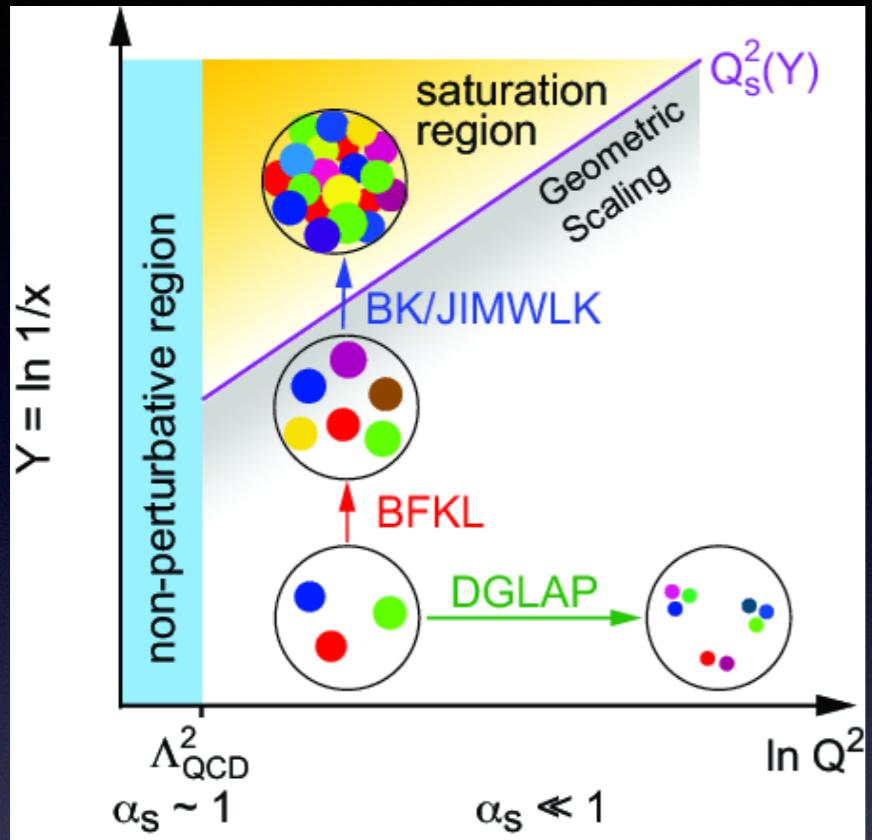


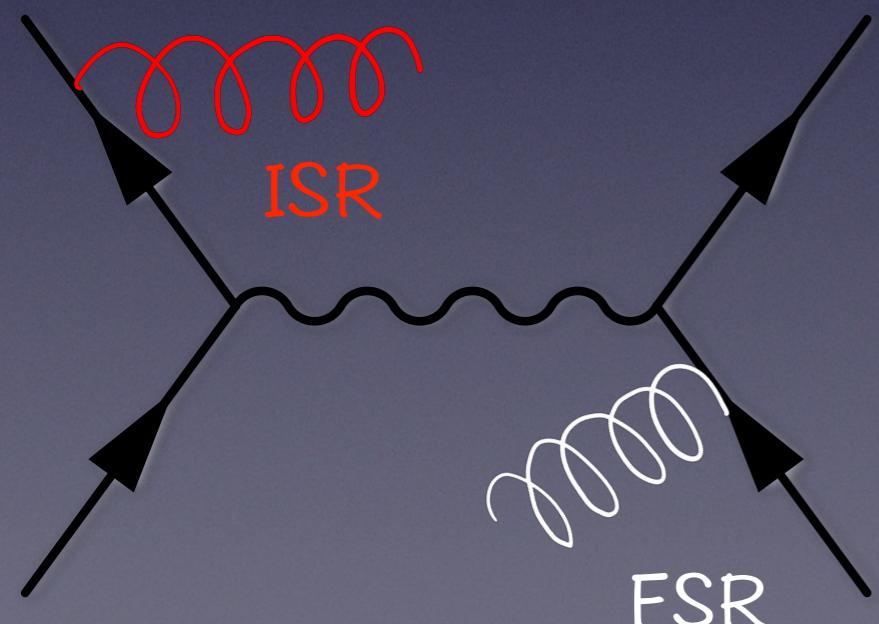
Measurement of Initial State Radiation @ CDF

Geumbong Yu for CDF Collaboration
Seoul National University

QCD in hadron collider



- Hadron is a complex bound state of quarks and gluons, and their dynamics (QCD) is a non-abelian gauge group theory, SU(3)
- Hadron collisions at high energy bring a variety of gluon radiation before and after the hard scattering
 - Initial state radiation (ISR): space-like shower, radiation from the incoming quarks
 - Final state radiation (FSR): time-like shower, radiation from the outgoing partons
- QCD evolves depending on which direction you look at:
 - Focus on the QCD evolution with Q^2 via the DGLAP equation: MC generators employ this evolution

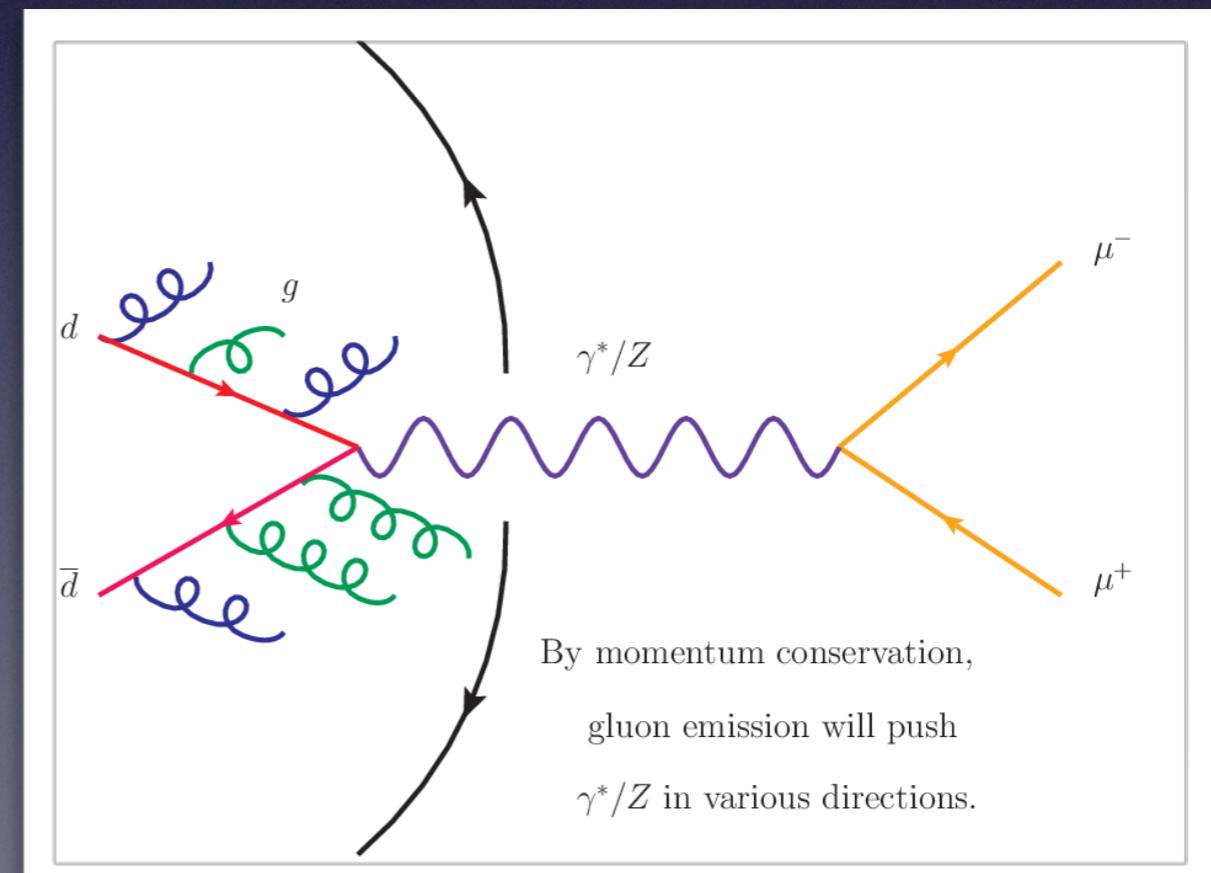


$$\frac{dq(x, Q^2)}{d \log Q^2} = \frac{\alpha_S(Q^2)}{2\pi} \int_x^1 \frac{dy}{y} q(y, Q^2) P\left(\frac{x}{y}\right)$$

Parton density Splitting function

ISR measurement using Drell-Yan

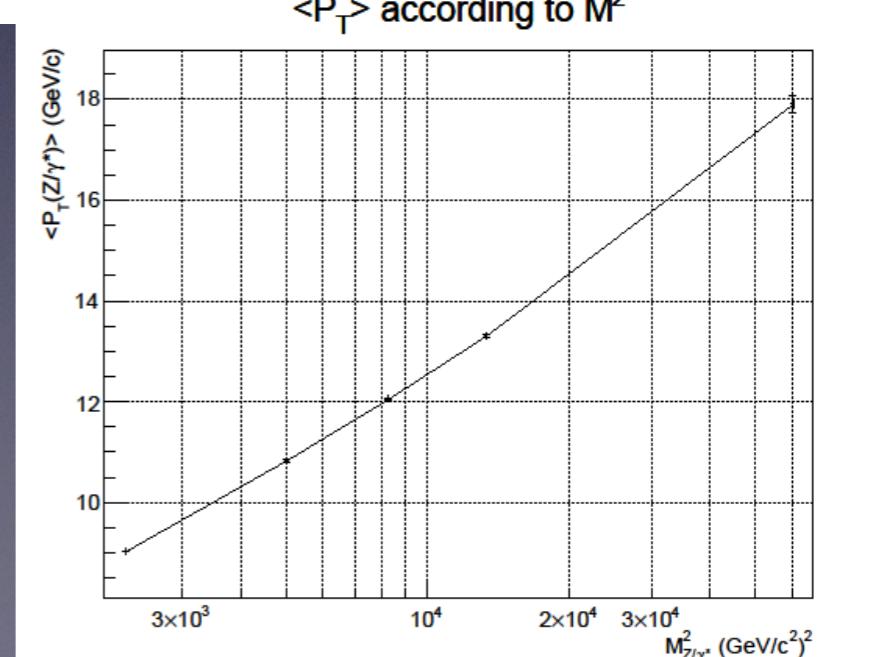
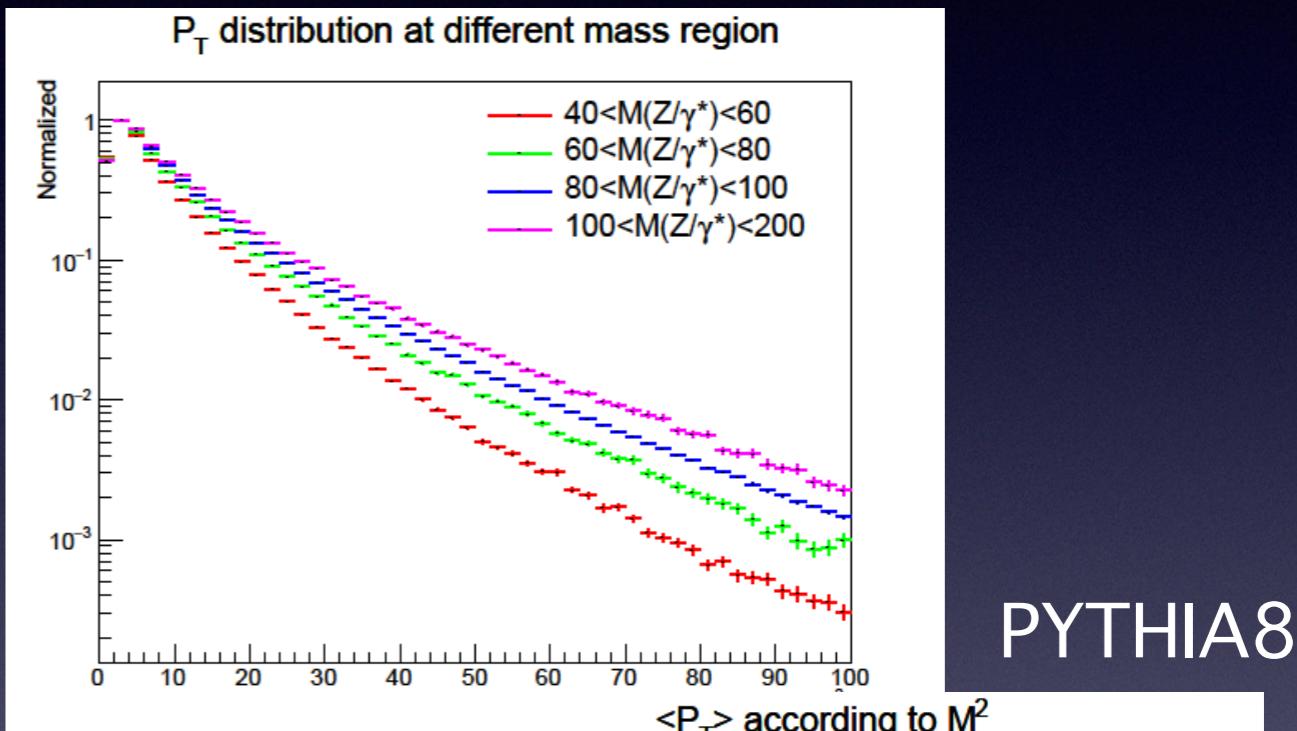
- QCD Initial State Radiation (ISR) has been a well-known but least-studied subject ever since the HERA experiments
 - Analyses deal with the inevitable uncertainty from ISR
- This measurement quantifies the effect of ISR as a function of collision energy and gives an idea of estimating the ISR for any physics processes at high energy collision
- Drell-Yan $Z/\gamma^* \rightarrow l^+l^-$ process restricts the gluon radiation being originated from incoming quarks
 - The transverse momentum of the process is a good observable to quantify the ISR



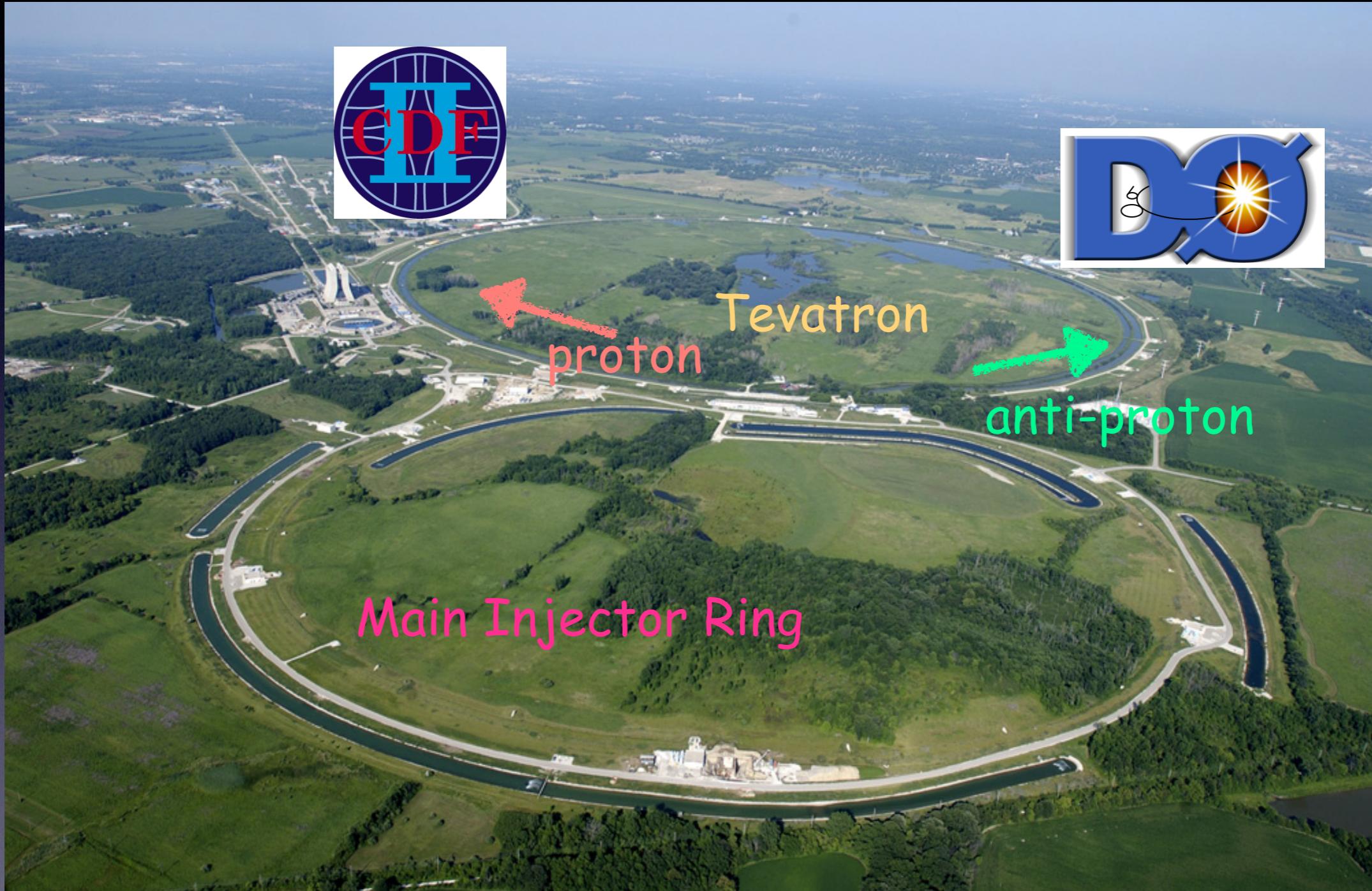
Strategy of the Measurement

$$\frac{dq(x, Q^2)}{d \log Q^2} = \frac{\alpha_S(Q^2)}{2\pi} \int_x^1 \frac{dy}{y} q(y, Q^2) P\left(\frac{x}{y}\right) \rightarrow \frac{\langle p_T^{\ell\ell} \rangle}{\log \langle m_{\ell\ell}^2 \rangle}$$

- The Drell-Yan mass square (m_{\parallel}^2) corresponds to the Q^2
- The amount of ISR is quantified by $\langle p_T^{\parallel} \rangle$
- Assumption is that the $\langle p_T^{\parallel} \rangle$ grows as the m_{\parallel} goes higher in the DY sample
- For simplifying the relation
 - Use 5 DY mass bins (GeV) for $\langle p_T^{\parallel} \rangle$: [40,60,80,100,200,350]
 - Too hard ISR removed: $p_T^{\parallel} < 100$ GeV



Collider Detector at Fermilab @ Tevatron



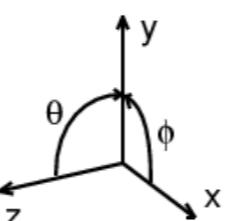
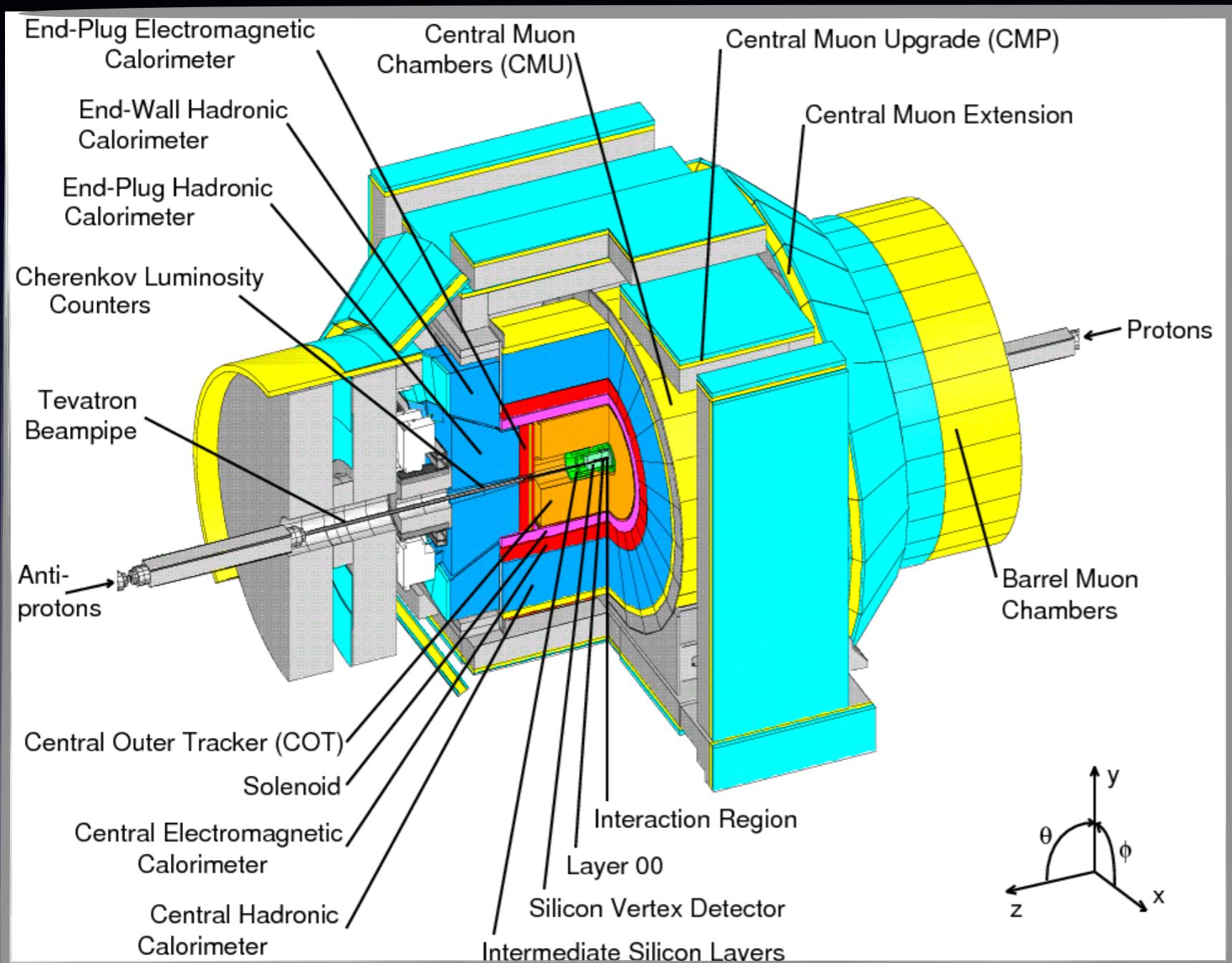
Run2 operation 1/3/2001—30/9/2011



Tevatron delivered $\sim 12 \text{ fb}^{-1}$ to each experiment, $\sim 10 \text{ fb}^{-1}$ recorded



The CDF II detector



Muon Chambers	$ n $ Coverage
CMU/CMP	<0.6
CMX	0.6–1.0
BMU	1.0–1.5

EM Calorimeter	$ n $ Coverage
Central	<1.1
End-Plug	1.1–3.64

<https://doi.org/10.1016/j.nima.2013.07.015>

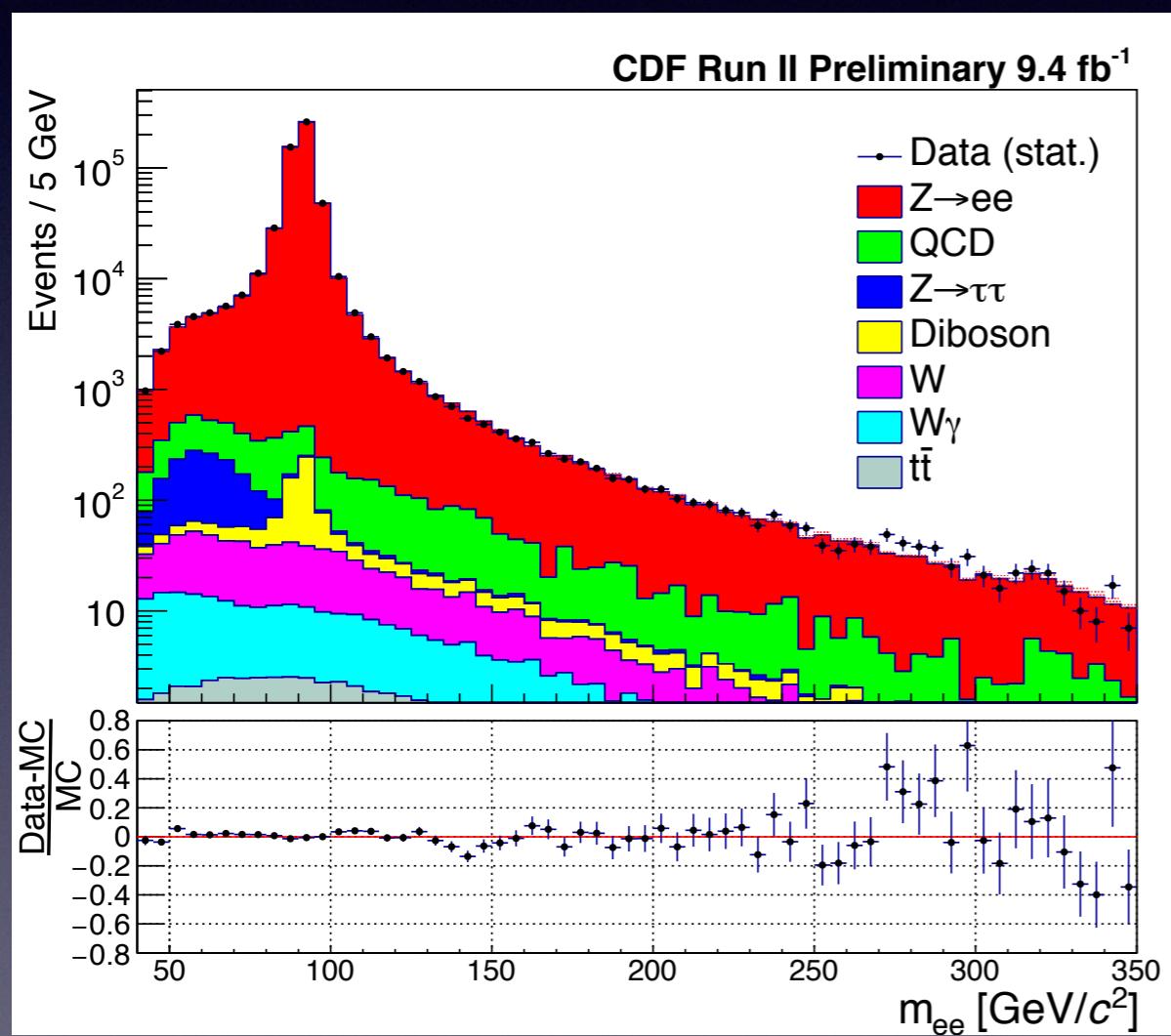
DiLepton Event Selection

CDF Run II data (9.4 fb⁻¹) with proton-antiproton collisions at 1.96 TeV

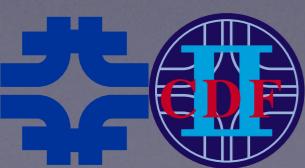
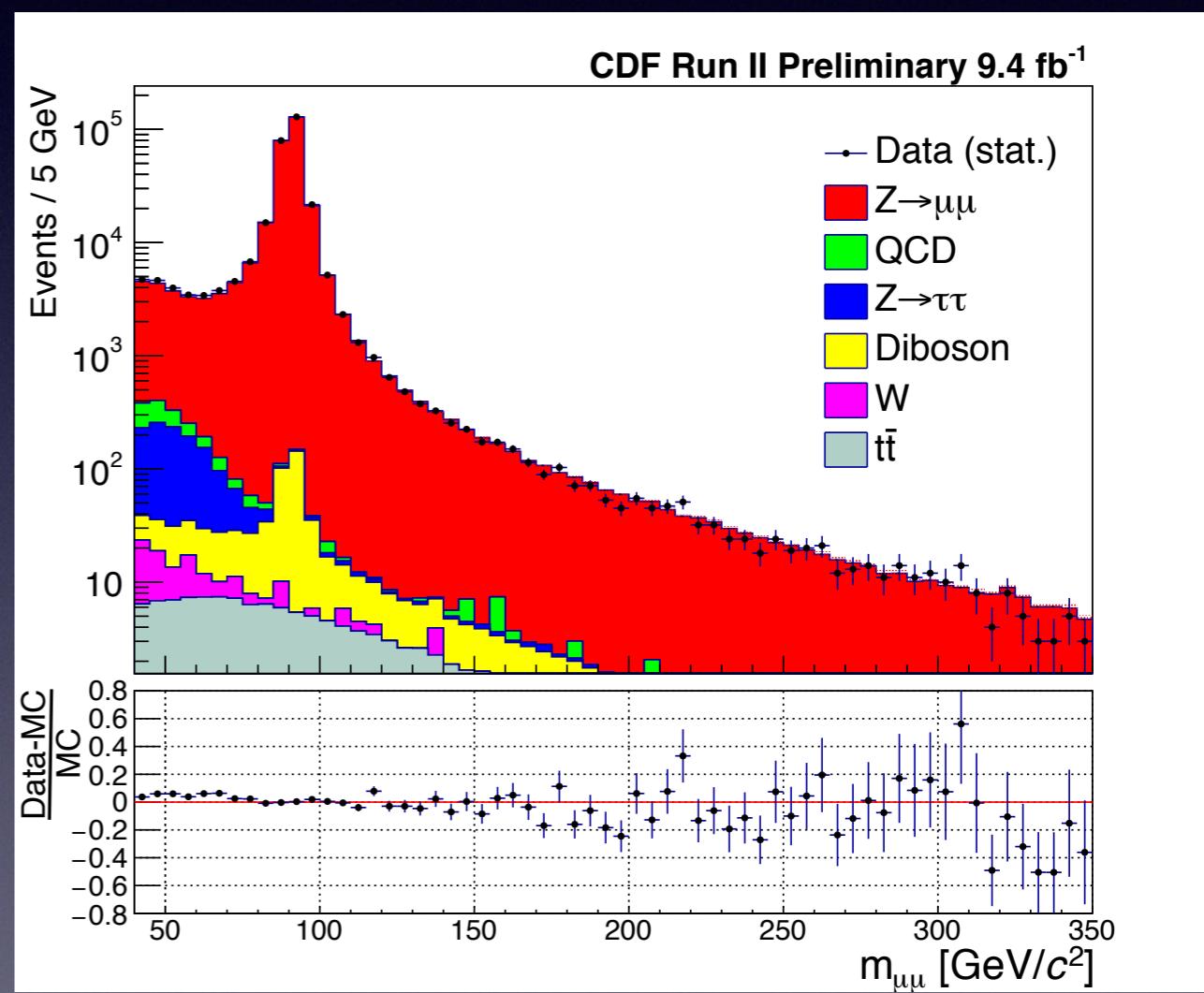
	$\mu\mu$ channel	ee channel
Trigger	Single Muon	Single Electron double e/ γ
Lepton	Opposite signed $\mu\mu$ <ul style="list-style-type: none"> - $p_T(\mu 1) > 20$ GeV - $p_T(\mu 2) > 12$ GeV - $\eta < 1.5$ 	Central-Central <ul style="list-style-type: none"> - Opposite signed - $p_T(e 1, e 2) > 25, 15$ GeV, $0.05 < \eta < 1.05$ Central-Plug <ul style="list-style-type: none"> - Central: $p_T > 20$ GeV, $0.05 < \eta < 1.05$ - Plug: $p_T > 20$ GeV, $1.2 < \eta < 2.8$ Plug-Plug <ul style="list-style-type: none"> - $p_T(e 1, e 2) > 25$ GeV, $1.2 < \eta < 2.8$ - Require electron pair from same side
Event Cut	$p_T(\mu\mu) < 100$ GeV	$p_T(ee) < 100$ GeV, Missing $E_T < 40$ GeV, FSR cut*
Background	CDF simulation (PYTHIA6): $Z \rightarrow \tau\tau, W, W\gamma, \text{dibosons}, tt$ Data-driven: multi-jet QCD	
Additional corrections	Number of vertex / Vertex position / Lepton energy/momentun / Z boson p_T^*	

DiLepton Mass

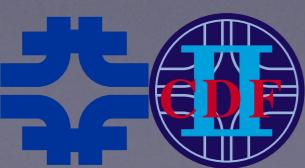
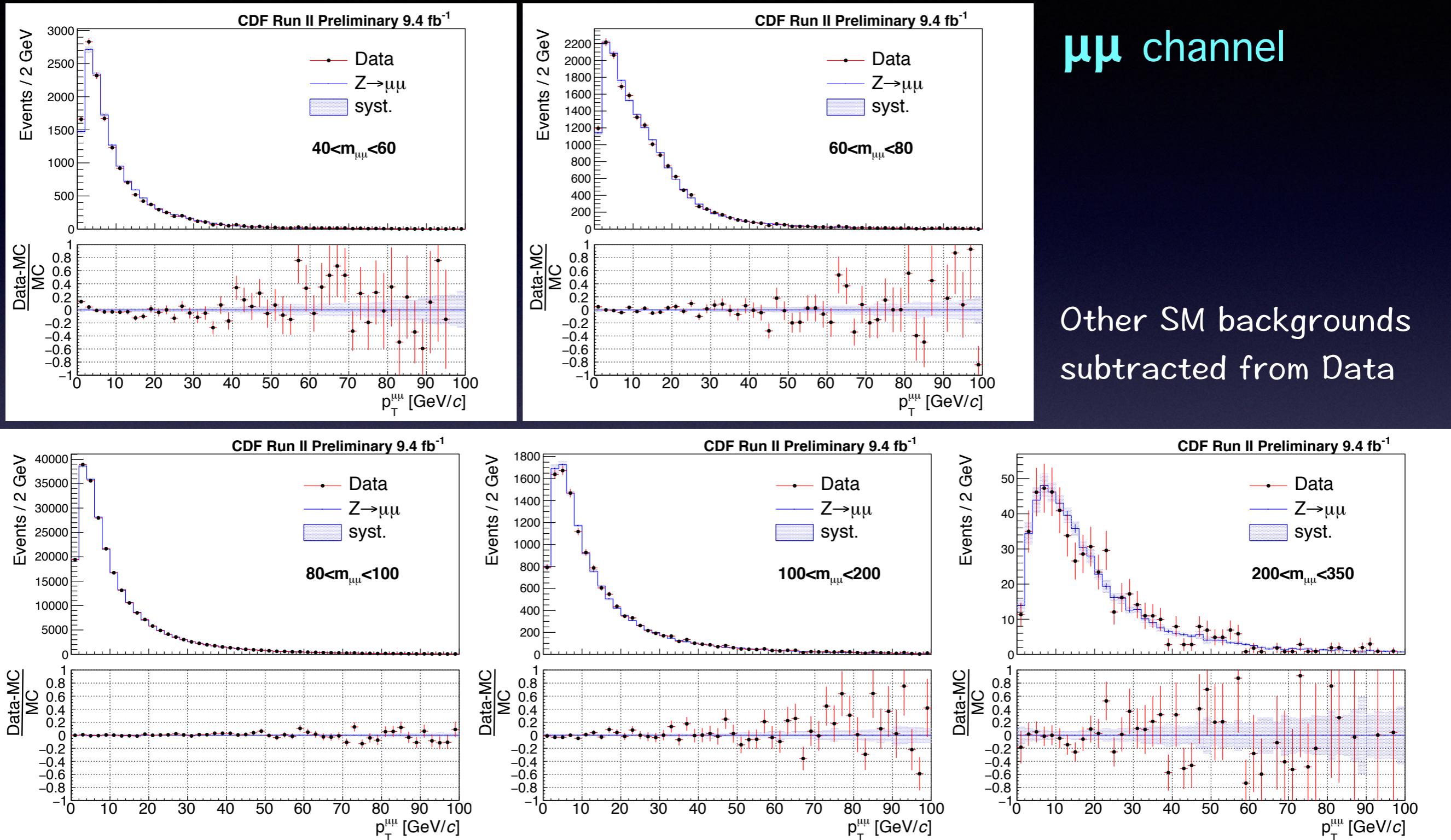
ee channel



$\mu\mu$ channel



DiLepton PT



Correction: reconstruction → generator

- Correction derived from Drell-Yan MonteCarlo sample:

- Multiplicative correction factor

- Reconstruction → generator level

$$\langle p_T \rangle_{data}^{corr.} = \boxed{\frac{\langle p_T \rangle_{MC}^{gen.}}{\langle p_T \rangle_{MC}^{reco.}}} \times \langle p_T \rangle_{data}^{reco.}$$

- The correction includes:

- Removing the effect from detector resolution and efficiency
 - Restoring the missing momentum due to QED FSR
 - Acceptance

Systematic Uncertainties

$\mu\mu$ channel

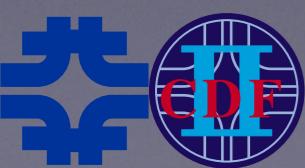
	Mass bin (GeV)	[40,60]	[60,80]	[80,100]	[100,200]	[200,350]
Statistical Unc.(%)	0.96	0.73	0.22	0.95	3.79	
Systematic Unc.(%)	1.31	1.33	0.26	0.91	2.84	
ISR model	0.93	0.93	0.24	0.52	2.38	
QED FSR model	0.87	0.93	0.03	0.18	0.41	
Momentum scale	0.11	0.13	0.04	0.20	0.85	
Momentum resolution	0.07	0.06	0.08	0.68	1.20	
Background norm.	0.28	0.10	0.03	0.16	0.25	

ee channel

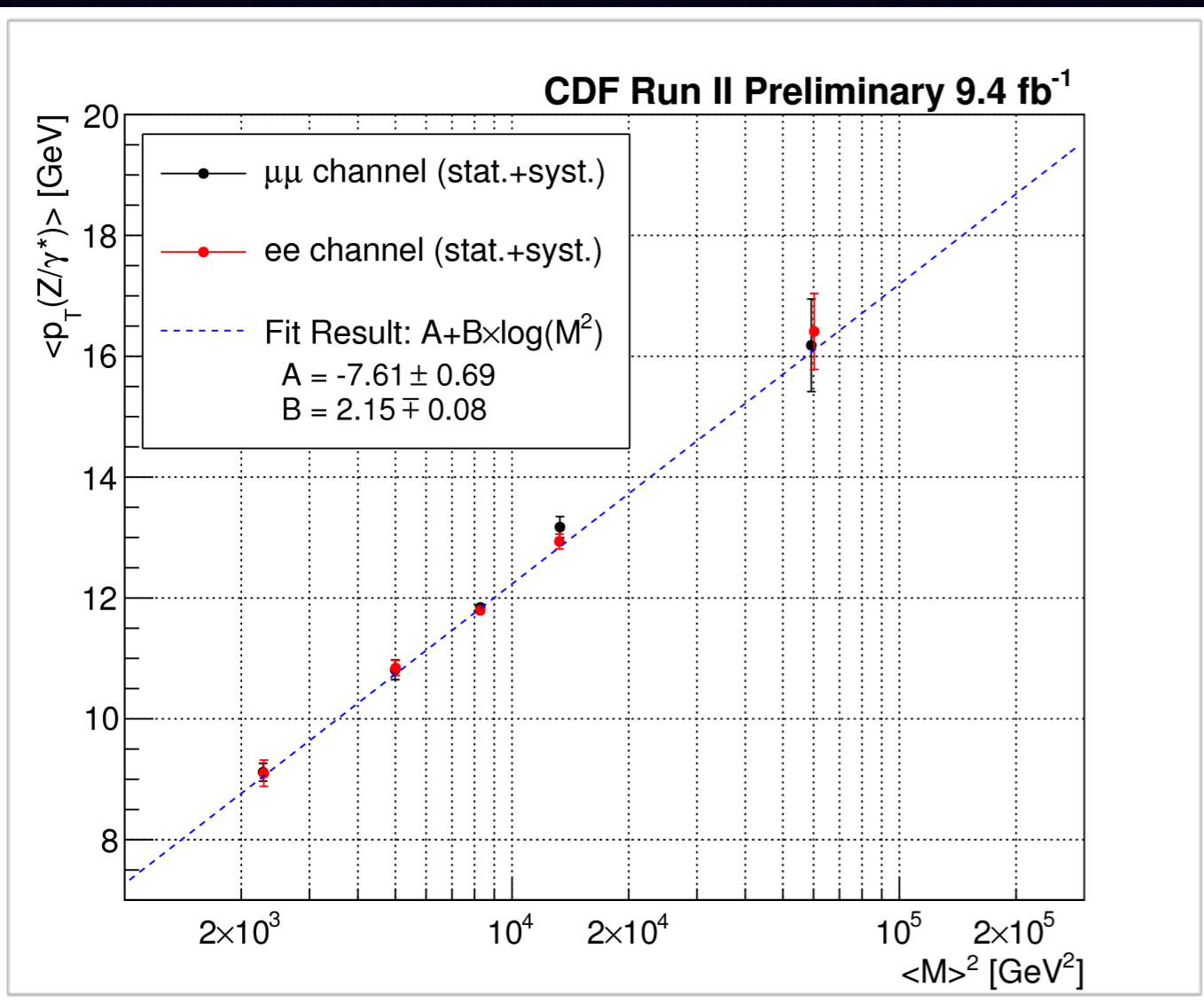
	Mass bin (GeV)	[40,60]	[60,80]	[80,100]	[100,200]	[200,350]
Statistical Unc.(%)	1.38	0.70	0.16	0.72	3.44	
Systematic Unc.(%)	1.96	0.91	0.17	0.63	1.67	
ISR model	1.26	0.51	0.13	0.15	1.07	
QED FSR model	1.39	0.72	0.05	0.22	0.67	
Energy scale	0.11	0.07	0.02	0.08	0.21	
Energy resolution	0.02	0.02	0.08	0.10	0.15	
Background norm.	0.57	0.21	0.03	0.56	1.06	

Dominant Sources:

- ISR model: variation of Z boson p_T correction
- QED FSR model: comparison between PYTHIA6 and PHOTOS++



Results



μμ channel

(GeV)

Mass bin	$\langle m_{DY} \rangle \pm \text{stat.} \pm \text{syst.}$	$\langle p_T \rangle \pm \text{stat.} \pm \text{syst.}$
[40,60]	$47.72 \pm 0.05 \pm 0.04$	$9.12 \pm 0.09 \pm 0.12$
[60,80]	$70.66 \pm 0.04 \pm 0.07$	$10.81 \pm 0.08 \pm 0.14$
[80,100]	$90.99 \pm 0.01 \pm 0.08$	$11.84 \pm 0.03 \pm 0.03$
[100,200]	$115.29 \pm 0.18 \pm 0.14$	$13.17 \pm 0.12 \pm 0.12$
[200,350]	$243.33 \pm 1.63 \pm 0.41$	$16.18 \pm 0.61 \pm 0.46$

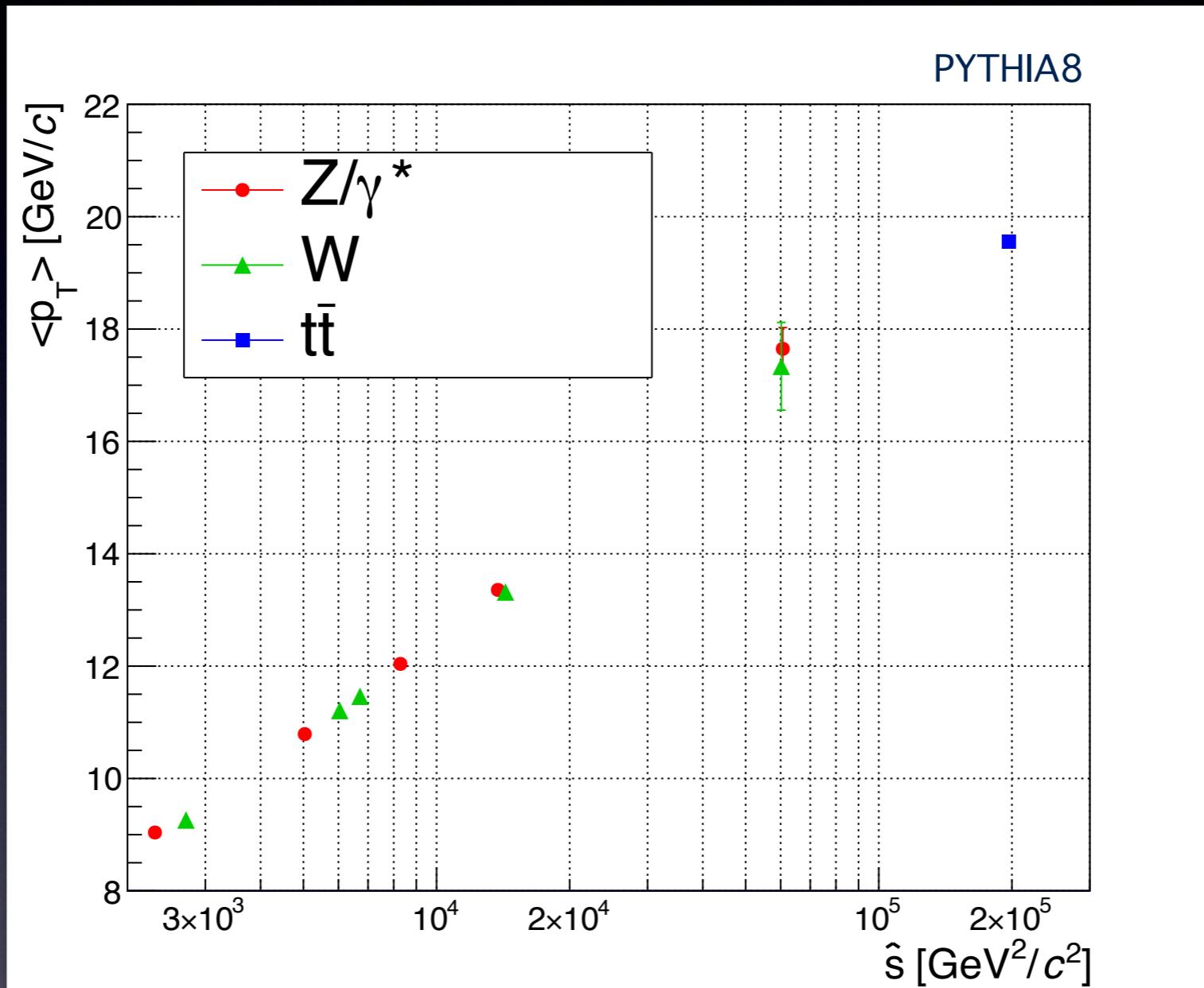
ee channel

(GeV)

Mass bin	$\langle m_{DY} \rangle \pm \text{stat.} \pm \text{syst.}$	$\langle p_T \rangle \pm \text{stat.} \pm \text{syst.}$
[40,60]	$47.83 \pm 0.05 \pm 0.07$	$9.10 \pm 0.13 \pm 0.18$
[60,80]	$70.76 \pm 0.04 \pm 0.04$	$10.84 \pm 0.08 \pm 0.10$
[80,100]	$90.98 \pm 0.01 \pm 0.07$	$11.79 \pm 0.02 \pm 0.02$
[100,200]	$115.11 \pm 0.13 \pm 0.14$	$12.93 \pm 0.09 \pm 0.08$
[200,350]	$245.46 \pm 1.29 \pm 0.36$	$16.41 \pm 0.56 \pm 0.27$

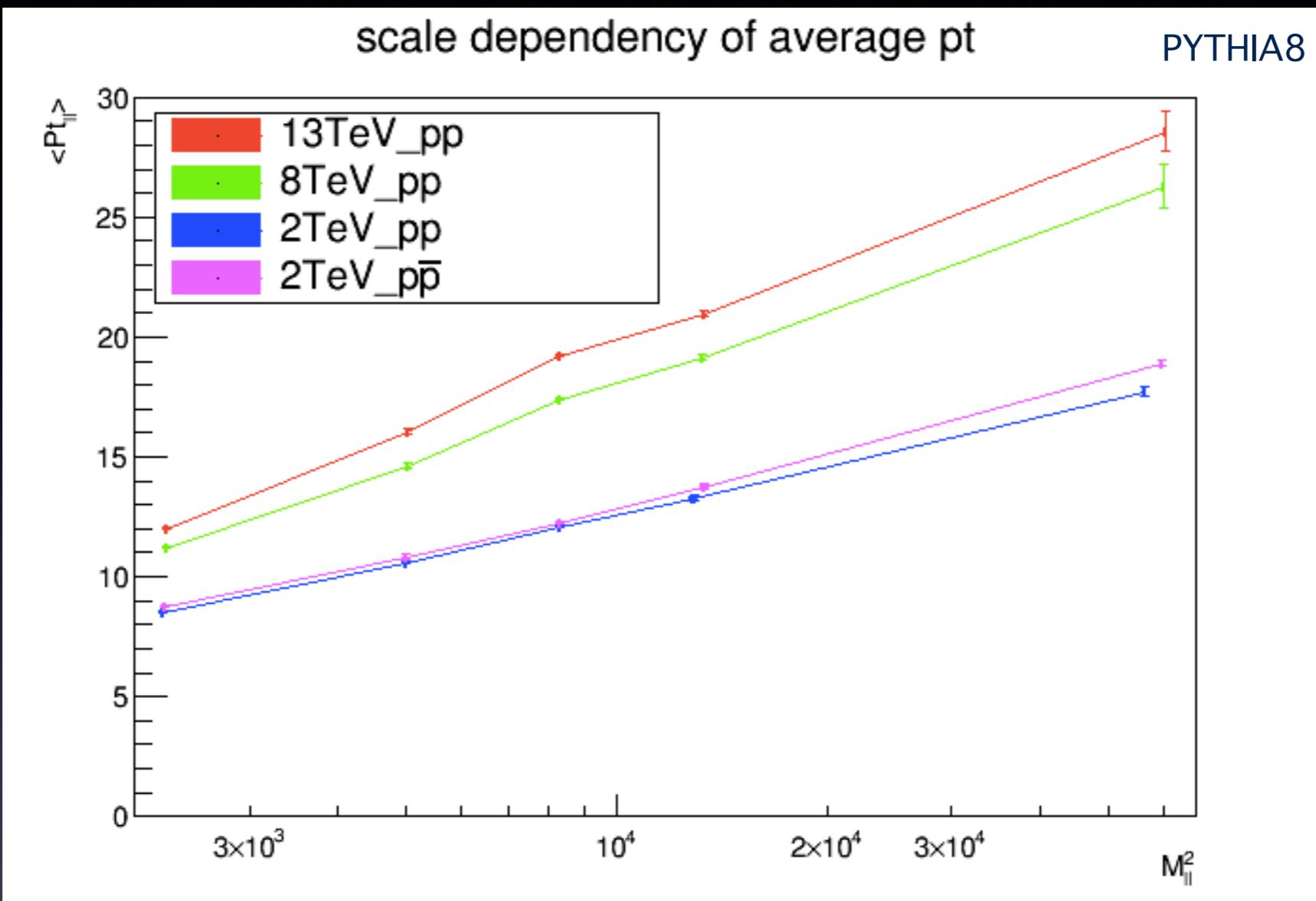


Universality



Physics processes lie on the ISR slope in $\langle p_T \rangle$ vs. $\langle Q^2 \rangle$

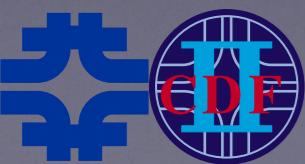
ISR activities projection



- Expected ISR activities does show slope changes by the collision energy

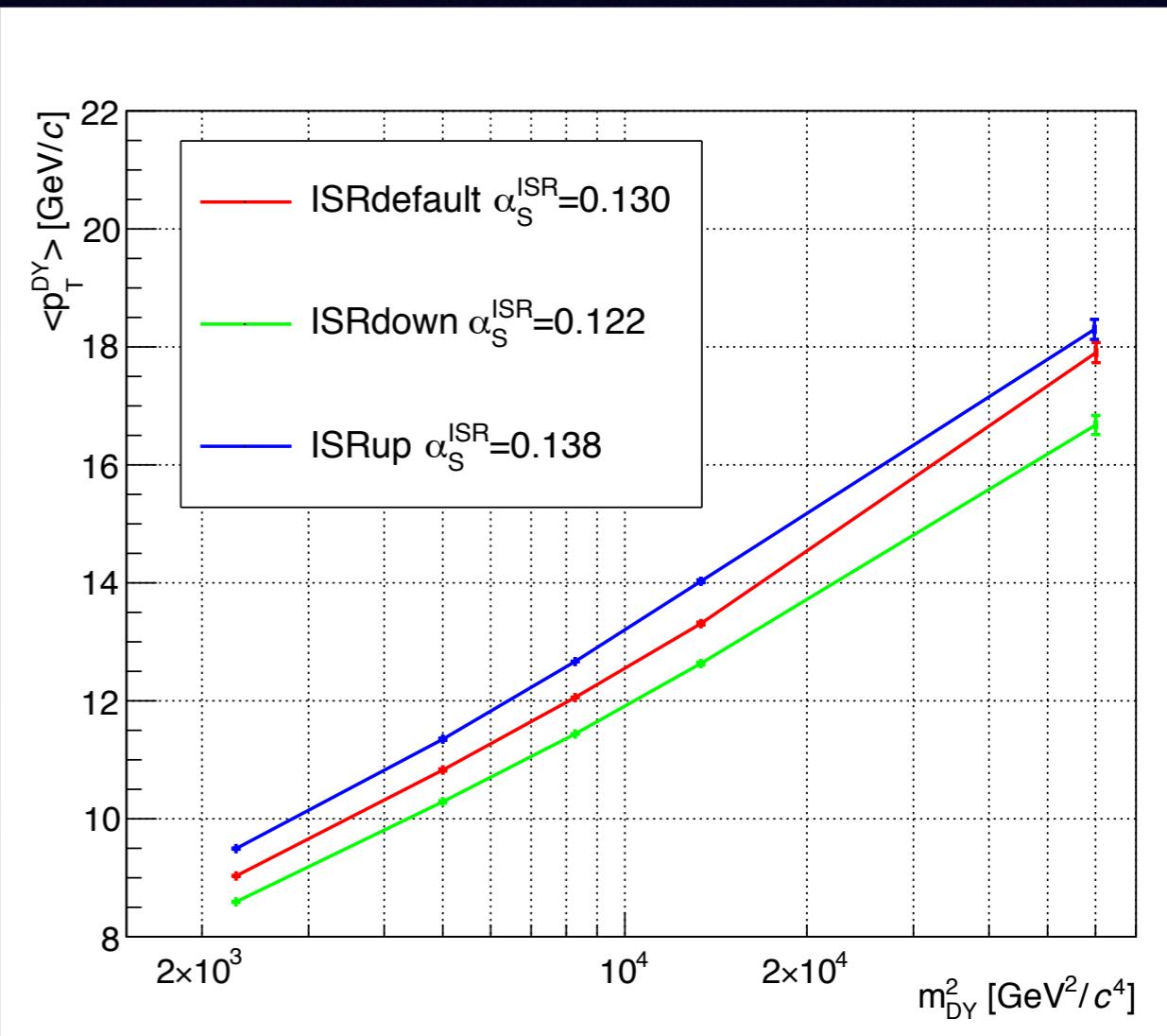
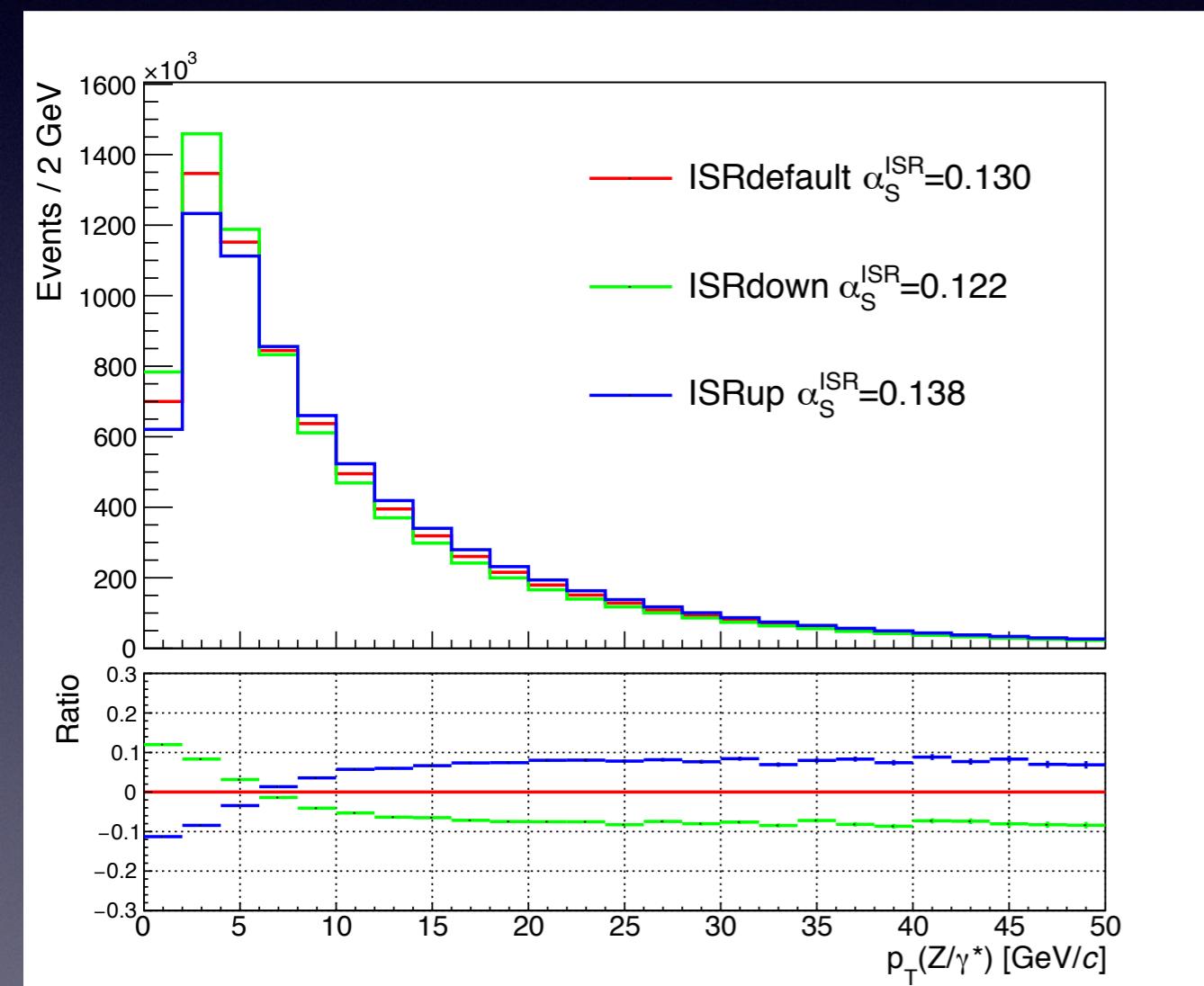
Summary

- QCD ISR is a process that is well-known but hard to study in hadron colliders although it is one of major systematic uncertainties in precision measurement
- Using Drell-Yan events in 9.4 fb^{-1} of CDF data, we measure the amount of ISR as p_T^{DY} depending on the Q^2 , m_{DY}^2 , and obtain a linear relation:
 - $p_T^{DY} = (-7.6 \pm 0.7) + (2.2 \mp 0.8) \times \log(m_{DY}^2)$
- This measurement gives an idea of estimating the p_T shifts induced by the ISR at high energy
- In preparation of paper submission

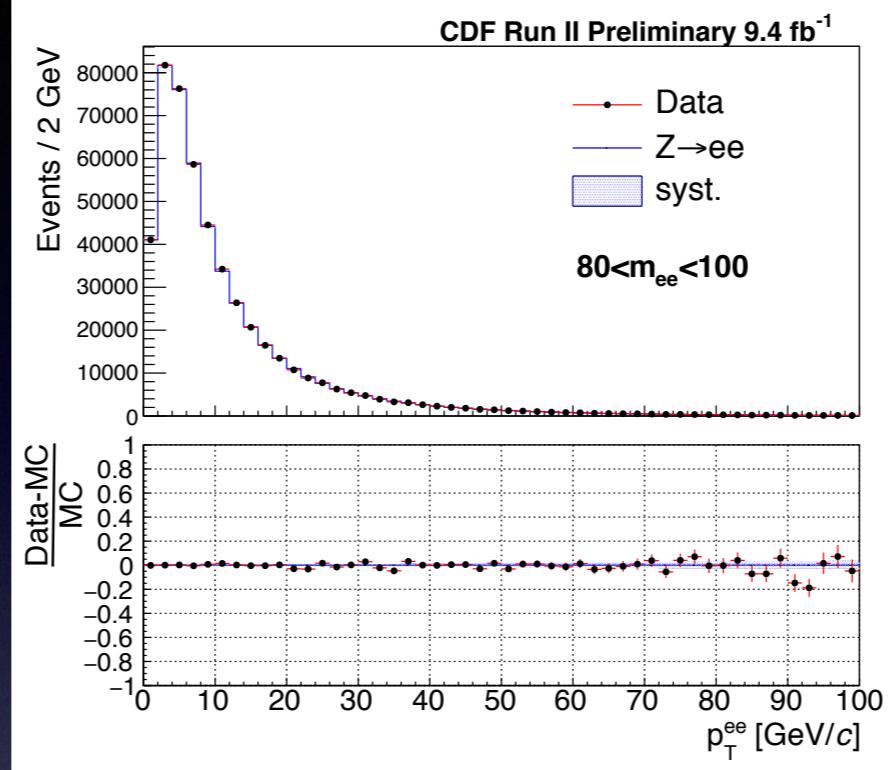
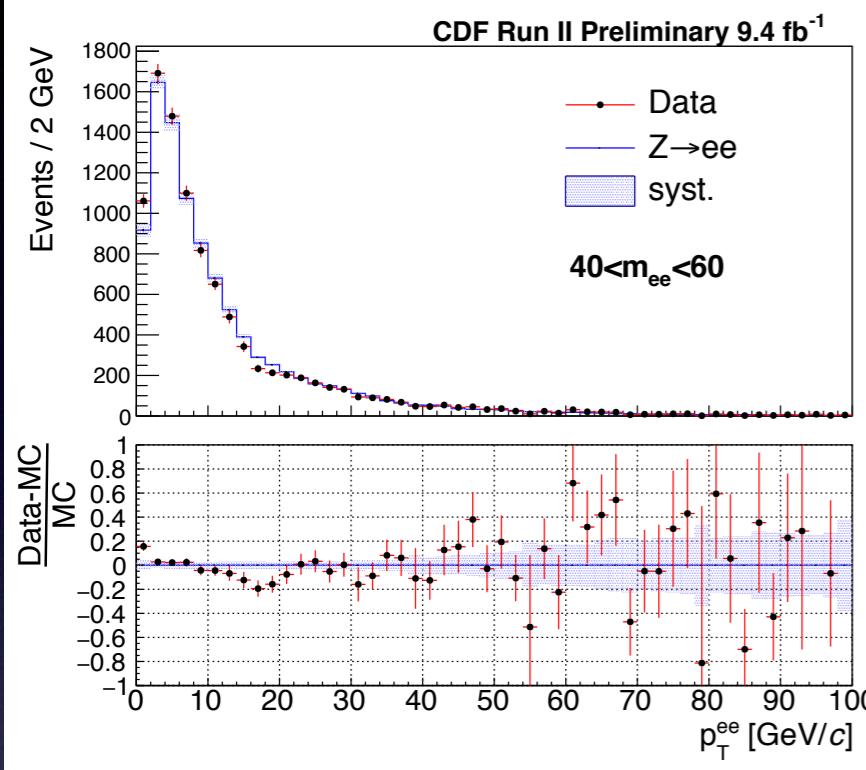


Backups

The measurement sensitive to α_S

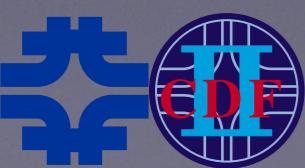
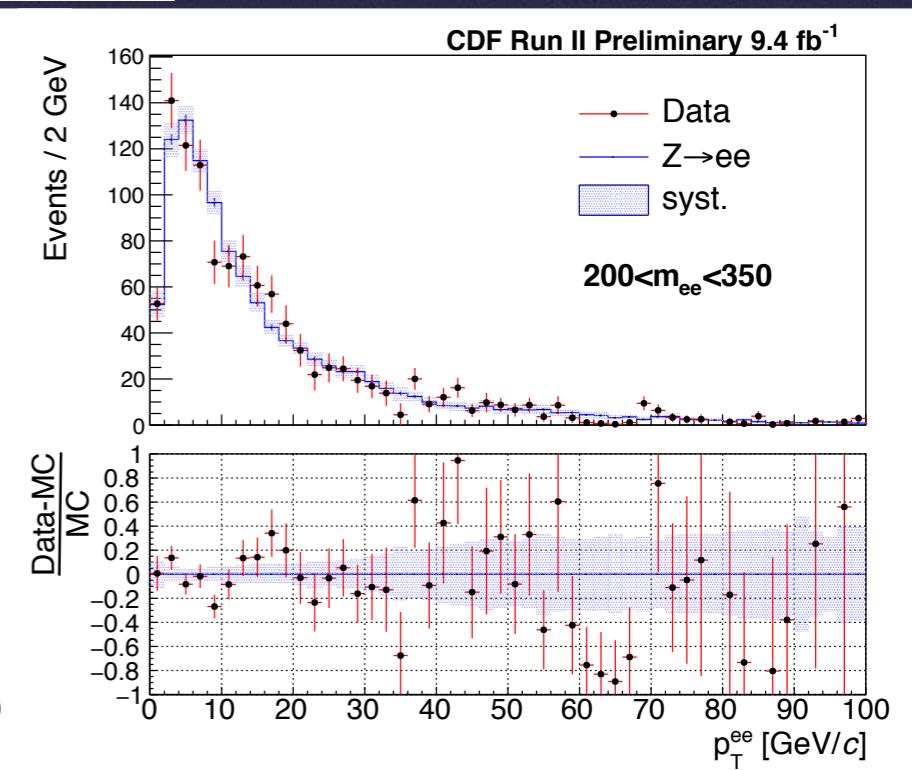
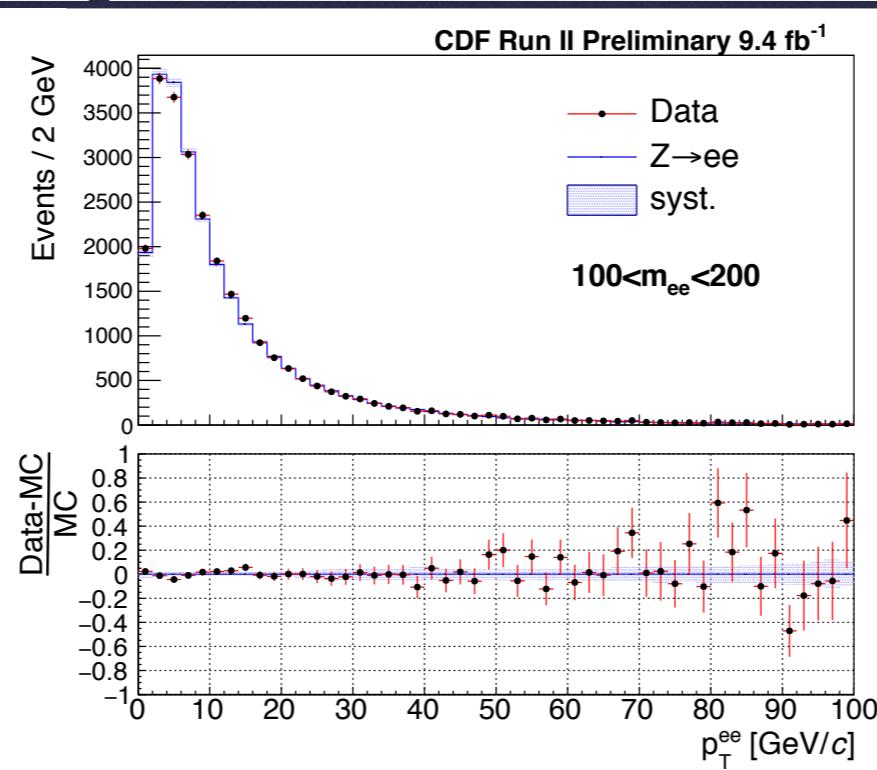
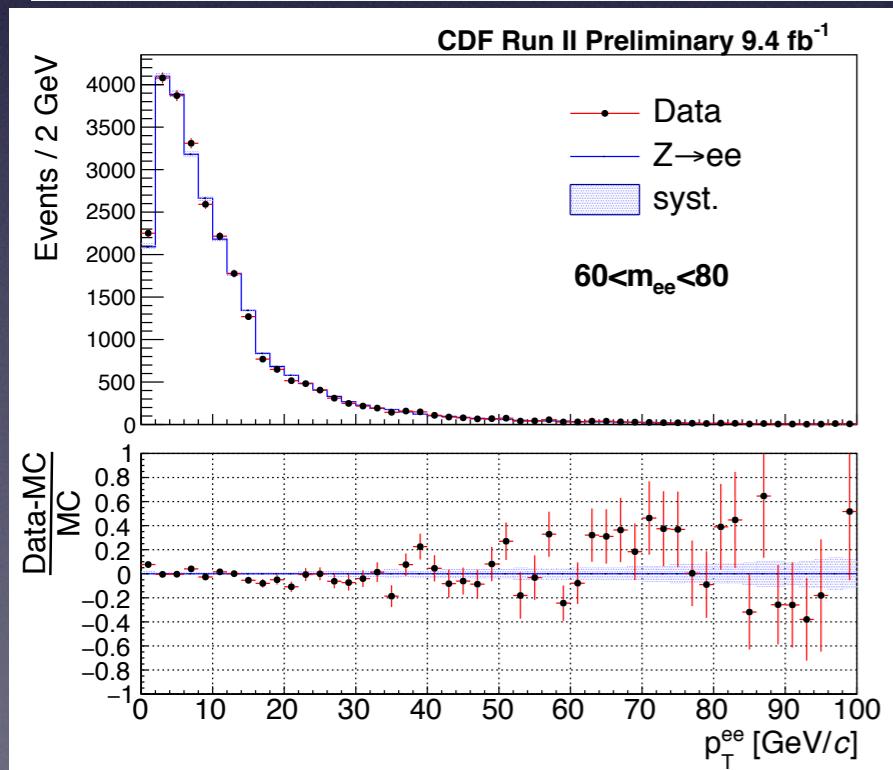


DiLepton PT



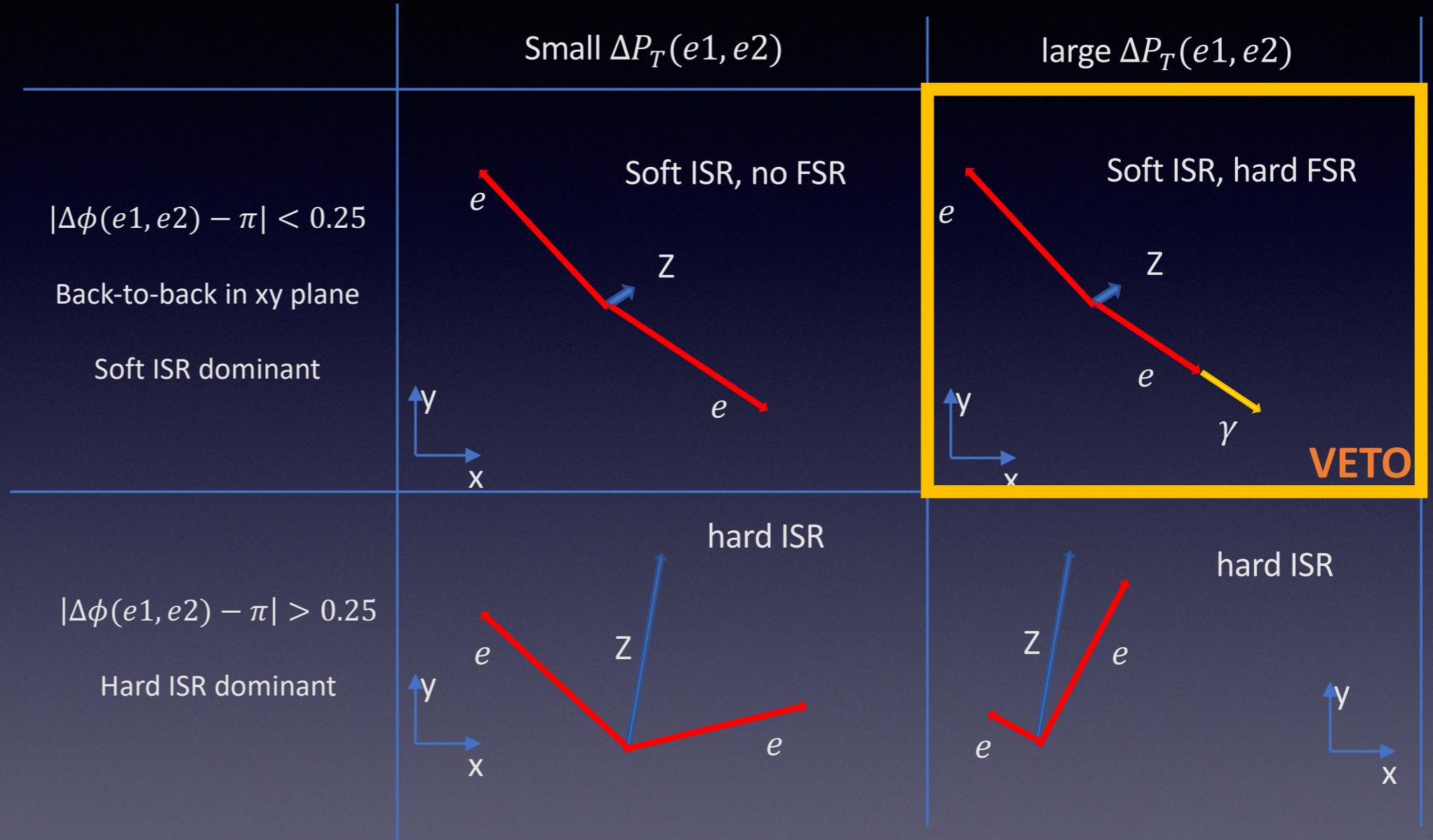
ee channel

Other SM backgrounds
subtracted from Data



FSR-suppression cut

$$\Delta p_T(e1, e2) = |p_T(e1) - p_T(e2)|, \Delta\phi(e1, e2) = |\phi(e1) - \phi(e2)|$$



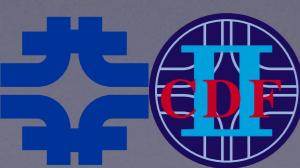
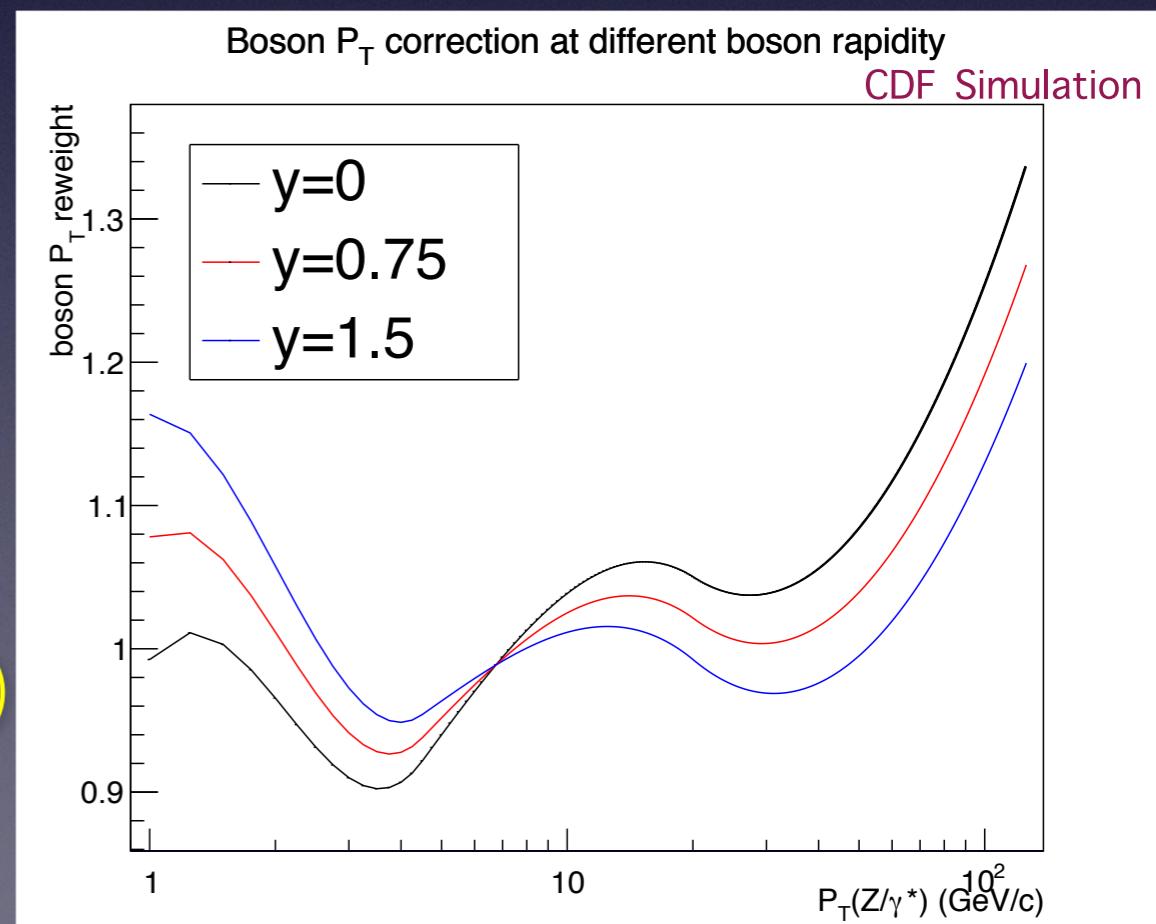
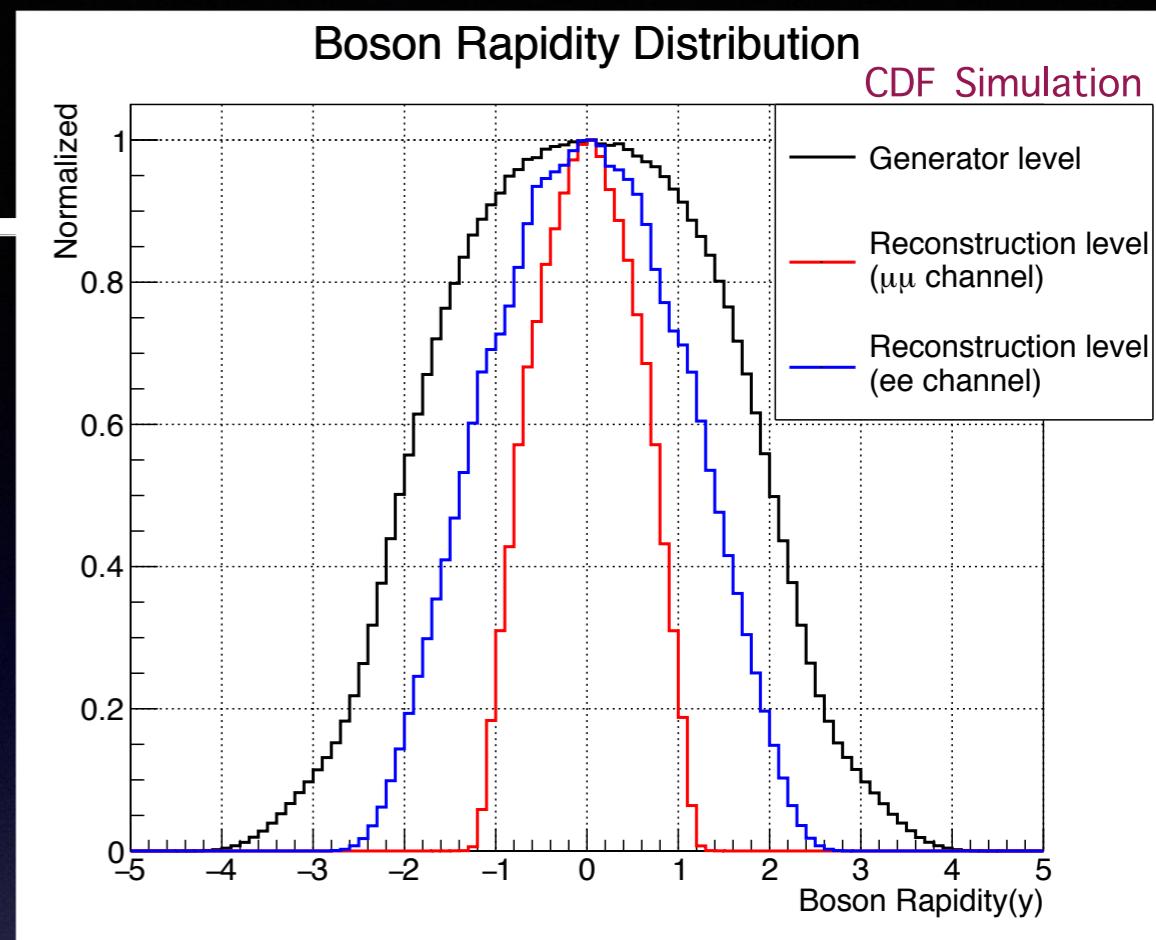
For $m_{ee} < 80$ GeV:

- $|\Delta\phi(e1, e2) - \pi| < 0.25 \text{ } \&\& \Delta p_T(e1, e2) > 15 \text{ GeV } \&\& \text{MET} < 15 \text{ GeV}$
- $|\Delta\phi(e1, e2) - \pi| < 0.25 \text{ } \&\& \Delta p_T(e1, e2) > 10 \text{ GeV } \&\& \text{MET} > 15 \text{ GeV}$



Boson pT correction

- No reason that the pT correction differs by the lepton flavor
- We fully correct the detector acceptance to the generator level
 - Different acceptance in each channel
- Correction differs by the boson rapidity
- Extracted the boson pT correction iteratively from MC to data comparison using both lepton channels in 2D
 - $weight(p_T, y) = f_1(p_T) + y \times f_2(p_T)$



CDF detector details

