Novel Proposal of a Low EMittance Muon Accelerator

M. Antonelli (LNF)



Most of the slides from: M. Boscolo, MAC, LNGS, 10 Oct. 2017

Low EMittance Muon Accelerator team:

INFN institutions involved: LNF, Roma1, Pd, Pi, Ts, Fe

Universities: Sapienza, Padova, Insubria

Contributions from: CERN, ESRF, LAL, SLAC

This new proposal covers different areas of research: accelerator physics, high energy, theory, engineering material science, ...

Many colleagues are interested to collaborate, informal contacts with international experts has started

We believe in the potential of this idea, but key challenges need to be demonstrated to prove its feasibility.

I will show the work done up to now that may lead to a Conceptual Design Report

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Benato Lisa	15	PD
Bertolin Alessandro	5	PD
Checchia Paolo	10	PD
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Palumbo Luigi	20	RM1
Camattari Riccardo	30	FE
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Vallazza Erik	50	TS
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Guiducci Susanna	20	LNF
Iafrati Matteo	100	LNF
Rotondo Marcello	20	LNF
Biagini Maria	20	LNF
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Low EMittance Muon Accelerator team



Additional national

M. Ricci (Uni. Marconi, INFN-LNF) A. Stella (LNF), G. Cavoto (La Sapienza), E. Bagli (INFN-Fe), M. Prest, M. Soldani, C. Brizzolari (Uni-Insubria&INFN), A. Lorenzon, S. Vanini, S. Ventura, D. Dattola(INFN-Uni. Padova), A. Wulzer (Uni. Pd & EPFL)

Additional international

- P. Raimondi, S. Liuzzo, N. Carmignani (ESRF)
- R. Di Nardo, P. Sievers, M. Calviani, S. Gilardoni (CERN)
- I. Chaikovska, R. Chehab (LAL-Orsay)
- L. Keller, T. Markiewicz (SLAC)

ARIES WP6: improving Accelerator PErformance and new Concepts task for muon collider

Task 6.6 Assessment of advanced muon-collider concepts without ionization cooling

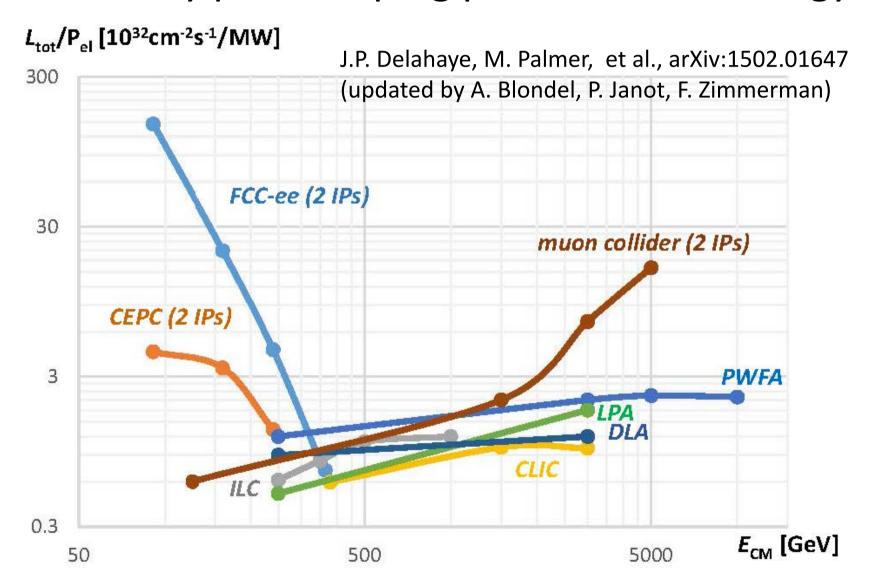
outline

- 1. Introduction
- 2. Physics Opportunities
 - Very High Energy
 - Multi-TeV
- 3. Low emittance muon beam production concept
 - Target options
 - Positron Source
 - Multipass scheme
- 4. First study of multi-TeV MC parameters
- 5. First design of the e⁺ ring
 - Multiturn simulations
 - First considerations about target thermo-mechanical stresses
 - First considerations on e⁺ source
- 6. Experimental tests
 - 45 GeV e⁺ beam
 - DAФNE
- 7. Conclusion and Plans

Muon based Colliders

- A $\mu^+\mu^-$ collider offers an ideal technology to extend lepton high energy frontier in the multi-TeV range:
 - No synchrotron radiation (limit of e⁺e⁻ circular colliders)
 - No beamstrahlung (limit of e⁺e⁻ linear colliders)
 - but muon lifetime is 2.2 μs (at rest)
- Best performances in terms of luminosity and power consumption
- Great potentiality if the technology proves its feasibility:
 - cooled muon source
 - fast acceleration
 - μ Collider
 - radiation Safety (muon decay in accelerator and detector)

Muon Colliders potential of extending leptons high energy frontier with high performance luminosity per wall-plug power vs c.m. energy



The strength of a μ -beam facility lies in its richness:

- Muon rare processes
- Neutrino physics
- Higgs factory
- Multi-TeV frontier



 μ –colliders can essentially do the HE program of e^+e^- colliders with added bonus (and some limitations)



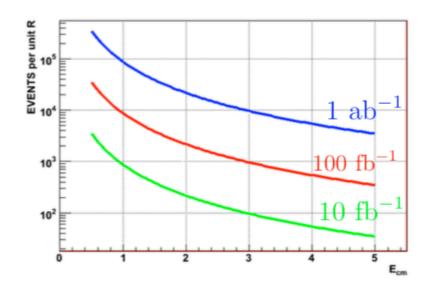
MultiTeV Lepton Collider Basics

- For √s < 500 GeV
 - SM threshold region: top pairs; W+W-; Z0Z0; Z0h; ...
- For √s > 500 GeV
 - For SM pair production ($|\theta| > 10^{\circ}$)

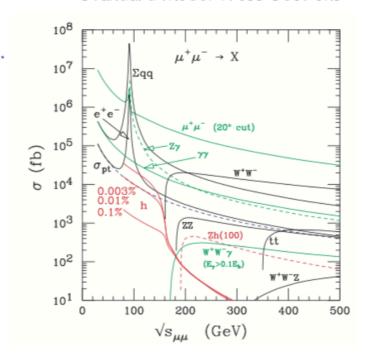
R =
$$\sigma / \sigma_{\text{QED}}(\mu^+\mu^- \rightarrow e^+e^-) \sim \text{flat}$$

$$\sigma_{\text{QED}}(\mu^+\mu^- \rightarrow e^+e^-) = \frac{4\pi\alpha^2}{3s} = \frac{86.8 \text{ fb}}{s(\text{TeV}^2)}$$

- High luminosity required



Standard Model Cross Sections



$$\sqrt{s} = 3.0 \text{ TeV}$$
 $\mathcal{L} = 10^{34} \text{ cm}^{-2} \text{sec}^{-1}$
 $\rightarrow 100 \text{ fb}^{-1} \text{year}^{-1}$

⇒ 965 events/unit of R

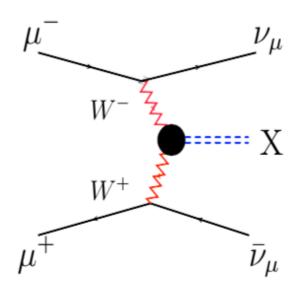
Processes with $R \ge 0.1$ can be studied

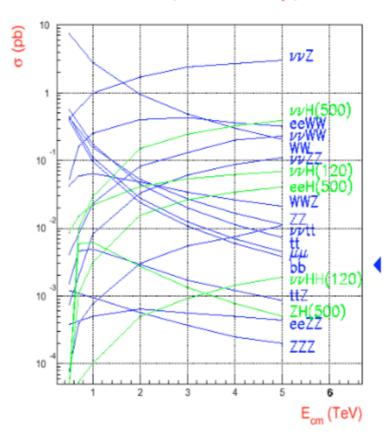
Total - 540 K SM events per year

$$== 10^{36} \text{ cm}^{-2} \text{ s}^{-1} @ \text{ Vs } 30 \text{ TeV}$$

Vector boson fusion

- For √s > 1 TeV Fusion Processes
 - Large cross sections
 - Increase with s.
 - Important at multi-Tev energies
 - M_X² < s
 - Backgrounds for SUSY processes
 - t-channel processes sensitive to angular cuts





$$\sigma(s) = C \ln(\frac{s}{M_{\rm X}^2}) + \dots$$

SM Higgs

(after ~10 years of running)

- Resonant Higgs production:
 - Unique measurements of mh and Th

(mh \sim 0.1 MeV, $\Gamma h \sim$ 0.2 MeV)

■ Best test of 2nd generation Higgs couplings (h $\rightarrow \mu + \mu -$)

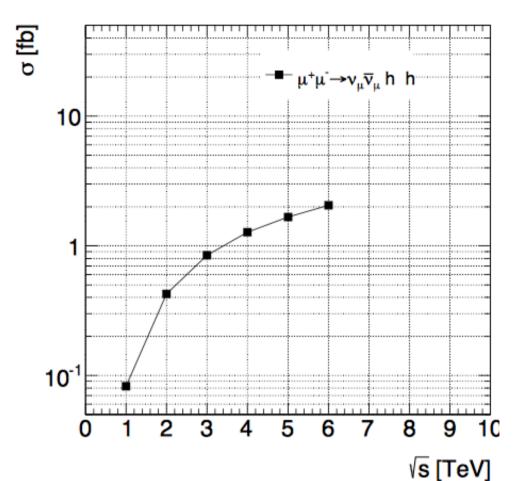
Error on	μμ resonance	ILC	FCC-ee
m _H (MeV)	0.06	30	8
$\Gamma_{\!\scriptscriptstyle \sf H}$ (MeV)	0.17	0.16	0.04
g _{Hbb}	2.3%	1.5%	0.4%
g _{HWW}	2.2%	0.8%	0.2%
g _{Hττ}	5%	1.9%	0.5%
$g_{H\gamma\gamma}$	10%	7.8%	1.5%
$g_{H\mu\mu}$	2.1%	20%	6.2%
g _{HZZ}	_	0.6%	0.15%
g _{Hcc}	_	2.7%	0.7%
\mathbf{g}_{Hgg}	-	2.3%	0.8%
BR _{invis}	-	<0.5%	<0.1%

P. Janot

- HZ production:
 - Similar to e⁺e⁻ measurements but lower statistics factor 10 (ILC/CEPC)
 100 FCC-ee
- VBF at mutiTeV
 - High xs(O(1Pb)@6TeV) & high lumi better statistics than FCC-ee?
 - Competitive (probably best) measurement of HH production

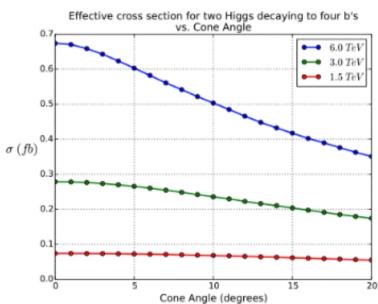
VBF HH production

@sqrt(s) = 3 TeV $\mu\mu$ ->vvHH : 0.9 fb



@sqrt(s) = 6 TeV $\mu\mu$ ->vvHH : 2.1 fb

Machine bkg limitations: xs with 4b in det. acceptance



Not yet detailed studies

A.Conway, H.Wenzel, R.Lipton and E.Eichten, arXiv:1405.5910

Muon Source

Goals

- Neutrino Factories: Rate > $10^{14} \mu$ /sec within the acceptance of a μ ring
- Muon Collider: luminosities >10³⁴/cm⁻²s⁻¹ at TeV-scale ($\approx N_{\mu}^2 1/\epsilon_{\mu}$)

Options

- Tertiary production through **proton on target:** cooling needed, baseline for Fermilab design study production Rate > $10^{13}\mu/\text{sec}$ N_{μ} = $2\cdot10^{12}/\text{bunch}$ (5 $10^8\,\mu/\text{sec}$ today @PSI)
- e⁺e⁻ annihilation: positron beam on target: very low emittance and no cooling needed, baseline for our proposal here production Rate $\approx 10^{11} \,\mu/\text{sec}$ N_u $\approx 6.10^9/\text{bunch}$
- by Gammas ($\gamma N \rightarrow \mu^+ \mu^- N$): GeV-scale Compton γ s not discussed here production Rate $\approx 5 \cdot 10^{10} \, \mu/\text{sec}$ $N_{\mu} \approx 10^6$ (Pulsed Linac) production Rate >10¹³ μ/sec $N_{\mu} \approx \text{few} \cdot 10^4$ (High Current ERL) see also: W. Barletta and A. M. Sessler NIM A 350 (1994) 36-44 (e-N $\rightarrow \mu^+ \mu^- e^- N$)

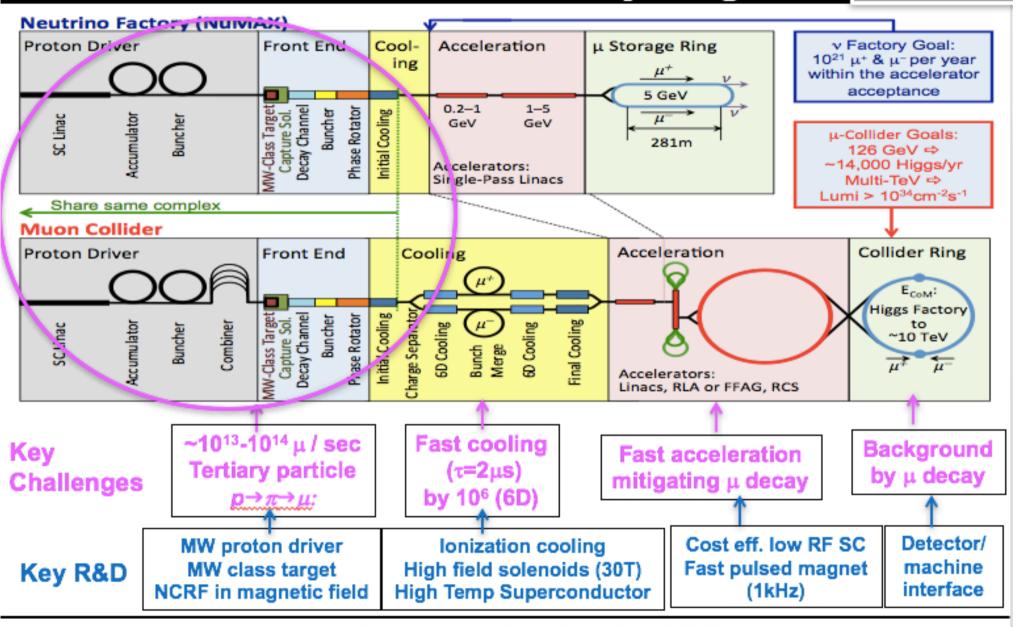
Muon source Comparison

	Physical process	Rate μ/s	normalized emittance e _N [μm-rad]
e+ on target	e+e-→ μ+μ-	0.9x10 ¹¹	0.04
Protons on target	p N \rightarrow πX, kX \rightarrow μ X'	10 ¹³	25
Compton γ on target	γ N→ μ+μ- N	5x10 ¹⁰	2

Proton-Based Source

Muon Accelerator Program (MAP) Muon based facilities and synergies

Mark Palmer



Unique properties of muon beams (Nov 18,2015)

M. Palmer

Muon Collider Parameters



	Muon Collid	er Paramete	rs		
			<u>Multi-TeV</u>		<u>eV</u>
Formulais Siles					Accounts for
		Production			Site Radiation
Parameter	Units	Operation			Mitigation
CoM Energy	TeV	0.126	1.5	3.0	6.0
Avg. Luminosity	10 ³⁴ cm ⁻² s ⁻¹	0.008	1.25	4.4	12
Beam Energy Spread	%	0.004	0.1	0.1	0.1
Higgs Production/10 ⁷ sec		/13,500	37,500	200,000	820,000
Circumference	km	0.3	2.5	4.5	6
No. of IPs		/ 1	2	2	2
Repetition Rate	Hz /	15	\ 15	12	6
β*	cm /	1.7	1 (0.5-2)	0.5 (0.3-3)	0.25
No. muons/bunch	10 ¹³	4	2	2	2
Norm. Trans. Emittance, ϵ_{T}	π mm-rad	0.2	0.025	0.025	0.025
Norm. Long. Emittance, $\epsilon_{\mbox{\tiny LN}}$	π mm-rad	1.5	70	70	70
Bunch Length, σ _s	/ cm	6.3	1	0.5	0.2
Proton Driver Power	MW	4	4	4	1.6
Wall Plug Power	/ MW	200	216	230	270

Exquisite Energy Resolution Allows Direct Measurement of Higgs Width Success of advanced cooling concepts

⇒ several ∠ 10³² [Rubbia proposal: 5∠10³²]



'novel' muon production concept: e⁺ on target

low emittance concept overcomes cooling

Exploring the potential for a Low Emittance Muon Collider

some References:

- M. Boscolo et al., "Studies of a scheme for low emittance muon beam production from positrons on target", IPAC17 (2017)
- M.Antonelli, "Very Low Emittance Muon Beam using Positron Beam on Target", ICHEP (2016)
- M.Antonelli et al., "Very Low Emittance Muon Beam using Positron Beam on Target", IPAC (2016)
- M. Antonelli, "Performance estimate of a FCC-ee-based muon collider", FCC-WEEK 2016
- M. Antonelli, "Low-emittance muon collider from positrons on target", FCC-WEEK 2016
- M. Antonelli, M. Boscolo, R. Di Nardo, P. Raimondi, "Novel proposal for a low emittance muon beam using positron beam on target", NIM A 807 101-107 (2016)
- P. Raimondi, "Exploring the potential for a Low Emittance Muon Collider", in Discussion of the scientific potential of muon beams workshop, CERN, Nov. 18th 2015
- M. Antonelli, Presentation Snowmass 2013, Minneapolis (USA) July 2013, [M. Antonelli and P. Raimondi, Snowmass Report (2013) also INFN-13-22/LNF Note

Also investigated by SLAC team:

- L. Keller, J. P. Delahaye, T. Markiewicz, U. Wienands:
 - ° Luminosity Estimate in a Multi-TeV Muon Collider using $e^+e^- \rightarrow \mu^+\mu^-$ as the Muon Source", MAP 2014 Spring workshop, Fermilab (USA) May '14
 - Advanced Accelerator Concepts Workshop, San Jose (USA), July '14

Idea for low emittance μ beam

```
from proton on target: p+target\to \pi/K \to \mu typically P_{\mu} \approx 100 MeV/c (\pi, K rest frame) whatever is the boost P_T will stay in Lab frame \to very high emittance at production point \to cooling needed!
```

from **direct** μ **pair production**:

Muons produced from $e^+e^-\rightarrow \mu^+\mu^-$ at \sqrt{s} around the $\mu^+\mu^-$ threshold ($\sqrt{s} \approx 0.212 GeV$) in asymmetric collisions (to collect μ^+ and μ^-)



NIM A Reviewer: "A major advantage of this proposal is the lack of cooling of the muons.... the idea presented in this paper may truly revolutionise the design of muon colliders ... "

Advantages:

- 1. Low emittance possible: θ_{μ} is tunable with \sqrt{s} in $e^+e^- \rightarrow \mu^+\mu^ \theta_{\mu}$ can be very small close to the $\mu^+\mu^-$ threshold
- 2. Low background: Luminosity at low emittance will allow low background and low v radiation (easier experimental conditions, can go up in energy)
- 3. Reduced losses from decay: muons can be produced with a relatively high boost in asymmetric collisions
- 4. Energy spread: muon energy spread also small at threshold, it gets larger as \sqrt{s} increases

Disadvantages:

• Rate: much smaller cross section wrt protons (\approx mb) $\sigma(e^+e^-\rightarrow \mu^+\mu^-)\approx 1~\mu b$ at most

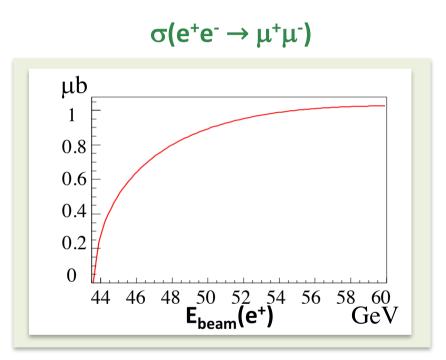
Possible Schemes

- Low energy collider with e⁺/e⁻ beam (e⁺ in the GeV range):
 - 1. Conventional asymmetric collisions (but required luminosity $\approx 10^{40}$ is beyond present capability)
 - 2. Positron beam interacting with continuous beam from electron cooling (too low electron density, 10²⁰ electrons/cm³ needed to obtain a reasonable conversion efficiency to muons)
- Electrons at rest (seems more feasible):
 - 3. e⁺ on Plasma target
 - 4. e⁺ on standard target (eventually crystals in channeling)
 - Need Positrons of ≈ 45 GeV
 - $\gamma(\mu)\approx$ 200 and μ laboratory lifetime of about 500 μ s

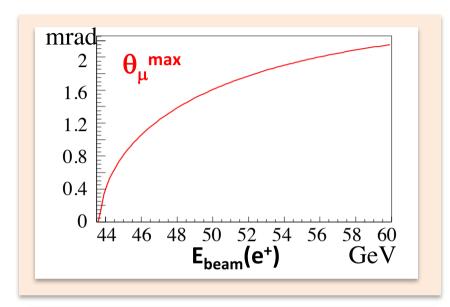


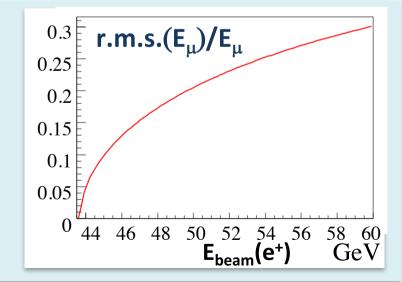
Ideally muons will copy the positron beam

Cross-section, muons beam divergence and energy spread as a function of the e+ beam energy

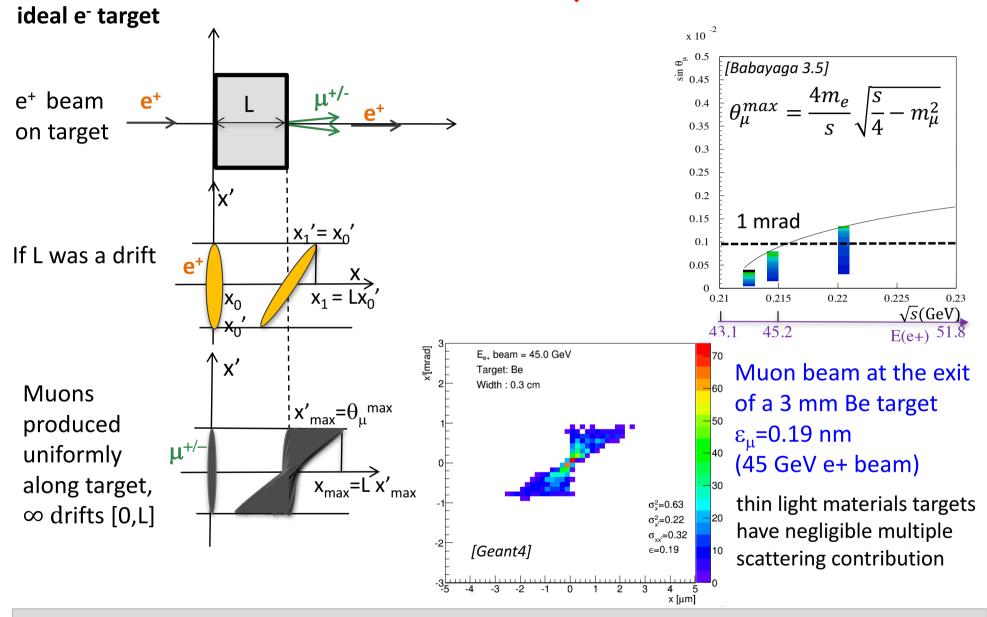


The value of sqrt(s) (i.e. E(e⁺) for atomic e⁻ in target) has to maximize the muons production and minimize the beam angular divergence and energy spread





Production contribution to μ beam emittance



The emittance contributions due to muon production angle: $\epsilon_{\mu} = x \, x'_{\text{max}}/12 = L \, (\theta_{\mu}^{\text{max}})^2/12$ $\rightarrow \epsilon_{\mu}$ completely determined by L and s -by target thickness and c.o.m. energy

Criteria for target design

Number of $\mu^+\mu^-$ pairs produced per e⁺e⁻ interaction is given by

$$N(\mu^+\mu^-)=\sigma(e^+e\to\mu^+\mu^-) N(e^+) \rho(e^-)L$$

N(e⁺) number of e⁺ ρ(e⁻) target electron density L target length

To maximise $N(\mu^+\mu^-)$:

- N(e⁺) max rate limit set by e⁺ source
- ρ(e⁻)L max occurs for L or ρ values giving total e⁺ beam loss
 - e⁻ dominated target: radiative Bhabha is the dominant e⁺ loss effect, giving a maximal $\mu^+\mu^-$ conversion efficiency $N(\mu^+\mu^-)/N(e^+) \approx \sigma(e^+e \longrightarrow \mu^+\mu^-)/\sigma_{rb} \approx 10^{-5}$
 - standard target: Bremsstrahlung on nuclei and multiple scattering are the dominant effects, Xo and electron density will matter $N(\mu^+\mu^-)/N(e^+) \approx \sigma(e^+e^-) + \mu^-\mu^-)/\sigma_{brem}$

Criteria for target design

Luminosity is proportional to N_{μ}^{2} 1/ ϵ_{μ}

optimal target: minimizes μ emittance with highest μ rate

- Heavy materials, thin target
 - minimize emittance (enters linearly) \rightarrow Copper has about same contributions to emittance from MS and $\mu^+\mu^-$ production
 - high e⁺ loss, Bremsstrahlung is dominant, not optimal μ rate
- Very light materials
 - maximize conversion efficiency (enters quad) → H₂
 - even for liquid need O(1m) target, $\epsilon_{\mu} \propto L \rightarrow \mu$ emittance increase
- Not too heavy materials (Be, C)
 - Allow low emittance with small e⁺ loss

optimal: not too heavy and thin

Criteria for target design

Luminosity is proportional to N_{μ}^{2} $1/\epsilon_{\mu}$ optimal target: minimizes μ emittance with highest μ rate

- Heavy materials, thin target
 - to minimize ε_{μ} : thin target ($\varepsilon_{\mu}^{\infty}$ L) with high density ρ Copper: MS and $\mu^{+}\mu^{-}$ production give about same contribution to ε_{μ} BUT high e⁺ loss (Bremsstrahlung is dominant) so $\sigma(e^{+}loss) \approx \sigma(Brem+bhabha) \approx (Z+1)\sigma(Bhabha) \rightarrow N(\mu^{+}\mu^{-})/N(e^{+}) \approx \sigma_{\mu}/[(Z+1)\sigma(Bhabha)] \approx 10^{-7}$
- Very light materials, thick target
 - maximize $\mu^+\mu^-$ conversion efficiency $\approx 10^{-5}$ (enters quad) \rightarrow H₂ Even for liquid targets O(1m) needed \rightarrow $\epsilon_{\mu} \propto$ L increase
- Not too heavy materials (Be, C)
 - Allow low ε_{μ} with small e⁺ loss $N(\mu^{+}\mu^{-})/N(e^{+}) \approx 10^{-6}$

not too heavy and thin in combination with stored positron beam to reduce requests on positron source

Application for Multi-TeV Muon Collider as an example

- Use thin target with high efficiency and small e⁺ loss
- Positrons in storage ring with high momentum acceptance
- No need of extreme beam energy spread

Preliminary scheme for low emittance µ beam production

Goal:

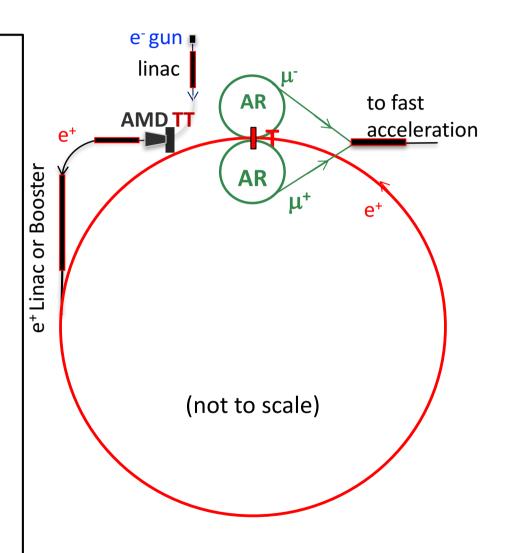
 $@T \approx 10^{11} \,\mu/s$

Efficiency $\approx 10^{-7}$ (with Be 3mm) \rightarrow 10¹⁸ e⁺/s needed @T \rightarrow

e⁺ stored beam with T

need the largest possible lifetime to minimize positron source rate

LHeC like e+ source required rate with lifetime(e+) \approx 250 turns [i.e. 25% momentum aperture (+/-12%)] \rightarrow n(μ)/n(e⁺ source) \approx 10⁻⁵



Preliminary scheme for low emittance μ beam production

from e⁺ SOURCE to RING:

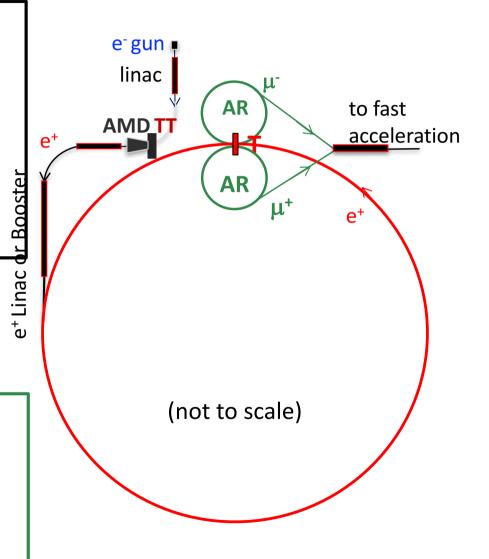
- e⁻ on conventional Heavy Thick Target (TT) for
 e⁺e⁻ pairs production.
- Adiabatic Matching Device (AMD) for e⁺ collection →
- acceleration (linac / booster), injection →

e⁺ RING:

 6.3 km 45 GeV storage ring with target T for muon production

from $\mu^+ \mu^-$ production to collider

- produced by the e⁺ beam on target T with $E(\mu) \approx 22$ GeV, $\gamma(\mu) \approx 200 \rightarrow \tau_{lab}(\mu) \approx 500 \mu s$
- AR: 60 m isochronous and high mom. acceptance rings will recombine μ bunches for ~ 1 $\tau_{\mu}^{\ \ lab} \approx 2500$ turns
- fast acceleration
- muon collider



Preliminary scheme for low emittance μ beam production

from e⁺ SOURCE to RING:

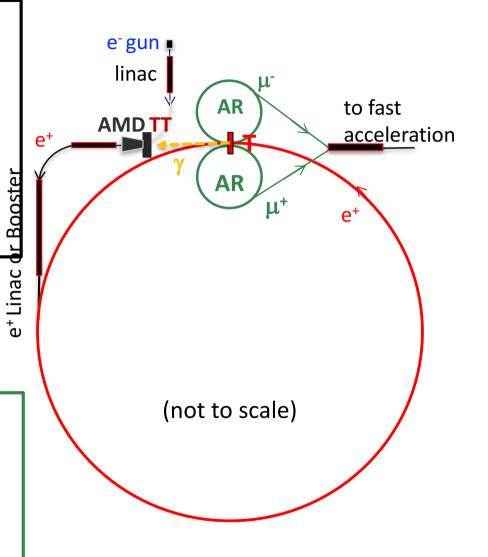
- e⁻ on conventional Heavy Thick Target (TT) for e⁺e⁻ pairs production.
- possibly with γ produced by e⁺ stored beam on $T \rightarrow$
- Adiabatic Matching Device (AMD) for e⁺ collection →
- acceleration (linac / booster), injection →

e⁺ RING:

 6.3 km 45 GeV storage ring with target T for muon production

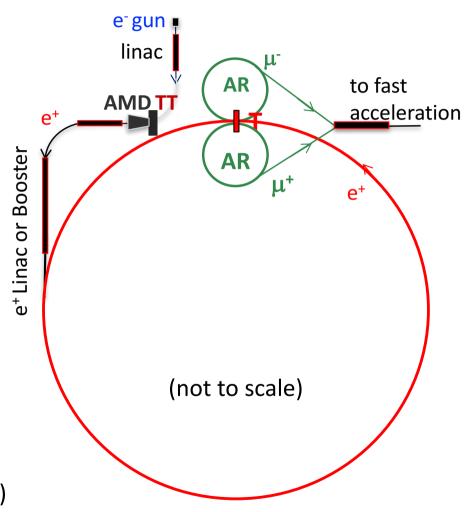
from $\mu^+ \mu^-$ production to collider

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- AR: 60 m isochronous and high mom. acceptance rings will recombine μ bunches for ~ 1 $\tau_{\mu}^{\ \ lab} \approx 2500$ turns
- fast acceleration
- muon collider



Preliminary scheme for low emittance μ beam production

e+ ring parameter	unit	
Circumference	km	6.3
Energy	GeV	45
bunches	#	100
e ⁺ bunch spacing = T _{rev} (AR)	ns	200
Beam current	mA	240
N(e+)/bunch	#	$3\cdot 10^{11}$
U_0	GeV	0.51
SR power	MW	120



(also 28 km foreseen to be studied as an option)

6 TeV μ collider draft Parameters

no lattice yet

 $\mu^{+}\mu^{-}$ rate = 9 10¹⁰ Hz [NIM A 807 ϵ_{N} = 40 nm

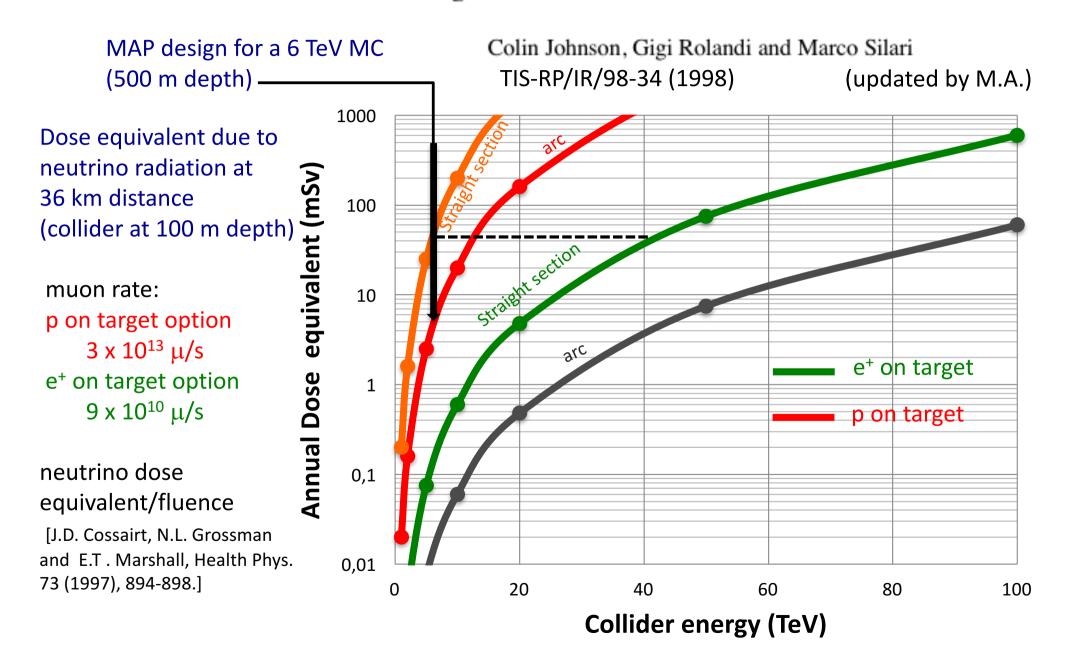
if: LHeC like e+ source with 25% mom. accept. e+ ring and ϵ dominated by μ production

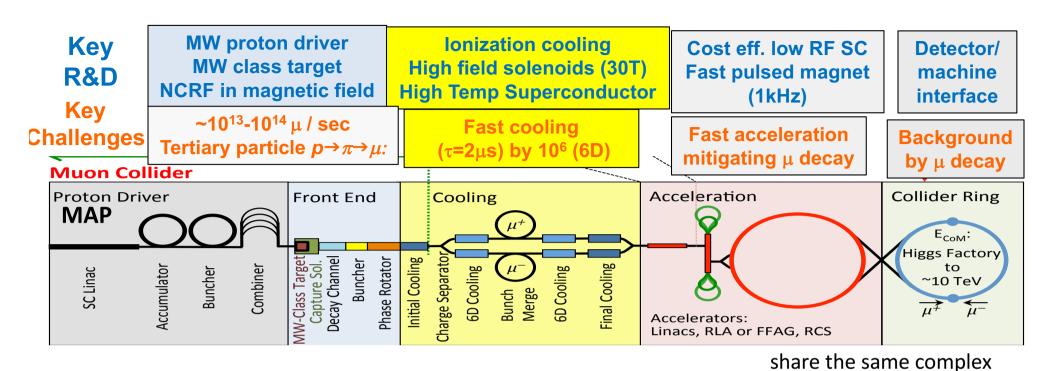
thanks to very small emittance (and lower beta*) comparable luminosity with lower Nµ/bunch (→ lower background)

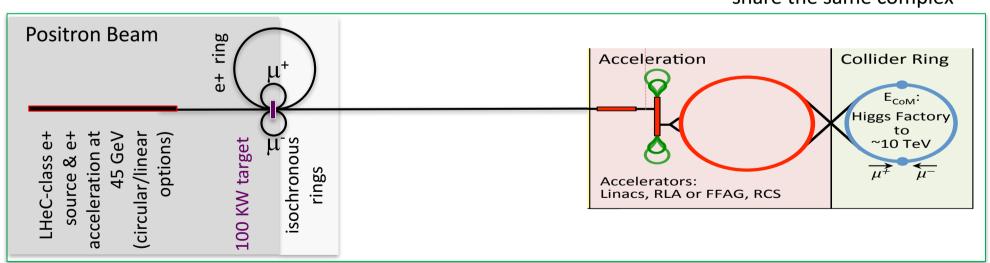
Of course, a design study is needed to have a reliable estimate of performances $\sigma_x \otimes \Gamma$

		LEMC-6TeV
Parameter	Units	
LUMINOSITY/IP	cm ⁻² s ⁻¹	5.09E+34
Beam Energy	GeV	3000
Hourglass reduction factor		1.000
Muon mass	GeV	0.10566
Lifetime @ prod	sec	2.20E-06
Lifetime	sec	0.06
c*tau @ prod	m	658.00
c*tau	m	1.87E+07
1/tau	Hz	1.60E+01
Circumference	m	6000
Bending Field	Т	15
Bending radius	m	667
Magnetic rigidity	T m	10000
Gamma Lorentz factor		28392.96
N turns before decay		3113.76
β _x @ IP	m	0.0002
β _y @ IP	m	0.0002
Beta ratio		1.0
Coupling (full current)	%	100
Normalised Emittance x	m	4.00E-08
Emittance x	m	1.41E-12
Emittance y	m	1.41E-12
Emittance ratio		1.0
Bunch length (zero current)	mm	0.1
Bunch length (full current)	mm	0.1
Beam current	mA	0.048
Revolution frequency	Hz	5.00E+04
Revolution period	s	2.00E-05
Number of bunches	#	1
N. Particle/bunch	#	6.00E+09
Number of IP	#	1.00
σ _x @ IP	micron	1.68E-02
_{σy} @ IP	micron	1.68E-02
σ _{x'} @ IP	rad	8.39E-05
σ _{y'} @ IP	rad	8.39E-05

Radiological hazard due to neutrinos from a muon collider







Key Challenges

~10¹¹ μ / sec from e+e- $\rightarrow \mu + \mu$ -

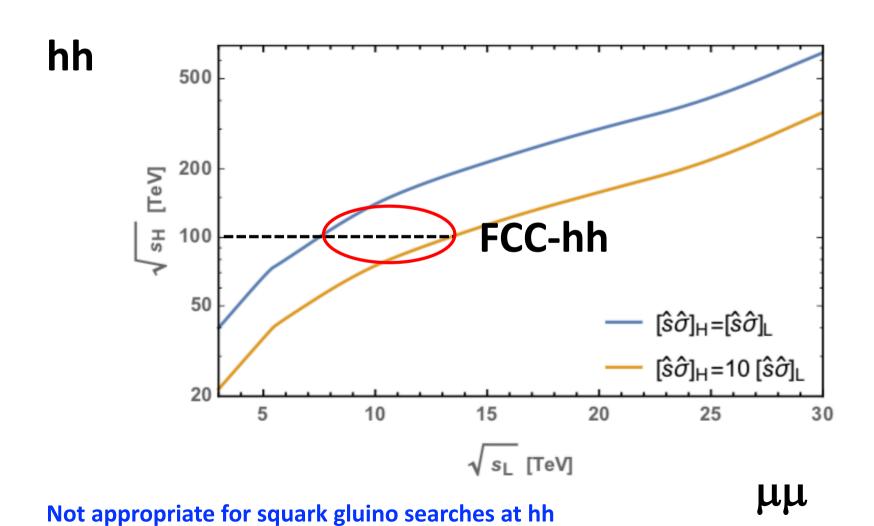
Key R&D

10¹⁵ e+/sec, 100 kW class target, NON distructive process in e+ ring

EASIER AND CHEAPER DESIGN,
IF FEASIBLE

Muon Colliders potential (hh vs μμ)

A wulzer

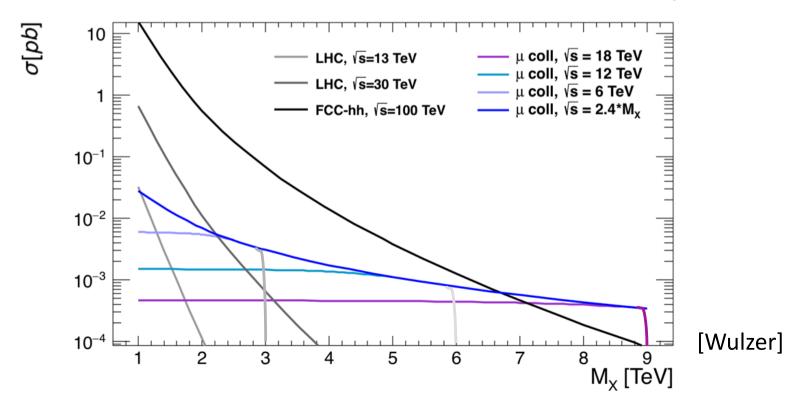


Muon collider reach: an example

- Study the same benchmark used for White Paper:
 - New heavy particles, both colored and EW charged (~vector like quarks)→ xsec can be predicted
 - FCC reach stops at M_x = 7 TeV

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 Hadron machine pays the price of the exponentially falling PDF → multi-TeV muon machine can be competitive!



CMC

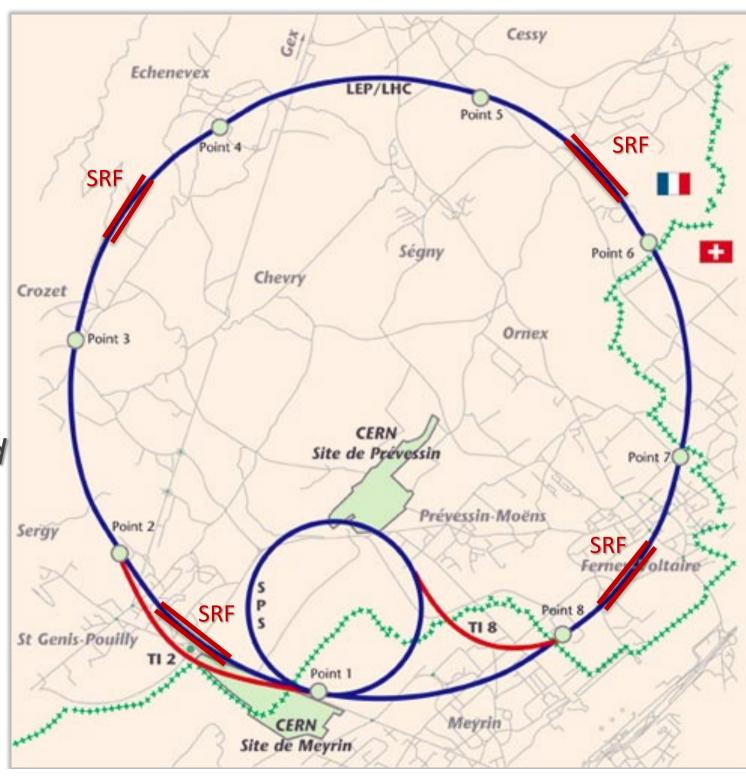
CERN Muon Collider 14 TeV cme

LHC tunnel SPS tunnel and mb PS

~7GeV SRF

Cost ~LHC

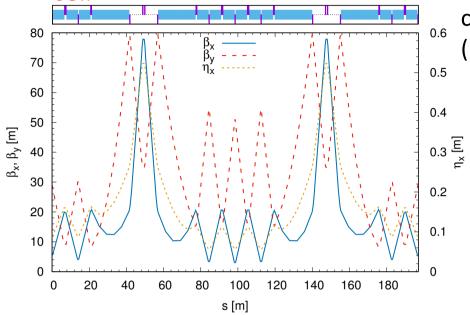
V. Shiltzev Fermilab



Key topics for this scheme

- Low emittance and high momentum acceptance 45 GeV e⁺ ring
- O(100 kW) class target in the e⁺ ring for $\mu^+ \mu^-$ production
- High rate positron source
- High momentum acceptance muon accumulator rings

Low emittance 45 GeV positron ring

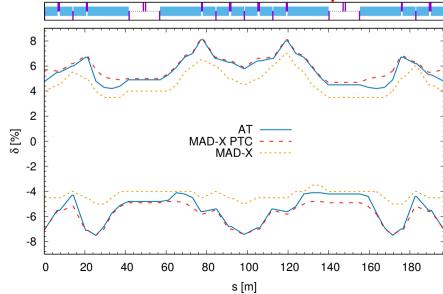


circumference 6.3 km: 197 m x 32 cells (no injection section yet)

Table e+ ring parameters

Parameter	Units	
Energy	GeV	45
Circumference	m	6300
Coupling(full current)	$\eta_{\rm o}$	1
Emittance x	m	5.73×10^{-9}
Emittance y	m	5.73×10^{-11}
Bunch length	mm	3
Beam current	mA	240
RF frequency	MHz	500
RF voltage	GV	1.15
Harmonic number	#	10508
Number of bunches	#	100
N. particles/bunch	#	3.15×10^{11}
Synchrotron tune		0.068
Transverse damping time	turns	175
Longitudinal damping time	turns	87.5
Energy loss/turn	GeV	0.511
Momentum compaction		1.1×10^{-4}
RF acceptance	$\sigma_{\!\scriptscriptstyle 0}$	± 7.2
Energy spread	dE/E	1×10^{-3}
SR power	MW	120

momentum acceptance



Physical aperture=5 cm constant no errors

Good agreement between MADX PTC / Accelerator Toolbox, both used for particle tracking in our studies

Multi-turn simulations

- 1. Initial 6D distribution from the equilibrium emittances
- 2. 6D e⁺ distribution tracking up to the target (AT and MAD-X PTC)
- 3. tracking through the target (with Geant4beamline and FLUKA and GEANT4)
- 4. back to tracking code

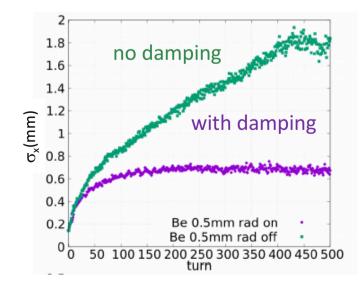
At each pass through the muon target the e+ beam

• gets an angular kick due to the **multiple Coulomb scattering**, so at each pass changes e⁺ beam divergence and size, resulting in an emittance increase.

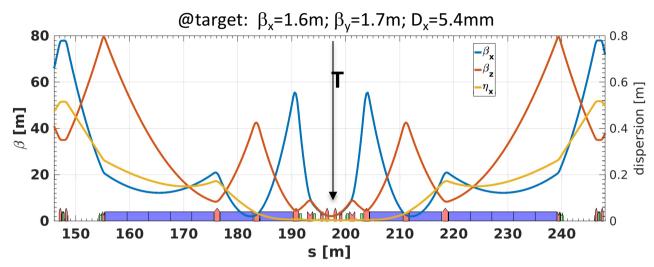
undergoes bremsstrahlung energy loss: to minimize the beam degradation due

to this effect, D_x=0 at target

 in addition there is natural radiation damping (it prevents an indefinite beam growth)

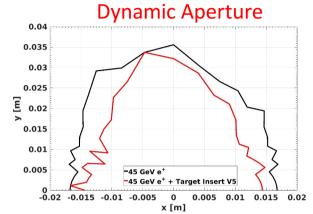


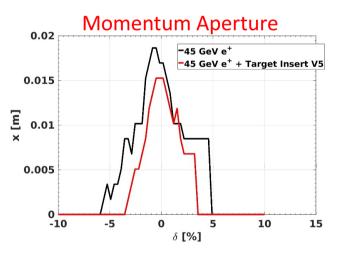
Preliminary low-β IR for muon target insertion



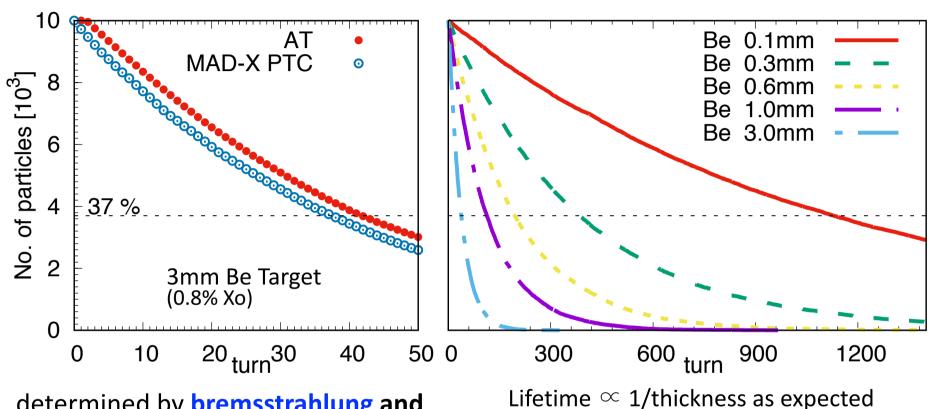


- $D_x \approx 0$
- low-β
- Further optimizations are underway:
 - match the transverse minimum beam size with constraints of target thermo-mechanical stress
 - match with other contributions to muon emittance (production, accumulation)
 - dynamic and momentum aperture can be optimized





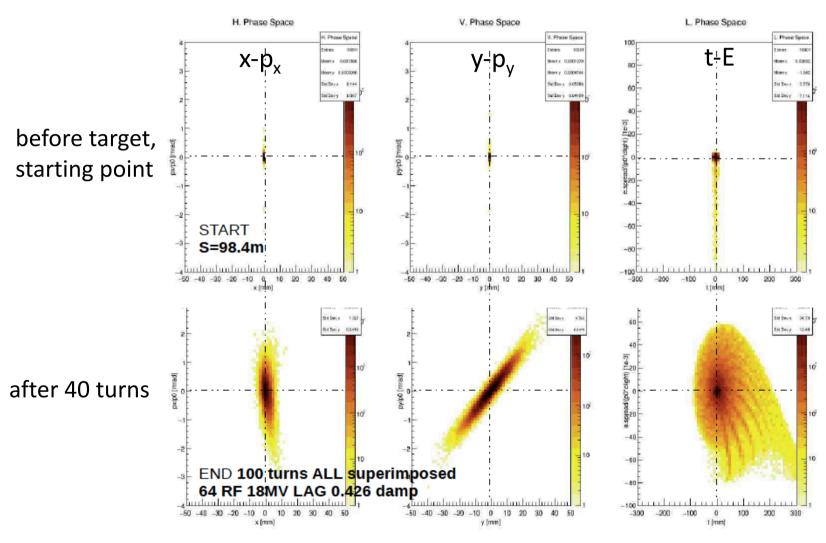
e+ lifetime with Be target



determined by bremsstrahlung and momentum acceptance
Lifetime with ~ 40 turns

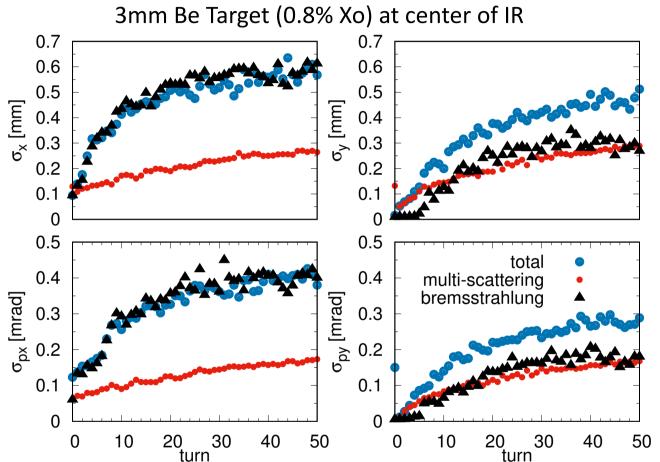
2-3% e+ losses happen in the first turn

e+ ring with target: beam evolution in the 6D phase space



MAD-X PTC & GEANT4 6-D tracking simulation of e+ beam with 3 mm Be target along the ring (not at IR center in this example)

Evolution of e+ beam size and divergence



bremsstrahlung and multiple scattering artificially separated by considering alternatively effects in longitudinal (dominated by bremsstrahlung)

and transverse (dominated by multiple scattering) phase space due to target; in blue the combination of both effects (realistic target)

Some bremsstrahlung contribution due to residual dispersion at target multiple scattering contribution in line with expectation: $\sigma_{MS} = \frac{1}{2} \sqrt{n} \sigma'_{MS} \beta$ one pass contribution due to the target: $\sigma'_{MS} = 25 \, \mu rad$

n number of turns

Control of emittance growth

Emittance growth controlled with proper lattice parameters

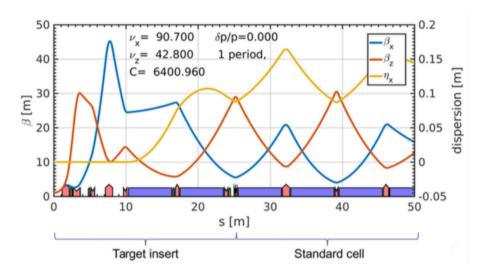
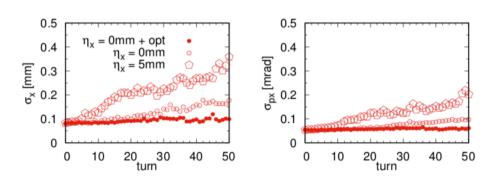
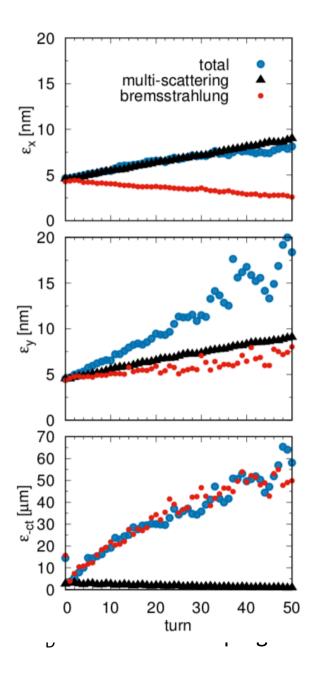


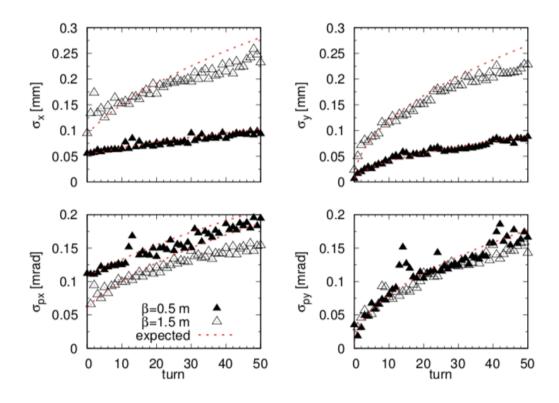
FIG. 9. Target insertion region and 25 m of the cell.





Control of emittance growth

Emittance growth controlled with proper lattice parameters



multiple scattering contribution in line with expectation: one pass contribution due to the target: $\sigma'_{MS}=25~\mu rad$

$$\sigma_{\rm MS} = \frac{1}{2} \sqrt{n} \sigma_{\rm MS}' \beta$$

n number of turns

Muon emittance

would like all contributions of same size

```
\varepsilon(\mu) = \varepsilon(e^+) \oplus \varepsilon(MS) \oplus \varepsilon(rad) \oplus \varepsilon(prod) \oplus \varepsilon(AR)
```

```
 \begin{array}{lll} \epsilon(e^+) &= e^+ \ emittance & knobs: \\ \hline \epsilon(MS) &= \ multiple \ scattering \ contribution \\ \hline \epsilon(rad) &= energy \ loss \ (brem.) \ contribution \\ \hline \epsilon(prod) &= \ muon \ production \ contribution \\ \hline \epsilon(AR) &= \ accumulator \ ring \ contribution \\ \hline \end{array} \qquad \begin{array}{ll} knobs: \\ \hline \beta_x \ \beta_y \ @target \ \& \ target \ material \\ \hline \beta_x \ \beta_y \ D_x \ @target \ \& \ target \ material \\ \hline E(e^+) \ \& \ target \ thickness \\ \hline AR \ optics \ \& \ target \\ \hline with \ constraints \ from \ target \ survival. \\ \hline \end{array}
```

now: $\varepsilon(\mu)$ dominated by $\varepsilon(MS) \oplus \varepsilon(rad)$ -> lower β -functions at target with beam spot at the limit of the target survival

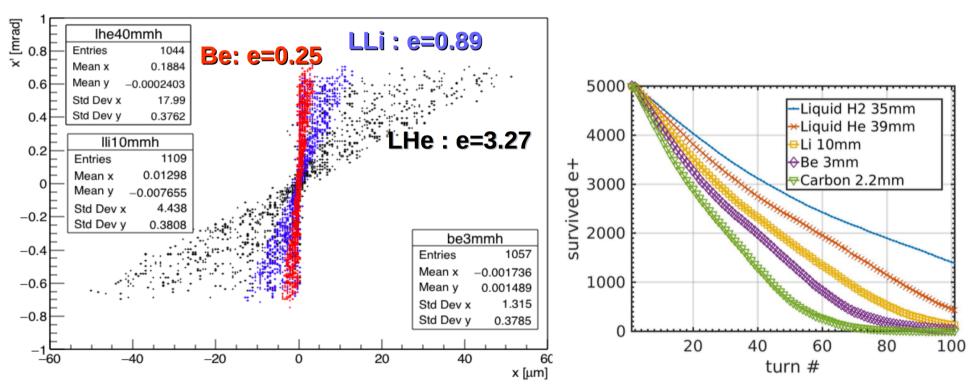
also test different material

- crystals in channeling better: $\varepsilon(MS)$, $\varepsilon(rad)$, $\varepsilon(prod)$ (also gain in lifetime)
- light liquid jet target better: $\varepsilon(MS)$, $\varepsilon(rad)$ also gain in lifetime & target power removal

Going to lighter targets for μ production

Be Beryllium

LLi Liquid Lithium, might be a good option (Proposed/tested for targets for n production) **LHe** Liquid Helium



e = muon emittance at production $[10^{-9}\text{m-rad}]$ E(e⁺)=45 GeV

Look to light liquid targets to reduce problems of thermo-mechanical stresses

Target: thermo-mechanical stresses considerations

Beam size as small as possible (matching various emittance contribution), but

- constraints for power removal (200 kW) and temperature rise
- to contrast the temperature rise
 move target (for free with liquid jet) and
 e+ beam bump every 1 bunch muon accumulation
- Solid target: simpler and better wrt temperature rise
 - Be, C

Be target: @HIRadMat safe operation with extracted beam from SPS, beam size 300 μ m, N=1.7x10¹¹ p/bunch, up to 288 bunches in one shot [Kavin Ammigan 6th High Power Targetry Workshop]

- Liquid target: better wrt power removal
 - Li, difficult to handle lighter materials, like H, He
 - LLi jets examples from neutron production, Tokamak divertor
 (200 kW beam power removal seems feasible), minimum beam size to be understood

Conventional options for μ target

- Aim at bunch ($3x10^{11}$ e⁺) transverse size on the 10 μ m scale: rescaled from test at HiRadMat ($5x10^{13}$ p on 100μ m) with **Be-based** targets and **C-based** (HL-LHC) [F. Maciariello *et al.*, IPAC2016]
- No bunch pileup ——— Fast rotating wheel (20000 rpm)
- Power removal by radiation cooling (see for instance PSI muon

beam upgrade project HiMB) [A. Knecht, NuFact17]]

- Need detailed simulation of thermo-mechanical stresses dynamics
 - Start using FLUKA + Ansys Autodyn (collaboration with CERN EN-STI)
- Experimental tests:
 - FACET-II available from 2019
 10¹¹ e-/bunch, 10 μm spot size, 100 Hz
 - DAFNE available from 2020, see later

μ Accumulator Rings considerations

isochronous optics with high momentum acceptance ($\delta \gtrsim 10\%$) optics to be designed

Multiple Scattering effect using one-turn matrix

beam divergence:

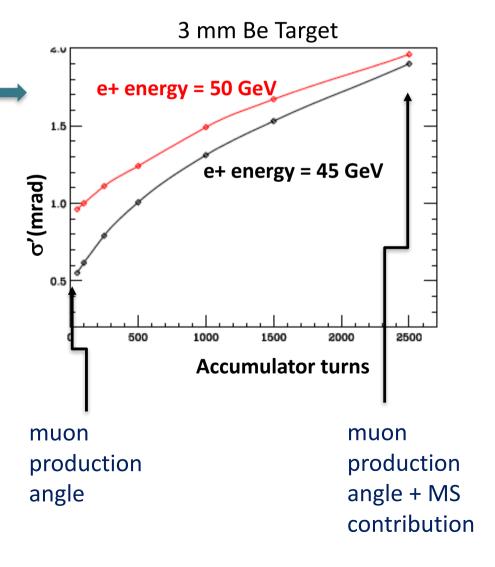
a factor 3-2 increase at 45-50 GeV w.r.t. muon production angle contribution

beam size:

depends on optics need low- β to suppress size increase

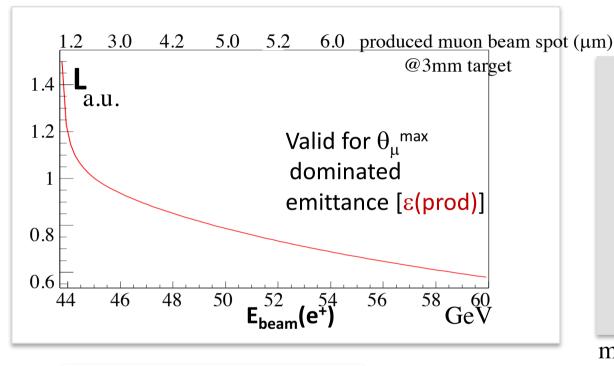
this contribution can be strongly reduced with crystals in channeling

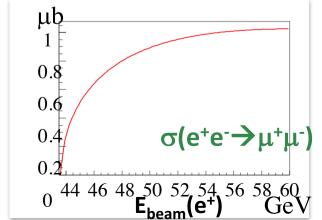
better performances at 50 GeV provided >15% momentum acceptance

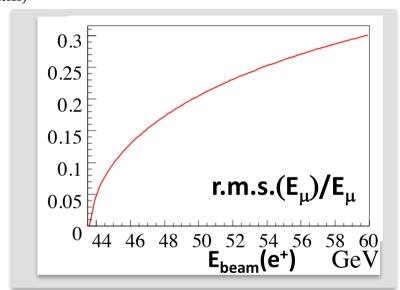


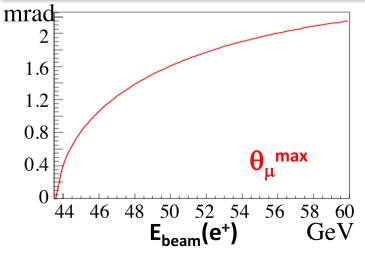
Luminosity of μ⁺μ⁻ Collider vs e⁺ beam energy

Optimal working point for $\varepsilon(e^+) \cong \varepsilon(MS) \cong \varepsilon(rad) \cong \varepsilon(prod) \cong \varepsilon(AR)$ and sustainable beam spot on target $\varepsilon(prod)$ and μ intensity ∞ positron beam energy:









Positron sources: studies on the market

• Summary of e⁺ sources projects (all very aggressive): In [F. Zimmermann, et al., 'POSITRON OPTIONS FOR THE LINAC-RING LHEC', WEPPR076 Proceedings of IPAC2012, New Orleans, Louisiana, USA]

	SLC	CLIC	ILC	LHeC	LHeC
				pulsed	ERL
E [GeV]	1.19	2.86	4	140	60
$\gamma \epsilon_x [\mu \text{m}]$	30	0.66	10	100	50
$\gamma \epsilon_y [\mu \mathrm{m}]$	2	0.02	0.04	100	50
$e^{+[10^{14}\text{s}^{-1}]}$	0.06	1.1	3.9	18	440

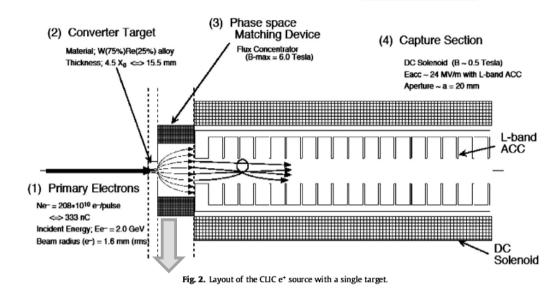
> This is a key issue to be studied

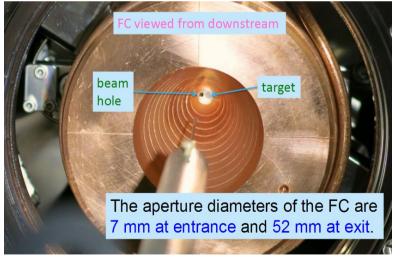
Example of Positron Source for CLIC

[L.Rinolfi et al. NIM B **309** (2013)50-55]

The target represented on the figure is a conventional one.

It would be also possible to have an hybrid positron source using a crystal providing channeling radiation and an amorphous converter for photon conversion into e+e-pairs





Flux concentrated used for the Adiabatic Matching Device (from T.Kamitani, LCWS-2014, Belgrade)

Embedded positron source?

Positron source extending the target complex? Possibility to use the γ 's from the μ production target to produce e+

e+ 45 GeV

Thin light target (eventually crystal in channeling)

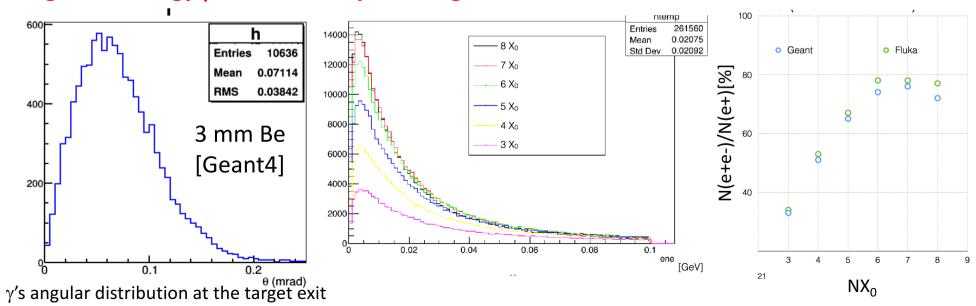
e+ e- pairs

Thick heavy target

Focusing based on AMD under study promising preliminary results on collection efficiency

Produce a fraction of e+ of the incoming positron beam

high rate energy γ thanks to very thin target and cw structure of the stored beam



FOCUSING SYSTEMS FOR POSITRON BEAMS

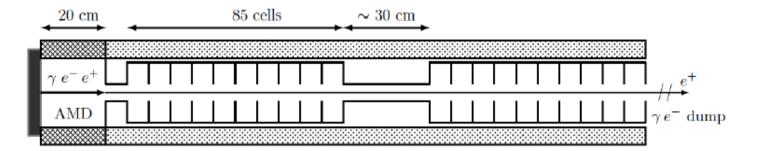
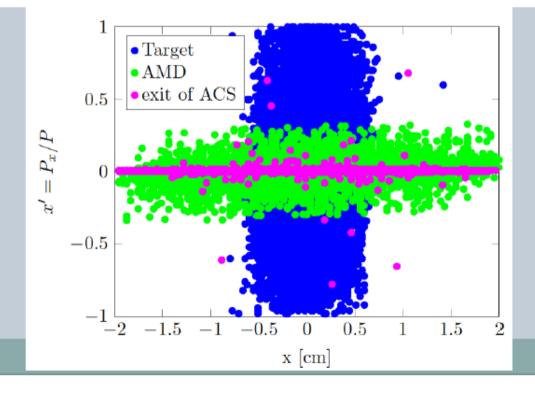


Figure 4.7: A fundamental scheme of the positron capture and primary acelerattion - A capture section based on the AMD followed by a pre-injector linac is used to capture and accelerate the positron beam up to the ~ 200 MeV.



positrons for muons

Test at DA⊕NE

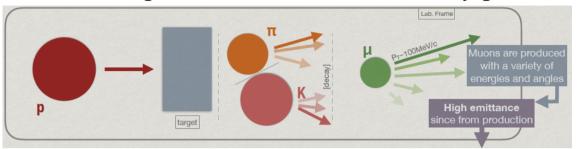
- Test of the ring-plus-target scheme:
 - beam dynamics
 - target heat load and thermo-mechanical stress

GOAL:

- Benchmark simulations with experimental data to validate LEMMA studies.
- Measurements on targets: various materials and thicknesses can be envisaged.
 - as validation for LEMMA studies
 - > interesting in the test itself

Test at CERN-NA

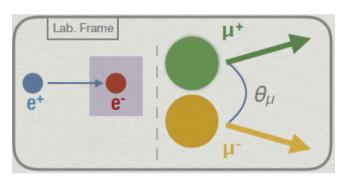
<u>Proton-based production:</u> muons as tertiary particles with tipically $P_T^{\mu} \sim 100 \text{ MeV}$



COOLING mandatory

<u>Direct production as in LEMMA proposal</u>: $e^+e^- \rightarrow \mu^+\mu^-$ close to production threshold

$$E(e^+) \sim 45 \text{ GeV} \implies E(\mu^+) \sim 22 \text{ GeV}, \ \gamma(\mu) \sim 200 \implies \tau_{LAB} \sim 500 \mu s$$

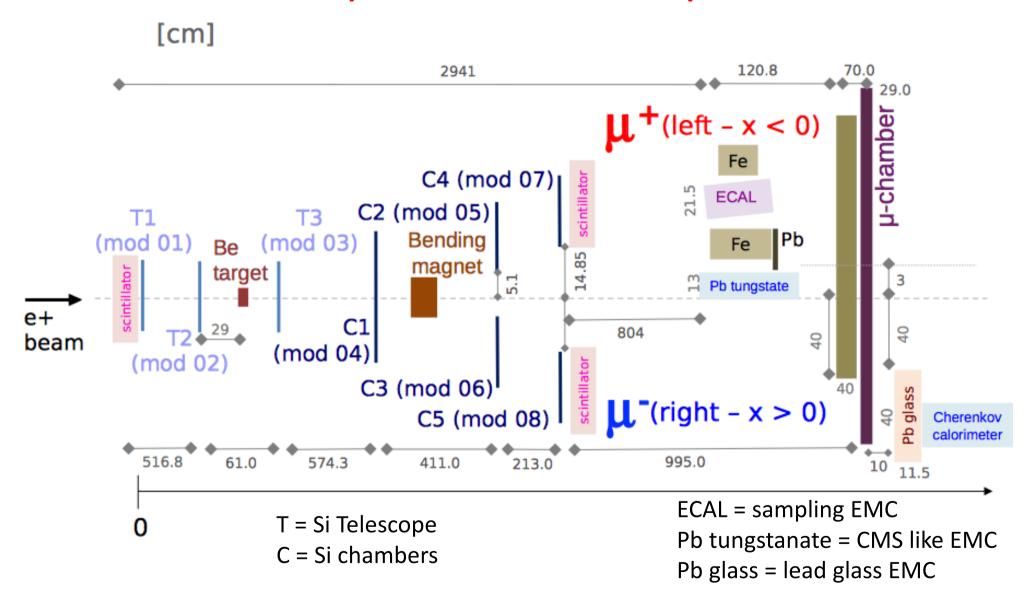


- Very small emittance => **no cooling needed!**
- Low background
- Large boost at production
 - Reduced losses from muon decays
- Much smaller muon production cross section
 - ~1µb for e^+ source vs ~1mb for proton source

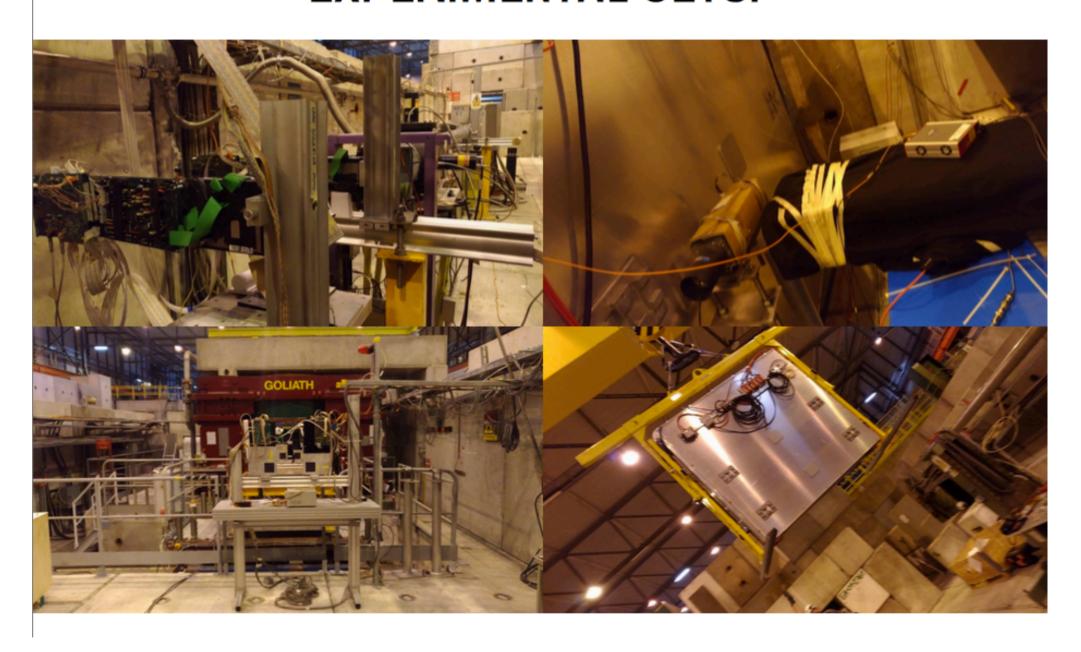
Several critical aspects must be experimentally verified to validate the approach (e.g.):

- optimization of the target features
- degradation of the positron beams (in order to recirculate)
- efficiency of the $\mu + \mu$ production, and parameters of the produced beams

Experimental set-up

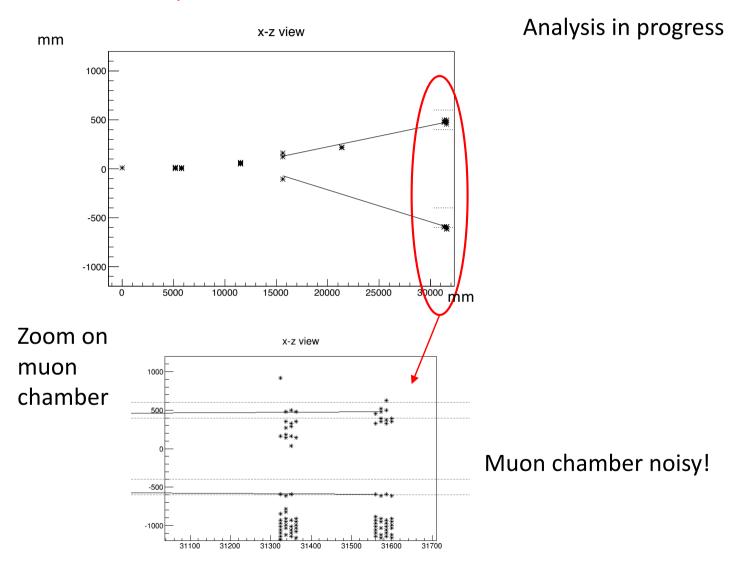


EXPERIMENTAL SETUP



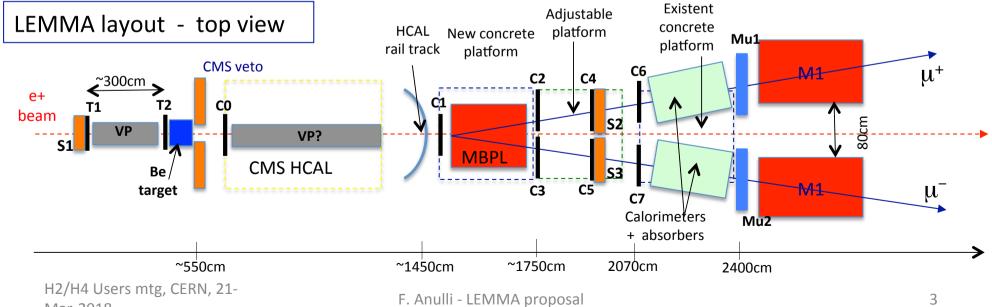
Track reconstruction based on information from silicon detectors and muon chamber

Run 4616 45 GeV positrons



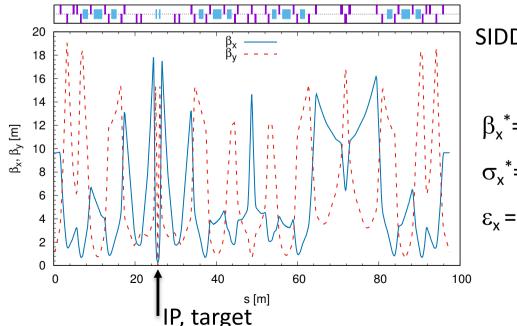
2018 Experimental layout

- Study of kinematic properties of the produced muons
 - Measure the $\mu^+\mu^-$ production rate for the provided positron beam features (momentum and energy spread)
 - Use Bhabha events for normalization
 - Measure muons momentum and emittance
- Trigger for Signal and Normalization events provided by the coincidence of the 3 scintillator S1 (intercept the incoming beam) and S2 and S3 intercepting the outcoming muons.
- Experimental setup modified with respect to the 2017 TB, also to account the different experimental hall (H4 -> H2)
 - additional tracking;
 - new calorimeters



Test at DA⊕NE

- The SIDDHARTA-2 run will end on 2019
- Test proposed after this run
- The target is at the IP:
 - To minimize modifications of the existing configuration
 - low- β and D_x=0 is needed
- First studies with the SIDDHARTA optics and target placed at the IP.
- Possible different locations for the target can be studied



SIDDHARTA 2008 optics

$$\beta_{x}^{*}$$
=26cm; β_{y}^{*} =0.9cm

$$\sigma_{x}^{*}$$
=0.27mm; σ_{v}^{*} =4.4 μ m

$$\varepsilon_x$$
 = 0.28 μ m

Goals of the Test at DA Φ NE

- Beam dynamics studies of the ring-plus-target scheme:
 - transverse beam size
 - current
 - lifetime
- Measurements on target:
 - temperature (heat load)
 - thermo—mechanical stress

Table 8: DAFNE parameters for the test with thin target at IP.

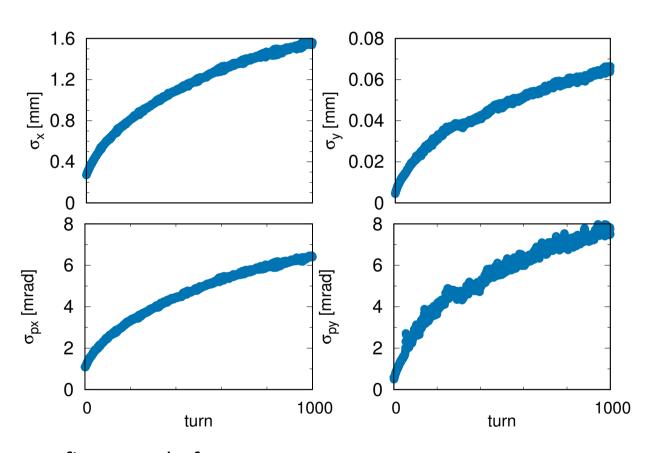
Parameter	Units	
Energy	GeV	0.51
Circumference	\mathbf{m}	97.422
Coupling(full current)	%	1
Emittance x	m	0.28×10^{-6}
Emittance y	\mathbf{m}	0.21×10^{-8}
Bunch length	$\mathbf{m}\mathbf{m}$	15
Beam current	mA	5
Number of bunches	#	1
RF frequency	MHz	368.366
RF voltage	kV	150
N. particles/bunch	#	1×10^{10}
Horizontal Transverse damping time	ms/turns	42 / 120000
Vertical Transverse damping time	ms/turns	37 / 110000
Longitudinal damping time	ms/turns	17.5 / 57000
Energy loss/turn	keV	9
Momentum compaction		1.9×10^{-2}
RF acceptance	%	± 1

Given the limited energy acceptance of the ring ($^{\sim}1\%$), we plan to insert light targets (Be, C) with thickness in the range 10-100 μ m.

Crystal targets can be foreseen too, modified G4 tool needed for the simulation

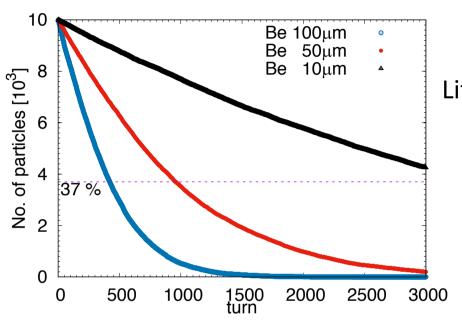
Evolution of e+ beam size and divergence

Beam evolution in the ring with 50µm Be target at IP



first turn, before target σ_x^* = 0.27 mm σ_v^* =4.4 μ m

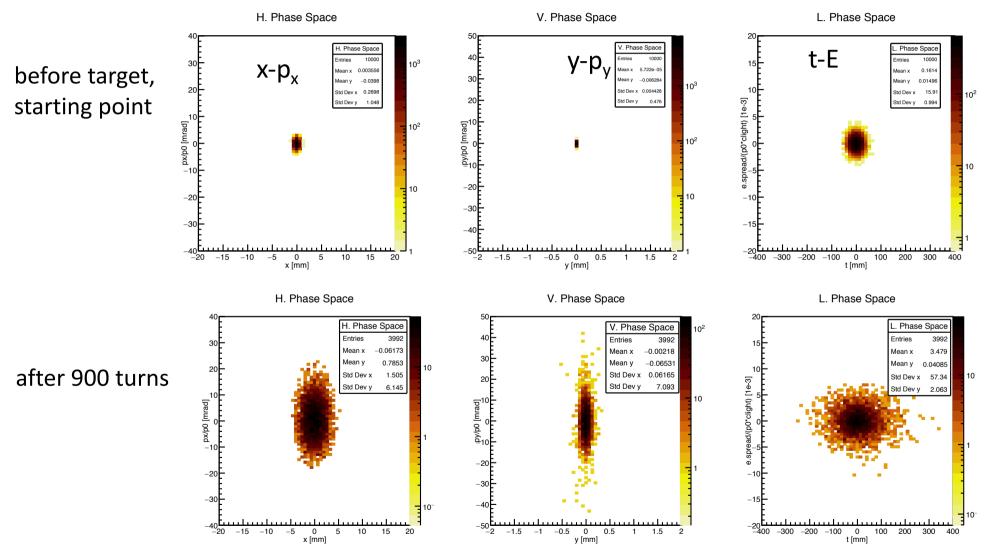
e+ lifetime with Be target



Lifetime with $^{\sim}$ 3500 turns for 10 μ m Be target as short as 1.6 ms

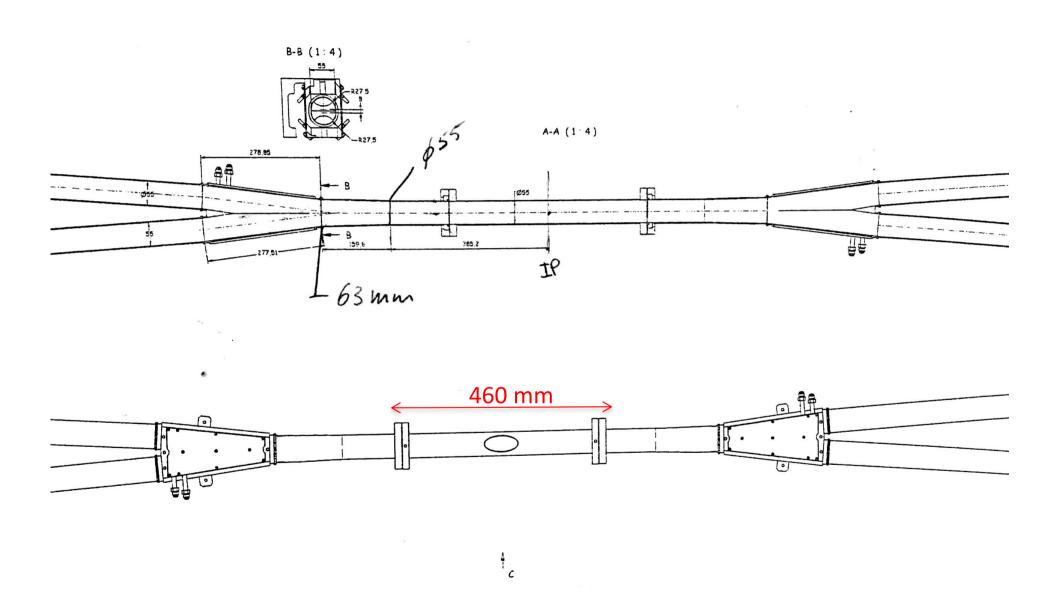
- Beam will not be stored
- Injection in single bunch mode
- turn-by-turn beam size and charge measurement

DAFNE e⁺ ring with 50µm Be target: beam evolution in the 6D phase space



MAD-X PTC & GEANT4 6-D tracking simulation

SIDDHARTA IR



M. Boscolo, MAC, LNGS, 10

Diagnostics for the test at DAFNE

beam characterization after interaction with target:

- additional beam diagnostic to be developed:
 - turn by turn charge measurement (lifetime)
 - ✓ existing diagnostic already used for stored current measurement
 - ✓ need software and timing reconfiguration
 - turn by turn beam size
 - ✓ beam imaging with synchrotron radiation
 - ✓ DAFNE CCD gated camera provides gating capabilities required to measure average beam size at each turn.
 - ✓ software modification and dedicated optics installation required.

Conclusion

- We presented a novel scheme for the production of muons starting from e⁺ beam on target
- We discussed the key challenges of this idea:
 - Low emittance and high momentum acceptance 45 GeV e⁺ ring
 - O(100 kW) class target in the e⁺ ring for $\mu^+ \mu^-$ production
 - High rate positron source
 - High momentum acceptance muon accumulator rings

First design of low emittance e⁺ ring with preliminary studies of beam dynamics

Optimization requires other issues to be preliminary addressed:

target material & characteristics e⁺ accelerator complex muon accumulator rings design luminosity parameters optimization

Preliminary studies for a low emittance muon source are promising We will continue to optimize all the parameters, lattices, targets, etc. in order to assess the ultimate performances of a muon collider based on this concept

Back-up

Accelerator design contributors

- optics and beam dynamics :
 - M. Antonelli, M. Biagini, O. Blanco, M. Boscolo, F. Collamati, S. Guiducci, L. Keller(SLAC), S. Liuzzo(ESRF), P. Raimondi(ESFR)
- positron source scheme:
 - A. Bacci, I. Chaikovska(LAL), R. Chehab(LAL), F. Collamati
- Test at DAFNE
 - D. Alesini, O. Blanco, M. Boscolo, A. Ghigo, A. Stella
- Temperature measurements of target:
 - R. Li Voti, L. Palumbo (SBAI, Sapienza)
- Target:
 - M. Iafrati, M. Ricci, L. Pellegrino,
 - M. Calviani (CERN), S. Gilardoni (CERN), P. Sievers(CERN)

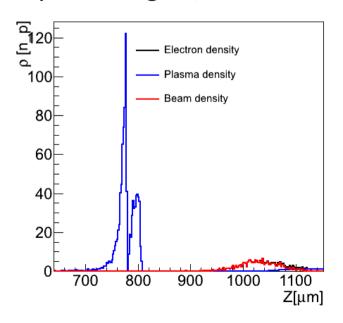
Experimental team

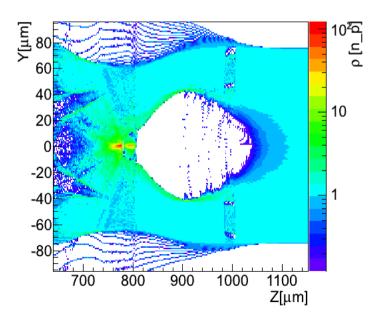
experiment at H4 CERN

M. Antonelli, F. Anulli, A. Bertolin, M. Boscolo, C. Brizzolari, G. Cavoto, F. Collamati, R. Di Nardo, M. Dreucci, F. Gonella, F. Iacoangeli, A. Lorenzon, D. Lucchesi, M. Prest, M. Ricci, R. Rossin, M. Rotondo, L. Sestini, M.Soldani, G. Tonelli, E. Vallazza, S. Vanini, S. Ventura, M. Zanetti

Few statements on the plasma option

- Plasma would be a good approximation of an ideal electron target ++ autofocussing by Pinch effect
- enhanced electron density (up x100) can be obtained at the border of the blowout region
- Simulations for $n_p=10^{16}$ e-/cm³ \Rightarrow e- high density region ~ 100 μ m (C. Gatti, P. Londrillo)
- high density region ~ 1/√n_p
- In our case plasma with $n_p \sim 10^{20}$ particles/cm³ is needed to get useful e- densities in very small region, it doesn't seem viable.





Crystals as a target?

Positrons

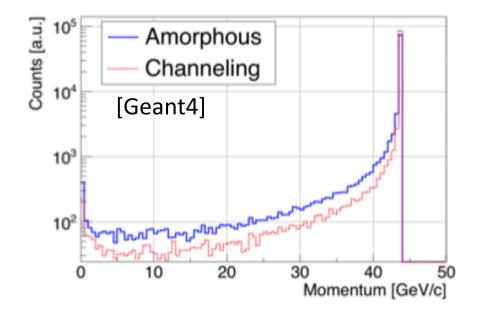
43.8 GeV e+

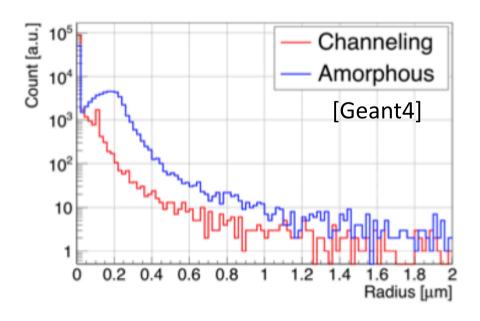
4.1 mm Si Target

Channeling plane: (110)

Momentum

Position

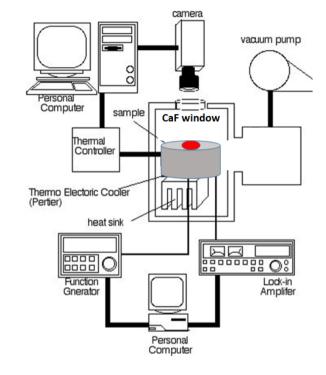




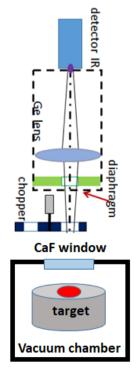
Temperature measurement in situ on the target

passive infrared:

very good spatial resolution 7.5μm~3μm/pixel. The frame rate can vary from 60Hz to 5000Hz



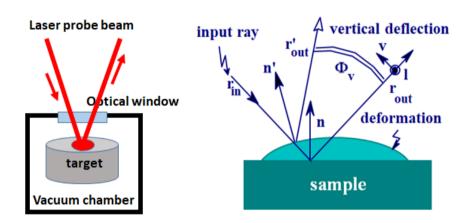
Experimental Setup - IR Emittance



Infrared radiometry:

temperature dynamics in the microsecond range, no spatial resolution

Target deformation measurement



contactless laser technique to measure indirectly the temperature.

This technique is very sensitive and can detect very weak deformation of the order of some picometer corresponding to less than 1°C. After a proper calibration can be used to follow the ultrafast dynamic of the temperature of the target

Possible target: 3 mm Be

45 GeV e⁺ impinging beam

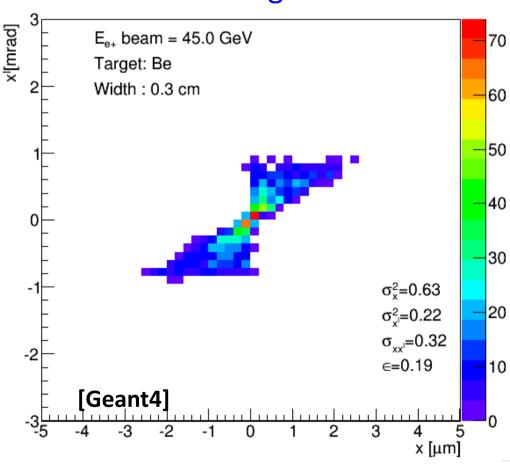
• Emittance at $E_{\mu} = 22 \text{ GeV}$:

$$\varepsilon_{x} = 0.19 \cdot 10^{-9} \text{ m-rad}$$

Multiple Scattering contribution is negligible

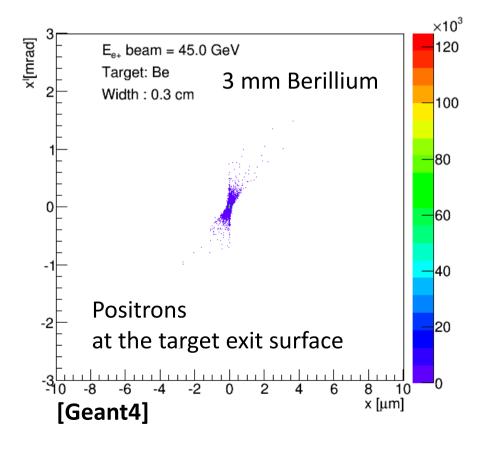
- -> μ after production is not affected by nuclei in target
- -> e+ beam emittance is preserved, not being affected by nuclei in target (see also next slide)
 - Conversion efficiency: 10⁻⁷
 - Muons beam energy spread: 9%

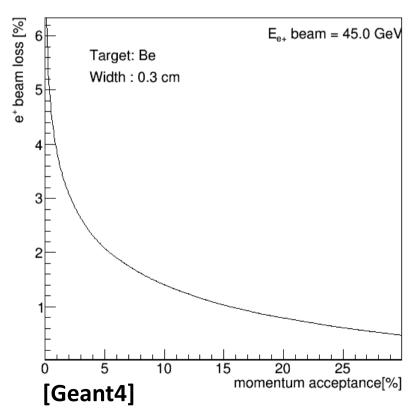
Muons at the target exit surface



Positrons Storage Ring Requirements

- Transverse phase space almost not affected by target
- Most of positrons experience a small energy deviation:
 - A large fraction of e⁺ can be stored (depending on the momentum acceptance)
 - 10% momentum acceptance will increase the effective muon conversion efficiency (produced muon pairs/produced positrons) by factor 100





Muon beam parameters

Assuming

- a positron ring with a total 25% momentum acceptance (10% easily achieved) and
- ~3 × LHeC positron source rate

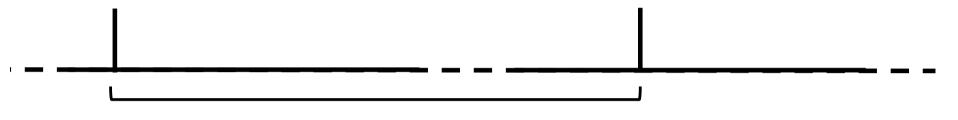
	positron source	proton source
$\mu \text{ rate[Hz]}$	$9\cdot 10^{10}$	$2\cdot 10^{13}$
μ /bunch	$4.5\cdot 10^7$	$2\cdot 10^{12}$
normalised ϵ [μ m-mrad]	40	25000

Very small emittance, high muon rates but relatively small bunch population:

The actual number of μ/bunch in the muon collider can be larger by a factor ~ τ_{μ}^{lab} (HE)/500 μs (~100 @6 TeV) by topping up.

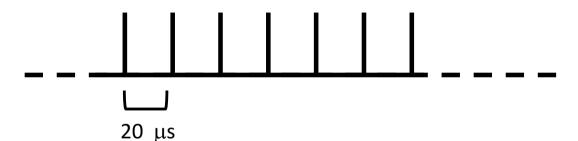
rebunching at 6 TeV

bunch structure from production



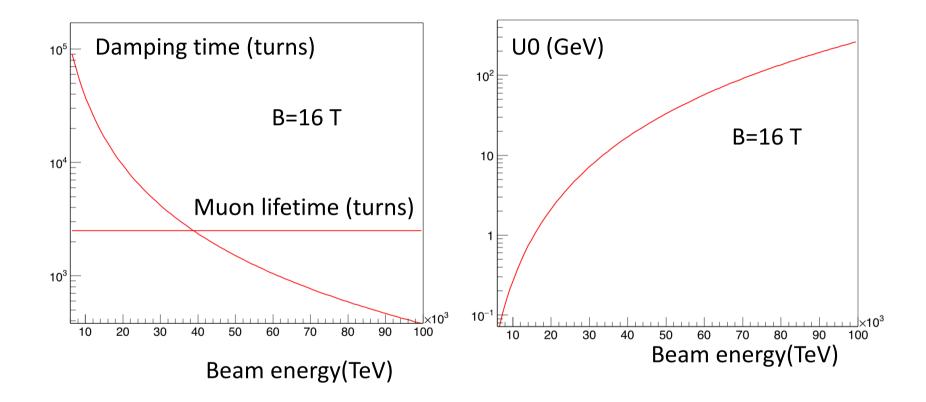
500 μs

bunch structure at collider

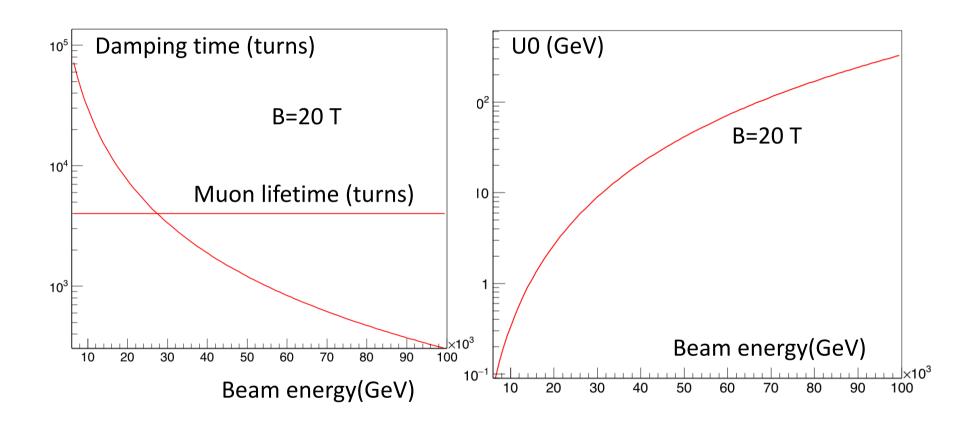


perform continuous injection every 500 μ s rebunch effective for ~ 1 muon lifetime 66 ms (factor 66/0.5) no damping -> fill transverse phase space maintaining lumi increase

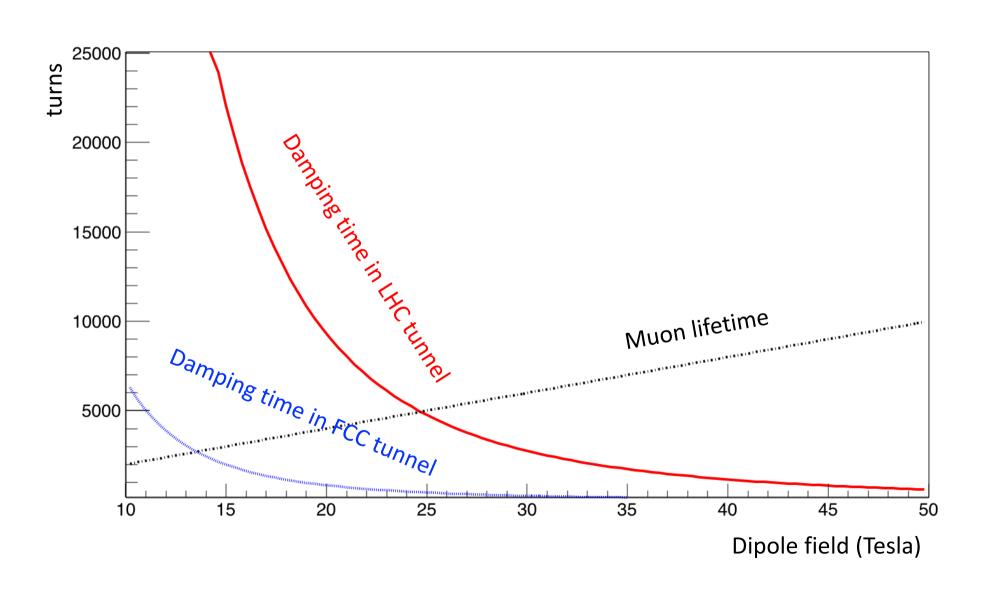
SR and damping in μ collider



SR and damping in μ collider



Damping time & muon lifetime



Solid target

 ω = 24000 turns/min

700 mm

V= 250 m/s

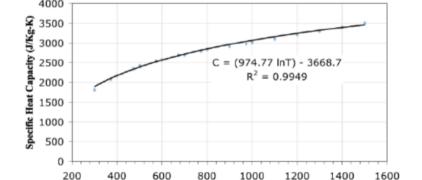
- Rotating disc
 - 24000 turns/min
 - Radial velocity V= 2 π ω (in turns) r=250 m/s
- Bunch spacing of $\Delta T = 200 \text{ns}$
 - Bunch separation on target L = V Δ T = 50 μ m
 - 12500 bunches in 1 turn

2D axisymmetric model showing effective total strain

4.9 x 10^{13} protons, $\sigma = 0.3$ mm, $\Delta T \sim 1025$ °C, 0.25 mm thick window

End of beam pulse $t = 7.2 \,\mu s$, $T_{max} \sim 1050 \,^{\circ}C$, $\varepsilon_{max} \sim 3.6 \,^{\circ}\%$

- Use 300 μm round e+ beam, 0.25 mm Be target, 5 x 10¹³ e+/b
- dE/e+ = (2.0 MeV.cm 2/g)(1.85 g/cm 3)(0.025 cm) = 0.09 MeV/e +
- dE = $5x 10^{13} 0.09 1.6 1.6 x 10^{-13} j/MeV = 0.74j$
- $dV = pi (0.025 cm)(0.03 cm)**2 = 7 x 10^{-5} cm3$ $m = dV \rho = 0.00013 g$ Cp = spec. heat Be = 1.8 j/g°C @ 373 K ; C = Cp m = 0.00024
- dT = dE/C = 3083 °C
- Cp = spec. heat Be = $2.8 \text{ j/g}^{\circ}\text{C}$ @ 1000 K ; C = Cp m = 0.0005
- dT =dE/C = 2000 °C
- x2 wrt LS-DYNA?
- Scale for $n = 3 \times 10^{11}$
- $(300\mu m)^2/200=(21\mu m)^2$



Temperature (K)

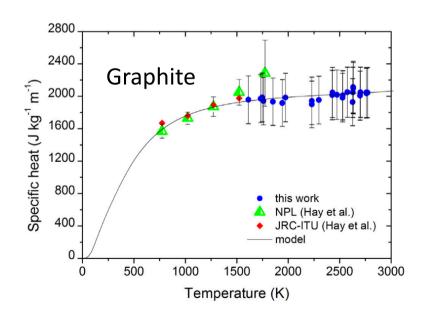
Specific Heat Capacity of Beryllium

Solid target

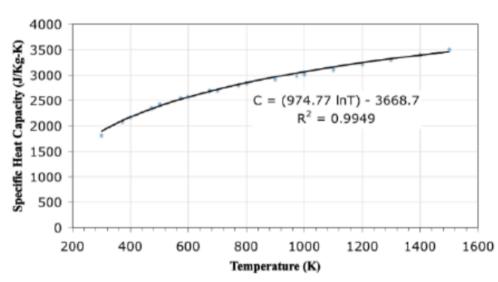
• Use 5 μ m round e+ beam, 0.3 cm Be target, 3 x 10¹¹ e+/b

$$Cp = 0.97477InT-3.6687$$

Dq = Cp DV ρ dT Q = DV ρ [(0.97477 T(lnT-1) - 3.6687 T) -0.97477 x 373(ln373-1) - 3.6687 x 373)]

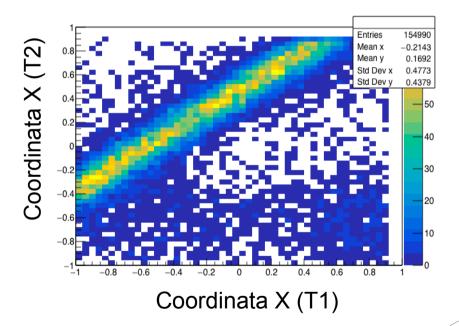


Specific Heat Capacity of Beryllium

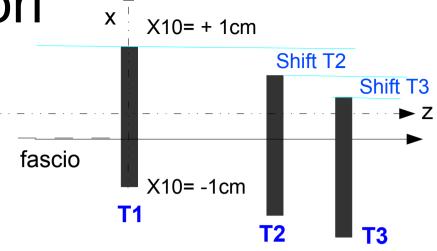


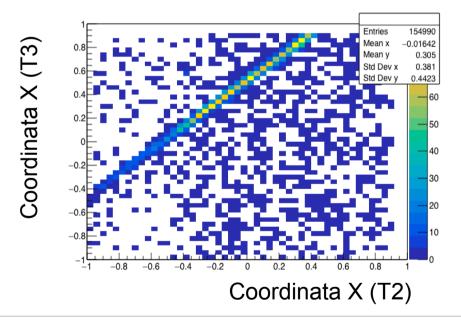
Allinemanto tracciatori

- Allineamento dei tracciatori effettuato con i run di calibrazione senza targhetta:
 - positroni da 22 GeV presi con campo magnetico diretto e invertito
 - Esempi relativi a T2 e T3 (tracciatori prima del dipolo)



Shift relativo T2 rispetto a T1: 0.5 cm Spread fascio in X: 0.26 mrad





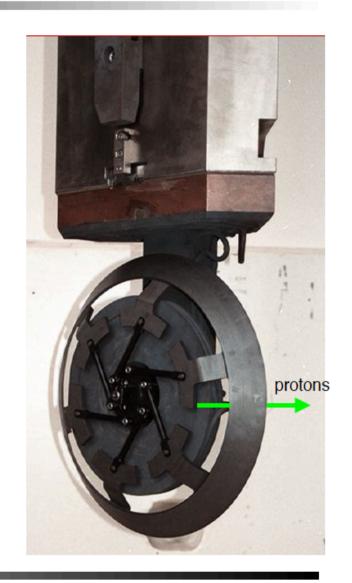
In corso allineamento dei tracciatori dopo il dipolo:

- 1) misure dei geometri
- 2) confronto tra direzioni predette e posizione misurate nei due bracci dello spettrometro

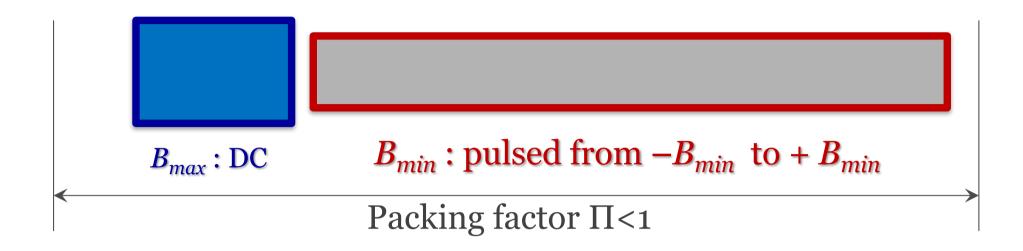
Target wheel of TgE station

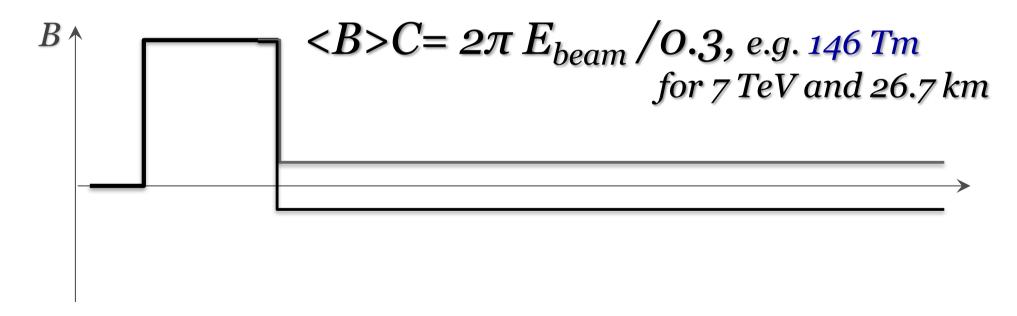


- 40 mm polycrystalline graphite
- ~40 kW power deposition
- ▶ Temperature 1700 K
- Radiation cooled @ 1 turn/s
- Beam loss 12% (+18% from scattering)



Assume RCS Acceleration





Example: 7 TeV, 26.7 km tunnel, 16T max

$$\frac{2\pi}{0.3}E_{max} = \langle B \rangle C = B_{max}\Pi C \frac{2R}{R(1+f)+1-f}$$

$$146 \text{ T} \times \text{km} \qquad 26.7 \text{km} \quad 16\text{T} \quad 0.85 \qquad 0.4=1/2.5$$

$$then: \qquad f = \frac{B_{max}}{B_{min}} \quad R = \frac{f-1}{f-4} \quad B_{min} \qquad E_{inj}$$

$$4.2 \qquad 16 \qquad 3.8\text{T} \qquad 0.45\text{TeV}$$

$$4.5 \qquad 7 \qquad 3.5\text{T} \qquad 1\text{TeV}$$

$$5 \qquad 4 \qquad 3.2\text{T} \qquad 4\text{TeV}$$

$$8 \qquad 1.75 \qquad 2.0\text{T} \qquad 9.1\text{TeV}$$

Example 2: 1 TeV, 6.9km tunnel, 16T max

$$\frac{2\pi}{0.3}E_{max} = \langle B \rangle C = B_{max}\Pi C \frac{2R}{R(1+f)+1-f}$$
20.9 T×km
6.9km 16T 0.9
0.21=1/5

then:	$f = \frac{B_{max}}{B_{min}}$	$R = \frac{f - 1}{f - 9}$	B_{min}	E_{inj}	
	10	9	1.6T	110 GeV	
	9.5	17	1.7T	60 GeV	

To sum up: 14 TeV CMC

• One can build a 14 TeV cme $\mu+\mu$ - collider at CERN if:

- Re-use tunnels 26.7km LHC, 6.9km SPS, 0.7km PS
- 16 T SC magnets (DC), need ~5 km
- Pulsed ±3.5 T magnets, with ramp ~100ms, need ~20km
- Pulsed ±2 T magnets, with ramp ~10ms, need ~6km
- Pulsed ±1 T magnet, with ramp ~1ms, need ~1km

• The $\alpha\beta\gamma$ -model predicts TPC ~12B\$ ±4

- 5B\$ SC magnets, 3B\$ NC magnets, 2B\$ SRF, 2B\$ 100MW power infrst.
- ~ cost of LHC; ~6B\$ in European accounting

"Free cookie" – if one has 24 T SC magnets

- Either 4x luminosity can be achieved with collider in SPC tunnel that requires 7 km of 24T magnets
- Or 7 TeV cme in the LHC tunnel with just 3T pulsed magnets