

Using merged BHs final  
spins and final masses to  
infer the formation history of  
their progenitors



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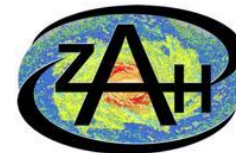
*Division of Astronomy, NSF*



**GEMMA 2018 Workshop**

*Università del Salento, Lecce*

*June 5th, 2018*



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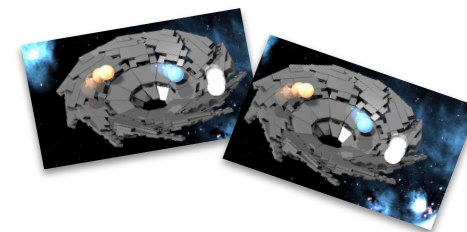


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## Outline

- The discovery of gravitational waves emitted by black hole binary mergers



- Black hole binaries formation channels

Isolated

Dynamical



- A link between the remnant black hole and its progenitors: masses and spins

- Isolated black hole binary mergers
- Dynamical black hole binary mergers

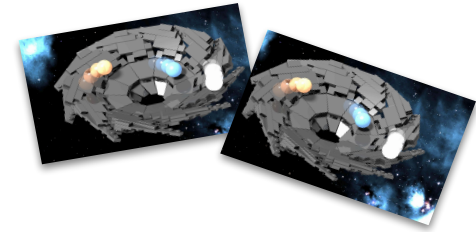


- Constraining the formation channel of the observed population of merged black hole binaries

- Conclusions



# The discovery of gravitational waves emitted by black hole binary mergers



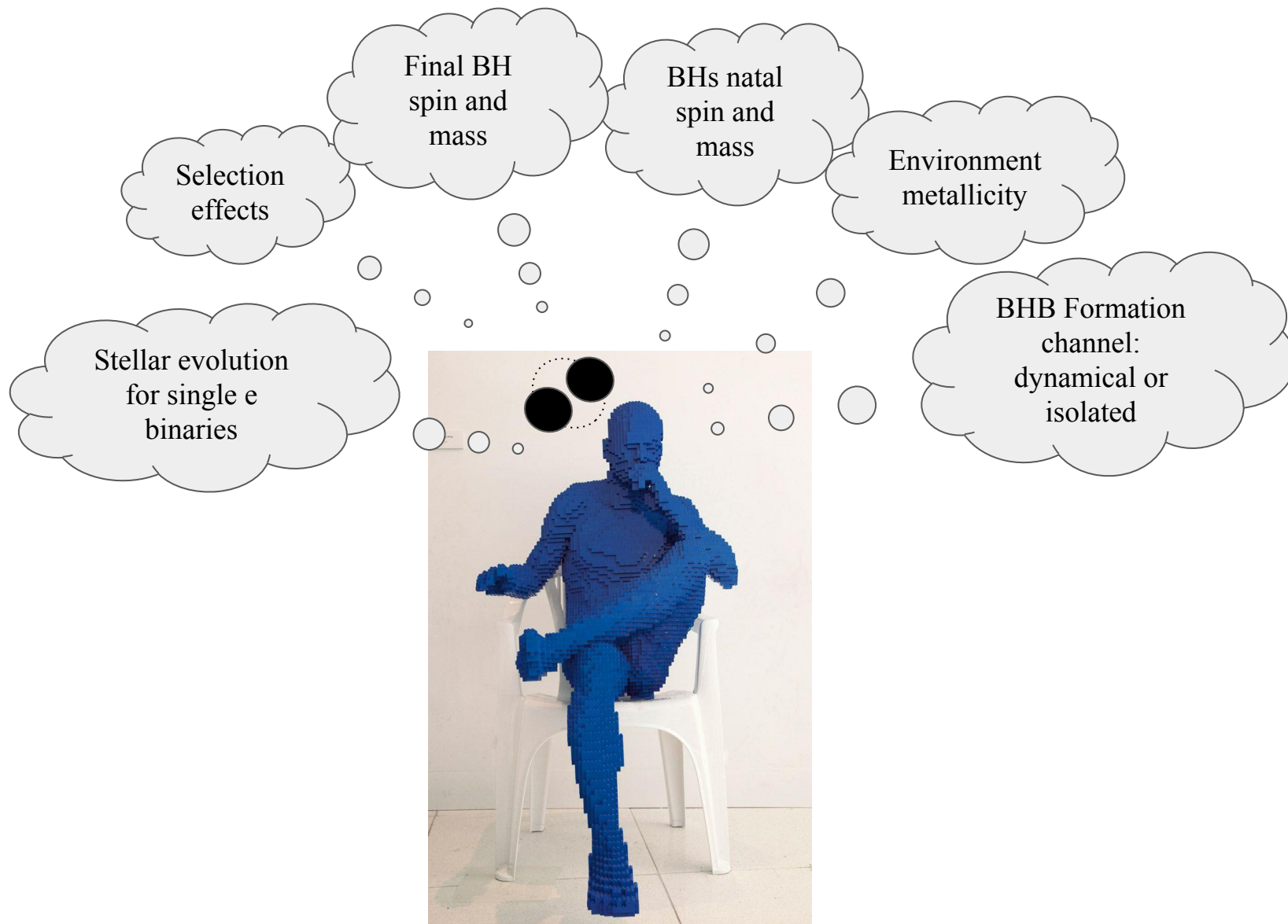
*On 23rd May 2018, if you search on ADS  
“2016-2018” + “LIGO” + “Gravitational waves” + “Abbott” (evidently the luckiest physicist ever):  
72 papers with 6462 citations*

## What did we learn?

1. **Black holes do exist**
2. **Black hole binaries do exist**
3. **Black holes heavier than 30 solar masses do exist**
4. **Black hole binaries heavier than 30 solar masses do exist**

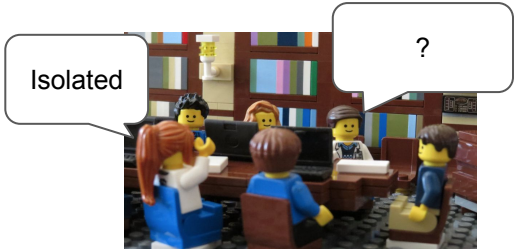



## Where are they from?



# Black hole binaries formation channels:

## General information

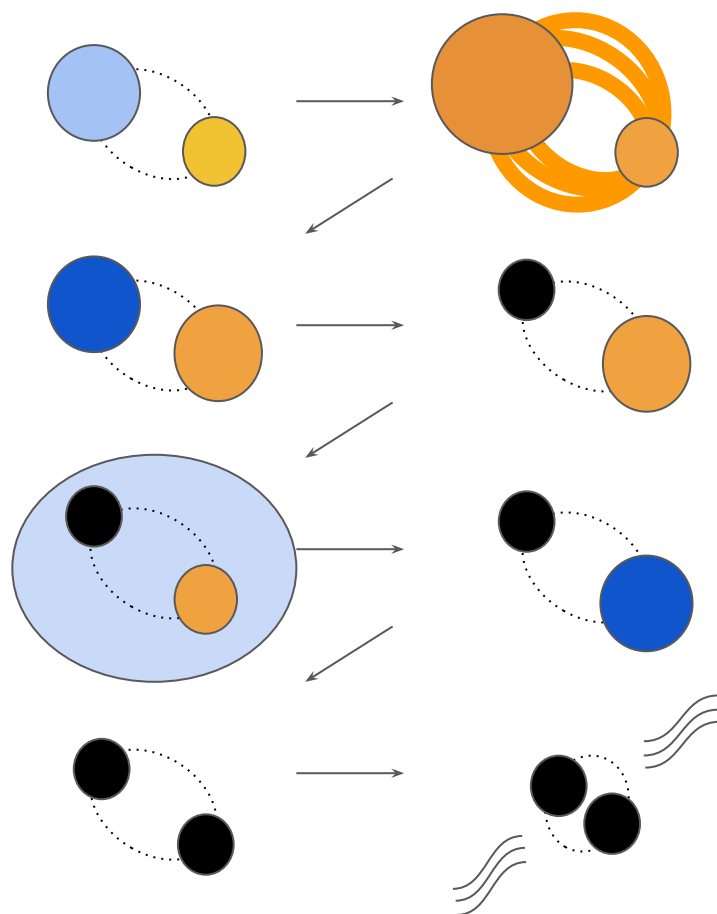
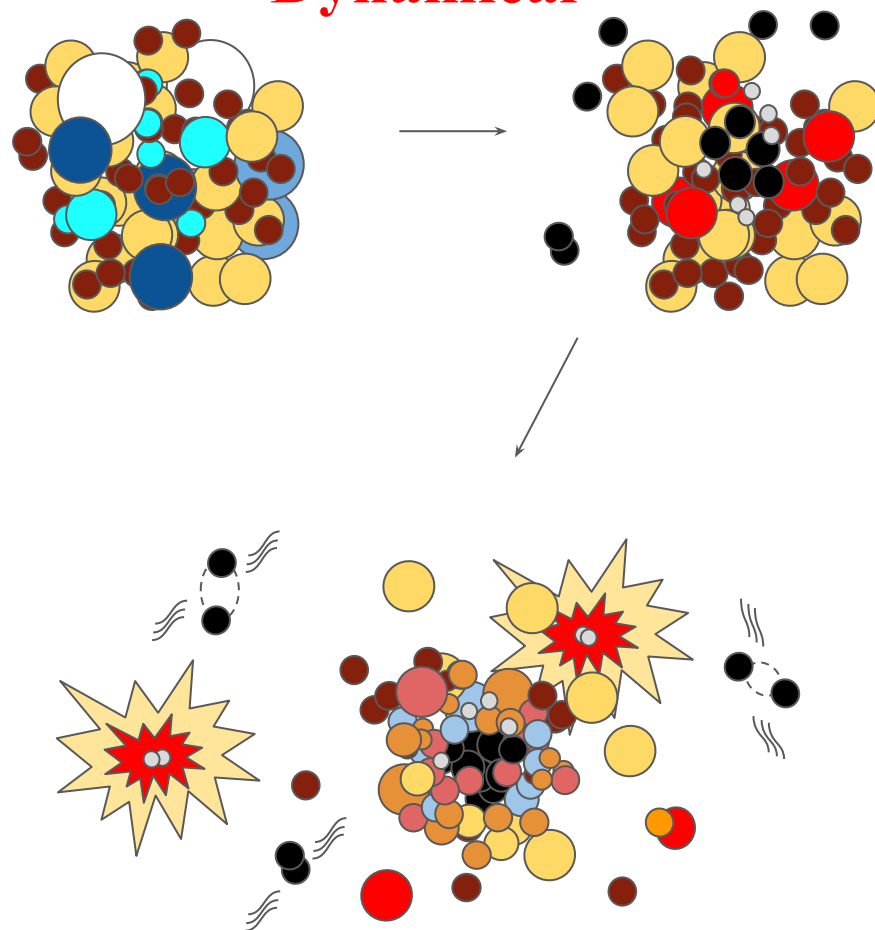


<b>Basic assumption:</b> Kroupa (2001) stellar mass function		<b>Total number of BHs:</b>		
$f(M_*) = \begin{cases} M^{-0.3} & M_* < 0.08 \text{ M}_\odot \\ M^{-1.3} & M_* \in [0.08 - 0.5] \text{ M}_\odot \\ M^{-2.3} & M_* > 0.5 \text{ M}_\odot \end{cases} \longrightarrow N_{\text{BH}} = 10^{-3} N_* \simeq \begin{cases} 10^7 & \text{Elliptical galaxies} \\ 10^4 & \text{Nuclear clusters} \\ 10^3 & \text{Globular clusters} \end{cases}$				
<b>Our sample:</b> $N_{\text{BBH}} = 7000$				
<b>Metallicity</b> (affect the BH natal mass and spin): $Z = \begin{cases} 2 \times 10^{-4} \\ 2 \times 10^{-3} \\ 2 \times 10^{-2} \end{cases} \left. \vphantom{\begin{cases} 2 \times 10^{-4} \\ 2 \times 10^{-3} \\ 2 \times 10^{-2} \end{cases}} \right\} \begin{matrix} \text{Globular clusters} \\ \\ \text{Solar neighbourhoods} \end{matrix}$		<b>Stellar evolution recipes</b> (affect the BH natal mass and spin):		
	<b>Sensitivity volume</b> (Fishbach & Holz 17) $V \propto (m_1 + m_2)^{2.2}$	<b>SSE (Hurley+00)</b> Single stellar evolution	<b>SEVN (Spera+15)</b> Single stellar evolution	<b>BSE (Hurley+02)</b> Binary stellar evolution
		Extracted from the Nbody6 code	Adapted from SEVN through fitting formulae	Extracted from the Nbody6 code
		<b><u>Name: SSE18</u></b>	<b><u>Name: SEVN18</u></b>	<b><u>Name: BSE18</u></b>

## Black hole binaries formation channels:

Isolated

Dynamical

**Isolated****Dynamical**



# Black hole binaries formation channels:

## Isolated: general information



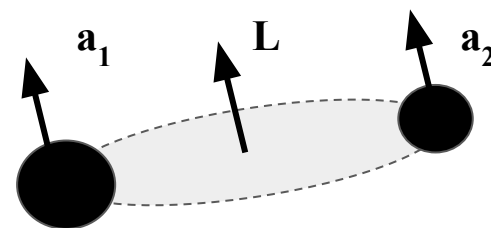
**Code used:**

**SSE18**

(Adpt. from Nbody6)

**SSEVN18**

(Adpt. from Spera+15)



**Aligned configuration**

- maximize the BBH effective spin
- maximize the BH final spin

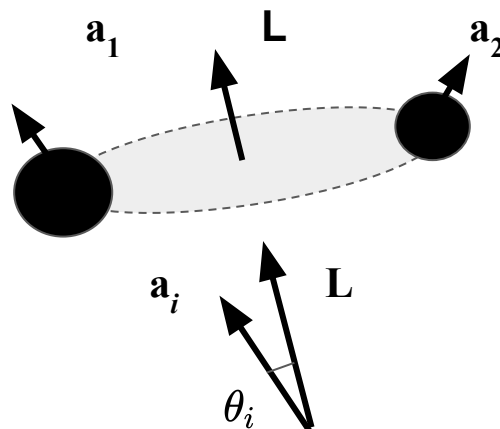
## Orbital properties

$$P(M_1) \propto M_1^{-2.3}$$

$$P(M_2) \propto M_2^0$$

**Basic assumption:**

a fraction of the BBH  
sample merge  
(no matter what orbital  
properties the BBH have)



**Mildly aligned configuration**

- required to get BH final spins below 0.7

$$P(\cos\theta_i) = (\cos\theta_i + 1)^{n_\theta}$$

$$\theta_i \rightarrow \infty \text{ aligned}$$

$$\theta_i \equiv 2 \text{ thermal}$$

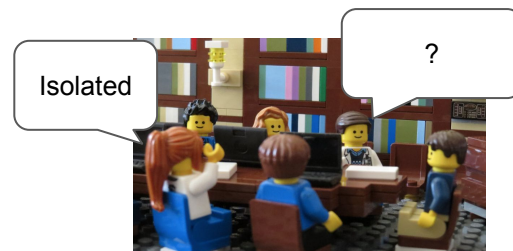
$$\theta_i \equiv 0 \text{ flat}$$

## Fun facts: a zoology of stellar binary evolution tools

**BSE/SSE** (Hurley+2002) , **StarTrack** (Belczynski+2002,2008...), **MOBSE** (Giacobbo+2016), **MOCCABSE** (Belloni+), **MESA** (Pavloski+16), **MC pop** (Mandel & de Mink 16)

# Black hole binaries formation channels:

## Isolated: method 2



**Code used:**

**BSE18**

(adapted from Nbody6)



## Orbital properties

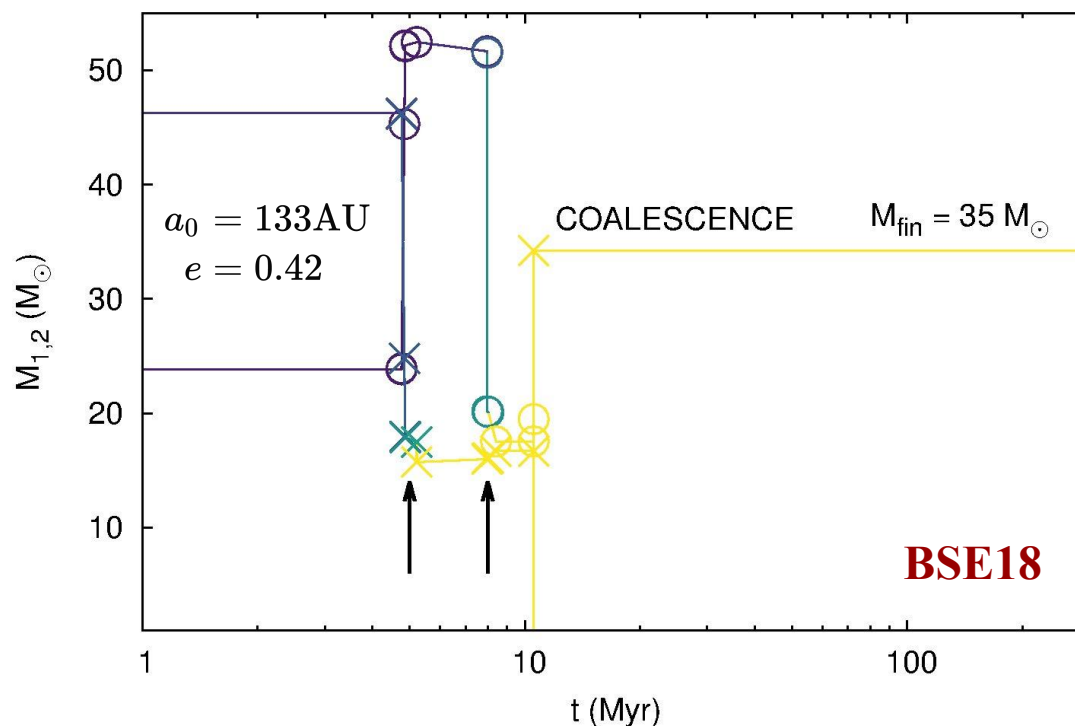
Sana et al. 2012

$$P(T_{\text{orb}}) \propto T_{\text{orb}}^{1/2}$$

$$P(e) \propto e^{-0.42}$$

$$P(M_1) \propto M_1^{-2.3}$$

$$P(M_2) \propto M_2^0$$



## Fun facts: a zoology of stellar binary evolution tools

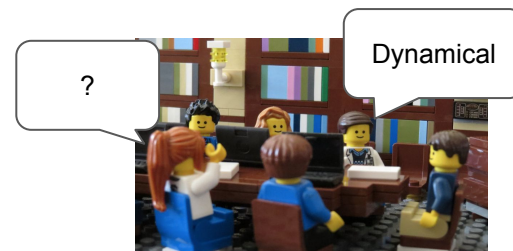
**BSE/SSE** (Hurley+2002) , **StarTrack** (Belczynski+2002,2008...), **MOBSE** (Giacobbo+2016), **MOCCABSE** (Belloni+), **MESA** (Pavloski+16), **MC pop** (Mandel & de Mink 16)



# Black hole binaries formation channels:

## Dynamical

BHB forms mainly through triple interactions



The BHB merges in the cluster due to

- Secular effects (like KL resonance)

**- Non-hierarchical interactions**

The BHB is ejected from the cluster

- Merger due solely to GW emission

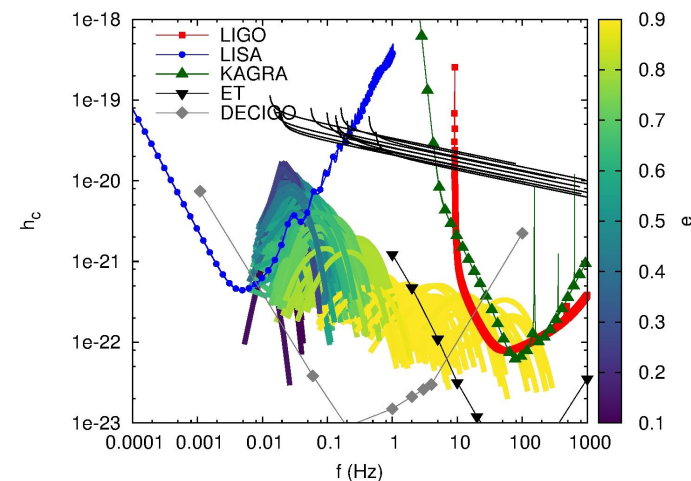
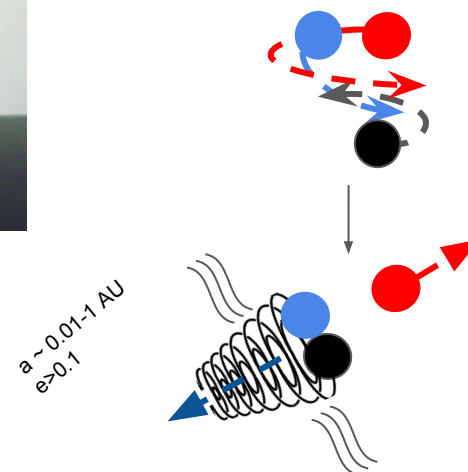
**- Ejection caused by 3B interactions**

The BHB breaks up

- New BHB formation possible

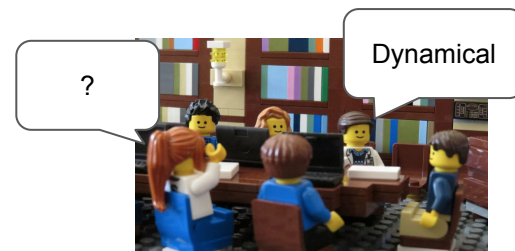
- Possible ejection of one or more BHs

Arca Sedda, Li and Kocsis, 2018, Arxiv: 1805.06458



# Black hole binaries formation channels:

## Dynamical



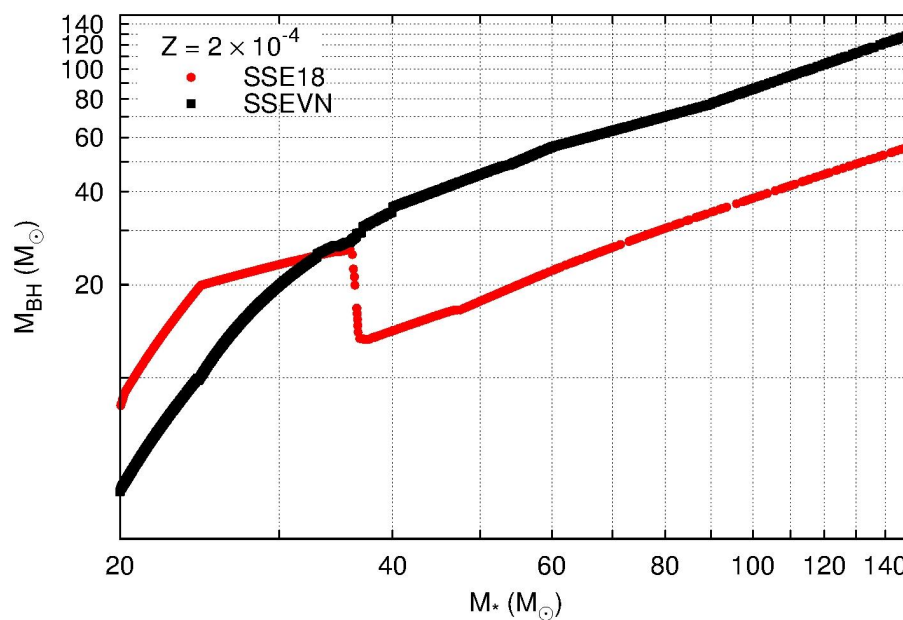
### Code used:

#### SSE18

(adapted from Nbody6)

#### SSEVN18

(adapted from Spera+15)



### Orbital properties

- Merging BBHs in star clusters have high mass-ratios (Rodriguez+15)
- A fraction of merged BHs undergo a second merger (Rodriguez+18)

### Fun facts: simulating a real star system? Take your time

Only 4 one-to-one direct N-body models of a Globular Cluster exists, but old stellar evolution recipes.  
Ran on GPU-enabled machine, required **~ 4 months each**, which means **~50 yrs on a normal laptop**

A link between the remnant black hole and its progenitors:  
masses and spins



### Chapter 1: Remnant masses and spins

$$M_{\text{rem}} = 1 - (b_0 + b_1/(b_2 + \chi)) (M_1 + M_2)$$

$$a_{\text{rem}} = (1 + q)^{-2} [a_1^2 + a_2^2 q^4 + 2a_1 a_2 q^2 \cos \alpha + \\ + 2(a_1 \cos \beta + a_2 q^2 \cos \gamma) l q + l^2 q^2]^{1/2},$$

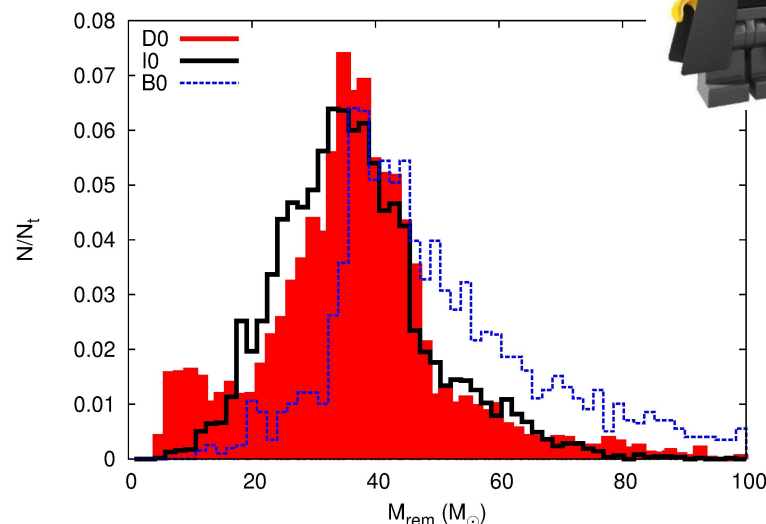
$$l = 2\sqrt{3} + t_2 \nu + t_3 \nu^2 + \\ s_4 (1 + q^2)^{-2} (a_1^2 + a_2^2 q^2 + 2a_1 a_2 q^2 \cos \alpha) + \\ (s_5 \nu + t_0 + 2)(1 + q^2)^{-1} (a_1 \cos \beta + a_2 q^2 \cos \gamma).$$



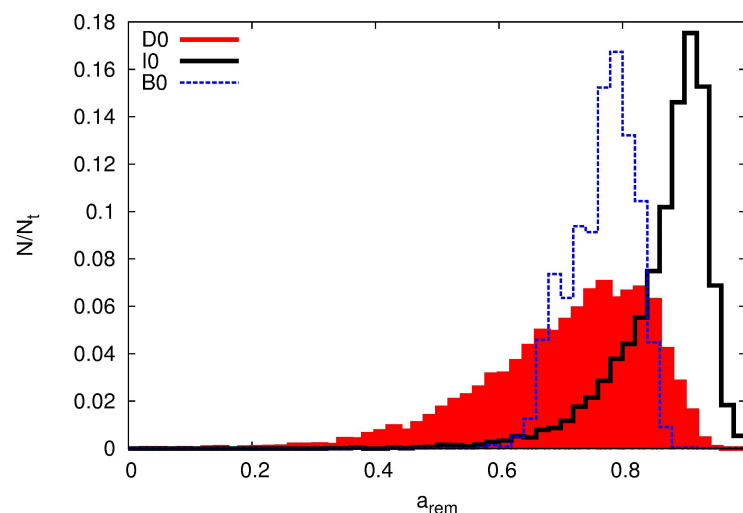
## Constraining the formation channel of the observed population of merged black hole binaries



- **Dynamical binaries (D0):** evidence for low-mass BHs, narrow peak at  $\sim 35$ -40  $M_{\text{sun}}$
- **Isolated binaries (I0, method 1):** broad mass distribution, cut-off at BH masses below 20  $M_{\text{sun}}$
- **Isolated binaries (B0, method 2):** cut-off at BH masses 30  $M_{\text{sun}}$ , long high-end tail.



- **Dynamical binaries:** broad distribution, cut-off above 0.82, shallow rise in the range 0-0.8
- **Isolated binaries (aligned, method 1):** narrow peak at 0.9, tiny fraction of BHs with spin below 0.6
- **Isolated binaries (aligned, method 2):** broad distribution limited in between 0.6 and 0.85



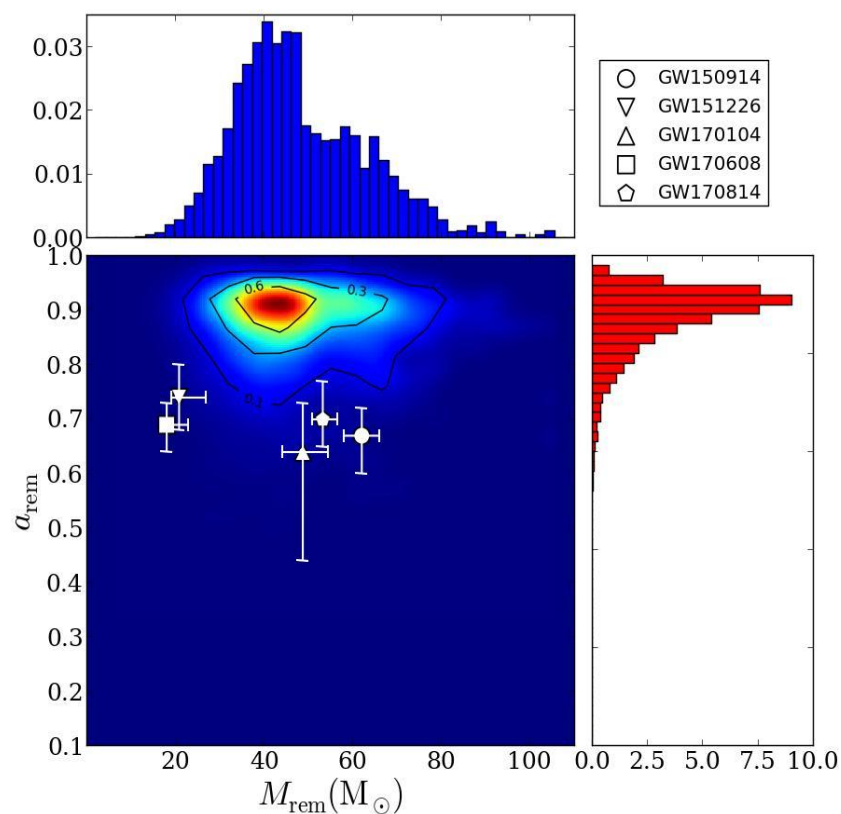
## Constraining the formation channel of the observed population of merged black hole binaries

### Isolated: method 1 (approximated)

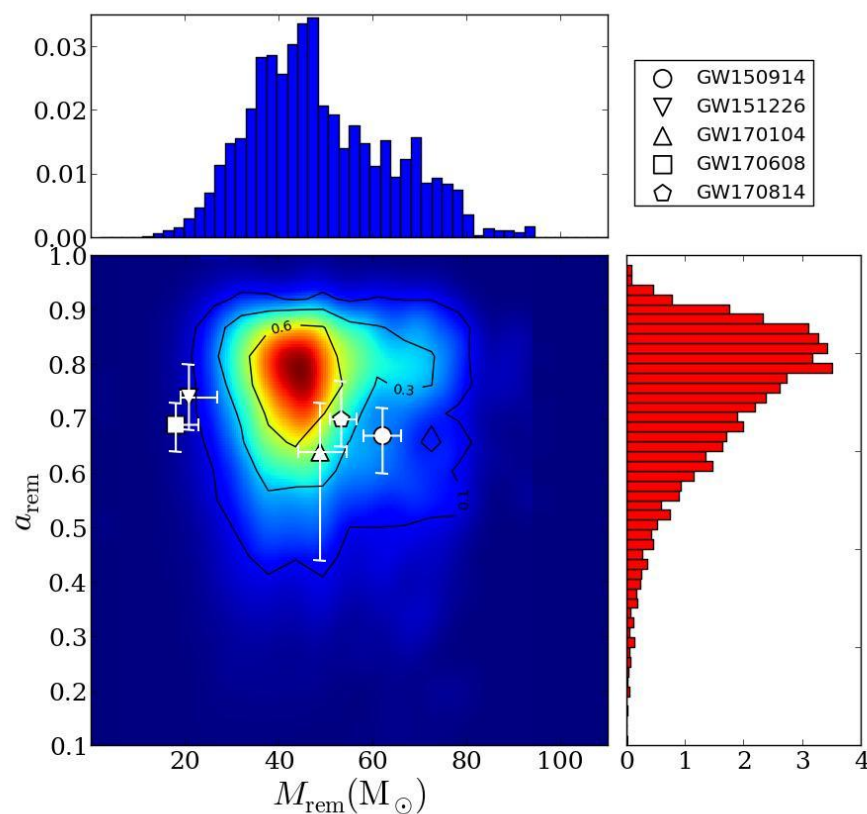
$$Z = 2 \times 10^{-4} = 0.01 Z_{\odot}$$



#### Fully aligned



#### Misaligned spins



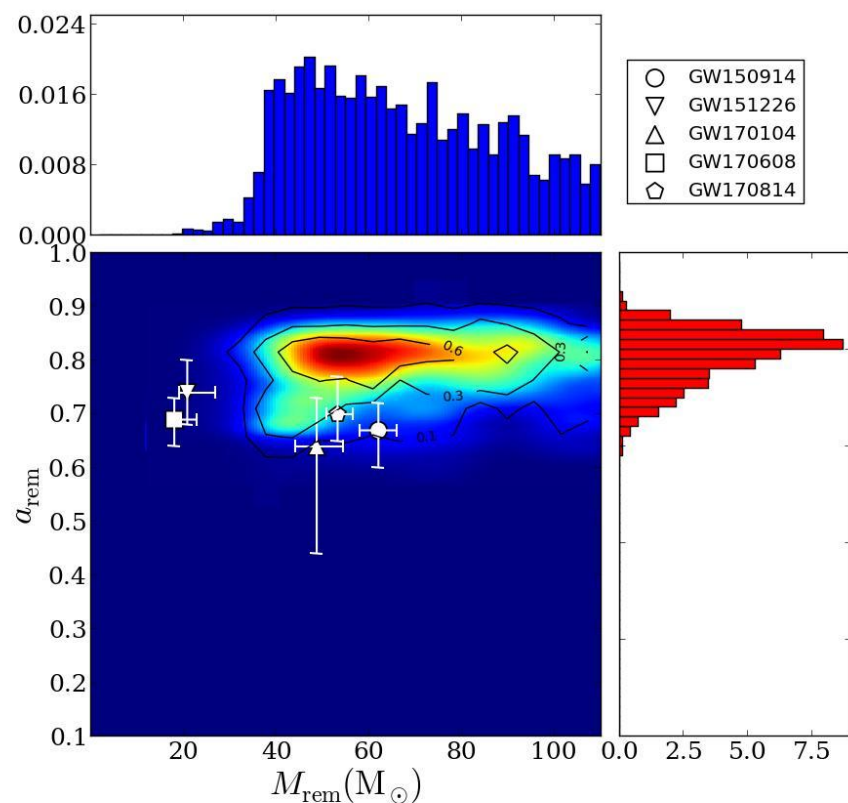
## Constraining the formation channel of the observed population of merged black hole binaries



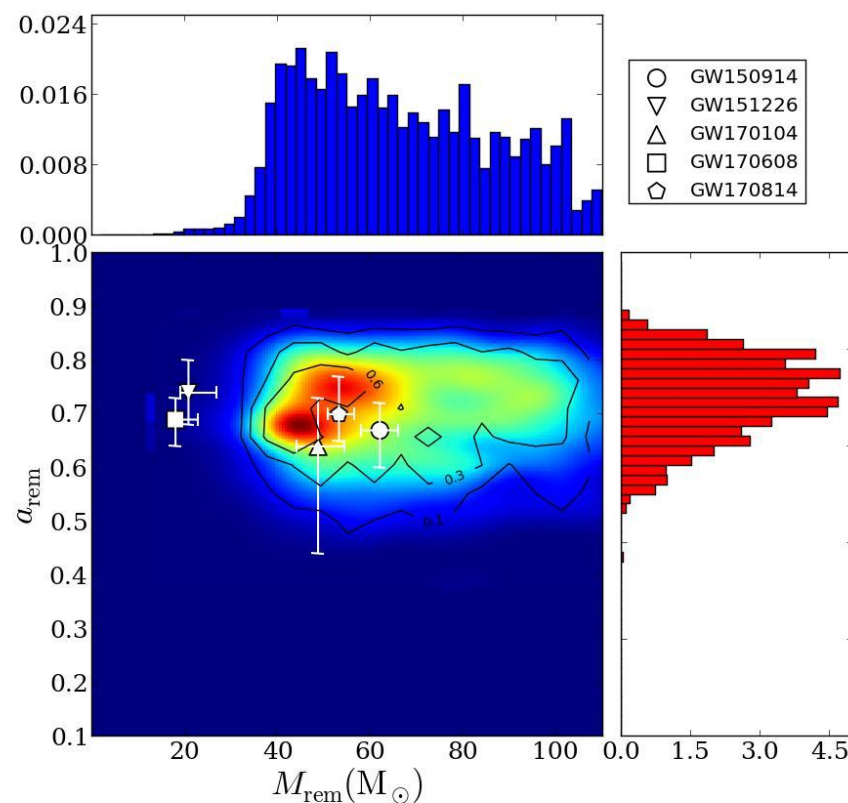
### Isolated: method 2 (self consistent)

$$Z = 2 \times 10^{-4} = 0.01 Z_{\odot}$$

#### Fully aligned



#### Misaligned spins





# Constraining the formation channel of the observed population of merged black hole binaries

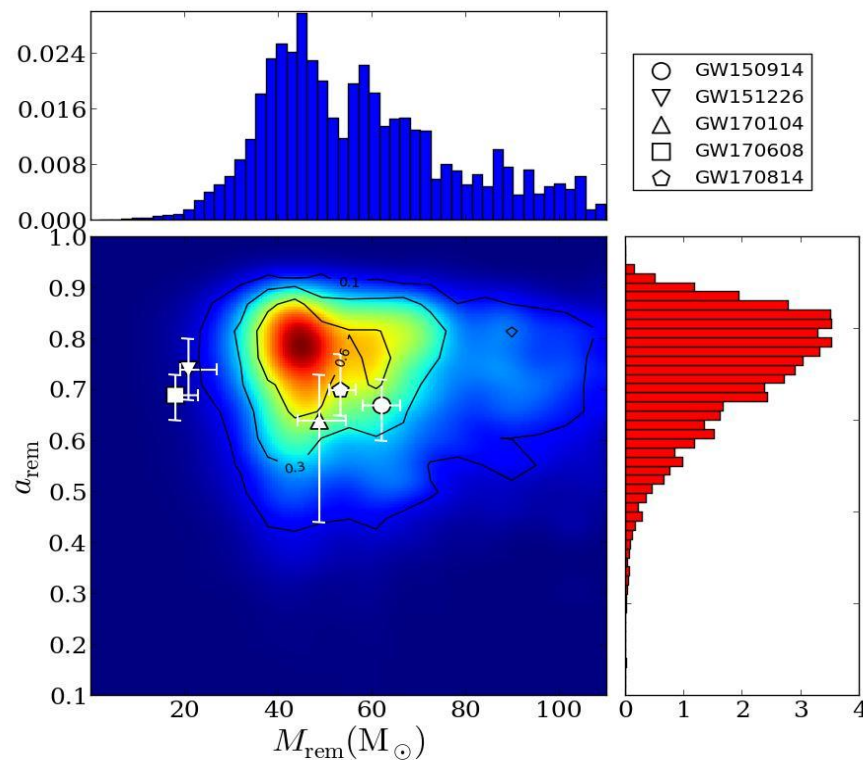
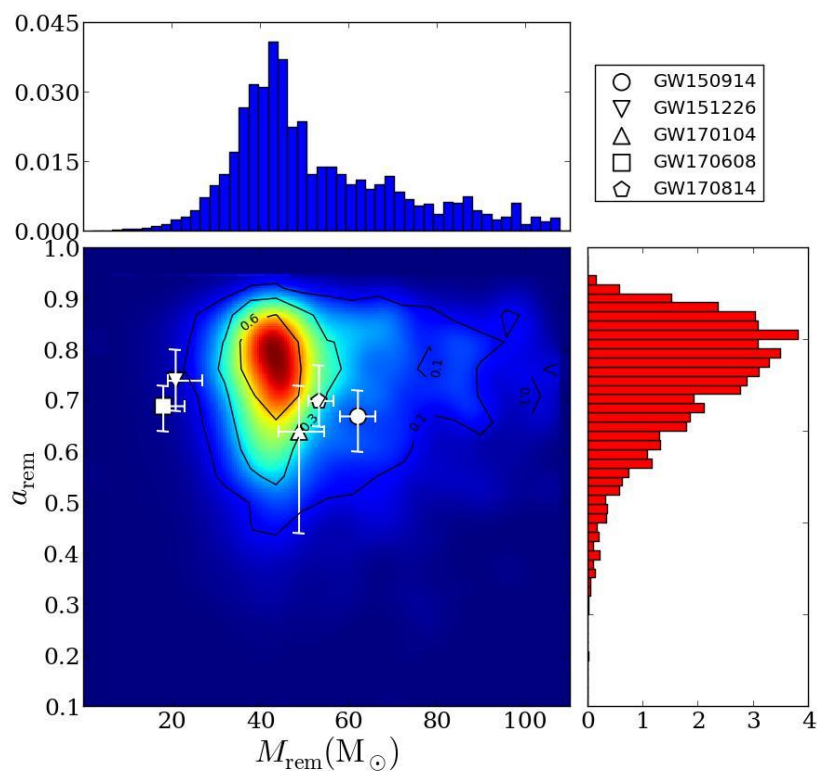


## Dynamical

$$Z = 2 \times 10^{-4} = 0.01 Z_{\odot}$$

$$q_{\min} = 0.5 \quad f_{\text{recy}} = 0.0$$

$$q_{\min} = 0.0 \quad f_{\text{recy}} = 0.1$$



Constraining the formation channel of the  
observed population of merged black hole binaries



**Much more possibilities**

**Metallicity:**

$$Z = (0.1 - 1)Z_{\odot}$$

**Disalignment level:**

$$P(\cos \theta_i) = (\cos \theta_i + 1)^{n_{\theta}}; \quad n_{\theta} = 2$$

**BHs natal spin:**

$$a_{\text{BH}} \neq a_{\text{BH}}(M_{\text{BH}}); \quad a_{\text{BH}} = a_{\text{BH}}(M_{\text{CO}})$$

**V – M<sub>BBH</sub> Relation :**

$$V \propto M_{\text{BBH}}^k; \quad k = 1.0, 1.5, 2.5$$

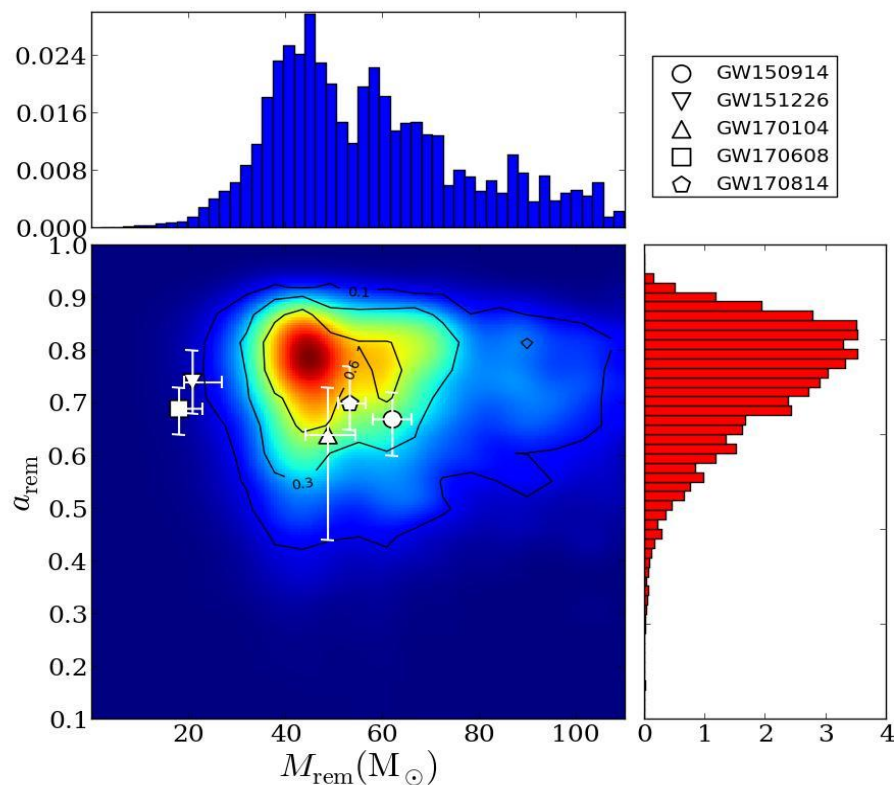
Constraining the formation channel of the  
observed population of merged black hole binaries

GW150914 - GW170104 - GW170814

$$Z = 2 \times 10^{-4} = 0.01 Z_{\odot}$$

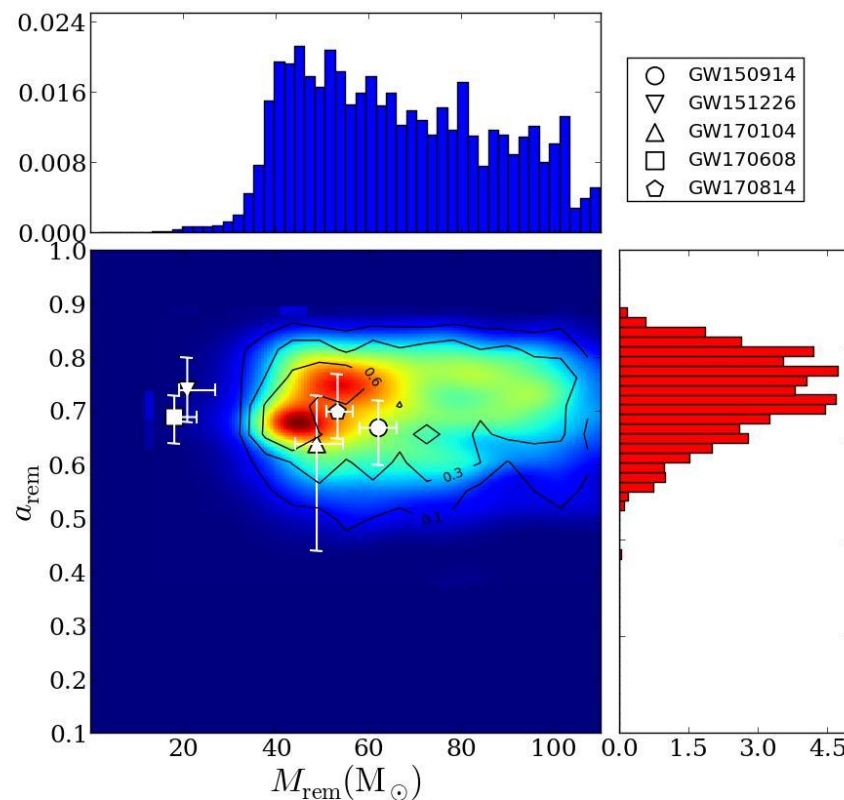


$$q_{\min} = 0.0 \quad f_{\text{recy}} = 0.1$$



Dense globular clusters  
Nuclear star clusters

Misaligned spins



Old elliptical galaxy

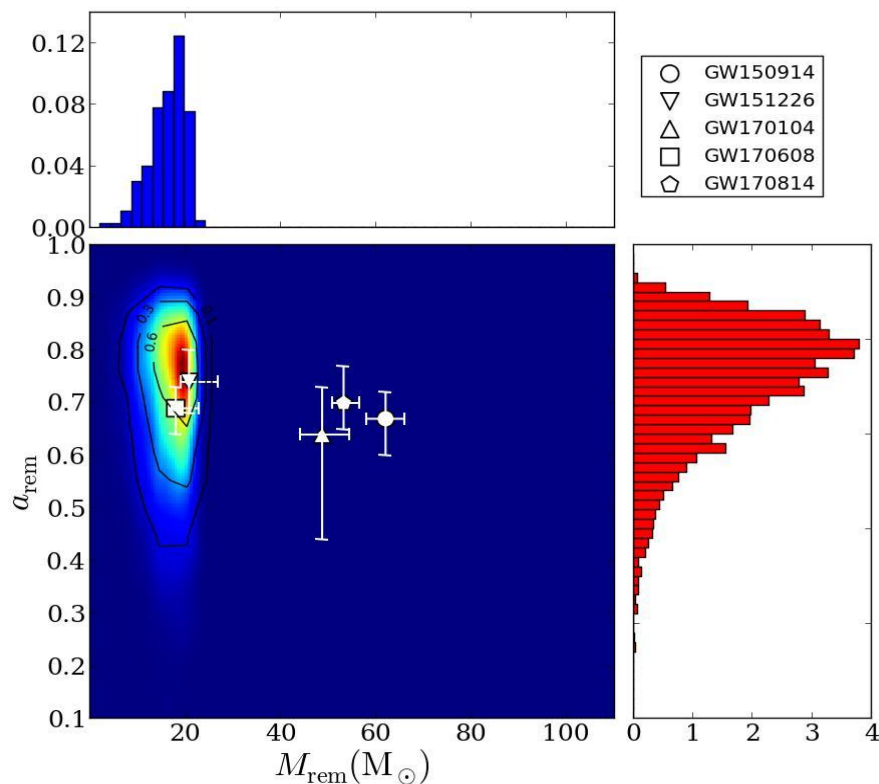
Constraining the formation channel of the  
observed population of merged black hole binaries

# GW151226 - GW170608

$$Z = 2 \times 10^{-2} = 1Z_{\odot}$$

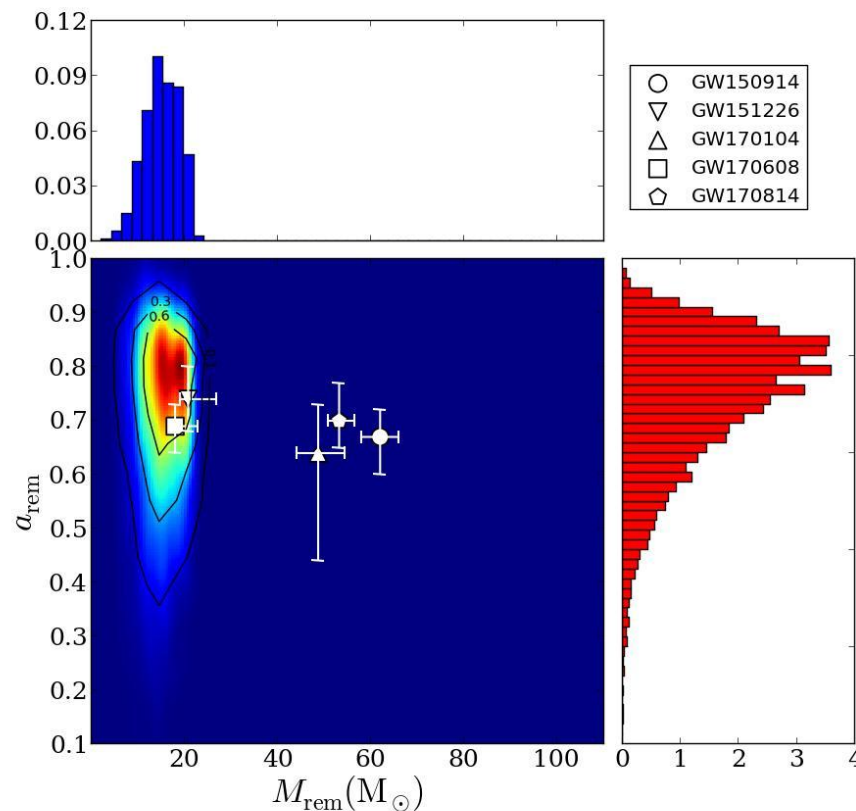


$$q_{\min} = 0.5 \quad f_{\text{recy}} = 0.0$$



Open clusters

## Misaligned spins



Metal rich galaxy

## Conclusions

### Arca Sedda and Benacquista, MNRAS res., on ArXiv tomorrow



- I. Final mass and spin of remnant BHs can be used to infer the formation history of their progenitor BBHs
- II. Many parameters can affect the calculations

**A. Stellar evolution for single stars → BH natal spin and mass**

**B. Stellar evolution for binaries**

**C. Global properties of dynamically formed BBHs**

**D. Remnant mass and spin**

Stellar evolution  
modelists

Star clusters modelists

GR modelists

- III. Under reliable assumptions

GW150914 **Dense Nuclear Cluster (Galaxy nucleus)**

Old elliptical Galaxy

GW151226 **Open Cluster (young, metal rich)**

Metal rich galaxy (spiral?starburst?)

GW170114 **Globular Cluster (old, metal poor)**

Elliptical Galaxy

GW170608 **Young massive cluster**

Starburst environment

GW170814 **Dense Nuclear Cluster (Galaxy nucleus)**

Old elliptical Galaxy