

# $E_6$ inspired $U(1)'$ Extended MSSM: From Dark Matter to LHC.

Jack Y. Araz, Gennaro Corcella, Mariana Frank, Benjamin Fuks

based on [PhysRevD96.015017](#) & [JHEP02\(2018\)092](#)

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INFN Frascati, Italy  
March 6th, 2018



- > **Introduction**
  - The Standard Model of Particle Physics
  - Problems with the Standard Model
  - Minimal Supersymmetric Extension of the SM
- > **Analysis Motivation**
  - Grand Unified Model Building
  - $U(1)'$  extended MSSM
- > **Muon Anomalous Magnetic Moment**
- > **The Dark Side of UMSSM**
- > **Heavy Z Bosons & Where to Find Them**
- > **Conclusion**



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## > Muon Anomalous Magnetic Moment

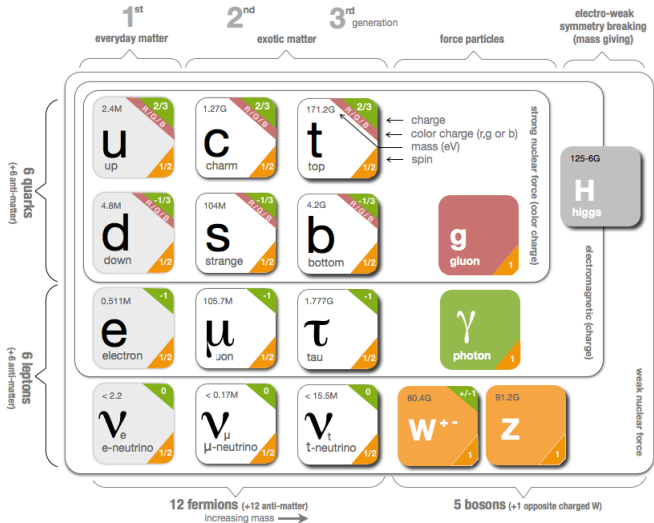
## > The Dark Side of UMSSM

## > Heavy Z Bosons & Where to Find Them

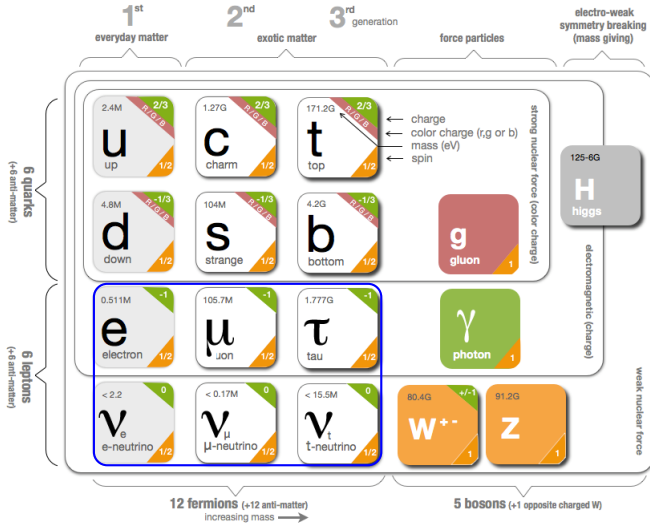
## > Conclusion



# The Standard Model of Particle Physics.



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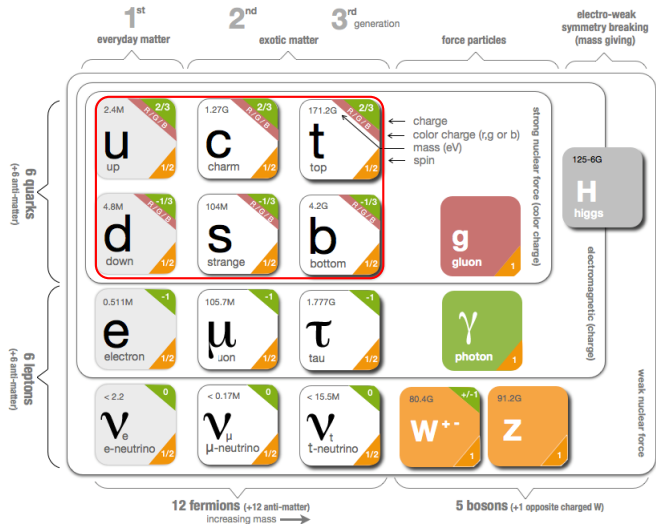


$$\mathcal{G}_{321} \equiv SU(2)_L \otimes U(1)_Y$$

	$SU(3)_C \otimes SU(2)_L \otimes U(1)_Y$	$I_3$	$Q_f [e]$
$L \equiv \begin{pmatrix} \nu_L \\ e_L \end{pmatrix}$	$(\mathbf{1}, \mathbf{2}, -1)$	$\frac{1}{2}$	0
$e_R$	$(\mathbf{1}, \mathbf{1}, -2)$	$-\frac{1}{2}$	-1
		0	-1



# The Standard Model of Particle Physics.

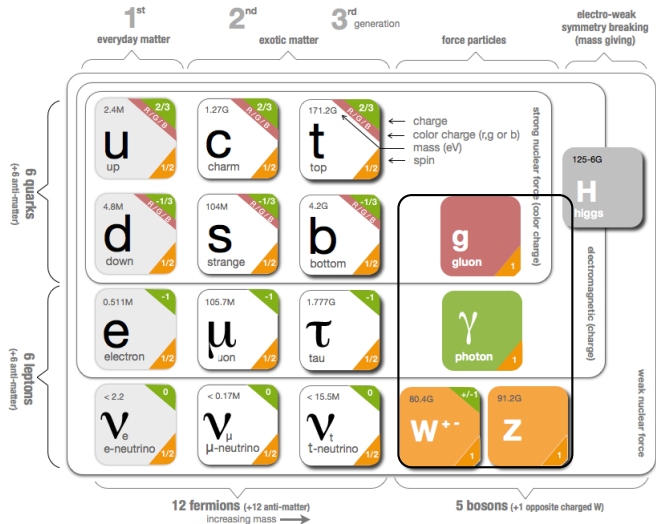


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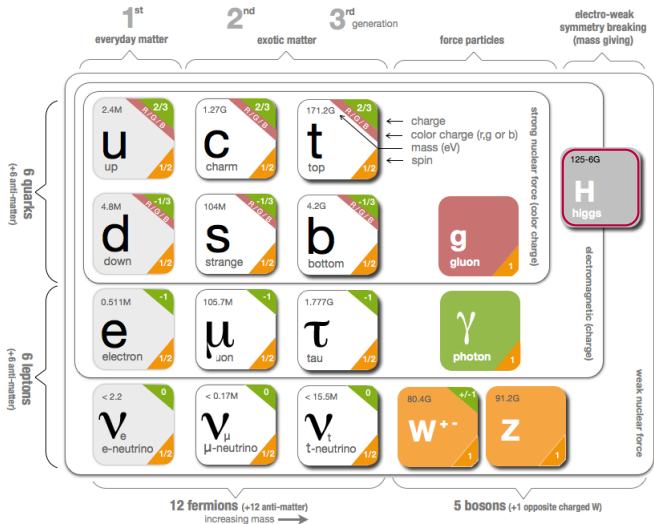


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$\Phi \equiv \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix}$	$(\mathbf{1}, \mathbf{2}, 1)$	$-\frac{1}{2}$	0

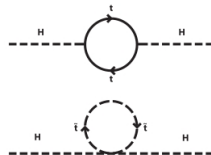
$$\mathcal{L} \equiv \frac{g_f}{\sqrt{2}} \bar{\Psi}_L \nu \Psi_R + \text{h.c.}$$





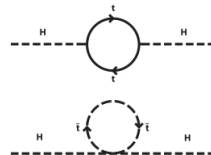
# The SM is not the chosen one!

## Gauge Hierarchy Problem!



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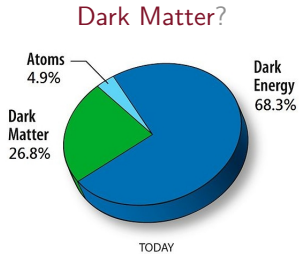
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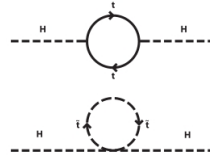
## Neutrino Mass & Oscillations!



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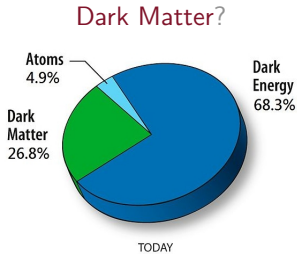
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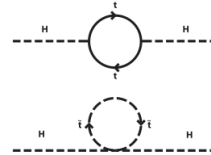
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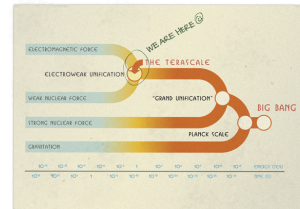
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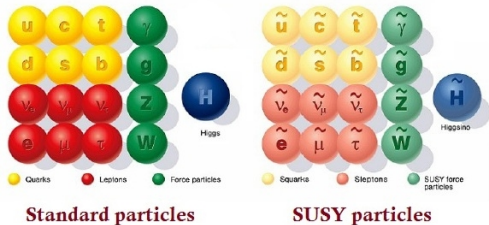
### Grand Unification!

- Supersymmetry has reasonable solutions to all of these problems.



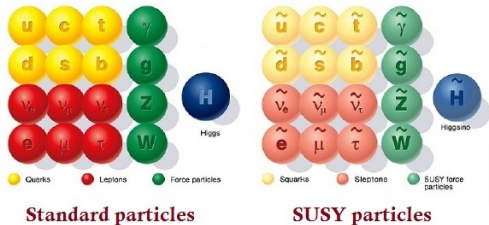
# Minimal Supersymmetric Extension of the Standard Model.

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$u_R$	$(\mathbf{\bar{3}}, \mathbf{1}, \frac{4}{3})$	0	$\frac{2}{3}$
$d_R$	$(\mathbf{\bar{3}}, \mathbf{1}, -\frac{2}{3})$	0	$-\frac{1}{3}$
$H_u \equiv \begin{pmatrix} H_u^+ \\ H_u^0 \end{pmatrix}$	$(\mathbf{1}, \mathbf{2}, 1)$	$-\frac{1}{2}$	0
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$$W = \mathbf{Y}_u \hat{u} \hat{Q} \hat{H}_u - \mathbf{Y}_d \hat{d} \hat{Q} \hat{H}_d - \mathbf{Y}_e \hat{e} \hat{L} \hat{H}_d + \mu \hat{H}_u \hat{H}_d$$

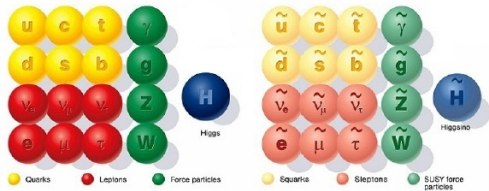
## Solutions to the SM problems:

- > Dark Matter candidate!
- > Cancellation terms to Higgs mass loop corrections.
- > Force Unification.



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Standard particles

SUSY particles

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## Solutions to the SM problems:

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## What's wrong?:

- > Neutrino mass?
- >  $\mu$  problem.
- > Proton decay!



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## What are the options?

- > Needs to be rank 4 or more.
- > Needs to satisfy the SM quantum numbers.
- > Needs to decompose to the SM group  $\mathcal{G}_{321}$ .
- $SU(n)$  ( $n \geq 5$ ),  $SO(4k + 2)$  ( $k \geq 2$ ) or  $E_6$

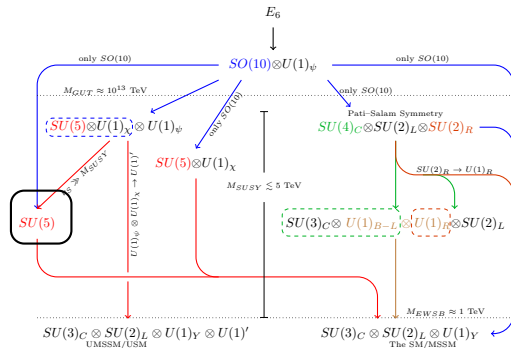


- [Slansky, R. \(1981\). Group theory for unified model building. Physics Reports, 79\(1\).](#)
- [arXiv:1801.10595](#)



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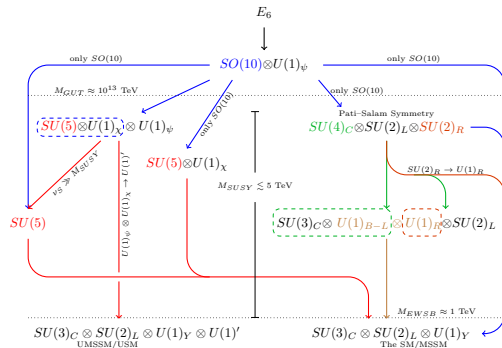
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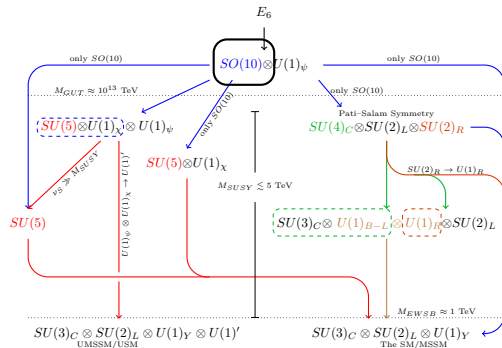
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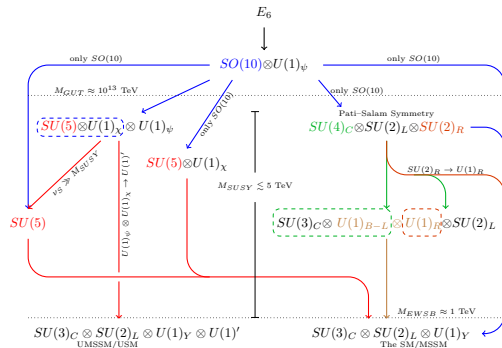
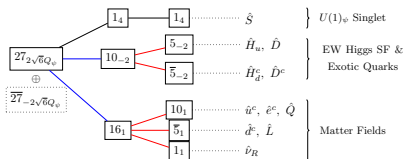


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# $U(1)'$ extended MSSM.

GUT-inspired  $U(1)'$  extended MSSM  
symmetry breaking scheme

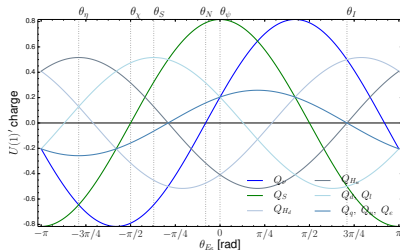
$$E_6 \longrightarrow SO(10) \otimes U(1)'_{\psi}$$

$$\longrightarrow (SU(5) \otimes U(1)'_{\chi}) \otimes U(1)'_{\psi}$$

$$Q'(\theta_{E_6}) = Q'_{\psi} \cos \theta_{E_6} - Q'_{\chi} \sin \theta_{E_6}$$

MSSM  $\otimes U(1)'$  Chiral Superfields

SF	Spin 0	Spin $\frac{1}{2}$	$U(1) \otimes SU(2) \otimes SU(3) \otimes U(1)'$
$\hat{q}$	$\tilde{q}$	$q$	$(\frac{1}{6}, \mathbf{2}, \mathbf{3}, Q_q)$
$\hat{l}$	$\tilde{l}$	$l$	$(-\frac{1}{2}, \mathbf{2}, \mathbf{1}, Q_l)$
$\hat{H}_d$	$H_d$	$\tilde{H}_d$	$(-\frac{1}{2}, \mathbf{2}, \mathbf{1}, Q_{H_d})$
$\hat{H}_u$	$H_u$	$\tilde{H}_u$	$(\frac{1}{2}, \mathbf{2}, \mathbf{1}, Q_{H_u})$
$\hat{d}$	$\tilde{d}_R^*$	$d_R^*$	$(\frac{1}{3}, \mathbf{1}, \bar{\mathbf{3}}, Q_d)$
$\hat{u}$	$\tilde{u}_R^*$	$u_R^*$	$(-\frac{2}{3}, \mathbf{1}, \bar{\mathbf{3}}, Q_u)$
$\hat{e}$	$\tilde{e}_R^*$	$e_R^*$	$(1, \mathbf{1}, \mathbf{1}, Q_e)$
$\hat{\nu}_R$	$\tilde{\nu}_R^*$	$\nu_R^*$	$(0, \mathbf{1}, \mathbf{1}, Q_\nu)$
$\hat{s}$	$S$	$\tilde{S}$	$(0, \mathbf{1}, \mathbf{1}, Q_s)$



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$$\longrightarrow (SU(5) \otimes U(1)'_{\chi}) \otimes U(1)'_{\psi}$$

$$Q'(\theta_{E_6}) = Q'_{\psi} \cos \theta_{E_6} - Q'_{\chi} \sin \theta_{E_6}$$

$$W = \mathbf{Y}_u \hat{u} \hat{q} \hat{H}_u - \mathbf{Y}_d \hat{d} \hat{q} \hat{H}_d - \mathbf{Y}_e \hat{e} \hat{l} \hat{H}_d + \mu \hat{H}_u \hat{H}_d$$

$$W_{\text{UMSSM}} = W_{\mu \rightarrow \mu_{\text{eff}}} + \mathbf{Y}_{\nu} \hat{l} \hat{H}_u \hat{\nu}_R$$

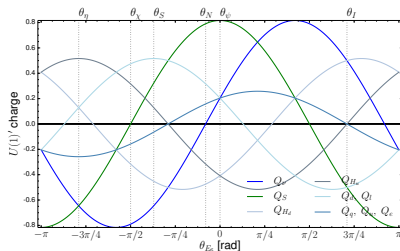
$$\mu_{\text{eff}} = \frac{\lambda v_S}{\sqrt{2}}, \quad \mu \hat{H}_u \hat{H}_d \rightarrow \lambda \hat{H}_u \hat{H}_d \hat{s}$$

$$M_{Z'}^2 = 2g'^2 (Q_{H_u}^2 \langle H_u \rangle^2 + Q_{H_d}^2 \langle H_d \rangle^2 + Q_S^2 \langle S \rangle^2)$$

- $\mu$ -problem
- Additional DM candidate
- Muon anomalous magnetic moment

MSSM  $\otimes U(1)'$  Chiral Superfields

SF	Spin 0	Spin $\frac{1}{2}$	$U(1) \otimes SU(2) \otimes SU(3) \otimes U(1)'$
$\hat{q}$	$\tilde{q}$	$q$	$(\frac{1}{6}, \mathbf{2}, \mathbf{3}, Q_q)$
$\hat{l}$	$\tilde{l}$	$l$	$(-\frac{1}{2}, \mathbf{2}, \mathbf{1}, Q_l)$
$\hat{H}_d$	$H_d$	$\tilde{H}_d$	$(-\frac{1}{2}, \mathbf{2}, \mathbf{1}, Q_{H_d})$
$\hat{H}_u$	$H_u$	$\tilde{H}_u$	$(\frac{1}{2}, \mathbf{2}, \mathbf{1}, Q_{H_u})$
$\hat{d}$	$\tilde{d}_R^*$	$d_R^*$	$(\frac{1}{3}, \mathbf{1}, \bar{\mathbf{3}}, Q_d)$
$\hat{u}$	$\tilde{u}_R^*$	$u_R^*$	$(-\frac{2}{3}, \mathbf{1}, \bar{\mathbf{3}}, Q_u)$
$\hat{e}$	$\tilde{e}_R^*$	$e_R^*$	$(1, \mathbf{1}, \mathbf{1}, Q_e)$
$\hat{\nu}_R$	$\tilde{\nu}_R^*$	$\nu_R^*$	$(0, \mathbf{1}, \mathbf{1}, Q_{\nu})$
$\hat{s}$	$S$	$\tilde{S}$	$(0, \mathbf{1}, \mathbf{1}, Q_s)$



## Universality Conditions<sup>1</sup>

### GUT Scale

- $M_{1,2,3,4} = M_{1/2}$
- $m_{\bar{q}, \bar{u}, \bar{d}}^2 = \text{diag}[M_0^2]$
- $g_1 = g_2 = g' \sqrt{3/5} \approx g_3$

### SUSY Scale

- Setting  $v_S, \lambda$  &  $A_\lambda$
- $m_{\bar{L}, \bar{e}, \bar{\nu}}^2$ ; split family
- $M_{SUSY} \leq 5 \text{ TeV}$



<sup>1</sup> Scalar soft-breaking terms,  $m_{H_{u,d}}^2$  &  $m_S^2$ , are derived from tadpole equations.



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Scanned range of the free parameters in the model.

Parameter	Scanned range	Parameter	Scanned range
$M_0$	[0, 3] TeV	$\mu$	[-2, 2] TeV
$M_{1/2}$	[0, 5] TeV	$A_\lambda$	[-7, 7] TeV
$A_0$	[-3, 3] TeV	$M_{Z'}$	[1.98, 5.2] TeV
$\tan \beta$	[0, 60]	$m_{\bar{\nu}}^2$	[-6.8, 9] TeV <sup>2</sup>
$\theta_{E_6}$	$[-\pi, \pi]$	$m_{\bar{e}, \bar{l}}^2$	[0, 1] TeV <sup>2</sup>

$$Y_\nu = \text{diag}[10^{-11}]$$

Experimental constraints imposed within our scanning procedure in order to determine the parameter space regions of interest.

Observable	Constraints	Observable	Constraints
$M_h$	$125.09 \pm 3 \text{ GeV}$	$\chi^2(\hat{\mu})$	$\leq 70$
$ \alpha_{ZZ'} $	$O(10^{-3})$	$M_{\tilde{g}}$	$> 1.75 \text{ TeV}$
$M_{\chi_{1,2}^0}$	$> 62.4 \text{ GeV}$	$M_{\chi_{1,2}^\pm}$	$> 99.9 \text{ GeV}$
$M_{\chi_{3,4}^0}$	$> 116 \text{ GeV}$	$M_{\tilde{\nu}_\tau}$	$> 103.5 \text{ GeV}$
$M_{\tilde{F}}$	$> 81 \text{ GeV}$	$M_{\tilde{E}}$	$> 107 \text{ GeV}$
$M_{\tilde{H}}$	$> 94 \text{ GeV}$	$M_{\tilde{I}}$	$> 900 \text{ GeV}$
$\text{BR}(B_s^0 \rightarrow \mu^+ \mu^-)$	$[1.1 \times 10^{-9}, 6.4 \times 10^{-9}]$	$\frac{\text{BR}(B \rightarrow \tau \nu_\tau)}{\text{BR}_{SM}(B \rightarrow \tau \nu_\tau)}$	$[0.15, 2.41]$
$\text{BR}(B^0 \rightarrow X_s \gamma)$	$[2.99, 3.87] \times 10^{-4}$		



<sup>1</sup> Scalar soft-breaking terms,  $m_{H_{u,d}}^2$  &  $m_S^2$ , are derived from tadpole equations.



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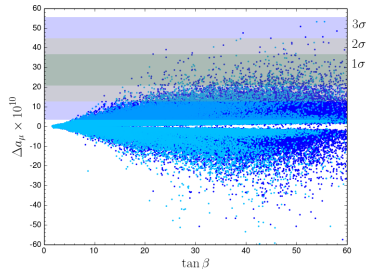
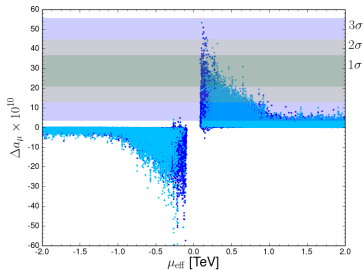
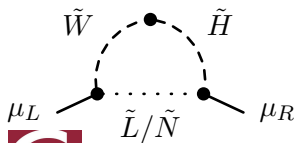
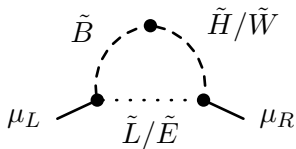


# Muon Anomalous Magnetic Moment.

$$a_\mu = \frac{g_\mu - 2}{2}$$

$$a_\mu^{\text{SM}} = a_\mu^{\text{QED}} + a_\mu^{\text{EW}} + a_\mu^{\text{Had}}$$

$$(3.4 < \Delta a_\mu < 55.6) \times 10^{-10} : 3\sigma$$

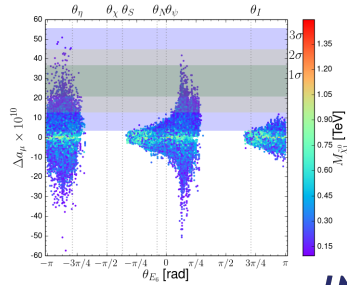
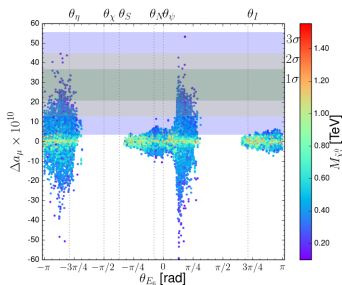
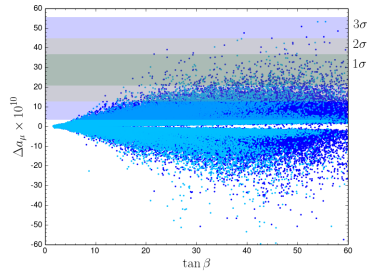
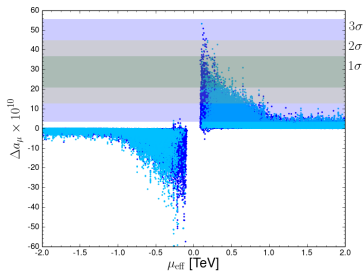
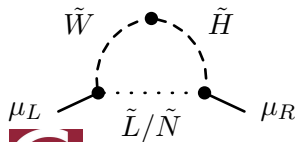
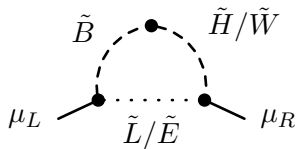


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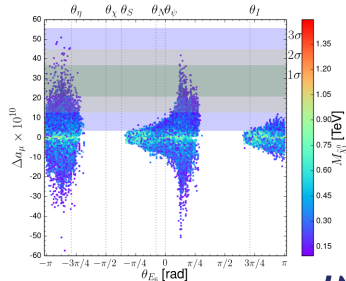
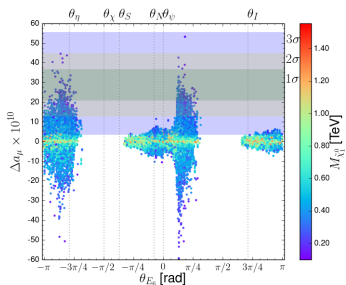
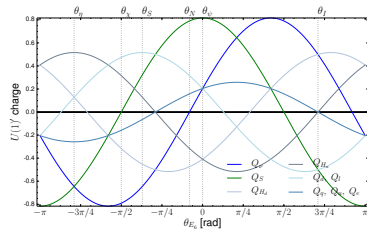
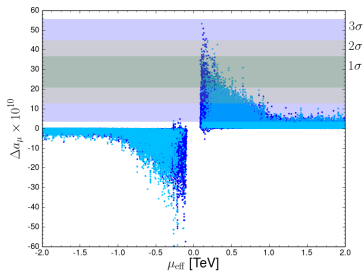
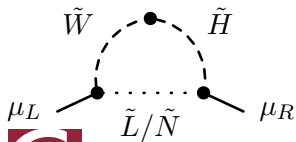
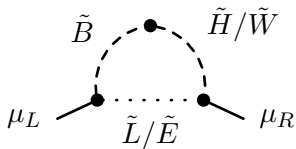


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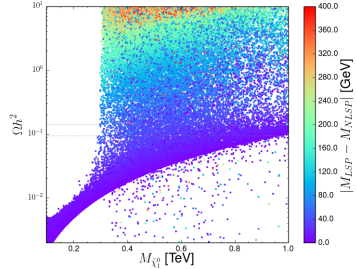
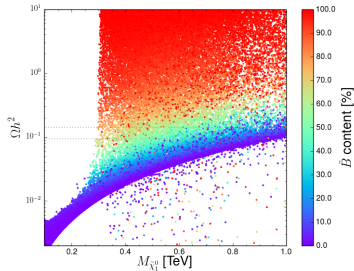
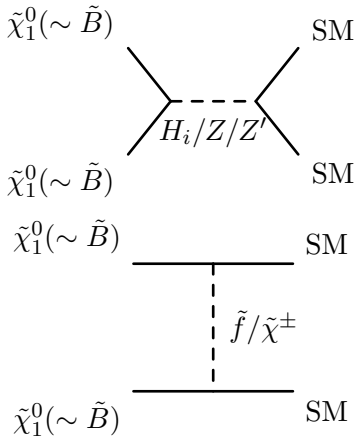
## > The Dark Side of UMSSM

## > Heavy Z Bosons & Where to Find Them

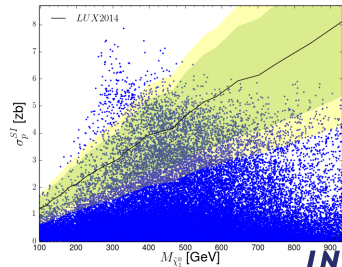
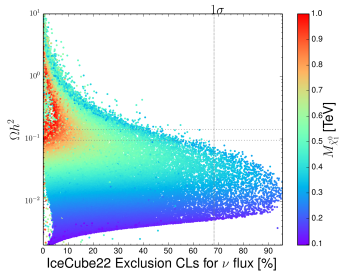
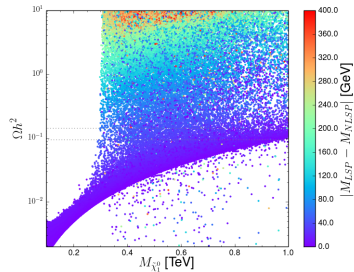
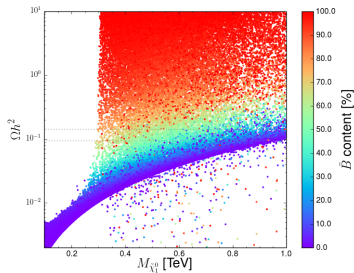
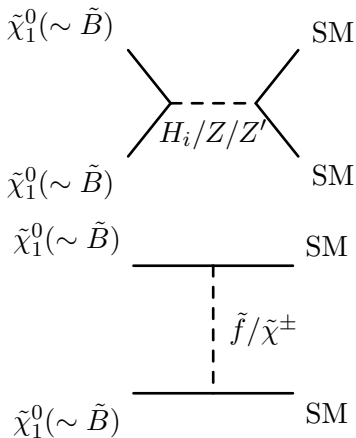
## > Conclusion



# Neutralino Dark Matter



# Neutralino Dark Matter

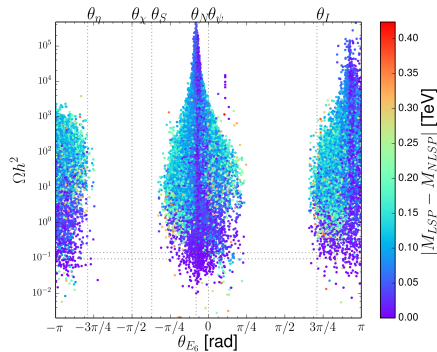




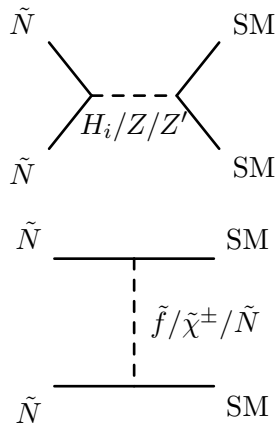
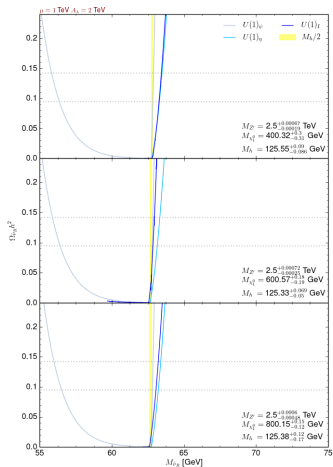
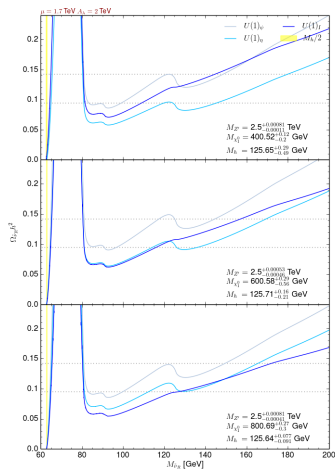
## Model based, mass scan for certain bench marks

- $\mu_{\text{eff}} = 1 - 1.7 \text{ TeV}$
- $A_\lambda = 1 - 2 \text{ TeV}$
- $M_{Z'} = 2 - 2.5 \text{ TeV}$
- $M_{\tilde{\chi}_1^0} = 400 - 600 - 800 \text{ GeV}$
- Fix slepton masses depending on  $\theta_{E_6}$

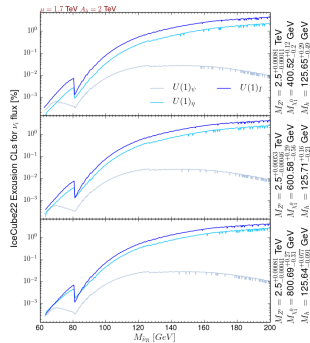
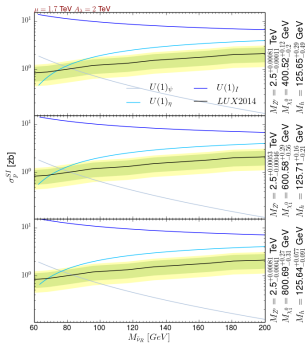
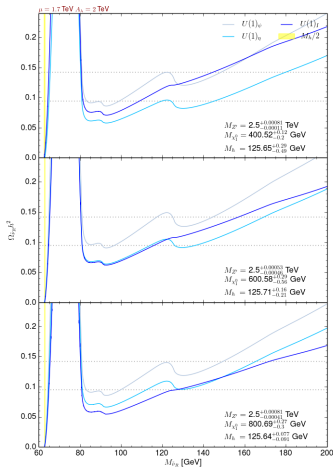
$U(1)'_N$  excluded due to unpredictable relic density.



# RH Scalar Neutrino Dark Matter.



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# Heavy Z Bosons & Where to Find Them.

Model	$\theta_{E_0}$ [rad]	Lower limits on $M_{Z'}$ [TeV]				
		$ee$		$\mu\mu$		$\ell\ell$
		Obs	Exp	Obs	Exp	Obs
$Z'_{SSM}$	-	4.3	4.3	4.0	3.9	4.5
$Z'_X$	$0.50 \pi$	3.9	3.9	3.6	3.6	4.1
$Z'_S$	$0.63 \pi$	3.9	3.8	3.6	3.5	4.0
$Z'_I$	$0.71 \pi$	3.8	3.8	3.5	3.4	4.0
$Z'_\eta$	$0.21 \pi$	3.7	3.7	3.4	3.3	3.9
$Z'_N$	$-0.08 \pi$	3.6	3.6	3.4	3.3	3.8
$Z'_\psi$	$0 \pi$	3.6	3.6	3.3	3.2	3.8

Retrieved from [JHEP 10 \(2017\) 182](#)

$$\mathcal{L}_{\text{int}} = -\bar{\psi}_i \gamma^\mu (g_1 Y_i \hat{B}_\mu + g' Q'_i \hat{Z}'_\mu) \psi_i$$

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# Heavy Z Bosons & Where to Find Them.

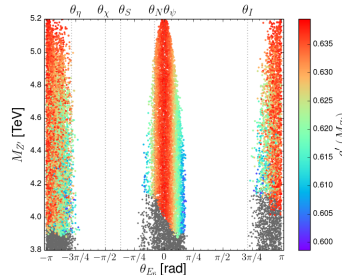
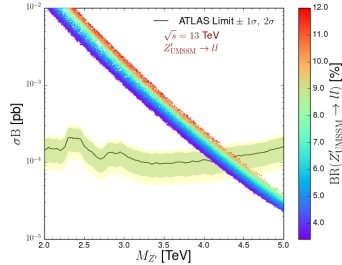
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$$g'(M_{\text{GUT}})/g_1 = \sqrt{5/3}$$



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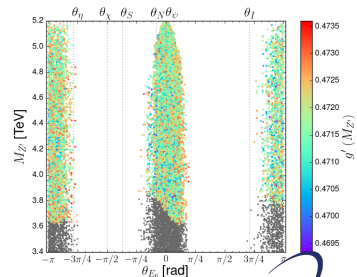
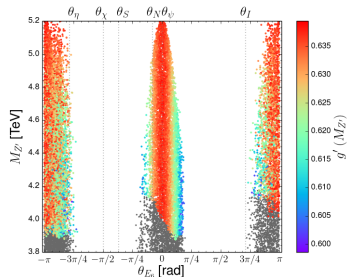
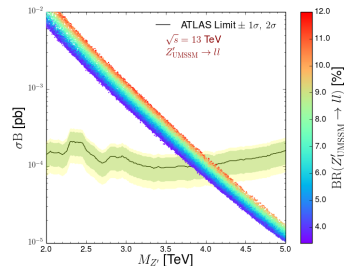
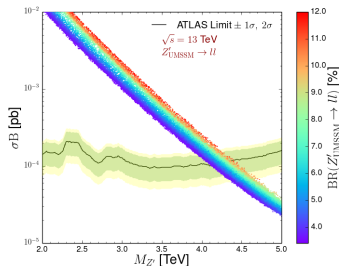
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$$g'(M_{Z'})/g_1 = \sqrt{5/3}$$



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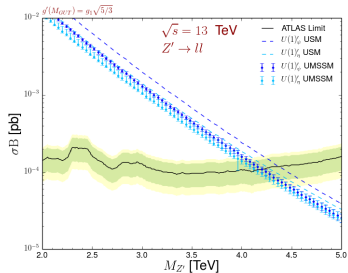
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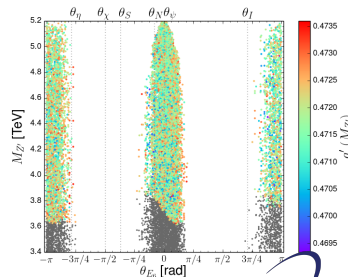
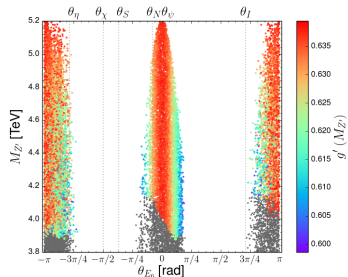
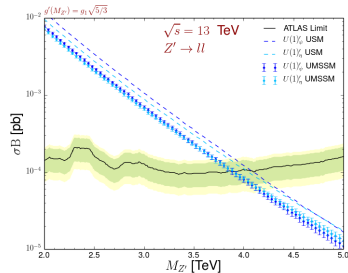
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$$g'(M_{\text{GUT}})/g_1 = \sqrt{5/3}$$

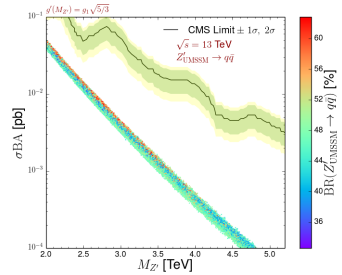
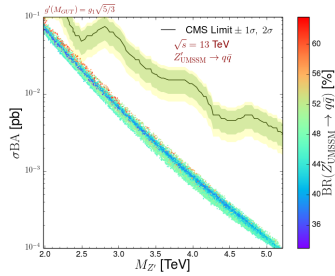
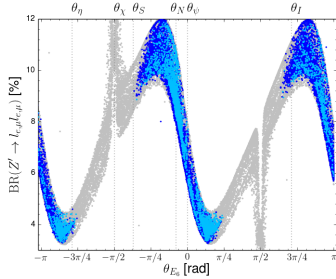


$$g'(M_{Z'})/g_1 = \sqrt{5/3}$$

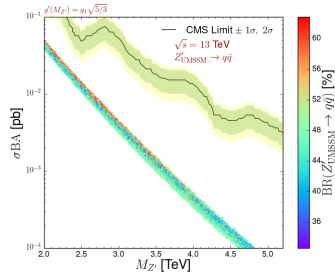
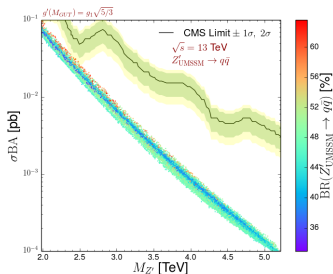
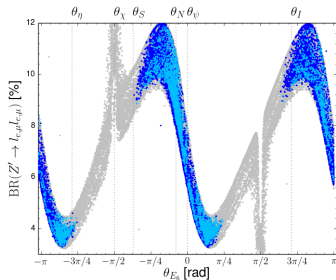




# Heavy Z Bosons & Where to Find Them.



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$$\mathcal{L}_{\text{kin}} = -\frac{1}{4} \hat{B}^{\mu\nu} \hat{B}_{\mu\nu} - \frac{1}{4} \hat{Z}'^{\mu\nu} \hat{Z}'_{\mu\nu} - \frac{\sin \chi}{2} \hat{B}^{\mu\nu} \hat{Z}'_{\mu\nu}$$

$$\begin{pmatrix} \hat{B}_\mu \\ \hat{Z}'_\mu \end{pmatrix} = \begin{pmatrix} 1 & -\tan \chi \\ 0 & \sec \chi \end{pmatrix} \begin{pmatrix} B_\mu \\ Z'_\mu \end{pmatrix}$$

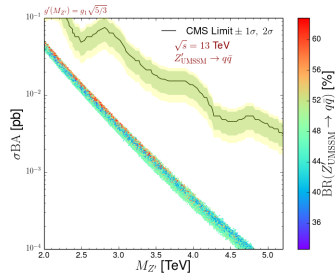
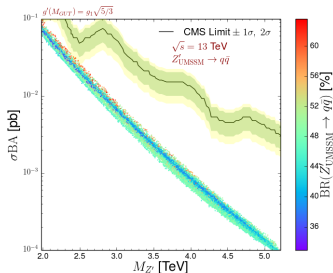
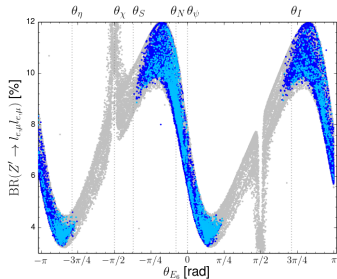
$$\mathcal{L}_{\text{int}} = -\bar{\psi}_i \gamma^\mu (g_1 Y_i B_\mu + g' \bar{Q}_i Z'_\mu) \psi$$

$$\bar{Q}_i = Q'_i \sec \chi - \frac{g_1}{g'} Y_i \tan \chi$$

$$\bar{Q}_L = \bar{Q}_E = 0, Y_L = -1/2, Y_E = -1$$



# Heavy Z Bosons & Where to Find Them.



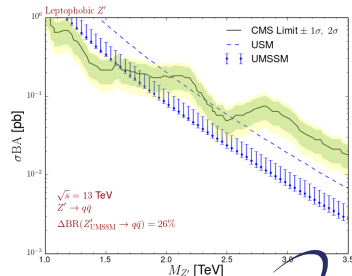
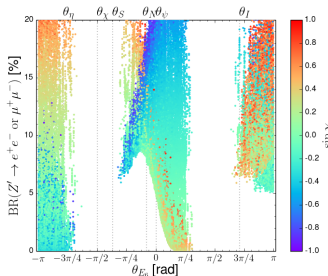
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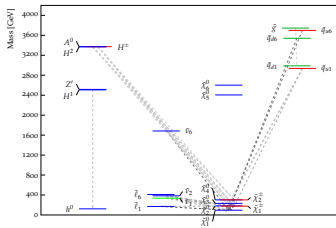
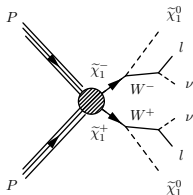
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$$\bar{Q}_i = Q'_i \sec \chi - \frac{g_1}{g'} Y_i \tan \chi$$

$$\bar{Q}_L = \bar{Q}_E = 0, Y_L = -1/2, Y_E = -1$$

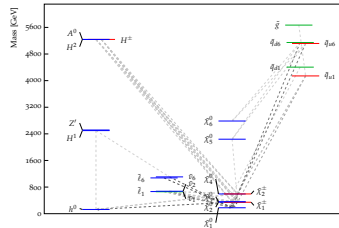


# Heavy Z Bosons & Where to Find Them.



BM I

Parameter	BM I
$\theta_{E_6}$	$-0.8\pi$
$\tan \beta$	9.11
$\sin \chi$	-0.35
$\mu$ [GeV]	218.87
$g'$	0.47
$\Gamma_{Z'}$	40.29
$\text{BR}(Z' \rightarrow jj)$ [%]	54.9
$\text{BR}(Z' \rightarrow \nu\nu)$ [%]	23.4
$\text{BR}(Z' \rightarrow \chi_1^\pm \chi_1^\mp)$ [%]	1.7
$\sigma_{NLO}^{\sqrt{s}=14\text{TeV}}(pp \rightarrow Z')$ [pb]	0.12



BM II

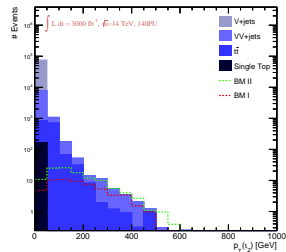
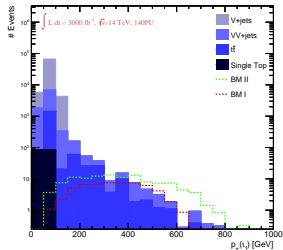
Parameter	BM II
$\theta_{E_6}$	$0.2\pi$
$\tan \beta$	16.09
$\sin \chi$	0.33
$\mu$ [GeV]	345.35
$g'$	0.47
$\Gamma_{Z'}$	38.48
$\text{BR}(Z' \rightarrow jj)$ [%]	53.7
$\text{BR}(Z' \rightarrow \nu\nu)$ [%]	22.8
$\text{BR}(Z' \rightarrow \chi_1^\pm \chi_1^\mp)$ [%]	6.3
$\sigma_{NLO}^{\sqrt{s}=14\text{TeV}}(pp \rightarrow Z')$ [pb]	0.12

- Background: Dibosons+Jets, Bosons+Jets, Top pair production, Single top production.
- Simulated with FastJet+Delphes using anti- $k_T$  algorithm with 60% tagging efficiency.



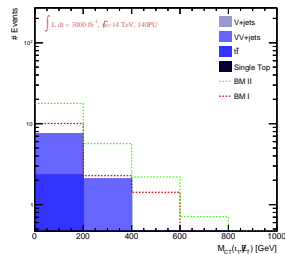
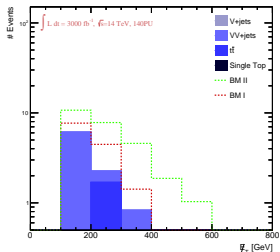
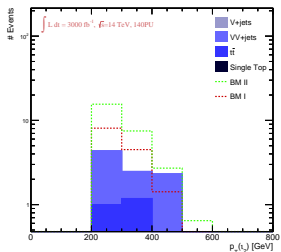
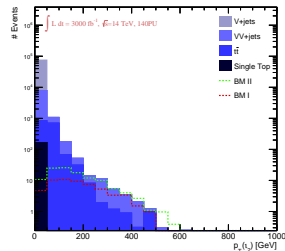
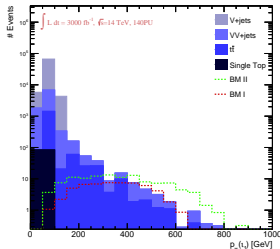
# Heavy Z Bosons & Where to Find Them.

Step	Requirements	Background	BM I	BM II
0	Initial	$1.7 \times 10^{11}$	$8.8 \times 10^3$	$1.9 \times 10^4$
1	$N^l = 2$	$6.1 \times 10^8$	401	860
2	Electron veto	$2.9 \times 10^8$	100	230
3	$ \eta^l  < 1.5$	$1.7 \times 10^8$	76	170
4	$I_{\text{rel}}^\mu < 0.15$	$7.9 \times 10^5$	63	130
5	$\Delta R(l_1, l_2) > 2.5$	$7.9 \times 10^5$	62	130
6	Jet veto	$7.7 \times 10^4$	57	120



# Heavy Z Bosons & Where to Find Them.

Step	Requirements	Background	BM I	BM II
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5	$\Delta R(l_1, l_2) > 2.5$	$7.9 \times 10^5$	62	130
6	Jet veto	$7.7 \times 10^4$	57	120
7	$p_T(l_1) > 300$ GeV	44	36	71
8	$p_T(l_2) > 200$ GeV	20	19	32
9	$\cancel{E}_T > 100$ GeV	10	14	27
	$Z_A$		$3.77\sigma$	$7.14\sigma$
			$3.03\sigma$	$5.05\sigma$



## > Introduction

- The Standard Model of Particle Physics
- Problems with the Standard Model
- Minimal Supersymmetric Extension of the SM

## > Analysis Motivation

- Grand Unified Model Building
- $U(1)'$  extended MSSM

## > Muon Anomalous Magnetic Moment

## > The Dark Side of UMSSM

## > Heavy Z Bosons & Where to Find Them

## > Conclusion



## Pro's

- > Up to  $1\sigma$  accuracy with  $(g - 2)_\mu$  experimental results
- > Two successive dark matter candidate
- > Up to  $7\sigma$  observability in HL-LHC

## Con's

- > No experimental evidence for RH neutrinos
- > Naturalness problem
- > Heavy higgs sector





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Gratitude, for your kind attention...

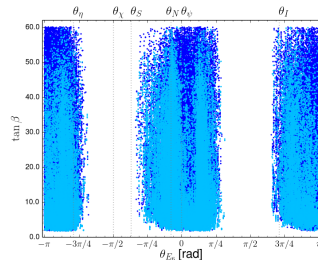
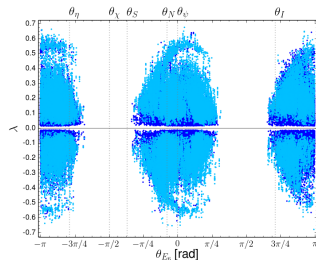
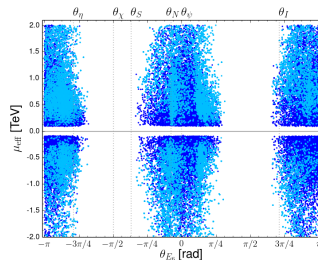
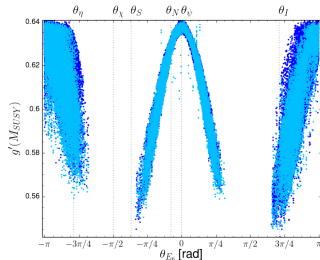
Special thanks to both LPTHE & INFN for the hospitality.



# BACKUP



# Parameter Space



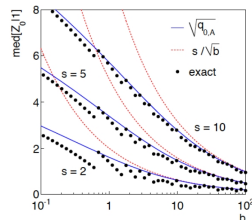
## > Standard Significance

$$s = \frac{S}{\sqrt{b + \sigma_b^2}}$$

- S: Expected number of events from signal
- b: Expected number of background events
- $\sigma$ : Variance, uncertainty of background

## > Asimov Significance

$$Z_A = \left[ 2 \left( (s + b) \ln \left[ \frac{(s + b)(b + \sigma_b^2)}{b^2 + (s + b)\sigma_b^2} \right] \right. \right. \\ \left. \left. \dots - \frac{b^2}{\sigma_b^2} \ln \left[ 1 + \frac{\sigma_b^2 s}{b(b + \sigma_b^2)} \right] \right) \right]^{\frac{1}{2}}$$



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