

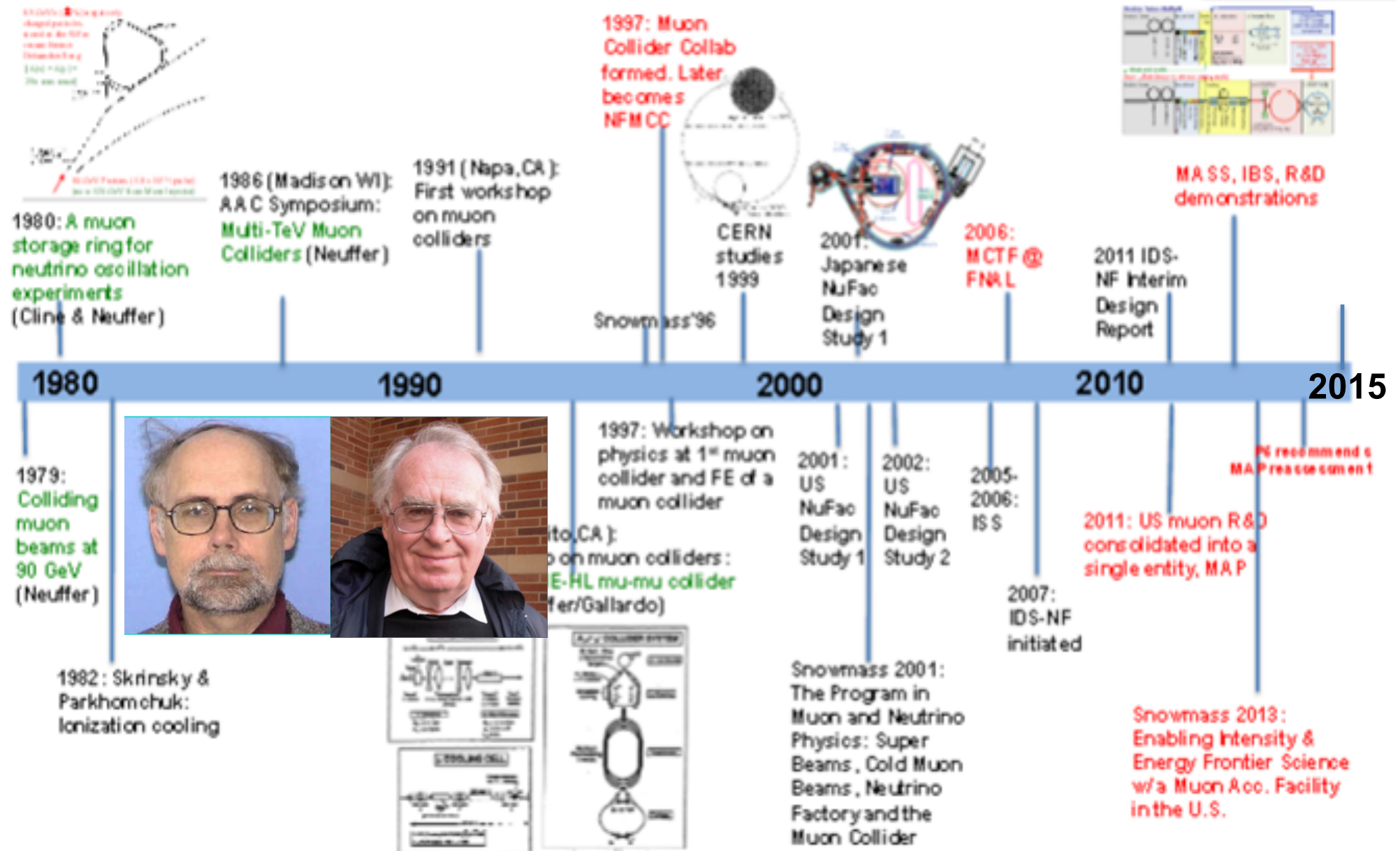
# **Muon colliders**

# Outline

- Muons case
- Muon accelerators challenges:
  - **muon production**
  - emittance reduction via **cooling**
  - high-gradient acceleration
- Conclusions

# Muons: a long history of development

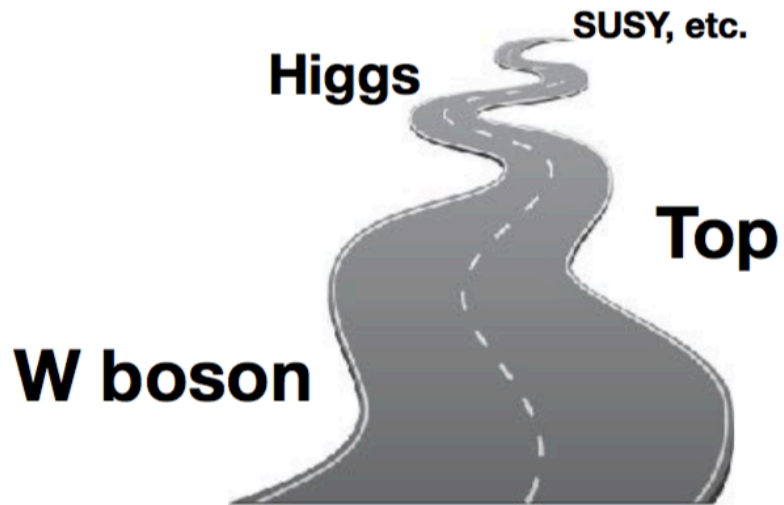
Rob Ryne



# Ideology

A. Wulzer at last  
LEMMA meeting, 20/4/18

## HEP before the LHC



## HEP before the F.C.



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## HEP before the LHC



## HEP before the F.C.



Particle physics is not **validation** anymore, rather it  
is **exploration of unknown territories** \*

\* Not necessarily a bad thing. Columbus left for his trip just  
because he had no idea of where he was going !!

# Ideology

A. Wulzer at last  
LEMMA meeting, 20/4/18

**No single experiment** can explore all directions at once.

**None** can guarantee discoveries.

The next big FC **will exist only if** capable to **explore many directions**, and be **conclusive** on some of those



# Dark Matter

A. Wulzer at last  
LEMMA meeting, 20/4/18

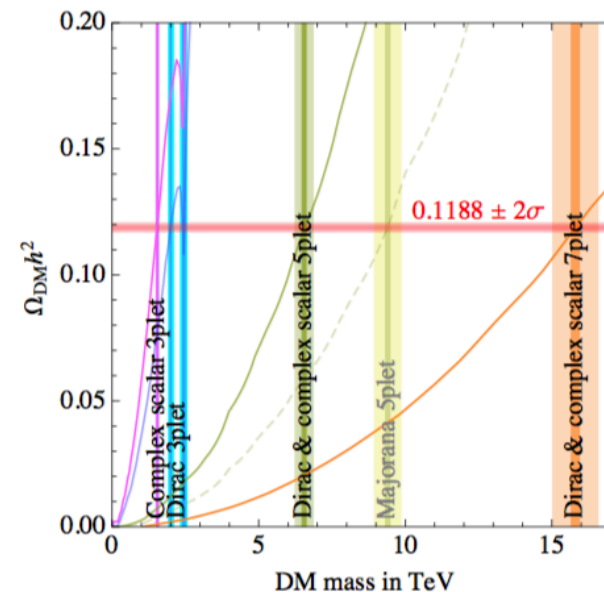
The FC should be capable to tell if DM is **WIMP**

WIMP can have up to **15 TeV** mass

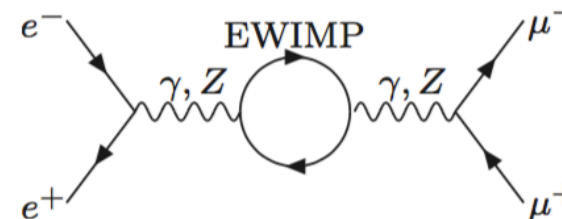
WIMP can be invisible to DD if **inelastic** or **leptophilic**

**Accidental DM:** stability from **accidental symmetries**

| $\chi$                             | $M_\chi^{(\text{DM})}$ [TeV] |
|------------------------------------|------------------------------|
| $(1, 3, \epsilon)_{\text{CS}}$     | 1.5                          |
| $(1, 3, \epsilon)_{\text{DF}}$     | 2.0                          |
| $(1, 3, 0)_{\text{MF}^*}$          | 3.0                          |
| $(1, 5, \epsilon)_{\text{CS, DF}}$ | 6.6                          |
| $(1, 5, 0)_{\text{MF}^{**}}$       | 9.6                          |
| $(1, 7, \epsilon)_{\text{CS, DF}}$ | 16                           |



Searched for directly, but also indirectly



# Naturalness

A. Wulzer at last  
LEMMA meeting, 20/4/18

$$\Delta \geq \frac{\delta m_H^2}{m_H^2} \simeq \left( \frac{126 \text{ GeV}}{m_H} \right)^2 \left( \frac{\Lambda_{\text{SM}}}{500 \text{ GeV}} \right)^2$$

LHC may push conventional Natural models to

$$\Lambda_{\text{SM}} \gtrsim 2 \text{ TeV} \longrightarrow \Delta \gtrsim 10$$

Still Naturalness might be there in the form of:

**Partial Unnaturalness**

$$\Delta \sim 100$$



$$\Lambda_{\text{SM}} \sim 5 \text{ TeV}$$

**Neutral Naturalness**

$$\Delta \sim \text{few} \longrightarrow \Lambda_{\text{SM}}^{\text{col.}} \sim 5 \text{ TeV}$$



$$\Lambda_{\text{SM}}^{\text{neut.}} \lesssim 1 \text{ TeV}$$

Need **5 TeV** reach on ordinary Top Partners

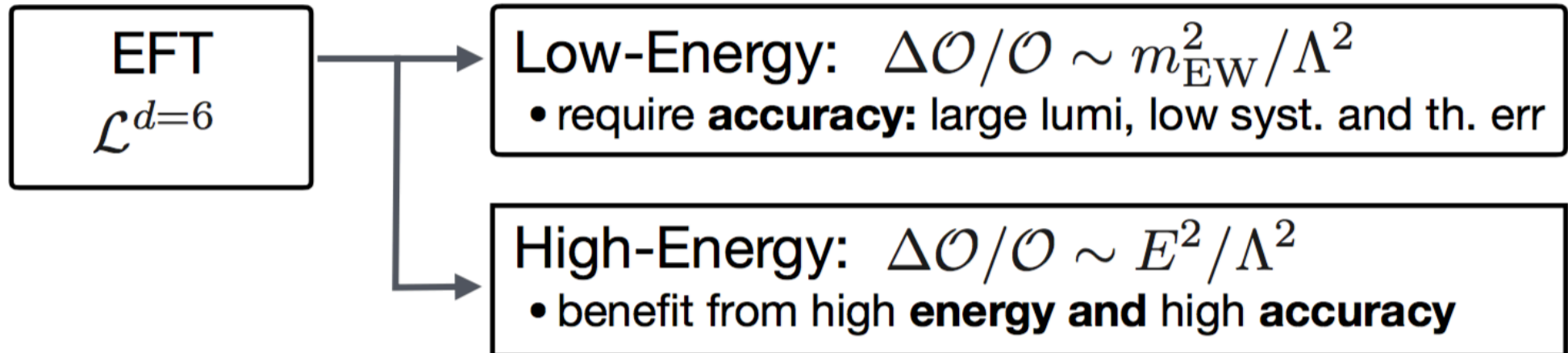
Still, the higher the reach, the better



# If Everything Fails

A. Wulzer at last  
LEMMA meeting, 20/4/18

The FC must have indirect reach superior to direct one,  
on BSM scale, by at least a few



Must be able to **measure** SM proc.'s, at **few% at least**

# Muon Colliders

A. Wulzer at last  
LEMMA meeting, 20/4/18

We should remind everybody about pdf's!

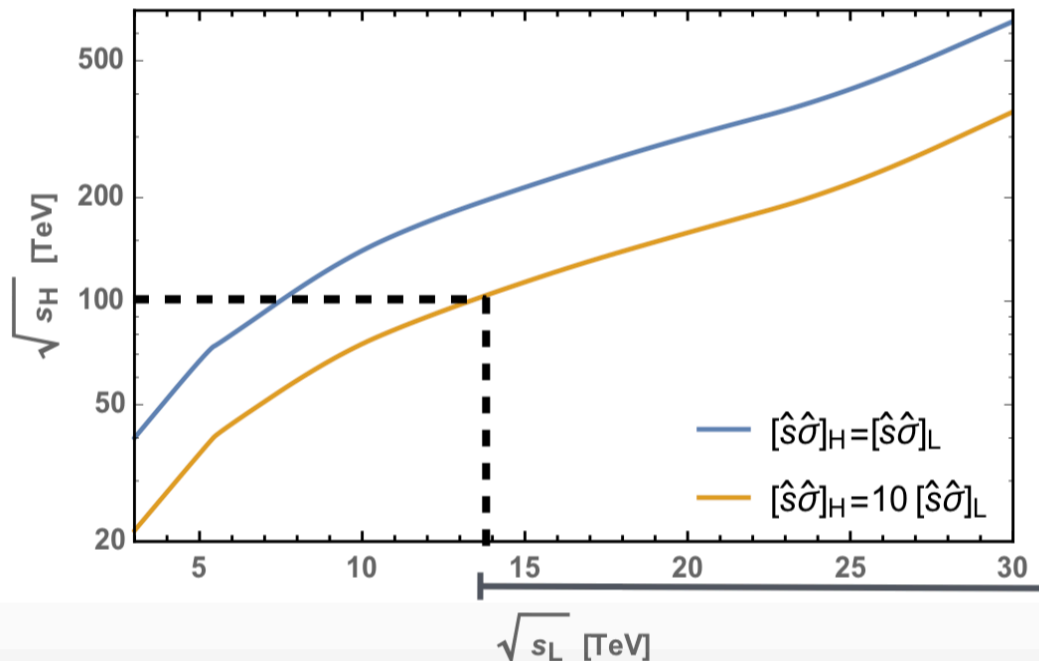
**Lepton coll.** operating at energy  $\sqrt{s_L}$ .  
Cross section for reaction at  $E \sim \sqrt{s_L}$   
(e.g., production of BSM at  $M=E$ )

$$\sigma_L(s_L) = \frac{1}{s_L} [\hat{\sigma}]_L$$

**Hadron coll.** operating at energy  $\sqrt{s_H}$ .  
Cross section for reaction at  $E$ .  
**Parton Luminosity suppression**

$$\sigma_H(E, s_H) = \frac{1}{s_H} \int_{E^2/s_H}^1 \frac{d\tau}{\tau} \frac{dL}{d\tau} [\hat{\sigma}]_H$$

Find **equivalent**  $\sqrt{s_H}$  for Had. Coll. have **same cross-section** as Lep. Coll.  
for reactions at  $E \sim \sqrt{s_L}$ . Use that  $[\hat{\sigma}]$  is nearly constant in  $\tau$ .



**QCD-coloured BSM** can easily have much larger partonic XS.  
Comparison even more favourable for **QCD-neutral BSM**

**14 TeV  $\mu$ -collider nearly as good as the FCC at 100 TeV?**

# Muon Colliders Requirements Specification

A. Wulzer at last  
LEMMA meeting, 20/4/18

The muon collider must:

0) Run for a reasonable time:  $10^{34}\text{cm}^{-2}\text{s}^{-1} \rightarrow 900\text{fb}^{-1}$   
“reasonable” here means 3\*LHC

1) Pair produce more than 100 EW particles:  
sufficient to probe “easy” decay modes (e.g., for top partners/stops)

$$N = 1300 \left( \frac{10 \text{ TeV}}{\sqrt{s}} \right)^2 \left( \frac{L}{10^{34}\text{cm}^{-2}\text{s}^{-1}} \right) \rightarrow L > \frac{1}{13} \left( \frac{\sqrt{s}}{10 \text{ TeV}} \right)^2 10^{34}\text{cm}^{-2}\text{s}^{-1}$$

2) Measure SM cross-sections:

simple estimate for  $2 \rightarrow 2$ . but what about WW scattering, HH prod...?

$$L > \left( \frac{\sqrt{s}}{10 \text{ TeV}} \right)^2 10^{34}\text{cm}^{-2}\text{s}^{-1}$$

3) Probe DM in mono- $\gamma$ /W/Z, EW singlets, ...

**L>?** This should be assessed!

# Muon based colliders great potential

As with an  $e^+e^-$  collider, a  $\mu^+\mu^-$  collider offers a precision probe of fundamental interactions without energy limitations

- By **synchrotron radiation** (limit of  $e^+e^-$  **circular** colliders)
- By **beam-strahlung** (limit of  $e^+e^-$  **linear** colliders)

**Muon Collider is the ideal technology to extend lepton high energy frontier in the **multi-TeV** range with **reasonable dimension, cost and power consumption****

**Muon based **Higgs factory** takes advantage of a strong coupling to Higgs mechanism by s resonance**

**IF THE MUON BEAM NOVEL TECHNOLOGY CAN BE DEMONSTRATED TO BE FEASIBLE**

# Muons: Issues & Challenges



- **Limited lifetime: 2.2  $\mu\text{s}$  (at rest)**

- Race against death: generation, acceleration & collision before decay

- Muons decay in accelerator and detector

- Shielding of detector and facility irradiation

- Collider and Physics feasibility with large background environment?

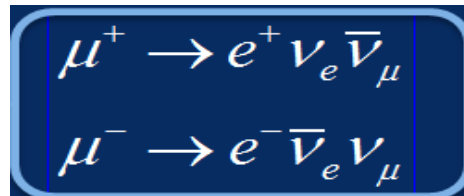
Not by beamshtrahlung as with e+/e- but by muon decay (e,  $\nu$ )

Reduced background at high energy due to increased muon lifetime



- Decays in neutrinos:

- Ideal source of well defined electron & muon neutrinos in equal quantities whereas Superbeams by pion decay only provide muon  $\nu$ :



The neutrino factory  
concept

- **Generated as tertiary particles in large emittances**

- powerful MW(s) proton driver and pion decay

- novel (fast) cooling and acceleration methods

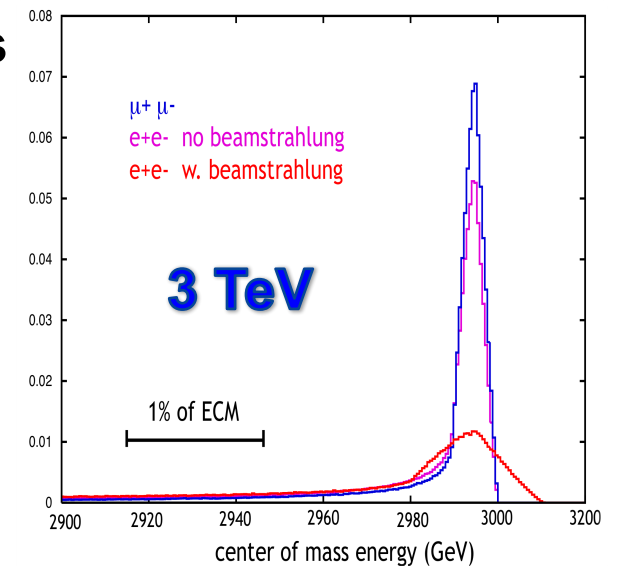


**Development of novel technologies  
with key accelerator and detector challenges**

# Muon beams specific properties

**Muons are leptons like electrons & positrons but with a mass ( $105.7 \text{ MeV}/c^2$ ) 207 times larger**

- **Negligible synchrotron radiation emission ( $\propto m^{-2}$ )**
  - **Multi-pass collisions (1000 turns) in collider ring**
    - High luminosity with reasonable beam power and wall plug power consumption
      - **relaxed beam emittances & sizes, alignment & stability**
    - Multi-detectors supporting broad physics communities
    - Large time ( $15 \mu\text{s}$ ) between bunch crossings
  - **No beam-strahlung at collision:**
    - narrow luminosity spectrum
  - **Multi-pass acceleration in rings or RLA:**
    - Compact acceleration system and collider
    - Cost effective construction & operation
  - **No cooling by synchrotron radiation in standard damping rings**
    - Requires development of novel cooling method



# Synchrotron radiation

$$P = \frac{2}{3} \frac{e^2 c}{4\pi\epsilon_0} \frac{\beta^4 \gamma^4}{\rho^2}$$

$$U_0 = \frac{e^2}{3\epsilon_0} \frac{\beta^3 \gamma^4}{\rho}$$

$$U_0 = 5.5 \times 10^{-18} \gamma^4 / \rho$$

$$\text{electrons } U_0 \text{ (GeV)} = 9 \cdot 10^{-5} E^4(\text{GeV}) / \rho(\text{m})$$

$$\text{muons } U_0 \text{ (GeV)} = 5 \cdot 10^{-14} E^4(\text{GeV}) / \rho(\text{m})$$

$$\text{protons } U_0 \text{ (GeV)} = 7 \cdot 10^{-18} E^4(\text{GeV}) / \rho(\text{m})$$

$r = 3000 \text{ m}$  (LEP/LHC tunnel)

@  $U_0/E_b \sim 10\%$  electrons are limited to  $\sim 150 \text{ GeV}$  ( $U_0 = 15 \text{ GeV}$ )

@  $U_0/E_b \sim 10\%$  muons can go up  $200 \text{ TeV}$  ( $U_0 = 20 \text{ TeV}$ )

# Multipass

$$E \approx P(\text{GeV}) = 0.3 B(\text{T}) \rho \text{ (m)}$$

$$\text{decay length} = \gamma \beta c \tau_{\mu} = 6000 E \quad \tau_{\mu} = 2.2 \mu\text{s}$$

$$L_{\text{acc}} = 2\pi \rho^{3/2} (\text{dipole filling factor})$$

$$L_{\text{acc}} \text{ (m)} = 3 \pi E / [0.3 B(\text{T})] \approx 30 / B(\text{T})$$



$$\text{Lifetime (machine turns)} = \text{decay length} / L_{\text{acc}} = 200 B(\text{T})$$

$$B = 16 \text{ T}$$

$$3000 \text{ turns}$$

Luminosity and RF acceleration can benefit of this factor !



# Luminosity



$$N(p) = \sigma(p) N(e^+) \rho(e^-) L$$

$N(e^+)$  number of  $e^+$   
 $\rho(e^-)$  target electron density  
 $L$  target length

$$N(p) = \sigma(p) N(e^+) N(e^-) / A$$

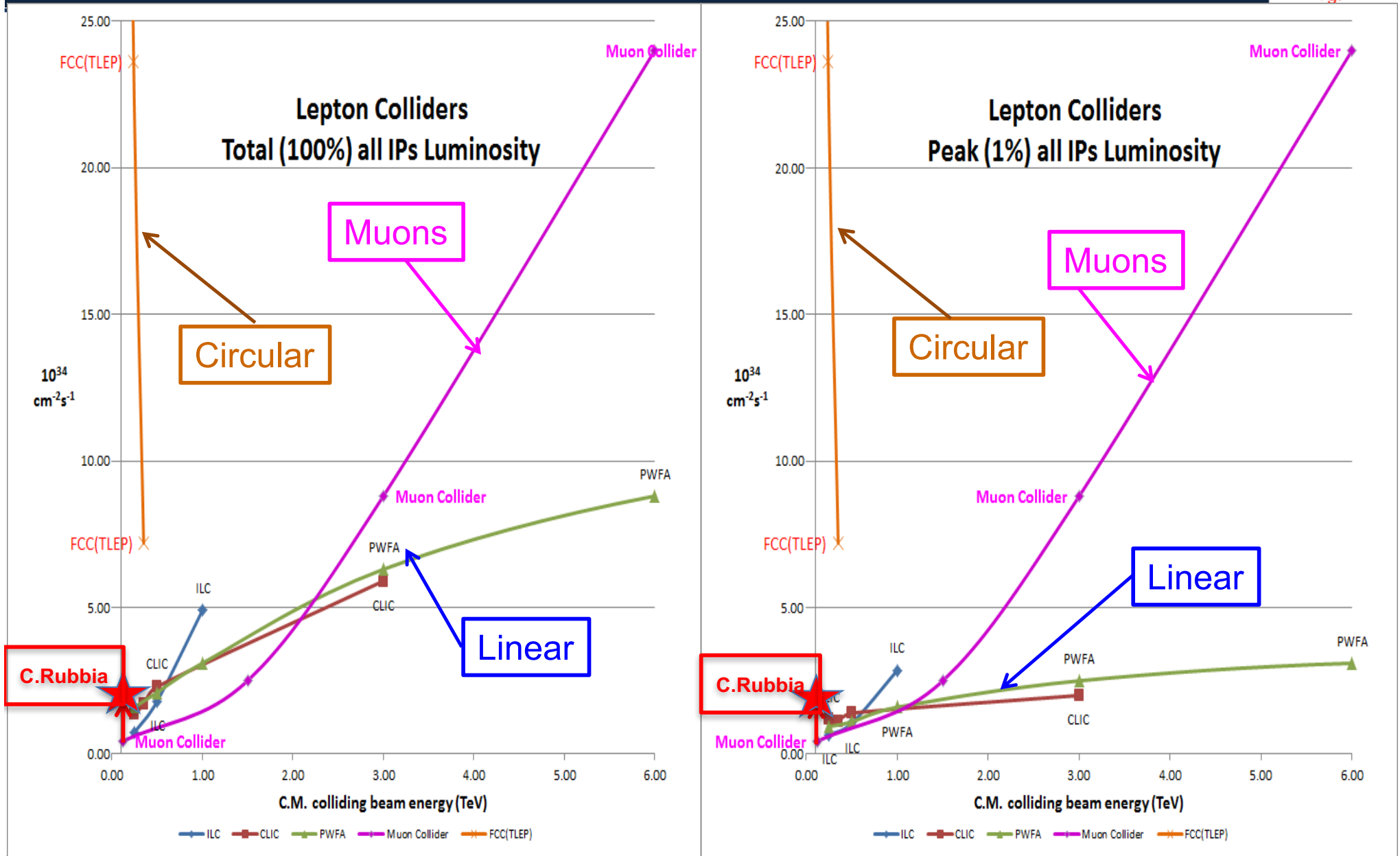
$N(e^+)$  number of  $e^+$   
 $N(e^-)$  number of  $e^-$   
 $A$  area of intersection

$$dN(p)/dt = \sigma(p) N(e^+) N(e^-) / A f$$

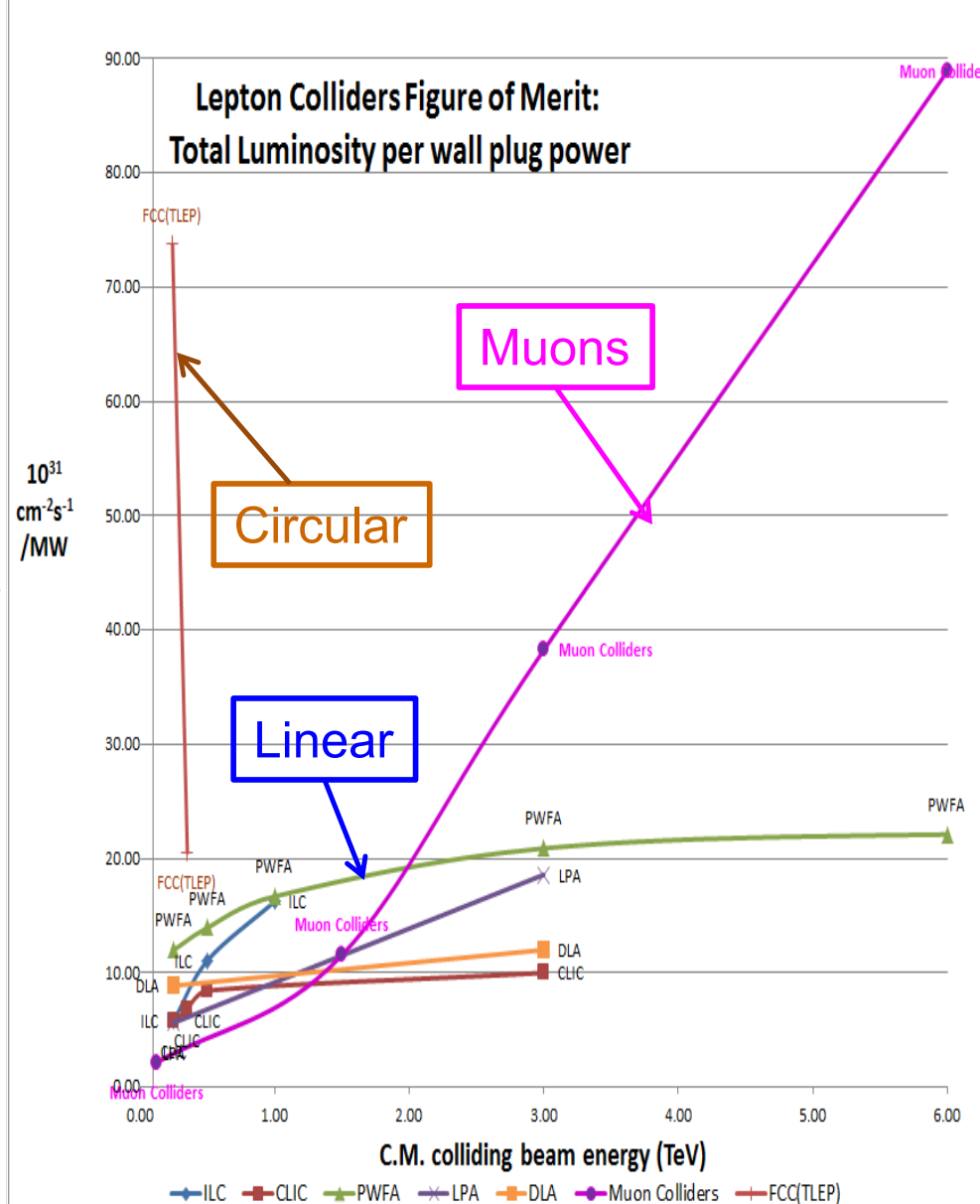
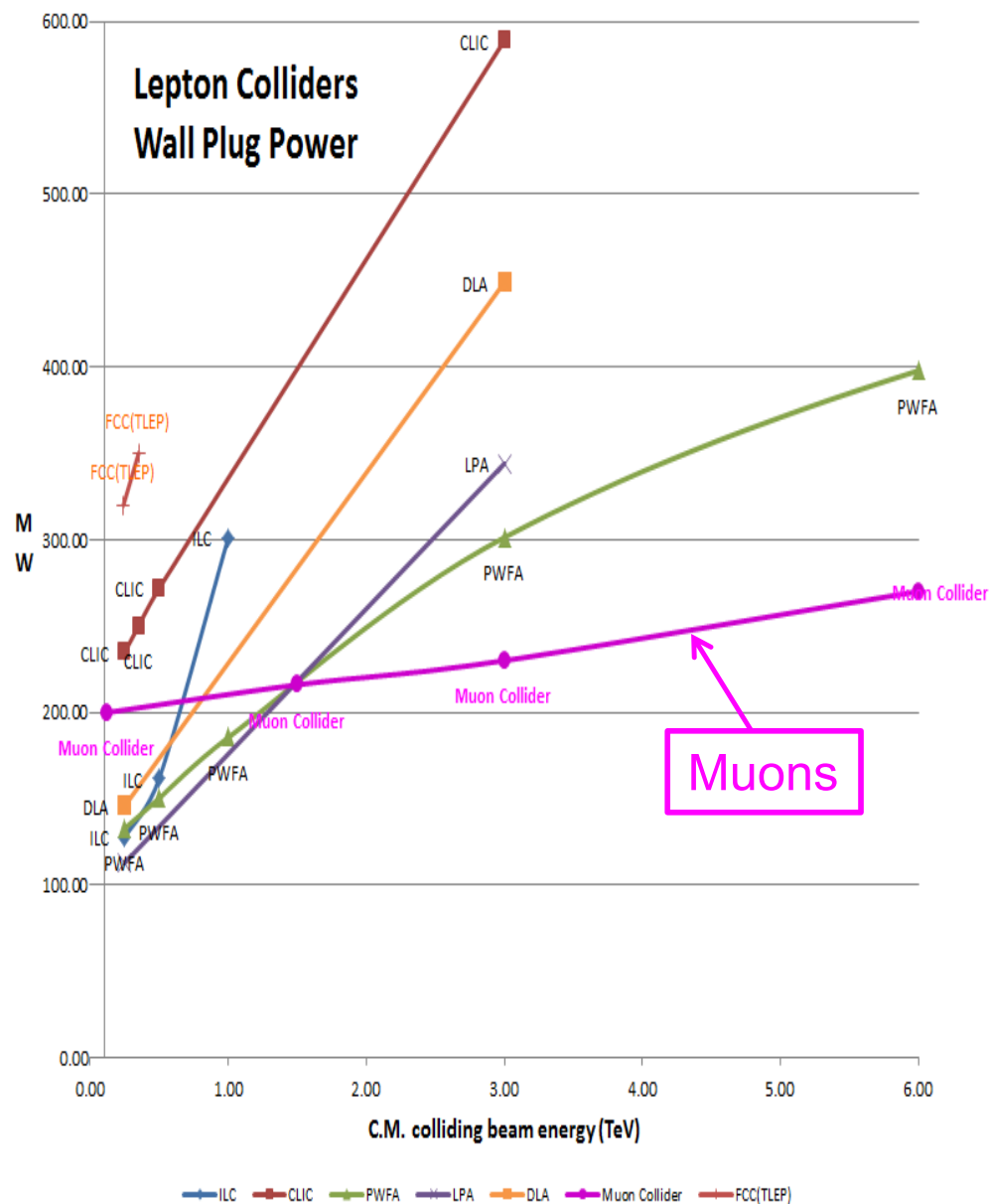
$$L = N(e^+) N(e^-) / A f$$

- $f$  intersection frequency
- injection frequency for linear colliders
  - revolution frequency for circular with stable particles

# Muon Colliders potential of extending leptons high energy frontier with high performance



# Muon Colliders extending leptons high energy frontier with potential of considerable power savings



# Muon Source

## Goals

- **Neutrino Factories:**  $O(10^{21})$   $\mu/\text{yr}$  within the acceptance of a  $\mu$  ring
- **Muon Collider:** luminosities  $>10^{34}/\text{cm}^{-2}\text{s}^{-1}$  at TeV-scale ( $\sim N_{\mu}^2$ )

## Options

Conventional: Tertiary production through **proton on target** (and then cool), baseline for Fermilab design study

$$\text{Rate} > 10^{13} \mu/\text{sec} \quad N_{\mu} = 2 \cdot 10^{12} / \text{bunch}$$

Unconventional:

- **$e^+e^-$  annihilation: positron beam on target** (very low emittance and no cooling needed), baseline for our proposal here

$$\text{Rate} \sim 10^{11} \mu/\text{sec} \quad N_{\mu} \sim 5 \times 10^7 / \text{bunch}$$

- **by Gammas: GeV-scale Compton  $\gamma$ s** not discussed here

$$\text{Rate} \sim 5 \cdot 10^{10} \mu/\text{sec} \quad N_{\mu} \sim 10^6 \quad (\text{Pulsed Linac}) \quad [\text{V. Yakimenko (SLAC)}]$$

$$\text{Rate} > 10^{13} \mu/\text{sec} \quad N_{\mu} \sim \text{few} \cdot 10^4 \quad (\text{High Current ERL})$$

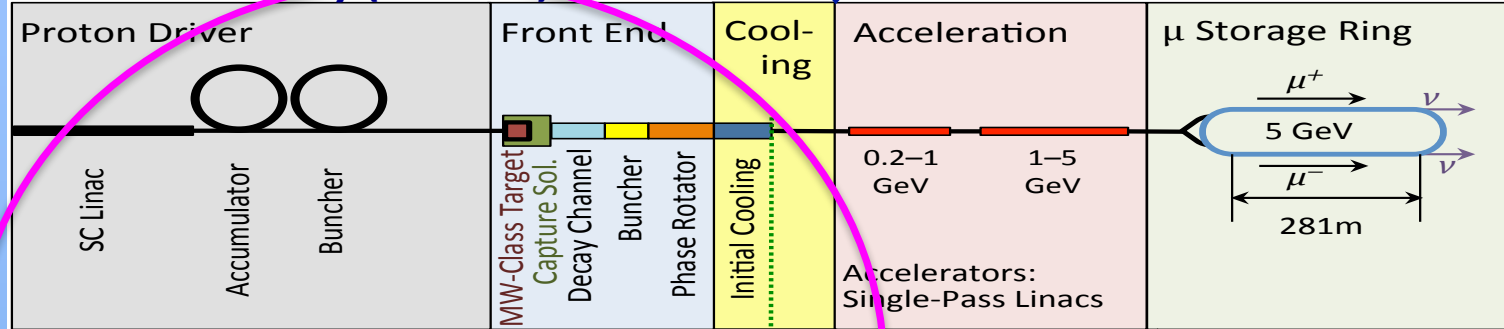
see also: W. Barletta and A. M. Sessler NIM A 350 (1994) 36-44

# Proton-Based Source

# Muon Accelerator Program (MAP)

## Muon based facilities and synergies

### Neutrino Factory (NuMAX)

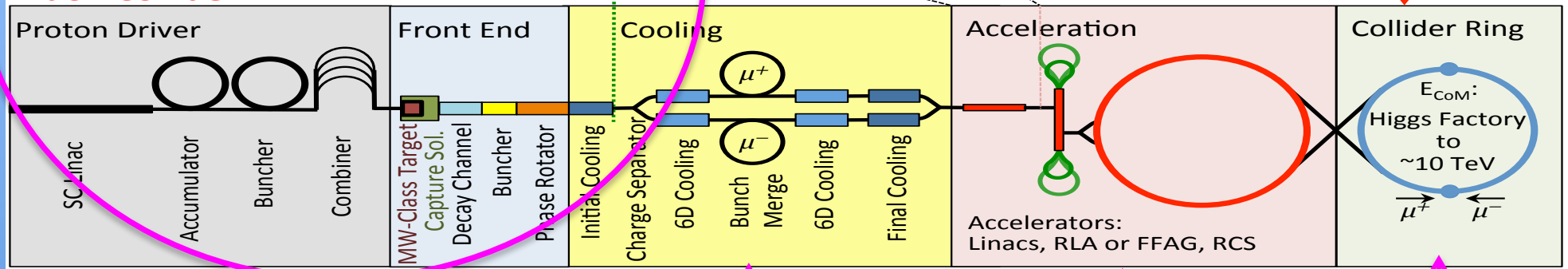


$\nu$  Factory Goal:  
 $10^{21}$   $\mu^+$  &  $\mu^-$  per year  
 within the accelerator  
 acceptance

$\mu$ -Collider Goals:  
 126 GeV  $\Rightarrow$   
 $\sim 14,000$  Higgs/yr  
 Multi-TeV  $\Rightarrow$   
 Lumi  $> 10^{34} \text{cm}^{-2}\text{s}^{-1}$

Share same complex

### Muon Collider



Key Challenges

$\sim 10^{13}-10^{14}$   $\mu$  / sec  
 Tertiary particle  
 $p \rightarrow \pi \rightarrow \mu$

Fast cooling  
 $(\tau=2\mu\text{s})$   
 by  $10^6$  (6D)

Fast acceleration  
 mitigating  $\mu$  decay

Background  
 by  $\mu$  decay

Key R&D

MW proton driver  
 MW class target  
 NCRF in magnetic field

Ionization cooling  
 High field solenoids (30T)  
 High Temp Superconductor

Cost eff. low RF SC  
 Fast pulsed magnet  
 (1kHz)

Detector/  
 machine  
 interface

# Muon beam facilities

## - Overview

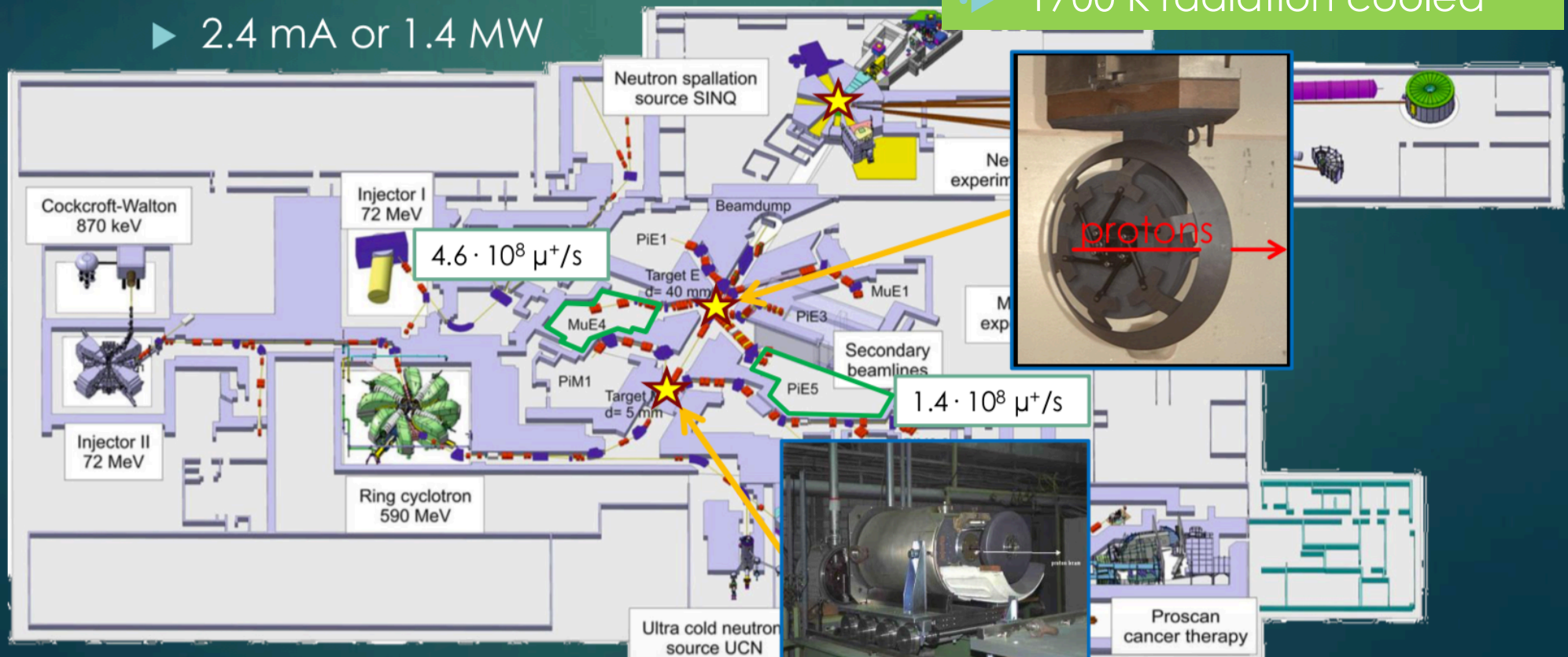
| Laboratory/Beamline          | Energy/<br>Power                   | Present Muon<br>$\mu^+/\mu^-$ Rates [Hz] | Future estimated<br>$\mu^+/\mu^-$ Rate [Hz] |
|------------------------------|------------------------------------|--|---|
| <b>PSI (CH)</b>              | 590 MeV, 1.3 MW DC                 |  |   |
| LEM                          |                                    | $4.2 \cdot 10^8 \mu^+$                   |   |
| $\pi E5$                     |                                    | $1.3 \cdot 10^8 \mu^+$                   |   |
| HiMB                         |                                    |  | $O(10^{10}) \mu^+ / O(10^8) \mu^-$          |
| <b>JPARC (JP)</b>            | 3 GeV, 1MW Pulsed<br>Reached 400kW |  | $2 \cdot 10^8 \mu^+ @ 1MW$                  |
| MUSE                         |                                    | $8 \cdot 10^7 / 4 \cdot 10^6$            | $10^7 \mu^- @ 1MW$                          |
| COMET                        | 8 GeV, 56kW Pulsed                 |  | $10^{11} \mu^-$ 2019/2020                   |
| <b>FNAL (USA)</b>            |                                    |  |   |
| Mu2e                         | 8GeV, 25kW Pulsed                  |  | $5 \cdot 10^{10} \mu^-$ 2019/2020           |
| RAON/RISP (KO)               | 600 MeV, 400kW DC)                 |  | $7 \cdot 10^8 \mu^+$                        |
| CSNS (CN)                    | 1.6 GeV, 100kW Pulsed              |  | $10^{10} \mu^+$                             |
| <b>TRIMUF (CA)</b>           | 500 MeV, 75kW, DC                  |  |   |
| M20/M9B                      |                                    | $2 \cdot 10^6 / 1.4 \cdot 10^6$          |   |
| RAL ISIS (UK)                | 800 MeV, 160kW, Pulsed             | $1.5 \cdot 10^6 / 7 \cdot 10^4$          |   |
| RIKEN RAL                    |                                    |  |   |
| <b>RCNP Osaka Univ. (JP)</b> | 400 MeV, 400W DC                   |  |   |
| MUSIC                        |                                    | $10^6 / 1 \cdot 10^5$                    | $4.2 \cdot 10^8 / 4.2 \cdot 10^7$           |

# PSI - the world's highest intensity surface $\mu^+$ beams

- ▶ Proton beam :
  - ▶ 590 MeV
  - ▶ 50 MHz / 20 ns  $\rightarrow$  CW surface muons
  - ▶ 2.4 mA or 1.4 MW

|      | Capture efficiency | Transmission | Overall efficiency |
|------|--------------------|--------------|--------------------|
| MuE4 | ~ 6 %              | ~ 7%         | ~ 0.4 %            |

- 50 kW proton beam energy deposit
- ▶ 1700 K radiation cooled

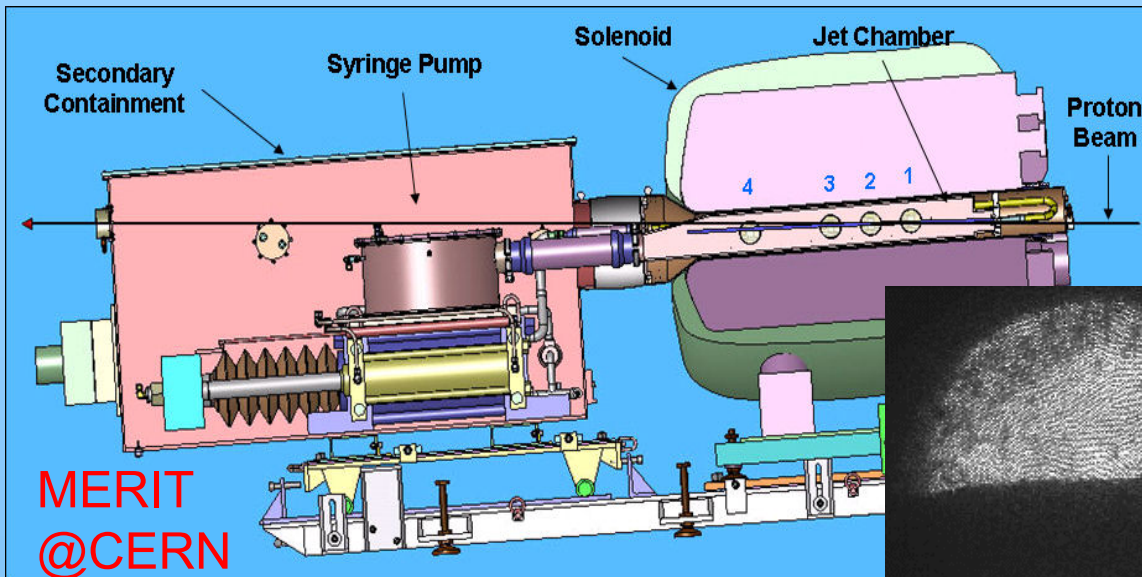




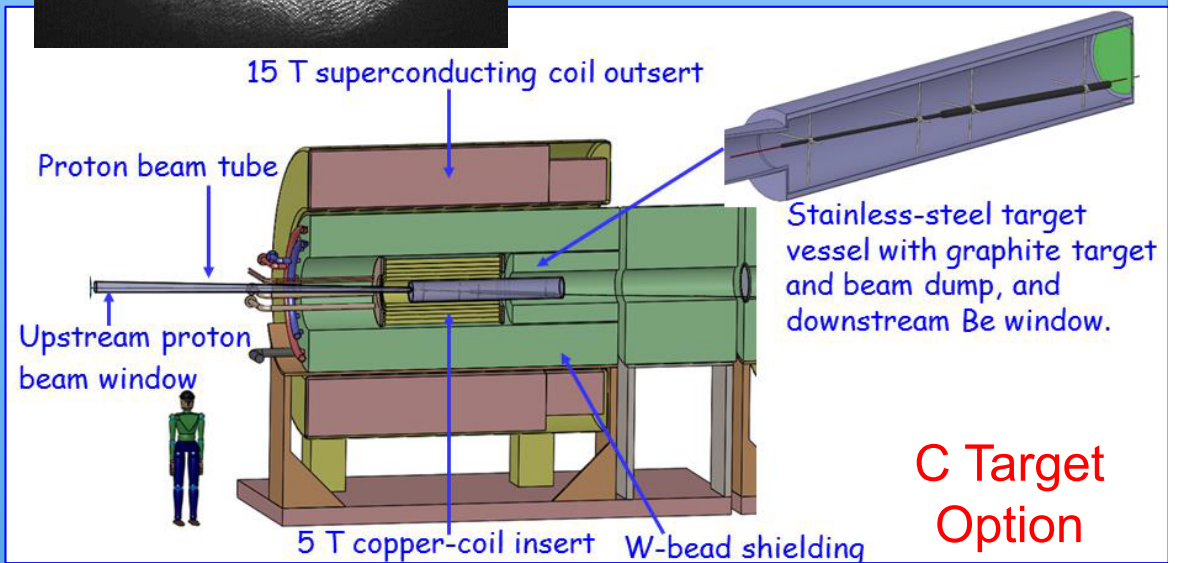
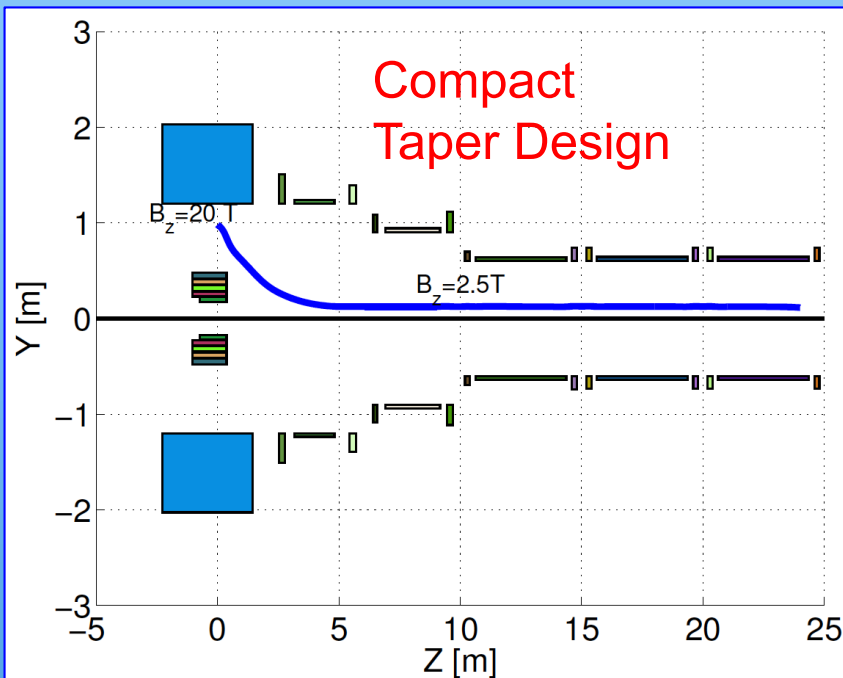
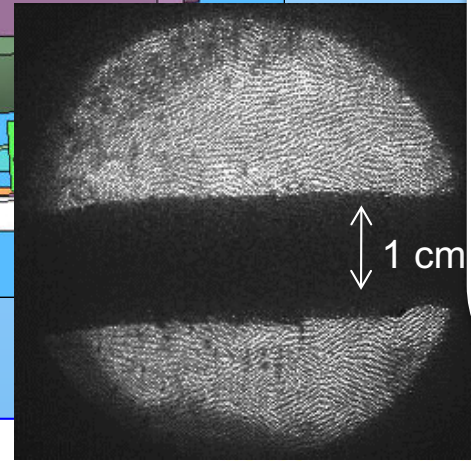
# Key Feasibility Issues

- Proton Driver
- Target
  - High Power Target Station
  - Capture Solenoid
- Front End
  - Energy Deposition
  - RF in Magnetic Fields
- Cooling
  - Magnet Needs ( $\text{Nb}_3\text{Sn}$  vs HTS)
  - Performance
- Acceleration
  - Acceptance (NF)
- Collider Ring
  - >400 Hz AC Magnets (MC)
- Collider MDI
  - IR Magnet Strengths/Apertures
  - SC Magnet Heat Loads ( $\mu$  decay)
- Collider Detector
  - Backgrounds ( $\mu$  decay)

# High Power Target



- ✓ MERIT Expt:
  - LHg Jet in 15T
  - Capability: 8MW @70Hz
- ✓ MAP Staging aims at 1-2 MW  $\Rightarrow$  C Target
- ✓ Improved Compact Taper Design
  - Performance & Cost



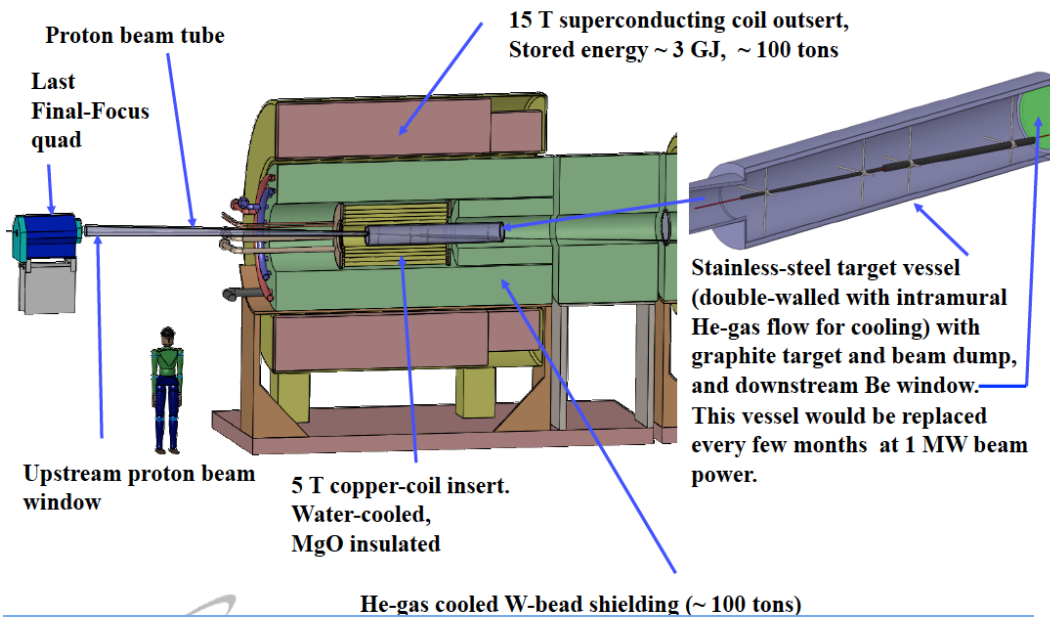
**C Target Option**

# MAP muon generation by Proton driver

H.Kirk  
(BNL)

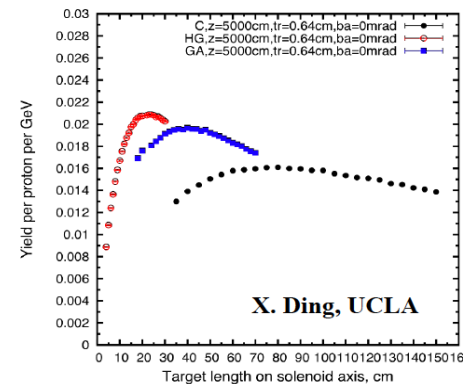


## A Graphite Target Core



- MW-Class proton driver at ~5-10 GeV
- Capture solenoid system ( $\mu^+$  &  $\mu^-$ )
  - 15 T outsert, 5 T insert
  - ~3GJ stored energy

## Choice of Target Materials II



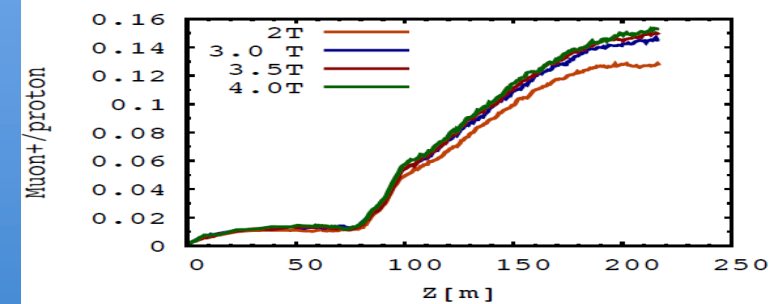
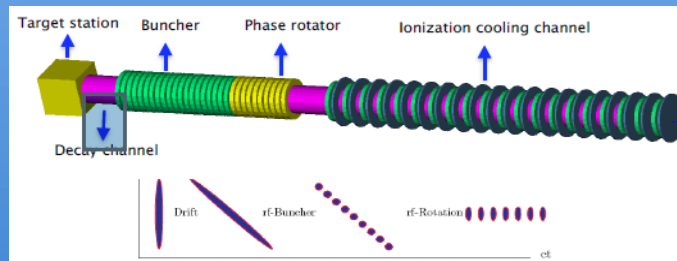
- High Z (e.g. Hg)
- Mid Z (e.g. Ga)
- Low Z (e.g. Carbon)

A **25%** advantage of using high-Z Hg compared to low-Z Carbon  
Low-z Carbon is attractive due to its simplicity and robustness

**Proton Beam: KE = 6.75 GeV**  
**Normalization: For Hg  $\Sigma(\mu^+ + \mu^-)/\text{proton} \approx 1$**

- Initial operation with 1MW carbon target
- Upgrade to multi-MW with Liquid Metal Jet Technology (demonstrated in MERIT Experim.)

H.K.Sayed  
(BNL)



Muon per proton production at Front End exit

# Ionization Cooling

- No damping from SR -> Ionization 'dE/dx' cooling:
  - Helical 6D Cooling
  - PIC
  - ...



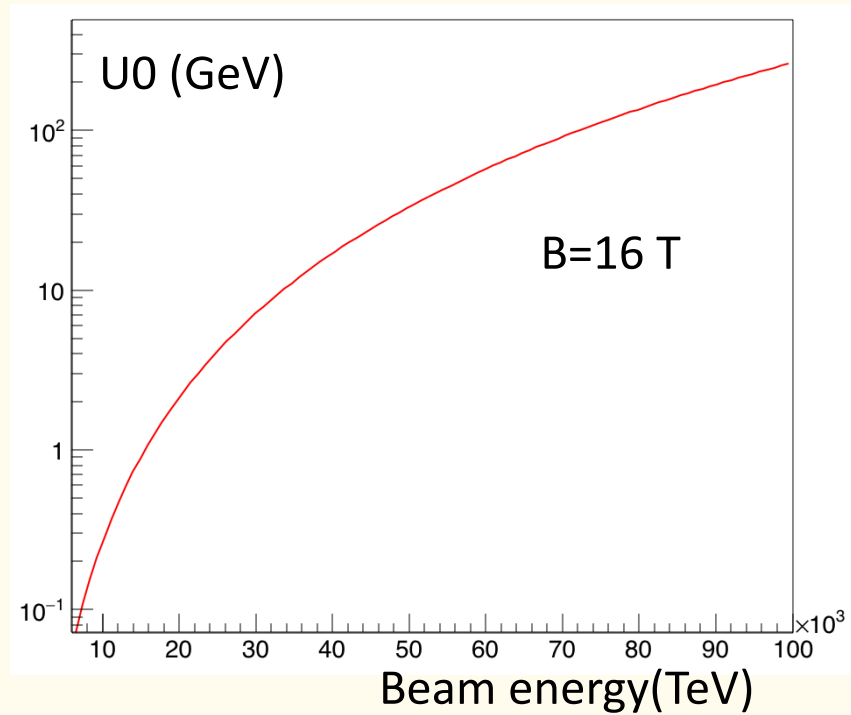
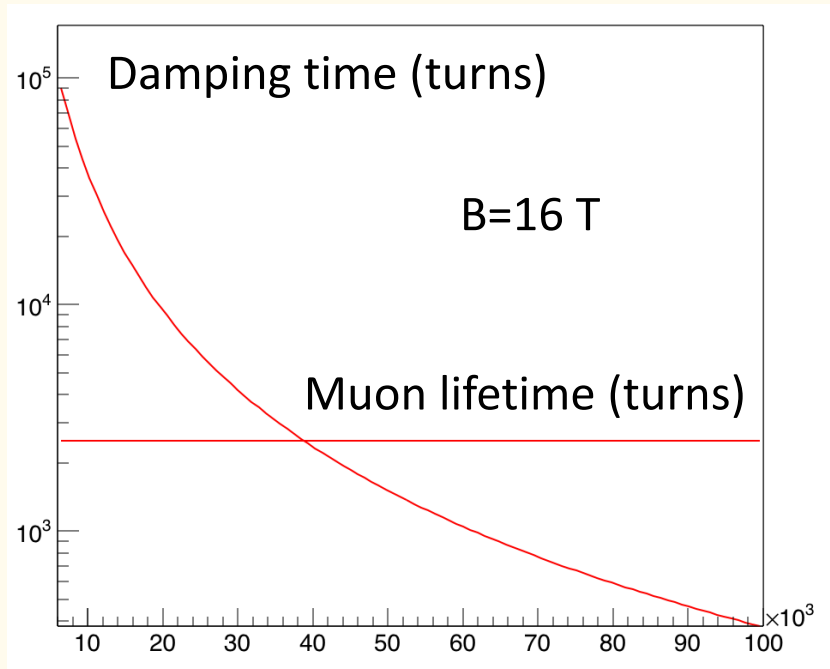
## Ionization Cooling Experimental R&D Program

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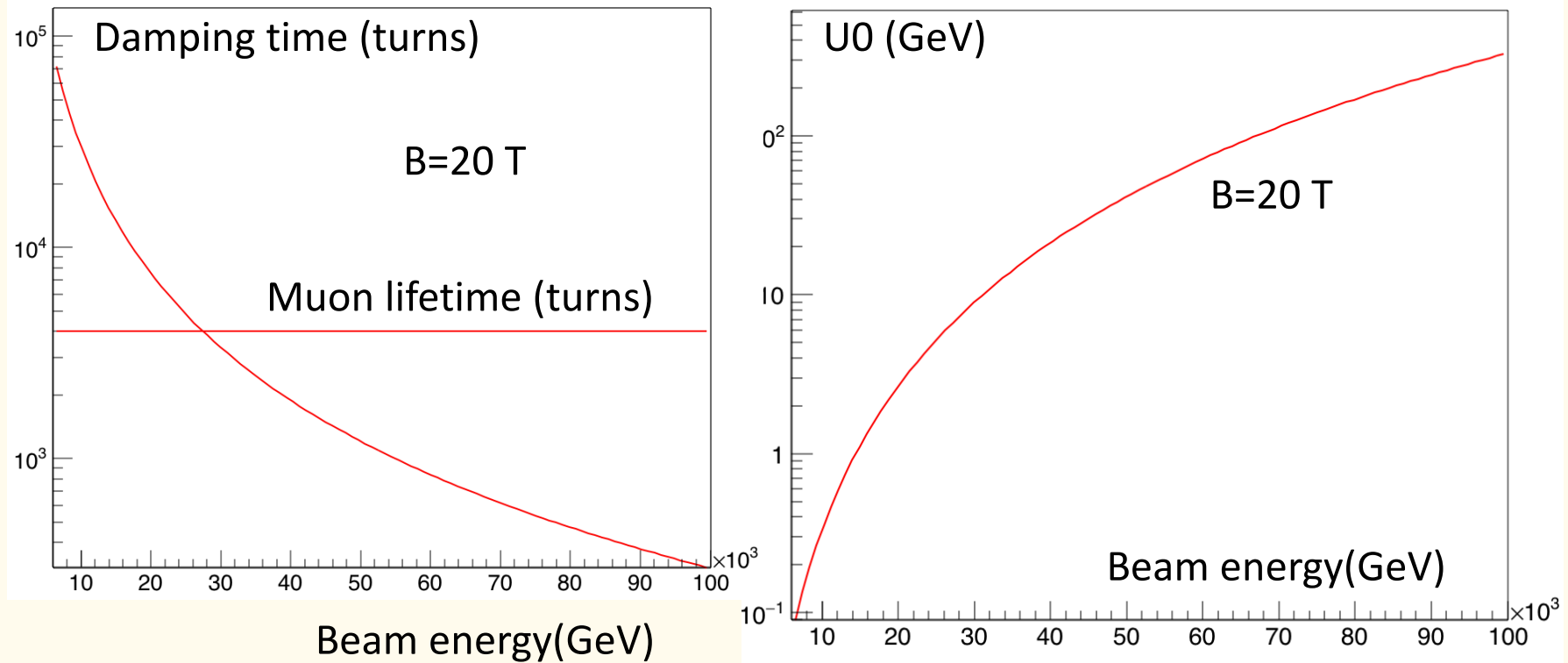
- **MICE** –International Muon Ionization Cooling Experiment
  - $\mu$ -beam at RAL ISIS
  - Systems test of complete cooling system
- **MuCOOL** Program
  - Rf, absorber, magnet R&D-supports MICE
  - MuCOOL test area (Fermilab)
  - Muon Collider Task Force
- **MUONS, Inc.** (R. Johnson, et al.)
  - High-pressure rf cavities
  - Helical cooler, Parametric resonance cooler

D. Neuffer

# SR and damping in $\mu$ collider

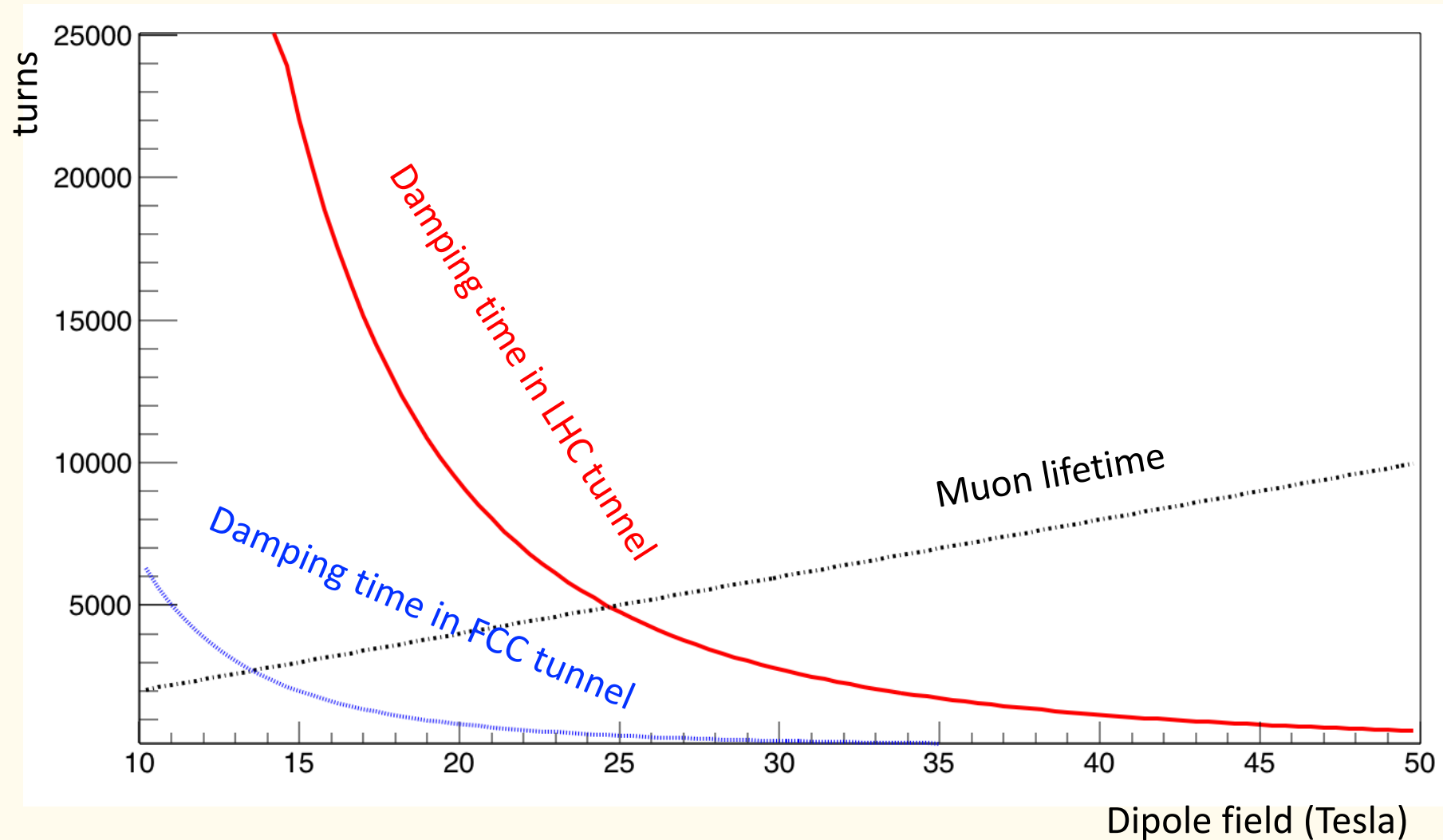


# SR and damping in $\mu$ collider



$$U_0 = 5.5 \times 10^{-18} \gamma^4 / \rho$$

# Damping time & muon lifetime

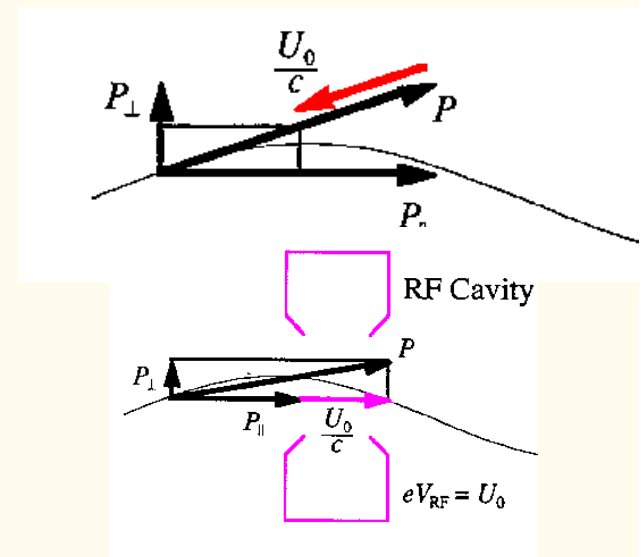
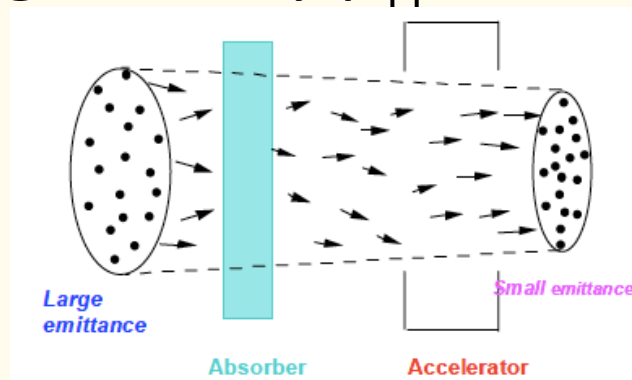


# Ionization Cooling-general principle

This method, called “**dE/dx cooling**” closely resembles to the synchrotron compression of relativistic electrons - with the multiple energy losses in a thin, low Z absorber substituting the synchrotron radiated light.

## Transverse Cooling:

- Particle loses momentum in material
- Particle gains only  $p_{||}$  in RF



On the other hand,  
Multiple scattering in material increases rms emittance





# Combining Cooling and Heating:

$$\frac{d\varepsilon_N}{ds} = -\frac{1}{\beta^2 E} \frac{dE}{ds} \varepsilon_N + \frac{\beta\gamma}{2} \beta_{\perp} \frac{d\langle \theta_{rms}^2 \rangle}{ds}$$

- **Low-Z** absorbers ( $H_2$ , Li, Be, ...) to reduce multiple scattering

- **High Gradient RF**

- To cool before  $\mu$ -decay ( $2.2\gamma \mu s$ )

- To keep beam bunched

- **Strong-Focusing** at absorbers  $\rightarrow$  **small beam size and large divergence then damped by absorber + RF**

- To keep multiple scattering

- less than beam divergence ...

$$\frac{d\langle \theta_{rms}^2 \rangle}{ds} = \frac{z^2 E_s^2}{\beta^2 c^2 p_{\mu}^2 L_R}$$

$\Rightarrow$  **Quad** focusing ?

$\Rightarrow$  **Li lens** focusing ?

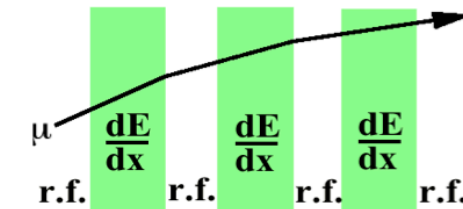
$\Rightarrow$  **Solenoid** focusing?

# Cooling Methods

- The particular challenge of muon cooling is its short lifetime
  - Cooling must take place very quickly
  - More quickly than any of the cooling methods presently in use
- ⇒ Utilize energy loss in materials with RF re-acceleration

Muon Ionization Cooling

## • Muons cool via $dE/dx$ in low-Z medium



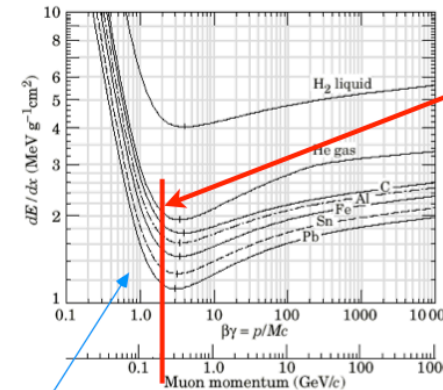
– Absorbers:

$$\begin{cases} E \rightarrow E - \langle \frac{dE}{dx} \rangle \Delta s \\ \theta \rightarrow \theta + \theta_{space}^{rms} \end{cases}$$

– RF cavities between absorbers replace  $\Delta E$

– Net effect: reduction in  $p_{\perp}$  at constant  $p_{\parallel}$ , i.e., transverse cooling

$$\frac{d\epsilon_N}{ds} \approx -\frac{1}{\beta^2} \left\langle \frac{dE_{\mu}}{ds} \right\rangle \frac{\epsilon_N}{E_{\mu}} + \frac{\beta_{\perp} (0.014 \text{ GeV})^2}{2\beta^3 E_{\mu} m_{\mu} X_0} \quad (\text{emittance change per unit length})$$



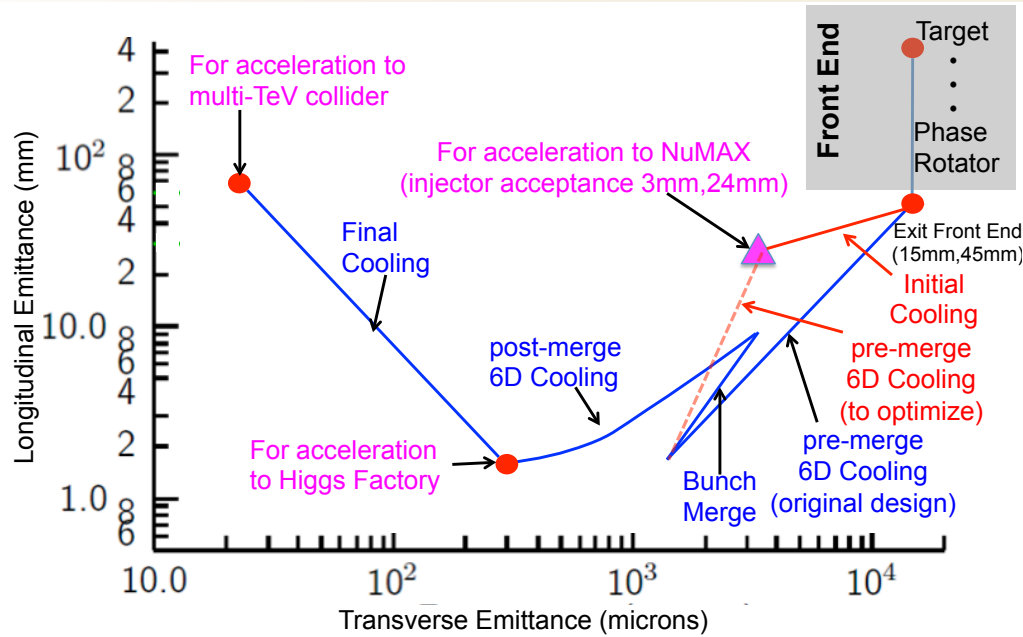
• ionization minimum is  $\approx$  optimal working point:  
 ▶ longitudinal +ive feedback at lower  $p$   
 ▶ straggling & expense of reacceleration at higher  $p$

• 2 competing effects  $\Rightarrow$   
 $\exists$  equilibrium emittance

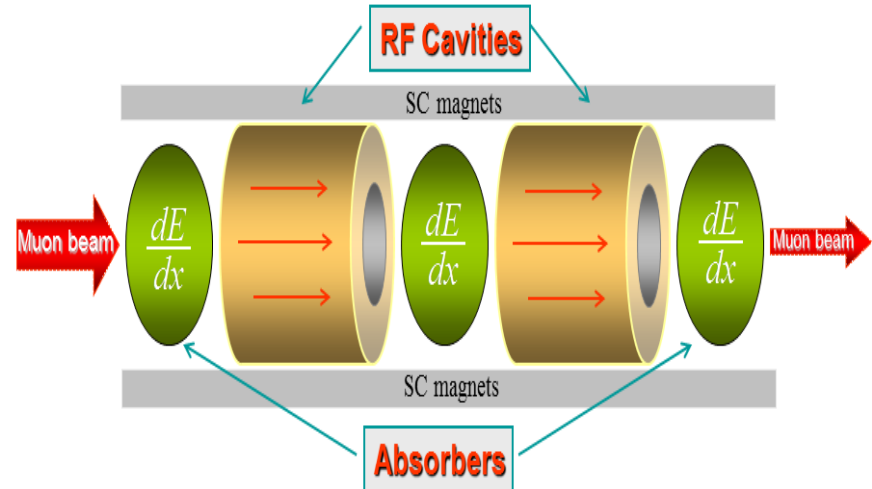
Kaplan

# MAP Cooling scheme overview

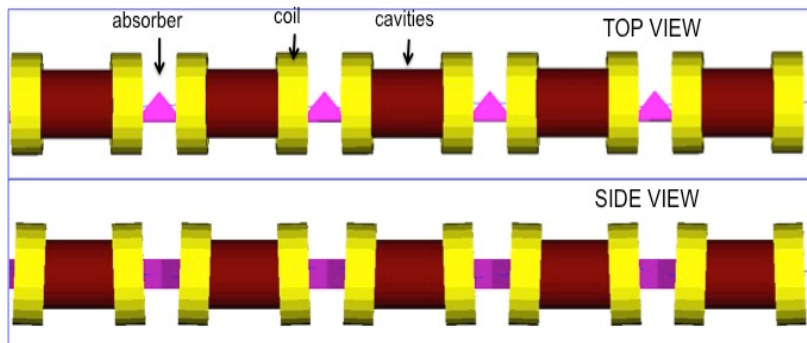
P.Snopok  
(IIT)



## Ionization cooling



## Vacuum Cooling Channel (VCC)

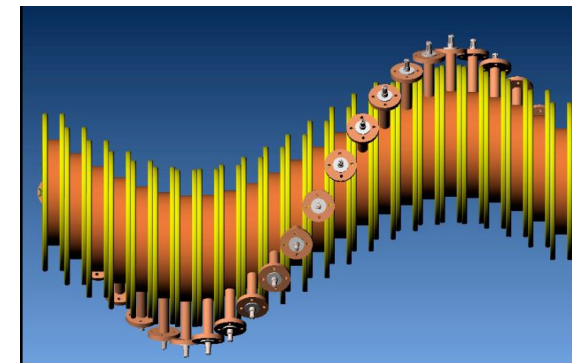


Two  
methods

Major  
challenges

Accelerating field limitation  
by magnetic field (10 T)

## Helical Cooling Channel (HCC)

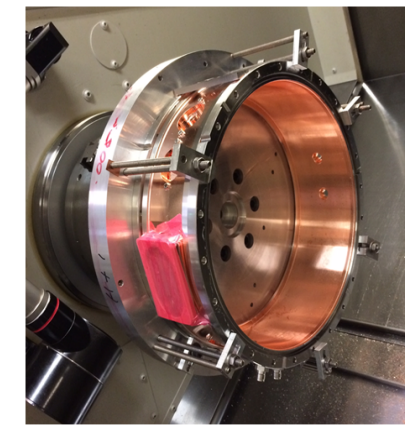
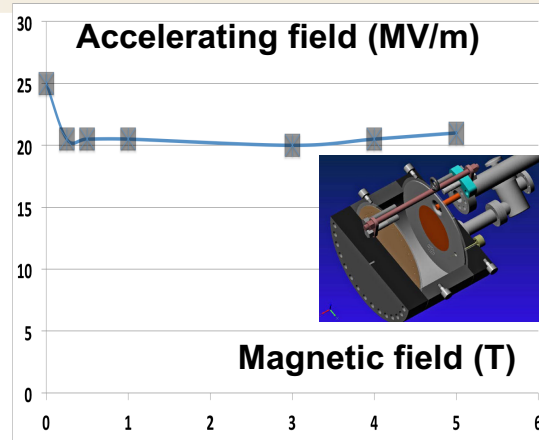
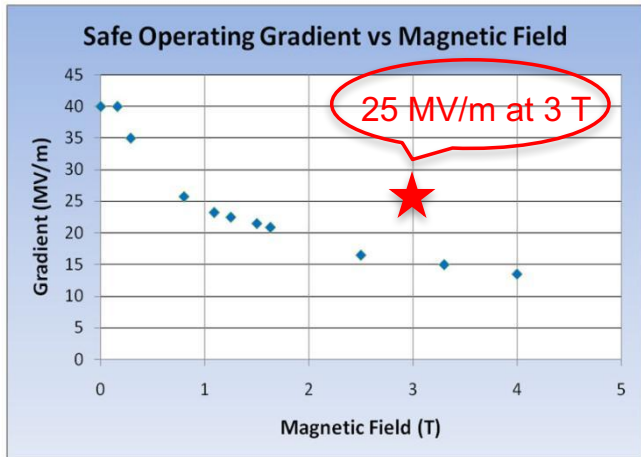


High pressure (160atm)  
Gas (GH2) filled RF cavities

# RF cavities in strong magnetic field

D.Li  
(LBNL)

## RF cavity in vacuum:

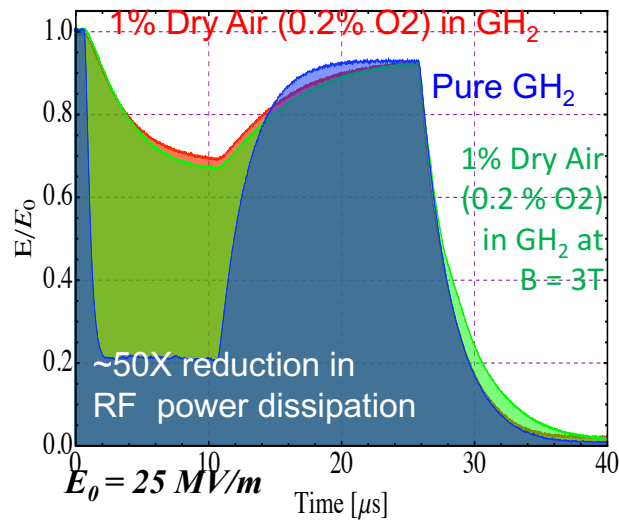


New cavity design very encouraging !

New cavity by LBNL/SLAC for tests in FNAL/MTA

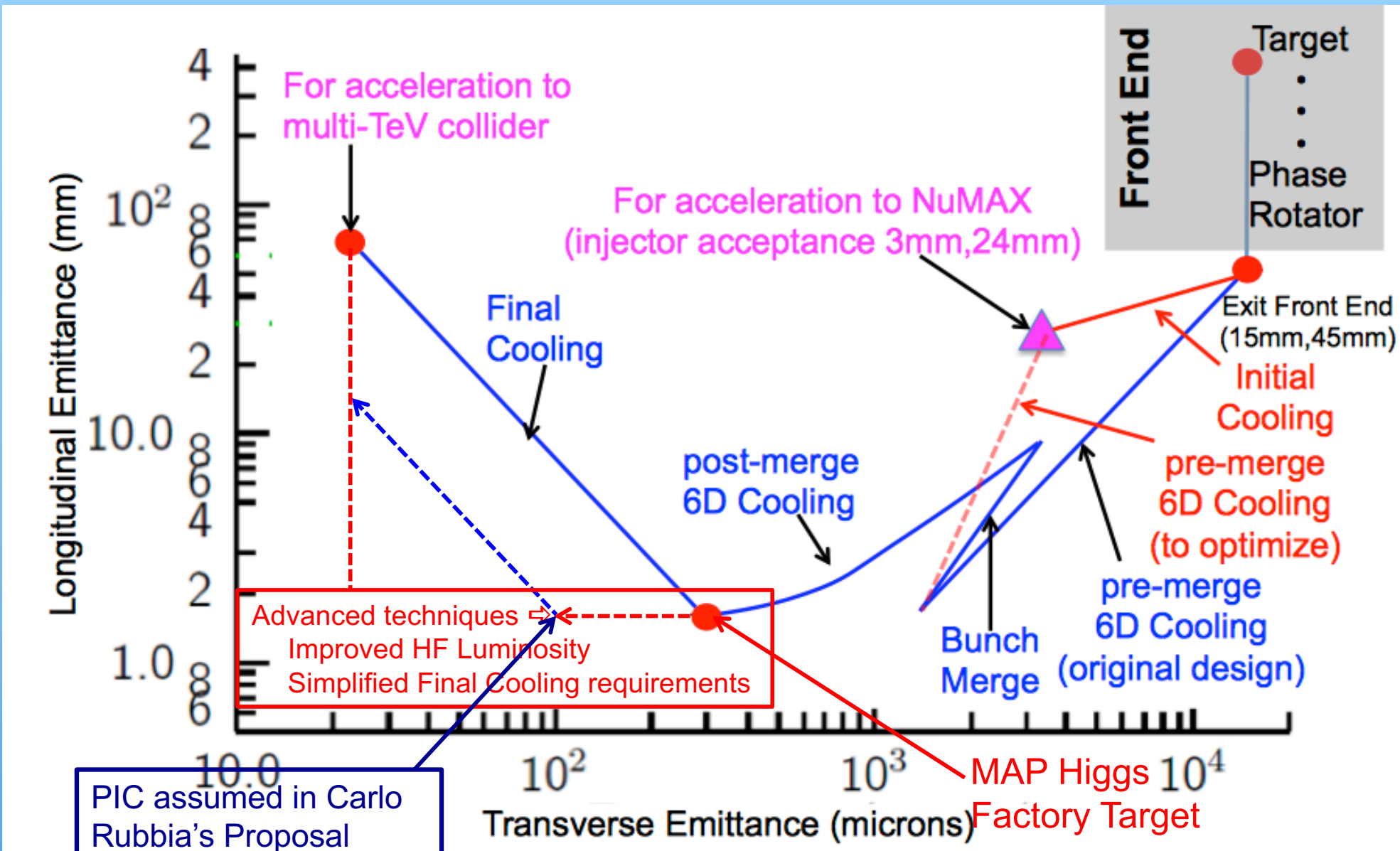
Breakdown by field emission

## RF cavity filled with gas



No accelerating field degradation up to 3 T  
Operation with beam under heavy beam loading

# Muon Ionization Cooling

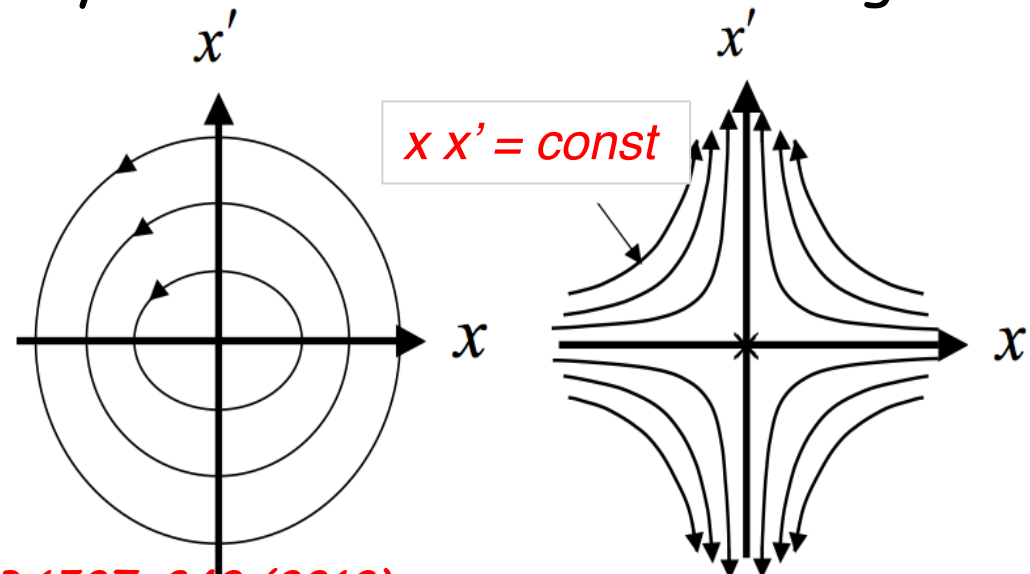


# 3.-PIC, the Parametric Resonance Cooling of muons

C. Rubbia

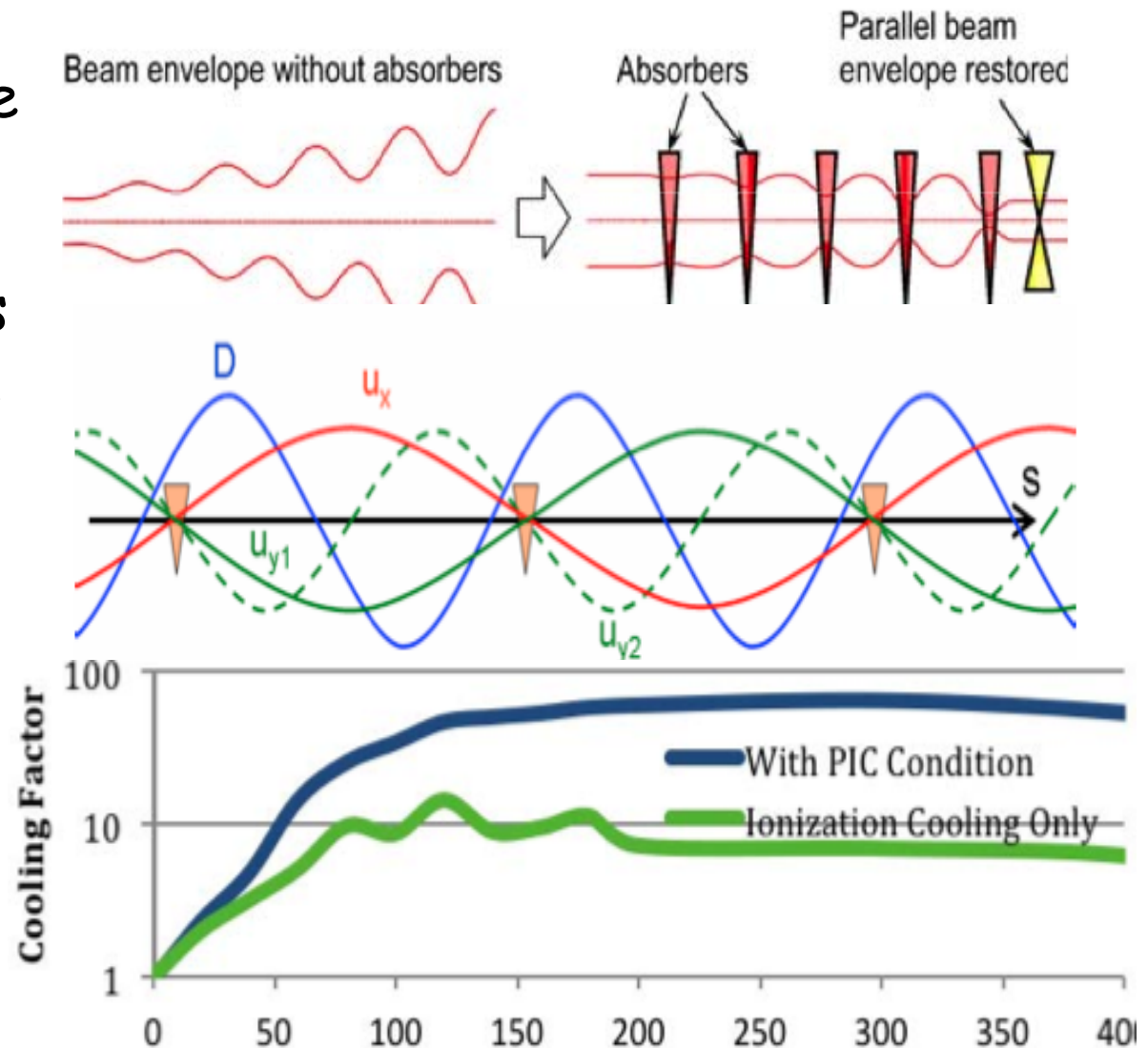
- Combining ionization cooling with parametric resonances is expected to lead to muon with much smaller transv. sizes.
- A linear magnetic transport channel has been designed by Ya.S. Derbenev et al where a **half integer resonance** is induced such that the normal elliptical motion of particles in  $x$ - $x'$  phase space becomes **hyperbolic**, with particles moving to smaller  $x$  and larger  $x'$  at the channel focal points.
- Thin absorbers placed at the focal points of the channel then cool the angular divergence by the usual ionization cooling.

*LEFT ordinary oscillations  
RIGHT hyperbolic motion  
induced by perturbations  
near an (one half integer)  
resonance of the betatron  
frequency.*



*V. S. Morozov et al, AIP 1507, 843 (2012);*

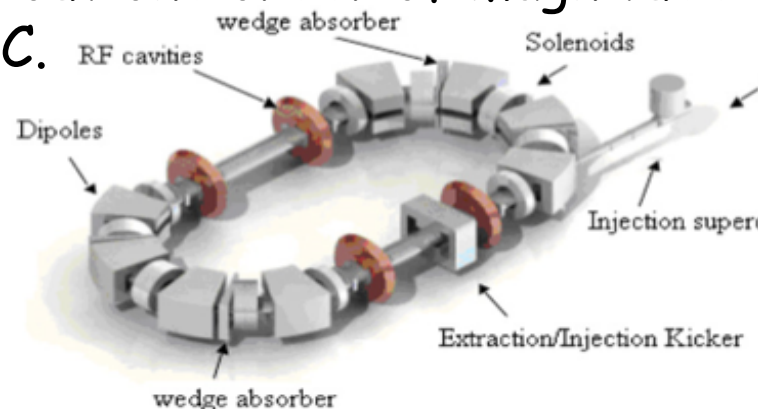
- Without damping, the beam dynamics is not stable because the beam envelope grows with every period. Energy absorbers at the focal points stabilizes the beam through the ionization cooling.
- The longitudinal emittance is maintained constant tapering the absorbers and placing them at points of appropriate dispersion, vertical  $\beta$  and two horizontal  $\beta$ .
- Comparison of cooling factors (ratio of initial to final 6D emittance) with and without the PIC condition vs number of cells: more than 10x gain



# Parametric Resonance Cooling

- The first muon cooling ring should present no unexpected behaviour and good agreement between calculations and experiment is expected both transversely and longitudinally
- The novel Parametric Resonance Cooling (PIC) involves instead the balance between a strong resonance growth and ionization cooling and it may involve significant and unexpected conditions which are hard to predict.
- Therefore the experimental demonstration of the cooling must be concentrated on such a resonant behaviour.
- On the other hand the success of the novel Parametric Resonance Cooling is a necessary premise for a viable luminosity of the initial proton parameters of the future CERN accelerators since the expected Higgs luminosity is proportional to the inverse of the transverse emittance, hence about one order of magnitude of increment is expected from PIC.

Carlo Rubbia – FNAL May 2015





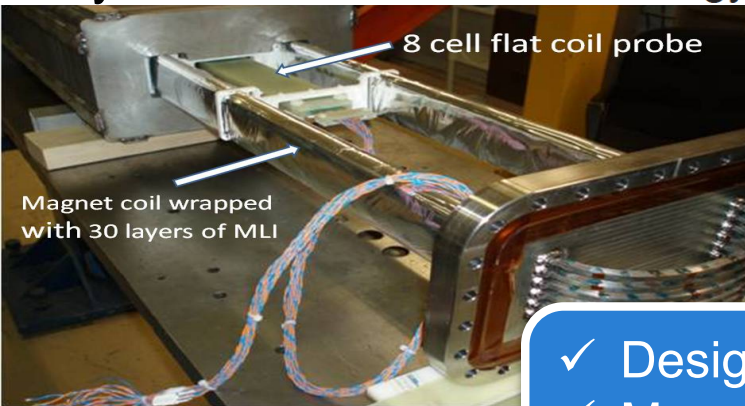
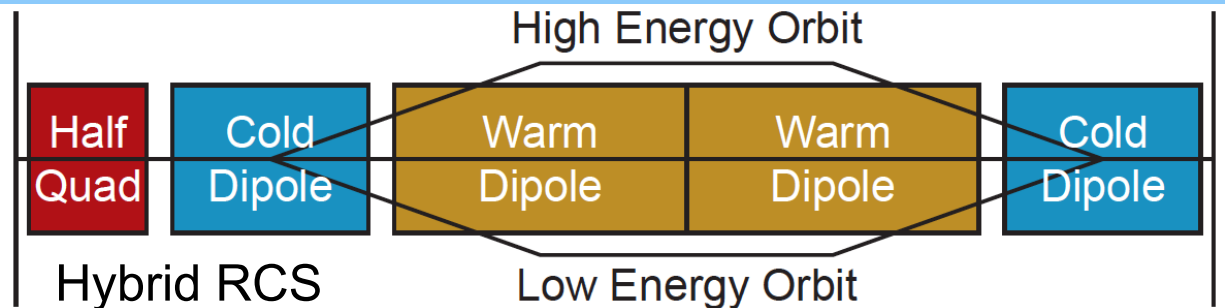
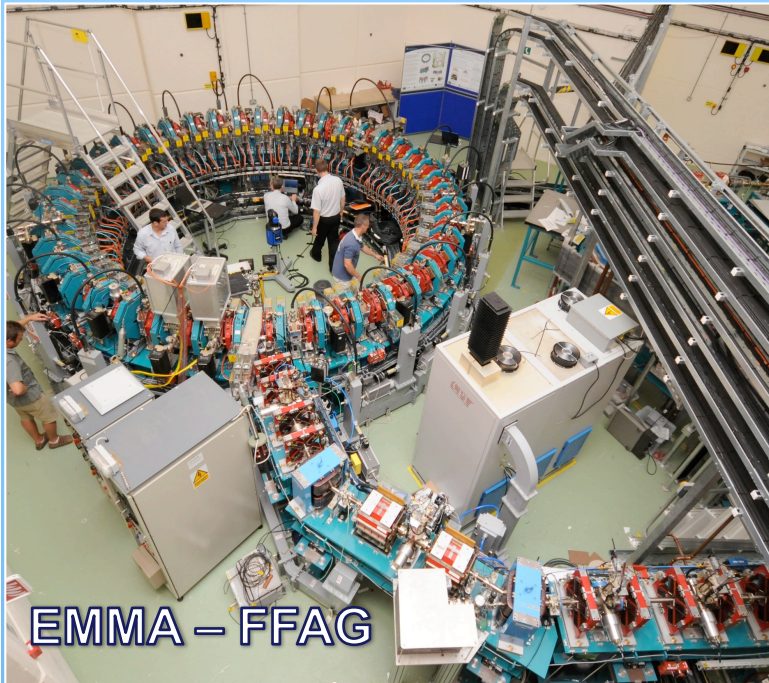
# Acceleration Requirements

- Key Issues:
  - Muon lifetime  $\Rightarrow$  ultrafast acceleration chain
  - NF with modest cooling  $\Rightarrow$  accelerator acceptance
  - Total charge  $\Rightarrow$  cavity beam-loading (stored energy)
  - TeV-scale acceleration focuses on hybrid Rapid Cycling Synchrotron  $\Rightarrow$  requires rapid cycling magnets
    - $B_{\text{peak}} \sim 2\text{T}$      $f > 400\text{Hz}$

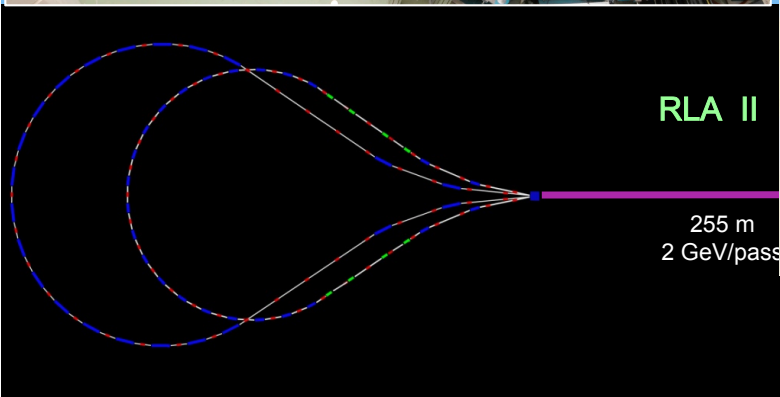
# Acceleration

Technologies include:

- Superconducting Linacs (NuMAX choice)
- Recirculating Linear Accelerators (RLAs)
- Fixed-Field Alternating-Gradient (FFAG) Rings
- (Hybrid) Rapid Cycling Synchrotrons (RCS) for TeV energies



RCS requires  
2 T p-p magnets  
at  $f > 400$  Hz  
(U Miss & FNAL)



- ✓ Design concepts in hand
- ✓ Magnet R&D indicates parameters achievable

# CMC

**CERN**

**Muon**

**Collider**

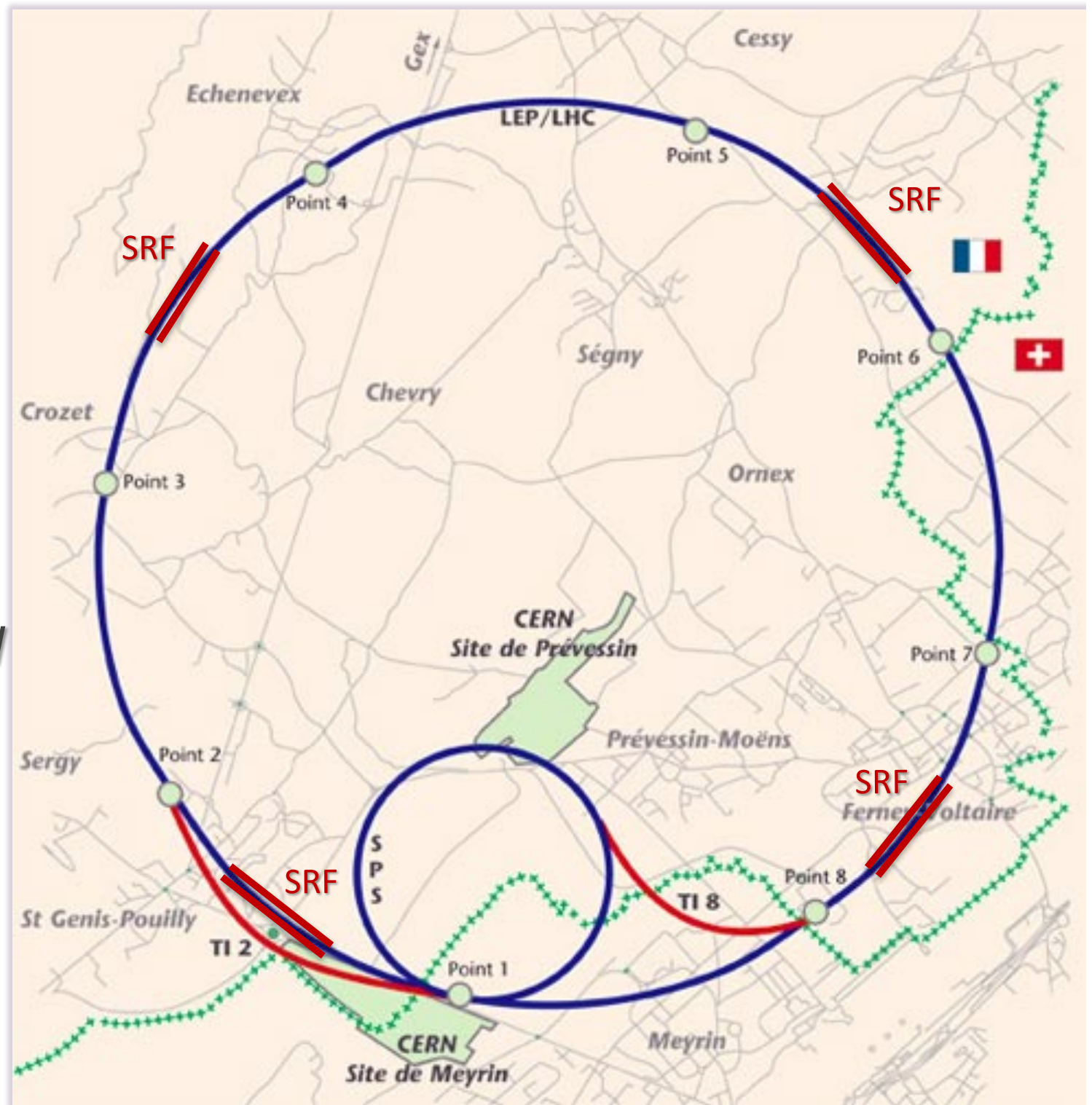
**14 TeV cme**

LHC tunnel  
SPS tunnel and  
mb PS

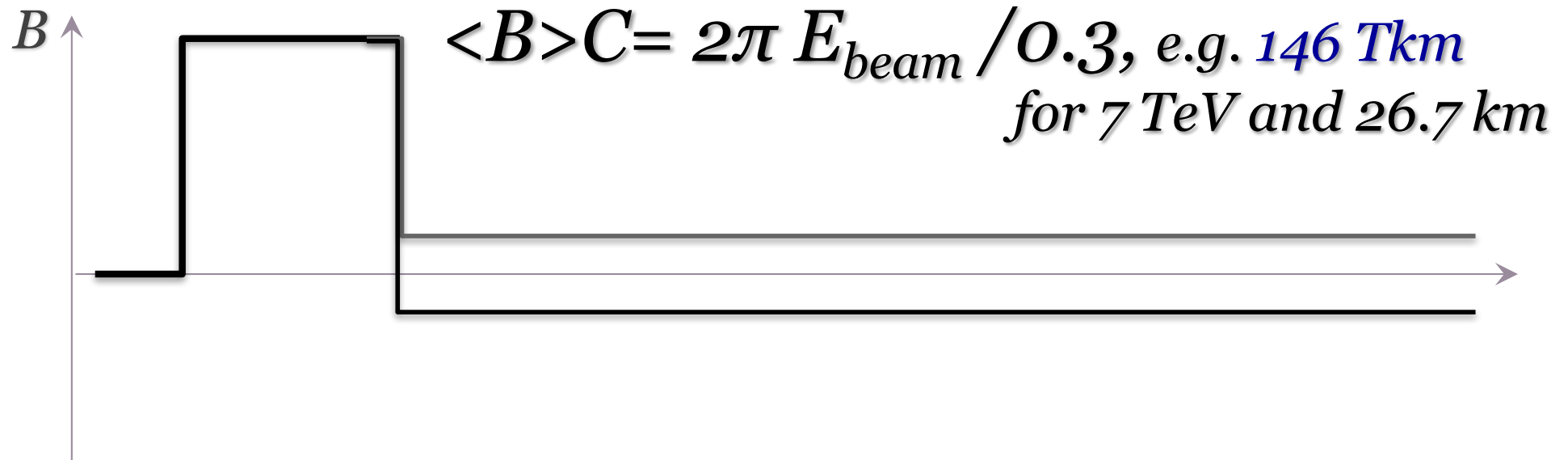
**~7GeV SRF**

**Cost ~LHC**

V.Shiltsev



# Assume RCS Acceleration



# (Simple math)



$$R = \frac{E_{max}}{E_{min}} = \frac{B_{max}L_{SC} + B_{min}L_{pulsed}}{B_{max}L_{SC} - B_{min}L_{pulsed}}$$

- If the ratio of fields :  $f = \frac{B_{max}}{B_{min}}$  then :  $\frac{L_{pulsed}}{L_{SC}} = f \frac{R - 1}{R + 1}$

- and equation for the required fields reads :

$$\frac{2\pi}{0.3} E_{max} = \langle B \rangle C = B_{max} \Pi C \frac{2R}{R(1 + f) + 1 - f}$$

# Example: 7 TeV, 26.7 km tunnel, 16T max



$$\frac{2\pi}{0.3} E_{max} = \langle B \rangle C = B_{max} \Pi C \frac{2R}{R(1+f) + 1 - f}$$

146 T × km
26.7km
16T
0.85
0.4=1/2.5

then :

| $f = \frac{B_{max}}{B_{min}}$ | $R = \frac{f - 1}{f - 4}$ | $B_{min}$ | $E_{inj}$ |
|-------------------------------|---------------------------|-----------|-----------|
| 4.2                           | 16                        | 3.8T      | 0.45TeV   |
| 4.5                           | 7                         | 3.5T      | 1TeV      |
| 5                             | 4                         | 3.2T      | 4TeV      |
| 8                             | 1.75                      | 2.0T      | 9.1TeV    |

# Example 2: 1 TeV, 6.9km tunnel, 16T max



$$\frac{2\pi}{0.3} E_{max} = \langle B \rangle C = B_{max} \Pi C \frac{2R}{R(1+f) + 1 - f}$$

20.9 T × km
6.9km
16T
0.9
0.21=1/5

then :

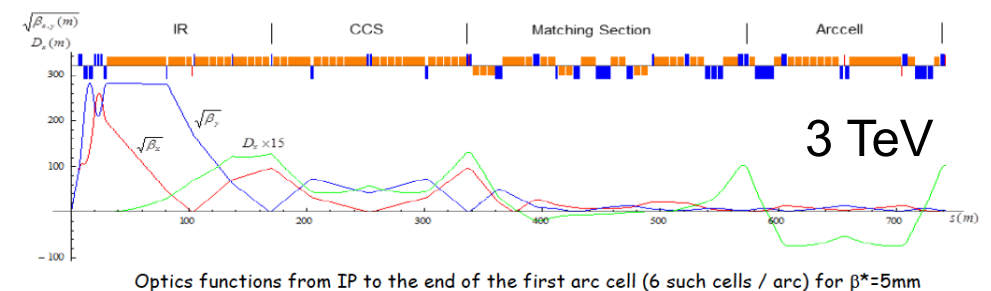
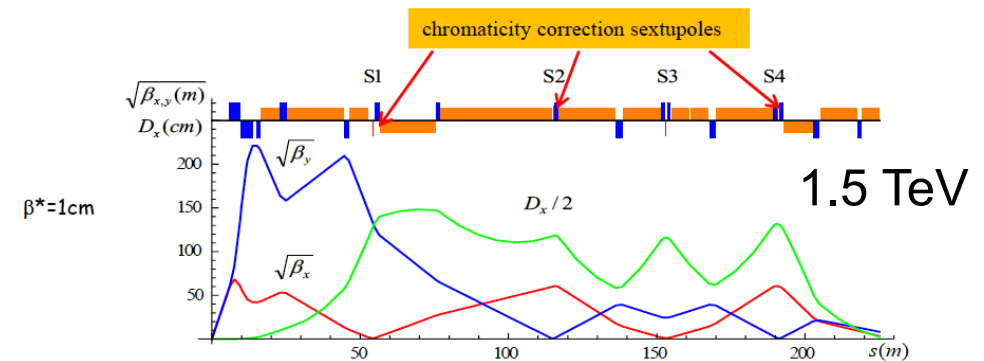
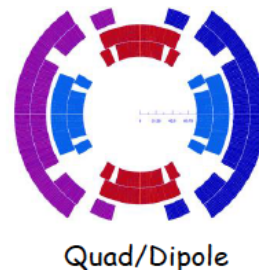
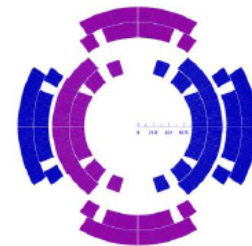
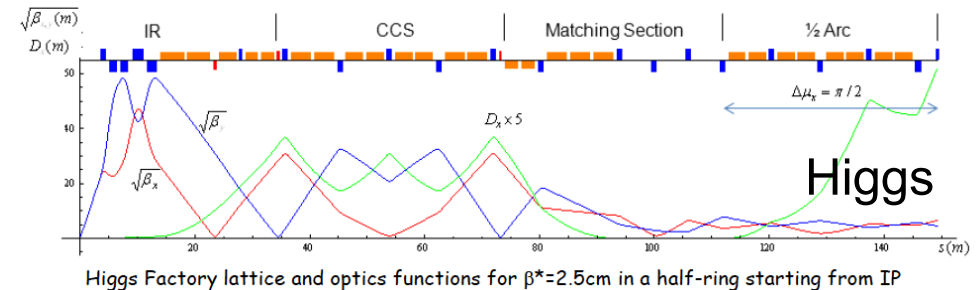
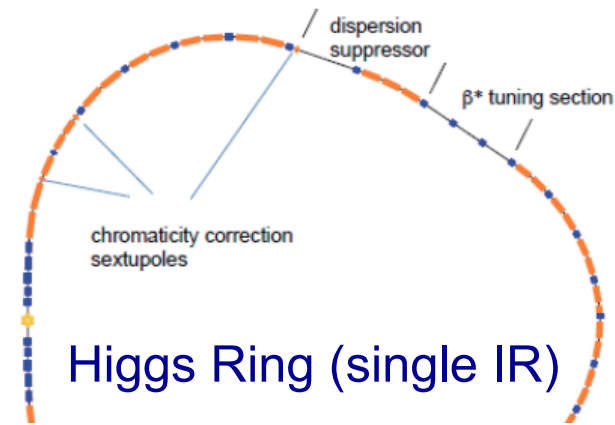
| $f = \frac{B_{max}}{B_{min}}$ | $R = \frac{f - 1}{f - 9}$ | $B_{min}$ | $E_{inj}$ |
|-------------------------------|---------------------------|-----------|-----------|
| 10                            | 9                         | 1.6T      | 110 GeV   |
| 9.5                           | 17                        | 1.7T      | 60 GeV    |

# Collider Rings

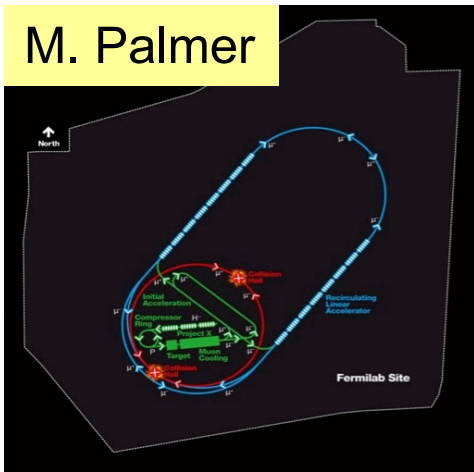
- Detailed optics studies for Higgs, 1.5 TeV, 3 TeV and now 6 TeV CoM
  - With supporting magnet designs and background studies

- ✓ Higgs, 1.5 TeV CoM and 3 TeV CoM Designs
  - With magnet concepts
  - Achieve target parameters
- ✓ Preliminary 6 TeV CoM design
  - Key issue is IR design and impact on luminosity
  - Utilizes lower power on target

M. Palmer







# Muon Collider Parameters



Muon Collider Parameters

| Parameter                                      | Units                                    | Higgs                |           | Multi-TeV   |  |
|--|--|----------------------|-----------|-------------|--|
|  |  | Production Operation |           |             | Accounts for Site Radiation Mitigation |
| CoM Energy                                     | TeV                                      | 0.126                | 1.5       | 3.0         | 6.0                                    |
| Avg. Luminosity                                | $10^{34} \text{ cm}^{-2} \text{ s}^{-1}$ | 0.008                | 1.25      | 4.4         | 12                                     |
| Beam Energy Spread                             | %  | 0.004                | 0.1       | 0.1         | 0.1                                    |
| Higgs Production/ $10^7$ sec                   |  | 13,500               | 37,500    | 200,000     | 820,000                                |
| Circumference                                  | km                                       | 0.3                  | 2.5       | 4.5         | 6                                      |
| No. of IPs                                     |  | 1                    | 2         | 2           | 2                                      |
| Repetition Rate                                | Hz                                       | 15                   | 15        | 12          | 6                                      |
| $\beta^*$                                      | cm                                       | 1.7                  | 1 (0.5-2) | 0.5 (0.3-3) | 0.25                                   |
| No. muons/bunch                                | $10^{12}$                                | 4                    | 2         | 2           | 2                                      |
| Norm. Trans. Emittance, $\epsilon_{\text{TN}}$ | $\pi \text{ mm-rad}$                     | 0.2                  | 0.025     | 0.025       | 0.025                                  |
| Norm. Long. Emittance, $\epsilon_{\text{LN}}$  | $\pi \text{ mm-rad}$                     | 1.5                  | 70        | 70          | 70                                     |
| Bunch Length, $\sigma_s$                       | cm                                       | 6.3                  | 1         | 0.5         | 0.2                                    |
| Proton Driver Power                            | MW                                       | 4                    | 4         | 4           | 1.6                                    |
| Wall Plug Power                                | MW                                       | 200                  | 216       | 230         | 270                                    |

Exquisite Energy Resolution Allows Direct Measurement of Higgs Width

Success of advanced cooling concepts  $\Rightarrow$  several  $\ll 10^{32}$  [Rubbia proposal:  $5 \ll 10^{32}$ ]

# Radiological hazard due to neutrinos from a muon collider

Colin Johnson, Gigi Rolandi and Marco Silari

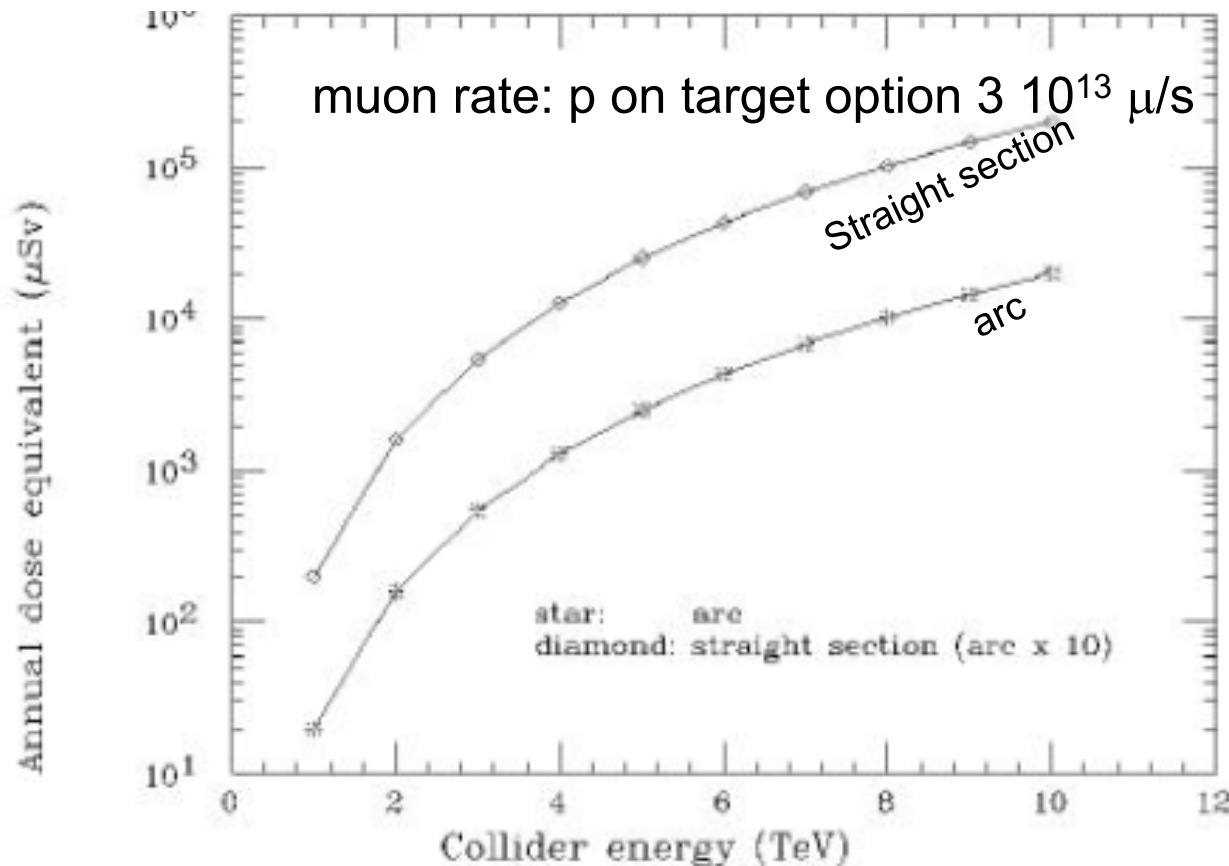


Fig. 1. Dose equivalent due to neutrino radiation at 36 km distance (collider at 100 m depth)

Limit in centre of mass energy @ 6 TeV

Still competitive with bigger sizes pp colliders?

Is then any way to operate @ lower fluxes?

Is then any way to operate @ lower fluxes?

$$L \sim 1/\sigma^2 \sim 1/\epsilon\beta$$

Need low emittances

Same as e+e- colliders

# Backup Slides

# Conclusion

- NF  $\Rightarrow$  precision  $\nu$  microscopes

- Multi-TeV MC  $\Rightarrow$  potentially only cost-effective route to lepton collider capabilities with  $E_{CM} > 5 \text{ TeV}$

- Key technical hurdles have been addressed:

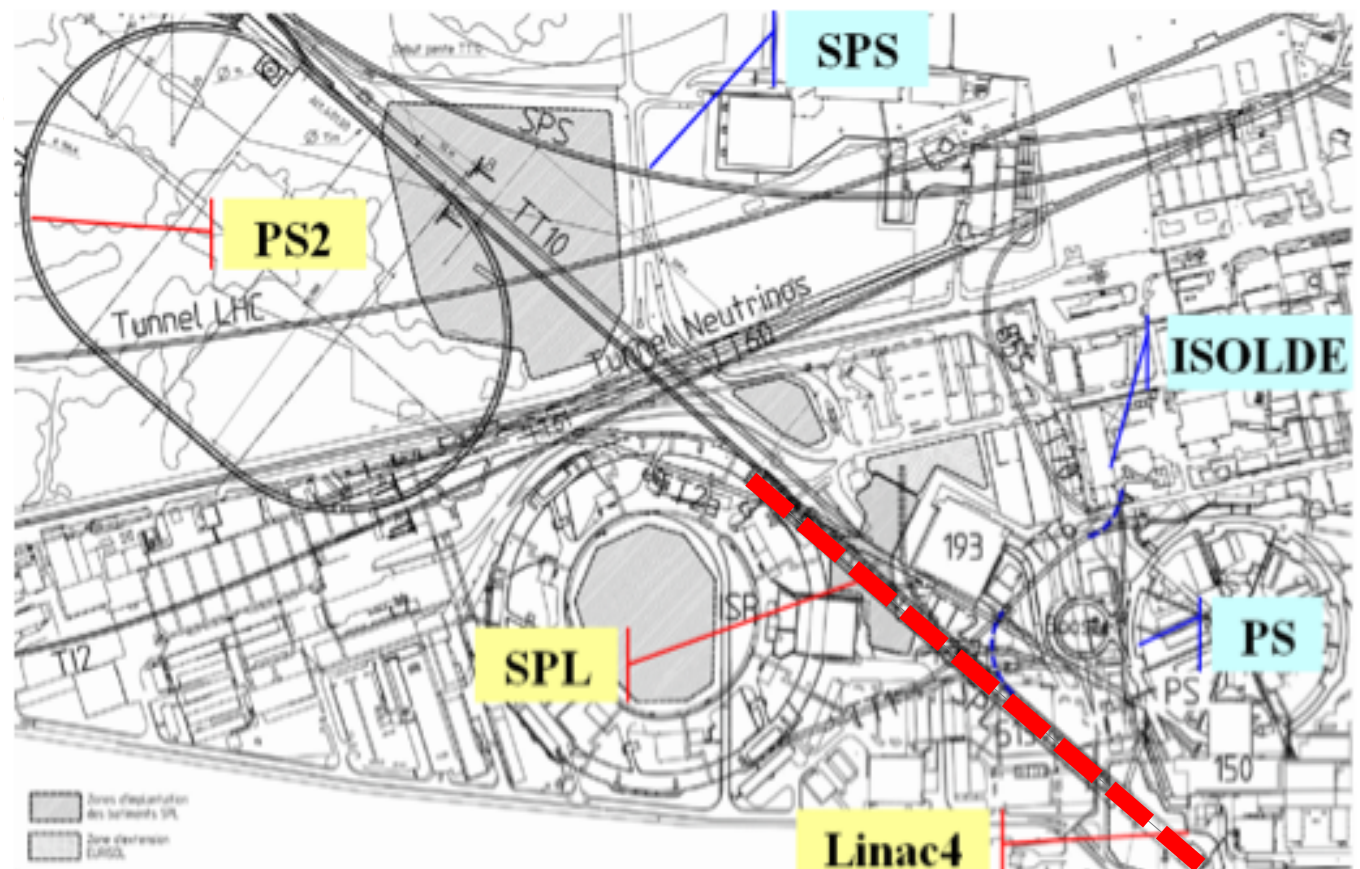
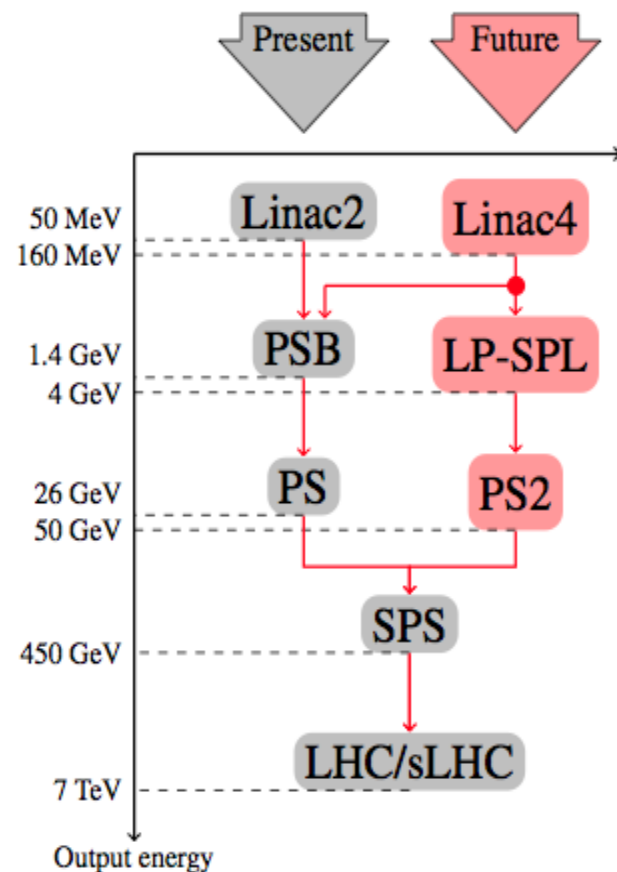
- High power target demo (MERIT)
- Realizable cooling channel designs with acceptable performance
- Breakthroughs in cooling channel technology
- Significant progress in collider & detector design concepts

*Muon accelerator capabilities offer unique potential for the future of high energy physics research*

| Accelerator  | Energy Scale          | Performance   |
|--|-----------------------|---|
| <b>Cooling Channel</b>                             | <b>~200 MeV</b>       | <b>Emittance Reduction</b>                          |
| <i>MICE</i>  | 160-240 MeV           | 5%  |
| <b>Muon Storage Ring</b>                           | <b>3-4 GeV</b>        | <b>Useable <math>\mu</math> decays/yr*</b>          |
| <i><math>\nu</math>STORM</i>                       | 3.8 GeV               | $3 \times 10^{17}$                                  |
| <b>Intensity Frontier <math>\nu</math> Factory</b> | <b>4-10 GeV</b>       | <b>Useable <math>\mu</math> decays/yr*</b>          |
| <i>NuMAX (Initial)</i>                             | 4-6 GeV               | $8 \times 10^{19}$                                  |
| <i>NuMAX+</i>                                      | 4-6 GeV               | $5 \times 10^{20}$                                  |
| <i>IDS-NF Design</i>                               | 10 GeV                | $5 \times 10^{20}$                                  |
| <b>Higgs Factory</b>                               | <b>~126 GeV CoM</b>   | <b>Higgs/<math>10^7</math>s</b>                     |
| s-Channel $\mu$ Collider                           | ~126 GeV CoM          | 3,500-13,500  |
| <b>Energy Frontier <math>\mu</math> Collider</b>   | <b>&gt; 1 TeV CoM</b> | <b>Avg. Luminosity</b>                              |
| <i>Opt. 1</i>                                      | 1.5 TeV CoM           | $1.2 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$ |
| <i>Opt. 2</i>                                      | 3 TeV CoM             | $4.4 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$ |
| <i>Opt. 3</i>                                      | 6 TeV CoM             | $12 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$  |

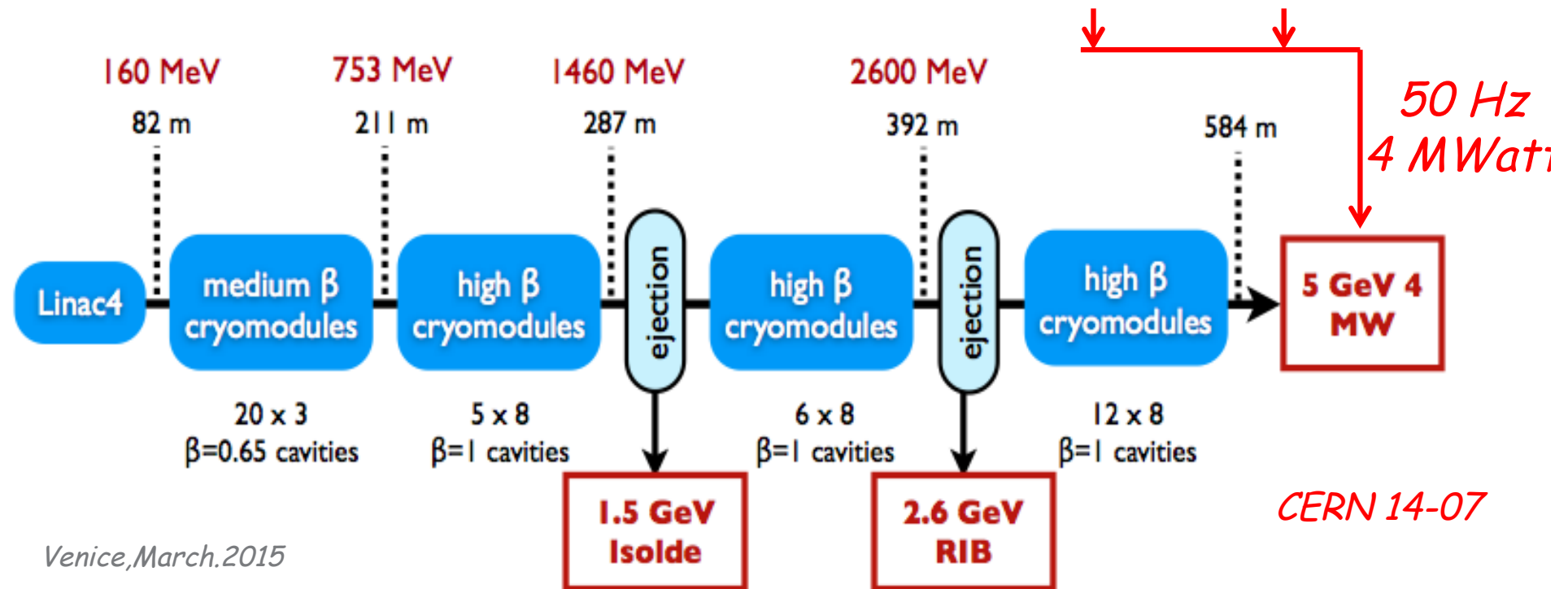
\* Decays of an individual species (ie,  $\mu^+$  or  $\mu^-$ )

- A new LHC injector complex to increase the collider luminosity 10x with the High Luminosity LHC (HL-LHC).
- Two accelerators (the LP-SPL and a new 50 GeV synchrotron, PS2) would replace the three existing ones (Linac2, the PSB, and the PS), with the injection of the SPS at 50 GeV,



- Layout of superconducting SPL with intermediate extractions.
- SPL design is very flexible and it can be adapted to the needs of many high-power proton beam applications.

| Parameter             | Units     | HP-SPL      |              | LP-SPL |
|-----------------------|-----------|-------------|--------------|--------|
|                       |           | Low-current | High-current |        |
| Energy                | GeV       | 5           | 5            | 4      |
| Beam power            | MW        | 4           | 4            | 0.144  |
| Repetition rate       | Hz        | 50          | 50           | 2      |
| Average pulse current | mA        | 20          | 40           | 20     |
| Peak pulse current    | mA        | 32          | 64           | 32     |
| Source current        | mA        | 40          | 80           | 40     |
| Chopping ratio        | %         | 62          | 62           | 62     |
| Beam pulse length     | ms        | 0.8         | 0.4          | 0.9    |
| Protons per pulse     | $10^{14}$ | 1.0         | 1.0          | 1.13   |



- A muon cooled Higgs factory can be easily housed within CERN
- The new 5 GeV Linac will provide at 50 c/s a multi MWatt H- beam with enough pions/muons to supply the muon factory.
- The basic additional accelerator structure will be the following:
  - Two additional small storage rings with  $R \approx 50$  m will strip H- to a tight p bunch and compress the LP-SPL beam to a few ns.
  - Muons of both signs are focused in a axially symmetric  $B = 20$  T field, reducing progressively pt with a horn and  $B = 2$  T
  - A buncher and a rotator compresses muons to  $\approx 250$  MeV/c
  - Muon Cooling in 3D compresses emittances by a factor 106.
  - Bunches of about  $2 \times 10^{12}$   $m^\pm$  are accelerated to 62.5 GeV
  - Muons are colliding in a SC storage ring of  $R \approx 60$  m (about one half of the CERN-PS ,1/100 of LHC) where about 104 Higgs events/y are recorded for each of the experiments.

# Staged Neutrino Factory and Muon Colliders main parameters



## Neutrino Factory at intensity frontier

## Muon Collider at the energy frontier

| System        | Parameters                             | Unit               | nuSTORM            | NuMAX Commissioning   | NuMAX                 | NuMAX+               |
|---------------|--|--------------------|--------------------|-----------------------|-----------------------|----------------------|
| Performance   | $\nu_e$ or $\nu_\mu$ to detectors/year | -                  | $3 \times 10^{17}$ | $4.9 \times 10^{19}$  | $1.8 \times 10^{20}$  | $5.0 \times 10^{20}$ |
|               | Stored $\mu^+$ or $\mu^-$ /year        | -                  | $8 \times 10^{17}$ | $1.25 \times 10^{20}$ | $4.65 \times 10^{20}$ | $1.3 \times 10^{21}$ |
| Detector      | <b>Far Detector:</b>                   | Type               | SuperBIND          | MIND / Mag LAr        | MIND / Mag LAr        | MIND / Mag LAr       |
|               | Distance from Ring                     | km                 | 1.9                | 1300                  | 1300                  | 1300                 |
|               | Mass                                   | kT                 | 1.3                | 100 / 30              | 100 / 30              | 100 / 30             |
|               | Magnetic Field                         | T                  | 2                  | 0.5-2                 | 0.5-2                 | 0.5-2                |
|               | <b>Near Detector:</b>                  | Type               | SuperBIND          | Suite                 | Suite                 | Suite                |
|               | Distance from Ring                     | m                  | 50                 | 100                   | 100                   | 100                  |
|               | Mass                                   | kT                 | 0.1                | 1                     | 1                     | 2.7                  |
| Neutrino Ring | Magnetic Field                         | T                  | Yes                | Yes                   | Yes                   | Yes                  |
|               | Ring Momentum                          | GeV/c              | 3.8                | 5                     | 5                     | 5                    |
|               | Circumference (C)                      | m                  | 480                | 737                   | 737                   | 737                  |
|               | Straight section                       | m                  | 184                | 281                   | 281                   | 281                  |
|               | Number of bunches                      | -                  | -                  | 60                    | 60                    | 60                   |
| Acceleration  | Charge per bunch                       | $1 \times 10^9$    | -                  | 6.9                   | 26                    | 35                   |
|               | Initial Momentum                       | GeV/c              | -                  | 0.25                  | 0.25                  | 0.25                 |
|               | Single-pass Linacs                     | GeV/c              | -                  | 1.0, 3.75             | 1.0, 3.75             | 1.0, 3.75            |
|               |  | MHz                | -                  | 325, 650              | 325, 650              | 325, 650             |
| Repetition    | Hz                                     | -                  | 30                 | 30                    | 60                    |                      |
| Cooling       |  |                    | No                 | No                    | Initial               | Initial              |
| Proton Driver | Proton Beam Power                      | MW                 | 0.2                | 1                     | 1                     | 2.75                 |
|               | Proton Beam                            | GeV                | 120                | 6.75                  | 6.75                  | 6.75                 |
|               | Protons/year                           | $1 \times 10^{21}$ | 0.1                | 9.2                   | 9.2                   | 25.4                 |
|               | Repetition                             | Hz                 | 0.75               | 15                    | 15                    | 15                   |

| Parameter                               | Units                                    | Higgs Factory      |                      | Top Threshold Options |                 | Multi-TeV Baselines |             | Accounts for Site Radiation Mitigation |
|---|--|--------------------|----------------------|-----------------------|-----------------|---------------------|-------------|--|
|   |  | Startup Operation  | Production Operation | High Resolution       | High Luminosity |                     |             |  |
| CoM Energy                              | TeV                                      | 0.126              | 0.126                | 0.35                  | 0.35            | 1.5                 | 3.0         | 6.0                                    |
| Avg. Luminosity                         | $10^{34} \text{ cm}^{-2} \text{ s}^{-1}$ | 0.0017             | 0.008                | 0.07                  | 0.6             | 1.25                | 4.4         | 12                                     |
| Beam Energy Spread                      | %  | 0.003              | 0.004                | 0.01                  | 0.1             | 0.1                 | 0.1         | 0.1                                    |
| Higgs* or Top* Production/ $10^7$ sec   |  | 3,500*             | 13,500*              | 7,000*                | 60,000*         | 37,500*             | 200,000*    | 820,000*                               |
| Circumference                           | km                                       | 0.3                | 0.3                  | 0.7                   | 0.7             | 2.5                 | 4.5         | 6                                      |
| No. of IPs                              |  | 1                  | 1                    | 1                     | 1               | 2                   | 2           | 2                                      |
| Repetition Rate                         | Hz                                       | 30                 | 15                   | 15                    | 15              | 15                  | 12          | 6                                      |
| $\beta^*$                               | cm                                       | 3.3                | 1.7                  | 1.5                   | 0.5             | 1 (0.5-2)           | 0.5 (0.3-3) | 0.25                                   |
| No. muons/bunch                         | $10^{12}$                                | 2                  | 4                    | 4                     | 3               | 2                   | 2           | 2                                      |
| No. bunches/beam                        |  | 1                  | 1                    | 1                     | 1               | 1                   | 1           | 1                                      |
| Norm. Trans. Emittance, $\epsilon_{TN}$ | $\pi$ mm-rad                             | 0.4                | 0.2                  | 0.2                   | 0.05            | 0.025               | 0.025       | 0.025                                  |
| Norm. Long. Emittance, $\epsilon_{LN}$  | $\pi$ mm-rad                             | 1                  | 1.5                  | 1.5                   | 10              | 70                  | 70          | 70                                     |
| Bunch Length, $\sigma_s$                | cm                                       | 5.6                | 6.3                  | 0.9                   | 0.5             | 1                   | 0.5         | 0.2                                    |
| Proton Driver Power                     | MW                                       | 4*                 | 4                    | 4                     | 4               | 4                   | 4           | 1.6                                    |
| <b>Cooling</b>                          |  | <b>6D no final</b> |                      |                       | <b>Full 6D</b>  |                     |             |  |

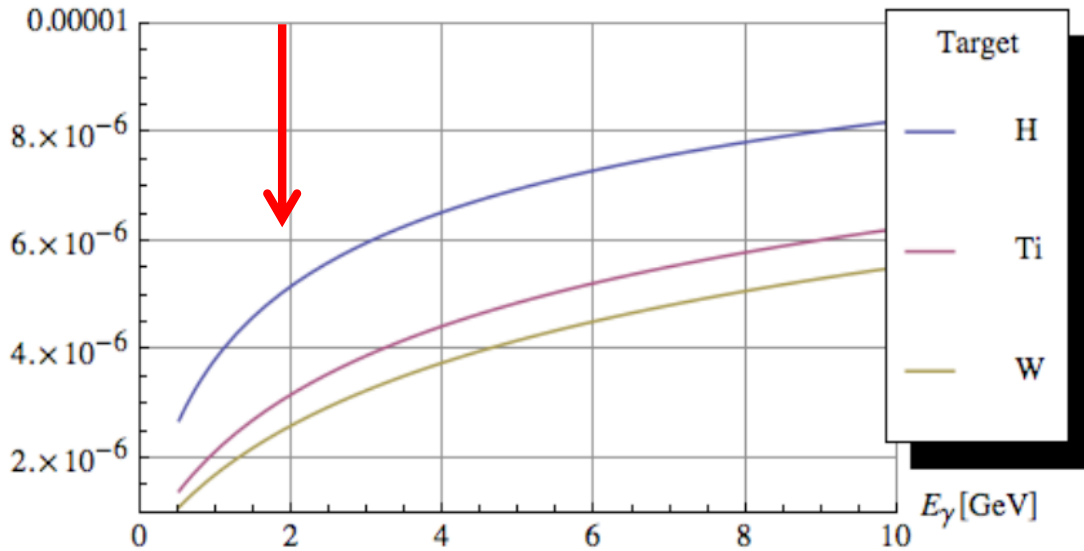


# Muon generation by GeV-scale Compton $\gamma$ s

V.Yakimenko (SLAC)

Probability of creating  $\mu^+\mu^-$  pairs as a function of the incident photon energy

$$\frac{\sigma_{\text{tot}_\mu}}{\sigma_{\text{tot}_e}} \approx \frac{1}{4} \frac{m_e^2}{m_\mu^2} \text{ or } 0.5 \cdot 10^{-5}$$



| 2GeV $\gamma$ beam                 | Pulsed Linac      | ERL                                 |
|------------------------------------|-------------------|-------------------------------------|
| e-beam energy [GeV]                | 36                | 11                                  |
| Laser wavelength [ $\mu\text{m}$ ] | 10                | 1                                   |
| Bunch charge [nC]                  | 10                | 1.5                                 |
| Rep. rate [kHz]                    | 0.2               | 20 / 200                            |
| Bunches per beam                   | 250               |                                     |
| Average current [mA]               | 2                 | 30 / 300                            |
| e-beam power [MW]                  | 18                | 330 / 3300                          |
| e-to- $\gamma$ convers. efficiency | 3                 | 0.33                                |
| $\gamma$ -beam power [MW]          | 3                 | 20 / 200                            |
| Total AC-to- $\gamma$ efficiency   | 10%               | 20% / 75%                           |
| Peak $\mu^+\mu^-$ [per bunch]      | $10^6$            | $3 \cdot 10^4$                      |
| Average $\mu^+\mu^-$ [per second]  | $5 \cdot 10^{10}$ | $3 \cdot 10^{11} / 3 \cdot 10^{12}$ |

- Brightness  $10^3$  larger than with proton driver
- $10^3$  too low with pulsed linac
- $10^2$  flux increase with high current ERL
- Approaching intensities desired for NF (but train structure not favorable for collider luminosity,  $N^2$  issue)