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Surface Plasmon Slowing Down and Cherenkov-Type THz Emission in Graphene Based Structure

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- 1. Introduction
- 2. Graphene and CNTs: physical properties
- 3. Surface plasmon in CNT and graphene
- 3. THz absorption peak
- 4. Nano -Traveling Wave Tube
- 5. Generation of THz radiation in multi-layer graphene/ polymer sandwiches
- 6. Conclusion & Acknowledgments



Which are current technological trends in applied electromagnetics?

- Miniaturization of electric circuits & components ...
- Energy consumption dropping ...
- Opening up the mm-Wave & THz frequency ranges

Owing to that, <u>nanosized</u> elementary circuits components, <u>nanoscale</u> integration, and <u>nanostructured</u> electromagnetic materials **are on demand**

Extra-small EM radiation sources are among them



Channel Length = Gate Length - 2 x (Diffusion Length)



Travelling-wave tubes



The Cherenkov radiation is governed by the synchronization condition w-ku=0, where k is the wave vector and u is the electron velocity Travelling-wave tubes: R Kompfner 1952 *Rep. Prog. Phys.* **15** 275

- an electron gun,
- a focusing structure,
- a slowing-down system,
- an electron collector



Can one provide the generation conditions on nanoscale?

- Ballisticity of electron motion on the proper distance
- Slowing down of EM wave to satisfy the synchronism condition with electron beam
- Large enough current density in a nanoobject



Graphene & Carbon Nanotube



Graphene & CNTs: Physical properties

PROBLE

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	Si	Cu	SWCNT	MWCNT	Graphene or GNR
Max current density (A/cm²)	-	107	>1x10 ⁹ Radosavljevic, et al., <i>Phys. Rev. B</i> , 2001	>1x10 ⁹ Wei, et al., <i>Appl. Phys. Let.</i> , 2001	>1x10 ⁸ Novoselov, et al., <i>Science</i> , 2001
Melting point (K)	1687	1356	3800 (graphite)		
Tensile strength (GPa)	7	0.22	22.2 ± 2.2	11-63	
Mobility (cm²/V-s)	1400		>10000		>10000
Thermal conductivity (×10 ³ W/m-K)	0.15	0.385	1.75-5.8 Hone, et al., <i>Phys. Rev. B</i> , 1999	3.0 Kim, et al., <i>Phys. Rev. Let.</i> , 2001	3.0-5.0 Balandin, et al., <i>Nano Let.</i> , 2008
Temp. Coefficient of Resistance (10 ⁻³ /K)	-	4	<1.1 Kane, et al., <i>Europhys. Lett.</i> , 1998	-1.37 Kwano et al., <i>Nano Lett.</i> , 2007	-1.47 Shao et al., <i>Appl. Phys. Lett.</i> , 2008
Mean free path (nm) @ room temp.	30	40	>1,000 McEuen, et al., Trans. Nano., 2002	25,000 Li, et al., <i>Phys. Rev. Let.</i> , 2005	~1,000 Bolotin, et al., Phys. Rev. Let., 2008
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Radial dependence of the conductivity below and in the optical transitions band



PHYSICAL REVIEW B

VOLUME 60, NUMBER 24

15 DECEMBER 1999-II

Electrodynamics of carbon nanotubes: Dynamic conductivity, impedance boundary conditions, and surface wave propagation

G. Ya. Slepyan and S. A. Maksimenko A. Lakhtakia O. Yevtushenko A. V. Gusakov



Electrodynamics of CNTs

PHYSICAL REVIEW B

VOLUME 60, NUMBER 24

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 $\lambda >> b, \lambda >> R_{cn}, b = 0.142 \,\text{HM}$

Electrodynamics of carbon nanotubes: Dynamic conductivity, impedance boundary conditions, and surface wave propagation

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In optical and below ranges

$$\left(1 + \frac{l_0}{k^2 (1 + i/\omega\tau)^2} \frac{\partial^2}{\partial z^2} \right) \left(H_{\phi} \Big|_{\rho = R + 0} - H_{\phi} \Big|_{\rho = R - 0} \right) = \frac{4\pi}{c} \sigma_{zz} E_z \Big|_{\rho = R},$$

$$H_z \Big|_{\rho = R - 0} - H_z \Big|_{\rho = R + 0} = 0, \quad E_{z, \phi} \Big|_{\rho = R - 0} - E_{z, \phi} \Big|_{\rho = R + 0} = 0$$

Spatial dispersion parameter $l_0 \sim 10^{-5}$ for metallic CNTs

Solution of the conductivity problem accounting for the spatial confinement effects couples classical electrodynamics and physics of nanostructures



Surface Wave in CNTs

The problem statement:

consider the propagation of surface waves along an isolated, infinitely long CNT in vacuum. The CNT conductivity is assumed to be axial. The investigated eigenwaves satisfy the Maxwell equations, EBCs and the radiation condition (absence of external field sources at the infinity)

The statement is analogous to the problem of macroscopic spiral slowdown systems for microwave range [L. Weinstein, Electromagnetic waves, 1988].

Dispersion equation of surface waves

$$\frac{\kappa^2}{k^2} K_q(\kappa R) I_q(\kappa R) = \frac{ic}{4\pi R\sigma_{zz}} \left(1 - \frac{\kappa^2 + k^2}{(\omega + i/\tau)^2} c^2 l_0\right).$$



Surface Wave Propagation

Complex-valued slow-wave coefficient **b** for a polarsymmetric surface wave

$$\operatorname{Re}\beta = \frac{v_{ph}}{c} = \operatorname{Re}\frac{k}{h}$$



G. Ya. Slepyan and S. A. Maksimenko A. Lakhtakia O. Yevtushenko A. V. Gusakov



Carbon Nanotube as EM device (primarily in THz range):

- ✓ Electromagnetic slow-wave line: v_{ph}/c ~0.02
- Dispersionless surface wave nanowaveguide and high-quality interconnects (PRB 1999)
- ✓ Terahertz-range antenna (PRB 1999,PRB 2006, PRB 2010, PRB2012)
- ✓ Thermal antenna (PRL 2008)
- Monomolecular traveling
 wave tube (PRB 2009)
- strong influencing the spontaneous decay rate (PRL 2002)

Antenna resonances for 1 mkm CNT are in the THz range because the plasmon slowing





Theory predicts the slowing-down of surface wave in a metallic SWCNT as much as 50-100 times;



The answer can be found from observing antenna resonances red shift



Experimental observations of THz peak in <u>C</u>NT-based composites



Fig. 1. (a) for the distribution of the distribution of the distribution of the distribution of the fill of the distribution (1) and α_{\perp} directions. The MG fits [Equation (1)] are also presented.

Bommeli F., et al. Synt. Met. **86,** 2307 (1997).





FIG. 3. (Color online) Temperature dependence of the optical conductivity of the two samples.



One can suppose that THz finitelength (antenna) resonances explain THz conductivity peak in CNT composites



(b) Real part of the conductivity together with the Drude and Lorentz contributions to the overall fit (solid line).

T. Kampfrath, phys. stat. sol. (b) 244, No. 11, 3950–3954 (2007)



Experimental evidence of localized plasmon resonance in composite materials containing single-wall carbon nanotubes

M. V. Shuba, A. G. Paddubskaya, A. O. Plyushch, P. P. Kuzhir, G. Ya. Slepyan, and S. A. Maksimenko Institute for Nuclear Problems, Belarus State University, Bobruiskaya 11, 220050 Minsk, Belarus

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THz peak: experiment

Direct experimental demonstration of the correlation between the THz peak frequency and the SWCNT length. That is, the **direct experimental evidence of the slowing down in CNTs and the FIR-THz antenna**





Method of the calibrated CNTs fabrication

Distribution of the CNT bundles before (a)



M V Shuba^{1,7}, A G Paddubskaya², P P Kuzhir^{1,3}, S A Maksimenko^{1,3}, E Flahaut⁴, V Fierro⁵, A Celzard⁵ and G Valusis^{2,6}

in the terahertz range

Shuba et al., **PRB 2013**

0

2-11



(a)

The basis of generation in CNTs and graphene

The possibility of strong slowing down of EM wave

- G.Ya. Slepyan, S. A. Maksimenko, A. Lakhtakia, O. Yevtushenko, A.V. Gusakov, Phys. Rev. B 60, 17136 (1999).
- M.V. Shuba et al., Phys. Rev. B 85 165435, 2012

Ballistic electron transport (up to tens of μm)

- C. Berger, P. Poncharal, Y. Yi, W.A. de Heer, J. Nanosci. Nanotechn., 3, 171 (2003);
- J. Baringhaus, M. Ruan, F. Edler, & W.A. de Heer, Nature 506, 349–354, 2014

Very large current density (up to 10^{10} A/cm²)

- M. Radosavljevi'c, J. Lefebvre, and A. T. Johnson, Phys. Rev. B 64, 241307, 2001;
- S.-B. Lee, K.B.K. Teo, L.A.W. Robinson, et al., J. Vac. Sci. Technol. B 20, 2773 (2002);

Čerenkov lasing in a CNT



K.G. Batrakov, P.P. Kuzhir*, S.A. Maksimenko

K. G. Batrakov, P. P. Kuzhir, S. A. Maksimenko, *Proc.SPIE* 6328, 63280Z (2006)
K. G. Batrakov, S. A. Maksimenko, P. P. Kuzhir, and C. Tomsen, *Phys. Rev. B* 79, 125408 (2009).
K.G. Batrakov, O.V. Kibis, Polina P. Kuzhir, M. R. Costa, and M. E. Portnoi, Vol. 4, 041665 (2010).
K. Batrakov, V. Saroka, S. Maksimenko, Chr. Thomsen, Journal of Nanophotonics, 6, 061719 (2012).



Dispersion equation

$$k - k_m = -\frac{\omega_L^2}{8mk_mc^2} \sum_l B_{nl} \left\{ \frac{1}{-\hbar\omega + \varepsilon_n(p_n) - \varepsilon_l(p_n - \hbar k)} + \frac{1}{\hbar\omega + \varepsilon_n(p_n) - \varepsilon_l(p_n + \hbar k)} \right\}$$

 ω_L^2 is the Langmuir frequency squared, proportional to the current density.

$$\varepsilon_{l}(p_{n} \pm \hbar k) \approx \varepsilon_{l}(p_{n}) \pm \hbar k \frac{\partial \varepsilon_{l}}{\partial p_{n}} + \frac{\hbar^{2}k^{2}}{2} \frac{\partial^{2}\varepsilon_{l}}{\partial p_{n}^{2}}$$

$$v_{l} = \frac{\partial \varepsilon_{l}(p_{n})}{\partial p_{n}} \longrightarrow \text{group velocity of nanotube electron}$$

$$\pm \hbar \omega + \varepsilon_n(p_n) - \varepsilon_l(p_n \pm k) = \pm \hbar(\omega - kv_l \pm \Omega_{nl}) + \frac{\hbar^2}{2} \frac{\partial^2 \varepsilon_l}{\partial p_n^2} k^2$$

Typical dispersion equation for second order Cherenkov instability:

$$k - k_m \sim -\frac{\omega_L^2}{\left(\omega - k v_l\right)^2}$$

Threshold Current and Instability Increment





Estimated wave retardation in a SWCNT reaches 50-100 times

• G. Slepyan et al, PRB 1999

In double-walled CNT:

For long wavelength, when l >> d (*d* is the distance between CNTs), frequencies can be approximately written as:

 $\omega_{+} \sim \omega_{1}(R_{1}) + \omega_{2}(R_{2})$ and $\omega_{-} \sim |\omega_{1}(R_{1}) - \omega_{2}(R_{2})|$

Phase velocity corresponding to frequency \mathcal{O}_{-} , $v_{ph-} = \mathcal{O}_{-}/k$, can be significantly less than the phase velocities in a single walled nanotube

• K.G. Batrakov, P.P. Kuzhir, S.A. Maksimenko, Physica B, 405, 3050(2010),

However $\omega_1(R_1) \neq \omega_2(R_2)$, therefore decreasing of phase velocity in two-walled CNT is limited.

Does bilayer graphene show no such drawback?.....



Decreasing the phase velocity in two-walled CNT is limited. Does bilayer graphene show no such drawback?....

It turns out that the phase velocity in bilayer graphene exceeds phase velocity in graphene monolayer. Electron tunneling between graphene layers is guilty.

Tunneling should be suppressed.

It can be realized in spatially separated double-layer or multilayer graphene.

 K. Batrakov, V. Saroka, S. Maksimenko, Chr. Thomsen, J. of Nanophotonics, 6, 061719 (2012)



Fabrication of multi-layerd PMMA/Graphene structures



Schematic representation of graphene sandwich fabrication, consisting of a number of repeating steps, and final graphene/PMMA multilayer structure containing here four graphene sheets. The lateral dimensions of the samples are 7.2 mm * 3.4 mm for MW measurements and cycle sample with diameter 1 cm for THz measurements.



Graphene-like thin films in microwaves

Graphene-like films being 100-1000 times thinner than skin depth provide reasonably high EM attenuation in microwave frequency range, caused by absorption mechanism



4 : 7191 (2014)

OPEN

SUBJECT AREAS: GRAPHENE ELECTRONIC PROPERTIES AND DEVICES NANOSCALE MATERIALS Flexible transparent graphene/polymer multilayers for efficient electromagnetic field absorption

K. Batrakov¹, P. Kuzhir¹, S. Maksimenko¹, A. Paddubskaya¹, S. Voronovich¹, Ph Lambin², T. Kaplas³ & Yu Svirko³

EM absorption is as high as 50% for PyC film of 75 nm thickness and a few layers graphene, 1.5-2 nm thick.



Fabrication of multi-layerd PMMA/Graphene structures



APPLIED PHYSICS LETTERS 108, 123101 (2016)

Enhanced microwave-to-terahertz absorption in graphene

K. Batrakov,^{1,a)} P. Kuzhir,¹ S. Maksimenko,¹ N. Volynets,¹ S. Voronovich,¹ A. Paddubskaya,⁴ G. Valusis,² T. Kaplas,³ Yu. Svirko,³ and Ph. Lambin⁴



The problem statement



Consider an electron beam propagating along the x axis parallel to a graphene sheet or multilayer graphene s and wich comprising graphene sheets separated by layers of a medium with a dielectric functions ε .

Let us examine the propagation of surface waves along the sandwich in free space, assuming the distances between the graphene layers to be large on the atomic scale and, therefore, neglecting electron interlayer tunneling in the sandwich.

The eigenwaves under study satisfy the Maxwell equations, the boundary conditions at the graphene surfaces in each layer, and the condition that there are no exterior current sources at infinity.



The advantage achieved by graphene doubling is the appearance of an acoustic mode among the plasmon oscillations inherent in the system. This mode's frequency is proportional to the difference in frequencies of the plasmonic oscillations in the layers.

As a result, the phase velocity of this wave appears to be much less than that achievable in monolayers. Owing to such a large slowing down, one can meet Cherenkov synchronism even for graphene π electrons whose velocity is ≈ 300 less than the speed of light.

Two spatially separated graphene monolayers

Solution of boundary problem with boundary conditions on graphene layers gives dispersion equation for eigenwaves

$$\mathbf{H}(z_i + 0) - \mathbf{H}(z_i - 0) = \frac{4\pi}{c} \left[\mathbf{j}_t(z_i) \times \mathbf{n} \right]$$

magnetic field discontinuity on opposite sides of graphene sheet

Dispersion equation for surface TM mode in two-layer graphene system

$$2 + \frac{4\pi}{c}\sigma\frac{k_zc}{\omega} \pm \frac{4\pi}{c}\sigma\frac{k_zc}{\omega}\exp\{-\sqrt{q^2 - \omega^2/c^2}l\} = 0$$

Here q is wave number, $k_z = \sqrt{\omega^2/c^2 - q^2}$, l is distance between graphene layers

Graphene conductactivity:

$$\sigma^{\text{intra}}(\omega,\mu,T,\gamma_{\text{trans}}) = \frac{e^2 g_s g_v}{16\hbar} \frac{8T}{\pi\hbar} \ln\left[2\cosh\left(\frac{\mu}{2T}\right)\right] \frac{i}{\omega + i\gamma_{\text{trans}}}$$

$$\tilde{\Omega} = \hbar \left(\omega + i \gamma_{\text{opt}} \right) / |\mu| \qquad \qquad \sigma^{\text{inter}} \left(\omega, \mu, T, \gamma_{\text{opt}} \right) = -\frac{i e^2 g_s g_v}{16 \pi \hbar} \tilde{\Omega} \int_0^\infty \frac{\sinh \left(x |\mu| / T \right)}{\cosh(\mu / T) + \cosh(x \mu / T)} \frac{dx}{x^2 - \tilde{\Omega}^2 / 4}$$

m is chemical potential, γ_{trans} are broadening parameters

Frequency tuning



by varying the chemical potential Cherenkov resonant frequency *vs* chemical potential at the electron beam energy 4 KeV (1), 10 KeV (2) and 60 KeV (3).

by varying the electron beam energy The Cherenkov frequency dependence on the electron beam energy. Chemical potential 0.1 eV (1) and 0.2 eV (2).

Chemical potential can be tuned by:

- 1) electrostatic doping (smooth frequency tuning);
- number of graphene layers, because in acoustic mode potential is proportional to this number (discrete tuning)





Generation equation

Continuity conditions on the beam boundaries and discontinuity conditions for magnetic field on graphene layers give dispersion equation for system "sandwich + electron beam" (generation equation)

$$I_b = -\frac{(2+\sigma_0)^2 - (\sigma_0)^2 \exp\{-2\sqrt{q^2 - \omega^2/c^2}l\}}{\sigma_0 \left[2+\sigma_0 + \exp\{-2\sqrt{q^2 - \omega^2/c^2}l\}(2-\sigma_0)\right]} \qquad \sigma_0 = (4\pi/\omega)k_z\sigma$$

In this equation

$$I_{b} = \exp(2ik_{z}h) \frac{(k_{bz}^{2} - k_{z}^{2}) \left\{ \exp(ik_{bz}\delta) - \exp(-ik_{bz}\delta) \right\}}{(k_{bz} - k_{z})^{2} \exp(ik_{bz}\delta) - (k_{bz} + k_{z})^{2} \exp(-ik_{bz}\delta)}$$

h is the distance between sandwich and electron beam, d is the beam thickness,

w_l is the electron beam Langmuir frequent

$$k_{bz} = k_z \sqrt{1 - \frac{\omega_l^2}{\gamma^3 (\omega - qu)^2}}$$



Quasi-Cherenkov radiation of an electron beam passing over the graphene/polymer sandwich structure



PHYSICAL REVIEW B **95**, 205408 (2017)

Graphene layered systems as a terahertz source with tuned frequency

K. Batrakov* and S. Maksimenko





- □ We theoretically predicted and proved experimentally strong slowing down of surface EM waves in CNTs and graphene
- □ We theoretically demonstrate feasibility of extra small THz range sources based on CNTs
- □ We theoretically predicted and experimentally proved strong absrption of GHz- & THz waves in grapahene
- □ We propose more realistic THz-range source on the base of multilayered graphene/polymer structures





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EU FP7 612285 CANTOR 318617 FAEMCAR 610875 NAMICEMC 604391 GRAPHENE FLAGSHIP



HORIZON 2020 649953 GRAPHENE FPA 644076 COEXAN 734164 GRAPHENE 3D



U.S. Air Force

AF20-15-61804-1 CRDF Global Agreement

Thank you for your attention!



Nanoelectromagnetics

A research discipline studying the behaviour of highfrequency electromagnetic radiation on nanometer scale is currently emerging as a synthesis of macroscopic electrodynamics and microscopic theory of electronic properties of different nanostructures

FUNDAMENTAL CHALENGE in NANOSCALE ELECTROMAGNETICS is

unusual constitutive properties of structural materials due to spatial confinement of the charge carriers motion

or INTERPLAY of SCHROEDINGER and MAXWELL EQUATIONS

> Maksimenko & Slepyan, Nanoelectromagnetics of low-dimensional structures

EE ELECTROMAGNETIC WAVES SERIES 36



Propagation, scattering and dissipation of electromagnetic waves





A. S. Ilyinsky, G. Ya. Slepyan and A. Ya. Slepyan

THE HANDBOOK OF NANOTECHNOLOGY



AKHLESH LAKHTAKIA, EDITOR















Scalar analyzer R2-408R(VSWR and Transmission Loss Meter R2-408R) 27-37 GHz

Commercial THz time-domain spectrometer T-Spec by EKSPLA.

A 1050+-40 nm wave length pumping laser having 50-150 fs pulse duration and more than 40 mW output power at approximately 80 MHz pulse repetition rate is used to excite a photoconductor antenna and produced THz radiation up to 2 THz.

The spectrometer, THz emitter, and detector consist of a microstrip antenna integrated with a photoconductor and silicon lens. The sample in the form of a plane parallel plate is placed between emitter and detector normally to the initial EM wave. The THz detector output is proportional to the instant electrical field strength of the THz pulse. 37



Axial surface conductivity of isolated single-wall carbon nanotube

$$\sigma_{zz}(\omega) = -\frac{ie^2\omega}{\pi^2\hbar R} \left\{ \frac{1}{\omega(\omega + i/\tau_1)} \sum_{s=1}^m \int_{1stBZ} \frac{\partial E_c}{\partial p_z} \frac{\partial F_c}{\partial p_z} dp_z - 2\sum_{s=1}^m \int_{1stBZ} |R_{cv}|^2 E_c \frac{F_c - F_v}{\hbar^2 \omega(\omega + i/\tau_1) - 4E_c^2} dp_z \right\},$$



PHYSICAL REVIEW B 85, 165435 (2012)

Experimental evidence of localized plasmon resonance in composite materials containing single-wall carbon nanotubes

Experimental proof of localized plasmon resonance was found in thin films containing either single-walled carbon nanotubes (SWNT) or SWNT bundles of different length. All samples were prepared by a simple technique

Our result has been confirmed in Nano Letters 13, 5991 (2013):

Letter

pubs.acs.org/NanoLett

Plasmonic Nature of the Terahertz Conductivity Peak in Single-Wall Carbon Nanotubes

Qi Zhang,[†] Erik H. Hároz,[†] Zehua Jin,[†] Lei Ren,[†] Xuan Wang,[†] Rolf S. Arvidson,[‡] Andreas Lüttge,^{‡,§} and Junichiro Kono^{*,†,||}

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Frequency (THz)

upper definition of the second second

NANO LETTERS

samples. Our experimental results show that the broad THz peak originates from a plasmon resonance in both the metallic and the doped semiconducting carbon nanotubes rather than the interband excitation of the curvature-induced gap in nonarmchair metallic nanotubes. The intraband free electron