

5th June 2018

FOOT collaboration





Alberto Mengarelli & Matteo Franchini



Control plots Monitoring

Tracking preselection (multi-tracking)

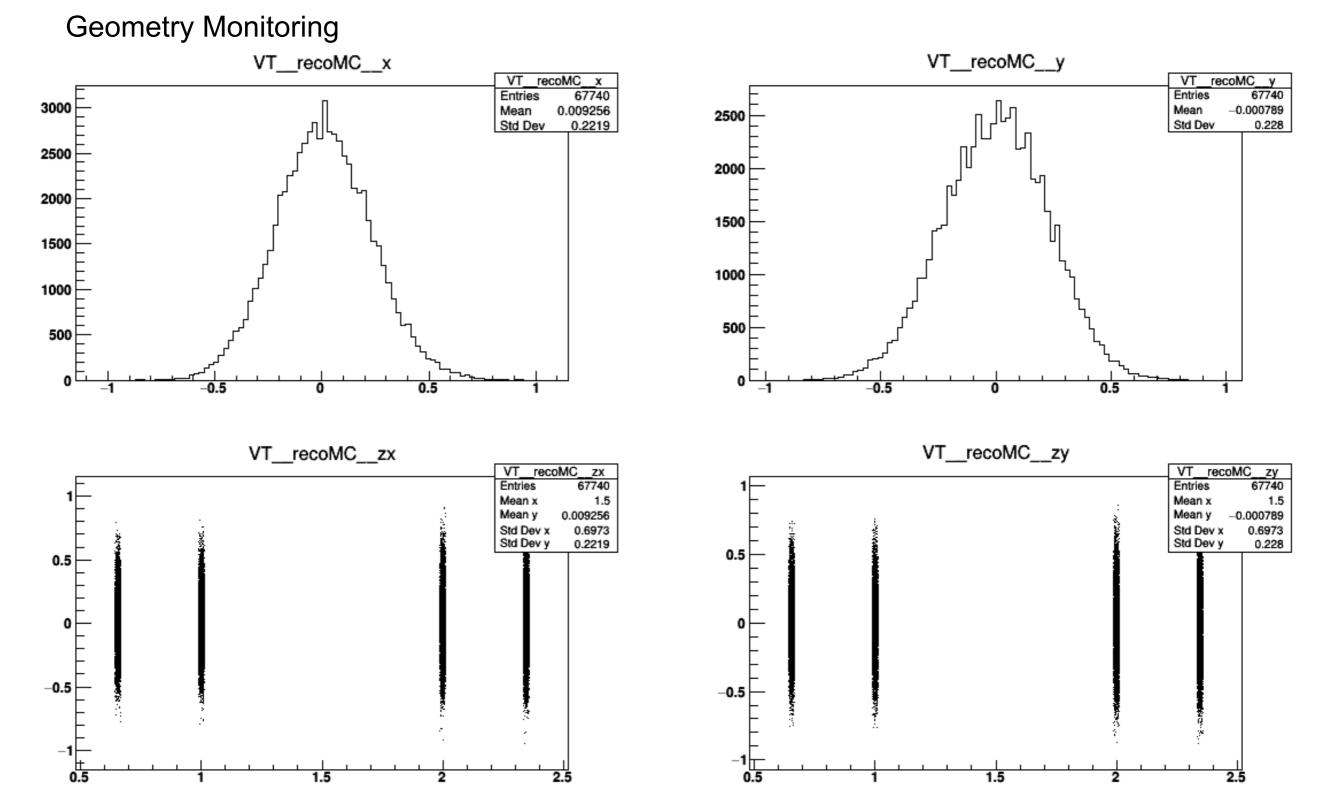


Stability test on magnetic field uncertainties

- Stability under positioning uncertainties
- VT & IT clustering & scintillator ready for tracking!
- Tracking & momentum resolution
- Software bulletin

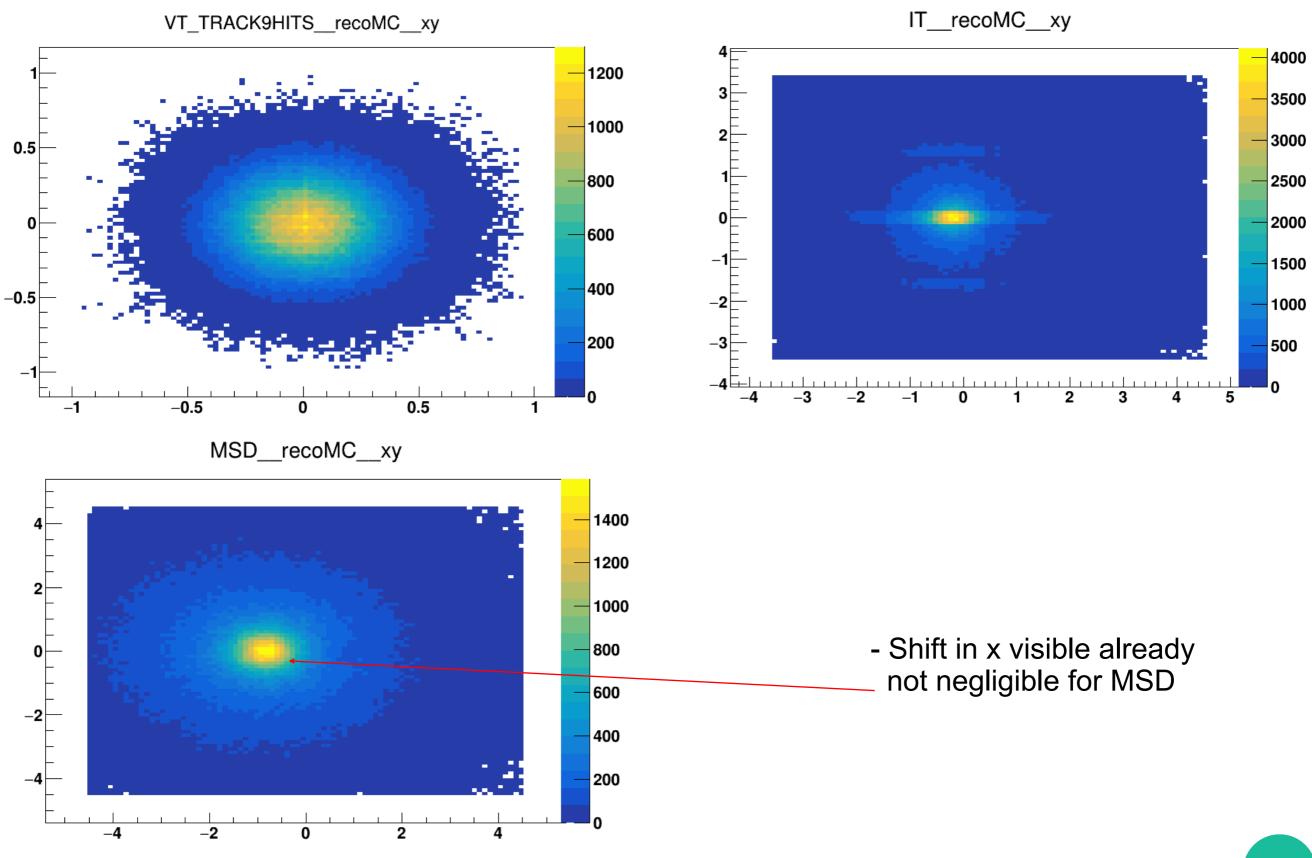
Finalising Monitoring Implementation

Control Plots for tracking inside SHOE



Running on V14.0.1

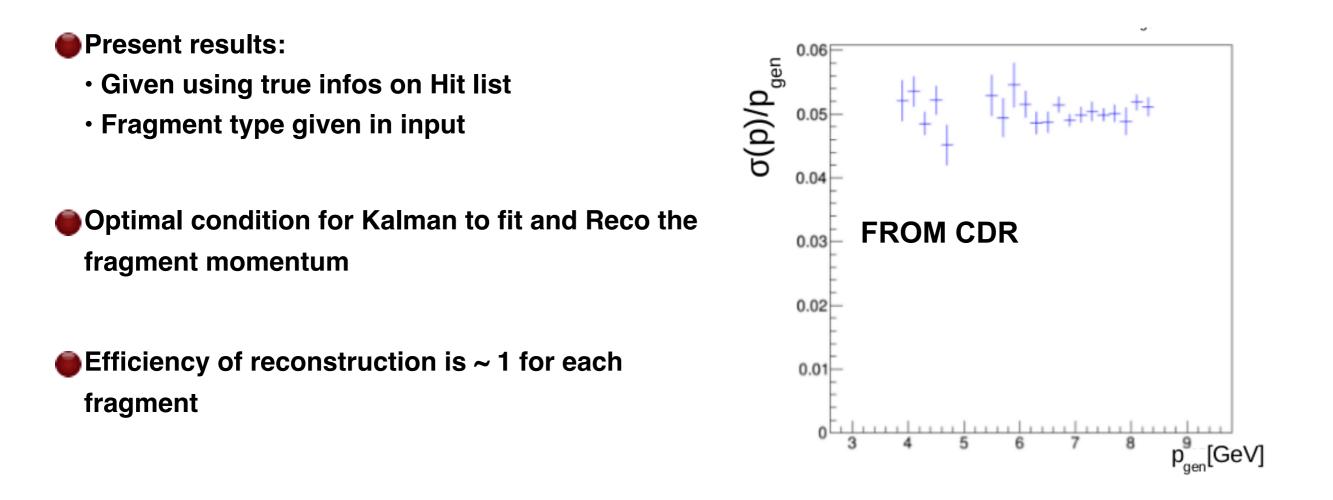
Geometry Monitoring



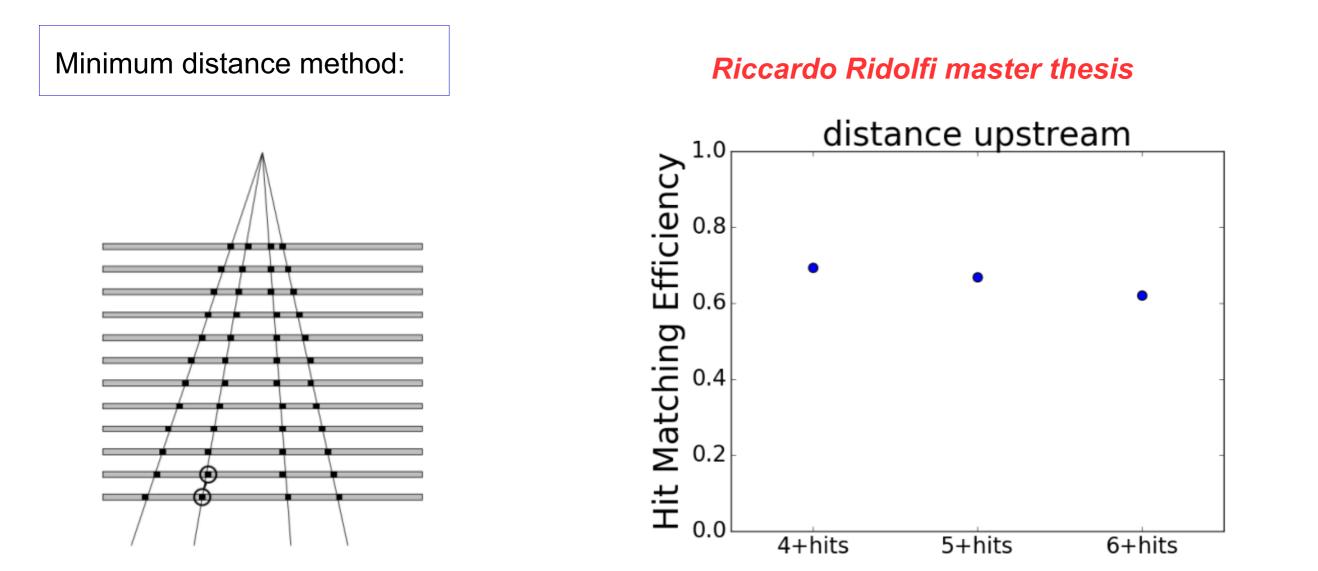
FOOT collaboration meeting

Tracking preselection (multi-tracking)

Preliminary study on multitracking



This is not realistic and could be done only with MC, while an efficient way to deal with multytracking and assignment of "true" hit list for each fragment track has to be developed

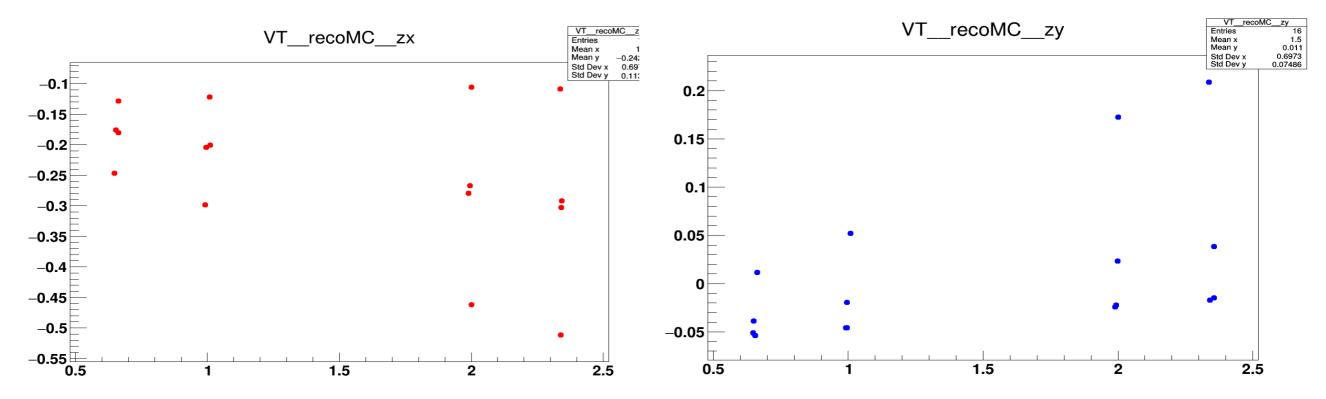


Efficiency of match the true track list of hits using minimum distance method is already ~70 % using 4 hits



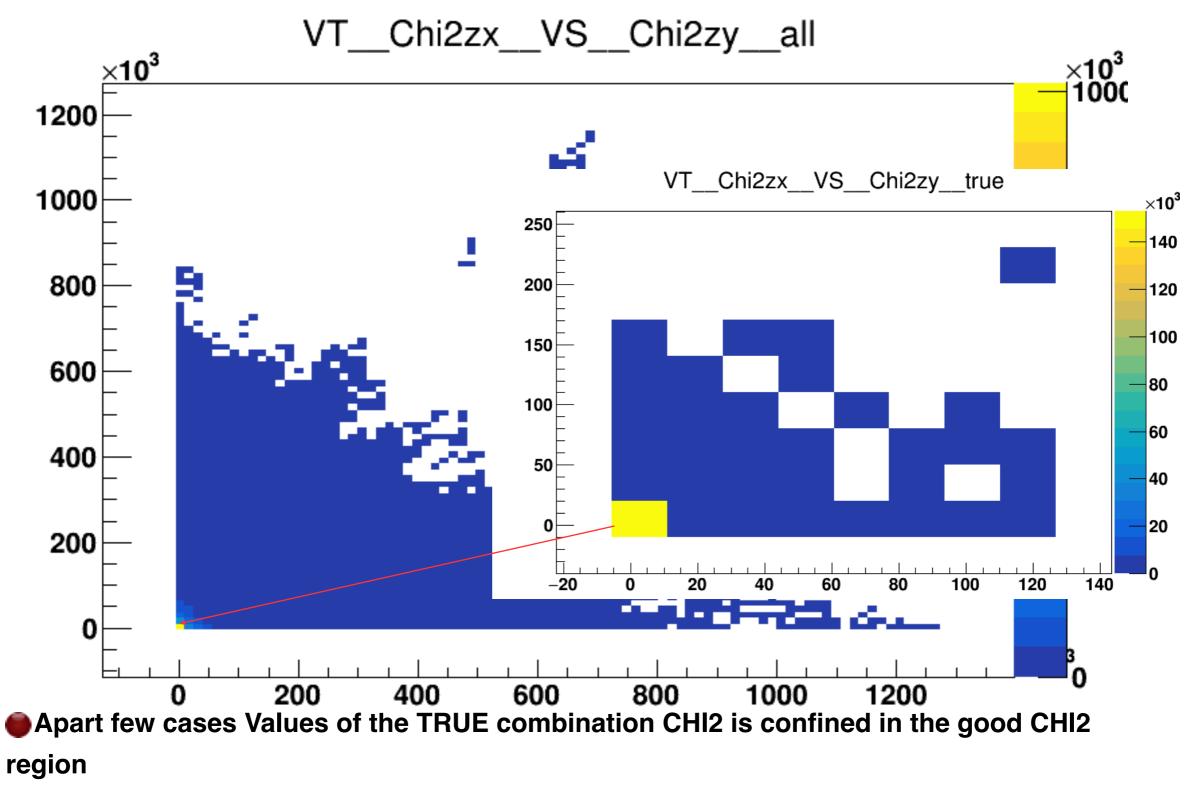
USING ONLY VT RECO HIT (V14.0.1)

■BASIC IDEA: Magnetic field in the VT region will not deflect the trajectory so much from a straight line → Fit the combination of the hits in each event to disentangle the true ones by mean of CrHI2 result



Event with 4 tracks ZX and ZY planes:

Selecting tracks with 9 hits, take th 4 hits in the VT, make all combination and look at the CHI2 of the fit with a line for the ZX and ZY planes



Cutting on CHI2_ZX < 5 and CHI2_ZY < 10 or viceversa the efficiency of selecting the true combination is ~99 % compared to ~75% of the minimum distance method</p>

Stability test on magnetic field uncertainties (1)

Magnetic Field Rotation tests

Aim of the tests: Understand possibile degradation of momentum resolution due to misalignment of magnetic field.

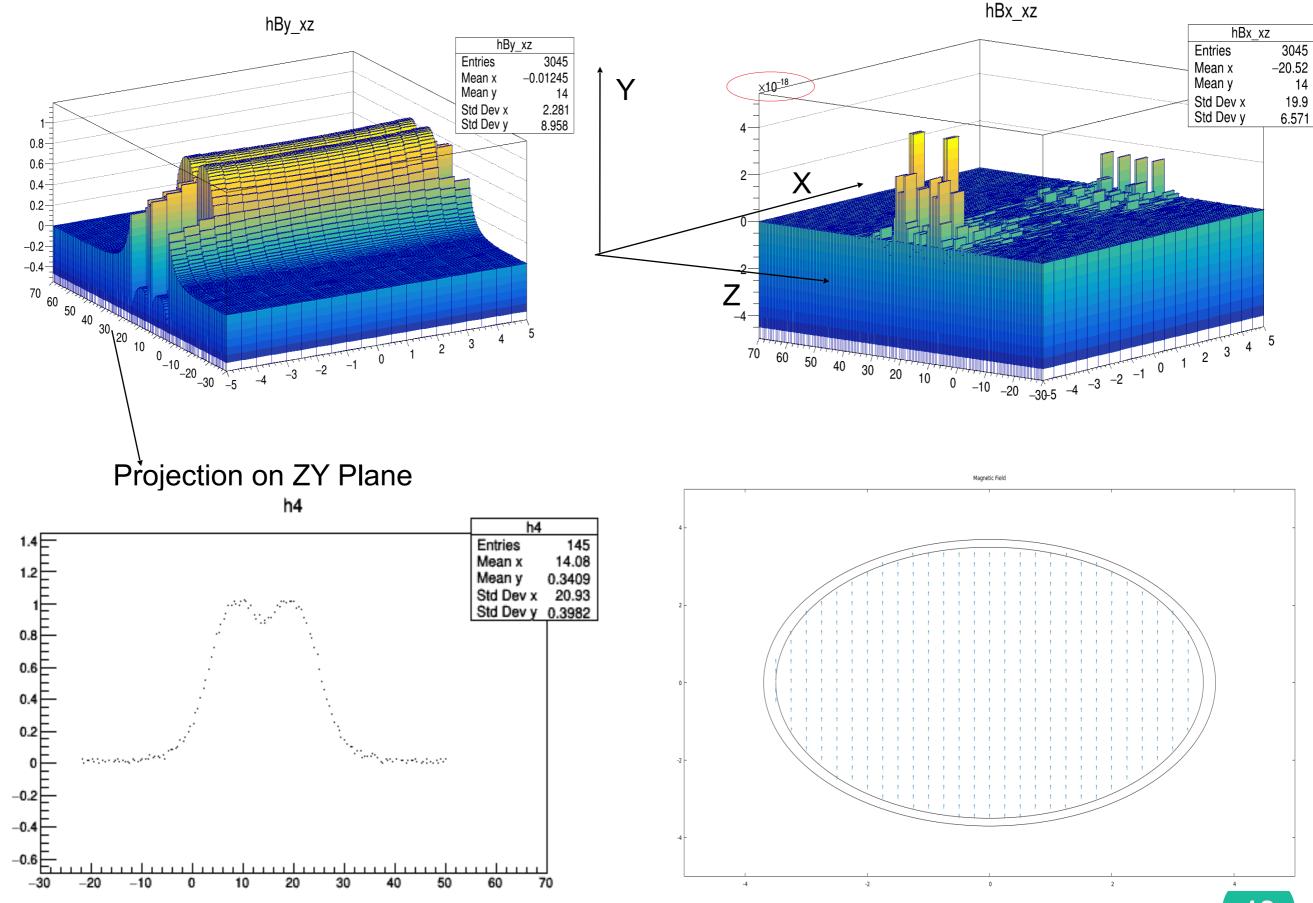
Rotation of the magnetic field cases:

1) Both magnet maps tilted \rightarrow total field rotation of 1 deg. (only in RECO)

- 2) Second magnet map rotation of 1 deg wrt the first one. (Only in RECO)
- 3) Same as 2) but the magnetic field maps are used both in generation (FLUKA) and reconstruction (SHOE) to evaluate momentum resolution

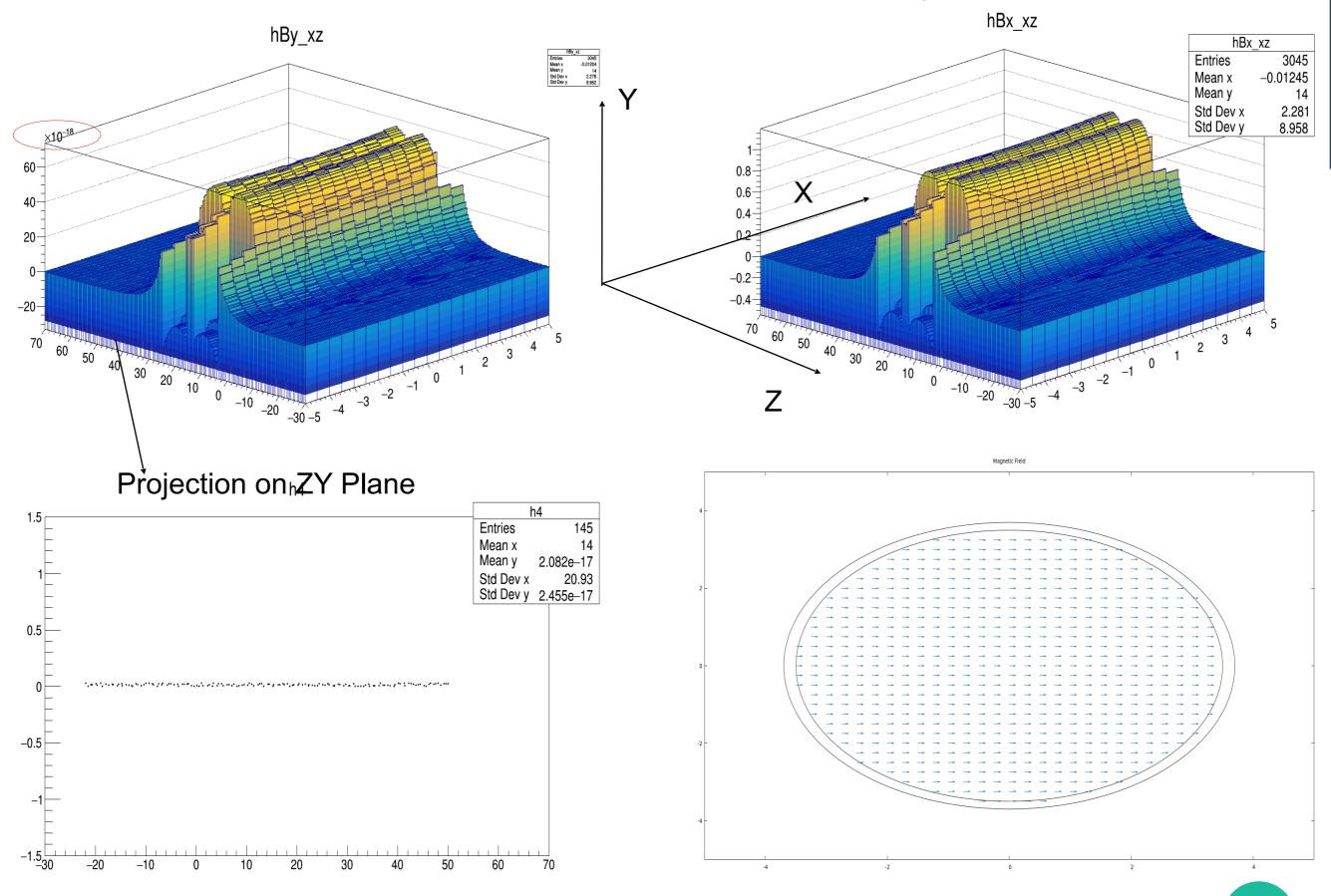
ROTATION CHECK:

NO ROTATION



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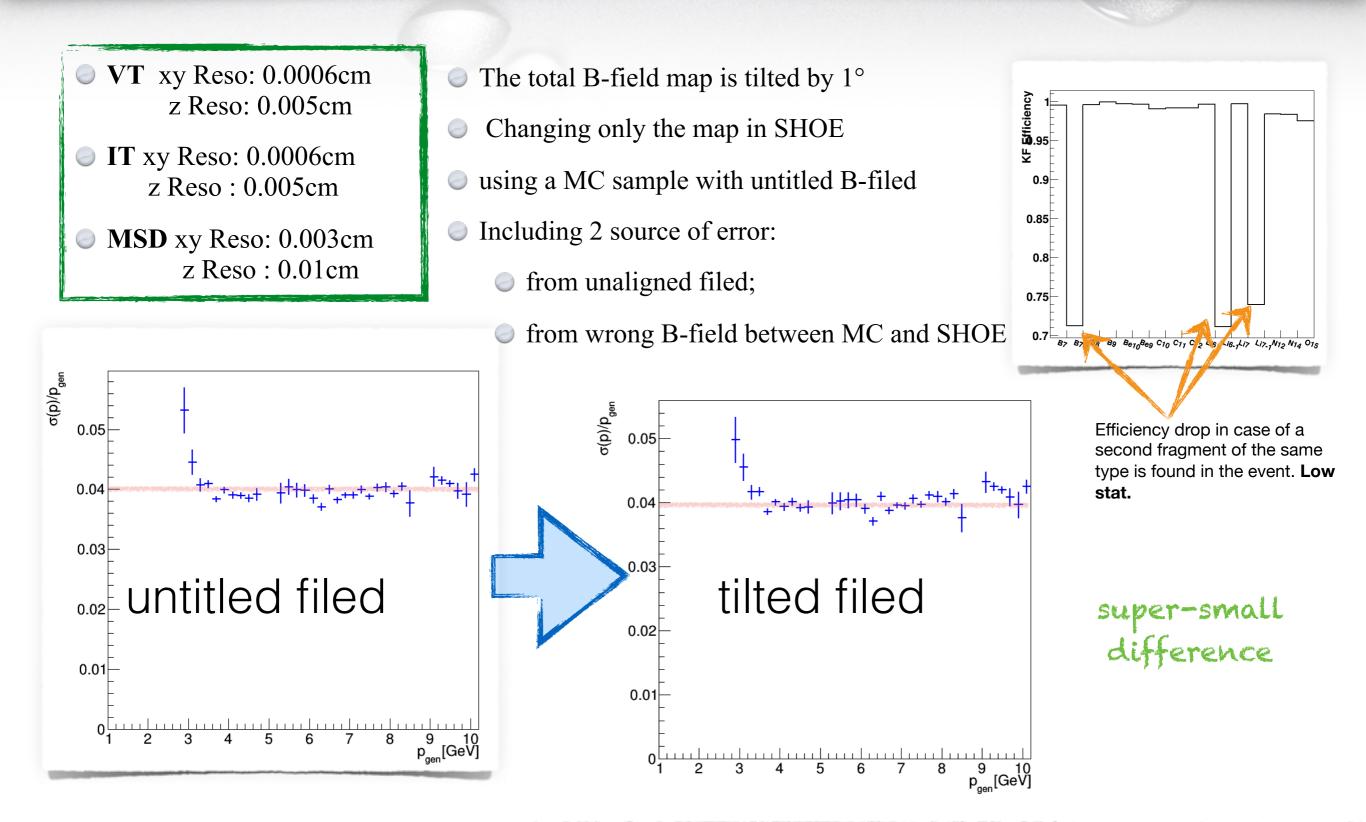
ROTATION CHECK: ROTATION 90 deg



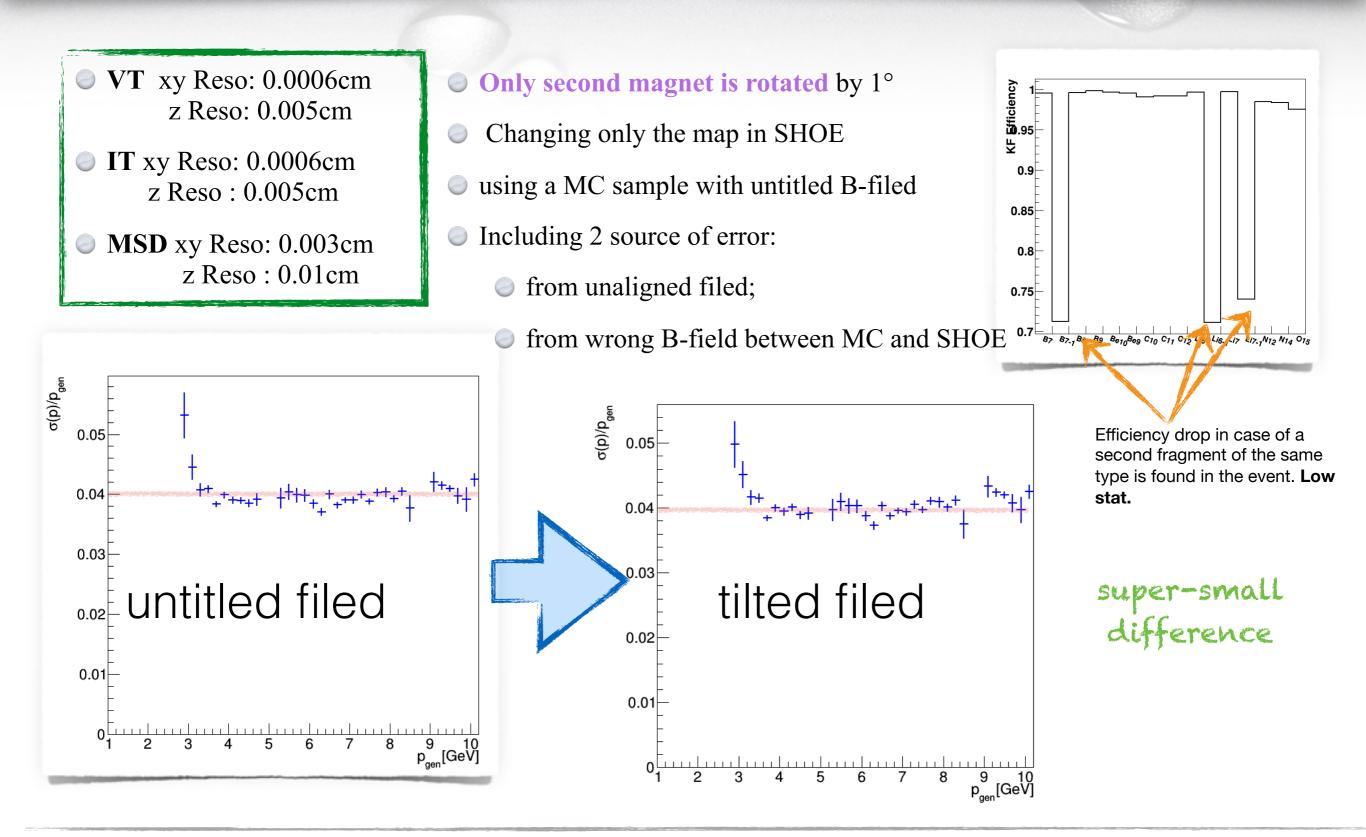
05/06/18

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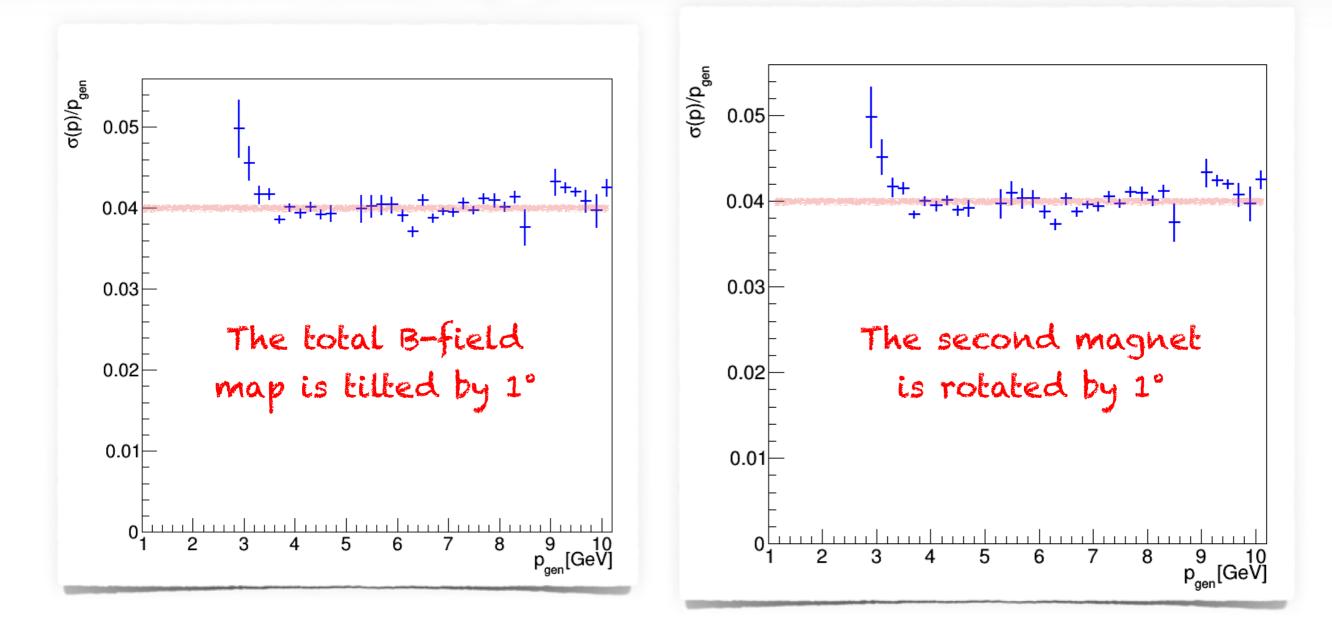
Lead B filed



TURCER BELECK



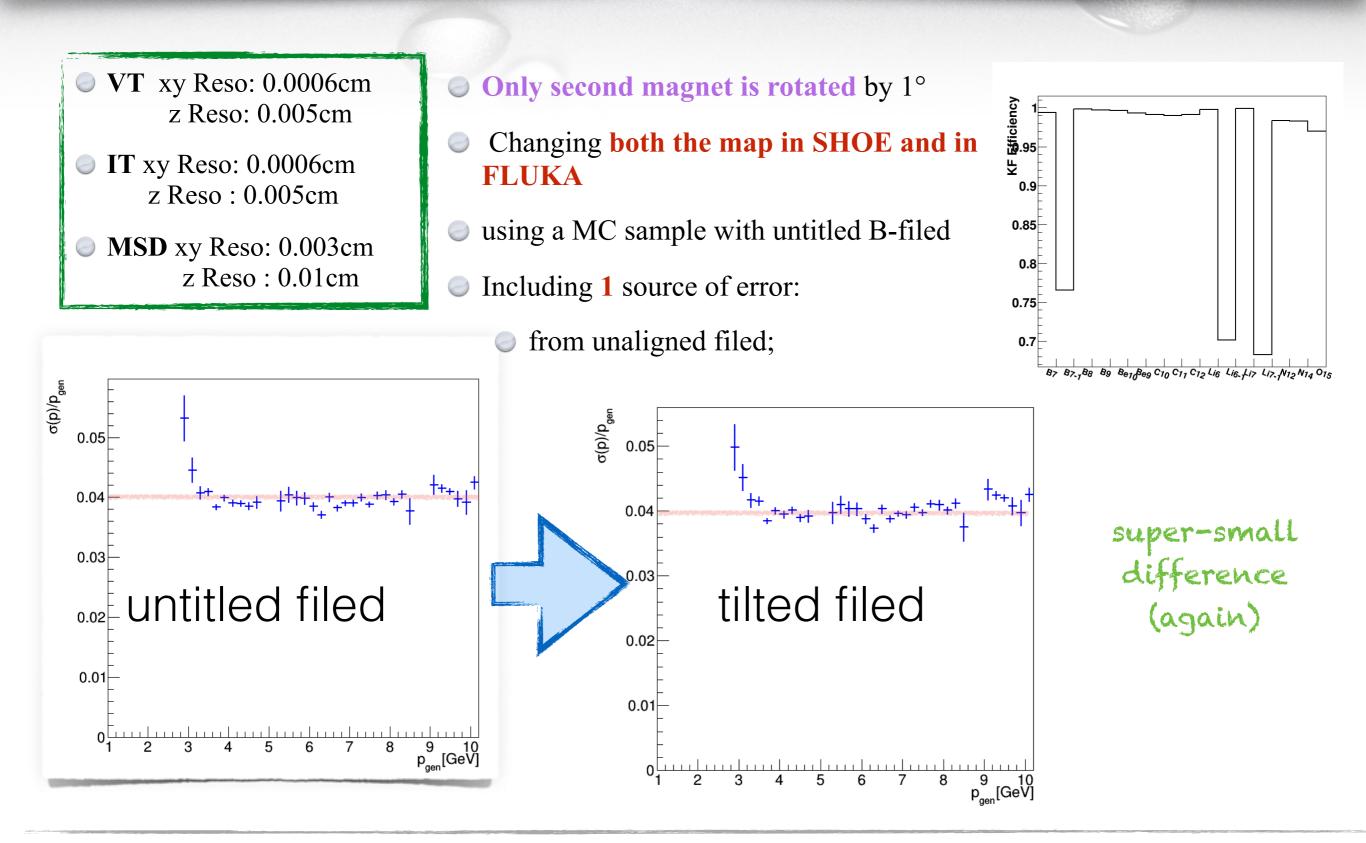
B-field Comparison



super-small difference

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ELECA BELEA III





Control plots for reco and geometry monitoring in SHOE

- Several tests with magnetic field rotations has been performed
- No significant momentum resolution change observed in the different configurations.
- Preliminary multitracking study
- CHI_2 method seems to be promising for VT (eff ~99%)
 - > To be checked using reclusterd hit.

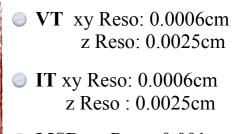
Stability test on magnetic field uncertainties (II)

Impact & Magnet uncertainty

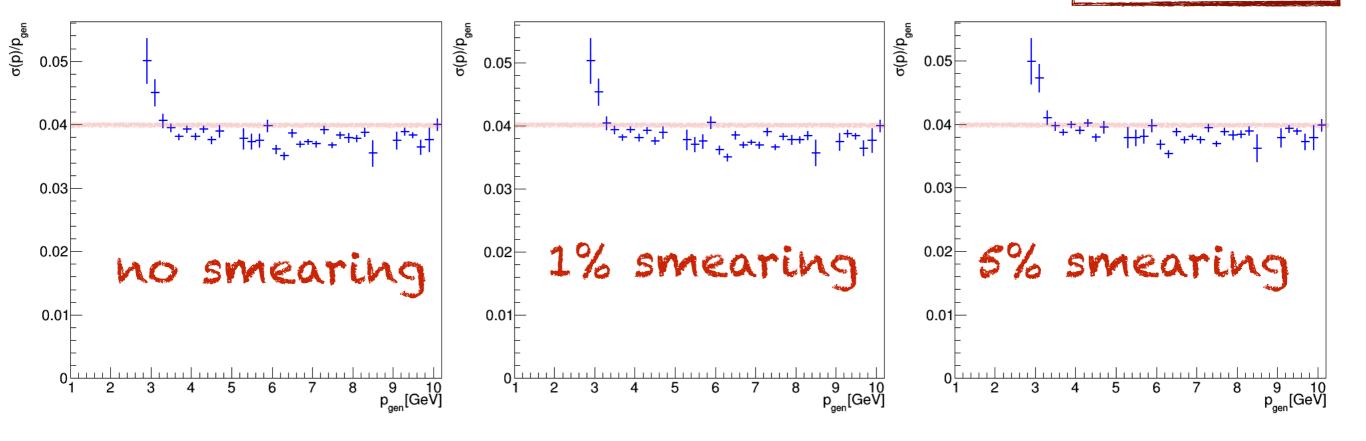
v14.0.1

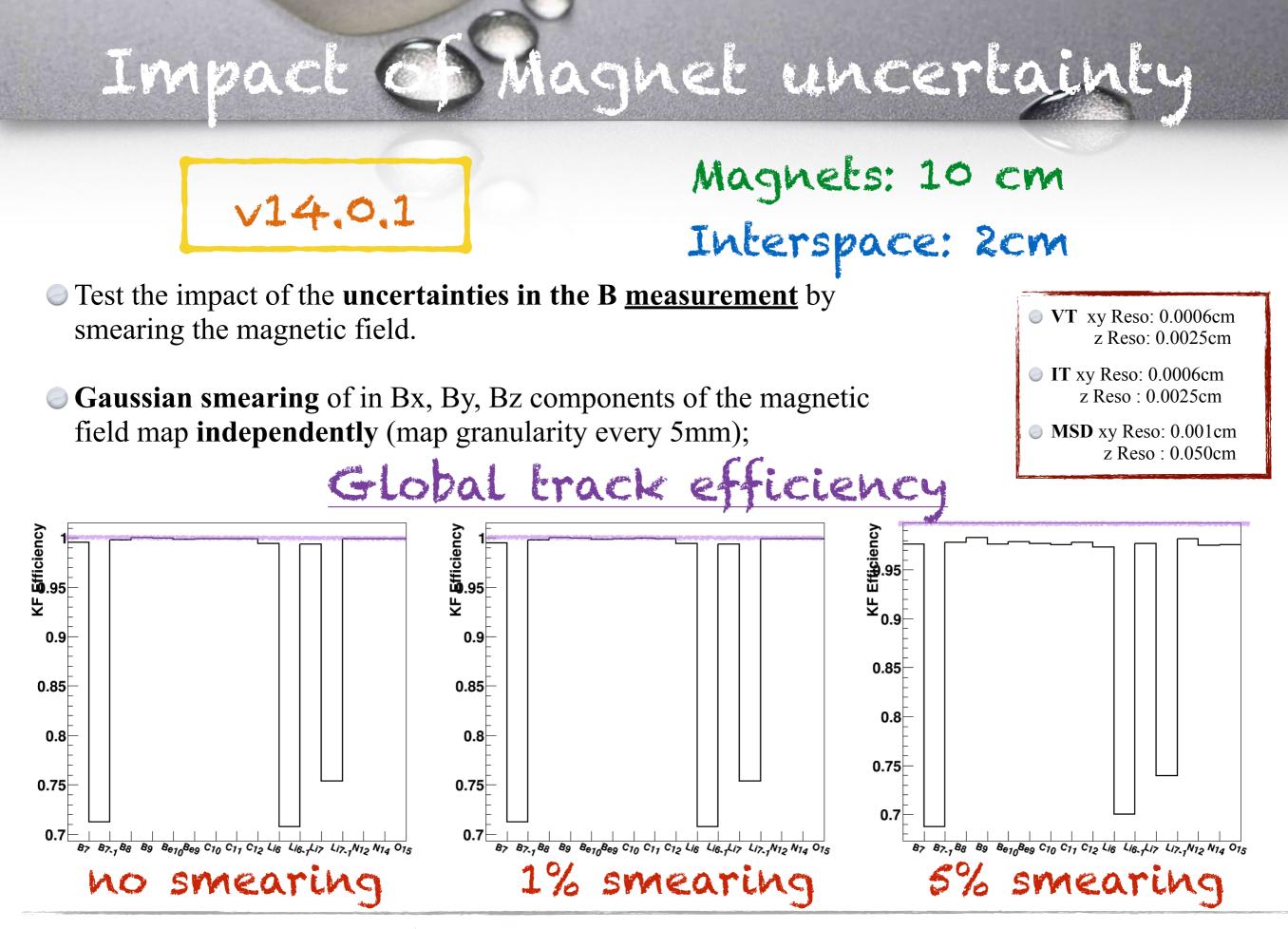
Magnets: 10 cm Interspace: 2cm

- Test the impact of the uncertainties in the B <u>measurement</u> by smearing the magnetic field.
- Gaussian smearing of in Bx, By, Bz components of the magnetic field map independently (map granularity every 5mm);



```
MSD xy Reso: 0.001cm
z Reso : 0.050cm
```

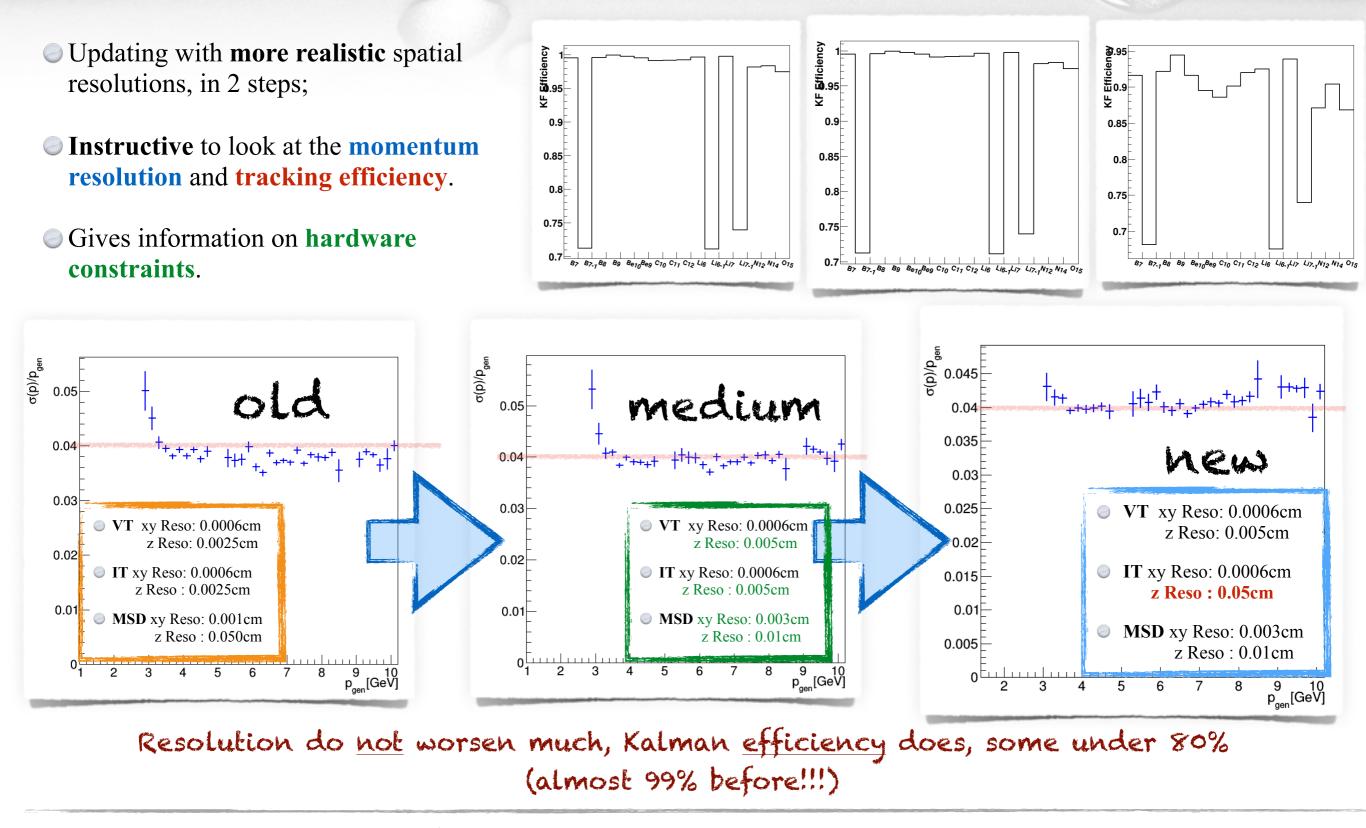




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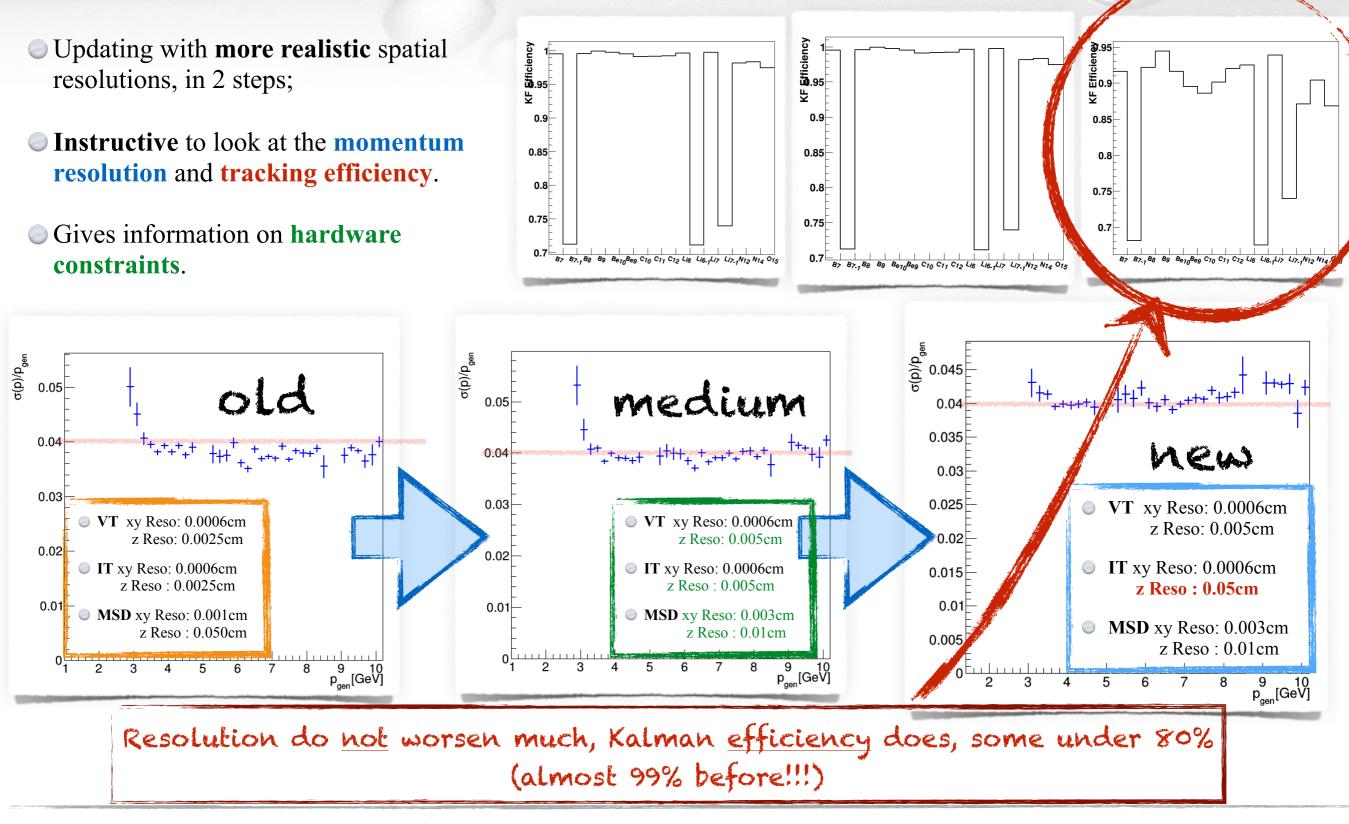
Stability under positioning uncertainties while-updating-reso too)

Updated Resolutions I



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Updaled Resolutions I



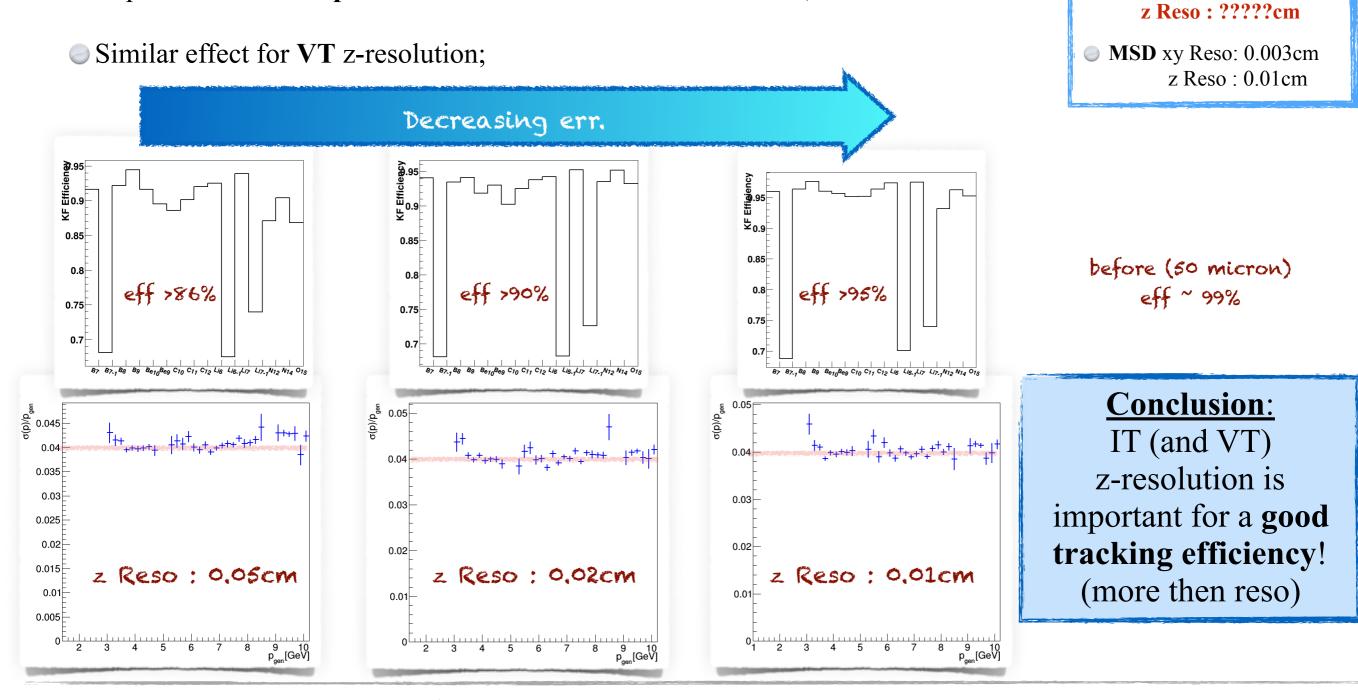
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Updale Resolutions II

Change of the IT z resolution ONLY

Focusing on the IT z-resolution only since have a non-negligible impact;

Important to set acceptable threshold for hardware constrains;



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● **VT** xy Reso: 0.0006cm

IT xy Reso: 0.0006cm

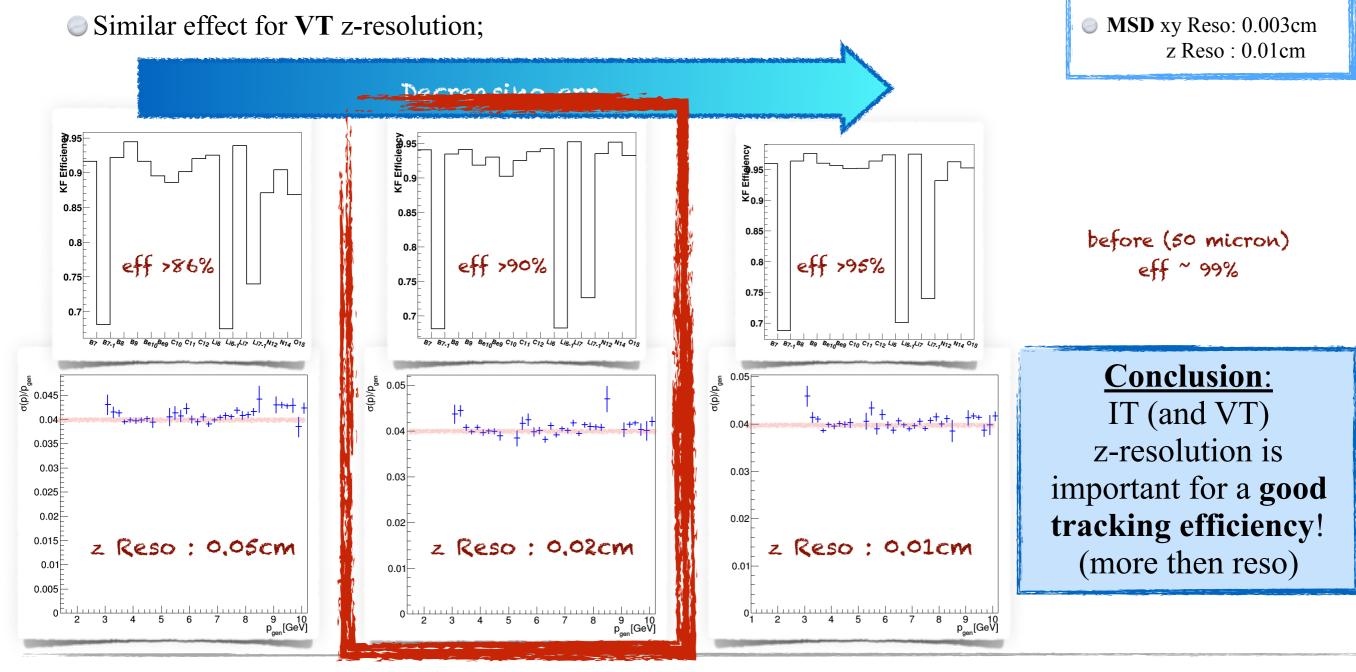
z Reso: 0.005cm

Updale Resolutions II

Change of the IT z resolution ONLY

Focusing on the IT z-resolution only since have a non-negligible impact;

Important to set acceptable threshold for hardware constrains;



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○ VT xy Reso: 0.0006cm

IT xy Reso: 0.0006cm

z Reso: 0.005cm

z Reso : ????cm



Obsentangle layer distance and module positioning;

IT detector center shifted by +0,05cm only in reconstruction;

suggestion by Giuseppe

^{ueb}d/(d) α(d) σ(p)/p_{gen} **VT** xy Reso: 0.0006cm 0.05 z Reso: 0.005cm 0.04 0.04 0.035 IT xy Reso: 0.0006cm z Reso : 0.02cm 0.03 0.03 0.025 MSD xy Reso: 0.003cm IT moved 0.02 z Reso : 0.01cm 0.02 0.015 0.01 0.01 0.005 $0 \frac{1}{1} \frac{2}{2} \frac{3}{3} \frac{4}{4} \frac{5}{5} \frac{6}{6} \frac{7}{7} \frac{8}{8} \frac{9}{9} \frac{10}{p_{ren}} [GeV]$ 2 3 4 5 6 7 8 9 10 p_{aen}[GeV]

Conclusion

Good reso stability, negligible eff. loss: smaller effect than increasing the uncertainty uncorrelated on both ITR planes to 500.

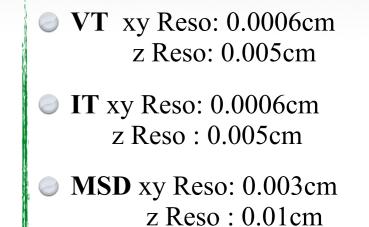
Oistance between plans much more precise them plume position.

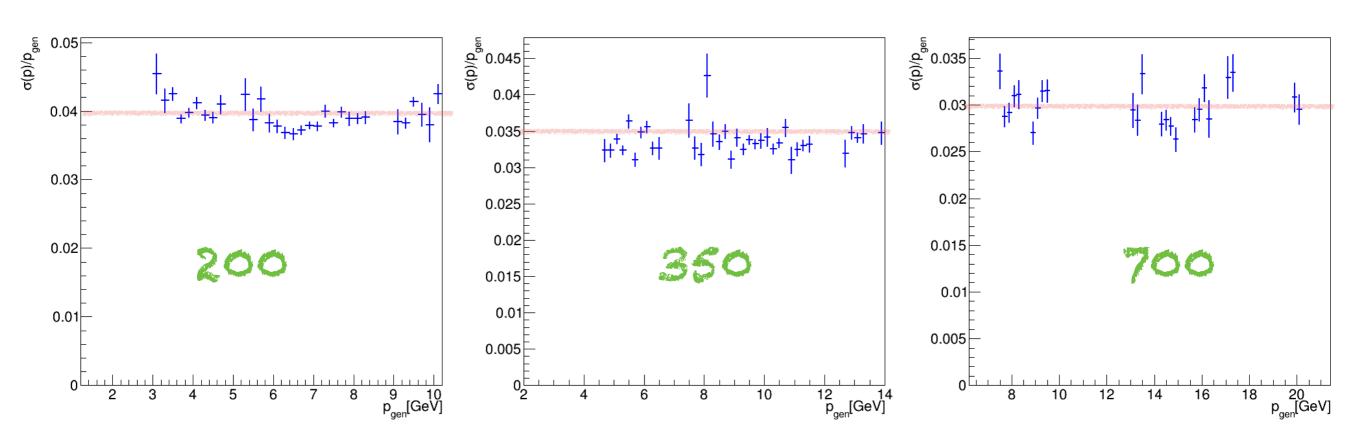


More energy



- Here more the momentum, more the resolution;
- Seems we're dominated by MS that decrease with increasing momentum.
- Then Kalman seems good at fitting also "poorly" bended tracks.





30

Momentum resolution plot given by different elements contribution

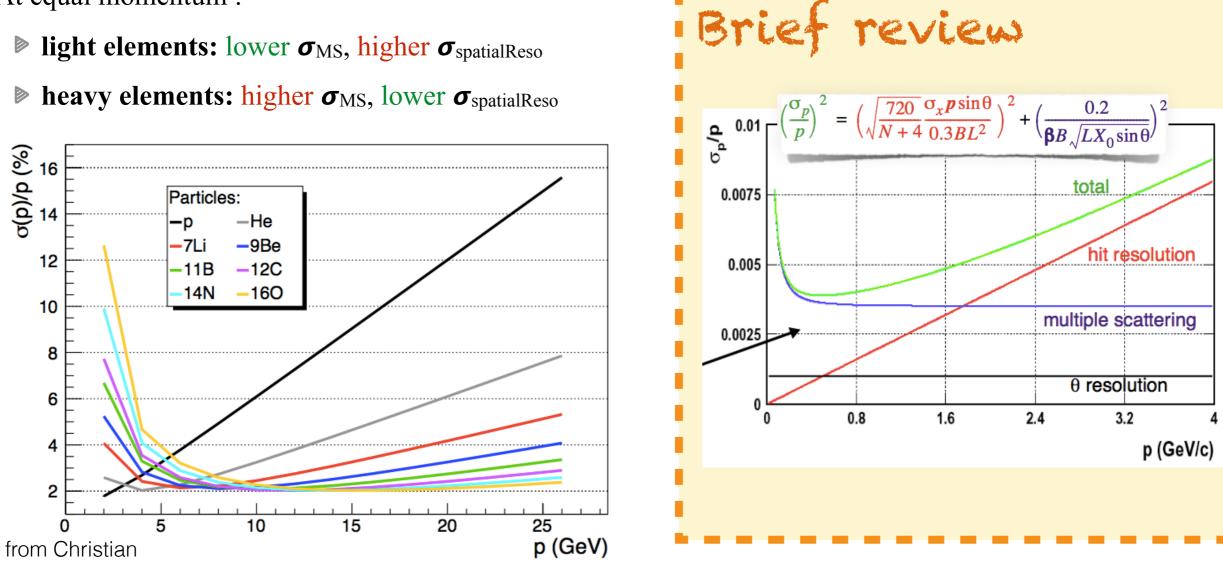
Moreover, elements has different momentum spectrum

because in fragmentation different elements are produced at different momentum, down from Li, up to O;

ELLE LC

At equal momentum :





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Resolution falls

At 200MeV/n, all elements are in the "decreasing" part, dominated by <u>MS contribution</u>;

- ▶ light elements have *lower p*: MS contribution fall earlier;
- heavy-elements have <u>higher p</u>: approaching minimum, MS not so high anymore;

● At 700MeV/n, all in region dominated by <u>spatial resolution</u>;

- light elements (steeper growth, lower-p minimum) have low p; still close to the minimum
- heavy elements (grows slower, higher-p minimum) have higher p but still close to the minimum

9 10 p_{gen}[GeV] d/(d

0.04

0.035

0.03

0.025

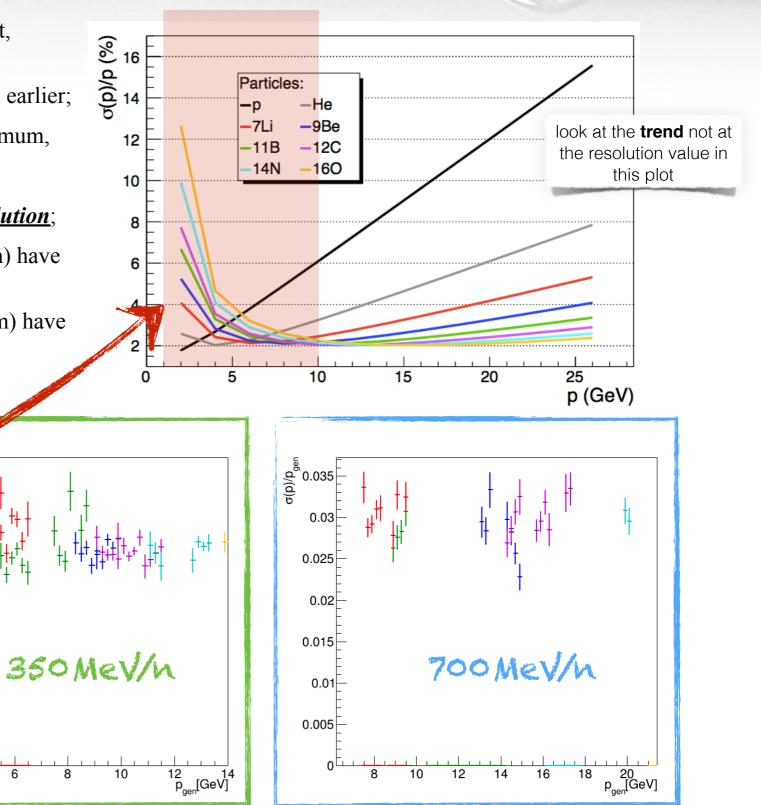
0.02

0.015

0.01

0.005

0.



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200 MeV/n

σ(p)/p_{gen}

0.05

0.04

0.03

0.02

0.01

• At 200MeV/n, all elements are in the "decreasing" part, dominated by *MS contribution*;

- ▶ **light elements** have *lower p*: MS contribution fall earlier;
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9 10 p_{gen}[GeV]

^{uə6} 0.045 d/(d)

0.04

0.035

0.03

0.025

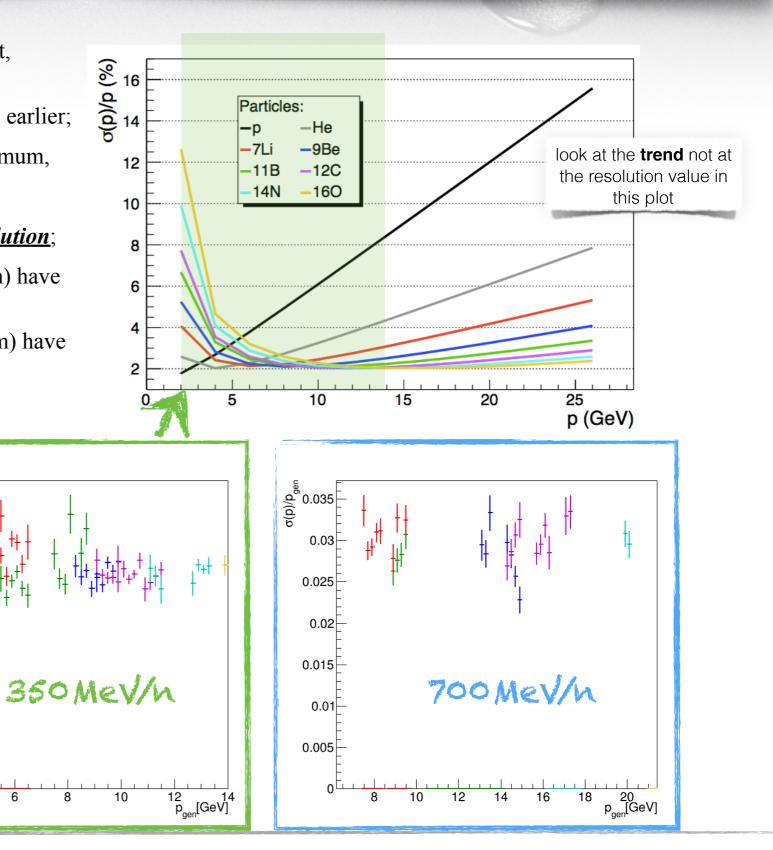
0.02

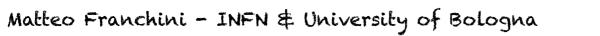
0.015

0.01

0.005

0,





200 MeV/n

σ(p)/p_{gen}

0.05

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⁴⁶⁶d/(d)

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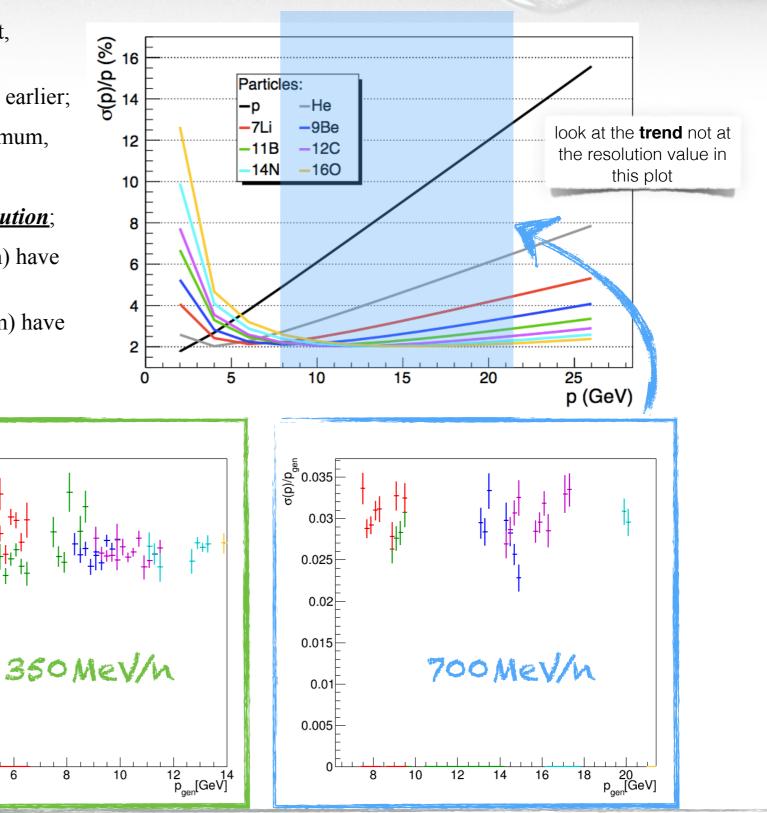
0.02

0.015

0.01

0.005

0,



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200 MeV/n

σ(p)/p_{gen}

0.05

0.04

0.03

0.02

0.01

FOOT Bologna 2018

(%) d/(d)0

12

10

8

6

0

Particles:

-p -7Li

-11B

-14N

-He

-9Be

-12C

-160

0

8

10

12

• At 200MeV/n, all elements are in the "decreasing" part, dominated by *MS contribution*;

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9 10 p_{gen}[GeV]

d/(d

0.04

0.035

0.03

0.025

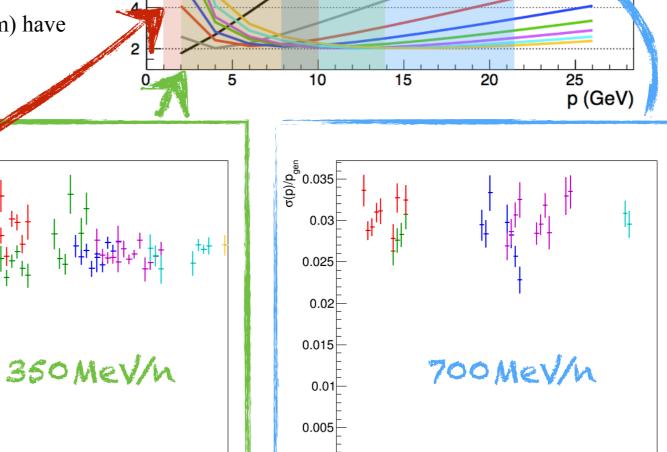
0.02

0.015

0.01

0.005

0.



200 MeV/n

σ(p)/p_{gen}

0.05

0.04

0.03

0.02

0.01

10

12 14 p_{gen}[GeV]

20 p_{gen}[GeV]

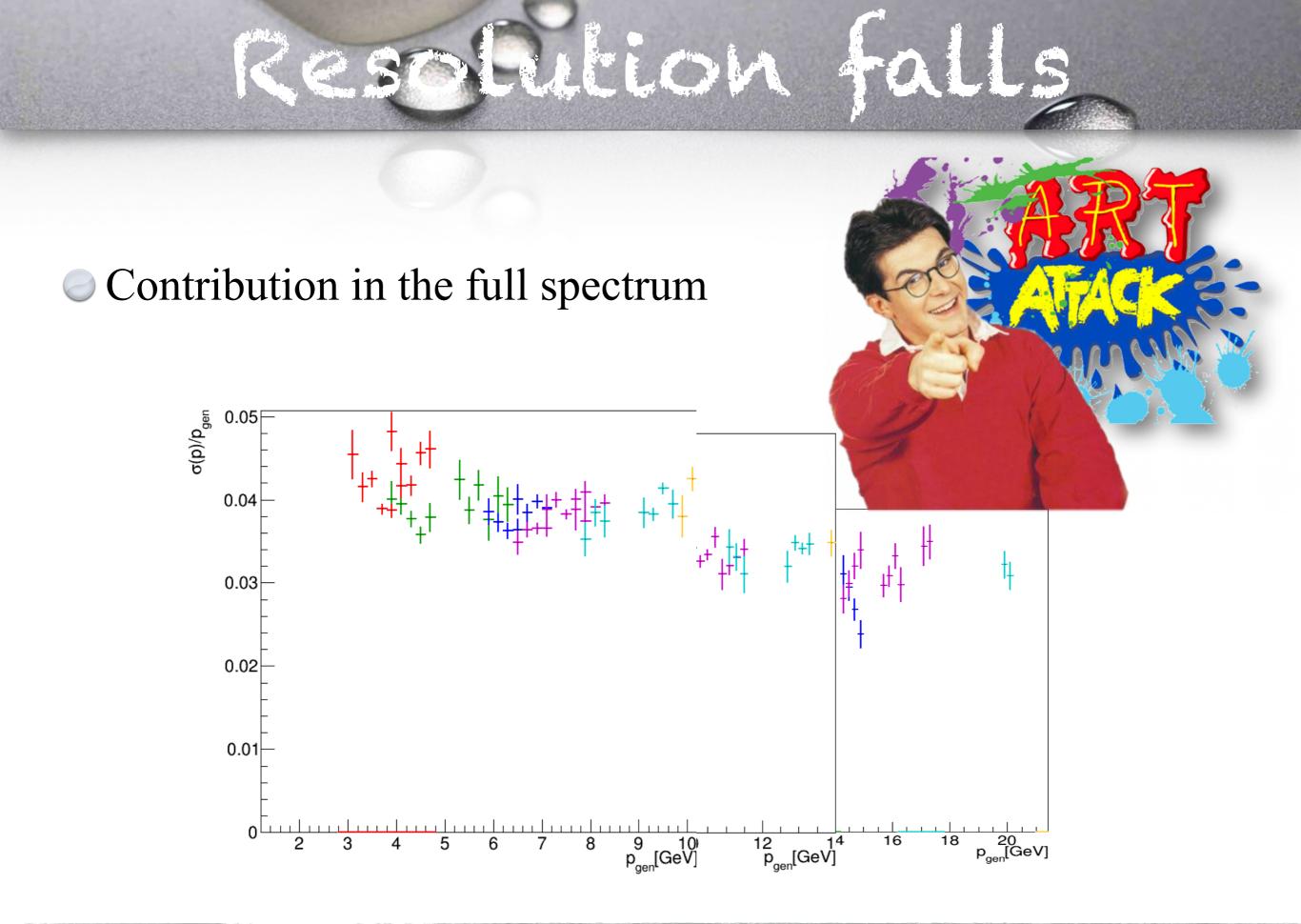
18

16

look at the trend not at

the resolution value in

this plot



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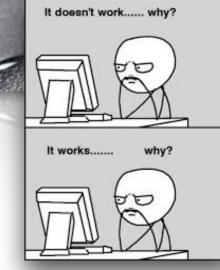
OT-& IT-elestering

Re-designed the clustering classes for both VT and IT...it works!

Casterina

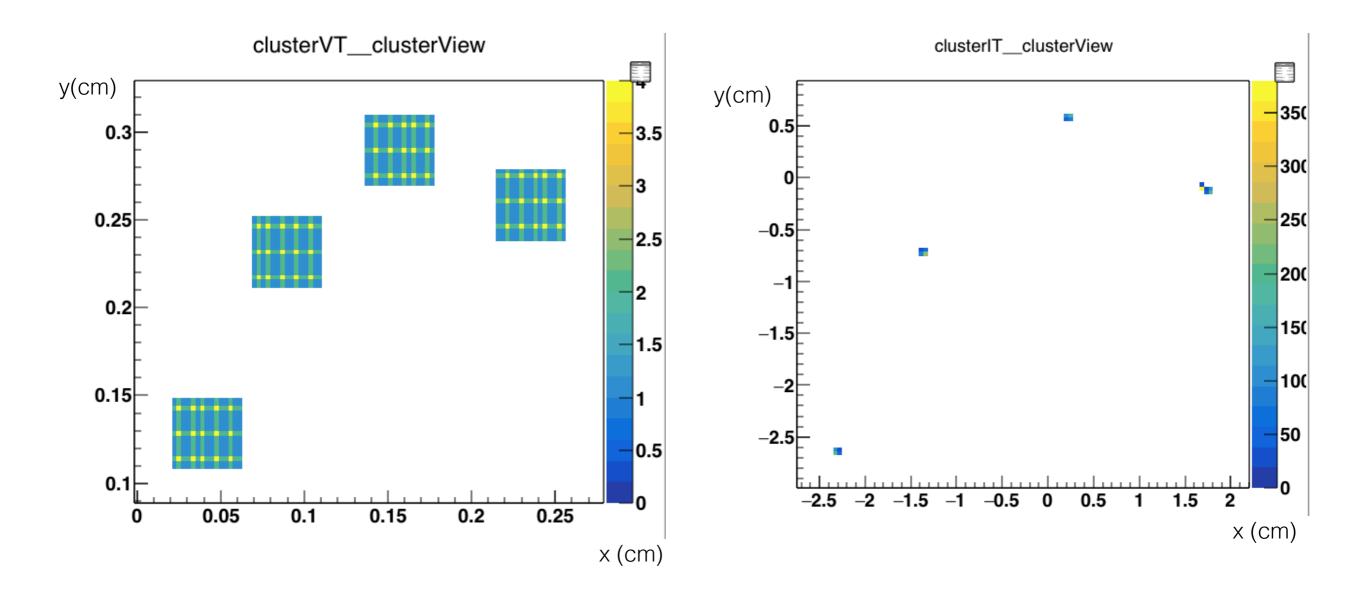
- Now pixels hits are categorised in different group depending on their origin (MC, cluster, noise, pileup, ...)
- Possible to cluster separately pixels from different groups;
- Simple clustering": group together neighbours pixels;
- On not consider possible contact-clusters: improbable, but to be checked;
- Ready for the digitisation, working on code harmonisation with Chris. <u>Close to finalisation</u>.







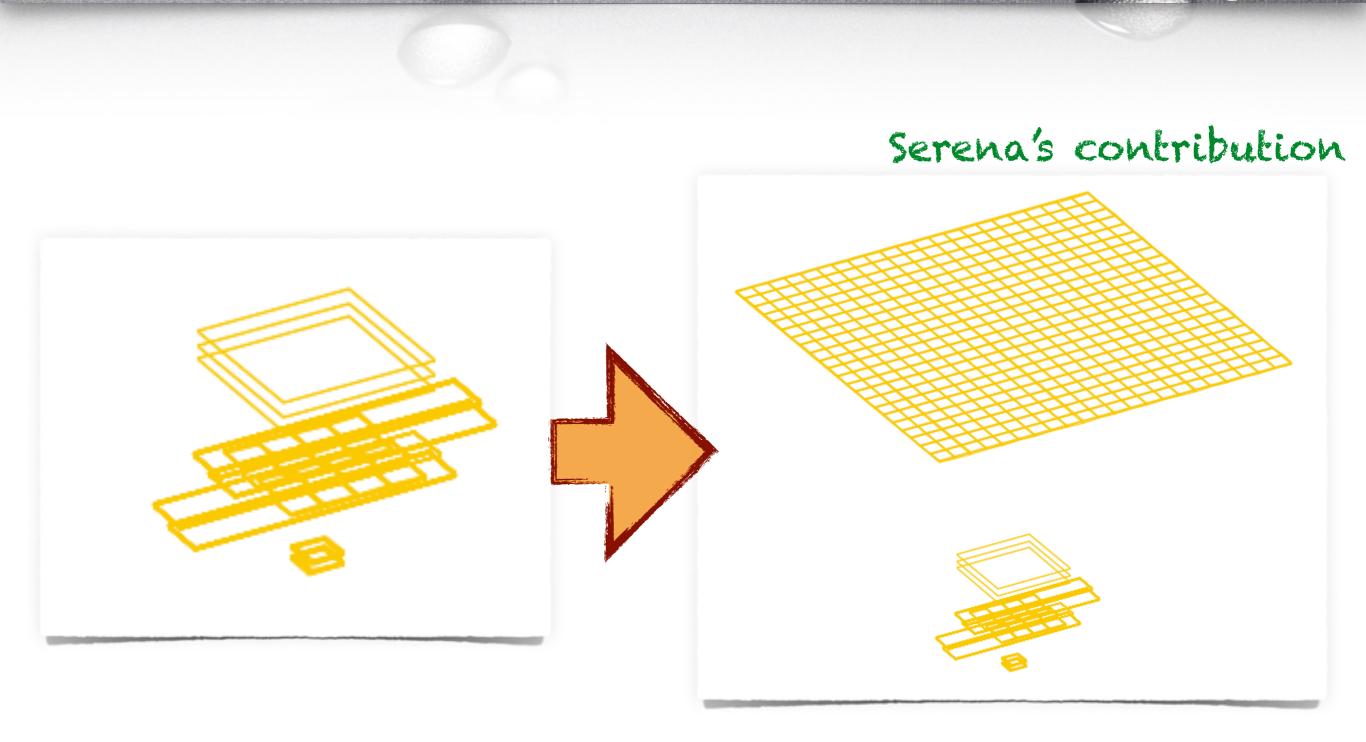
(20px square around MC hits for testing)



istering

Scintillator ready for tracking

Scintillator in tracking



Scintillator in tracking

18

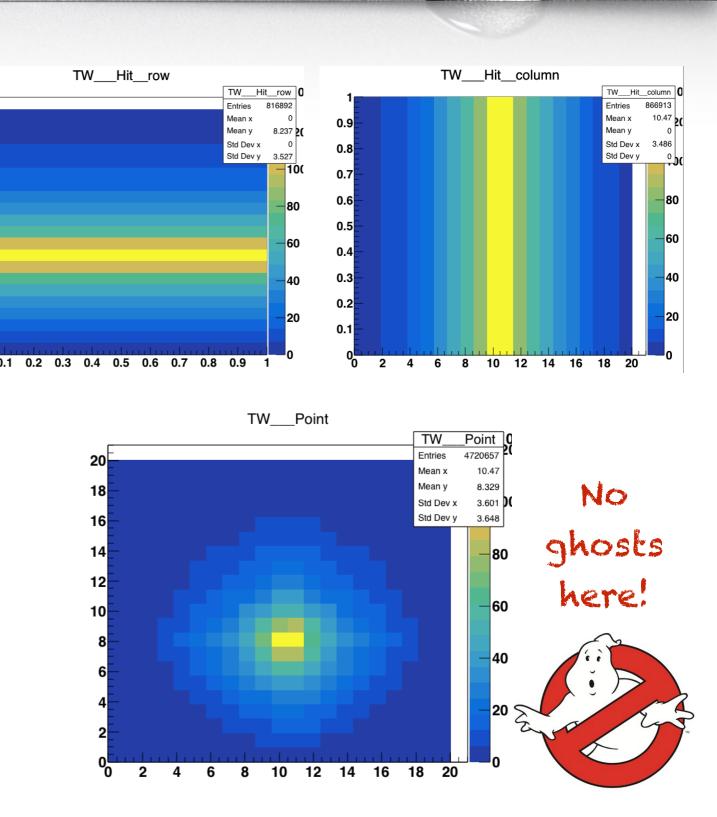
16

14

12

10

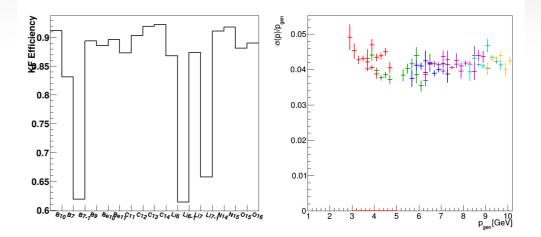
- Included the Scintillator in the Global Reconstruction;
- Spatial position (x, y) given by the hit bar, spatial resolution given by
 - $\checkmark \sqrt{12^* \text{lenght}} = 0,57 \text{cm}.$
- Founding all the intersections between bars with at least one hit;
- Using only non-ghost intersections for tracking

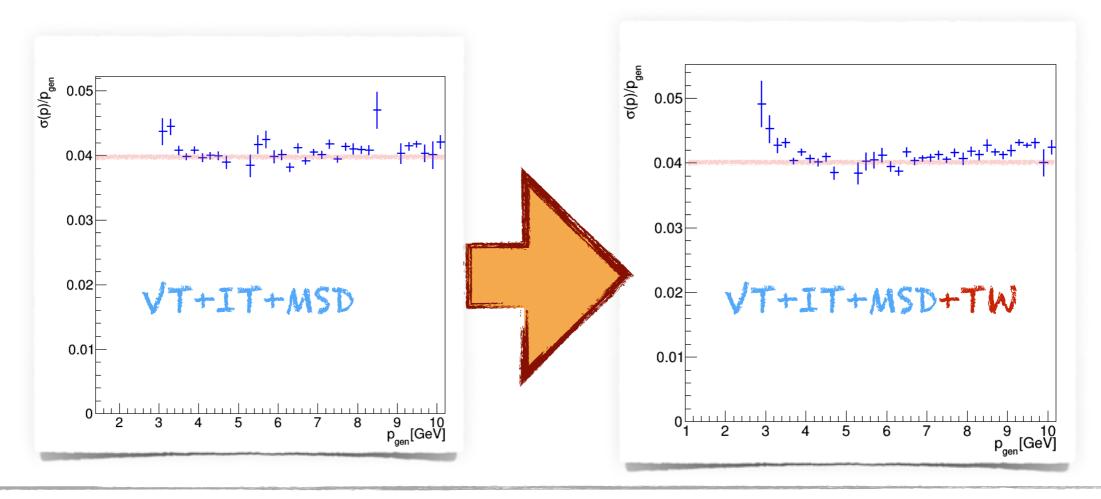


Scintinger in tracking

Longer lever-arm, worse resolution;

- Very preliminary result: cannot improve momentum resolution much...
- but probably useful for trackfounding in the tracking process





Software-bulletin

software bulletin

- New developer mailing list foot-software-develop@lists.infn.it, please add if you're thinking to **Contribute** to code developing. In the future, a user mailing list will be created;
- Developer contribute is always welcome;
- Useful link: <u>http://arpg-serv.ing2.uniroma1.it/twiki/bin/view/Main/</u> FOOTReconstruction#The_reconstruction_of_data_event
- Code will be soon moved to a FOOT common code git repository;
- One **Branch** for each simulation version, helps to keep order!

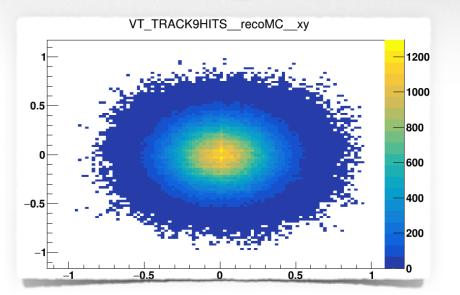
Updates:

- Association between reco hits and true particles;
- Hit categorisation and VT&IT clustering;
- TW fully functioning;
- ▶ ...



GOACLUSION

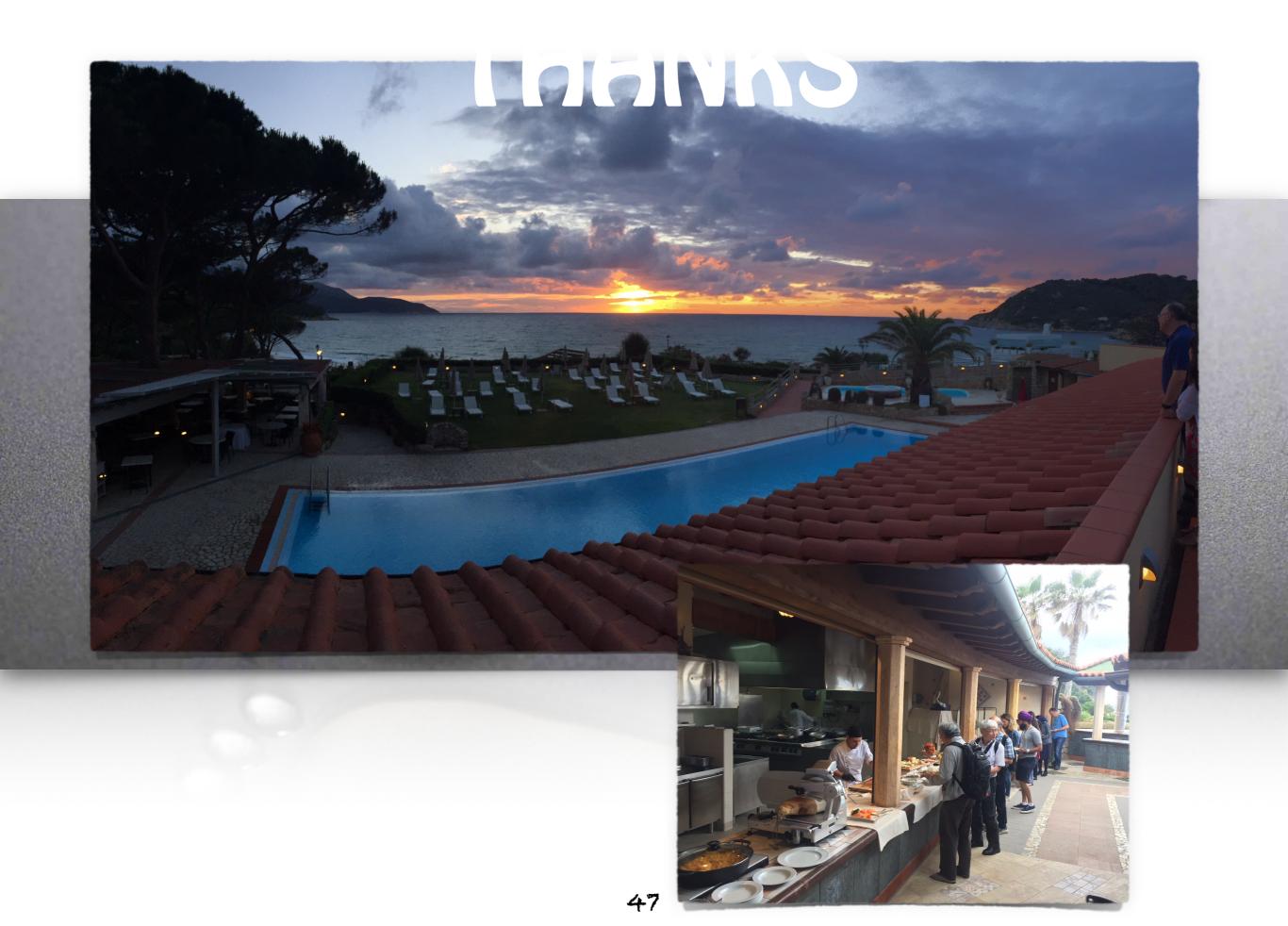
- Control plots for reco and geometry monitoring in SHOE
- Several tests with magnetic field rotations has been performed
- No significant momentum resolution change observed in the different configurations.
- Preliminary multitracking study
- CHI_2 method seems to be promising for VT (eff ~99%)
 - To be checked using reclusterd hit.



- Tested magnetic map stability to different stress and uncertainties;
- Found some desiderata on hardware design for good tracking performances
- Resolution decrease with momentum explained, great for high energy beams!
- Clustering in place
- Scintillator fully integrated!

VT xy Reso: 0.0006cm z Reso: 0.005cm

- IT xy Reso: 0.0006cm z Reso : 0.02cm
- MSD xy Reso: 0.003cm z Reso : 0.01cm
- Tolerate 500micron zuncertainty on IT module positioning







- ⊘ v14.0.1 -> mag 10cm, interspace 2cm:
 - Total mag field on the FOOT axis (from VT to MDS cm) = 239.389 kG*cm
 - integration step: ~100 micron

Soften bulletin

New developer mailing list, please add if you're thinking to contribute to code developing;

- In the future, a user mailing list will be created;
- One Branch for each simulation version

Association between reco hits and true particles

TW fully functioning

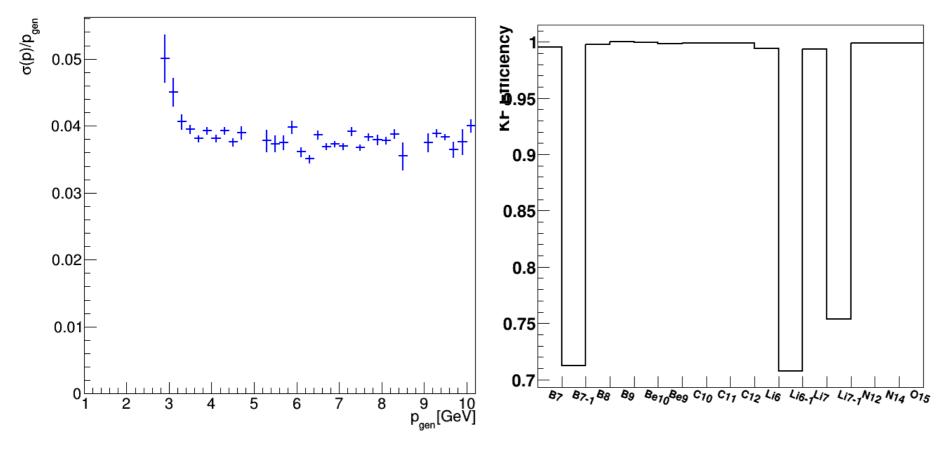
Next:

- Digitisation VT, IT
- Digitisation MSD
- Geometry of truncated pyramids for Calorimeter
- Hit managing for Calorimeter
- ▶ real-data reading, starting with test-beam
- vertexing
- Mutitracking

Momentan Resolution

- VT xy Reso: 0.0006cm z Reso: 0.0025cm
- IT xy Reso: 0.0006cm z Reso : 0.0025cm
- MSD xy Reso: 0.001cm z Reso : 0.050cm

V14.0.1 Magnets: 10 cm no smearing

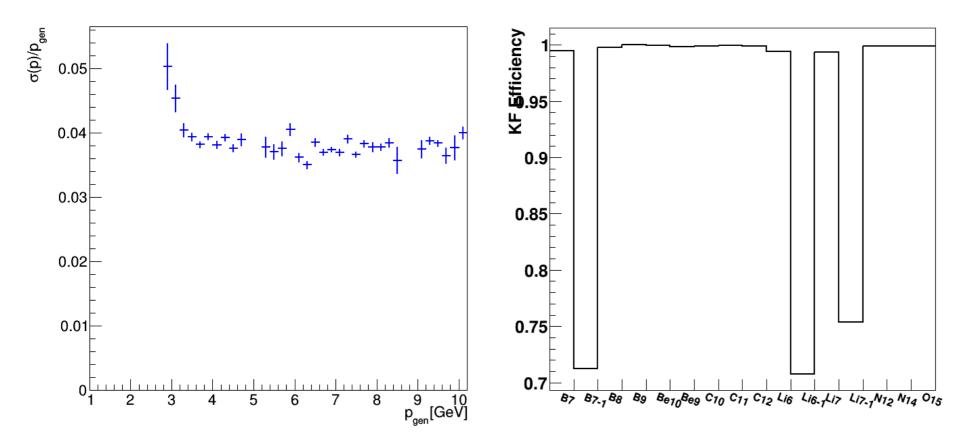


no change% Efficiency B7 = 0.99514 4914 4938 Efficiency B7-1 = 0.7125 114 160 Efficiency B8 = 0.99754 1622 1626 Efficiency B9 = 1 1038 1038 Efficiency Be10 = 0.999582 4784 4786 Efficiency Be9 = 0.998433 3824 3830 Efficiency C10 = 0.998694 6116 6124 Efficiency C11 = 0.999053 8440 8448 Efficiency C12 = 0.999111 4496 4500 Efficiency Li6 = 0.99441 9784 9839 Efficiency Li6-1 = 0.707581 196 277 Efficiency Li7 = 0.993751 4612 4641 Efficiency Li7-1 = 0.753425 55 73 Efficiency N12 = 0.999226 1291 1292 Efficiency N14 = 0.999137 6945 6951 Efficiency O15 = 0.999085 1092 1093

Momentan Resolution

- VT xy Reso: 0.0006cm z Reso: 0.0025cm
- IT xy Reso: 0.0006cm z Reso : 0.0025cm
- MSD xy Reso: 0.001cm z Reso : 0.050cm

V14.0.1 Magnets: 10 cm 1% smearing

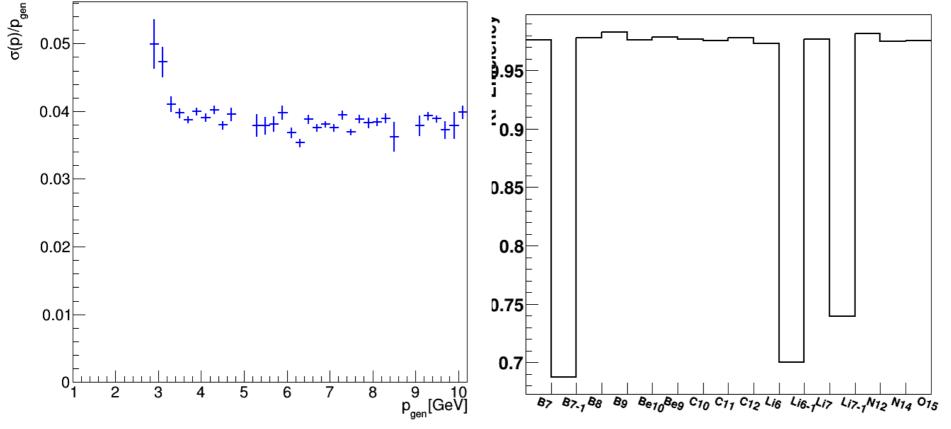


0.1% Efficiency B7 = 0.994735 4912 4938 Efficiency B7-1 = 0.7125 114 160 Efficiency B8 = 0.99754 1622 1626 Efficiency B9 = 1 1038 1038 Efficiency Be10 = 0.999582 4784 4786 Efficiency Be9 = 0.998172 3823 3830 Efficiency C10 = 0.99902 6118 6124 Efficiency C11 = 0.99929 8442 8448 Efficiency C12 = 0.999111 4496 4500 Efficiency Li6 = 0.994105 9781 9839 Efficiency Li6-1 = 0.707581 196 277 Efficiency Li7 = 0.99332 4610 4641 Efficiency Li7-1 = 0.753425 55 73 Efficiency N12 = 0.999226 1291 1292 Efficiency N14 = 0.998993 6944 6951 Efficiency O15 = 0.999085 1092 1093

MOMERTIN RESOLUCION

- VT xy Reso: 0.0006cm z Reso: 0.0025cm
- IT xy Reso: 0.0006cm z Reso : 0.0025cm
- MSD xy Reso: 0.001cm z Reso : 0.050cm

V14.0.1 Magnets: 10 cm 5% smearing



5%

Efficiency B7 = 0.975901 4819 4938 Efficiency B7-1 = 0.6875 110 160 Efficiency B8 = 0.97786 1590 1626 Efficiency B9 = 0.982659 1020 1038 Efficiency Be10 = 0.976389 4673 4786 Efficiency Be9 = 0.978329 3747 3830 Efficiency C10 = 0.976486 5980 6124 Efficiency C11 = 0.975852 8244 8448 Efficiency C12 = 0.978 4401 4500 Efficiency Li6 = 0.973066 9574 9839 Efficiency Li6-1 = 0.700361 194 277 Efficiency Li7 = 0.976514 4532 4641 Efficiency Li7-1 = 0.739726 54 73 Efficiency N12 = 0.981424 1268 1292 Efficiency N14 = 0.974968 6777 6951 Efficiency O15 = 0.975297 1066 1093

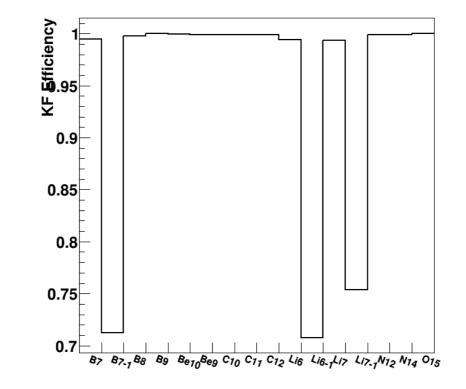
Momentan Resolution

VT xy Reso: 0.0006cm z Reso: 0.0025cm

IT xy Reso: 0.0006cm z Reso : 0.0025cm

MSD xy Reso: 0.001cm z Reso : 0.050cm V14.0.1 Magnets: 10 cm 0,5% smearing

plot no needed looking at the others...



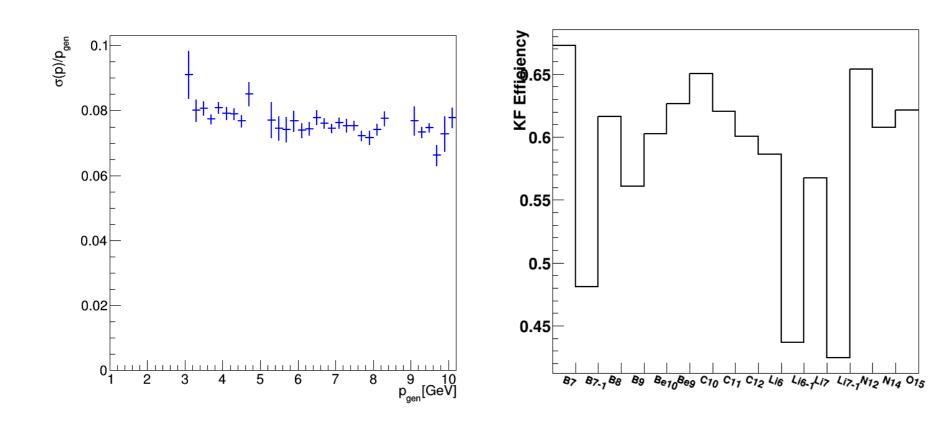
0,5%

Efficiency B7 = 0.994937 4913 4938 Efficiency B7-1 = 0.7125 114 160 Efficiency B8 = 0.99754 1622 1626 Efficiency B9 = 1 1038 1038 Efficiency Be10 = 0.999582 4784 4786 Efficiency Be9 = 0.998695 3825 3830 Efficiency C10 = 0.998694 6116 6124 Efficiency C11 = 0.999053 8440 8448 Efficiency C12 = 0.998889 4495 4500 Efficiency Li6 = 0.994308 9783 9839 Efficiency Li6-1 = 0.707581 196 277 Efficiency Li7 = 0.993751 4612 4641 Efficiency Li7-1 = 0.753425 55 73 Efficiency N12 = 0.999226 1291 1292 Efficiency N14 = 0.999137 6945 6951 Efficiency O15 = 1 1093 1093

Momentan Resolution

- VT xy Reso: 0.0006cm z Reso: 0.0025cm
- IT xy Reso: 0.0006cm z Reso : 0.0025cm
- MSD xy Reso: 0.001cm z Reso : 0.050cm

V14.0.1 Magnets: 10 cm 50% smearing



50%

Efficiency B7 = 0.672539 3321 4938 Efficiency B7-1 = 0.48125 77 160 Efficiency B8 = 0.616236 1002 1626 Efficiency B9 = 0.560694 582 1038 Efficiency Be10 = 0.602382 2883 4786 Efficiency Be9 = 0.626371 2399 3830 Efficiency C10 = 0.650229 3982 6124 Efficiency C11 = 0.620265 5240 8448 Efficiency C12 = 0.600667 2703 4500 Efficiency Li6 = 0.586035 5766 9839 Efficiency Li6-1 = 0.436823 121 277 Efficiency Li7 = 0.56755 2634 4641 Efficiency Li7-1 = 0.424658 31 73 Efficiency N12 = 0.654025 845 1292 Efficiency N14 = 0.607826 4225 6951 Efficiency O15 = 0.621226 679 1093



no change%

Efficiency B7 = 0.99514 4914 4938 Efficiency B7-1 = 0.7125 114 160 Efficiency B8 = 0.99754 1622 1626 Efficiency B9 = 1 1038 1038 Efficiency Be10 = 0.999582 4784 4786 Efficiency Be9 = 0.998433 3824 3830 Efficiency C10 = 0.998694 6116 6124 Efficiency C11 = 0.999053 8440 8448 Efficiency C12 = 0.999111 4496 4500 Efficiency Li6 = 0.99441 9784 9839 Efficiency Li6-1 = 0.707581 196 277 Efficiency Li7 = 0.993751 4612 4641 Efficiency Li7-1 = 0.753425 55 73 Efficiency N12 = 0.999226 1291 1292 Efficiency N14 = 0.999137 6945 6951 Efficiency O15 = 0.999085 1092 1093

1%

Efficiency B7 = 0.994735 4912 4938 Efficiency B7-1 = 0.7125 114 160 Efficiency B8 = 0.99754 1622 1626 Efficiency B9 = 1 1038 1038 Efficiency Be10 = 0.999582 4784 4786 Efficiency Be9 = 0.998172 3823 3830 Efficiency C10 = 0.99902 6118 6124 Efficiency C11 = 0.99929 8442 8448 Efficiency C12 = 0.999111 4496 4500 Efficiency Li6 = 0.994105 9781 9839 Efficiency Li6-1 = 0.707581 196 277 Efficiency Li7 = 0.99332 4610 4641 Efficiency Li7-1 = 0.753425 55 73 Efficiency N12 = 0.999226 1291 1292 Efficiency N14 = 0.998993 6944 6951 Efficiency O15 = 0.999085 1092 1093

0.5%

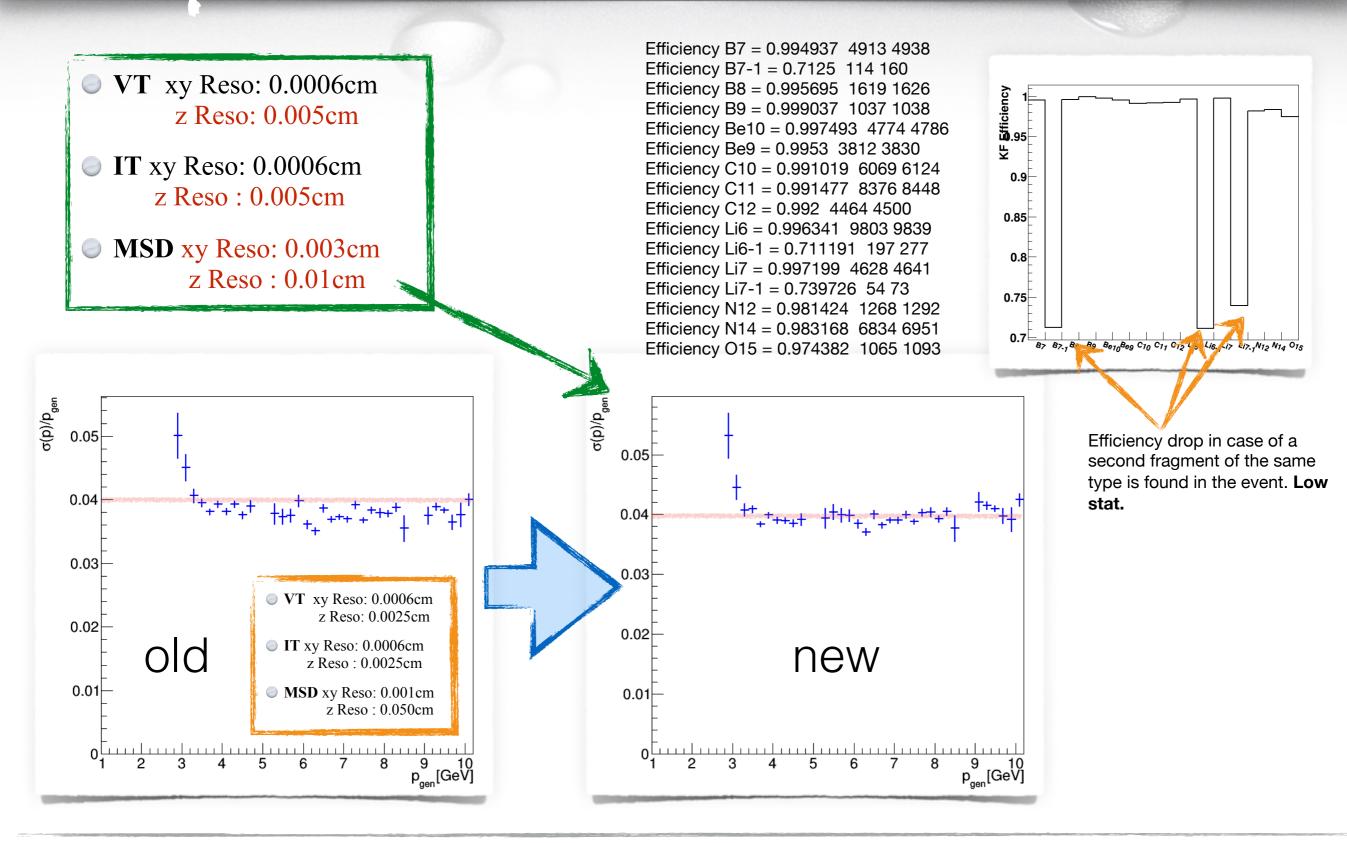
-)
Efficiency B7 = 0.994937 4913 4938
Efficiency B7-1 = 0.7125 114 160
Efficiency B8 = 0.99754 1622 1626
Efficiency B9 = 1 1038 1038
Efficiency Be10 = 0.999582 4784 4786
Efficiency Be9 = 0.998695 3825 3830
Efficiency C10 = 0.998694 6116 6124
Efficiency C11 = 0.999053 8440 8448
Efficiency C12 = 0.998889 4495 4500
Efficiency Li6 = 0.994308 9783 9839
Efficiency Li6-1 = 0.707581 196 277
Efficiency Li7 = 0.993751 4612 4641
Efficiency Li7-1 = 0.753425 55 73
Efficiency N12 = 0.999226 1291 1292
Efficiency N14 = 0.999137 6945 6951
Efficiency $O15 = 1,1002,1002$

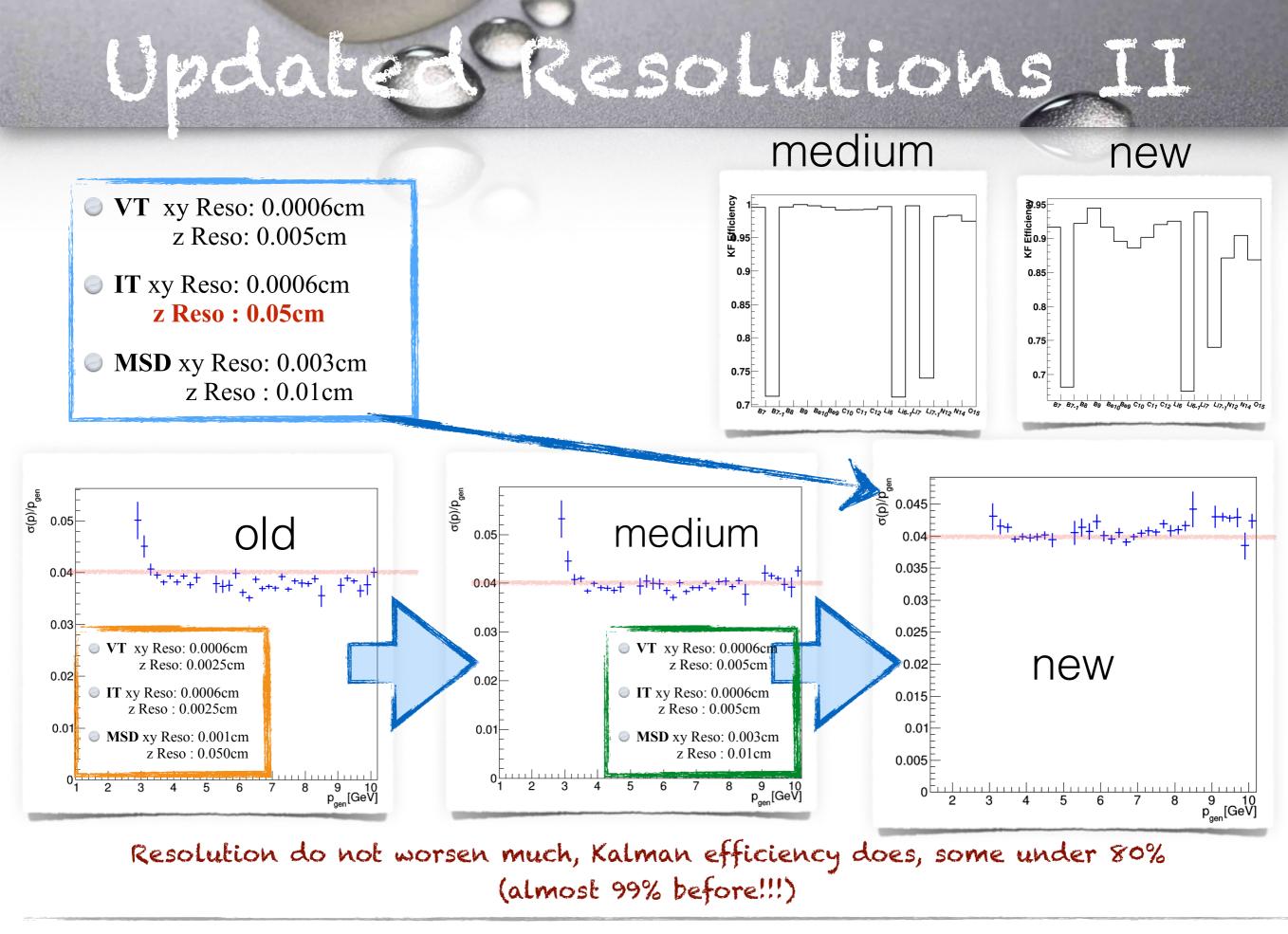
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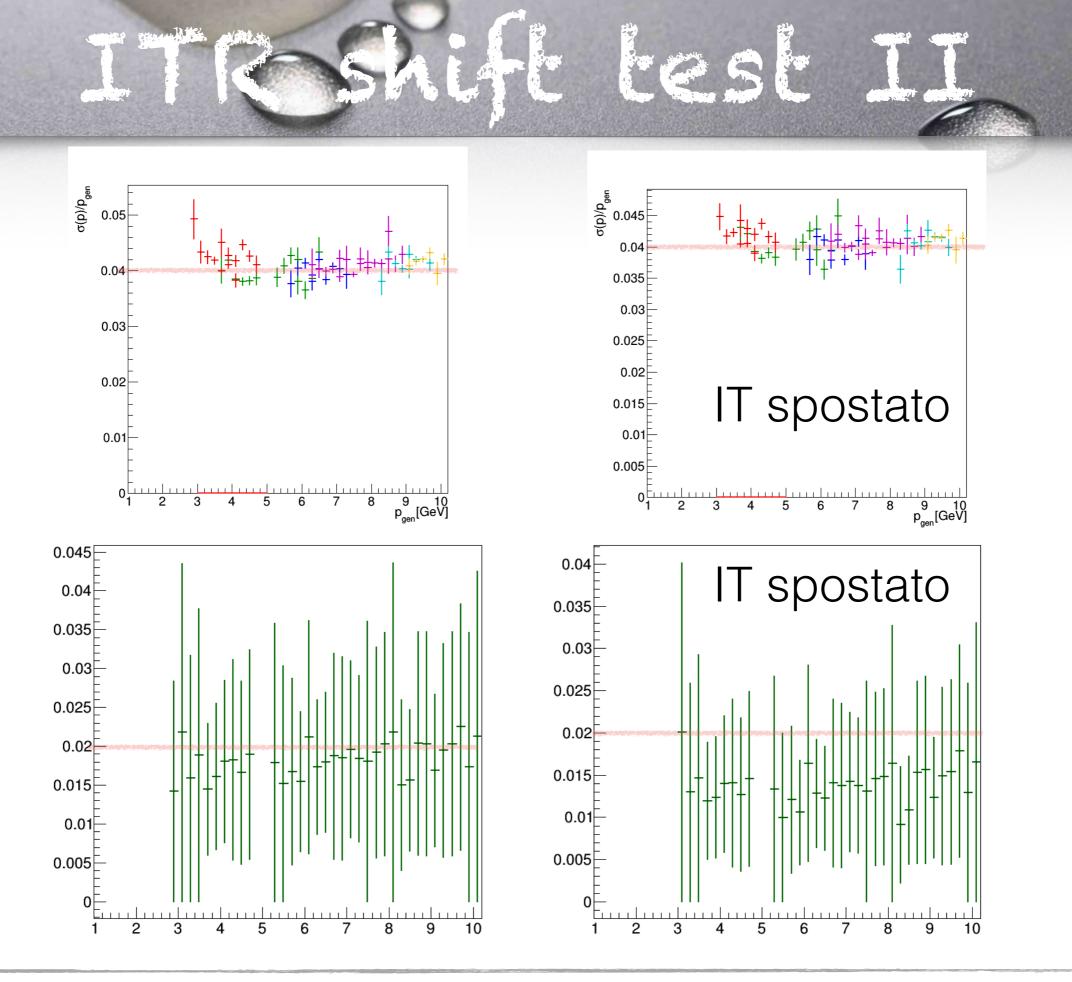
5%

Efficiency B7 = 0.975901 4819 4938 Efficiency B7-1 = 0.6875 110 160 Efficiency B8 = 0.97786 1590 1626 Efficiency B9 = 0.982659 1020 1038 Efficiency Be10 = 0.976389 4673 4786 Efficiency Be9 = 0.978329 3747 3830 Efficiency C10 = 0.976486 5980 6124 Efficiency C11 = 0.975852 8244 8448 Efficiency C12 = 0.978 4401 4500 Efficiency Li6 = 0.973066 9574 9839 Efficiency Li6-1 = 0.700361 194 277 Efficiency Li7 = 0.976514 4532 4641 Efficiency Li7-1 = 0.739726 54 73 Efficiency N12 = 0.981424 1268 1292 Efficiency N14 = 0.974968 6777 6951 Efficiency O15 = 0.975297 1066 1093









TW___Hit__row TW___Hit__column TW___Hit__row 0 TW__Hit_column 0 816892 Entries Entries 866913 20 10.47 20 Mean x Mean x 0 0.9 Mean y 18 Mean y 8.237 2(Std Dev x 3.486 Std Dev x 0 0.8 Std Dev y Std Dev y 3.527 ື່ມເ 16 KE Efficiency 100 0.7 14 80 0.6 0.04 80 12 0.5 0.035 10 60 60 0.4 8 0.03 0.3 40 0.8 40 0.025 0.2 20 20 0.75 0.02 0.1 0.015 0 0 6 8 10 12 14 16 18 20 0.1 0.2 0.3 0.4 0.5 0.6 0.7 0.8 0.9 0.7 1 2 4 TW___Point 0.01 ط(d)/(ben س∈ (b)//ben σ(p)/p_{gen} 0.05 0.05 KF Efficie@cy 0.04 0.04 0.03 0.03 0.85 0.02 0.02 0.8 0.01 0.75 0.01 3 0.7 $0_{1}^{-1} 2 3 4 5 6 7 8 9 10 \\ p_{gen}[GeV]$

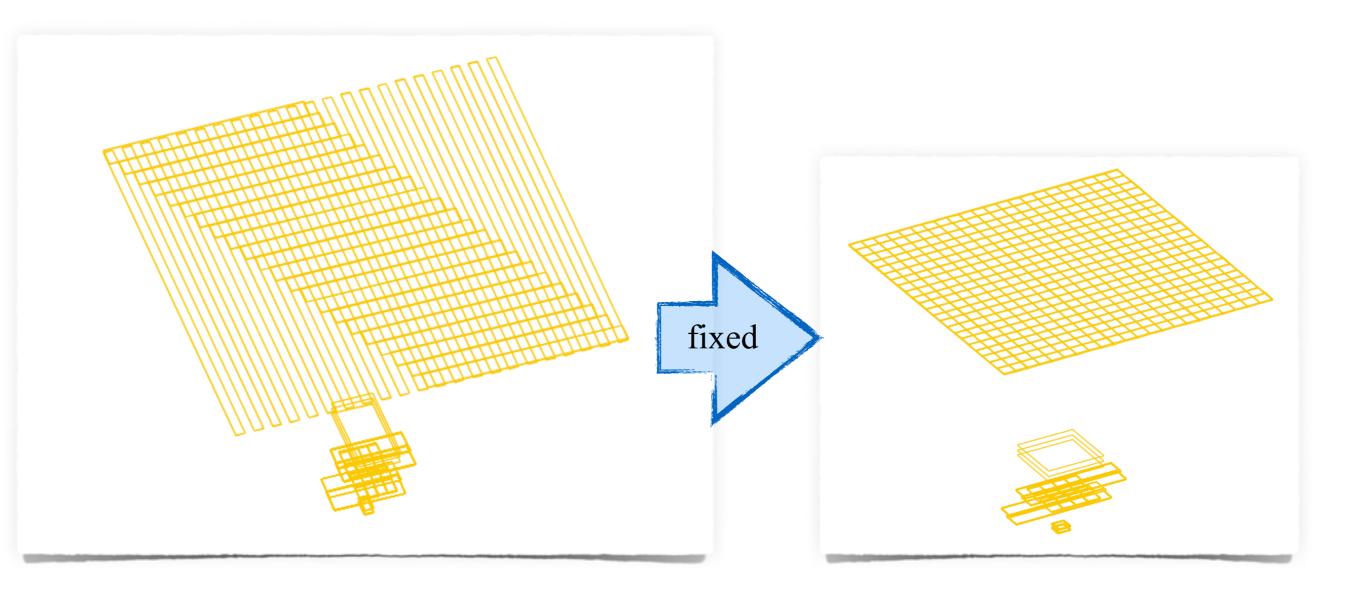
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60

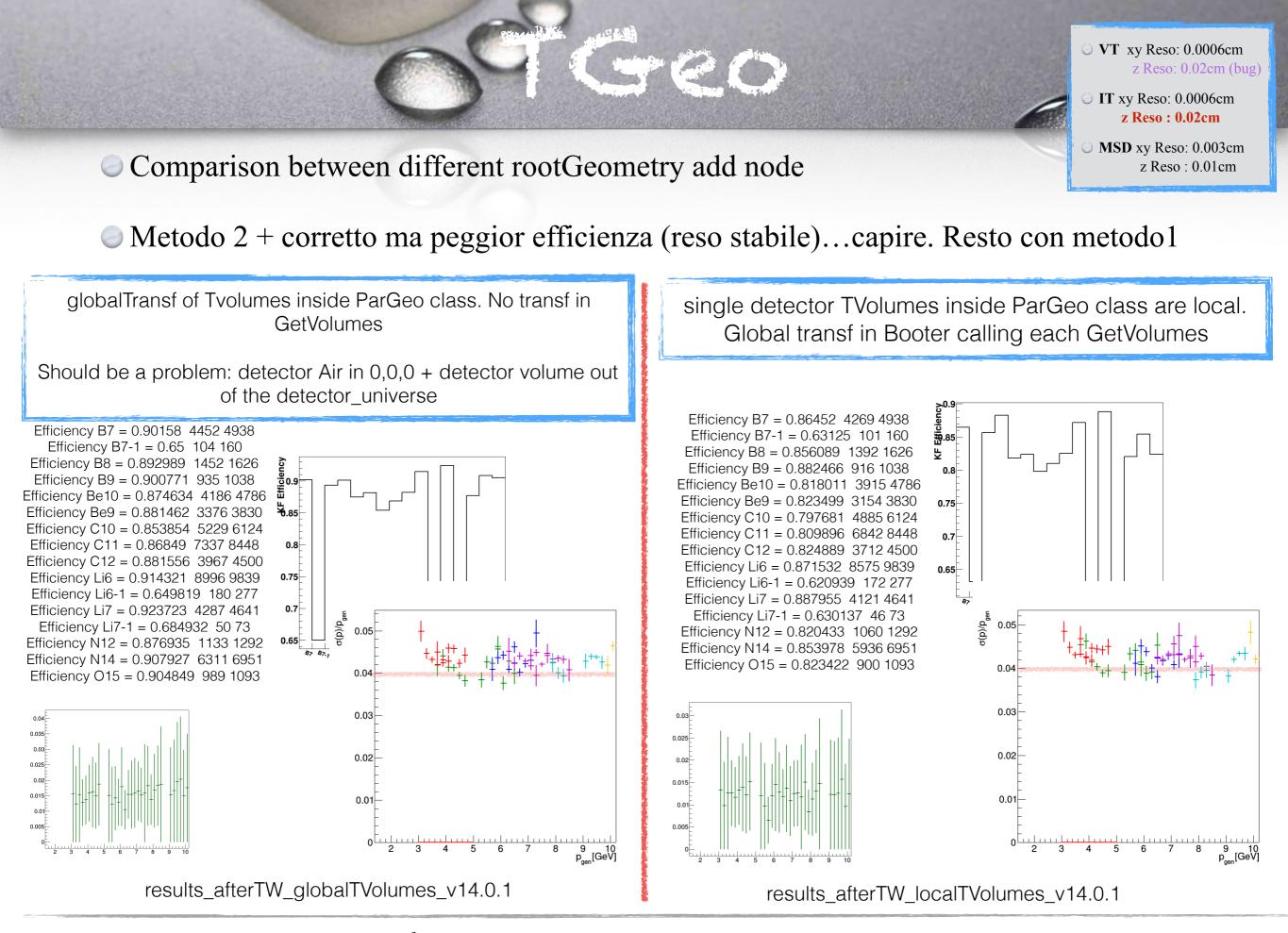


const Double_t SCN_BAR_WIDTH =2.0;//strip dimension in x (I lay) or y (II lay)
 const Double_t SCN_BAR_HEIGHT =44.0;//strip dimension in y (I lay) or x (II lay)

oconst Double_t SCN_BAR_THICK =0.3;//strip (layer) thickness



20/5/2018



FOOT Bologna 2018

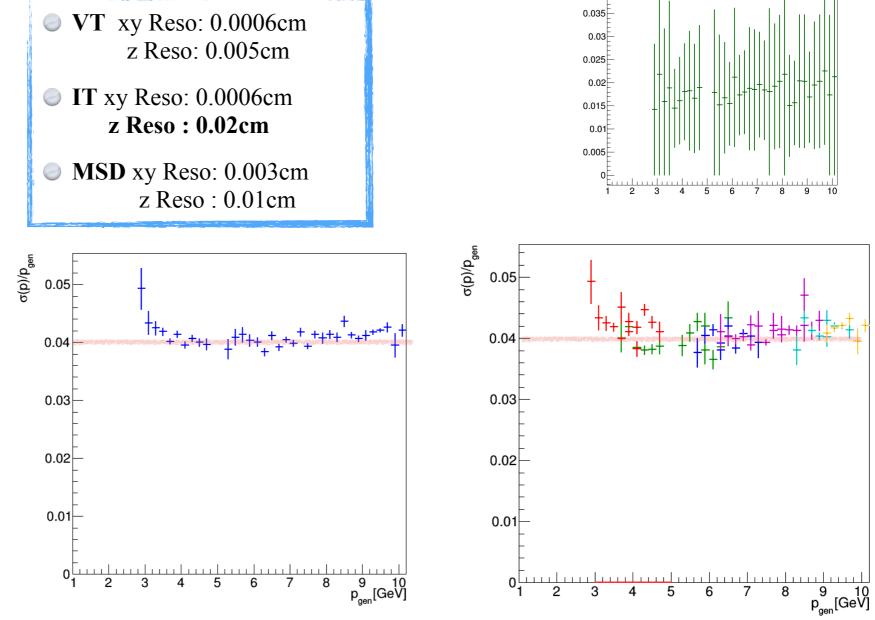
○ 20/5/2018 - master update.

inserting correct reso, all clustering and scintillator, correct mass in PDG.

⊘ v14.0.1

Status

Efficiency B10 = 0.941233 977 1038 Efficiency B7 = 0.940867 4646 4938 Efficiency B7-1 = 0.675 108 160 Efficiency B9 = 0.930504 1513 1626 Efficiency Be10 = 0.927937 3554 3830 Efficiency Be11 = 0.918721 4397 4786 Efficiency C11 = 0.902025 5524 6124 Efficiency C12 = 0.924598 7811 8448 Efficiency C13 = 0.938 4221 4500 Efficiency C14 = 0.943324 982 1041 Efficiency Li6 = 0.946438 9312 9839 Efficiency Li6-1 = 0.6787 188 277 Efficiency Li7 = 0.958199 4447 4641 Efficiency Li7-1 = 0.739726 54 73 Efficiency N14 = 0.941641 6438 6837 Efficiency N15 = 0.951805 6616 6951 Efficiency O15 = 0.927495 8187 8827 Efficiency O16 = 0.929552 1016 1093



0.045

0.04