

13<sup>th</sup> International Workshop on Heavy Quarkonium (QWG2019),  
13–17 May 2019, Torino

# Update on $e^+e^- \rightarrow \Upsilon(nS) \pi^+\pi^-$ scan at Belle

*arxiv:1905.05521*

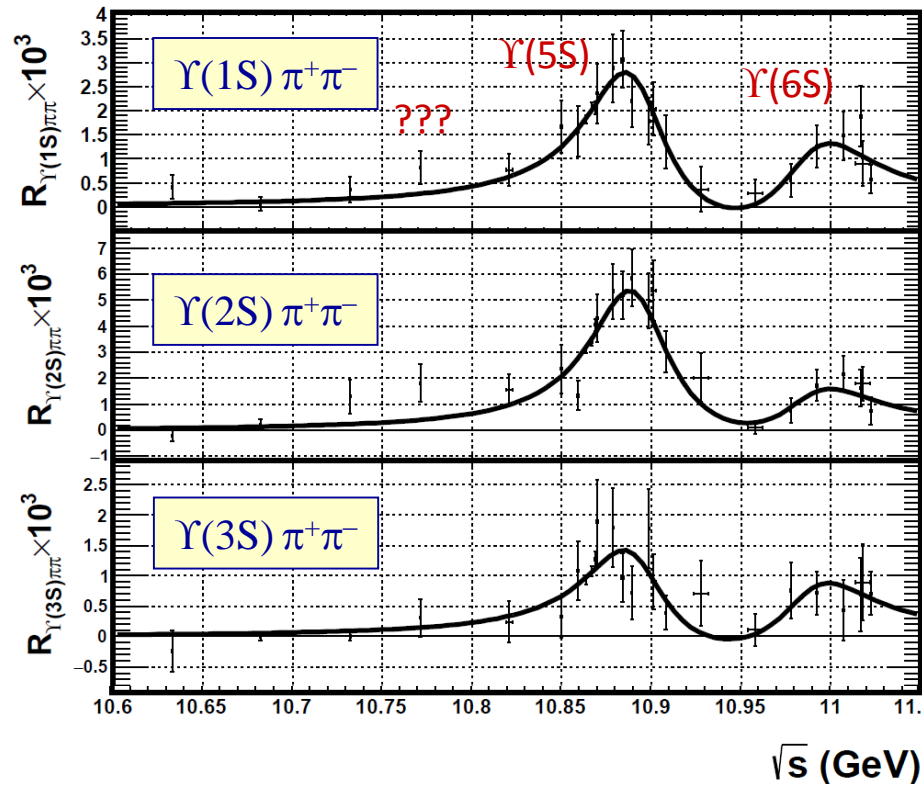


Roman Mizuk

Lebedev Physical Institute, Moscow

# Previous measurement

Belle PRD93,011101(2016)



Clear signals of  $\Upsilon(5S)$ ,  $\Upsilon(6S)$ . Excess near 10.77 GeV ?

Which vector states are expected in this energy range?

$\Upsilon(3D)$  mixed with  $\Upsilon(4S,5S)$  mixing could be enhanced due to hadron loops

Exotic states: hadrobottomonia, compact tetraquarks

⇒ Motivation for update.

Badalian,Bakker,Danilkin  
PAN73,138(2010)

# Changes in the new measurement

The same data samples, improvements in the analysis:

## PREVIOUS

Use more decay channels

$$\Upsilon(nS) \rightarrow \mu^+ \mu^-$$

Improve statistical treatment of data

Count events in the signal and  
sideband regions with  
1/Efficiency weights

## NEW

$$\Upsilon(nS) \rightarrow \mu^+ \mu^- \text{ and } e^+ e^-$$

Find signal yield from a fit,  
then apply efficiency correction

Need 3-body matrix element to  
generate MC PRD91,072003(2015)

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accuracy is improved by a factor  $\sim 1.3$

Use ISR in high statistics  
 $\Upsilon(5S)$  on-resonance data  
to study cross section  
energy dependence

# Data samples

Scan data: 22 points  $\times 1 \text{ fb}^{-1}$

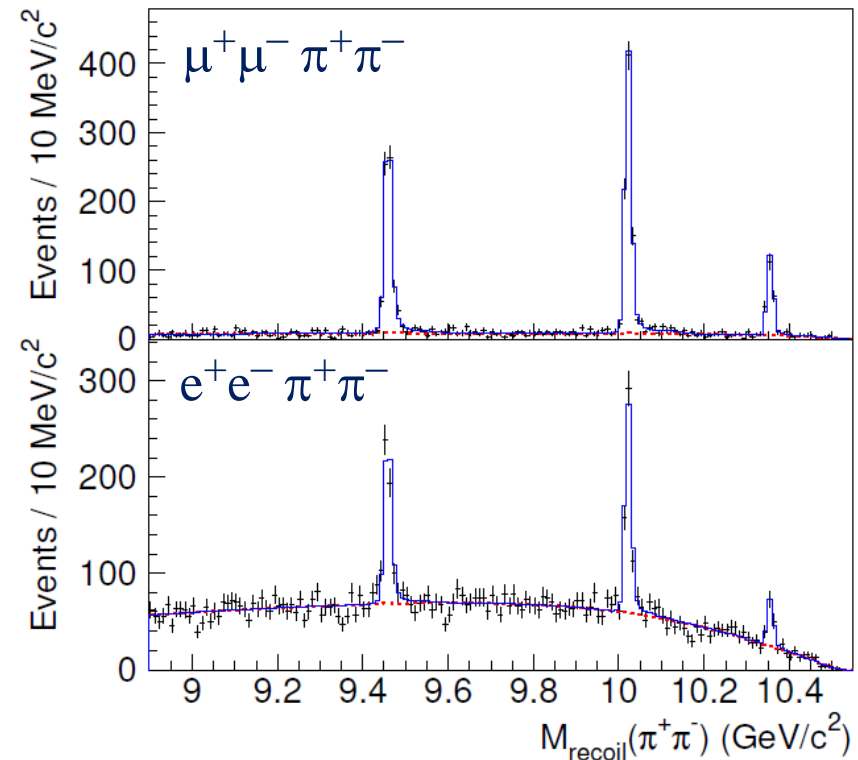
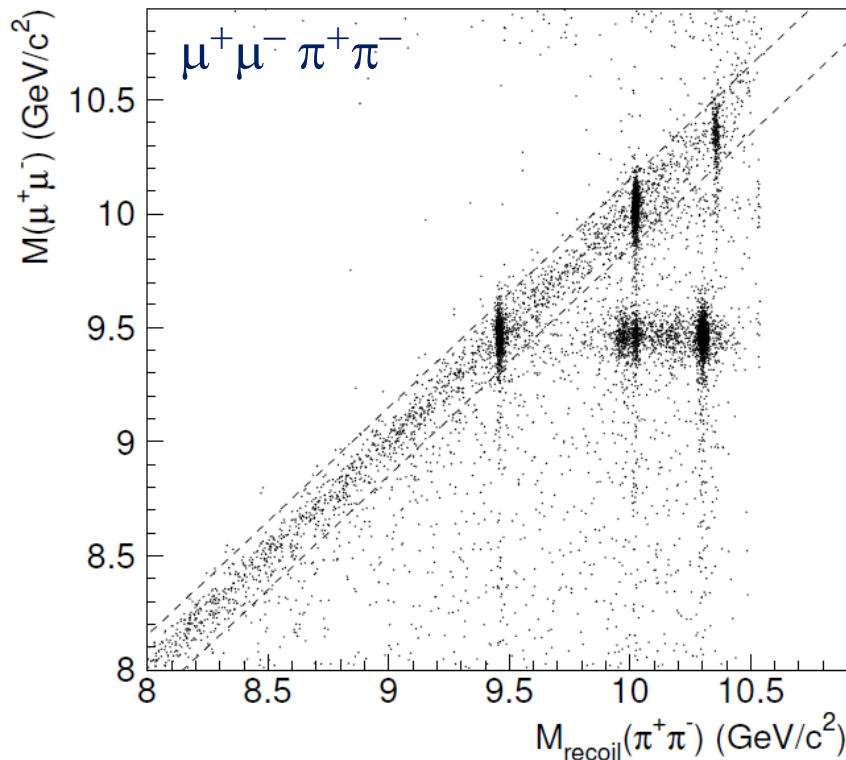
$\Upsilon(5S)$  on-resonance data:  $121 \text{ fb}^{-1}$  at 5 points,  $E_{\text{max}} - E_{\text{min}} = 3 \text{ MeV}$

Continuum data,  $10.52 \text{ GeV}$ :  $61 \text{ fb}^{-1}$

## Selection requirements

$\mu^+\mu^-\pi^+\pi^- / e^+e^-\pi^+\pi^-$  require PID, energy balance;  
extra in  $e^+e^-$  channel:  $M_{\text{recoil}}(e^+e^-) > 350 \text{ MeV}$ ,  $\cos\theta_{e^-} < 0.82$

Background: QED  
production of 4 tracks



# Signal shape in $M_{\text{recoil}}(\pi^+\pi^-)$

## Calculation scheme

Momentum resolution

includes effects of

- FSR
- decays-in-flight
- secondary interactions

$\otimes$

ISR

Kuraev-Fadin radiator function

$\times \sigma(E_{\text{cm}})$

$\times \varepsilon(E\gamma_{\text{ISR}})$

$\otimes$  Ecm spread

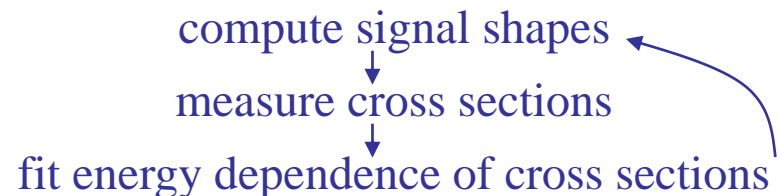
Gaussian  $\times \sigma(E_{\text{cm}})$

5.4 MeV

$\times$   $\varepsilon$  of energy balance requirement

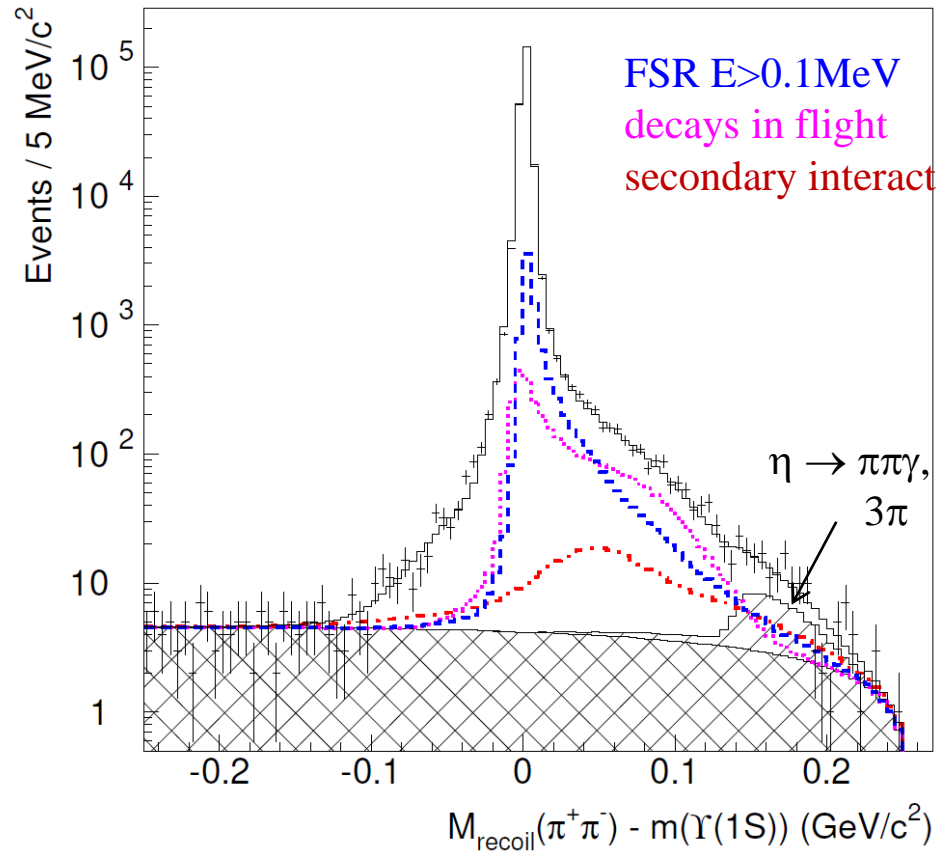
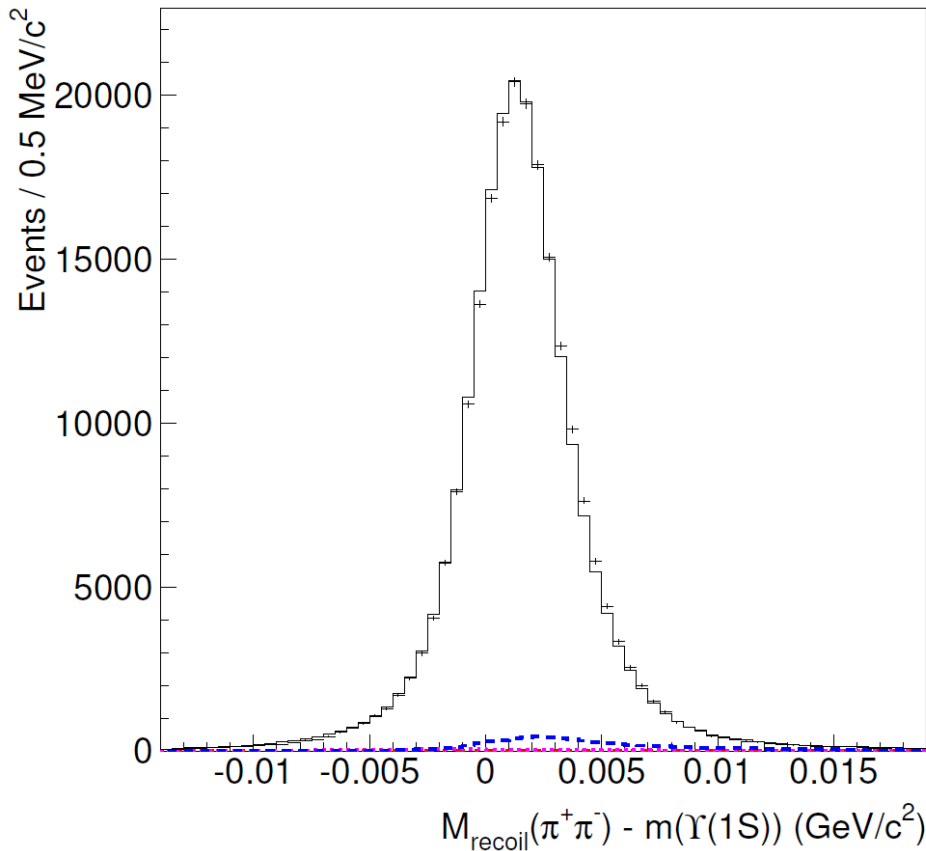
soft cut-off at  $\sim 200$  MeV

$\sigma(E_{\text{cm}})$  is being measured  $\Rightarrow$  iterations



# Verification of signal shape

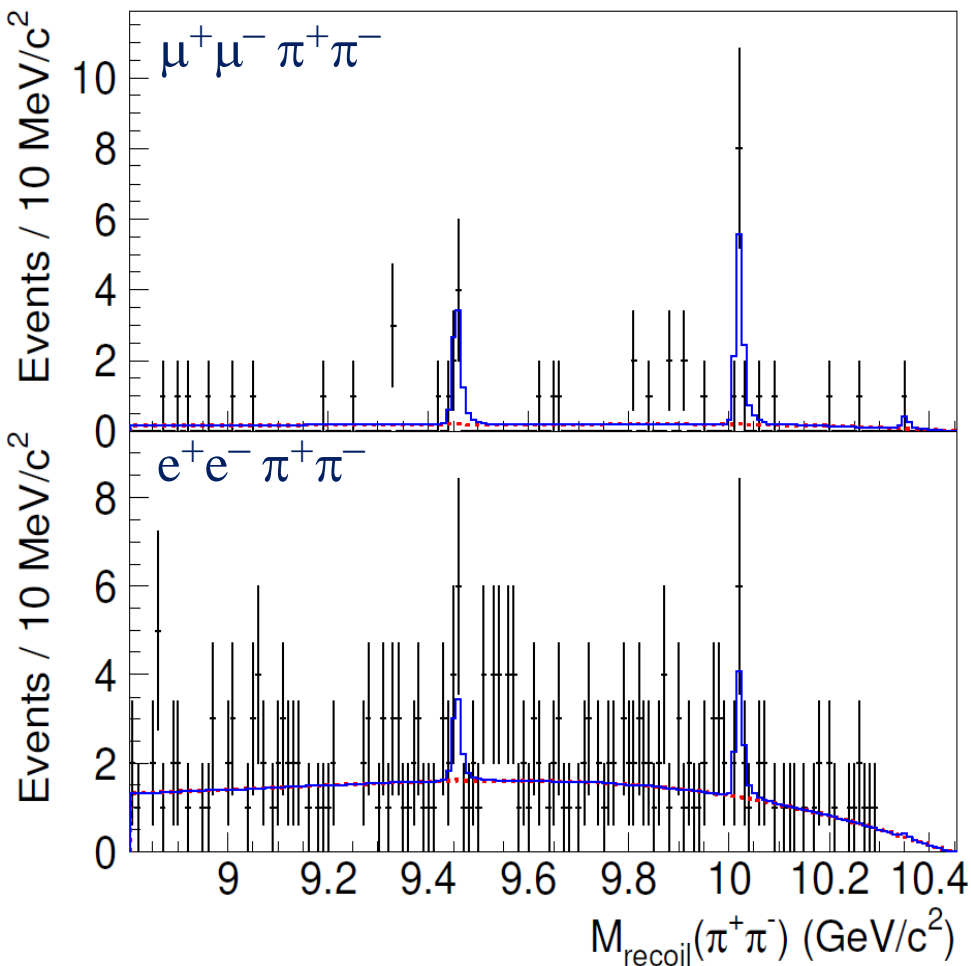
$\Upsilon(2S)$  data  $24\text{fb}^{-1}$      $\Upsilon(2S)$  is narrow  $\Rightarrow$  no contributions of ISR and energy spread



Shapes from MC; floated parameters are yield, overall shift and momentum resolution fudge factor  $f = 1.160 \pm 0.003$

Use  $\Upsilon(3S)$  data  $3\text{fb}^{-1}$  to study energy dependence of  $f \Rightarrow$  constant

# Fit to $M_{\text{recoil}}(\pi^+\pi^-)$



Signal:

fix ratio of  $ee/\mu\mu$  yields,  
float  $\mu\mu$  yields and overall shift  
 $\Rightarrow E_{\text{cm}}$  calibration

Non-peaking background:

$$B(x) = A (x - x_0)^p P_3(x)$$

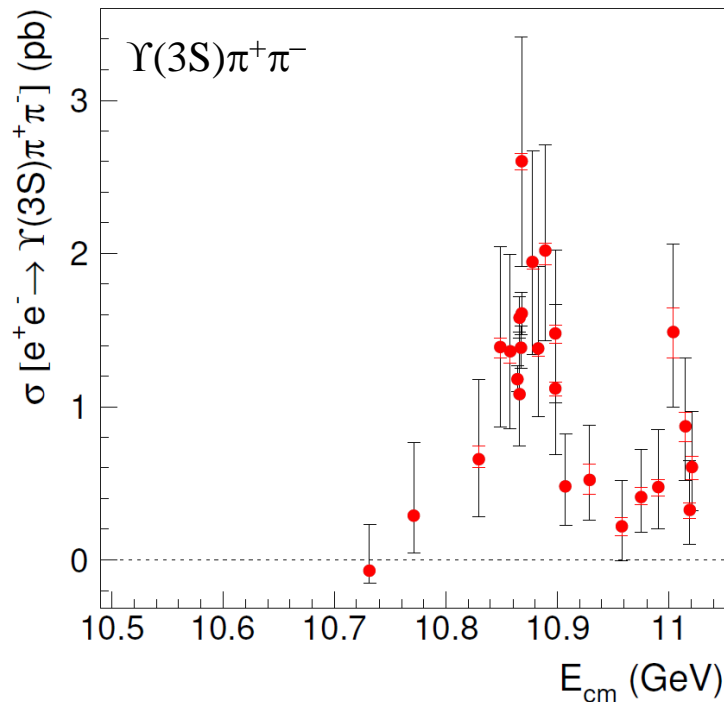
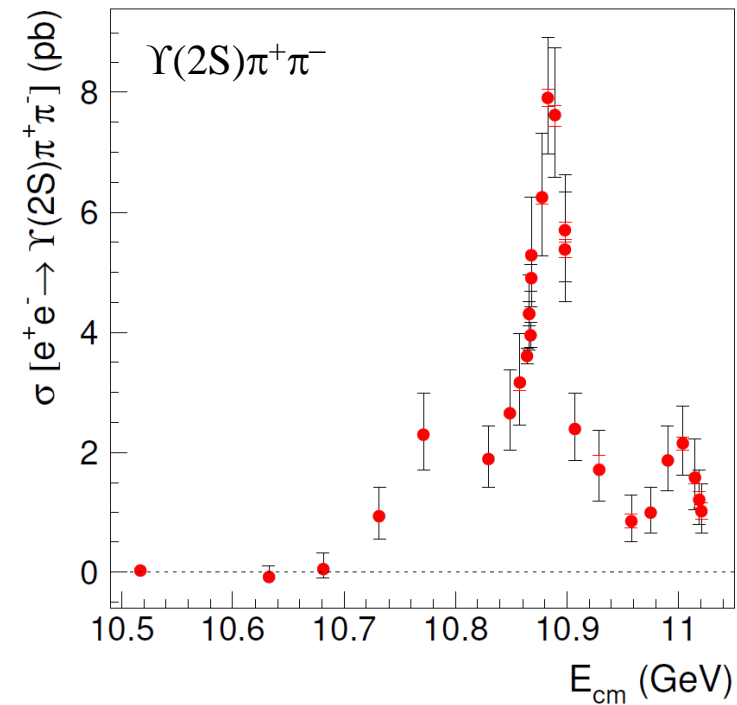
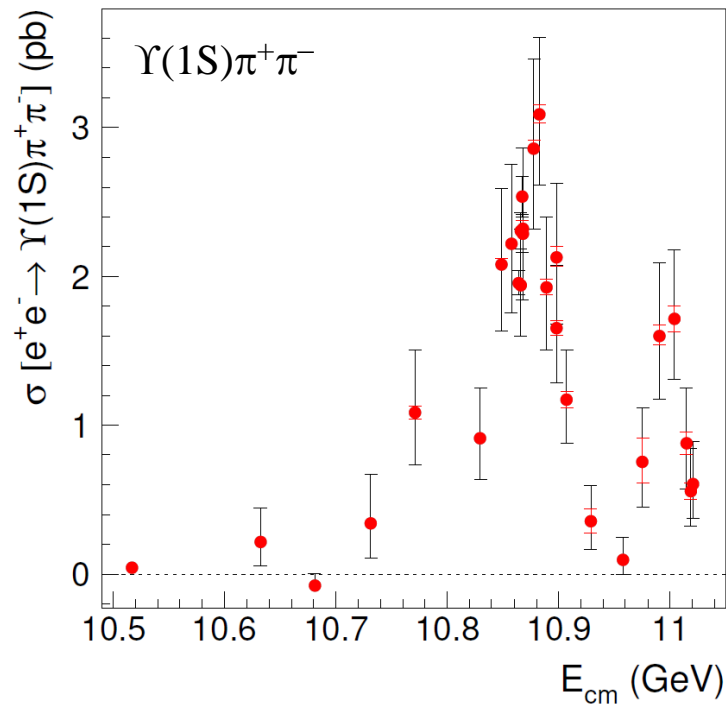
Peaking background:

$$\text{e.g. } e^+e^- \rightarrow \gamma^*\gamma^* \rightarrow \Upsilon(nS) \pi^+\pi^- \rightarrow \mu^+\mu^-$$

from MC, small contribution

Shamov et al., to be published in  
proceedings of PhiPsi 2019

# Born cross sections



errors: stat. , uncor. syst.

Clear signals of  $\Upsilon(5S)$ ,  $\Upsilon(6S)$ ;  
new structure near 10.77 GeV ?



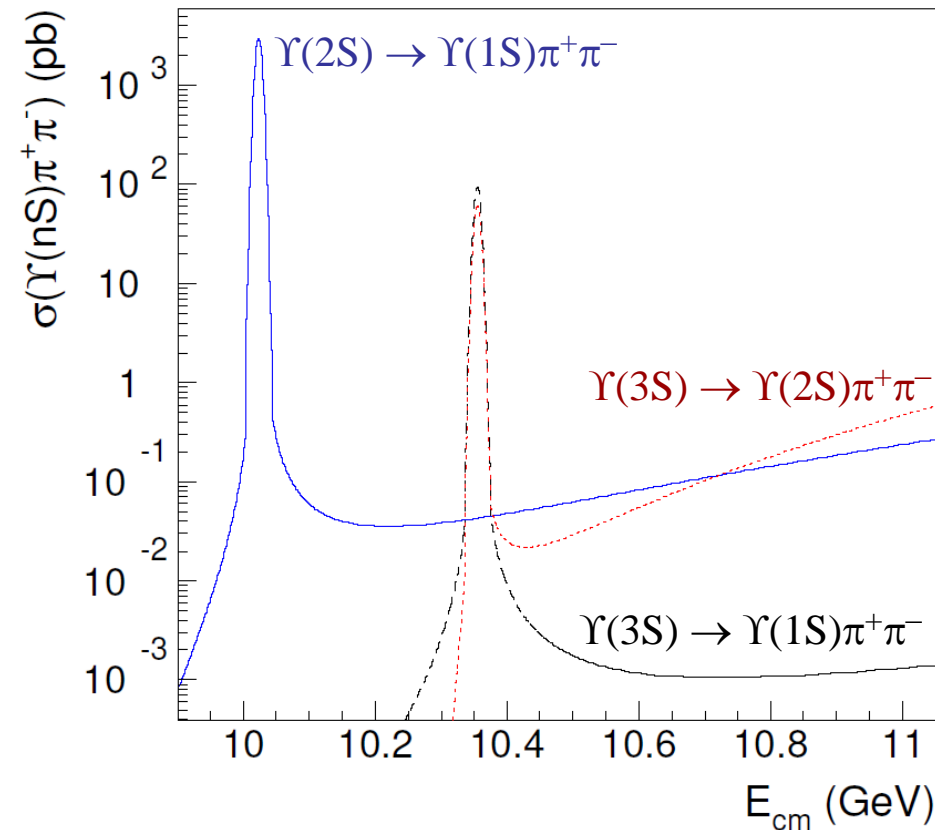
# Continuum below $\Upsilon(4S)$

Hints for non-zero values:

$$\sigma[e^+e^- \rightarrow \Upsilon(1S)\pi^+\pi^-] = 40_{-19}^{+21} \text{ fb}$$

$$\sigma[e^+e^- \rightarrow \Upsilon(2S)\pi^+\pi^-] = 25_{-25}^{+29} \text{ fb}$$

What could be the origin?



Expectations:

$$e^+e^- \rightarrow \Upsilon(2S) \rightarrow \Upsilon(1S)\pi^+\pi^- = 71 \text{ fb}$$

$$e^+e^- \rightarrow \Upsilon(3S) \rightarrow \Upsilon(1S)\pi^+\pi^- = 2 \text{ fb}$$

$$e^+e^- \rightarrow \Upsilon(3S) \rightarrow \Upsilon(2S)\pi^+\pi^- = 35 \text{ fb}$$

$\Leftarrow$  BW with  $M, \Gamma, \Gamma_{ee}, B_f$  from PDG.

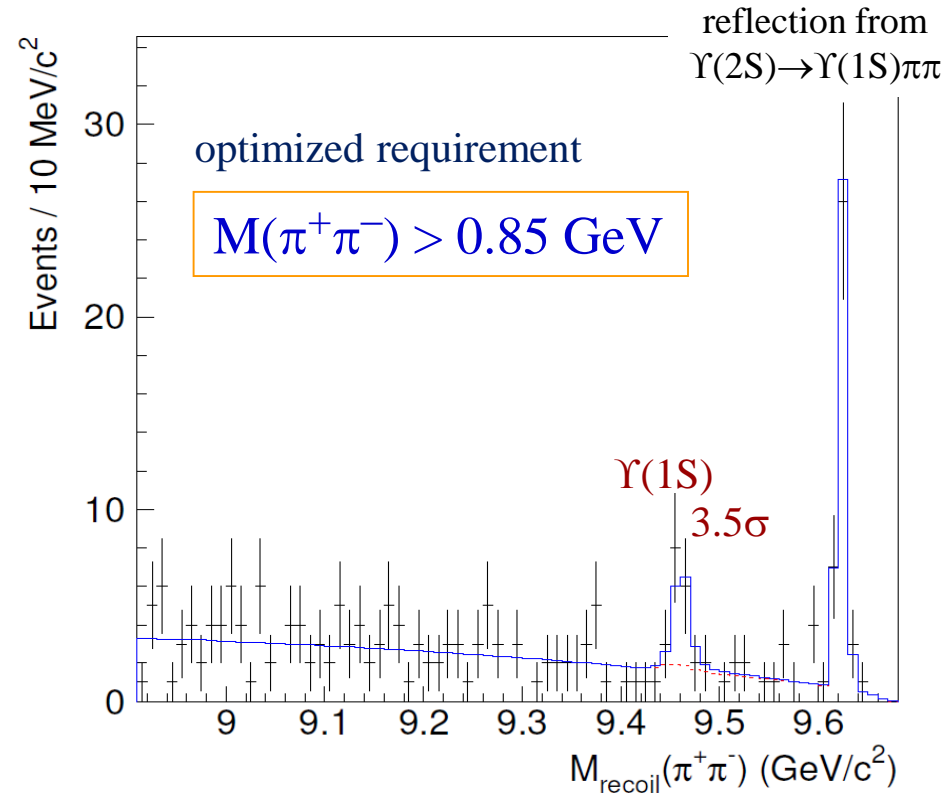
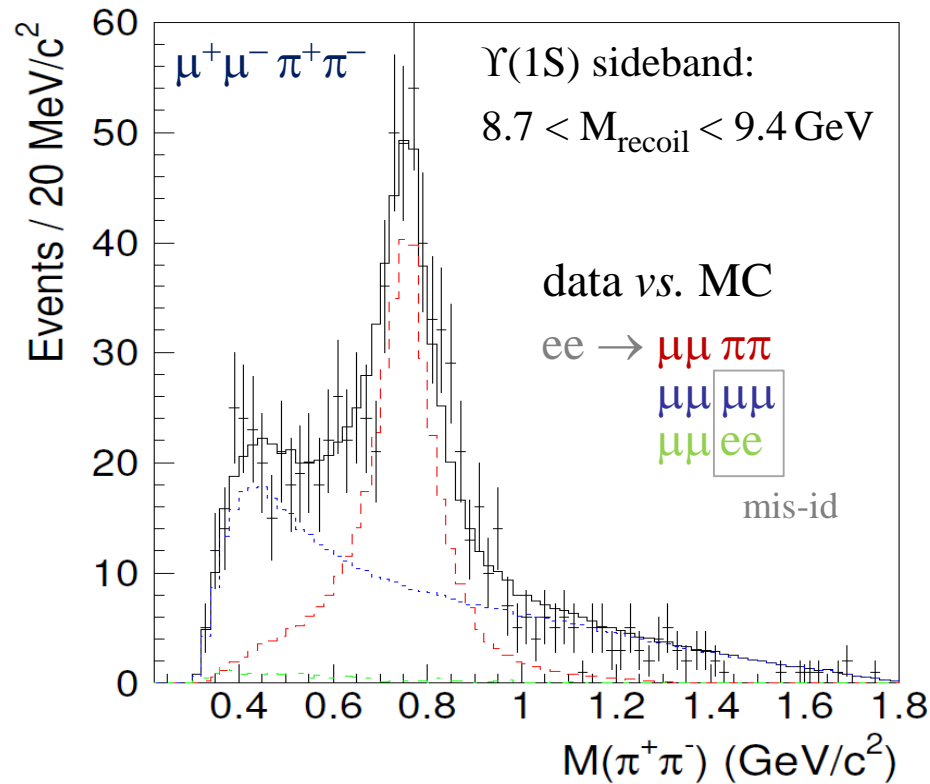
$\Gamma_f(s)$  : integrate ME over Dalitz plot.

ME rapidly increase with  $M(\pi^+\pi^-) \Rightarrow$   
BW tails increase with energy

$\Rightarrow$  Large contributions at high energy

# Continuum below $\Upsilon(4S)$

$M(\pi^+\pi^-)$  distribution: distinguish signal from background



$$\sigma[e^+e^- \rightarrow \Upsilon(1S)\pi^+\pi^-] =$$

with  $M(\pi\pi)$  cut

$$42^{+17}_{-15} \text{ fb}$$

stat.

w/o  $M(\pi\pi)$  cut

$$40^{+21}_{-19} \text{ fb}$$

agree

Evidence for  $e^+e^- \rightarrow \Upsilon(1S)\pi^+\pi^-$  in  
 continuum at  $E_{\text{cm}} = 10.52 \text{ GeV}$ .

# Fit to energy dependence of cross sections

## Fit function

$$|\text{BW}_{\Upsilon(5S)}^{(n)} + e^{i\alpha_n} \text{BW}_{\Upsilon(6S)}^{(n)} + e^{i\beta_n} \text{BW}_{\text{new}}^{(n)} + e^{i\gamma_n} \text{BW}_{\Upsilon((n+1)S)}^{(n)}|^2 \otimes \text{Gaussian}$$

The new structure might have resonant or non-resonant origin.

The two effects are difficult to distinguish  $\Leftarrow$  similar line shape, phase motion.

$\Rightarrow$  Breit-Wigner – reasonable approximation in both cases.

Bugg EPL96,11002(2011)

...

*we do not claim that the new structure is a resonance*

$$\text{BW}(s, M, \Gamma, \Gamma_{ee}^0 \times \mathcal{B}_f) = \frac{\sqrt{12\pi} \Gamma \Gamma_{ee}^0 \times \mathcal{B}_f}{s - M^2 + iM\Gamma} \sqrt{\frac{\Gamma_f(s)}{\Gamma_f(M^2)}}$$

Floated parameters:  $M, \Gamma$  for  $\Upsilon(5S), \Upsilon(6S),$  new structure  
 $\Gamma_{ee}^0 \times \mathcal{B}_f, \text{ complex phases}$  for all contributions, for all channels

# Fit

default

w/o new structure

$\Upsilon(4S)$  is shown  
for illustration

New structure

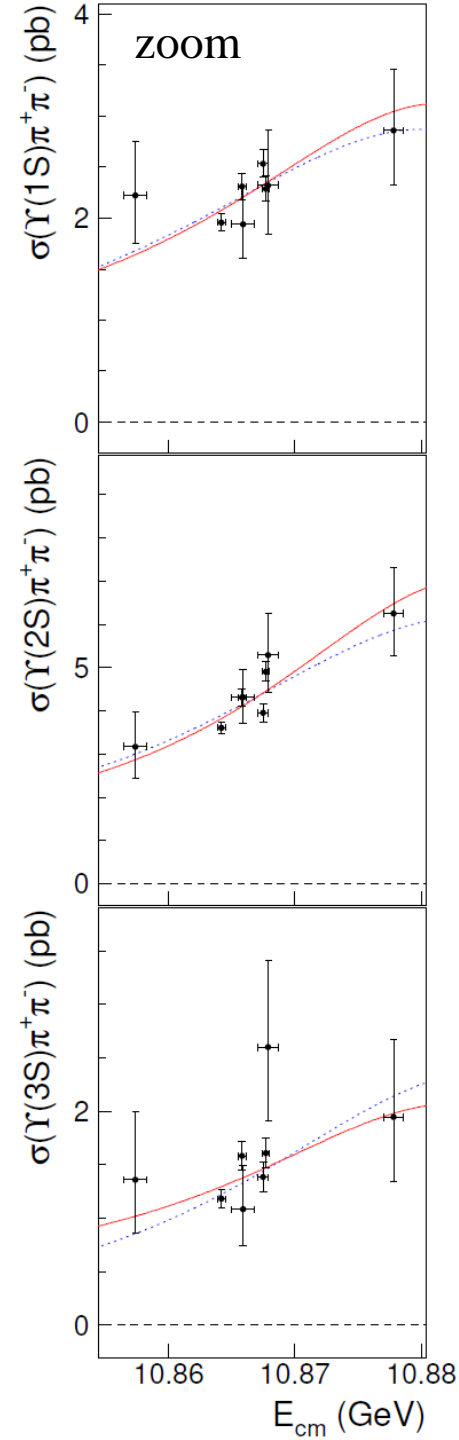
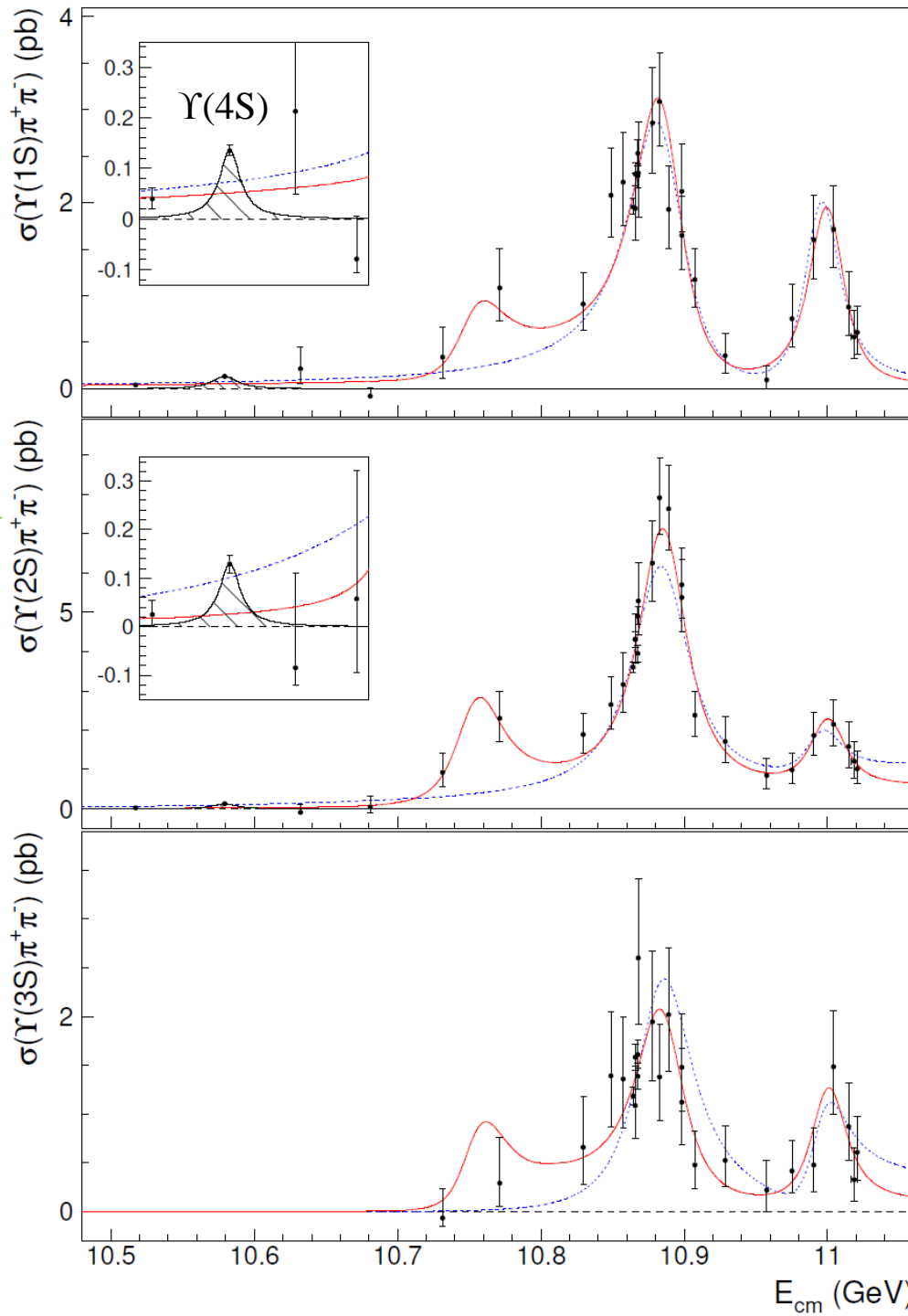
$\Upsilon(1S)\pi\pi$   $2.4\sigma$

$\Upsilon(2S)\pi\pi$   $5.3\sigma$

w/ syst.

Combined  
global  
significance

w/ syst.  $6.7\sigma$



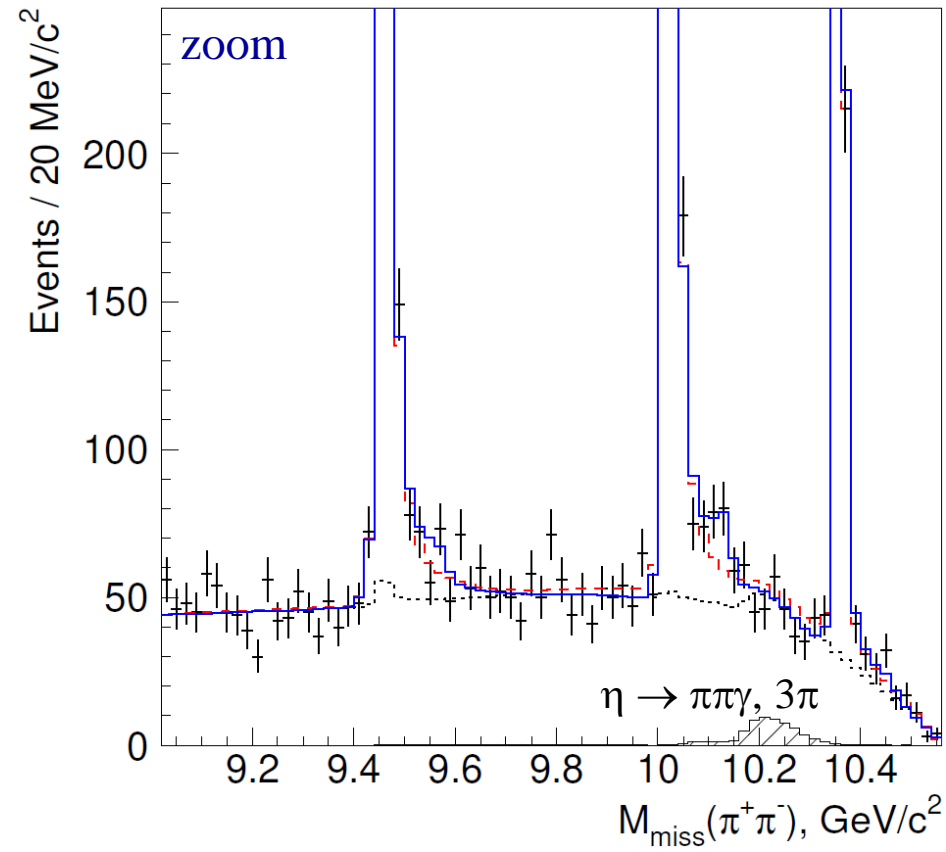
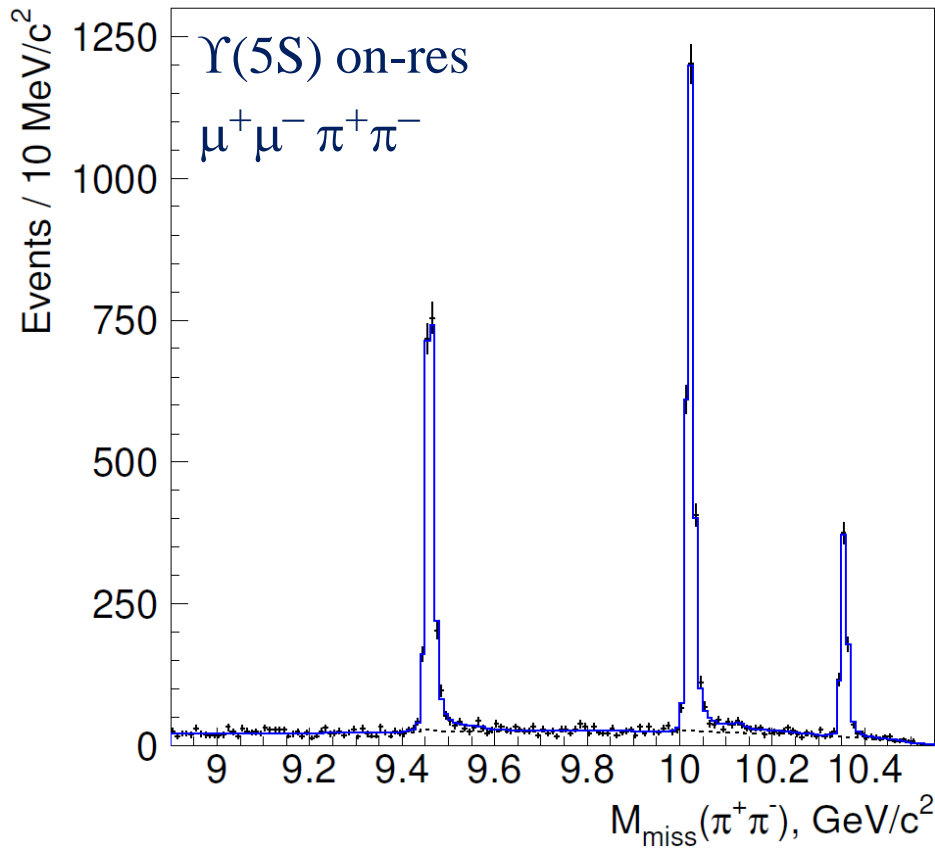
# Fit

ISR tails of the  $\Upsilon(nS)\pi\pi$  signals are sensitive to the cross section shapes.  
 $\Rightarrow$  Include the  $M_{\text{recoil}}(\pi^+\pi^-)$  distribution into the fit.

*simultaneous fit to the cross sections and  $M_{\text{recoil}}(\pi^+\pi^-)$*

default

w/o new structure



Excellent description of ISR tails.

# Fit results

	$\Upsilon(10860)$	$\Upsilon(11020)$	new structure
$M \text{ (MeV}/c^2)$	$10885.3 \pm 1.5^{+2.2}_{-0.9}$	$11000.0^{+4.0}_{-4.5} {}^{+1.0}_{-1.3}$	$10752.7 \pm 5.9^{+0.7}_{-1.1}$
$\Gamma \text{ (MeV)}$	$36.6^{+4.5}_{-3.9} {}^{+0.5}_{-1.1}$	$23.8^{+8.0}_{-6.8} {}^{+0.7}_{-1.8}$	$35.5^{+17.6}_{-11.3} {}^{+3.9}_{-3.3}$

Previous  
measurement

$$10891.1 \pm 3.2^{+0.6}_{-1.7}$$

$$53.7^{+7.1}_{-5.6} {}^{+1.3}_{-5.4}$$

$$10987.5^{+6.4}_{-2.5} {}^{+9.0}_{-2.1}$$

$$61^{+9}_{-19} {}^{+2}_{-20}$$

PRD93,011101(2016)

many differences, e.g.  
model: new structure, tails  
 $\sigma^{\text{vis}} \Leftrightarrow \sigma^{\text{B}}$

C.f.  $h_b\pi\pi$

$$10884.7^{+3.6}_{-3.4} {}^{+8.9}_{-1.0}$$

$$40.6^{+12.7}_{-8.0} {}^{+1.1}_{-19.1}$$

$$10999.0^{+7.3}_{-7.8} {}^{+16.9}_{-1.0}$$

$$27^{+27}_{-11} {}^{+5}_{-12}$$

PRL117,142001(2016)

good agreement

# Branching fractions

Multiple solutions: sum of N BW amplitudes –  $2^{N-1}$  solutions (4 or 8 in our case)

		$\Gamma_{ee} \times \mathcal{B}$ (in eV)		
		$\Upsilon(10860)$	$\Upsilon(11020)$	new
Ranges: min – max	$\Upsilon(1S)\pi^+\pi^-$	0.75 – 1.43	0.38 – 0.54	0.12 – 0.47
	$\Upsilon(2S)\pi^+\pi^-$	1.35 – 3.80	0.13 – 1.16	0.53 – 1.22
	$\Upsilon(3S)\pi^+\pi^-$	0.43 – 1.03	0.17 – 0.49	0.21 – 0.26

$\Upsilon(4S)$

Belle PRD96,052005(2017)

Implications?

$$\mathcal{B}(\Upsilon(4S) \rightarrow \Upsilon(1S)\pi^+\pi^-) = (8.2 \pm 0.5 \pm 0.4) \times 10^{-5}$$

$$\mathcal{B}(\Upsilon(4S) \rightarrow \Upsilon(2S)\pi^+\pi^-) = (7.9 \pm 1.0 \pm 0.4) \times 10^{-5}$$

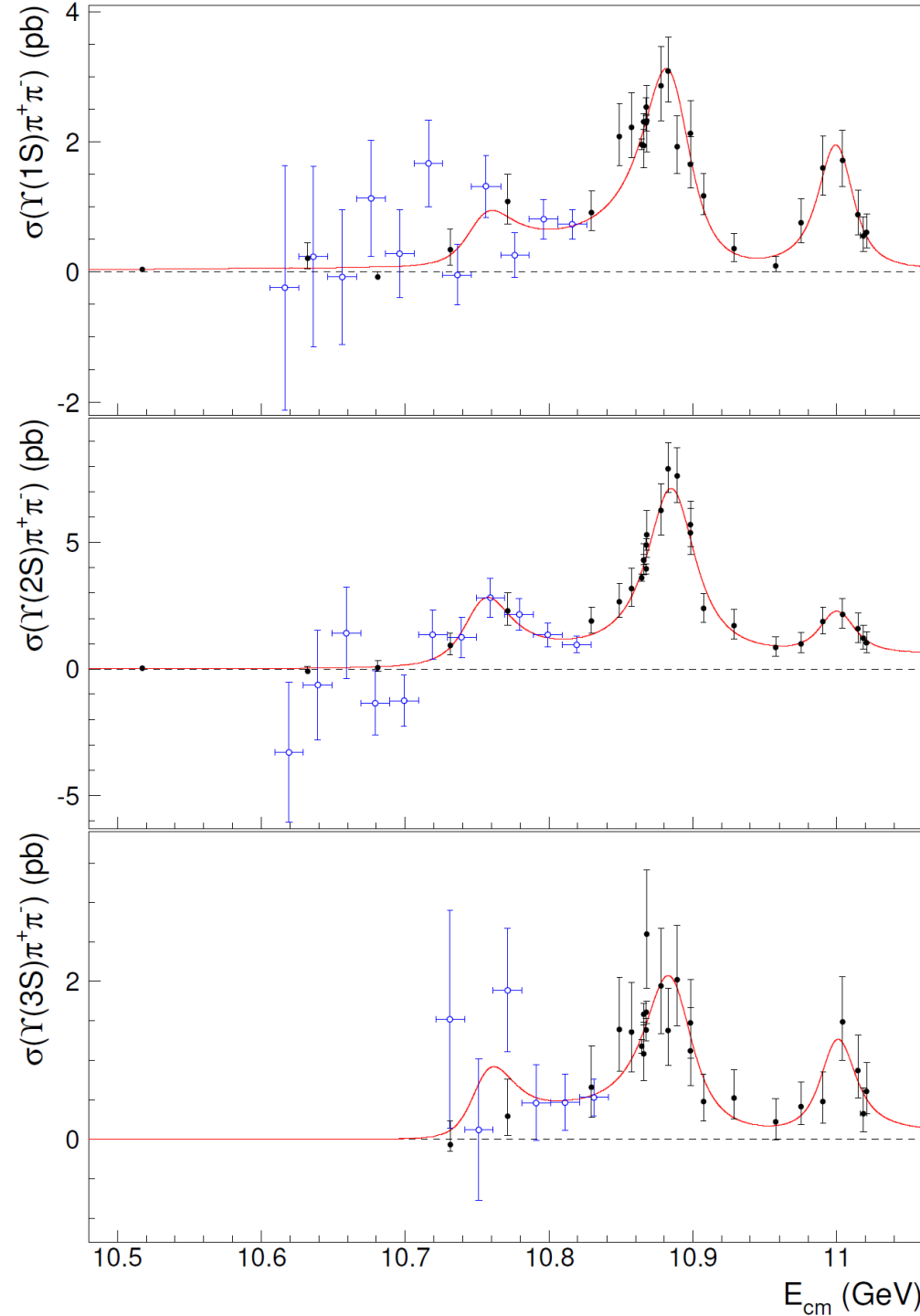
Include  $\Upsilon(4S)$  in the fit, scan FCN in  $B \Rightarrow$   $(1.2 - 16) \times 10^{-5}$  67% C.L.  
 $(1.3 - 9.6) \times 10^{-5}$

# Visualization

Blue points: cross sections  
estimated using ISR tails

Not to be used in the fit:

1. Stat. errors only.
2. ISR luminosity changes rapidly  
w/ energy  $\Rightarrow$  difficult to estimate  
effects of spread & resolution.





# Conclusions

Observation of new structure

$$M = 10752.7 \pm 5.9^{+0.7}_{-0.4} \text{ MeV}$$

$$\Gamma = 35.5^{+17.6}_{-11.3} \pm 3.4 \text{ MeV}$$

Global significance including systematics:  $6.7\sigma$ .

arxiv:1905.05521

Evidence for  $e^+e^- \rightarrow \Upsilon(1S) \pi^+\pi^-$  at  $E_{\text{cm}} = 10.52 \text{ GeV}$

– implications for  $\text{BF}[\Upsilon(4S) \rightarrow \Upsilon(1,2S) \pi^+\pi^-]$

All results are preliminary

Interpretation?

Resonance?  $\Upsilon(3D)$ , exotics,...

Non-resonant effect? Complicated rescattering,...

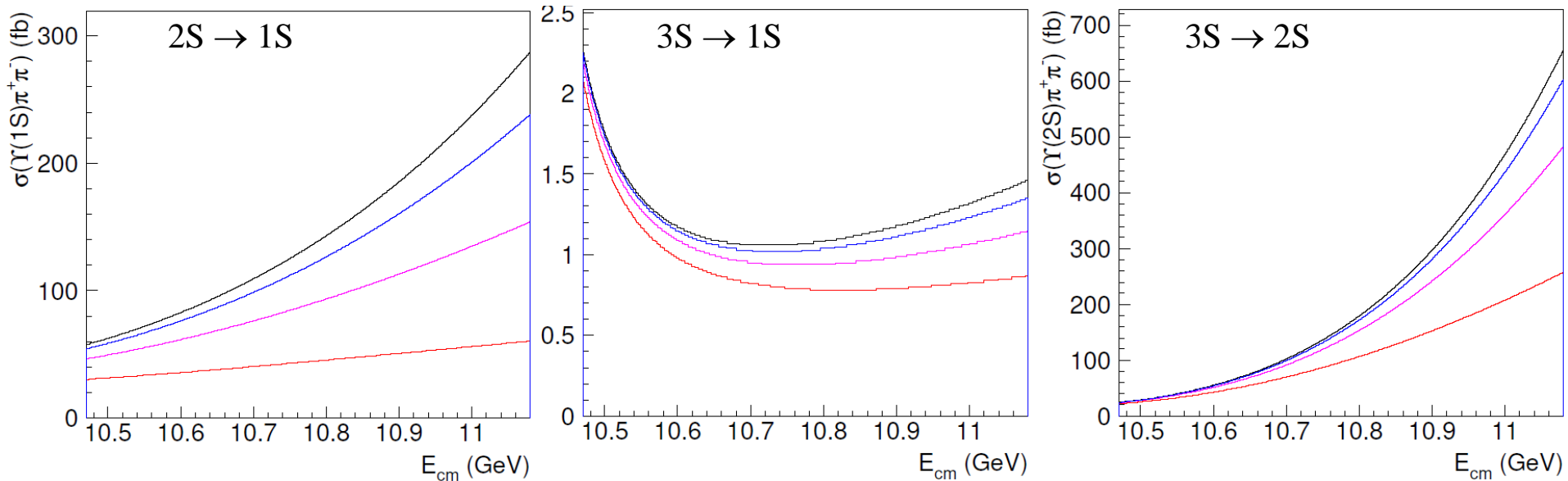
Need information on other channels to clarify the origin.

Back-up

# Tails

Matrix elements of  $\Upsilon(2S,3S) \rightarrow \Upsilon(1S,2S)\pi^+\pi^-$  have terms proportional to  $M^2(\pi^+\pi^-)$

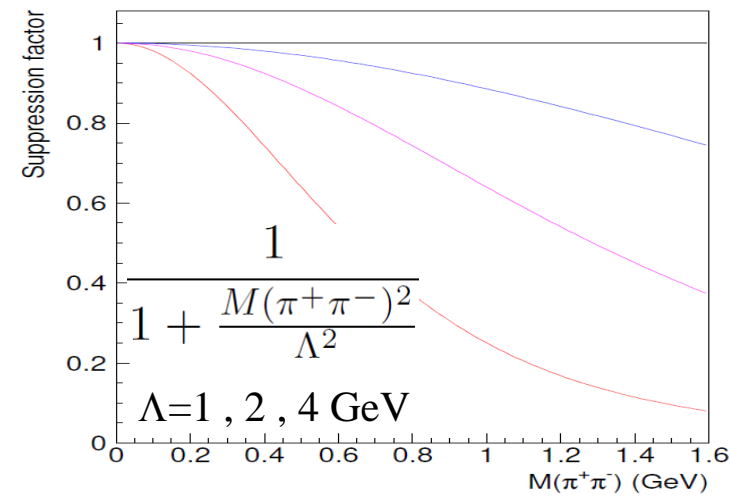
⇒ Contributions rise quickly as PHSP grows with c.m. energy



Why could there be deviations from these estimations?

M. Voloshin: high  $M(\pi^+\pi^-)$  could be suppressed due to some form factor

$\Upsilon(5S) \rightarrow \Upsilon(1S)\pi^+\pi^-$  - no sign of suppression



# Global significance

Exclude new structure in all channels:  $\Delta(-2\ln L) = 66$ .

52. – cross sections

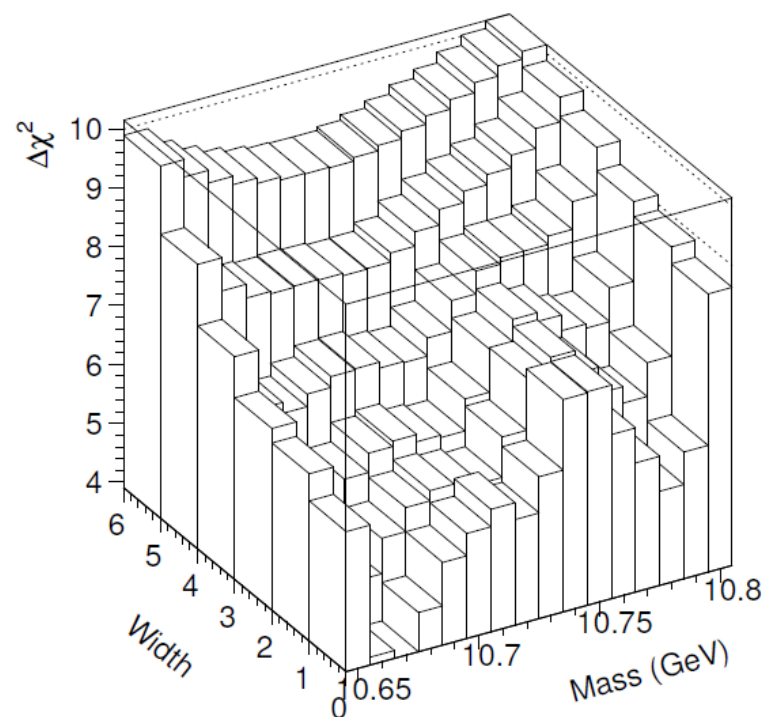
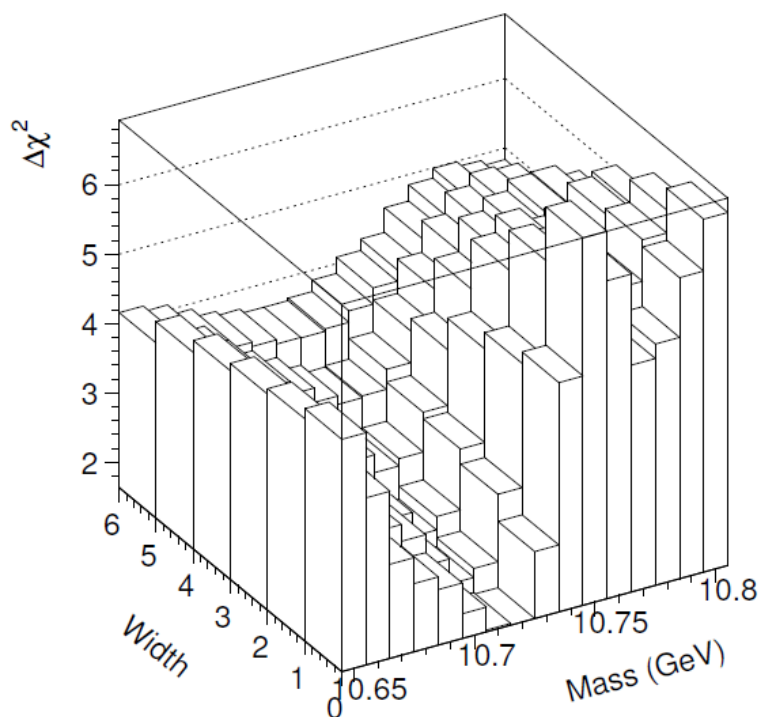
14. – recoil mass

global?

local significance  $7.0\sigma$

Astropart. Phys. **35**, 230 (2011)

Gross-Vitells: toy MC, scan  $\Delta(-2\ln L)$  in  $M, \Gamma$  ( $=30,40,50,70,100,150$  MeV)



Euler characteristic

$$p = \chi_6^2(u) + e^{-u/2} u^2 (A \sqrt{u} + B(u - 5))$$

“Look elsewhere effect”: p-value  $\times 4.5$ , global significance  $6.8\sigma$

w/ syst.  
 $6.7\sigma$