

# Low Emittance Muon Collider (LEMMA)

**M. Antonelli (INFN-LNF)**

# Outline

- Introduction
- Positron driven source
- LEMMA scheme
- Optics & Beam dynamics
- R&D on key topics
- Goal parameter table for Multi-TeV MC
- Conclusion

# Muon based Colliders

- **A  $\mu^+\mu^-$  collider offers an ideal technology to extend lepton high energy frontier in the multi-TeV range**
  - No synchrotron radiation (limit of  $e^+e^-$  circular colliders)
  - No beamstrahlung (limit of  $e^+e^-$  linear colliders)
  - but muon lifetime is 2.2  $\mu\text{s}$  at rest
- **Great potentiality if the technology proves its feasibility**
- **Best performances in terms of luminosity and power consumption**

**Recent review paper:** M.Boscolo, J. P. Delahaye and M. Palmer, ``The future prospects of muon colliders and neutrino factories," in publication by Rev.Accel.Sci.Tech. arXiv:1808.01858

# Muon Source

**Proton  
driven**

**Tertiary production from protons on target:**  $p + \text{target} \rightarrow \pi/K \rightarrow \mu$   
typically  $P_\mu \approx 100 \text{ MeV}/c$  ( $\pi, K$  rest frame)  
whatever is the boost  $P_T$  will stay in Lab frame  
 $\rightarrow$  **very high emittance** at production  $\rightarrow$  **cooling needed**  
production Rate  $> 10^{13} \mu/\text{sec}$      $N_\mu = 2 \cdot 10^{12}/\text{bunch}$

**MAP**

**Positron  
driven**

from **direct  $\mu$  pair production**:  
muons produced from  $e^+e^- \rightarrow \mu^+\mu^-$  at  $\sqrt{s}$  around the  $\mu^+\mu^-$  threshold  
( $\sqrt{s} \approx 0.212 \text{ GeV}$ ) in asymmetric collisions (to collect  $\mu^+$  and  $\mu^-$ )  
 $e^+e^-$  annihilation:  **$e^+$  beam on target**  
 $\rightarrow$  **cooled muon beam with low emittance** at production  
Goal: production Rate  $\approx 10^{11} \mu/\text{sec}$      $N_\mu \approx 6 \cdot 10^9/\text{bunch}$

**LEMMA**

**by Gammas** ( $\gamma \text{ Nuclei} \rightarrow \mu^+\mu^- \text{ Nuclei}$ ): **GeV-scale Compton  $\gamma$ s**

[V. Yakimenko  
(SLAC)]

also: ( **$e^- \text{ Nuclei} \rightarrow \mu^+\mu^- e^- \text{ Nuclei}$** ) W. Barletta and A. M. Sessler NIM A 350 (1994) 36-44



# Muon source Comparison

	Physical process	Rate $\mu/s$	normalized emittance $e_N [\mu\text{m-rad}]$
<b><math>e^+</math> on target</b>	<b><math>e^+e^- \rightarrow \mu^+\mu^-</math></b>	<b><math>0.9 \times 10^{11}</math></b>	<b>0.04</b>
Protons on target	$p N \rightarrow \pi X, K X \rightarrow \mu X'$	$10^{13}$	25
Compton $\gamma$ on target	$\gamma N \rightarrow \mu^+\mu^- N$	$5 \times 10^{10}$	2

# Exploring the potential for a Low Emittance Muon Collider

## some References:

- M. Boscolo *et al.*, “Studies of a scheme for low emittance muon beam production from positrons on target”, **IPAC17 (2017)**
- M. Antonelli, “Very Low Emittance Muon Beam using Positron Beam on Target”, **ICHEP (2016)**
- M. Antonelli *et al.*, “Very Low Emittance Muon Beam using Positron Beam on Target”, **IPAC (2016)**
- M. Antonelli, “Performance estimate of a FCC-ee-based muon collider”, **FCC-WEEK 2016**
- M. Antonelli, “Low-emittance muon collider from positrons on target”, **FCC-WEEK 2016**
- M. Antonelli, M. Boscolo, R. Di Nardo, P. Raimondi, “Novel proposal for a low emittance muon beam using positron beam on target”, **NIM A 807 101-107 (2016)**
- P. Raimondi, “Exploring the potential for a Low Emittance Muon Collider”, in **Discussion of the scientific potential of muon beams workshop**, CERN, Nov. 18<sup>th</sup> 2015
- M. Antonelli, **Presentation Snowmass 2013**, Minneapolis (USA) July 2013, [M. Antonelli and P. Raimondi, Snowmass Report (2013) also INFN-13-22/LNF Note

Also investigated by SLAC team:

L. Keller, J. P. Delahaye, T. Markiewicz, U. Wienands:

- “Luminosity Estimate in a Multi-TeV Muon Collider using  $e^+e^- \rightarrow \mu^+\mu^-$  as the Muon Source”, MAP 2014 Spring workshop, Fermilab (USA) May '14
- Advanced Accelerator Concepts Workshop, San Jose (USA), July '14

# LEMMA:

## Low EMittance Muon Accelerator

Concept based on a positron driven source

It opens the perspective to a Multi-TeV Muon Collider

- Muons are produced in positron annihilation on  $e^-$  at rest  
→  $e^+$  beam impinging on target
- It is a low emittance muon source
- Low emittance concept overcomes muon cooling
- Low emittance allows operations at very high c.o.m. energy

LEMMA concept was proposed at Snowmass 2013 by M. Antonelli and P. Raimondi:  
M. Antonelli, “Ideas for muon production from positron beam interaction on a plasma target”, INFN-13-22/LNF Note, M. Antonelli and P. Raimondi, Snowmass Report (2013)

# Summary of LEMMA pro&cons features

## Pro LEMMA:

$\theta_\mu$  is tunable with  $\sqrt{s}$  in  $e^+e^- \rightarrow \mu^+\mu^-$

$\mu$  beam divergence can be **very small** close to the  $\mu^+\mu^-$  threshold

## Cons LEMMA: Low $\mu$ prod. Rate

much smaller cross section. wrt proton-driven-source

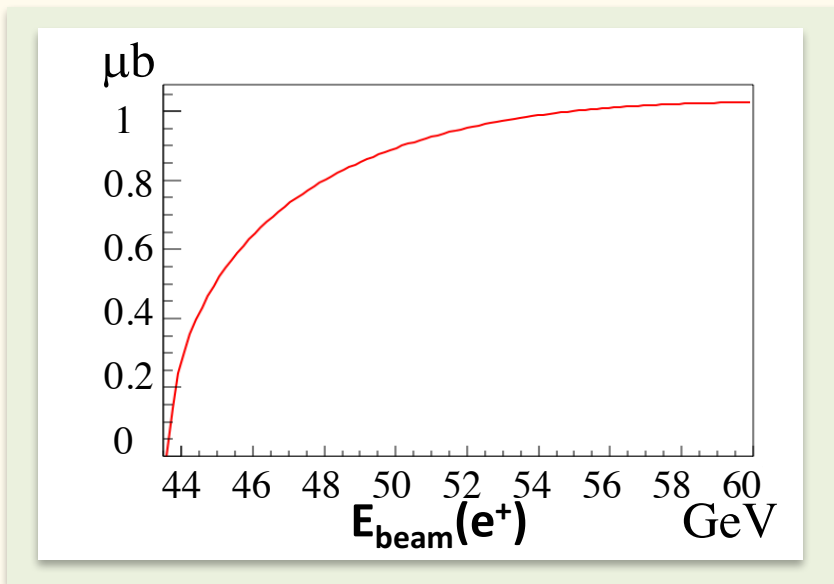
$\sigma(e^+e^- \rightarrow \mu^+\mu^-) \approx 1 \mu\text{b}$  at most wrt  $\sigma(\text{from } p) \approx \text{mb}$

## Pro LEMMA:

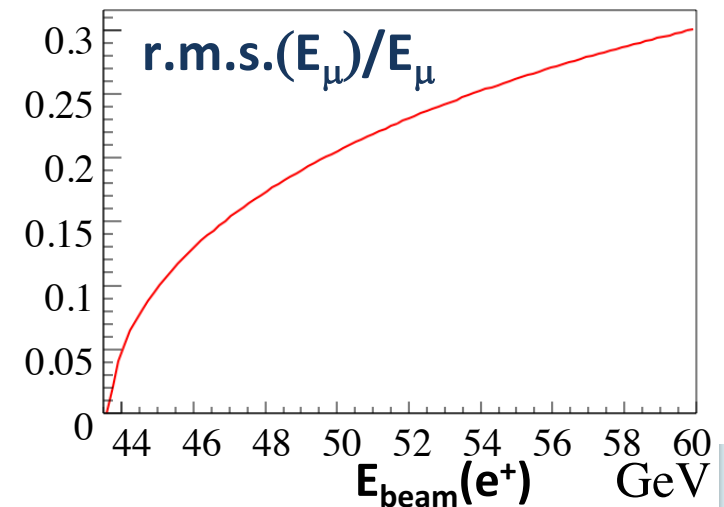
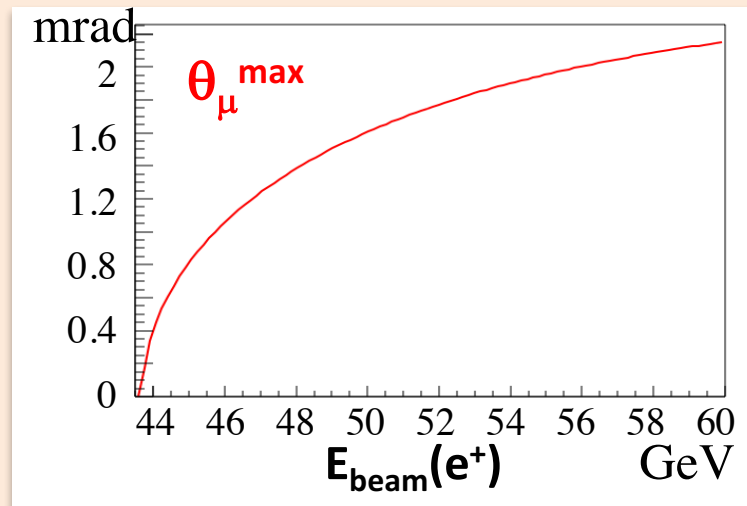
- **Reduced losses from decay:** high collection efficiency
- **Low background:** Luminosity at low emittance will allow low background and low neutrino radiation  $\rightarrow$  easier experimental conditions & can go to higher energies
- **Energy spread:** muon energy spread might be also small at threshold, it gets larger as  $\sqrt{s}$  increases

# Cross-section, muons beam divergence and energy spread as a function of the $e^+$ beam energy

$$\sigma(e^+e^- \rightarrow \mu^+\mu^-)$$



The value of  $\sqrt{s}$  (*i.e.*  $E(e^+)$  for atomic  $e^-$  in target) has to maximize the muons production and minimize the beam angular divergence and energy spread



# Radiological hazard due to neutrinos from a MC

- First studies by B.J.King in Proc. EPAC98, p. 841-843 and Proc. 1999 PAC p. 319
- C. Johnson, G. Rolandi and M. Silari, TIS-RP/IR/98-34 (1998)
- J.D. Cossairt, N.L. Grossman and E.T. Marshall, Health Phys. 73 (1997), 894-898  
(on neutrino dose equivalent/fluence)

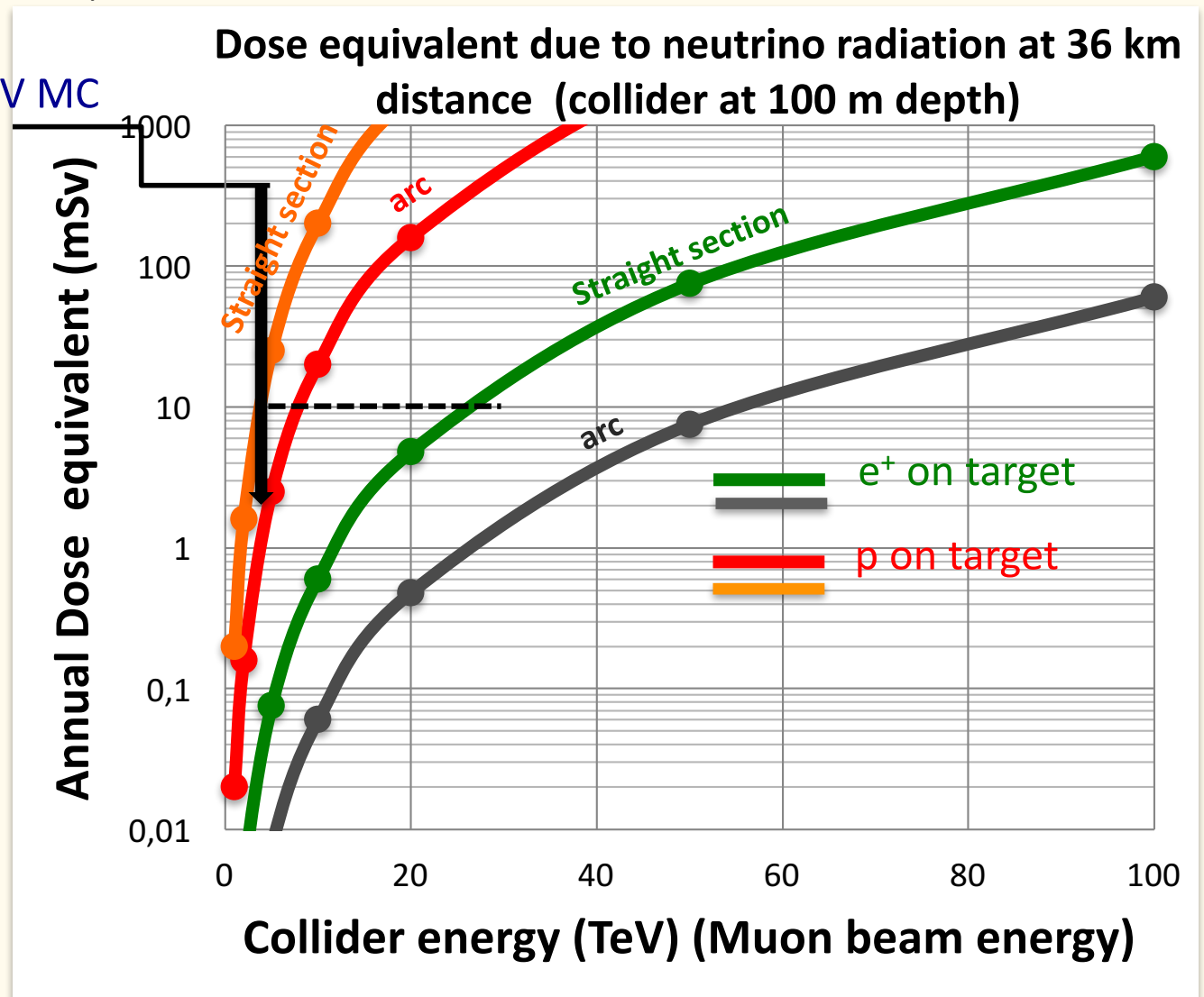
MAP design for a 6 TeV MC  
(500 m depth)

muon rate:

p on target option  
 $3 \times 10^{13} \mu/s$

$e^+$  on target option  
 $9 \times 10^{10} \mu/s$

This plot is based on numbers  
reported in C. Johnson et al  
adding Lemma, M. Antonelli



# Possible Schemes

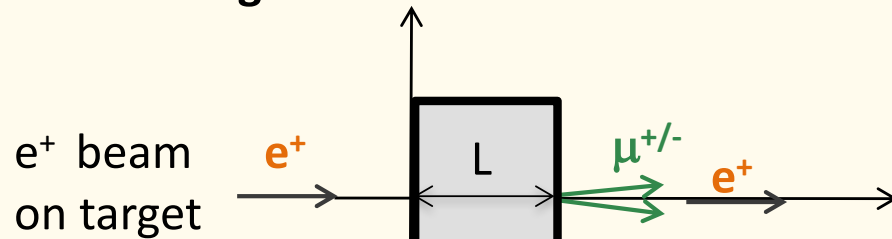
- **Low energy collider with  $e^+/e^-$  beam ( $e^+$  in the GeV range):**
  1. Conventional asymmetric collisions (but required luminosity  $\approx 10^{40}$  is beyond present capability)
  2. Positron beam interacting with continuous beam from electron cooling (too low electron density,  $10^{20}$  electrons/cm<sup>3</sup> needed to obtain a reasonable conversion efficiency to muons)
- **Electrons at rest (seems more feasible):**
  3.  $e^+$  on Plasma target
  4.  $e^+$  on standard target (eventually crystals in channeling)
    - **Need Positrons of  $\approx 45$  GeV**
    - $\gamma(\mu) \approx 200$  and  $\mu$  laboratory lifetime of about 500  $\mu$ s



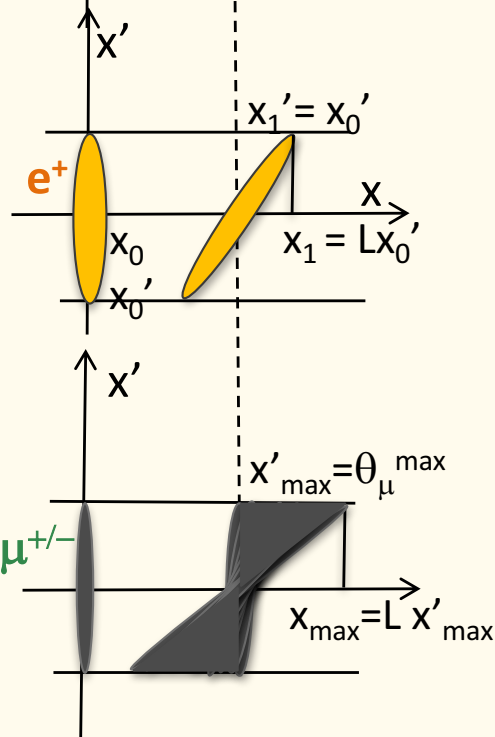
**Ideally muons will *copy* the positron beam**

# Production contribution to $\mu$ beam emittance

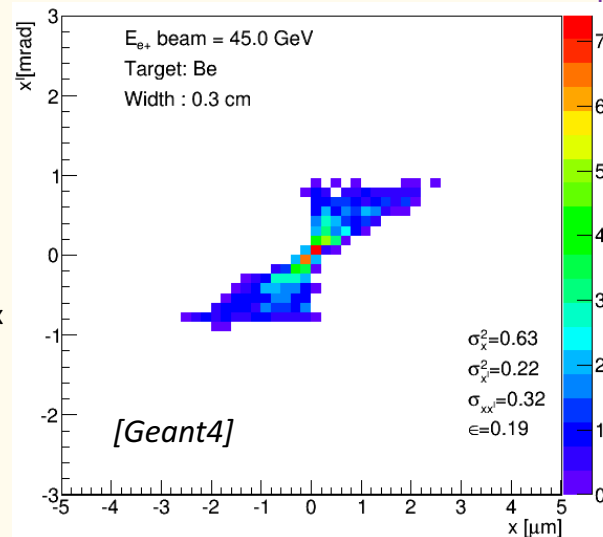
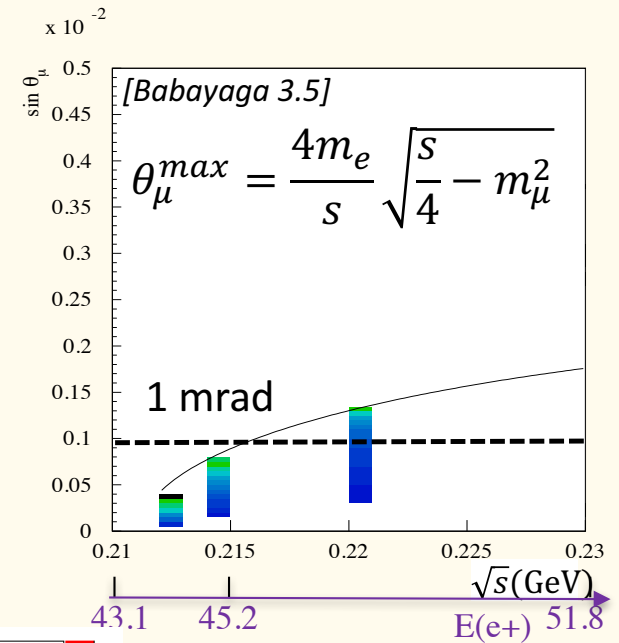
ideal  $e^-$  target



If  $L$  was a drift



Muons produced uniformly along target,  $\infty$  drifts  $[0, L]$



Muon beam at the exit of a 3 mm Be target  
 $\epsilon_{\mu} = 0.19 \text{ nm}$   
 (45 GeV  $e^+$  beam)

thin light materials targets have negligible multiple scattering contribution

The emittance contributions due to muon production angle:  $\epsilon_{\mu} = x x'_{\max} / 12 = L (\theta_{\mu}^{\max})^2 / 12$   
 $\rightarrow \epsilon_{\mu}$  completely determined by  $L$  and  $s$  -by target thickness and c.o.m. energy



# Criteria for target design

Number of  $\mu^+\mu^-$  pairs produced per  $e^+e^-$  interaction is given by

$$N(\mu^+\mu^-) = \sigma(e^+e^- \rightarrow \mu^+\mu^-) N(e^+) \rho(e^-) L$$

$N(e^+)$  number of  $e^+$

$\rho(e^-)$  target electron density

$L$  target length

To maximise  $N(\mu^+\mu^-)$ :

- $N(e^+)$  max rate limit set by  $e^+$  source
- $\rho(e^-)L$  max occurs for  $L$  or  $\rho$  values giving total  $e^+$  beam loss
  - **$e^-$  dominated target:** radiative Bhabha is the dominant  $e^+$  loss effect, giving a maximal  $\mu^+\mu^-$  conversion efficiency  
 $N(\mu^+\mu^-)/N(e^+) \approx \sigma(e^+e^- \rightarrow \mu^+\mu^-)/\sigma_{rb} \approx 10^{-5}$
  - **standard target:** Bremsstrahlung on nuclei and multiple scattering are the dominant effects,  $X_0$  and electron density will matter  $N(\mu^+\mu^-)/N(e^+) \approx \sigma(e^+e^- \rightarrow \mu^+\mu^-)/\sigma_{brem}$

# Criteria for target design

Luminosity is proportional to  $N_\mu^2 / \varepsilon_\mu$

**optimal target: minimizes  $\mu$  emittance with highest  $\mu$  rate**

- **Heavy materials , thin target**
  - **minimize emittance** (enters linearly)  $\rightarrow$  Copper has about same contributions to emittance from MS and  $\mu^+\mu^-$  production
  - high  $e^+$  loss, Bremsstrahlung is dominant, **not optimal  $\mu$  rate**
- **Very light materials**
  - **maximize conversion efficiency** (enters quad)  $\rightarrow$   $H_2$
  - even for liquid need O(1m) target,  $\varepsilon_\mu \propto L \rightarrow \mu$  **emittance increase**
- **Not too heavy materials (Be, C )**
  - Allow **low emittance with small  $e^+$  loss**

**optimal: not too heavy and thin**

# Criteria for target design

Luminosity is proportional to  $N_\mu^2 \propto 1/\varepsilon_\mu$

**optimal target: minimizes  $\mu$  emittance with highest  $\mu$  rate**

- **Heavy materials, thin target**

- to minimize  $\varepsilon_\mu$ : thin target ( $\varepsilon_\mu \propto L$ ) with high density  $\rho$

Copper: MS and  $\mu^+\mu^-$  production give about same contribution to  $\varepsilon_\mu$

BUT high  $e^+$  loss (Bremsstrahlung is dominant) so

$$\sigma(e^+\text{loss}) \approx \sigma(\text{Brem}+\text{bhabha}) \approx (Z+1)\sigma(\text{Bhabha}) \rightarrow$$

$$N(\mu^+\mu^-)/N(e^+) \approx \sigma_\mu / [(Z+1)\sigma(\text{Bhabha})] \approx 10^{-7}$$

- **Very light materials, thick target**

- maximize  $\mu^+\mu^-$  conversion efficiency  $\approx 10^{-5}$  (enters quad)  $\rightarrow H_2$

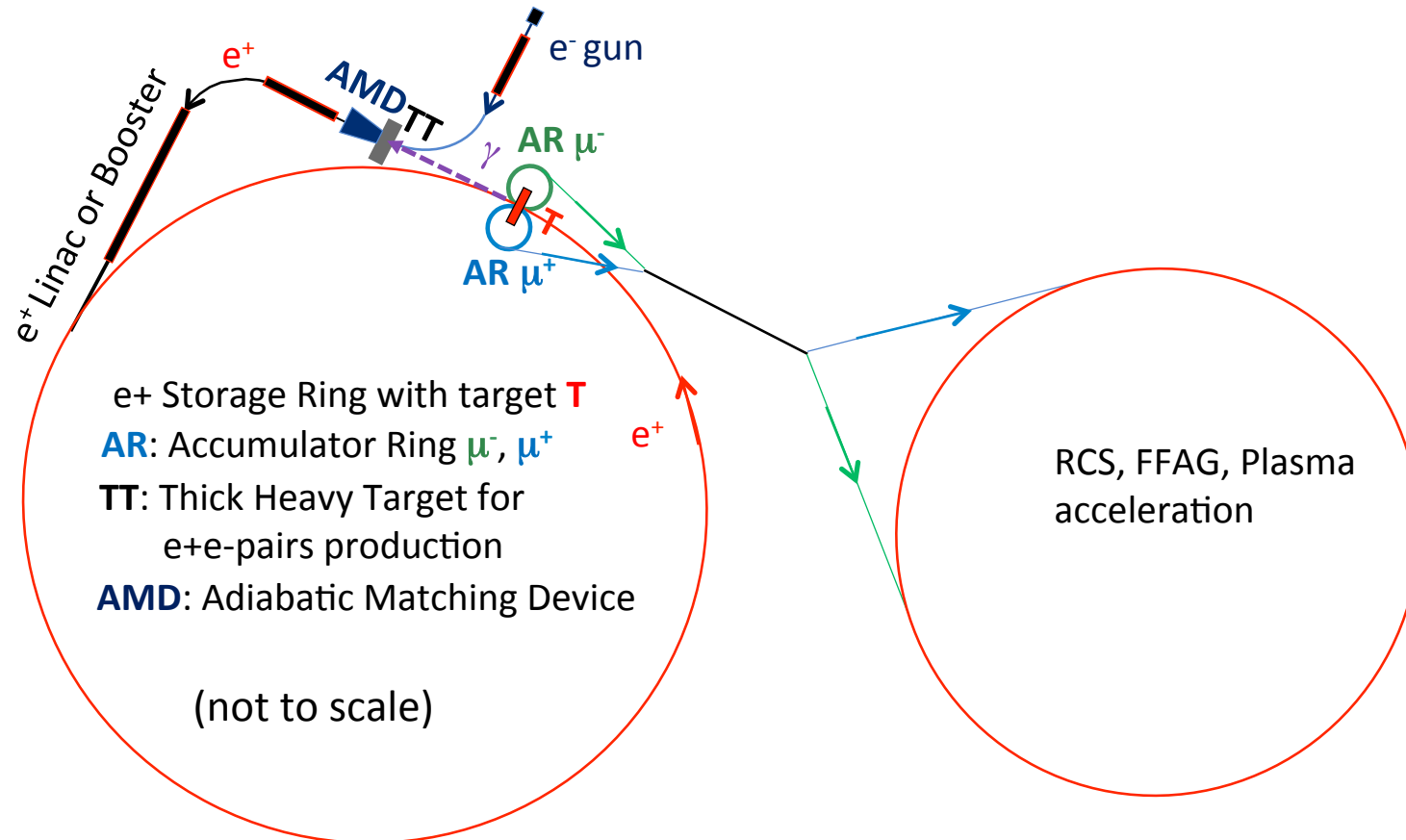
Even for liquid targets O(1m) needed  $\rightarrow \varepsilon_\mu \propto L$  increase

- **Not too heavy materials (Be, C)**

- Allow low  $\varepsilon_\mu$  with small  $e^+$  loss  $N(\mu^+\mu^-)/N(e^+) \approx 10^{-6}$

**not too heavy and thin in combination with stored positron beam  
to reduce requests on positron source**

# LEMMA scheme

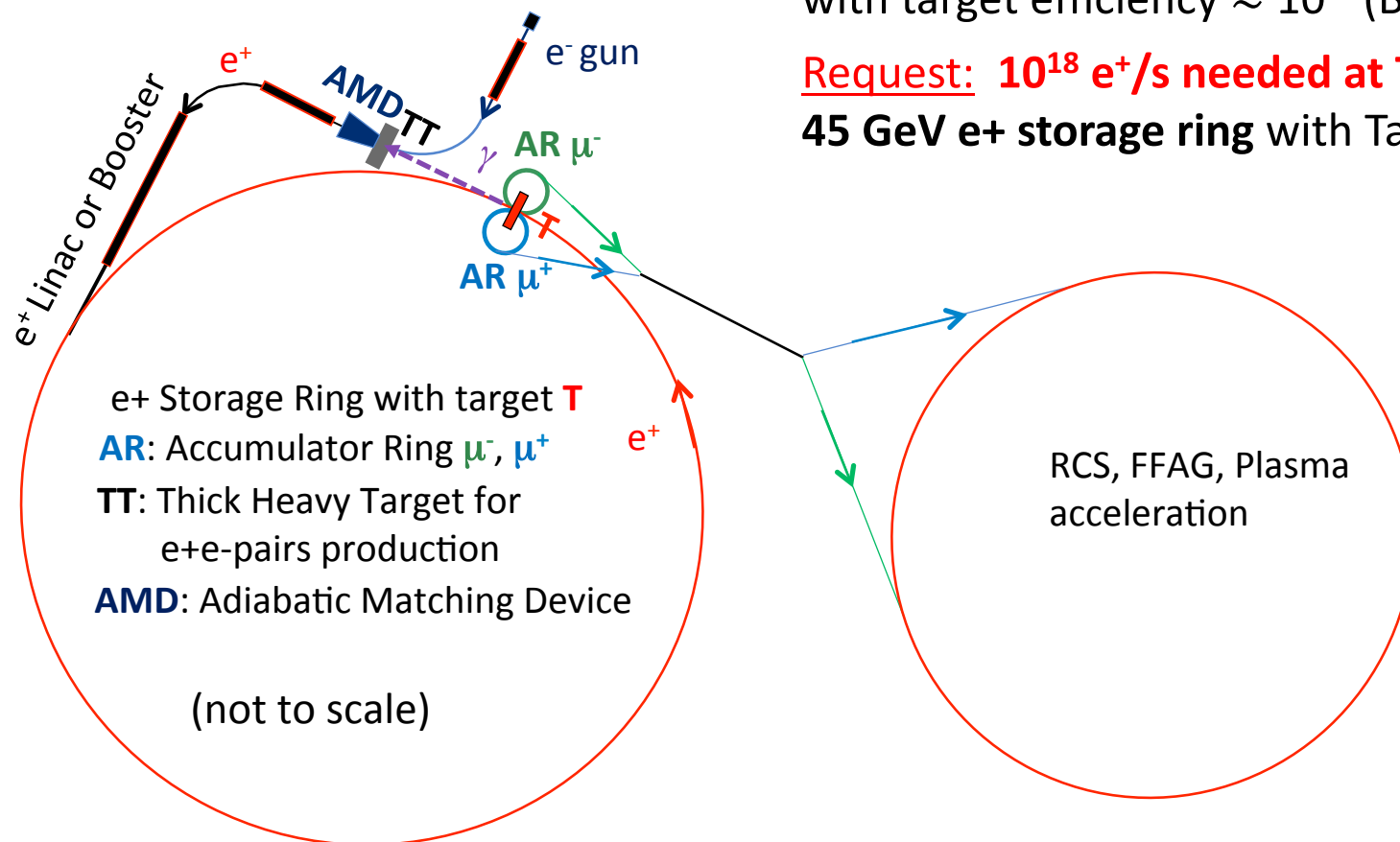


# LEMMA scheme

Goal:  $\approx 10^{11} \mu/s$  produced at Target

with target efficiency  $\approx 10^{-7}$  (Be 3mm)

Request:  $10^{18} e^+/s$  needed at Target  $\rightarrow$   
45 GeV  $e^+$  storage ring with Target insertion

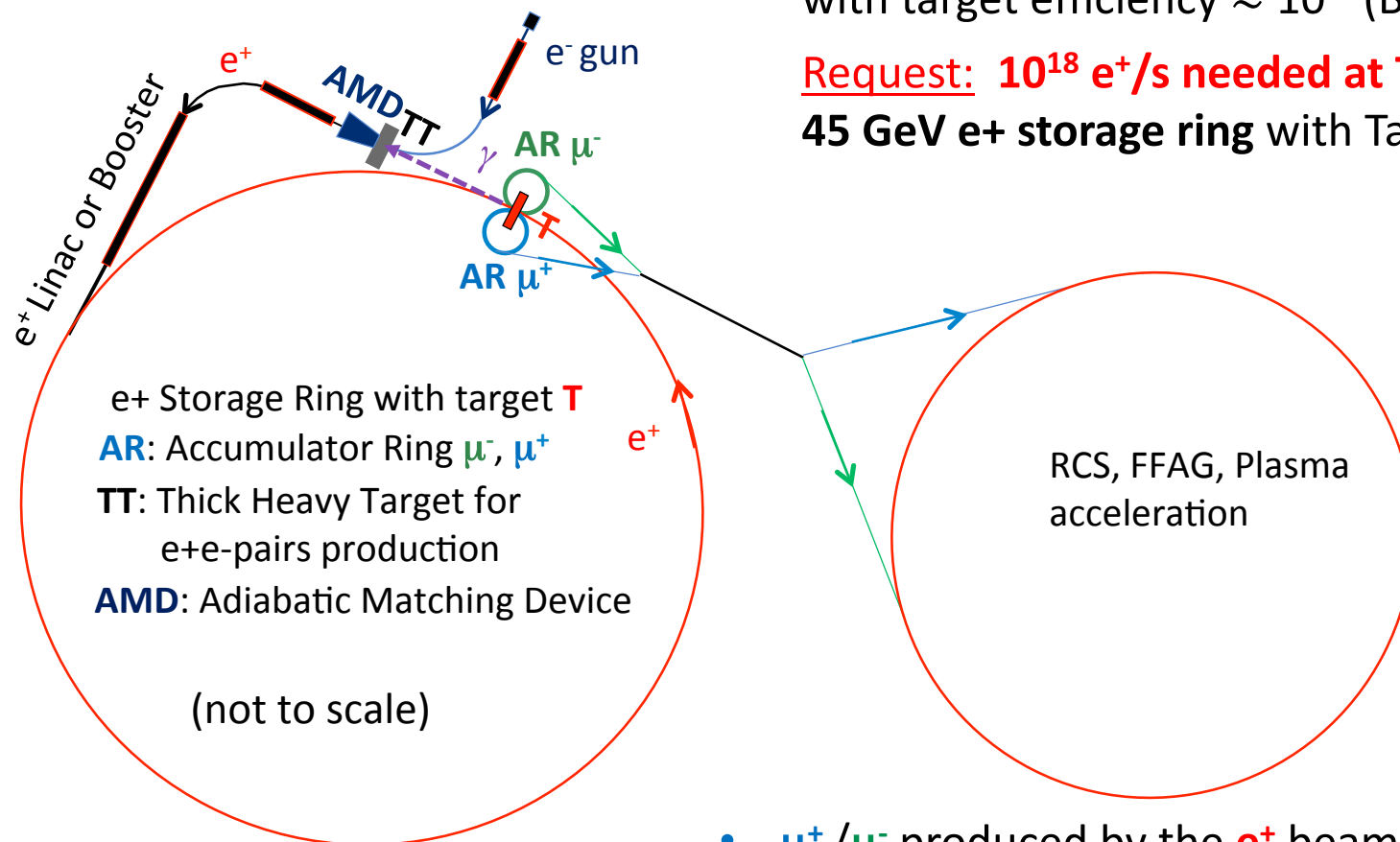


# LEMMA scheme

Goal:  $\approx 10^{11} \mu/s$  produced at Target

with target efficiency  $\approx 10^{-7}$  (Be 3mm)

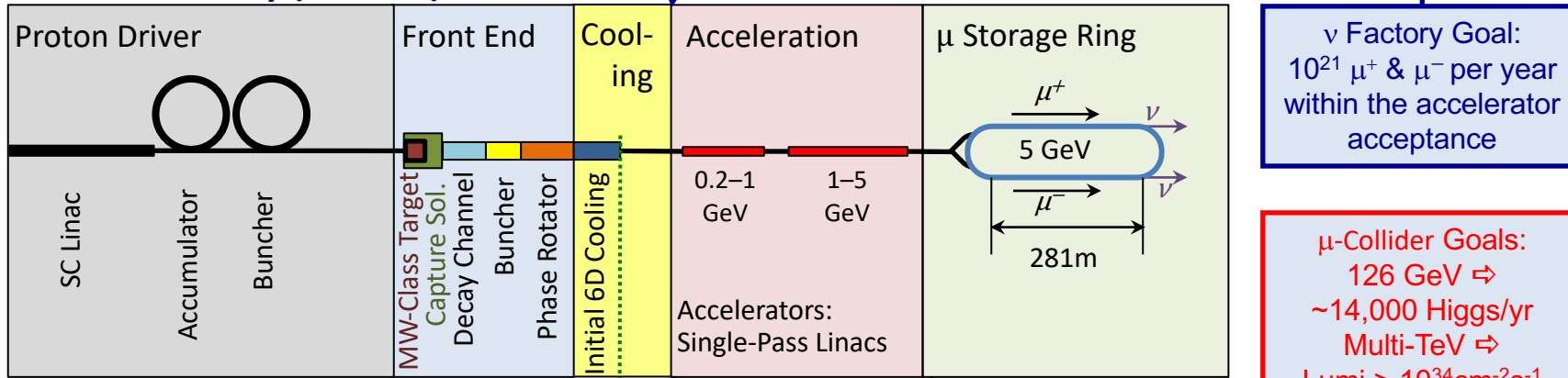
Request:  $10^{18} e^+/s$  needed at Target  $\rightarrow$   
45 GeV  $e^+$  storage ring with Target insertion



from  $\mu^+ \mu^-$  production to collider

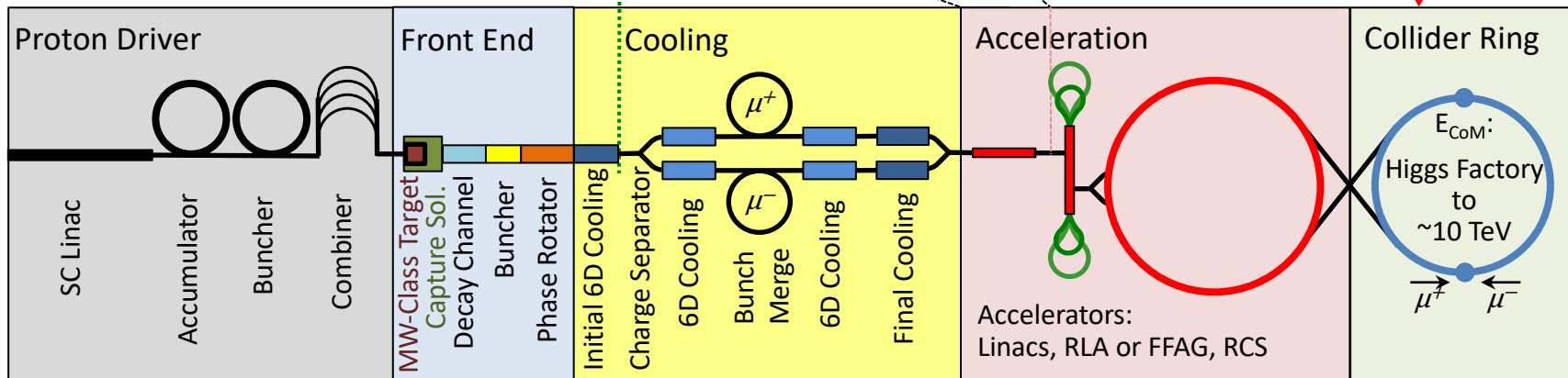
- $\mu^+/\mu^-$  produced by the  $e^+$  beam on target **T** at about **22 GeV**  $\rightarrow \tau_{lab}(\mu) \approx 500\mu s$  ( $\gamma(\mu) \approx 200$ )
- Accumulator Rings (**AR**) isochronous with high momentum acceptance, they recombine  $\mu$  bunches for  $\sim 1 \tau_{\mu}^{lab} \approx 2500$  turns
- fast acceleration and to collider

## Neutrino Factory (NuMAX)



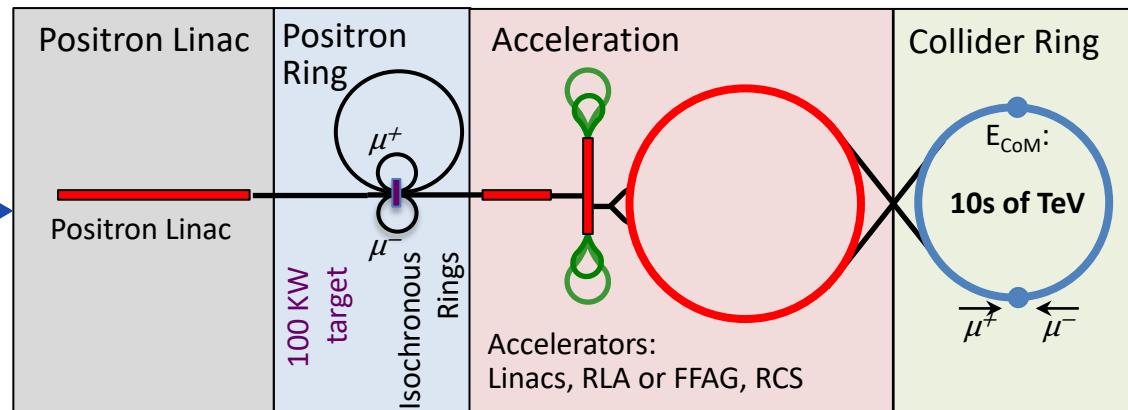
Share same complex

## Muon Collider

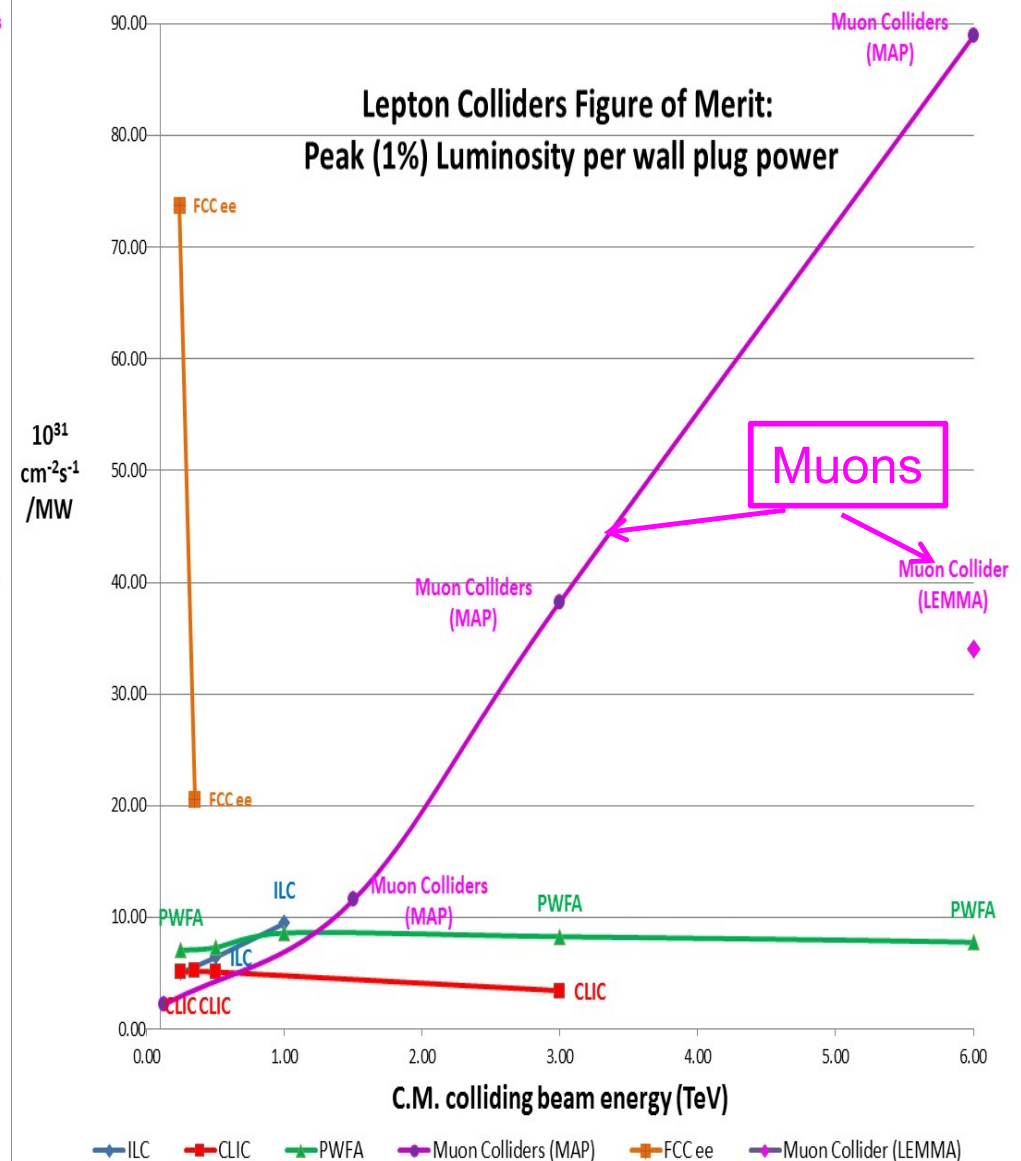
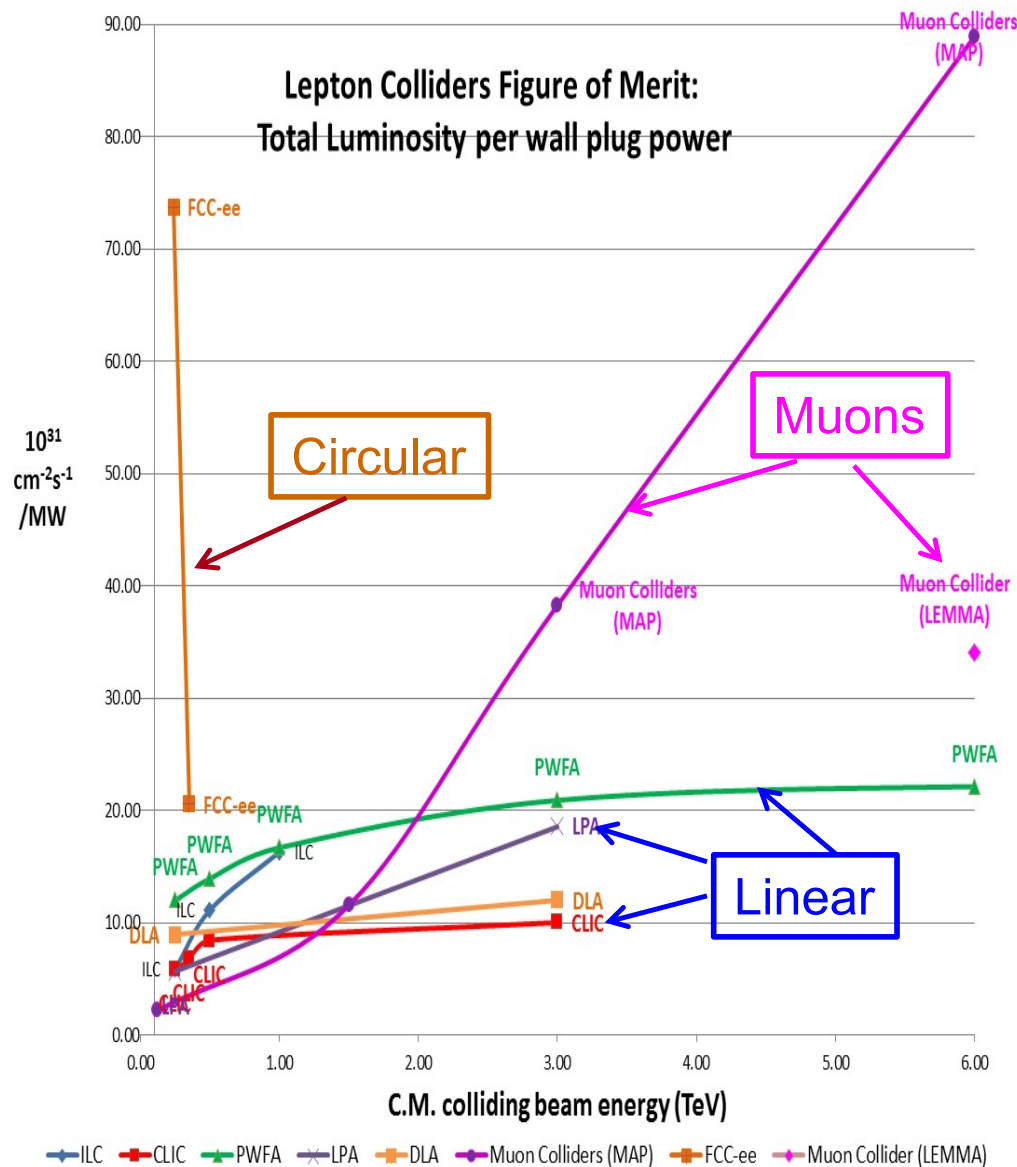


### Low EMittance Muon Accelerator (LEMMA):

$10^{11} \mu$  pairs/sec from  $e^+e^-$  interactions. The small production emittance allows lower overall charge in the collider rings – hence, lower backgrounds in a collider detector and a higher potential CoM energy due to neutrino radiation.



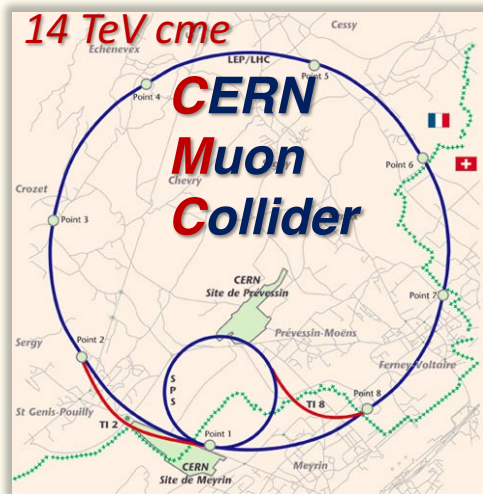
# Figure of merit: Luminosity per wall plug power



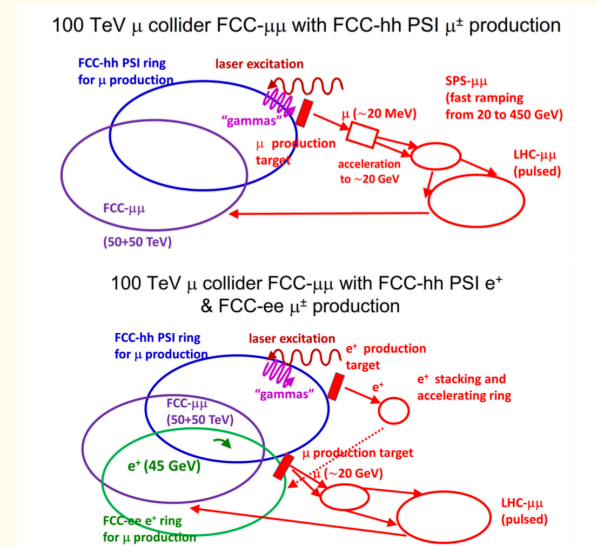


# LEMMA concept and MC prospects

- The LEMMA concept renewed the interest and extended the reach of Multi-TeV Muon Colliders
- Two interesting recent proposals:
  - **CERN Muon Collider @14 TeV** [V. Shiltzev and D. Neuffer, MOPMF072, IPAC18]
  - **LHC/FCC based MC** [F. Zimmermann, MOPMF065, IPAC18]



MOPMF072, IPAC18, V. Shiltzev, D. Neuffer



MOPMF065, IPAC18, F. Zimmermann

- In view of the European Strategy Update an international WG has been established last September 2017 on MC, to prepare a document for the ESU on this subject

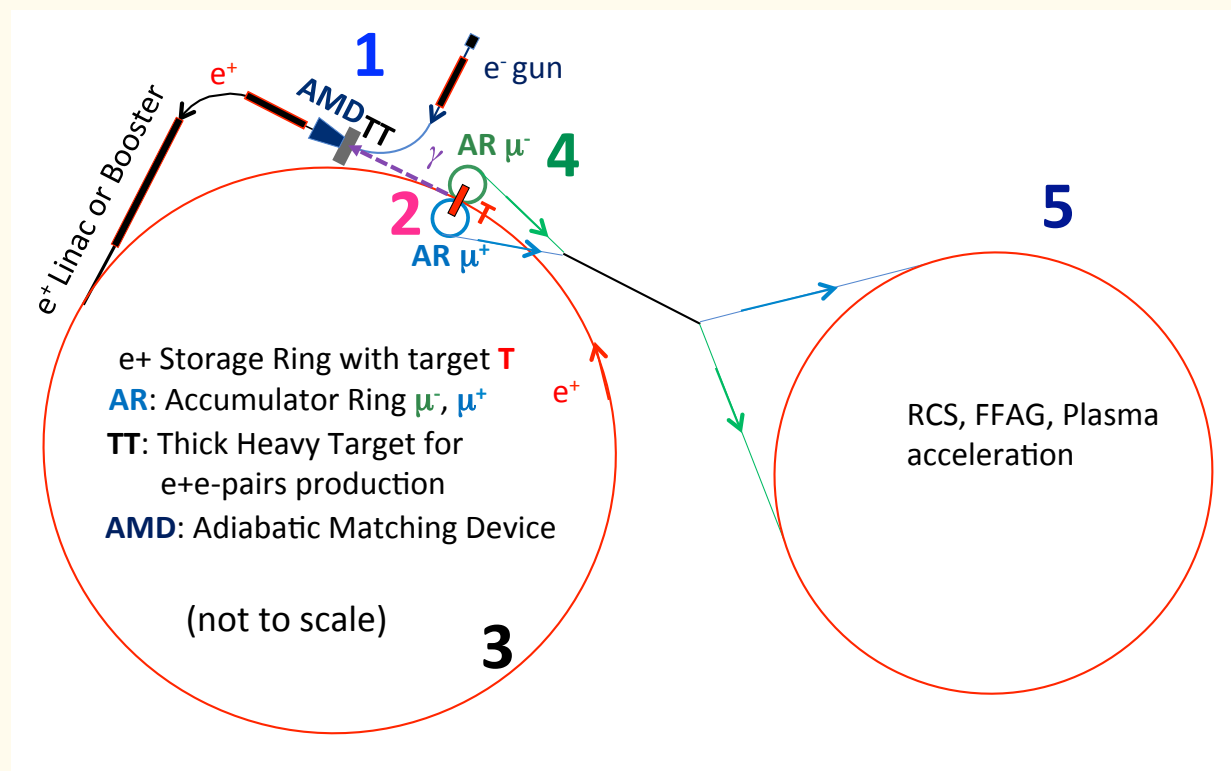
# On going activity on the LEMMA proposal

- Our goal is to define the potentiality of this concept for a multi-TeV MC:
  - in terms of luminosity and beam power
  - design the optics for the accelerator complex
  - identify and possibly start with the necessary key R&D
- Updates of our studies can be found in Refs.:
  - *“The future prospects of muon colliders and neutrino factories”*, M. Boscolo, J.P.Delahaye and M. Palmer, ArXiv: 1808.01858, 6 August 2018
  - *“Low emittance muon accelerator studies with production from positrons on target”*, Phys. Rev. Accel. and Beams 21, 061005 (June 2018)
  - *“Muon accumulator ring requirements for a low emittance muon collider from positrons on target”*, M. Boscolo et al., in Proc. IPAC18, MOPMF087 (May 2018)
  - *“Proposal of an experimental test at DAΦNE for the low emittance muon beam production from positrons on target”*, in Proc. IPAC18, MOPMF086 (May 2018)

# Key steps of the study

1. High rate  $e^+$  source
2.  $\mu^+/-$  production target (high peak energy density deposition (PEDD), power  $O(100 \text{ kW})$ )
3. Positron ring (low  $\varepsilon$  and high momentum acceptance)
4. Muon Accumulator Rings (high momentum acceptance)
5. Fast acceleration
6. Muon Collider

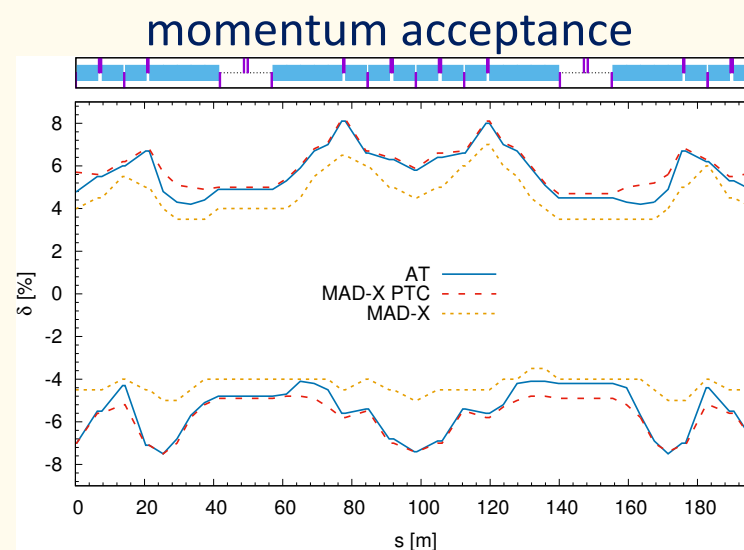
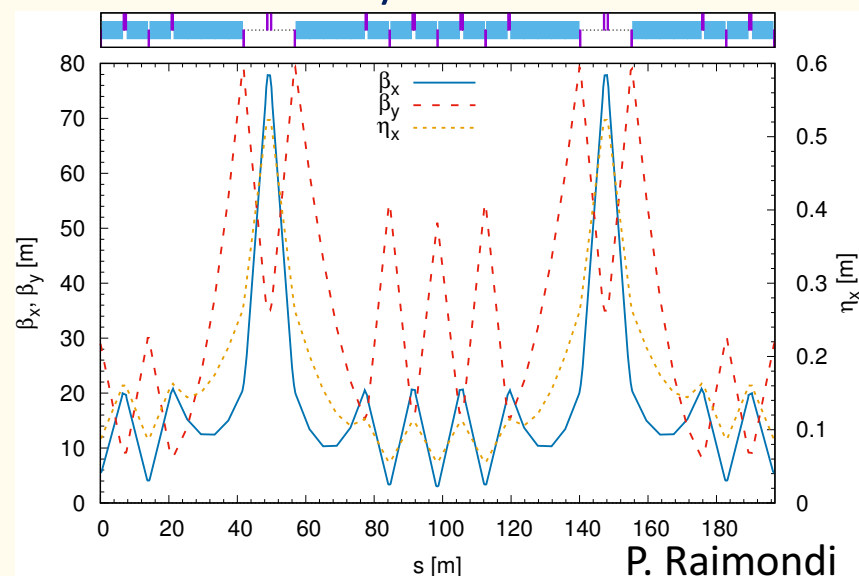
All require R&D study and present challenges



# Optics design positron ring

e+ ring parameter	unit	MAP option	LHC tunnel
Energy	GeV	45	45
Circumference	km	6.3	27
No.part./bunch	#	$3 \cdot 10^{11}$	
bunches	#	100	
e <sup>+</sup> bunch spacing = T <sub>rev</sub> (AR)	ns	200	
Beam current	mA	240	
Emittance	nm	6	0.7
U <sub>0</sub>	GeV	0.51	0.12
SR power	MW	120	29

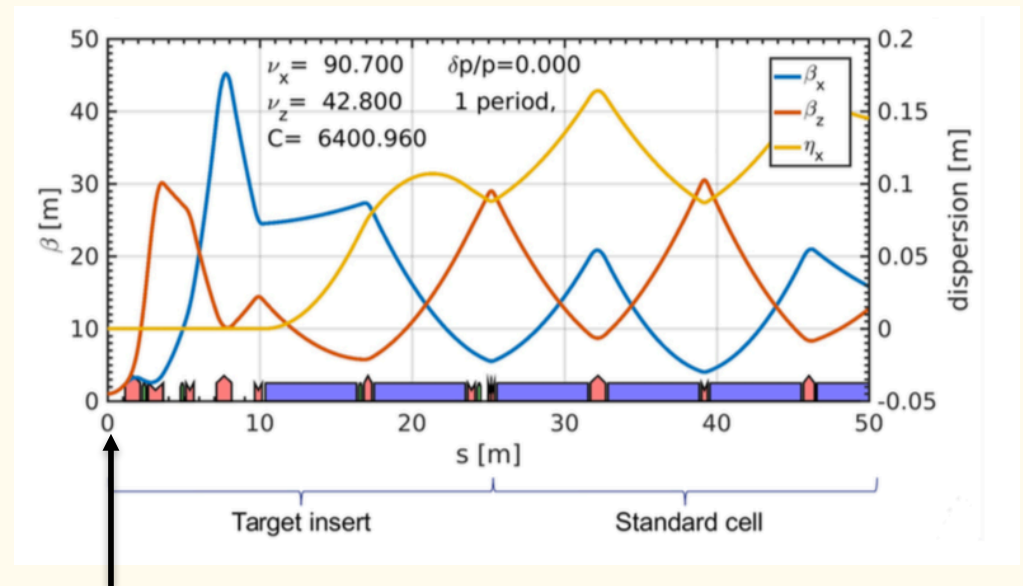
Cell based on the Hybrid Multi Bend Achromat



# Optics design positron ring

e+ ring parameter	unit	MAP option	LHC tunnel
Energy	GeV	45	45
Circumference	km	6.3	27
No.part./bunch	#	$3 \cdot 10^{11}$	
bunches	#	100	
e <sup>+</sup> bunch spacing = T <sub>rev</sub> (AR)	ns	200	
Beam current	mA	240	
Emittance	nm	6	0.7
U <sub>0</sub>	GeV	0.51	0.12
SR power	MW	120	29

## Target Insertion Region



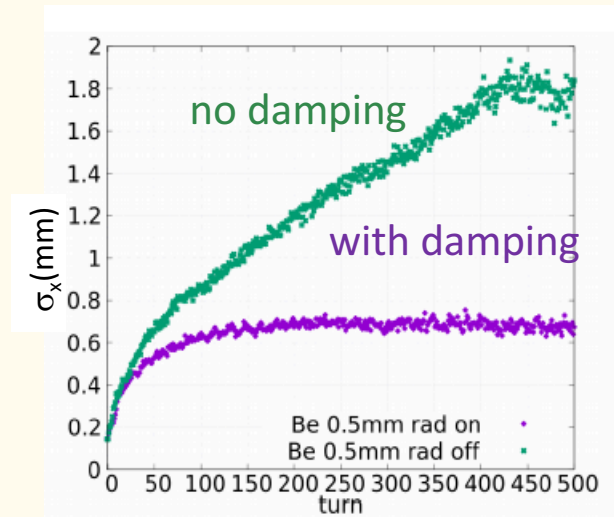
@target  $\left\{ \begin{array}{l} D_x \approx 0 \\ \text{low-}\beta \text{ } (\beta_{x,y} = 0.5 \text{ m}) \end{array} \right.$

# Multi-turn simulations

1. Initial 6D distribution from the equilibrium emittances
2. 6D  $e^+$  distribution tracking up to the target (AT and MAD-X PTC)
3. tracking through the target (with Geant4beamline and FLUKA and GEANT4)
4. back to tracking code

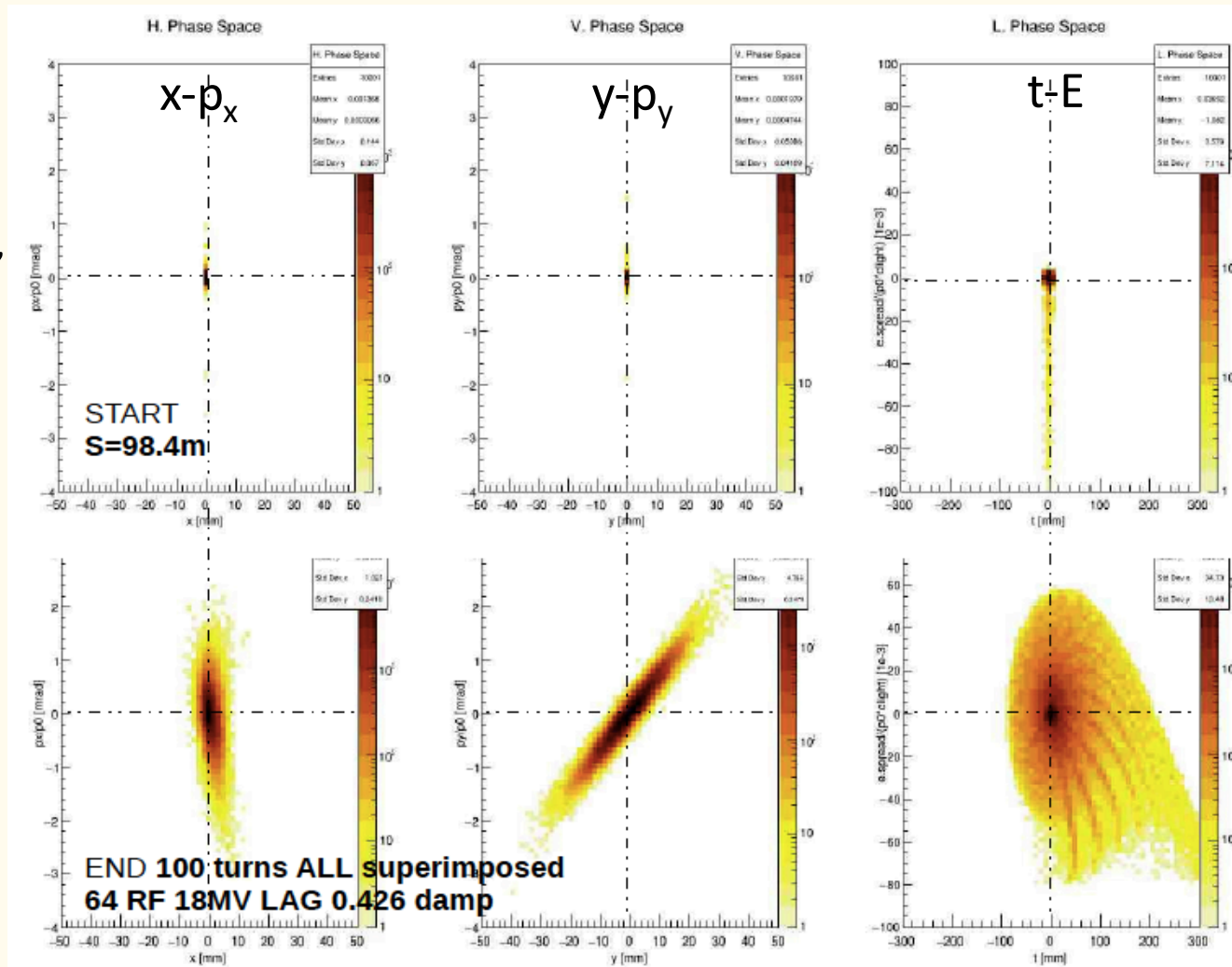
At each pass through the muon target the  $e^+$  beam

- gets an angular kick due to the **multiple Coulomb scattering**, so at each pass changes  $e^+$  beam divergence and size, resulting in an emittance increase.
- undergoes **bremsstrahlung energy loss**: to minimize the beam degradation due to this effect,  $D_x=0$  at target
- in addition there is natural radiation **damping** (it prevents an indefinite beam growth)



# $e^+$ ring with target: beam evolution in the 6D phase space

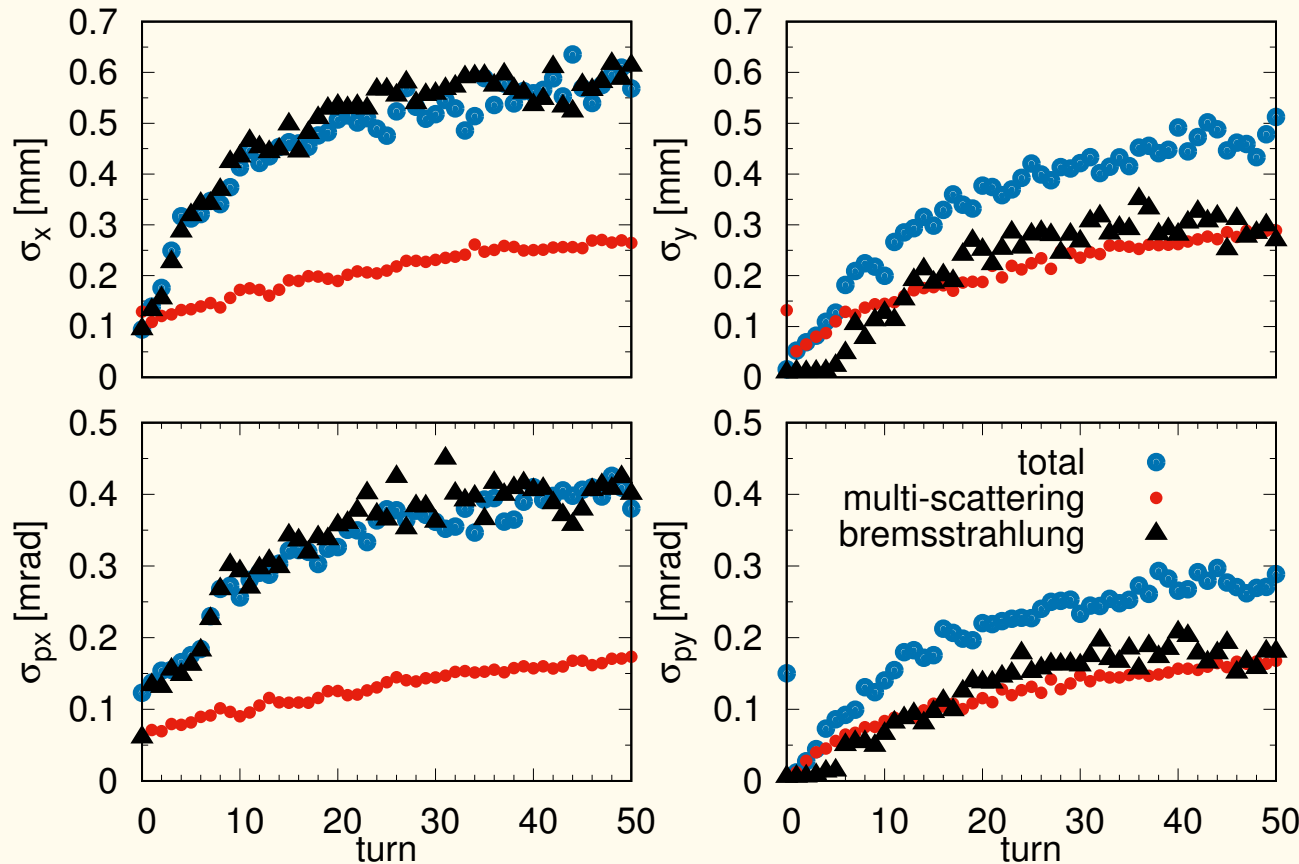
before target,  
starting point



MAD-X PTC & GEANT4 6-D tracking simulation of  
 $e^+$  beam with 3 mm Be target along the ring (not at IR center in this example)

# Evolution of e+ beam size and divergence

3mm Be Target (0.8% Xo) at center of IR



bremsstrahlung and multiple scattering artificially separated by considering alternatively effects in longitudinal (dominated by **bremsstrahlung**) and transverse (dominated by **multiple scattering**) phase space due to target; in **blue** the combination of both effects (realistic target)

Some bremsstrahlung contribution due to residual dispersion at target

multiple scattering contribution in line with expectation:  $\sigma_{MS} = \frac{1}{2} \sqrt{n_D} \sigma'_{MS} \beta$

one pass contribution due to the target:  $\sigma'_{MS} = 25 \mu\text{rad}$

$n_D$  number of damping turns

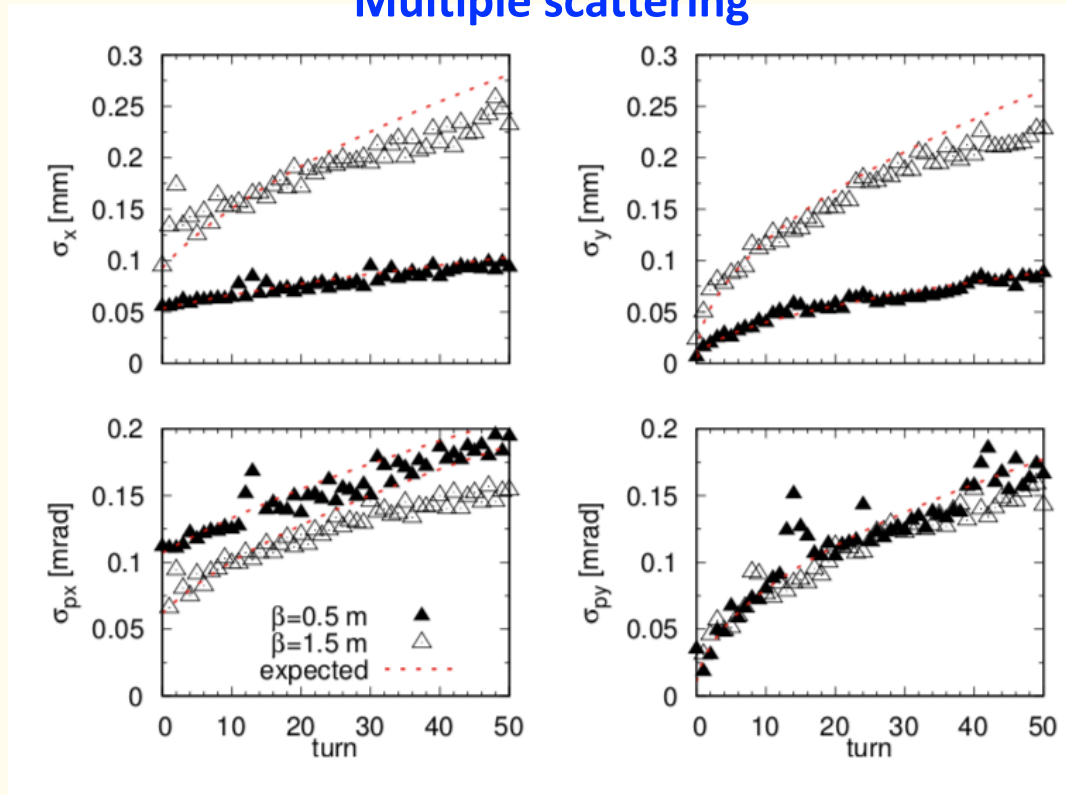


# Beam dynamics e<sup>+</sup> beam in ring-with-target

More details in: PR-AB 21, 061005 (2018)

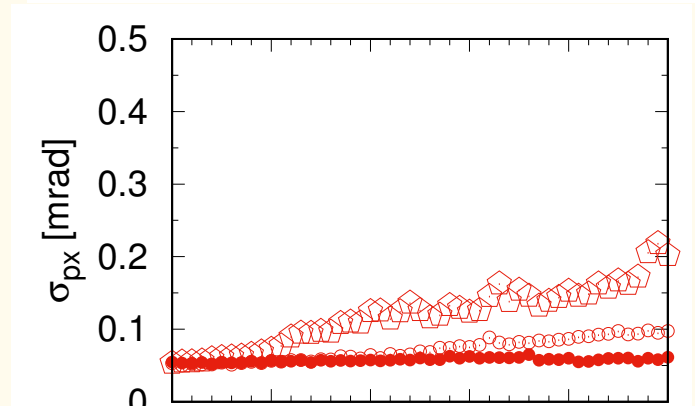
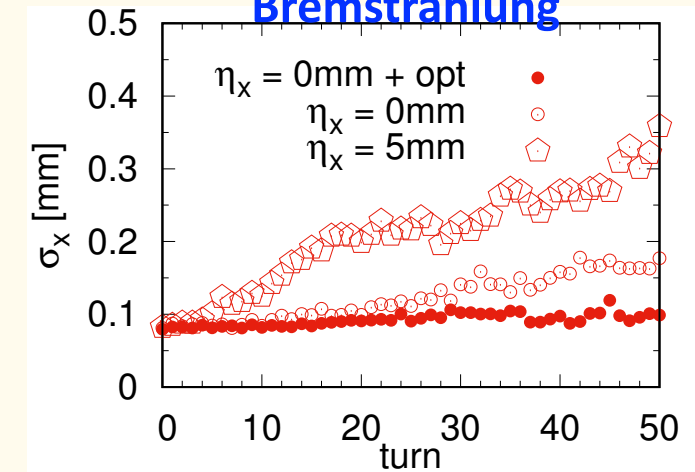
e<sup>+</sup> emittance growth controlled with proper  $\beta$  and D values @ target

## Multiple scattering



After 40 turns  $\sigma'_{MS} = 25 \mu\text{rad}$

## Bremstrahlung



@Target :

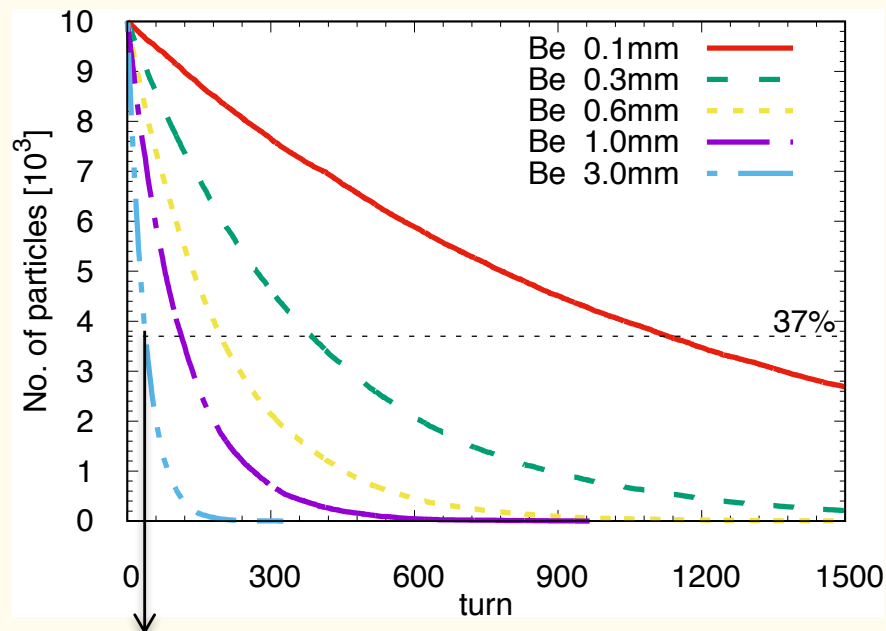
linear and non-linear terms  
of horizontal dispersion  $\eta_x = 0$

# Beam dynamics $e^+$ beam in ring-with-target

More details in:  
Arxiv. [1803.06696](https://arxiv.org/abs/1803.06696)

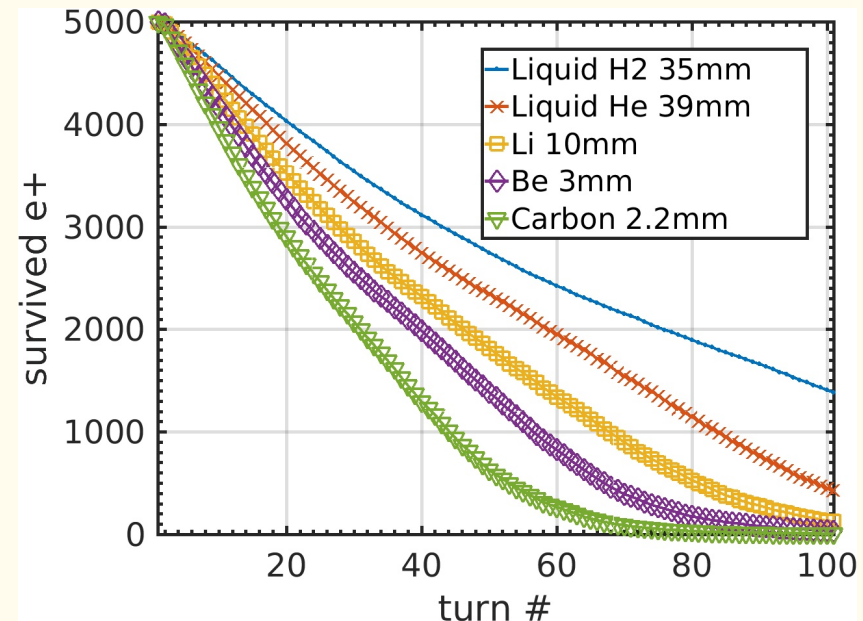
Particle tracking with: MADX/ PTC/GEANT4/FLUKA & Accelerator Toolbox/G4-Beamline

Lifetime  $\propto 1/\text{thickness}$  as expected



**Lifetime ~ 40 turns  
for Be 3 mm**

Lifetime determined by  
bremsstrahlung and  
momentum acceptance  
2-3%  $e^+$  losses in the first turn



Number of  $e^+$  vs turns for different target  
materials.  
Target thickness gives constant muon  
yield.

# Muon emittance contributions

$$\varepsilon(\mu) = \varepsilon(e^+) \oplus \varepsilon(\text{MS}) \oplus \varepsilon(\text{rad}) \oplus \varepsilon(\text{prod}) \oplus \varepsilon(\text{AR})$$

$\varepsilon(e^+)$  =  $e^+$  emittance

$\varepsilon(\text{MS})$  = multiple scattering contribution

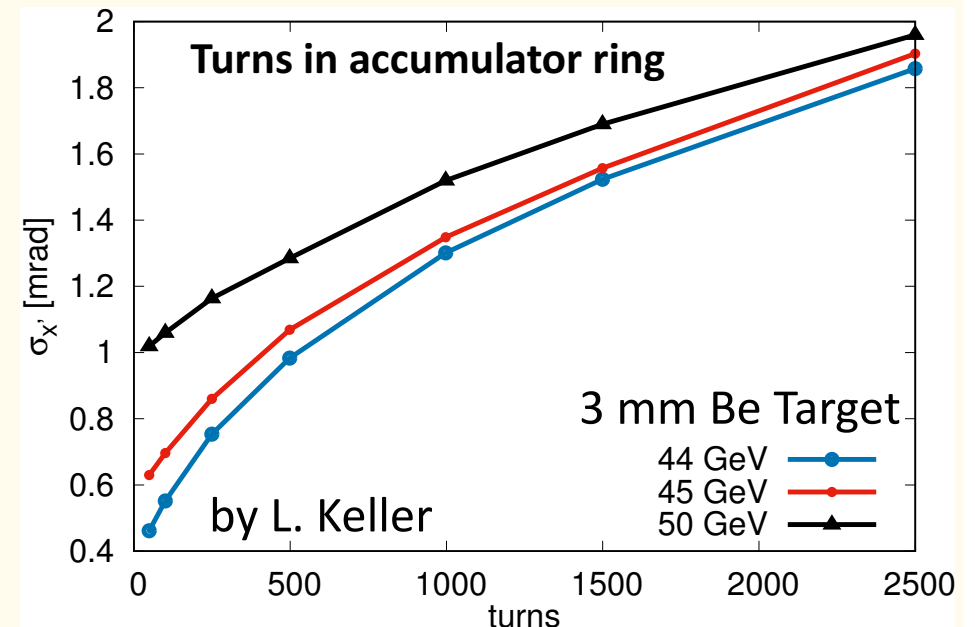
$\varepsilon(\text{rad})$  = energy loss (brem.) contribution

$\varepsilon(\text{prod})$  = muon production contribution

$\varepsilon(\text{AR})$  = accumulator ring contribution

**All these values need to be matched to minimize emittance growth due to beam filamentation.**

$\sigma_x$  and  $\sigma_{x'}$  and correlations of  $e^+$  and  $\mu$  beams have to be similar



muon  
production  
angle

Proc. of IPAC18, Vancouver, MOPMF087

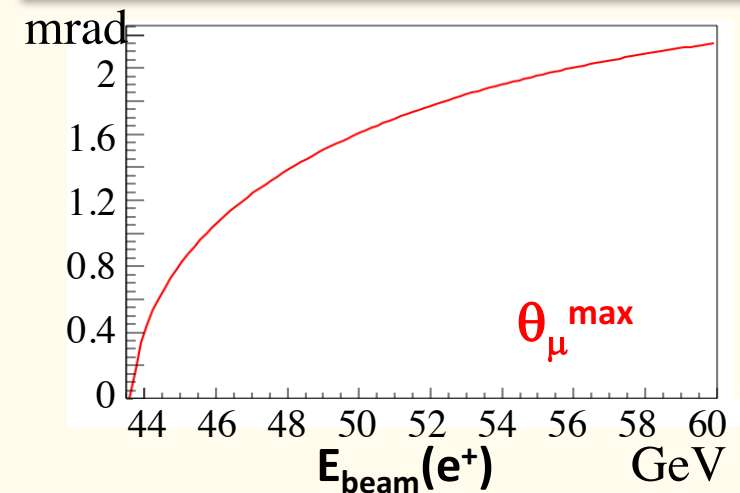
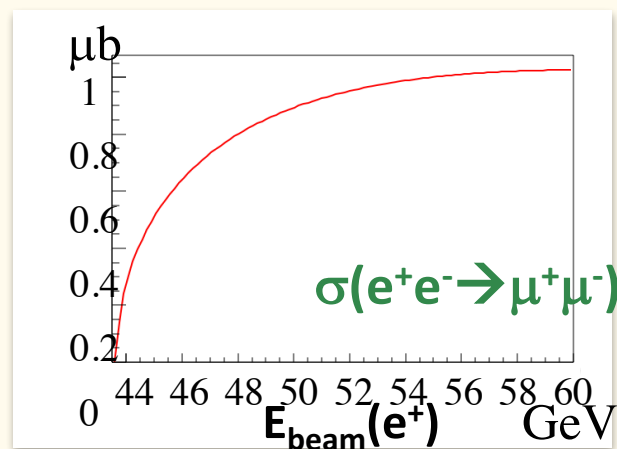
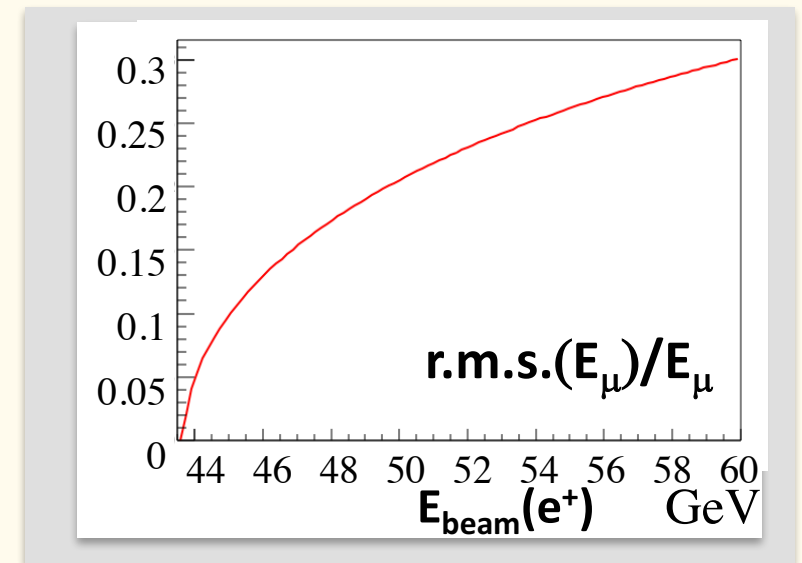
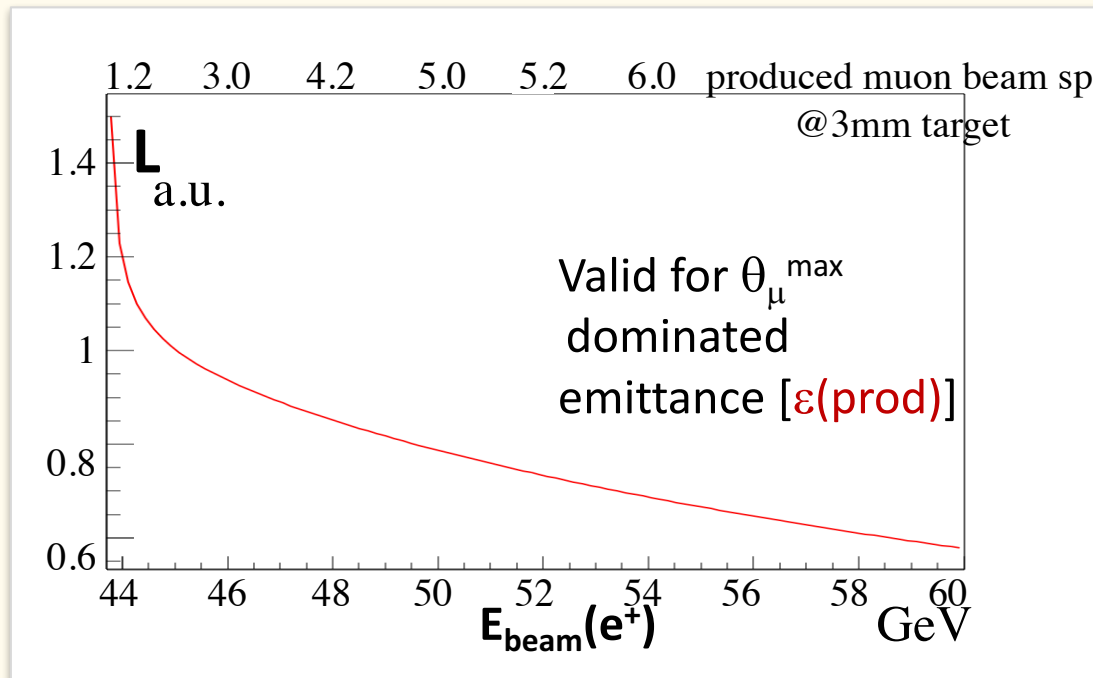
muon  
production  
angle + MS  
contribution

# Luminosity of $\mu^+\mu^-$ Collider vs $e^+$ beam energy

Optimal working point for  $\varepsilon(e^+) \cong \varepsilon(MS) \cong \varepsilon(\text{rad}) \cong \varepsilon(\text{prod}) \cong \varepsilon(\text{AR})$

and sustainable beam spot on target

$\varepsilon(\text{prod})$  and  $\mu$  intensity  $\propto$  positron beam energy:

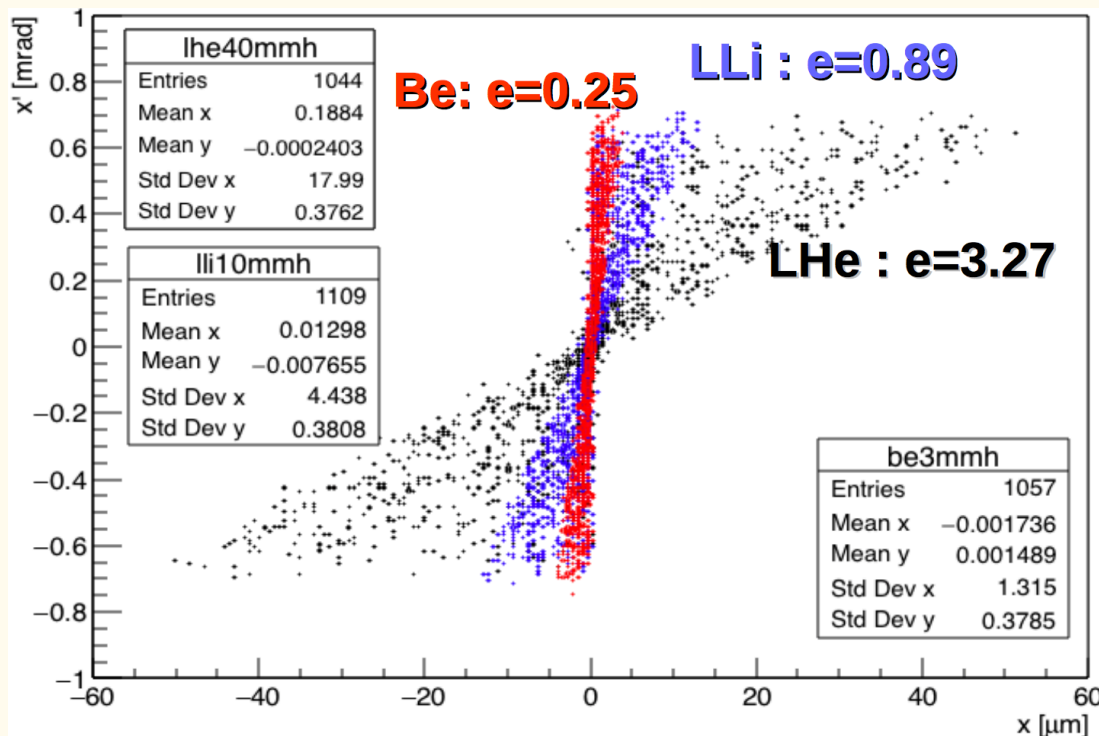


# Going to lighter targets for $\mu$ production

**Be** Beryllium

**LLi** Liquid Lithium, might be a good option (Proposed/tested for targets for n production)

**LHe** Liquid Helium



$e$  = muon emittance at production [ $10^{-9}$ m-rad]

$E(e^+)=45$  GeV

Look to light liquid targets to reduce problems  
of thermo-mechanical stresses

also test different material

- crystals in channeling better:  
 $\epsilon(MS)$ ,  $\epsilon(rad)$ ,  $\epsilon(prod)$  (also  
gain in lifetime)
- light liquid jet target better:  
 $\epsilon(MS)$ ,  $\epsilon(rad)$

also gain in lifetime &  
target power removal

# R&D for the muon production target

- This is the core topic of LEMMA feasibility.
- Thermo-mechanical stress is the main issue (very high Peak Energy Density Deposition )
- Engineering simulations and experimental tests will be required to find the optimal target material, considering mechanical stress and heat load resistance properties.
- We are considering now:
  - Beryllium seemed optimal from first MADX-/Geant-4 simulations
  - Carbon composites
  - Liquid Lithium
  - Hydrogen pellet
  - Crystals or more exotic targets

# Target: thermo-mechanical stresses considerations

Beam size as small as possible (matching various emittance contributions), but

- constraints for **power removal (200 kW)** and **temperature rise**
- to contrast the **temperature rise**  
**move target** (for free with liquid jet) and  
**e<sup>+</sup> beam bump** every 1 bunch muon accumulation

- **Solid target:** simpler and better wrt temperature rise

- Be, C

Be target: @HIRadMat safe operation with extracted beam from SPS, beam size 300  $\mu\text{m}$ ,  $N=1.7 \times 10^{11}$  p/bunch, up to 288 bunches in one shot [Kavin Ammigan 6<sup>th</sup> High Power Targetry Workshop]

- **Liquid target:** better wrt power removal

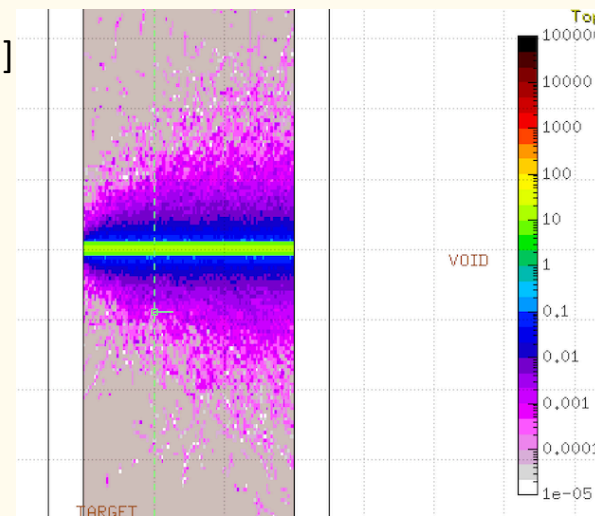
- Li, difficult to handle lighter materials, like H, He

- LLi jets examples from neutron production, Tokamak divertor

(200 kW beam power removal seems feasible) , minimum beam size to be understood

# Conventional options for $\mu$ target

- Aim at bunch ( $3 \times 10^{11}$   $e^+$ ) transverse size on the 10  $\mu\text{m}$  scale: rescaled from test at HiRadMat ( $5 \times 10^{13}$  p on 100  $\mu\text{m}$ ) with **Be-based** targets and **C-based** (HL-LHC) [F. Maciariello *et al.*, IPAC2016]
- No bunch pileup  $\longrightarrow$  **Fast rotating wheel** (20000 rpm)
- **Power removal by radiation cooling** (see for instance PSI muon beam upgrade project HiMB) [A. Knecht, NuFact17]
- Need detailed simulation of thermo-mechanical stresses dynamics
  - Start using **FLUKA + Ansys Autodyn** (collaboration with CERN EN-STI)
- **Experimental tests:**
  - **DAFNE** available from 2020



Alternative options like H pellet, crystals or more exotic targets are under consideration



# Positron sources: studies on the market

- Summary of  $e^+$  sources projects (all very aggressive):

In [F. Zimmermann, et al., '**POSITRON OPTIONS FOR THE LINAC-RING LHeC**', WEPPR076 Proceedings of IPAC2012, New Orleans, Louisiana, USA]

	SLC	CLIC	ILC	LHeC pulsed	LHeC ERL
$E$ [GeV]	1.19	2.86	4	140	60
$\gamma\epsilon_x$ [ $\mu\text{m}$ ]	30	0.66	10	100	50
$\gamma\epsilon_y$ [ $\mu\text{m}$ ]	2	0.02	0.04	100	50
$e^+[10^{14}\text{s}^{-1}]$	0.06	1.1	3.9	18	440

➤ This is a key issue to be studied

# Example of Positron Source for CLIC

[L.Rinolfi *et al.* NIM B **309** (2013)50-55]

The target represented on the figure is a conventional one.

It would be also possible to have an *hybrid positron source* using a crystal providing channeling radiation and an amorphous converter for photon conversion into  $e^+e^-$  pairs

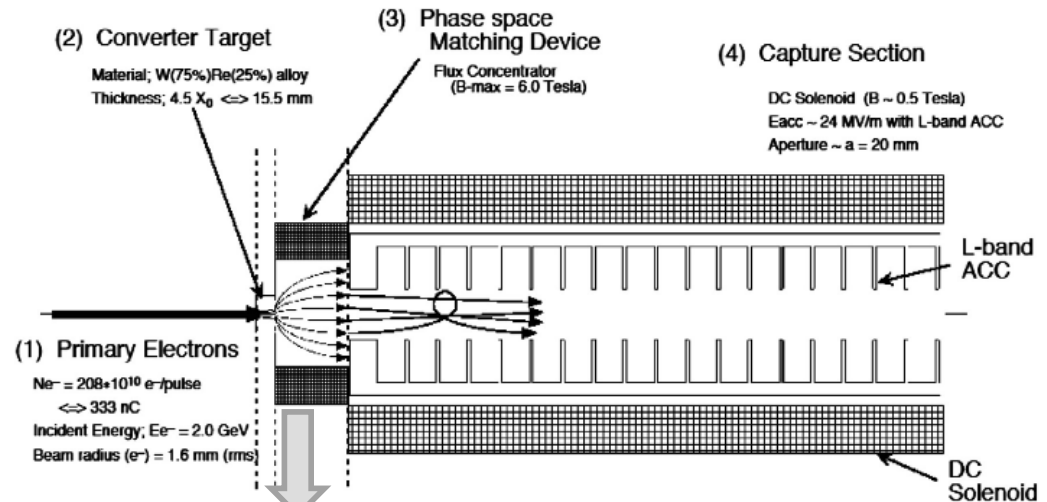
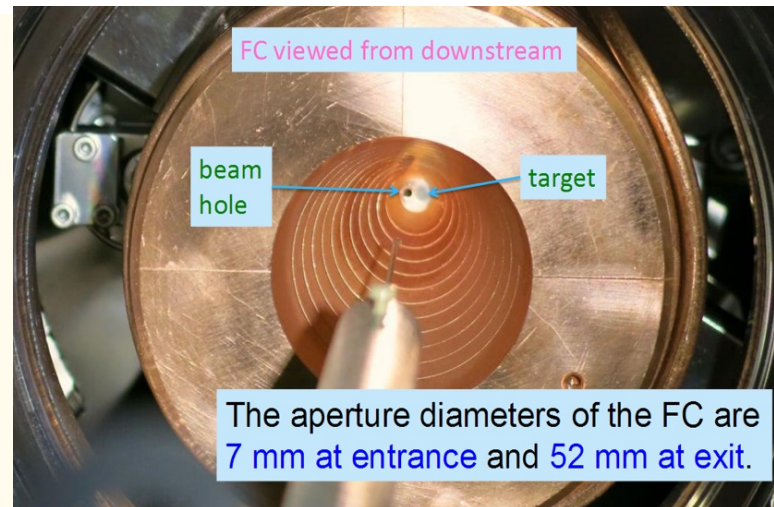
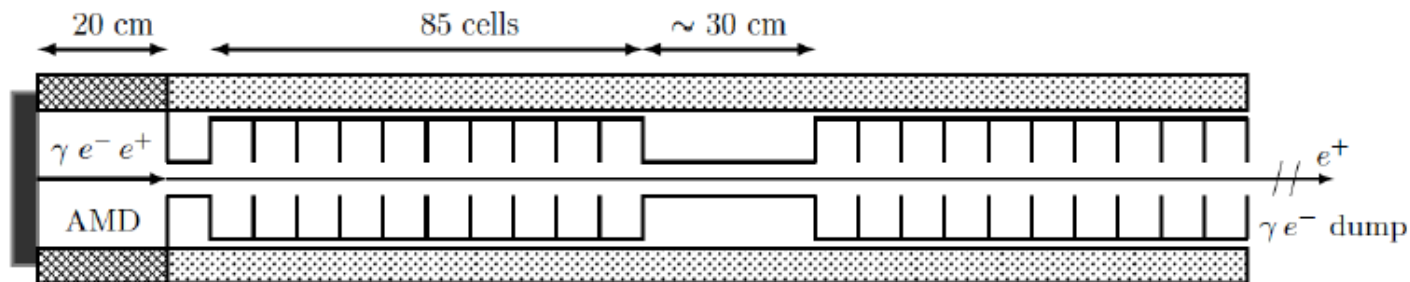


Fig. 2. Layout of the CLIC  $e^+$  source with a single target.

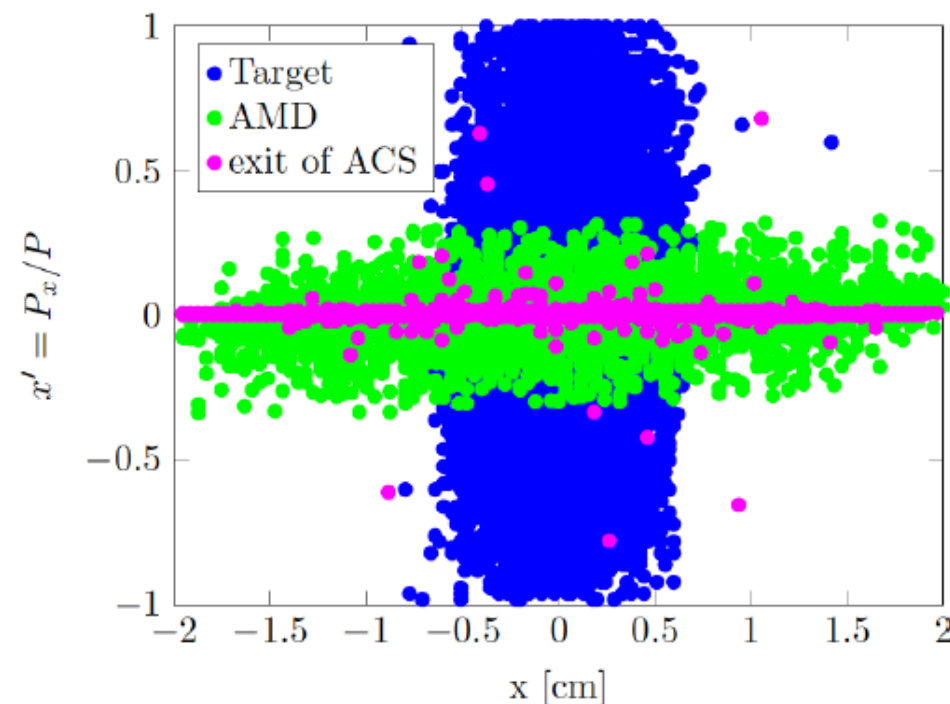


Flux concentrated used for the Adiabatic Matching Device  
(from T.Kamitani, LCWS-2014,Belgrade)

# FOCUSING SYSTEMS FOR POSITRON BEAMS



**Figure 4.7:** A fundamental scheme of the positron capture and primary acceleration - A capture section based on the AMD followed by a pre-injector linac is used to capture and accelerate the positron beam up to the  $\sim 200$  MeV.



# R&D on high rate positron source

- R&D on this topic can take advantage of significant synergies with future collider studies as FCC-ee, ILC and CLIC.
- The required intensity for LEMMA is strongly related to the beam lifetime, determined by the momentum acceptance and the target material.
- So, also optics and beam dynamics optimization is necessary.

$e^+$  production rates achieved (SLC) or needed

	S-KEKB	SLC	CLIC (3 TeV)	ILC (H)	FCC-ee (Z)	LEMMA(Be)	LEMMA(LH2)
$10^{14} e^+ / s$	0.025	0.06	1.1	2	0.05	100	40



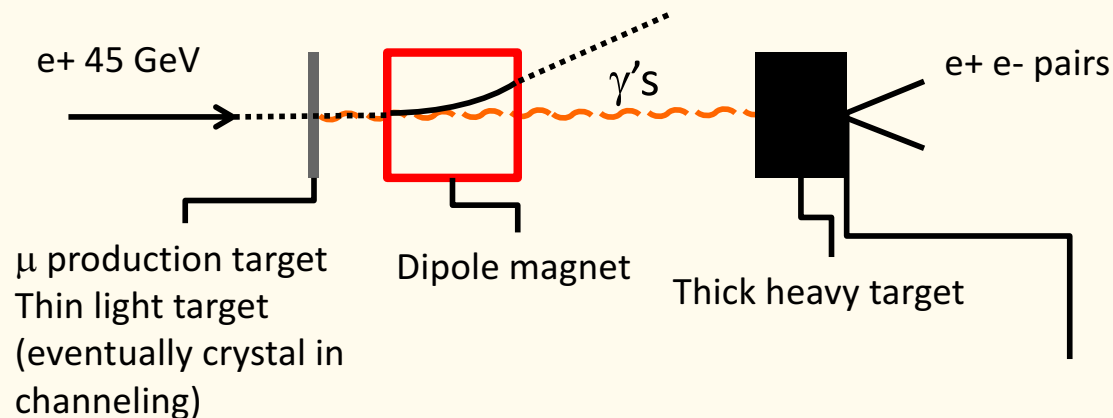
Present: 3 mm Be, 40 turns lifetime(DP/P<6%),  $\Delta N/N=2.5\%$ , P= 247 MW  
35 mm LH2, 100 turns lifetime(DP/P<6%),  $\Delta N/N=1\%$ , P= 98 MW

Goal: 3 mm Be, 240 turns lifetime(DP/P<25%),  $\Delta N/N=0.4\%$ , P=39 MW  
35 mm LH2, 625 turns lifetime(DP/P<25%),  $\Delta N/N=0.1\%$ , P= 16 MW

# R&D on high rate positron source

## Embedded e<sup>+</sup> source to relax e<sup>+</sup> source requirement

Positron source extending the target complex  
Possibility to use the  $\gamma$ 's from the  $\mu$  production target to produce e<sup>+</sup>



About 0.6 new e<sup>+</sup> produced per e<sup>+</sup> on thin target

Required collection efficiency feasible with standard design

not yet found a system able to transform the temporal structure of the produced positrons to one that is compatible with the requirement of a standard positron injection chain

# R&D on Fast Acceleration for LEMMA

- Muon beams must be accelerated to high energy in a very short period of time to account for their short lifetime.
- Synchrotron radiation is not a limiting factor in accelerating muons at the TeV-scale, so multi-pass acceleration is preferred for cost considerations.
- LEMMA scheme utilizes a **natural cycle time of 2.2 KHz and cannot be matched to** the slower ramp rate of the MAP hybrid **Rapid Cycling Synchrotron**.
- For LEMMA two acceleration options to study are:
  - the Recirculating Linear Accelerator (**RLA**)
  - fixed-field alternating gradient (**FFAG**) machines with large energy acceptance
- Also accelerator technologies developed for the e<sup>+</sup>e<sup>-</sup> linear collider could be of benefit. Muon beams with low emittance and low current allow the use of novel acceleration technologies like X-band cavities

# Muon collider at 6 TeV com energy

Values considered for this table:

- $\mu^+\mu^-$  rate =  $0.9 \cdot 10^{11}$  Hz
- $\varepsilon_N = 40$  nm (as ultimate goal)
- 3 mm Beryllium target

Comparison with MAP:

muon source	Rate $\mu/s$	$\varepsilon_{norm}$ $\mu m$
MAP	$10^{13}$	25
LEMMA	$0.9 \times 10^{11}$	0.04

Same L thanks to lower  $\beta^*$   
(nanobeam scheme)

no lattice for the muon collider yet

This table summarizes the goals of  
the LEMMA design study

Parameter	unit	LEMMA-6 TeV
Beam energy	Tev	3
Luminosity	$cm^{-2}s^{-1}$	$5.1 \times 10^{34}$
Circumference	km	6
Bending field	T	15
N particles/bunch	#	$6 \times 10^9$
N bunches	#	1
Beam current	mA	0.048
Emittance x,y (geo)	m-rad	$1.4 \times 10^{-12}$
$\beta_{x,y}$ @IP	mm	0.2
$\sigma_{x,y}$ @IP	m	$1.7 \times 10^{-8}$
$\sigma_{x',y'}$ @IP	rad	$8.4 \times 10^{-5}$
Bunch length	mm	0.1
Turns before decay	#	3114
muon lifetime	ms	60

# Comment on the parameters table

- **Low Emittance:** is the core of LEMMA idea, the greatest benefit of the positron driven source. The ultimate value has to be determined by R&D studies, we know that it will be given by the convolution of different contributions. Our goal is to reduce multiple scattering to a negligible value and have the best possible matching at target [with 3 mm Be target the multiple scattering contributes for a factor 15 in emittance increase]
- **Bunch intensity  $6 \times 10^9$**  : a muon bunch charge of  $4.5 \times 10^7$  is provided by the AR, an enhancement by a factor 120 can be obtained by a combination scheme either in the longitudinal [D. Schulte] or in the transverse [P.Raimondi] plane. Feasibility needs to be studied, also to verify impact on emittance. Alternatively at very high energy use SR damping
- **$\beta^* = 0.2$  mm:** aim is nano-beam scheme, final focus lattice not designed yet high field quads have to be used.



# Experimental Tests

# Test @CERN

## Experiments in H4:

45 GeV  $e^+$  on target, beam spot 2 cm, mrad divergence

**High intensity** (up to  $5 \times 10^6$   $e^+$ /spill) with 6 cm Be target (spill  $\sim 15$ s)  
goal: measure muon production rate and muons kinematic properties

### Low intensity

measure beam degradation (emittance energy spectrum)

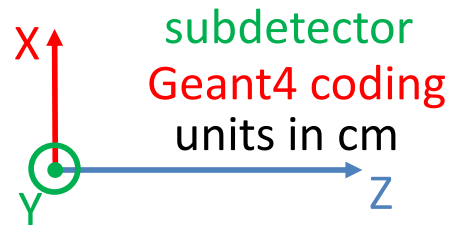
measure produced photons flux and spectrum

- 3 week assigned 2017/2018

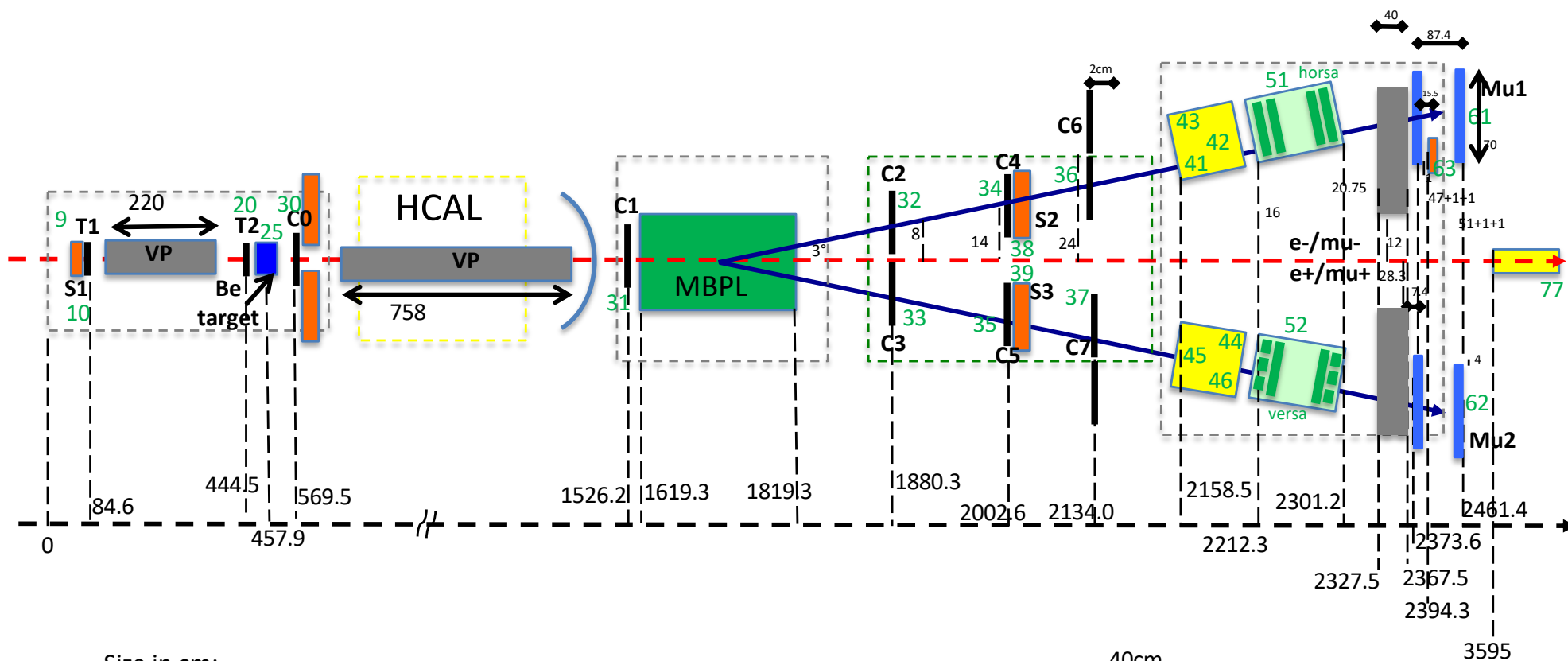
Priority to High intensity (had 2 days at  $\approx 10^6$   $e^+$  /spill)

- **2018 data taking**

- 3 positron beam energy (45 GeV, 46.5 GeV, 49 GeV)
- 2 different targets (Be S-200-F H and C-Mo)
- Collected few 1000  $\mu^+ \mu^-$  events



Last update: 20-aug-2018 v. 20



Size in cm:

T1-2: 1.9x1.9

C0-1,4-5: 9.3x9.3

C2-3: 8x8

C6-7: 18x18

**FINAL FOR 2018a TB!!**

40cm  
11.5\*3cm  
lead-glass  
(3 blocks)

86.86cm  
30cm  
quartz  
cherenkov

Post Geo

# Test at DAΦNE

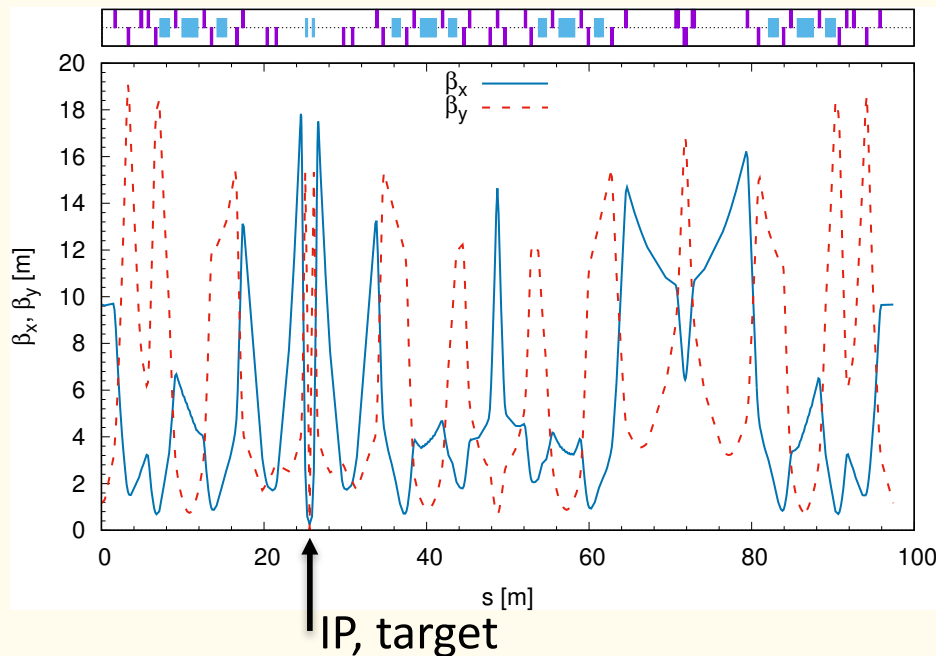
- **Test of the ring-plus-target scheme:**
  - **beam dynamics**
  - **target heat load and thermo-mechanical stress**

## GOAL:

- Benchmark simulations with experimental data to validate LEMMA studies.
- Measurements on targets: various materials and thicknesses can be envisaged.
  - as validation for LEMMA studies
  - interesting in the test itself

# Test at DAΦNE

- The SIDDHARTA-2 run will end on 2019
- Test proposed after this run
- The target is at the IP:
  - To minimize modifications of the existing configuration
  - low- $\beta$  and  $D_x=0$  is needed
- First studies with the SIDDHARTA optics and target placed at the IP.
- Possible different locations for the target can be studied



SIDDHARTA 2008 optics

$$\beta_x^* = 26\text{cm}; \beta_y^* = 0.9\text{cm}$$

$$\sigma_x^* = 0.27\text{mm}; \sigma_y^* = 4.4\mu\text{m}$$

$$\varepsilon_x = 0.28\mu\text{m}$$

# Goals of the Test at DAFNE

- Beam dynamics studies of the ring-plus-target scheme:
  - transverse beam size
  - current
  - lifetime
- Measurements on target:
  - temperature (heat load)
  - thermo—mechanical stress

Table 8: DAFNE parameters for the test with thin target at IP.

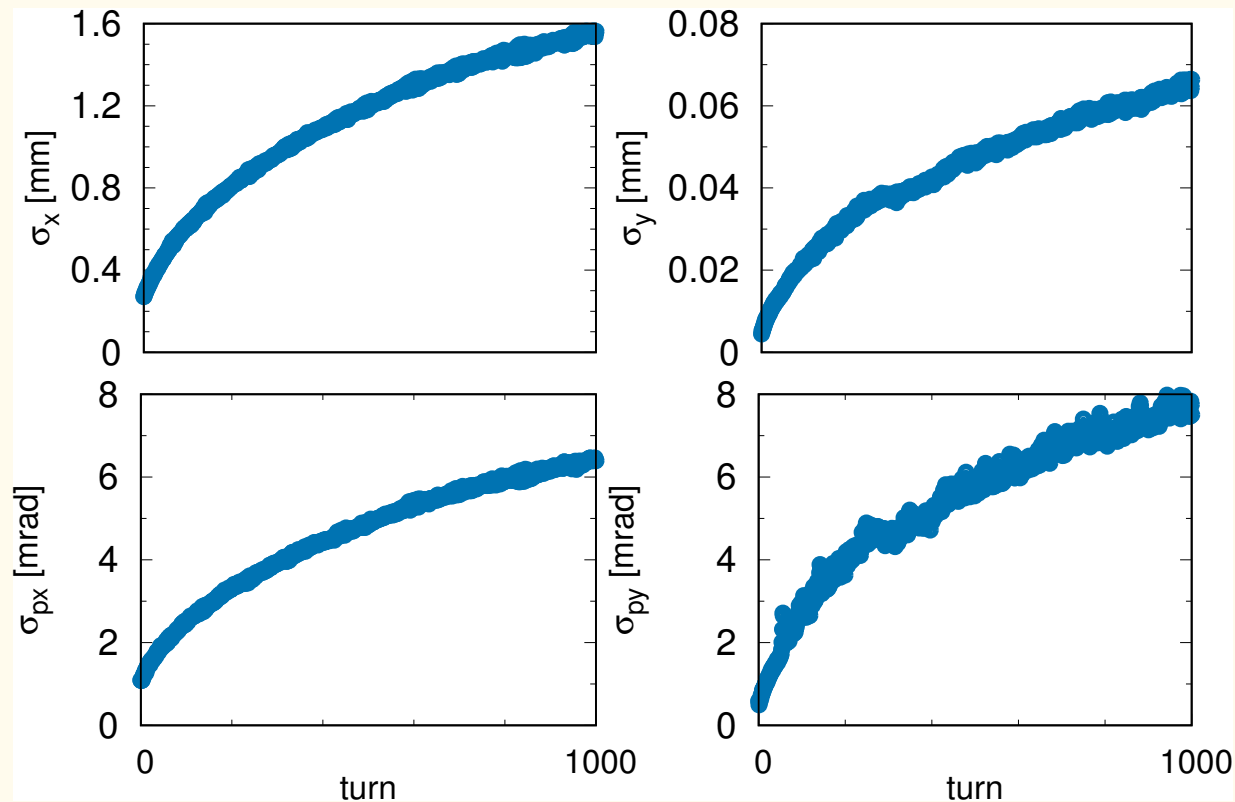
Parameter	Units	
Energy	GeV	0.51
Circumference	m	97.422
Coupling(full current)	%	1
Emittance x	m	$0.28 \times 10^{-6}$
Emittance y	m	$0.21 \times 10^{-8}$
Bunch length	mm	15
Beam current	mA	5
Number of bunches	#	1
RF frequency	MHz	368.366
RF voltage	kV	150
N. particles/bunch	#	$1 \times 10^{10}$
Horizontal Transverse damping time	ms/turns	42 / 120000
Vertical Transverse damping time	ms/turns	37 / 110000
Longitudinal damping time	ms/turns	17.5 / 57000
Energy loss/turn	keV	9
Momentum compaction		$1.9 \times 10^{-2}$
RF acceptance	%	$\pm 1$

Given the limited energy acceptance of the ring ( $\sim 1\%$ ), we plan to insert light targets (Be, C) with thickness in the range 10-100 $\mu\text{m}$ .

Crystal targets can be foreseen too, modified G4 tool needed for the simulation

# Evolution of e+ beam size and divergence

Beam evolution in the ring with 50 $\mu$ m Be target at IP

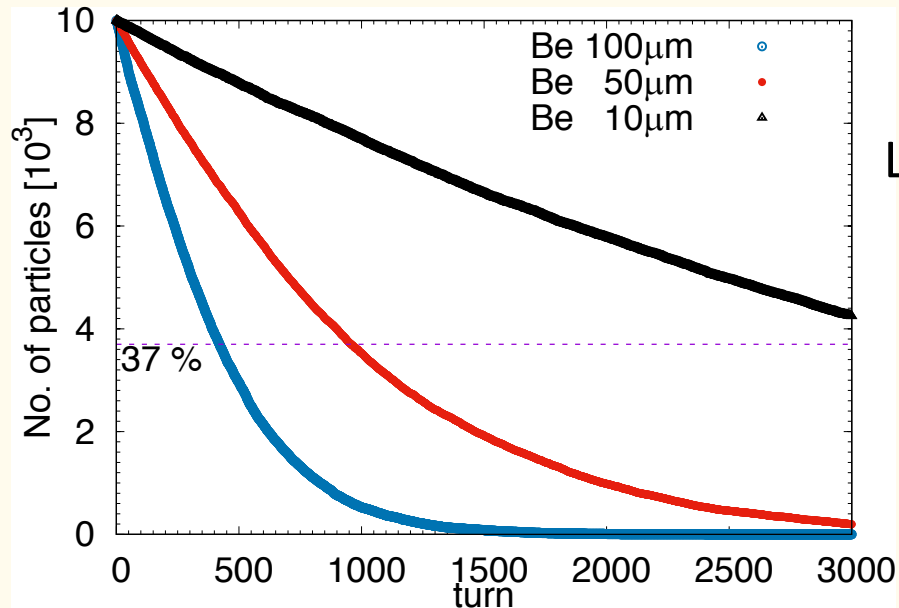


first turn, before target

$$\sigma_x^* = 0.27 \text{ mm}$$

$$\sigma_y^* = 4.4 \mu\text{m}$$

# e+ lifetime with Be target



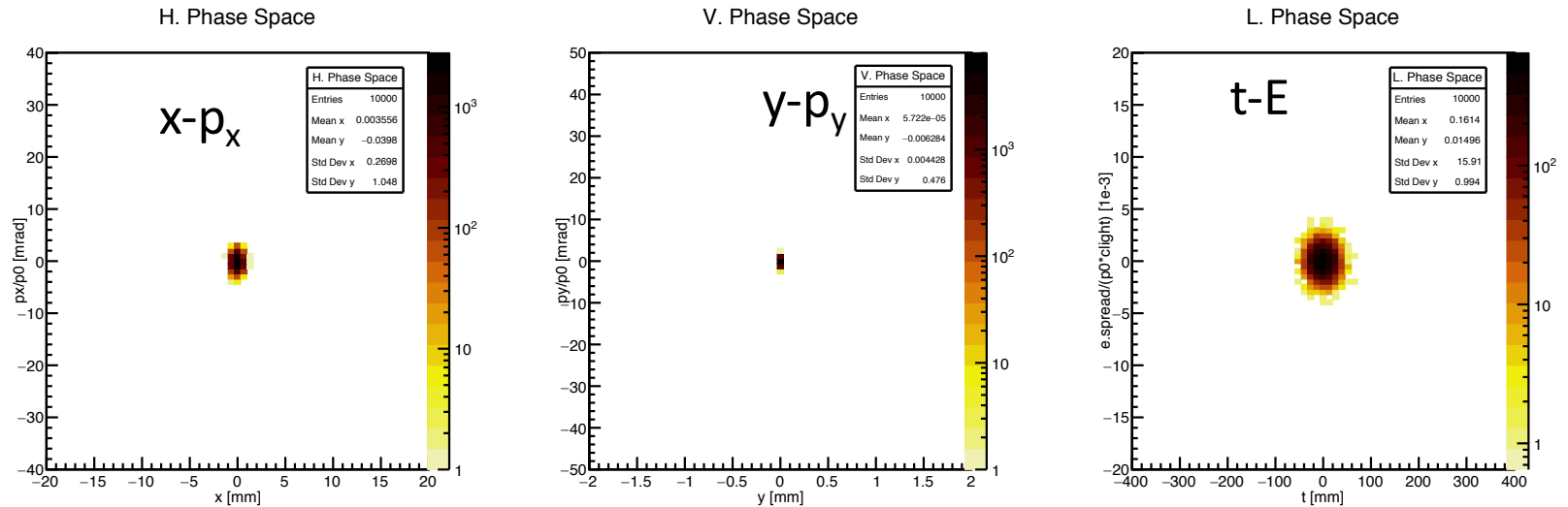
Lifetime with  $\sim 3500$  turns for 10  $\mu\text{m}$  Be target  
as short as 1.6 ms

- Beam will not be stored
- Injection in single bunch mode
- turn-by-turn beam size and charge measurement

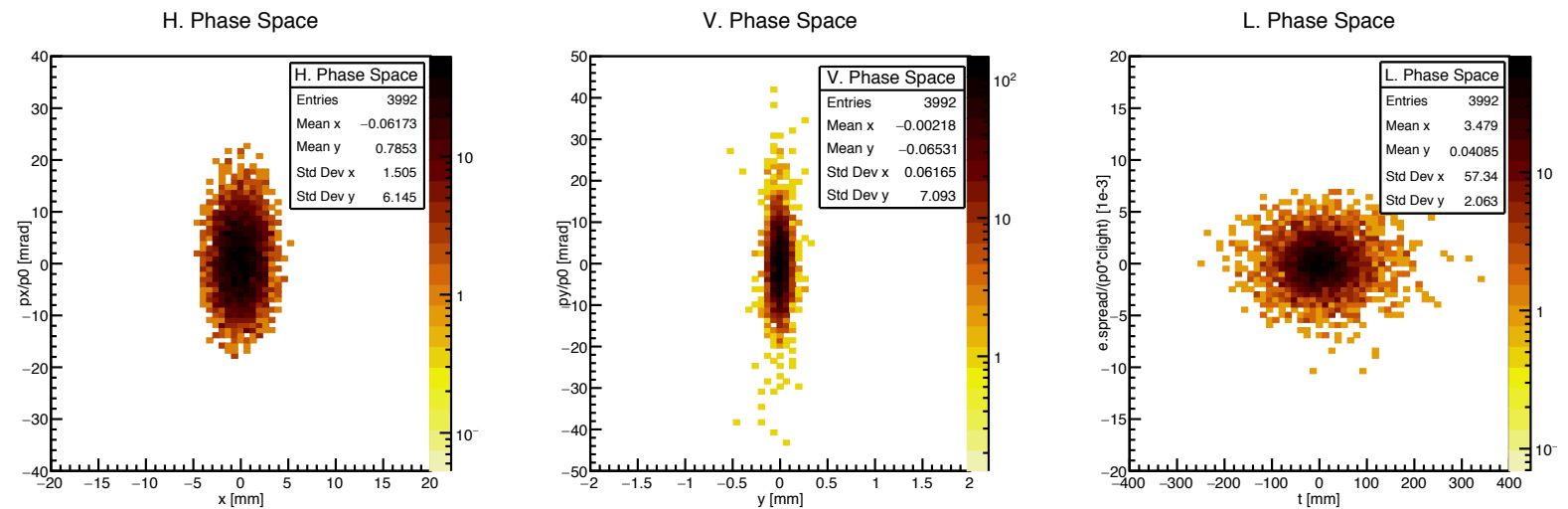


# DAFNE $e^+$ ring with 50 $\mu\text{m}$ Be target: beam evolution in the 6D phase space

before target,  
starting point



after 900 turns



MAD-X PTC & GEANT4 6-D tracking simulation

M. Boscolo, MAC, LNGS, 10



# Diagnostics for the test at DAFNE

## beam characterization after interaction with target:

- additional beam diagnostic to be developed:
  - turn by turn charge measurement (lifetime)
    - ✓ existing diagnostic already used for stored current measurement
    - ✓ need software and timing reconfiguration
  - turn by turn beam size
    - ✓ beam imaging with synchrotron radiation
    - ✓ DAFNE CCD gated camera provides gating capabilities required to measure average beam size at each turn.
    - ✓ software modification and dedicated optics installation required.

# Year of the Strategy Input

Observation: Existing SPS and LHC rings give long-term perspective to pursuit of LEMMA scheme

- LHC tunnel ideal to house 45 GeV positron ring
- SPS requires much more installed voltage and power
- SPS tunnel can house 3+3 TeV muon collider
- LHC tunnel can house 7+7 or 14+14 TeV muon collider
- LEP3 collider in LHC tunnel is consistent with doing muon production studies, spot on for Z production

Thinking strategy  
L. Evans, S. Stapnes,  
D. Schulte

Considered phased approach:

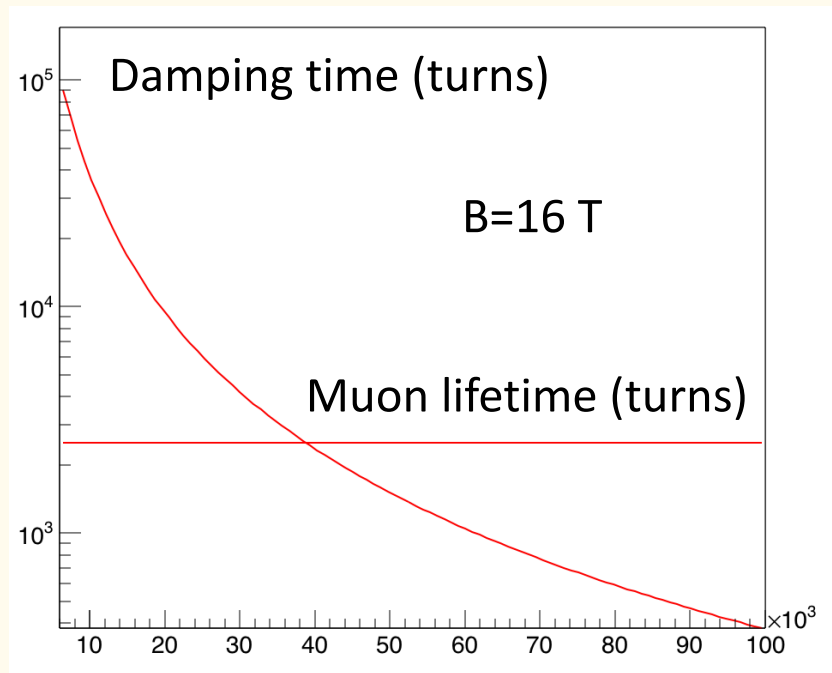
- Phase 1: eSPS would be entry point for all options
- Phase 2: LEP3 or CLIC (use to test and develop muon production)
- Phase 3: Muon collider in SPS or LHC tunnel
- Allows to develop all technologies and wait for physics input to define energy scales and choices



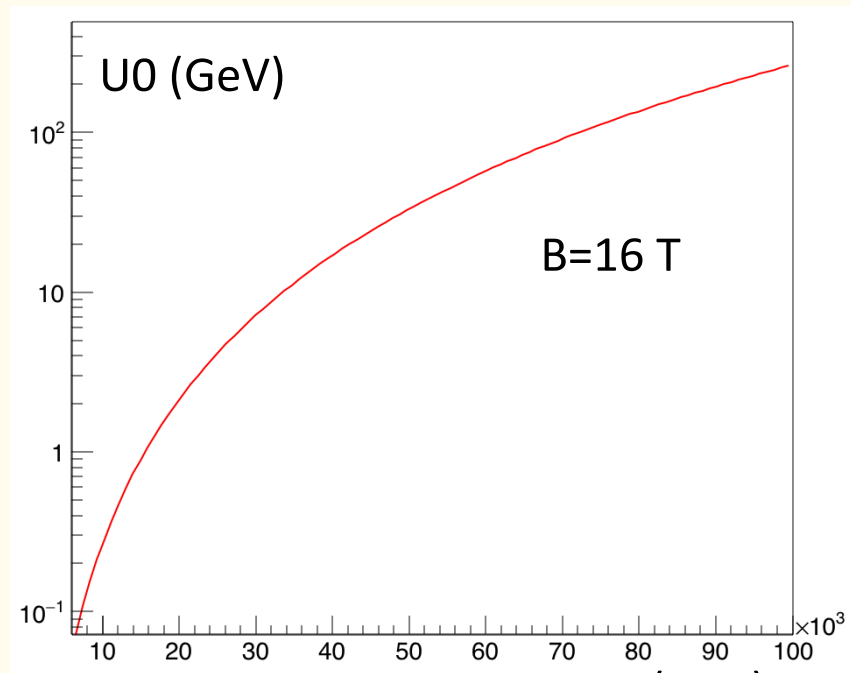
# Conclusion

- LEMMA is a novel concept for muon production, that renewed the interest and extended the reach of Multi-TeV Muon Colliders
- Key topics for the LEMMA feasibility validation:
  - **Positron ring-with-target: low emittance and high momentum acceptance**
  - **Muon Accumulator Rings: compact, isochronous and high  $(\Delta p/p)_{\text{accept}}$**
  - **Muon production target: extreme Peak Energy Density Deposition**
  - **High positron source rate**
  - **Fast acceleration**
  - **Final focus at MC**
- Preliminary studies pioneered by the INFN-LNF group are promising, progresses require to continue the design study of the accelerator complex.
- Experimental tests at DAFNE&CERN-NA for validation of some fundamental topics LEMMA are fundamental opportunities.

# SR and damping in $\mu$ collider

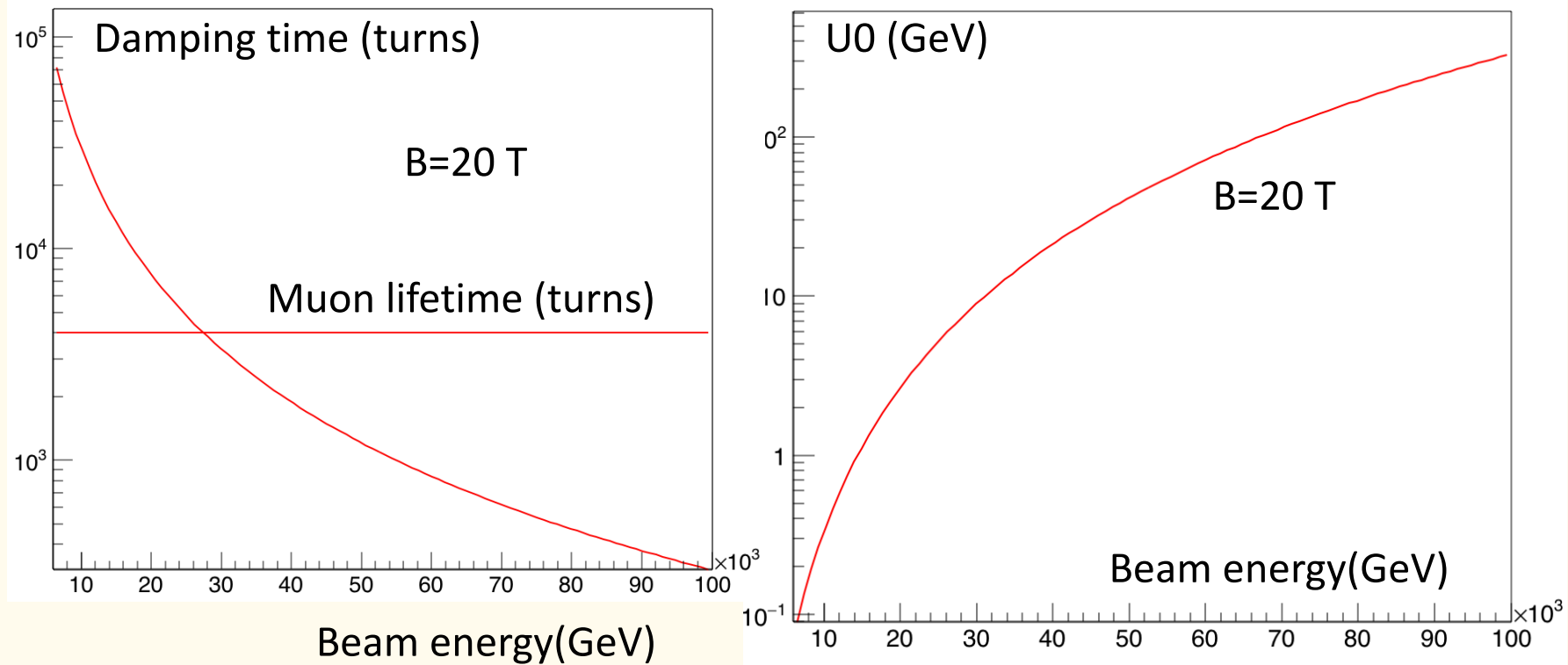


Beam energy(GeV)



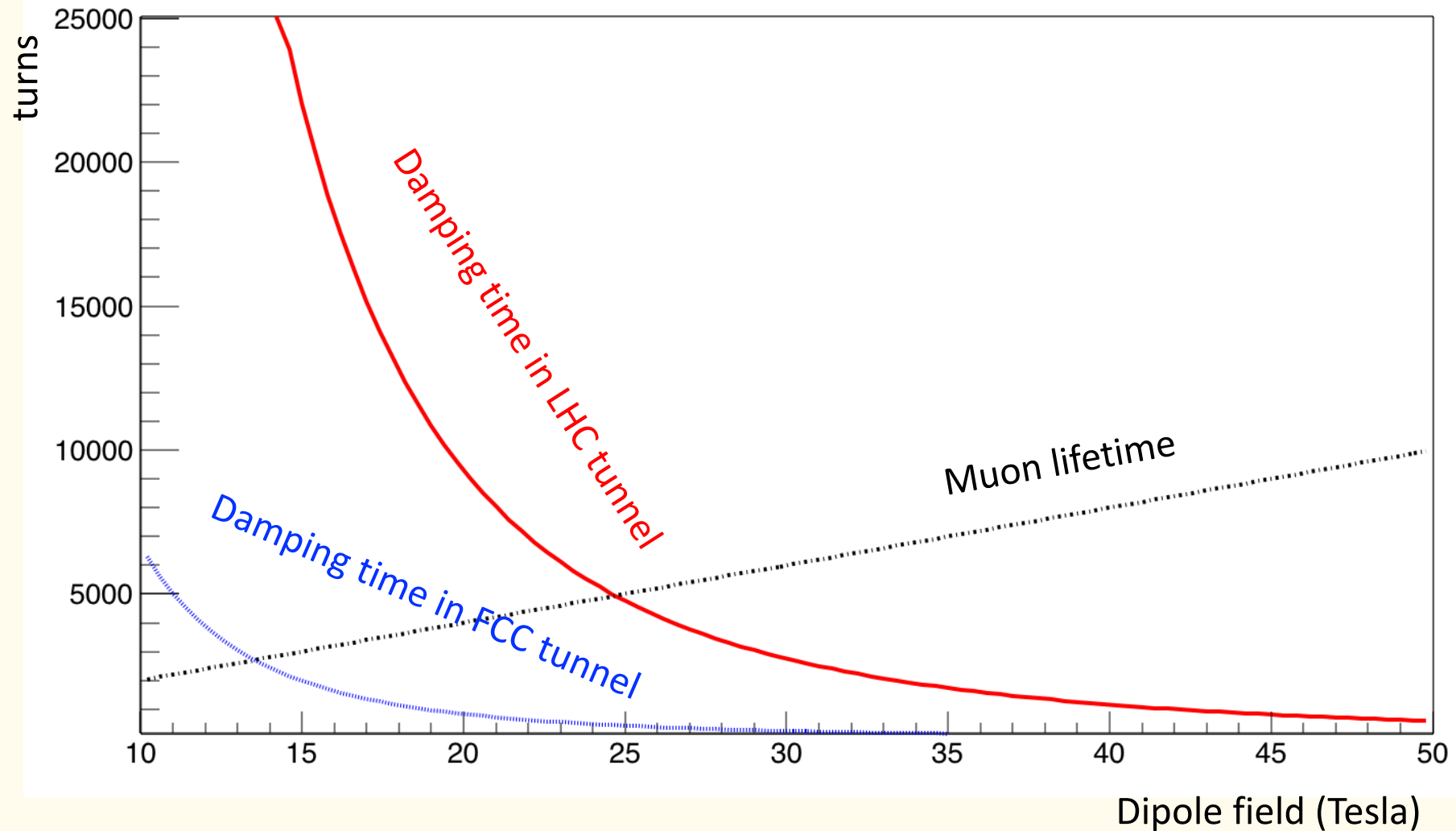
Beam energy(GeV)

# SR and damping in $\mu$ collider



$$U_0 = 5.5 \times 10^{-18} \gamma^4 / \rho$$

## Damping time & muon lifetime





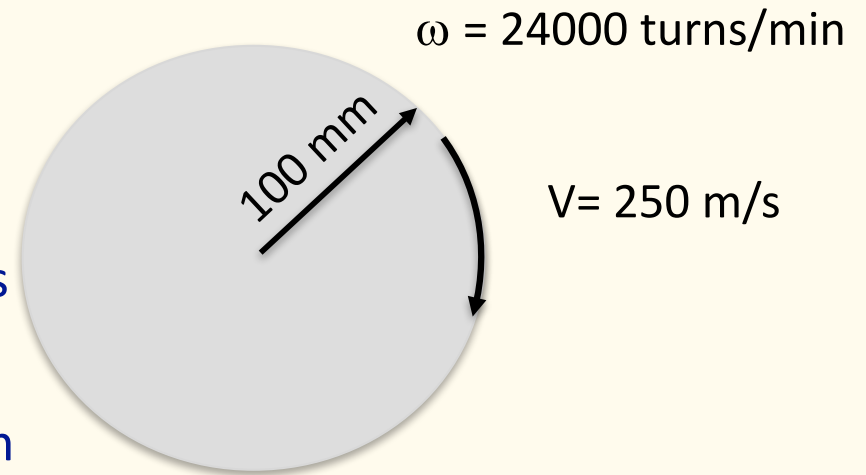
# Solid target

## Rotating disc

- 24000 turns/min
- Radial velocity  $V = 2 \pi \omega (\text{in turns}) r = 250 \text{ m/s}$

## Bunch spacing of $\Delta T = 200 \text{ ns}$

- Bunch separation on target  $L = V \Delta T = 50 \mu\text{m}$
- 12500 bunches in 1 turn



$$C_p = 0.97477 \ln T - 3.6687$$

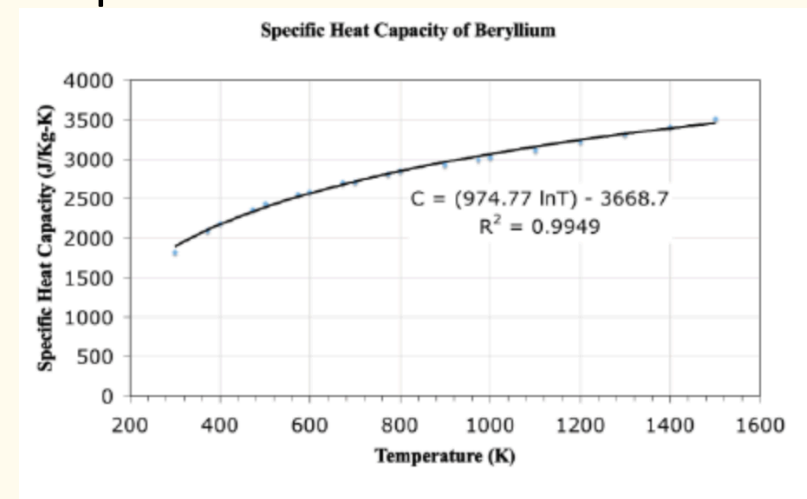
## 2D axisymmetric model showing effective total strain

$4.9 \times 10^{13}$  protons,  $\sigma = 0.3$  mm,  $\Delta T \sim 1025$  °C, 0.25 mm thick window

End of beam pulse

$t = 7.2 \mu\text{s}$ ,  $T_{\text{max}} \sim 1050$  °C,  $\varepsilon_{\text{max}} \sim 3.6$  %

- Use 300  $\mu\text{m}$  round e+ beam, 0.25 mm Be target,  $5 \times 10^{13}$  e+/b
- $dE/e+ = (2.0 \text{ MeV.cm}^2/\text{g})(1.85 \text{ g/cm}^3)(0.025 \text{ cm}) = 0.09 \text{ MeV/e+}$
- $dE = 5 \times 10^{13} \times 0.09 \times 1.6 \times 10^{-13} \text{ J/MeV} = 0.74 \text{ J}$
- $dV = \pi (0.025 \text{ cm})(0.03 \text{ cm})^2 = 7 \times 10^{-5} \text{ cm}^3$   
 $m = dV \rho = 0.00013 \text{ g}$   
 $C_p = \text{spec. heat Be} = 1.8 \text{ J/g}^\circ\text{C} @ 373 \text{ K} ; C = C_p m = 0.00024$
- $dT = dE/C = 3083$  °C
- $C_p = \text{spec. heat Be} = 2.8 \text{ J/g}^\circ\text{C} @ 1000 \text{ K} ; C = C_p m = 0.0005$
- $dT = dE/C = 2000$  °C
- x2 wrt LS-DYNA ?
- Scale for  $n = 3 \times 10^{11}$
- $(300 \mu\text{m})^2 / 200 = (21 \mu\text{m})^2$



# Solid target

- Use 5  $\mu\text{m}$  round e+ beam, 0.3 cm Be target,  $3 \times 10^{11}$  e+/b

$$C_p = 0.97477 \ln T - 3.6687$$

$$Dq = C_p DV \rho dT$$

$$Q = DV \rho [(0.97477 T (\ln T - 1) - 3.6687 T) - 0.97477 \times 373 (\ln 373 - 1) - 3.6687 \times 373]$$

