



# $\eta'_c$ HADROPRODUCTION AT NLO AND ITS RELEVANT TO $\psi'$ PRODUCTION

HUA-SHENG SHAO



QUARKONIUM 2019, TORINO  
14 MAY 2019

# MOTIVATION

- Why we are interested in  $\eta_{c,b}$  and  $h_{c,b}$ ?

# MOTIVATION

- Why we are interested in  $\eta_{c,b}$  and  $h_{c,b}$ ?
- Test heavy quark spin symmetry Bodwin, Braaten, Lepage (1995)

$$\eta_c \leftrightarrow J/\psi$$

$$h_c \leftrightarrow \chi_c$$

$$\langle \mathcal{O}^{\eta_c} (^1S_0^{[1,8]}) \rangle = \langle \mathcal{O}^{J/\psi} (^3S_1^{[1,8]}) \rangle / 3 \quad \langle \mathcal{O}^{h_c} (^1S_0^{[8]}) \rangle = 3 \langle \mathcal{O}^{\chi_{c0}} (^3S_1^{[8]}) \rangle$$

$$\langle \mathcal{O}^{\eta_c} (^1P_1^{[8]}) \rangle = 3 \langle \mathcal{O}^{J/\psi} (^3P_0^{[8]}) \rangle \quad \langle \mathcal{O}^{h_c} (^1P_1^{[1]}) \rangle = 3 \langle \mathcal{O}^{\chi_{c0}} (^3P_0^{[1]}) \rangle$$

$$\langle \mathcal{O}^{\eta_c} (^3S_1^{[8]}) \rangle = \langle \mathcal{O}^{J/\psi} (^1S_0^{[8]}) \rangle$$

Power counting	$\eta_c, \eta_b$	$J/\psi, \psi(2S), \Upsilon$	$h_c, h_b$	$\chi_{cJ}, \chi_{bJ}$
$v^3$	$^1S_0^{[1]}$	$^3S_1^{[1]}$	—	—
$v^5$	—	—	$^1P_1^{[1]}, ^1S_0^{[8]}$	$^3P_J^{[1]}, ^3S_1^{[8]}$
$v^7$	$^1S_0^{[8]}, ^3S_1^{[8]}, ^1P_1^{[8]}$	$^1S_0^{[8]}, ^3S_1^{[8]}, ^3P_J^{[8]}$	—	—

- HQSS basically plays a central role in quarkonium physics

- In quarkonium production, we always assumed

$$\langle \mathcal{O}^{\chi_{QJ}}(^3P_J^{[1]}) \rangle = (2J + 1) \langle \mathcal{O}^{\chi_{Q0}}(^3P_0^{[1]}) \rangle$$

$$\langle \mathcal{O}^{\chi_{QJ}}(^3S_1^{[8]}) \rangle = (2J + 1) \langle \mathcal{O}^{\chi_{Q0}}(^3S_1^{[8]}) \rangle$$

$$\langle \mathcal{O}^{\psi}(^3P_J^{[8]}) \rangle = (2J + 1) \langle \mathcal{O}^{\psi}(^3P_0^{[8]}) \rangle$$

- In quarkonium polarisation, it is assumed no spin-flip for electric (like) dipole transitions

$$\hat{S}_z \left| c\bar{c} (^3S_1^{[8]}) \right\rangle = \hat{S}_z \left| \psi \right\rangle \quad \text{two E1 transitions}$$

$$\hat{S}_z \left| c\bar{c} (^3P_J^{[8]}) \right\rangle = \hat{S}_z \left| \psi \right\rangle \quad \text{an E1 transition}$$

- NRQCD velocity scaling rule tells us the above equations are violated only by higher-order in  $v^2$

## HEAVY QUARKONIUM PHYSICS

hep-ph/0412158



- It was suggested to look at  $\eta_c$  in 2004
- It was overlooked since then because of “difficult to measure”

$$\eta_c \rightarrow \gamma\gamma$$

overwhelmed by background

**Authors:** *QWG & Topic conveners:* N. Brambilla<sup>42</sup>, M. Krämer<sup>16</sup>, R. Mussa<sup>26</sup>, A. Vairo<sup>42,36</sup>;  
*Topic Conveners:* G. Bali<sup>19</sup>, G. T. Bodwin<sup>1</sup>, E. Braaten<sup>45</sup>, E. Eichten<sup>17</sup>, S. Eidelman<sup>6</sup>, S. Godfrey<sup>7</sup>,  
A. Hoang<sup>43</sup>, M. Jamin<sup>44</sup>, D. Kharzeev<sup>5</sup>, M. P. Lombardo<sup>24</sup>, C. Lourenço<sup>11</sup>, A. B. Meyer<sup>20</sup>,  
V. Papadimitriou<sup>17,58</sup>, C. Patrignani<sup>25</sup>, M. Rosati<sup>28</sup>, M. A. Sanchis-Lozano<sup>62</sup>, H. Satz<sup>4</sup>, J. Soto<sup>2</sup>;  
*Contributors:* D. Z. Besson<sup>30</sup>, D. Bettoni<sup>23</sup>, A. Böhrer<sup>55</sup>, S. Boogert<sup>37</sup>, C.-H. Chang<sup>9,29</sup>, P. Cooper<sup>17</sup>,  
P. Crochet<sup>13</sup>, S. Datta<sup>4</sup>, C. Davies<sup>19</sup>, A. Deandrea<sup>39</sup>, R. Faustov<sup>53</sup>, T. Ferguson<sup>8</sup>, R. Galik<sup>14</sup>,  
F. A. Harris<sup>21</sup>, O. Iouchtchenko<sup>11</sup>, O. Kaczmarek<sup>4</sup>, F. Karsch<sup>4</sup>, M. Kienzle<sup>18</sup>, V. V. Kiselev<sup>54</sup>,  
S. R. Klein<sup>33</sup>, P. Kroll<sup>64</sup>, A. Kronfeld<sup>17</sup>, Y.-P. Kuang<sup>61</sup>, V. Laporta<sup>3</sup>, J. Lee<sup>32</sup>, A. Leibovich<sup>49</sup>,  
J. P. Ma<sup>29</sup>, P. Mackenzie<sup>17</sup>, L. Maiani<sup>50</sup>, M. L. Mangano<sup>11</sup>, A. Meyer<sup>17</sup>, X. H. Mo<sup>22</sup>,  
C. Morningstar<sup>8</sup>, A. Nairz<sup>11</sup>, J. Napolitano<sup>51</sup>, S. Olsen<sup>21</sup>, A. Penin<sup>31</sup>, P. Petreczky<sup>52</sup>, F. Piccinini<sup>47</sup>,  
A. Pineda<sup>2</sup>, A. D. Polosa<sup>3,10</sup>, L. Ramello<sup>48</sup>, R. Rapp<sup>57</sup>, J. -M. Richard<sup>12</sup>, V. Riquer<sup>11</sup>, S. Ricciardi<sup>38</sup>,  
E. Robutti<sup>25</sup>, O. Schneider<sup>34</sup>, E. Scomparin<sup>60</sup>, J. Simone<sup>17</sup>, T. Skwarnicki<sup>56</sup>, G. Stancari<sup>17,23</sup>,  
I. W. Stewart<sup>41</sup>, Yu. Sumino<sup>59</sup>, T. Teubner<sup>35</sup>, J. Tseng<sup>46</sup>, R. Vogt<sup>15,33</sup>, P. Wang<sup>22</sup>, B. Yabsley<sup>63</sup>,  
C. Z. Yuan<sup>22</sup>, F. Zantow<sup>4</sup>, Z. G. Zhao<sup>40</sup>, A. Zieminski<sup>27</sup>

variation has also been observed in a ratio of production rates of P-wave states, namely the  $\chi_{c1}$  to  $\chi_{c2}$  ratio. More precise measurements of these and other ratios would be valuable. Of particular importance would be measurements of ratios of production rates of spin-singlet and spin-triplet quarkonium states, such as the  $\eta_c$  to  $J/\psi$  ratio. The absence of clean signatures for spin-singlet quarkonium states makes such measurements difficult.

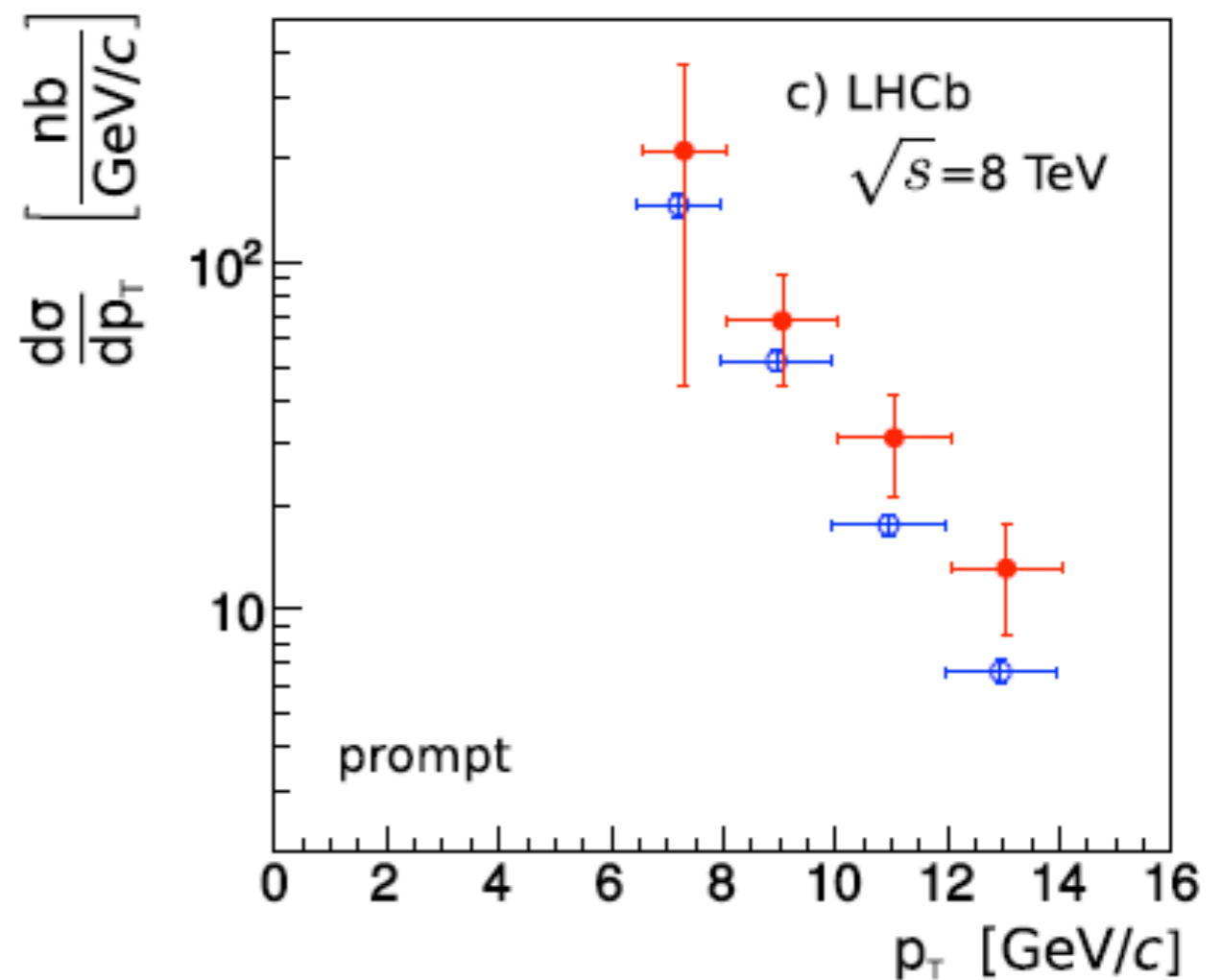
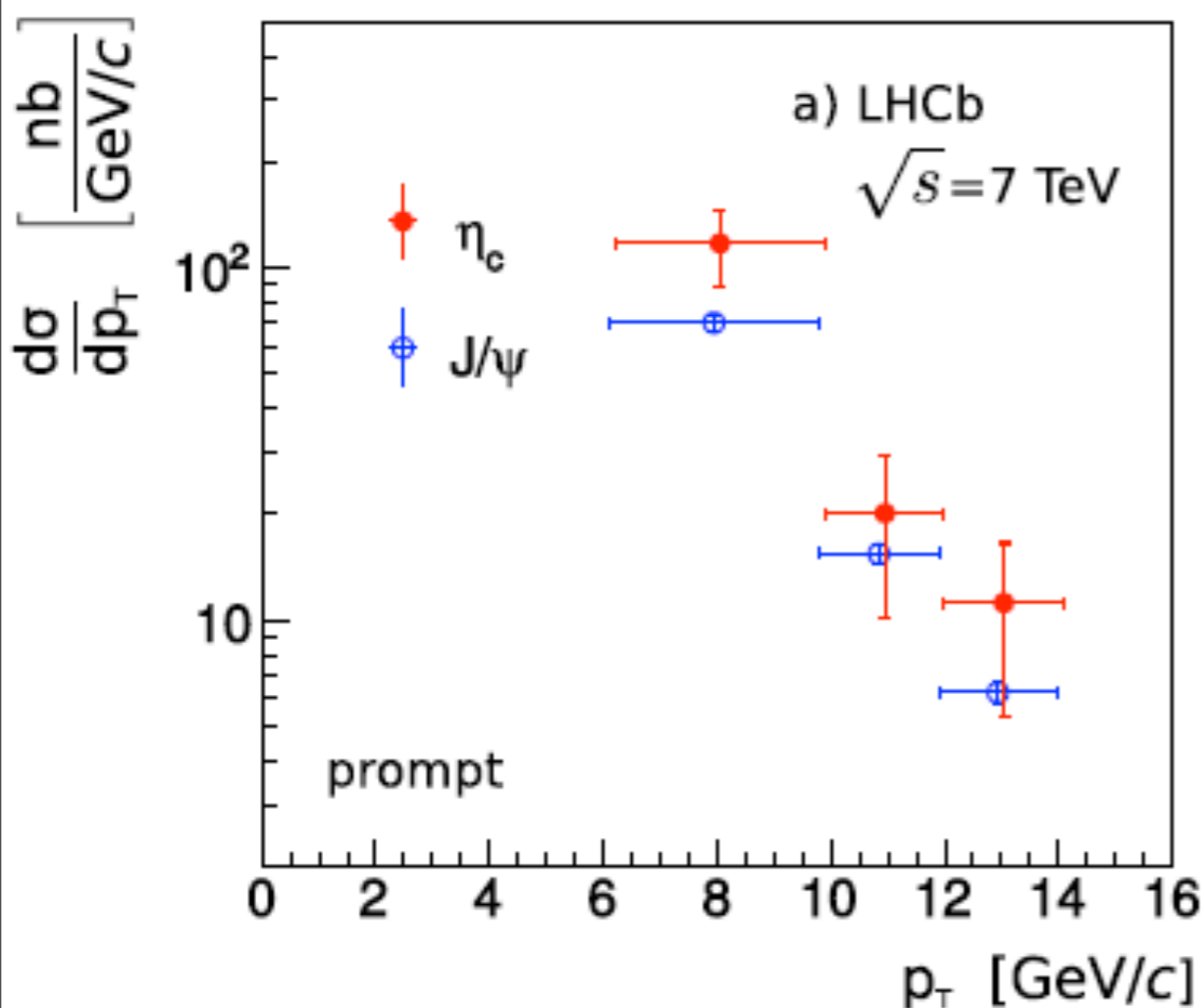
# LHC MEASUREMENTS ON 1S

- It was proposed to use  $\eta_c \rightarrow p\bar{p}$  in 2012

Barsuk, He, Kou, Viaud (2012)

- In 2014, LHCb released a first measurement

Aaij et al., (2014)



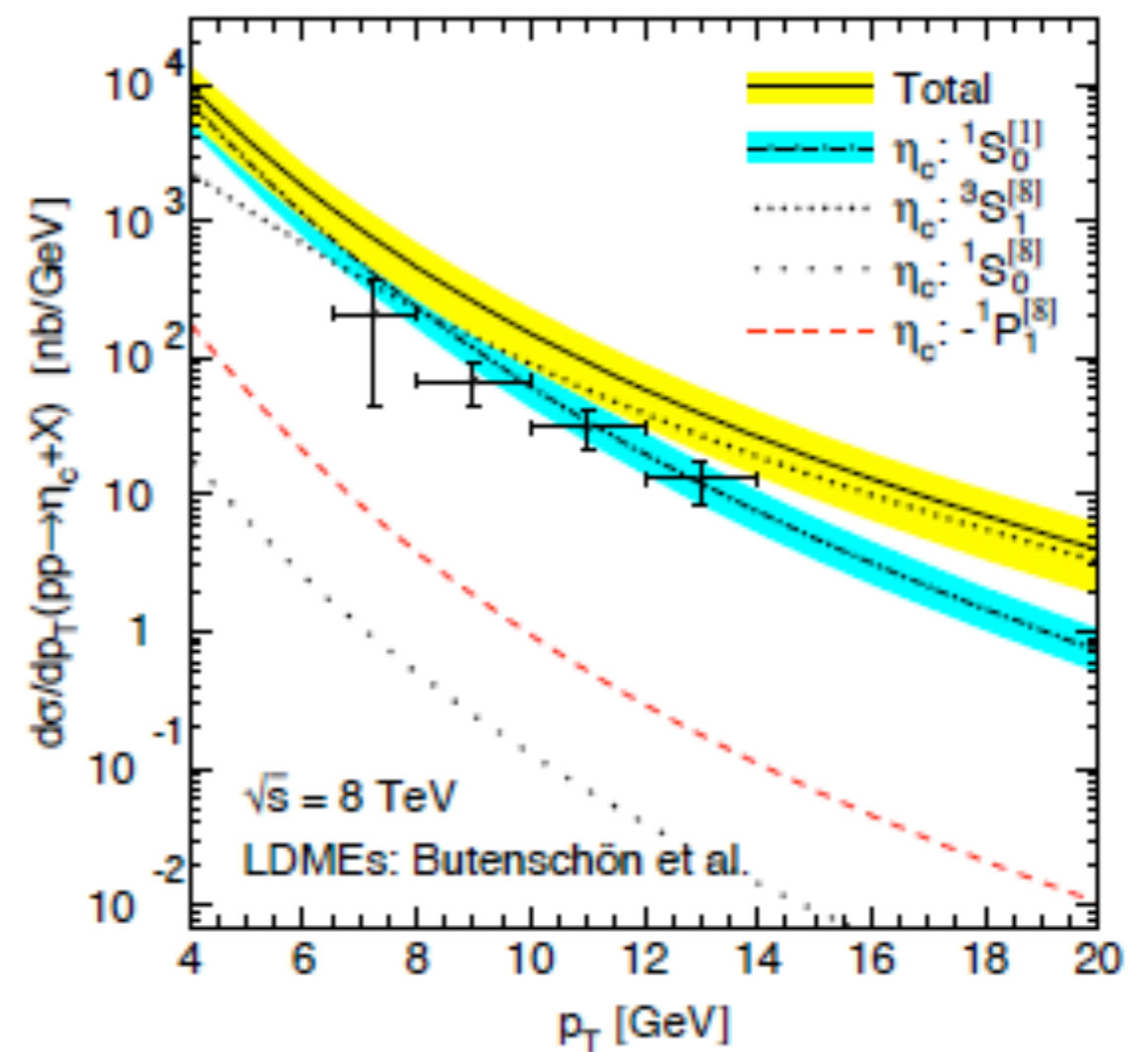
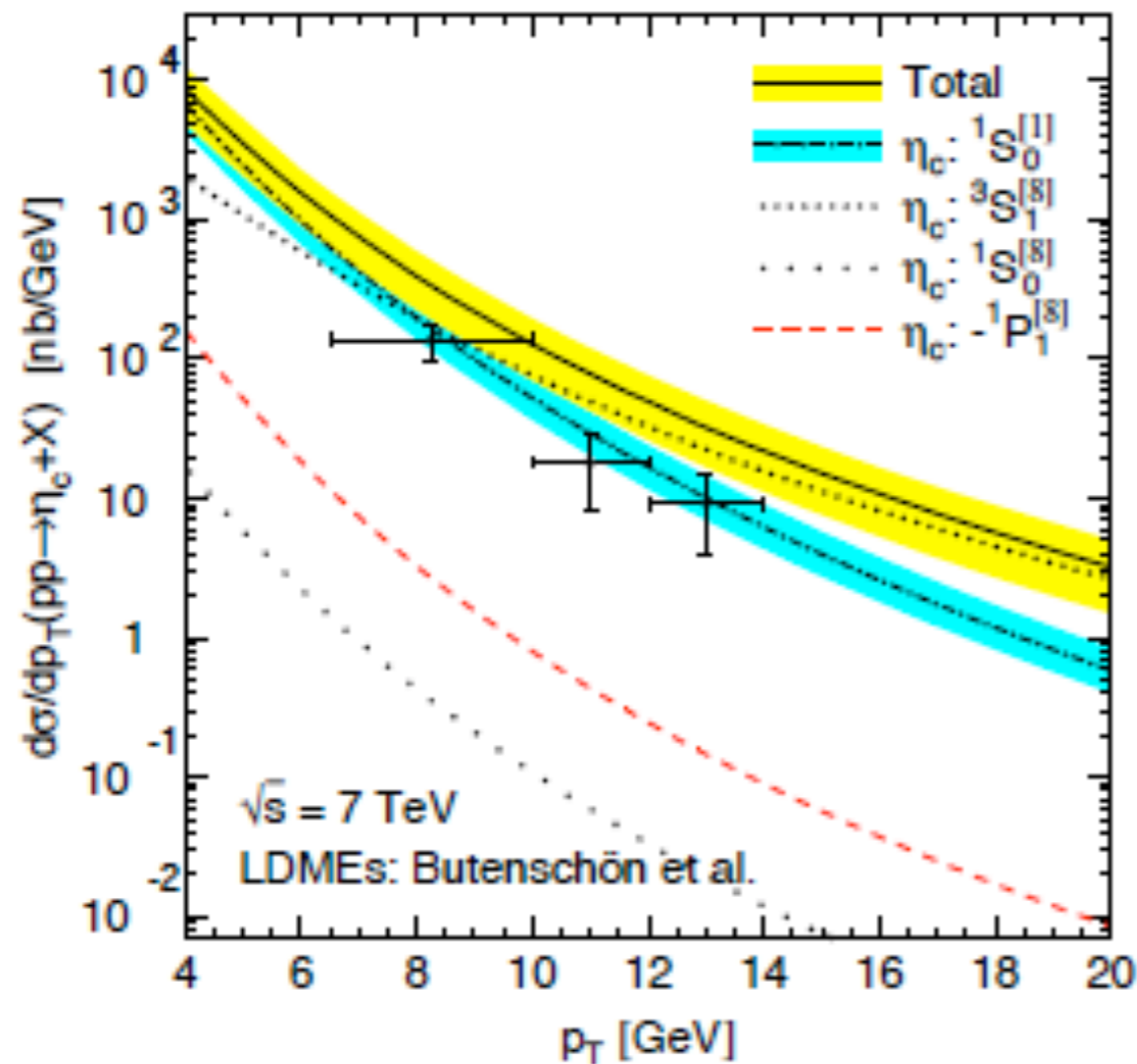
# LHC MEASUREMENTS ON 1S

- The LHCb measurement inspires theoretical studies

Butenschoen, He, Kniehl, (2014); Han et al., (2014); Zhang et al., (2014)

- Global fit + HQSS greatly overshoot the LHCb data

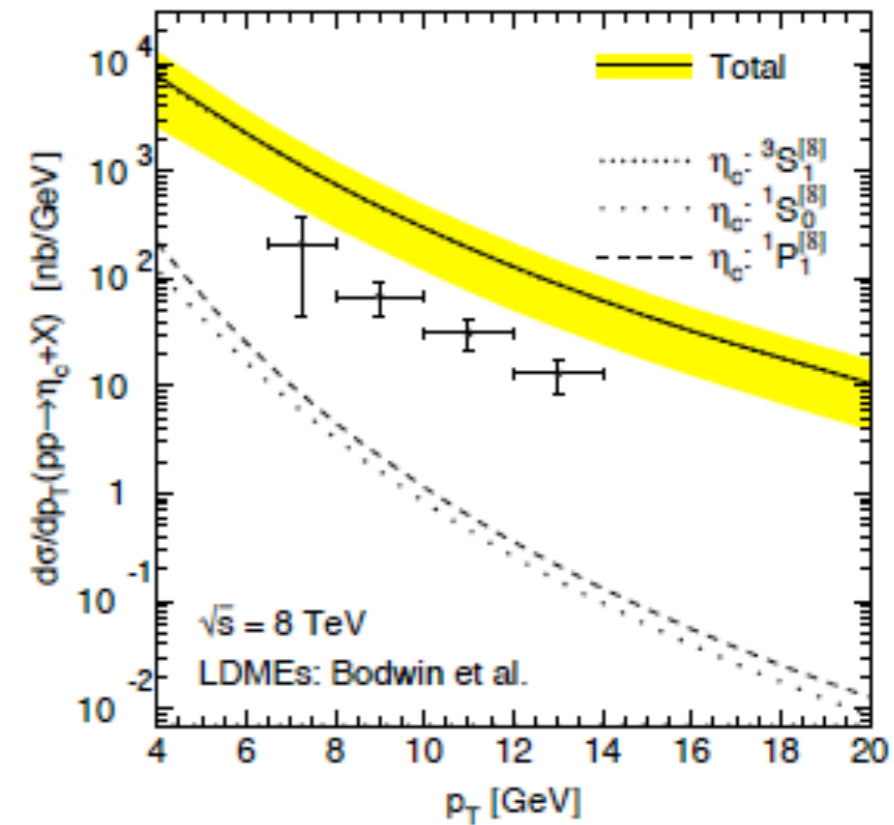
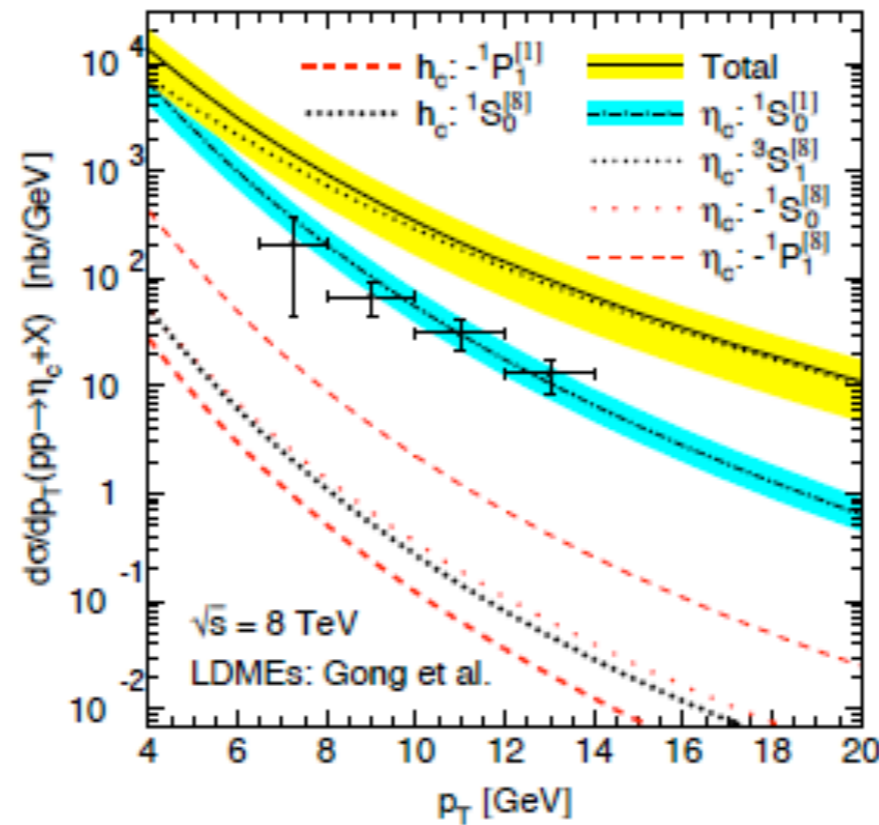
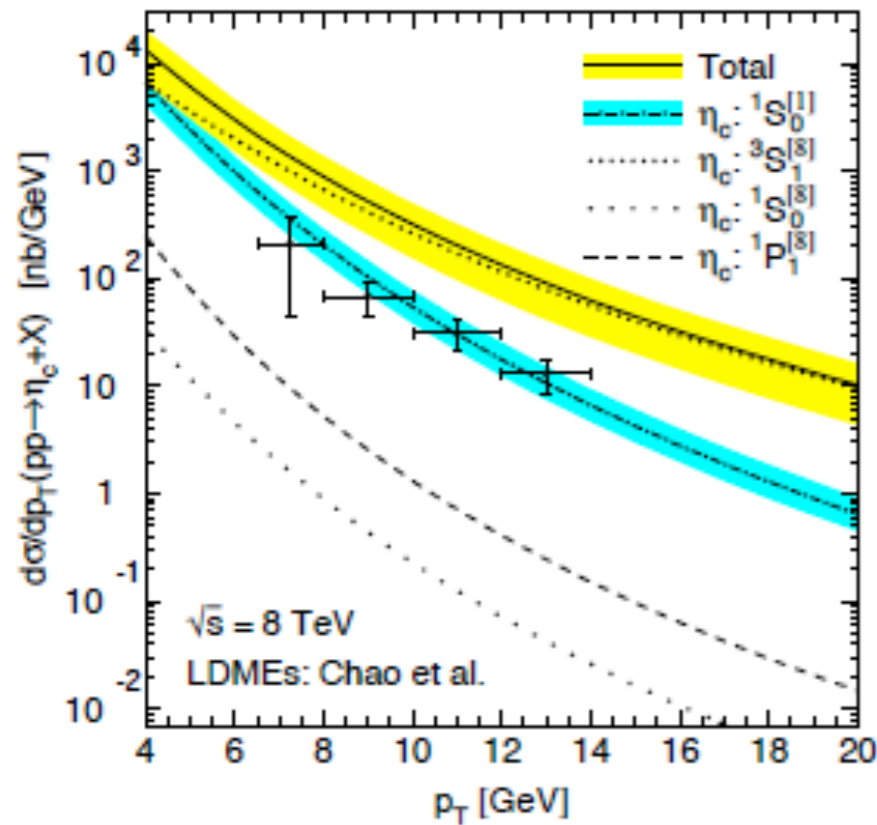
Butenschoen, He, Kniehl, (2014)



# LHC MEASUREMENTS ON 1S

- Actually, the constrain is more powerful under HQSS

Butenschoen, He, Kniehl, (2014)



$\langle \mathcal{O}(S_1^{[1]}) \rangle$ GeV <sup>3</sup>	$\langle \mathcal{O}(S_0^{[8]}) \rangle$ 10 <sup>-2</sup> GeV <sup>3</sup>	$\langle \mathcal{O}(S_1^{[8]}) \rangle$ 10 <sup>-2</sup> GeV <sup>3</sup>	$\langle \mathcal{O}(P_0^{[8]}) \rangle / m_c^2$ 10 <sup>-2</sup> GeV <sup>3</sup>
1.16	8.9 ± 0.98	0.30 ± 0.12	0.56 ± 0.21
1.16	0	1.4	2.4
1.16	11	0	0

1. It excludes our central fit without FD  
Chao et al. (2012)

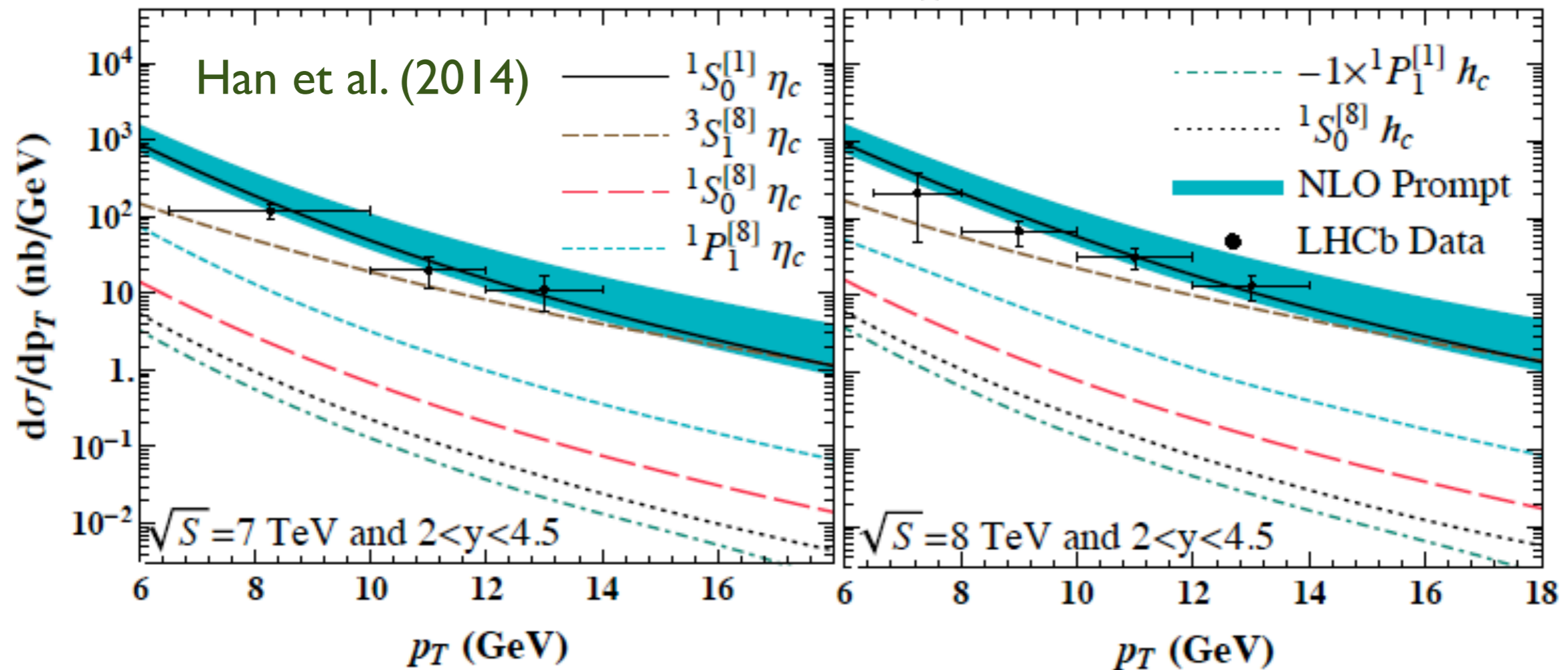
2. and other two fits based on large p<sub>T</sub>  
Gong et al. (2013); Bodwin et al. (2014)



# LHC MEASUREMENTS ON 1S

- The measurement provides additional constraint on the LDME of J/psi based on HQSS
- Interestingly, the only relevant channels are

$$1S_0^{[1]} \quad \text{and} \quad 3S_1^{[8]}$$



- Colour-singlet alone works pretty well

# LHC MEASUREMENTS ON 1S

- LHCb data + HQSS helps to constrain  $\langle \mathcal{O}^{J/\psi} (^1S_0^{[8]}) \rangle$

$$\langle \mathcal{O}^{J/\psi} (^1S_0^{[8]}) \rangle = \langle \mathcal{O}^{\eta_c} (^3S_1^{[8]}) \rangle$$

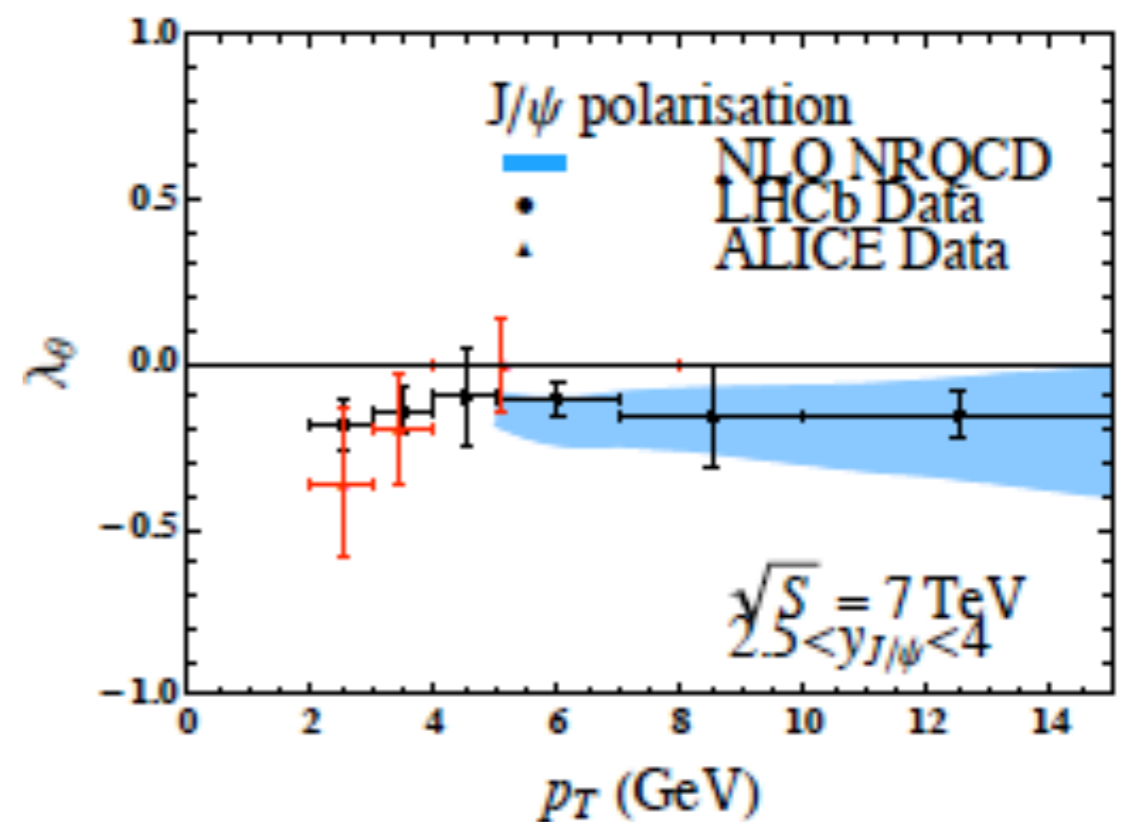
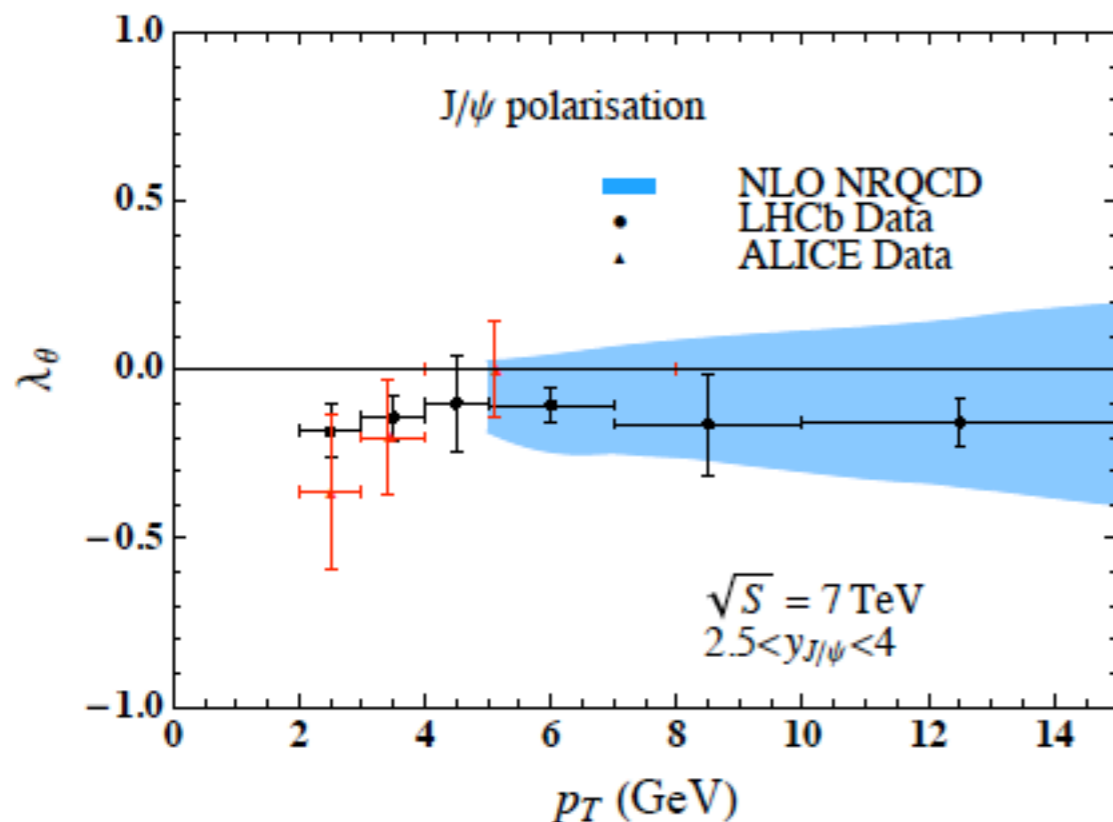
- A conservative upper limit was set via

$$\langle \mathcal{O}^{\eta_c} (^3S_1^{[8]}) \rangle \hat{\sigma}(c\bar{c} [^3S_1^{[8]}]) = \sigma_{\text{LHCb data}}$$

**Before**

$$0 < \langle \mathcal{O}^{\eta_c} (^3S_1^{[8]}) \rangle < 1.46 \times 10^{-2} \text{ GeV}^3$$

**After** Han et al. (2014)



- Another upper limit without ignoring colour-singlet

$$\langle \mathcal{O}^{\eta_c}({}^3S_1^{[8]}) \rangle \lesssim 5 \times 10^{-3} \text{ GeV}^3 \quad \text{Lansberg (1903.09185)}$$

- It challenges the simple interpretation of “ $\langle \mathcal{O}^{J/\psi}({}^1S_0^{[8]}) \rangle$  dominance” in order to explain the unpolarised data

- How about the excited state  $\eta'_c$  ?

- Is  $\eta'_c \rightarrow p\bar{p}$  still feasible ? The channel is just seen !

$\Gamma(\eta_c(2S) \rightarrow p\bar{p})/\Gamma_{\text{total}}$  PDG 2018  $\Gamma_{14}/\Gamma$

VALUE	EVTS	DOCUMENT ID	TECN	COMMENT
seen	106	<sup>1</sup> AAIJ	2017AD LHCb	$p p \rightarrow B^+ X \rightarrow p\bar{p}K^+ X$

<sup>1</sup> AAIJ 2017AD report a 6.4 standard deviation signal, with  $B(B^+ \rightarrow \eta_c(2S)K^+ \rightarrow p\bar{p}K^+)/B(B^+ \rightarrow J/\psi K^+ \rightarrow p\bar{p}K^+) = 0.0158 \pm 0.0033 \pm 0.0009$ .

**References:**

AAIJ	2017AD	PL B769 305	Observation of $\eta_c(2S) \rightarrow p\bar{p}$ and Search for $X(3872) \rightarrow p\bar{p}$ Decays
------	--------	-------------	---

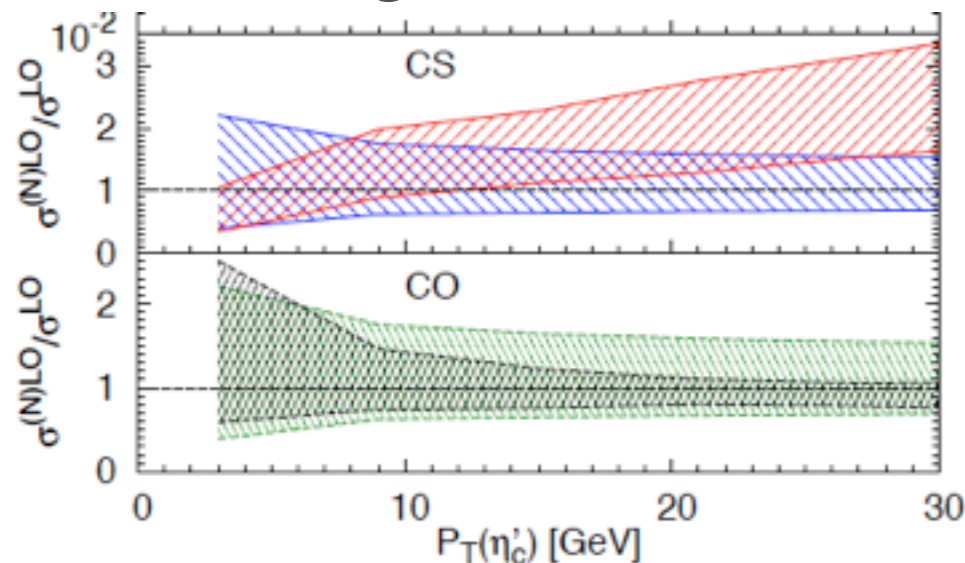
# LHC FUTURE MEASUREMENTS ON $2S$

- The possible decay channels at the LHCb

Lansberg, HSS, Zhang (2017)

Channel	$\eta'_c$ <del>partial width</del> <sup>branching ratio</sup>	status
$p\bar{p}$	$(1.0 \pm 0.5) \times 10^{-4}$	measured
$\gamma\gamma$	$(1.9 \pm 1.2) \times 10^{-4}$	measured
$K\bar{K}\pi$	$(1.9 \pm 1.2) \times 10^{-2}$	measured
$\phi\phi$	$(1 \div 4) \times 10^{-4}$	extrapolated
$\Lambda\bar{\Lambda}$	$O(10^{-4})$	estimated
$\Xi\bar{\Xi}$	$O(10^{-4})$	estimated

- Like other (inclusive) quarkonium states, it is necessary to include NLO QCD at large  $p_T$



$$1 S_0^{[1]}$$

Giant K factor

$$3 S_1^{[8]}$$

Reduce scale uncertainty

- Using different  $\langle \mathcal{O}^{\psi'} (^1S_0^{[8]}) \rangle$  extractions

Reminding HQSS:  $\langle \mathcal{O}^{\psi'} (^1S_0^{[8]}) \rangle = \langle \mathcal{O}^{\eta'_c} (^3S_1^{[8]}) \rangle$

Shao et al. (2014) Gong et al. (2013) Bodwin et al. (2015)

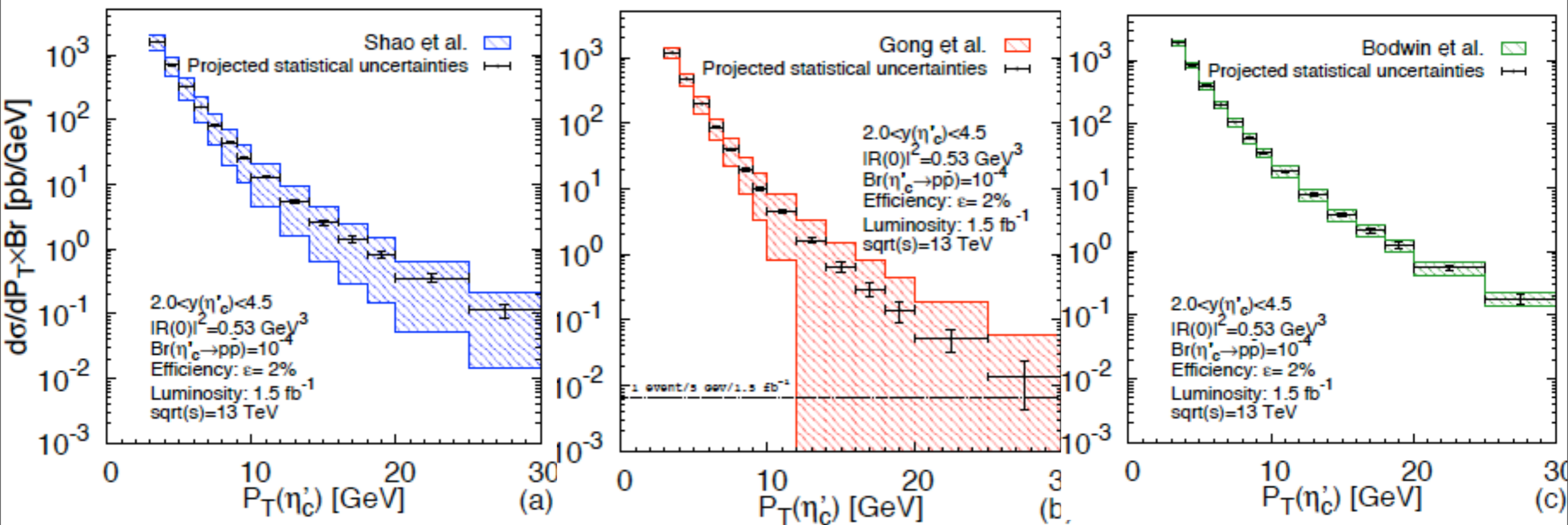
	Shao et al. [21]	Gong et al. [22]	Bodwin et al. [23]
$\langle \mathcal{O}^{\eta'_c} (^3S_1^{[8]}) \rangle$ [10 <sup>-2</sup> GeV <sup>3</sup> ]	[0, 3.82]	[-0.881, 0.857]	[2.35, 3.93]

# LHC FUTURE MEASUREMENTS ON 2S

- As anticipated, the predicted yields strongly depend on  $\langle O^{\eta'_c}({}^3S_1^{[8]}) \rangle$

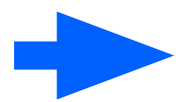
➔ Potential power to differentiate different extractions

Lansberg, HSS, Zhang (2017)

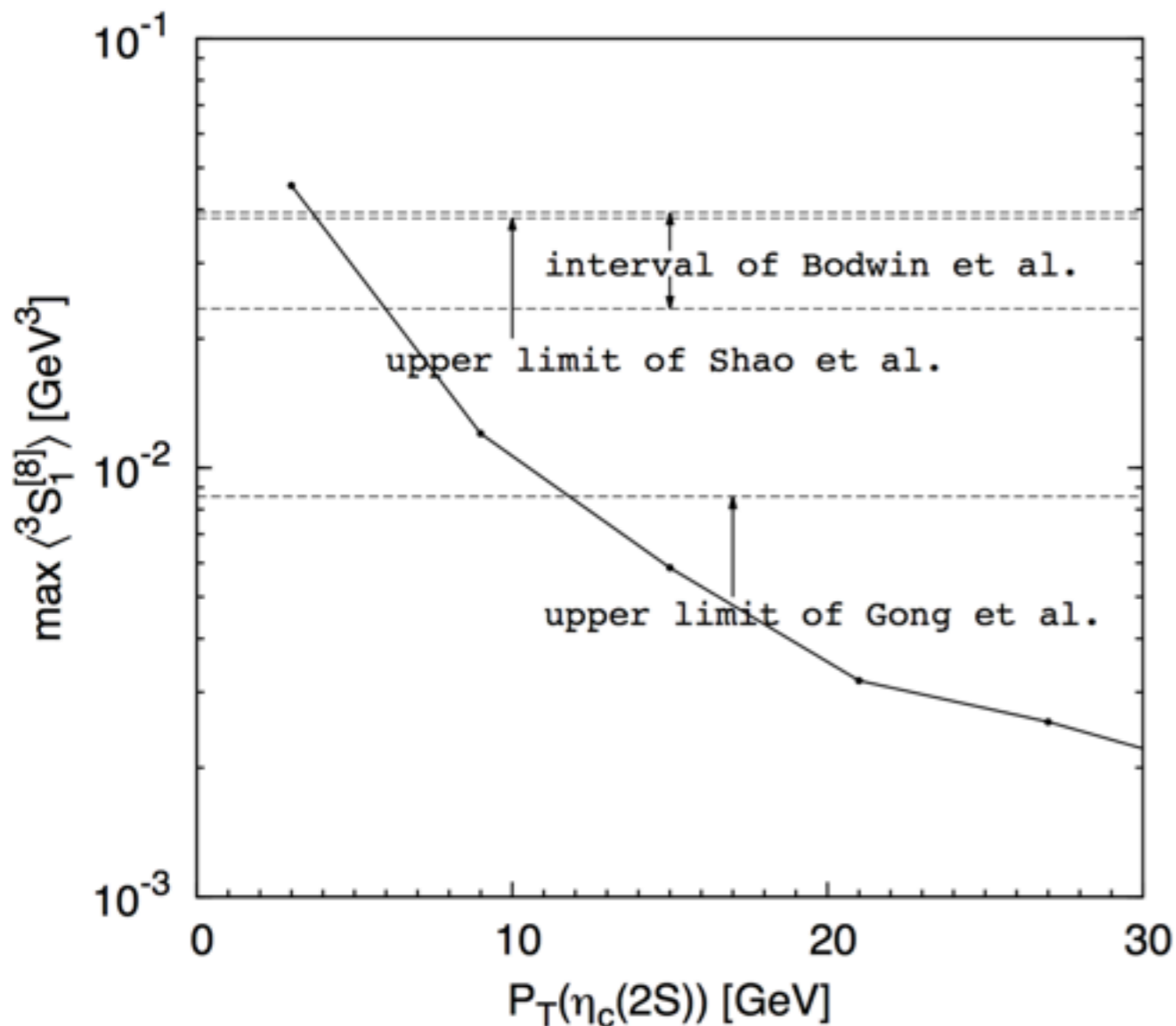


# LHC FUTURE MEASUREMENTS ON 2S

- As anticipated, the predicted yields strongly depend on  $\langle \mathcal{O}^{\eta_c}({}^3S_1^{[8]}) \rangle$



I would favor a larger  $p_T$  but less precise measurement than a smaller  $p_T$  and precise one



- Like IS state, by assuming the observed data described by CS alone
- Use CO to saturate the data to draw a conservative upper limit

# FINAL WORDS

- NRQCD predicts HQSS should hold also in the colour-octet sector, which definitely should be tested by experiments.
- $\eta_c$  and  $\eta'_c$  provide very useful information of CO LDMEs of  $J/\psi$  and  $\psi'$ , while the measurement of the former by the LHCb already gives us many surprises.
- Our study shows that there are already enough statistics to measure  $\eta'_c$  at the LHCb.
- To our LHCb colleagues, please also open a specific trigger window for  $\eta'_c$ , like what you did for  $\eta_c$  in run I and run II.



**I NOW WELCOME YOUR COMMENTS**