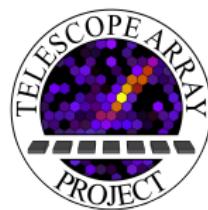


# The Telescope Array experiment

Armando di Matteo for the Telescope Array collaboration  
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Université Libre de Bruxelles (ULB)  
Brussels, Belgium



eXtreme19  
22–25 January 2019  
Padova, Italy

# The Telescope Array collaboration

142 members, 35 institutions, 6 countries

R.U. Abbasi<sup>1</sup>, M. Abe<sup>2</sup>, T. Abu-Zayyad<sup>1</sup>, M. Allen<sup>1</sup>, R. Azuma<sup>3</sup>, E. Barcikowski<sup>1</sup>, J.W. Belz<sup>1</sup>, D.R. Bergman<sup>1</sup>, S.A. Blake<sup>1</sup>, R. Cady<sup>1</sup>, B.G. Cheon<sup>4</sup>, J. Chiba<sup>5</sup>, M. Chikawa<sup>6</sup>, A. di Matteo<sup>7</sup>, T. Fujii<sup>8</sup>, K. Fujita<sup>9</sup>, M. Fukushima<sup>10,11</sup>, G. Furlich<sup>1</sup>, T. Goto<sup>9</sup>, W. Hanlon<sup>1</sup>, M. Hayashi<sup>12</sup>, Y. Hayashi<sup>9</sup>, N. Hayashida<sup>13</sup>, K. Hibino<sup>13</sup>, K. Honda<sup>14</sup>, D. Ikeda<sup>10</sup>, N. Inoue<sup>2</sup>, T. Ishii<sup>14</sup>, R. Ishimori<sup>3</sup>, H. Ito<sup>15</sup>, D. Ivanov<sup>1</sup>, H.M. Jeong<sup>16</sup>, S. Jeong<sup>16</sup>, C.C.H. Jui<sup>1</sup>, K. Kadota<sup>17</sup>, F. Kakimoto<sup>3</sup>, O. Kalashev<sup>18</sup>, K. Kasahara<sup>19</sup>, H. Kawai<sup>20</sup>, S. Kawakami<sup>9</sup>, S. Kawana<sup>2</sup>, K. Kawata<sup>10</sup>, E. Kido<sup>10</sup>, H.B. Kim<sup>4</sup>, J.H. Kim<sup>1</sup>, J.H. Kim<sup>21</sup>, S. Kishigami<sup>9</sup>, S. Kitamura<sup>3</sup>, Y. Kitamura<sup>3</sup>, V. Kuzmin<sup>18\*</sup>, M. Kuznetsov<sup>18</sup>, Y.J. Kwon<sup>22</sup>, K.H. Lee<sup>16</sup>, B. Lubsandorzhiev<sup>18</sup>, J.P. Lundquist<sup>1</sup>, K. Machida<sup>14</sup>, K. Martens<sup>11</sup>, T. Matsuyama<sup>9</sup>, J.N. Matthews<sup>1</sup>, R. Mayta<sup>9</sup>, M. Minamino<sup>9</sup>, K. Mukai<sup>14</sup>, I. Myers<sup>1</sup>, K. Nagasawa<sup>2</sup>, S. Nagataki<sup>15</sup>, R. Nakamura<sup>23</sup>, T. Nakamura<sup>24</sup>, T. Nonaka<sup>10</sup>, H. Oda<sup>9</sup>, S. Ogio<sup>9</sup>, J. Ogura<sup>3</sup>, M. Ohnishi<sup>10</sup>, H. Ohoka<sup>10</sup>, T. Okuda<sup>25</sup>, Y. Omura<sup>9</sup>, M. Ono<sup>15</sup>, R. Onogi<sup>9</sup>, A. Oshima<sup>9</sup>, S. Ozawa<sup>19</sup>, I.H. Park<sup>16</sup>, M.S. Pshirkov<sup>18,26</sup>, J. Remington<sup>1</sup>, D.C. Rodriguez<sup>1</sup>, G. Rubtsov<sup>18</sup>, D. Ryu<sup>21</sup>, H. Sagawa<sup>10</sup>, R. Sahara<sup>9</sup>, K. Saito<sup>10</sup>, Y. Saito<sup>23</sup>, N. Sakaki<sup>10</sup>, T. Sako<sup>10</sup>, N. Sakurai<sup>9</sup>, L.M. Scott<sup>27</sup>, T. Seki<sup>23</sup>, K. Sekino<sup>10</sup>, P.D. Shah<sup>1</sup>, F. Shibata<sup>14</sup>, T. Shibata<sup>10</sup>, H. Shimodaira<sup>10</sup>, B.K. Shin<sup>9</sup>, H.S. Shin<sup>10</sup>, J.D. Smith<sup>1</sup>, P. Sokolsky<sup>1</sup>, B.T. Stokes<sup>1</sup>, S.R. Stratton<sup>1,27</sup>, T.A. Stroman<sup>1</sup>, T. Suzawa<sup>2</sup>, Y. Takagi<sup>9</sup>, Y. Takahashi<sup>9</sup>, M. Takamura<sup>5</sup>, M. Takeda<sup>10</sup>, R. Takeishi<sup>16</sup>, A. Taketa<sup>28</sup>, M. Takita<sup>10</sup>, Y. Tameda<sup>29</sup>, H. Tanaka<sup>9</sup>, K. Tanaka<sup>30</sup>, M. Tanaka<sup>31</sup>, S.B. Thomas<sup>1</sup>, G.B. Thomson<sup>1</sup>, P. Tinyakov<sup>7,18</sup>, I. Tkachev<sup>18</sup>, H. Tokuno<sup>3</sup>, T. Tomida<sup>23</sup>, S. Troitsky<sup>18</sup>, Y. Tsunesada<sup>9</sup>, K. Tsutsumi<sup>3</sup>, Y. Uchihori<sup>32</sup>, S. Udo<sup>13</sup>, F. Urban<sup>33</sup>, T. Wong<sup>1</sup>, M. Yamamoto<sup>23</sup>, R. Yamane<sup>9</sup>, H. Yamaoka<sup>31</sup>, K. Yamazaki<sup>13</sup>, J. Yang<sup>34</sup>, K. Yashiro<sup>5</sup>, Y. Yoneda<sup>9</sup>, S. Yoshida<sup>20</sup>, H. Yoshii<sup>35</sup>, Y. Zhezher<sup>18</sup>, and Z. Zundel<sup>1</sup>



# Outline

## 1 Introduction

- Ultra-high-energy cosmic rays (UHECRs)
- The Telescope Array (TA) experiment

## 2 Main results

- Energy spectrum
- Mass composition
- Arrival directions

## 3 Future prospects

- The ongoing Telescope Array extension: TA $\times 4$

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## 1 Introduction

- Ultra-high-energy cosmic rays (UHECRs)
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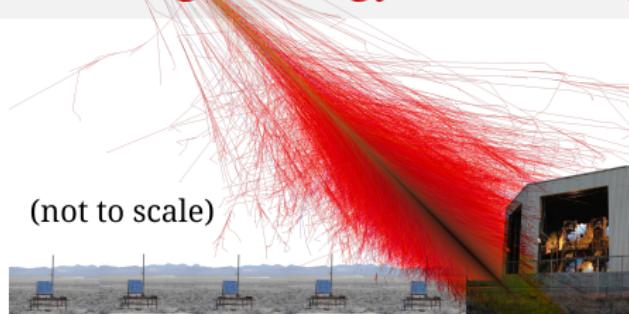
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# Ultra-high-energy cosmic rays (UHECRs)



- Atomic nuclei from space with  $E > 1 \text{ EeV} = 10^{18} \text{ eV} \approx 0.16 \text{ J}$
- Deflected by magnetic fields → arrival direction  $\neq$  source position ( $\Delta\theta \sim 30Z \left(\frac{E}{10 \text{ EeV}}\right)^{-1}$  degrees)
- In the atmosphere, they initiate extensive air showers (EAS),

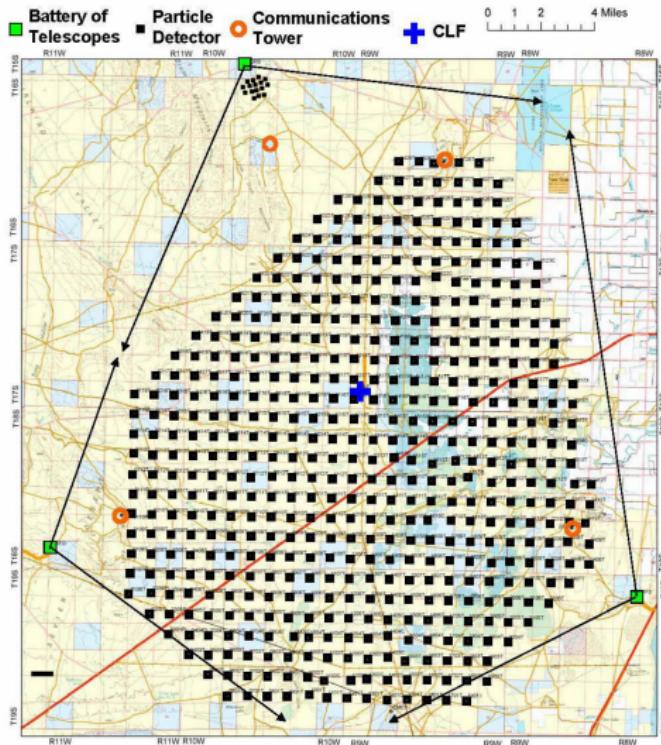
which can be detected by:

- Surface detector arrays (duty cycle  $\sim 100\%$ , but severely model-dependent)
- Fluorescence telescopes (more precise reconstruction, but only in clear moonless nights, duty cycle  $\sim 15\%$ )
- With hybrid detectors, we can use fluorescence measurements to calibrate the energy scale for surface detectors.

Largest operating UHECR detectors: the Pierre Auger Observatory (Auger;  $3000 \text{ km}^2$ , Argentina) and the Telescope Array (TA;  $700 \text{ km}^2$ , Utah, USA)

# The Telescope Array experiment

The largest cosmic-ray detector in the Northern Hemisphere



- Location:  $39.3^\circ \text{ N}, 112.9^\circ \text{ W}$ ,  
1400 m a.s.l. ( $\approx 880 \text{ g/cm}^2$ )  
Millard County, Utah, USA
- Main array for UHE:
  - 507 surface detectors (SD),  
1.2 km spacing ( $700 \text{ km}^2$ )
  - 3 fluorescence detector (FD)  
sites (38 telescopes in total)
- Low-energy extension (TALE):
  - 10 extra FD telescopes at  
higher elevation
  - 103 extra SDs with 400 m  
and 600 m spacing
- Main SD array taking data  
since 11 May 2008

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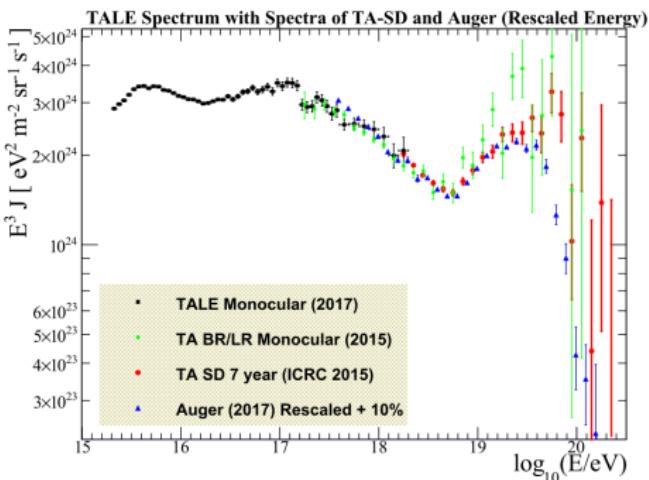
## 3 Future prospects

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# The energy spectrum

ApJ 865 (2018) 74 (TALE), APh 80 (2016) 131 (TA FD), PoS ICRC2015 (2016) 035 (TA SD)

- Self-consistent measurements of spectrum over 5 decades



- (TALE, TA FD and TA SD data not artificially shifted in energy or normalization)

- Features:

knee*, $10^{15.6}$ eV	$\gamma \approx 2.7$
low- $E$ ankle, $10^{16.2}$ eV	$\gamma = 3.1$
2nd knee, $10^{17.0}$ eV	$\gamma = 2.9$
ankle, $10^{18.7}$ eV	$\gamma = 3.2$
cutoff, $10^{19.8}$ eV	$\gamma = 2.7$
	$\gamma = 4.6$

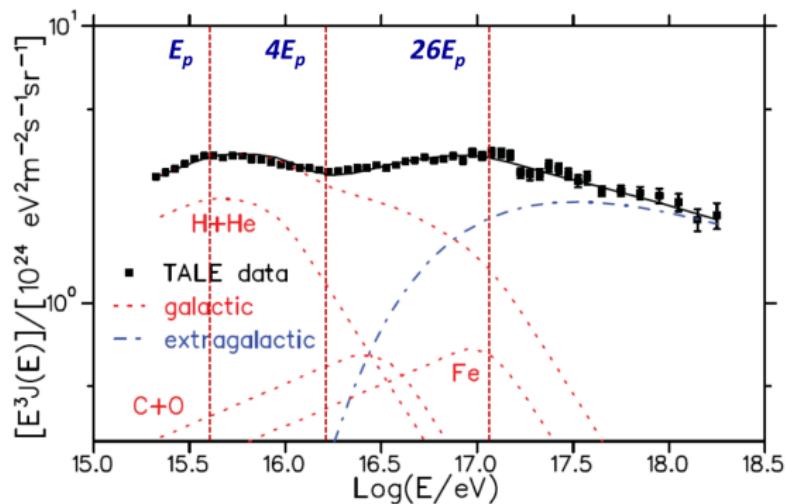
\*We haven't tried to fit it with TALE data (reduced efficiency, large systematics), but low-energy experiments see it there, too.

- Compatible with Auger, except for  $\approx 10\%$   $E$  shift (well within systematics,  $\pm 14\%$ <sub>Auger</sub>  $\pm 21\%$ <sub>TA</sub>), except at the highest energies

# Possible interpretation of the spectrum

T. Abu-Zayyad et al., arXiv:1803.07052 (not a full TA collaboration paper!)

(Galactic composition extrapolated from satellite measurements at lower  $E$ ;  
cutoff assumed rigidity-dependent, i.e. proportional to  $Z$ )

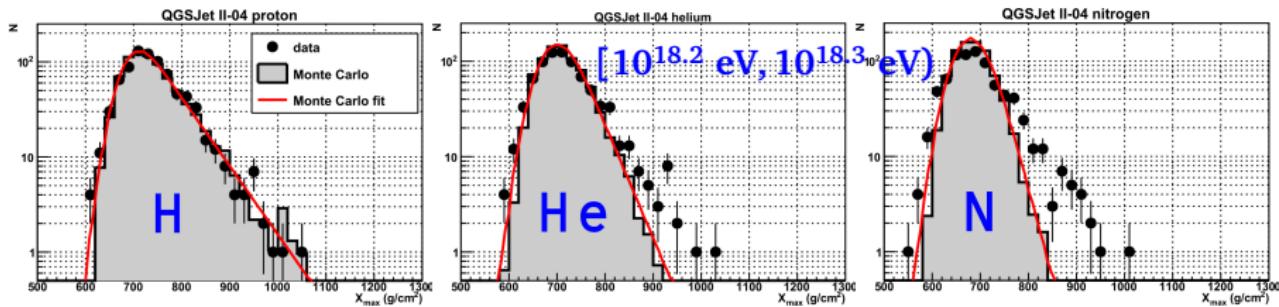


Knee due to Galactic H/He cutoff, low-energy ankle due to Li/Be/B scarcity,  
second knee due to Galactic Fe cutoff?

# Mass composition from FD measurements ( $X_{\max}$ )

Astrophys. J. 858 (2018) 76, arXiv:1801.09784

- $X_{\max}$  distribution predicted by QGSJet II-04, but allowed to be shifted to take into account model uncertainty (and measurement systematics)



$E \lesssim 10^{18.8} \text{ eV}$  Any pure element other than H excluded at  $p < 10^{-3}$

- Auger-like H+He+N mix not excluded (PoS ICRC2017 (2018) 522), but mixed compositions outside the scope of the work

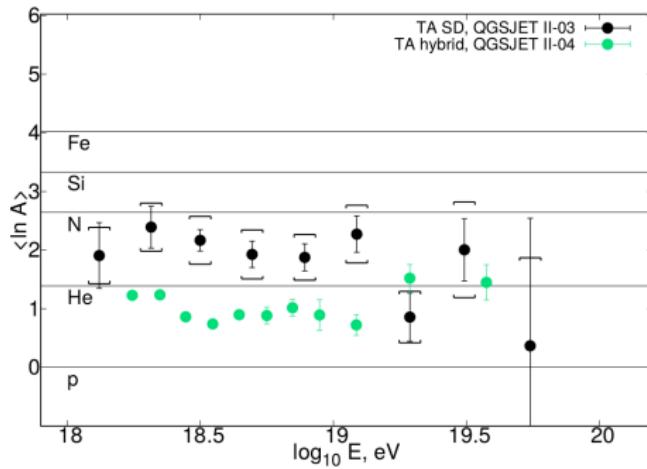
$E \lesssim 10^{19.2} \text{ eV}$  Pure elements other than H or He excluded at  $p < 10^{-3}$

$E \gtrsim 10^{19.4} \text{ eV}$  Not enough data to exclude anything from H to Fe at  $p < 5\%$

# Mass composition from SD measurements

Phys. Rev. D (in press), arXiv:1808.03680

- Boosted decision tree using 14 observables, trained on QGSJet II-03 proton and iron simulations



- Medium-light composition,  $\langle \ln A \rangle = 2.0 \pm 0.1_{\text{stat}} \pm 0.4_{\text{syst}}$
- No evidence for energy dependence

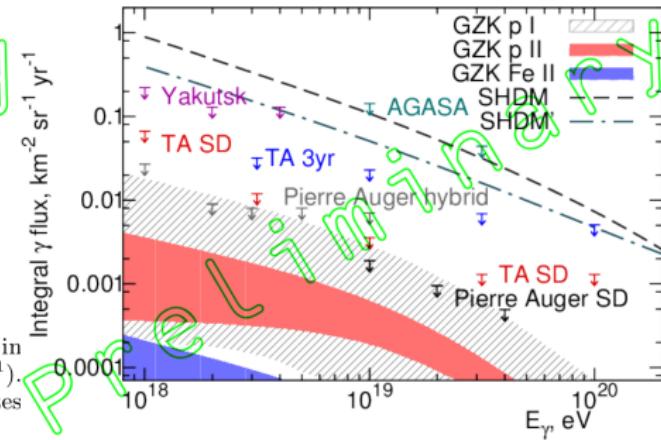
# Limits on diffuse UHE photon fluxes

arXiv:1811.03920

- Boosted decision tree using 16 observables, trained on QGSJet II-03 proton and EGS4 photon simulations

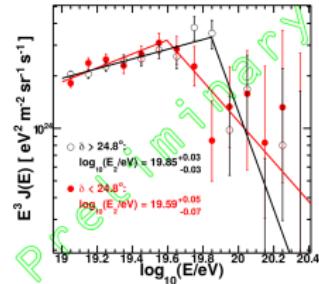
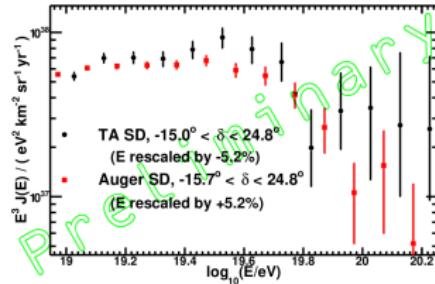
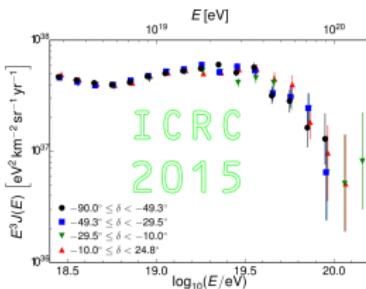
	$E_0, \text{eV}$				
	$10^{18.0}$	$10^{18.5}$	$10^{19.0}$	$10^{19.5}$	$10^{20.0}$
$\gamma$ candidates	1	0	0	0	1
$b$	0.55	1.01	0.97	0.80	0.49
$\bar{n} <$	5.14	3.09	3.09	3.09	5.14
$A_{eff}$	77	255	852	2351	4055
$F_\gamma <$	0.067	0.012	0.0036	0.0013	0.0013

TABLE II. 95% CL upper limits on the number of photons in the data set  $\bar{n}_\gamma$  and on the photon flux  $F_\gamma$  ( $\text{km}^{-2}\text{yr}^{-1}\text{sr}^{-1}$ ).  $b$  is an expected number of background photon candidates obtained with proton MC.



# Declination dependence of spectrum

Preliminary!

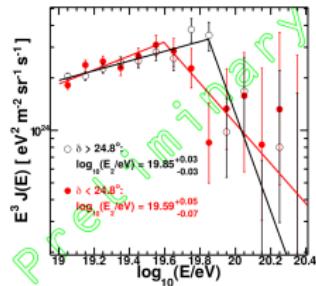
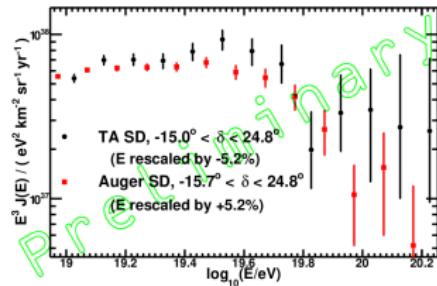
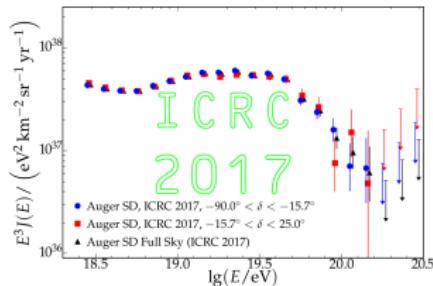


TA, north	large difference ( $3.5\sigma_{\text{post}}$ )	<a href="#">arXiv:1801.07820</a>
TA, equator	small difference?	<a href="#">PoS (ICRC 2017) 498</a>
Auger + 11%, equator	no difference	<a href="#">PoS (ICRC 2015) 271</a>
Auger + 11%, south		

- Remaining difference in common declination band being investigated by joint Auger–TA spectrum working group (see UHECR18 report)

# Declination dependence of spectrum

Preliminary!



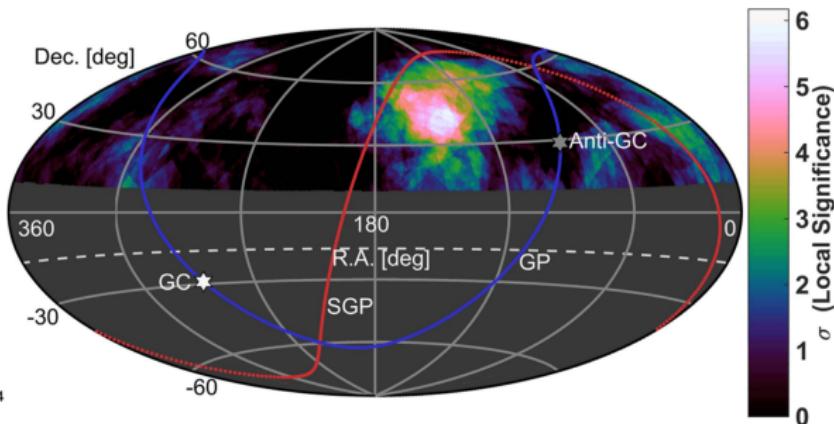
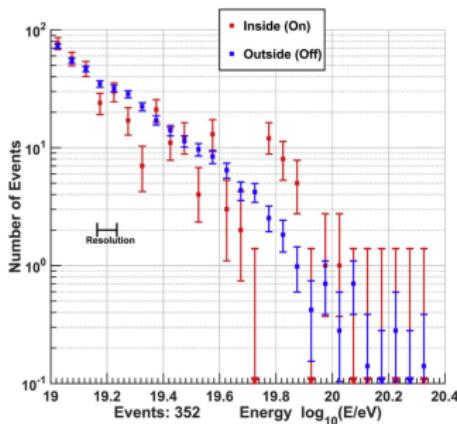
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Auger + 11%, south		

- Remaining difference in common declination band being investigated by joint Auger–TA spectrum working group (see UHECR18 report)

# Hotspot and coldspot

Astrophys. J. 862 (2018) 91, arXiv:1802.05003

- Excess of events  $> 10^{19.75}$  eV within  $\approx 30^\circ$  of  $(\alpha = 9^h 16^m, \delta = +45^\circ)$
- Deficit of lower-energy events in the same region

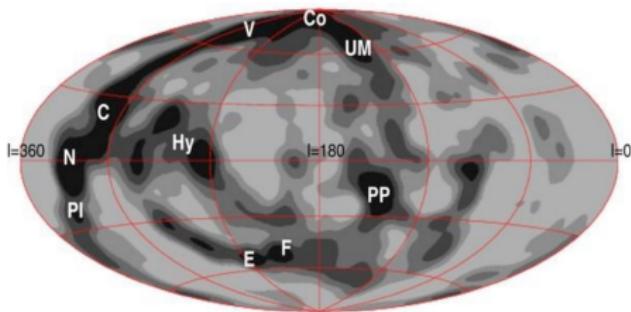


- $6.17\sigma$  pre-trial significance ( $3.74\sigma$  post-trial)

# Correlation with large-scale structures

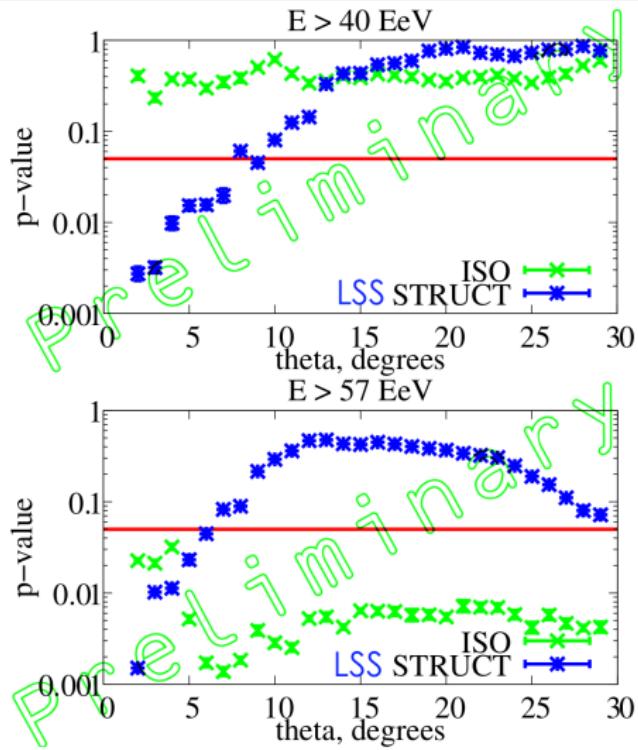
Preliminary update of *Astrophys. J.* 757 (2012) 26, arXiv:1205.5984

- LSS from the 2MASS galaxy catalog (XSCz), assuming CR lumin.  $\propto$  matter density



( $6^\circ$  smearing; rotated Galactic coordinates)

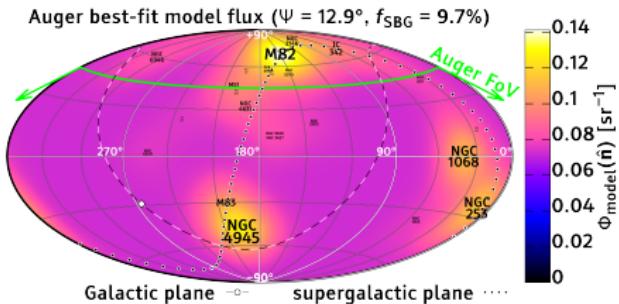
- Data above 57 EeV in tension with isotropic expectations



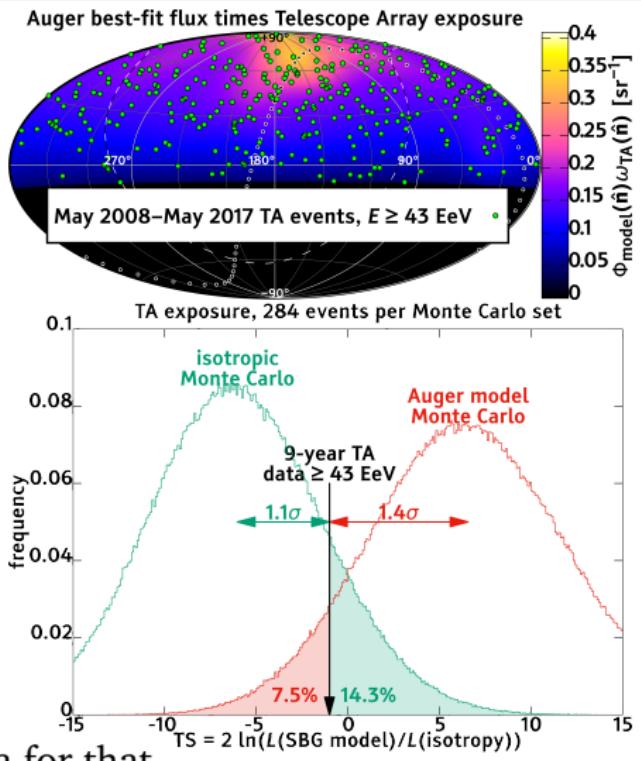
# Correlation with starburst galaxies (or lack thereof)

Astrophys. J. Lett. 867 (2018) L27, arXiv:1809.01573

- Auger arr. directions  $> 39$  EeV been reported to correlate with a catalog of nearby SBGs ( $4\sigma_{\text{post}}$  over isotropy,  $3\sigma_{\text{post}}$  over LSS)

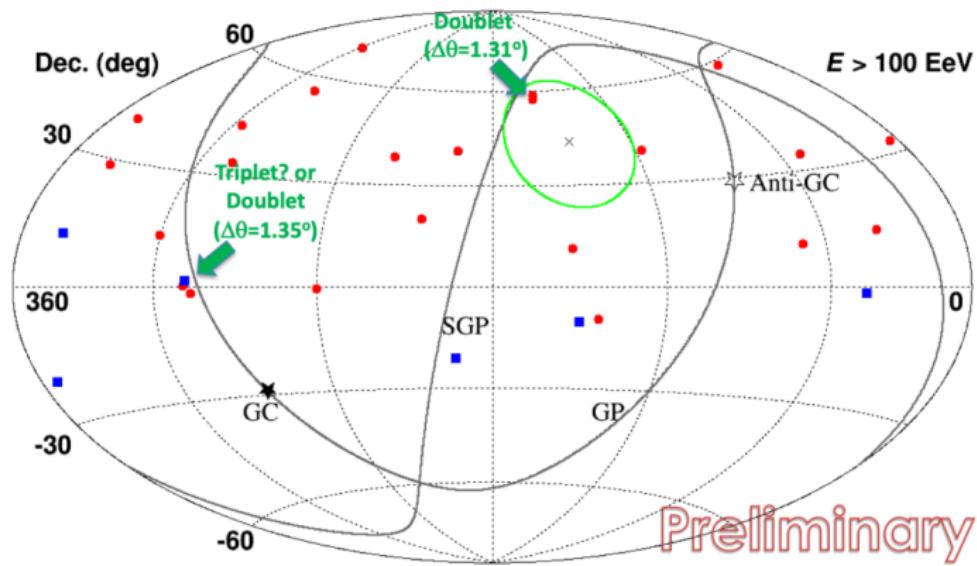


- North polar cap (incl. e.g. M82) outside the Auger field of view  
→ TA replication interesting  
... but not (yet) enough data for that.



# Small-scale anisotropy search above 100 EeV

Very preliminary!



- TA 9 years (23 events) ■ Auger 10 years (6 events) (nominal energies)  
 $p(\geq 2 \text{ doublets within } \sqrt{2}^\circ) = 0.3\% (2.8\sigma)$

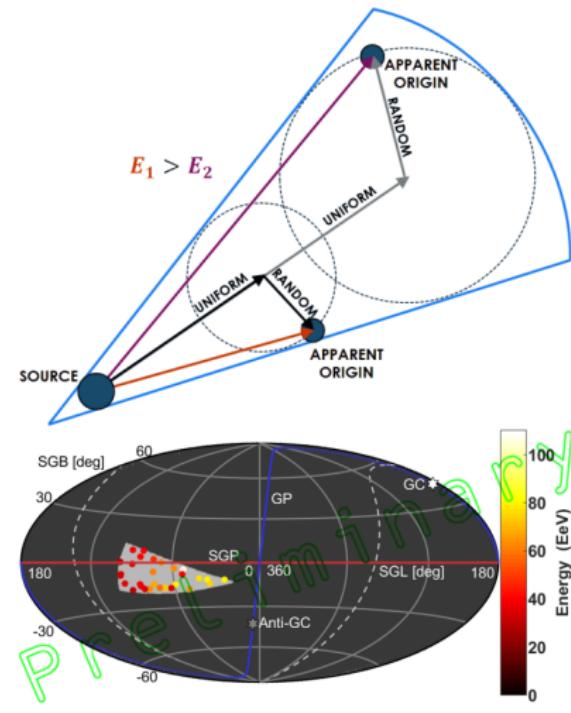
# Supergalactic structure of multiplets

1/2

Presented at the UHECR2018 conference (Paris, October 2018), proceedings in preparation

- UHECRs from a point source deflected by coherent and turbulent magnetic fields should form “wedges” in which the distance from the vertex anticorrelates with the energy.
- We can estimate the density of sources at a given point from the strength of the most significant anticorrelation among all possible energy thresholds and wedge widths, lengths and orientations.

$E \geq 30$  EeV, wedge width =  $30^\circ$ , length =  $80^\circ$ , orientation =  $270^\circ$  (supergal. coordinates) →

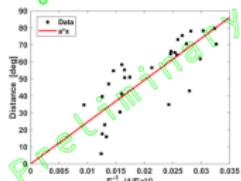
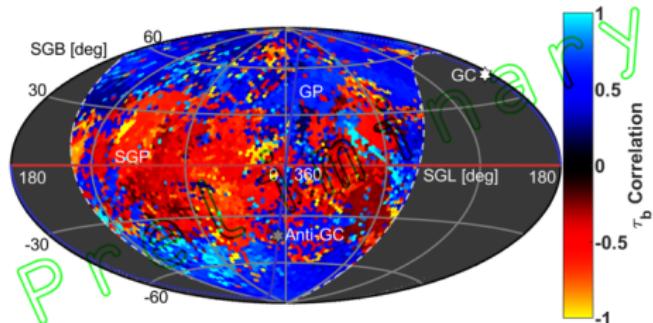
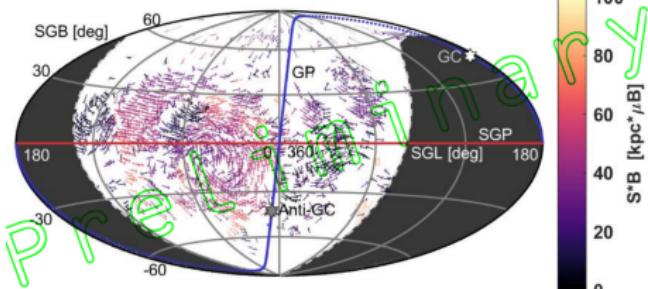


- We did this everywhere in our FoV ...

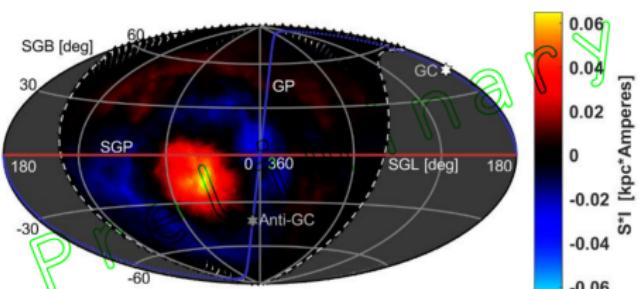
# Supergalactic structure of multiplets

2/2

- Anticorrelations stronger near supergalactic plane (significant at  $\gtrsim 4\sigma_{\text{post}}$ )
- Coh. field strength at each point estimated by fitting  $\Delta\theta \propto 1/E$  in ‘best’ wedge; field direction: wedge orientation rotated by 90°
- Current flowing towards us estimated as  $\propto \nabla \times \mathbf{B}$



$$B = 13 \text{ nG} \\ \text{if } Z = 1, D = 3.7 \text{ Mpc} \\ (\text{e.g. M82})$$

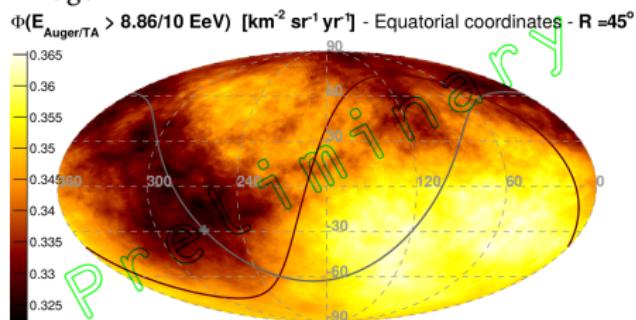


# Full-sky anisotropy searches with Auger + TA

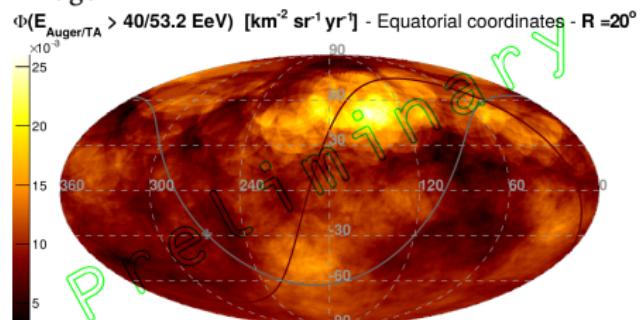
Presented at the UHECR2018 conference (Paris, October 2018), proceedings in preparation

Energy thresholds cross-calibrated via events in the intersection of FoVs

$$E_{\text{Auger}} > 8.86 \text{ EeV}, E_{\text{TA}} > 10 \text{ EeV}:$$



$$E_{\text{Auger}} > 40 \text{ EeV}, E_{\text{TA}} > 53.2 \text{ EeV}:$$



- Indications for a dipole moment (possibly also a quadrupole)
- Indications for warmspots along the supergalactic plane

Further analyses in preparation — stay tuned!

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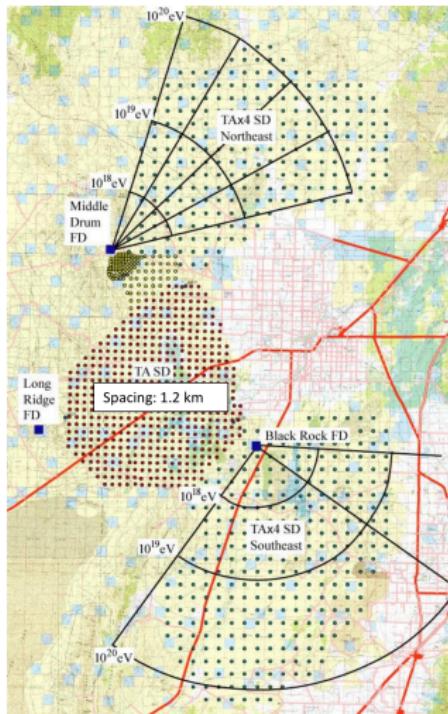
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# The ongoing Telescope Array extension: TA×4



- 500 new SDs with 2.08 km spacing (construction ongoing)
- 4 + 8 new FD telescopes (northern site already taking data; southern site under construction)
- 4 times the TA aperture at highest energies  
→ Anisotropy studies with 4× more statistics

Stay tuned!

# Back-up slides

- 4 SD observables used by boosted decision trees
  - For the composition study
  - For the search for photons
- 5 More about Auger–TA working group reports
  - Spectrum
  - Composition
  - Anisotropy
- 6 Details about the supergalactic multiplet study

# Outline

## 4 SD observables used by boosted decision trees

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- Anisotropy

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# SD observables used by BDTs for the composition study

- ① Linsley front curv. param.,  $a$
- ② Area-over-peak (AoP) of signal at  $r_0 = 1\,200$  m,  $\alpha$
- ③ AoP slope parameter,  $\beta$   
( $\text{AoP}(r) = \alpha - \beta(r/r_0 - 1)$ )
- ④ Number of detectors hit
- ⑤ Number of detectors excluded from shower front fit
- ⑥  $\chi^2/n$  of joint geometry–LDF fit
- ⑦  $S_b$  parameter for  $b = 3$   
$$(S_b = \sum_{i=1}^N S_i (r_i/r_0)^b, \quad S_i = \text{signal in } i\text{-th detector})$$
- ⑧  $S_b$  parameter for  $b = 4.5$
- ⑨ Sum of all signals ( $S_{b=0}$ )
- ⑩ Asymm. of signal at upper and lower layers of detectors
- ⑪ Total number of peaks within all FADC traces
- ⑫ Number of peaks in detector with largest signal
- ⑬ No. of peaks only in upp. layer
- ⑭ No. of peaks only in lower layer

# SD observables used by BDTs for the photon search

- ① Zenith angle,  $\theta$
- ② Signal at 800 m from core
- ③ Linsley front curv. param.,  $a$
- ④ Area-over-peak (AoP) of signal at  $r_0 = 1\,200$  m,  $\alpha$
- ⑤ AoP slope parameter,  $\beta$   
( $\text{AoP}(r) = \alpha - \beta(r/r_0 - 1)$ )
- ⑥ Number of detectors hit
- ⑦ Number of detectors excluded from shower front fit
- ⑧  $\chi^2/n$  of joint geometry–LDF fit
- ⑨  $S_b$  parameter for  $b = 3$   
( $S_b = \sum_{i=1}^N S_i(r_i/r_0)^b$ ,  
 $S_i$  = signal in  $i$ -th detector)
- ⑩  $S_b$  parameter for  $b = 4.5$
- ⑪ Sum of all signals ( $S_{b=0}$ )
- ⑫ Asymm. of signal at upper and lower layers of detectors
- ⑬ Total number of peaks within all FADC traces
- ⑭ Number of peaks in detector with largest signal
- ⑮ No. of peaks only in upp. layer
- ⑯ No. of peaks only in lower layer

# Outline

## 4 SD observables used by boosted decision trees

- For the composition study
- For the search for photons

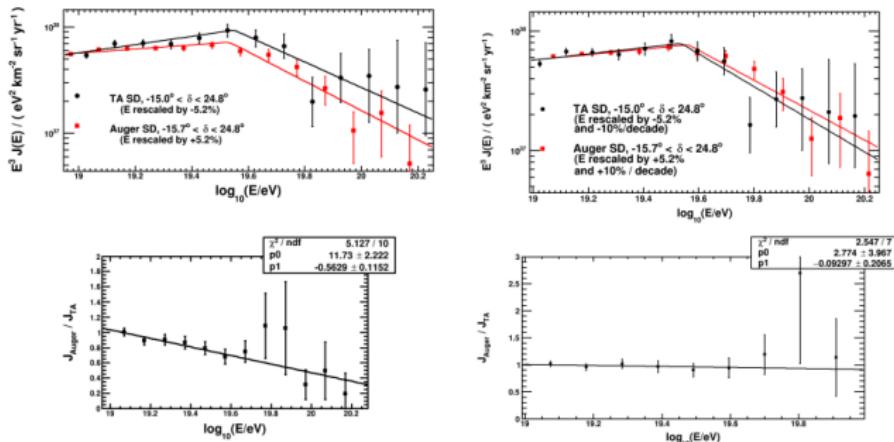
## 5 More about Auger-TA working group reports

- Spectrum
- Composition
- Anisotropy

## 6 Details about the supergalactic multiplet study

# From the last Auger-TA spectrum WG report

## TA-Auger Difference



- Agreement in the common declination band after a correction of Auger energies by +10% per decade, and TA by -10% per decade, starting at  $10^{19}$  eV
- TA energy-dependent bias:  $-0.3 \pm 9\%$  per decade of energy, and SD reconstruction checked using Monte Carlo and constant intensity cut methods.
- Auger energy-dependent bias: within 3% per decade of energy and SD reconstruction checked using two different constant intensity cut methods.

# From the last Auger-TA composition WG report

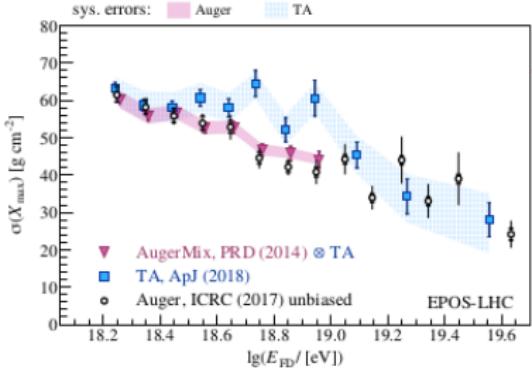
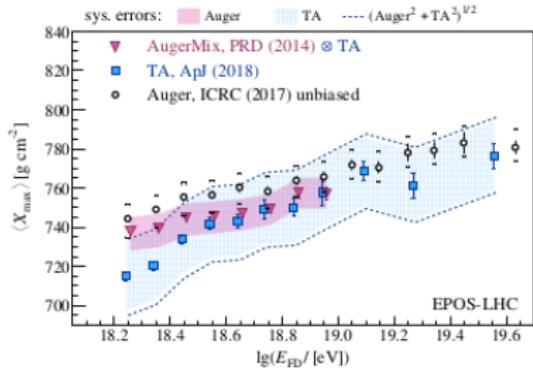
## Summary

$\langle X_{\max}^{\text{TA}} \rangle < \langle X_{\max}^{\text{Auger}} \rangle$  for almost all energies

agreement within (stat + sys) errors

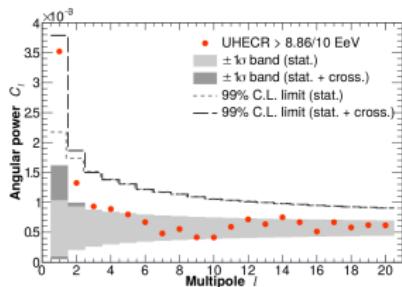
$\sigma(X_{\max}^{\text{TA}}) > \sigma(X_{\max}^{\text{Auger}})$  for  $\lg(E/\text{eV}) = 18.6 - 19.0$

Next: comparison to Auger ICRC (2017) data and energies  $\lg(E/\text{eV}) > 19.0$



# From the last Auger-TA anisotropy WG report

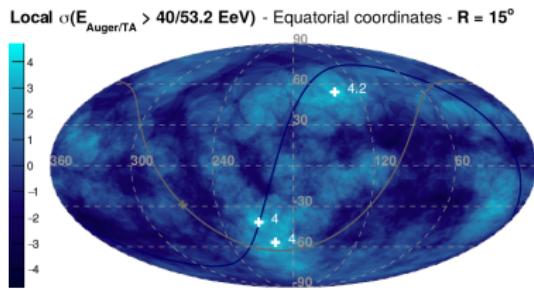
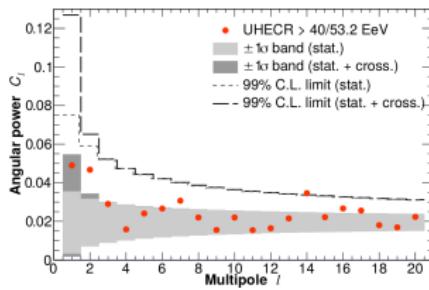
## Low-energy angular power spectrum and dipole components



Dipole along ( $d_z$ ) and perpendicular to ( $d_{\perp}$ ) Earth's axis:

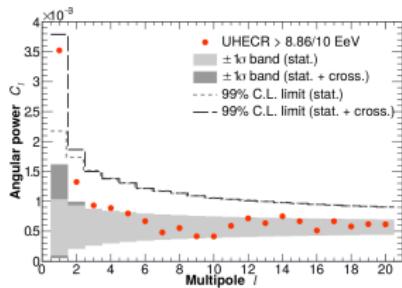
	$d_z$ [%]	$d_{\perp}$ [%]
Auger only, $\ell \leq 1$ [1]	$-2.6 \pm 1.5$	$6.0 \pm 1.0$
Auger only, $\ell \leq 2$ [2]	$-2 \pm 4$	$5.0 \pm 1.3$
Auger + TA (this work)	$-2.6 \pm 1.3_{\text{stat}} \pm 1.4_{\text{cross}}$	$4.3 \pm 1.1_{\text{stat}} \pm 0.04_{\text{cross}}$

## High-energy angular power spectrum and blind search for excesses



# From the last Auger-TA anisotropy WG report

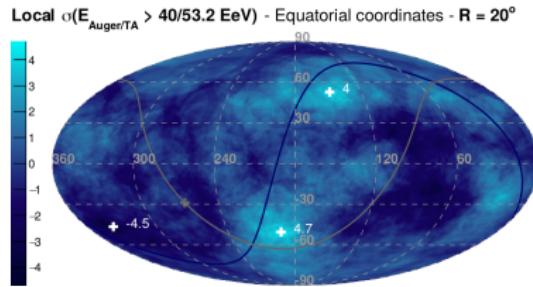
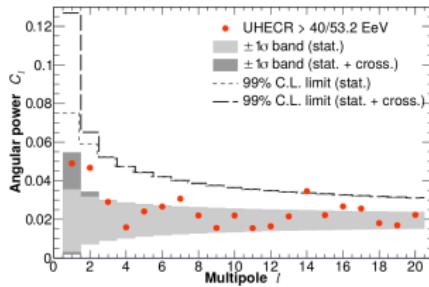
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## High-energy angular power spectrum and blind search for excesses



# Outline

## 4 SD observables used by boosted decision trees

- For the composition study
- For the search for photons

## 5 More about Auger–TA working group reports

- Spectrum
- Composition
- Anisotropy

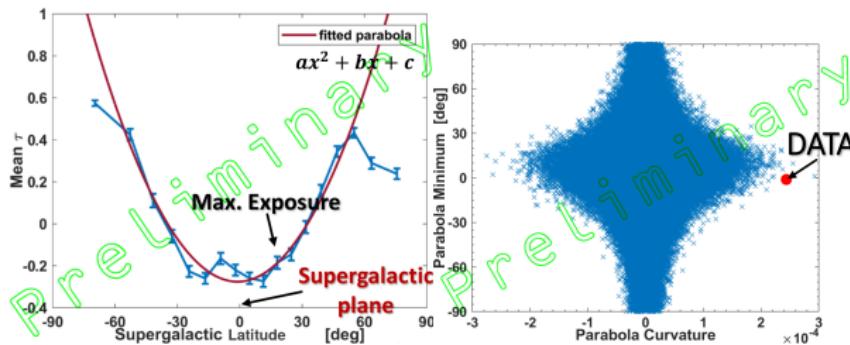
## 6 Details about the supergalactic multiplet study

# Details about the supergalactic multiplet study

*p*-values computed by permutation

Parameter scan ranges:

- thresh.  $E/\text{EeV}$ : 10, 15, ..., 100
- wedge vertex: on a  $2^\circ \times 2^\circ$  grid
- " width:  $10^\circ, 20^\circ, \dots, 90^\circ$
- " length:  $15^\circ, 20^\circ, \dots, 90^\circ$
- " pointing:  $0^\circ, 5^\circ, \dots, 355^\circ$



Kendall's correlation coefficient:

$\tau = \text{avg}_{i < j} \text{sign}((E_i - E_j)(\theta_i - \theta_j))$ ,  
only depends on rankings  
( $\tau = 1$  for any monotonic function)

Most signif.  $\tau$  value for each vertex  
binned in supergalactic latitude  
and fitted to  $ax^2 + bx + c$ ;  
 $a$  value compared to MC distribution

estim. current

