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# Fusion probability of massive nuclei in reactions leading to heavy composite nuclear systems

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- 1.  $P_{CN}$  as a key value for the estimates of production cross sections for the heaviest nuclei
- 2.  $P_{\rm CN}$  values and their scaling for the data obtained from fission study
- 3.  $P_{\rm CN}$  values and their scaling as obtained with ER cross section data
- 4. Summary and conclusion

#### Theoretical and experimental estimates of P<sub>CN</sub>



W. Loveland, EPJ Web Conf. 131, 04003 (2016)

#### Experiment

#### **Fission study**

P<sub>CN</sub> values are estimated by comparing the total yield of FF corresponding to the capture process and the FF yield attributed to true CN-fission. CN-fission events are usually extracted with proper decompositions of fission fragment TKE, mass and angular distributions

#### **ER cross-section data**

 $P_{\rm CN}$  values are estimated by comparing production cross sections for a very asymmetric projectile-target combination, assuming  $P_{\rm CN} \approx 1$ , and those for a less asymmetric one, which is under study and leads to the came CN

#### Twofold estimates of P<sub>CN</sub> in reactions leading to <sup>202</sup>Pb<sup>\*</sup> CN





A.M. Stefanini *et al.*, Eur. Phys. J. A **23**, 473 (2005) G.N. Knyazheva *et al.*, Phys.Rev. C **76**, 054604 (2007)  $P_{\rm CN}$  in <sup>48</sup>Ca+<sup>154</sup>Sm reaction was estimated by comparing ER cross sections obtained in <sup>16</sup>O+<sup>186</sup>W and <sup>48</sup>Ca+<sup>154</sup>Sm reactions and by decomposing fission fragment mass, angular and TKE distributions obtained in <sup>48</sup>Ca+<sup>154</sup>Sm

### **P**<sub>CN</sub> from fission reactions leading to strongly fissile compound nuclei





#### **P**<sub>CN</sub> data scaling using extra-extra push model representation

Critical RLDM value  $(Z_{CN}^2/A_{CN})_{cr} = 50.883\{1 - 1.7826[(A_{CN} - 2Z_{CN})/A_{CN}]^2$ CN fissility:  $x_{CN} = Z_{CN}^2/A_{CN})/(Z_{CN}^2/A_{CN})_{cr}$ 

Effective equilibrated fissility:  $x_{eff}^{eq} = \frac{(Z^2/A)_{eff}^{eq}}{(Z_{CN}^2/A_{CN})_{cr}}$ , where  $(Z^2/A)_{eff}^{eq} = 4A_pA_tZ_{CN}^2/[A_p^{\frac{1}{3}}A_t^{\frac{1}{3}}(A_p^{\frac{1}{3}} + A_t^{\frac{1}{3}})A_{CN}^2]$  H. Gägeller *et al.*, Z. Phys. A **316**, 291 (1984); F.P. Heßberger, GSI-85-11; HIVAP Effective fissility:  $x_{eff}^{eq} = 4x_{CN}(k^2 + k + k^{-1} + k^{-2})$ , where  $k = (A_p/A_t)^{-1/3}$  J.P. Blocki *et al.*, Nucl. Phys. **A459**, 145 (1986) Characteristic ee – push energy:  $E_{ch}^{xx} = 7.601 \cdot 10^{-4}A_p^{\frac{1}{3}}A_t^{\frac{1}{3}}(A_p^{\frac{1}{3}} + A_t^{\frac{1}{3}})^2(Z_{CN}^2/A_{CN})_{cr}/A_{CN}$ Fusion barrier shift  $\Delta E = a_{push}^2 E_{ch}^{xx}(x_{mean}^{eq} - x_{thr})^2$ 



R. Yanez *et al.*, Phys. Rev. C **88**, 014606 (2013)

# Scaling of $P_{CN}^0$ data obtained from fission studies



# ER cross section data analysis for the extraction of *P*<sub>CN</sub> values using barrier passing and statistical models (HIVAP)

 $\Sigma \sigma_{xn} = \sum_{L=0}^{L_{max}} \sigma_{cap} (E, L) P_{CN}(E, L) W_{sur}(E_{CN}^*, L),$ Measured Calculated with SM

Measured 
$$\sigma_{cap} = \pi/k^2 \sum_{L=0}^{L_{max}} (2L+1)T_L(E,L).$$

**Described in calculations with BPM** 

#### **Barrier** passing model (*P*<sub>CN</sub> = 1 for very asymmetric projectile-target combinations)

- Coupling to various entrance channels via the radius (barrier) fluctuations  $\sigma(r_0)/r_0$  generated using a Gaussian distribution with the mean value  $r_0$  and width  $\sigma(r_0)$
- The exponential nuclear potential with adjusting  $V_0$  and  $\sigma(r_0)/r_0$ , fixed  $r_0=1.12$  fm and d=0.75 fm
- The WKB approximation for transmission coefficients of partial waves penetrating the barrier

#### Statistical model approximations for description of $W_{sur}$

- Intrinsic level density only with the shell damping energy E<sub>D</sub> = 18.5 MeV
- The expression of W. Reisdorf for the macroscopic level density parameters in the fission and evaporation channels of the CN decay  $(\tilde{a}_f / \tilde{a}_v > l)$
- ER and fission cross section calculations adjusted with the LD barrier scaling using a scaling parameter  $k_f$  as a main fitted parameter:  $B_f(L) = k_f B_f^{LD}(L) \Delta W_{gs}$
- Calculations of ground-state shell correction ΔW<sub>gs</sub> (a difference between empirical and LD masses), excitation and separation energies with empirical masses



#### **P**<sub>CN</sub> for reactions leading to <sup>202</sup>Po<sup>\*</sup> and <sup>207</sup>At<sup>\*</sup> compound nuclei





#### **P**<sub>CN</sub> for reactions leading to <sup>210</sup>Rn<sup>\*</sup> and <sup>213</sup>Fr<sup>\*</sup> compound nuclei



#### **P**<sub>CN</sub> for reactions leading to <sup>220</sup>Th<sup>\*</sup> CN



#### **P**<sub>CN</sub> for reactions leading to <sup>248</sup>Fm<sup>\*</sup> and <sup>256</sup>No<sup>\*</sup> compound nuclei







#### **P**<sub>CN</sub> for reactions leading to the trans-actinide compound nuclei

## $P_{\rm CN}^0$ data scaling using ER cross section data analysis



# **Summary and conclusion**

• Being critical and correlating values in the estimates of ER cross sections,  $P_{CN}$  and survivability in CN-reactions leading to heavy and heaviest nuclei were considered using available experimental fission data and ER cross-section data. The latter could be described in the framework of the barrier passing model for a capture and the statistical model (SM) for a CN-decay using  $P_{CN}$  as an adjustable parameter.

• *P*<sub>CN</sub> values obtained in fission reactions corresponding to the decay of heavy composite system formed in nucleus-nucleus collisions were scaled with the Coulomb factor and in the framework of the representation of the extra-extra-push model.

•  $P_{\rm CN}$  values were also deduced by comparing ER production cross sections obtained in very asymmetric projectile-target combinations, assuming that  $P_{\rm CN}$ =1 and those obtained in less asymmetric ones for which  $P_{\rm CN}$  values have to be found. The survivability of heavy nuclei produced in very asymmetric projectile-target combinations can be reproduced by adjusting the liquid-drop component of fission barriers in the framework of SM approximations. These barriers were used for the empirical estimates of  $P_{\rm CN}$  for more symmetric reactions leading to the same CN.

•  $P_{\rm CN}$  values obtained with the ER production cross sections were also scaled with the Coulomb factor and in the framework of the representation of the extra-extra-push model, as in the case of fission data. A comparison of both dependencies shows that  $P_{\rm CN}$  values deduced with the ER data as functions of the Coulomb factor and equilibrated mean fissility drop faster than of the similar values obtained from fission data.

