

# PHOTON 2019 - International Conference on the Structure and the Interactions of the Photon

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6-7 June 2019

## Recent results on two photon processes at BaBar

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State  
University  
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# Outline

- **Introduction**
- **Collider and Detector**
- **Two photon processes at BaBar**
- **Summary**

# Introduction. Classification of $\gamma\gamma$ Experiments

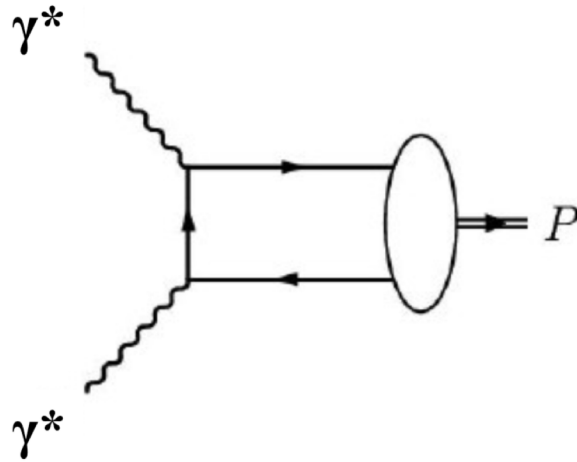
There are three different types of  $\gamma\gamma$  experiments depending on whether or not initial electrons are detected:

- Both  $e^\pm$  not detected – no tag  
(small  $q_{1,2}^2$ , quasireal photons)
- One  $e^\pm$  is detected – single tag
- Both  $e^\pm$  detected – double tag

In some cases experiments have a dedicated tagging system (tagger) to detect outgoing  $e^\pm$ 's (TPC- $2\gamma$ , MD-1 in the past, KEDR in Novosibirsk, KLOE-2 in Frascati - today)

**Detectors with a large solid angle (CLEO, BaBar, Belle, BES-III) can perform single-tag experiments, when one final lepton is detected**

# Introduction. Transition FormFactor



The amplitude of the  $\gamma^*\gamma^*\rightarrow\mathbf{P}$  transition

$$A = e^2 \varepsilon_{\mu\nu\alpha\beta} e_1^\mu e_2^\nu q_1^\alpha q_2^\beta F(q_1^2, q_2^2),$$

$\mathbf{P}$  — pseudoscalar meson

$e_{1,2}$  — photon polarization

$q_{1,2}$  — 4-momentum of photon

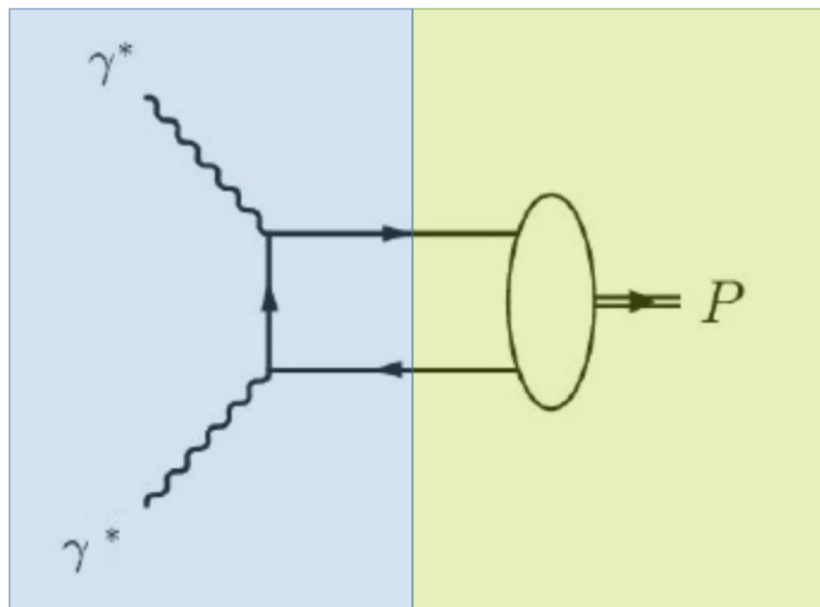
- there are a lot of experimental study of pseudoscalar meson production via the fusion of real (**on-shell**) and virtual (**off-shell**) photons

$$\gamma^*\gamma \rightarrow \mathbf{P}: \pi^0, \eta, \eta', \eta_c$$

- there are **no** measurements of the double **off-shell** transitions

$$\gamma^*\gamma^* \rightarrow \mathbf{P}$$

# Introduction. $F(Q_1^2, Q_2^2)$ at large $Q^2$



Hard part

Warm part

$$F(Q_1^2, Q_2^2) = \int T(x, Q_1^2, Q_2^2) \varphi(x, Q_1^2, Q_2^2) dx$$

$x$  - is the fraction of the meson momentum carried by one of the quarks

$T(x, Q_1^2, Q_2^2)$  - hard scattering amplitude for  $\gamma^* \gamma^* \rightarrow q\bar{q}$  transition which is calculable in pQCD  
 $\varphi(x, Q_1^2, Q_2^2)$  - nonperturbative meson distribution amplitude (DA) describing transition  $P \rightarrow q\bar{q}$

$$T_H(x, Q_1^2, Q_2^2) = \frac{1}{2} \cdot \frac{1}{xQ_1^2 + (1-x)Q_2^2} \cdot \left( 1 + C_F \frac{\alpha_S(Q^2)}{2\pi} \cdot t(x, Q_1^2, Q_2^2) \right) + (x \rightarrow 1-x) + \mathcal{O}(\alpha_S^2) + \mathcal{O}(\Lambda_{QCD}^4/Q^4)$$

NLO Correction [E. Braaten, Phys. Rev. D **28**, 3 (1983)]

- The meson DA  $\varphi(x, Q_1^2, Q_2^2)$  plays an important role in theoretical descriptions of many QCD processes. Its shape ( $x$  dependence) is unknown, but its evolution with  $\mu^2 = Q_1^2 + Q_2^2$  is predicted by pQCD:

$$\mu^2 \frac{d}{d\mu^2} \varphi(x, \mu) = \frac{\alpha_S(\mu)}{2\pi} \int_0^1 dy V(x, y) \varphi(y, \mu)$$

At the limit  $\mu \rightarrow \infty$   $\varphi_P(x, \mu) = A_P 6x(1-x)(1 + \mathcal{O}(\Lambda_{QCD}^2/\mu^2))$

S. J. Brodsky and G. P. Lepage, Phys. Rev. D **24**, 7 (1981)

# Introduction. $F(Q_1^2, Q_2^2)$ at low $Q^2$

- $F(0,0)$  is related to axial anomaly:

$$\Gamma_{\eta' \rightarrow 2\gamma} = \frac{\pi\alpha^2 m_{\eta'}^3}{4} |F(0,0)|^2 = 4.30 \pm 0.16 \text{ keV} \quad \longrightarrow \quad F(0,0) = 0.342 \pm 0.006 \text{ GeV}^{-1}.$$

- The vector meson dominance model is commonly used to describe TFF at low  $Q^2$ :

$$F_{\eta'}(Q_1^2, Q_2^2) = \frac{F_{\eta'}(0,0)}{(1 + Q_1^2/\Lambda_P^2)(1 + Q_2^2/\Lambda_P^2)}$$

- In case of the TFF with one off-shell photon the pQCD and VMD models leads to the same asymptotic behaviour  $F(Q^2) \propto 1/Q^2$  at  $Q^2 \rightarrow \infty$ .

	VMD	pQCD
$Q_1^2 \approx 0, Q_2^2 \rightarrow \infty$	$1/Q^2$	$1/Q^2$
$Q_1^2, Q_2^2 \rightarrow \infty$	$1/Q^4$	$1/Q^2$

## A.V. Radyushkin, R. Ruskov, Nuclear Physics B481 (1996) 625-680

$$F_{\gamma^* \gamma^* \pi^0}^{LO}(q^2, Q^2) = \frac{4\pi}{3} \int_0^1 \frac{\varphi_\pi(x)}{xQ^2 + \bar{x}q^2} dx, \quad (1.1)$$

where  $\varphi_\pi(x)$  is the pion distribution amplitude and  $x, \bar{x} \equiv 1 - x$  are the fractions of the pion light-cone momentum carried by the quarks. In the region where both photon virtualities are large:  $q^2 \sim Q^2 \gtrsim 1 \text{ GeV}^2$ , the pQCD predicts the overall  $1/Q^2$  fall-off of the form factor, which differs from the naive vector meson dominance expectation  $F_{\gamma^* \gamma^* \pi^0}(q^2, Q^2) \sim 1/q^2 Q^2 \sim 1/Q^4$ . Thus, establishing the  $1/Q^2$  power law in this region is a crucial test of pQCD for this process. The study of  $F_{\gamma^* \gamma^* \pi^0}(q^2, Q^2)$  over a wide range of the ratio  $q^2/Q^2$  of two large photon virtualities can then provide non-trivial information about the shape of  $\varphi_\pi(x)$ .

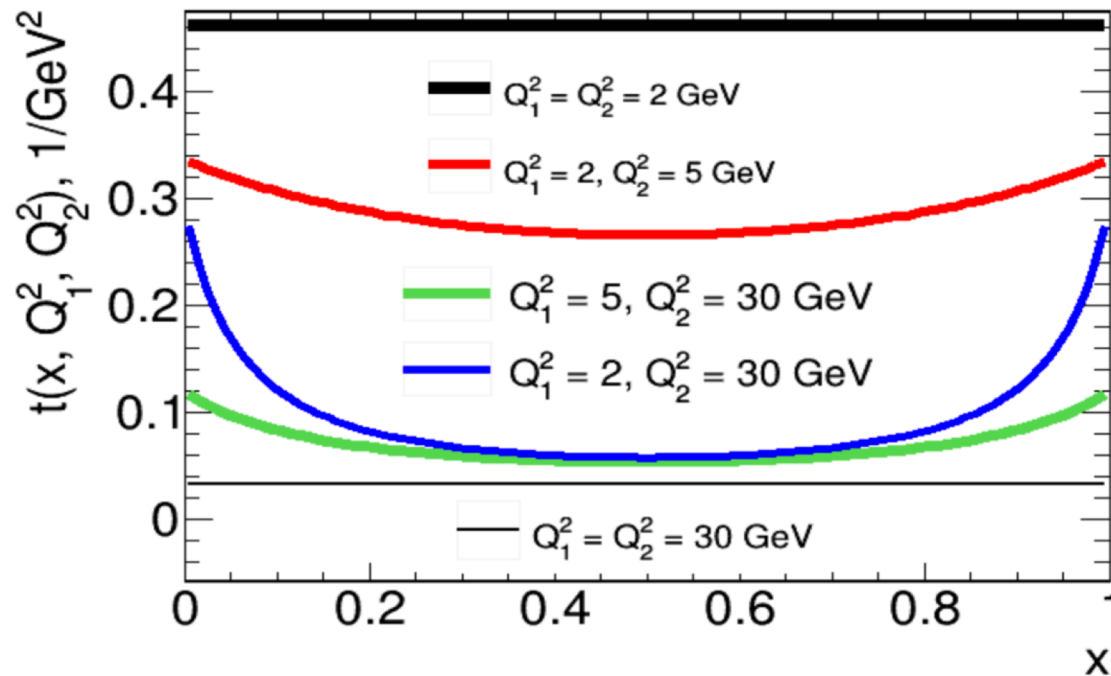
# Introduction. $F(Q_1^2, Q_2^2)$ at large $Q^2$

## Master Formula

$$F_{\eta'}(Q_1^2, Q_2^2) = \left( \frac{5\sqrt{2}}{9} f_n \sin \phi + \frac{2}{9} f_s \cos \phi \right) \int_0^1 dx \frac{1}{2} \cdot \frac{6x(1-x)}{xQ_1^2 + (1-x)Q_2^2} \cdot \left( 1 + C_F \frac{\alpha_s(Q^2)}{2\pi} \cdot t(x, Q_1^2, Q_2^2) \right) + (x \rightarrow 1-x)$$

**NLO Correction**

## The meson DA

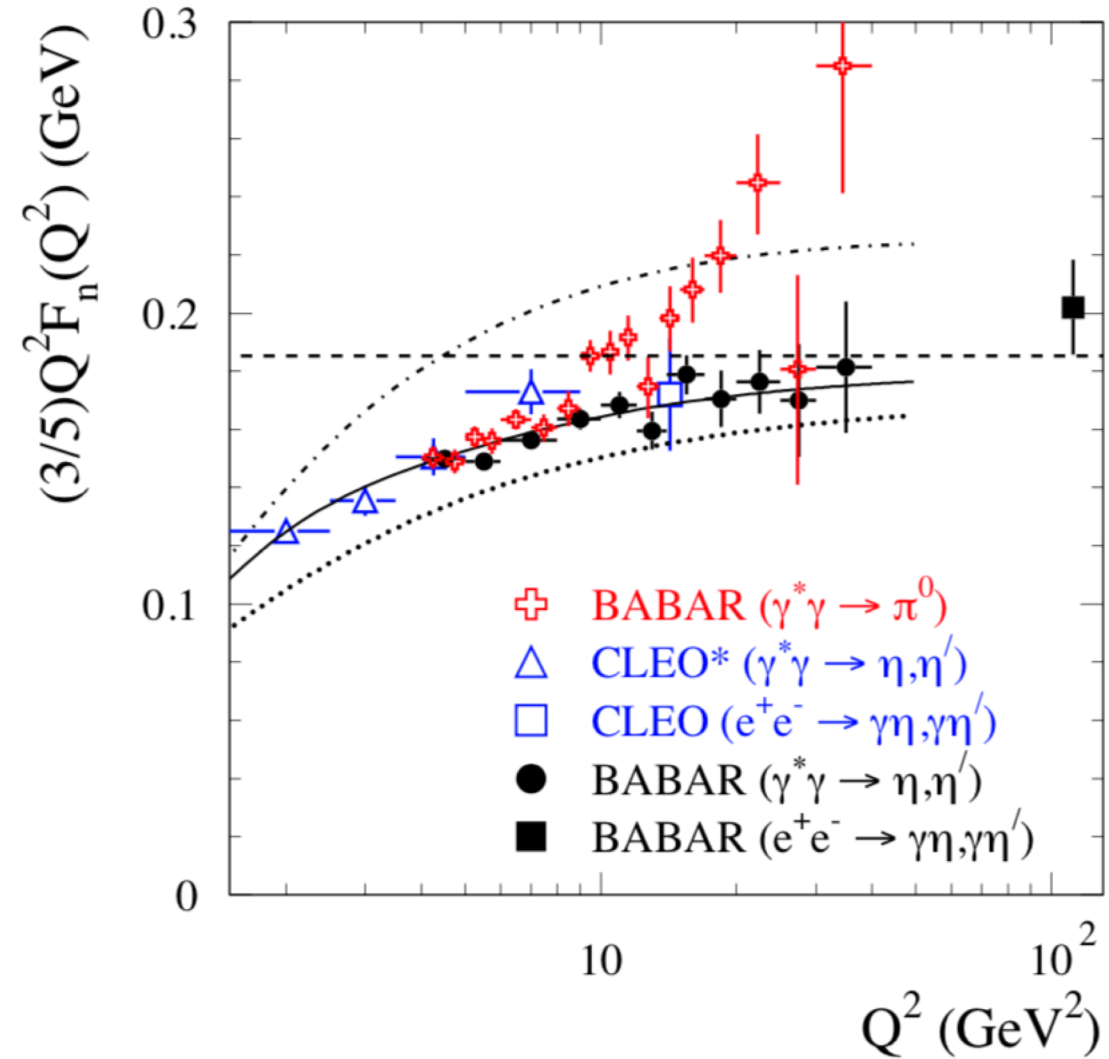


1. The double-virtual transition FF is less sensitive to NLO than the single-virtual one.

2. The form  $1/[xQ_1^2 + (1-x)Q_2^2]$  is not divergent, so double-virtual transition FF is less sensitive to a shape of the meson DA than the single-virtual FF.



# Summary of TFF results



# Analysis overview

The analysis is based on the previous BaBar study

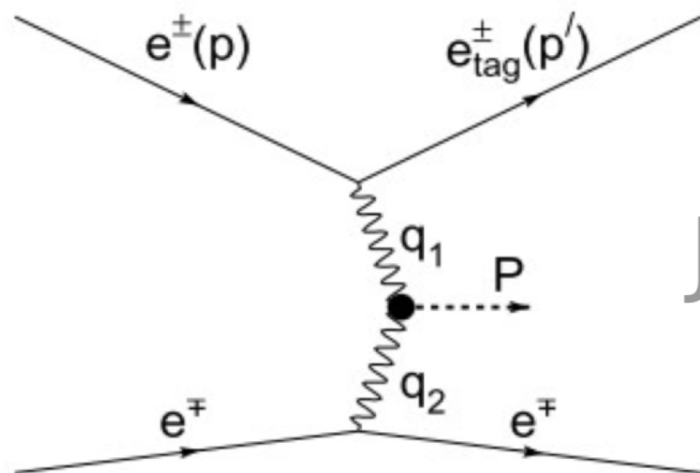
## previous

Phys. Rev. D 84, 052001 (2011)

$\gamma\gamma^* \rightarrow \eta'$

Single tagged

~ 5000 signal events



$$J^{PC} = 0^{-+}$$

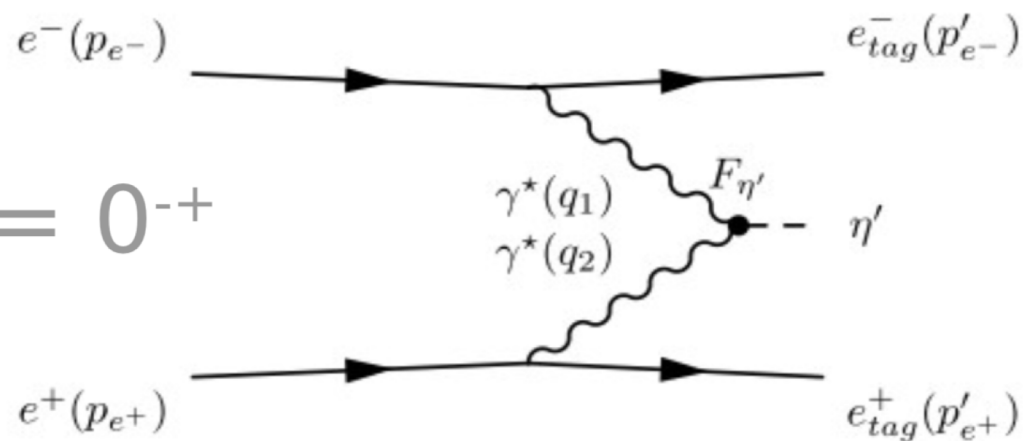
## new

Phys. Rev. D 98, 112002 (2018)

$\gamma^*\gamma^* \rightarrow \eta'$

Double tagged

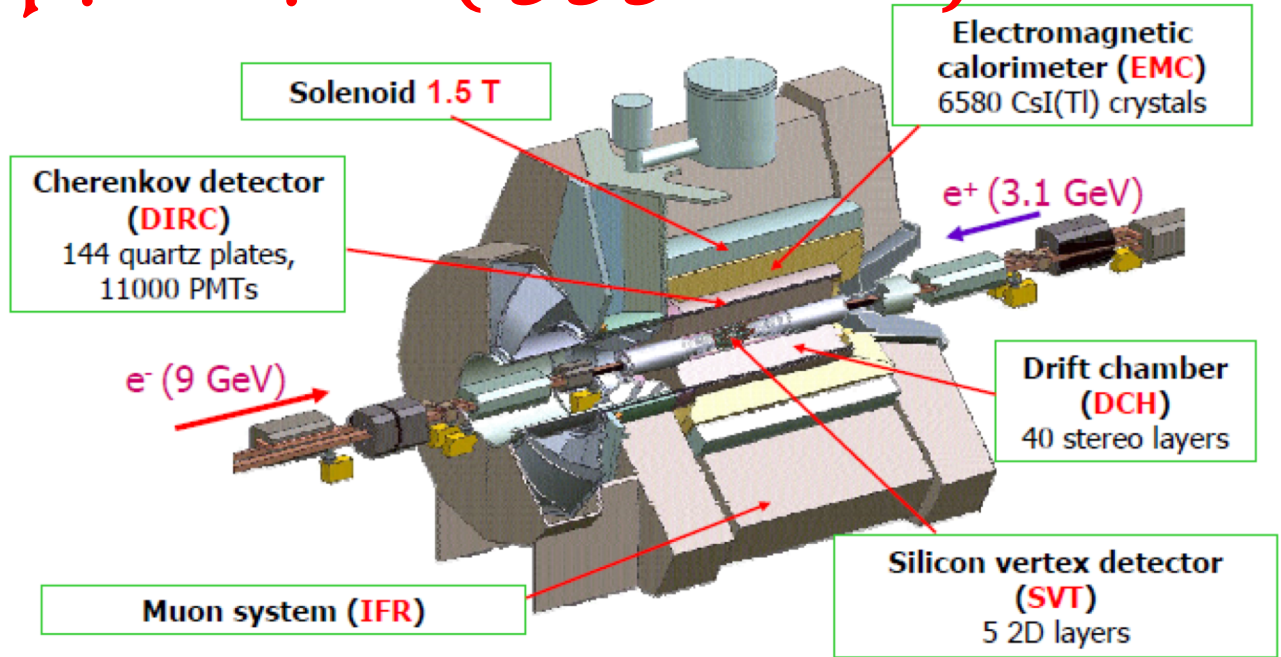
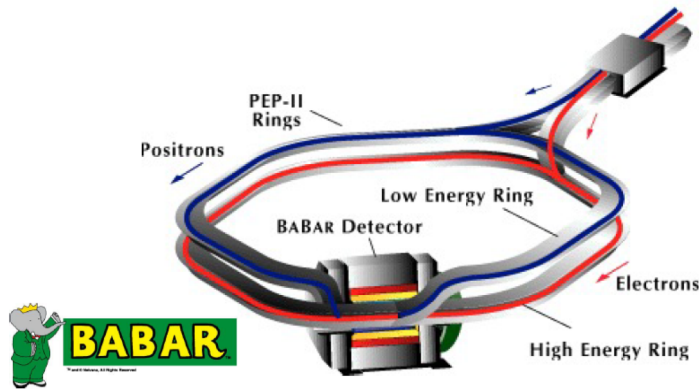
$46^{+8}_{-7}$  signal events



- A large number of systematic uncertainties were studied in our previous work where the number of signal events was significantly larger.

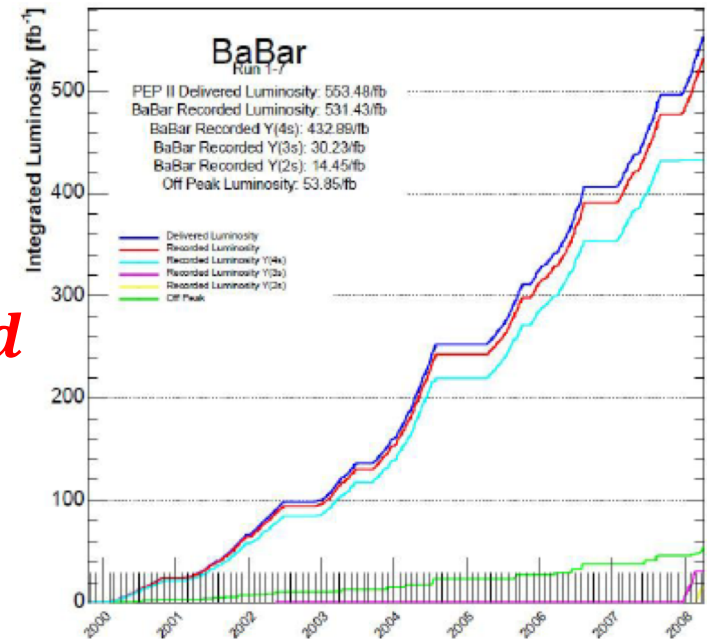
# BaBar Experiment (1999-2008)

PEP-II:  $e^+e^-$  collider,  $3.1 \times 9 \text{ GeV}^2$   
 $\sqrt{s} = 10.58 \text{ GeV} [\Upsilon(4S)]$

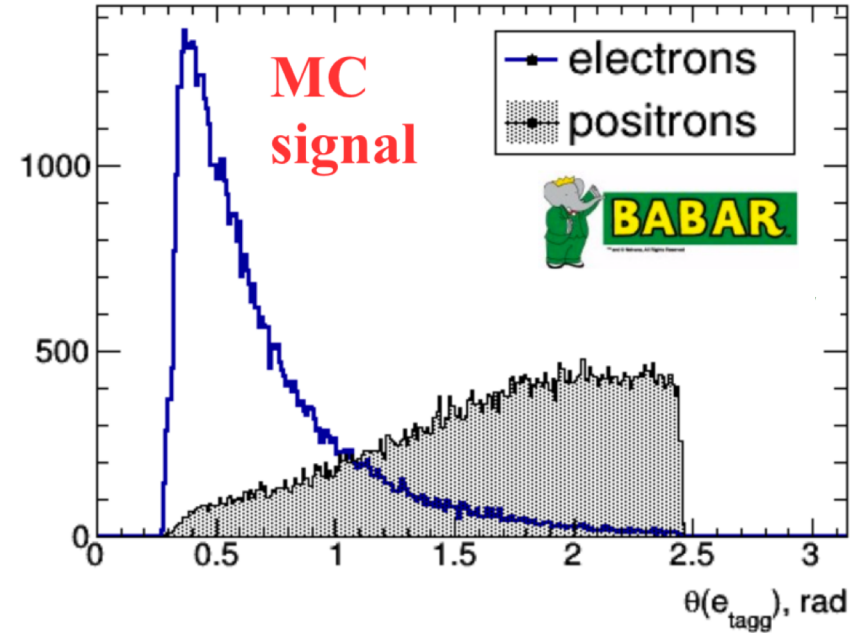
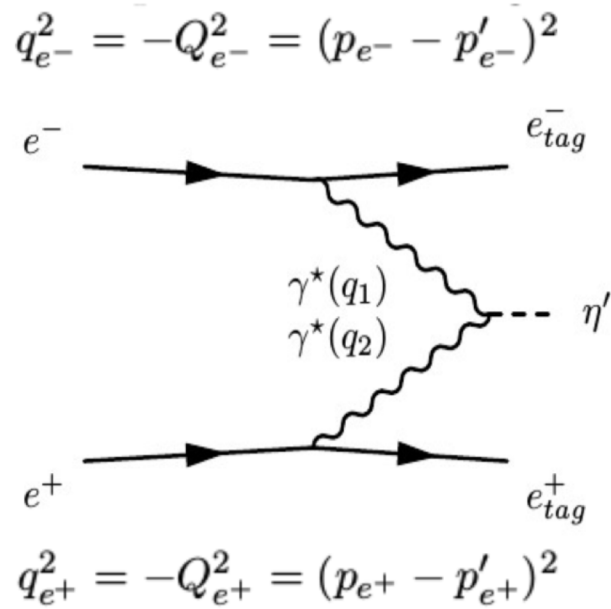


$$\mathcal{L}_{\text{peak}} = 12.069 \times 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$$

- $\int \mathcal{L} dt \approx 430 \text{ fb}^{-1} @ \Upsilon(4S)$  and  $45 \text{ fb}^{-1}$  40 MeV below  $\Upsilon(4S)$
- 470 M BB pairs
- Total  $\int \mathcal{L} dt \approx 550 \text{ fb}^{-1}$



# Technique.

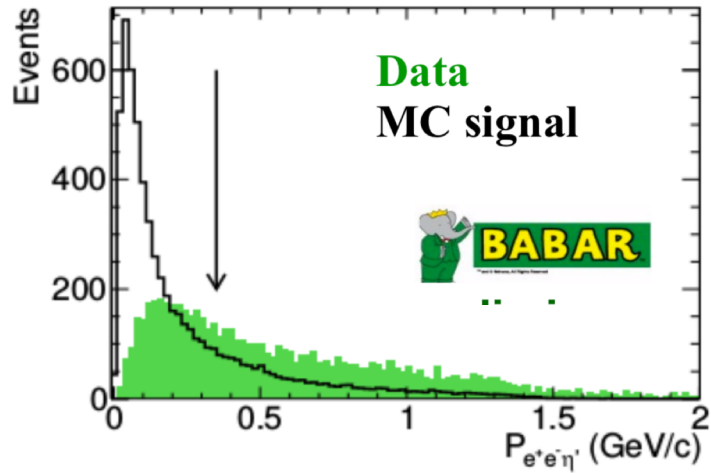


- The decay chain  $\eta' \rightarrow \pi^+ \pi^- \eta \rightarrow \pi^+ \pi^- 2\gamma$  is used *Polar angle distribution for tagged electrons (positrons)*
- A total integrated luminosity  $L = 469 \text{ fb}^{-1}$
- GGResRc event generator is used [[arXiv:1010.5969](https://arxiv.org/abs/1010.5969)]. Initial and final state radiative corrections as well as vacuum polarization effects are included. The form factor is fixed to the constant value  $F(0,0)$ .

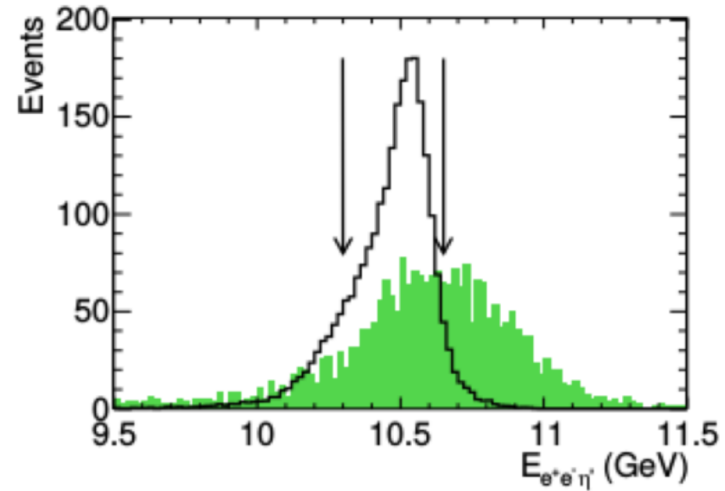
The strategy:  $dN/dQ^2 \longrightarrow d\sigma/dQ^2 \longrightarrow |F(Q^2)|$

# Event Selection (I).

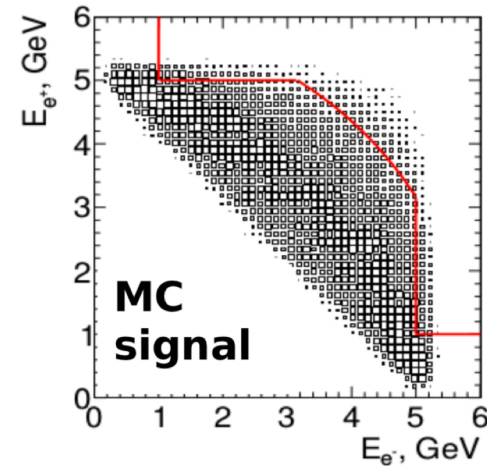
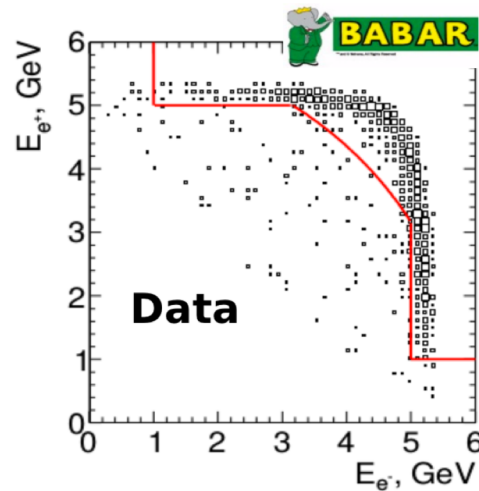
- The total reconstructed **momentum** of  $e^+e^-\pi^+\pi^-\eta$  system in c.m. frame is less than 0.35 GeV/c.



- The total reconstructed **energy** of  $e^+e^-\pi^+\pi^-\eta$  system in c.m. frame belongs to the range [10.3:10.7] GeV

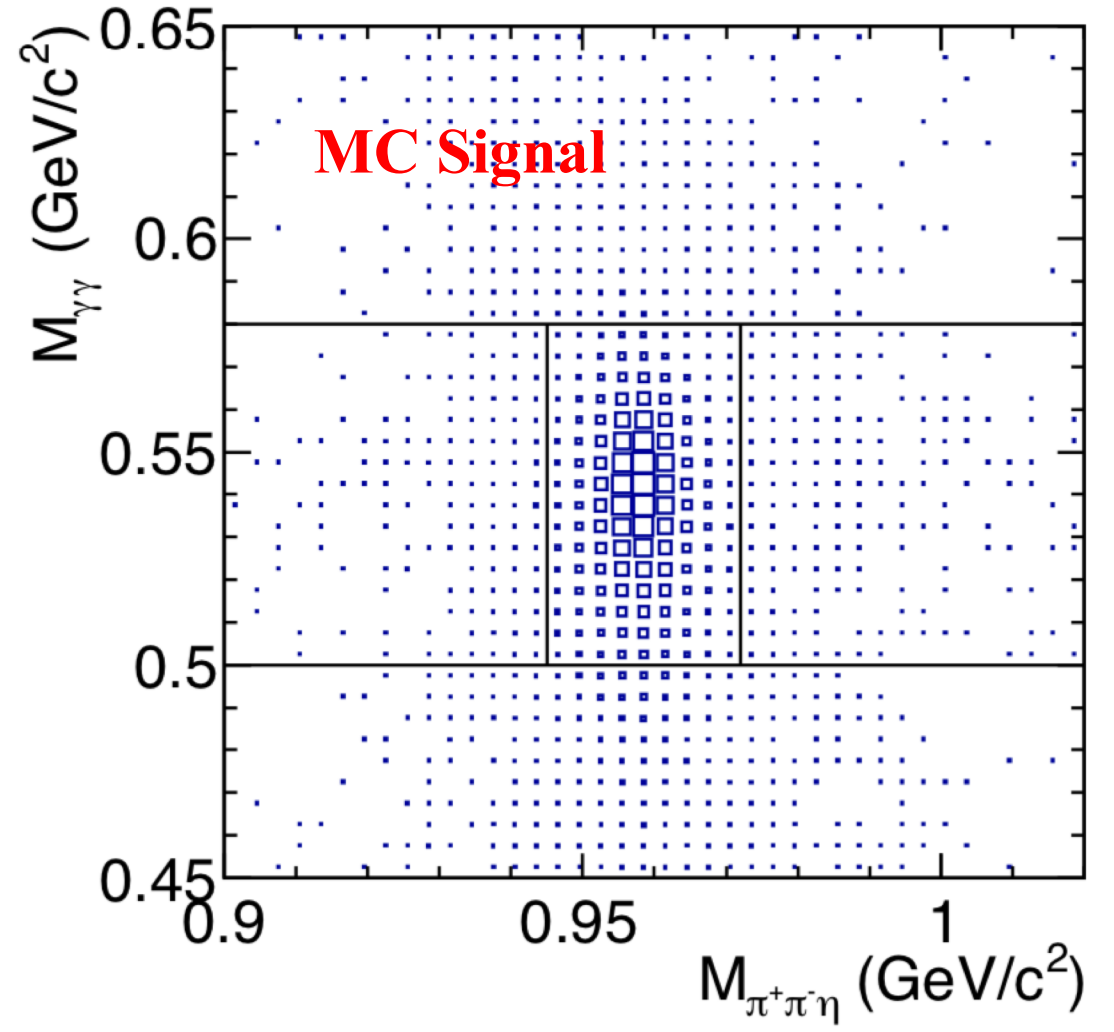
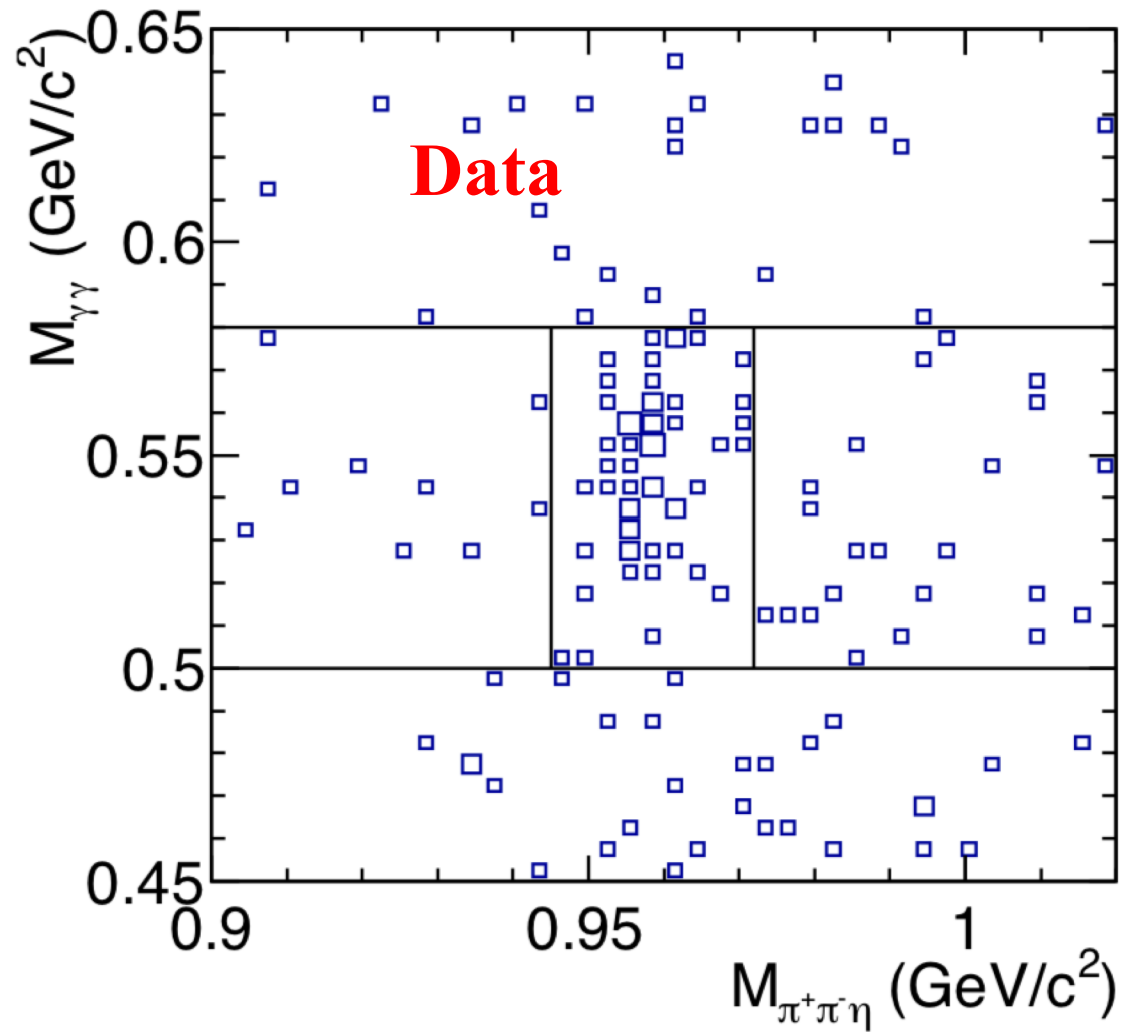


- Events that lie above and on the right of the lines (mostly, Bhabha scattering) are rejected.

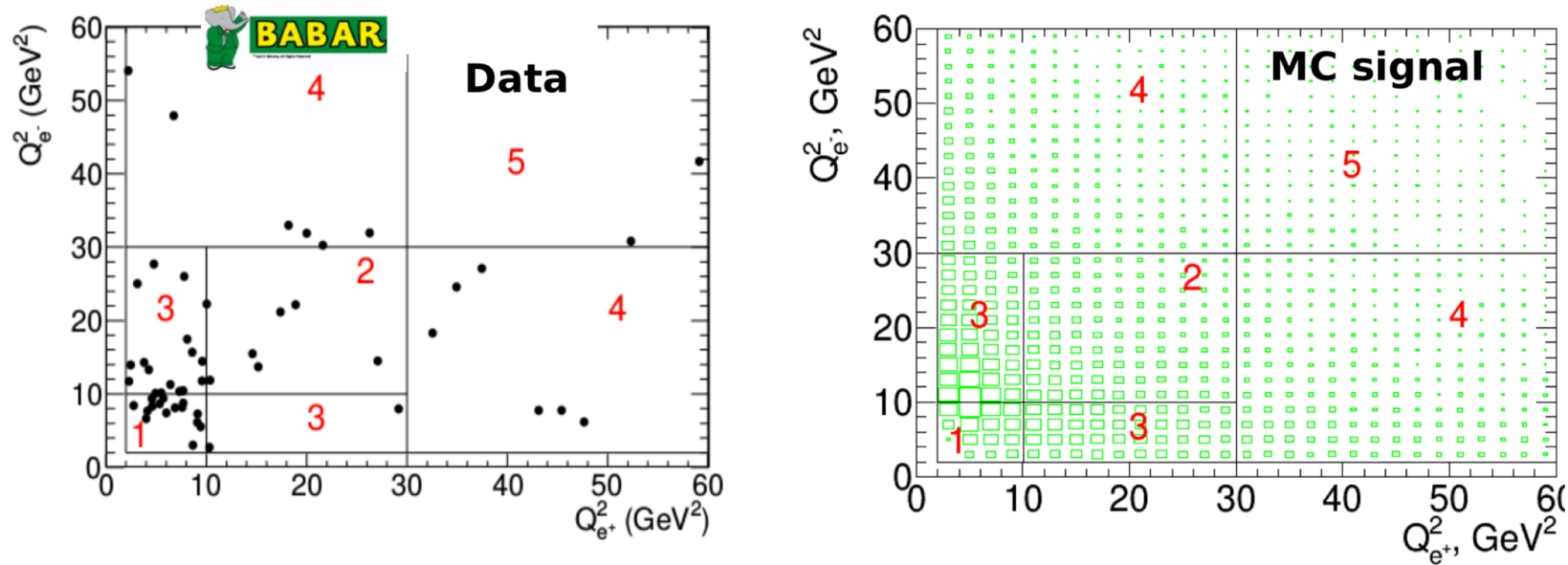


The positron c.m. energy vs. the electron c.m. energy

# Event Selection (II).



# Event Selection (IV).

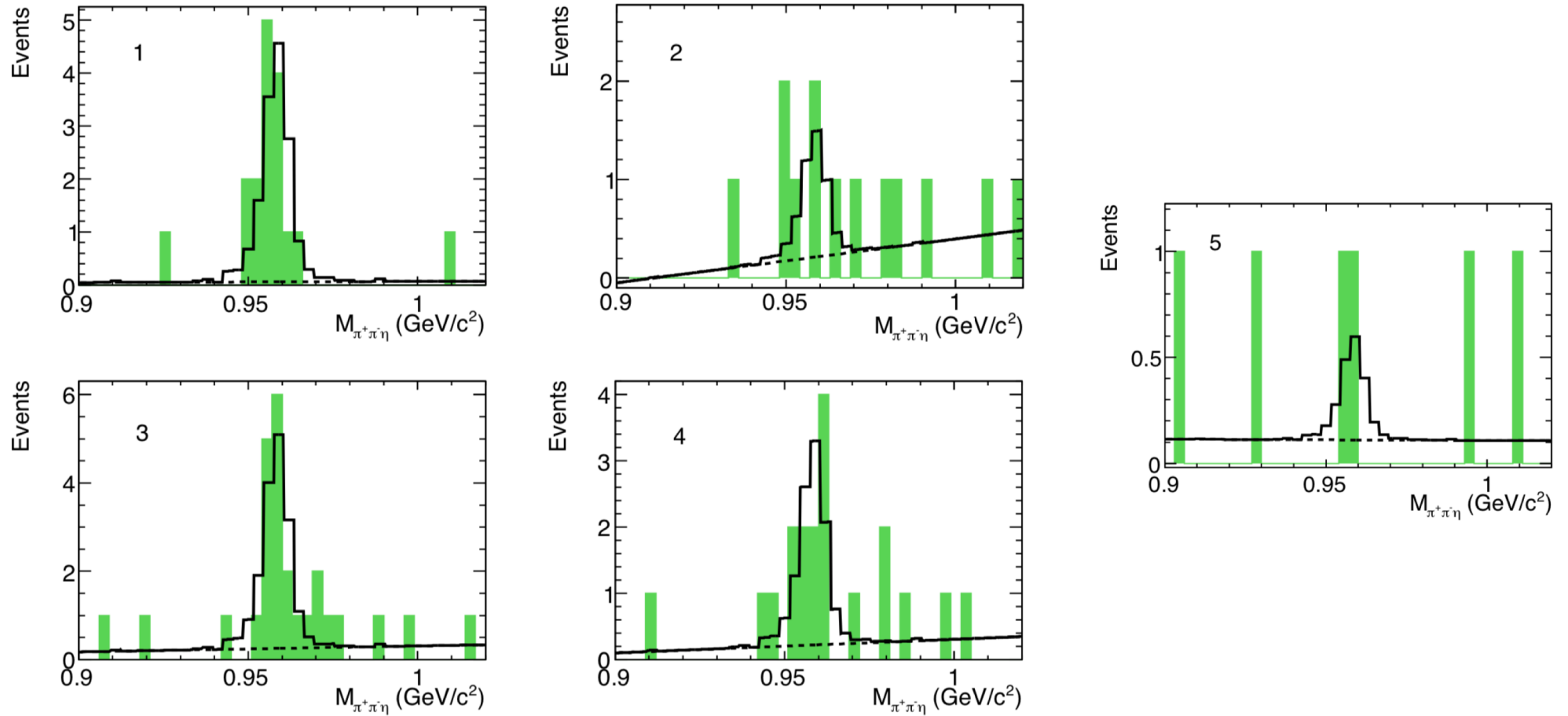


The  $Q_{e-}^2$  vs.  $Q_{e+}^2$  for events with  $0.945 < m_{2\pi\eta} < 0.972$  GeV/c<sup>2</sup>

- New definition:  $Q_1^2 = \max(Q_{e+}^2, Q_{e-}^2)$ ,  $Q_2^2 = \min(Q_{e+}^2, Q_{e-}^2)$
- The average momentum transfers for each region are calculated using the data spectrum normalized to the detection efficiency:

$$\overline{Q_{1,2}^2} = \frac{\sum_i Q_{1,2}^2(i) / \epsilon(Q_1^2, Q_2^2)}{\sum_i 1 / \epsilon(Q_1^2, Q_2^2)}$$

# Event Selection (V).



The  $\pi^+\pi^-\eta$  mass spectra for data events from the five  $(Q_1^2, Q_2^2)$  regions of Fig. 7. The open histograms are the fit results. The dashed lines represent fitted background.

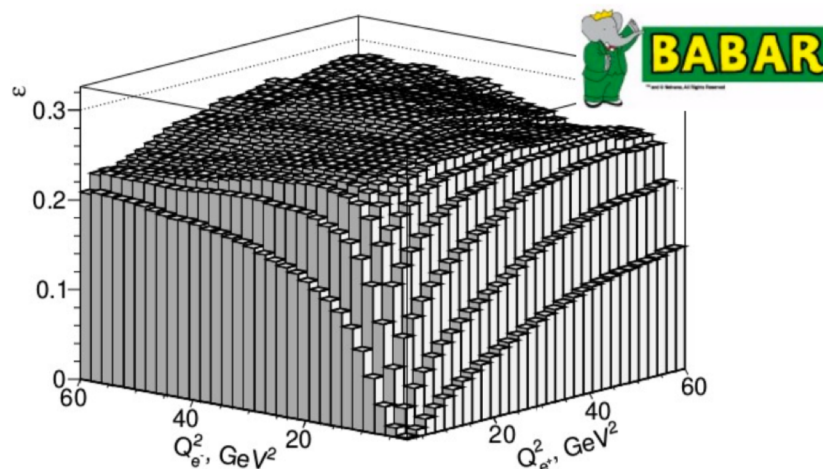


# Detection efficiency.

- The detector acceptance limits the  $e^-e^+$  detection efficiency at small  $Q^2$ . The minimum  $Q^2$  equals to  $2 \text{ GeV}^2$ .

$$\epsilon_{true} = \frac{\int \epsilon(Q_1^2, Q_2^2) F_{\eta'}^2(Q_1^2, Q_2^2) dQ_1^2 dQ_2^2}{\int F_{\eta'}^2(Q_1^2, Q_2^2) dQ_1^2 dQ_2^2}$$

$F_{\eta'}$ , from master formula at Slide #8



*The dependence of detection efficiency on momentum transfers.*

- Radiative corrections  $R(Q_1^2, Q_2^2) = \frac{\sigma^{rad}(Q_1^2, Q_2^2)}{\sigma^{born}(Q_1^2, Q_2^2)}$
- R leads to the decrease of the detection efficiency by  $\sim 15 \%$ .
- The maximum energy of the photon emitted from the initial state is restricted by the requirement  $E_\gamma < 0.05\sqrt{s}$ , where  $\sqrt{s}$  is the  $e^+e^-$  center-of-mass (c.m.) energy.

# Cross section and FormFactor.

- The differential cross section for  $e^+e^- \rightarrow e^+e^-\eta'$  is calculated as

$$\frac{d^2\sigma}{dQ_1^2 dQ_2^2} = \frac{1}{\epsilon_{\text{true}} R L B} \frac{d^2 N}{dQ_1^2 dQ_2^2}$$

$$F^2(\overline{Q}_1^2, \overline{Q}_2^2) = \frac{(d^2\sigma / (dQ_1^2 dQ_2^2))_{\text{data}}}{(d^2\sigma / (dQ_1^2 dQ_2^2))_{\text{MC}}} F_{\eta'}^2(\overline{Q}_1^2, \overline{Q}_2^2)$$

- $B = B(\eta' \rightarrow \pi^+\pi^-\eta) \times B(\eta \rightarrow 2\gamma) = (0.3941 \pm 0.0020) \times (0.429 \pm 0.007) = 0.169 \pm 0.003$

- $\sigma_{e^+e^- \rightarrow e^+e^-\eta'} (2 < Q_1^2, Q_2^2 < 60 \text{ GeV}^2) = (11.4^{+2.8}_{-2.4}) \text{ fb}$

$\overline{Q}_1^2, \overline{Q}_2^2, \text{ GeV}^2$	$\epsilon_{\text{true}}$	$R$	$N_{\text{events}}$	$d^2\sigma / (dQ_1^2 dQ_2^2) \times 10^4, \text{ fb/GeV}^4$	$F(\overline{Q}_1^2, \overline{Q}_2^2) \times 10^3, \text{ GeV}^{-1}$
6.48, 6.48	0.019	1.03	$14.7^{+4.3}_{-3.6}$	$1471.8^{+430.1}_{-362.9}$	$14.32^{+1.95}_{-1.89} \pm 0.83 \pm 0.14$
16.85, 16.85	0.282	1.10	$4.1^{+2.7}_{-2.7}$	$4.2^{+2.8}_{-2.8}$	$5.35^{+1.54}_{-1.54} \pm 0.31 \pm 0.42$
14.83, 4.27	0.145	1.07	$15.8^{+4.8}_{-4.0}$	$39.7^{+12.0}_{-10.2}$	$8.24^{+1.16}_{-1.13} \pm 0.48 \pm 0.65$
38.11, 14.95	0.226	1.11	$10.0^{+3.9}_{-3.2}$	$3.0^{+1.2}_{-1.0}$	$6.07^{+1.09}_{-1.07} \pm 0.35 \pm 1.21$
45.63, 45.63	0.293	1.22	$1.6^{+1.8}_{-1.1}$	$0.6^{+0.7}_{-0.6}$	$8.71^{+3.96}_{-8.71} \pm 0.50 \pm 1.04$

Statistical uncertainty is dominated

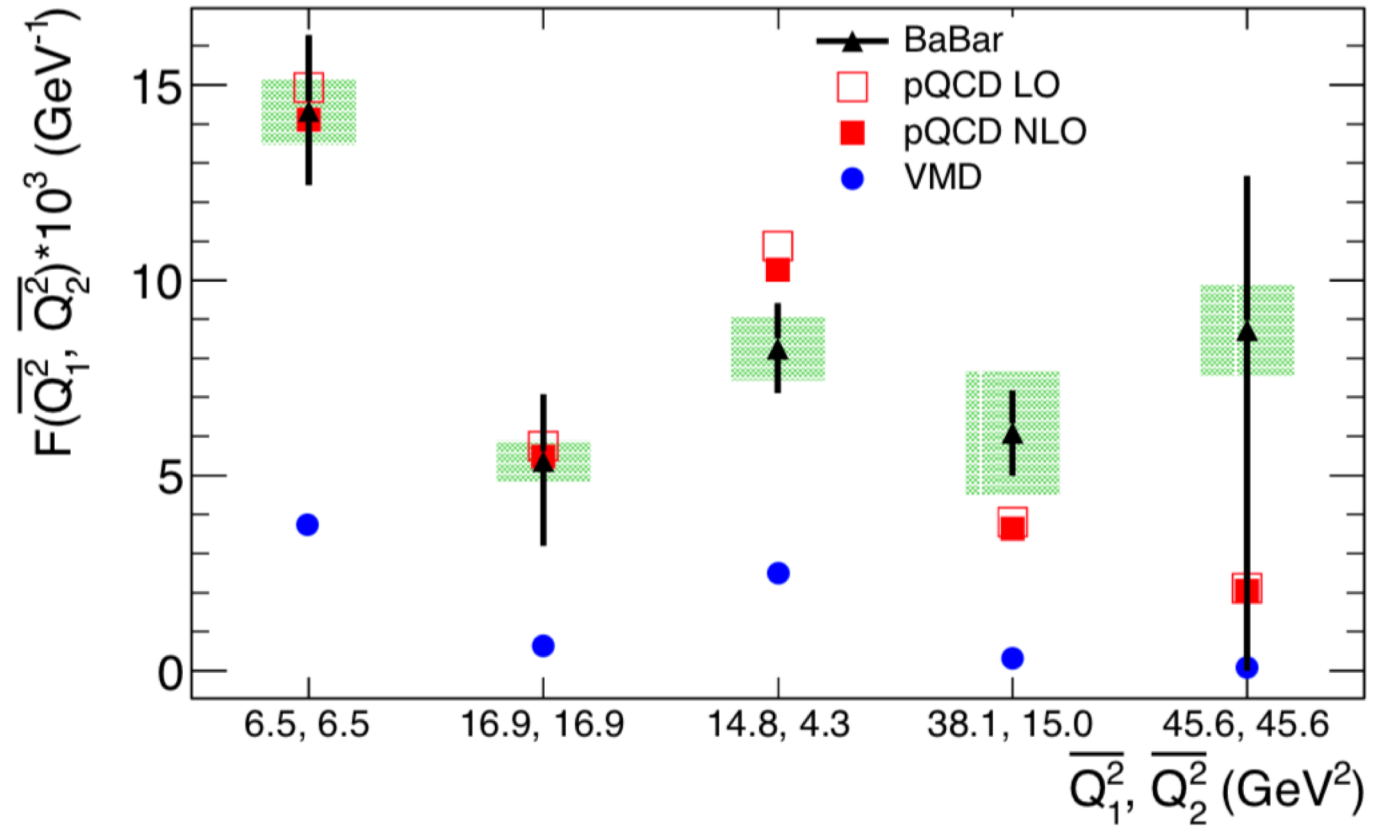
Statistical

Systematic

Model<sup>18</sup>

# Summary

- About 46 events of  $e^+e^- \rightarrow e^+e^-\eta'$  were observed in the double tagged mode for the first time
- The  $\gamma^*\gamma^* \rightarrow \eta'$  transition formfactor  $F(Q_1^2, Q_2^2)$  has been measured for  $Q^2$  range from 2 to 60  $\text{GeV}^2$ .
- The formfactor is in reasonable agreement with the pQCD prediction and contradicts the prediction of VDM



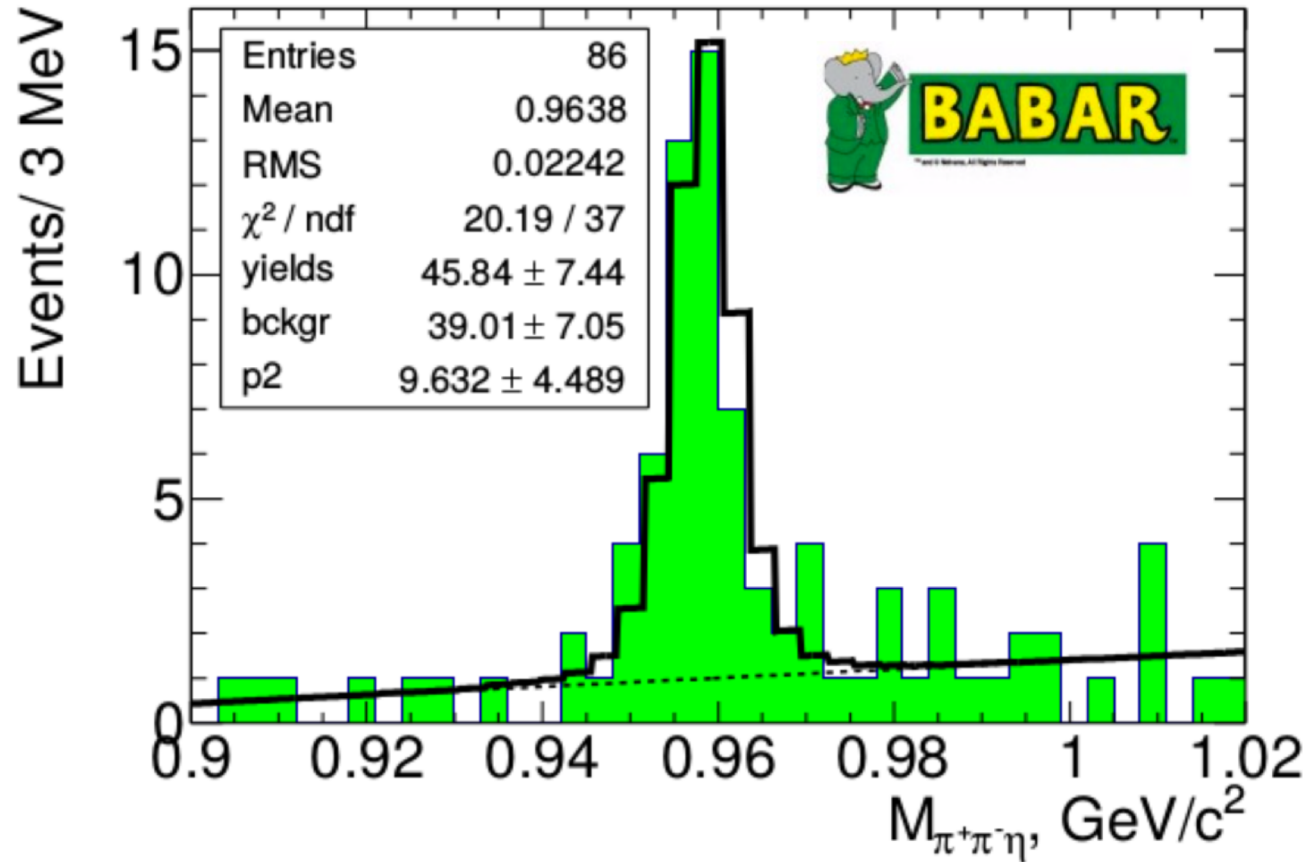
# Spare Slides



# Introduction. Basic features of $\gamma\gamma$ collisions

- $\sigma(e^+e^- \rightarrow e^+e^- \gamma^* \gamma^* \rightarrow e^+e^- f) \propto \alpha^4 \log^2 E/m_e$   
compared to  
 $\sigma(e^+e^- \rightarrow \gamma^* \rightarrow f) \propto \alpha^2/E^2$
- Particles produced in  $\gamma\gamma$  collisions have  $C = +1$  and  $J^P = 0^\mp, 2^\mp$  while those in single-photon annihilation have  $C = -1$  and  $J^P = 1^-$
- Special kinematics:
  - Initial electrons tend to fly in their original directions and lose a small part of their energy
  - The produced system of particles  $f$  has  $E_{\text{tot}} \ll \sqrt{s} = 2E$  and tends to have small transverse momentum

# Event Selection (III).



*The  $\pi^+\pi^-\eta$  mass spectra for data events. The open histogram is the fit result. The dashed line represents fitted background.*