

# $\Lambda$ Fragmentation Functions

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Fragmentation Functions 2018

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# Outline

- Unpolarized  $\Lambda$  Fragmentation Functions - brief intro
- Polarizing  $\Lambda$  Fragmentation Functions:
  - Conclusions from existing data of  $p p \rightarrow \Lambda^\uparrow X$  and  $e^+ e^- \rightarrow \Lambda^\uparrow h X$
  - Tests in  $p p \rightarrow \Lambda^\uparrow \text{jet } X$  at midrapidity & application in  $p A \rightarrow \Lambda^\uparrow X$  at forward rapidity (small  $x$ )
- $D_{LL}(G_I)$  &  $D_{NN}(H_I)$

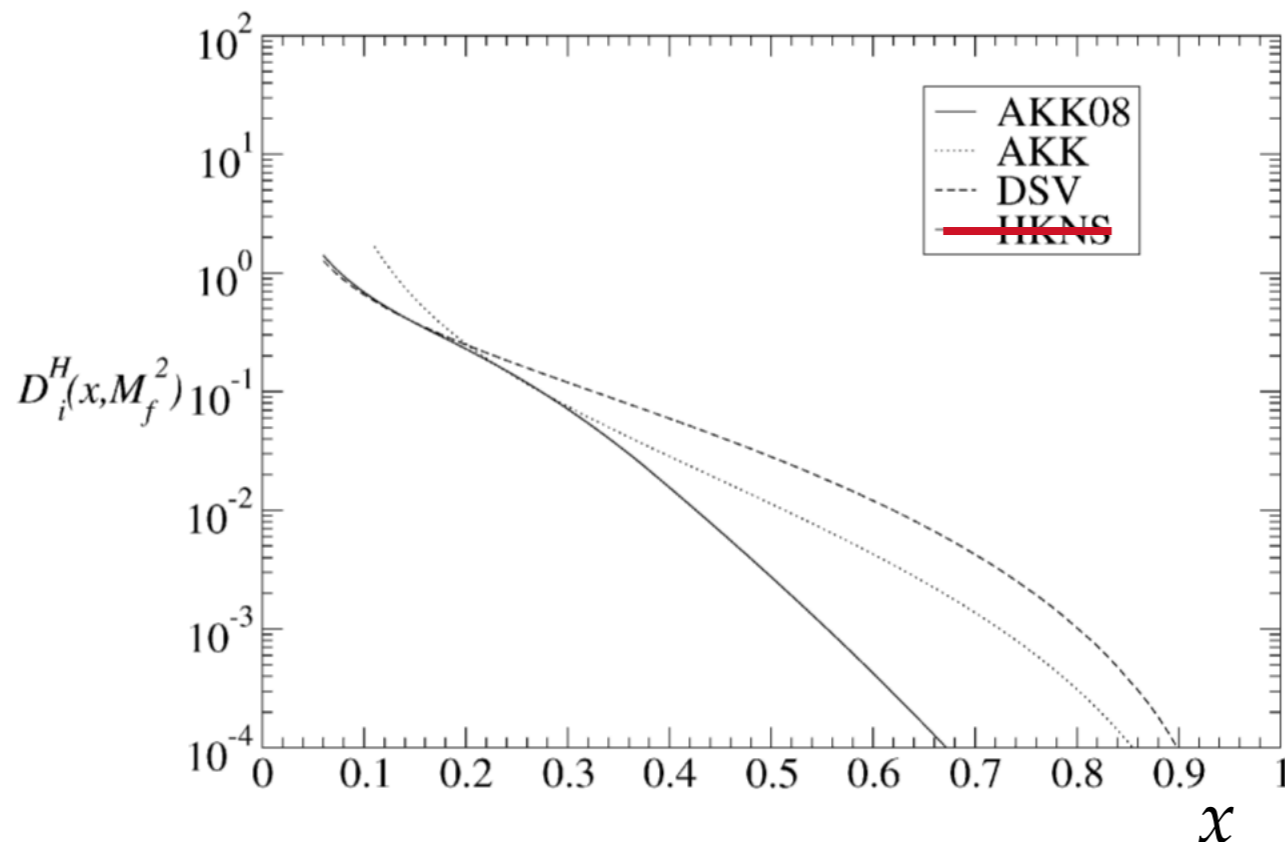
Unpolarized  $\Lambda$  FF

# Unpolarized $\Lambda$ fragmentation functions

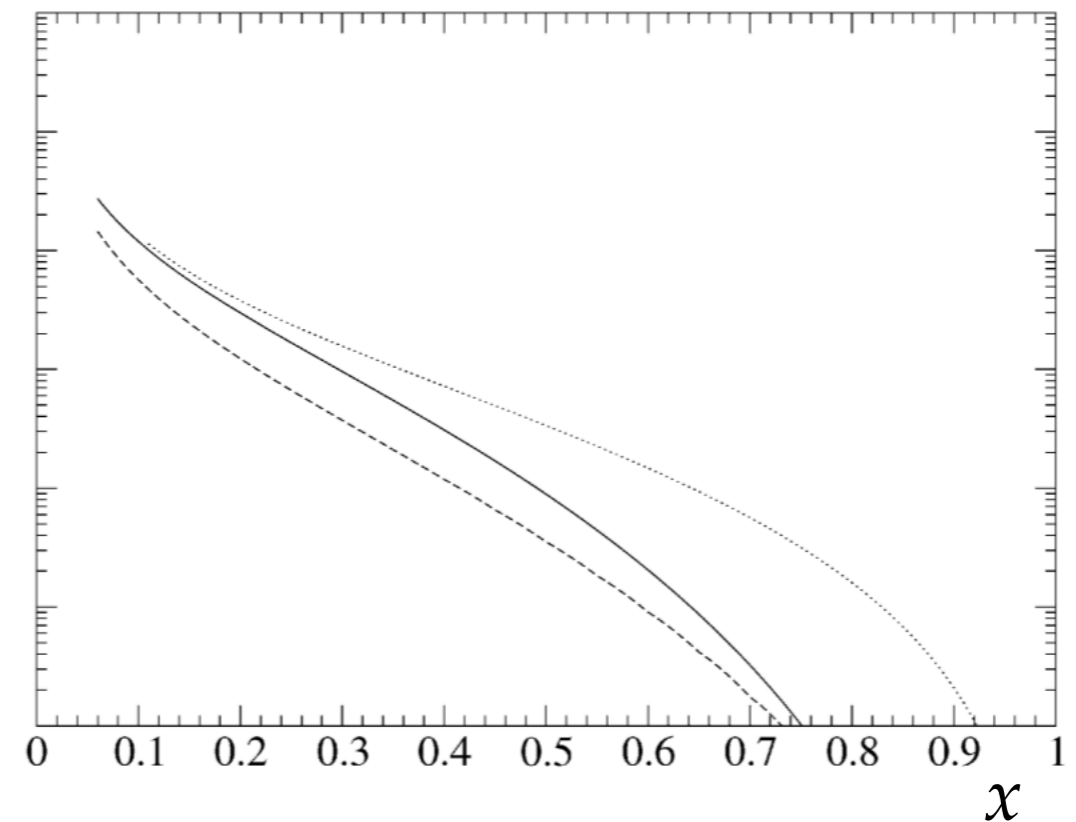
Unpolarized  $\Lambda$  FFs have been extracted by various groups:

- De Florian, Stratmann, Vogelsang [DSV] (PRD 57 (1998) 5811) [ $e^+e^-$  data & SU(3) sym]
- Indumathi, Mani, Rastogi [IMR] (PRD 58 (1998) 094014) [ $e^+e^-$  data & SU(3) breaking]
- Boros, Londergan, Thomas [BLT] (PRD 62 (2000) 014007) [ $e^+e^-$  data & SU(3) breaking]
- Albino, Kniehl, Kramer [AKK] (NPB 734 (2006) 50) [ $e^+e^-$  data & flavour separation]
- AKK update [AKK08] (NPB 803 (2008) 42) [including RHIC & CDF data]

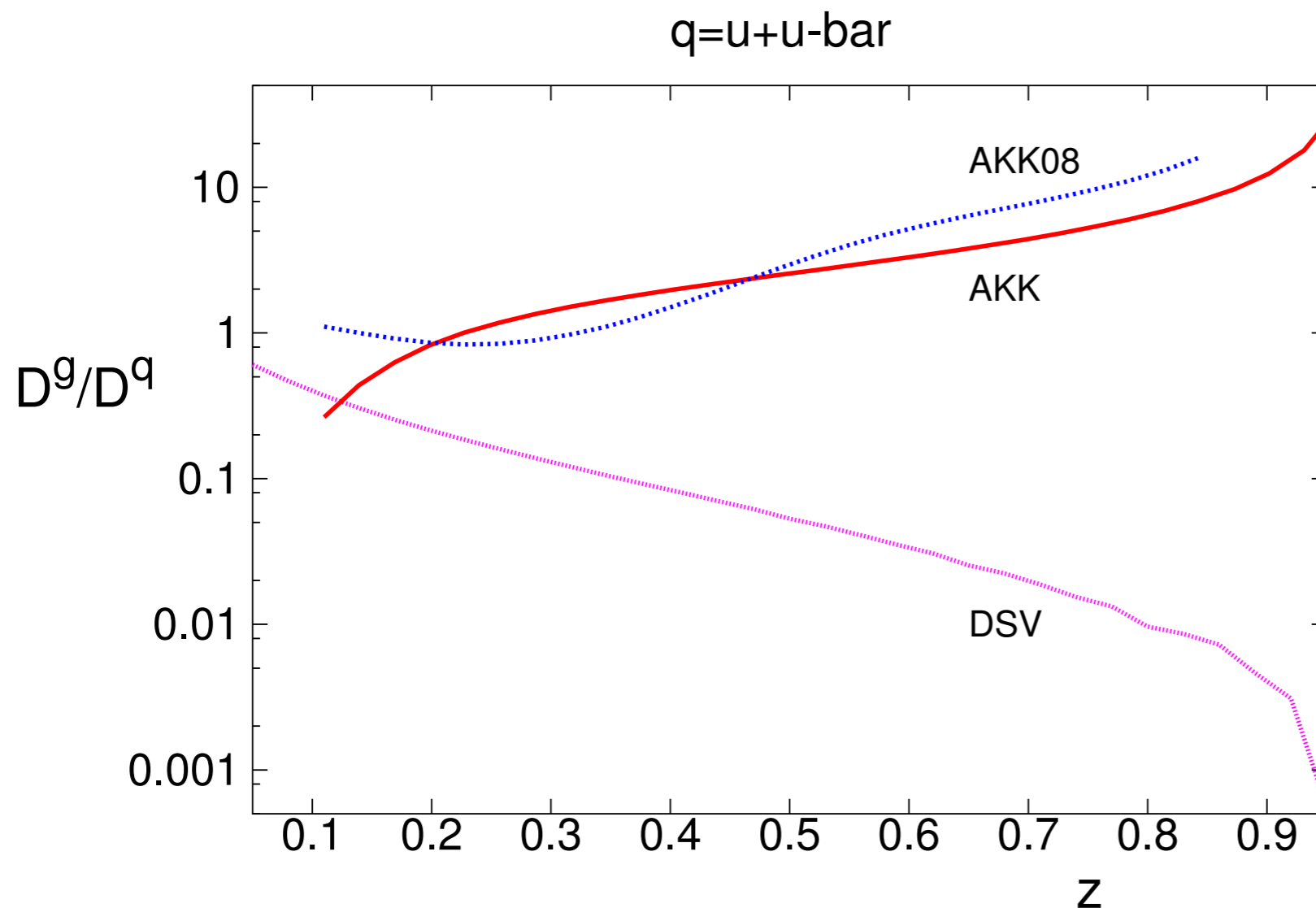
$H=\Lambda/\bar{\Lambda}, i=u, M_f=91.2 \text{ GeV}$



$H=\Lambda/\bar{\Lambda}, i=g, M_f=91.2 \text{ GeV}$



# Role of $g \rightarrow \Lambda X$



$D_1^g / D_1^{u+\bar{u}}$  at LO

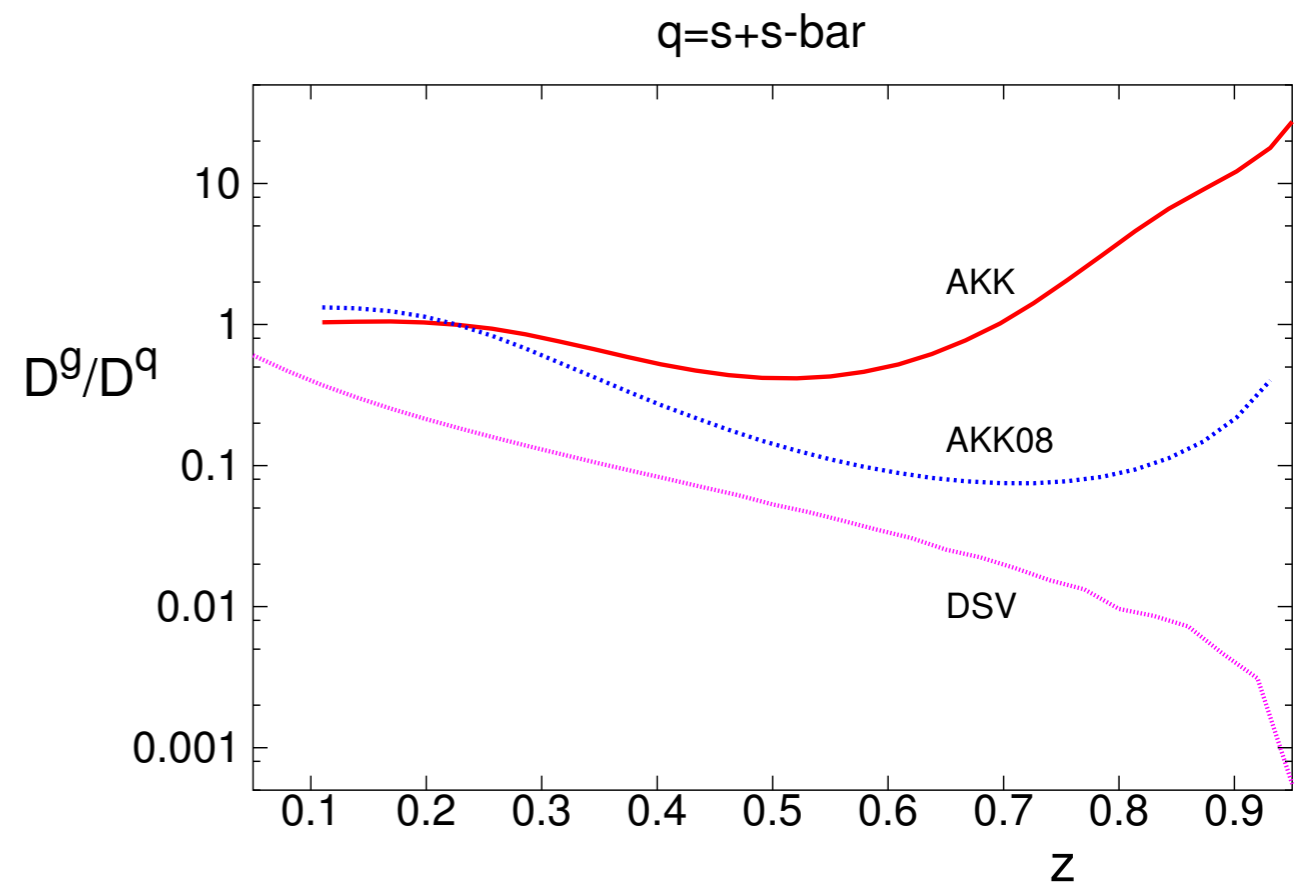
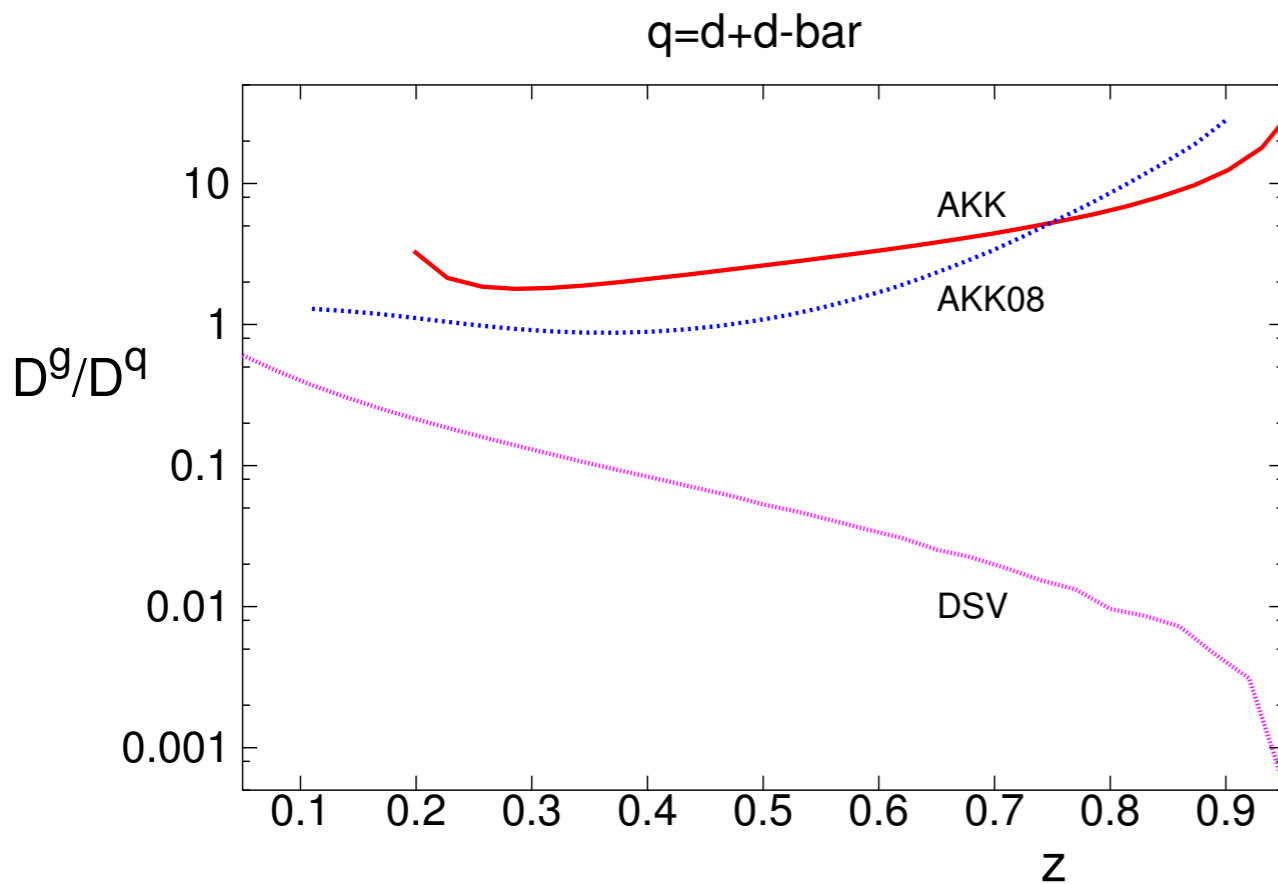
Q = 10 GeV

De Florian, Stratmann, Vogelsang [DSV] (PRD 57 (1998) 5811) ( $e^+e^-$  data only)

Albino, Kniehl, Kramer [AKK] (NPB 734 (2006) 50) (STAR data motivated gluon FF)

AKK update [AKK08] (NPB 803 (2008) 42) (STAR & CDF data including in fit)

# Role of $g \rightarrow \Lambda X$

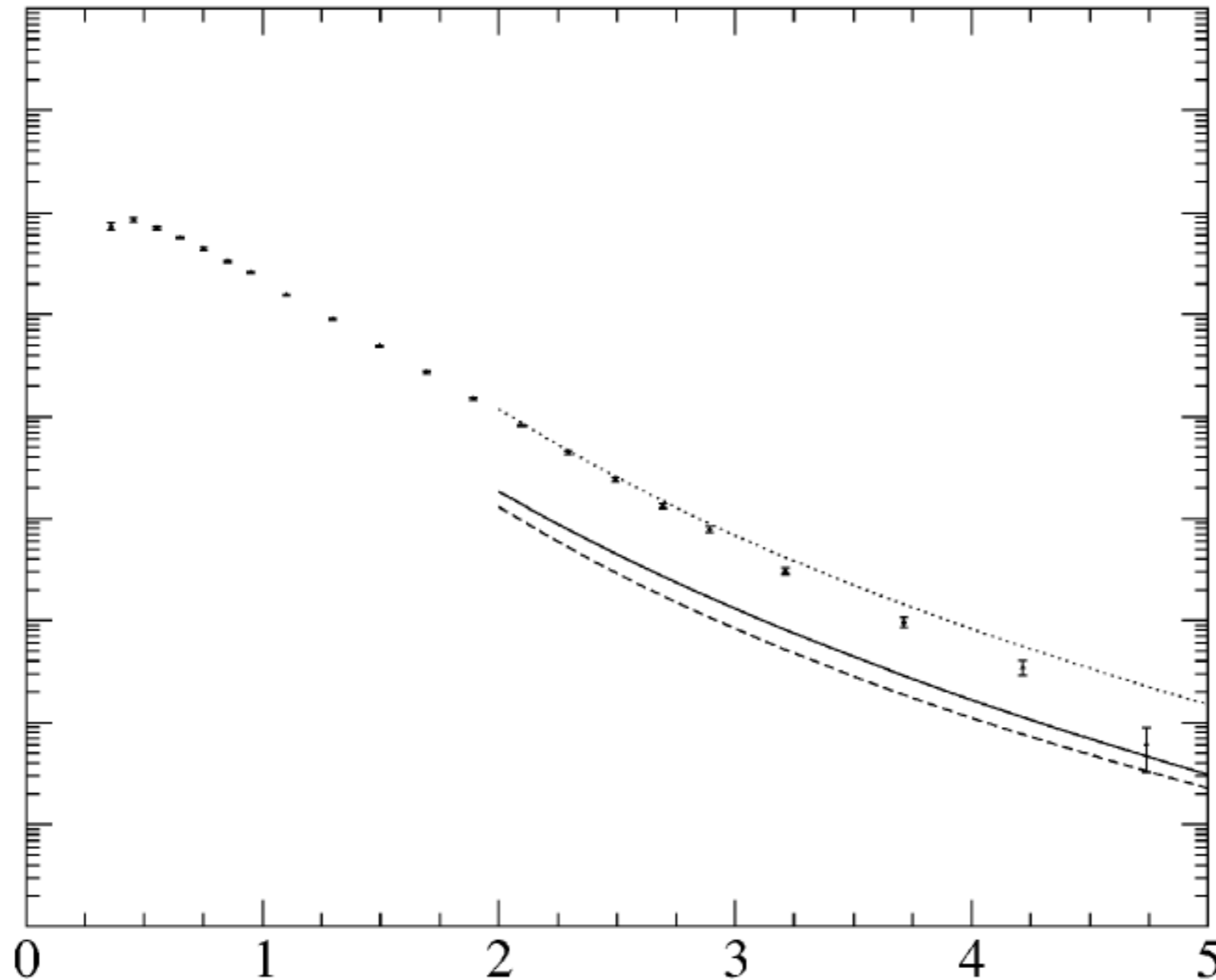


Fits of  $D_1$  to only  $e^+e^- \rightarrow \Lambda X$  data not very sensitive to  $g \rightarrow \Lambda X$

AKK08 that includes RHIC and CDF data turns out to be also problematic

# $\Lambda$ fragmentation function problem

$$pp \rightarrow \Lambda/\bar{\Lambda} + X \quad (-0.5 < y < 0.5), \quad \sqrt{s} = 200 \text{ GeV}$$



$p_T$  distribution

solid: AKK08

dotted: AKK

dashed: DSV

data: STAR

“a possible inconsistency between the pp and  $e^+e^-$  reaction data for  $\Lambda/\bar{\Lambda}$  production”

Polarizing  $\Lambda$  FF

-

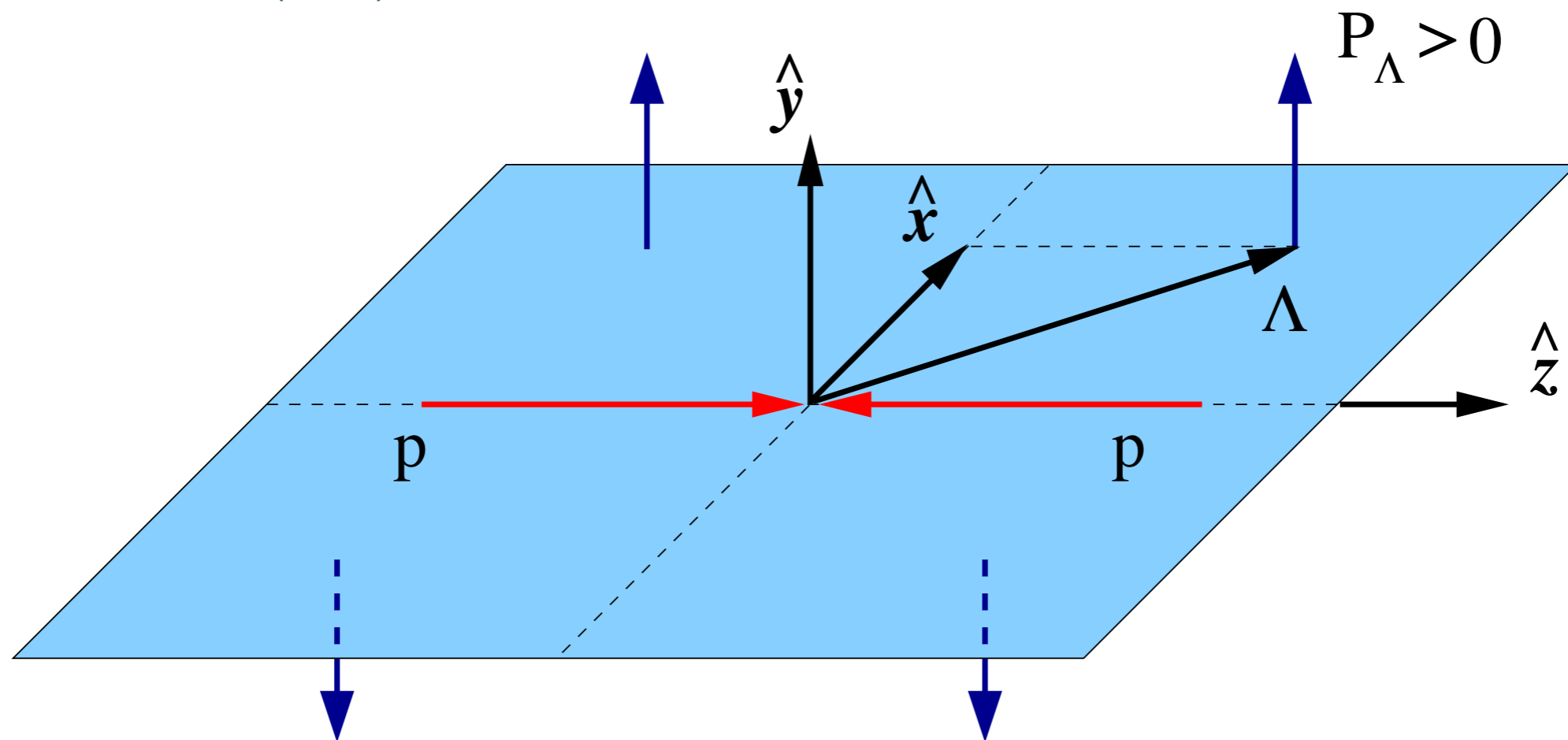
past & present



# Transverse $\Lambda$ polarization in unpolarized scattering

Large asymmetries have been observed in  $p + p \rightarrow \Lambda^\uparrow + X$

G. Bunce *et al.*, PRL 36 (1976) 1113



Blue arrows indicate the direction of positive transverse (w.r.t. production plane) polarization  $P_\Lambda$ , in the four quadrants

For symmetry reasons  $P_\Lambda=0$  at midrapidity in pp collisions in the c.o.m.  
 $P_\Lambda(-x_F) = -P_\Lambda(x_F)$  does not automatically apply in pA collisions or in fixed target experiments

# pp data - $x_F$ dependence

$P_\Lambda$  turns out to be negative

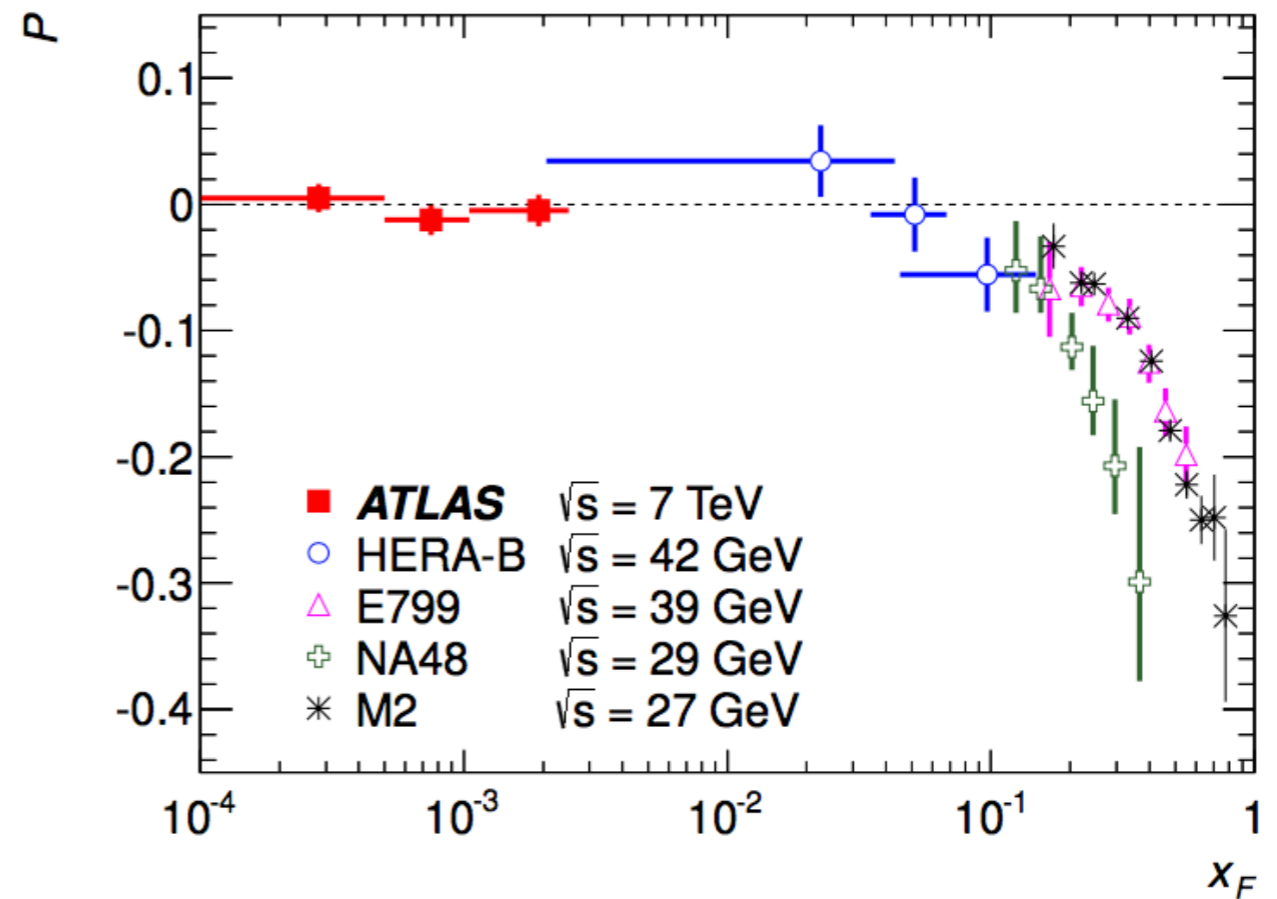
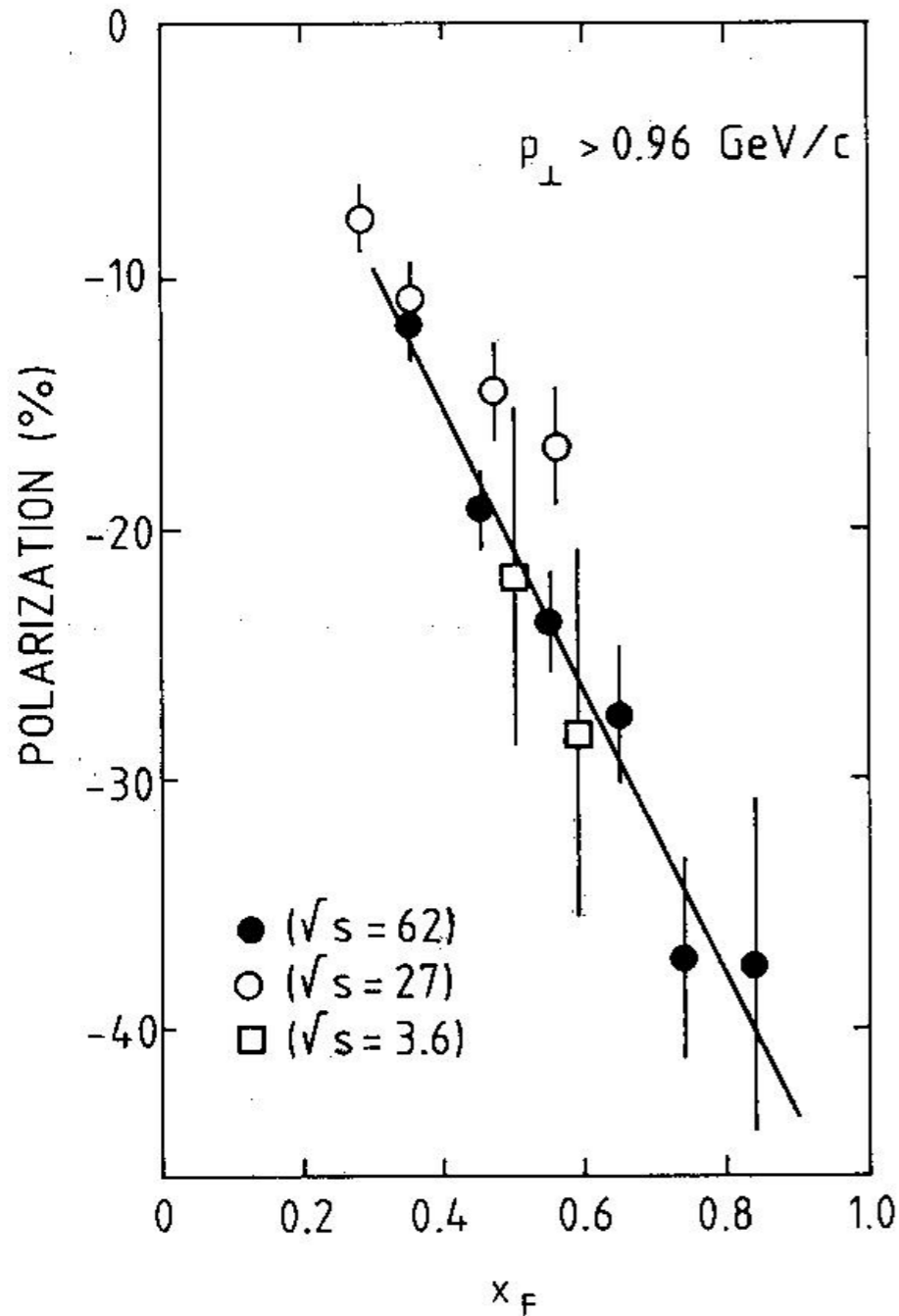
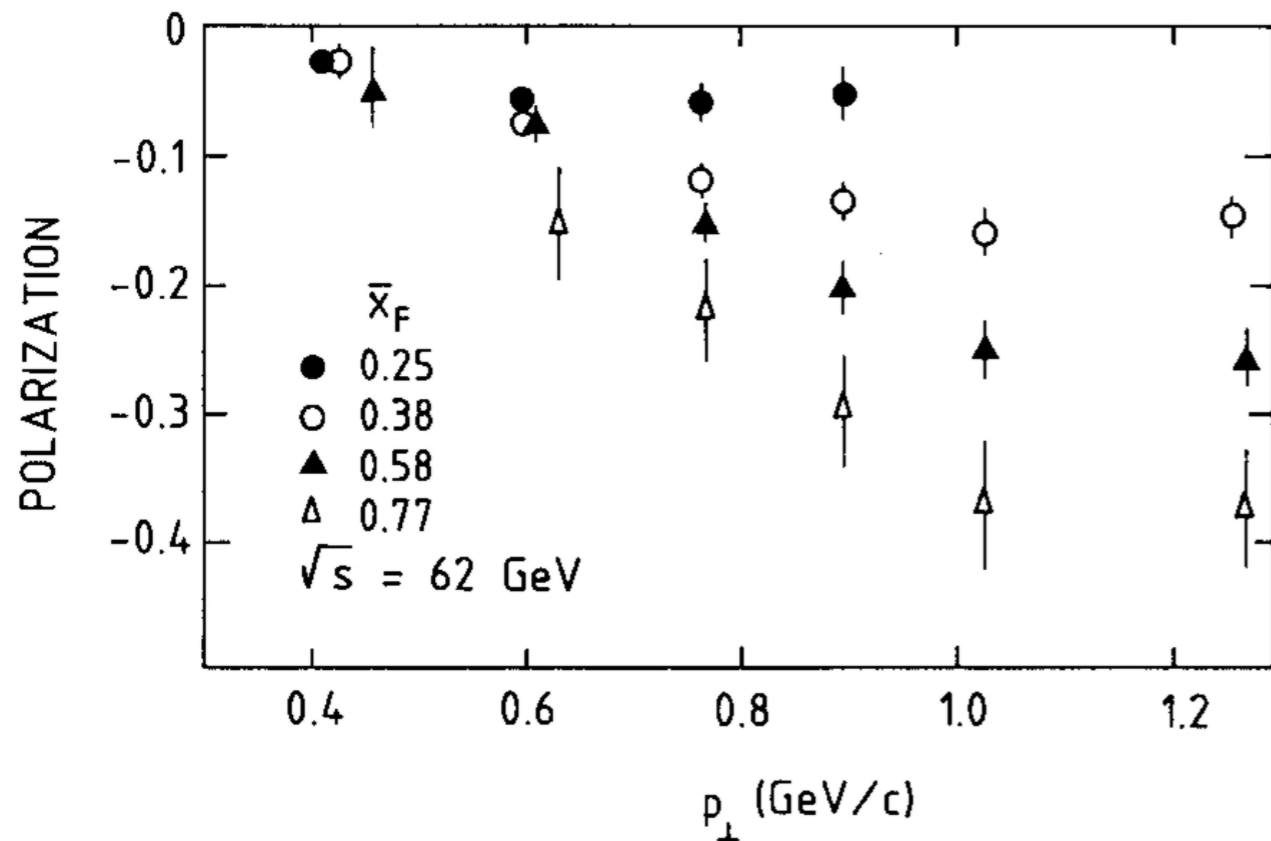


FIG. 8. The  $\Lambda$  transverse polarization measured by ATLAS compared to measurements from lower center-of-mass energy experiments. HERA-B data are taken from Ref. [5], NA48 from Ref. [4], E799 data from Ref. [3], and M2 from Ref. [2]. The HERA-B results are transformed to positive values of  $x_F$  using Eq. (1).

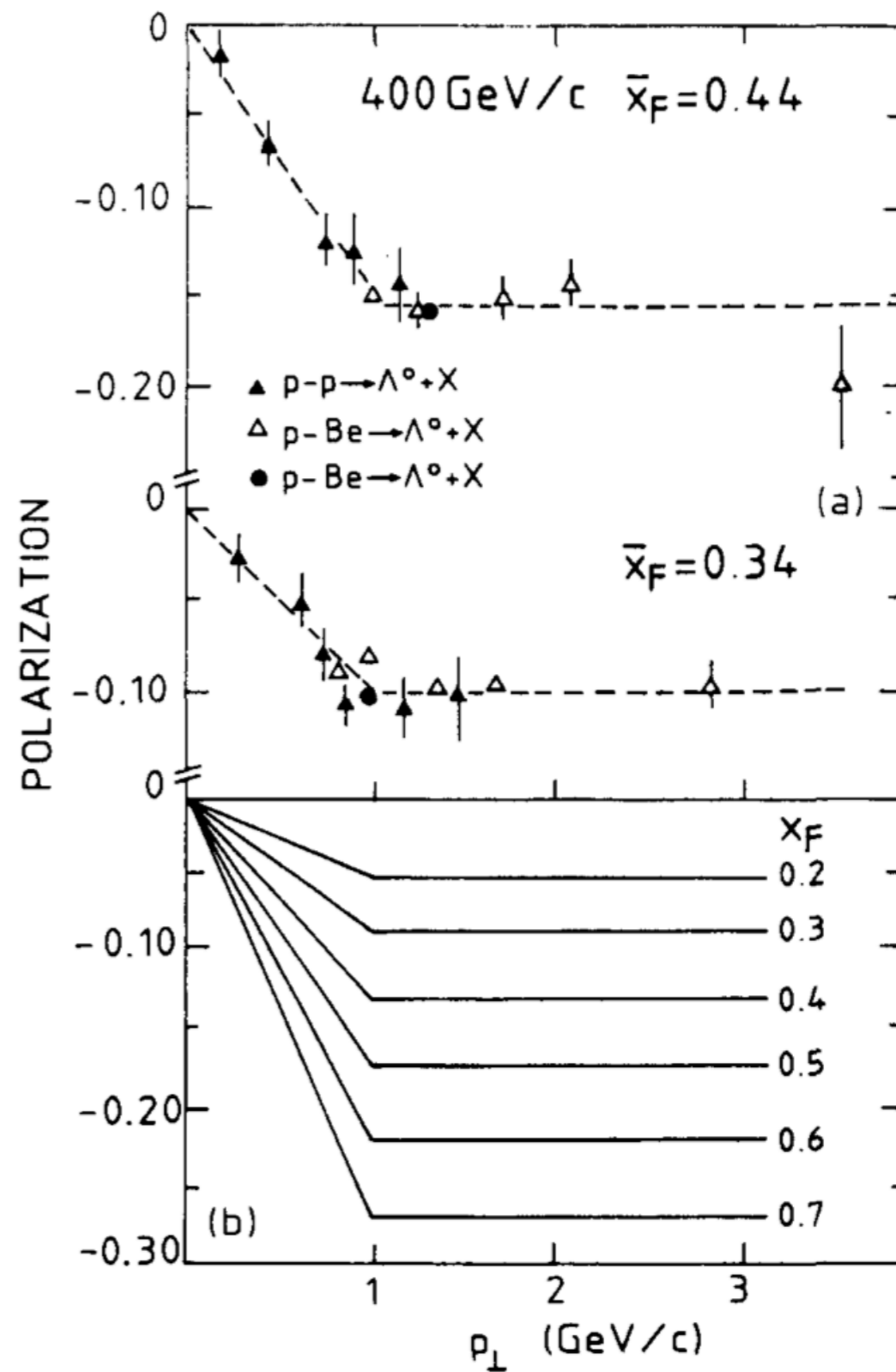
ATLAS Collab, Phys.Rev. D91 (2015) 032004

Eq. (1):  $P(-x_F) = -P(x_F)$  applied to the fixed target experiment HERA-B for pC and pW

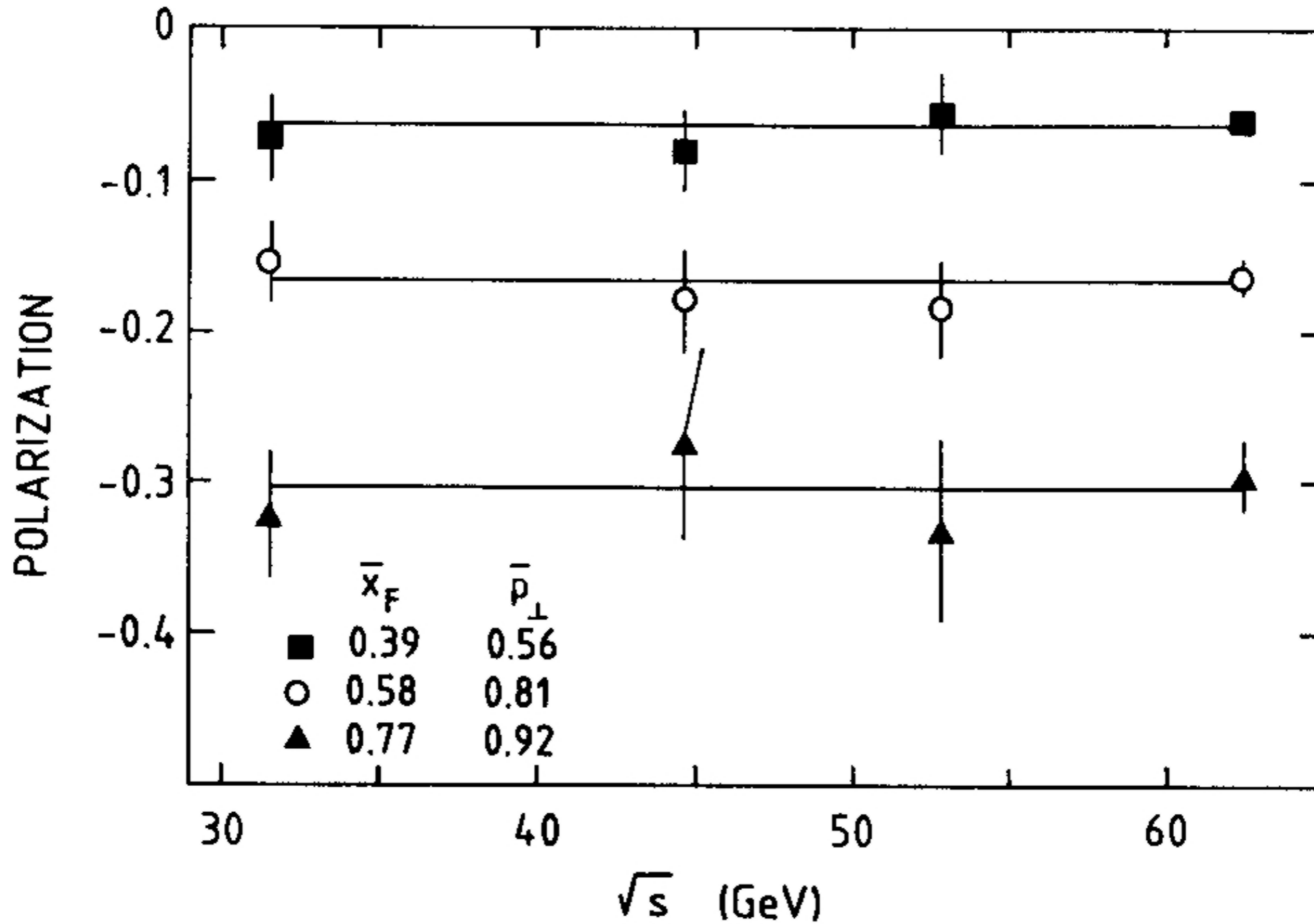
# pp data - $p_T$ dependence



For  $p_T$  above 1 GeV/c  $P_\Lambda$  becomes flat  
(measured up to  $p_T \sim 4$  GeV/c)



# pp data - $\sqrt{s}$ (in)dependence



Comprehensive review of data by [A.D. Panagiotou](#) (Int.J.Mod.Phys.A 5 (1990) 1197)

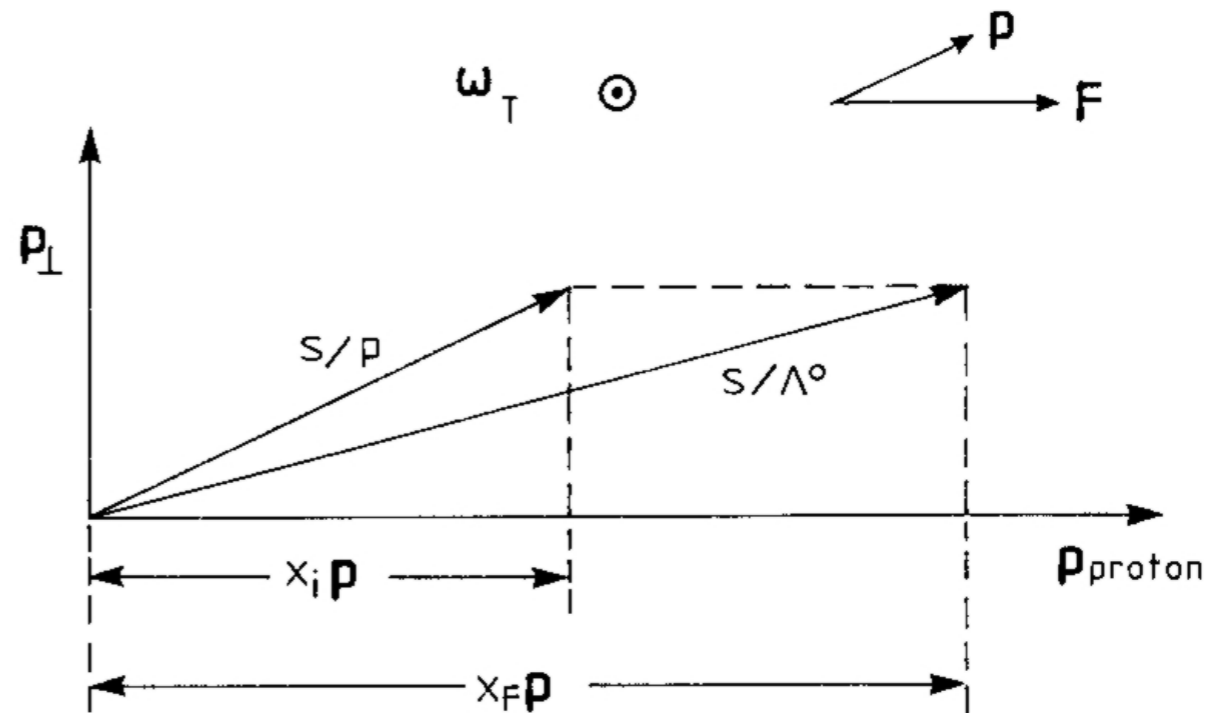
# Theoretical considerations

Most models give only qualitative descriptions of the data for  $p_T \sim 1 - 2 \text{ GeV}/c$

J. Felix, Mod.Phys.Lett.A 14 (1999) 827-842

E.g. the DeGrand-Miettinen model (based on recombination of a  $ud$  diquark from the proton and an  $s$  quark from the sea; spin-orbit coupling creates the polarization)

PRD 23 (1981) 1227 & 24 (1981) 2419



$P_\Lambda$  stays large at least until the highest measured  $p_T \sim 4 \text{ GeV}/c$

For large  $p_T$  perturbative QCD and collinear factorization should apply

pQCD conserves helicity, which leads to  $P_\Lambda \sim \alpha_s m_q / \sqrt{\hat{s}}$  (= small)

Kane, Pumplin & Repko, PRL 41 (1978) 1689

# Collinear factorization

Consider for example the  $qg \rightarrow qg$  subprocess

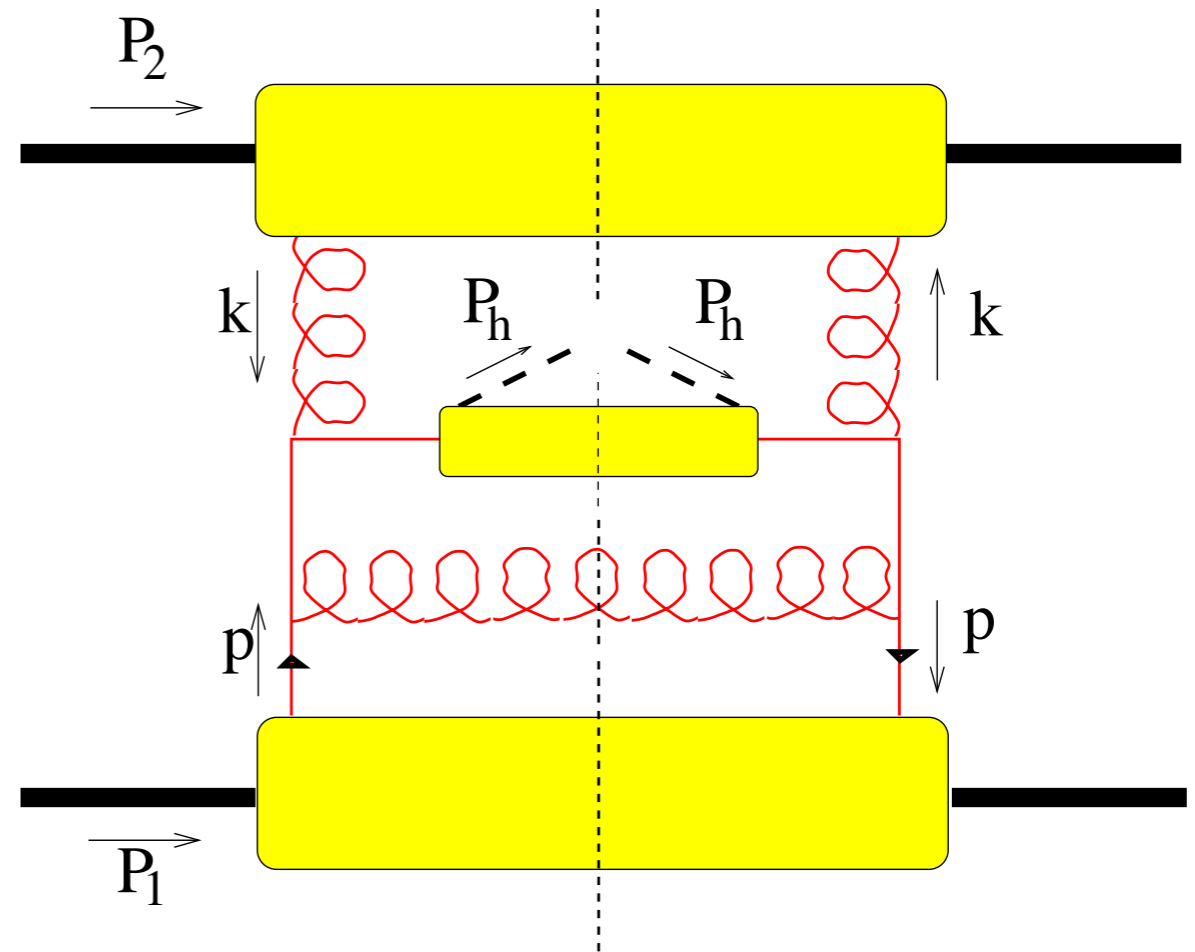
$$\sigma \sim q(x_1) \otimes g(x_2) \otimes \sigma_{qg \rightarrow qg} \otimes D_{\Lambda/q}(z)$$

$q(x_1)$  = quark density

$g(x_2)$  = gluon density

$D_{\Lambda/q}(z)$  =  $\Lambda$  fragmentation function

$$P_{\Lambda} \sim q(x_1) \otimes g(x_2) \otimes \sigma_{qg \rightarrow qg} \otimes ?$$



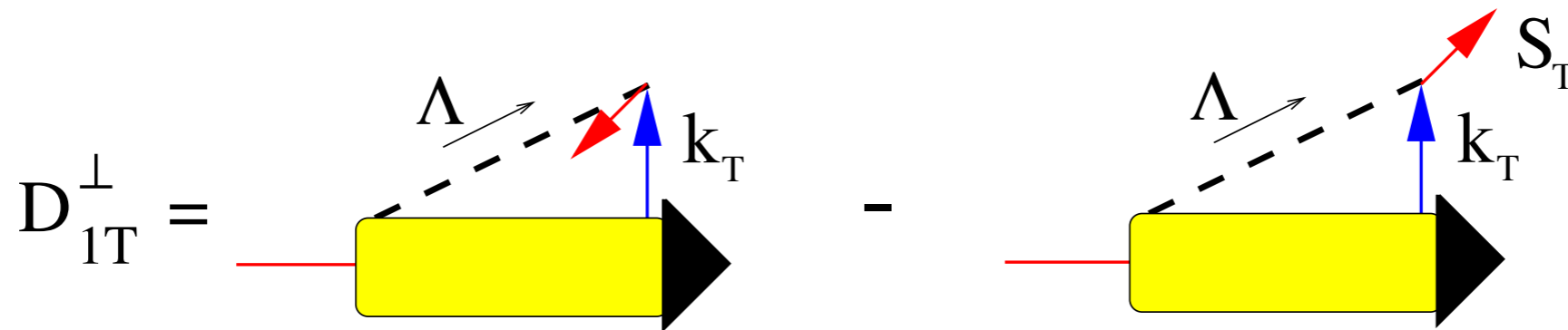
No leading twist collinear fragmentation function exists for  $q \rightarrow \Lambda^{\uparrow} X$

(due to symmetry reasons)

It would be necessarily higher twist, which leads to a fall-off as  $1/p_T$

# Noncollinear factorization

Dropping the requirement of **collinear** factorization, does allow for a solution



- **Transverse momentum dependent:**  $D_{1T}^\perp(z, k_T)$
- A nonperturbative  $k_T \times S_T$  dependence in the fragmentation process
- Allowed by the symmetries (parity and time reversal)

$\Lambda$  polarization arises in the fragmentation of an **unpolarized quark**

Mauro Anselmino suggested the name “polarizing fragmentation function”

However,  $p + p \rightarrow \Lambda^\uparrow + X$  is not TMD factorizing (like  $p^\uparrow p \rightarrow \pi X$ )

Nevertheless, **reasonable functions were obtained**

# Polarizing fragmentation functions

$D_{1T}^\perp$  has been extracted from fixed target  $p + p(\text{Be}) \rightarrow \Lambda^\uparrow(\bar{\Lambda}^\uparrow) + X$  data

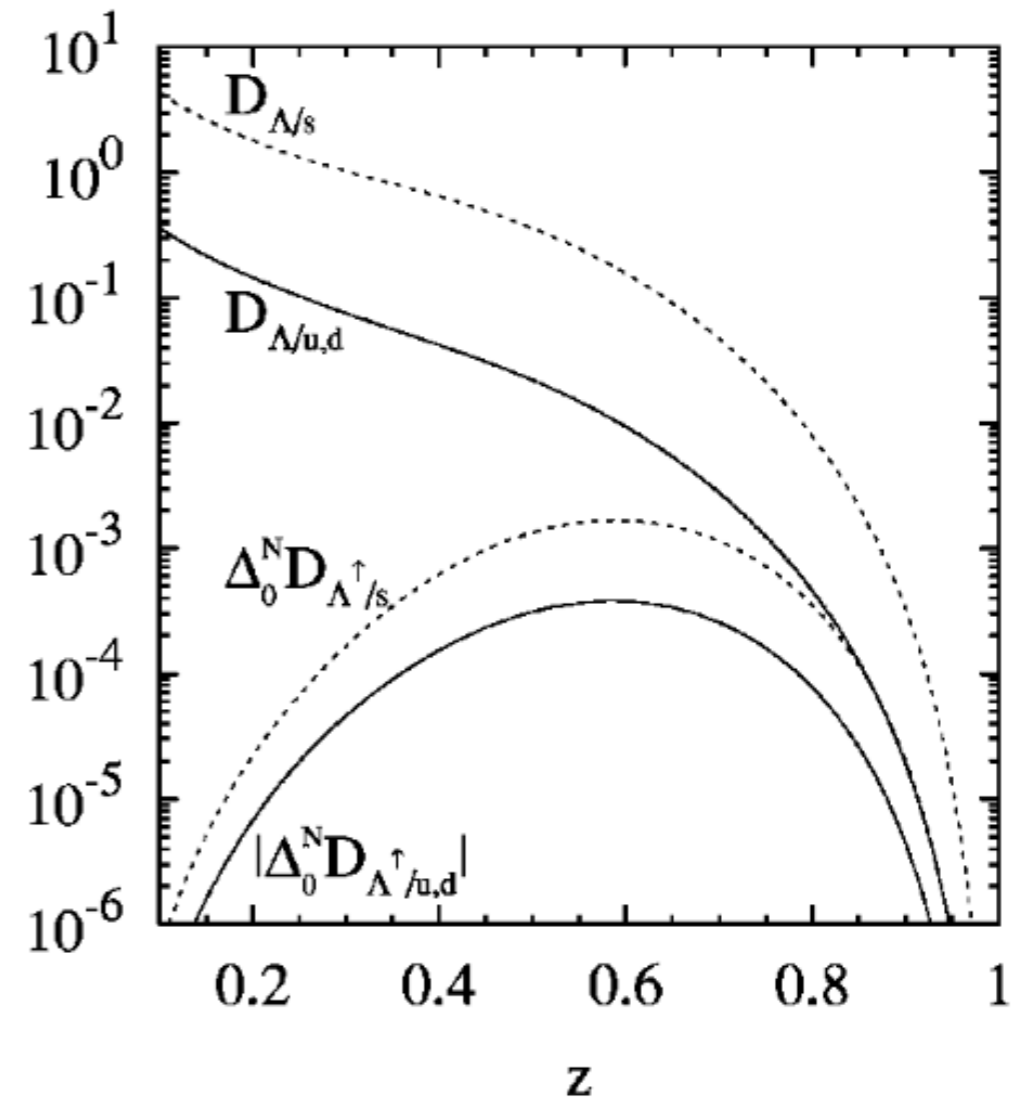
Anselmino, D.B., D'Alesio & Murgia, PRD 63 (2001) 054029

Using unpolarized FF by Indumathi, Mani, Rastogi:

PRD 58 (1998) 094014

Includes SU(3) breaking

$$\Delta_0^N D_{\Lambda^\uparrow/q} \sim \langle k_\perp \rangle D_{1T}^\perp(z, \langle k_\perp \rangle)$$



Resulting  $D_{1T}^\perp$  has opposite signs for u, d versus s quarks; the latter is larger

This leads to cancellations in order that  $P_{\bar{\Lambda}} \approx 0$

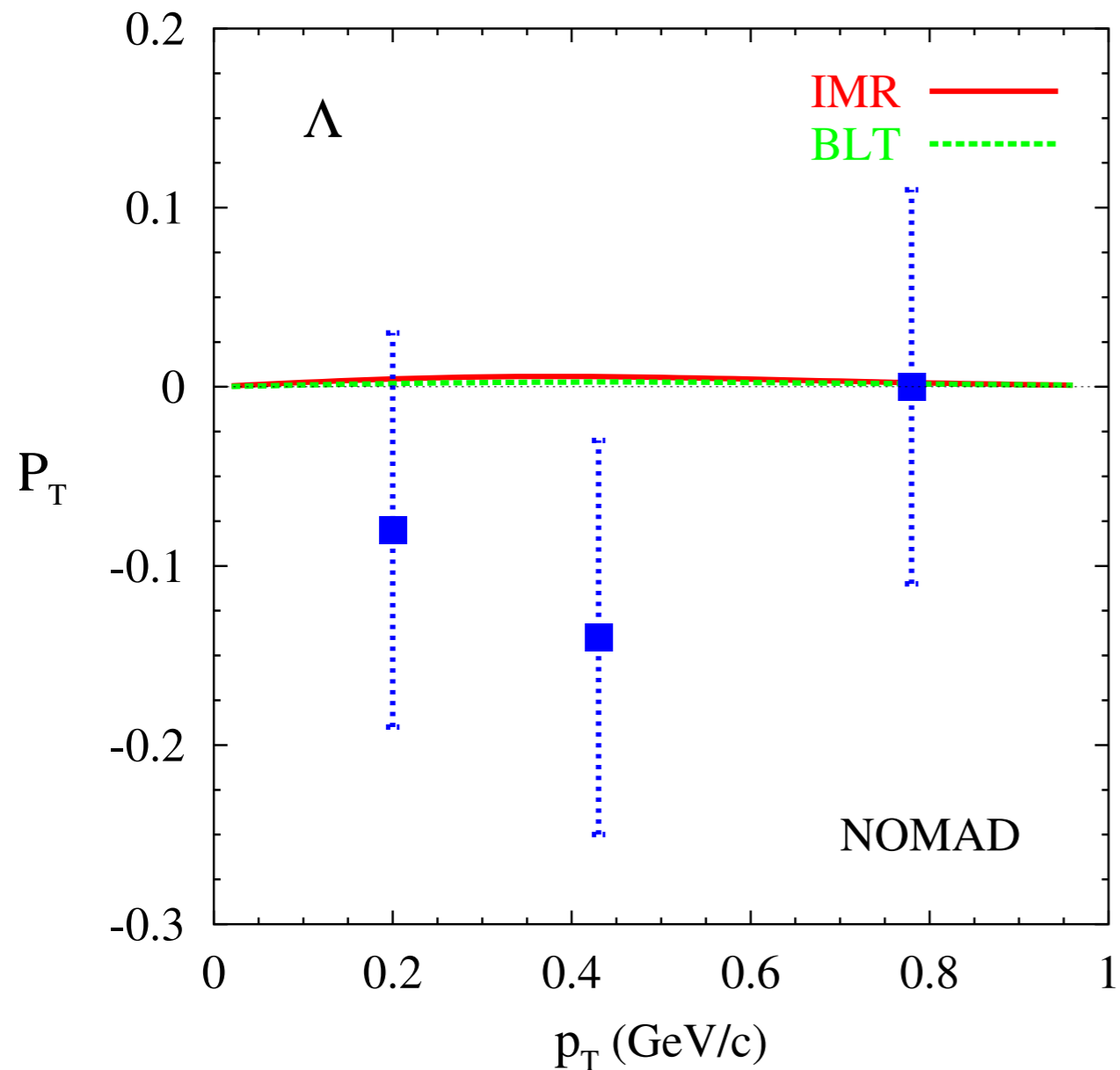
Extraction done under the restriction of  $p_T > 1 \text{ GeV}/c$  to exclude the soft regime



# Predictions for SIDIS

Semi-inclusive DIS:  $ep \rightarrow e' \Lambda^\uparrow X$  (NC) and  $\nu_\mu p \rightarrow \mu \Lambda^\uparrow X$  (CC)

Anselmino, D.B., D'Alesio & Murgia, PRD 65 (2002) 114014



Only available SIDIS data in the current fragmentation region was on  $\nu_\mu p \rightarrow \mu \Lambda^\uparrow X$

Astier et al., NOMAD Collab., NPB 588 (2000) 3

Data and curves are for:

$\langle x_F \rangle = 0.21$  &  $\langle z_h \rangle = 0.34$

$\langle Q^2 \rangle = 9 \text{ GeV}^2$

# Newer SIDIS data

The ZEUS Collaboration: Measurement of  $K_S^0$ ,  $\Lambda$  and  $\bar{\Lambda}$  production at HERA

	High- $Q^2$ DIS	Polarization (%) Low- $Q^2$ DIS	Photoproduction
$\Lambda$	$-1.3 \pm 4.3(\text{stat.})^{+4.0}_{-0.8}(\text{syst.})$	$-4.0 \pm 5.3(\text{stat.})^{+4.7}_{-4.0}(\text{syst.})$	$-2.4 \pm 2.2(\text{stat.})$
$\bar{\Lambda}$	$-2.2 \pm 4.2(\text{stat.})^{+2.4}_{-1.3}(\text{syst.})$	$-8.5 \pm 5.5(\text{stat.})^{+4.7}_{-2.1}(\text{syst.})$	$-5.8 \pm 2.2(\text{stat.})$
$K_S^0$	$-1.5 \pm 1.1(\text{stat.})$	$-0.05 \pm 1.5(\text{stat.})$	$-0.5 \pm 0.2(\text{stat.})$

**Table 1.** The transverse polarization values for  $\Lambda$  and  $\bar{\Lambda}$ , expressed here in %, in the high- $Q^2$  DIS ( $Q^2 > 25 \text{ GeV}^2$  and  $0.02 < y < 0.95$ ), low- $Q^2$  DIS ( $5 < Q^2 < 25 \text{ GeV}^2$  and  $0.02 < y < 0.95$ ), and photoproduction ( $Q^2 < 1 \text{ GeV}^2$ ,  $0.2 < y < 0.85$  and with two jets  $E_T^{\text{jet}} > 5 \text{ GeV}$  and  $|\eta^{\text{jet}}| < 2.4$ ) samples. Only  $\Lambda$  and  $\bar{\Lambda}$  in the range  $0.6 < P_T^{\text{LAB}} < 2.5 \text{ GeV}$  and  $|\eta^{\text{LAB}}| < 1.2$  are considered. The statistical error is quoted for all samples, together with the systematic uncertainty associated with the measurement for the high- $Q^2$  and low- $Q^2$  samples. A similar systematic uncertainty is expected for the photoproduction sample. Also shown, as a test of any systematic effect, are the polarization values obtained by investigating the angular distribution of the higher-momentum  $\pi$  from  $K_S^0$  decays

ZEUS Collab., Eur. Phys. J. C 51 (2007) 1

Other ep data are either in the target fragmentation region or for quasi-real production (E665, HERMES)

# Polarizing FFs from $e^+e^-$



ELSEVIER

Nuclear Physics B 504 (1997) 345–380



## Asymmetries in polarized hadron production in $e^+e^-$ annihilation up to order $1/Q$

D. Boer<sup>a</sup>, R. Jakob<sup>a</sup>, P.J. Mulders<sup>a,b</sup>

$$\frac{d\sigma^O(e^+e^- \rightarrow hX)}{d\Omega dz_h} = \frac{3\alpha^2}{Q^2} \sum_{a,\bar{a}} e_a^2 \left\{ A(y) D_1^a(z_h) + C(y) D(y) |S_{hT}| \sin(\phi_{S_h}) \frac{2M_h}{Q} \frac{D_T^a(z_h)}{z_h} \right\} \quad (80)$$

$\Lambda$  polarization in  $e^+e^- \rightarrow \Lambda^\uparrow X$  is twist-3

$$\frac{d\sigma(e^+e^- \rightarrow h \text{ jet } X)}{d\Omega dz_h d^2q_T} = \frac{3\alpha^2}{Q^2} z_h^2 \sum_{a,\bar{a}} e_a^2 \left\{ A(y) \left[ D_1^a(z_h, z_h^2 Q_T^2) + |S_{hT}| \sin(\phi_h - \phi_{S_1}) \frac{Q_T}{M_h} D_{1T}^{\perp a}(z_h, z_h^2 Q_T^2) \right] \right\}$$

in  $e^+e^- \rightarrow (\Lambda^\uparrow \text{ jet}) X$  it is not power suppressed

# $\Lambda$ polarization in $e^+e^-$

OPAL data  $Q=M_Z$

Eur.Phys.J C2 (1998) 49

Transverse polarization

compatible with zero at the

$\sim 3$  percent level

**Table 6.** Measured transverse polarization of  $\Lambda$  baryons as a function of  $p_T$  (the transverse momentum of the  $\Lambda$  measured relative to the event thrust axis). The first error is statistical, the second systematic

$p_T$ (GeV/c)	$P_T^\Lambda$ (%)
$< 0.3$	$-1.8 \pm 3.1 \pm 1.0$
$0.3 - 0.6$	$0.4 \pm 1.8 \pm 0.7$
$0.6 - 0.9$	$1.0 \pm 1.9 \pm 0.7$
$0.9 - 1.2$	$0.8 \pm 2.2 \pm 0.6$
$1.2 - 1.5$	$0.0 \pm 2.7 \pm 0.6$
$> 1.5$	$1.8 \pm 1.6 \pm 0.5$
$> 0.3$	$0.9 \pm 0.9 \pm 0.3$
$> 0.6$	$1.1 \pm 1.0 \pm 0.4$

This measurement is closer to  $e^+e^- \rightarrow (\Lambda^\uparrow \text{jet}) X$  than to  $e^+e^- \rightarrow \Lambda^\uparrow X$

Twist-3 description applies to collinear factorization for  $p_T$  integrated case

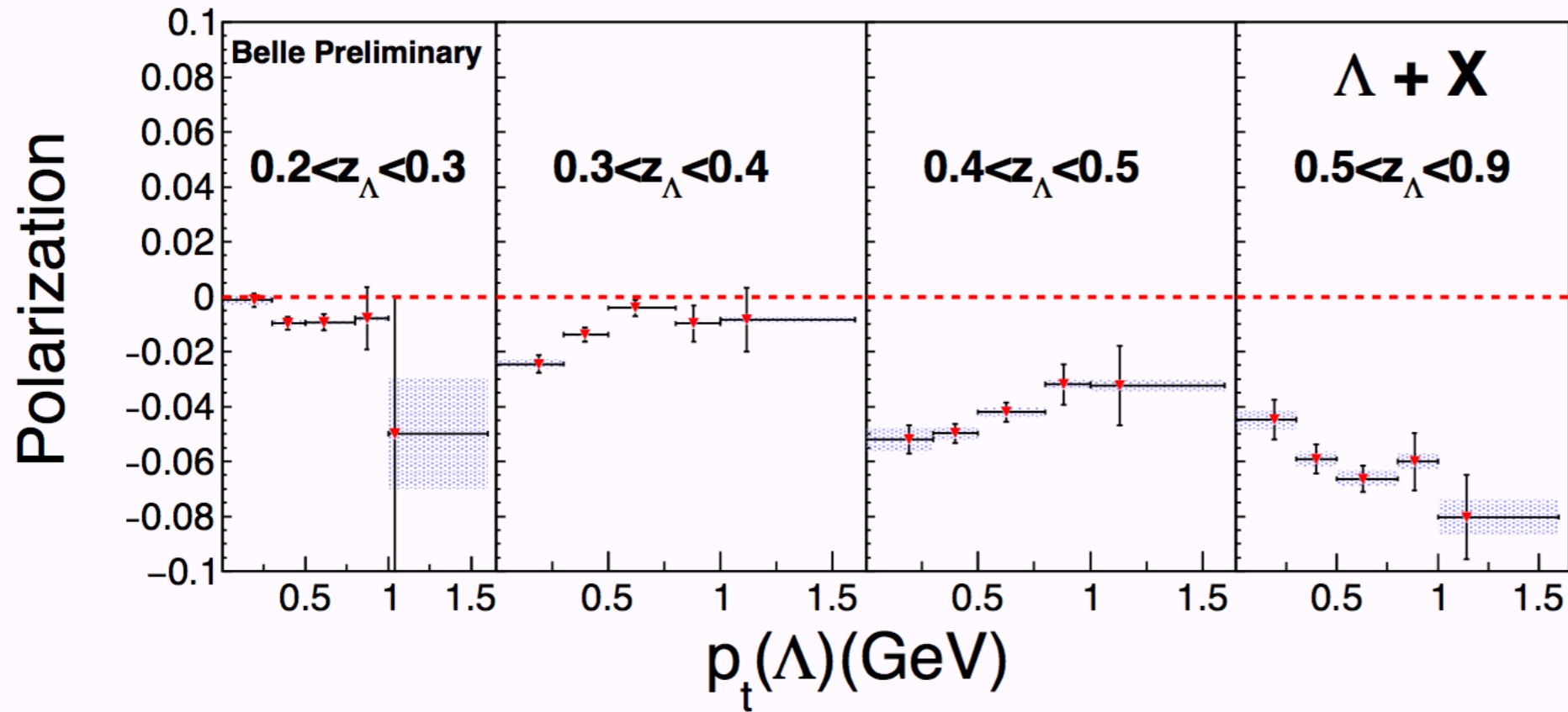
Schlegel at Transversity 2018 (in collab with Gamberg, Kang, Pitonyak & Yoshida)

TMD evolution of observables with a single  $k_T$ -odd function is approx  $1/\sqrt{Q}$

Belle polarization is then expected to be  $\sqrt{(91.2/10.6)} \approx 3$  times larger than

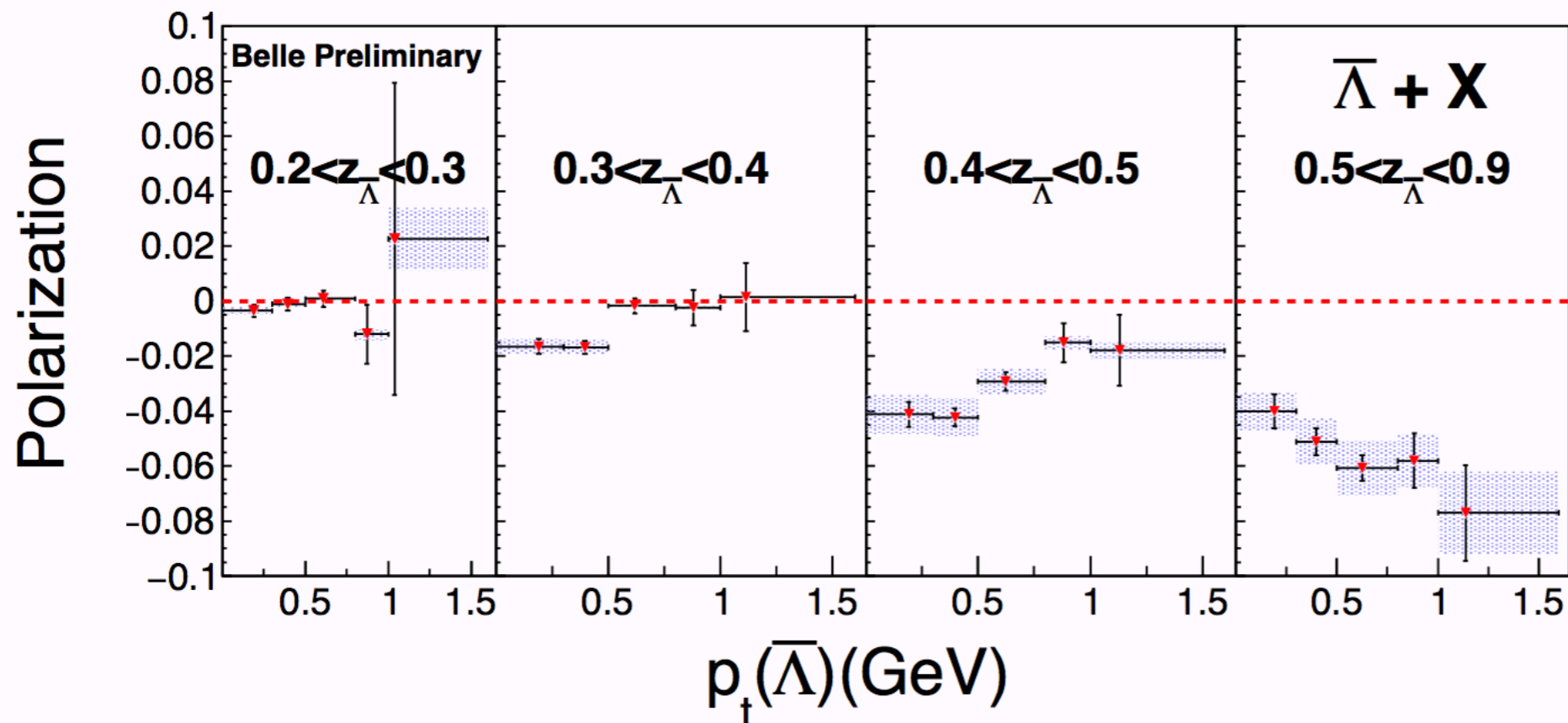
OPAL data (for  $z$  integrated)

# $\Lambda$ polarization in $e^+e^-$



$p_T$  w.r.t. thrust axis

BELLE Collaboration  
arXiv:1611.06648



Again: this is closer  
to  $e^+e^- \rightarrow (\Lambda^\uparrow \text{jet}) X$   
than to  $e^+e^- \rightarrow \Lambda^\uparrow X$

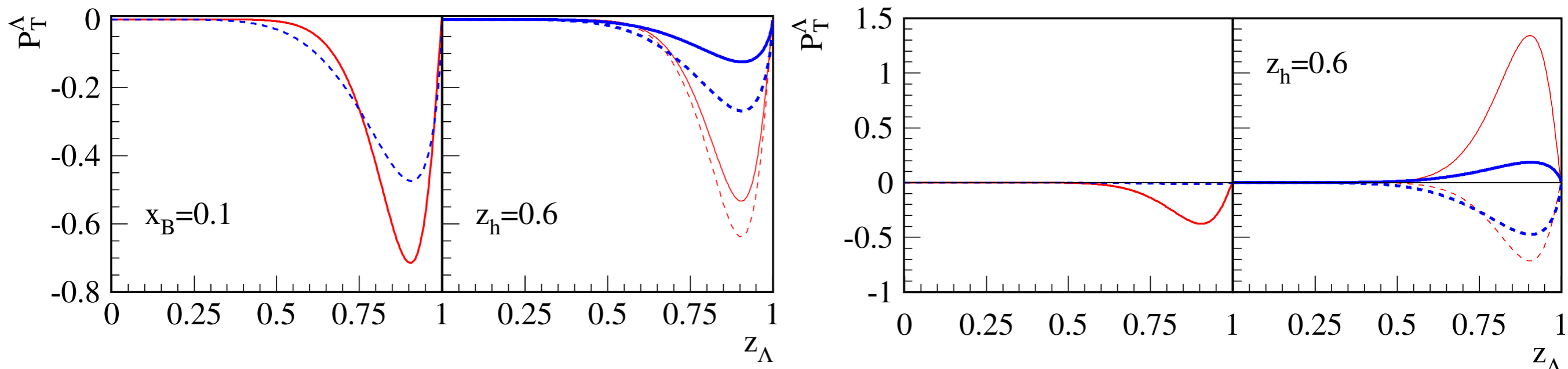
As expected anti- $\Lambda$   
is similar to  $\Lambda$ ,  
unlike the pp case

# Associated production

$e^+e^- \rightarrow \Lambda^\uparrow X$  is very sensitive to cancellations between u, d and s contributions

It is better to study  $\Lambda$  produces in association with a  $\pi$  or K

This allows for flavor selection



D.B., Kang, Vogelsang, Yuan, PRL 2010

Fig 1: SIDIS, SU(3)-symmetric (solid) and broken (dashed) spin-averaged FFs

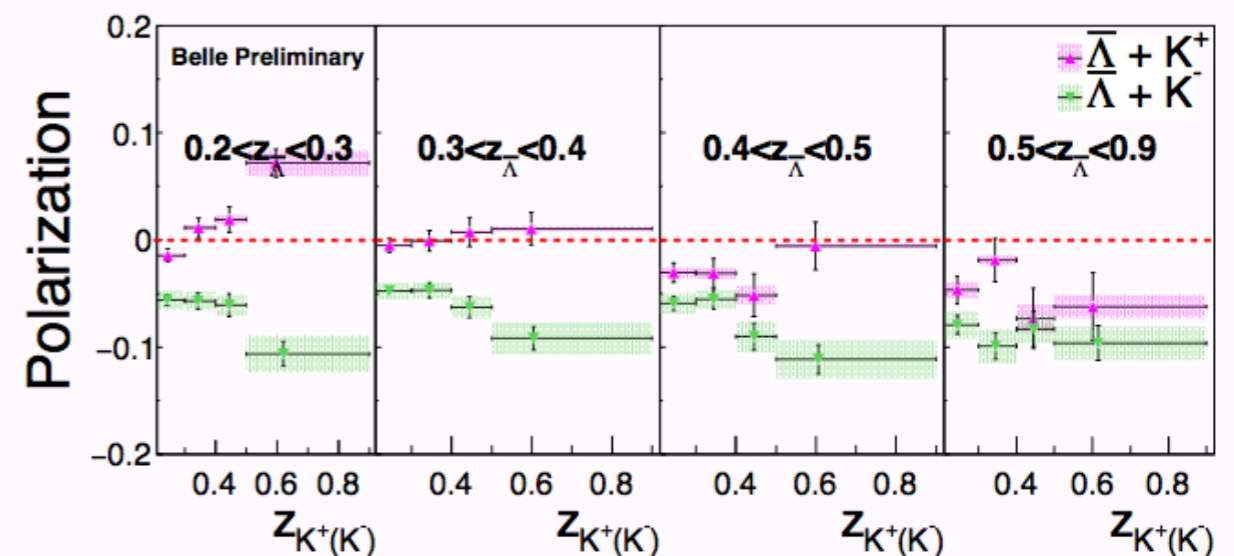
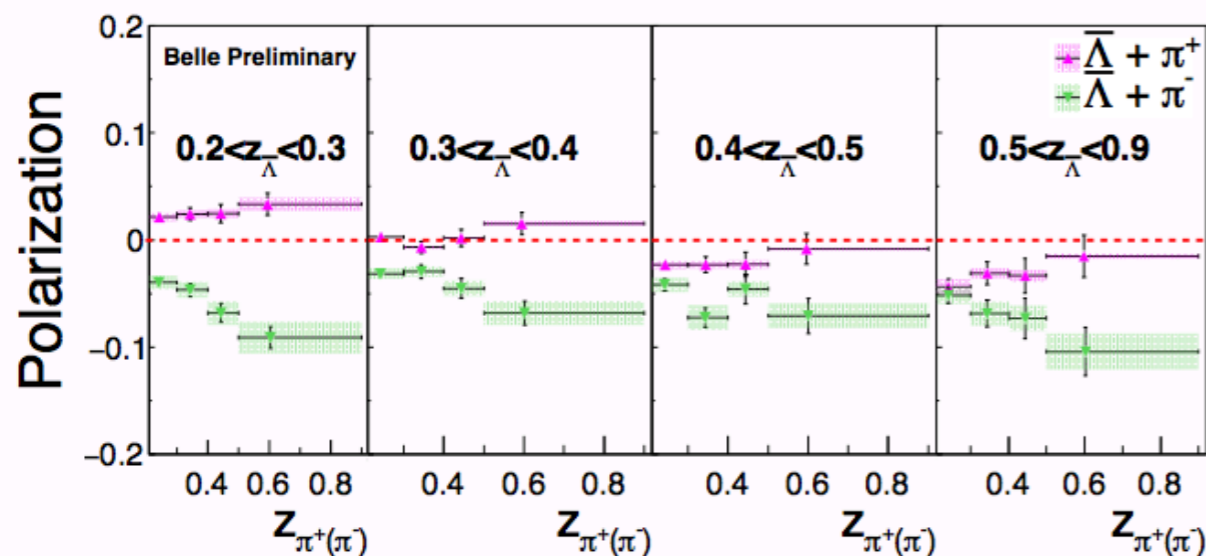
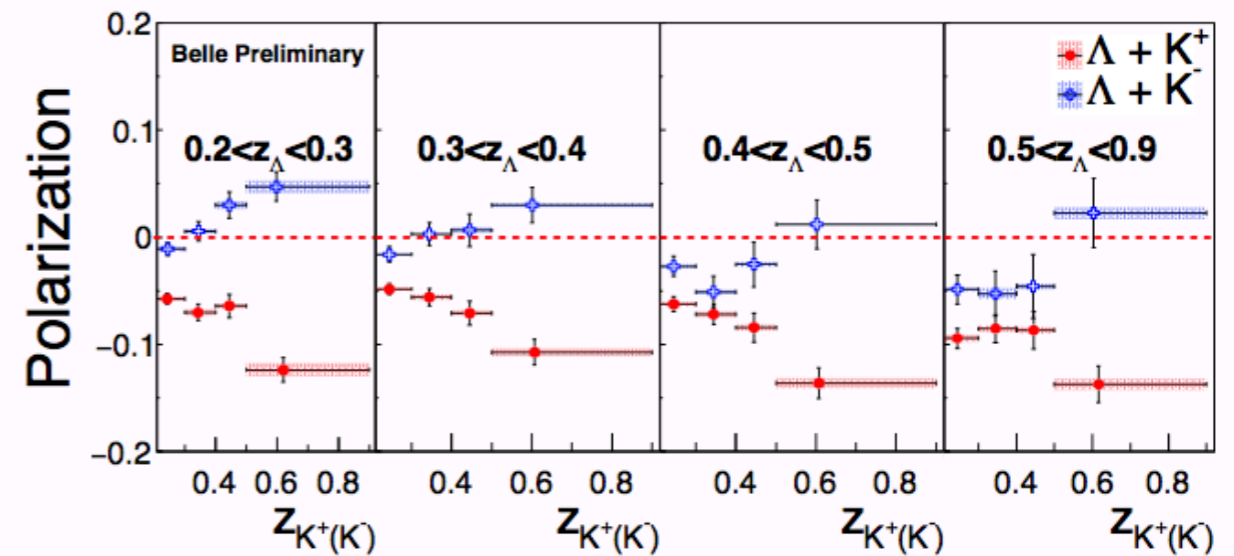
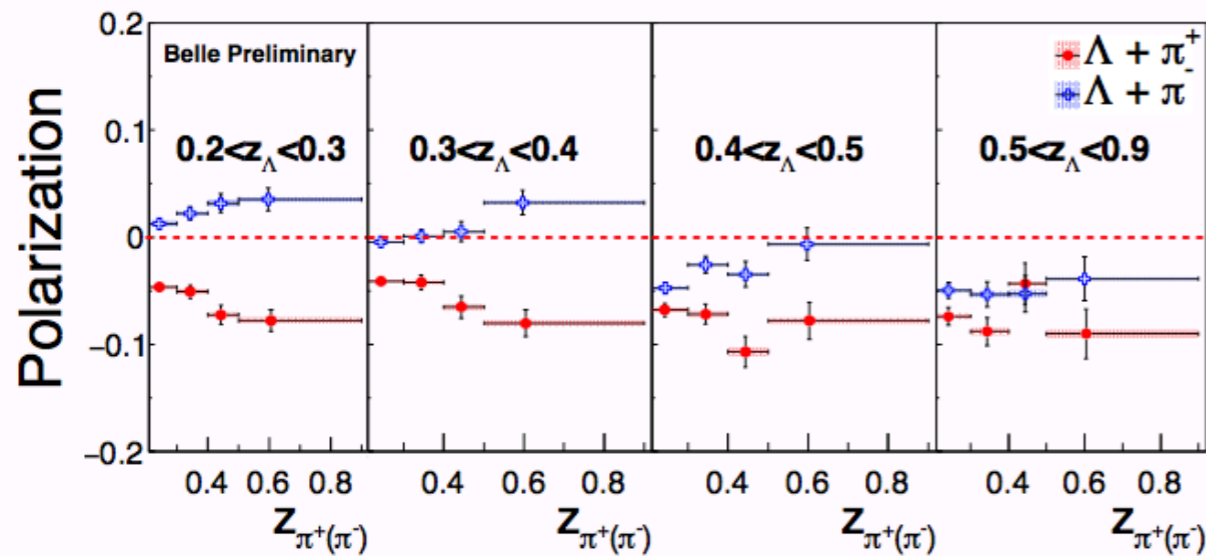
Fig 2:  $e^+e^- \rightarrow \pi^\pm + \Lambda^\uparrow + X$ , SU(3)-symmetric (thin) and broken (thick), solid/dashed is  $\pi^\pm$

Fig 3:  $e^+e^- \rightarrow \text{jet} + \Lambda^\uparrow + X$ , SU(3)-symmetric (solid) and broken (dashed) spin-averaged FFs

Fig 4:  $e^+e^- \rightarrow K^\pm + \Lambda^\uparrow + X$ , SU(3)-symmetric (thin) and broken (thick), solid/dashed is  $K^\pm$

Comparison to  $ep \rightarrow e'\Lambda^\uparrow X$  can be used to test universality of  $D_{1T^\perp}$

# Associated production at Belle



BELLE Collaboration, arXiv:1611.06648

Data does not follow our expectations, e.g. for  $\pi^+$  larger polarization than for  $\pi^-$

Needs to be looked into

Polarizing  $\Lambda$  FF

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future



# Using high energy hadron colliders

Validity of factorized description depends on a proper cross section description

This requires data at higher energies and higher  $p_T$

Available data is from experiments with  $\sqrt{s} \leq 62$  GeV, requiring large K factors

Why no  $\Lambda^\uparrow$  data from high energy hadron colliders, such as RHIC or Tevatron?

Capabilities to measure  $\Lambda$  polarization via  $\Lambda \rightarrow p \pi^-$  are usually restricted to the midrapidity region, where the degree of transverse polarization is very small

$P_\Lambda = 0$  at  $\eta=0$  in pp collisions in cms

Alternative: consider jet+ $\Lambda$  production:  $p p \rightarrow (\Lambda^\uparrow \text{jet}) \text{jet} X$

Such an asymmetry does not need to vanish at  $\eta = 0$

D.B., Bomhof, Hwang & Mulders, PLB 659 (2008) 127; D.B., arXiv:0907.1610

In fact, for  $E_{\text{jet}}/\sqrt{s} \ll 1$  (easily valid at LHC) and universal FFs, one can study

$p p \rightarrow (\Lambda^\uparrow \text{jet}) X$

D.B., arXiv:1007.3145

# Jet+ $\Lambda$ production

Consider two jets, with momenta  $K_j$  and  $K_{j'}$ , such that  $K_j \cdot K_{j'} = O(\hat{s})$

The  $\Lambda$  is part of one of the two jets, and has momentum  $K_\Lambda$  and polarization  $S_\Lambda$

An asymmetry can arise that is proportional to:  $\epsilon_{\mu\nu\alpha\beta} K_j^\mu K_{j'}^\nu K_\Lambda^\alpha S_\Lambda^\beta$

In principle, it is not power suppressed and it does not need to vanish at  $\eta = 0$

In the center of mass frame of the two jets the asymmetry is of the form:

$$SSA = \frac{d\sigma(+\mathbf{S}_\Lambda) - d\sigma(-\mathbf{S}_\Lambda)}{d\sigma(+\mathbf{S}_\Lambda) + d\sigma(-\mathbf{S}_\Lambda)} = \frac{\hat{\mathbf{K}}_j \cdot (\mathbf{K}_\Lambda \times \mathbf{S}_\Lambda)}{z M_\Lambda} \frac{d\sigma_T}{d\sigma_U}$$

$d\sigma_T/d\sigma_U$  depends on  $D_{1T}^\perp$

For further details see D.B., Bomhof, Hwang & Mulders, PLB 659 (2008) 127

Considered in hybrid factorization approach (assumption that initial partonic  $k_T$  distribution hardly affects the relative momentum of the  $\Lambda$  w.r.t. its jet for large jet transverse momentum)

# Jet+ $\Lambda$ production

The process  $p p \rightarrow (\Lambda^\uparrow \text{jet}) \text{jet} X$  can be studied at RHIC and LHC

For instance, ALICE can measure  $\Lambda$ 's over a wide  $p_T$  range, in a typical yearly run at least up to 16 GeV/c

Rapidity coverage of ALICE:  $-0.9 \leq \eta \leq +0.9$

For jet rapidities in this kinematic region, the cross section is dominated by gluon-gluon ( $gg \rightarrow gg$ ) scattering, if gluons fragmenting into  $\Lambda$ 's are as important as quarks

This leads to

$$\frac{d\sigma_T}{d\sigma_U} \approx \frac{D_{1T}^{\perp g}(z, K_{\Lambda T}^2)}{D_1^g(z, K_{\Lambda T}^2)}$$

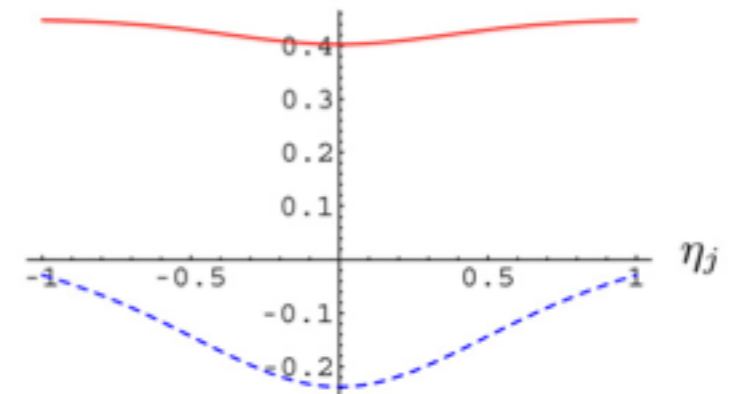
No model or fit for  $D_{1T}^{\perp g}$  is available yet, so no predictions can be made yet

Recall that the fit of  $D_{1T}^\perp$  to  $pp \rightarrow \Lambda^\uparrow X$  data is not sensitive to  $g \rightarrow \Lambda X$

# Jet+ $\Lambda$ production at the LHC

If it happens that  $D_{1T}^{\perp g} \ll D_{1T}^{\perp q}$ , then one finds for  $\eta_j' \approx -\eta_j$  ( $x \equiv x_1 \approx x_2$ )

$$\frac{d\sigma_T}{d\sigma_U} \approx \frac{\sum_q f_1^q(x) D_{1T}^{\perp q}(z, K_{\Lambda T}^2)}{\sum_q f_1^q(x) (D_1^q(z, K_{\Lambda T}^2) + D_1^g(z, K_{\Lambda T}^2)) + f_1^g(x) D_1^g(z, K_{\Lambda T}^2) / 0.8}$$

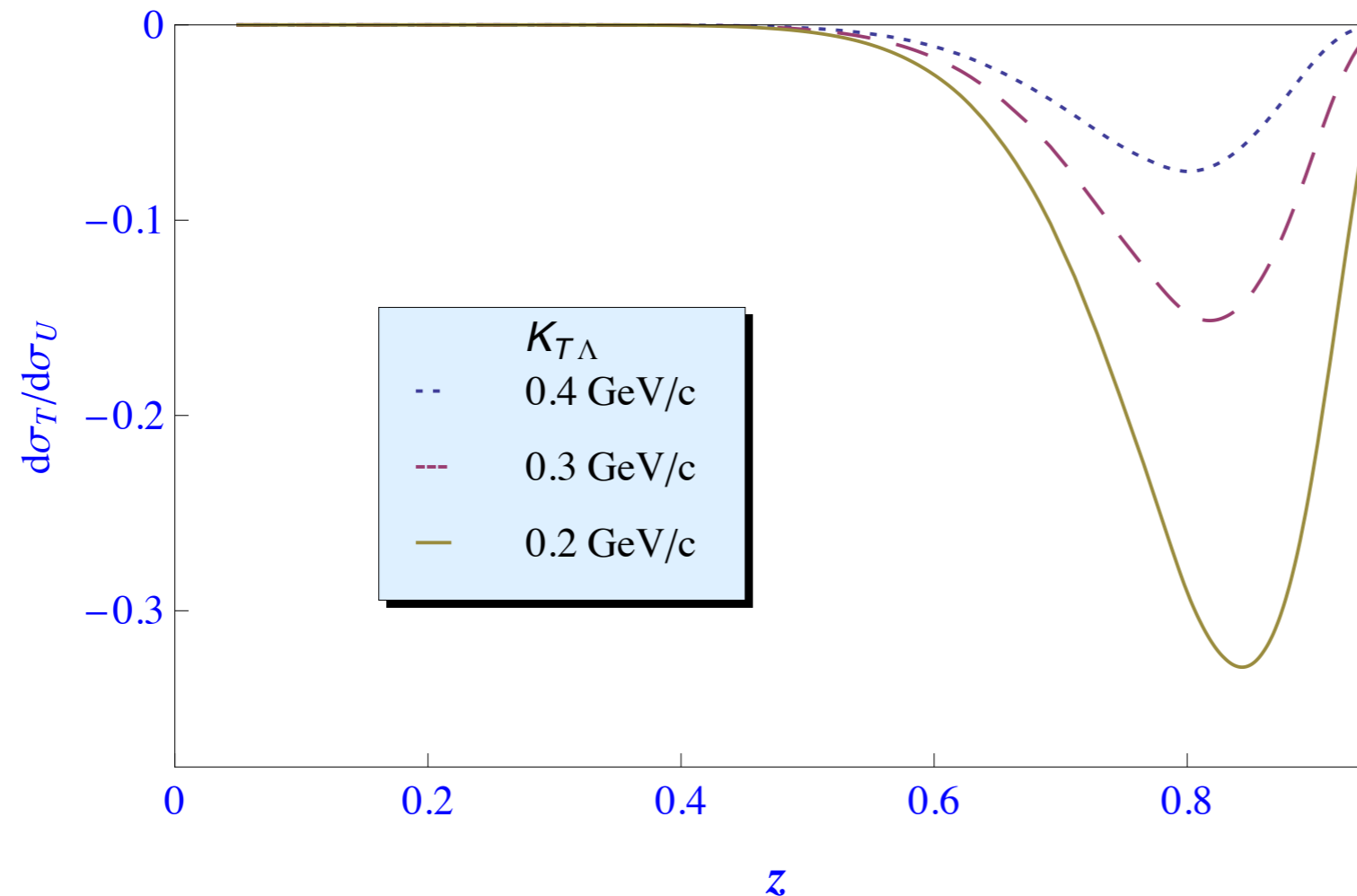


This includes also in the denominator the  $qg \rightarrow qg$  subprocess

Will use extracted ratios for  $D_{1T}^{\perp q}/D_{1T}^{\perp q}$  with DSV & IMR which have  $D_1^g \ll D_1^q$

Expected to yield qualitative estimates only

# Jet+ $\Lambda$ production at the LHC



using DSV

$\eta_j, \eta_{j'} = 0$

$|K_{\perp j}|, |K_{\perp j'}| = 70 \text{ GeV}$

The asymmetry exceeds -1 for smaller  $K_{T\Lambda}$  at large  $z$ , hence is overestimated

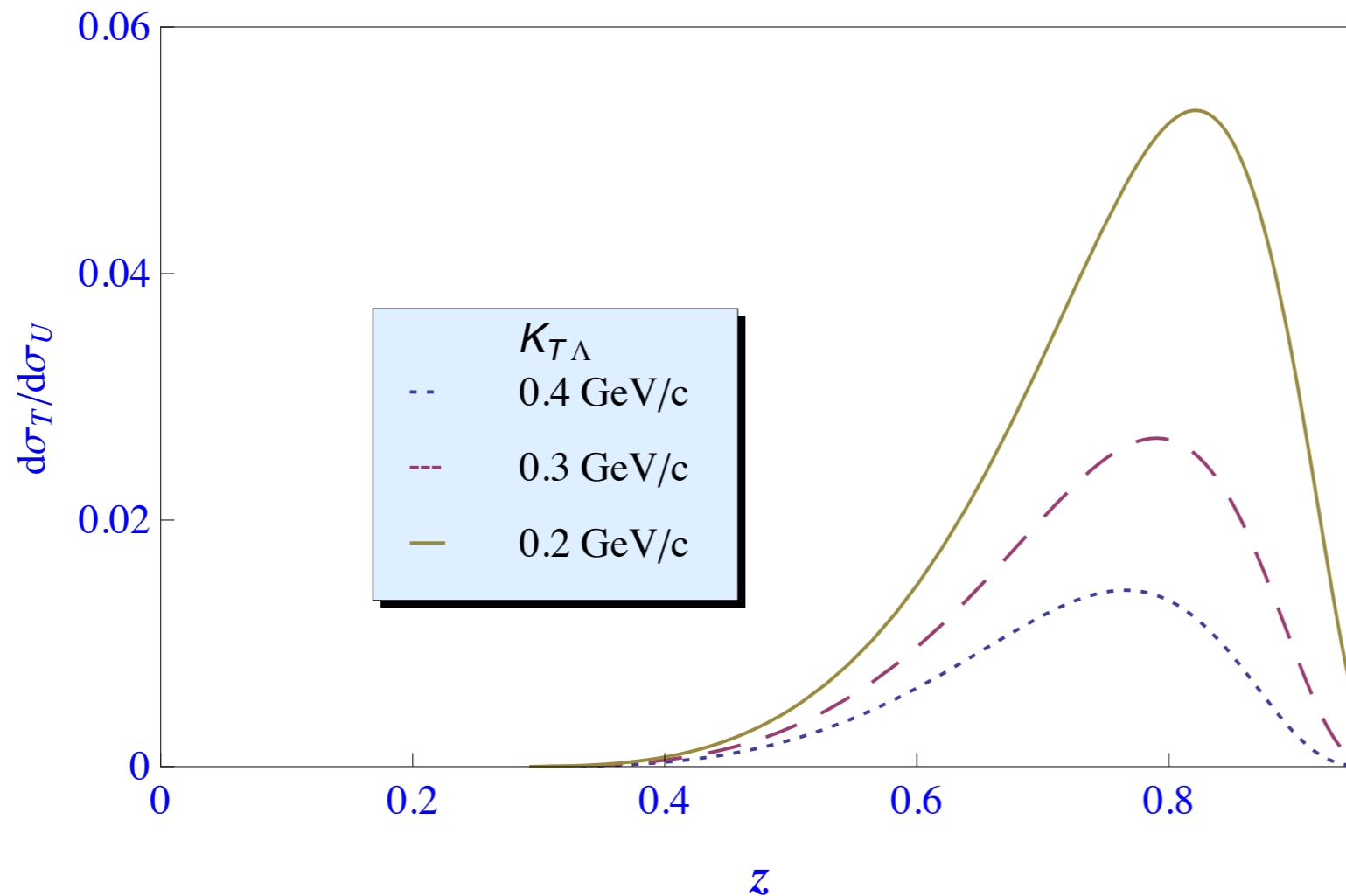
Hardly any asymmetry at smaller  $z$  due to fit to low energy data

Need not be realistic at high energies

# Jet+ $\Lambda$ production at the LHC

$D_{1T}^\perp$  extracted using SU(3) breaking unpolarized FFs [IMR] yields very different result

Indumathi et al., PRD 58 (1998) 094014



Asymmetry is very sensitive to the cancellation between u, d and s contributions

# Universality of $D_{1T}^\perp$

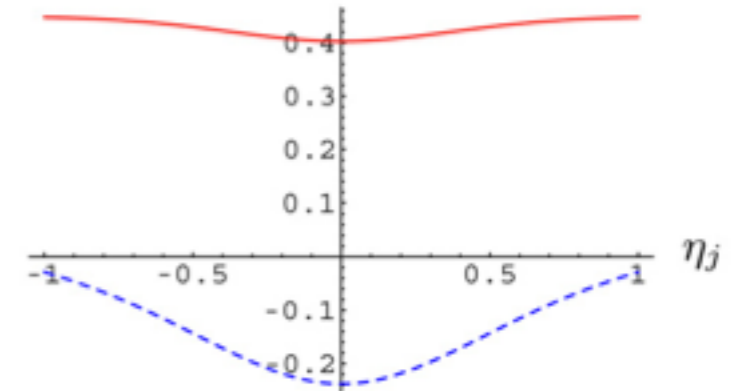
$p p \rightarrow (\Lambda^\uparrow \text{jet}) \text{ jet } X$  allows a test of universality at RHIC and LHC through  $\hat{t}/\hat{s}$  dependence, but not too distinctive

$$a_g(y) = \frac{d\hat{\sigma}_{gg \rightarrow [g]g}}{d\hat{\sigma}_{gg \rightarrow gg}}$$

$$a_q(y) = \frac{d\hat{\sigma}_{qg \rightarrow [q]g}}{d\hat{\sigma}_{qg \rightarrow qg}}$$

$$b(y) = \frac{d\hat{\sigma}_{qg \rightarrow qg}}{d\hat{\sigma}_{gg \rightarrow gg}}$$

$b(y) + b(1-y)$  (solid line) and  $b(y)a_q(y) + b(1-y)a_q(1-y)$



Comparing  $e^+e^-$  and  $ep$  seems more promising

Assuming universality of  $D_{1T}^\perp$  one can consider  $p p \rightarrow (\Lambda^\uparrow \text{jet}) X$  if  $E_{\text{jet}}/\sqrt{s} \ll 1$

D.B., 1007.3145

The away-side jet is then not needed, allowing to study a rather simple **asymmetry in the lab frame**  $\propto K_j \cdot (K_\Lambda \times S_\Lambda)$  with analyzing power:

$$\frac{\int \frac{dy}{y} \sum_q (f^{qg} + f^{gq}) d\hat{\sigma}_{qg} D_{1T}^{\perp q}}{\int \frac{dy}{y} \left[ \sum_q (f^{qg} + f^{gq}) d\hat{\sigma}_{qg} (D_1^q + D_1^g) + f^{gg} d\hat{\sigma}_{gg} D_1^g \right]}$$

$$f^{ab} \equiv x_1 f_1^a(x_1) x_2 f_1^b(x_2), \quad d\hat{\sigma}_{ab} \equiv d\hat{\sigma}_{ab \rightarrow ab}(y) + d\hat{\sigma}_{ab \rightarrow ab}(1-y) \quad \text{with } y = -\hat{t}/\hat{s}$$

# Forward rapidity data

$\Lambda$  polarization is also very interesting in  $pA$  reactions at very high  $\sqrt{s}$ , large  $A$  and  $\eta$

In this kinematic regime of small  $x$ , saturation of the gluon density is expected

The saturation scale  $Q_s$  and even its evolution with  $x$  could be probed in this way

D.B. & Dumitru, PLB 556 (2003) 33; D.B., Utermann & Wessels, PLB 671 (2009) 91

However, in the forward direction often protons cannot be identified, which hampers the measurement of  $\Lambda$  polarization

None of the existing data is in the saturation regime

Suggestion: use neutral decays  $\Lambda \rightarrow n \pi^0$  (B.R. 1/3) to measure  $\Lambda$  polarization at forward rapidities

Cork et al., PR 120 (1960) 1000; Olsen et al., PRL 24 (1970) 843



# Hadron production in the saturation regime

The cross section of forward hadron production in the (near-)saturation regime:

$$\text{pdf} \otimes \text{dipole cross section} \otimes \text{FF}$$

Dumitru & Jalilian-Marian, PRL 89 (2002) 022301

Since  $D_{IT}^\perp$  is  $k_T$ -odd, it essentially probes the derivative of the dipole cross section

At transverse momenta of  $O(Q_s)$  the dipole cross section changes most

This leads to a  $Q_s$ -dependent peak in the  $\Lambda$  polarization

First demonstrated for the McLerran-Venugopalan model, which has constant  $Q_s$

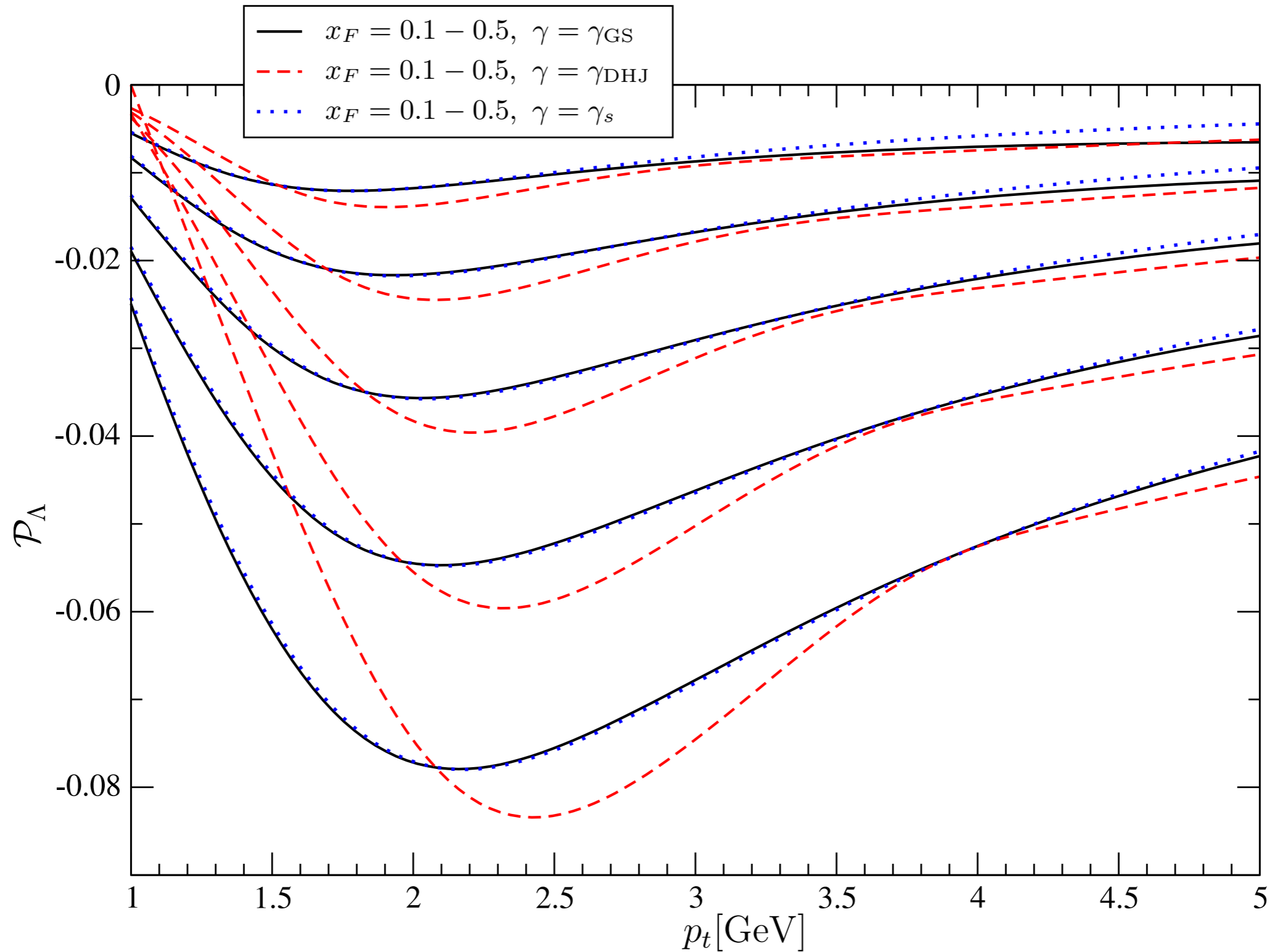
D.B. & Dumitru, PLB 556 (2003) 33

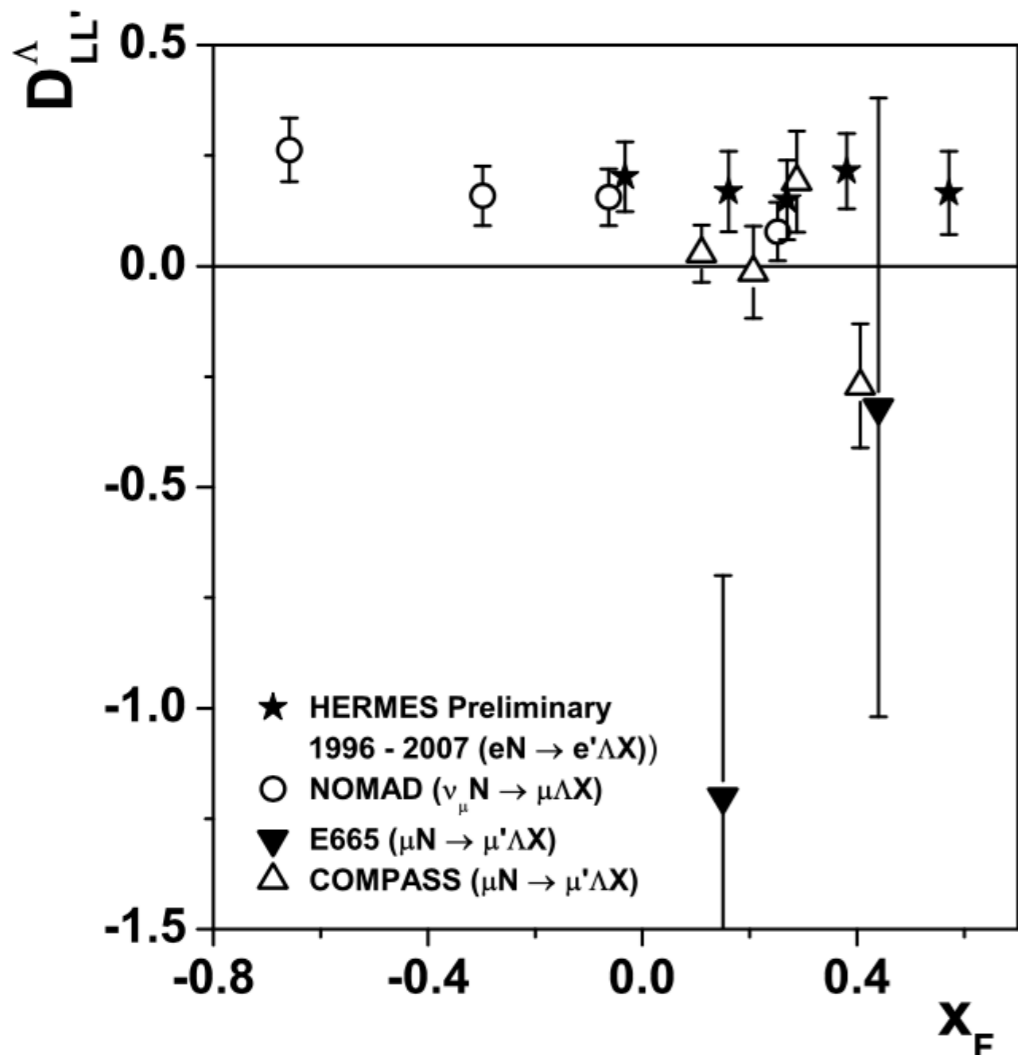
For an  $x$ -dependent  $Q_s$  it is a priori not clear whether this signature remains

But various CGC models lead to same conclusion about peak of  $\Lambda$  polarization:

Its  $x_F$  dependence is to very good approximation the  $x$  dependence of  $Q_s$ !

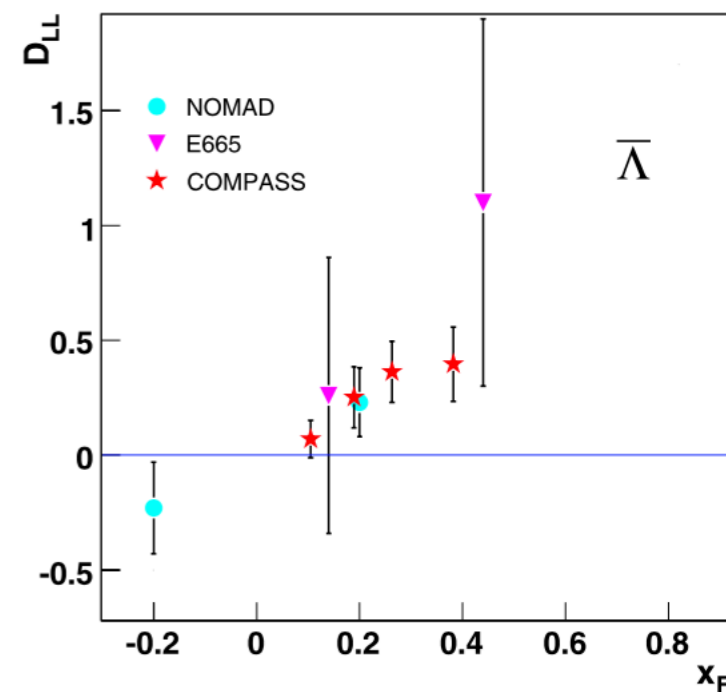
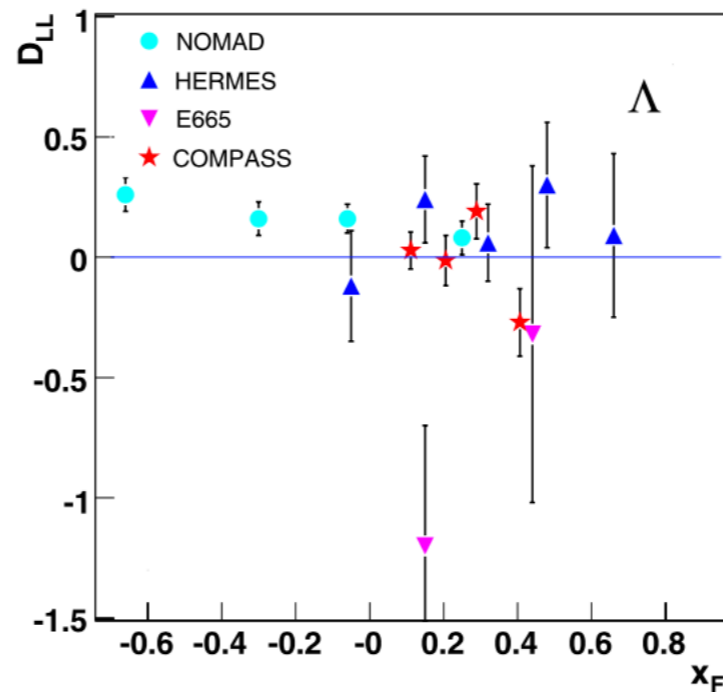
# $\Lambda$ polarization in $p + \text{Pb} \rightarrow \Lambda^\uparrow + X$ at $\sqrt{s} = 8.8 \text{ TeV}$



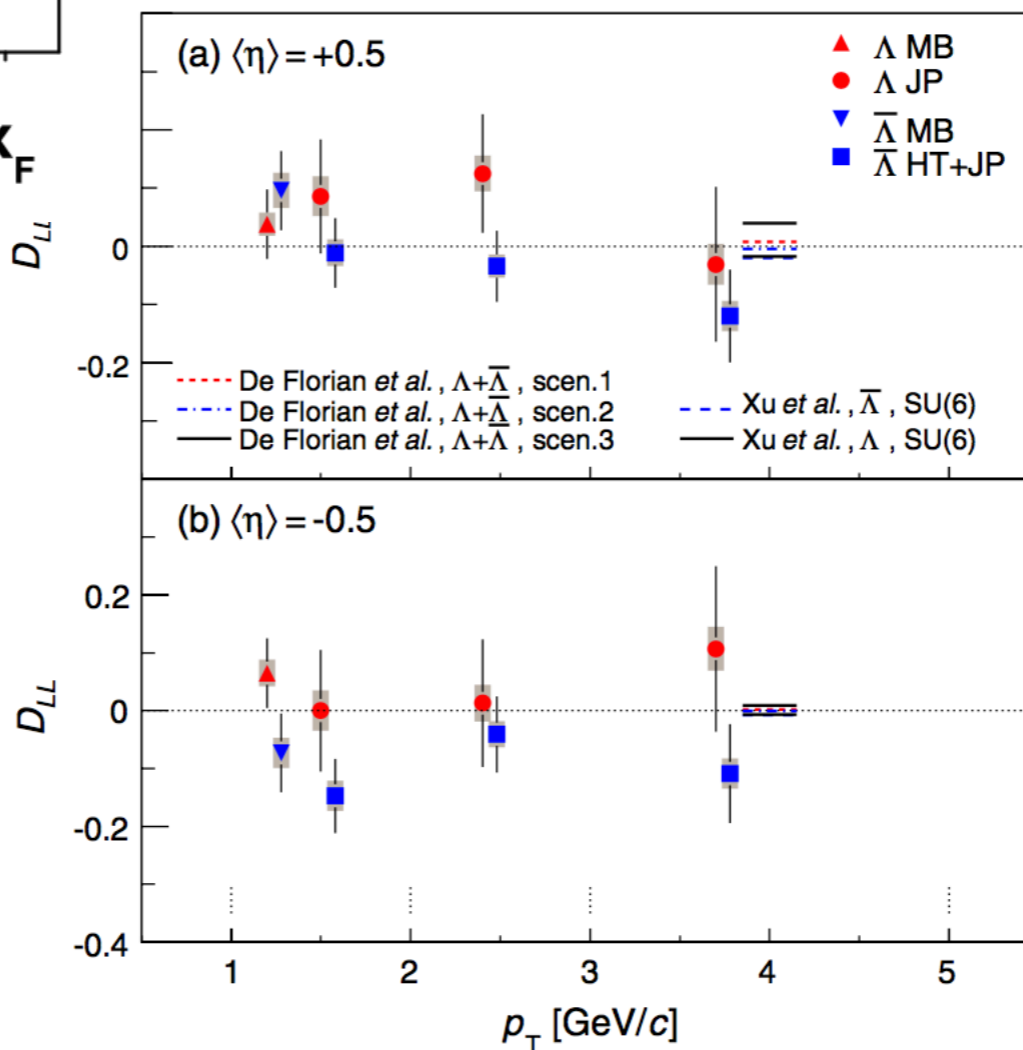


HERMES@SPIN2010

$D_{LL}$

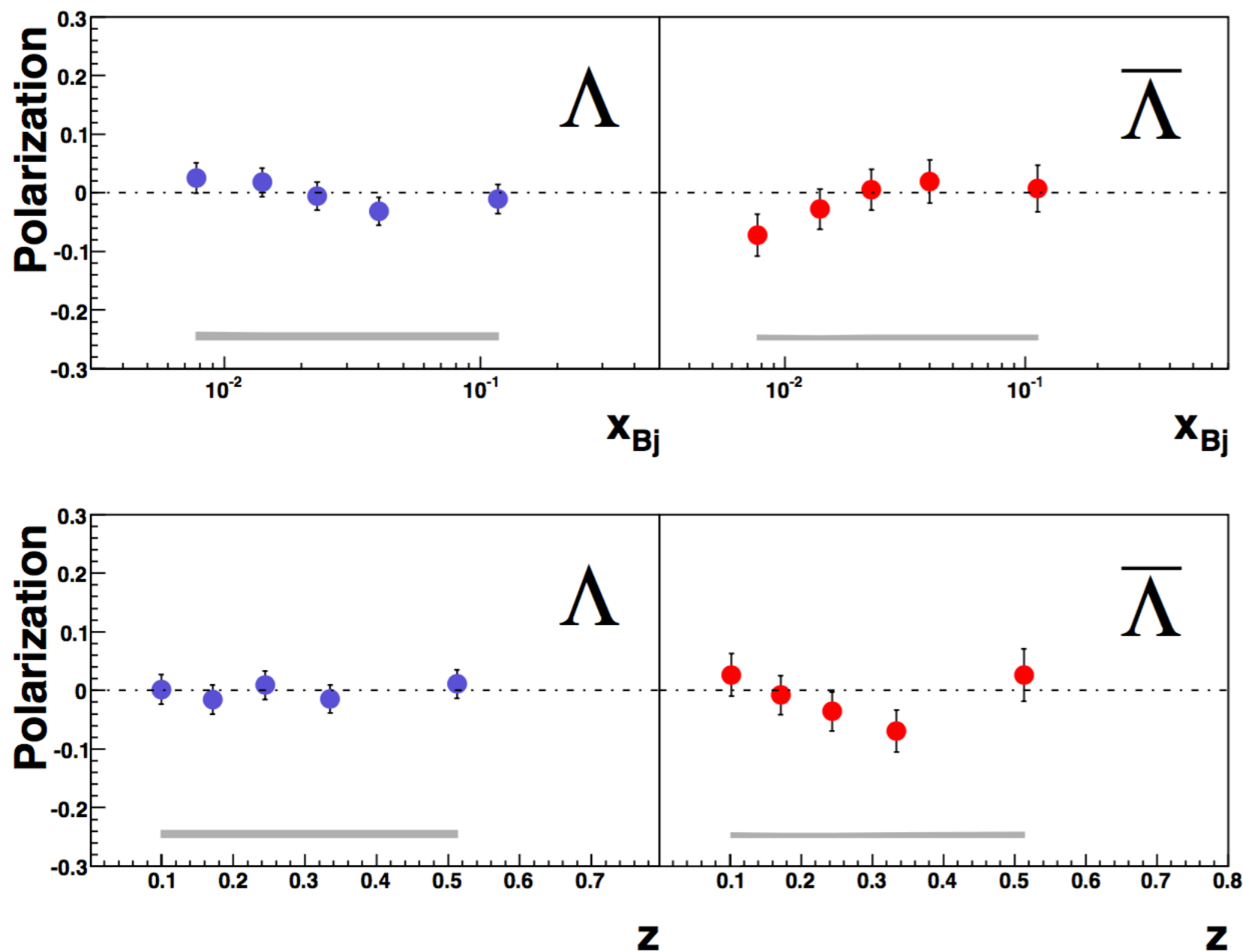


COMPASS, EPJC 2009



STAR, PRD 2009

# D<sub>NN</sub> in SIDIS ( $\mu p^\uparrow \rightarrow \mu \Lambda^\uparrow X$ )

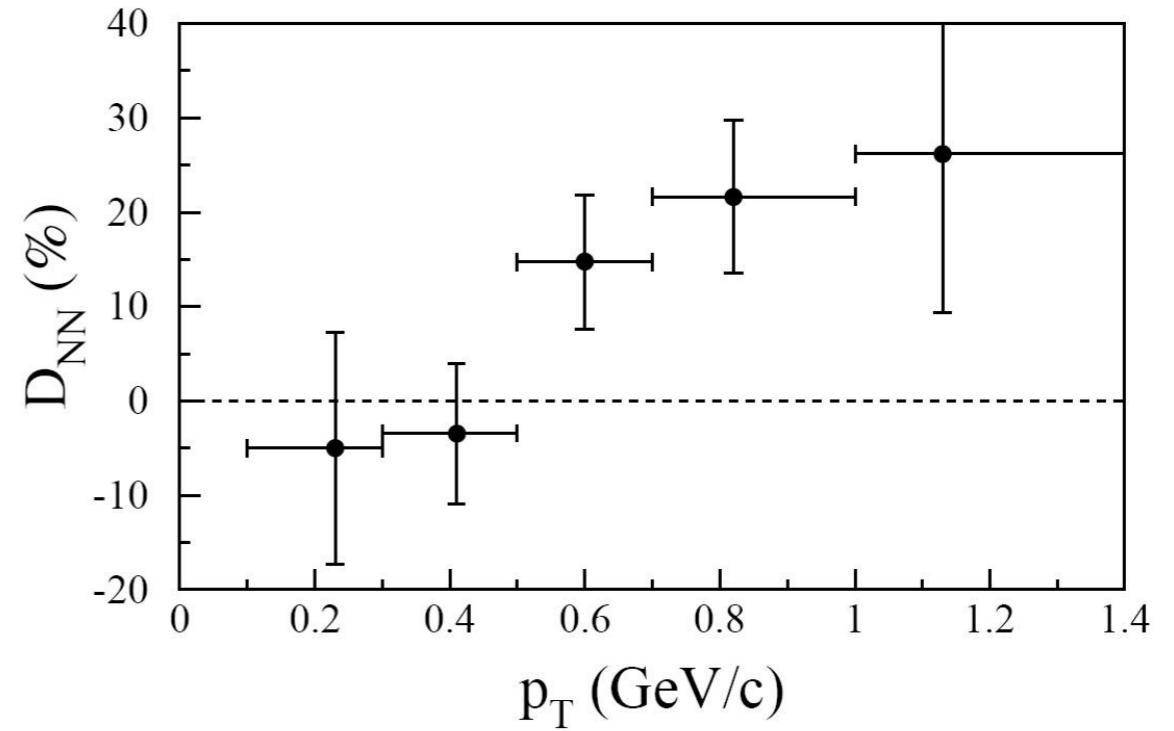
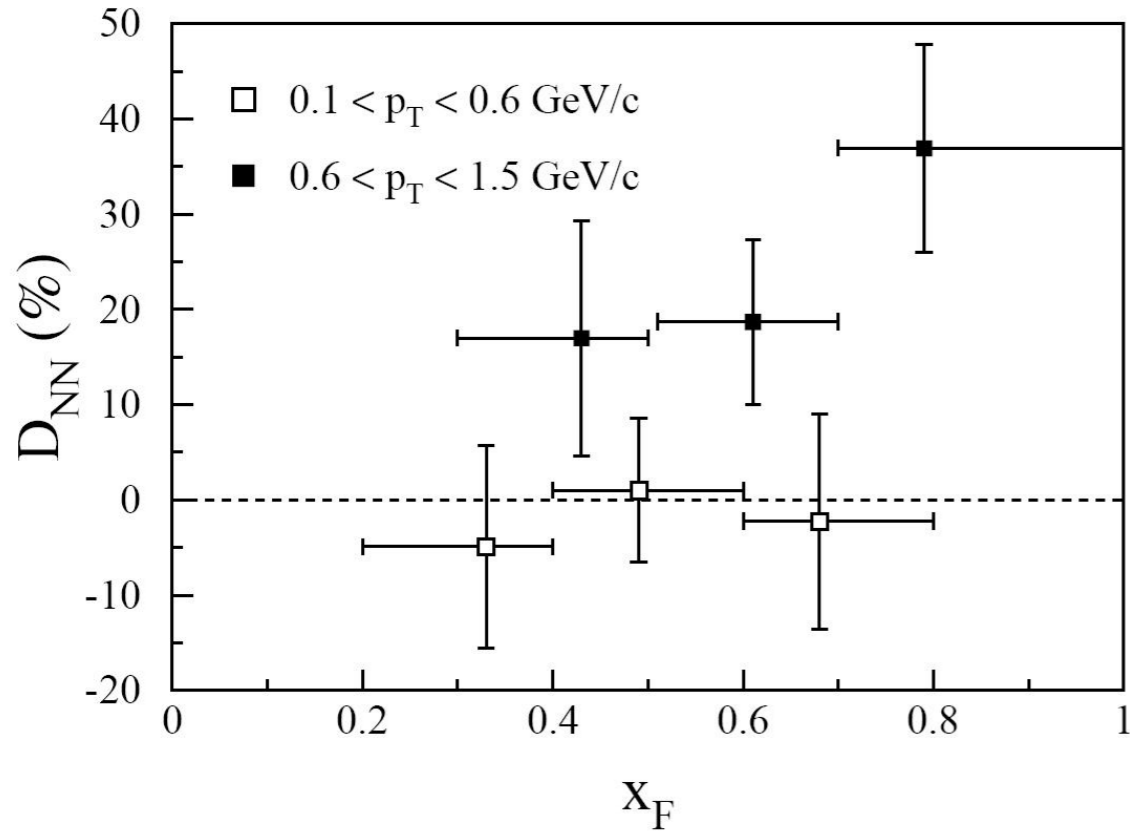


T. Negrini, COMPASS,  
PhD thesis, 2009

Figure 6.3:  $\Lambda$  and  $\bar{\Lambda}$  polarizations with statistical errors as a function of  $x_{Bj}$  and  $z$  in the 2007 COMPASS data on a transversely polarized proton target with  $Q^2 > 1$  (GeV/c)<sup>2</sup> and  $0.1 < y < 0.9$ . The lower band shows the upper limit of the systematic error, estimated by the pulls distribution of false polarizations (same as Fig. 5.15).

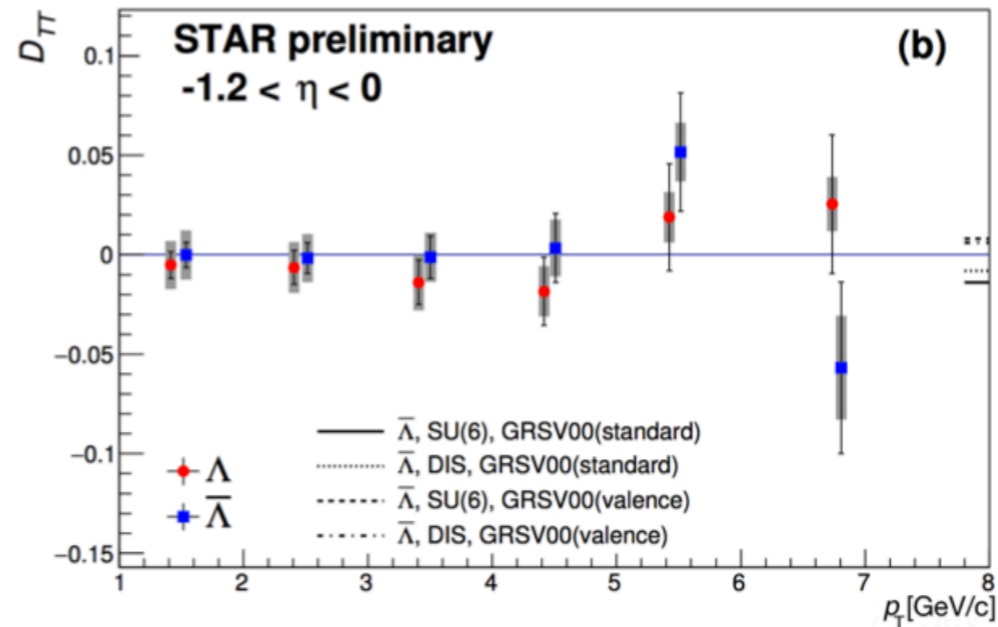
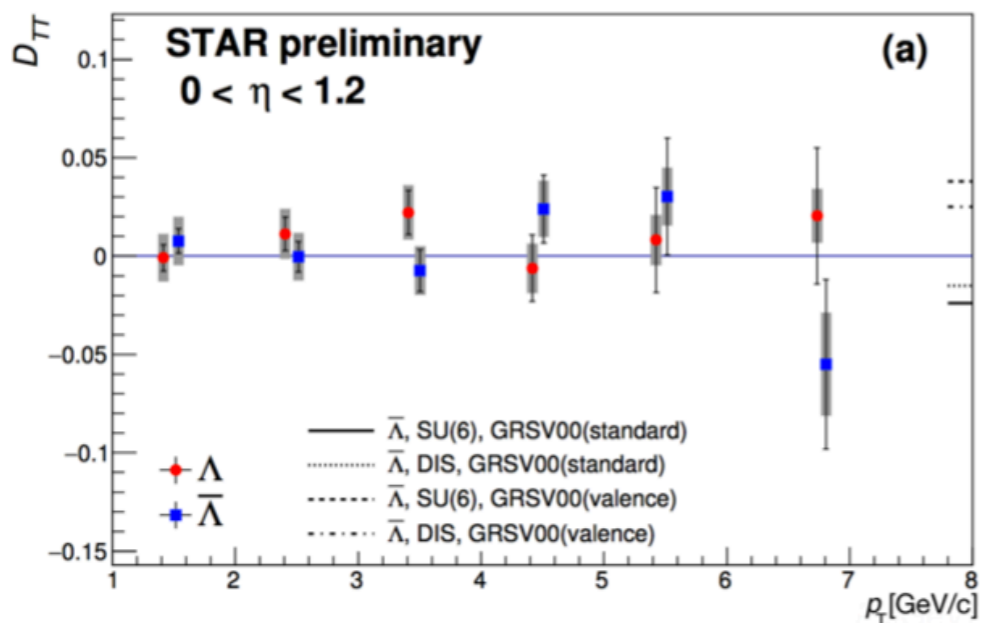
Likely implies small  $H_1^{u,d}(z)$  and/or small  $h_1^s(x)$  in the measured range

# D<sub>NN</sub> in pp



E704 Collaboration, Bravar et al., PRL 78 (1997) 4003

At E704 ( $\sqrt{s} \approx 20$  GeV) not  $h_1H_1$  (factorization is doubtful at low  $p_T < 1.5$  GeV)



STAR Collab.,  
PoS DIS2017  
(2018) 225

# Conclusions

# Open issues

- $\Lambda$  FFs are not yet fitted with data from LHC. AKK08's observation of "a possible inconsistency between the pp and  $e^+e^-$  reaction data" not yet solved
- More SIDIS  $\Lambda^\uparrow$  data is needed & comparison to ZEUS data needs to be made
- Evolution from BELLE to LEP might work regarding magnitude, to be checked
- Systematics of associated production at BELLE needs to be understood still
- Nonzero  $D_{1T^\perp} \Rightarrow$  unsuppressed  $K_j \cdot (K_\Lambda \times S_\Lambda)$  asymmetry in  $pp \rightarrow (\Lambda^\uparrow \text{jet}) X$  at midrapidity, not yet experimentally studied, may clarify the role of gluons
- The  $k_T$ -odd nature of  $D_{1T^\perp}$  can be of use to small- $x$  physics:  $x_F$  dependence of the peak of  $\Lambda$  polarization directly probes the  $x$  dependence of  $Q_s$   
In principle possible at LHC (at RHIC the peak is likely at too low  $p_T$ )
- Still not clear from  $D_{NN}$  whether transversity FF is sizable