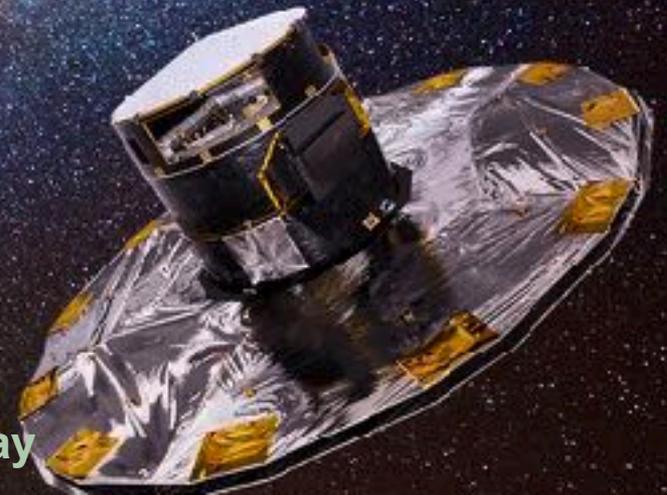


Testing gravity with Gaia

Mariateresa Crosta

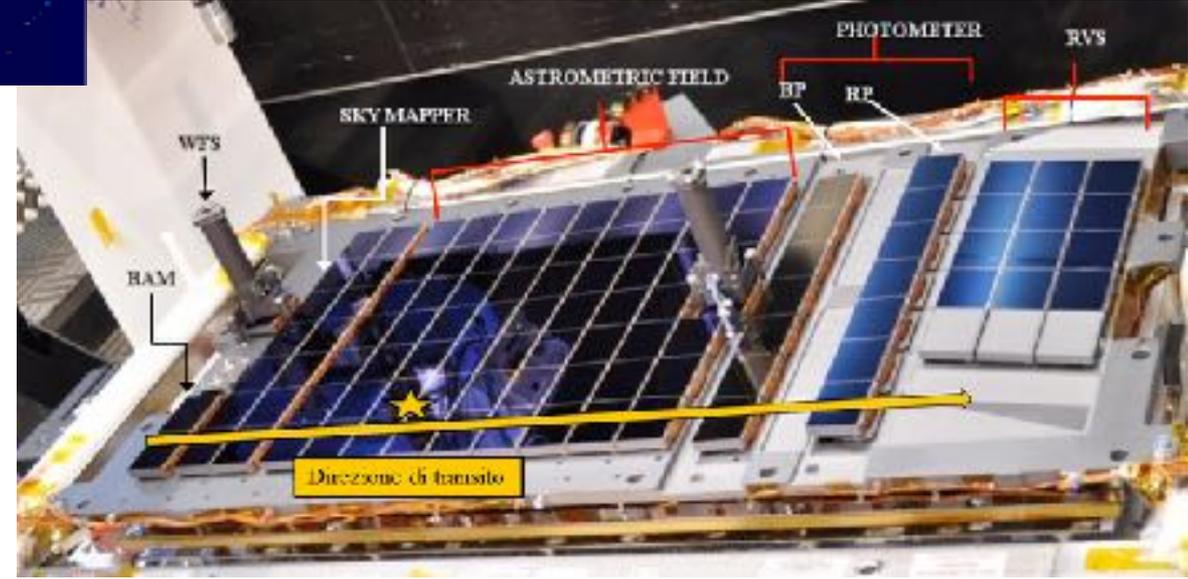
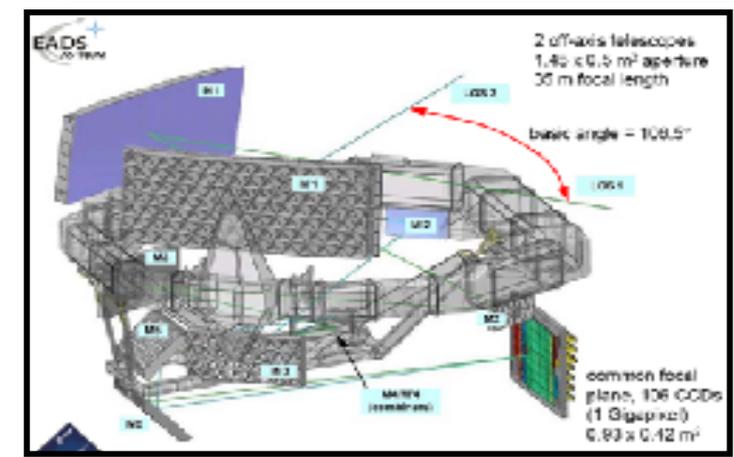
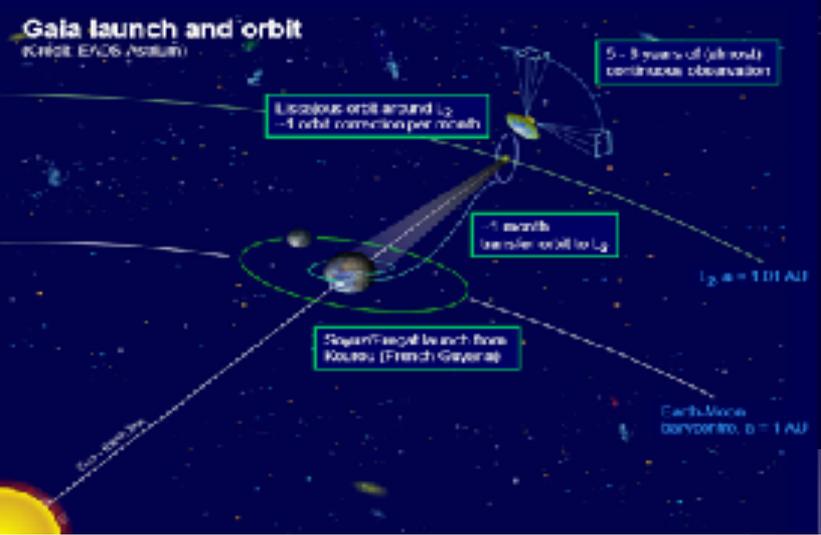
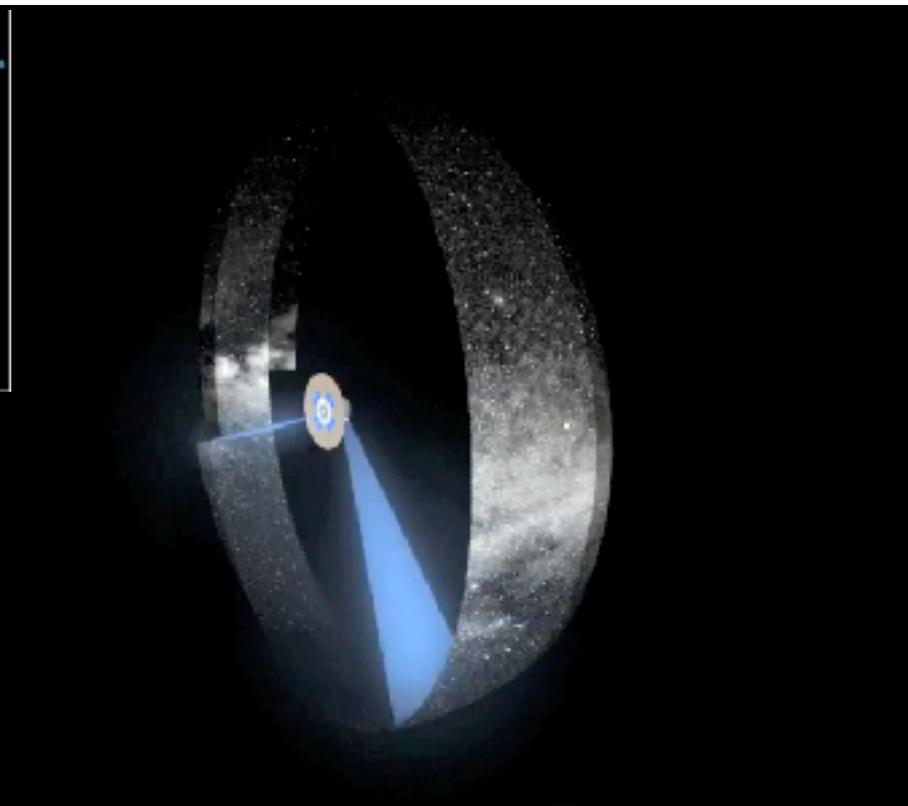
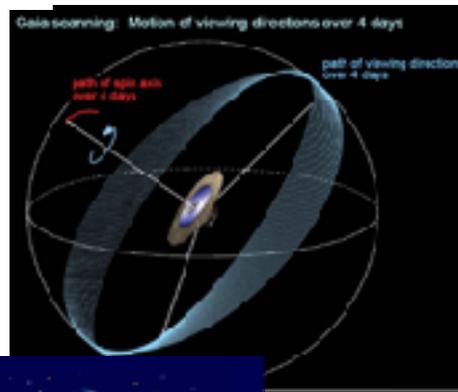
INAF
Osservatorio Astrofisico di Torino



Vulcano Workshop 2018, 21-26 May

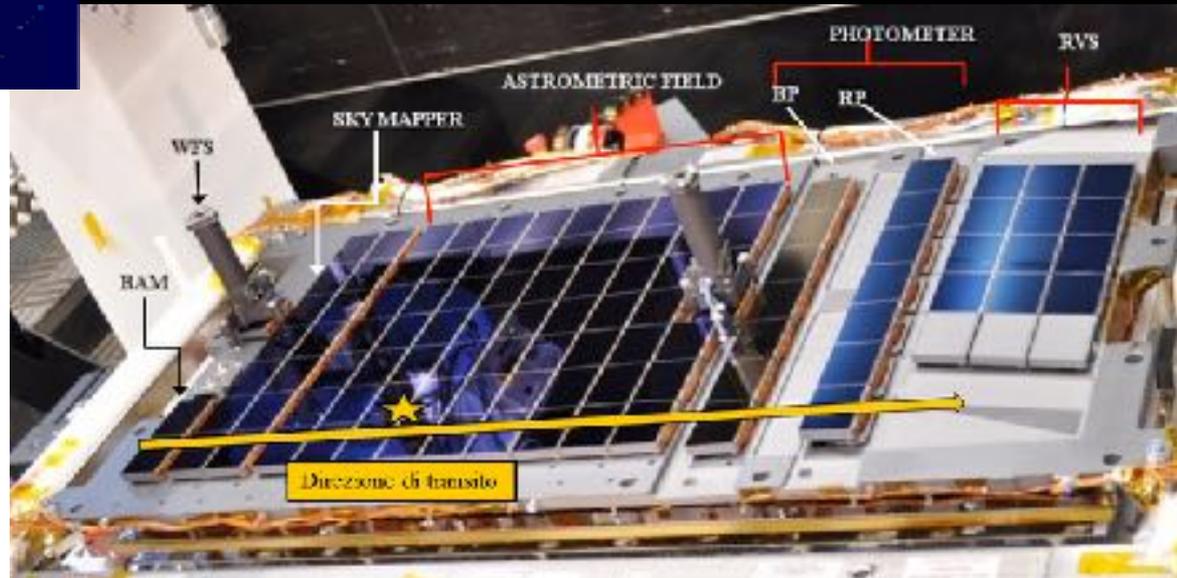
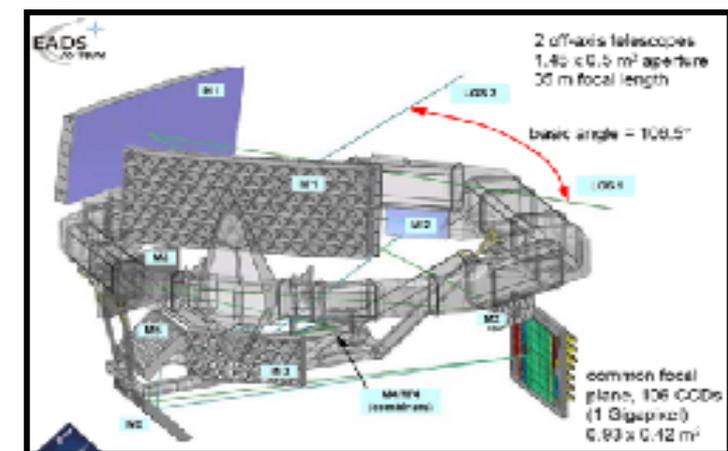
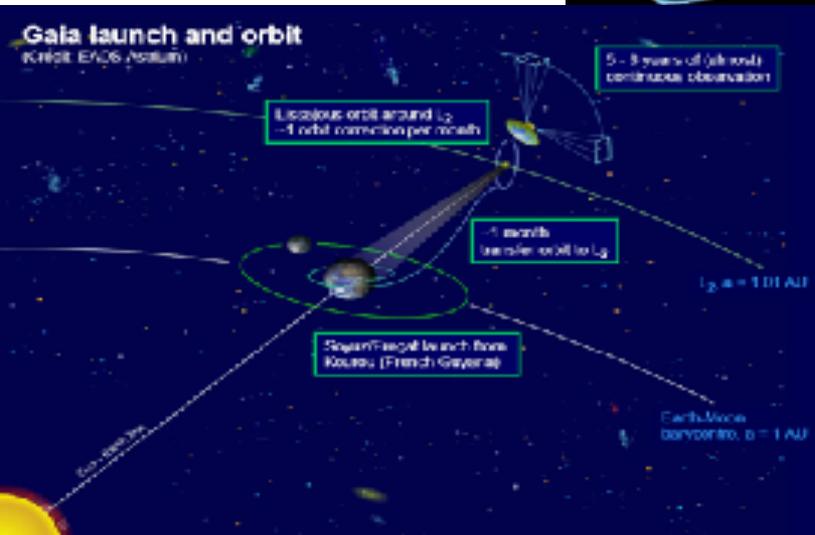
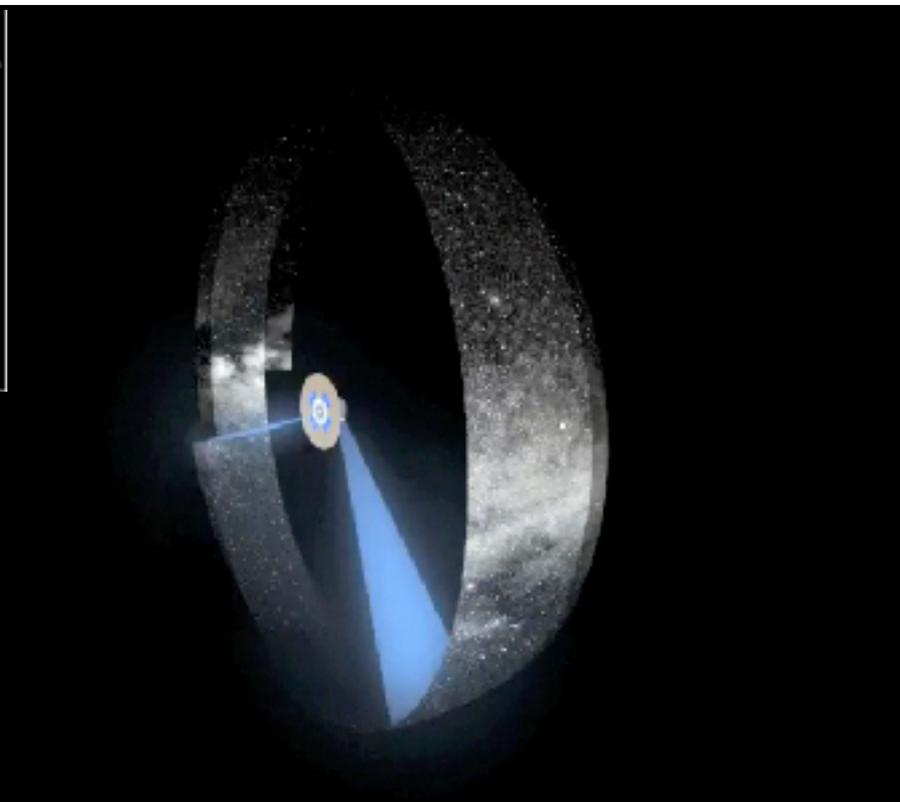
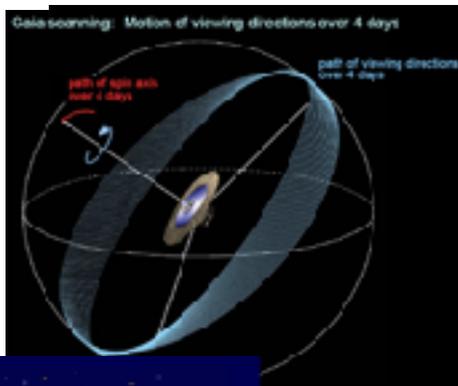


Gaia





Gaia



Gaia – main characteristics and status

<https://www.cosmos.esa.int/web/gaia/home>

science with **one/two billion objects in 3 dimension**

from structure and evolution of the MW to GR

Astrometry, photometry, spectroscopy (RVS)

- Astrometry and photometry $G < 20.7$ mag
- Stars brighter than $G=3$ captured with Sky Mapper imager
- Spectra still to $G_{RVS}=16.2$

Satellite (including payload) by industry, management and operations by ESA, data processing by scientists (DPAC)

Nominal mission end: mid-2019

Extension: possible up to end-of-2023 \pm 1 year

✓ Now in 5-year routine operations (since 25/7/2014)

✓ First DR end of summer 2016

2 million stars complete to $V=11.5$, sub-mas: 10 % at 300 pc

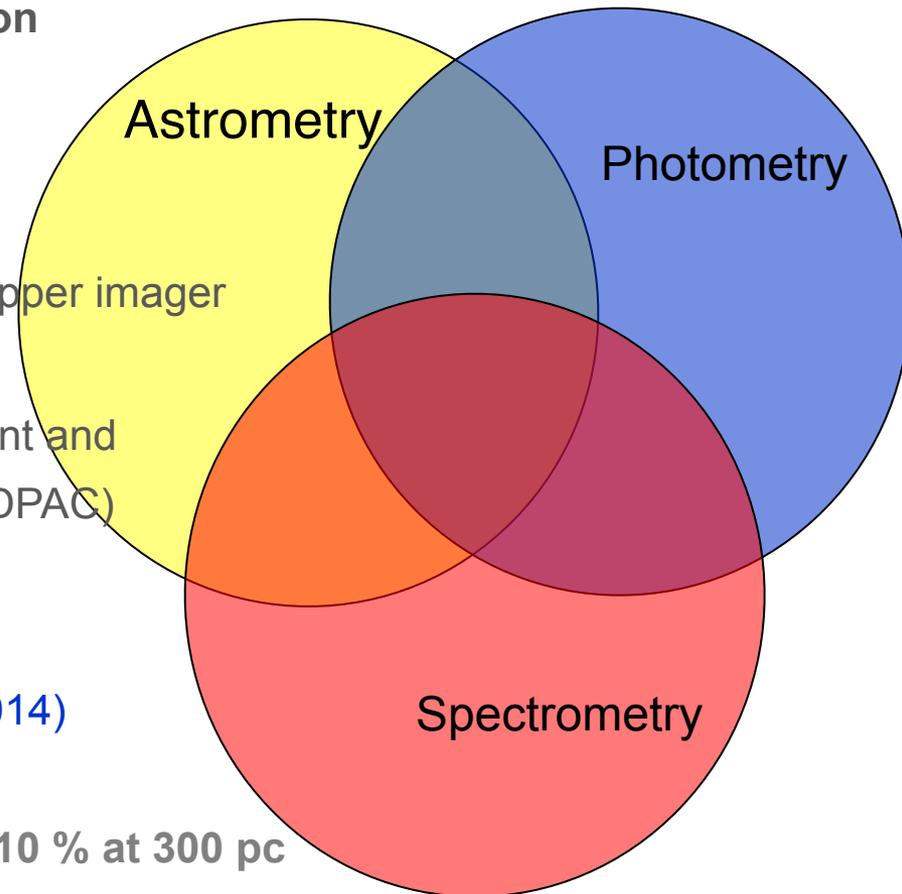
✓ Second DR on April 25th 2018, 22 months of data collection

1.3 billion stars complete astrometry (parallax) between $G=12$ and $G=17$,

100 μ as: 10 % 1kpc, solar neighborhood much more detailed

✓ Last DR in 2022 (or 2025) with full accuracy (10 μ as for the bright stars)

Data Release Scenario <http://www.cosmos.esa.int/web/gaia/release>



Gaia – main characteristics and status

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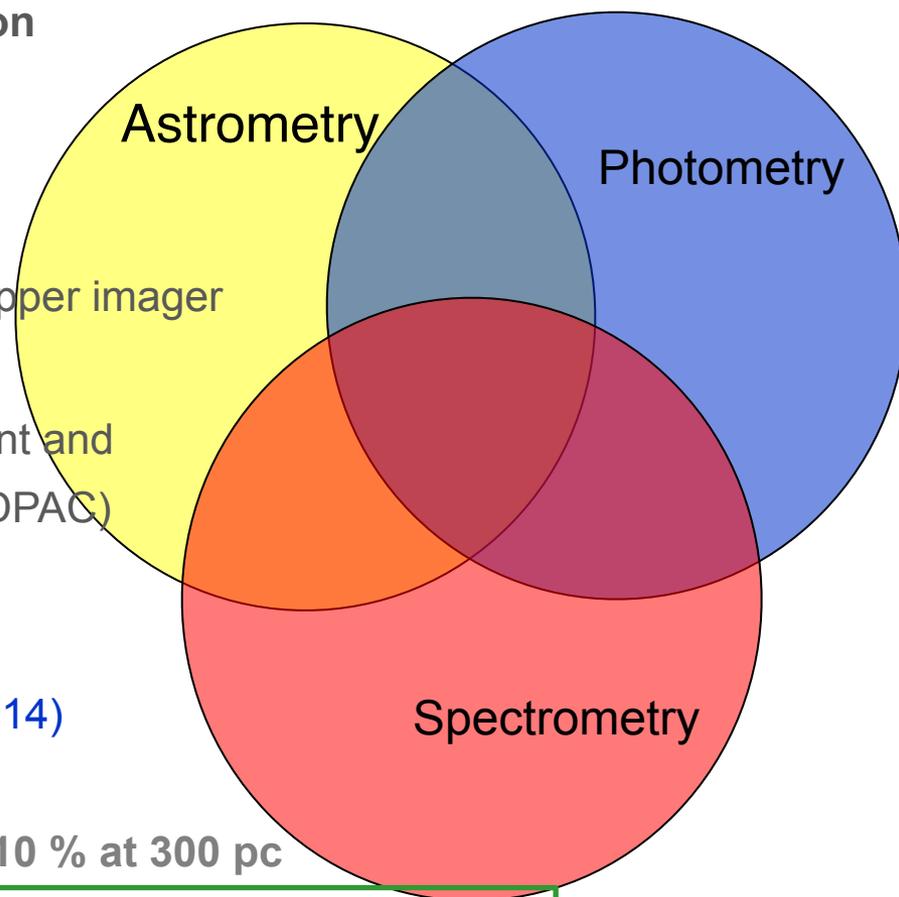
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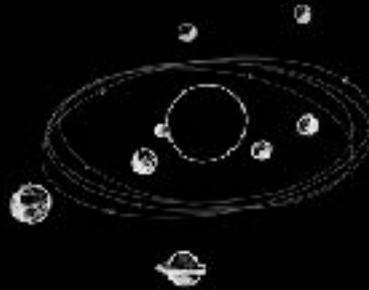


Second Data Release Scenario

<https://www.cosmos.esa.int/web/gaia/dr2>



Earth & Gaia



Solar System objects



Stars near the Sun



Milky Way: disc and bulge



Celestial reference frame: distant quasars



Nearby galaxies



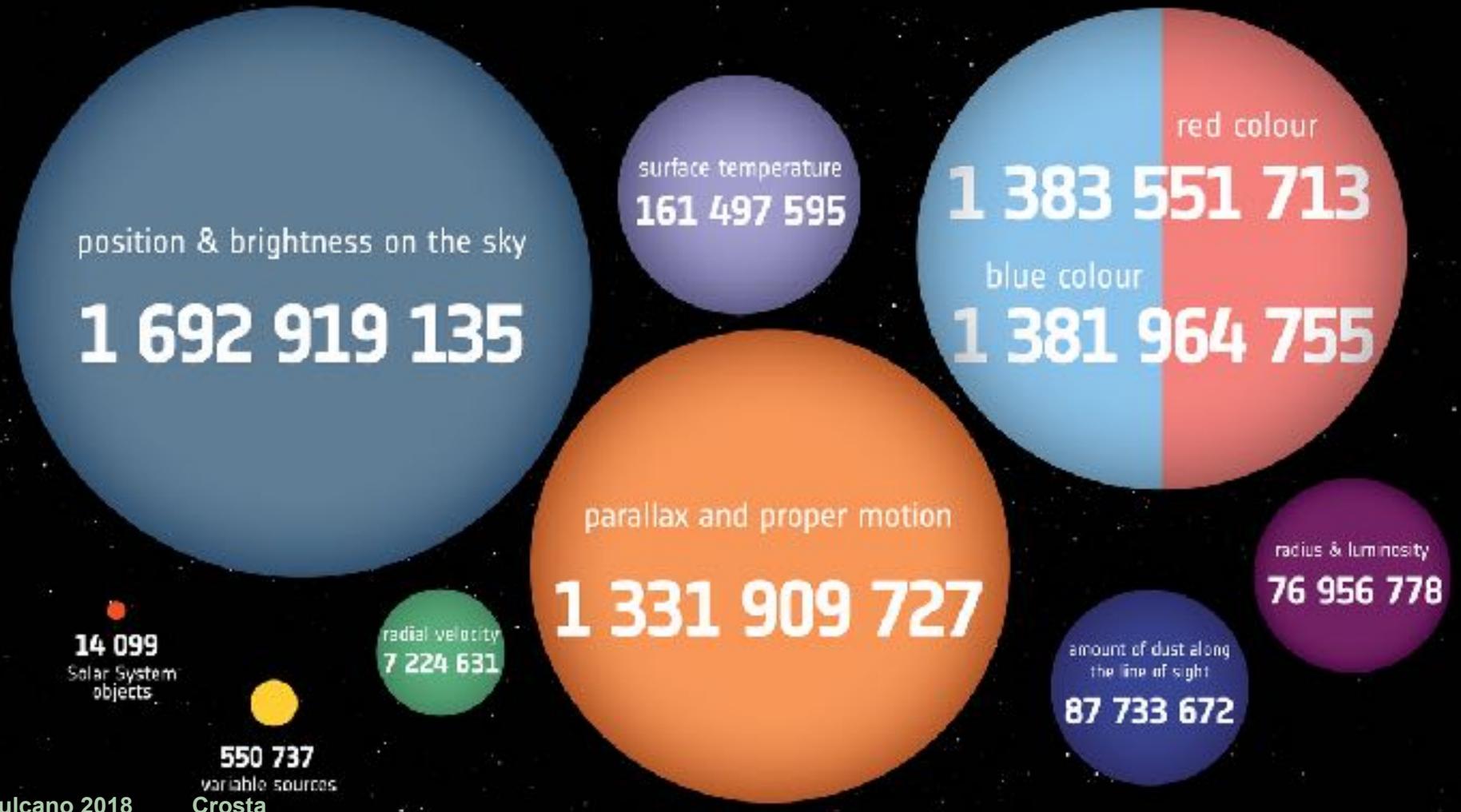
Milky Way: halo and globular clusters

Second Data Release Scenario

<https://www.cosmos.esa.int/web/gaia/dr2>



→ HOW MANY STARS WILL THERE BE IN THE SECOND GAIA DATA RELEASE?

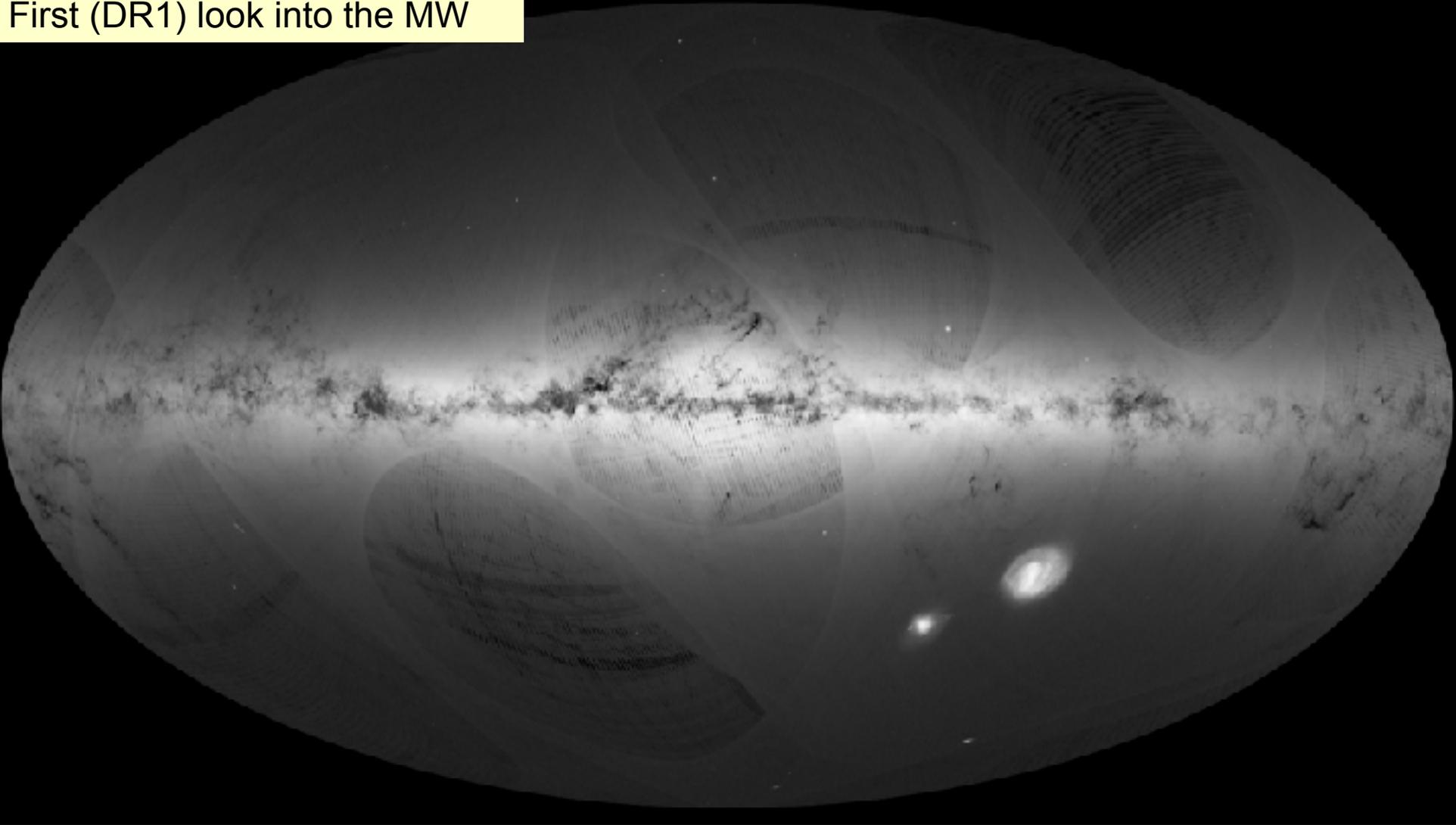


Gaia's look into the Milky Way

<http://www.cosmos.esa.int/web/gaia/science>

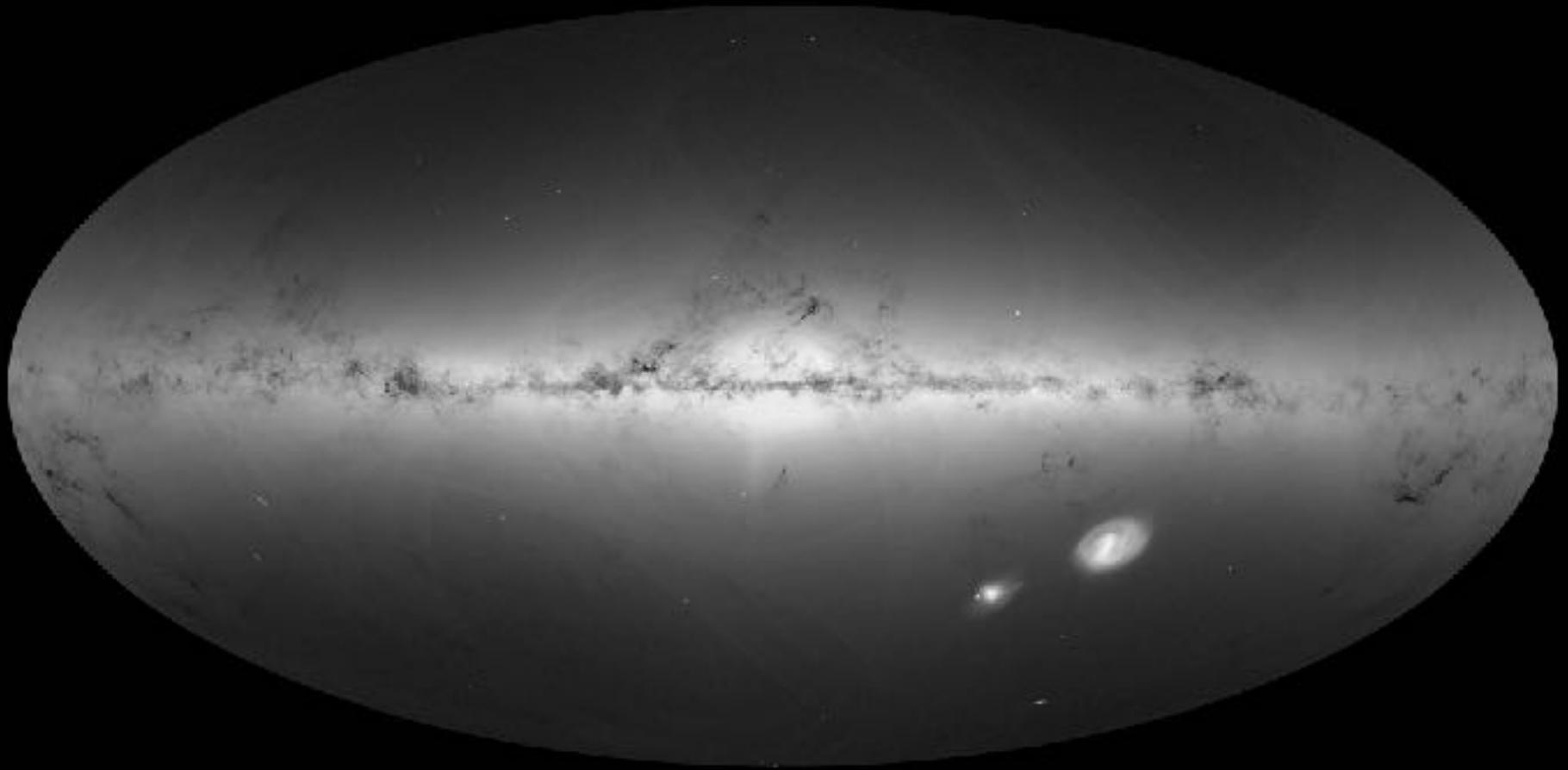
Gaia's look into the Milky Way

First (DR1) look into the MW



<http://www.cosmos.esa.int/web/gaia/science>

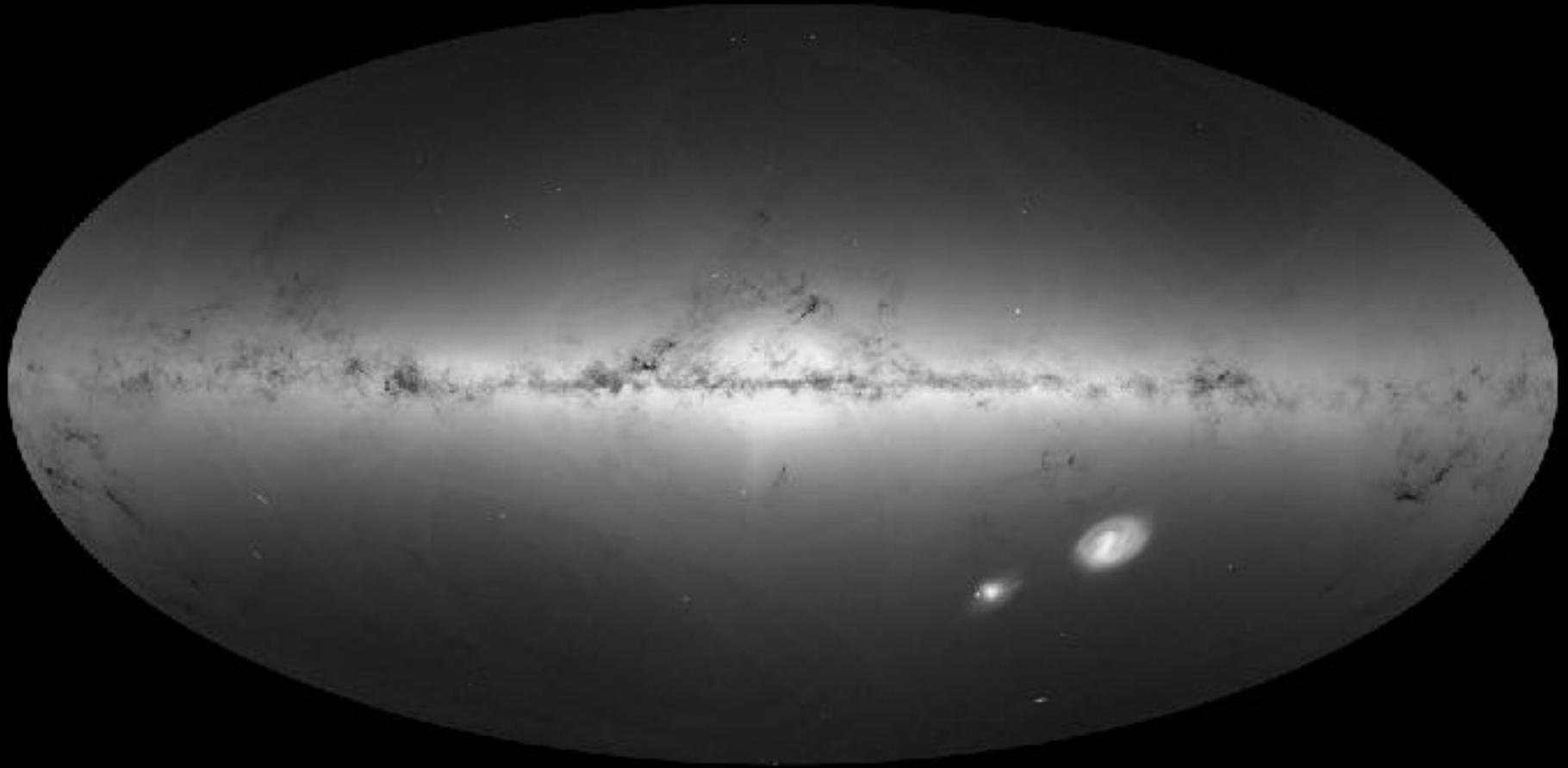
Gaia's look into the Milky Way



Acknowledgement: Gaia Data Processing and Analysis Consortium (DPAC); A. Moitinho / A. F. Silva / M. Barros / C. Barata, University of Lisbon, Portugal; H. Savietto, Fork Research, Portugal.

Gaia's look into the Milky Way

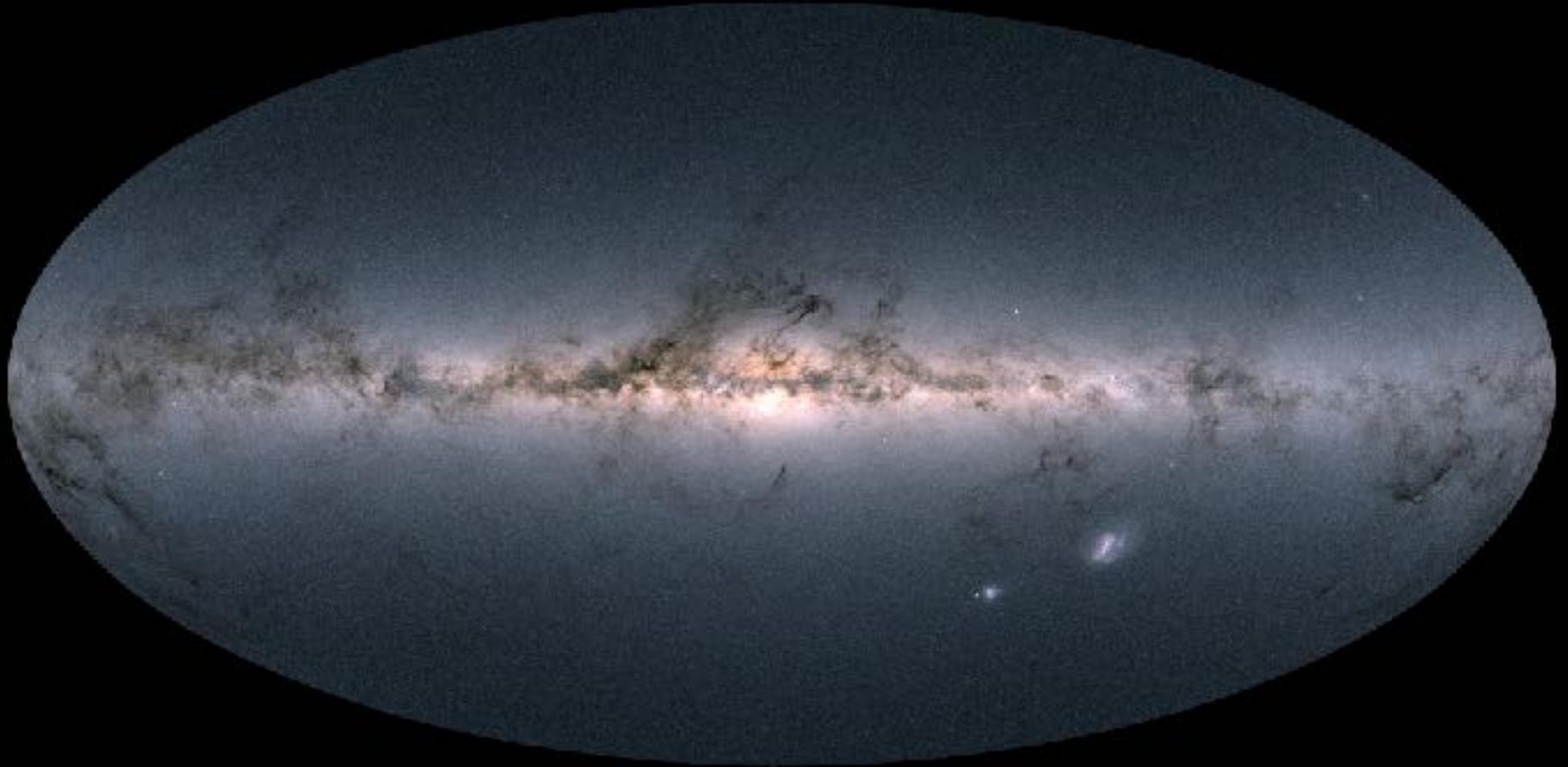
Second (DR2) look into the MW



Acknowledgement: Gaia Data Processing and Analysis Consortium (DPAC); A. Moitinho / A. F. Silva / M. Barros / C. Barata, University of Lisbon, Portugal; H. Savietto, Fork Research, Portugal.

Gaia's look into the Milky Way

Second (DR2) look into the MW



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Gaia's look into the Milky Way

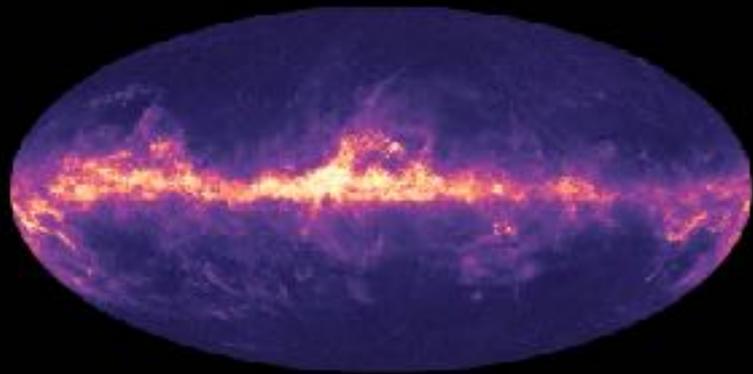
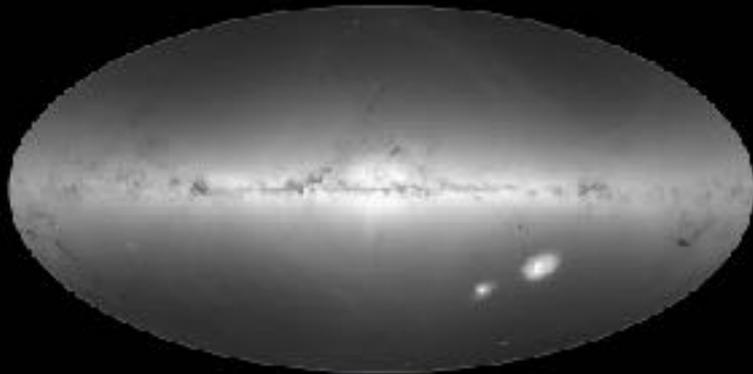
Second (DR2) look into the MW



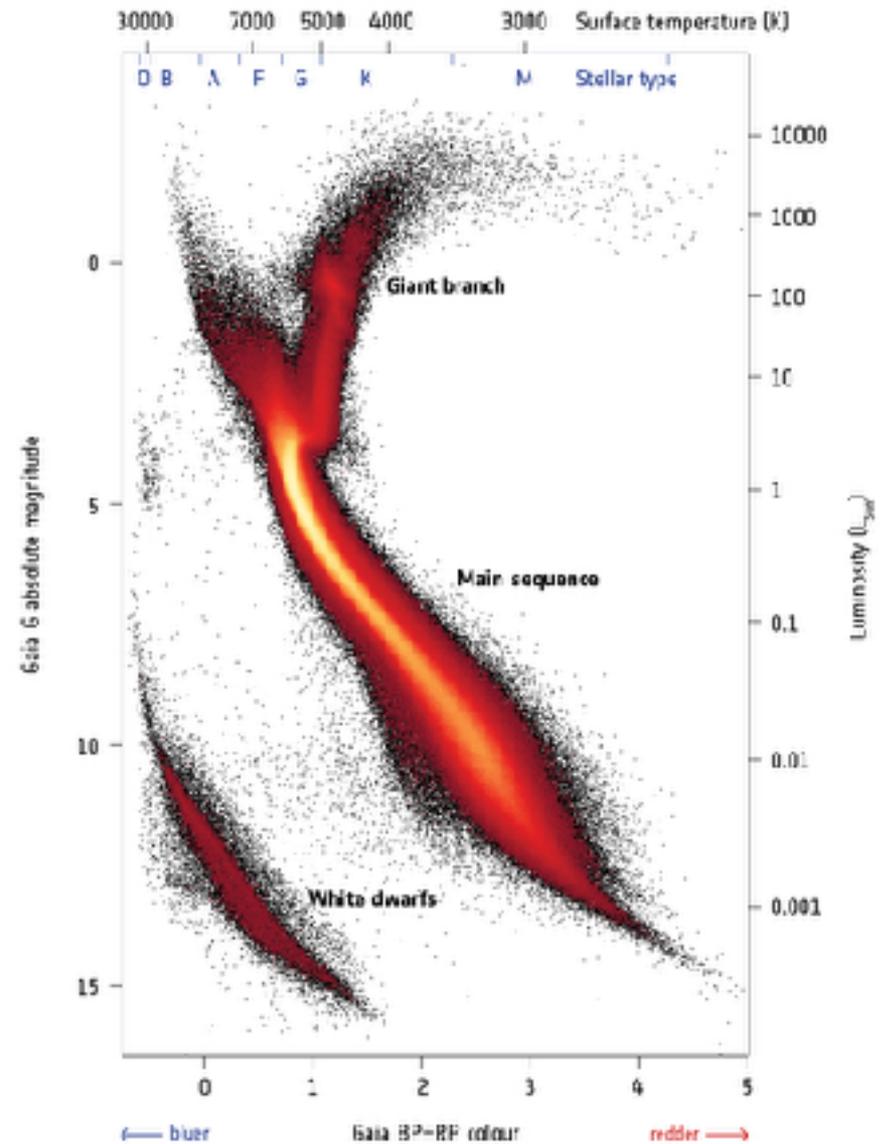
end-of-mission
astrometric accuracies
better than 5-10 μ as
for the brighter stars and
130-600 μ as for faint
targets

Acknowledgement: Gaia Data Processing and Analysis Consortium (DPAC); A. Moitinho / A. F. Silva / M. Barros / C. Barata, University of Lisbon, Portugal; H. Savietto, Fork Research, Portugal.

→ GAIA: THE GALACTIC CENSUS TAKES SHAPE

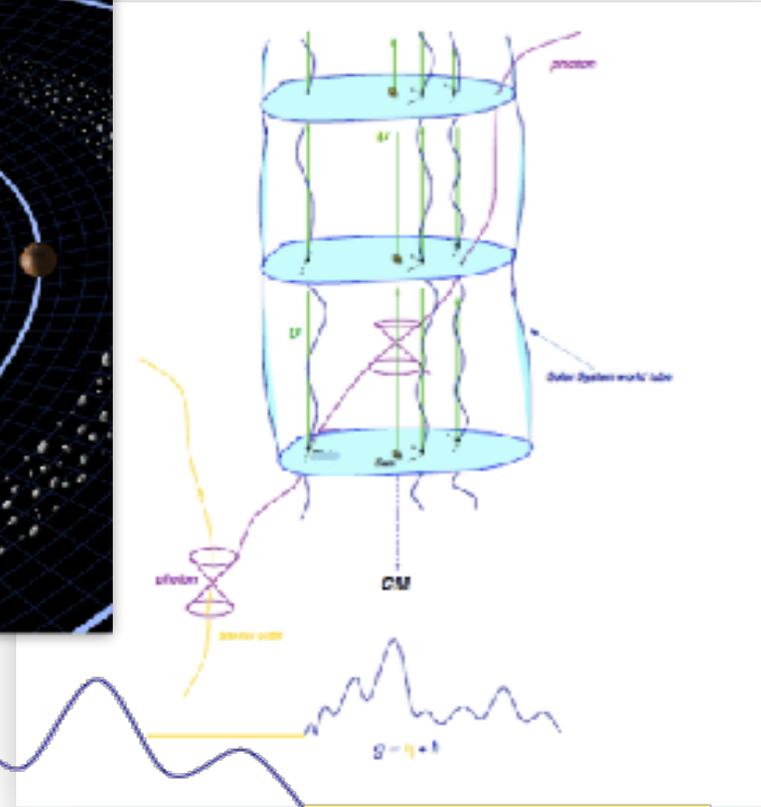
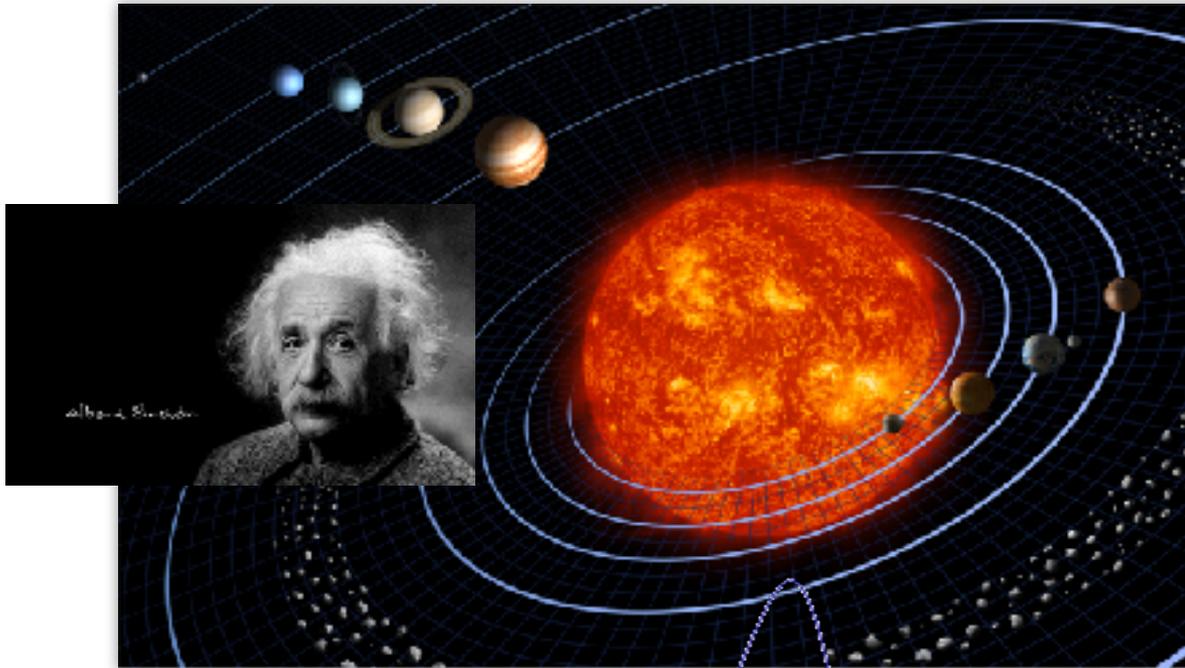


→ GAIA'S HERTZSPRUNG-RUSSELL DIAGRAM



**Our laboratory:
the Solar System**

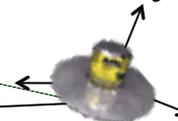
micro-arcsecond accuracy+ dynamical
gravitational fields=> relativistic models of
light propagation:
RELATIVISTIC ASTROMETRY



solar system metric

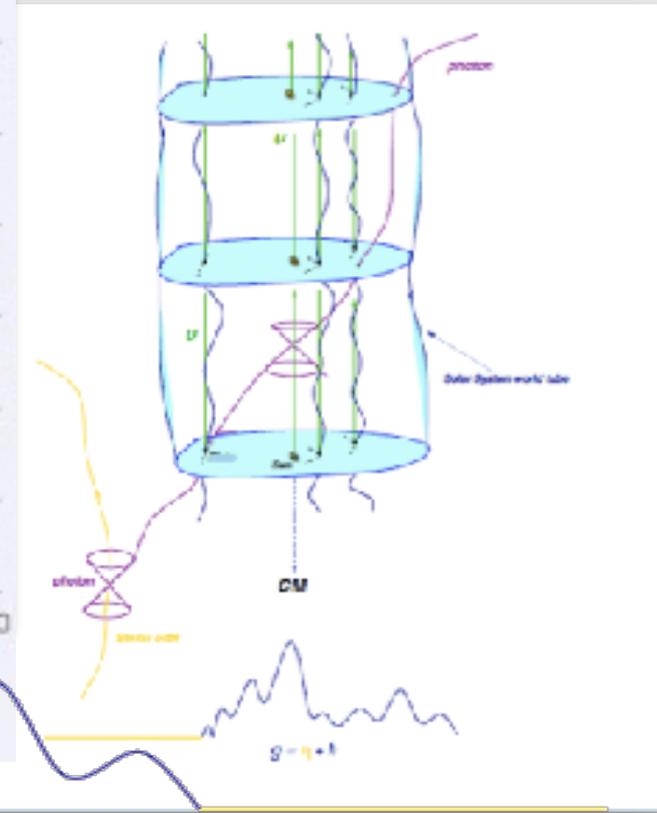
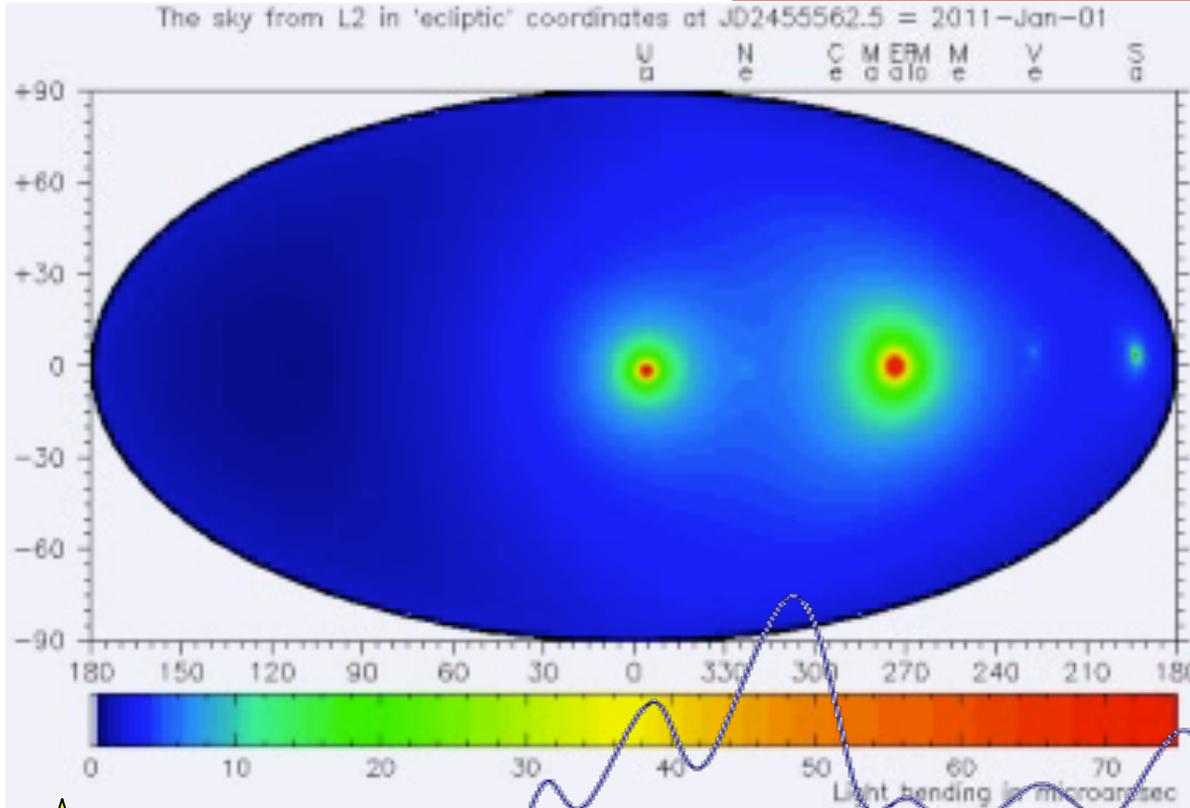
$$g = \eta + h$$

h perturbations at μ -arcsec due to
the solar system bodies



**Our laboratory:
the Solar System**

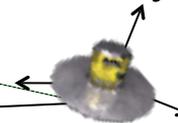
micro-arcsecond accuracy+ dynamical
gravitational fields=> relativistic models of
light propagation:
RELATIVISTIC ASTROMETRY



solar system metric

$$g = \eta + h$$

h perturbations at μ -arcsec due to
the solar system bodies



Light crossing the metric of the Solar System

$$g_{\alpha\beta} = \eta_{\alpha\beta} + h_{\alpha\beta} + O(h^2)$$

$$|h_{\alpha\beta}| \ll 1$$

according to the Virial Theorem

$$|h_{\alpha\beta}| \leq U/c^2 \sim v^2/c^2 \rightarrow \epsilon^2$$

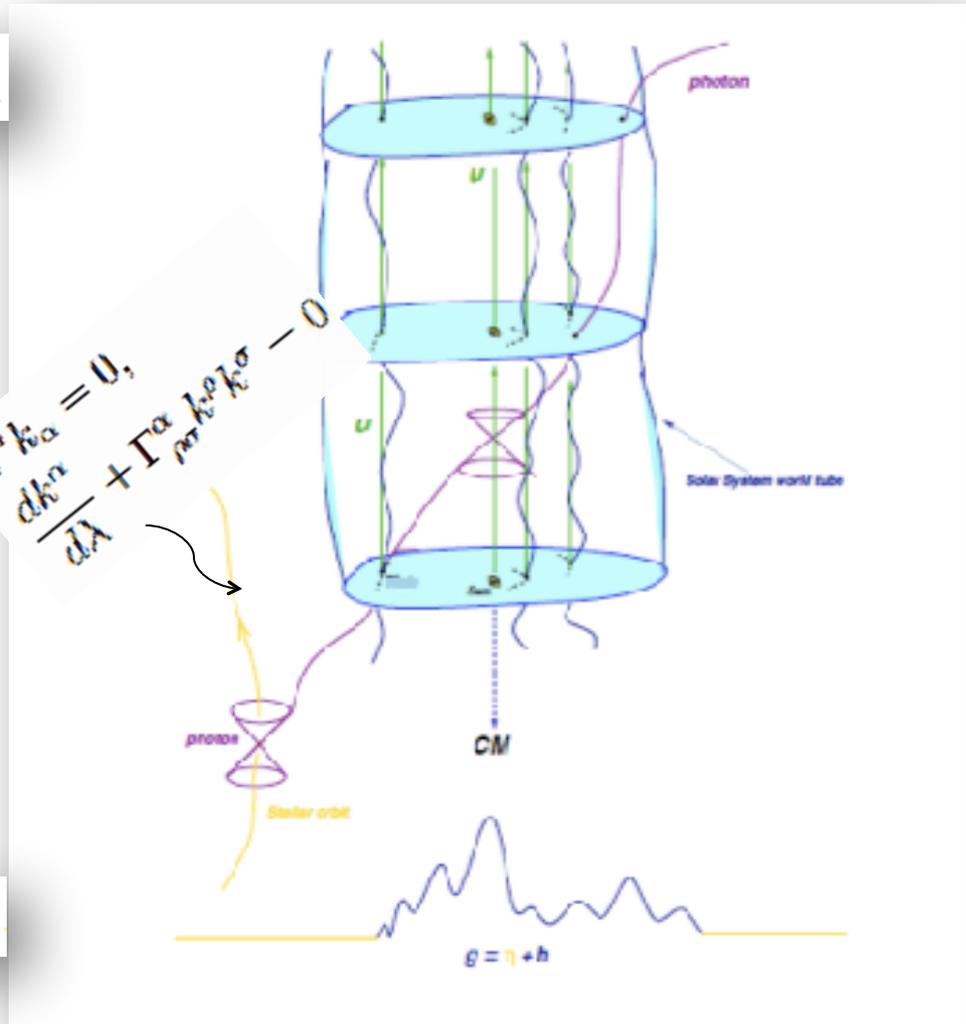
$$\sim v^2/c^2 \sim GM/rc^2 \sim \text{mas accuracy}$$

which requires determination of
 g_{00} even terms in ϵ , lowest order $\epsilon^2 \sim \text{mas}$
 g_{0j} odd terms in ϵ , lowest order $\epsilon^3 \sim \mu\text{-as}$
 g_{ij} even terms in ϵ , lowest order $\epsilon^2 \sim \text{mas}$

Time variation of the order of

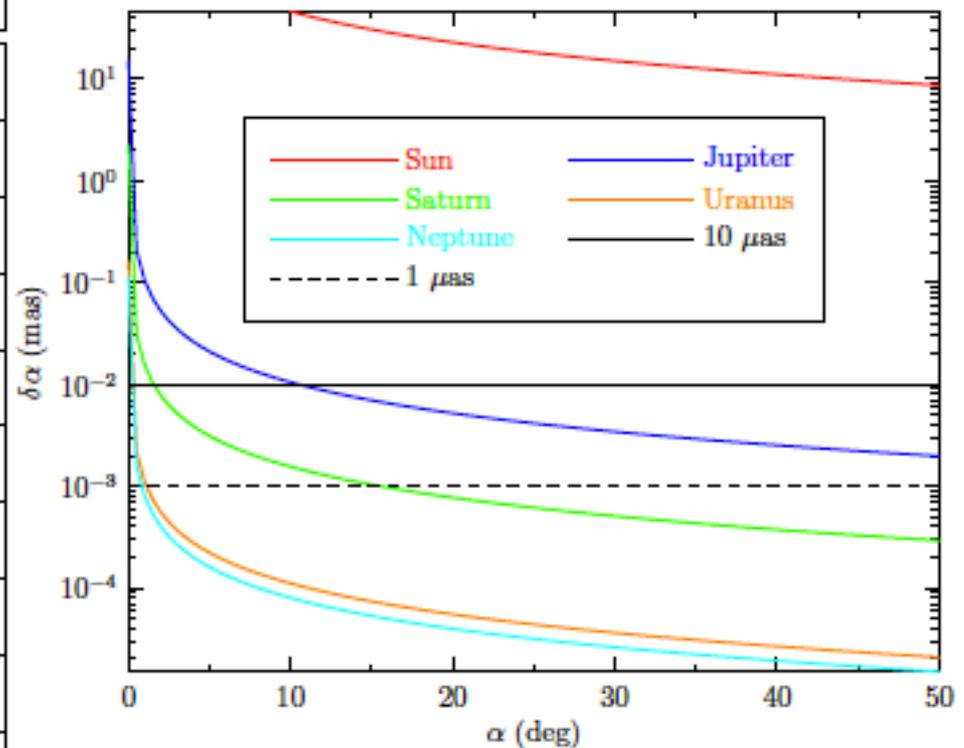
$$\epsilon |h_{\alpha\beta}|$$

→ **IAU metric!**



Detectable relativistic deflections at L2 at 1-PN level for grazing light ray

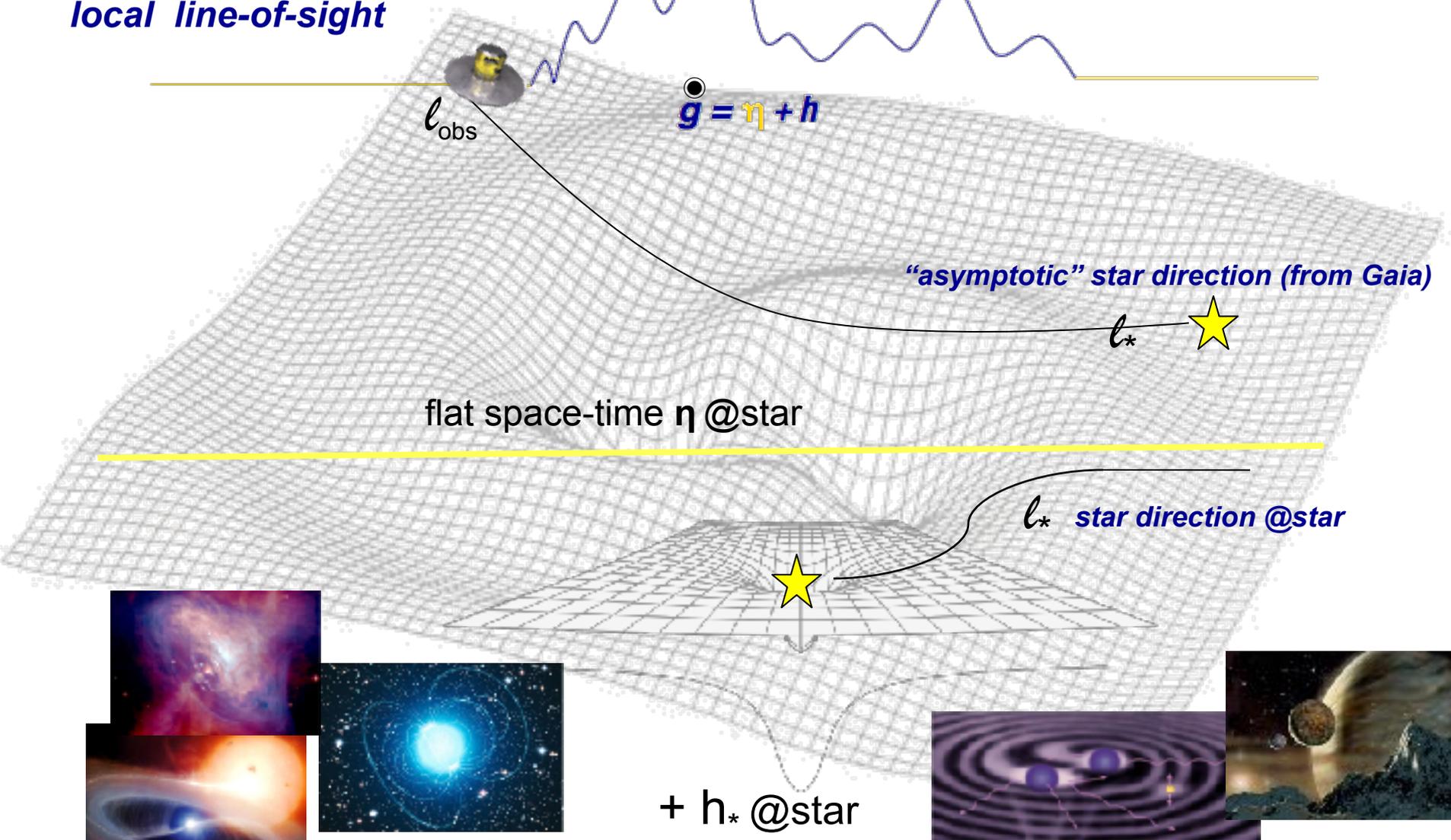
Body	$\delta\alpha_M$ (μas)	$\delta\alpha_Q$ (μas)
Sun	1.75×10^6	~ 1
Mercury	83	
Venus	493	
Earth	574	0.6
Moon	26	
Mars	116	0.2
Jupiter	16270	240
Saturn	5780	95
Uranus	2080	8
Neptune	2533	10



from the observer to the star through space-time: null geodesic

- in tracing back light rays we need to keep consistency, at any level of approximations, with GR
- this implies a new rendition of the astronomical observables and it may open, at the sub- μas level, a new detection window of many subtle relativistic effects naturally folded in the light while it propagates through the geometry of space-time up to the "local" observer

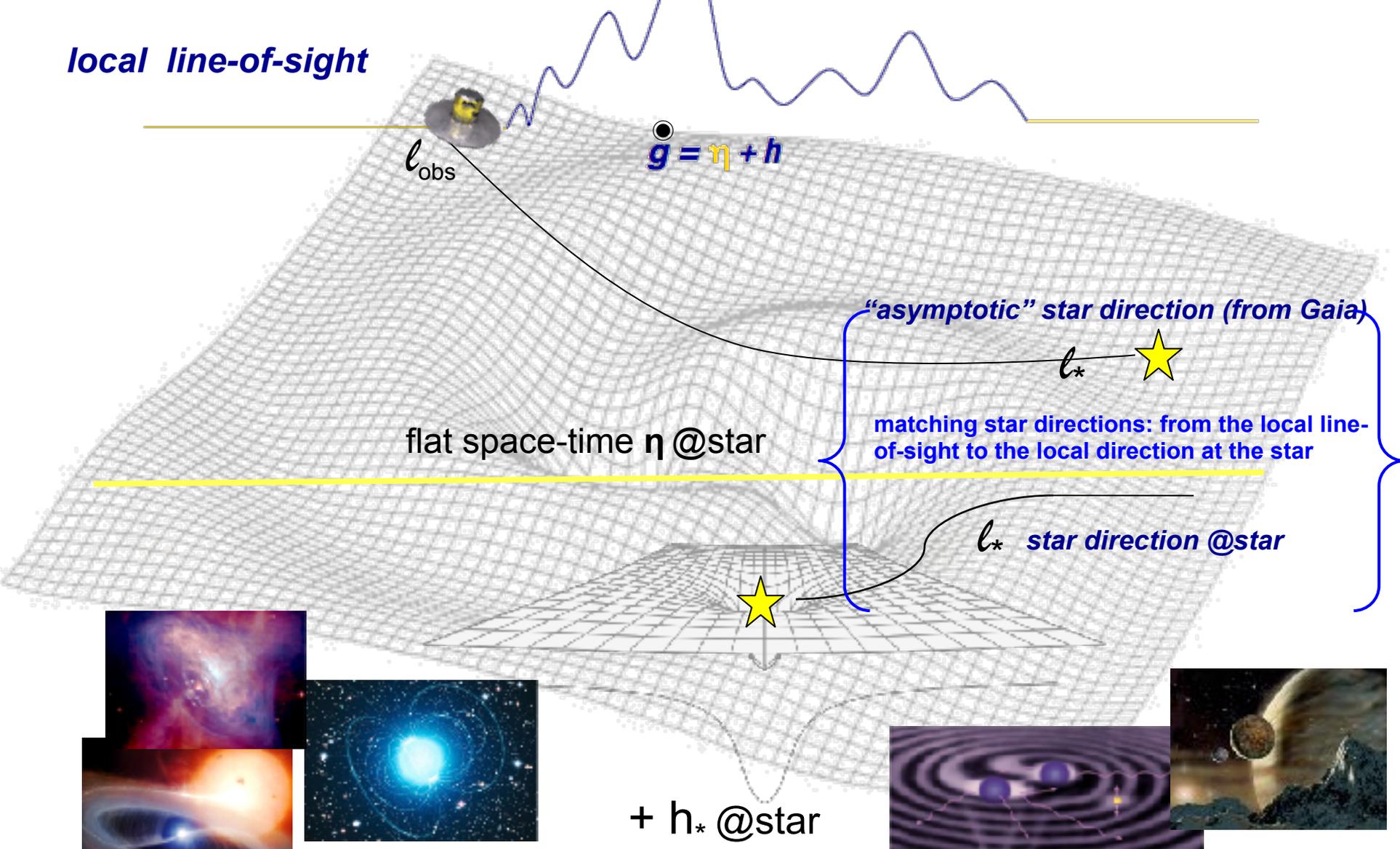
local line-of-sight



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local line-of-sight

+GWs!

l_{obs}

$g = \eta + h$

"asymptotic" star direction (from Gaia)

l_*

flat space-time η @star

matching star directions: from the local line-of-sight to the local direction at the star

l_*

star direction @star

+ h_* @star



Vulcano 2018

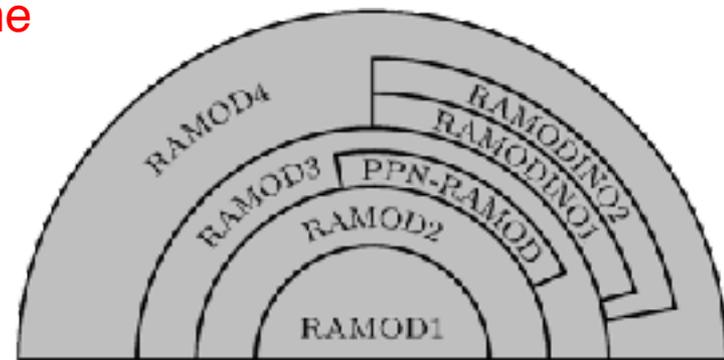
Crosta



Gaia, CU3- REMAT: RELativistic Models And Tests

- The core processes of the astrometric pipeline is the so-called Global Astrometric Sphere Reconstruction, which uses global astrometric techniques on a subset of primary stars/QSO's to materialize the IC reference frame (ICRF).
- Given the absolute character of such reconstruction, the the Consortium constituted for the Gaia data reduction (DPAC) agreed to set up **two independent sphere solutions: AGIS and GSR**.
- GSR stands for Global Sphere Reconstruction (and Comparison), and its twofold goal is to provide the DPAC with an independent global sphere and to compare it to its AGIS (Astrometric Global Iterative Solution, baseline) analogue (GREM model)
- The theoretical model implemented in GSR is the RAMOD family (Relativistic Astrometric MODEL) -> Astrometric Verification Unit (AVU, the 3rd fundamental component of the astrometric error budget) at the Italian data center (DPCT)

both models/solutions work on the same
Gaia data: independent validation process



RAMOD is a framework of general relativistic astrometric models with increasing intrinsic accuracy, adapted to many different observer's settings, **interfacing numerical and analytical relativity**
RAMOD applies the measurement protocol (MP) in GR



Italian Data Processing Center

All Gaia operations activities (daily and cyclic) done in Italy are implemented at the DPCT, the Italian provided HW and SW operations system designed, built and run by ALTEC (To) and INAF-OATo for ASI.

DPCT was established through a specific ASI contract via a partnership between INAF-OATo and ALTEC S.p.A.

- M. Castronuovo (RC, MLA-SC repr.)
- B. Negri (EOS Head)

This is the only Data Processing Center, within the network of 6 DPCs dedicated to Gaia, which specializes in the treatment of the satellite astrometric data

The DPCT hosts the systems AVU:

Essential components of Gaia's astrometric error budget

- ❖ CCD-level precision and accuracy (Astrometric Instrument Monitoring - AIM)
- ❖ Accuracy at the Optical System level (Basic Angle Monitoring - BAM/AVU)
- ❖ Precision & accuracy on the celestial sphere (Global Sphere Reconstruction - GSR)



DPCT at full capacity. Current size about 500 TB of data.

Size at completion ~ 1.2 PB

- ❖ MoU CINECA-INAf



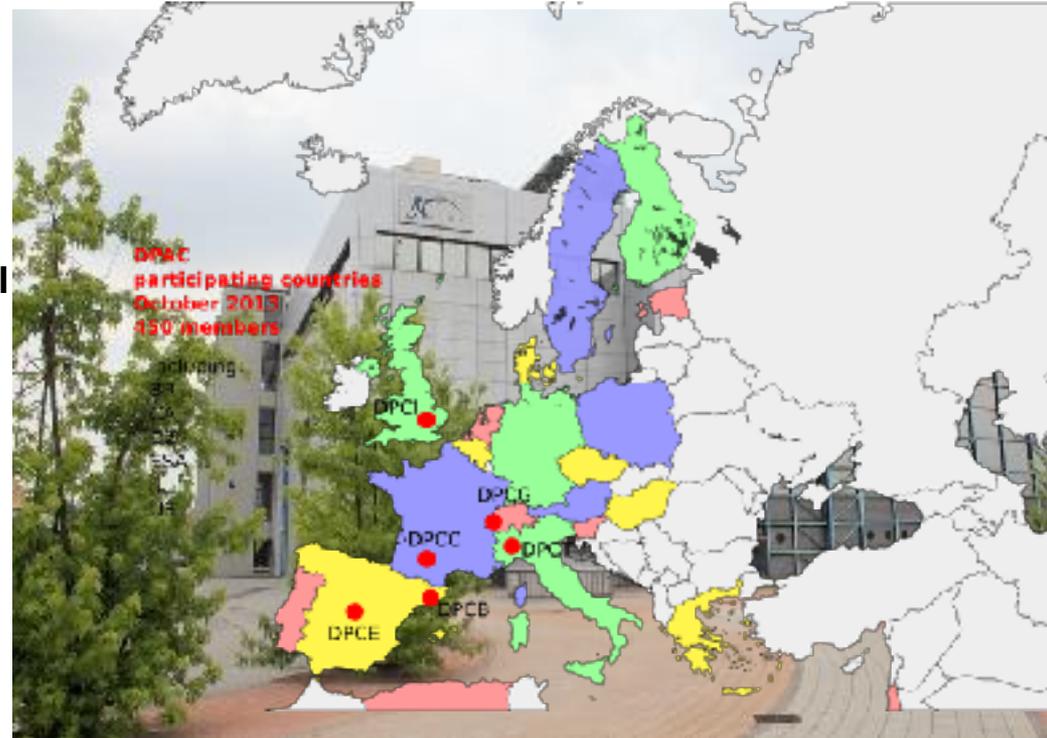
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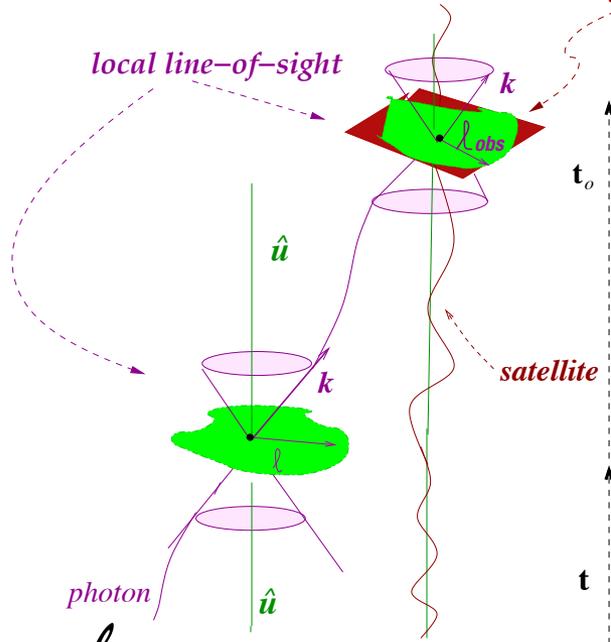
- ❖ MoU CINECA-INAf

RAMOD vs GREM

RAMOD-like models aim to estimate the astrometric parameters of celestial objects from a well-defined set of relativistically measured quantity

$$\ell^\alpha = P_\beta^\alpha(u) k^\beta(\tau) \rightarrow \frac{d\ell^\alpha}{d\sigma} = F^\alpha(\partial_\beta h(x, y, z, t), \ell^i(\sigma(x)))$$

attitude frame of the satellite



$$\mathbf{x}_* = F(\mathbf{x}_{\text{obs}}, \mathbf{g}_{\mu\nu}, \ell_{\text{obs}}, E_a, \dots)$$

The RAMOD local-line-of-sight is not exactly equal to the light direction used in the semi-classical approximation

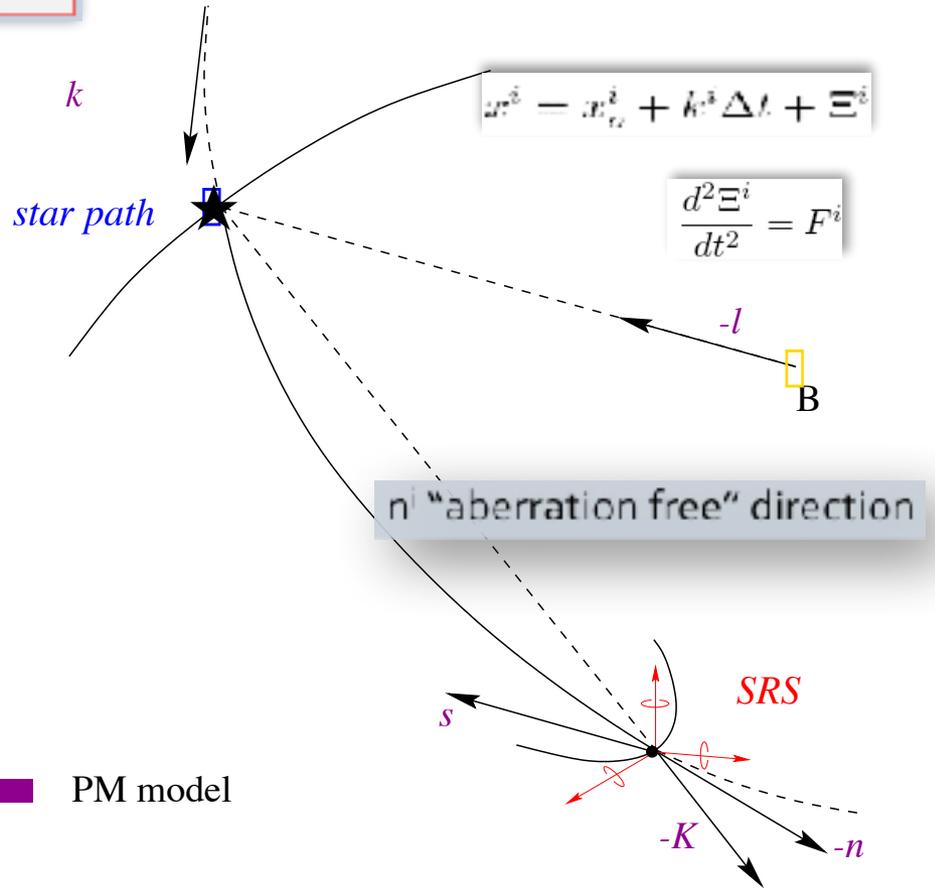
$$\bar{\ell}^i = n^i \left(1 - \frac{h_{00}}{2} \right) + \mathcal{O} \left(\frac{v^4}{c^4} \right)$$

aberrated (gravitational) direction

$$h_{00}/2 \approx U/c^2 \text{ (local potential) [IAU solution]}$$



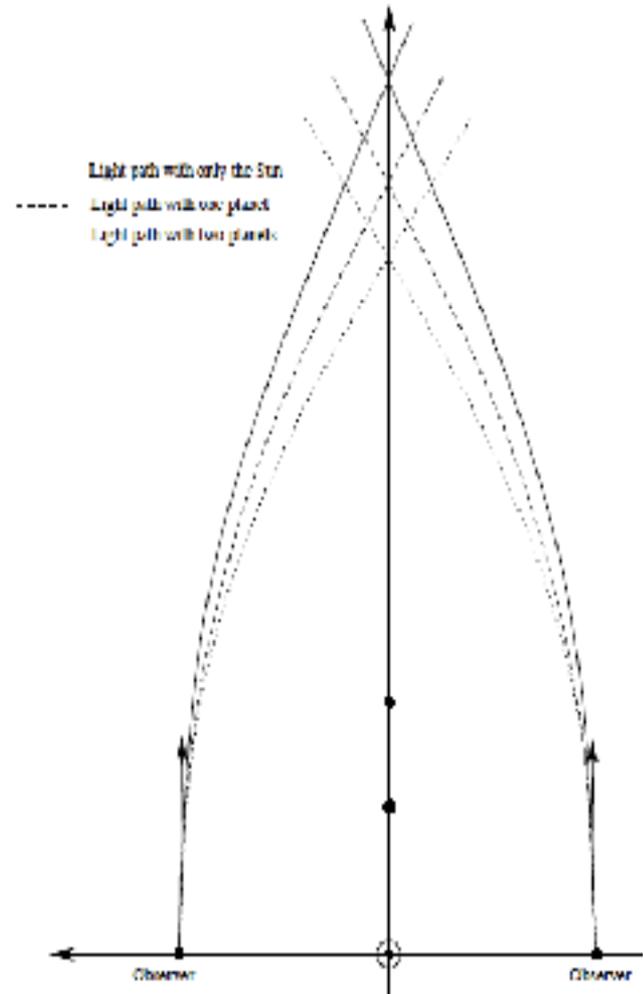
100 μas!



PM model

from the local line-of-sight to the star “position”

	☉	☉+♃	☉+♃+♅	☉+♃+♅+♁	☉+♃+♅+♁+♄
distance ~ 1 pc					
d (AU)	206261.338	206259.698	206259.216	206259.142	206259.054
p_i (")	1.00001775	1.00002571	1.00002804	1.00002840	1.00002883
$p_{☉} - p_i$ (μarcsec)		-7.95	-10.29	-10.65	-11.07
$\Delta\psi_i$ (μarcsec)		-8.00	-10.30	-10.60	-11.10
distance ~ 10 pc					
d (AU)	2062283.55	2062120.14	2062072.27	2062064.94	2062056.3
p_i (")	0.10001777	0.10002569	0.10002802	0.10002837	0.10002879
$p_{☉} - p_i$ (μarcsec)		7.93	10.25	10.60	11.02
$\Delta\psi_i$ (μarcsec)		-8.00	-10.30	-10.60	-11.00
distance ~ 100 pc					
d (AU)	20589921.6	20573645.4	20568881.5	20568152.5	20567292.3
p_i (")	0.01001777	0.01002569	0.01002801	0.01002837	0.01002879
$p_{☉} - p_i$ (μarcsec)		-7.93	-10.25	-10.60	-11.02
$\Delta\psi_i$ (μarcsec)		-7.99	-10.30	-10.60	-11.00
distance ~ 1000 pc					
d (AU)	202664764	201098829	200644596	200575248	200493473
p_i (")	0.00101776	0.00102569	0.00102801	0.00102837	0.00102879
$p_{☉} - p_i$ (μarcsec)		-7.93	-10.25	-10.60	-11.02
$\Delta\psi_i$ (μarcsec)		-7.99	-10.30	-10.60	-11.00
distance ~ 10000 pc					
d (AU)	1751489760	1641052370	1611285280	1609051510	1603803810
p_i (")	0.00011777	0.00012569	0.00012801	0.00012819	0.00012861
$p_{☉} - p_i$ (μarcsec)		-7.93	-10.25	-10.42	-10.84
$\Delta\psi_i$ (μarcsec)		-7.99	-10.30	-10.60	-11.00

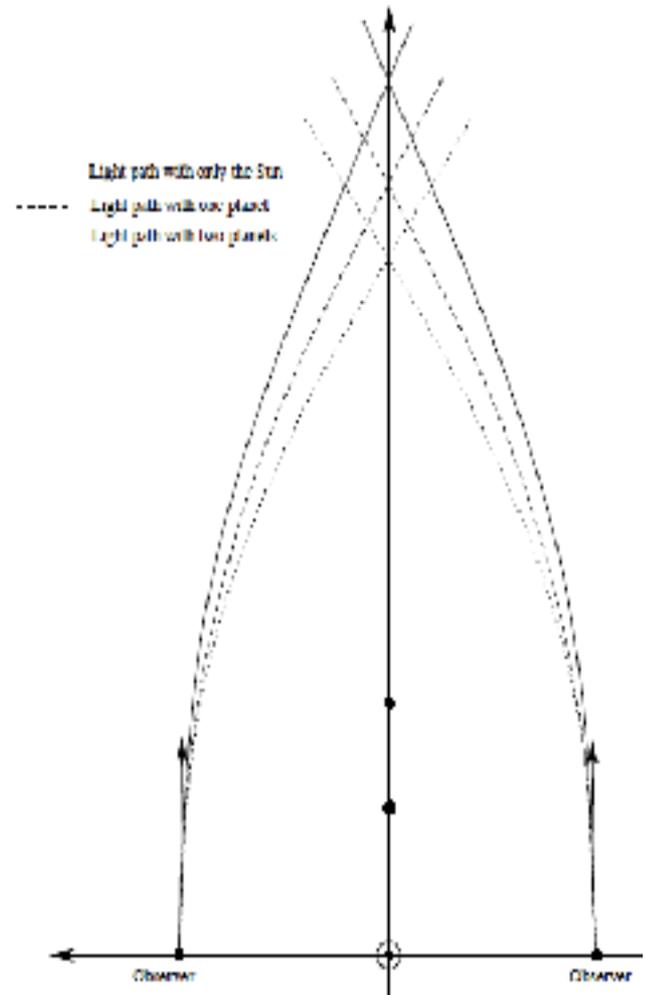


relative error in mag with no planets
(only the Sun) for $d=10\text{kpc}$

$$\sigma_{m-M} \approx 2 \sigma_d / d \approx 0.2 \text{ mag!}$$

from the local line-of-sight to the star “position”

	☉	☉+♃	☉+♃+♅	☉+♃+♅+♁	☉+♃+♅+♁+♄
distance ~ 1 pc					
d (AU)	206261.338	206259.698	206259.216	206259.142	206259.054
p_i (")	1.00001775	1.00002571	1.00002804	1.00002840	1.00002883
$p_{☉} - p_i$ (μarcsec)		-7.95	-10.29	-10.65	-11.07
$\Delta\psi_i$ (μarcsec)		-8.00	-10.30	-10.60	-11.10
distance ~ 10 pc					
d (AU)	2062283.55	2062120.14	2062072.27	2062064.94	2062056.3
p_i (")	0.10001777	0.10002569	0.10002802	0.10002837	0.10002879
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distance ~ 1000 pc					
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distance ~ 10000 pc					
d (AU)	1751489760	1641052370	1611285280	1609051510	1603803810
p_i (")	0.00011777	0.00012569	0.00012801	0.00012819	0.00012861
$p_{☉} - p_i$ (μarcsec)		-7.93	-10.25	-10.42	-10.84
$\Delta\psi_i$ (μarcsec)		-7.99	-10.30	-10.60	-11.00



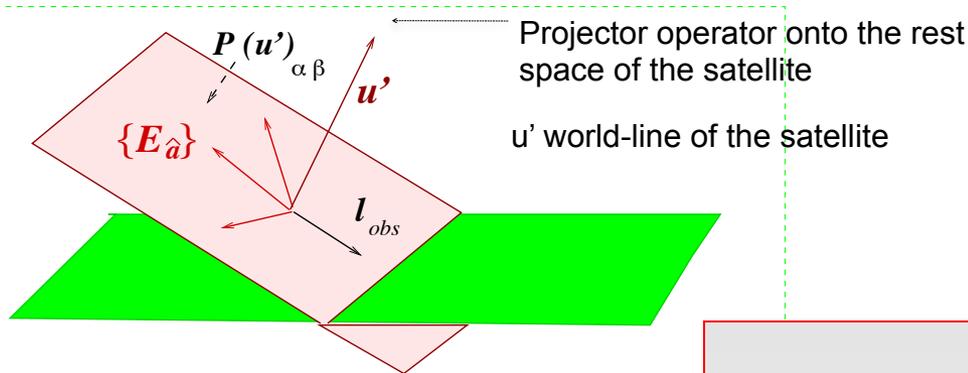
relative error in mag with no planets
(only the Sun) for $d=10\text{kpc}$



$$\sigma_{m-M} \approx 2 \sigma_d / d \approx 0.2 \text{ mag!}$$

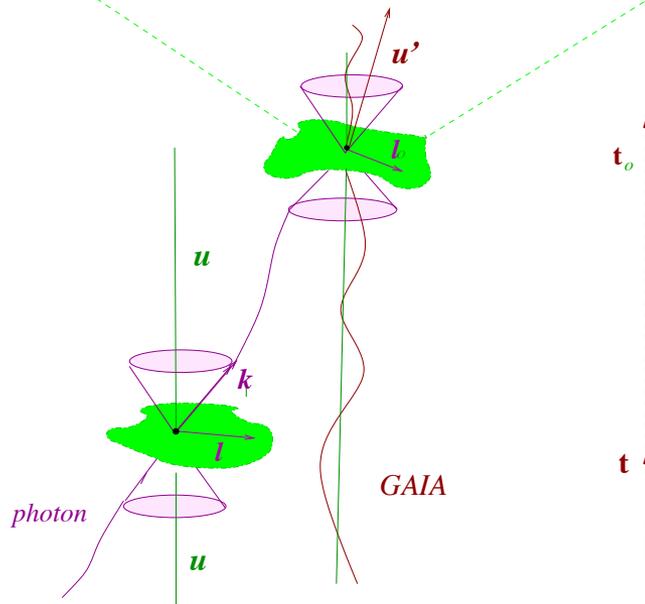
The astrometric observable in RAMOD/AVU

$E_{\alpha\beta}$ "attitude tetrad" -> ESSENTIAL to define the boundary condition

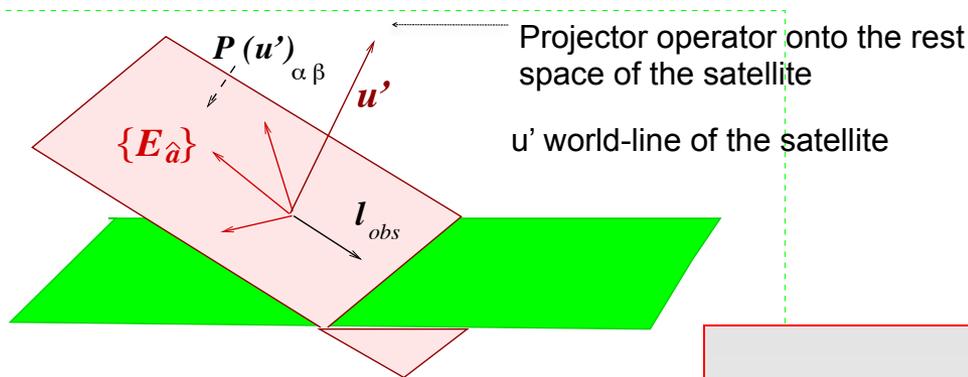


$$\cos \psi_{(E_{\hat{a}}, l_{obs})} \equiv e_{\hat{a}} = \frac{P(u')_{\alpha\beta} l_{obs}^{\alpha} E_{\hat{a}}^{\beta}}{(P(u')_{\alpha\beta} k^{\alpha} k^{\beta})^{1/2}}$$

Observation equation



The astrometric observable in RAMOD/AVU



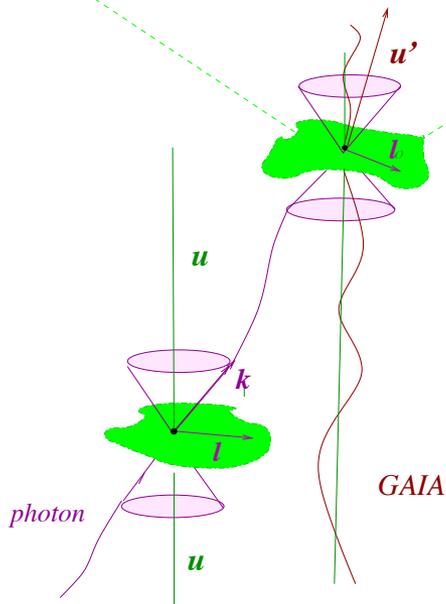
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Observation equation

$$-\sin \phi d\phi = \underbrace{\frac{\partial F}{\partial \alpha_s} \delta \alpha_s + \frac{\partial F}{\partial \delta_s} \delta \delta_s + \frac{\partial F}{\partial \varpi_s} \delta \varpi_s + \dots}_{\text{Astrometric parameters}}$$

$$\sum_{ij} \frac{\partial F}{\partial \sigma_i^{(j)}} \delta \sigma_i^{(j)} + \sum_i \frac{\partial F}{\partial c_i} \delta c_i + \frac{\partial F}{\partial \gamma} \delta \gamma + \dots$$



t_o

t

$$\phi_{obs} - \phi_{calc}$$

All derivatives are calculated at appropriate "catalog" values

The concept of the Global Sphere Reconstruction

$$\cos \phi = F \left(\underbrace{\alpha_s, \delta_s, \bar{\omega}_s, \mu_{\alpha_s}, \mu_{\delta_s}}_{\text{Astrometric parameters}}, \underbrace{\sigma_1^{(1)}, \sigma_2^{(1)}, \sigma_3^{(1)}, \sigma_1^{(3)}, \sigma_2^{(3)}, \sigma_3^{(3)}}_{\text{Attitude parameters}}, \underbrace{c_1, c_2, \dots}_{\text{Instrument}}, \underbrace{\gamma, \dots}_{\text{Global}} \right)$$

Solving the linearized GSR sphere in the Least-Squares sense

Known

Unknown

Unknown

$$\sin \psi_i^{(1)} \Delta \psi_i^{(1)} = \frac{\partial f}{\partial \alpha_i} \Delta \alpha_i + \frac{\partial f}{\partial \delta_i} \Delta \delta_i + \frac{\partial f}{\partial \pi_i} \Delta \pi_i + \dots + \frac{\partial f}{\partial \gamma} \Delta \gamma$$

$$\sin \psi_i^{(2)} \Delta \psi_i^{(2)} = \frac{\partial f}{\partial \alpha_i} \Delta \alpha_i + \frac{\partial f}{\partial \delta_i} \Delta \delta_i + \frac{\partial f}{\partial \pi_i} \Delta \pi_i + \dots + \frac{\partial f}{\partial \gamma} \Delta \gamma$$

• • • • •

$$\sin \psi_i^{(n)} \Delta \psi_i^{(n)} = \frac{\partial f}{\partial \alpha_i} \Delta \alpha_i + \frac{\partial f}{\partial \delta_i} \Delta \delta_i + \frac{\partial f}{\partial \pi_i} \Delta \pi_i + \dots + \frac{\partial f}{\partial \gamma} \Delta \gamma$$

1 obs. \Rightarrow 1 condition eq.



(linearized) system of solution with dimensions $\sim 10^{10} \times 10^8$

parallelized implementation of the LSQR iterative algorithm (Paige & Saunders, 1982) tailored for the sphere solution problem

The concept of the Global Sphere Reconstruction

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Crosta et al. Phys. Rev. D 96,104030, 2017 "General relativistic observable for gravitational astrometry in the context of the Gaia mission and beyond"

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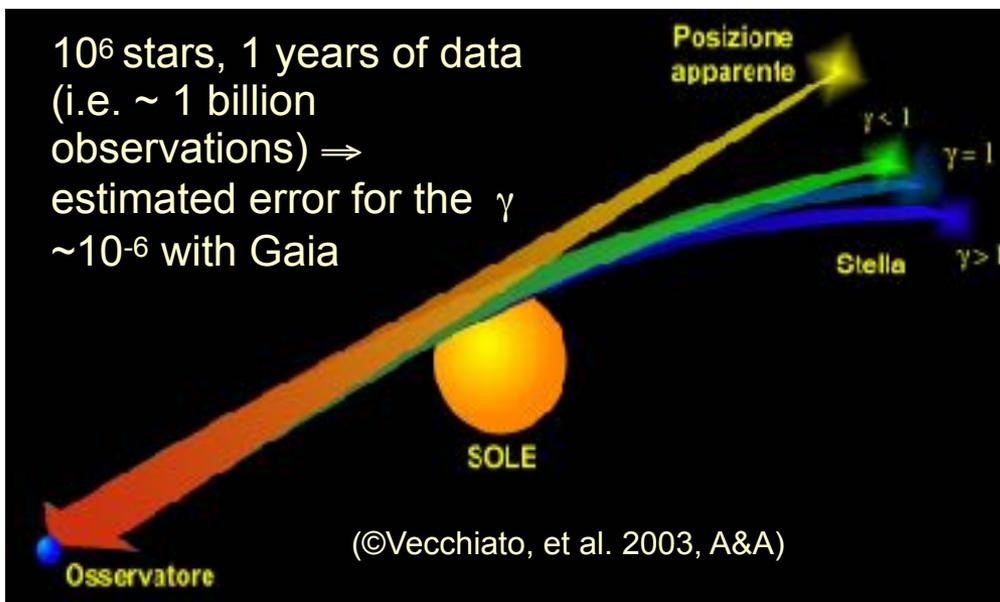


(linearized) system of solution with dimensions $\sim 10^{10} \times 10^8$

parallelized implementation of the LSQR iterative algorithm (Paige & Saunders, 1982) tailored for the sphere solution problem

Fundamental Physics tests via global astrometry

10^6 stars, 1 years of data
(i.e. ~ 1 billion observations) \Rightarrow
estimated error for the γ
 $\sim 10^{-6}$ with Gaia



deviations from GR depends on the particular scalar-tensor theory adopted (quantum theory of gravity, verification of inflationary models, violation of the principle of equivalence, constancy of the physical constants, low-energy limits of string theories, accelerated cosmological expansion, Galaxy cluster dynamics, Galaxy rotation curves and DM halos, etc.)

\rightarrow *given the number of celestial objects (a real Galilean method applied on the sky!) and directions involved (the whole celestial sphere!), the largest experiment in General Relativity ever made with astrometric methods (since 1919) from space*

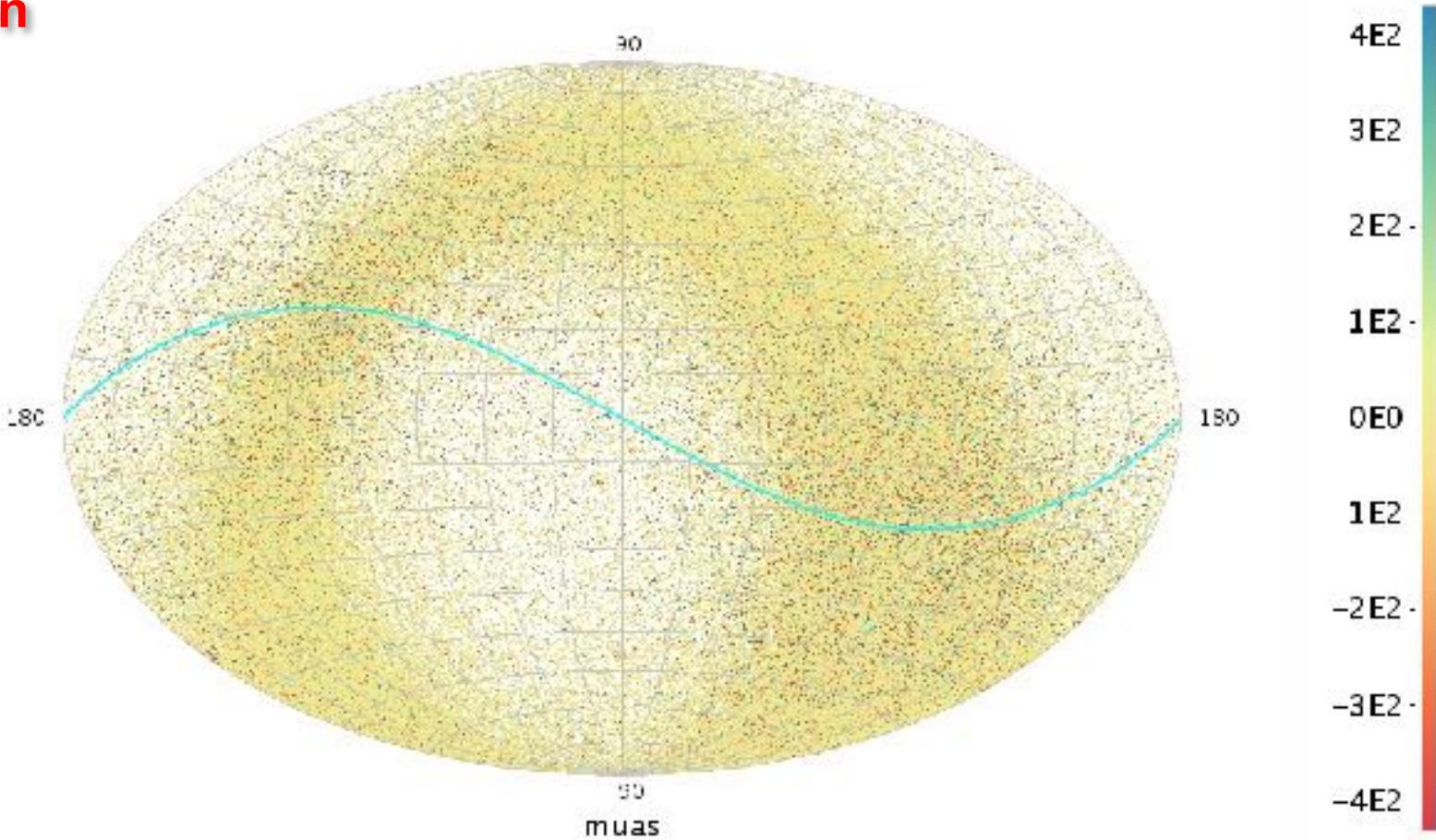
A massive repetition of the Eddington et al. astrometric test of GR with 21st century technology, thank to the interfacing of analytical&numerical relativity methods!

with **DR2** too many systematic errors, final calibrations including bright stars will improve the measurements of deviation from one

Demonstration Run: 1 million primary sources, whole mag range, 5 years, blind simulation

The AVU-GSR sphere reconstruction
(the 3rd fundamental component of the astrometric error budget)

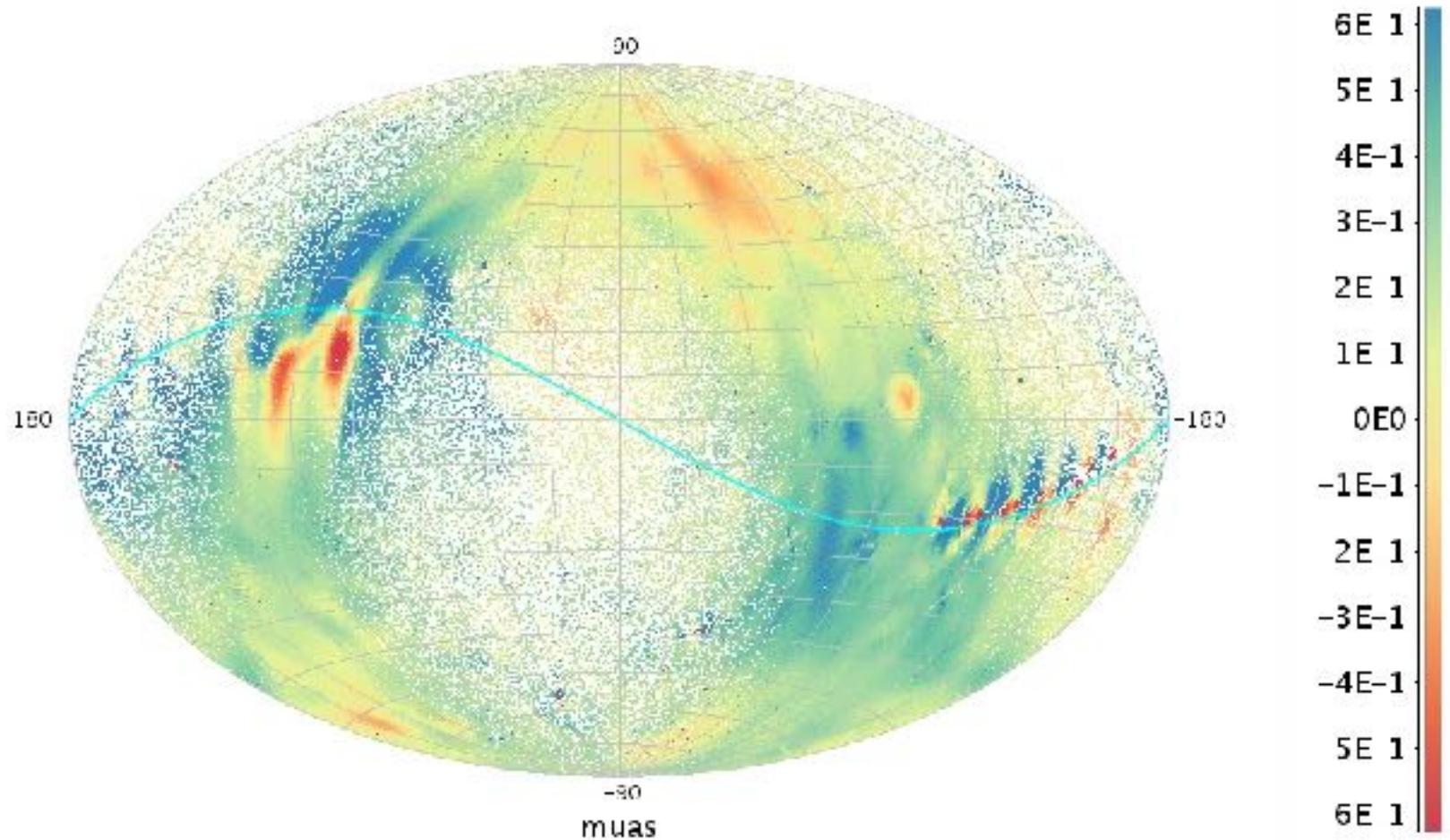
Parallax residual:



Courtesy of Bucciarelli, Lattanzi, Vecchiato

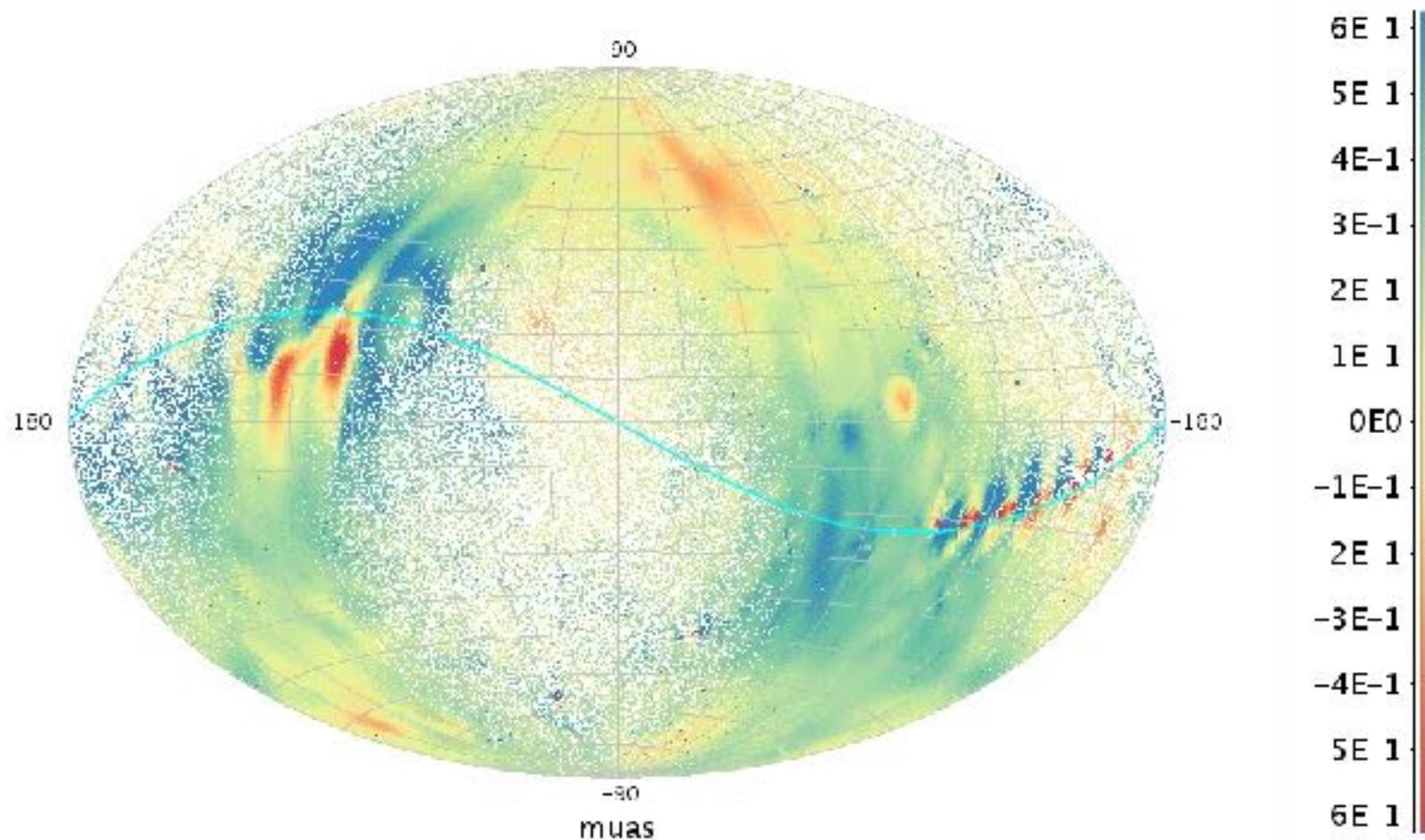
(From Vecchiato, MGL, Bucciarelli, ..., GAIA-C3-TN-INAF-AVE-027-01, 26 Oct 17; A&A, 2018, submitted)

Parallax residuals



Courtesy of Bucciarelli, Lattanzi, Vecchiato
(From Vecchiato, MGL, Bucciarelli, ..., GAIA-C3-TN-INAF-
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Parallax residuals



Bertone et al. A&A, v. 608, id.A83, 2017, Application of time transfer functions to *Gaia*'s global astrometry - Validation on DPAC simulated *Gaia*-like observations->TTF/GREM comparison

Courtesy of Bucciarelli, Lattanzi, Vecchiato
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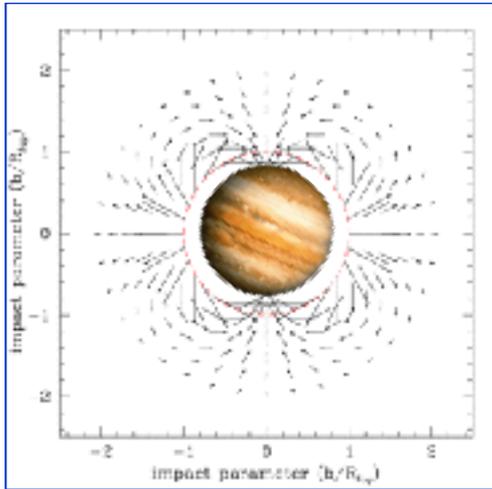
✓ Stressing the point

The Gaia-like observer is positioned inside the Solar System, a **weak gravitational regime which turns out to be "strong" when one has to perform high accurate measurements**

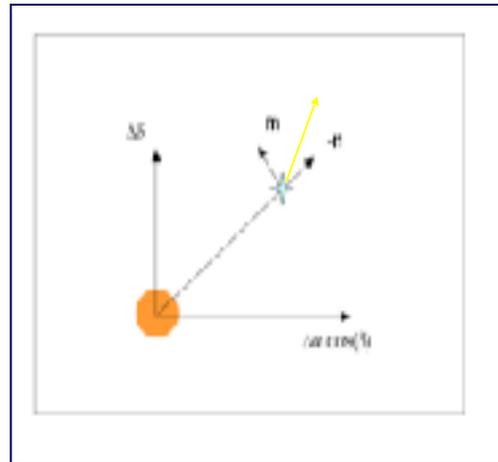
- Any discrepancy between the relativistic models, if it can not be attributed to errors of different nature, will mean either a limit in the modeling/interpretation - that a correct application of GR should fix - and therefore a validation of GR, or, maybe, a clue that we need to refine our approach to GR
 - Independent relativistic astrometric model;
 - Independent relativistic attitude model;
 - Independent (iterative) solution method (all-unknowns solved at once);
 - Direct calculation of variances of Primary solution (possibility of covariances!)
 - At first comparison, common set of initial primary stars and instrument model;
 - GSR compares to AGIS for verification at CU3 level (all-sky)

- all the goals of Gaia will not be achieved without the correct characterization and exploitation of the ``relativistic'' astrometric data.

GAREQ (GAia Relativistic Experiment on Quadrupole) (light deflection by Jupiter's quadrupole)



Crosta, M., Mignard, F. (2006, **CQGr**, 23, 4853)
Crosta, et al. (2008, **GAIA-C3-TN-INAf-MTC-003-1**)



aim: first quantitative measurement of the gravitational potential due to a non-spherical lens

$$\Delta\Phi_1 = \frac{2(1+\gamma)M}{b} \left[1 + J_2 \frac{R^2}{b^2} \left(1 - 2(\mathbf{n} \cdot \mathbf{z})^2 - (\mathbf{t} \cdot \mathbf{z})^2 \right) \right]$$

$$\Delta\Phi_2 = \frac{4(1+\gamma)M J_2 R^2}{l^3} (\mathbf{m} \cdot \mathbf{z})(\mathbf{n} \cdot \mathbf{z})$$

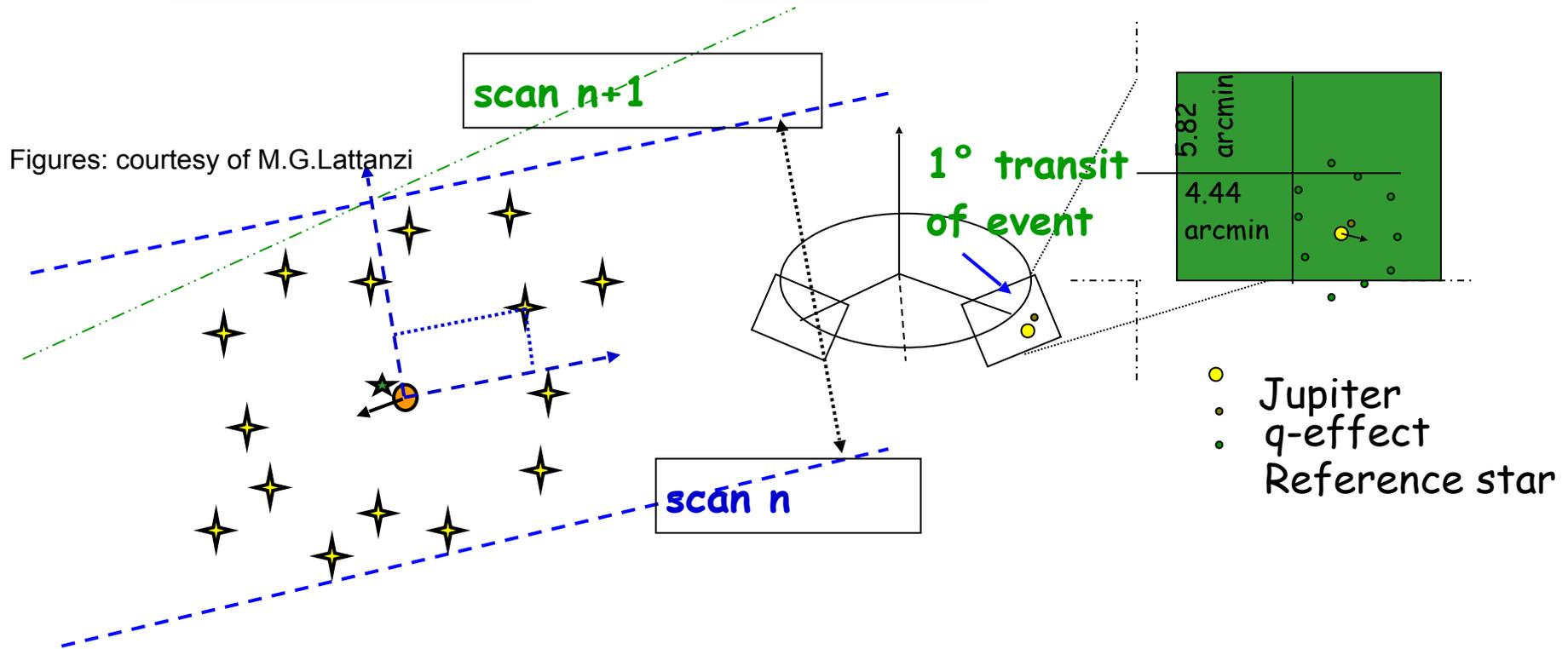
$$\Delta\Phi = \Delta\Phi_1 \mathbf{n} + \Delta\Phi_2 \mathbf{m},$$

“q-effect”

further validation of GR → screening of alternative theories, confirmation of multipolar patterns of the gravitational lens generated by galaxy clusters provided that GR works as expected

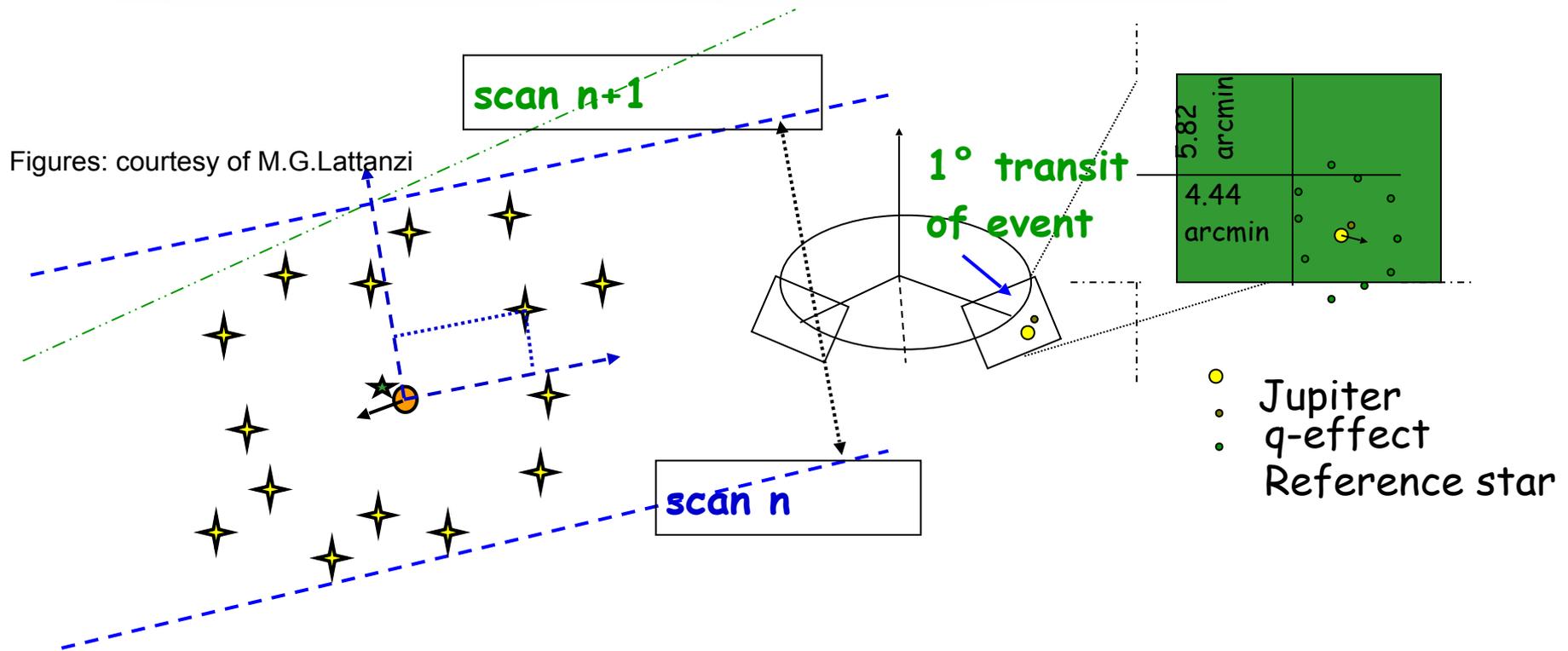
Differential Astrometry in the GAREQ scenario: Q-DIFF

collaborators: U, Abbas B. Bucciarelli, M. G. Lattanzi, R. Morbidelli,
D. Busonero, A. Vecchiato & R. Messineo



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(On the same subject we have a multi-epoch, multi-orbit HST proposal – PI S. Casertano (STScI). Executed successfully, under reduction)

->#Gaia spin axis orientation optimised to catch a star close to the limb of Jupiter in 2017 for a precise light deflection measurement.

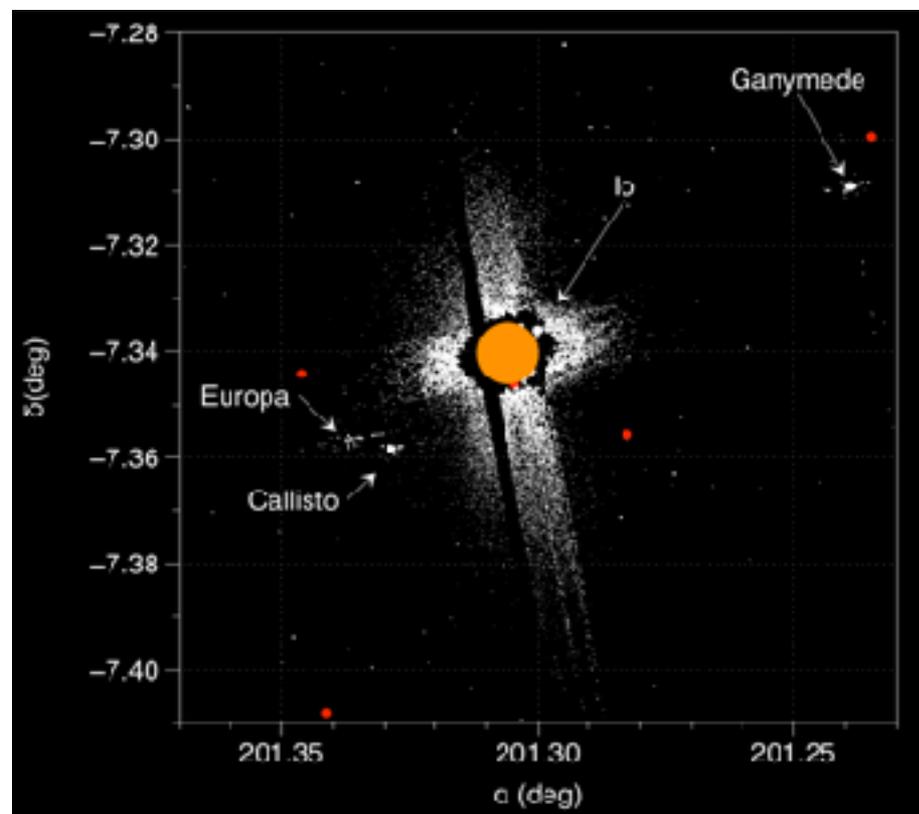
- Initial spin axis orientation decided 2014 to maximise measurement success
- Spin phase adjustment 8 Feb 2017
- Scan-law change for GAREQ event (spin phase change is 82.5°)

Observation of the first GAREQ event

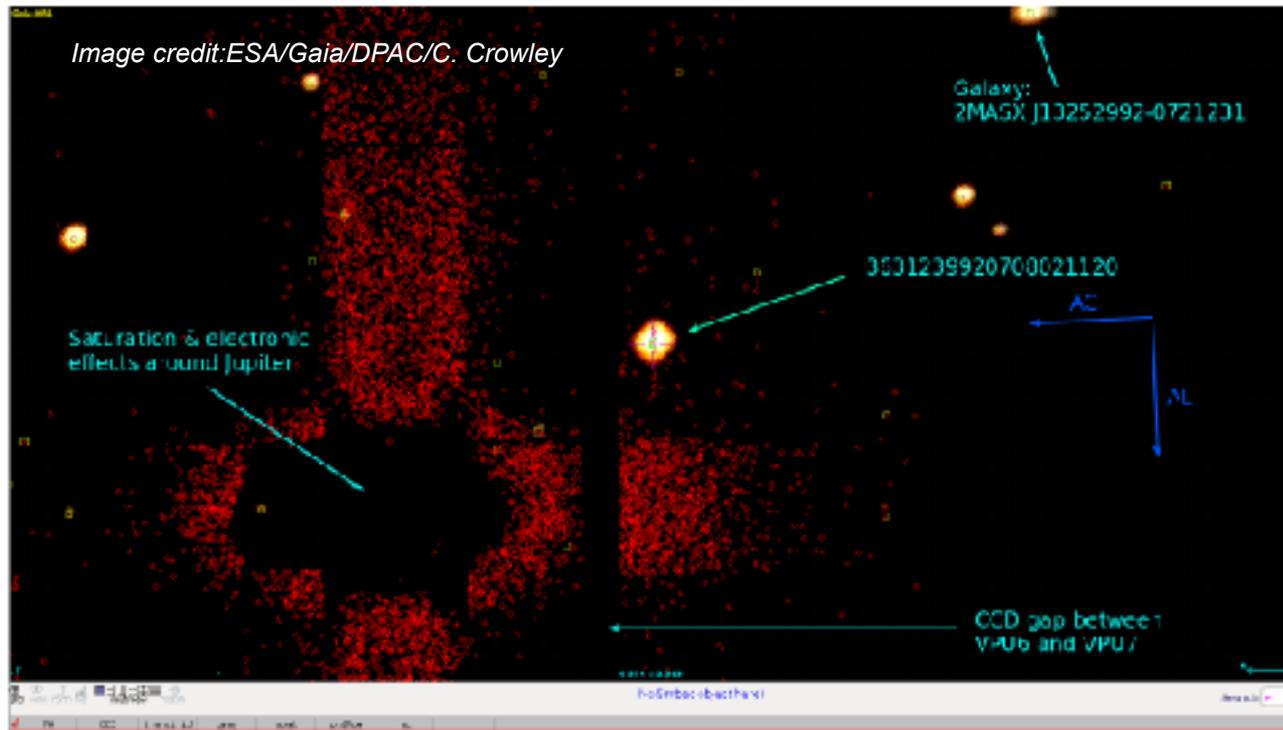
At the beginning of 2017, towards the end of February 2017, Gaia provided measurements for 31 bright reference stars ($G < 13$ mag) all lying within a field of 0.8×1.3 degs surrounding a target star ($G = 12.68$ mag) of particular interest.

The target star was seen a total of 26 times over a 2 month period out of which we use 15 transits over a short time interval of a couple of days surrounding the observation at closest approach

Credit: Mignard



Observation of GAREQ event

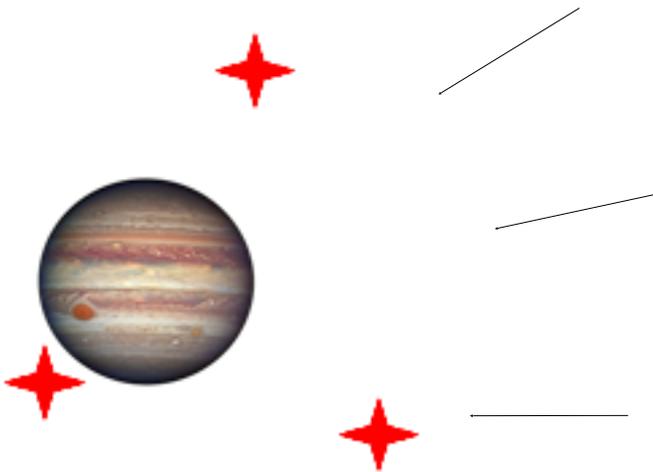


Scene around the target star successfully detected onboard during a transit on 2017-02-22T19:08:12.954 (UTC) at a predicted angular distance of 67.65" from Jupiter's limb. Note the gap between the detectors in CCD rows 6 and 7. Whilst Jupiter was observed in row 6, one of the measured bright star happened to be scanned in row 7.

Star field on different transits

diifferential astrometry to adjust all the frames to a common frame by means of translations, rotations and possible distortion terms if necessary

Image credit:ESA/Gaia/DPAC



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diifferential astrometry to adjust all the frames to a common frame by means of translations, rotations and possible distortion terms if necessary

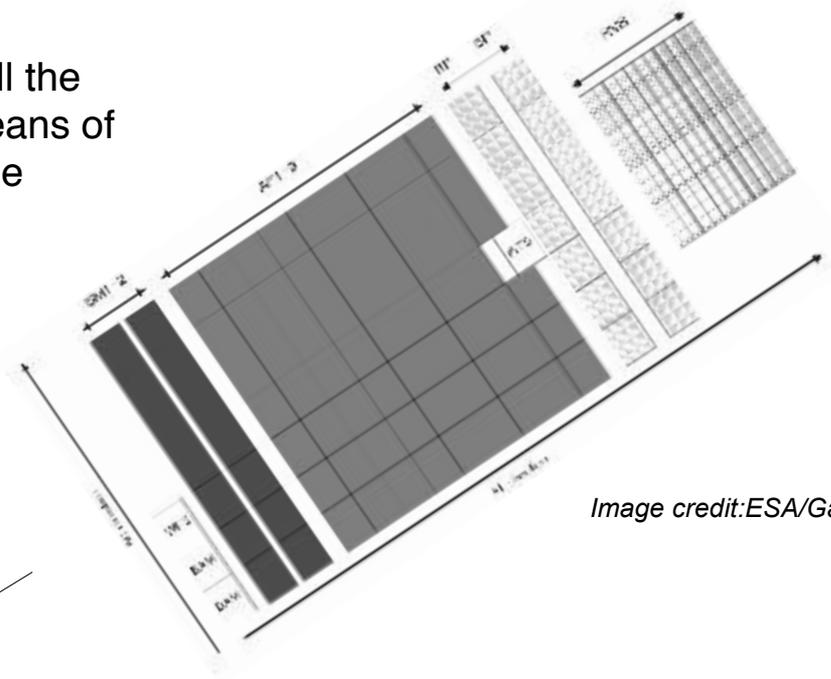
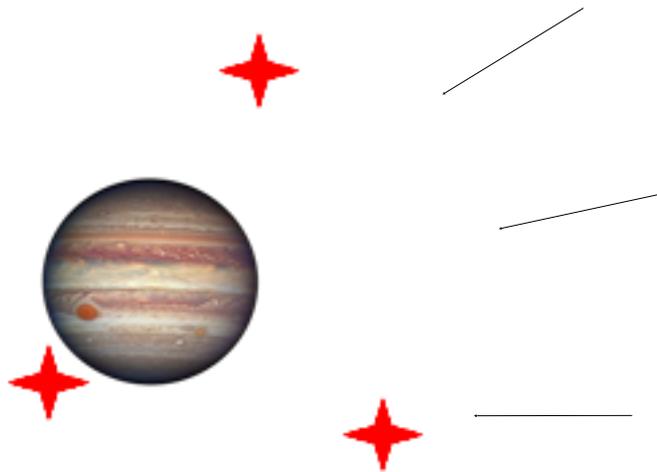
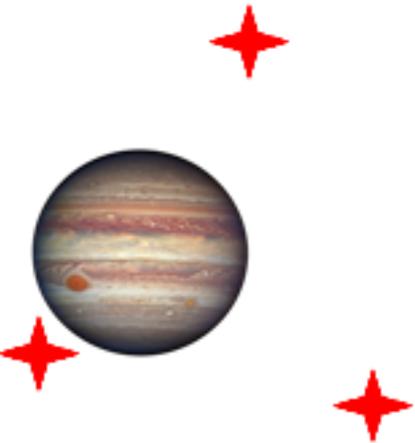
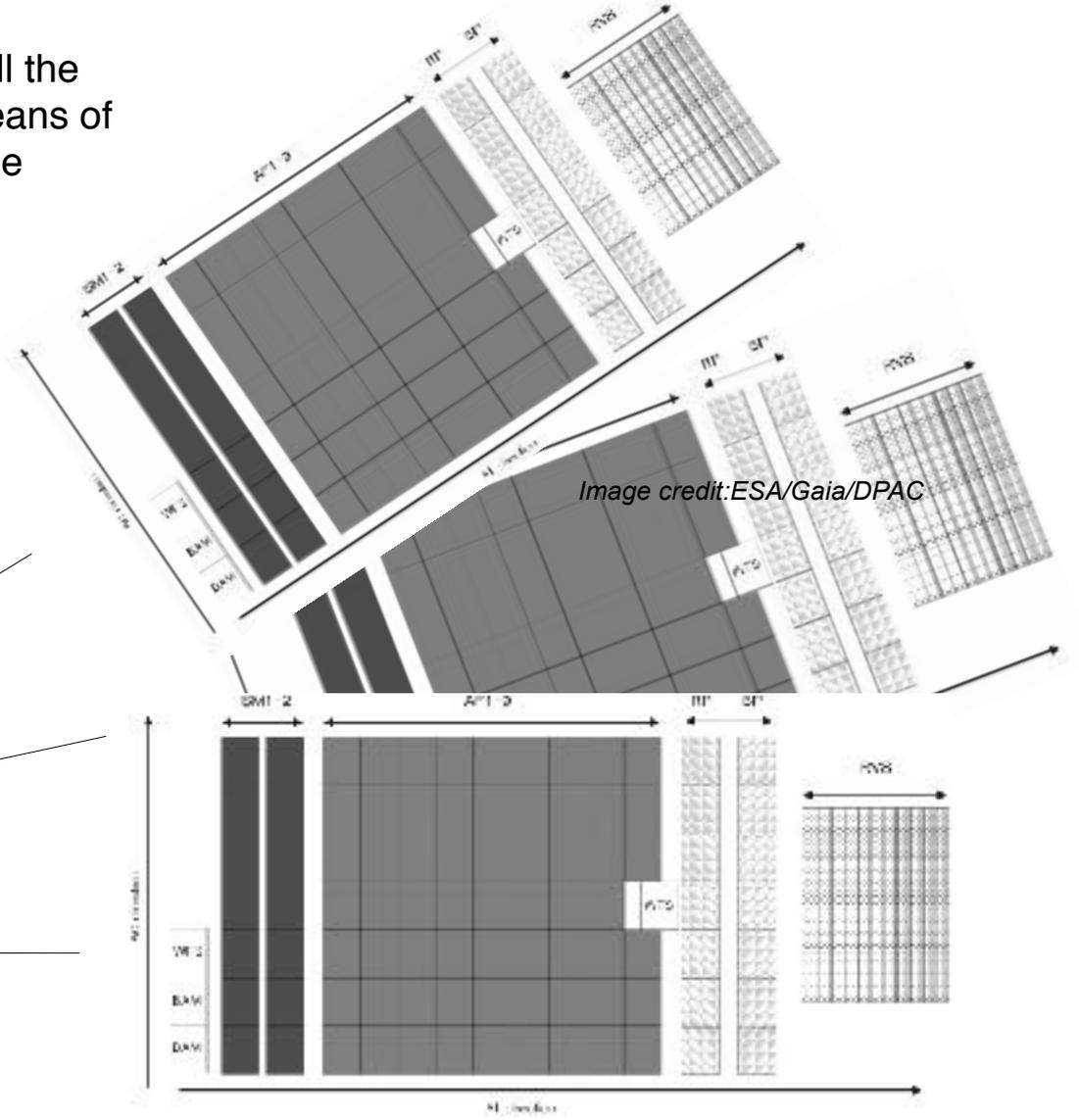


Image credit:ESA/Gaia/DPAC



Star field on different transits

diifferential astrometry to adjust all the frames to a common frame by means of translations, rotations and possible distortion terms if necessary



Differential astrometric analysis of the star observations developed at INAF-OATo via the DPCT

Different scenes of stars (red points) around the Target star (blue point) as seen by Gaia on different transits. The top left panel also shows the positions of Jupiter during the Feb transits as large red points.

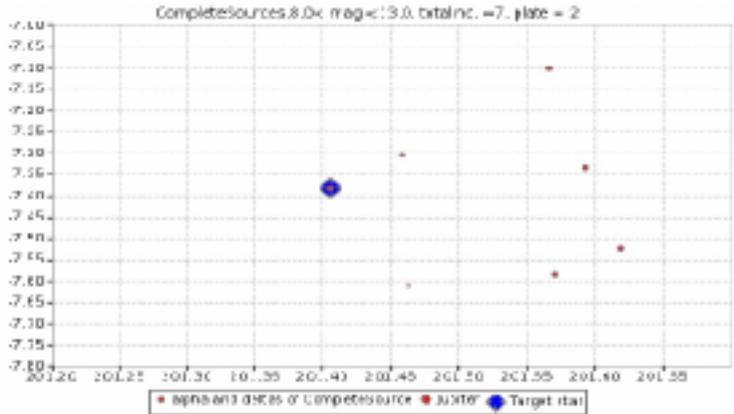
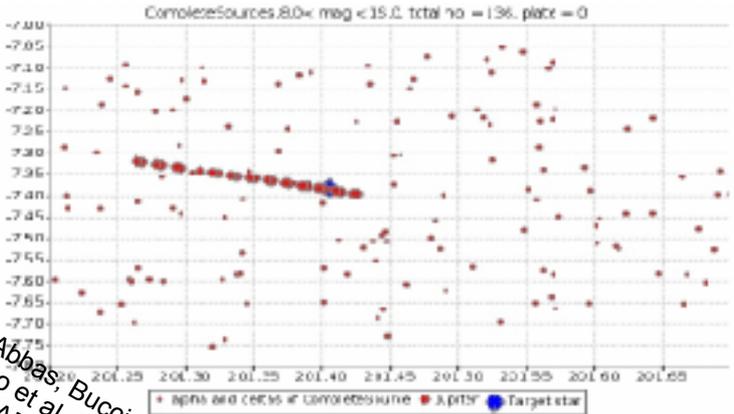


Figure: Stars seen on 2nd transit

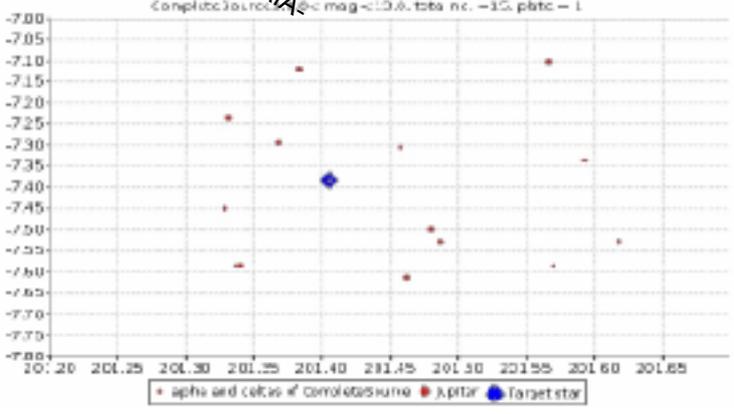


Figure: Stars seen on 1st transit

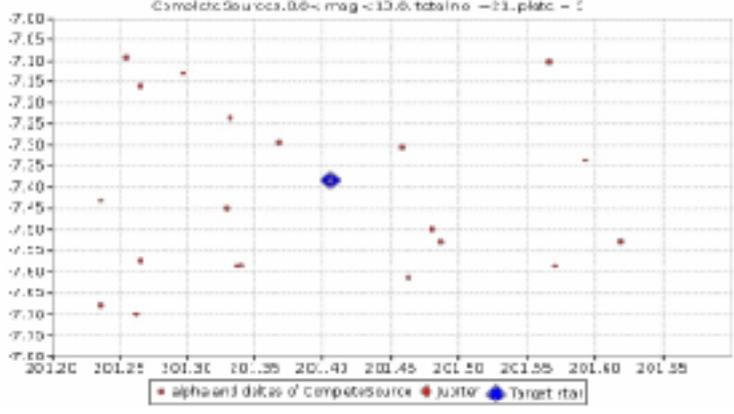
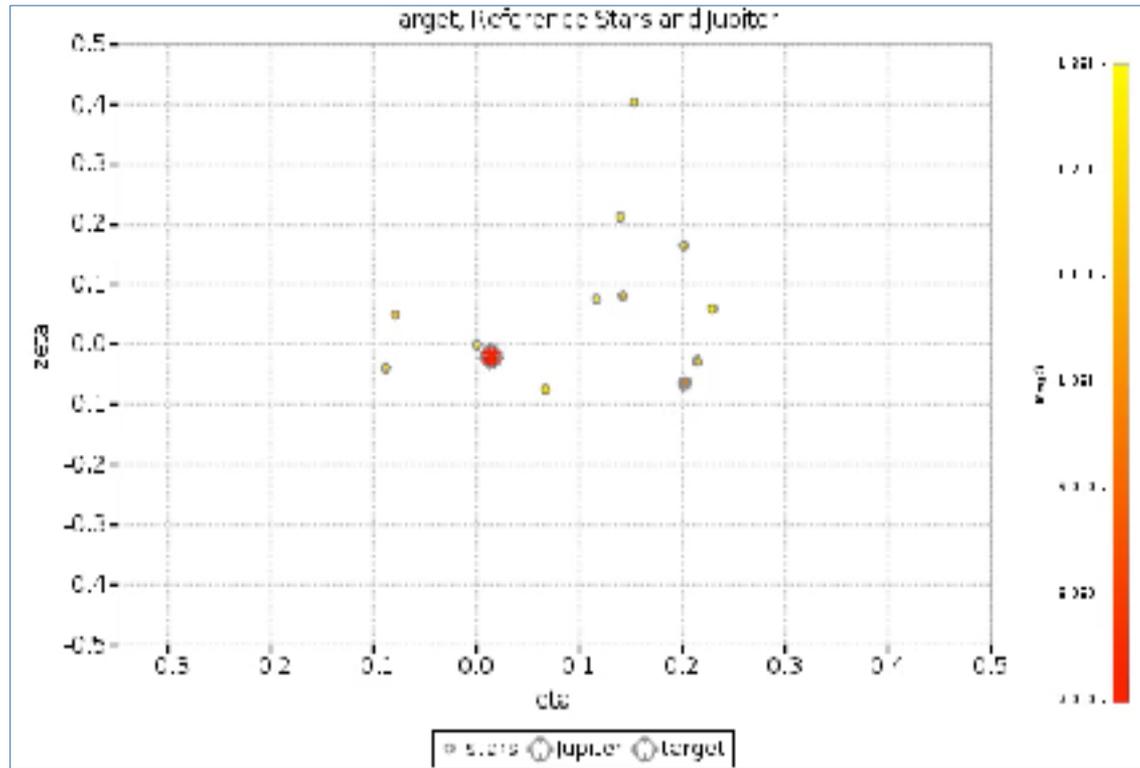


Figure: Stars seen on 3rd transit

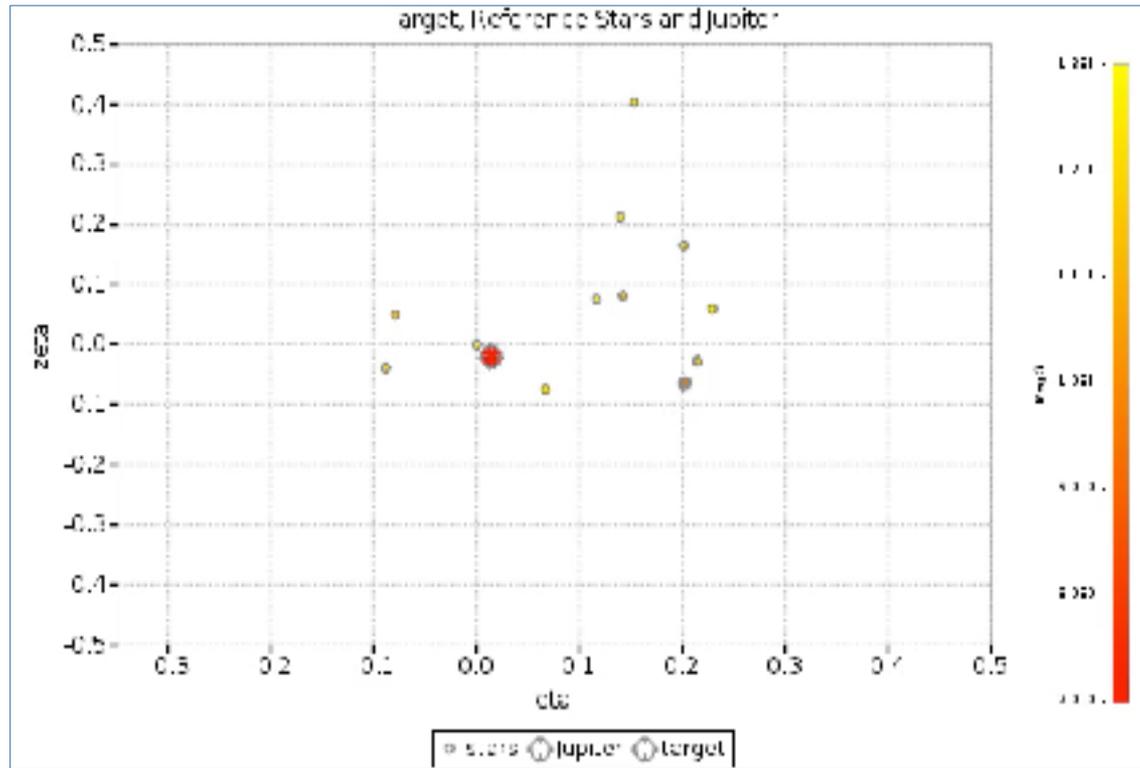
(From Abbas, Bucciarelli, Crosta, MGL, Busonero et al. 2017, Gaia TN, GAIA-C3-TN-INAF-UA-005-01)

Challenges of the scenario

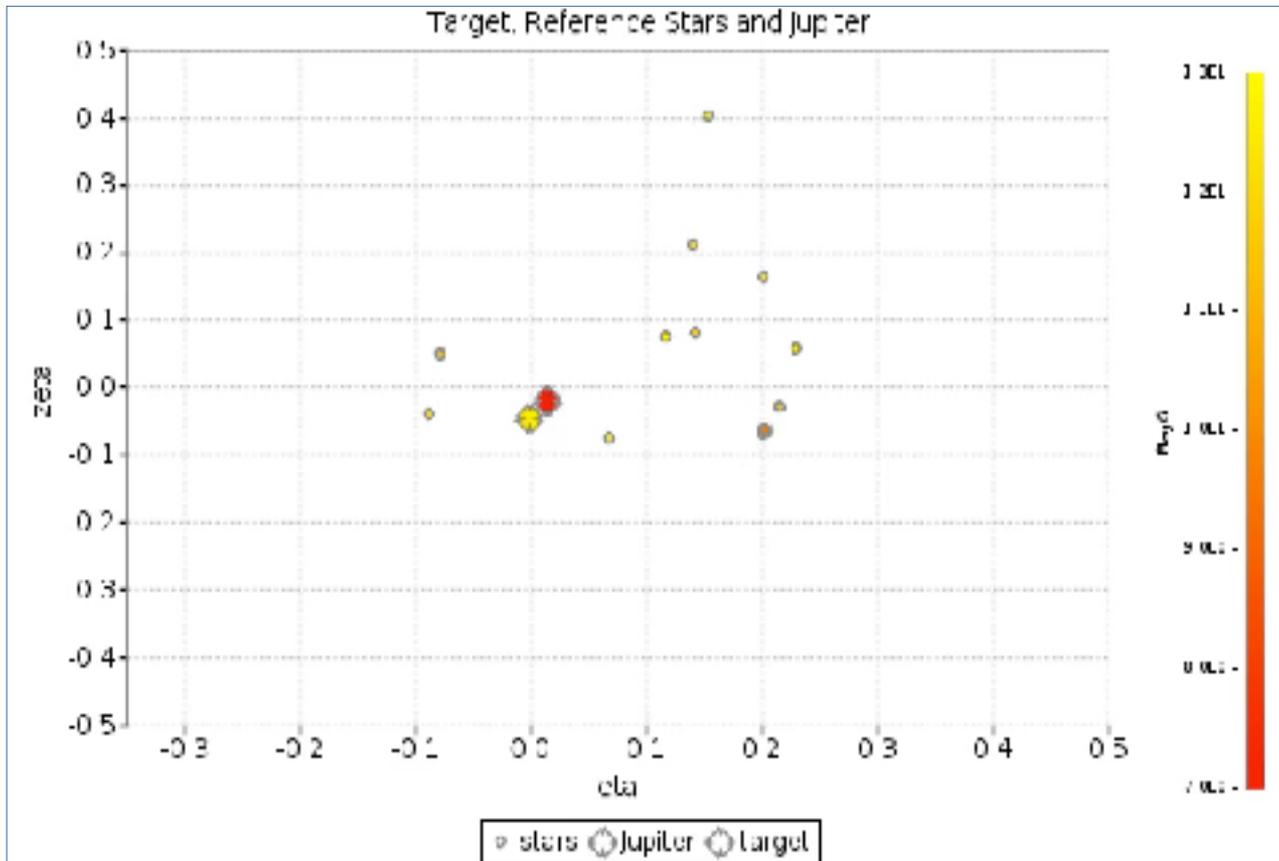


The star field ($G < 13$ mag) as seen by Gaia (simulation) on a succession of transits (15 transits chosen around the time of closest approach by the target) along with the motion of Jupiter.

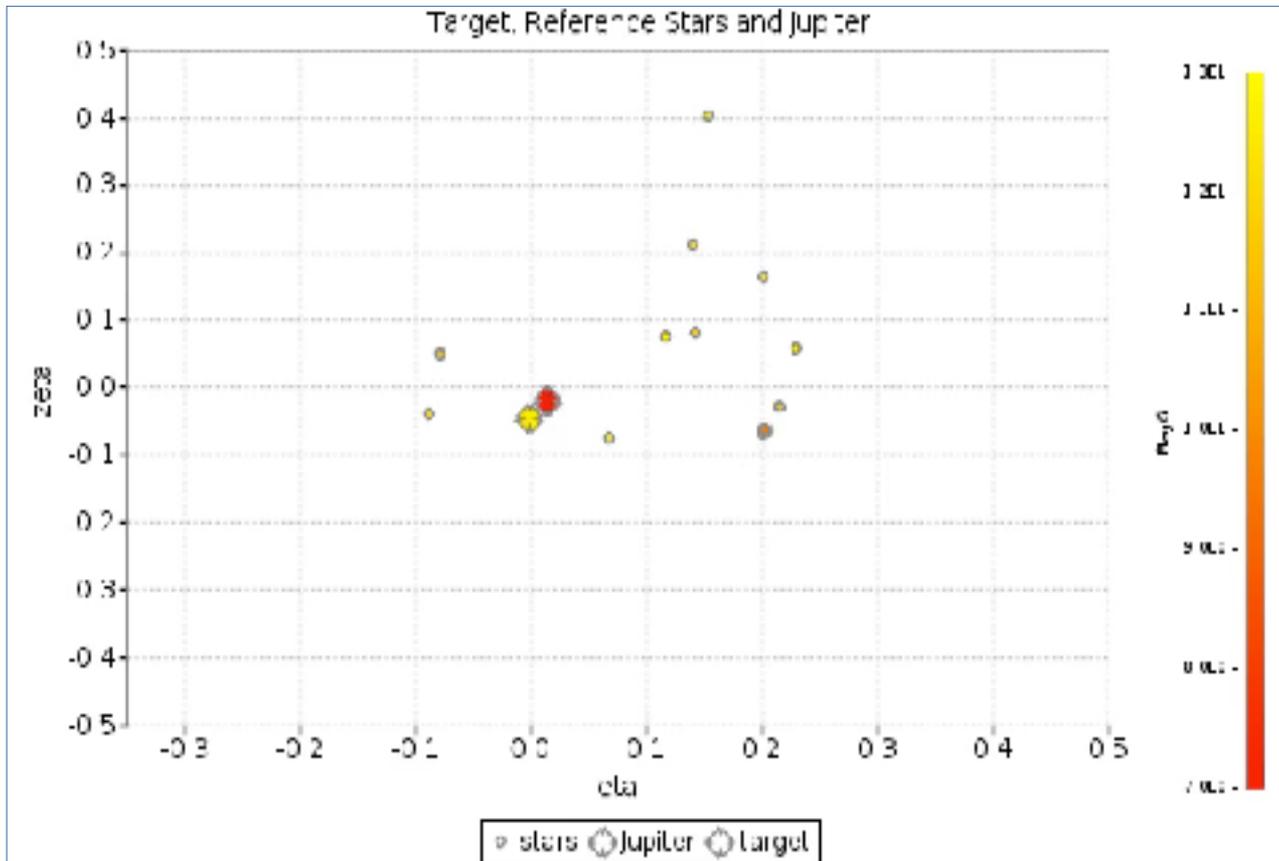
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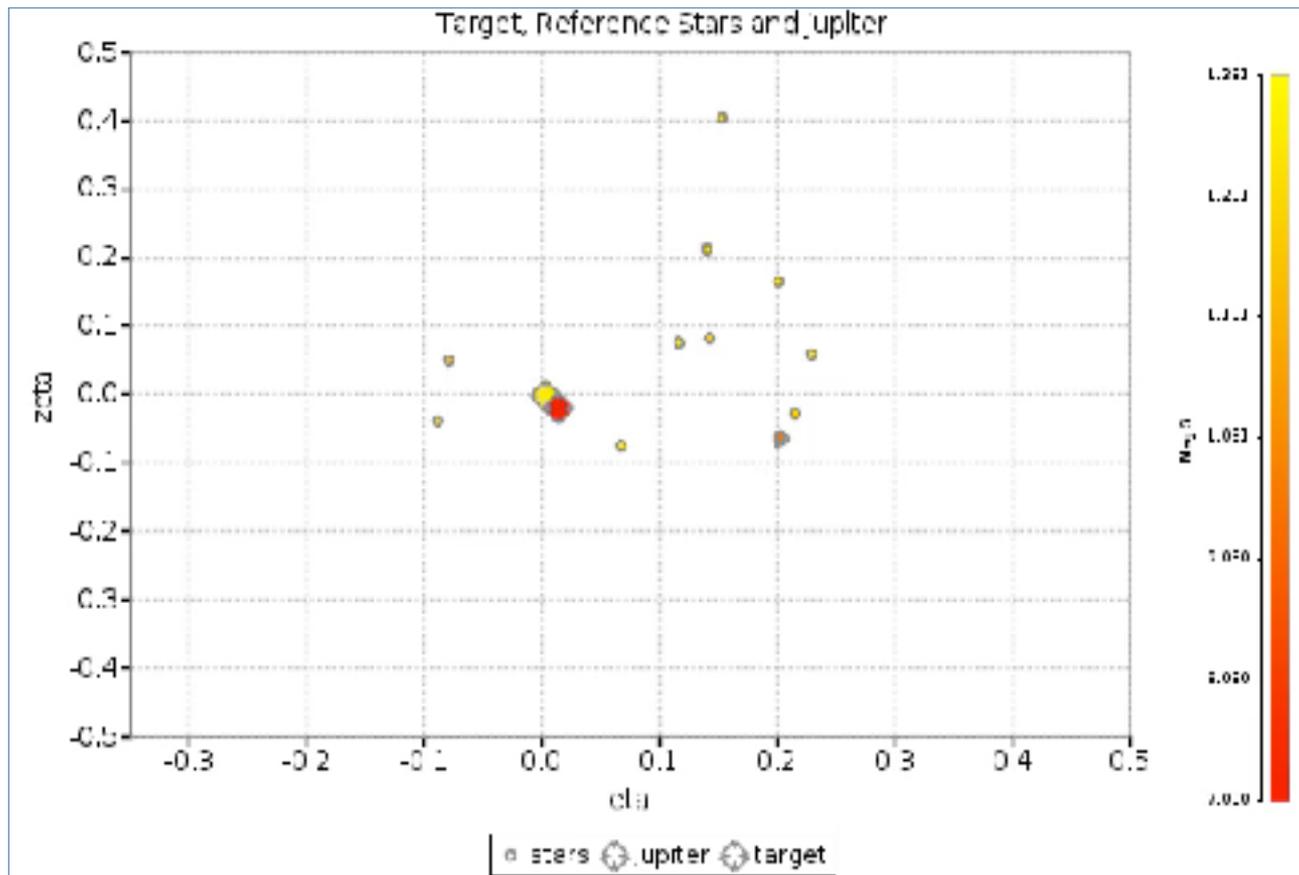
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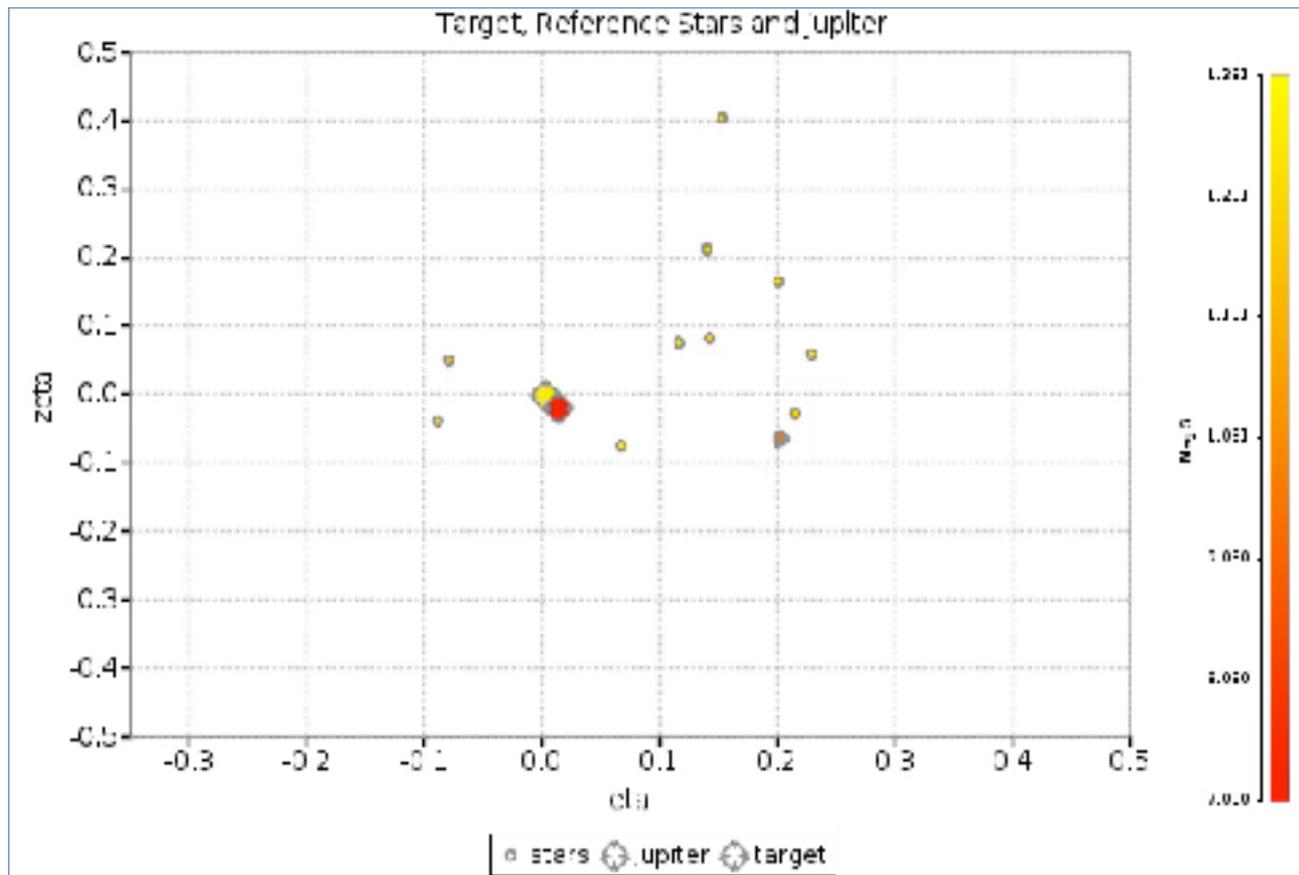
Simulation of the monopole deflection effect shown here enlarged by a factor of 50,000.



Simulation of the monopole deflection effect shown here enlarged by a factor of 50,000.

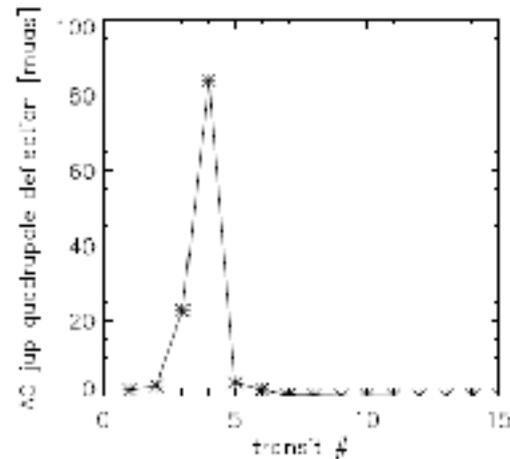
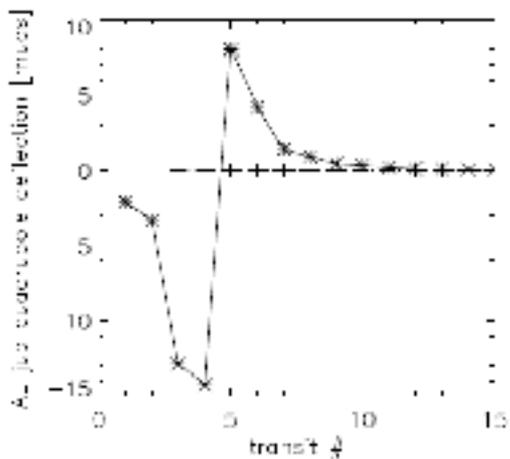
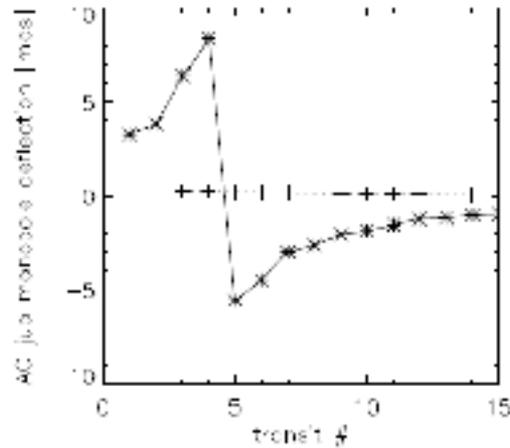
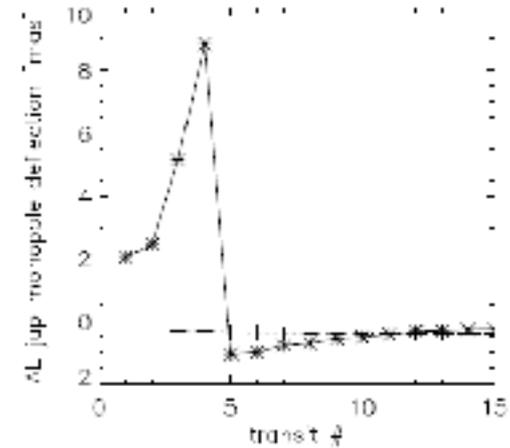


*Simulation of the quadrupole deflection effect shown here enlarged by a factor of 70*50,000.*



*Simulation of the quadrupole deflection effect shown here enlarged by a factor of 70*50,000.*

Deflection signal



Upper panels show the simulated AL/AC monopole deflection signal and lower panels the quadrupole deflection signal.

Asterisks denote the target star and plus signs a randomly chosen reference star.

QDIFF: Systematic Effects

Physical Effects

- *Gravitational deflection of light due to Solar System Objects*
- *Aberration due to motion of Observer wrt barycenter of the Solar System*
- *Effect due to the AL-AC motion of a star*
- *Star's Proper Motion leads to differential effects of several tens of micro-arcsec*

Instrumental Effects

- *Time-dependent instrument model describing the layout of the CCDs*
- *physical geometry of each individual CCD and its configuration in the FP assembly*
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- *nominal values of the focal length and basic angle*

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$$\delta\theta_{ab} = \frac{v}{c} \sin\theta \left[1 + \frac{1}{c^2}(1+\gamma)w(x_0) + \frac{1}{4} \frac{v^2}{c^2} \right] - \frac{1}{4} \frac{v^2}{c^2} \sin 2\theta + \frac{1}{12} \frac{v^3}{c^3} \sin 3\theta + O(c^{-4})$$

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- **Star's Proper Motion** leads to differential effects of several $\zeta(t_i) = \zeta(t_s) + \frac{d\zeta}{dt} * (t_i - t_s) c$

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$$\frac{d\eta}{dt} = -\omega_z + [\omega_x \cos \varphi + \omega_y \sin \varphi] \tan \zeta$$
$$\frac{d\zeta}{dt} = -\omega_x \sin \varphi + \omega_y \cos \varphi$$

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$$\eta_{fn}(\mu, t) = \eta_n^0 + \sum_{r=0}^2 \Delta\eta_{r,fn} T_r^{\hat{}}\left(\frac{\mu}{1966}\right)$$

QDIFF: Systematic Effects

Physical Effects

- *Gravitational deflection of light due to Solar System Objects*
- *Aberration due to motion of Observer wrt barycenter of the Solar System*
- *Effect due to the AL-AC motion of a star*
- *Star's Proper Motion leads to differential effects of several tens of micro-arcsec*

Instrumental Effects

- *Time-dependent instrument model describing the layout of the CCDs*
- *physical geometry of each individual CCD and its configuration in the FP assembly*
- *the distortions and aberrations in the optical system*
- *nominal values of the focal length and basic angle*

QDIFF: modeling

linear 'plate model'

$$X'_{ij}(t_{it}) = X_{ij}(t_{ij}) + \sum_{r=0}^2 \Delta\eta_{rfn} L_r^* \left(\frac{\rho - 13.5}{1966} \right) \\ + (-\omega_{zv} + [\omega_{xv} \cos \varphi + \omega_{yv} \sin \varphi] \tan \zeta) * (t_{it} - t_{ij})$$

$$Y'_{ij}(t_{it}) = Y_{ij}(t_{ij}) + \sum_{r=0}^2 \Delta\xi_{rfn} L_r^* \left(\frac{\rho - 13.5}{1966} \right) \\ + (-\omega_{xv} \sin \varphi + \omega_{yv} \cos \varphi) * (t_{it} - t_{ij})$$

$$\eta'_{0j}(t_{0t}) = a_i X'_{ij}(t_{it}) + b_i Y'_{ij}(t_{it}) + c_i - \mu_{\eta j} \Delta t_{ij}$$

$$\xi'_{0j}(t_{0t}) = d_i X'_{ij}(t_{it}) + e_i Y'_{ij}(t_{it}) + g_i - \mu_{\xi j} \Delta t_{ij}$$

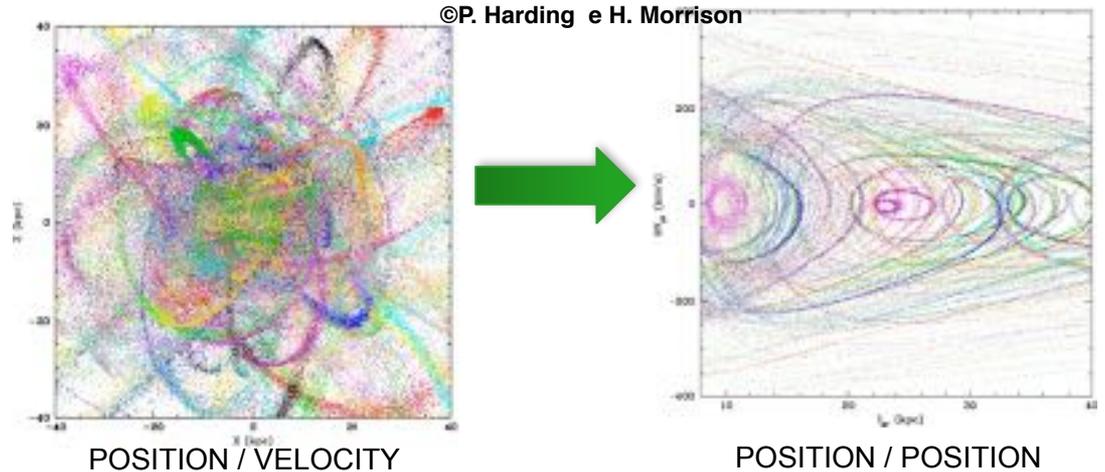
Abbas, Bucciarelli et al. 2017

*Parameters estimated using GaussFit (Jefferys et al. 1988):
robust least squares estimator*

Local cosmology with Gaia/galactic rotational curve

Milky Way (MW) as a product of a cosmological evolution at $z=0$

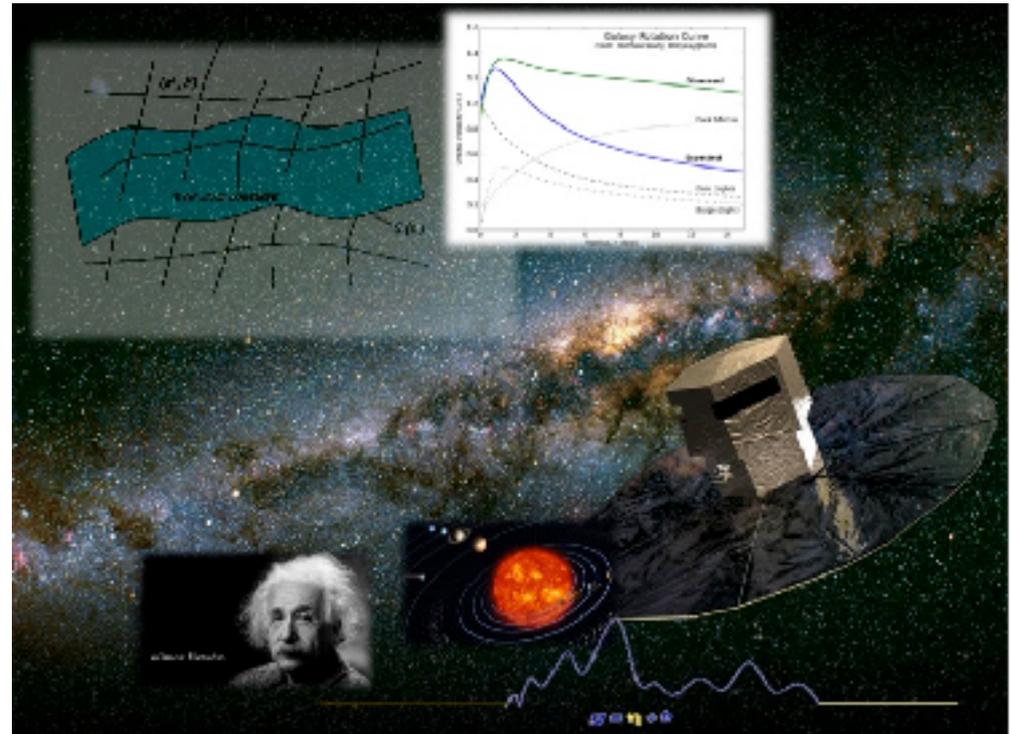
The thick disk and the local inner halo of Milky Way as chemo-dynamical lab for testing galactic models and compare (Λ) CDM predictions/GR



Gravitational Astrometry and relativistic Galactic models

PHD-INAf *M. Giammaria*

SV *M. Crosta*
co-SV *MGL Lattanzi*



✓ Stressing the point

- In the most advanced simulations nowadays, GR is only partially considered:

“ Friedeman tells space how to curve and Newton tells mass how to move”

[arXiv:1612.09309v2](https://arxiv.org/abs/1612.09309v2), [Alan A. Coley, David L. Wiltshire](#)

standards Lambda-CDM cosmology assumes an average FLRW evolution while growth in structure is treated by Newtonian N-body simulations

-The use of Gaia data must be parallel with the utilization of the most advanced cosmological simulations with baryonic matter (gas and stars) tracing its chemo-dynamics evolution at a high resolution level

- the position and velocity data comprising the output of the Gaia mission are fully GR compliant -> building **consistent observables**

➤ Once a relativistic model for the data reduction has been implemented, any subsequent scientific exploitation should be consistent with the precepts of the theory underlying such a model

-The GR picture of the MW is the only way to ensure a strong and coherent Local Cosmology laboratory against which the current formation and evolution model can be totally tested.

the failure of GR should be proved using the GR theory not the Newtonian one!

In general one assumes that:

velocity of stars in Galaxy is small: $v/c < 10^{-3}$

gravity is weak in Galaxy (besides the centre)

then locally Newton approximation valid at each point!

But Galaxy is not a point source but an extended source..

a “toy model” for Galaxy disk:

exact stationary axially symmetric solutions of the 4-dim. Ein.eq. with co-rotating pressureless perfect fluid source

$$ds^2 = -(dt - N d\phi)^2 + r^2 d\phi^2 + e^\nu (dr^2 + dz^2)$$

3-velocity distribution of the co-rotating dust as seen by an asymptotic observer at rest wrt to the center of the Galaxy (or the rotation axis)



$$V(r, z) = \frac{N(r, z)}{r}$$



$$N(r, z) = V_0(R - r_0) + \frac{V_0}{2} \sum_{\pm} \left(\sqrt{(z \pm r_0)^2 + r^2} - \sqrt{(z \pm R)^2 + r^2} \right)$$

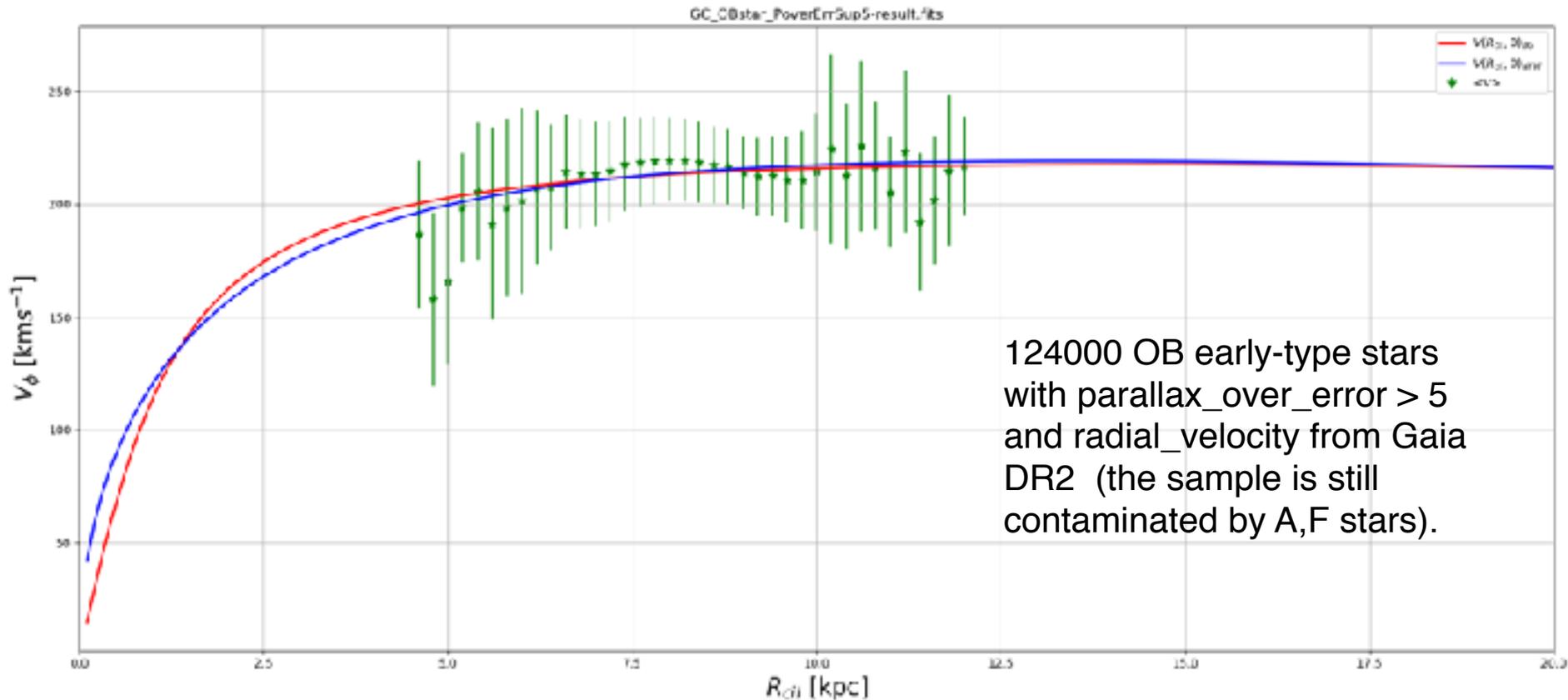
$$(V_0 \approx 200 \text{ km/s} \approx 7 * 10^{-4})$$

$$V(r, 0) = \frac{V_0}{r} \left(R - r_0 + \sqrt{r_0^2 + r^2} - \sqrt{R^2 + r^2} \right)$$

bulge radius r_0 is set to 1 kpc and R to 100 kpc.

Balasin and Grumiller (**BG**),
2008, Int.J.Mod.Phys.D17:475-488,2008

preliminary fit with the Gaia DR2 data



Green dots represent stellar average velocity in a shell of $(r, r+ 0.2)$ kpc, error = velocity dispersion inside the corresponding shell.

- blue Navarro- Frenk_White profile -> virial radius about 180 kpc, velocity about 160 km/s, halo scale radius about 10 kpc
- red BG galactic “relativistic” curve -> “cylindrical “ internal radius z about 1kpc, external “viral “ radius about 135 kpc, V_{rot} from the Sun about 230 km/s

fits compatible with the data and same χ^2

✓ Concluding remarks

The realization of the **relativistic celestial sphere** is an all-sky scientific validation of the absolute parallax and proper motions in Gaia. But reaching 10-20 μs accuracy on individual parallax and annual proper motions for bright stars ($V < 16$) is also the largest GR experiment ever attempted from space

Lesson from Gaia: ***the power of the weak (non-linear) gravitational fields both at Solar System/MW scales***

astrometry cannot be set apart from fundamental physics, high accuracy needs new refinement of the observable according to GR

***To trace light trajectories back to the emitting stars requires an appropriate treatment of local gravity and a relativistic definition of the observable, according to the measurement protocol of GR.
Null geodesic should be as fundamental
as the equation of stellar evolution!***

GR weak field regime *is not* always equivalent to Newtonian regime..

- DR1 results and DR2 processing and validation are indicating that the Gaia mission can fulfill most of the science promised

At DR2 and after (with external photometric and spectroscopic information)

- Global (all-sky) GR tests from within the Solar System
- Non-Newtonian rotational curves
- Hypervelocity stars
- Local Cosmology:
 - Galactic Warp via new proper motions/distances of O-B stars
 - Thick Disk velocity-metallicity correlation at 8 kpc from Gal. Cen.
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✓ Beyond Gaia

Gaia represents ONLY the 1-step... increasing the level of the measurement precision requires to refine consistently the metric of the solar system, the solution for the null geodesic and so on..

➤ **individual distances, space-phase stellar distributions can be achieved only from “in situ” investigations** i.e. from within the local universe

➤ μ s accuracy is not enough to probe directly Mpc scale -> nanoarcsec regime and GWs!

➤ Gaia's astrometric released data fully compliant with the prescriptions of GR. The comparison, simulated data are not!

”One day, our actual knowledge of the composition of the fixed stars sky, the apparent motion of the fixed stars, and the position of the spectral lines as a function of the distance will probably have come far enough for us to be able to decide empirically the question whether or not Λ vanishes”

[Einstein, 1917, letter to de Sitter]