

# SM&FT 2019

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AND NONPERTURBATIVE FIELD THEORY

## *Challenges in Computational Theoretical Physics*

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## **How phase transitions trigger the emergence of Collective Intelligence in human groups? An experimental investigation**

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# Collective Intelligence

- **Ability** of human groups to perform well on a variety of tasks (Woolley et al. 2010)
- Literature focuses on **determinants** and processes leading to its emergence (Woolley et al., 2015; De Vincenzo et al. 2017; Massari, Giannoccaro, Carbone 2018)
- Decision-making models inspired by statistical physics are able to capture its emergence (Carbone, Giannoccaro 2005, De Vincenzo, Carbone, Giannoccaro 2017)



# The model of collective decision making

- **$M$  interacting members** solve a combinatorial problem: finding the vector of choices on decisions, i.e.  $d = (d_1, d_2, \dots, d_N)$ , with the highest fitness value  $V$  on a complex landscape
- The state vector of the whole system results as  $\mathbf{s} = (\mathbf{s}_1, \mathbf{s}_2, \dots, \mathbf{s}_N) = (\sigma_1^1, \sigma_2^1, \dots, \sigma_M^1, \dots, \sigma_1^N, \sigma_2^N, \dots, \sigma_M^N)$
- The **Hamiltonian** of the system is defined as:

$$H(\mathbf{s}) = -\frac{1}{2} J A I \mathbf{s} \cdot \mathbf{s} - \rho V(\mathbf{s}) = -\frac{1}{2} J \sum_{ij} A_{ij} I_{ij} s_i s_j - \rho V(\mathbf{s})$$

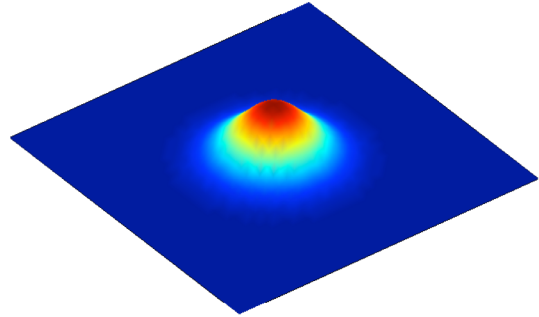
# The dynamics

$$\frac{dP(\mathbf{s}, t)}{dt} = - \sum_l w(\mathbf{s}_l \rightarrow \mathbf{s}'_l) P(\mathbf{s}_l, t) + \sum_l w(\mathbf{s}'_l \rightarrow \mathbf{s}_l) P(\mathbf{s}'_l, t)$$

$$w(\mathbf{s}_l \rightarrow \mathbf{s}'_l) = \frac{1}{2} \left[ 1 - s_l \tanh \left( \frac{\beta J}{\langle \kappa \rangle} \sum_h A_{lh} I_{lh} s_h \right) \right] \times \exp \{ \beta' [\Delta V(\mathbf{s}'_l, \mathbf{s}_l)] \}$$

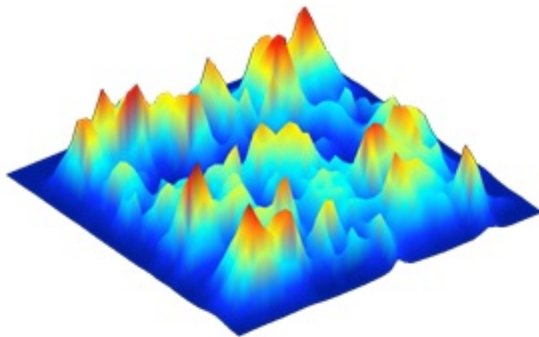
- $\beta$  is the inverse of social temperature
- $J$  is the coupling constant of social interactions
- $A = A_{lh}$  is a N-block adjacency matrix describing who interacts with whom
- $\beta'$  is related to the degree of uncertainty associated with the knowledge of the fitness landscape (the higher  $\beta'$ , the less the uncertainty)
- $\Delta V(\mathbf{s}'_l, \mathbf{s}_l)$  is the change in pay-off perceived by member  $i$  when the opinion flips from  $s'_l$  to  $s_l$

# Group Performance



## Features of a NK Kauffman landscape:

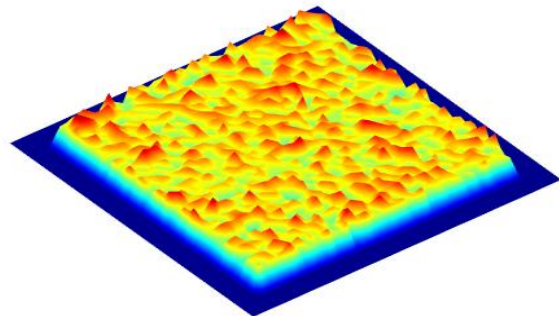
- $N$  – Number of binary decisions
- $K$  – Number of interacting decisions
- $\mathbf{d}_k = (d_1, d_2, \dots, d_N)$ , the vector of decision values, made by  $k$ -th agent
- The pay-off function  $V(\mathbf{d})$  associates a fitness value to each vector  $\mathbf{d}$



## Group Performance:

$$V(\mathbf{d}) = \frac{1}{N} \sum_{j=1}^N W_j \left( d_j, d_1^j, d_2^j, \dots, d_K^j \right)$$

**FITNESS**

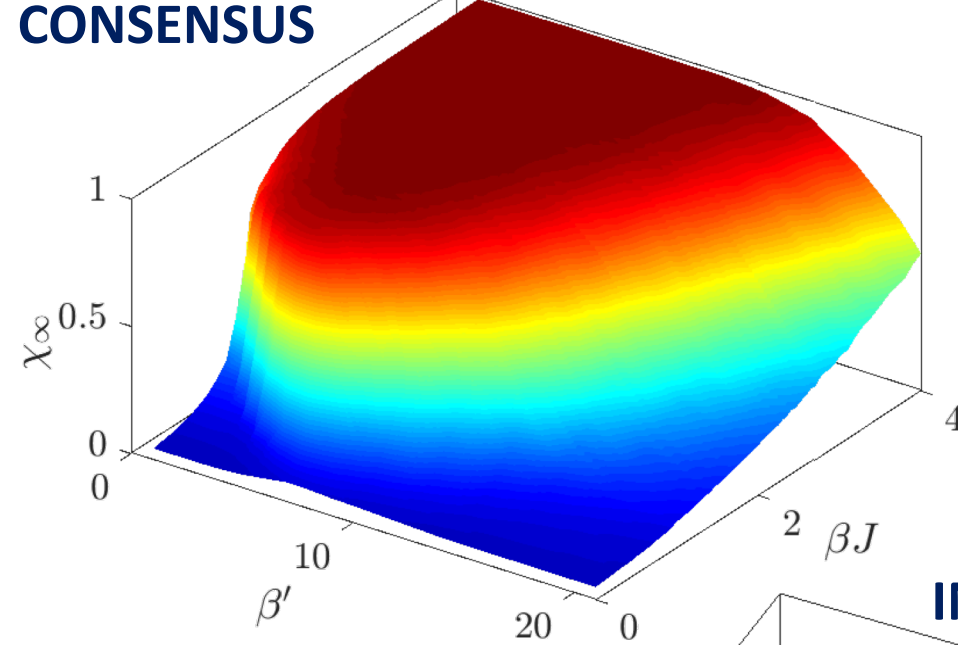
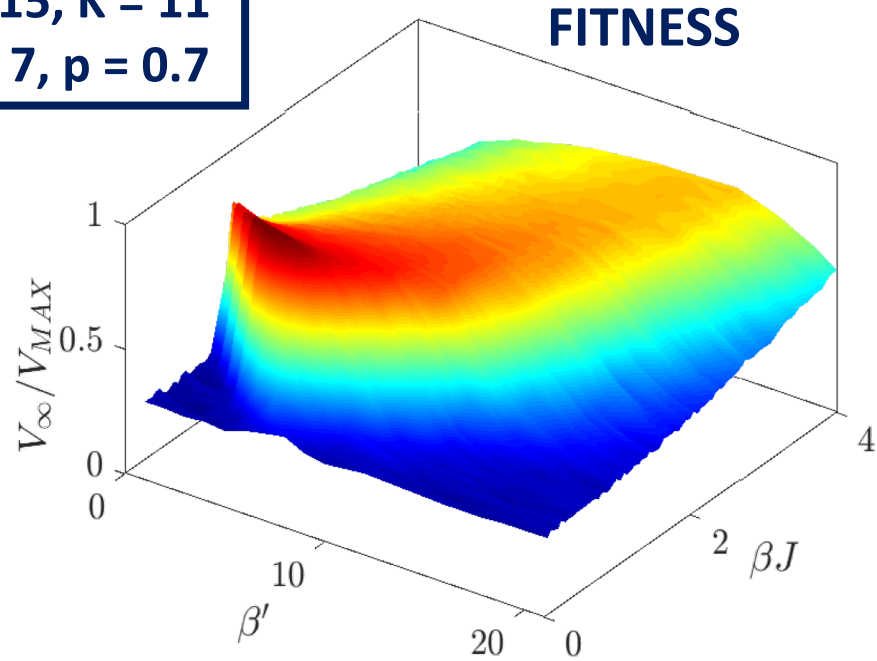


$$\langle C(t) \rangle = \frac{1}{M^2 N} \sum_{j=1}^N \sum_{kh=1}^M \langle \sigma_k^j(t) \sigma_h^j(t) \rangle$$

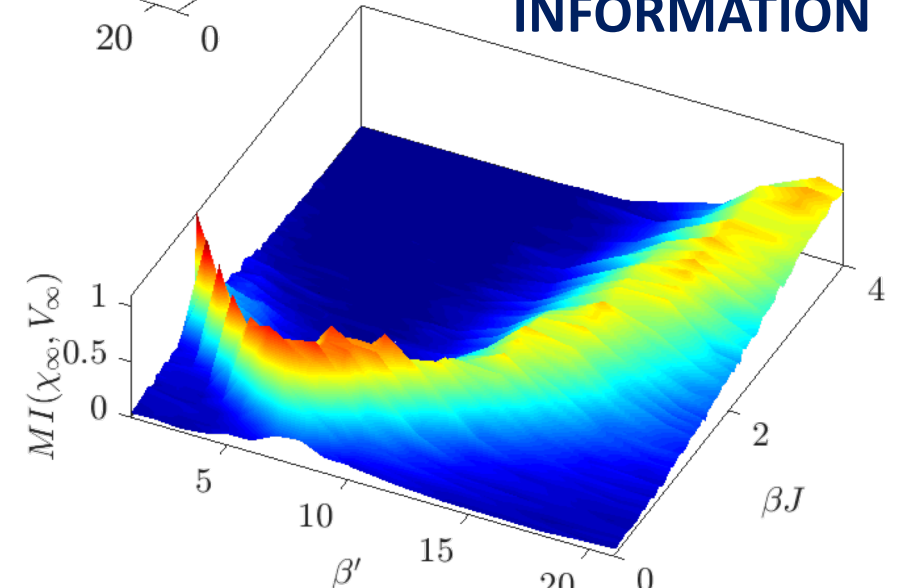
**CONSENSUS**

# The emergence of CI

$N = 15, K = 11$   
 $M = 7, p = 0.7$



**MUTUAL INFORMATION**



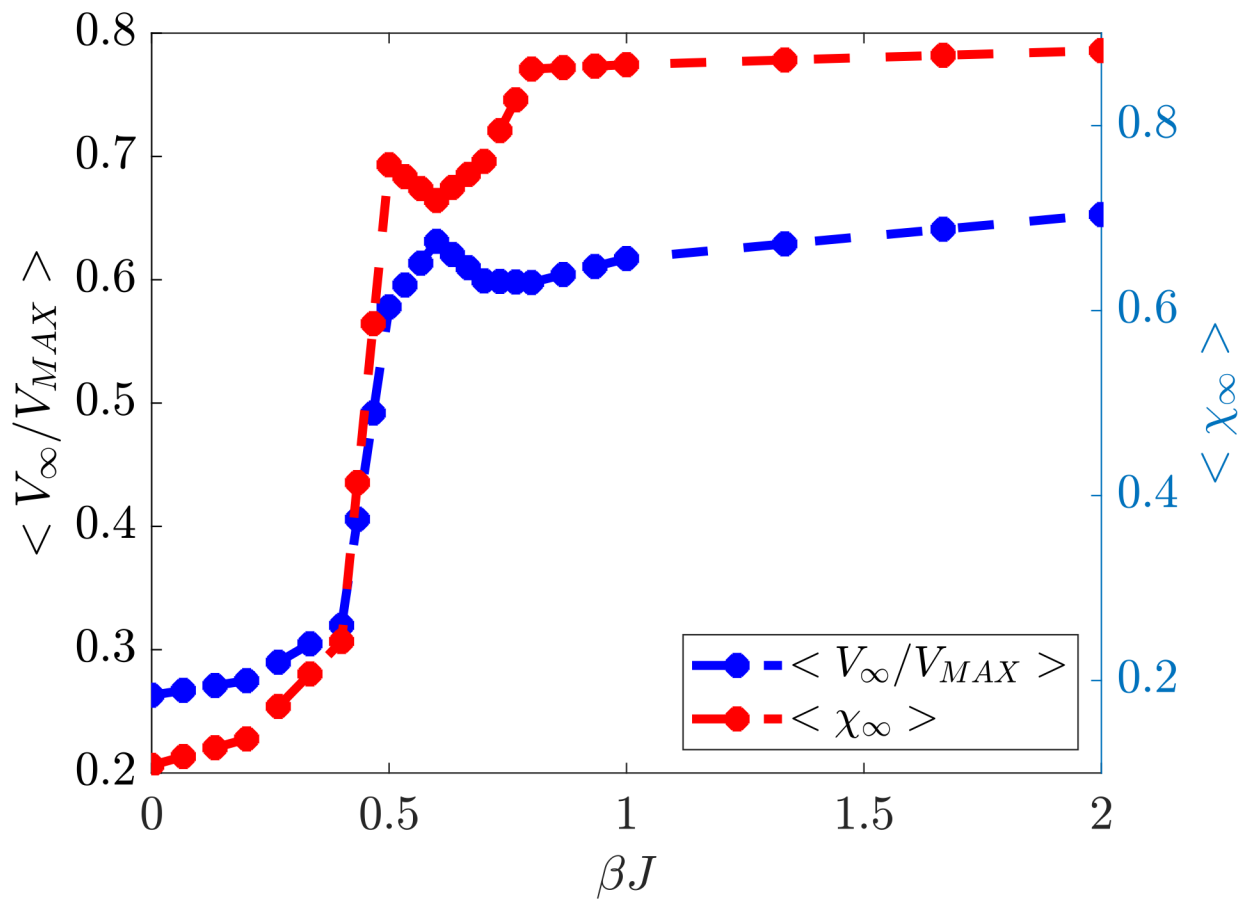
- **Critical conditions** ( $\beta', \beta J$ ) lead to a phase transition of the consensus value. A similar step increase is observed on group fitness value
- The **collective intelligence region**, where the group achieves its highest fitness value, is located close the minimum point ( $\beta'_{min}, \beta J_{min}$ ) of the U-shaped critical front

# The research aim

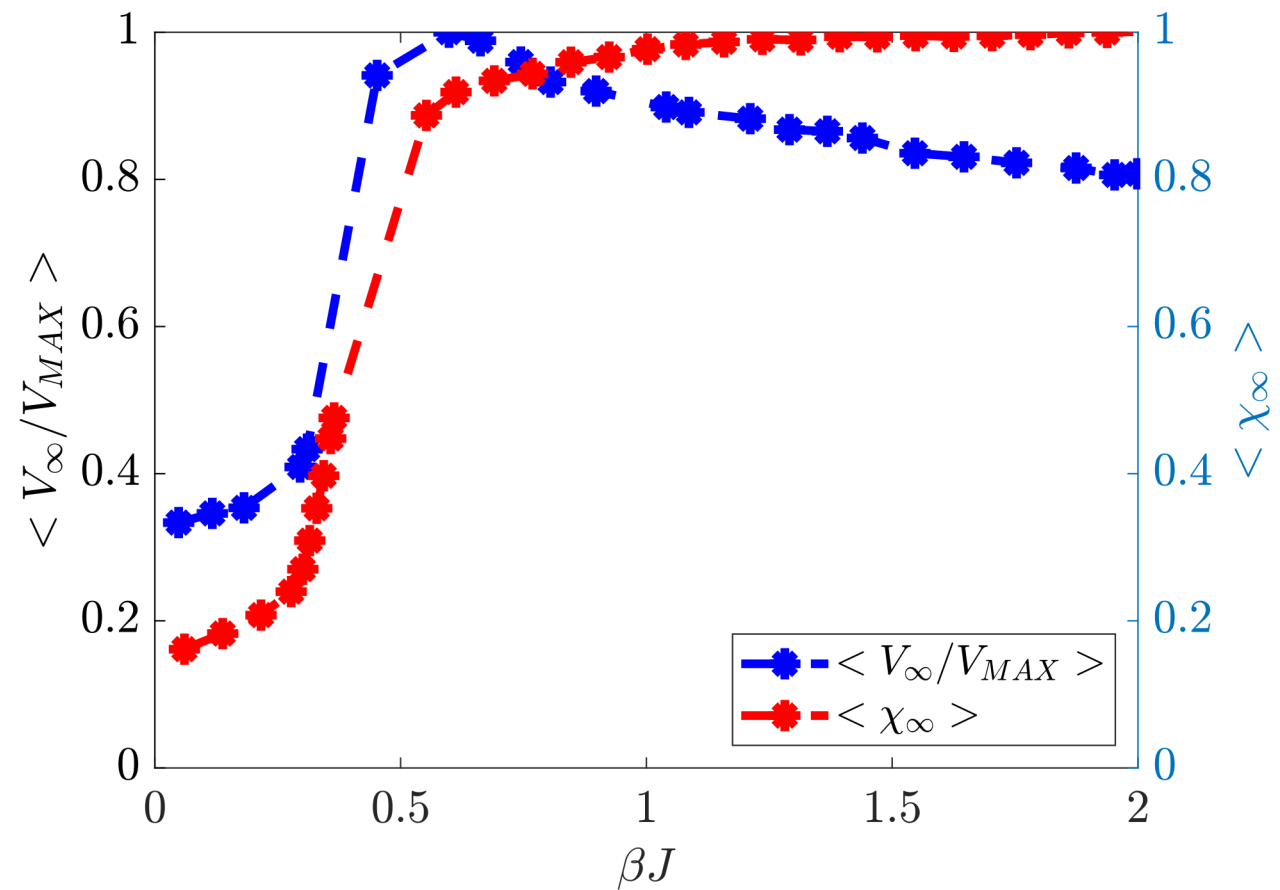
- To perform behavioural experiments of group decision-making that mimic the DMM
- To investigate whether and how the strength of social interaction influences the group performance

# The emergence of CI ...

## EXPERIMENTS



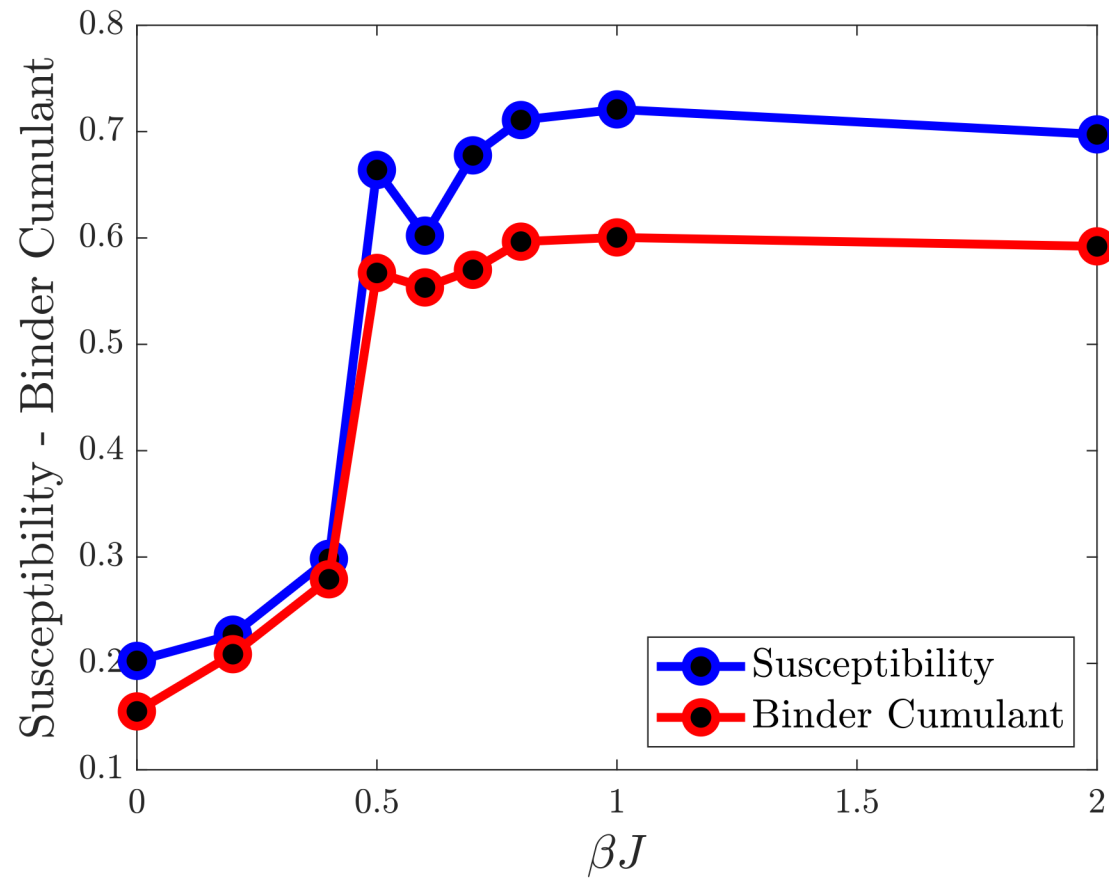
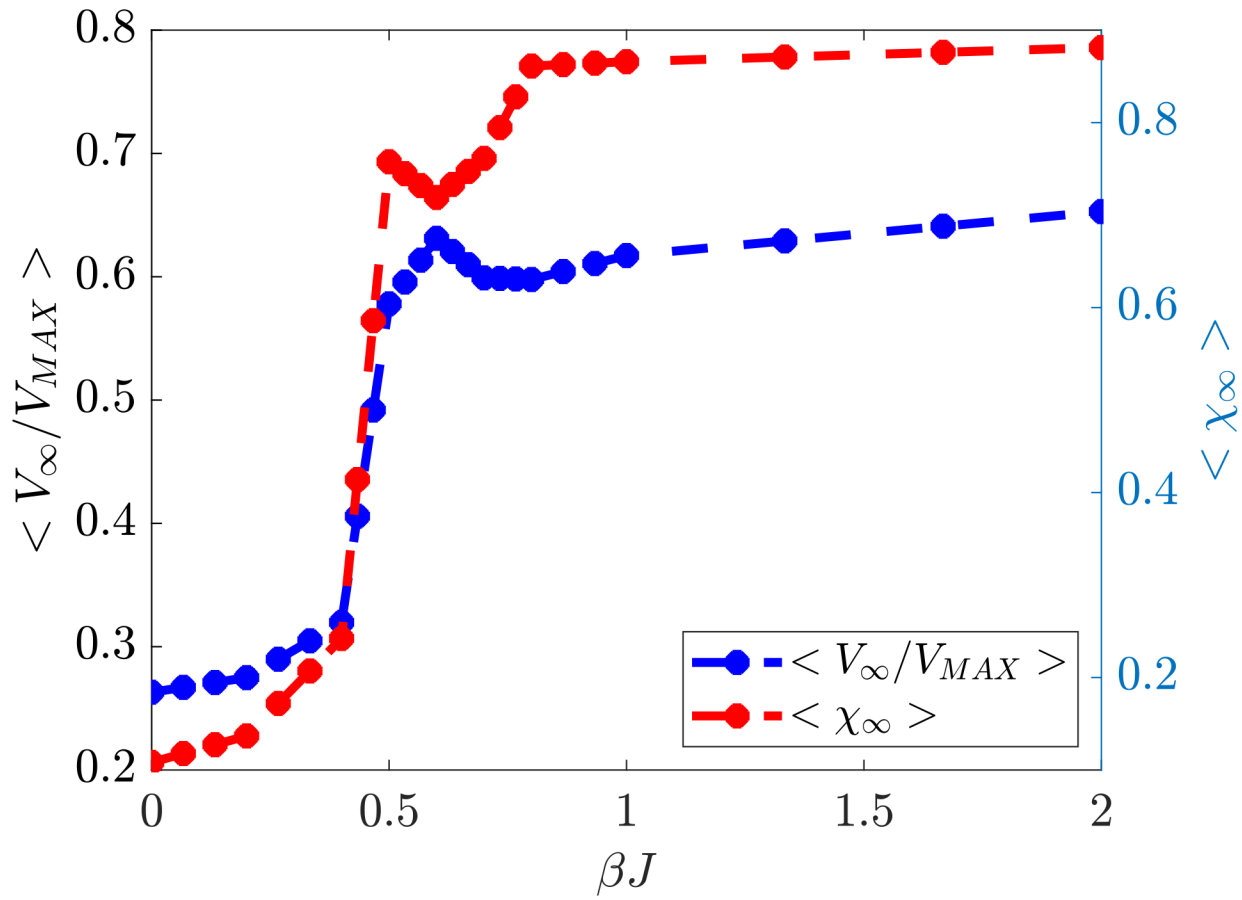
## MODEL





# ... with signs of criticality

## EXPERIMENTS



# Conclusions

- We performed behavioural experiments of group decision-making on real human groups to investigate whether and how the strength of social interaction influences the group performance
- The strength of social interaction affects the group performance. At criticality, a phase transition from low to high values of the level of consensus and a similar steep increase in the group fitness occur
- Further investigations will be devoted to studying the phenomenon of *groupthink* that occurs in highly-interacting groups

# Collective Intelligence Research Group



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**Thanks to all ...**