

GRAVITATIONAL-WAVE DETECTION  
WITH CAVITY-ASSISTED  
ATOM INTERFEROMETRY

Miguel Dovale Álvarez

GRASS in Padova, 1-2 March 2018

# Birmingham Institute of Gravitational Wave Astronomy

[sr.bham.ac.uk/gwgroup/](http://sr.bham.ac.uk/gwgroup/)



UNIVERSITY OF BIRMINGHAM - [birmingham.ac.uk](http://birmingham.ac.uk)



@UoBIGWaves

Cold Atoms group:

Miguel Dovale Álvarez

Daniel D Brown

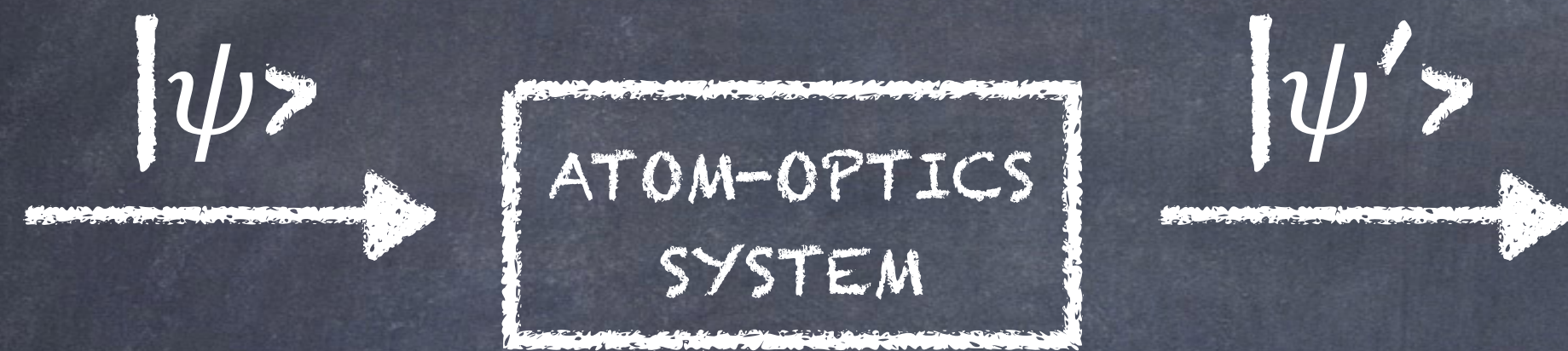
Aaron W Jones

Conor M Mow-Lowry

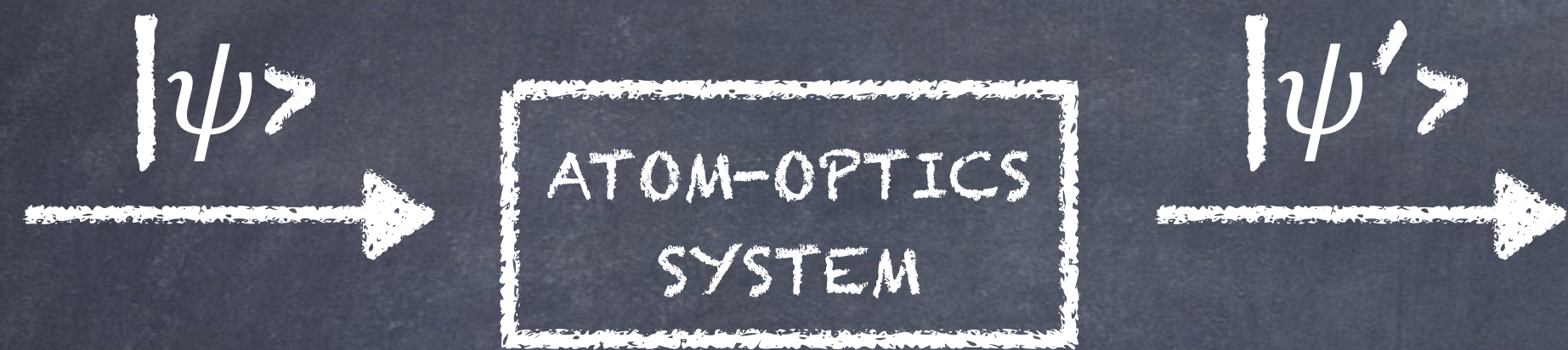
Haixing Miao

Andreas Freise

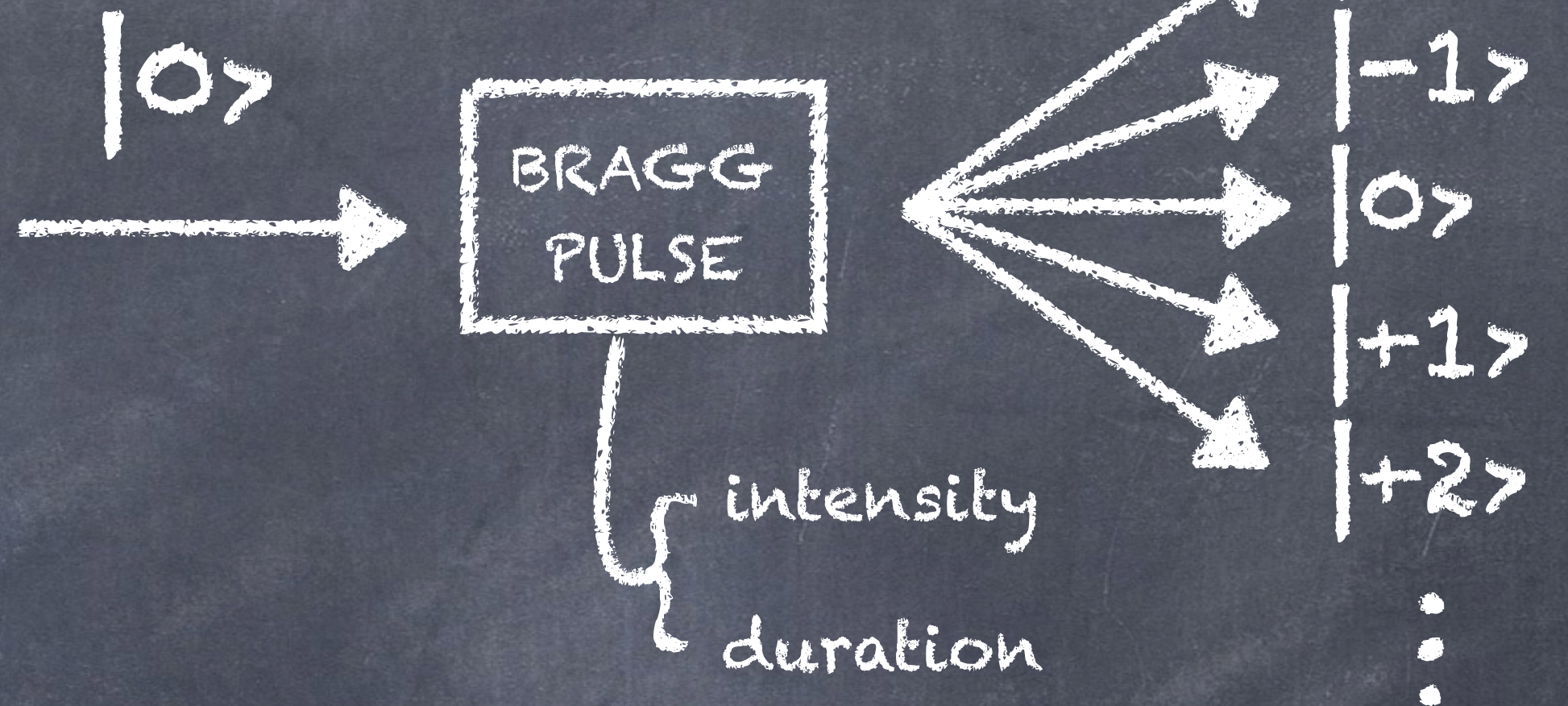
• Atom optics



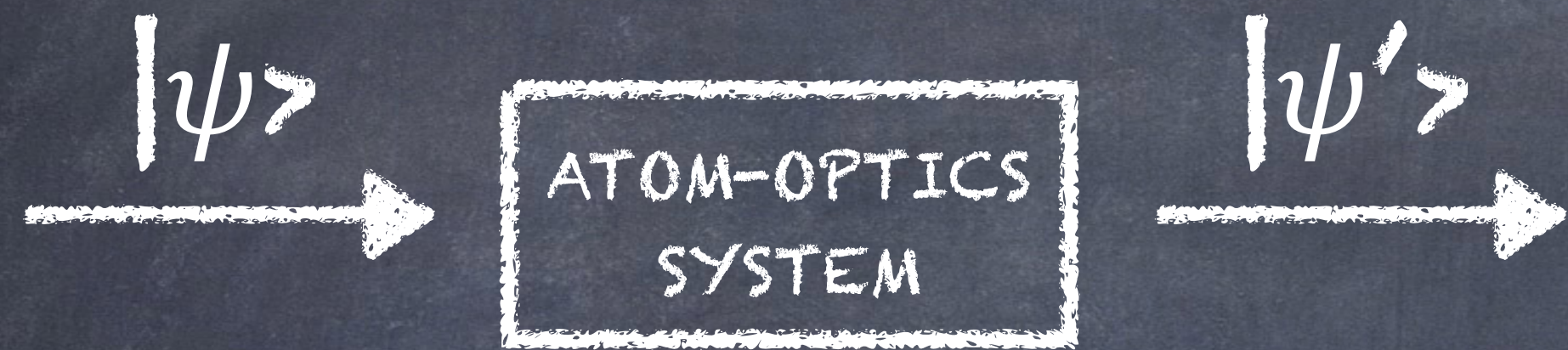
# • Atom optics



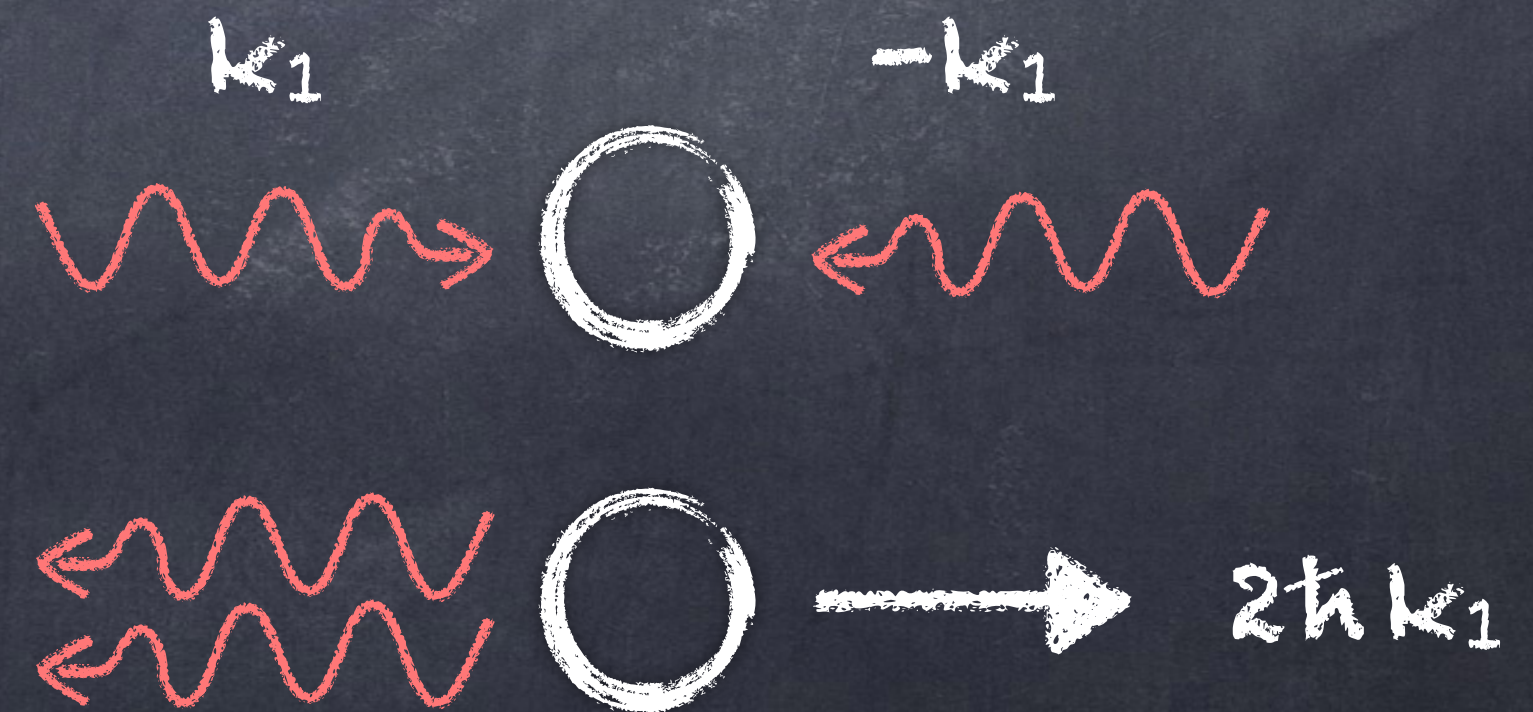
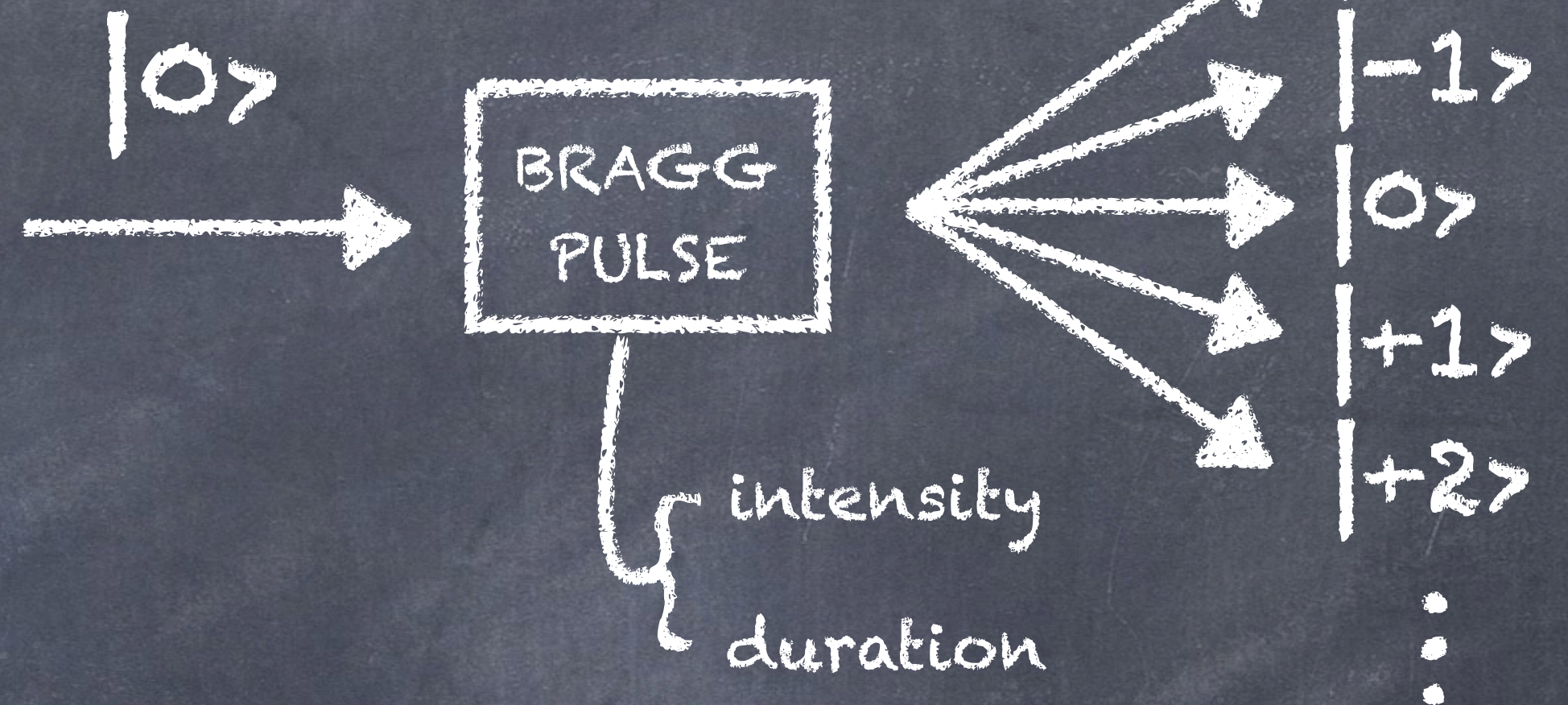
E.g.: Bragg diffraction



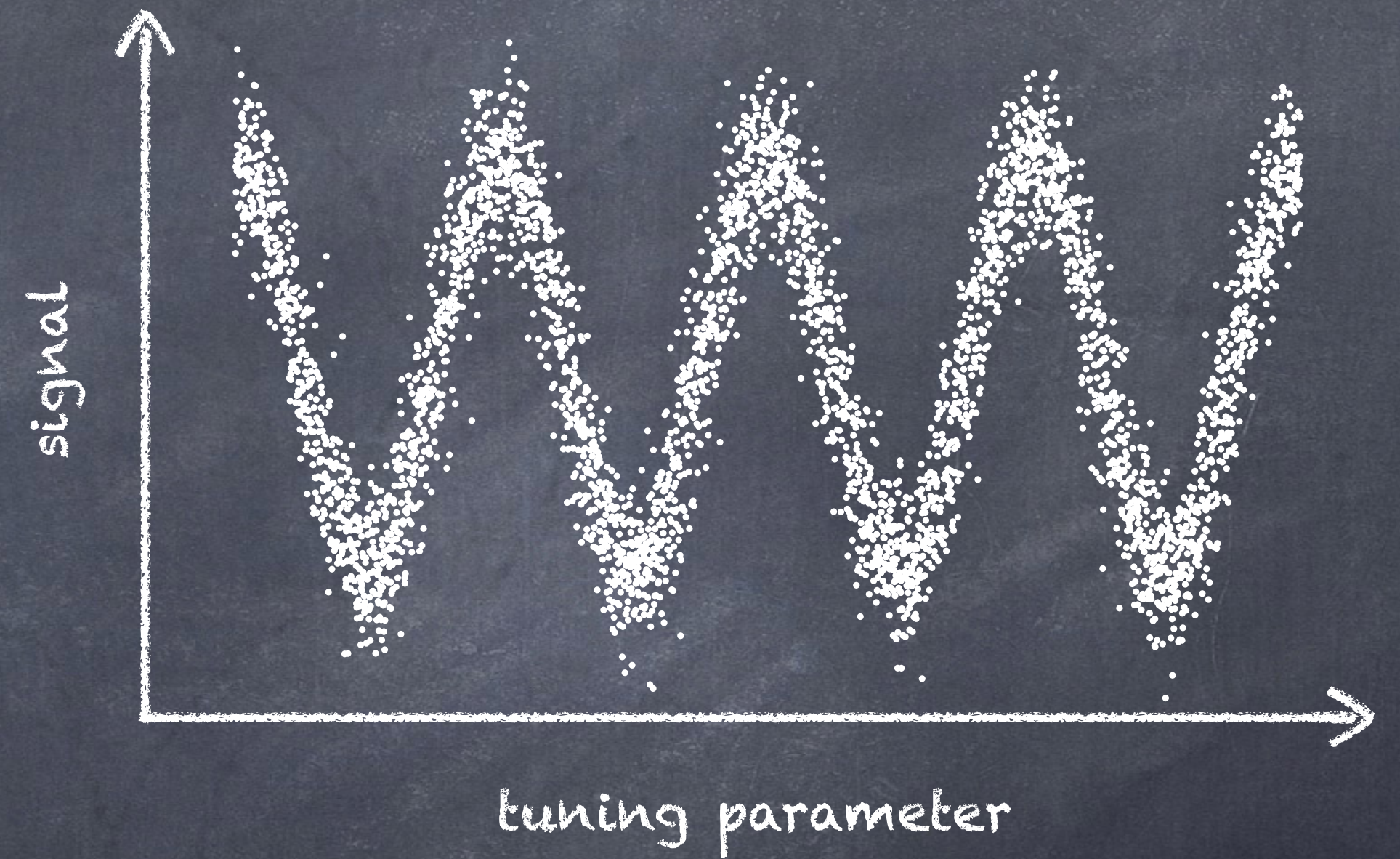
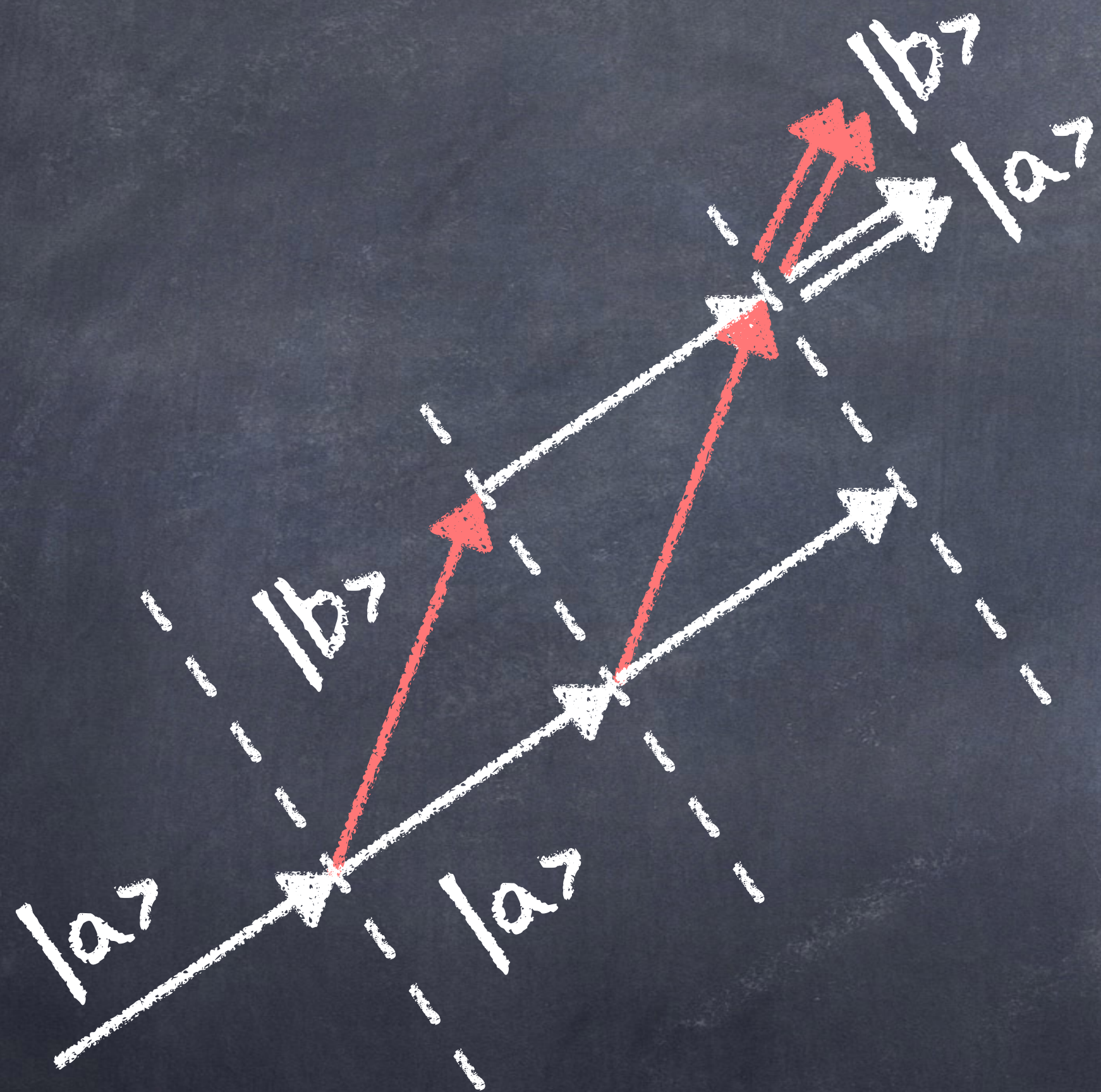
# • Atom optics



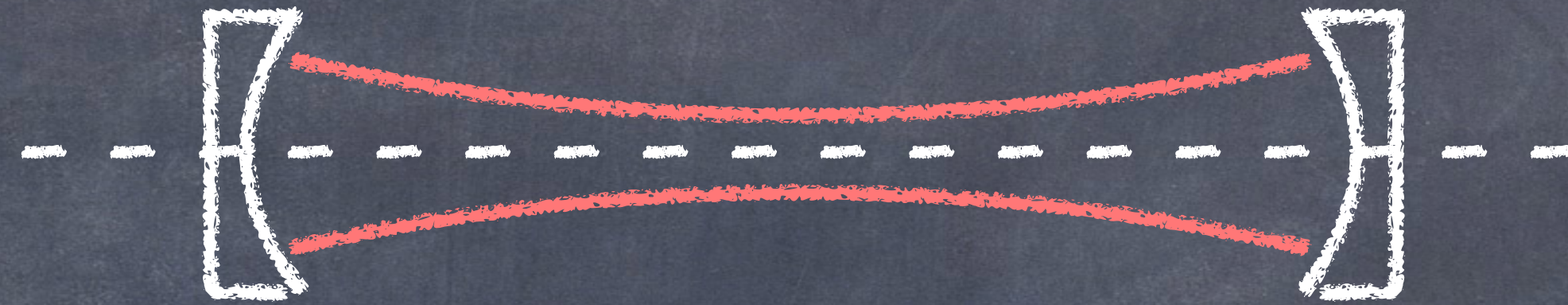
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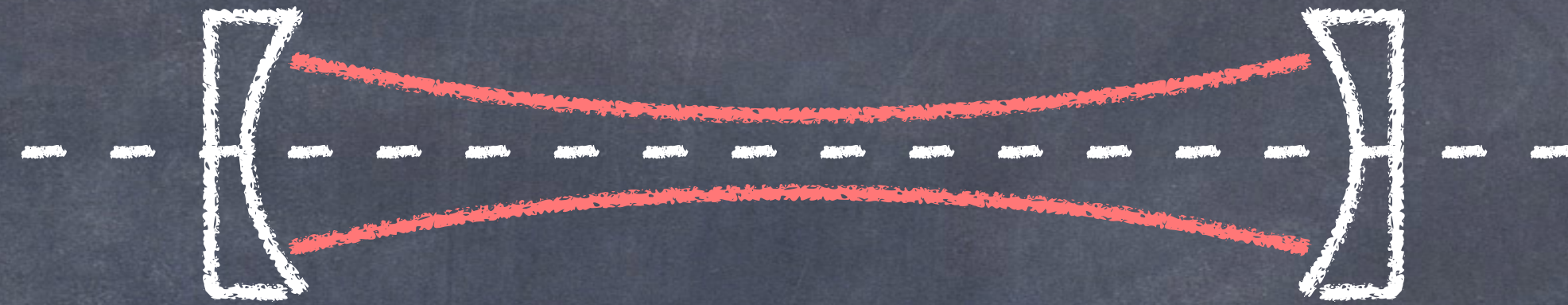
• Atom optics



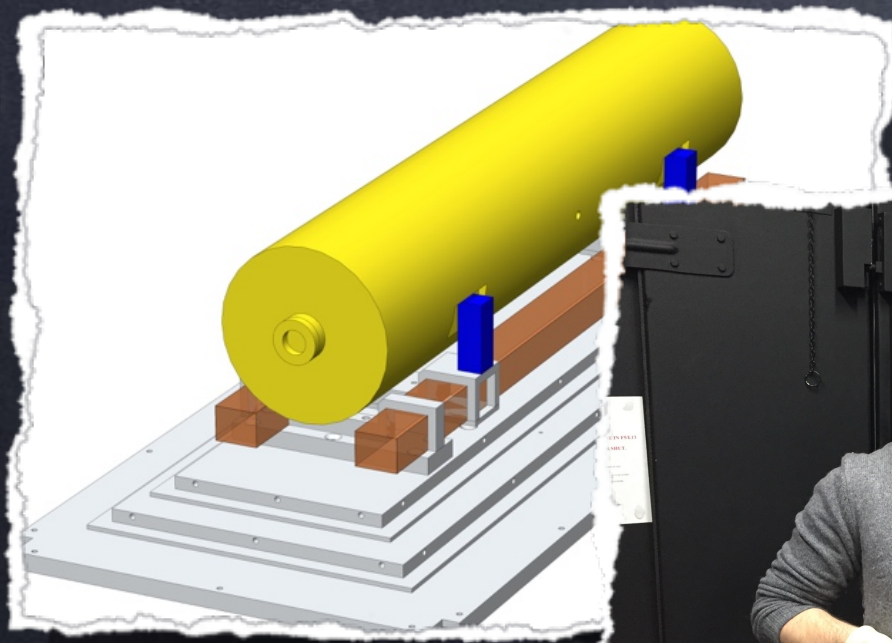
- Optical cavities



- Optical cavities

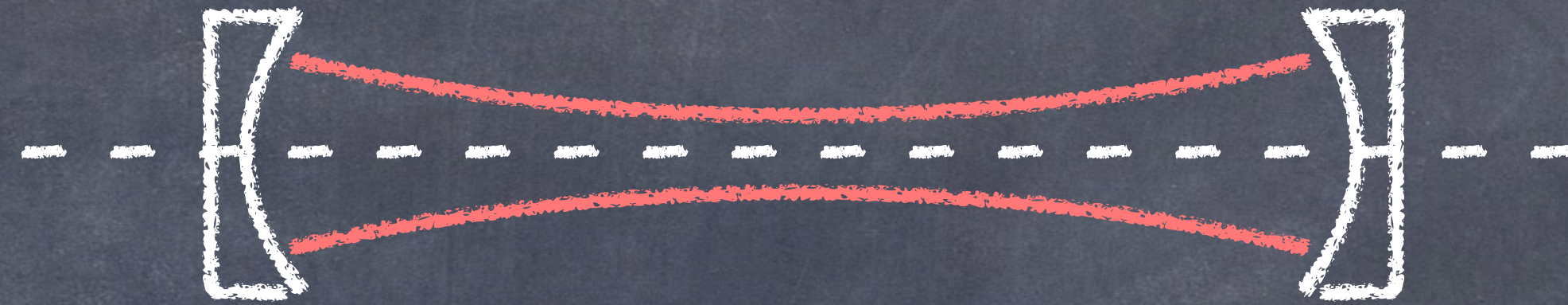


NPL

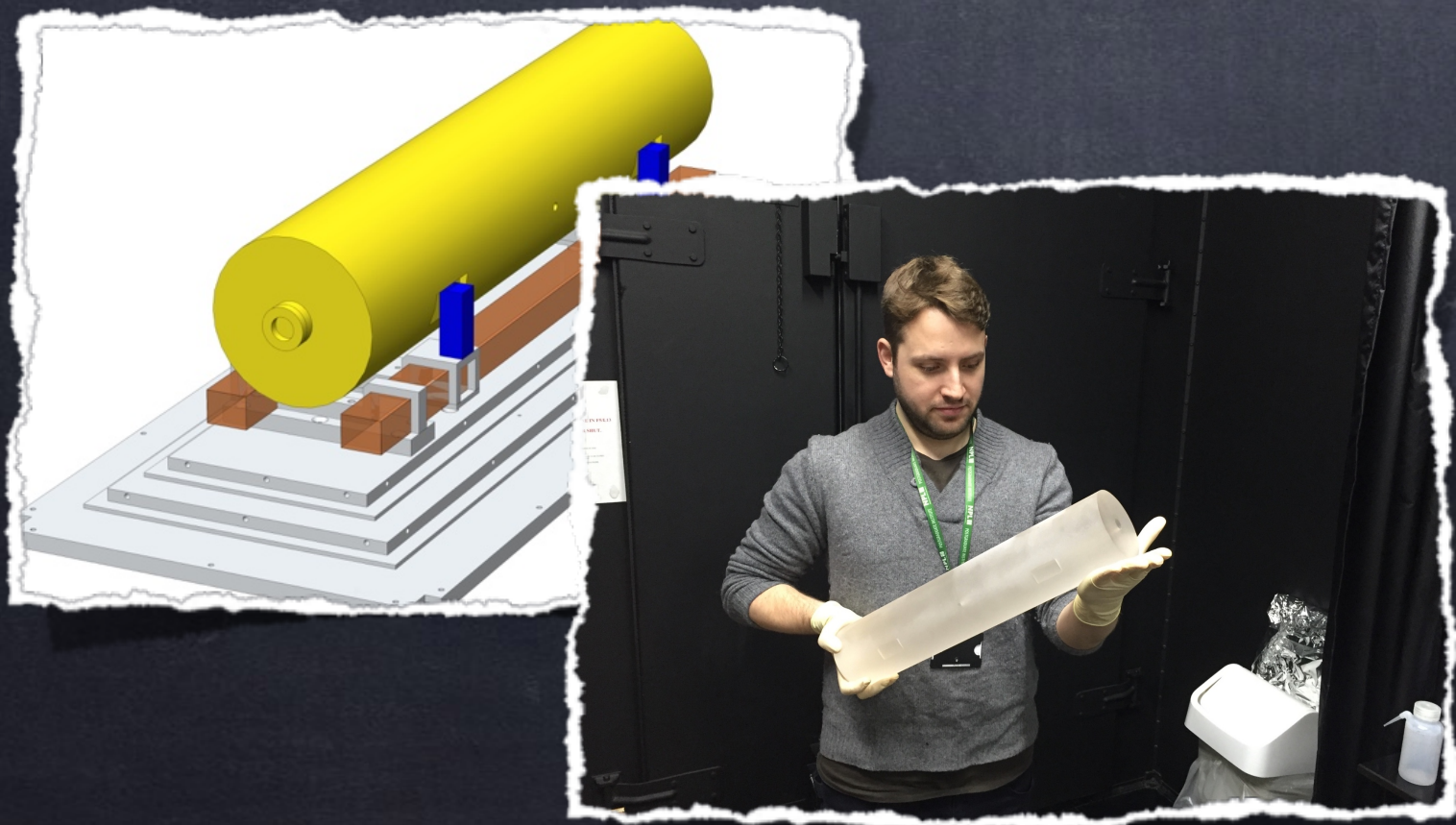




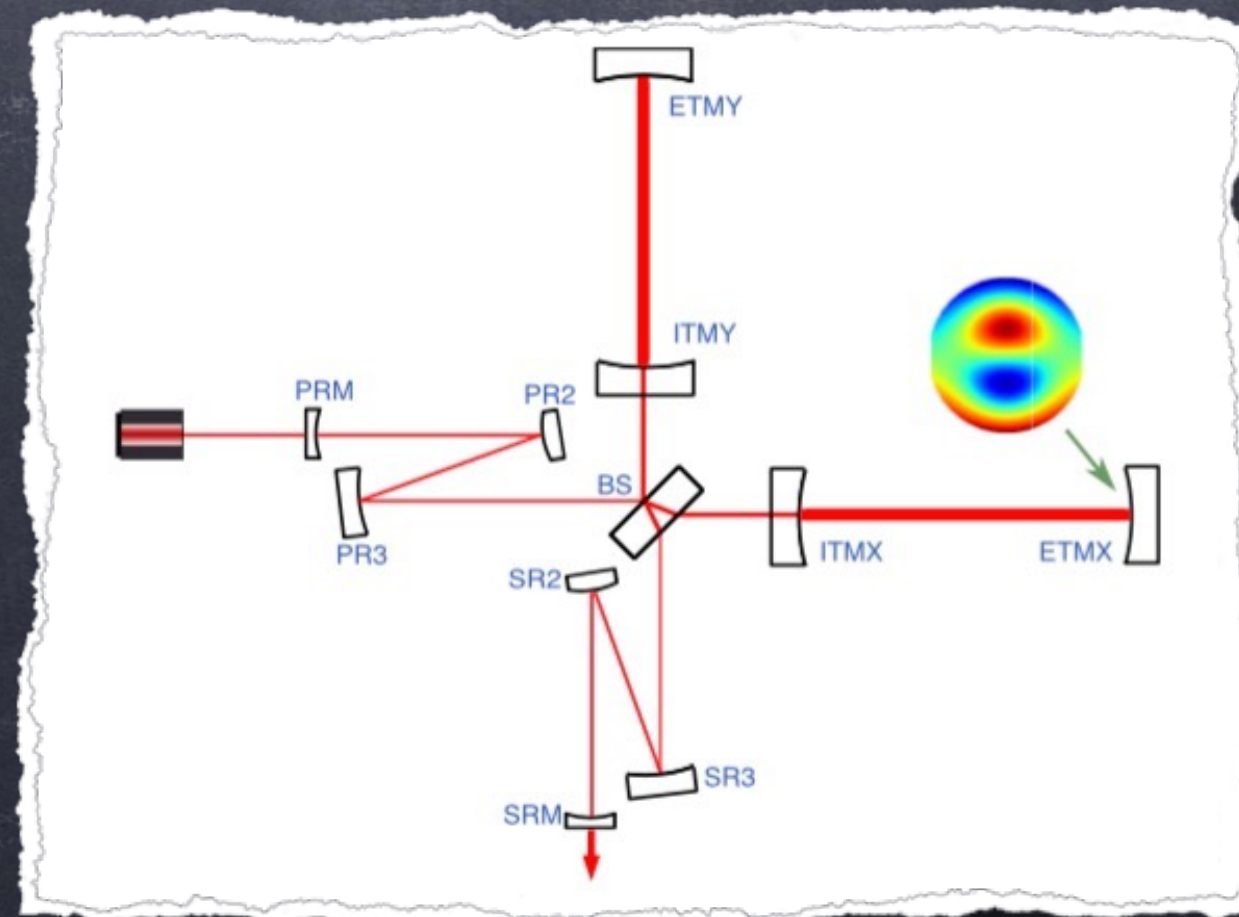
# • Optical cavities



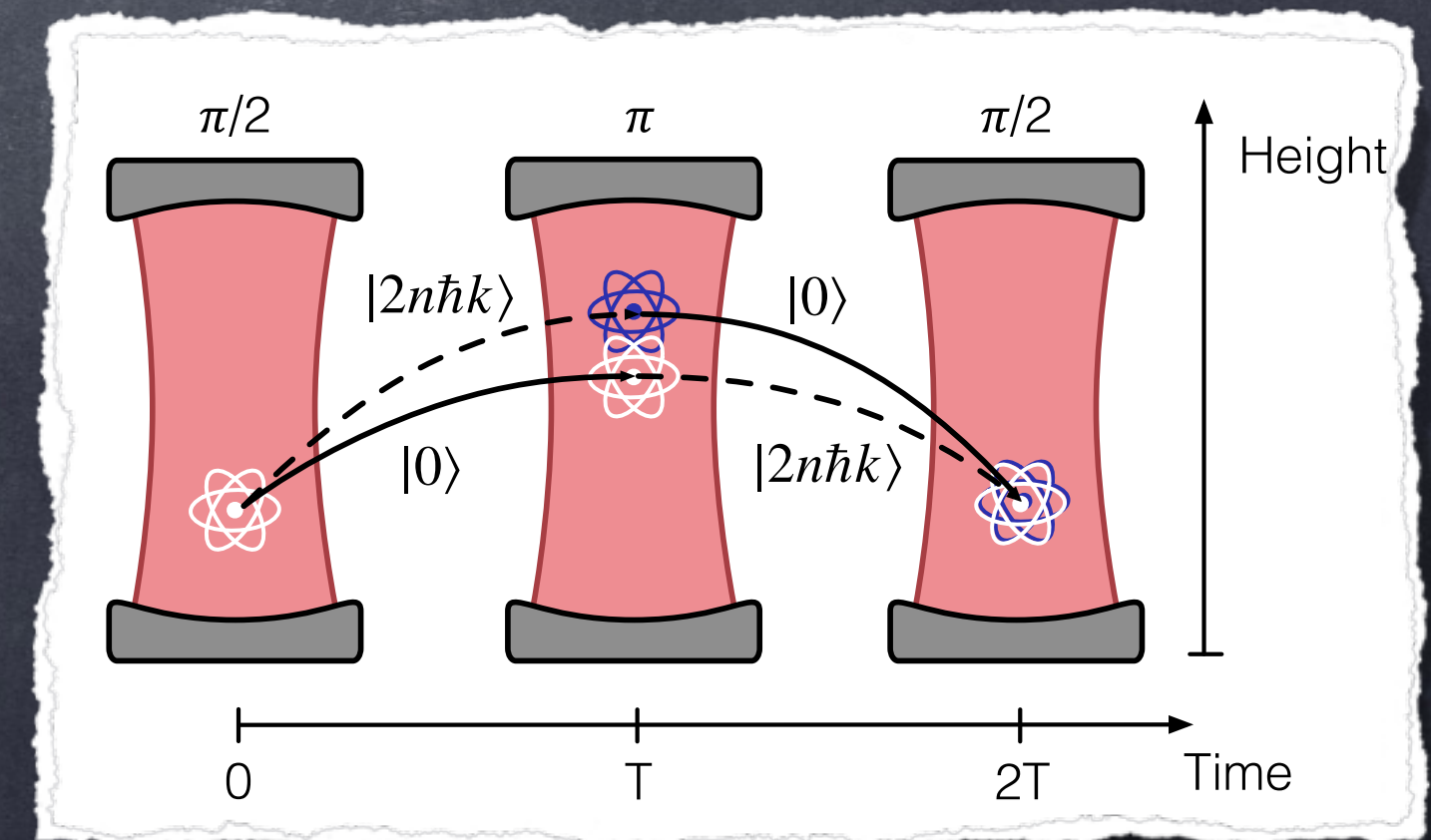
## NPL



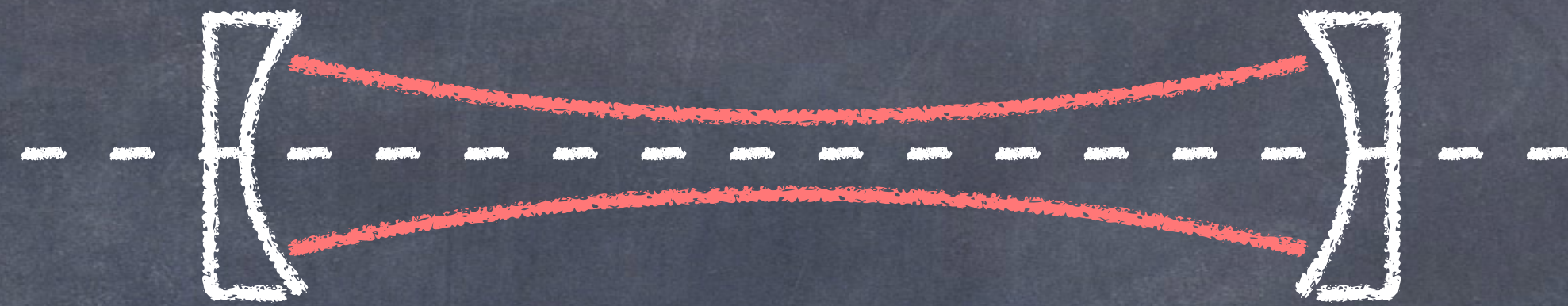
## LIGO



## Cold Atoms



- Optical cavities



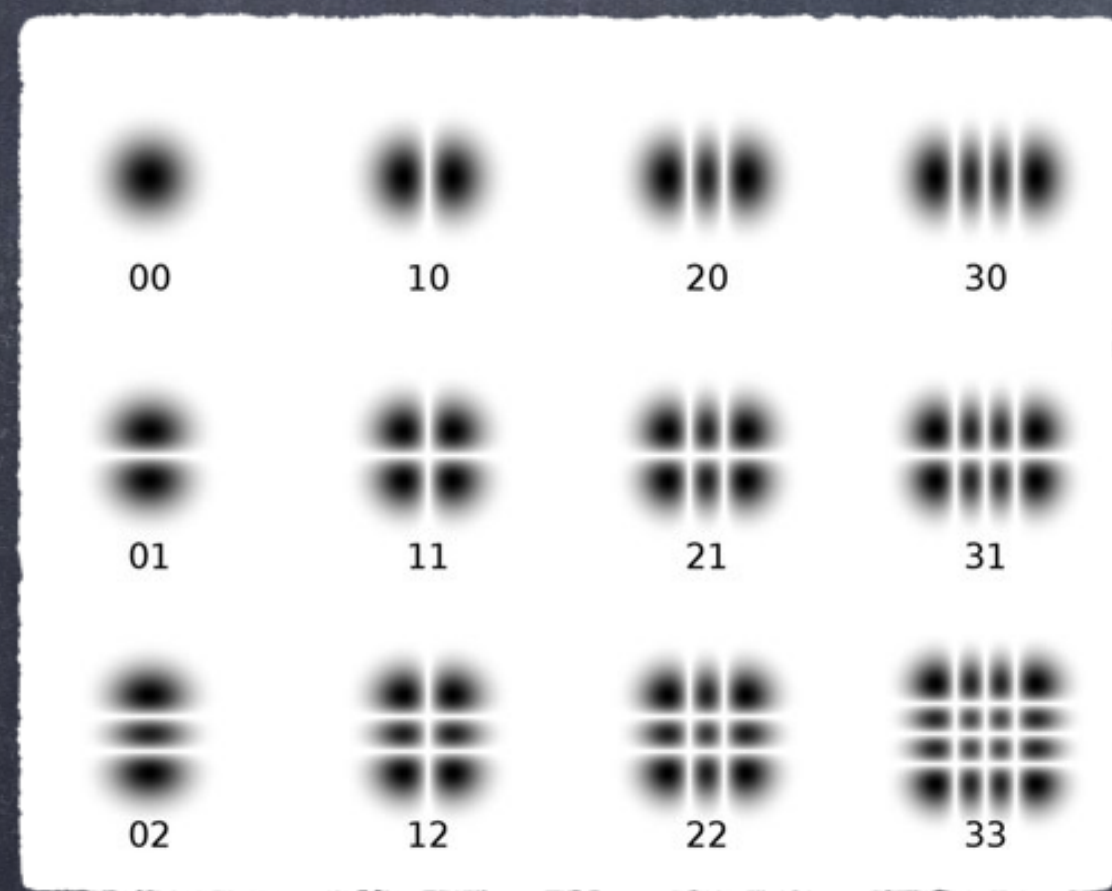
$$\text{field} = \sum_{nm} c_{nm} \text{HG}_{nm}$$

"Hermite-Gauss"  
modes

An arrow points from the  $\text{HG}_{nm}$  term in the equation to the text "Hermite-Gauss" modes.

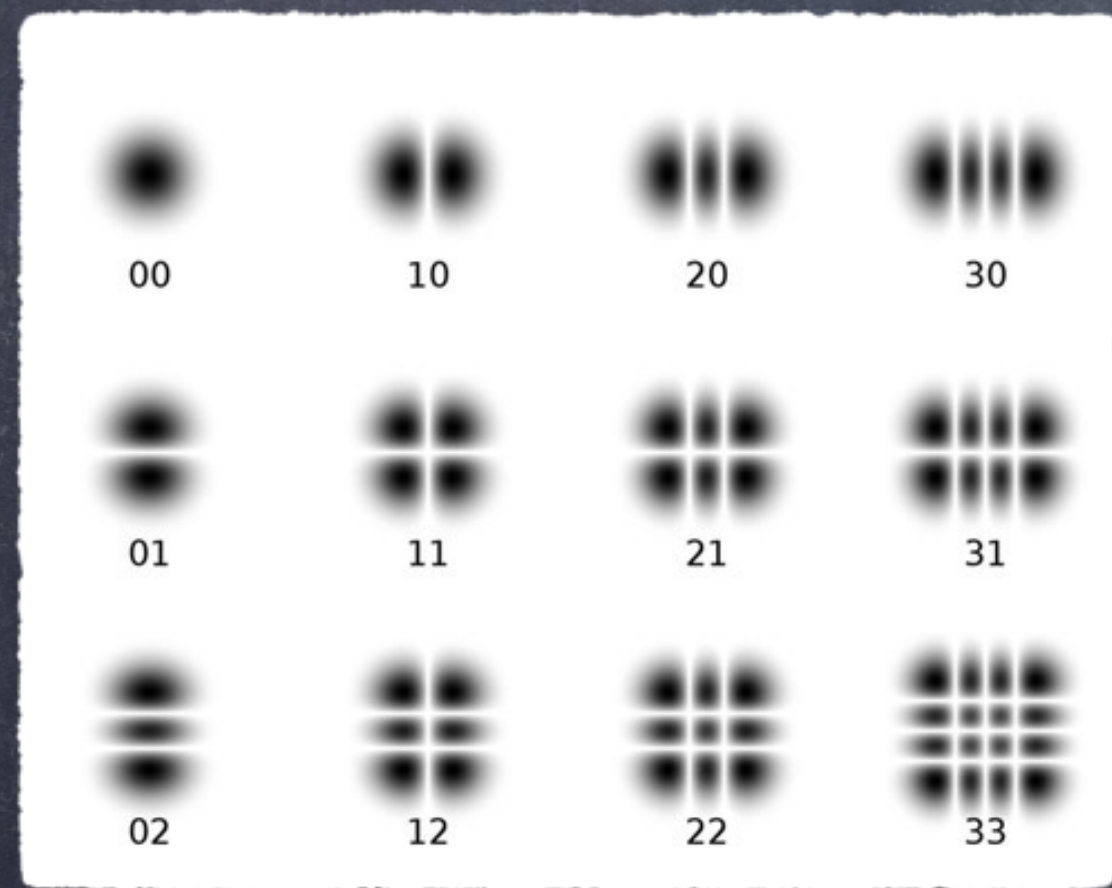
- Optical cavities

$$\text{field} = \sum_{nm} c_{nm} H_{nm}$$

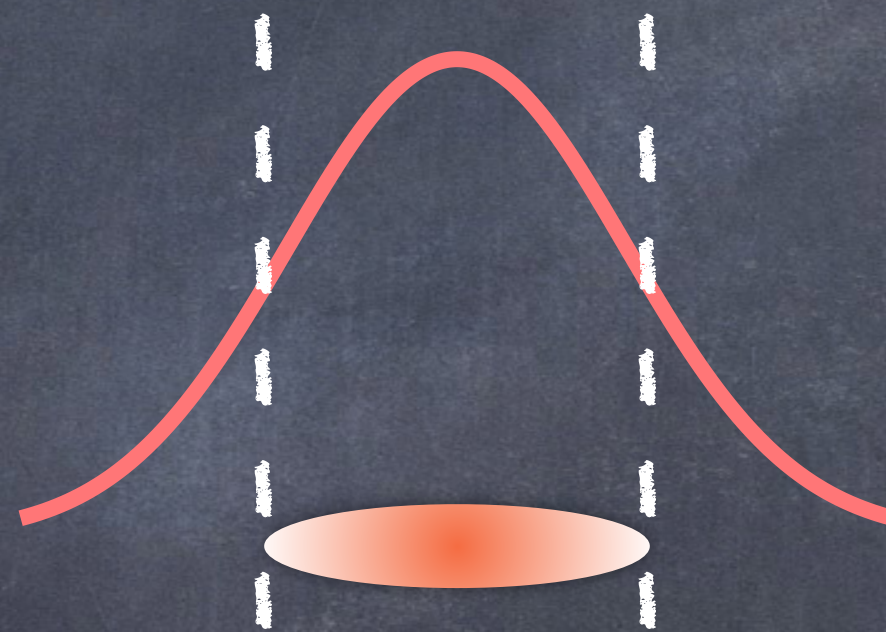


# • Optical cavities

$$\text{field} = \sum_{nm} c_{nm} \text{HG}_{nm}$$

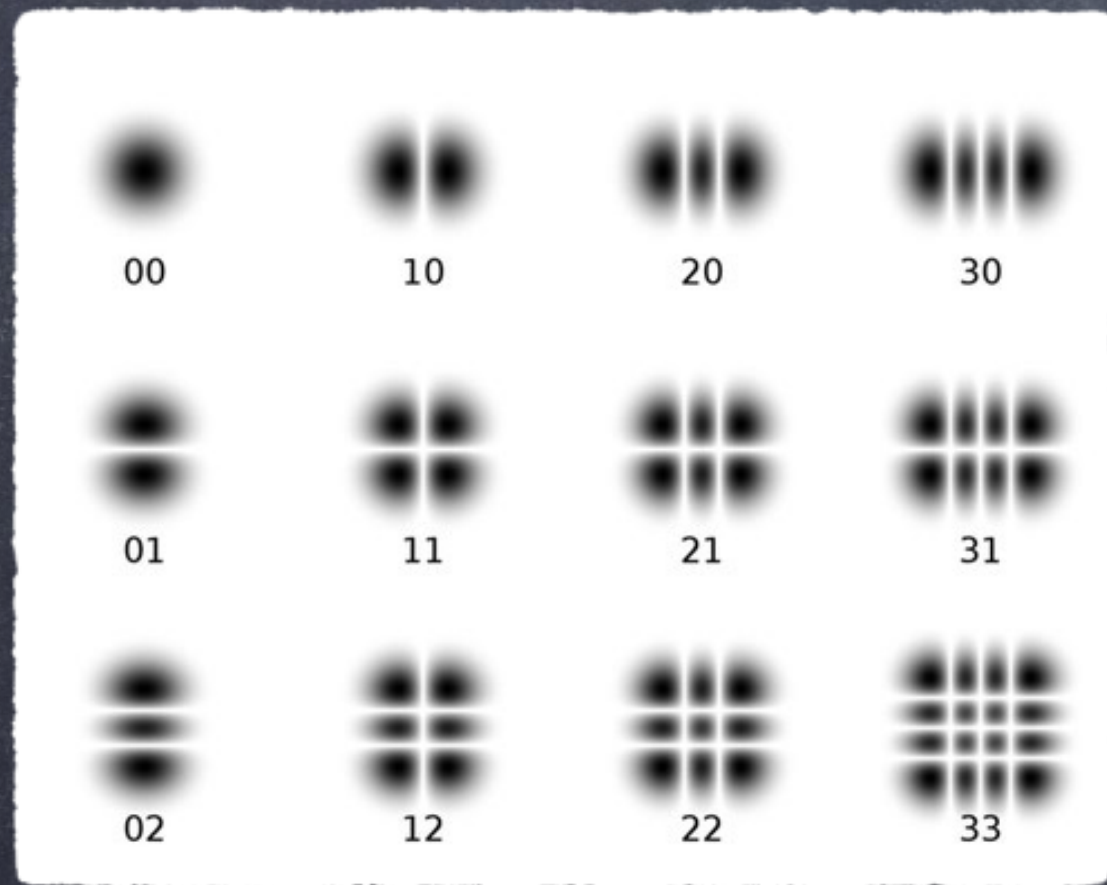


Ideal field = HG<sub>00</sub>



# • Optical cavities

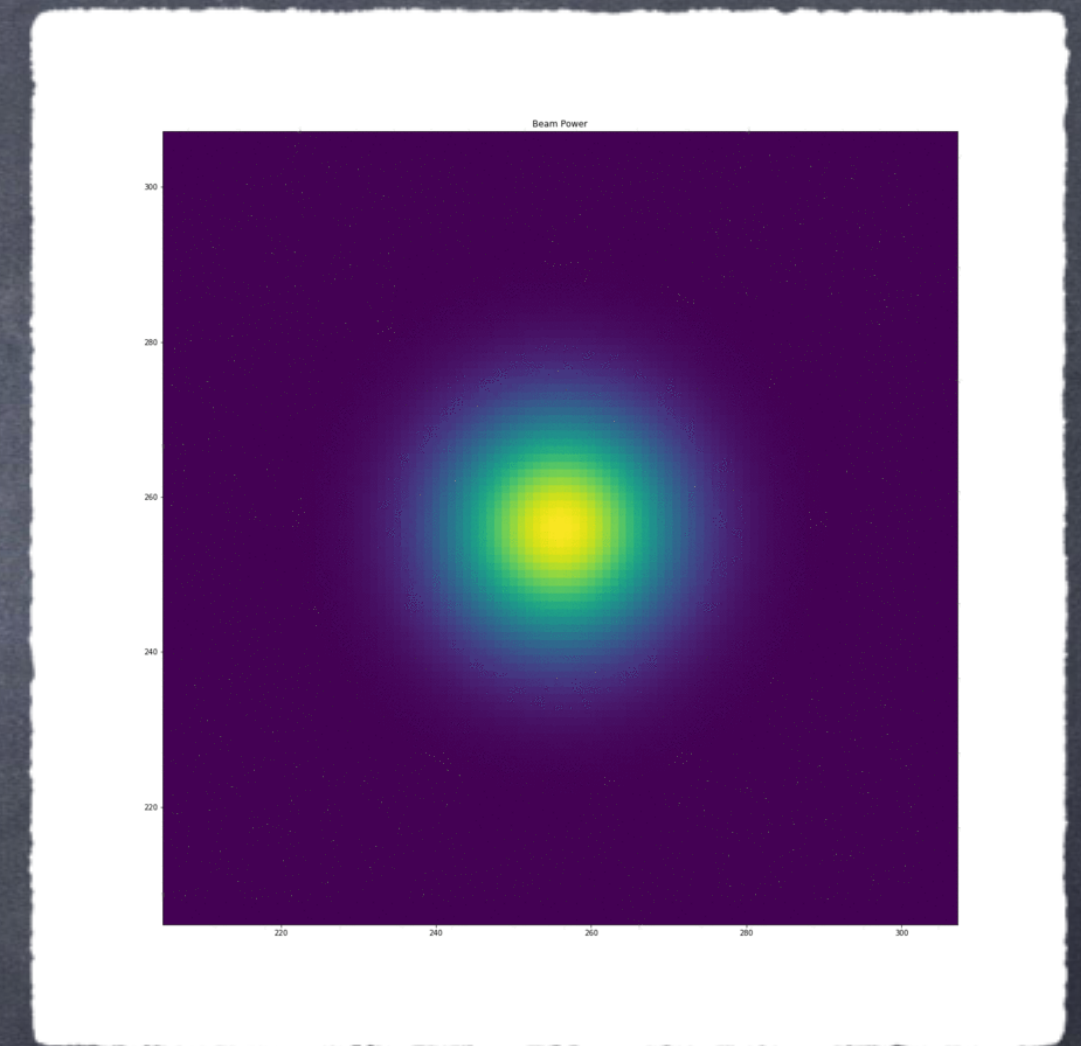
$$\text{field} = \sum_{nm} c_{nm} \text{HG}_{nm}$$



Ideal field = HG<sub>00</sub>

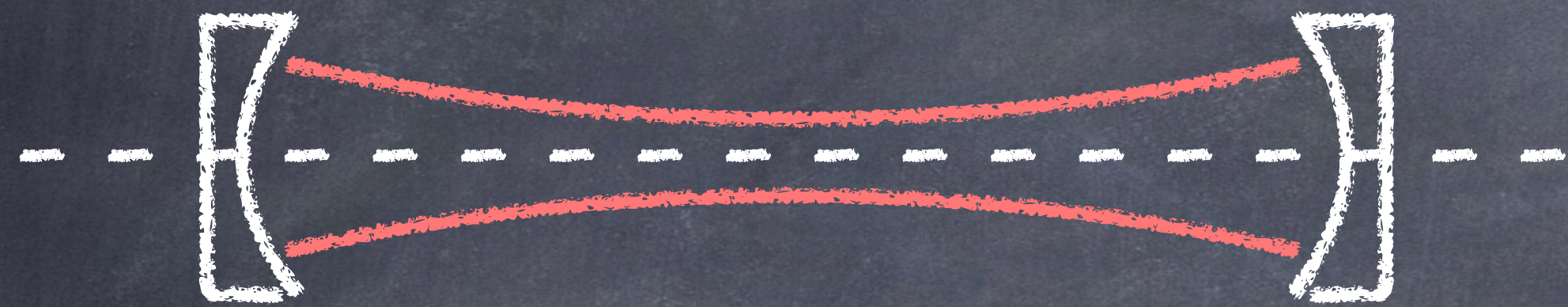


HG<sub>00</sub>+HG<sub>01</sub>



Generated with PyKat  
[gwoptics.org/pykat/](http://gwoptics.org/pykat/)

• Optical cavities



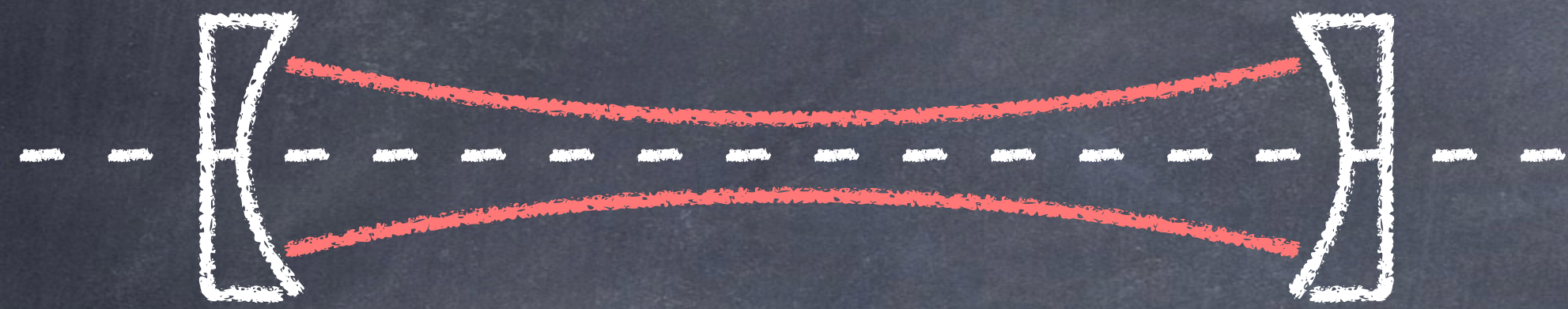
ROC } Gouy phase shift  
Length }  $\Delta f = 2 \arccos(\pm\sqrt{g_1 g_2})$



$$\Delta\phi_{nm} = (n+m) \Delta f$$

# • Optical cavities

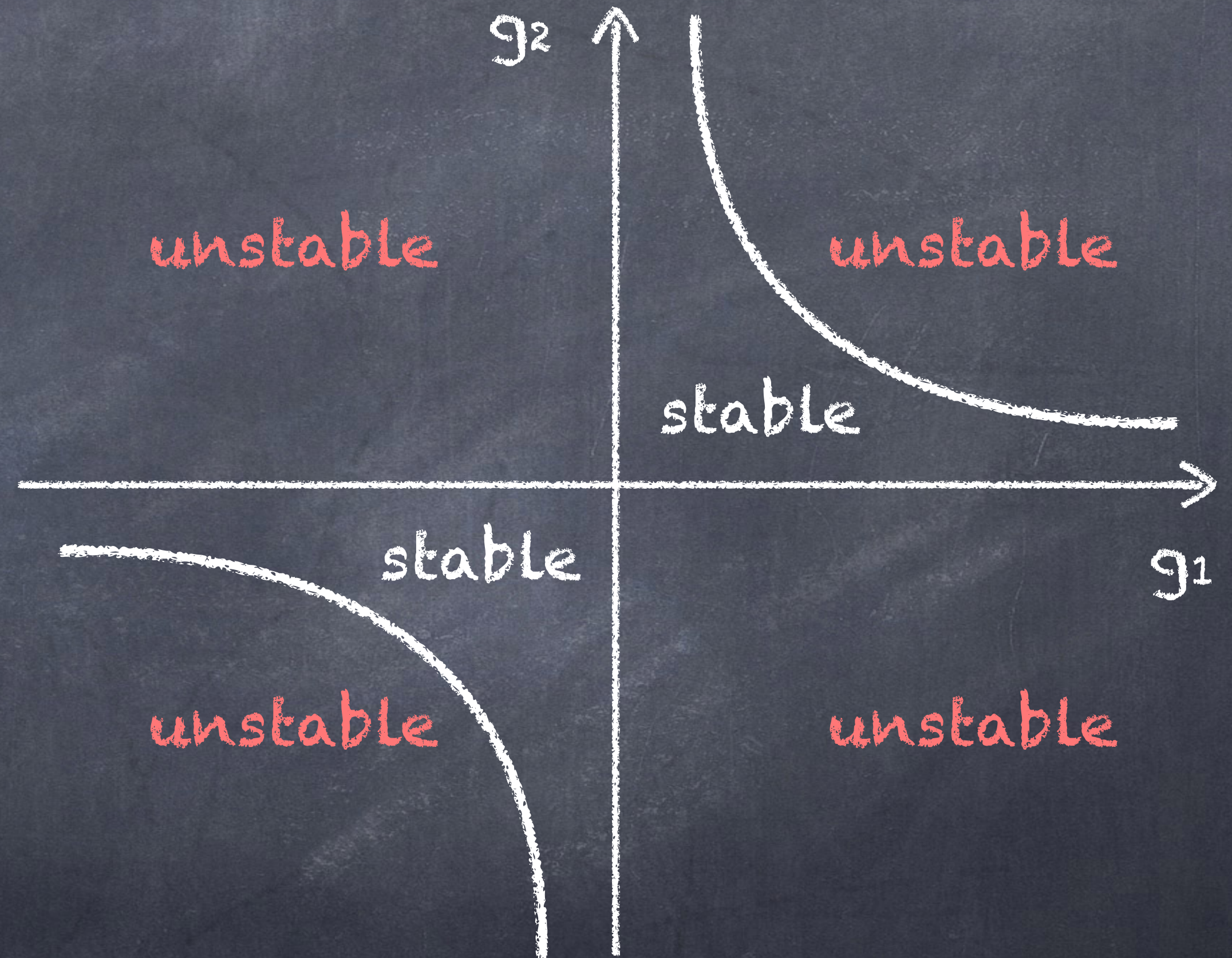
$$g_i = 1 - R_i/L$$



ROC } Gouy phase shift  
 Length }  $\Delta f = 2 \arccos(\pm\sqrt{g_1 g_2})$



$$\Delta\phi_{nm} = (n+m) \Delta f$$



- Optical cavities



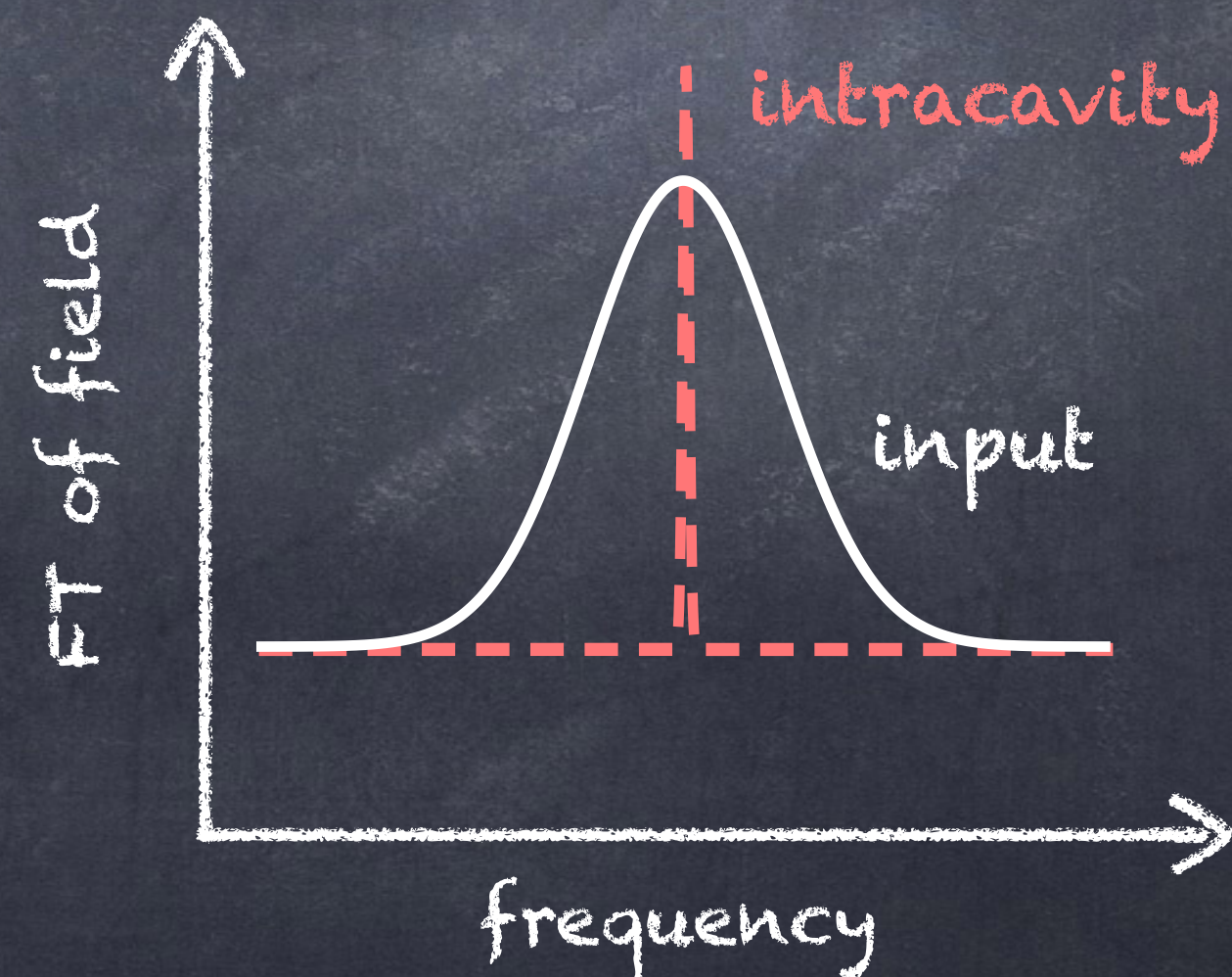
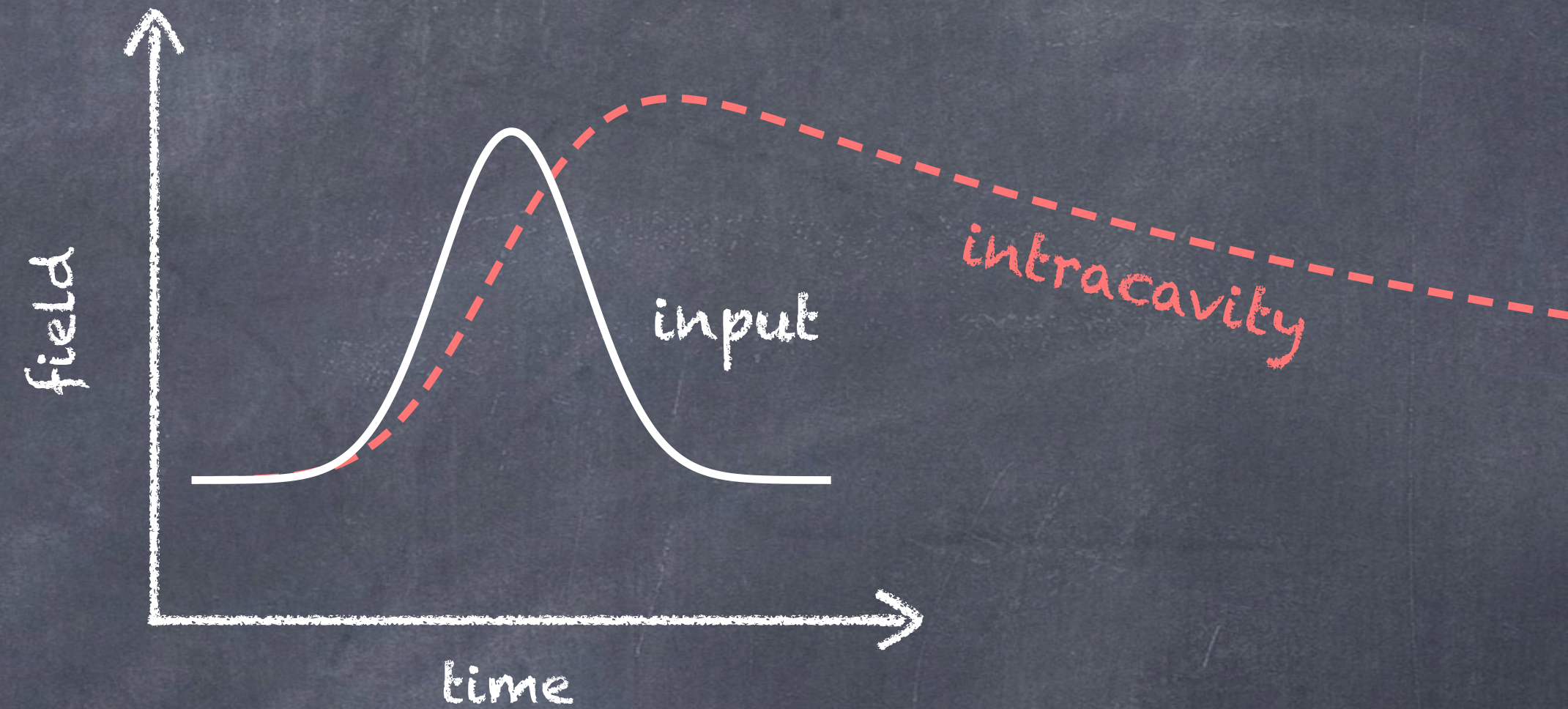
Finesse } Bandwidth,  $\Delta\nu = c/(2LF)$   
Length } Photon lifetime,  $\Delta t = \pi c/(LF)$



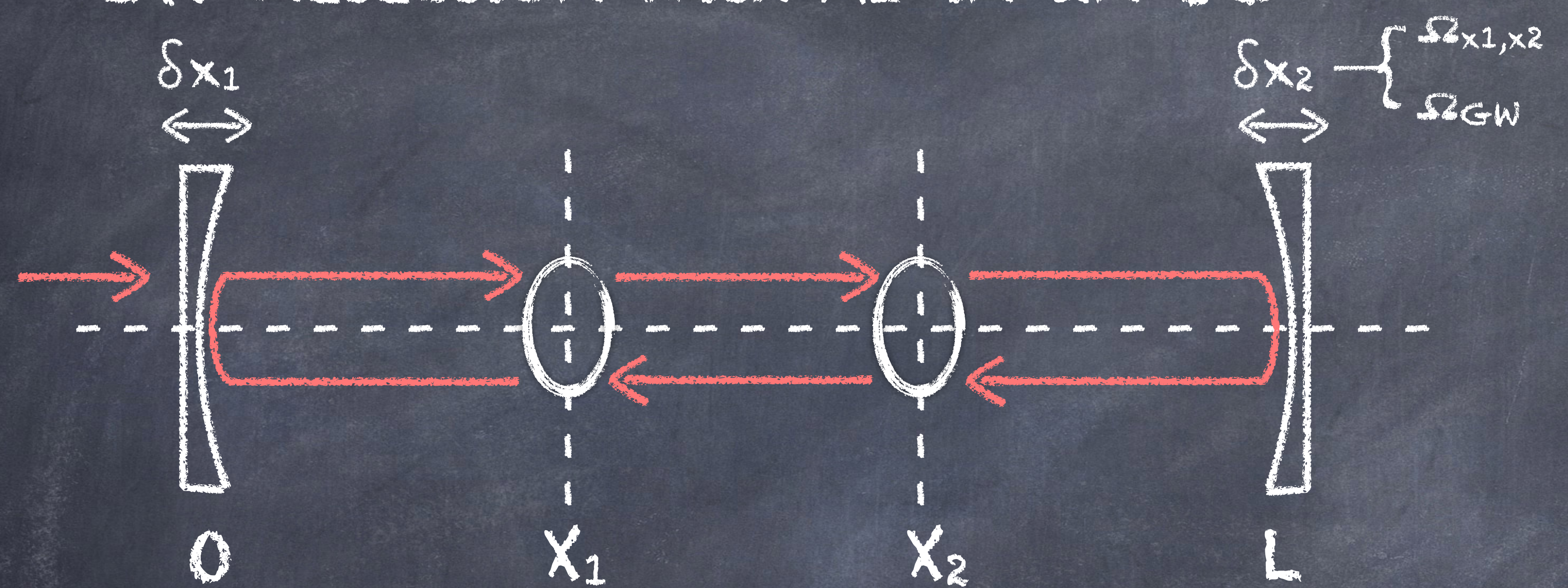
# • Optical cavities



Finesse } Bandwidth,  $\Delta\nu = c/(2LF)$   
 Length } Photon lifetime,  $\Delta t = \pi c/(LF)$



• GW detection with AI in an OC



Differential signal:  $\Delta\phi_1 - \Delta\phi_2$

$$\downarrow$$

$$\Delta\phi_1 = \Delta\phi_{\text{field}} + \Delta\phi_{\text{inertial}} + \Delta\phi_{\text{noise}}$$

$$\downarrow$$

$$\Delta\phi_{\text{field}} \propto n \Delta L_{RT} v(t)$$

$\left\{ \begin{array}{l} \text{Mirror vibration} \\ \text{GW strain} \end{array} \right.$

# • Effect of the cavity on the atomic transitions

- How do the cavity parameters affect the transitions?
- Are there optimal values?
- How does the order of the process come into play?
- Can we set interferometer constraints based on the performance of the cavity?

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- How does the order of the process come into play?
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PHYSICAL REVIEW A **96**, 053820 (2017)

**Fundamental limitations of cavity-assisted atom interferometry**

M. Dovale-Álvarez,<sup>\*</sup> D. D. Brown, A. W. Jones, C. M. Mow-Lowry, H. Miao, and A. Freise

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*Birmingham B15 2TT, United Kingdom*

(Received 25 September 2017; published 8 November 2017)

[arxiv.org/abs/1710.02448](https://arxiv.org/abs/1710.02448)

# • Effect of the cavity on the atomic transitions

BRAGG  
PULSE

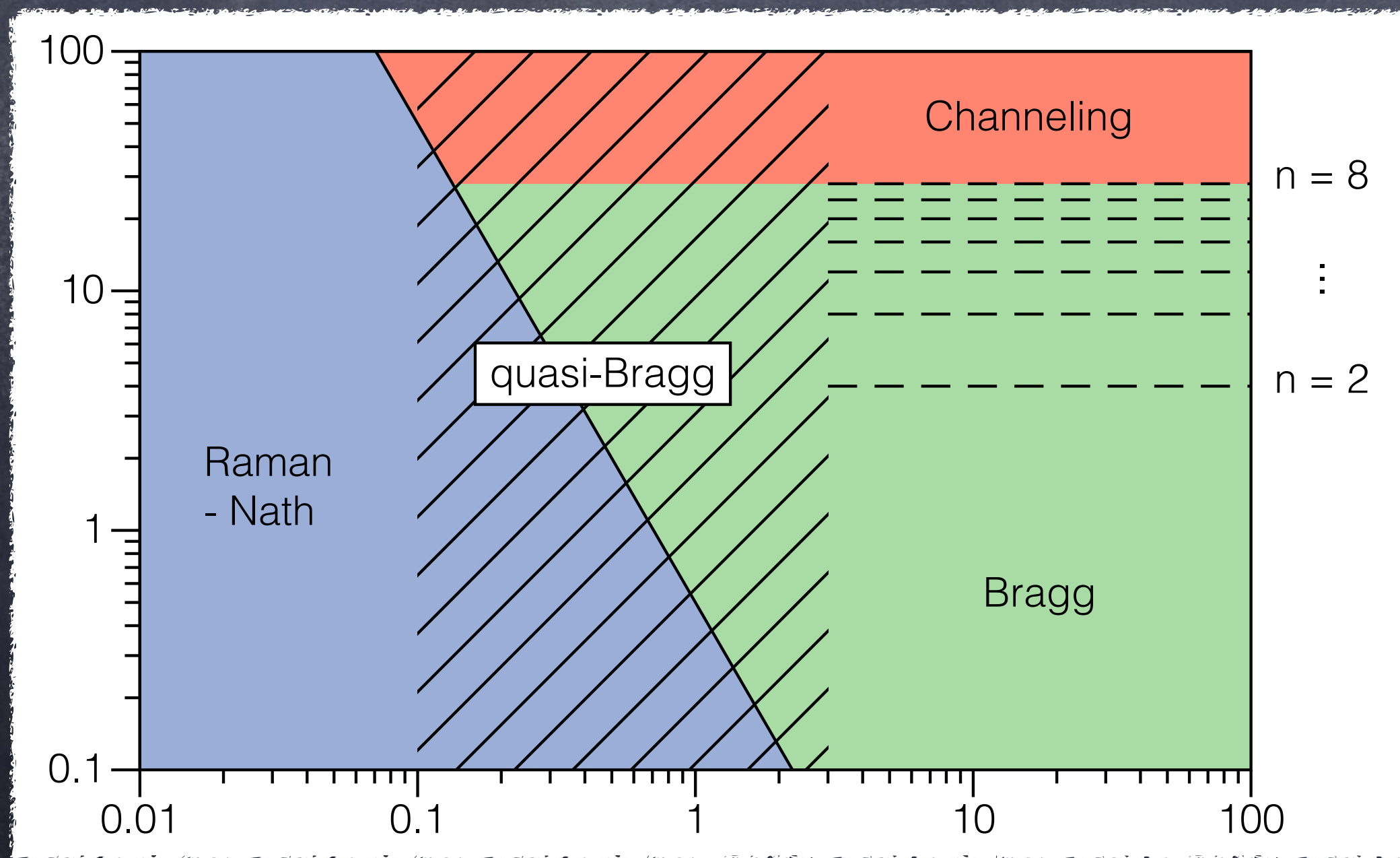
intensity  
duration

# • Effect of the cavity on the atomic transitions

BRAGG  
PULSE

intensity  
duration

Intensity

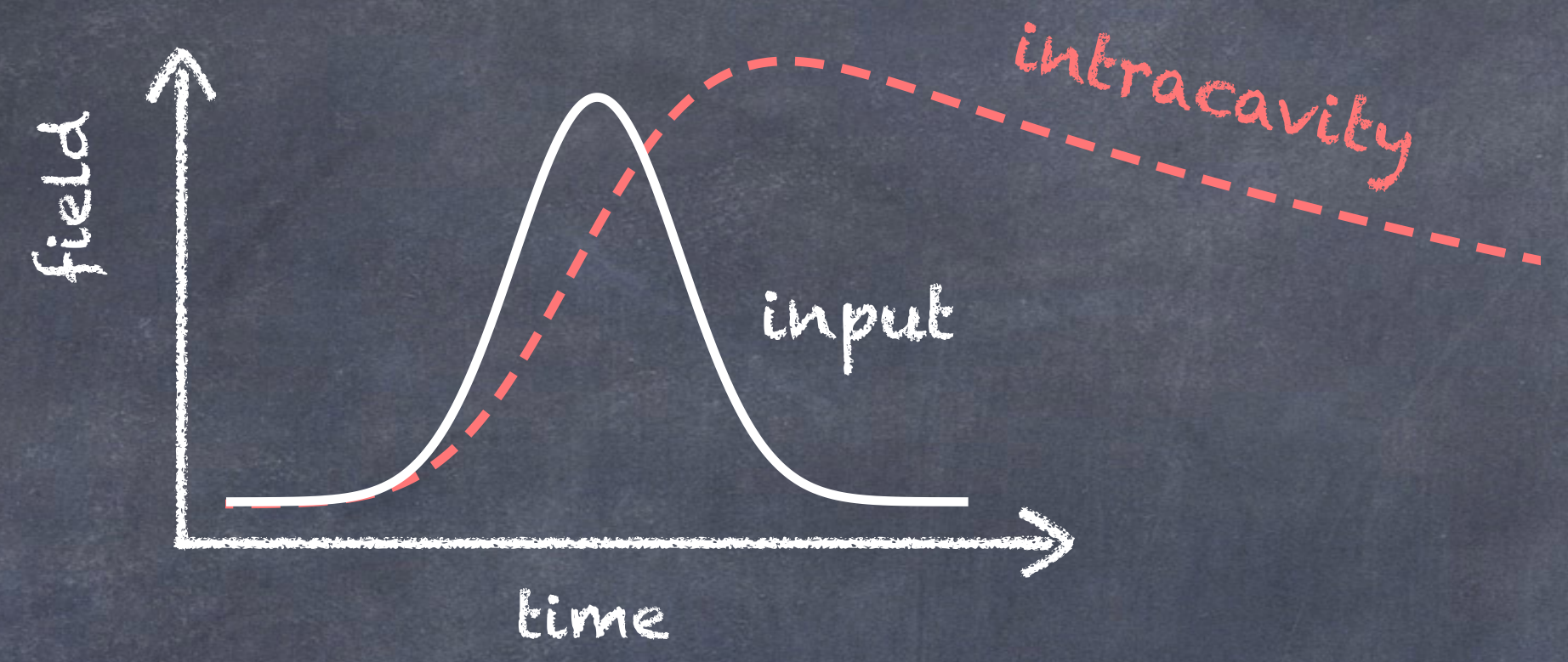


Duration

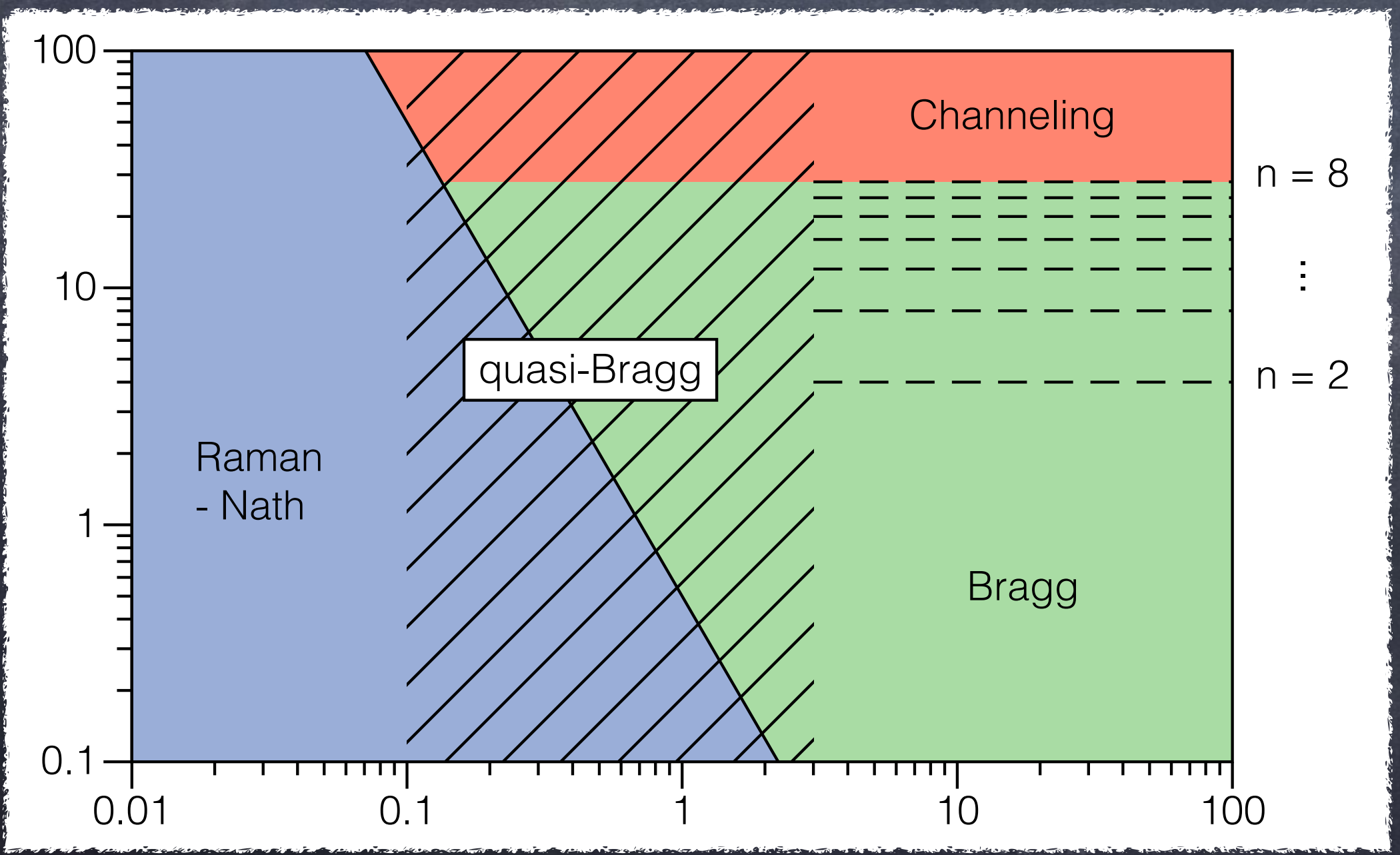
# • Effect of the cavity on the atomic transitions

BRAGG PULSE

intensity  
duration



Intensity

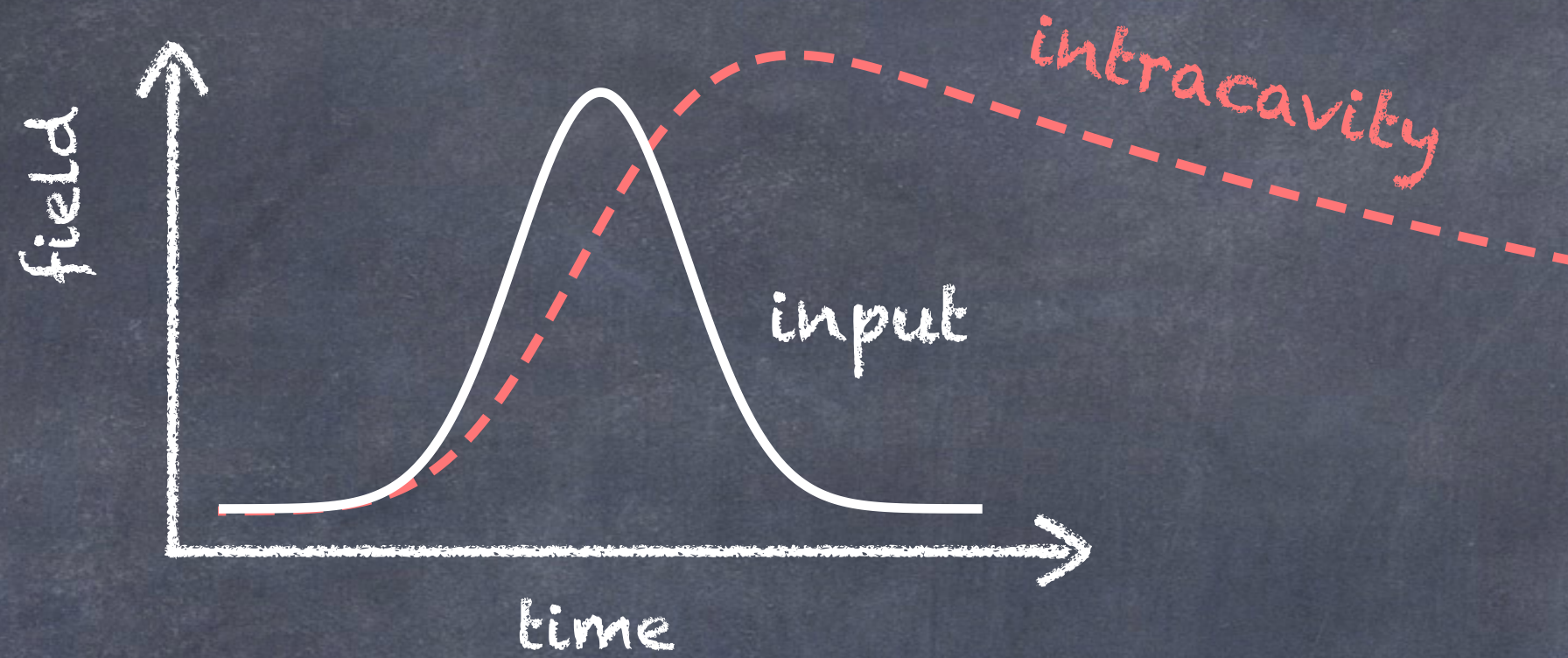


Duration

# • Effect of the cavity on the atomic transitions

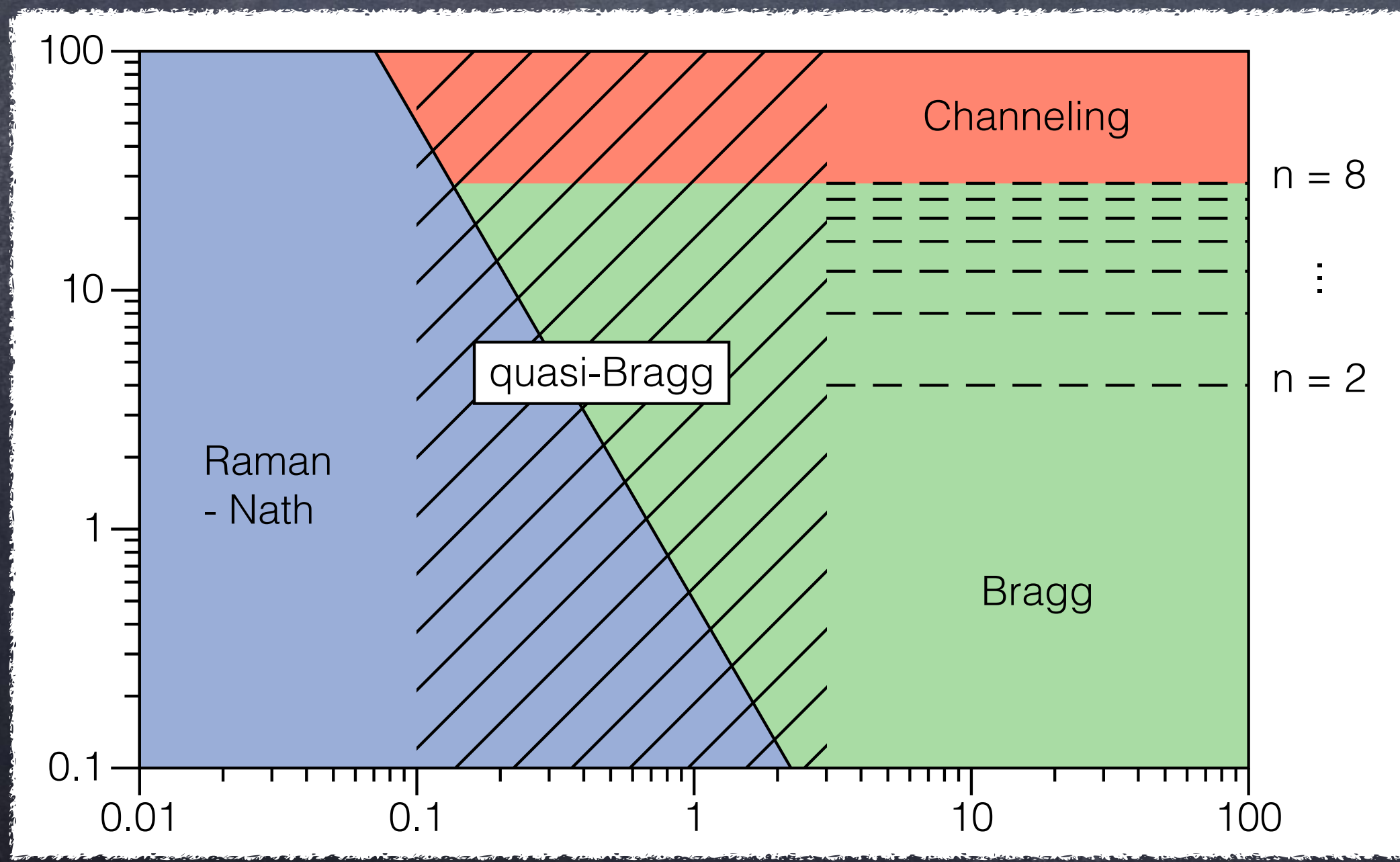
BRAGG PULSE

intensity  
duration

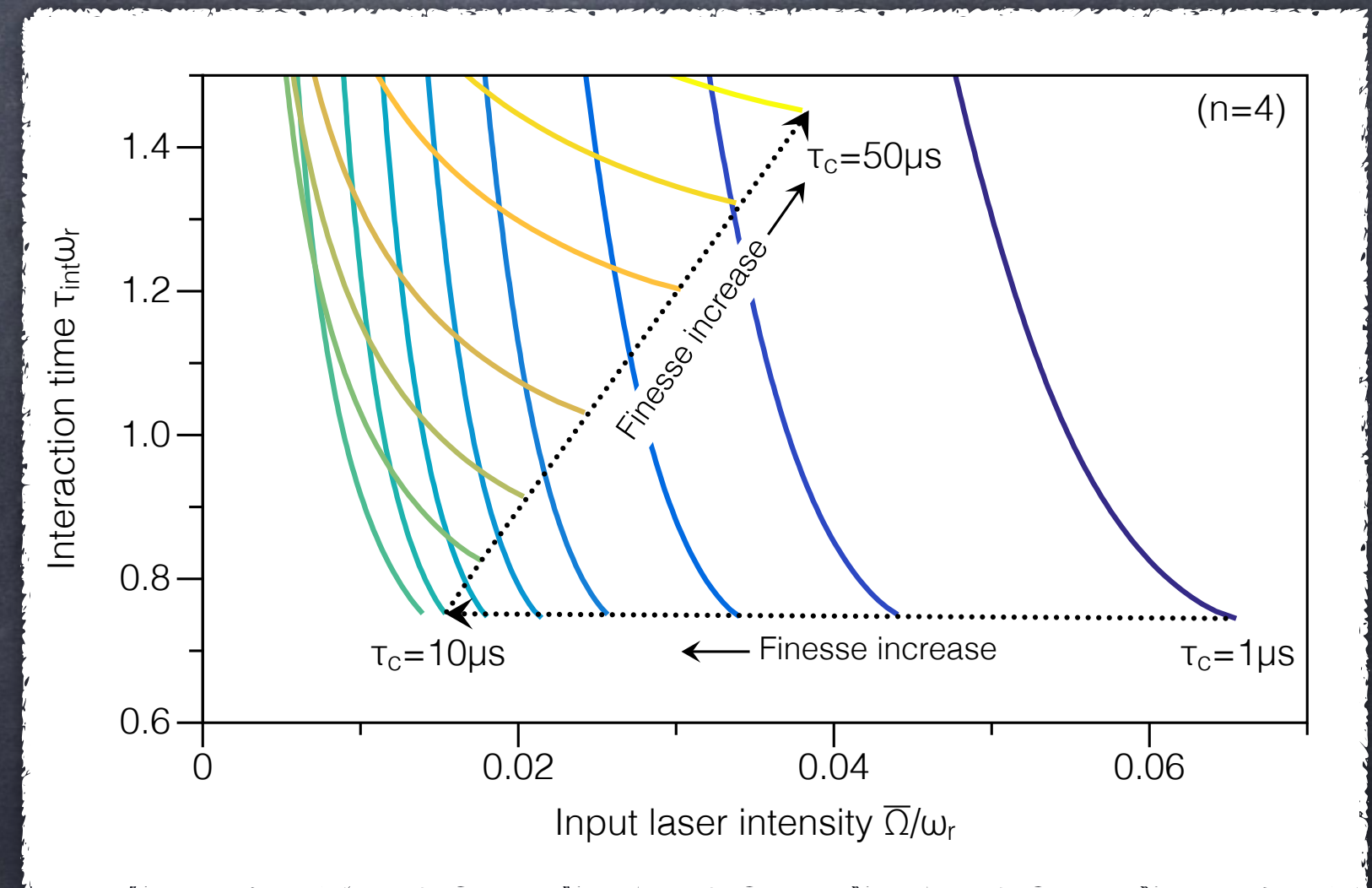


• Cavity length/finesse changes will transform the landscape in the parameter space of the interaction.

Intensity



Duration

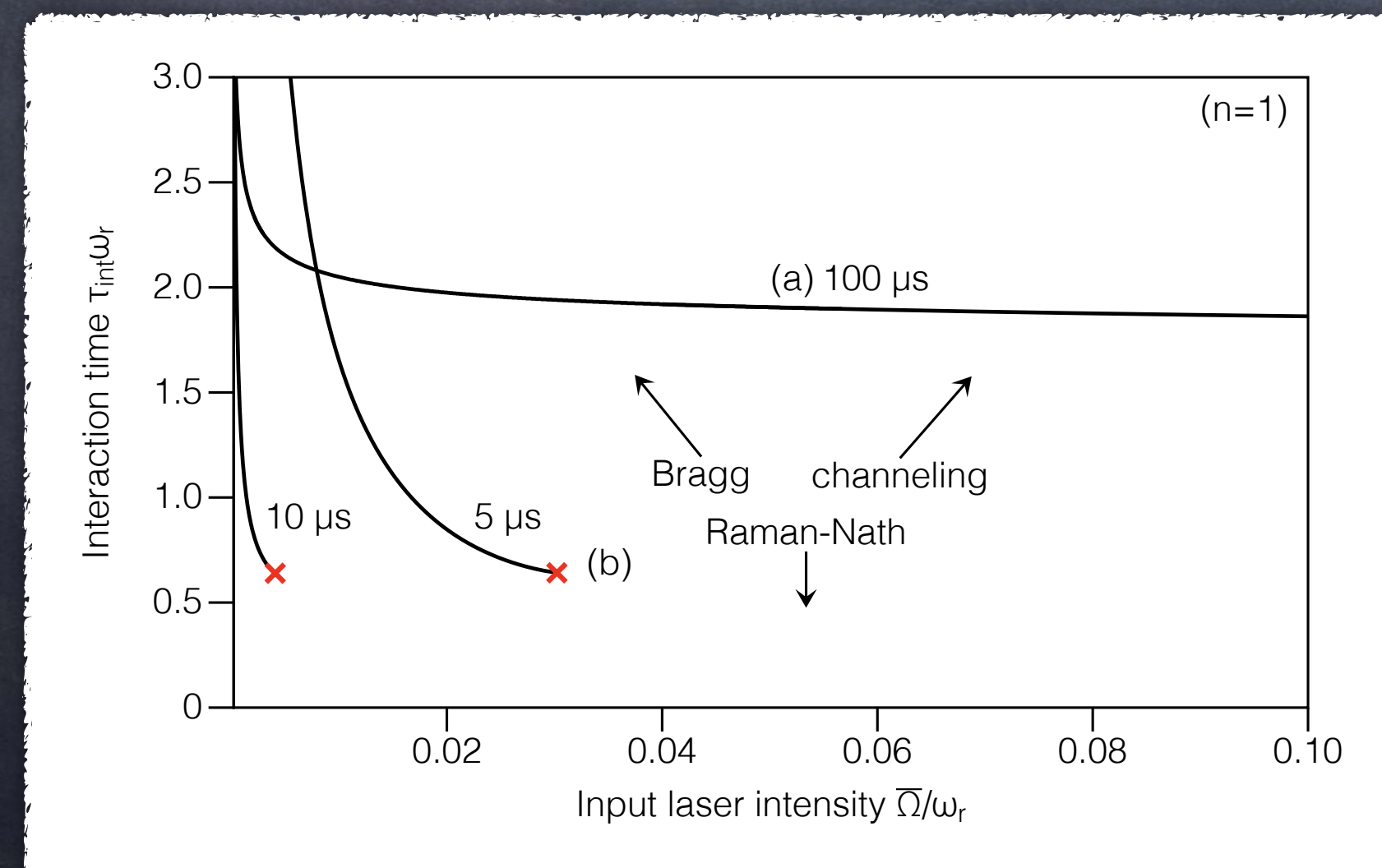




# • Effect of the cavity on the atomic transitions

• Cavity "pushes" the interactions to the Bragg and channeling regimes, and away from the Raman-Nath and quasi-Bragg zone.

• There is an optimal photon lifetime, above which the minimum interaction time increases linearly.  
 $\Rightarrow$  the transitions become adiabatic.



• The order of the process makes the intensity/duration variation over the optimal photon lifetime more steep.

# • Effect of the cavity on the atomic transitions

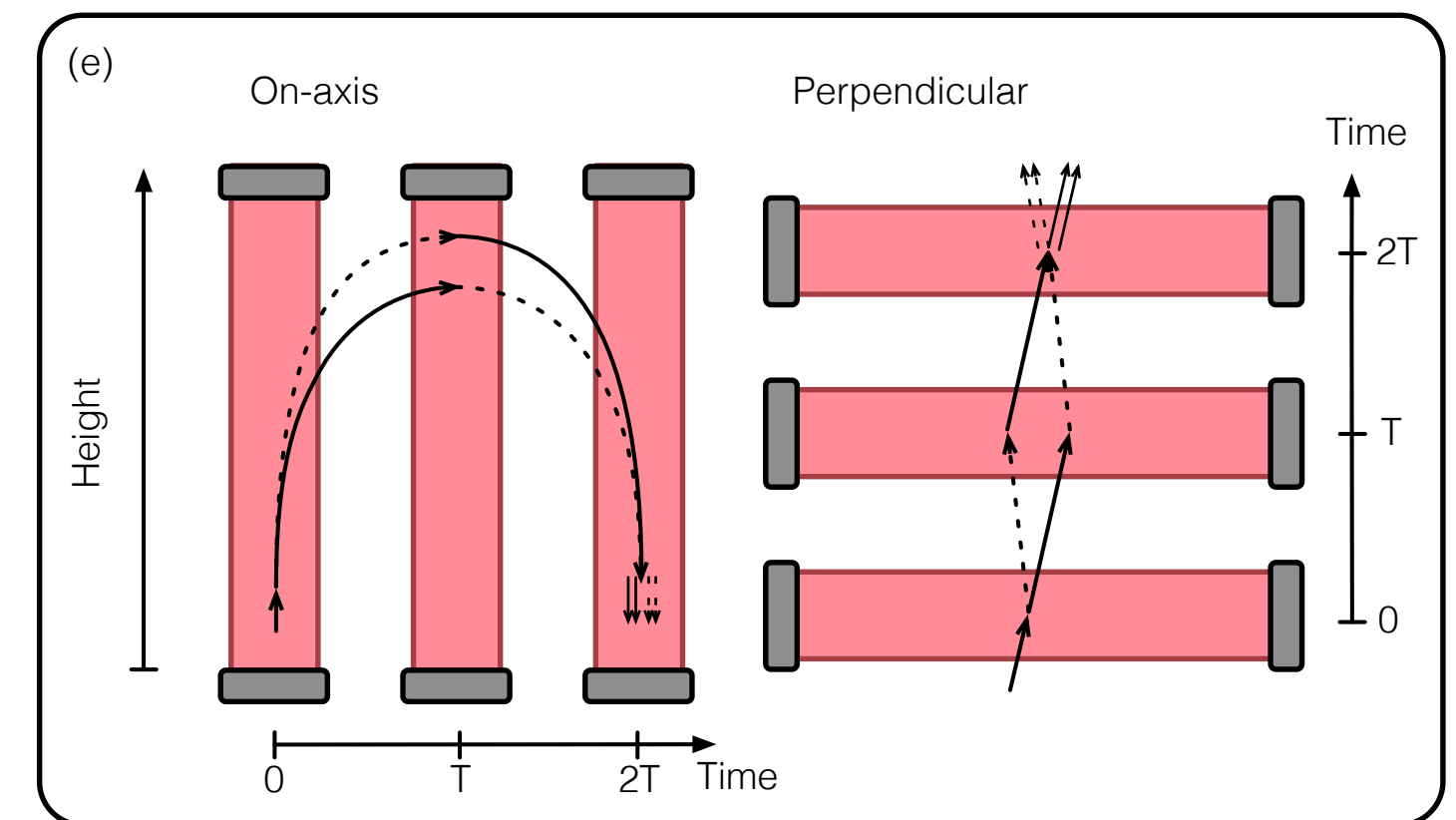
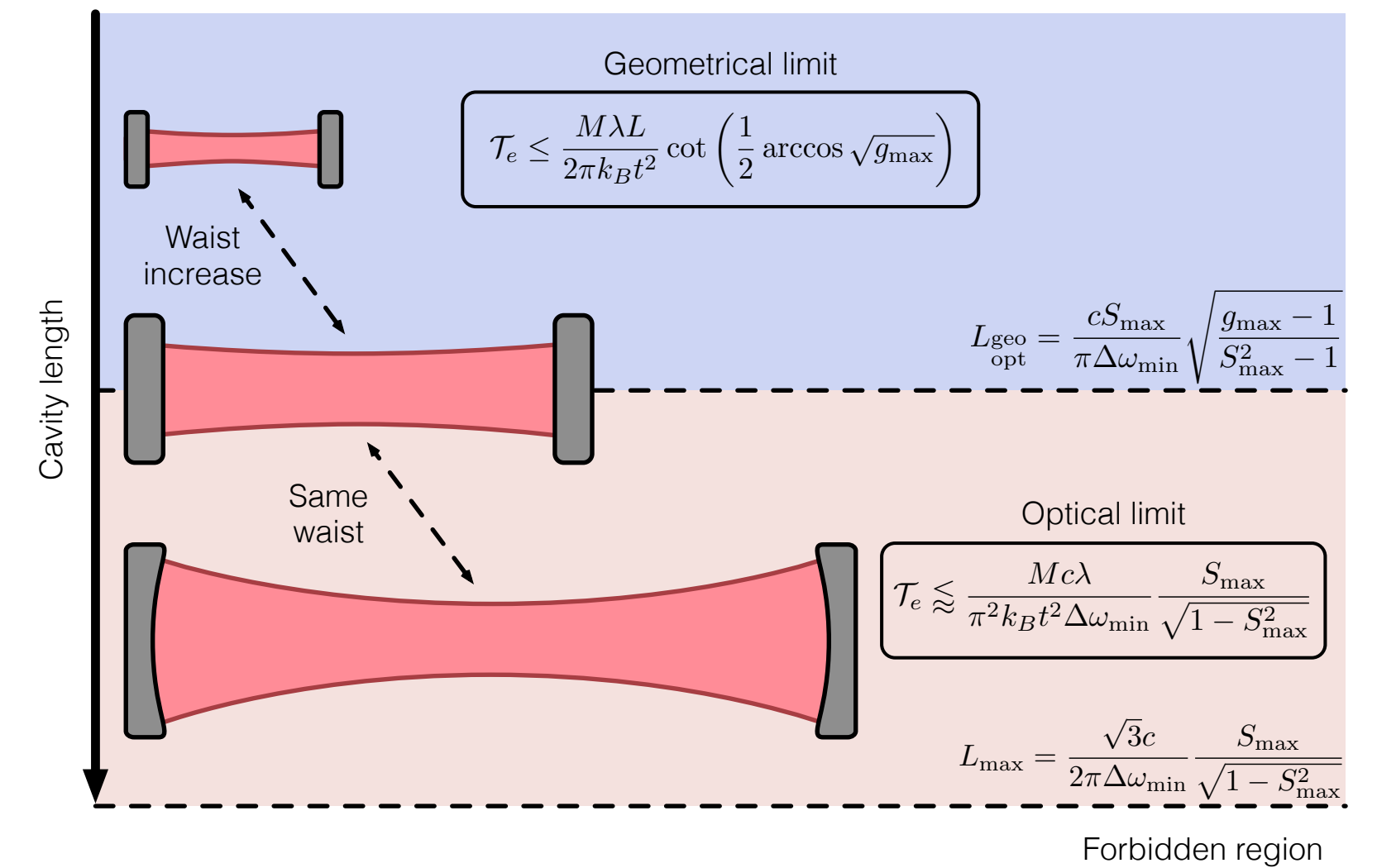
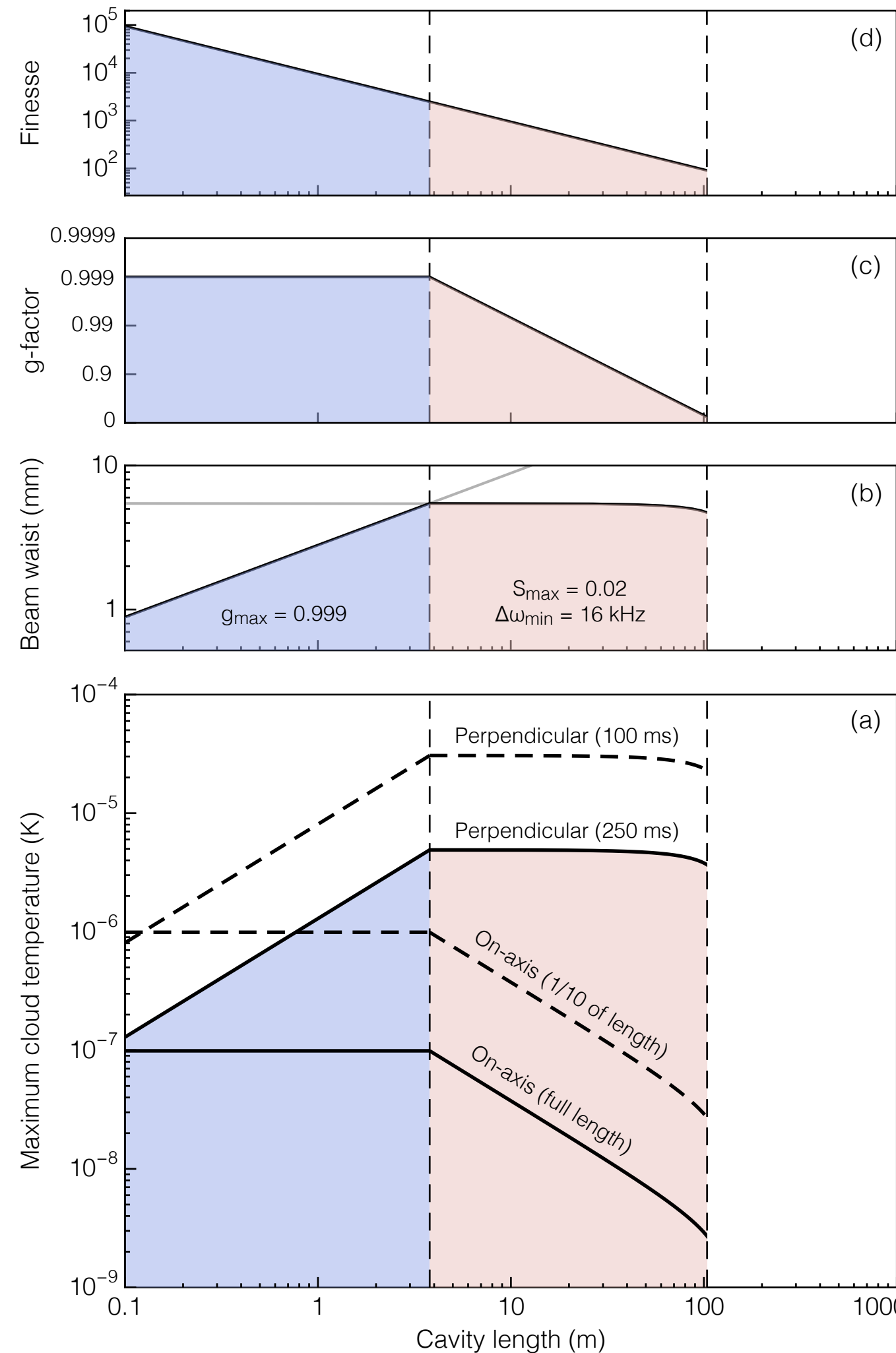
Geometrical limit:

$$g \leq g_{\max}$$

Optical limit:

$$S_{01}, S_{02} \leq S_{\max}$$

$$\Delta\omega \geq \Delta\omega_{\min}$$



- Cavities have an optimal photon lifetime or bandwidth for Bragg diffraction.
- It depends on the order of diffraction, higher orders have more acute intensity/duration changes around the turning point.
- Taking that as a design limit, we can derive temperature limits based on:
  - Having a geometrically stable configuration.
  - Achieving a certain level of spatial filtering.
- Cavities are great for atom interferometry and GW detection.

## Future work

- Previous work only 1D (constrain on beam quality introduced by optical suppression of HOMs)
- Future modelling work to include full-3D wavefront model (constrain on beam quality introduced by target interferometric contrast)
- Currently developing a four-mirror large-waist cavity with a total Gouy phase shift close to 180 degrees.

# Thank you!

## My papers:

Feasibility of near-unstable cavities for future gravitational-wave detectors  
PRD **97**, 022001 (2018)

Fundamental limitations of cavity-assisted atom interferometry  
PRA **96**, 053820 (2017)

The influence of dual-recycling on parametric instabilities at Advanced LIGO  
CQG **34**, 205004 (2017)

Thermal modelling of Advanced LIGO test masses  
CQG **34**, 115001 (2016)

Development of a four-mirror large-waist optical cavity for atom optics  
*In preparation (2018)*

Ultra-stable low-drift laser towards  $10^{-17}$   
*In preparation (2018)*

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Web: [migueldovale.com](http://migueldovale.com)

Currently  
job-seeking