



# CHARMONIUM(-LIKE) STATES AT BELLE

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on behalf of the Belle collaboration

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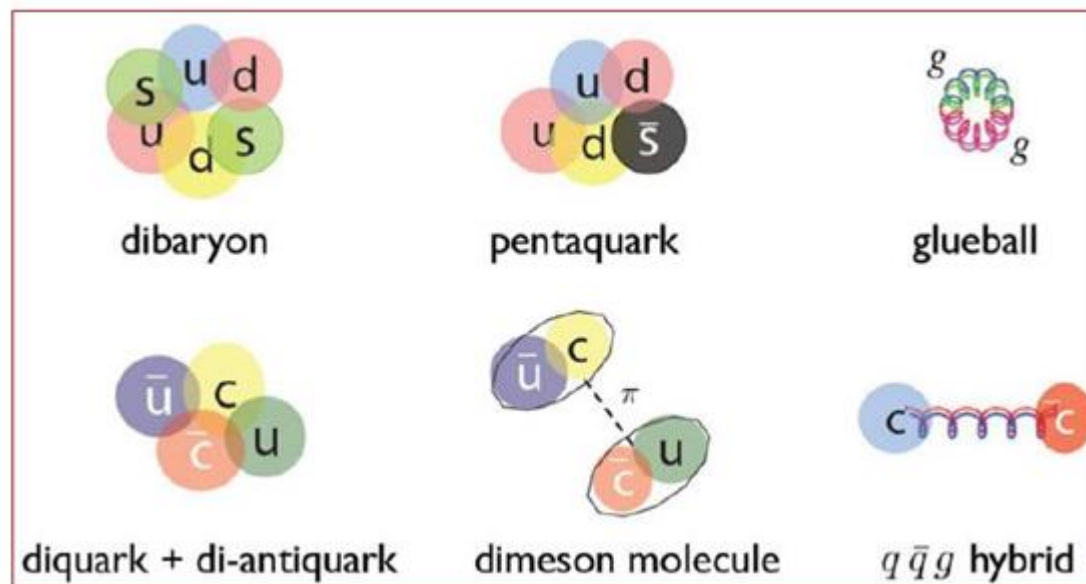
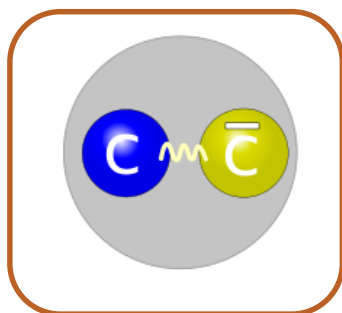
# Introduction



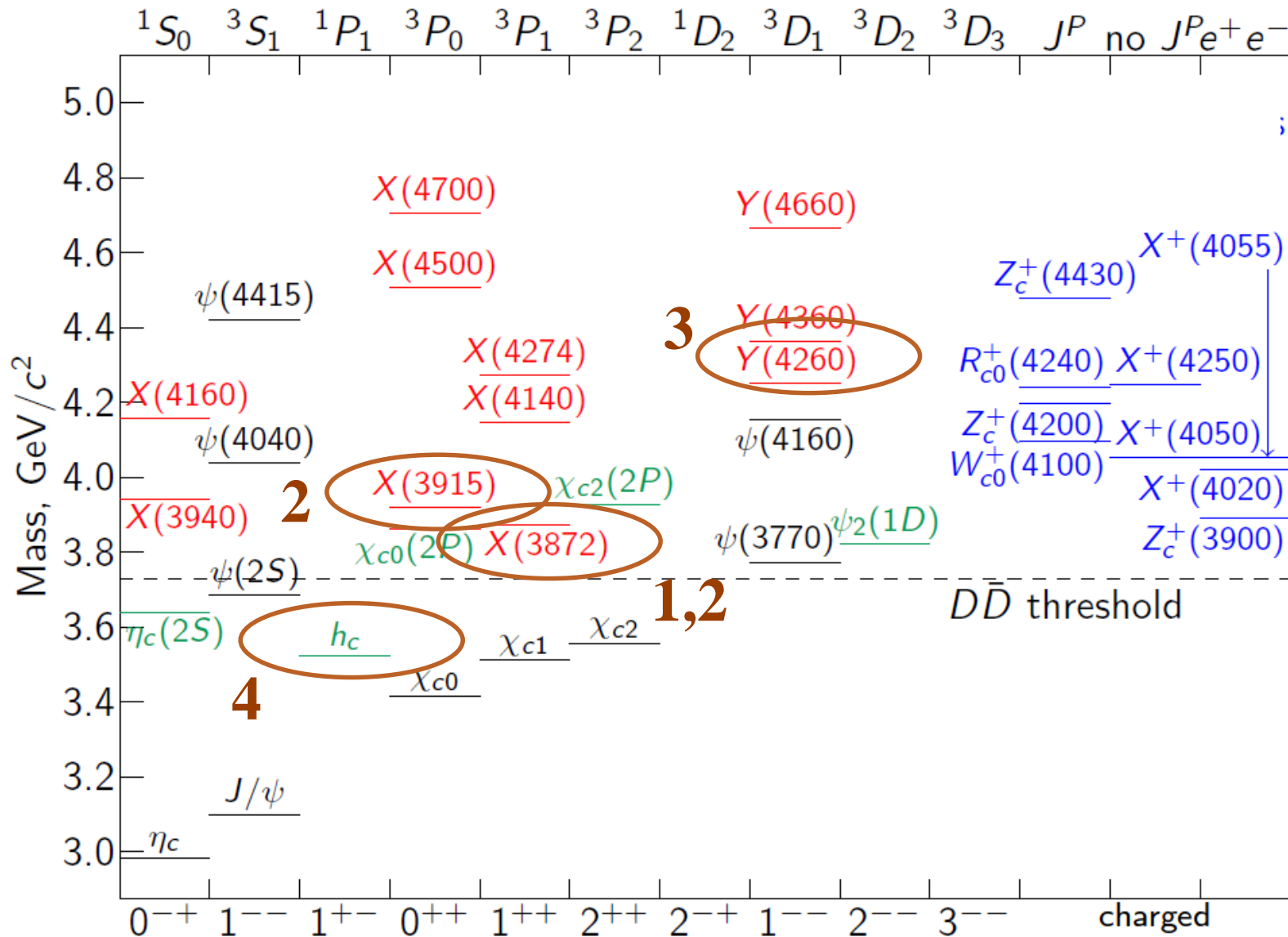
- After 2002 six new conventional charmonium states + more than a dozen of exotic charmonium-like states were discovered.
- Charmonium consists of two heavy c quarks and allows to study strong interactions and to check different theoretical models of heavy quarkonia.
- Charmonium-like states are not predicted by potential models and seem to have a more complex structure than charmonia.
- Naming scheme: Y states ( $1^{--}$ ), Z states (charged), X states (all the rest).

charmonium-like

charmonium



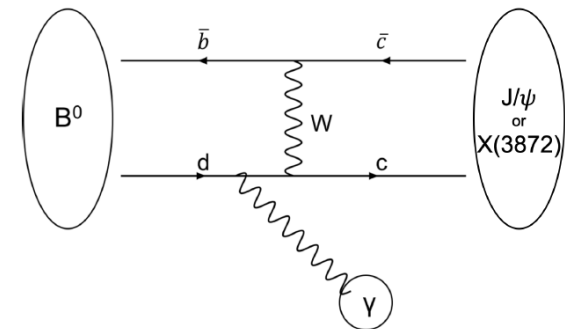
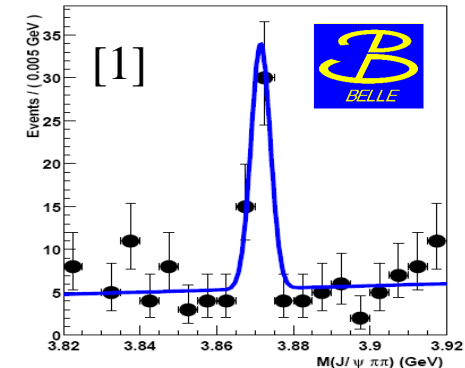
# Plan of my talk



Full Belle  $Y(4S)$  data sample of 711 fb<sup>-1</sup> is used for these analyses.

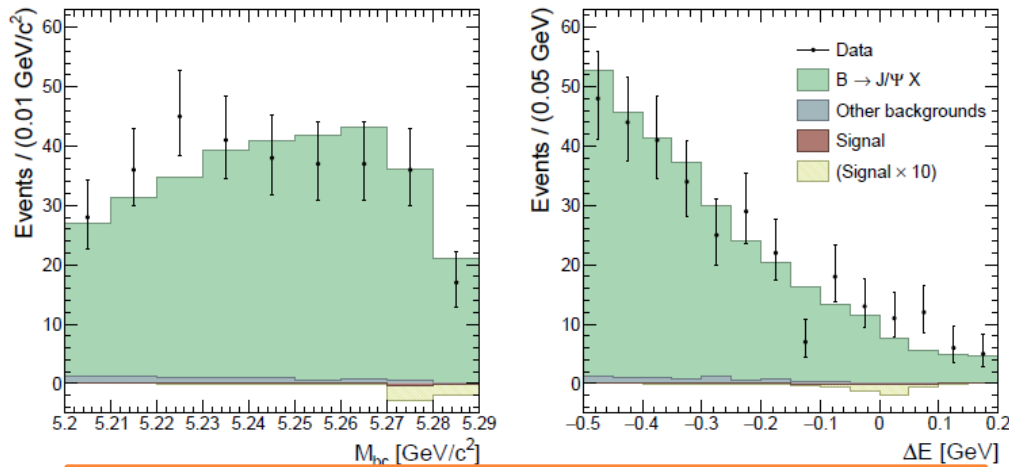
## Motivation

- $X(3872)$  is the first discovered and most famous exotic state:
  - observed by Belle in 2003 in  $J/\psi\pi^+\pi^-$  mode [1],
  - mass near  $D^0D^{*0}$  threshold,
  - small width ( $< 1.2$  MeV).
- Info on similar  $\mathcal{B}(B^0 \rightarrow J/\psi\gamma)$ :
  - $7.65 \times 10^{-9}$  from QCD factorization [2],
  - $4.5 \times 10^{-7}$  from pQCD [3],
  - $< 1.5 \times 10^{-6}$  from LHCb experiment [4].
- $X(3872)$  probably contains other components than c and anti-c quarks  $\Rightarrow \mathcal{B}(B^0 \rightarrow X(3872)\gamma) \Rightarrow$  should be smaller than  $\mathcal{B}(B^0 \rightarrow J/\psi\gamma)$ .
- New Physics contributions may enhance  $B^0 \rightarrow X(3872)\gamma$ !

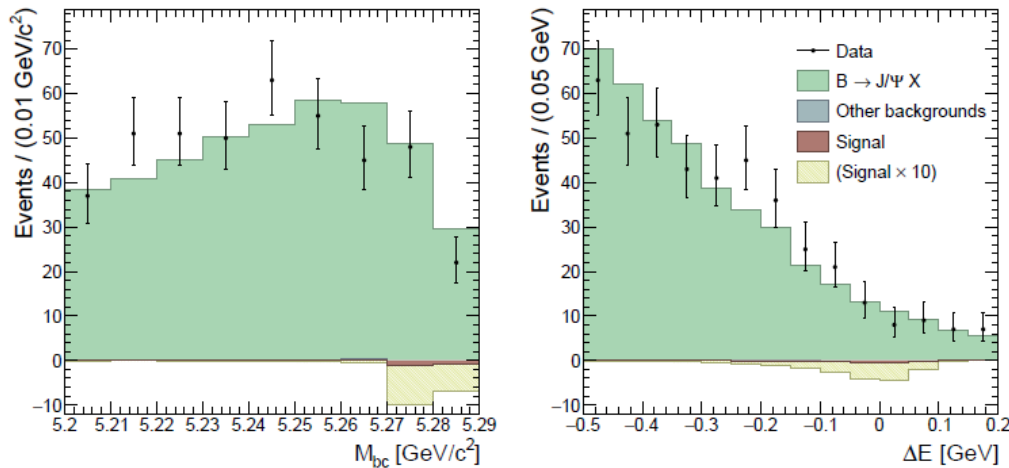


## Analysis features

- $X(3872) \rightarrow J/\psi\pi^+\pi^-$ ,  $J/\psi \rightarrow l^+l^-$  ( $l=e,\mu$ );
- selections on  $|M(l\pi\pi) - M(l\bar{l})|$  to reduce combinatorial bkg and bkg from misidentified  $\gamma$  conversions;
- photon selections:  $E_\gamma > 600$  MeV,  $E9/E25 > 0.87$ ,  $\pi^0$  veto;
- MVA to suppress main bg from  $B \rightarrow J/\psi X$  (33 variables).



$B^0 \rightarrow X(3872)\gamma, X(3872) \rightarrow J/\psi\pi^+\pi^-, J/\psi \rightarrow \mu^+\mu^-$



$B^0 \rightarrow X(3872)\gamma, X(3872) \rightarrow J/\psi\pi^+\pi^-, J/\psi \rightarrow e^+e^-$

## Signal yields

- Feldman-Cousins counting method is used to get UL;
- fitting method for cross-check;
- to calibrate the efficiency in the signal region the  $B^0 \rightarrow K_S^0\pi^+\pi^-\gamma$  control sample is used.

## Preliminary result

$$\mathcal{B}(B^0 \rightarrow X(3872)\gamma) \times \mathcal{B}(X(3872) \rightarrow J/\psi\pi^+\pi^-) < 5.1 \times 10^{-7} \text{ (90\% C.L.)}$$

# $B^+ \rightarrow X(3872, 3915) K^+$

I

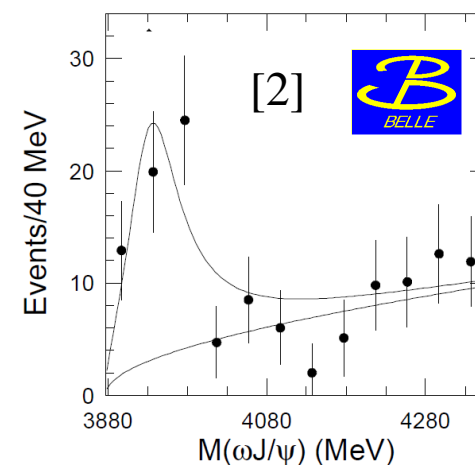
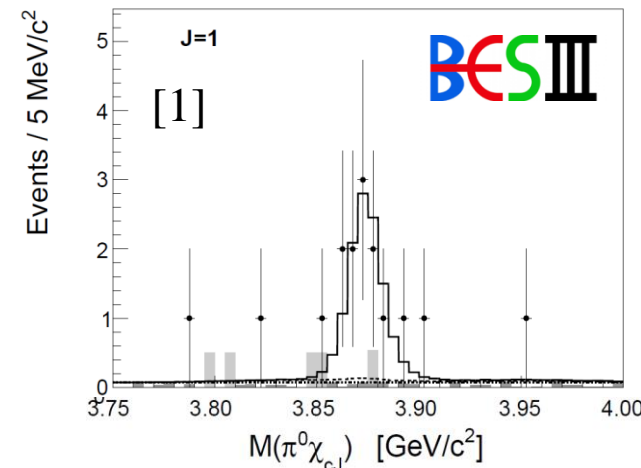


## Motivation

- New decay of  $X(3872)$  was recently observed by BESIII in  $e^+e^- \rightarrow X(3872)\gamma \rightarrow \chi_{c1}\pi^0\gamma$  [1].
- $\mathcal{B}(X(3872) \rightarrow \chi_{c1}\pi^0) / \mathcal{B}(X(3872) \rightarrow J/\psi\pi^+\pi^-) = 0.88^{+0.33}_{-0.27} \pm 0.10$  is large compared to  $\mathcal{B}(\psi(2S) \rightarrow J/\psi\pi^0) / \mathcal{B}(\psi(2S) \rightarrow J/\psi\pi^+\pi^-) = 3.66 \times 10^{-3}$ .
- This result disfavors  $\chi_{c1}(2P)$  interpretation of  $X(3872)$  (isospin breaking otherwise).
- Worth checking this ratio from Belle data!
- $X(3915)$  was first observed by Belle in  $B \rightarrow X(3915)K \rightarrow J/\psi\omega K$  [2].
- $J^{PC} = 0^{++} \Rightarrow$  may be  $\chi_{c0}(2P)$ , but too narrow and decay to  $J/\psi\omega$  is not suppressed.
- If  $X(3915)$  is a non-conventional state, single pion transitions may be enhanced.

## Analysis features

- $X(3872) \rightarrow \chi_{c1}\pi^0, X(3915) \rightarrow \chi_{c1}\pi^0$ ;
- $\chi_{c1} \rightarrow J/\psi\gamma, J/\psi \rightarrow l^+l^- (l=e, \mu)$ ;
- photon selections:  $E_\gamma > 100$  MeV,  $E9/E25 > 0.85, \pi^0$  veto.



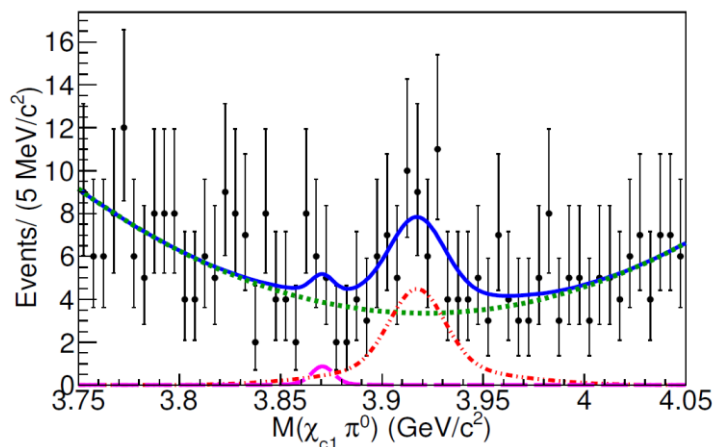
# $B^+ \rightarrow X(3872, 3915) K^+$

II

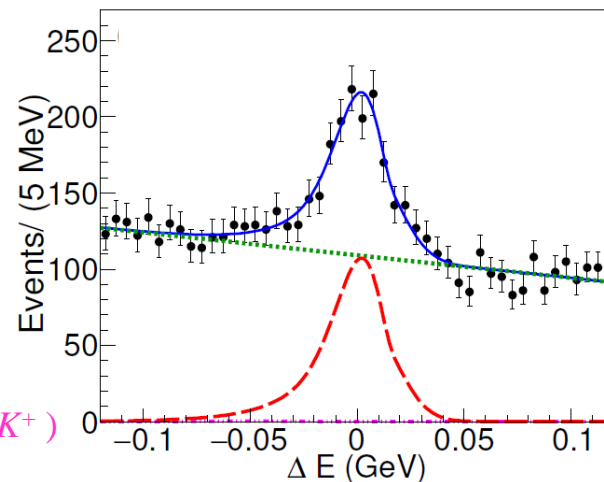


UML fit to  $\Delta E$  gives  $(806 \pm 69)$  signal events (consistent with similar previous Belle study of  $B^+ \rightarrow \chi_{c1} \pi^+ \pi^- K^+$  [5]).

Veto on  $B^+ \rightarrow \chi_{c1} K^{*0}$ :  $791.8 \text{ MeV} < M(K^+ \pi^0) < 991.8 \text{ MeV}$ .



signal  
combinatorial bg  
peaking bg ( $B^+ \rightarrow \chi_{c2} \pi^0 K^+$ )  
Total



## Signal yields

$X(3872)$ :  $2.7 \pm 5.5$  ( $0.3 \sigma$ )

$X(3915)$ :  $42 \pm 14$  ( $2.3 \sigma$ )

## Upper limits

$$\mathcal{B}(B^+ \rightarrow X(3872) K^+) \times \mathcal{B}(X(3872) \rightarrow \chi_{c1} \pi^0) < 8.1 \times 10^{-6} \text{ (90\% C.L.)}$$

$$\mathcal{B}(B^+ \rightarrow X(3915) K^+) \times \mathcal{B}(X(3915) \rightarrow \chi_{c1} \pi^0) < 3.8 \times 10^{-5} \text{ (90\% C.L.)}$$

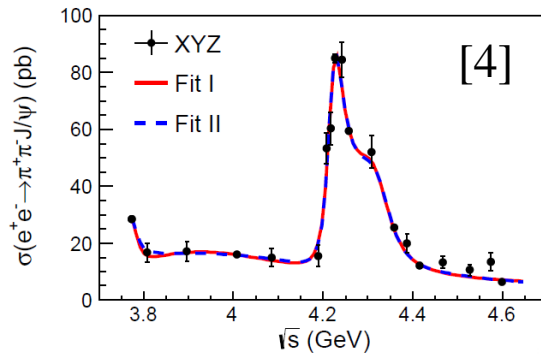
$$\mathcal{B}(X(3872) \rightarrow \chi_{c1} \pi^0) / \mathcal{B}(X(3872) \rightarrow J/\psi \pi^+ \pi^-) < 0.97 \text{ (90\% C.L.)}$$

No contradiction with BESIII result.

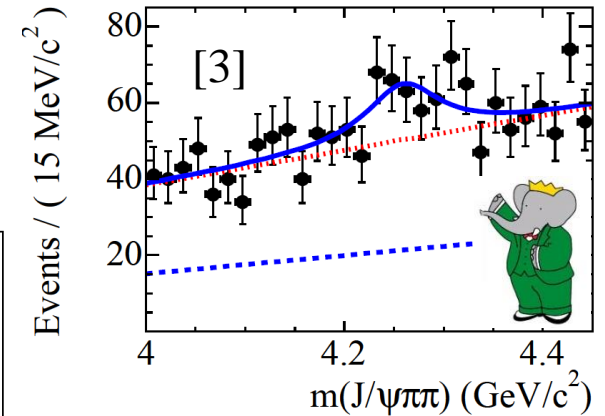
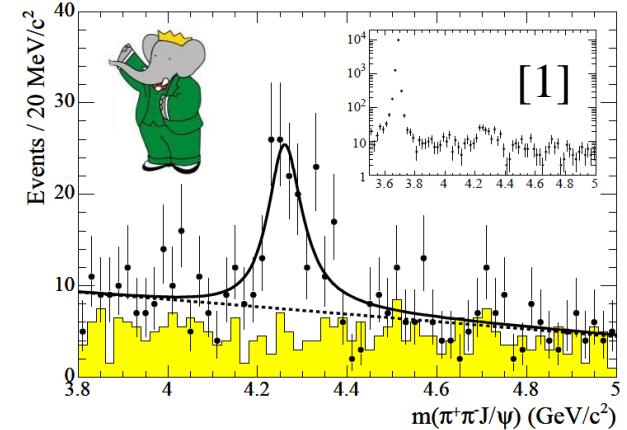
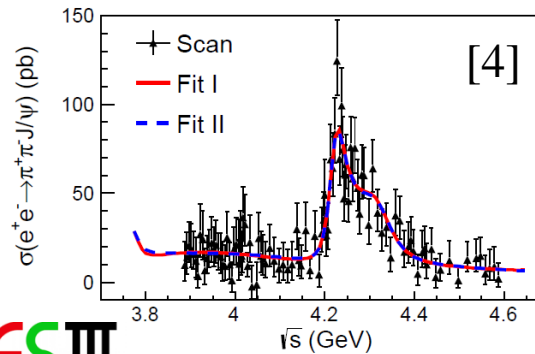
Compatible with the interpretation of  $X(3872)$  as an admixture of  $D^0 D^{*0}$  molecule and  $\chi_{c1}(2P)$  charmonium state.

## Motivation

- $Y(4260)$  first seen by BaBar in  $e^+e^- \rightarrow Y(4260)\gamma_{ISR} \rightarrow J/\psi\pi^+\pi^-\gamma_{ISR}$  [1].
- If  $Y(4260)$  is an admixture of charmonium and tetraquark state, from QCD sum rules  $\mathcal{B}(B^+ \rightarrow Y(4260)K^+) \times \mathcal{B}(Y(4260) \rightarrow J/\psi\pi^+\pi^-)$  is in range  $(3.0 \times 10^{-8} : 1.8 \times 10^{-6})$  [2].
- BaBar observed  $128 \pm 42$  signal events ( $3.1 \sigma$ ) using  $211 \text{ fb}^{-1}$  and set a 95 % C.L. UL on  $\mathcal{B}(B^+ \rightarrow Y(4260)K^+) \times \mathcal{B}(Y(4260) \rightarrow J/\psi\pi^+\pi^-) < 2.9 \times 10^{-5}$  [3].
- Two resonant structures observed by BESIII in  $e^+e^- \rightarrow J/\psi\pi^+\pi^-$  are interpreted as  $Y(4260)$  and  $Y(4360)$  [4].
- Need to search for  $Y(4260)$  in B decays!



BESIII



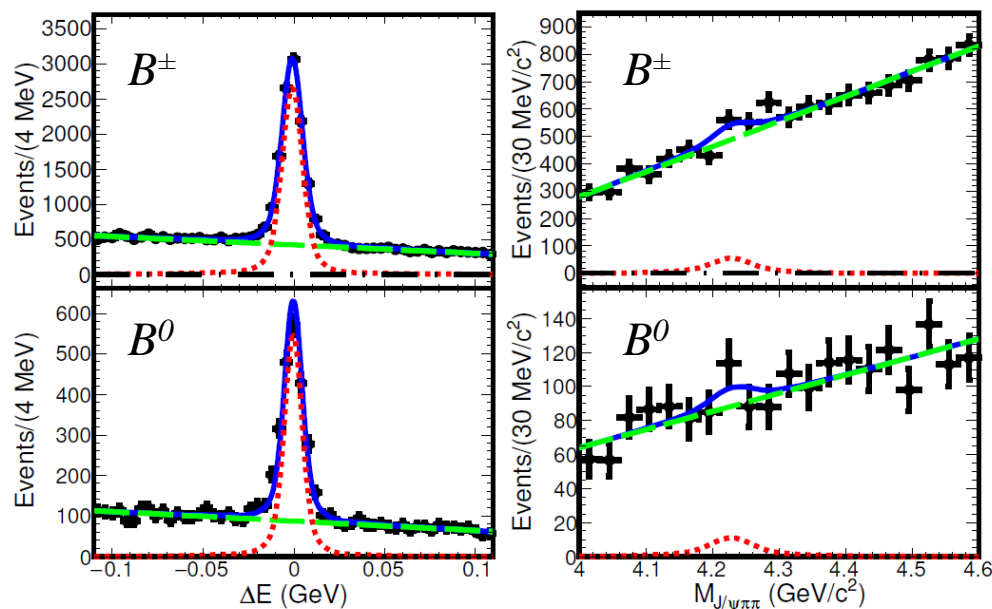


## Analysis features

- $B^\pm$  and  $B^0$  are considered,  $Y(4260) \rightarrow J/\psi \pi^+ \pi^-$ ,  $J/\psi \rightarrow l^+ l^-$  ( $l=e, \mu$ );
- $B \rightarrow \psi(2S)K$  and  $B \rightarrow X(3872)K$  are used as control samples;
- UML fit of  $\Delta E$ , signal yield from weighted  $M(J/\psi \pi^+ \pi^-)$  by  $\mathcal{P}lot$ .

Consistent with BaBar  
but more stringent.

Given for the first time.



## Upper limits

Decay	$\epsilon$ (%)	$N_S$	$\Sigma$ ( $\sigma$ )	U.L.
$B^+ \rightarrow Y(4260)K^+, Y(4260) \rightarrow J/\psi \pi^+ \pi^-$	19.8	$179 \pm 53^{+55}_{-41}$	2.1	$1.4 \times 10^{-5}$
$B^0 \rightarrow Y(4260)K^0, Y(4260) \rightarrow J/\psi \pi^+ \pi^-$	10.6	$39 \pm 28^{+7}_{-31}$	0.9	$1.7 \times 10^{-5}$

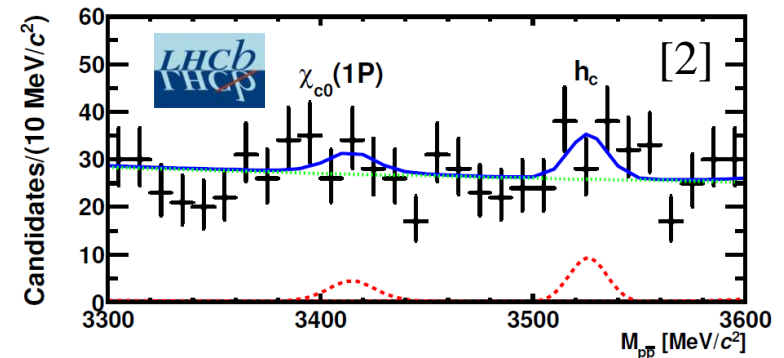
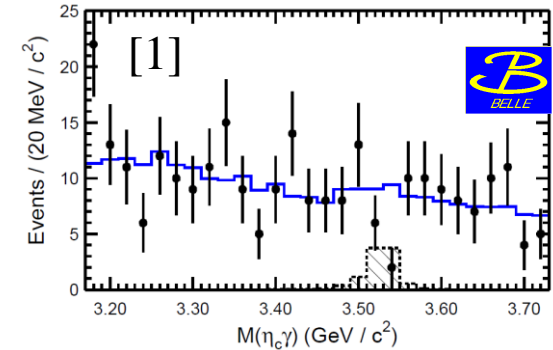
## Motivation

- Both  $B^+ \rightarrow h_c K^+$  and  $B^+ \rightarrow \chi_{c0} K^+$  are suppressed by factorization.
- Since  $\mathcal{B}(B^+ \rightarrow \chi_{c0} K^+) = (1.49^{+0.15}_{-0.14}) \times 10^{-4}$  (world average),  $\mathcal{B}(B^+ \rightarrow h_c K^+)$  should be of the same order. However has not been observed so far!
- Best upper limits:
  - Belle with  $h_c \rightarrow \eta_c \gamma$ ,  $\eta_c \rightarrow K_S K^\pm \pi^\pm$  and  $pp$  using  $253 \text{ fb}^{-1}$   
 $\mathcal{B}(B^+ \rightarrow h_c K^+) < 3.8 \times 10^{-5}$  [1];
  - LHCb with  $h_c \rightarrow pp$   
 $\mathcal{B}(B^+ \rightarrow h_c K^+) \times \mathcal{B}(h_c \rightarrow pp) < 6.4 \times 10^{-4}$  [2].
- Theoretical predictions:
  - $2.7 \times 10^{-5}$  from QCD factorization [3];
  - $3.6 \times 10^{-5}$  from pQCD [4];
  - $(3.1 \times 10^{-5} : 5.7 \times 10^{-5})$  from QCD factorization including the charmonium bound-state scales [5];
- Needs to be updated!

## Analysis features

- $B^\pm$  and  $B^0$  are considered,  $h_c \rightarrow \eta_c \gamma$  and  $pp\pi^+\pi^-$  (recently observed by BESIII [6]);
- $\eta_c$  candidates are reconstructed in 10 decay channels ( $K^+ K_S^0 \pi^-$ ,  $K^+ K^- \pi^0$ ,  $K_S^0 K_S^0 \pi^0$ ,  $K^+ K^- \eta$ ,  $K^+ K^- K^+ K^-$ ,  $\eta'(\rightarrow \eta \pi^+ \pi^-) \pi^+ \pi^-$ ,  $pp$ ,  $pp\pi^0$ ,  $pp\pi^+ \pi^-$ , and  $\Lambda\Lambda$ );
- MVA is used for each channel to separate signal from bkg;

K. Chilikin et al. arXiv: 1903.06414 (submitted to PRD)



[1] PRD 74 012007 (2006)

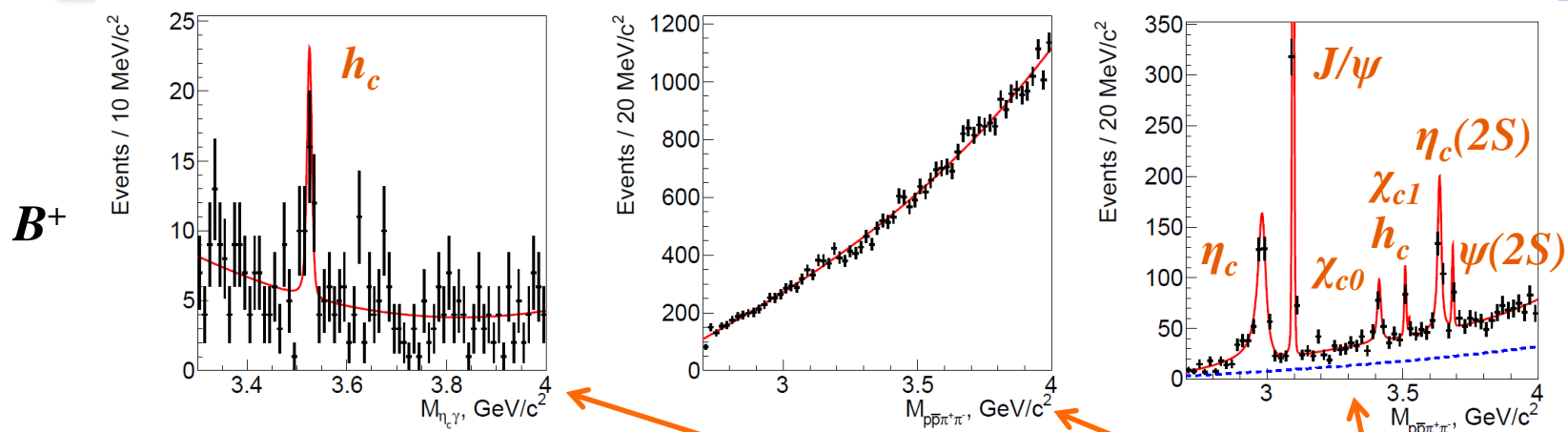
[2] EPJ C73 2462 (2013)

[3] hep-ph/06072201

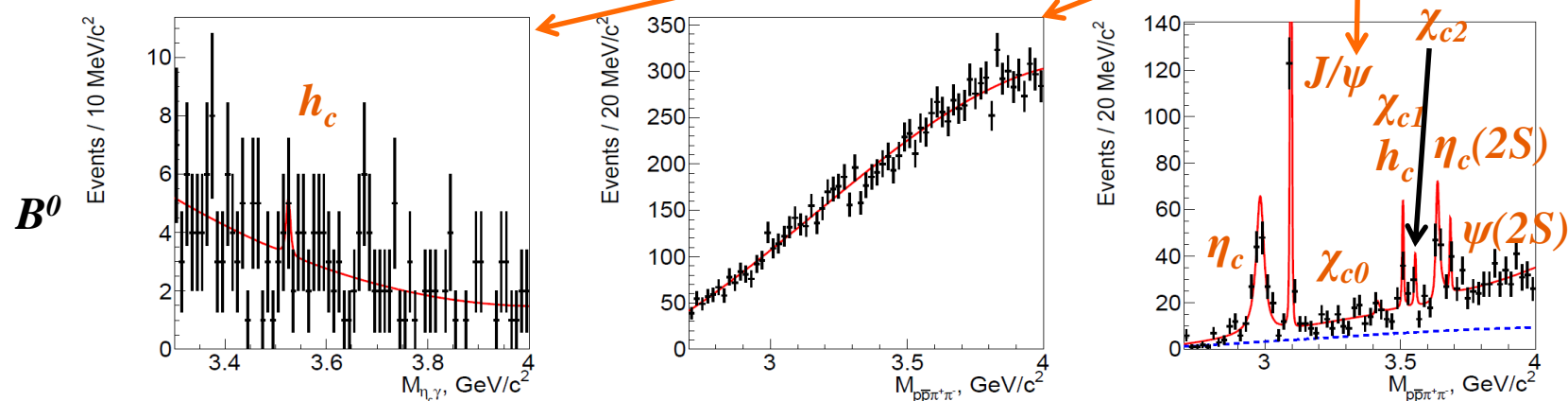
[4] PRD 74 114029 (2006)

[5] NPB 811 155 (2009)

[6] arXiv:1810.12023



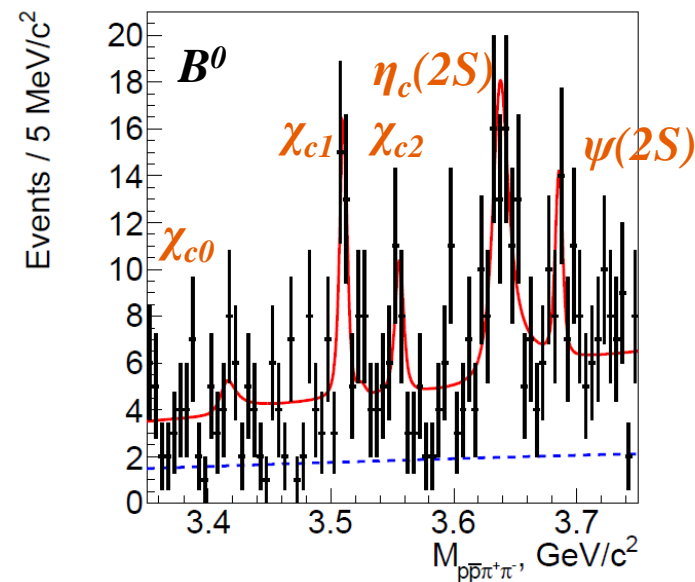
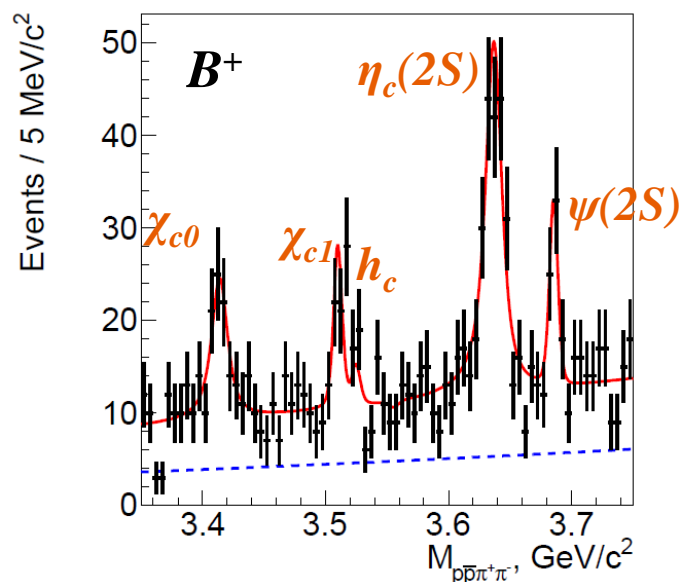
Simultaneous UML fit to  $h_c \rightarrow \eta_c \gamma$  signal and  $h_c \rightarrow pp\pi^+\pi^-$  bkg & signal



## Signal yields

- $B^+ \rightarrow h_c K^+$ :  $32.6 \pm 8.0$  ( $4.8 \sigma$  taking into account systematics)  $\rightarrow$  **evidence!**
- $B^0 \rightarrow h_c K_S^0$ :  $3.1 \pm 3.7$  ( $0.7 \sigma$  taking into account systematics)

A closer look at  $h_c \rightarrow p\bar{p}\pi^+\pi^-$  signal in  $\chi_{cJ}$  region...



State	$B^+ \rightarrow (c\bar{c})K^+$	$B^0 \rightarrow (c\bar{c})K_S^0$
$\eta_c$	$20.1\sigma$	$12.5\sigma$
$J/\psi$	$33.9\sigma$	$20.8\sigma$
$\chi_{c0}$	$6.0\sigma$	$0.6\sigma$
$\chi_{c1}$	$4.9\sigma$	$4.5\sigma$
$\chi_{c2}$	$0.3\sigma$	$2.5\sigma$
$\eta_c(2S)$	$12.3\sigma$	$5.9\sigma$
$\psi(2S)$	$5.0\sigma$	$2.8\sigma$

Observation of the new  $\eta_c(2S)$  decay channel:  
 $\eta_c(2S) \rightarrow p\bar{p}\pi^+\pi^-$  !

Other charmonium signals are consistent with PDG.

# Summary



## ○ $B^0 \rightarrow X(3872)\gamma$

- Upper limit is set on  $\mathcal{B}(B^0 \rightarrow X(3872)\gamma) \times \mathcal{B}(X(3872) \rightarrow J/\psi \pi^+ \pi^-)$ .

## ○ $B^+ \rightarrow X(3872, 3915)K^+$

- Upper limits are set on the product branching fractions  $\mathcal{B}(B^+ \rightarrow X(3872)K^+) \times \mathcal{B}(X(3872) \rightarrow \chi_{c1} \pi^0)$  and  $\mathcal{B}(B^+ \rightarrow X(3915)K^+) \times \mathcal{B}(X(3915) \rightarrow \chi_{c1} \pi^0)$ . Compatible with the interpretation of  $X(3872)$  as an admixture of  $D^0 \bar{D}^{*0}$  molecule and  $\chi_{c1}(2P)$  charmonium state.
- Branching ratio  $\mathcal{B}(X(3872) \rightarrow \chi_{c1} \pi^0) / \mathcal{B}(X(3872) \rightarrow J/\psi \pi^+ \pi^-) < 0.97$  (90% C.L.). No contradiction with BESIII result.

## ○ $B \rightarrow Y(4260)K$

- Upper limit on  $\mathcal{B}(B^+ \rightarrow Y(4260)K^+) \times \mathcal{B}(Y(4260) \rightarrow J/\psi \pi^+ \pi^-)$  is consistent with BaBar but more stringent.
- Upper limit on  $\mathcal{B}(B^0 \rightarrow Y(4260)K^0) \times \mathcal{B}(Y(4260) \rightarrow J/\psi \pi^+ \pi^-)$  is given for the first time.

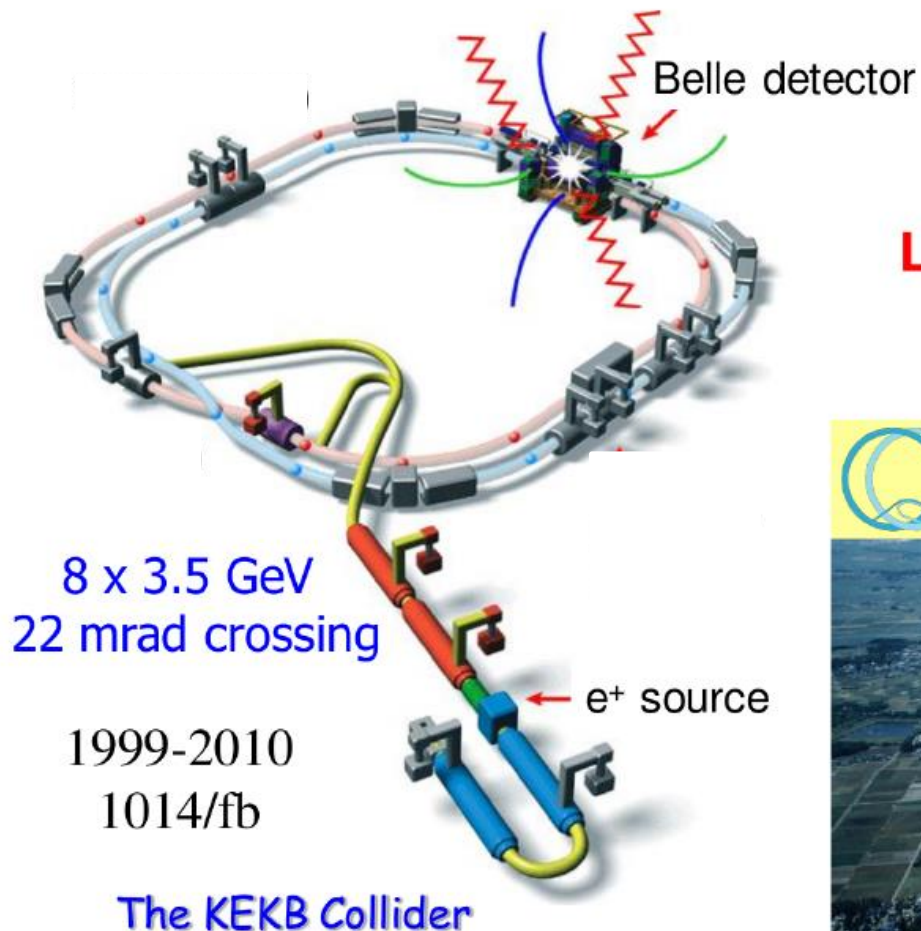
## ○ $B \rightarrow h_c K$

- Evidence of the decay  $B^+ \rightarrow h_c K^+$  is found, and  $\mathcal{B}(B^+ \rightarrow h_c K^+) = (3.7^{+1.0}_{-0.9} \pm 0.8) \times 10^{-5}$  is consistent with the existing limit and theoretical predictions.
- Upper limit is set on  $\mathcal{B}(B^0 \rightarrow h_c K_S^0)$ .
- First observation of  $\eta_c(2S) \rightarrow p p \pi^+ \pi^-$  decay with  $12.1\sigma$  significance.



# Backup

# Belle experiment



World record:  
 **$L = 2.1 \times 10^{34}/\text{cm}^2/\text{sec}$**



The new generation SuperKEKB has been launched, and Belle II recorded the first collisions on April 26, 2018, JST!

$$B^0 \rightarrow X(3872)\gamma$$



Source	Dimuon	Dielectron
$N_{B\bar{B}}$	1.4%	1.4%
Tracking (4 tracks)	1.4%	1.4%
$\mathcal{B}(J/\psi \rightarrow \ell^+ \ell^-)$	0.6%	0.5%
$\gamma$ detection	3.1%	3.1%
MC gen. model	1.1%	1.9%
$\pi^\pm$ identification	1.3%	1.3%
$\ell^\pm$ identification	2.1%	1.8%
Bkg. suppression	2.3%	2.5%
$\pi^0$ veto	0.8%	0.8%
Signal box eff.	3.5%	3.5%
Total	6.2%	6.4%



$$B^+ \rightarrow X(3872, 3915) K^+$$



Source	$\mathcal{B}$ (%)		$R_{\chi_{c1}/\psi}^X$ (%)
	$X(3915)$	$X(3872)$	
Lepton identification	2.3	2.2	-
Kaon identification	1.0	1.0	-
Efficiency	0.5	0.5	2.2
$B\bar{B}$ pairs	1.4	1.4	-
Tracking	1.1	1.1	0.7
$\gamma$ identification	2.0	2.0	2.0
$\pi^0$ veto	1.2	1.2	1.2
$\pi^0$ reconstruction	2.2	2.2	2.2
Signal extraction	+16.1 -19.5	+37.0 -44.4	+37.1 -44.5
Secondary $\mathcal{B}$	3.0	3.0	2.9
Total	+17.0 -20.2	+37.4 -44.7	+37.4 -44.8

# $B \rightarrow Y(4260)K$

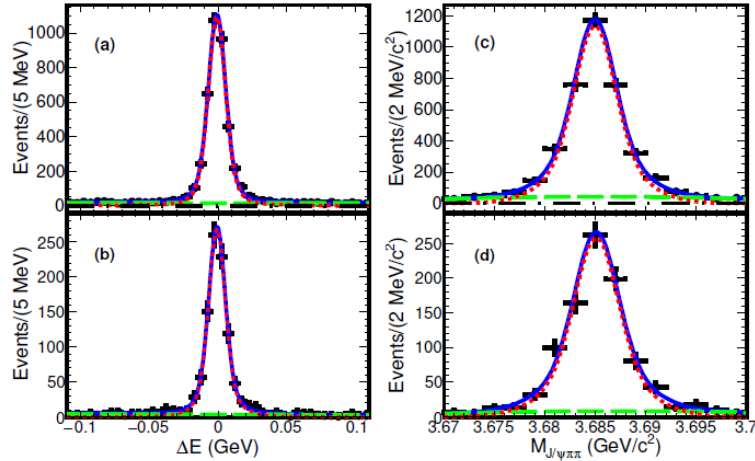


FIG. 1. Fit to the  $\Delta E$  ((a) and (b)) and  $s$ Plot of  $M_{J/\psi\pi\pi}$  ((c) and (d)) distributions for  $B^+ \rightarrow \psi(2S)(\rightarrow J/\psi\pi^+\pi^-)K^+$  decays (top) and  $B^0 \rightarrow \psi(2S)(\rightarrow J/\psi\pi^+\pi^-)K_S^0$  decays (bottom), respectively. The curves show the fit functions for the signal (red dotted curve), background (green dashed curve) and their sum (blue solid line).

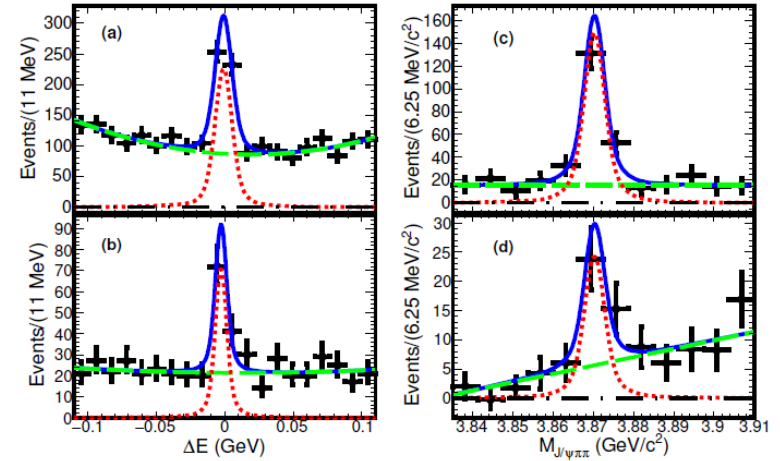


FIG. 2. Fit to the  $\Delta E$  ((a) and (b)) and  $s$ Plot of  $M_{J/\psi\pi\pi}$  ((c) and (d)) distributions for  $B^+ \rightarrow X(3872)(\rightarrow J/\psi\pi^+\pi^-)K^+$  decays (top) and  $B^0 \rightarrow X(3872)(\rightarrow J/\psi\pi^+\pi^-)K_S^0$  decays (bottom), respectively. Fit follow the same convention as Fig. 1.

Decay	$\epsilon$ (%)	$N_S$	$\mathcal{B}$	$\mathcal{B}_{\text{PDG}}$
$B^+ \rightarrow \psi(2S)K^+$	16.8	$3481 \pm 95$	$(6.54 \pm 0.18) \times 10^{-4}$	$(6.21 \pm 0.23) \times 10^{-4}$
$B^0 \rightarrow \psi(2S)K^0$	10.3	$856 \pm 74$	$(5.25 \pm 0.45) \times 10^{-4}$	$(5.8 \pm 0.5) \times 10^{-4}$
$B^+ \rightarrow X(3872)K^+, X(3872) \rightarrow J/\psi\pi^+\pi^-$	22.2	$185 \pm 13$	$(9.07 \pm 0.64) \times 10^{-6}$	$(8.6 \pm 0.8) \times 10^{-6}$
$B^0 \rightarrow X(3872)K^0, X(3872) \rightarrow J/\psi\pi^+\pi^-$	13.1	$29.9 \pm 6.2$	$(4.97 \pm 1.03) \times 10^{-6}$	$(4.3 \pm 1.3) \times 10^{-6}$

Source $\rightarrow$ Decay $\downarrow$	Tracking	Particle identification				PDF modeling	Y(4260) parameters	Fit bias	$N_{BB}$	$\mathcal{B}(J/\psi \rightarrow \ell^+\ell^-)$	Total
		$K_S^0$	Kaon	Pion	Lepton						
$B^+ \rightarrow Y(4260)K^+$	1.8	-	0.9	1.3	1.2	+8.0 -11.1	+29.0 -19.5	4.3	1.4	0.4	+30.5 -23.0
$B^0 \rightarrow Y(4260)K_S^0$	2.1	0.7	-	1.3	1.2	+7.7 -77.0	+14.0 -17.3	6.5	1.4	0.4	+17.5 -79.2
Simultaneous	1.9	0.2	0.7	1.3	1.2	+5.3 -15.3	+25.0 -18.0	4.8	1.4	0.4	+26.2 -24.3



## Resolution

New:  $B \rightarrow h_c K$

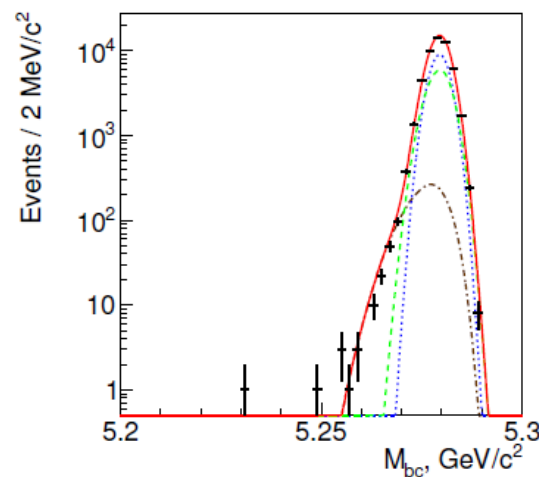
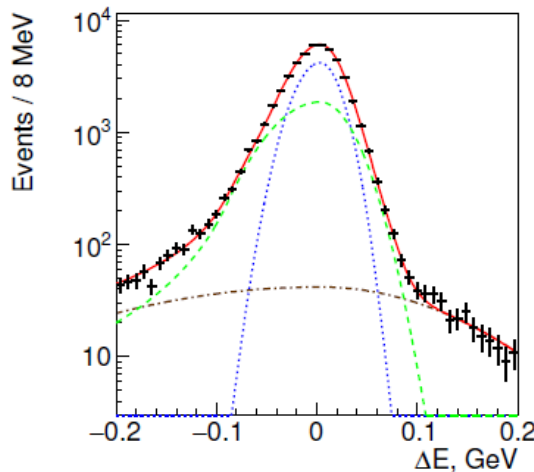
The resolution is parameterized by the function

$$S(\Delta E, M_{bc}) = N_{CB} F_{CB}(x_1) G_a^{(12)}(y_1) + N_{G1} G_a^{(21)}(x_2) G_a^{(22)}(y_2) + N_{G2} G_a^{(31)}(x_3) G_a^{(32)}(y_3), \quad (1)$$

where  $F_{CB}$  is an asymmetric Crystal Ball function,  $G_a^{(ij)}$  are asymmetric Gaussian functions,  $N_{CB}$ ,  $N_{G1}$  and  $N_{G2}$  are normalizations and  $x_i$  and  $y_i$  ( $i = 1, 2, 3$ ) are rotated variables that are given by

$$\begin{pmatrix} x_i \\ y_i \end{pmatrix} = \begin{pmatrix} \cos \alpha_i & \sin \alpha_i \\ -\sin \alpha_i & \cos \alpha_i \end{pmatrix} \begin{pmatrix} \Delta E - (\Delta E)_0 \\ M_{bc} - (M_{bc})_0 \end{pmatrix}. \quad (2)$$

Here,  $((\Delta E)_0, (M_{bc})_0)$  is the central point and  $\alpha_i$  are the rotation angles. Resolution for  $B^+ \rightarrow h_c K^+$  with  $\eta_c \rightarrow K^+ K^- \pi^0$ :



## Fit to the $(\Delta E, M_{bc})$ distribution

New:  $B \rightarrow h_c K$

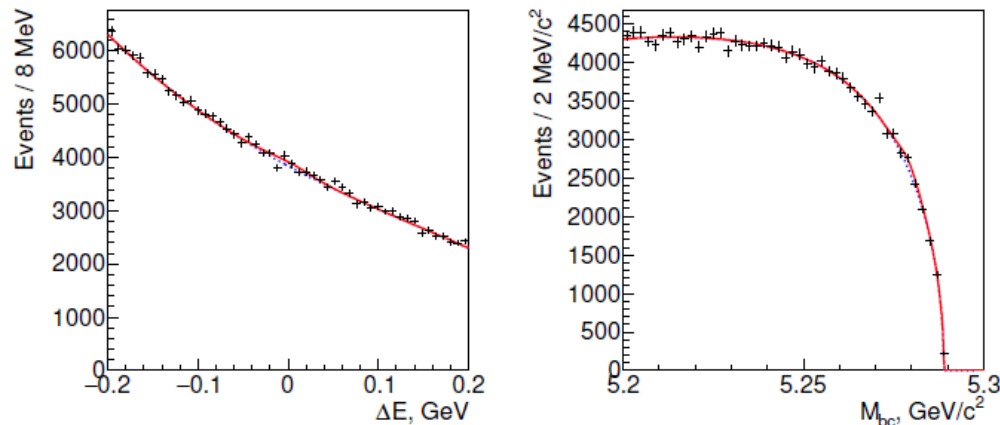
The  $(\Delta E, M_{bc})$  distribution is fitted in order to estimate the expected number of the background events in the signal region. The distribution is fitted to the function

$$N_S S(\Delta E, M_{bc}) + B(\Delta E, M_{bc}), \quad (3)$$

where  $N_S$  is the number of signal events and  $B$  is the background density function that is given by

$$B(\Delta E, M_{bc}) = \sqrt{m_0 - M_{bc}} \exp[-a(m_0 - M_{bc})] P_3(\Delta E, M_{bc}), \quad (4)$$

where  $m_0$  is the threshold mass,  $a$  is a rate parameter and  $P_3$  is a two-dimensional third-order polynomial. The region with  $\Delta E < -0.12$  GeV is excluded for the channel  $h_c \rightarrow p\bar{p}\pi^+\pi^-$  because of peaking backgrounds from partially reconstructed B decays with an additional  $\pi$  meson. Background for  $B^+ \rightarrow h_c K^+$  with  $\eta_c \rightarrow K^+ K^- \pi^0$  (with  $M_{bc} > 5.272$  GeV/ $c^2$  for the projection onto  $\Delta E$  and  $|\Delta E| < 20$  MeV for the projection onto  $M_{bc}$ ):



$$B \rightarrow h_c K$$



## Multivariate analysis

New:  $B \rightarrow h_c K$

A multivariate analysis is performed for each channel using the MLP from TMVA. Variables:

- All channels: thrust angles  $B$  daughters - remaining particles in the event and all tracks - all photons, ratio of the Fox-Wolfram moments  $F_2/F_0$ , the  $B$  production angle, vertex-fit quality.
- $h_c \rightarrow \eta_c \gamma$ : the  $h_c$  helicity angle, the  $\eta_c$  mass, the numbers of  $\pi^0$  candidates that have the  $h_c$  daughter photon as one of their daughters.
- $\eta_c \rightarrow K^+ K_S^0 \pi^-$ ,  $\eta_c \rightarrow K^+ K^- \pi^0$  and  $\eta_c \rightarrow K_S^0 K_S^0 \pi^0$ : invariant masses of both  $(K, \pi)$  combinations.
- Channels with the corresponding particles in the final state:  $K$  and  $p$  particle-identification likelihoods.
- Channels with a  $\pi^0$  or  $\eta$ : the  $\pi^0$  ( $\eta$ ) mass, the minimal energy of its daughter photons in the laboratory frame, the numbers of  $\pi^0$  candidates that have the  $\pi^0$  ( $\eta$ ) daughter photon as one of their daughters.
- Channels with  $\eta \rightarrow \pi^+ \pi^- \pi^0$  or  $\eta' \rightarrow \eta \pi^+ \pi^-$ : the  $\eta$  ( $\eta'$ ) mass.

## Optimization of the selection requirements

New:  $B \rightarrow h_c K$

An elliptical channel-dependent signal region is selected:  $\left(\frac{\Delta E}{R_{\Delta E}^{(i)}}\right)^2 + \left(\frac{M_{bc}}{R_{M_{bc}}^{(i)}}\right)^2 < 1$ . The following variables are optimized for each decay channel: half-axes  $R_{\Delta E}^{(i)}$ ,  $R_{M_{bc}}^{(i)}$ , and cutoff for MLP output ( $v_0$ ). The value being maximized is  $F_{\text{opt}} = (\sum_i N_{\text{sig}}^{(i)}) / (\frac{a}{2} + \sqrt{\sum_i N_{\text{bg}}^{(i)}})$ , where  $a = 3$  is the target significance. The optimization is performed separately for all  $\eta_c \gamma$  channels and  $p\bar{p}\pi^+\pi^-$ . Results ( $B^+ \rightarrow h_c K^+$ ):

Channel	Parameters			Efficiency		
	$R_{\Delta E}^{(i)}$	$R_{M_{bc}}^{(i)}$	$v_0^{(i)}$	$\epsilon_{\text{SR}}^{(i)}$	$\epsilon_S^{(i)}(v_0^{(i)})$	$\epsilon_B^{(i)}(v_0^{(i)})$
$\eta_c(\rightarrow K^+ K_S^0 \pi^-) \gamma$	32.7	4.82	0.804	6.27%	59.5%	5.08%
$\eta_c(\rightarrow K^+ K^- \pi^0) \gamma$	36.2	3.90	0.958	4.27%	31.7%	0.56%
$\eta_c(\rightarrow K_S^0 K_S^0 \pi^0) \gamma$	42.3	4.49	0.976	1.79%	17.8%	0.18%
$\eta_c(\rightarrow K^+ K^- \eta_{2\gamma}) \gamma$	34.4	4.16	0.977	4.21%	20.2%	0.22%
$\eta_c(\rightarrow K^+ K^- \eta_{3\pi}) \gamma$	24.9	3.59	0.978	1.75%	29.7%	0.23%
$\eta_c(\rightarrow K^+ K^- K^+ K^-) \gamma$	25.3	4.13	0.770	4.89%	53.2%	6.69%
$\eta_c(\rightarrow \eta'(\rightarrow \eta_{2\gamma} \pi^+ \pi^-) \pi^+ \pi^-) \gamma$	30.5	4.21	0.958	2.69%	40.5%	0.63%
$\eta_c(\rightarrow \eta'(\rightarrow \eta_{3\pi} \pi^+ \pi^-) \pi^+ \pi^-) \gamma$	26.8	4.16	0.990	1.01%	29.2%	0.13%
$\eta_c(\rightarrow p\bar{p}) \gamma$	38.9	5.48	0.654	17.70%	75.7%	10.66%
$\eta_c(\rightarrow p\bar{p} \pi^0) \gamma$	30.2	3.75	0.954	4.65%	30.3%	0.50%
$\eta_c(\rightarrow p\bar{p} \pi^+ \pi^-) \gamma$	24.1	4.03	0.912	6.31%	30.0%	1.53%
$\eta_c(\rightarrow \Lambda \bar{\Lambda}) \gamma$	40.4	5.66	0.727	4.04%	70.6%	6.79%
$p\bar{p} \pi^+ \pi^-$	13.5	4.36	0.598	14.81%	64.6%	18.40%

Efficiencies:  $\epsilon_{\text{SR}}^{(i)}$  - reconstruction and signal region selection;  $\epsilon_S^{(i)}(v_0^{(i)})$ ,  $\epsilon_B^{(i)}(v_0^{(i)})$  - MLP for signal and background, respectively.



## Data fitting procedure

New:  $B \rightarrow h_c K$

We perform a simultaneous extended unbinned likelihood fit to the  $h_c \rightarrow \eta_c \gamma$  signal,  $h_c \rightarrow p\bar{p}\pi^+\pi^-$  background and  $h_c \rightarrow p\bar{p}\pi^+\pi^-$  signal distributions. The signal PDF for the channel  $h_c \rightarrow \eta_c \gamma$  is given by

$$S_{\eta_c \gamma}(M) = (N_{h_c} |A_{h_c}(M)|^2) \otimes R_{h_c}^{(\eta_c \gamma)}(\Delta M) + P_2(M), \quad (5)$$

where  $N_{h_c}$  is the number of signal events,  $R_{h_c}^{(\eta_c \gamma)}$  is the  $h_c$  mass resolution, and  $P_2$  is a second-order polynomial. The background PDF  $B_{p\bar{p}\pi^+\pi^-}(M)$  for the channel  $h_c \rightarrow p\bar{p}\pi^+\pi^-$  is a third-order polynomial. The signal PDF for the channel  $h_c \rightarrow p\bar{p}\pi^+\pi^-$  is given by

$$S_{p\bar{p}\pi^+\pi^-}(M) = \left( |P_3(M) + \sum_{R=\eta_c, \chi_{c0}, \eta_c(2S)} \sqrt{N_R} e^{i\varphi_R} A_R(M)|^2 + \sum_{R=J/\psi, \chi_{c1}, h_c, \chi_{c2}, \psi(2S)} N_R |A_R(M)|^2 \right) \otimes R_{h_c}(\Delta M), \quad (6)$$

where  $P_3$  is a third-order polynomial representing the noncharmonium signal. The wide states are added coherently to the signal PDF, while the states that are narrower than the resolution are added incoherently. The amplitudes are normalized in such a way that all the parameters  $N$  represent the yields of the corresponding states. The signal distribution is fitted to the function  $S_{p\bar{p}\pi^+\pi^-}(M) + wB_{p\bar{p}\pi^+\pi^-}(M)$ , where  $w$  is the weight of the background events in the signal region that is calculated as the ratio of integrals of the background distribution in  $(\Delta E, M_{bc})$  over the signal and background regions.

# $B \rightarrow h_c K$



Model	$h_c$ significance		$\eta_c(2S) \rightarrow p\bar{p}\pi^+\pi^-$ significance	
	$B^+ \rightarrow h_c K^+$	$B^0 \rightarrow h_c K_S^0$	$B^+ \rightarrow h_c K^+$	$B^0 \rightarrow h_c K_S^0$
Default	$5.0\sigma$	$0.8\sigma$	$12.3\sigma$	$5.9\sigma$
Free masses and widths	$5.0\sigma$	$0.8\sigma$	$12.3\sigma$	$6.0\sigma$
Polynomial order ( $h_c \rightarrow \eta_c \gamma$ )	$4.8\sigma$	$0.8\sigma$	$12.3\sigma$	$5.9\sigma$
Polynomial order ( $h_c \rightarrow p\bar{p}\pi^+\pi^-$ background)	$5.0\sigma$	$0.8\sigma$	$12.2\sigma$	$5.9\sigma$
Polynomial order ( $h_c \rightarrow p\bar{p}\pi^+\pi^-$ signal)	$5.0\sigma$	$0.9\sigma$	$12.2\sigma$	$5.9\sigma$
Fitting range variation ( $h_c \rightarrow \eta_c \gamma$ )	$5.0\sigma$	$0.9\sigma$	$12.3\sigma$	$5.9\sigma$
Fitting range variation ( $h_c \rightarrow p\bar{p}\pi^+\pi^-$ )	$5.0\sigma$	$0.8\sigma$	$12.1\sigma$	$5.8\sigma$
Scaled resolution	$5.0\sigma$	$0.8\sigma$	$12.3\sigma$	$6.0\sigma$
Fraction of $h_c \rightarrow \eta_c \gamma$ and $h_c \rightarrow p\bar{p}\pi^+\pi^-$	$4.9\sigma$	$0.7\sigma$	$12.2\sigma$	$5.9\sigma$

Branching fraction	Value or confidence interval (90 % C. L.)	World-average value
$\mathcal{B}(B^+ \rightarrow h_c K^+)$	$(3.7^{+1.0+0.8}_{-0.9-0.8}) \times 10^{-5}$	$< 3.8 \times 10^{-5}$
$\mathcal{B}(B^+ \rightarrow \eta_c K^+) \times \mathcal{B}(\eta_c \rightarrow p\bar{p}\pi^+\pi^-)$	$(39.4^{+4.1+2.2}_{-3.9-1.8}) \times 10^{-7}$	$(57.8 \pm 20.2) \times 10^{-7}$
$\mathcal{B}(B^+ \rightarrow J/\psi K^+) \times \mathcal{B}(J/\psi \rightarrow p\bar{p}\pi^+\pi^-)$	$(56.4^{+3.3+2.7}_{-3.2-2.5}) \times 10^{-7}$	$(60.6 \pm 5.3) \times 10^{-7}$
$\mathcal{B}(B^+ \rightarrow \chi_{c0} K^+) \times \mathcal{B}(\chi_{c0} \rightarrow p\bar{p}\pi^+\pi^-)$	$(3.7^{+1.2+0.2}_{-1.0-0.3}) \times 10^{-7}$	$(3.1 \pm 1.1) \times 10^{-7}$
$\mathcal{B}(B^+ \rightarrow \chi_{c1} K^+) \times \mathcal{B}(\chi_{c1} \rightarrow p\bar{p}\pi^+\pi^-)$	$(4.7^{+1.3+0.4}_{-1.2-0.2}) \times 10^{-7}$	$(2.4 \pm 0.9) \times 10^{-7}$
$\mathcal{B}(B^+ \rightarrow \chi_{c2} K^+) \times \mathcal{B}(\chi_{c2} \rightarrow p\bar{p}\pi^+\pi^-)$	$< 1.9 \times 10^{-7}$	$(0.15 \pm 0.06) \times 10^{-7}$
$\mathcal{B}(B^+ \rightarrow \eta_c(2S) K^+) \times \mathcal{B}(\eta_c(2S) \rightarrow p\bar{p}\pi^+\pi^-)$	$(11.2^{+1.8+0.5}_{-1.6-0.7}) \times 10^{-7}$	not seen
$\mathcal{B}(B^+ \rightarrow \psi(2S) K^+) \times \mathcal{B}(\psi(2S) \rightarrow p\bar{p}\pi^+\pi^-)$	$(4.7^{+1.2+0.3}_{-1.1-0.3}) \times 10^{-7}$	$(3.7 \pm 0.3) \times 10^{-7}$
$\mathcal{B}(B^0 \rightarrow h_c K_S^0)$	$< 1.4 \times 10^{-5}$	not seen
$\mathcal{B}(B^0 \rightarrow \eta_c K_S^0) \times \mathcal{B}(\eta_c \rightarrow p\bar{p}\pi^+\pi^-)$	$(19.0^{+3.2+1.3}_{-2.9-4.7}) \times 10^{-7}$	$(20.9 \pm 7.8) \times 10^{-7}$
$\mathcal{B}(B^0 \rightarrow J/\psi K_S^0) \times \mathcal{B}(J/\psi \rightarrow p\bar{p}\pi^+\pi^-)$	$(24.3^{+2.3+1.2}_{-2.2-1.3}) \times 10^{-7}$	$(26.2 \pm 2.4) \times 10^{-7}$
$\mathcal{B}(B^0 \rightarrow \chi_{c0} K_S^0) \times \mathcal{B}(\chi_{c0} \rightarrow p\bar{p}\pi^+\pi^-)$	$< 1.3 \times 10^{-7}$	$(1.5 \pm 0.6) \times 10^{-7}$
$\mathcal{B}(B^0 \rightarrow \chi_{c1} K_S^0) \times \mathcal{B}(\chi_{c1} \rightarrow p\bar{p}\pi^+\pi^-)$	$(3.7^{+1.2+0.3}_{-1.0-0.2}) \times 10^{-7}$	$(1.0 \pm 0.4) \times 10^{-7}$
$\mathcal{B}(B^0 \rightarrow \chi_{c2} K_S^0) \times \mathcal{B}(\chi_{c2} \rightarrow p\bar{p}\pi^+\pi^-)$	$[0.7, 3.8] \times 10^{-7}$	not seen
$\mathcal{B}(B^0 \rightarrow \eta_c(2S) K_S^0) \times \mathcal{B}(\eta_c(2S) \rightarrow p\bar{p}\pi^+\pi^-)$	$(4.2^{+1.4+0.3}_{-1.2-0.3}) \times 10^{-7}$	not seen
$\mathcal{B}(B^0 \rightarrow \psi(2S) K_S^0) \times \mathcal{B}(\psi(2S) \rightarrow p\bar{p}\pi^+\pi^-)$	$[0.6, 3.9] \times 10^{-7}$	$(1.7 \pm 0.2) \times 10^{-7}$