# CHALLENGES IN SEMILEPTONIC B DECAYS 

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Torino, 22 May 2018

## The importance of $\left|V_{c b}\right|$

The most important CKM unitarity test is the Unitarity Triangle (UT) $\mathrm{V}_{\mathrm{cb}}$ plays an important role in UT $\varepsilon_{K} \approx x\left|V_{c b}\right|^{4}+\ldots$, $\propto\left|V_{t b} V_{t s}\right|^{2} \simeq\left|V_{c b}\right|^{2}\left[1+O\left(\lambda^{2}\right)\right]$
where it often dominates the theoretical uncertainty.
$\mathrm{V}_{\mathrm{ub}} / \mathrm{V}_{\mathrm{cb}}$ constrains directly the UT


Since several years, exclusive decays prefer smaller $\left|V_{u b}\right|$ and $\left|V_{c b}\right|$

## STATUS of $V_{c b}$ and $V_{u b}$



New $V_{\text {ub }}$ incl by Babar in agreement with exclusive PRD 95 (2017) 7, 072001

New HPQCD $B \rightarrow D^{*}$ result at zero recoil arXiv:1711.11013

New Belle $B \rightarrow D^{*}$ result: with FNAL $V_{c b}=37.4(1.3) 10^{-3}$ arXiv:1702.01521

## UNLIKELY PLACE FOR NEW PHYSICS?

The difference in $\mathrm{V}_{\mathrm{cb}}$ incl vs excl $\mathrm{D}^{*}$ with FNAL/MILC form factor is large: $3 \sigma$ or about $8 \%$. The perturbative corrections to inclusive $\mathrm{V}_{\mathrm{cb}}$ total $5 \% \ldots$

## Right Handed currents now excluded since

$$
\begin{aligned}
& \left|V_{c b}\right|_{i n c l} \simeq\left|V_{c b}\right|\left(1+\frac{1}{2}|\delta|^{2}\right) \\
& \left|V_{c b}\right|_{B \rightarrow D^{*}} \simeq\left|V_{c b}\right|(1-\delta) \\
& \left|V_{c b}\right|_{B \rightarrow D} \simeq\left|V_{c b}\right|(1+\delta)
\end{aligned}
$$

Chen,Nam,Crivellin,Buras,Gemmler, Isidori,Mannel,...
$\delta=\epsilon_{R} \frac{\tilde{V}_{c b}}{V_{c b}} \approx 0.08$

Most general SU(2) invariant dim 6 NP (without RH light neutrino) can explain results, but it is incompatible with $\mathrm{Z} \rightarrow \mathrm{b} \overline{\mathrm{b}}$ data

Crivellin, Pokorski 1407.1320
(though this may not apply to the tensor operator Colangelo, De Fazio)

## RH CURRENTS DON'T HELP Vub EITHER

- Can ease $\left|\mathrm{V}_{\mathrm{ub}}\right|$ tension by allowing small righthanded contribution to Standard-Model weak current [Crivellin, PRD81 (2010) 031301]
- RH currents disfavored by $\wedge_{\mathrm{b}}$ decays (taking $\left|\mathrm{V}_{\mathrm{cb}}\right|$ from $B \rightarrow D^{*} l v+$ HFAG to obtain $\left|\mathrm{V}_{\mathrm{ub}}\right|$ )
 [based on Bernlochner et al., PRD 90, 094003 (2014)]
R. van de Water

Also here $\mathrm{SU}(2) \mathrm{xU}(1)$ invariant NP cannot explain discrepancies 1407.1320

## LEPTON FLAVOUR UNIVERSALITY VIOLATION?



## SEMILEPTONIC B DECAYS



Allow for the determination of $V_{c b}$, which drops out of $R\left(D, D^{*}\right)$. There are $1(2)$ and $3(4)$ FFs for $D$ and $D^{*}$ for light (heavy) leptons, for instance

$$
\left\langle D\left(p^{\prime}\right)\right| \bar{c} \gamma^{\mu} b|\bar{B}(p)\rangle \Leftrightarrow f_{+, 0}\left(q^{2}\right)
$$

## INCLUSIVE vs EXCLUSIVE B DECAYS



Even when a lattice QCD calculation is available, it is generally limited to the high $q^{2}$ region: need parametrization

## MODEL INDEPENDENT FF PARAMETRIZATION

CROSSING + ANALITYCITY


## UNITARITY CONSTRAINTS

$$
\begin{gathered}
\left(-g^{\mu \nu}+\frac{q^{\mu} q^{\nu}}{q^{2}}\right) \Pi^{T}\left(q^{2}\right)+\frac{q^{\mu} q^{\nu}}{q^{2}} \Pi^{L}\left(q^{2}\right) \equiv i \int d^{4} x e^{i q x}\langle 0| T J^{\mu}(x) J^{\dagger \nu}(0)|0\rangle \\
\chi^{L}\left(q^{2}\right)=\frac{\partial \Pi^{L}}{\partial q^{2}}, \quad \chi^{T}\left(q^{2}\right)=\frac{1}{2} \frac{\partial^{2} \Pi^{T}}{\partial\left(q^{2}\right)^{2}}
\end{gathered}
$$

SATISFY UNSUBTRACTED DISP REL, PERT CALCULATION FOR $q^{2}=0$ Boyd, Grinstein, Lebed 1995

$$
\begin{aligned}
& \chi_{V}^{T}(0)=\left[5.883+0.552_{\alpha_{s}}+0.050_{\alpha_{s}^{2}}\right] 10^{-4} \mathrm{GeV}^{-2}=6.486(48) 10^{-4} \mathrm{GeV}^{-2} \\
& \chi_{V}^{L}(0)=\left[5.456+0.782_{\alpha_{s}}-0.034_{\alpha_{s}^{2}}\right] 10^{-3}=6.204(81) 10^{-3} \& \text { analogous for axial etc }
\end{aligned}
$$

USING UP-TO-DATE QUARK MASSES AND 3LOOP CALCULATION Grigo et al 2012

$$
\tilde{\chi}^{T}(0)=\chi^{T}(0)-\sum_{n=1,2} \frac{f_{n}^{2}\left(B_{c}^{*}\right)}{M_{n}^{4}\left(B_{c}^{*}\right)} \quad \begin{gathered}
\text { SUBTRACT } \\
\text { BOUND STATE } \\
\text { CONTRIBUTIONS }
\end{gathered}
$$

| Type | Mass (GeV) | Decay constants (GeV) |
| :---: | :---: | :---: |
| $1^{-}$ | $6.329(3)$ | $0.422(13)$ |
| $1^{-}$ | $6.920(20)$ | $0.300(30)$ |
| $1^{-}$ | 7.020 |  |
| $1^{-}$ | 7.280 |  |
| $0^{+}$ | 6.716 |  |
| $0^{+}$ | 7.121 |  |

## UNITARITY CONSTRAINTS

$$
z=\frac{\sqrt{1+w}-\sqrt{2}}{\sqrt{1+w}+\sqrt{2}} \quad w=\frac{m_{B}^{2}+m_{D^{*}}^{2}-q^{2}}{2 m_{B} m_{D^{*}}} \quad 0<z<0.056
$$



TRUNCATED AT ORDER N

$$
\sum_{n=0}^{N}\left(a_{n}^{i}\right)^{2}<1
$$

WEAK UNITARITY CONSTRAINTS assuming saturation by single hadron channel

## LATTICE + EXP FIT for B $\rightarrow$ DIv

Bigi, PG 1606.08030


## LATTICE + EXP FIT for B $\rightarrow$ DIv

Bigi, PG 1606.08030


Experiment [HFLAV update]
0.407(39)(24)

2016/17 theory results, using new lattice and exp. data:

| [Bigi Gambino 1606.08030] | $0.299(3)$ | $2.4 \sigma$ |
| :---: | :--- | :--- |
| [Bernlochner Ligeti Papucci Robinson 1703.05330] | $0.299(3)$ | $2.4 \sigma$ |
| [Jaiswal Nandi Patra 1707.09977] | $0.302(3)$ | $2.3 \sigma$ | 2012 theory results:

[Fajfer Kamenik Nisandzic 1203.2654]
[Celis Jung Li Pich 1210.8443]
[Tanaka Watanabe 1212.1878]

| $0.296(16)$ | $2.3 \sigma$ |
| :---: | :---: |
| $0.296\binom{8}{6}(15)$ | $2.3 \sigma$ |
| $0.305(12)$ | $2.2 \sigma$ |

LATTICE ONLY RESULTS
HPQCD 2015: 0.300(8), FNAL/MILC 2015: 0.299(11)

## Strong Unitarity Bounds

Information on other channels makes the constraints tighter. HQS implies that all $B^{(*)} \rightarrow D^{(*)}$ ff either vanish or are prop to the Isgur-Wise function: any ff $\mathrm{F}_{\mathrm{j}}$ can be expressed as

$$
F_{j}(z)=\left(\frac{F_{j}}{F_{i}}\right)_{\mathrm{HQET}} F_{i}(z)
$$

which leads to (hyper)ellipsoids in the ai space for S, P,V, A currents

Caprini Lellouch Neubert (CLN, 1998) exploit NLO HQET relations between form factors + QCD sum rules to reduce parameters for ff... up to $<2 \%$ uncertainty, never included in exp analysis.

$$
h_{A 1}(z)=h_{A 1}(1)\left[1-8 \rho^{2} z+\left(53 \rho^{2}-15\right) z^{2}-\left(231 \rho^{2}-91\right) z^{3}\right]
$$

nice: only 2 parameters! but theoretical uncertainty?

## $\left|V_{c b}\right|$ from $B \rightarrow D^{*} / v$ (usual way)

So far LQCD gives only light lepton FF at zero recoil, $w=I$, where rate vanishes. Experimental results must therefore be extrapolated to zerorecoil

Exp error only ~ I.3\%: $\quad \mathcal{F}(I) \eta_{\text {ew }}\left|V_{c b}\right|=35.6 \mid(45) \times 10^{-3}$
(extrapolation with CLN parameterization)
Two unquenched lattice calculations

$$
\mathcal{F}(I)=0.906(I 3)
$$

Bailey et al I403.0635 (FNAL/MILC)
Using their average 0.904(I2):

$$
\mathcal{F}(\mathrm{I})=0.895(26)
$$

Harrison et al I7II.IIOI3 (HPQCD)
$\left|V_{c b}\right|=39.13(75) 10^{-3}$
$\sim 2.9 \sigma$ or $\sim 7 \%$ from inclusive determination 42.00 (65) $10^{-3}$
PG,Healey,Turczyk 2016

## 2017 preliminary Belle analysis

w and angular deconvoluted distributions (independent of parameterization). All previous analyses are CLN based.


Bands show two parametrizations both fitting data well, with $6 \%$ different $\mathrm{V}_{\mathrm{cb}}$

## HQS breaking in FF relations

HQET: $F_{i}(w)=\xi(w)\left[1+c_{\alpha_{s}}^{i} \frac{\alpha_{s}}{\pi}+c_{b}^{i} \epsilon_{b}+c_{c}^{i} \epsilon_{c}+\ldots\right] \quad \epsilon_{b, c}=\bar{\Lambda} / 2 m_{b, c}$
$\mathrm{Cb}_{\mathrm{b}, \mathrm{c}}$ can be computed using subleading IW functions from QCD sumrules
Neubert, Ligeti, Nir I992-93, Bernlochner et al I703.05330
RATIOS $\quad \frac{F_{j}(w)}{V_{1}(w)}=A_{j}\left[1+B_{j} w_{1}+C_{j} w_{1}^{2}+D_{j} w_{1}^{3}+\ldots\right] \quad w_{1}=w-1$
Roughly $\quad \epsilon_{c} \sim 0.25, \quad \epsilon_{c}^{2} \sim 0.06 \quad$ but coefficients??
In a few cases we can compare these ratios with recent lattice results: there are $5-13 \%$ differences, always > NLO correction. For ex.:

$$
\left.\frac{A_{1}(1)}{V_{1}(1)}\right|_{\mathrm{LQCD}}=0.857(15),\left.\quad \frac{A_{1}(1)}{V_{1}(1)}\right|_{\mathrm{HQET}}=0.966(28)
$$

The size of NLO corrections varies strongly. Some ff are protected by Luke's theorem (no I/m corrections at zero recoil), others are linked by kinematic relations at max recoil to those protected

NNLO corrections can be sizeable and are naturally $\mathrm{O}(10-20) \%$
$\frac{F_{j}(w)}{V_{1}(w)}=A_{j}\left[1+B_{j} w_{1}+C_{j} w_{1}^{2}+D_{j} w_{1}^{3}+\ldots\right]$

| $F_{j}$ | $A_{j}$ | $B_{j}$ | $C_{j}$ | $D_{j}$ |
| :---: | ---: | ---: | ---: | ---: |
| $S_{1}$ | 1.0208 | -0.0436 | 0.0201 | -0.0105 |
| $S_{2}$ | 1.0208 | -0.0749 | -0.0846 | 0.0418 |
| $S_{3}$ | 1.0208 | 0.0710 | -0.1903 | 0.0947 |
| $P_{1}$ | 1.2089 | -0.2164 | 0.0026 | -0.0007 |
| $P_{2}$ | 0.8938 | -0.0949 | 0.0034 | -0.0009 |
| $P_{3}$ | 1.0544 | -0.2490 | 0.0030 | -0.0008 |
| $V_{1}$ | 1 | 0 | 0 | 0 |
| $V_{2}$ | 1.0894 | -0.2251 | 0.0000 | 0.0000 |
| $V_{3}$ | 1.1777 | -0.2651 | 0.0000 | 0.0000 |
| $V_{4}$ | 1.2351 | -0.1492 | -0.0012 | 0.0003 |
| $V_{5}$ | 1.0399 | -0.0440 | -0.0014 | 0.0004 |
| $V_{6}$ | 1.5808 | -0.1835 | -0.0009 | 0.0003 |
| $V_{7}$ | 1.3856 | -0.1821 | -0.0011 | 0.0003 |
| $A_{1}$ | 0.9056 | -0.0704 | -0.0580 | 0.0276 |
| $A_{2}$ | 0.9656 | -0.0280 | -0.0074 | 0.0023 |
| $A_{3}$ | 0.9656 | -0.0629 | -0.0969 | 0.0470 |
| $A_{4}$ | 0.9656 | -0.0009 | -0.1475 | 0.0723 |
| $A_{5}$ | 0.9656 | 0.3488 | -0.2944 | 0.1456 |
| $A_{6}$ | 0.9656 | -0.2548 | 0.0978 | -0.0504 |
| $A_{7}$ | 0.9656 | -0.0528 | -0.0942 | 0.0455 |

## Updating Strong Unitarity Bounds

Fit to new Belle's data + total branching ratio (world average) in I707.09509 with UPDATED strong unit. bounds (including uncertainties \& LQCD inputs) for reference $C L N$ fit $V_{c b} \mid=0.0392(12)$

| BGL Fit: | Data + lattice | Data + lattice + LCSR | Data + lattice | Data + lattice + LCSR |
| :---: | :---: | :---: | :---: | :---: |
| unitarity | weak | weak | strong | strong |
| $\chi^{2} /$ dof | $28.2 / 33$ | $32.0 / 36$ | $29.6 / 33$ | $331 / 36$ |
| $\left\|V_{c b}\right\|$ | $0.0424(18)$ | $0.0413(14)$ | $0.0415(13)$ | $0.0406\left({ }_{-13}^{+12}\right)$ |

LCSR: Light Cone Sum Rule results from Faller et al, 0809.0222
Using strong unitarity bounds brings BGL closer to CLN and reduce uncertainties but 3.5-5\% difference persists

## CONSISTENCY WITH HQET

Comparison of $\mathrm{R}_{1,2}$ from BGL fit vs HQET+QCD sum rule predictions (with parametric $+15 \%$ th uncertainty)
black points from preliminary FNAL-MILC calculation according to Bernlochner et al I 708.07I34 (before continuum and chiral extrapolations...)


- HQET $R_{1}$ HQET $R_{2}$
- BGL $R_{1}$
- BGL $R_{2}$

- HQET $R_{1}$ HQET $R_{2}$
$-\mathrm{BGL}+\mathrm{LCSR} R_{1}$
$-\mathrm{BGL}+\mathrm{LCSR} R_{2}$


## CALCULATION of $R\left(D^{*}\right)$

$$
\begin{aligned}
& \frac{d \Gamma_{\tau}}{d w}=\frac{d \Gamma_{\tau, 1}}{d w}+\frac{d \Gamma_{\tau, 2}}{d w}\left\{\begin{array}{l}
\frac{d \Gamma_{\tau, 1}}{d w}=\left(1-\frac{m_{\tau}^{2}}{q^{2}}\right)^{2}\left(1+\frac{m_{\tau}^{2}}{2 q^{2}}\right) \frac{d \Gamma}{d w}, \\
\frac{d \Gamma_{\tau, 2}}{d w}=k \frac{m_{\tau}^{2}\left(m_{\tau}^{2}-q^{2}\right)^{2} r^{3}(1+r)^{2}\left(w^{2}-1\right)^{\frac{3}{2}}}{\left(q^{2}\right)^{3}} \underbrace{P_{1}(w)^{2}}_{ \pm 30 \%!!}
\end{array}\right. \\
& R\left(D^{*}\right)=R_{\tau, 1}\left(D^{*}\right)+R_{\tau, 2}\left(D^{*}\right) \\
& R_{\tau, 1}\left(D^{*}\right)=\frac{\int_{1}^{w_{\tau, \text { max }}} d w d \Gamma_{\tau, 1} / d w}{\int_{1}^{w_{\max }} d w d \Gamma / d w} . \\
& w_{\max } \approx 1.56, \quad w_{\tau, \max } \approx 1.35 \\
& R_{\tau, 2}\left(D^{*}\right)=\frac{\int_{1}^{w_{\tau, \max }} d w d \Gamma_{\tau, 2} / d w}{\int_{1}^{w_{\max }} d w d \Gamma / d w} .
\end{aligned}
$$

$P_{1}$ is a new FF, for which no lattice calculation
is yet available, but its contribution is only $\sim 10 \%$$R_{\tau, 1} \sim 90 \% R_{\tau} \quad R_{\tau, 2} \sim 10 \% R_{\tau}$
Again, normalize $P_{1}$ to one of the FF with proper uncertainties

$$
P_{1}=\left(P_{1} / V_{1}\right)_{\mathrm{HQET}} V_{1}^{\text {exp }} \quad P_{1}=\left(P_{1} / A_{1}\right)_{\mathrm{HQET}} A_{1}^{\text {exp }} \quad P_{1}=\xi(w)(1+\ldots)_{\mathrm{HQET}}
$$



Important endpoint constraint

$$
P_{1}\left(w_{\max }\right)=A_{5}\left(w_{\max }\right)=0.545 \pm 0.025
$$

$$
R\left(D^{*}\right)=0.260(5)(6)=0.260(8)
$$

Consistent with previous estimates but with larger uncertainty

Experiment [HFLAV update]
0.304(13)(7)

2017 theory results, using new lattice and exp. data:

| [Bernlochner Ligeti Papucci Robinson 1703.05330] | $0.257(3)$ | $3.1 \sigma$ |
| :---: | :--- | :--- |
| Our result [Bigi Gambino Schacht 1707.09509] | 0.260(8) | $2.6 \sigma$ |
| [Jaiswal Nandi Patra 1707.09977] | $0.257(5)$ | $3.0 \sigma$ |

2012 theory results:
[Fajfer Kamenik Nisandzic 1203.2654]
[Celis Jung Li Pich 1210.8443]
[Tanaka Watanabe 1212.1878]
0.252(3)
$3.5 \sigma$
0.252(2)(3) $\quad 3.4 \sigma$
0.252(4)
$3.4 \sigma$

## SUMMARY

- Is the $\mathrm{V}_{\mathrm{cb}}$ puzzle resolved? No, but a few pieces fit together. The uncertainty of $\mathrm{B} \rightarrow \mathrm{D}^{*} \mathrm{l} v$ was underestimated and the result was likely biased: old data should be reanalysed.
- We revisited main ideas behind CLN, using LQCD \& exp results and conservative theory uncertainties, and obtained new strong unitarity bounds. We do not give a simplified parametrization. Our results provide a framework for future exp analyses. Lattice will soon settle the matter with calculations at non-zero recoil.
- For $R\left(D^{*}\right)$ we know little about $P$, and we have to rely on HQET + QCD sum rules. Hence a larger uncertainty, but the anomaly persists. The upcoming LQCD determination of $P$ । at zero recoil could cut the uncertainty by $\sim 2$.
- Lessons for Belle-Il: avoid CLN, document your results in model-indep way to facilitate reanalyses, update backgrounds...


## INCLUSIVE DECAYS: BASICS



- Simple idea: inclusive decays do not depend on final state, long distance dynamics of the B meson factorizes. An OPE allows to express it in terms of B meson matrix elements of local operators
- The Wilson coefficients are perturbative, matrix elements of local ops parameterize non-pert physics: double series in $\alpha_{s}, \Lambda / m_{b}$
- Lowest order: decay of a free $b$, linear $\Lambda / m_{b}$ absent. Depends on $m_{b, c}, 2$ parameters at $\mathrm{O}\left(1 / \mathrm{mb}^{2}\right), 2$ more at $\mathrm{O}\left(1 / \mathrm{mb}^{3}\right) \ldots$


## CUTS IN $B \rightarrow X_{u} l v$

Experiments often use kinematic cuts to avoid the $\mathrm{b} \rightarrow \mathrm{clv}$ background:

$$
m_{X}<M_{D} \quad E_{\ell}>\left(M_{B}^{2}-M_{D}^{2}\right) / 2 M_{B} \quad q^{2}>\left(M_{B}-M_{D}\right)^{2} \ldots
$$

The cuts destroy convergence of the OPE that works so well in $b \rightarrow c$. OPE expected to work only away from pert singularities

Rate becomes sensitive to local b-quark wave function properties like Fermi motion. Dominant nonpert contributions can be resummed into a SHAPE FUNCTION $f\left(k_{+}\right)$.
Equivalently the SF is seen to emerge from soft gluon resummation


## HOW TO ACCESS THE SF?

$$
\frac{d^{3} \Gamma}{d p_{+} d p_{-} d E_{\ell}}=\frac{G_{F}^{2}\left|V_{u b}\right|^{2}}{192 \pi^{3}} \int d k C\left(E_{\ell}, p_{+}, p_{-}, k\right) F(k)+O\left(\frac{\Lambda}{m_{b}}\right)
$$

$\underset{\text { e.g. at } \mathrm{q}^{2}=\mathrm{o}}{\text { OPE constaints }} \int_{-\infty}^{\bar{\Lambda}} k^{2} F(k) d k=\frac{\mu_{\pi}^{2}}{3}+O\left(\frac{\Lambda^{3}}{m_{b}}\right)$ etc.

Predictions based on resummed pQCD

Dress Gluon
Exponentiation, ADFR

Subleading SFs

| Predictions based on <br> resummed pQCD <br> Dress Gluon <br> Exponentiation, ADFR | OPE constraints + <br> parameterization <br> without/with resummation <br> GGOU, BLNP |
| :---: | :---: |

Fit semileptonic (and radiative) data SIMBA, NNVub

## $V_{u b} \mid$ DETERMINATIONS

## Inclusive: 5\% total error

| HFAG 2014 | Average IV |
| :---: | :---: |
| DGE | $4.52(16)(16)$ |
| BLNP | $4.45(16)(22)$ |
| GGOU | $4.51(16)(15)$ |

UT fit (without direct $\mathrm{V}_{\text {ub }}$ ):

$$
V_{u b}=3.66(12) 10^{-3}
$$

Recent experimental results are theoretically cleanest ( $2 \%$ ) but based on background modelling.
 Signal simulation also relies on theoretical models...

## NEW Babar endpoint analysis 1611.05624

High sensitivity of the BR on the shape of the signal in the endpoint region. Single most precise measurement to date, not yet in HFAG

$$
\text { GGOU: }\left|V_{u b}\right|=\left(3.96 \pm 0.10_{e x p} \pm 0.17_{t h}\right) \times 10^{-3}
$$




What happens if same is done in other BaBar analyses? What's going on with BLNP? NB Belle multivariate analysis uses GGOU+DN for the inclusive part

## SHAPE FUNCTIONS IN GGOU

$$
W_{i}\left(q_{0}, q^{2}\right) \sim \int d k_{+} F_{i}\left(k_{+}, q^{2}, \mu\right) W_{i}^{\text {pert }}\left[q_{0}-\frac{k_{+}}{2}\left(1-\frac{q^{2}}{m_{b} M_{B}}\right), q^{2}, \mu\right]
$$

3 SFs, one for each form factor No subleading SFs, but SF depend on $\mathrm{q}^{2}$ through moments



In the past each SF parametrized by simple 2-parameter functional forms

## THE NNVub PROJECT

- Use Artificial Neural Networks to parametrise SFs without bias and extract $\mathrm{V}_{\mathrm{ub}}$ from theoretical constraints and data, together with HQE parameters in a model independent way (without assumptions on functional form). Similar to NNPDF. Applies to $\mathrm{b} \rightarrow \mathrm{ulv}, \mathrm{b} \rightarrow \mathrm{s} \gamma, \mathrm{b} \rightarrow \mathrm{sl}+\mathrm{l}-$
- Belle-ll will measure some kinematic distributions, thus constraining directly the shape functions. NNVub will provide a flexible tool to analyse data.
- NN provide unbiased parameterization of a continuous function: in the limit of infinite nodes they are universal approximators, highly non-linear functions
- Weights are trained to reproduce desired response: random weights undergo random modifications, retaining only those that improve response (e.g. better $\chi^{2}$ ): genetic algorithm $\rightarrow$ replicas
- Used in pattern recognition, computationally intensive, data-driven

Selection of NN replicas trained on the first three moments only. They are not sufficient. But we know photon spectrum in bsgamma: single peak dominance, not too steep

Beware: sampling can be biased by implementation, e.g. random initialization, or selection based on training speed




Comparison with 2007 paper, same inputs


NNVub GGOU(HFAG 2014)

| Experimental cuts (in GeV or $\mathrm{GeV}^{2}$ ) | $\left\|V_{u b}\right\| \times 10^{3}$ | $\left\|V_{u b}\right\| \times 10^{3}[15]$ |
| :---: | :---: | :---: |
| $M_{X}<1.55, E_{\ell}>1.0$ Babar [44] | $4.30(20)\left({ }_{27}^{26}\right)$ | 4.29(20) ${ }_{22}^{21}$ ) |
| $M_{X}<1.7, E_{\ell}>1.0$ Babar [44] | $4.05(23)\binom{19}{20}$ | $4.09(23)\binom{18}{19}$ |
| $M_{X} \leq 1.7, q^{2}>8, E_{\ell}>1.0$ Babar[44] | $4.23(23)\left({ }^{28}\right)$ | $4.32(23)(30)$ |
| $E_{\ell}>2.0$ Babar [41] | $4.47(26)\left(\begin{array}{c}27 \\ 27\end{array}\right.$ | $4.50(26)\binom{18}{25}$ |
| $E_{\ell}>1.0$ Belle [45] | $4.58(27)\binom{10}{11}$ | $4.60(27)\binom{10}{11}$ |

Inputs for constraints from sl fit by Alberti et al, 2014 with full uncertainties and correlations

## The $b \rightarrow s \gamma$ spectrum <br> E. Lunghi, M.Misiak, S.Schacht, PG in progress



Belle fully incl.


Babar sum excl.









Up-to-date theoretical description of spectrum to get i) leading $S F$ at $q^{2}=0$ for $V_{u b}$, ii) HQE elements to compare with s.l. fit iii) reliable extrapolation to low cuts.

## PROSPECTS

- Learning @ Belle-II from kinematic distributions, e.g. M× spectrum
- OPE parameters checked/ improved in $b \rightarrow$ ulv (moments): global NN+OPE fit
- include all relevant information with correlations
- check signal dependence at endpoint
- full phase space implementation of $\boldsymbol{\alpha}_{s}{ }^{2}$ and $\boldsymbol{\alpha}_{s} / \mathrm{mb}^{2}$ corrections

- model/exclude high $q^{2}$ tail

At Belle-II we can expect to bring inclusive $\mathrm{V}_{\mathrm{ub}}$ at almost the same level as $\mathrm{V}_{\mathrm{cb}}$

## BACKUP

## Role of HQET relations in $V_{c b}$ extraction (prelim Belle data only)

- "practical" $\mathrm{CLN}:\left|\mathrm{V}_{\mathrm{cb}}\right|=38.2(1.5) \times 10^{-3}[1,5,6,7,8]$
- $\mathrm{CLN}+\mathrm{QCD}$ sumrule errors $+\mathrm{B} \rightarrow \mathrm{D}\left|\mathrm{V}_{\mathrm{cb}}\right|=38.5(1.1) \times 10^{-3}[2]$
- same + lattice at non-zero recoil $\left|\mathrm{V}_{\mathrm{cb}}\right|=39.3(1.0) \times 10^{-3}[2]$
- $\mathrm{BGL}+\mathrm{HQET}+\mathrm{B} \rightarrow \mathrm{D}$ with nuisance $\left|\mathrm{V}_{\mathrm{cb}}\right|=40.9(0.9) \times 10^{-3}[3]$
- BGL+strong unitarity $\left|\mathrm{V}_{\mathrm{cb}}\right| \sim 40.8(1.5) \times 10^{-3}[4]$
- BGL+weak unitarity $\left|\mathrm{V}_{\mathrm{cb}}\right|=41.7(2.0) \times 10^{-3}[5,6,7,8]$
[1] Belle coll. 1702.01521
[2] Bernlochner et al. 1703.05330
[3] Jaiswal, Nandi, Patra, 1707.09977
[4] Bigi, Gambino, Schacht 1707.09509
[5] Bigi, Gambino, Schacht 1703.06124
[6] Harrison et al. 1711.11013 (HPQCD)
[7] Bernlochner et al 1708.07134
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