

# Excess Johnson noise in non-uniform TESs

Jan van der Kuur



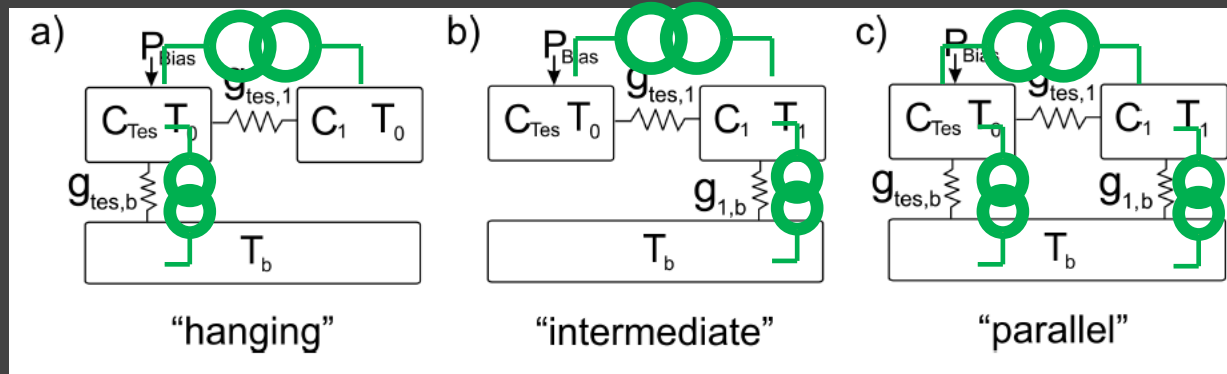
# Overview

- Background
- Non-uniformity model
- Results
- Conclusions

# Multi body models

In multi-body TES models it is assumed that:

- There is a single body TES
- One or more temperature insensitive heat capacities
- Phonon noise across each thermal link



➤ Time constants can be measured with impedance measurements

Analytical expressions in: [arXiv:1205.5693v2](https://arxiv.org/abs/1205.5693v2) (Maasilta)

# Definition M-factor noise

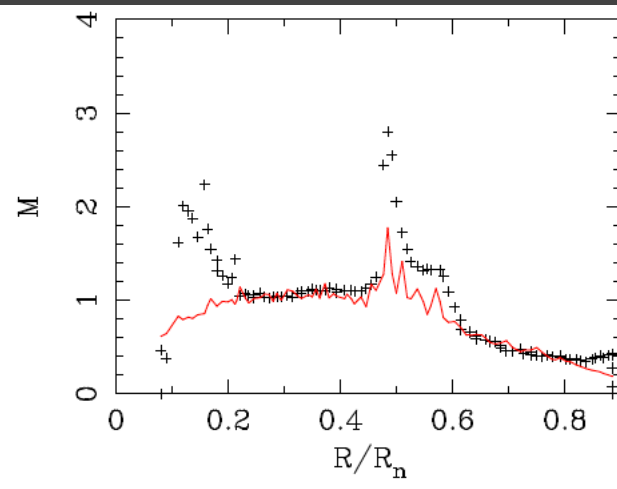
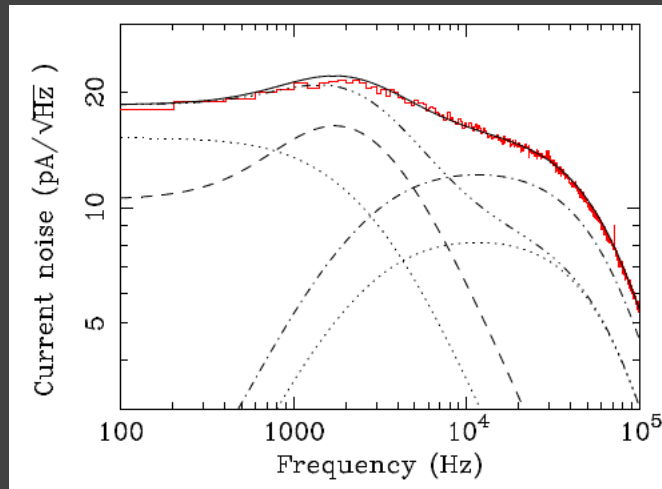
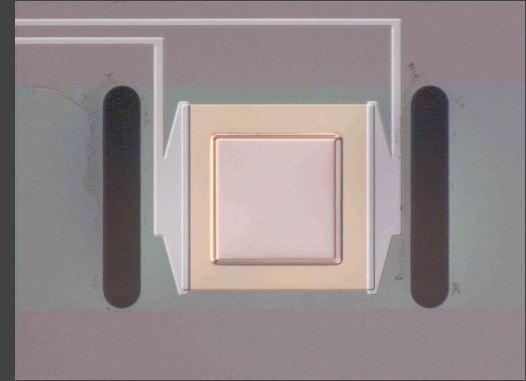
Noise which:

- cannot be explained by thermal (multi-body) models
- Cannot be explained by non-equilibrium Johnson noise
- Shows the spectral shape of Johnson noise

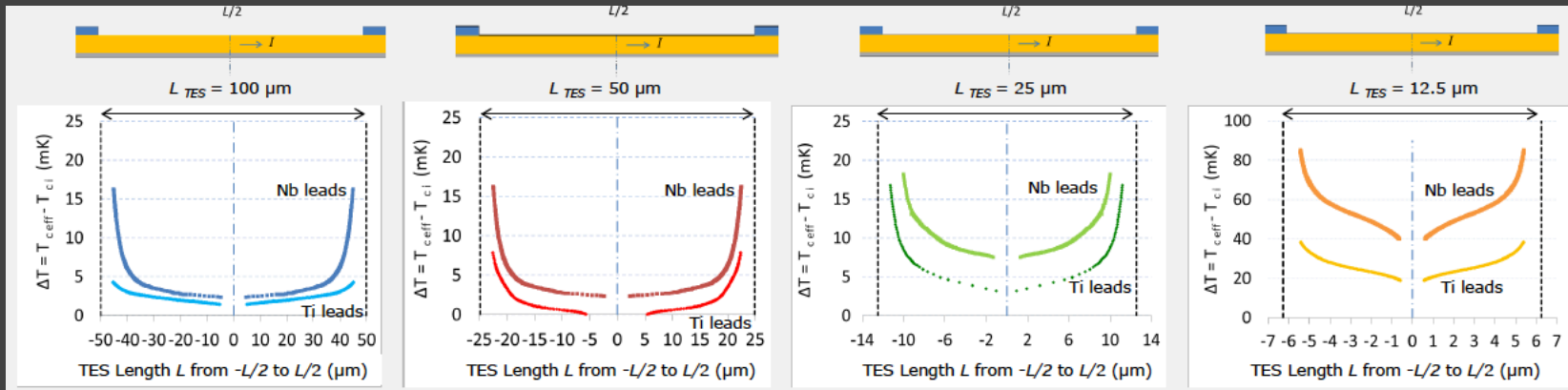
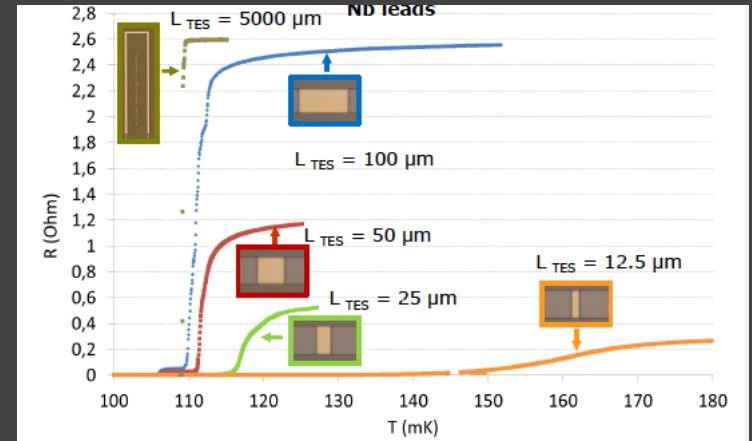
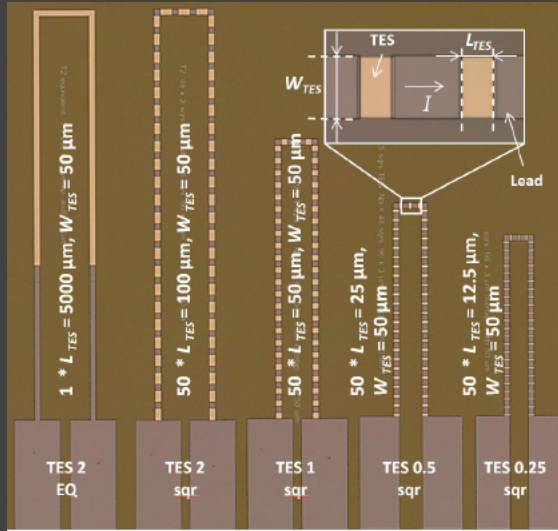
$$\sqrt{4k_bTR(1 + 2\beta)(1 + M^2)}$$

# Observed M-factor SRON pixel (old design)

- Both multibody and M-factor noise present
- M-factor peaks at high-alpha regions

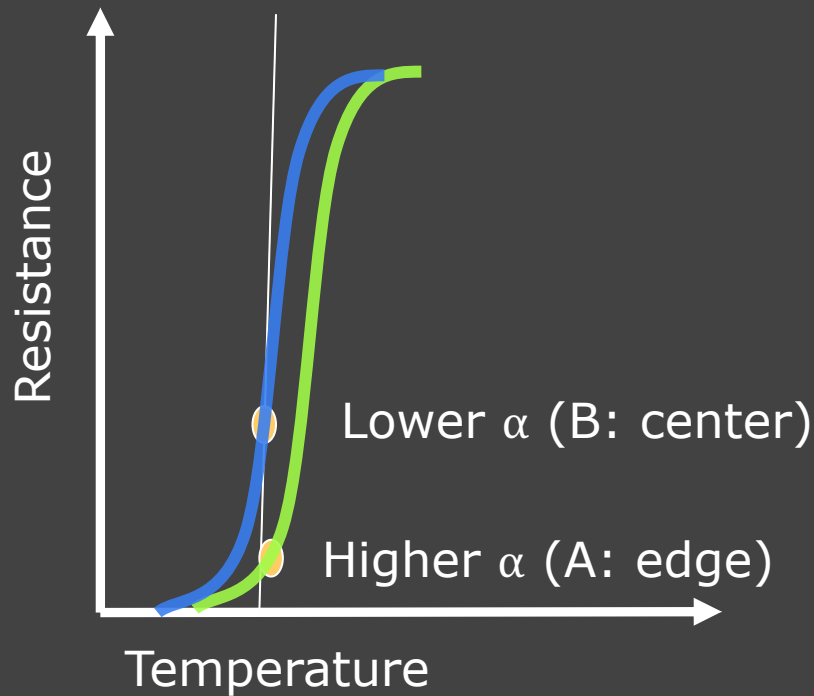


# Tc gradients observed

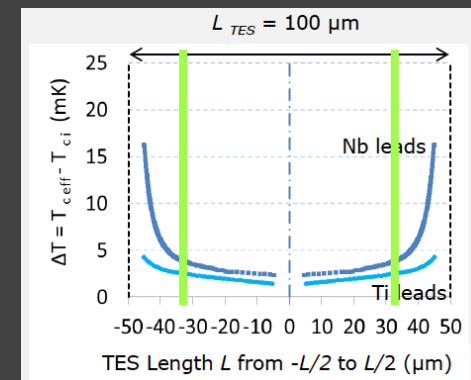
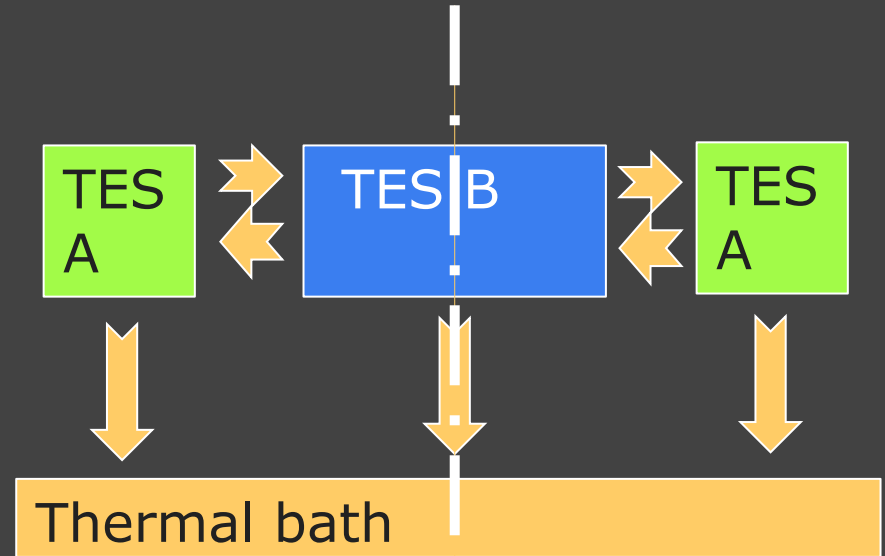


See poster M.Ridder (351)

# Translation Tc gradient in 2-body TES model



=> Net observed  $\alpha$ :  
resistance weighted average  
of  $\alpha$  of the different areas



# Internal temperature fluctuations noise (ITFN) in a non-uniform TES

- Adiabatic condition:

$$C_A \Delta T_A + C_B \Delta T_B = 0$$

-> no observable resistance change in uniform TES as net resistance change equals zero

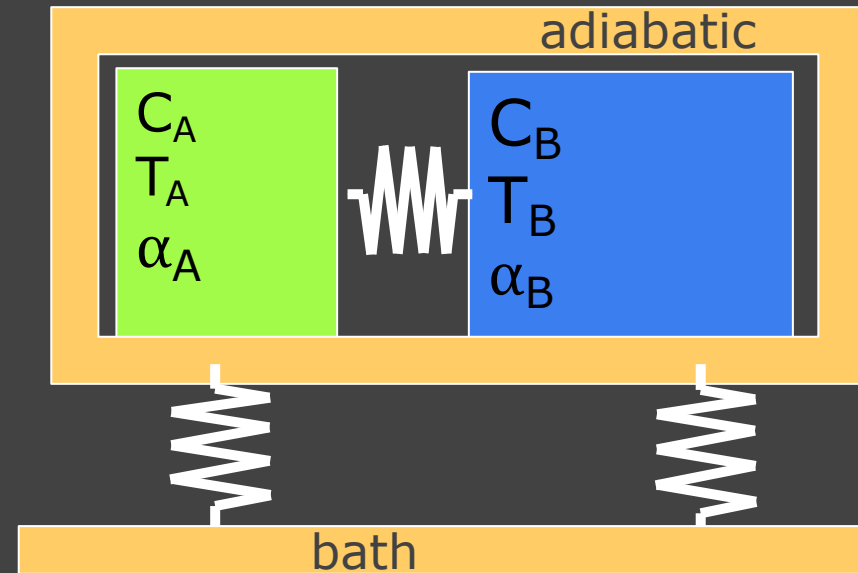
- Non-uniform TES:

$$\alpha_A \neq \alpha_B$$

=> observable ITFN when TES non-uniform

- Also: Positive internal ETF above thermal cutoff:

$$\Delta T \sim \sqrt{\frac{4\gamma k_b T^2}{G_{tes}}} \frac{1}{1 - \frac{P\Delta\alpha}{GT}}$$

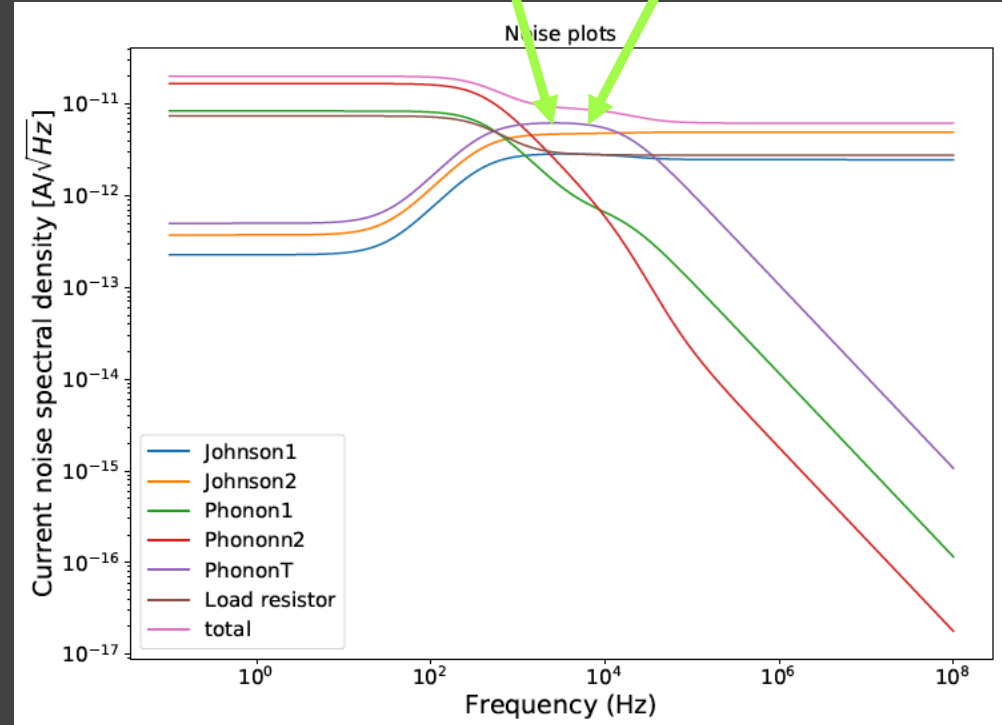
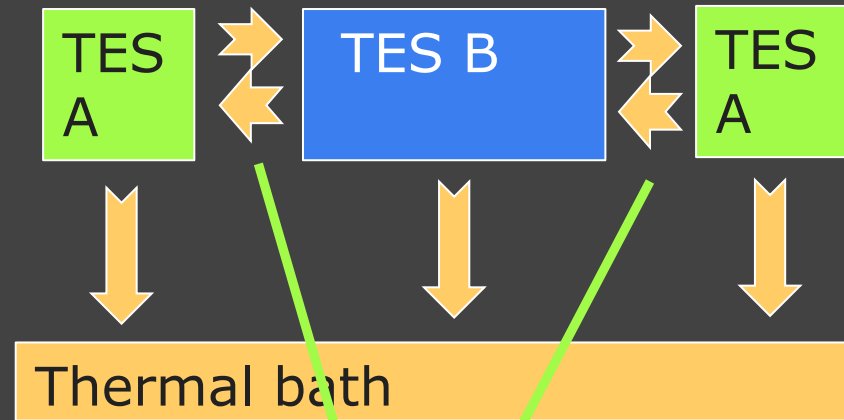




# Model calculations

Assumptions:

- Two types of TES
- Adiabatic heat exchange between TES bodies
- Internal heat conductivity  $\sim 100$  times conductivity to bath
- $\alpha_B \sim 0.4 \alpha_A$
- $M \sim 1.6$
- Impedance deviates from semi circle, like in any 2-body model



# Observations/ consequences

- Further work is needed to test the model on experimental data
- The model provides an alternative mechanism to explain 2<sup>nd</sup> order impedance observations in absorber-less TESs
- Within a uniform TES internal fluctuations do not lead to observable ITFN
- Lowering the square resistance helps to spread the noise effects over a larger bandwidth
- Normal metal bars might function as thermal shorts
- Reducing the lateral proximity effect should help to reduce the TES non-uniformity

**Thank you**