

# Forecasting CMB x Euclid constraints : Outline and current state

S. Ilić

# Foreword

---

- **To keep in mind :**

- Not completely independent: inputs from IST
- Not completely free on our side

# Foreword

---

- **To keep in mind :**

- Not completely independent: inputs from IST
- Not completely free on our side

- **Throughout the talk :**

- **Green text** : point ~ agreed upon
- **Red text** : point still to be discussed

# Foreword

---

- **To keep in mind :**

- Not completely independent: inputs from IST
- Not completely free on our side

- **Throughout the talk :**

- **Green text** : point ~ agreed upon (in my opinion)
- **Red text** : point still to be discussed (in my opinion)

# Recipe for Euclid x CMB forecasts

- Main ingredient : likelihood

$$\mathcal{L}(M|\mathcal{O})$$

# Recipe for Euclid x CMB forecasts

- Main ingredient : likelihood

$$\mathcal{L}(M|\mathcal{O})$$

1) Which observables ?

# Recipe for Euclid x CMB forecasts

- Main ingredient : likelihood

$$\mathcal{L}(M|\mathcal{O})$$

1) Which observables ?

$$C_\ell$$

# Recipe for Euclid x CMB forecasts

- Main ingredient : likelihood

$$\mathcal{L}(M|\mathcal{O})$$

1) Which observables ?

$$\mathcal{C}_\ell$$

- Euclid: GCp/s, WL, GCp x WL, (secondary ?)
- CMB: T, E,  $\phi$ , T x E, T x  $\phi$ , E x  $\phi$ , (B ? t/kSZ ?)
- Euclid x CMB: GCp x T, GCp x  $\phi$ , GCp x E  
GCs x T, GCs x  $\phi$ , GCs x E  
WL x T, WL x  $\phi$ , WL x E



# Recipe for Euclid x CMB forecasts

- Main ingredient : likelihood

$$\mathcal{L}(M|\mathcal{O})$$


1) Which observables ?

$$\mathcal{C}_\ell$$

- Euclid:  $GC_p/s$ ,  $WL$ ,  $GC_p \times WL$ , (secondary ?)
- CMB:  $T$ ,  $E$ ,  $\phi$ ,  $T \times E$ ,  $T \times \phi$ ,  $E \times \phi$ , (B ? t/kSZ ?)
- Euclid x CMB:  $GC_p \times T$ ,  $GC_p \times \phi$ ,  $GC_p \times E$   
 $GC_s \times T$ ,  $GC_s \times \phi$ ,  $GC_s \times E$   
 $WL \times T$ ,  $WL \times \phi$ ,  $WL \times E$

Let's converge on the ones agreed upon:  
after that, the sky is the limit !

# Recipe for Euclid x CMB forecasts

- Main ingredient : likelihood

$$\mathcal{L}(M|\mathcal{O})$$

2) Which model(s) ?

# Recipe for Euclid x CMB forecasts

- Main ingredient : likelihood

$$\mathcal{L}(M|\mathcal{O})$$

2) Which model(s) ?

Those decided by the IST

# Recipe for Euclid x CMB forecasts

- Main ingredient : likelihood

$$\mathcal{L}(M|\mathcal{O})$$

2) Which model(s) ?

Those decided by the IST

- Good old  $\Lambda$ CDM
- Neutrinos : 2 choices of non-zero  $\sum m_\nu$
- $w_0/w_a$  parametrisation and/or curvature
- MG model: "gamma"

# Recipe for Euclid x CMB forecasts

- Main ingredient : likelihood

$$\mathcal{L}(M|\mathcal{O})$$

2) Which model(s) ?

Those decided by the IST

- Good old  $\Lambda$ CDM
- Neutrinos : 2 choices of non-zero  $\sum m_\nu$
- $w_0/w_a$  parametrisation and/or curvature
- MG model: "gamma" → problem with CMB (?)

# Recipe for Euclid x CMB forecasts

- Main ingredient : likelihood

$$\mathcal{L}(M|\mathcal{O})$$

Bonus issue :  
choice of the parameter basis

- $\mathcal{O}$
- $M$
- $\mathcal{V}$
- MG model: "gamma" → problem with CMB (?)

# Recipe for Euclid x CMB forecasts

- Main ingredient : likelihood

$$\mathcal{L}(M|\mathcal{O})$$

Bonus issue :  
choice of the parameter basis

- $\Omega_m$ 
  - Theta versus  $H_0$
  - $A_s$  versus  $\sigma_8$
  - "Small" versus "Big" omegas
- $\nu$
- MG model: "gamma" → problem with CMB (?)

# Recipe for Euclid x CMB forecasts

- Main ingredient : likelihood

$$\mathcal{L}(M|\mathcal{O})$$

2) Which model(s) ?

Those decided by the IST

- Good old  $\Lambda$ CDM
  - Neutrinos : 2 choices of non-zero  $\sum m_\nu$
  - $w_0/w_a$  parametrisation and/or curvature
  - MG model: "gamma" → problem with CMB (?)
- + "Survey model":  $n(z)$ , bias,  $z$  bins, ... → IST



# Recipe for Euclid x CMB forecasts

- Main ingredient : likelihood

$$\mathcal{L}(M|\mathcal{O})$$

3) Which form ?

Gaussian likelihood

# Recipe for Euclid x CMB forecasts

- Main ingredient : likelihood

3) Which form ?

Gaussian likelihood

$$\mathcal{L}(M|\mathcal{O}) = \det(2\pi\Sigma_M)^{-1/2} \exp\left(-\frac{1}{2}(\mathcal{O} - \mu_M)^T \Sigma_M^{-1} (\mathcal{O} - \mu_M)\right)$$

# Recipe for Euclid x CMB forecasts

- Main ingredient : likelihood

3) Which form ?

Gaussian likelihood

$$\mathcal{L}(M|\mathcal{O}) = \det(2\pi\Sigma_M)^{-1/2} \exp\left(-\frac{1}{2}(\mathcal{O} - \mu_M)^T \Sigma_M^{-1} (\mathcal{O} - \mu_M)\right)$$

Two points :

- Is a Gaussian likelihood OK ? (low ell)

# Recipe for Euclid x CMB forecasts

- Main ingredient : likelihood

3) Which form ?

Gaussian likelihood

$$\mathcal{L}(M|\mathcal{O}) = \det(2\pi\Sigma_M)^{-1/2} \exp\left(-\frac{1}{2}(\mathcal{O} - \mu_M)^T \Sigma_M^{-1} (\mathcal{O} - \mu_M)\right)$$

Two points :

- Is a Gaussian likelihood OK ? (low ell's)
- Choice of covariance matrix ?
  - Pure analytic "Gaussian" or beyond ? (cf. Fabien's talk)
  - Accounting for incomplete sky ? (insight from estimators)
  - Planck-like ? Or next-gen-like ?

# Recipe for Euclid x CMB forecasts

- Main ingredient : likelihood

3) Which form ?

Gaussian likelihood

$$\mathcal{L}(M|\mathcal{O}) = \det(2\pi\Sigma_M)^{-1/2} \exp\left(-\frac{1}{2}(\mathcal{O} - \mu_M)^T \Sigma_M^{-1} (\mathcal{O} - \mu_M)\right)$$

Two points

Again: bound by some of IST's choices

• Is a Gaussian

• Gaussian likelihood at all ell

• Choice

• Simple analytical covariance

→ Pure

• fsky approximation

→ Account

• Do Planck-like and next-gen-like

→ Planck

(as talk)  
(estimators)

# Recipe for Euclid x CMB forecasts

- Produce forecasts from the likelihood

$$\mathcal{L}(M|\mathcal{O})$$

# Recipe for Euclid x CMB forecasts

- Produce forecasts from the likelihood

$$\mathcal{L}(M|\mathcal{O})$$

Fisher matrices

$$F_{\alpha\beta} = \left\langle -\frac{\partial^2 \ln \mathcal{L}}{\partial \theta_\alpha \partial \theta_\beta} \right\rangle = \frac{1}{2} \Sigma_{ab}^{-1} \frac{\partial \Sigma_{bc}}{\partial \theta_\alpha} \Sigma_{cd}^{-1} \frac{\partial \Sigma_{da}}{\partial \theta_\beta} + \Sigma_{ab}^{-1} \frac{\partial \mu_a}{\partial \theta_\alpha} \frac{\partial \mu_b}{\partial \theta_\beta}$$

# Recipe for Euclid x CMB forecasts

- Produce forecasts from the likelihood

$$\mathcal{L}(M|\mathcal{O})$$

Fisher matrices

$$F_{\alpha\beta} = \left\langle -\frac{\partial^2 \ln \mathcal{L}}{\partial \theta_\alpha \partial \theta_\beta} \right\rangle = \frac{1}{2} \Sigma_{ab}^{-1} \frac{\partial \Sigma_{bc}}{\partial \theta_\alpha} \Sigma_{cd}^{-1} \frac{\partial \Sigma_{da}}{\partial \theta_\beta} + \Sigma_{ab}^{-1} \frac{\partial \mu_a}{\partial \theta_\alpha} \frac{\partial \mu_b}{\partial \theta_\beta}$$



# Recipe for Euclid x CMB forecasts

- Produce forecasts from the likelihood

$$\mathcal{L}(M|\mathcal{O})$$

Fisher matrices

$$F_{\alpha\beta} = \left\langle -\frac{\partial^2 \ln \mathcal{L}}{\partial \theta_\alpha \partial \theta_\beta} \right\rangle = \frac{1}{2} \Sigma_{ab}^{-1} \frac{\partial \Sigma_{bc}}{\partial \theta_\alpha} \Sigma_{cd}^{-1} \frac{\partial \Sigma_{da}}{\partial \theta_\beta} + \Sigma_{ab}^{-1} \frac{\partial \mu_a}{\partial \theta_\alpha} \frac{\partial \mu_b}{\partial \theta_\beta}$$

Remarks:

- Lessons from IST: beware of derivatives
- Alternative: MCMC with “fake” data

# Current status of forecasts

---

# Current status of forecasts

## Guidelines:

- Get the best accuracy/agreement on Cells
- No need to redo the IST's work
- Use Euclid probes as benchmark
- Involve IST people
- Always at least 2 codes

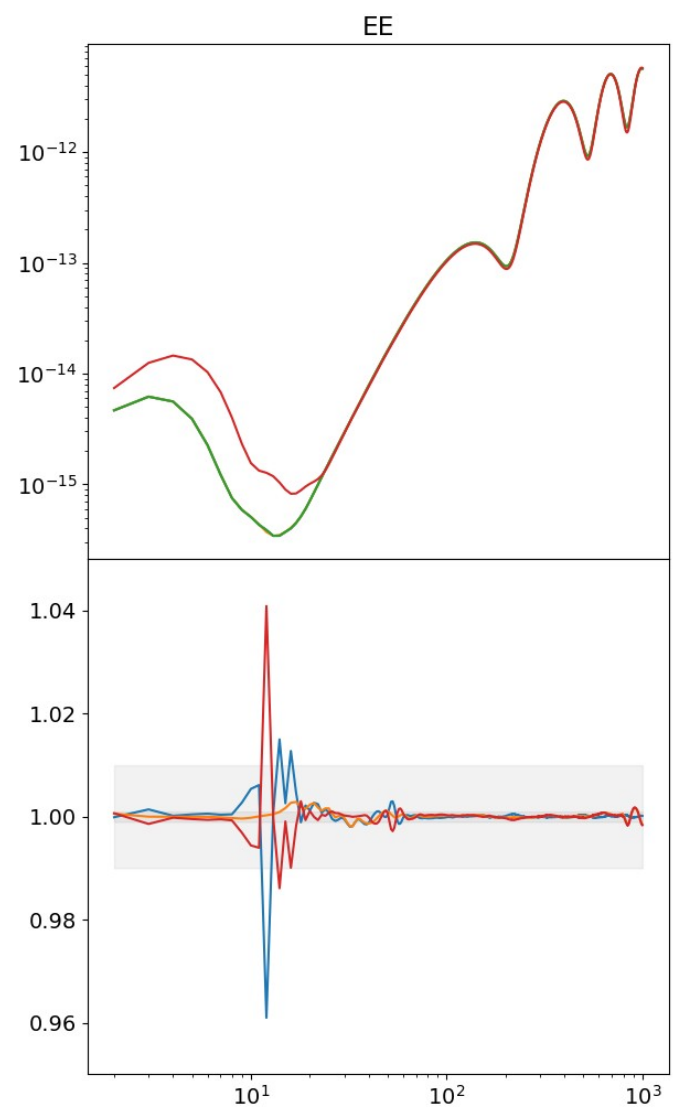
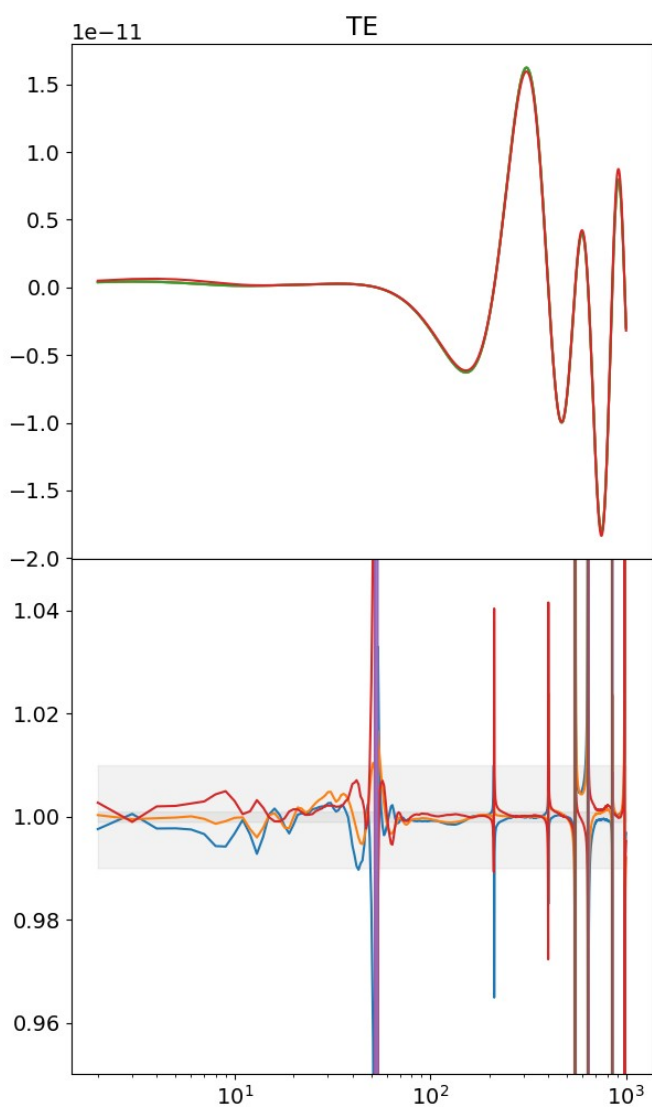
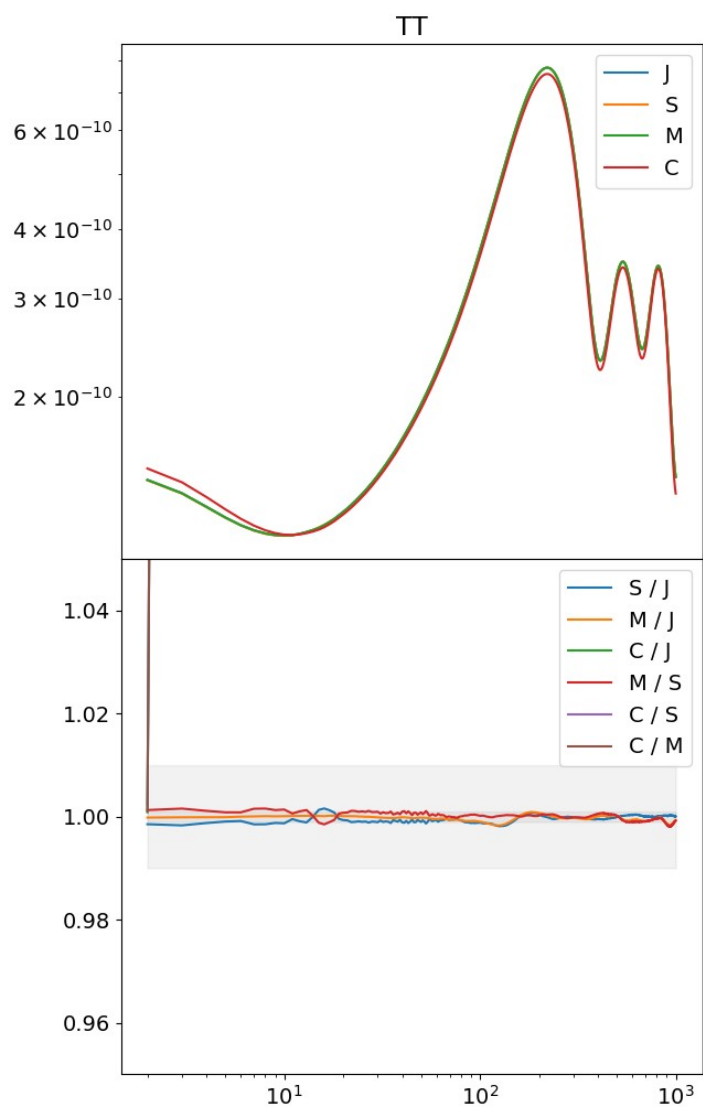
# Current status of forecasts

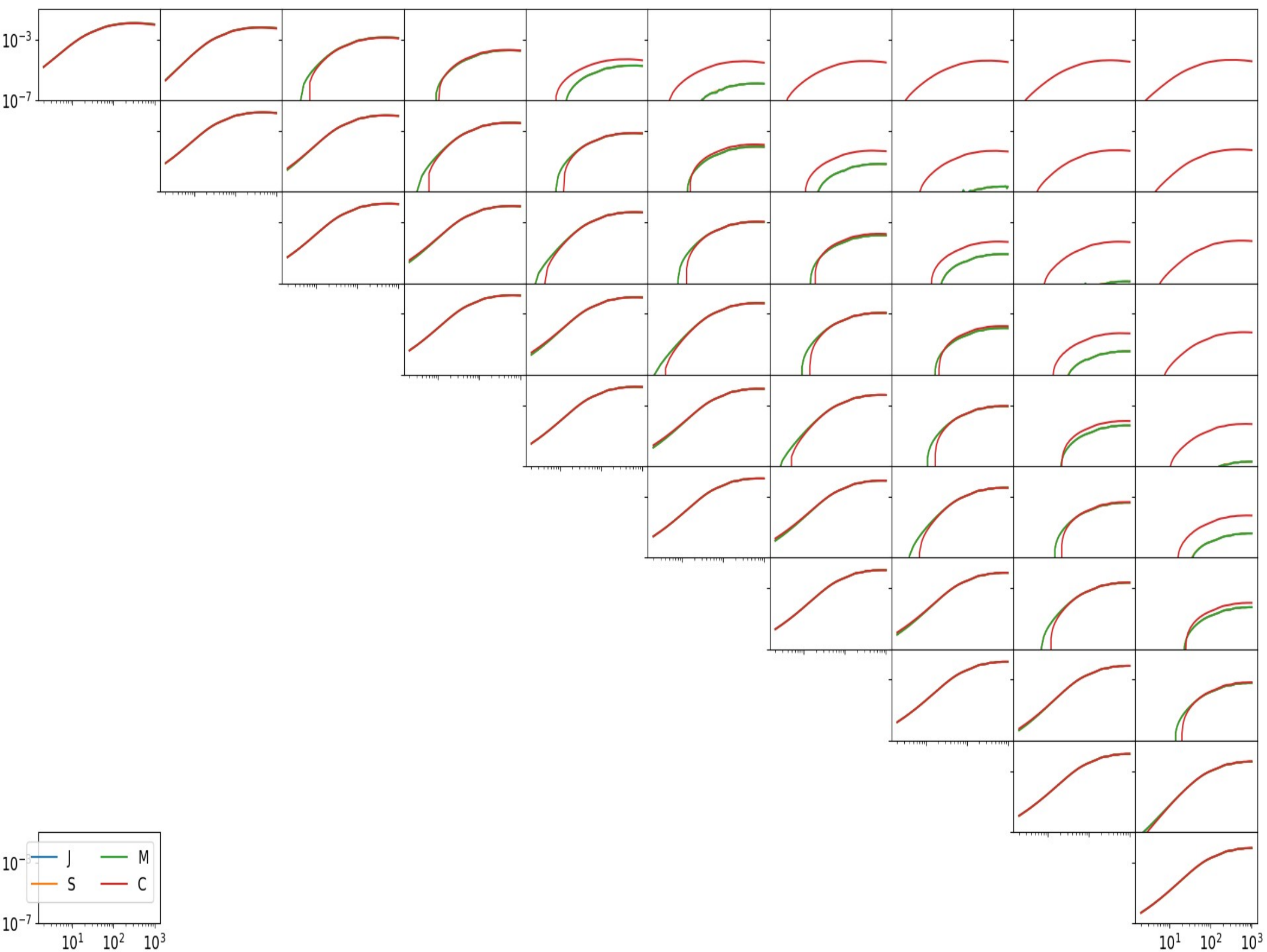
- **People:** José, Stéphane, Matteo, Carlos, Marco
- **Codes:** CAMB sources-based, or CLASS/CAMB + custom
- **Successful convergence on GC, Limber case ( $< \sim 0.1\%$ )**
- **Individual progress in parallel (cf. José's talk)**

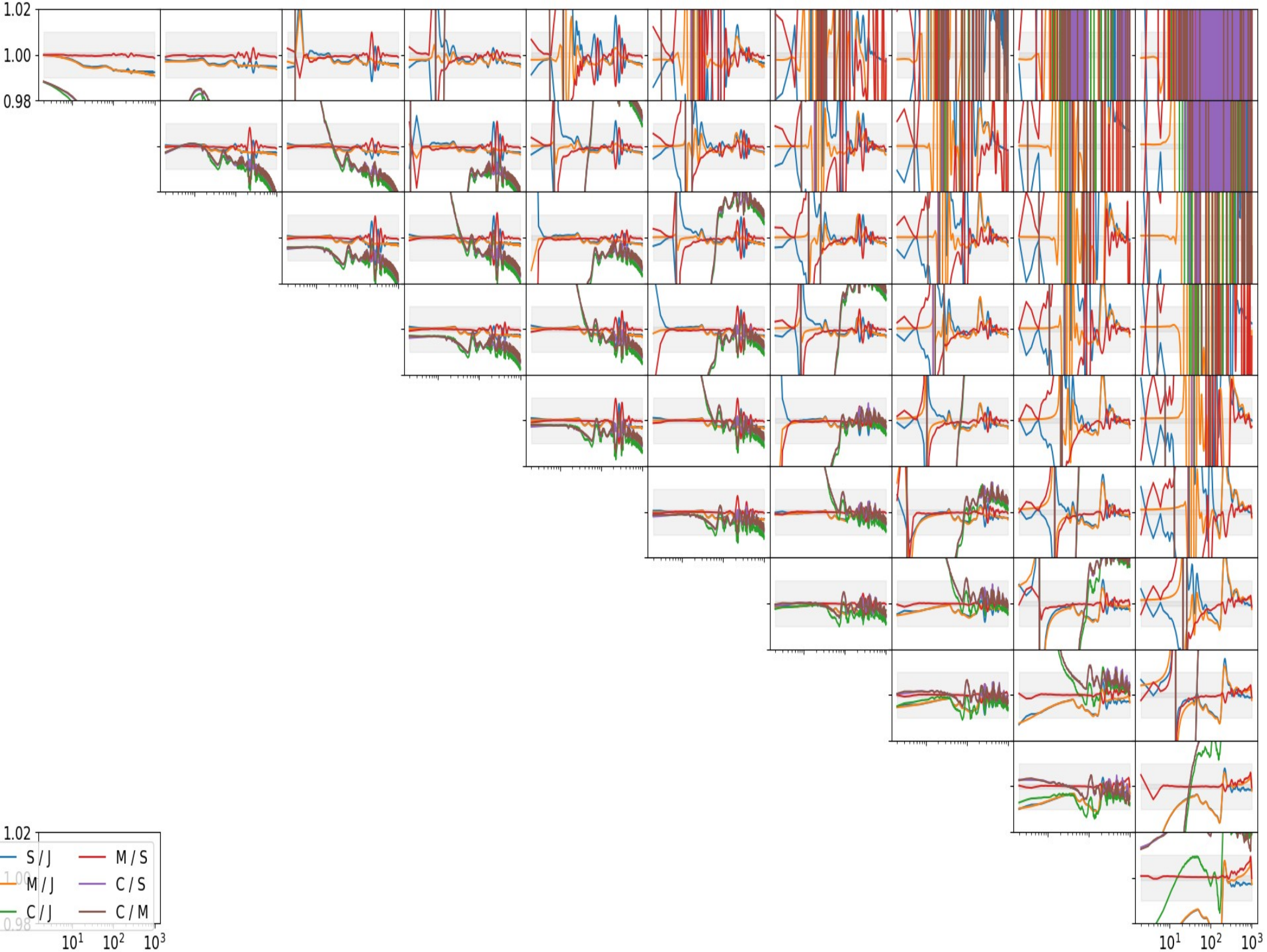
# Current status of forecasts

---

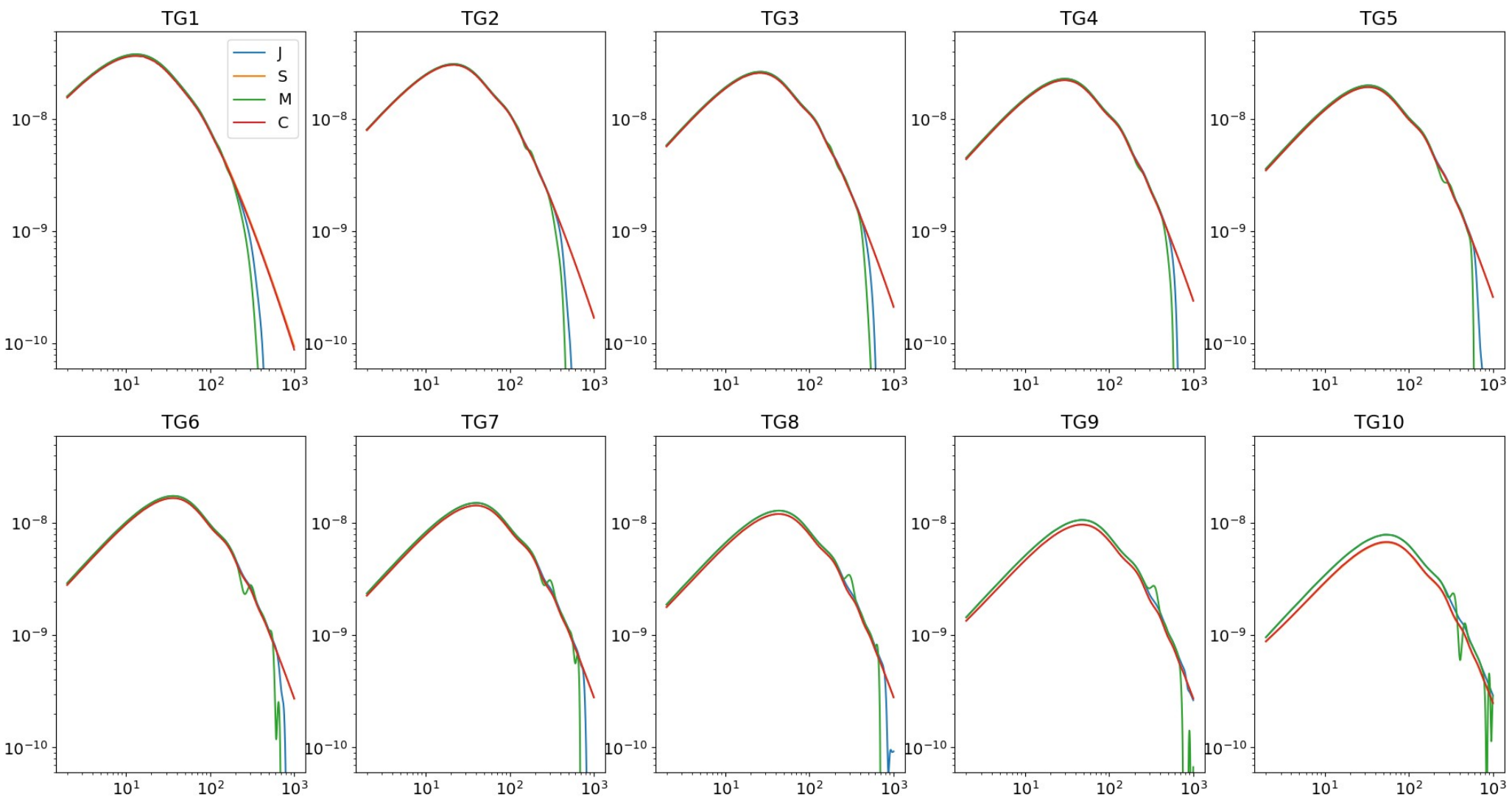
Fresh results  
(03/10/2018)

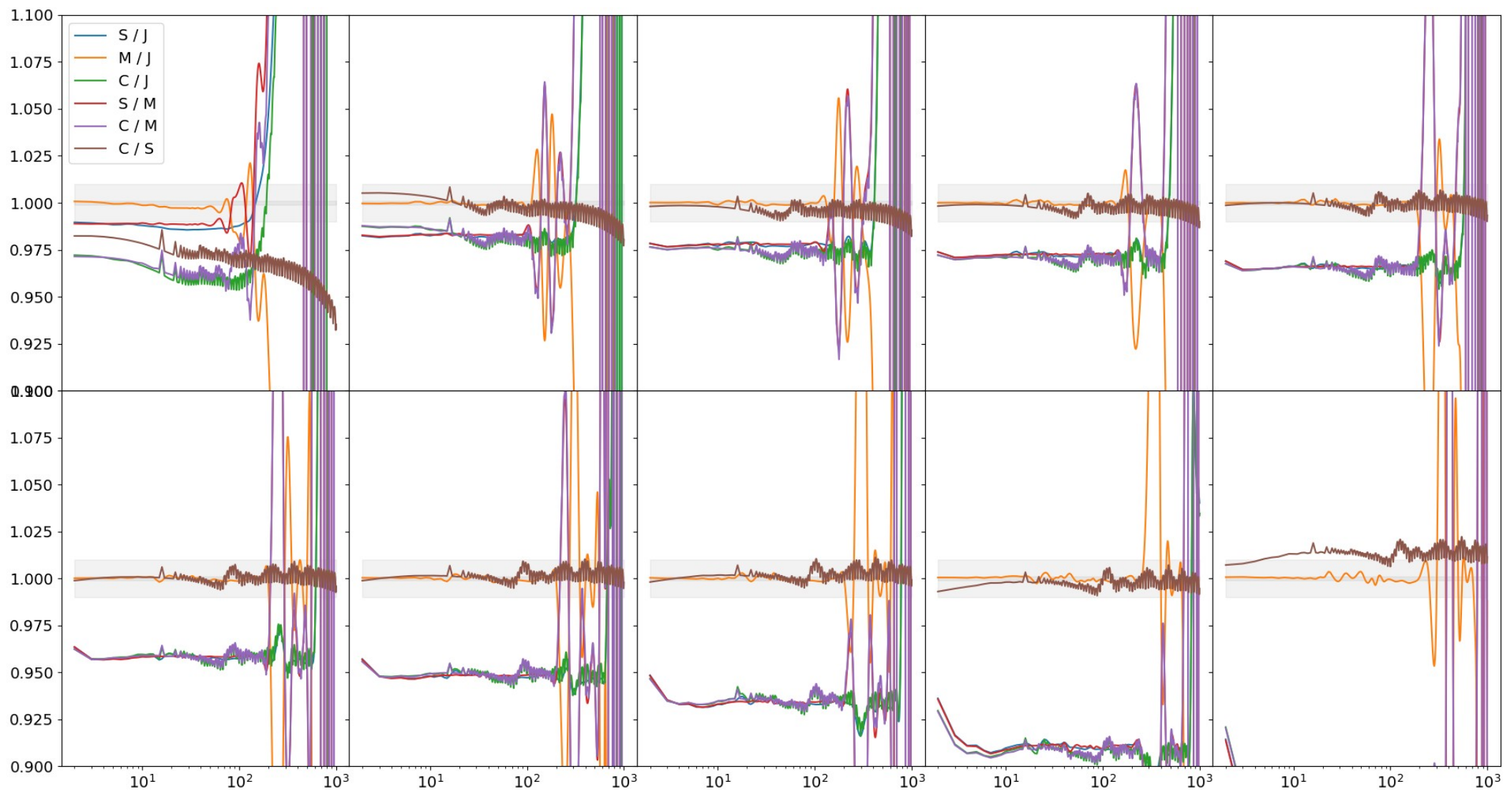












# The end (for now)

---

Thank you for  
your attention !