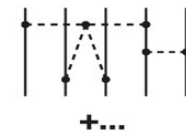
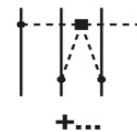
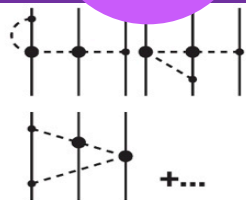
N³LO
 $(Q/\Lambda_\chi)^4$



N⁴LO
 $(Q/\Lambda_\chi)^5$



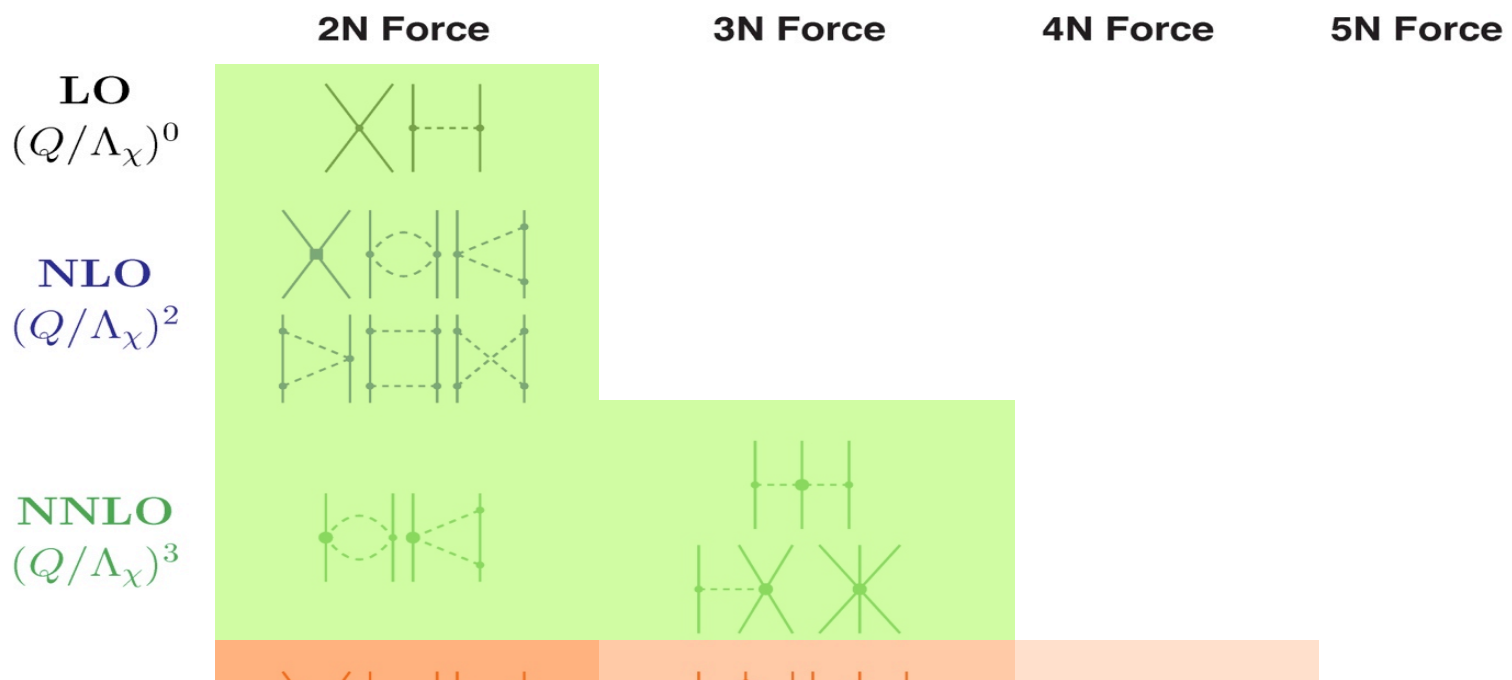
N⁵LO
 $(Q/\Lambda_\chi)^6$



Chiral Nuclear Interactions

Elba, 25 June 2019

R. Machleidt



3NF contacts at N4LO

Girlanda, Kievsky, Viviani, PRC 84, 014001 (2011)

$\mathbf{k}_i = \mathbf{p}_i - \mathbf{p}'_i$ and $\mathbf{Q}_i = \mathbf{p}_i + \mathbf{p}'_i$, \mathbf{p}_i and \mathbf{p}'_i being the initial and final momenta of nucleon i , the potential in momentum space is found to be

$$\begin{aligned}
 V = \sum_{i \neq j \neq k} & \left[-E_1 \mathbf{k}_i^2 - E_2 \mathbf{k}_i^2 \boldsymbol{\tau}_i \cdot \boldsymbol{\tau}_j - E_3 \mathbf{k}_i^2 \boldsymbol{\sigma}_i \cdot \boldsymbol{\sigma}_j - E_4 \mathbf{k}_i^2 \boldsymbol{\sigma}_i \cdot \boldsymbol{\sigma}_j \boldsymbol{\tau}_i \cdot \boldsymbol{\tau}_j \right. \\
 & - E_5 (3\mathbf{k}_i \cdot \boldsymbol{\sigma}_i \mathbf{k}_i \cdot \boldsymbol{\sigma}_j - \mathbf{k}_i^2) - E_6 (3\mathbf{k}_i \cdot \boldsymbol{\sigma}_i \mathbf{k}_i \cdot \boldsymbol{\sigma}_j - \mathbf{k}_i^2) \boldsymbol{\tau}_i \cdot \boldsymbol{\tau}_j \\
 & + \frac{i}{2} E_7 \mathbf{k}_i \times (\mathbf{Q}_i - \mathbf{Q}_j) \cdot (\boldsymbol{\sigma}_i + \boldsymbol{\sigma}_j) + \frac{i}{2} E_8 \mathbf{k}_i \times (\mathbf{Q}_i - \mathbf{Q}_j) \cdot (\boldsymbol{\sigma}_i + \boldsymbol{\sigma}_j) \boldsymbol{\tau}_j \cdot \boldsymbol{\tau}_k \\
 & \left. - E_9 \mathbf{k}_i \cdot \boldsymbol{\sigma}_i \mathbf{k}_j \cdot \boldsymbol{\sigma}_j - E_{10} \mathbf{k}_i \cdot \boldsymbol{\sigma}_i \mathbf{k}_j \cdot \boldsymbol{\sigma}_j \boldsymbol{\tau}_i \cdot \boldsymbol{\tau}_j \right], \tag{15}
 \end{aligned}$$

Including N4LO 3NF contacts, Girlanda et al.

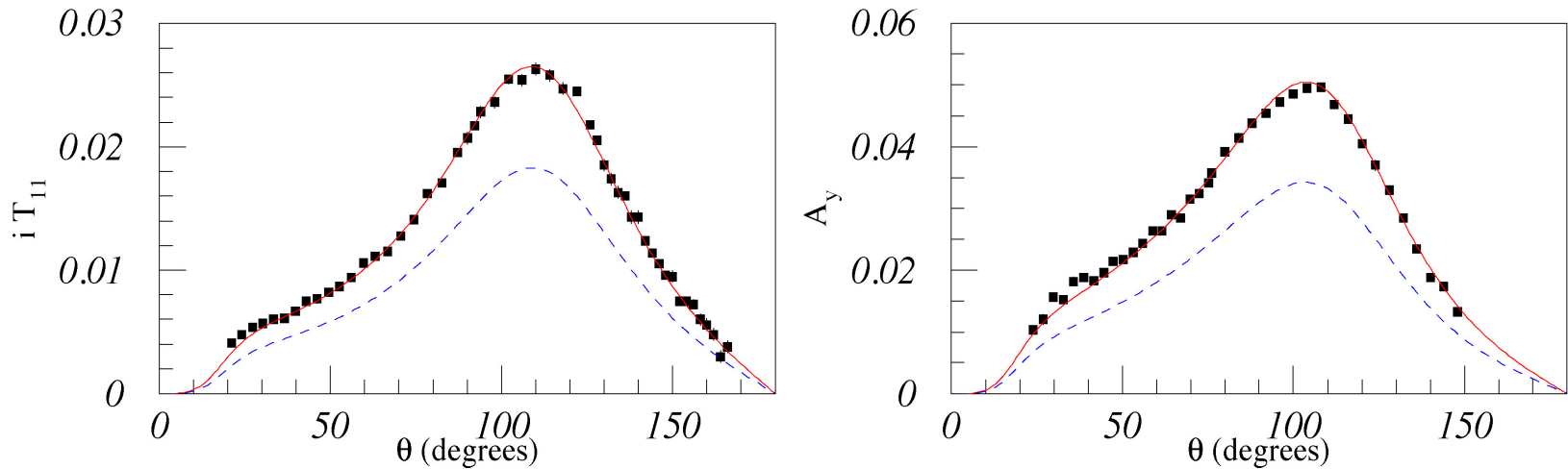


Figure 3: 8-parameter fit to $B(^3\text{H})$, $^2a_{Nd}$ and all considered $p-d$ scattering observables at 3 MeV proton energy, for $\Lambda = 300$ MeV. Blue dashed curves corresponding to the AV18 NN interaction, while the red solid ones include the fitted TNI.

2N Force

3N Force

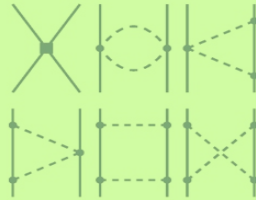
4N Force

5N Force

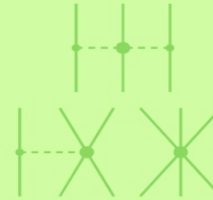
LO
 $(Q/\Lambda_\chi)^0$



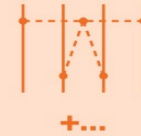
NLO
 $(Q/\Lambda_\chi)^2$



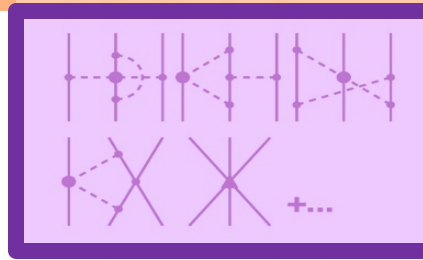
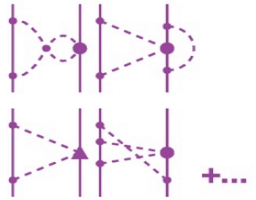
NNLO
 $(Q/\Lambda_\chi)^3$



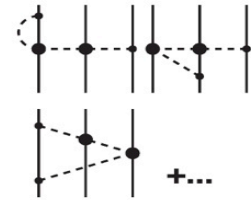
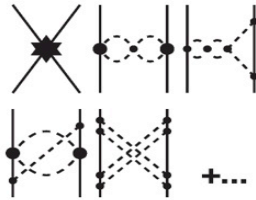
N³LO
 $(Q/\Lambda_\chi)^4$



N⁴LO
 $(Q/\Lambda_\chi)^5$



N⁵LO
 $(Q/\Lambda_\chi)^6$



Chiral Nuclear Interactions

Elba, 25 June 2019

R. Machleidt

2N Force

3N Force

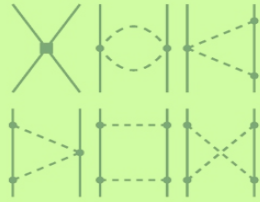
4N Force

5N Force

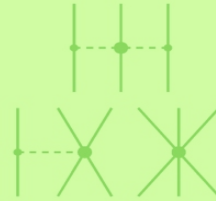
LO
 $(Q/\Lambda_\chi)^0$



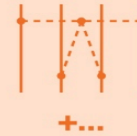
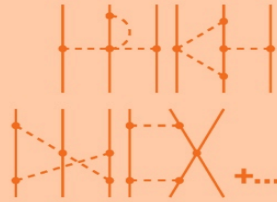
NLO
 $(Q/\Lambda_\chi)^2$



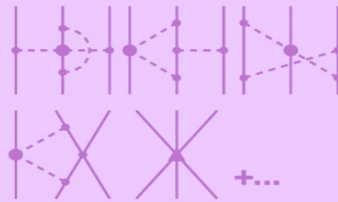
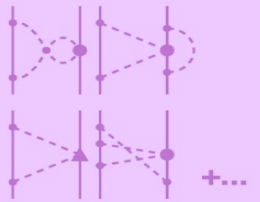
NNLO
 $(Q/\Lambda_\chi)^3$



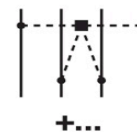
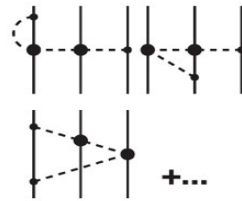
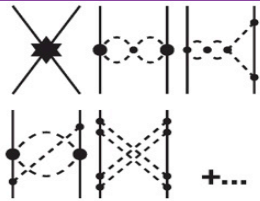
N³LO
 $(Q/\Lambda_\chi)^4$



N⁴LO
 $(Q/\Lambda_\chi)^5$



N⁵LO
 $(Q/\Lambda_\chi)^6$



Chiral Nuclear Interactions

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R. Machleidt

2N Force

3N Force

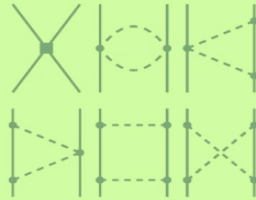
4N Force

5N Force

LO
 $(Q/\Lambda_\chi)^0$



NLO
 $(Q/\Lambda_\chi)^2$



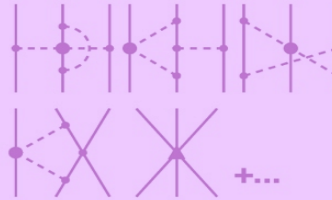
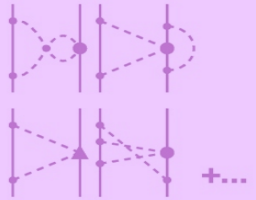
NNLO
 $(Q/\Lambda_\chi)^3$



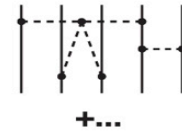
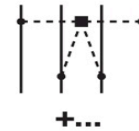
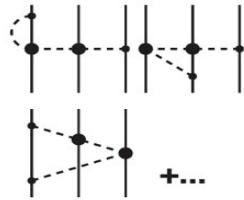
N³LO
 $(Q/\Lambda_\chi)^4$



N⁴LO
 $(Q/\Lambda_\chi)^5$



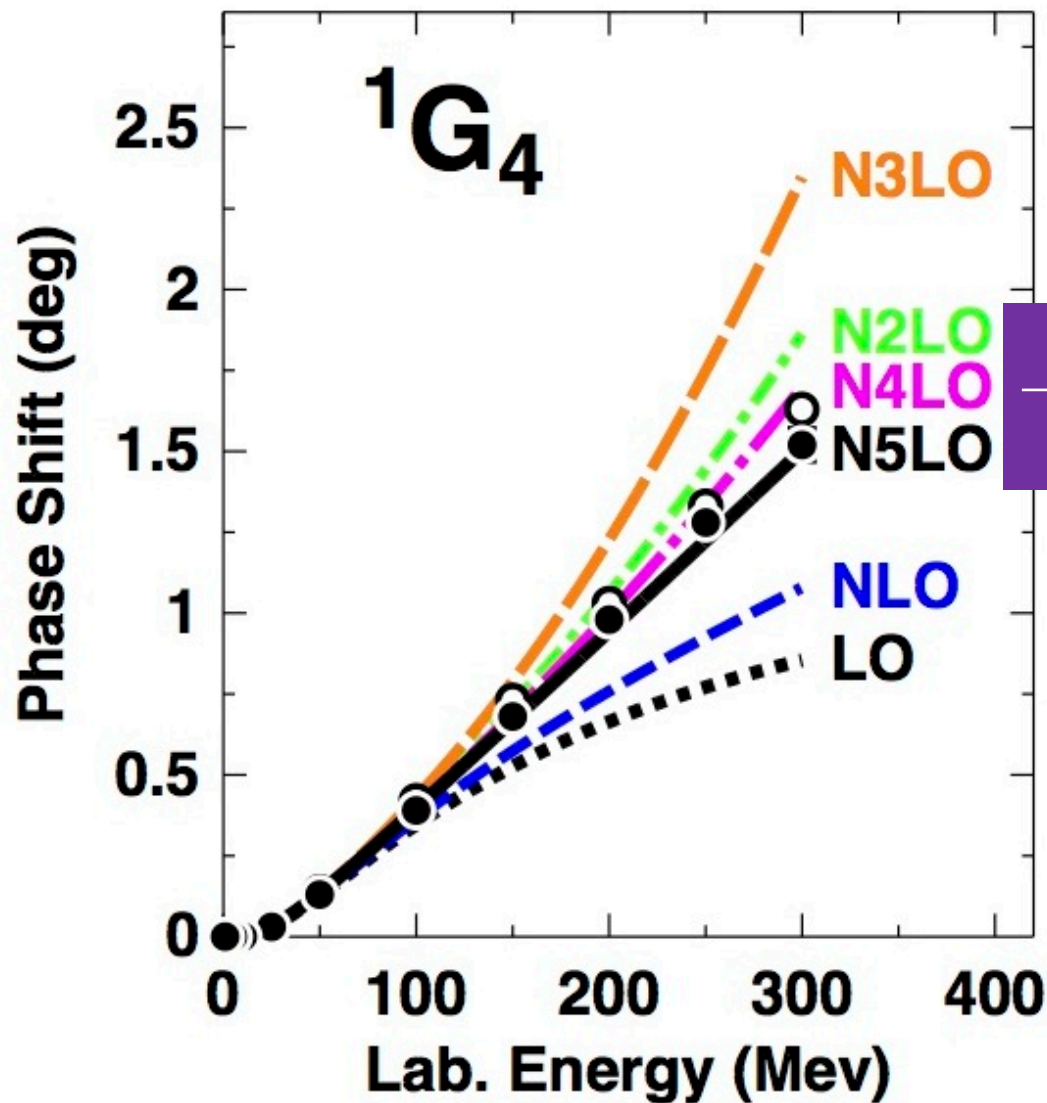
N⁵LO
 $(Q/\Lambda_\chi)^6$



Chiral Nuclear Interactions

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R. Machleidt



From Entem, Kaiser, Machleidt, Nosyk, PRC 92, 064001 (2015)

2N Force

3N Force

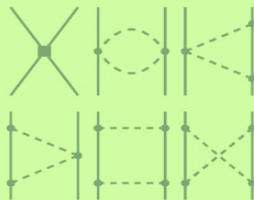
4N Force

5N Force

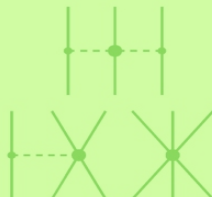
LO
 $(Q/\Lambda_\chi)^0$



NLO
 $(Q/\Lambda_\chi)^2$



NNLO
 $(Q/\Lambda_\chi)^3$



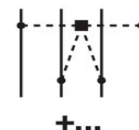
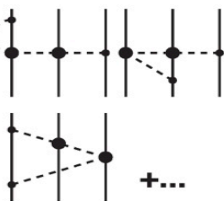
N³LO
 $(Q/\Lambda_\chi)^4$



N⁴LO
 $(Q/\Lambda_\chi)^5$



N⁵LO
 $(Q/\Lambda_\chi)^6$



**Status
 A.D.
 2019**

*The Map of the
 Chartered Waters
 Of the Forces*

AND SO, RECENTLY, POTENTIALS HAVE BEEN CONSTRUCTED UP TO N⁴LO BY ...

- Entem, Machleidt, Nosyk, PRC **96**, 024004 (2017); **non-local**.
- Reinert, Krebs, Epelbaum, Eur. Phys. J. A **54**, 86 (2018); **local**.

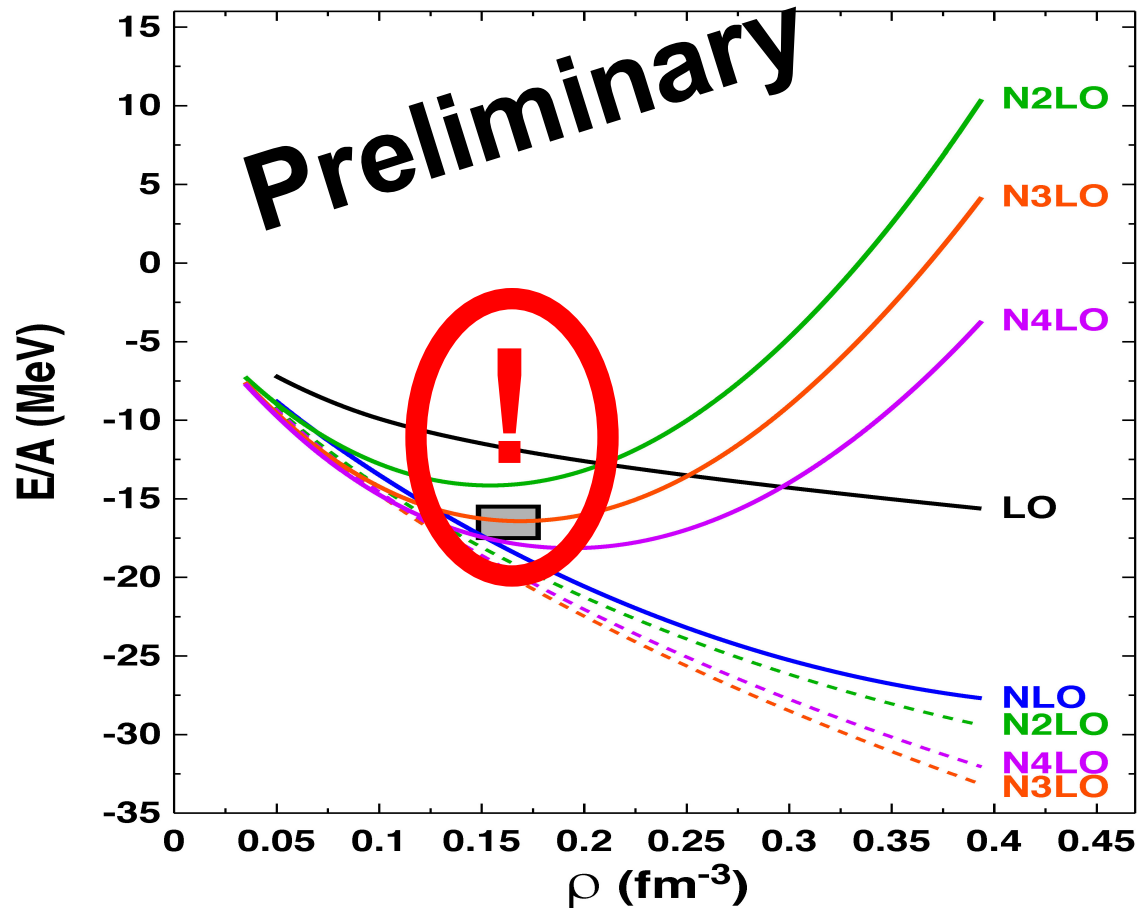
... with an excellent reproduction of the NN Data ...

TABLE V: χ^2/datum for the fit of the 2016 NN data base by NN potentials at various orders of chiral EFT ($\Lambda = 500$ MeV in all cases).

T_{lab} bin (MeV)	No. of data	LO	NLO	NNLO	N ³ LO	N ⁴ LO
proton-proton						
0-100	795	520	18.9	2.28	1.18	(Includes ct's in F-waves.)
0-190	1206	430	43.6	4.64	1.69	1.12
0-290	2132	360	70.8	7.60	2.09	1.21
neutron-proton						
0-100	1180	114	7.2	1.38	0.93	0.94
0-190	1697	96	23.1	2.29	1.10	1.06
0-290	2721	94	36.7	5.28	1.27	1.10
<i>pp</i> plus <i>np</i>						
0-100	1975	283	11.9	1.74	1.03	1.00
0-190	2898	285	31.6	2.87	1.25	1.08
0-290	4853	206	51.5	6.30	1.63	1.15

The above for Entem, Machleidt, Nosyk;
Reinert, Krebs, Epelbaum similar.

... and the following nuclear matter saturation properties ...

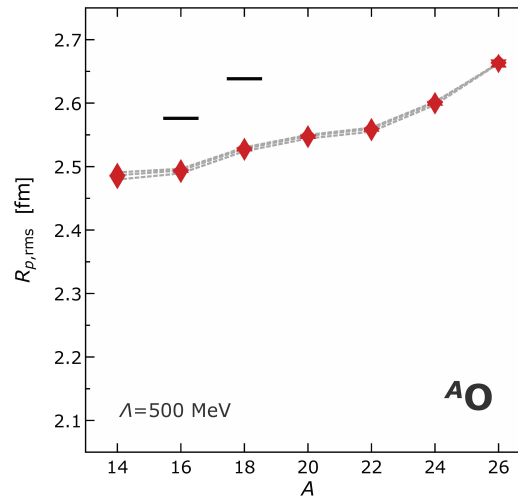
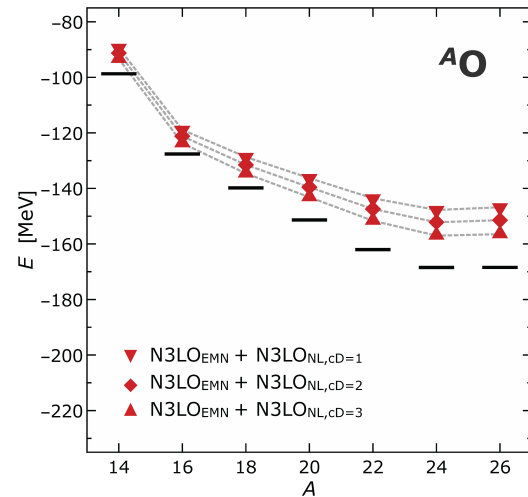


Applying the Entem, Machleidt, Nosyk potentials.

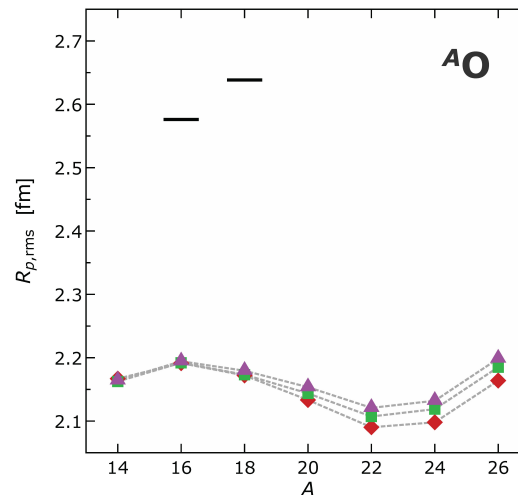
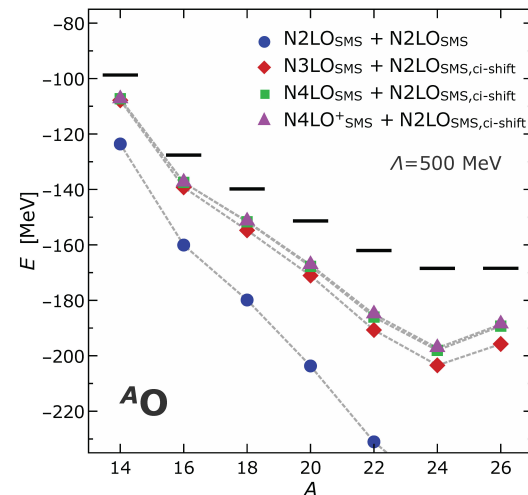
From F. Sammarruca *et al.*, to be published. R. Machleidt

... and the following properties of finite nuclei ...

(Calculations by R. Roth et al., Darmstadt)



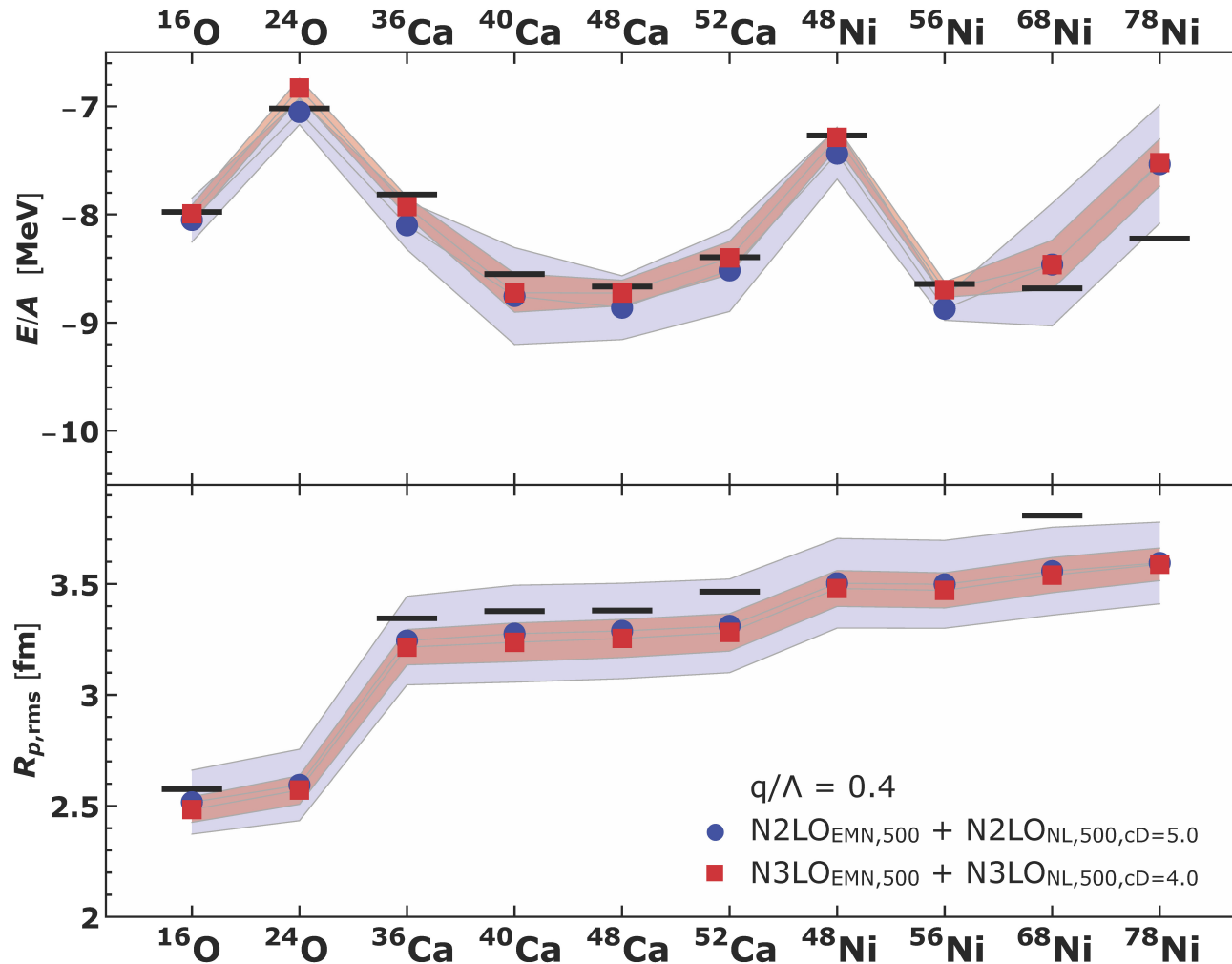
Applying the
Entem, Machleidt, Nosyk
Potentials which are
Non-local



Applying the
Reinert, Krebs, Epelbaum
Potentials which are
Local

... and more properties of finite nuclei ...

(Calculations by R. Roth et al., Darmstadt)



Applying the
Entem,
Machleidt,
Nosyk
Potentials which
are
Non-local

CONCLUSIONS

- Recently, there has been tremendous progress in the development of better nuclear forces based upon chiral EFT.
- Very quantitative NN potentials up to N4LO are available now.
- First applications in intermediate-mass nuclei show that the **non-local versions are very successful**, while **the local versions fail**.
- Further applications of the **successfully tested potentials** to issues like momentum distributions and short-range correlations (SRC) is now called for.

THE
NUCLEAR FORCE
IN THE

III. MILLENIUM

AFTER JESUS CHRIST :

a **Status Report**

R. MACHLEIDT
U. of IDAHO

ECBA
JUNE 26-30, 2000

THE PROGRAM FOR THE NEW MILLENIUM

For a reliable derivation of
nuclear forces, we need

- a basic theory
 χ eff. field theory ✓
- that is amenable to calculations

χ PTh ✓

- yields quantitative results. ✓

~~Let's hope for it!~~

THE PROGRAM FOR THE NEW MILLENIUM

For a reliable derivation of
nuclear forces, we need

- a basic theory
off. field theory

Mission accomplished

that is amenable to calculations

χ PT

- yields quantitative results.

~~Let's hope for it!~~