

# Constraining DM models with extremely distant galaxies

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with:

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M. Totzauer, A. Lamastra

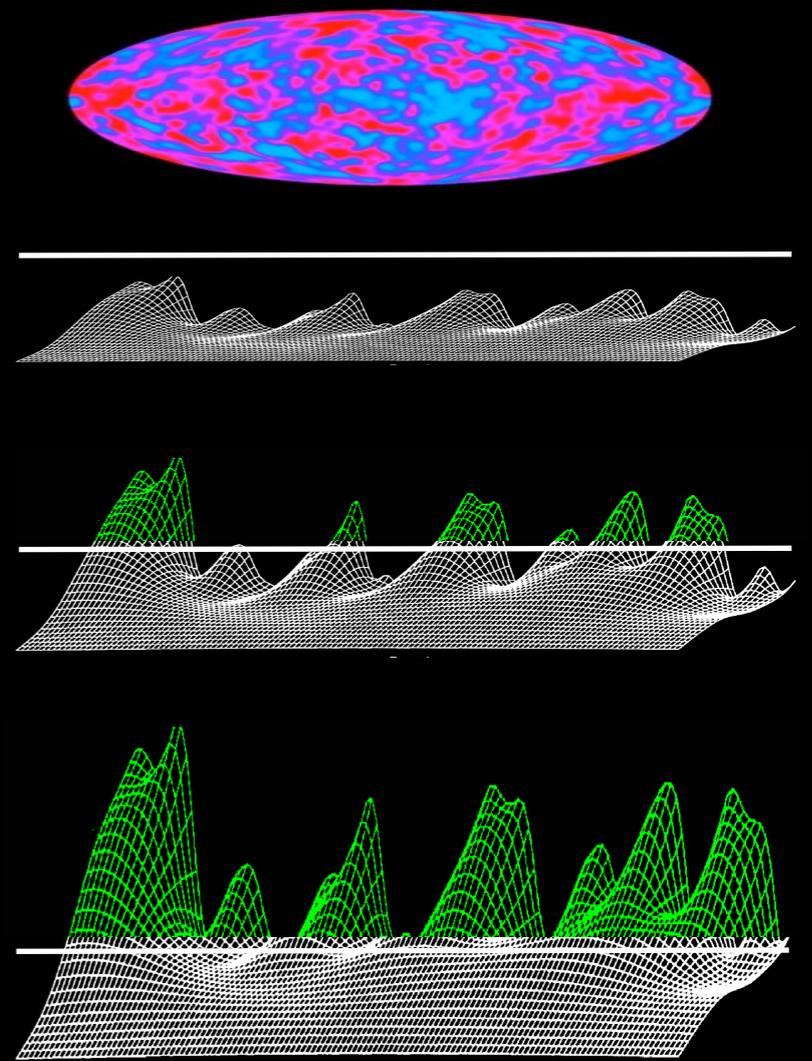
The Nature of DM determines the shape of the power spectrum  $P(k)$  and hence of the variance  $\sigma^2(M)$

Mean (square) value of perturbations of size  $R(\sim 1/k)$  enclosing a mass  $M$

$$P(k) = \frac{1}{V} \langle |\delta_k|^2 \rangle$$

$$\sigma_M^2 = \frac{1}{(2\pi)^3 V} \int^{M \leftrightarrow k} dk k^2 P(k)$$

$$\sigma_M^2 \leftrightarrow P(k)$$



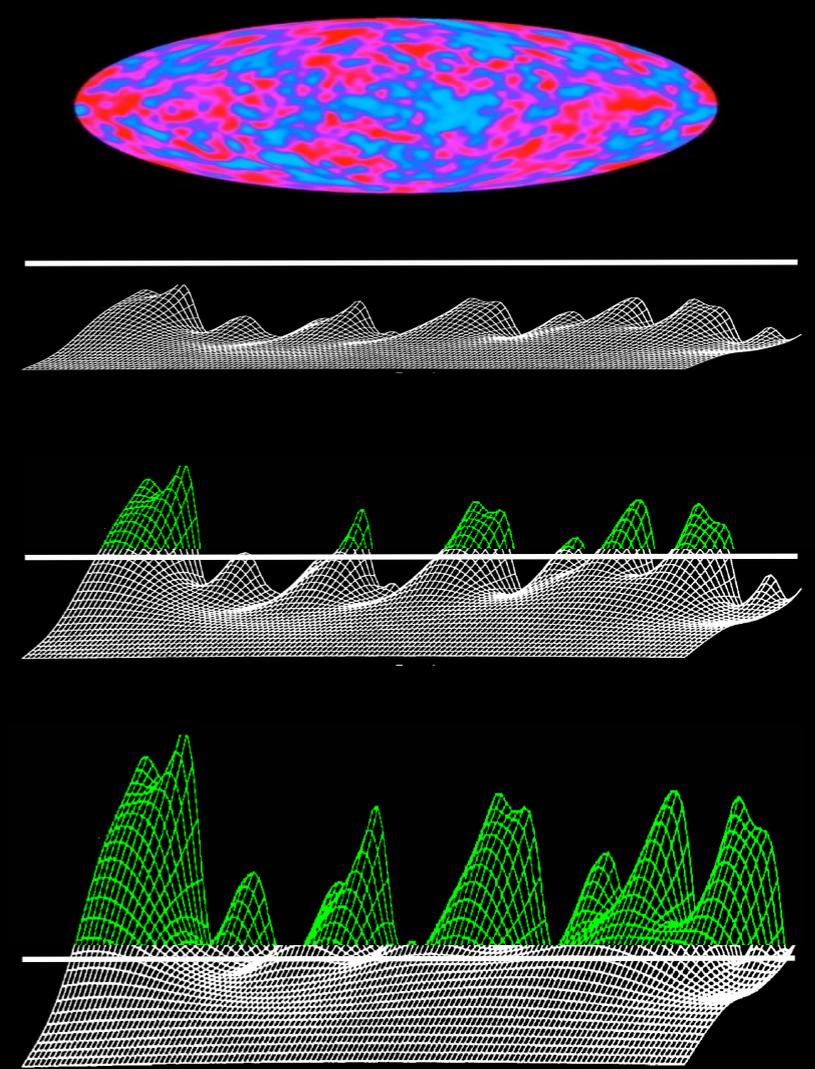
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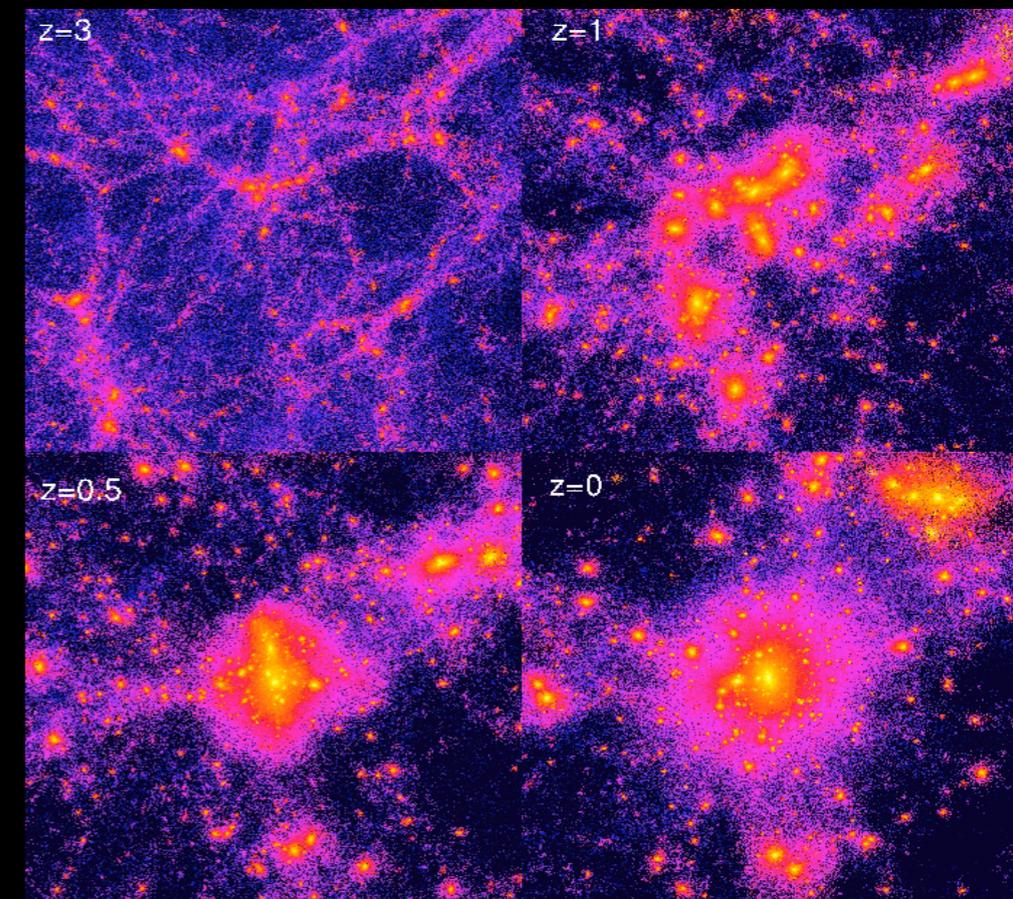
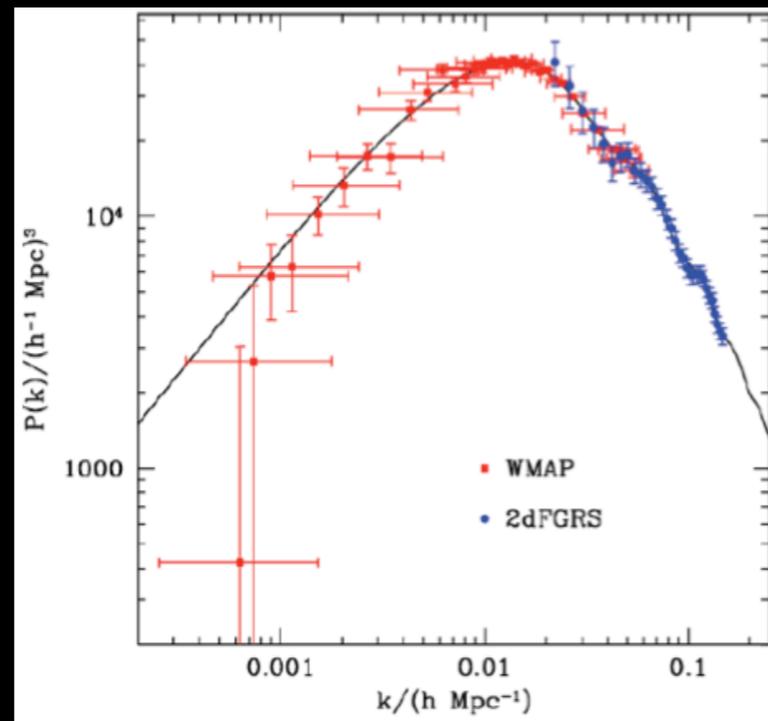
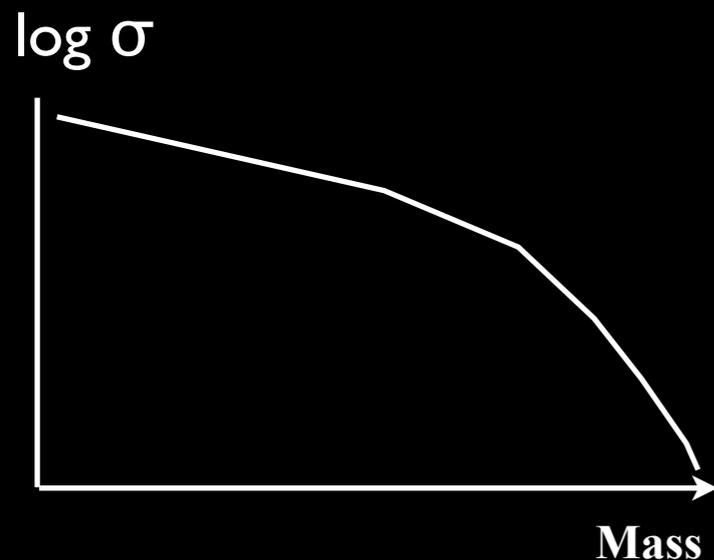
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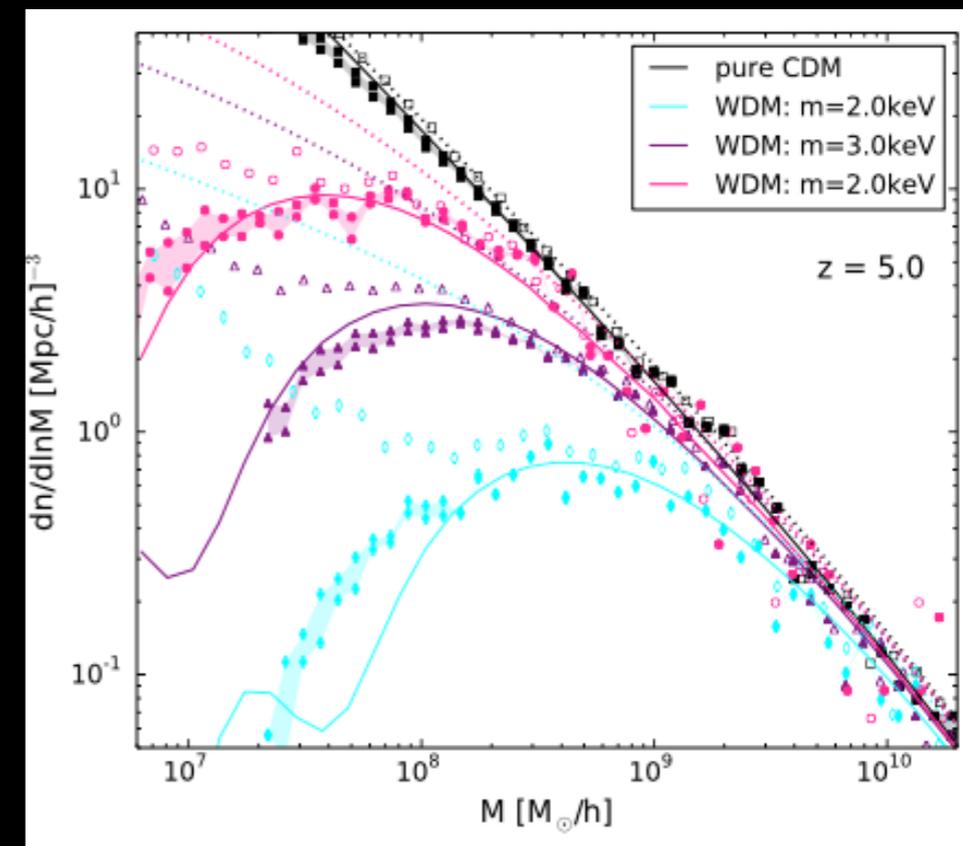
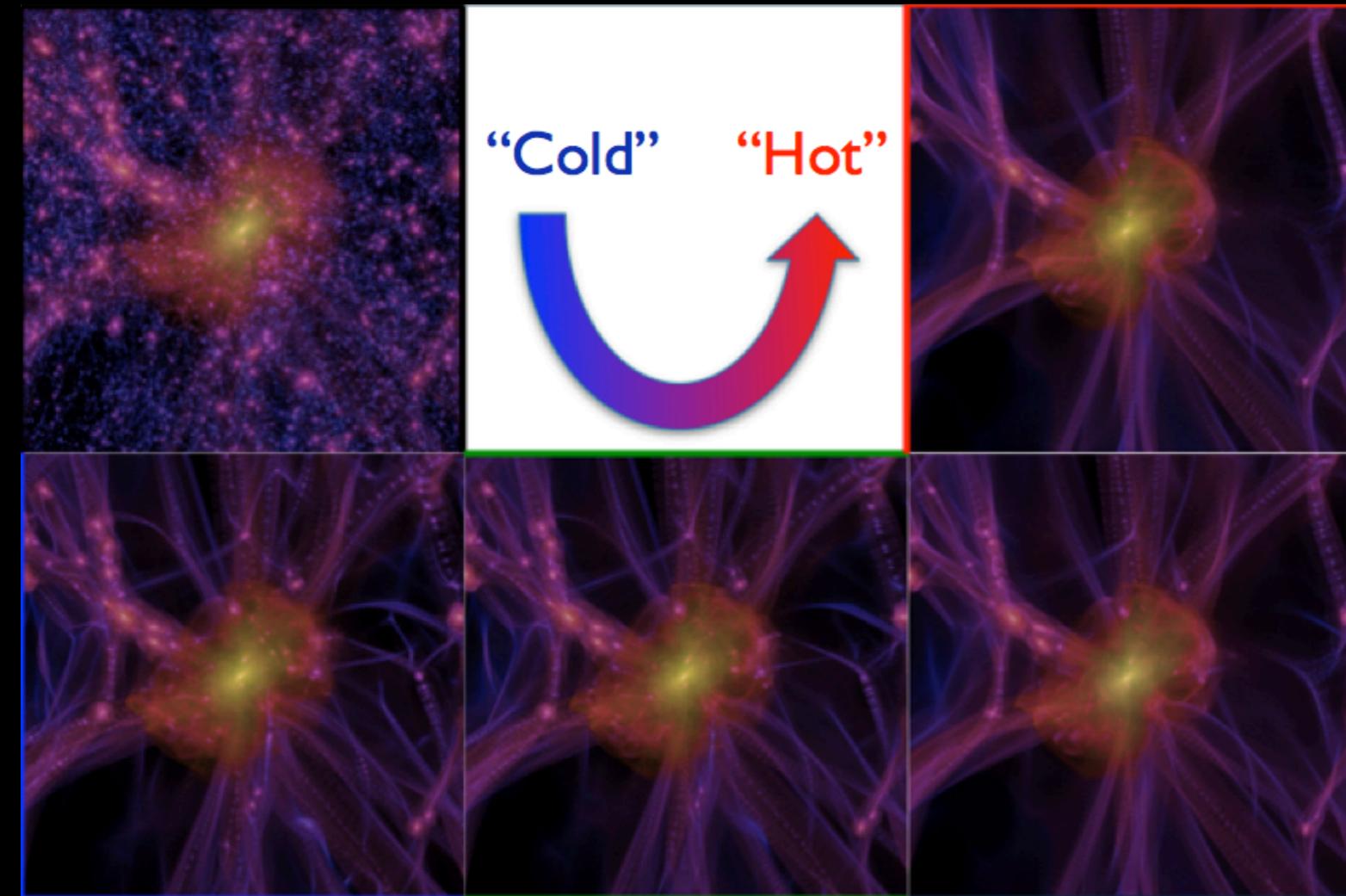
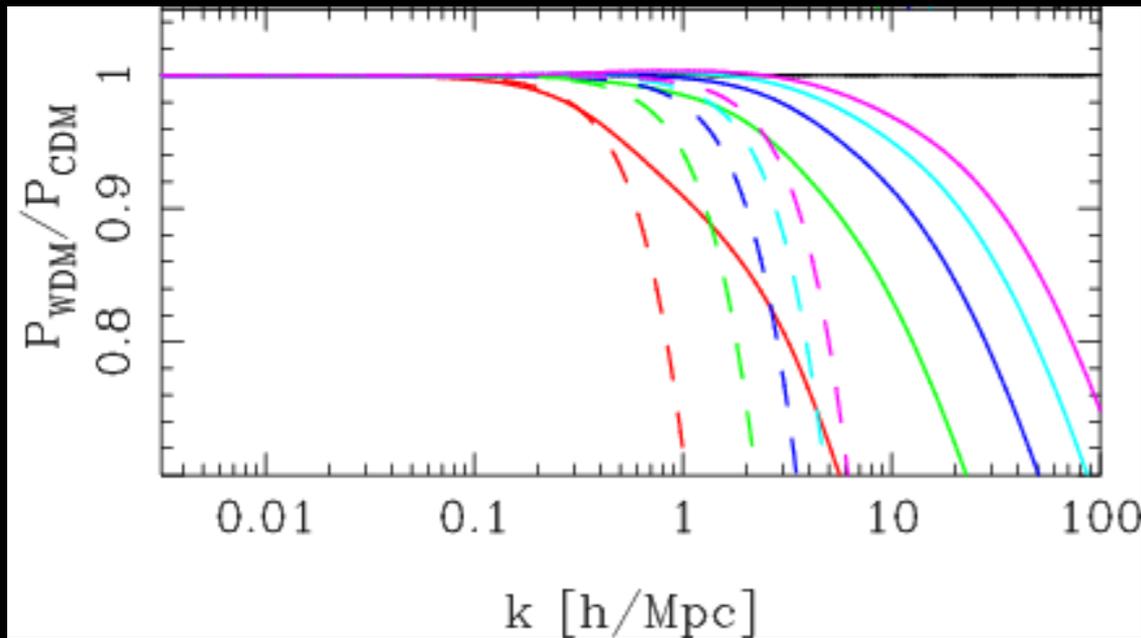


E.g. **CDM** generally assumes DM to be constituted by thermal relics with low velocity dispersion. Low-mass perturbations are not dissipated.



**Thermal WDM** The simplest case. Small-scale perturbations smoothed by free-streaming

1 parameter: the particle mass  $m_x$  in the range.  **$m_x = 1 - 5 \text{ keV}$**



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1 parameter: the particle mass  $m_\chi$  in the range.  **$m_\chi = 1 - 5 \text{ keV}$**

### Constraints on $m_\chi$

from comparing the observed abundance of small-scale clumps (dwarf galaxies, Lyman- $\alpha$  absorbers) to the predicted abundance of low-mass DM clumps

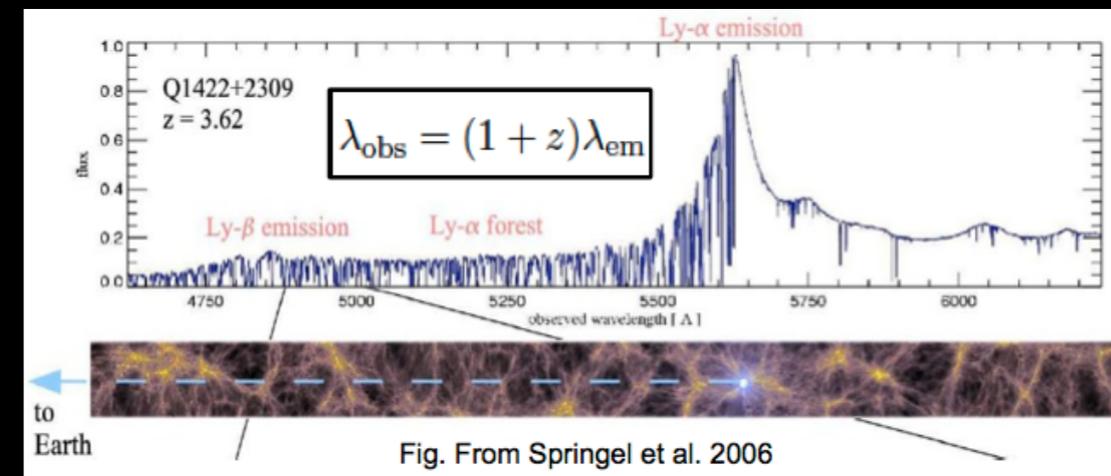
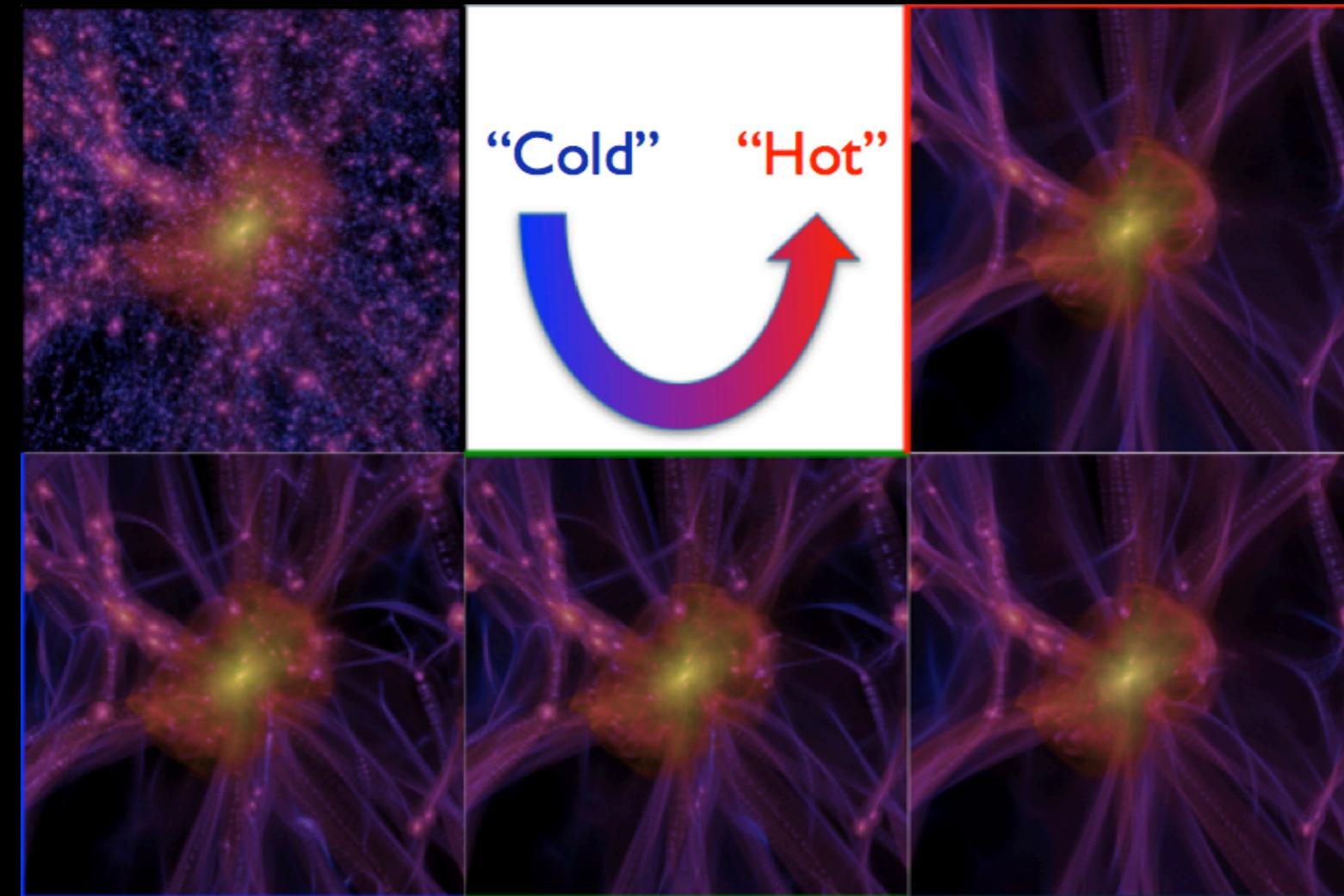
This involves modelling the baryon physics to relate the observed structures to DM

Lower limits on  $m_\chi$  from abundance of sub-structures

$m_\chi \geq 1.5 \text{ keV}$  Polisensky & Ricciotti 2011;

Lovell et al. 2012, 2015 Horiuchi et al. 2014,

Belokurov et al. 2010



Lyman- $\alpha$  absorbers yield  $m_\chi > 3 \text{ keV}$

when compared to hydro simulations (intergalactic gas physics)

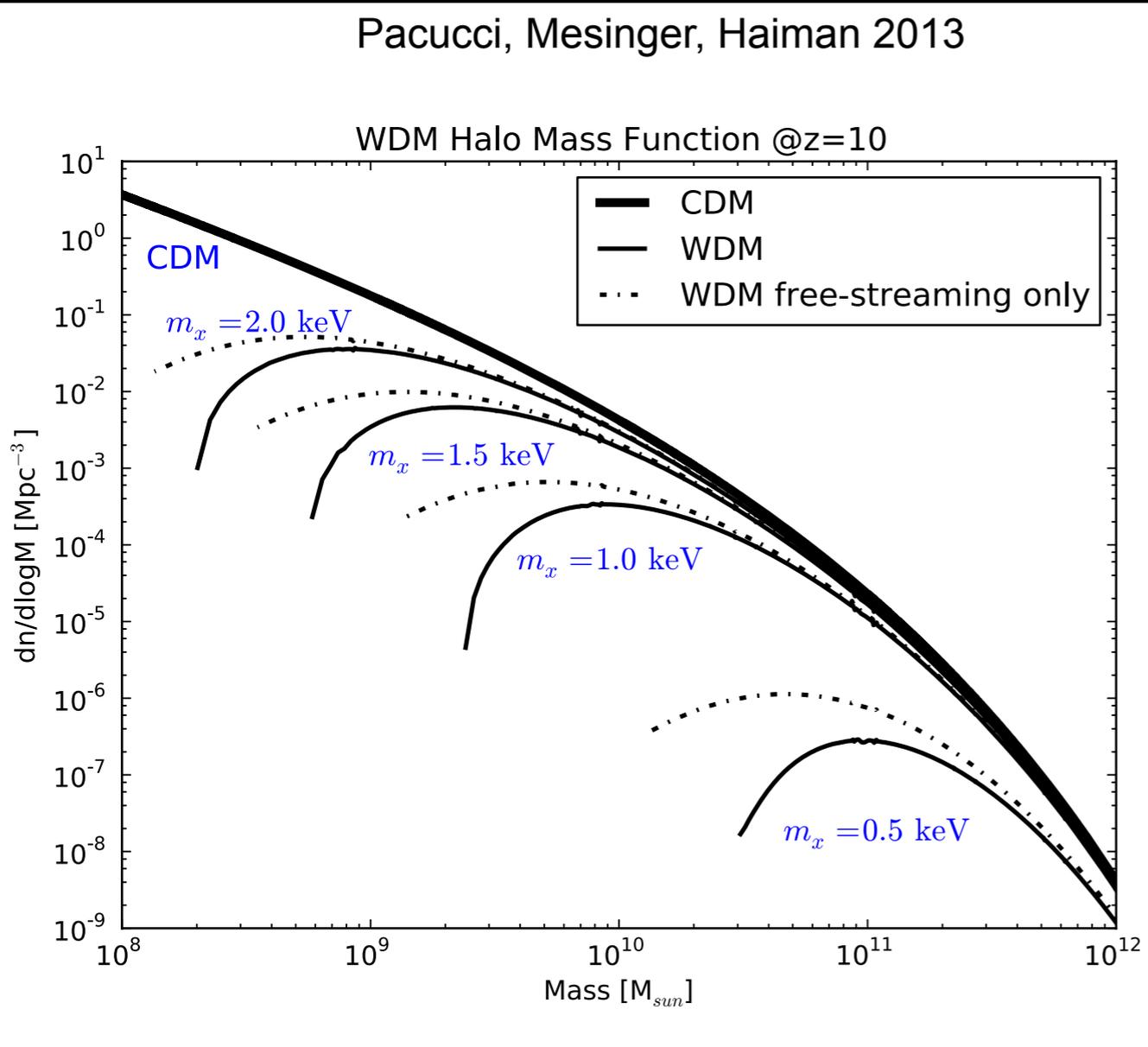
Viel+2005, 2013

# Constraints on $m_x$ from the abundance of low-mass galaxies: getting rid of degeneracy with astrophysics of gas and stars

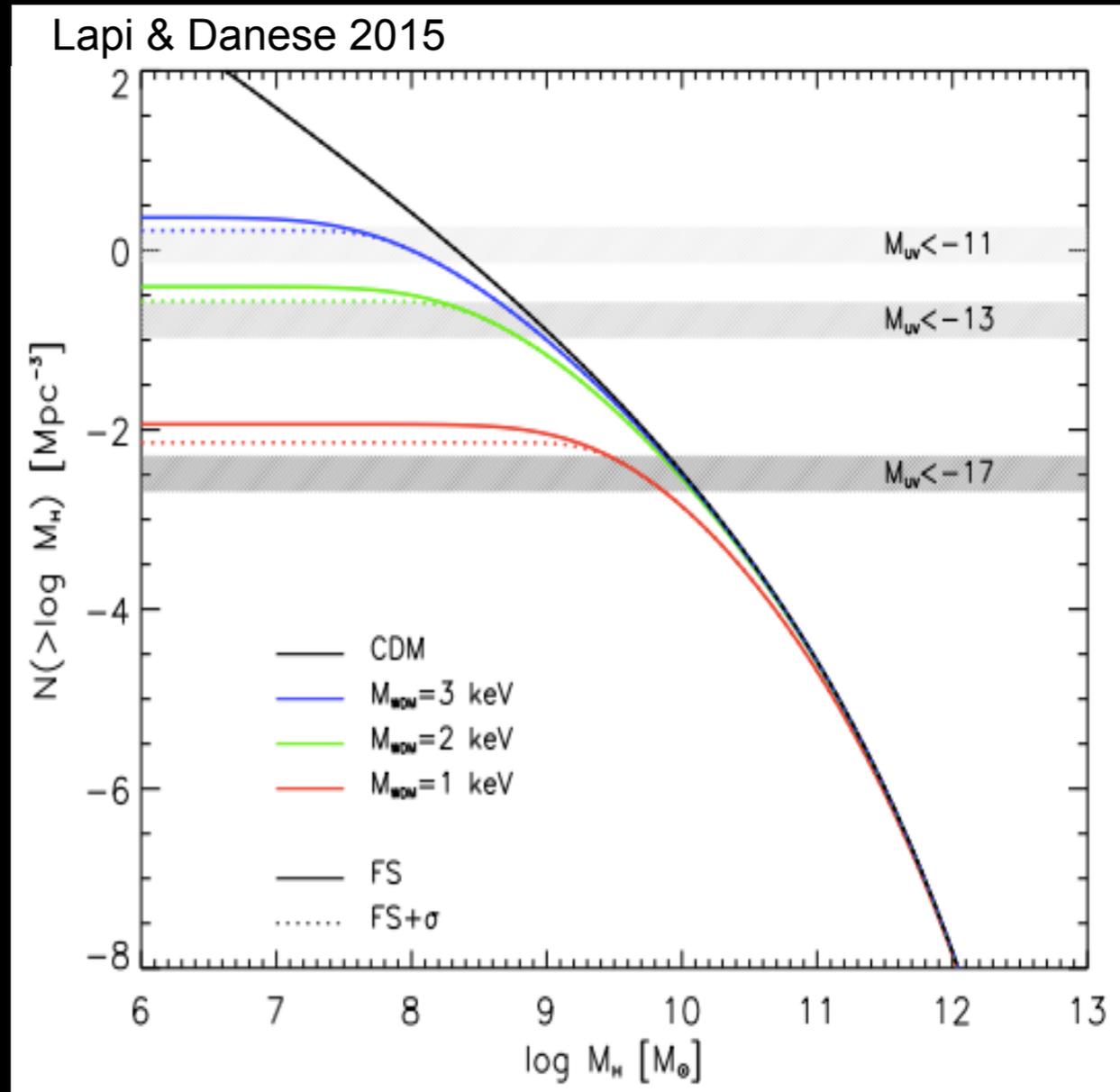
WDM mass functions exhibit a down turn at masses close to the half-mode mass  
Correspondingly, the number density of halos per  $\text{Mpc}^3$  saturates to a maximum value at small  $M$

Observe galaxy density larger than such a maximum value would rule out the corresponding WDM particle mass independently of L/M relation

### Differential Halo Mass function



### Cumulative Halo Mass function (number / $\text{Mpc}^3$ )



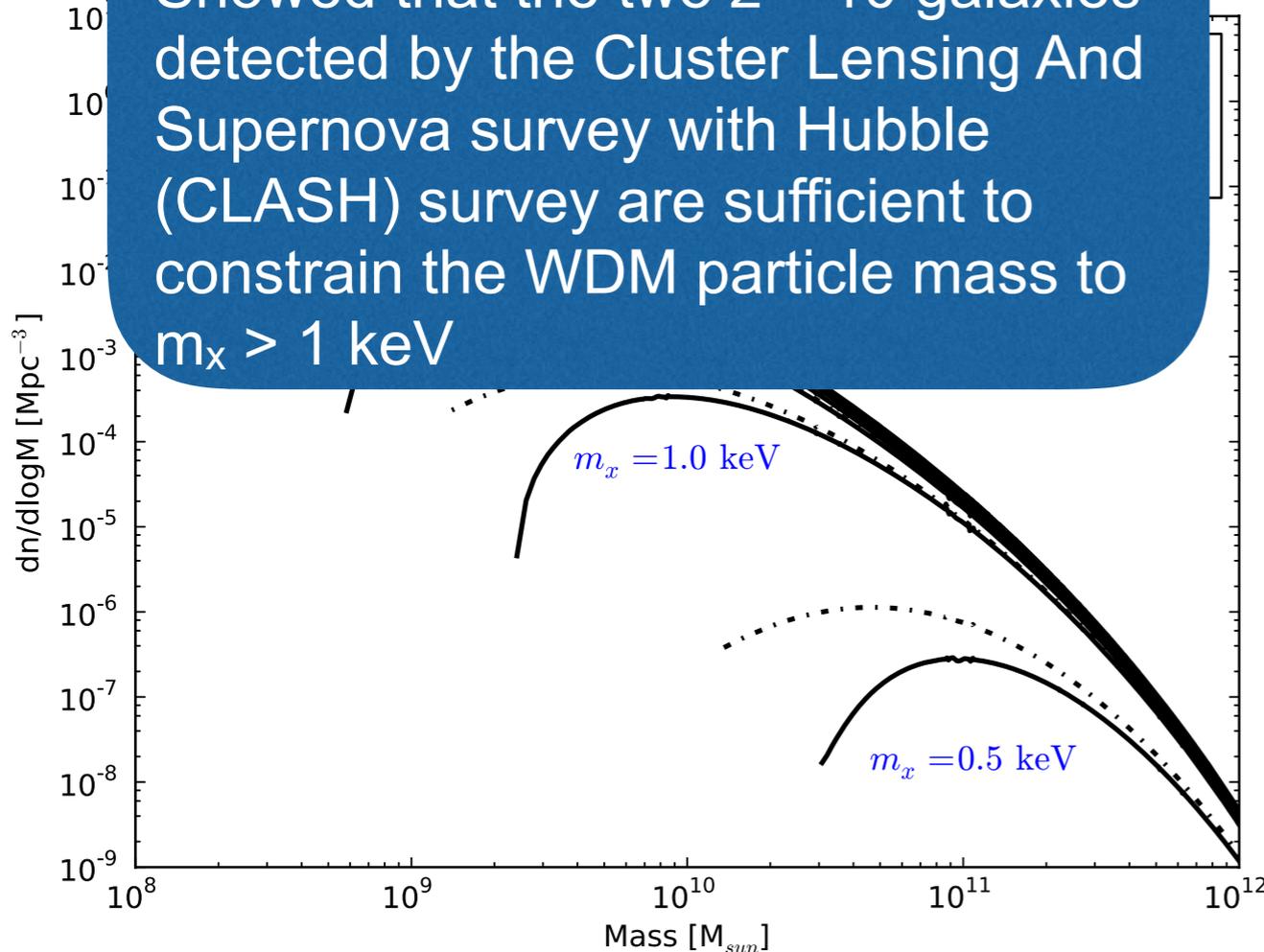
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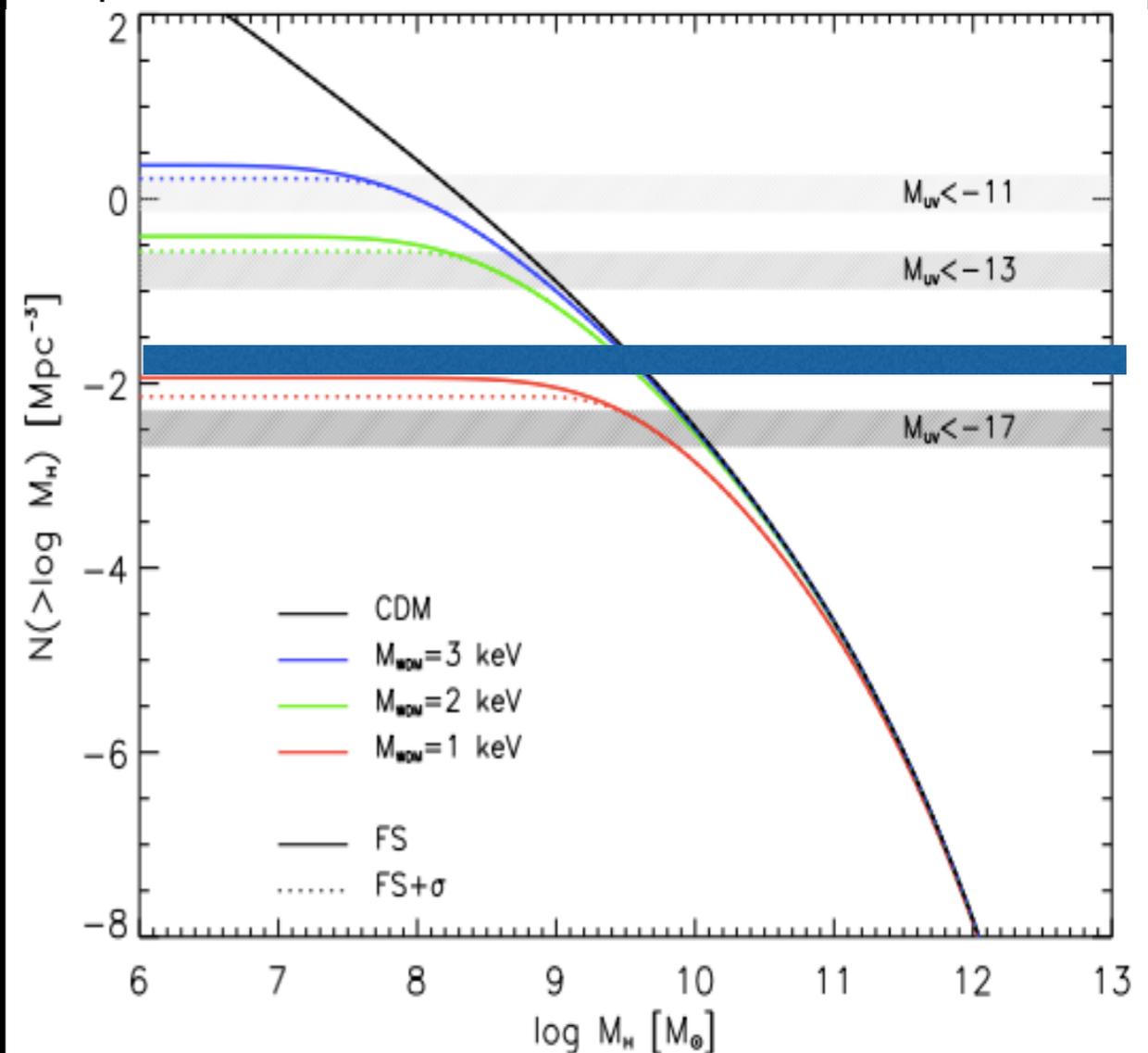
Differential Halo Mass function

Cumulative Halo Mass function  
(number /  $\text{Mpc}^3$ )

Pacucci, Mesinger, Haiman 2013  
Showed that the two  $z \approx 10$  galaxies detected by the Cluster Lensing And Supernova survey with Hubble (CLASH) survey are sufficient to constrain the WDM particle mass to  $m_x > 1 \text{ keV}$

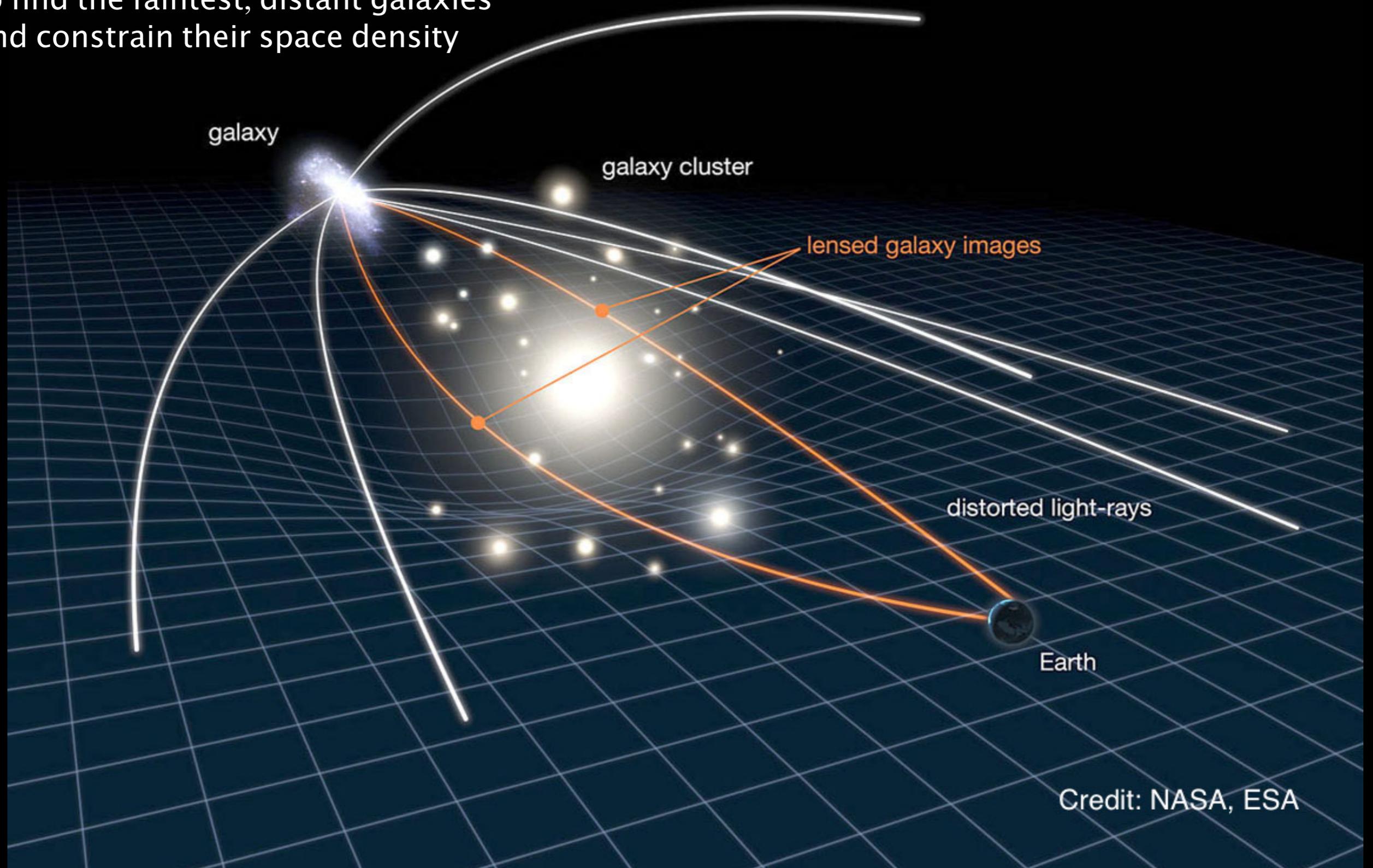


Lapi & Danese 2015



# Finding the faintest galaxies

Gravitational lensing is the tool we need to find the faintest, distant galaxies and constrain their space density



Credit: NASA, ESA

# The Hubble Frontier Fields survey

HST Treasury program

Deep multi-band survey of 6 strong lensing clusters.

Designed to reach to the faintest high-redshift galaxies thanks to the combined power of ultra-deep space observations and lensing magnification

## The Frontier Fields Goals

Using Director's Discretionary (DD) observing time, HST is undertaking a revolutionary deep field observing program to peer deeper into the Universe than ever before and provide a first glimpse of JWST's universe.

These Frontier Fields will combine the power of HST with the natural gravitational telescopes of high-magnification clusters of galaxies. Using both the Wide Field Camera 3 and Advanced Camera for Surveys in parallel, HST will produce the deepest observations of clusters and their lensed galaxies ever obtained, and the second-deepest observations of blank fields (located near the clusters). These images will reveal distant galaxy populations ~10-100 times fainter than any previously observed, improve our statistical understanding of galaxies during the epoch of reionization, and provide unprecedented measurements of the dark matter within massive clusters.

This program is based upon the 2012 recommendations from the Hubble Deep Fields Initiative Science Working group: [SWG Report 2012](#)

Abell 2744

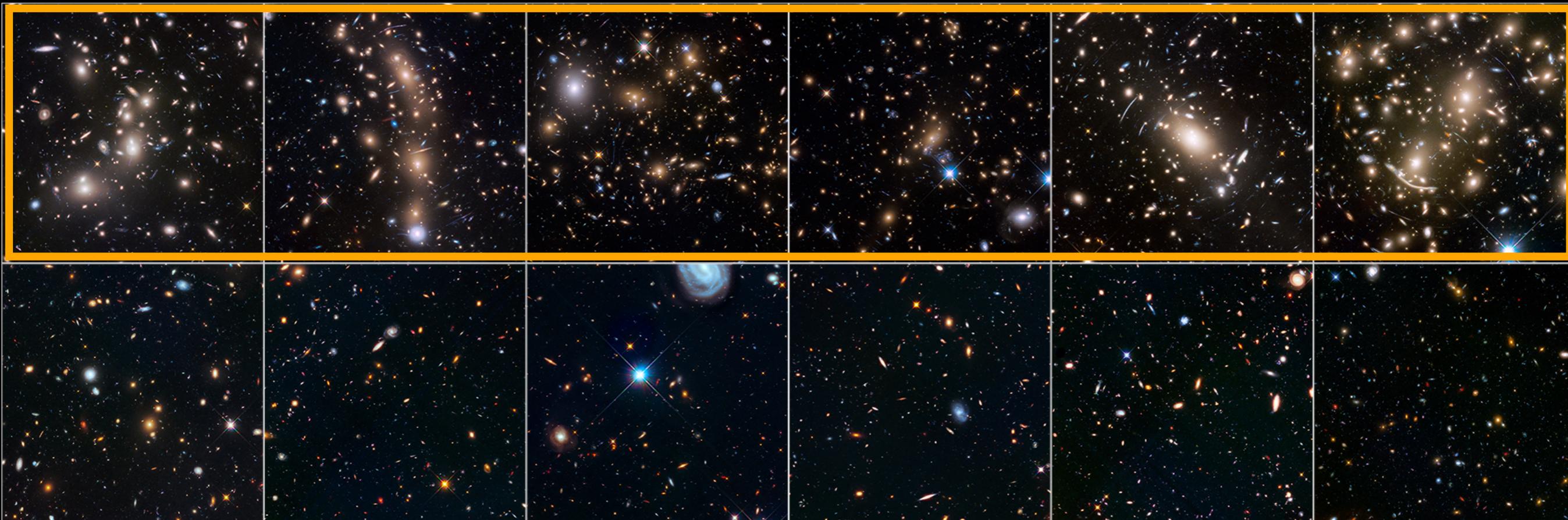
MACS J0416.1-2403

MACS J0717.5+3745

MACS J1149.5+2223

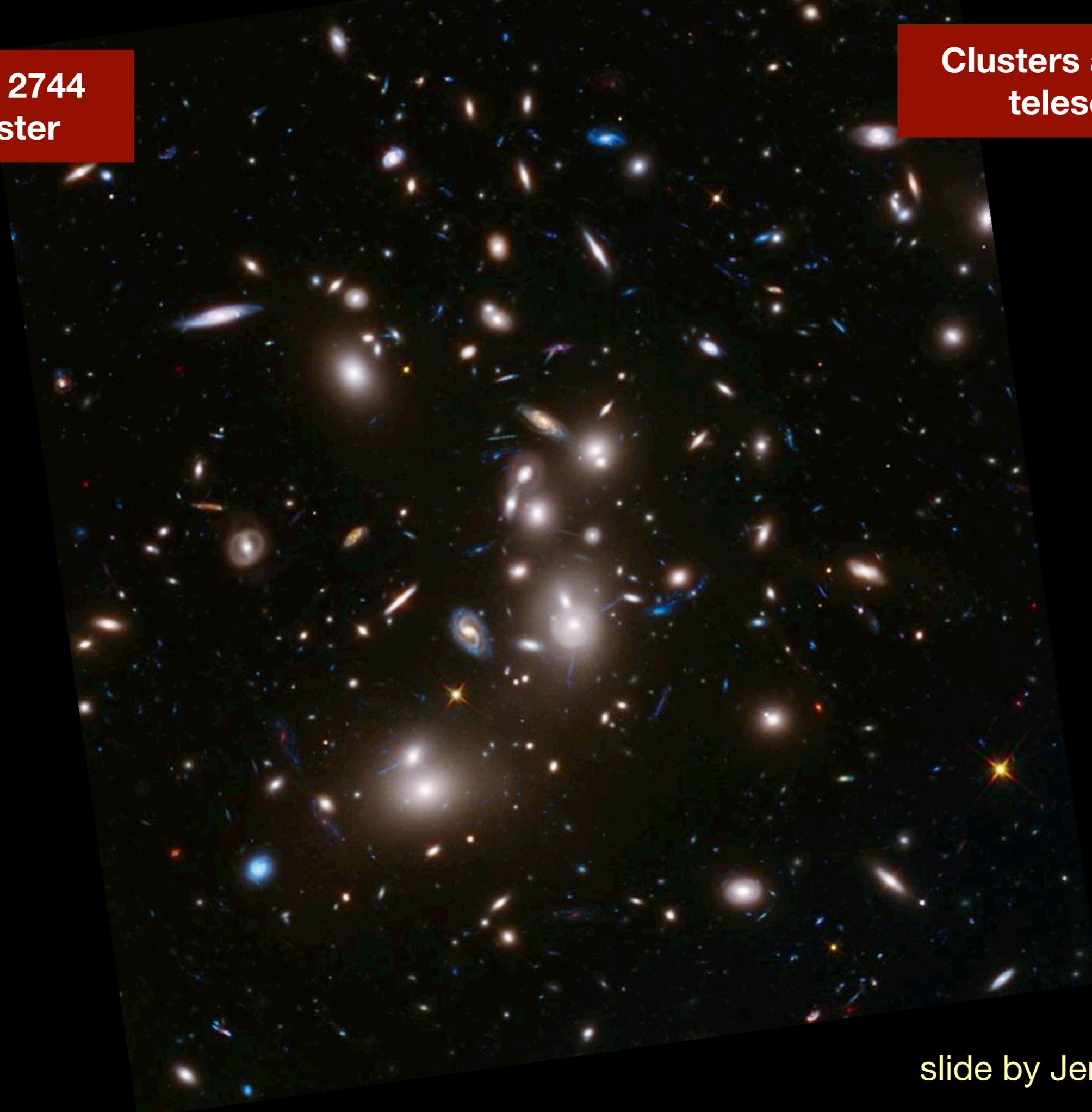
Abell S1063

Abell 370



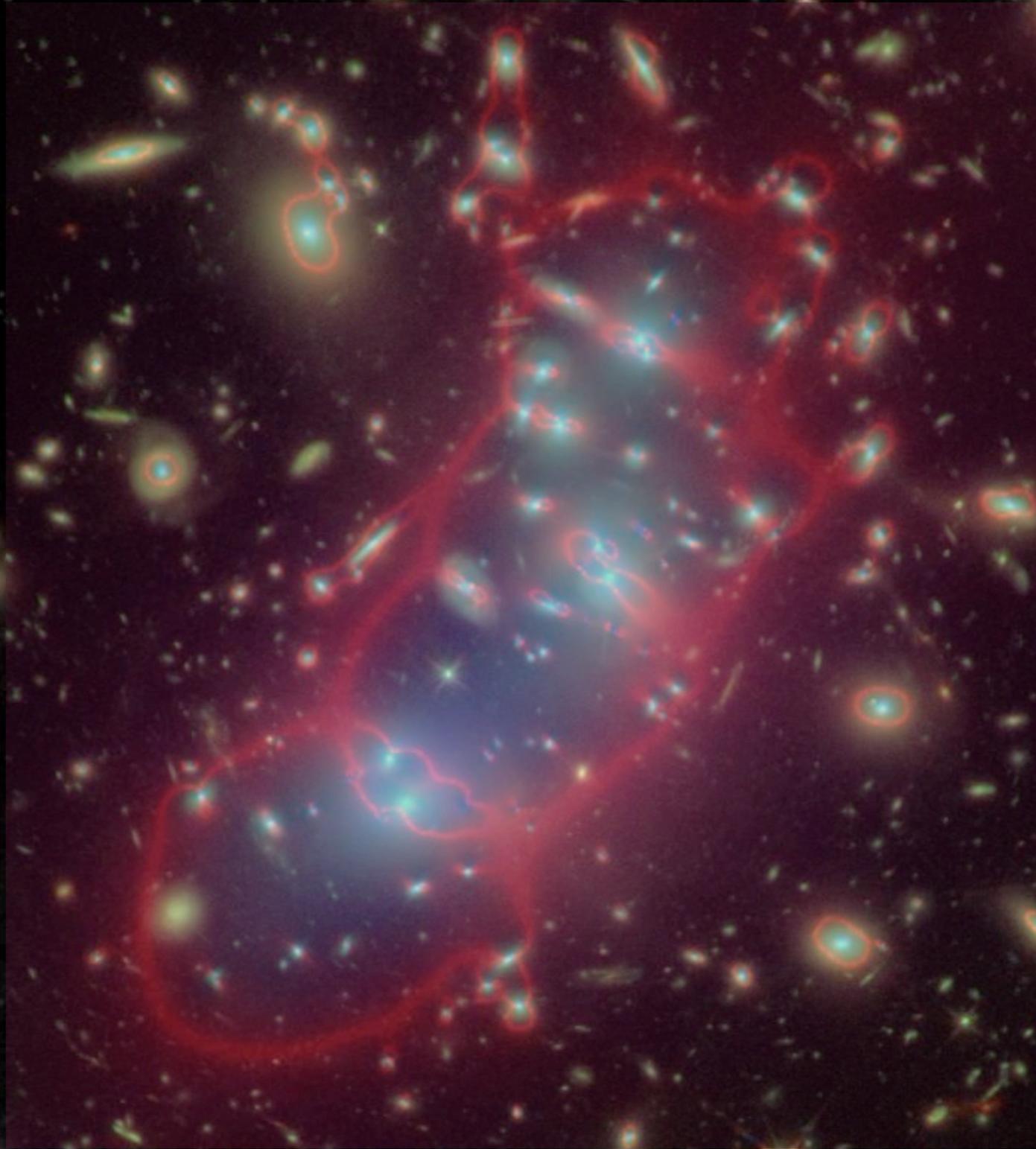
**Abell 2744  
Cluster**

**Clusters as lensing  
telescopes**

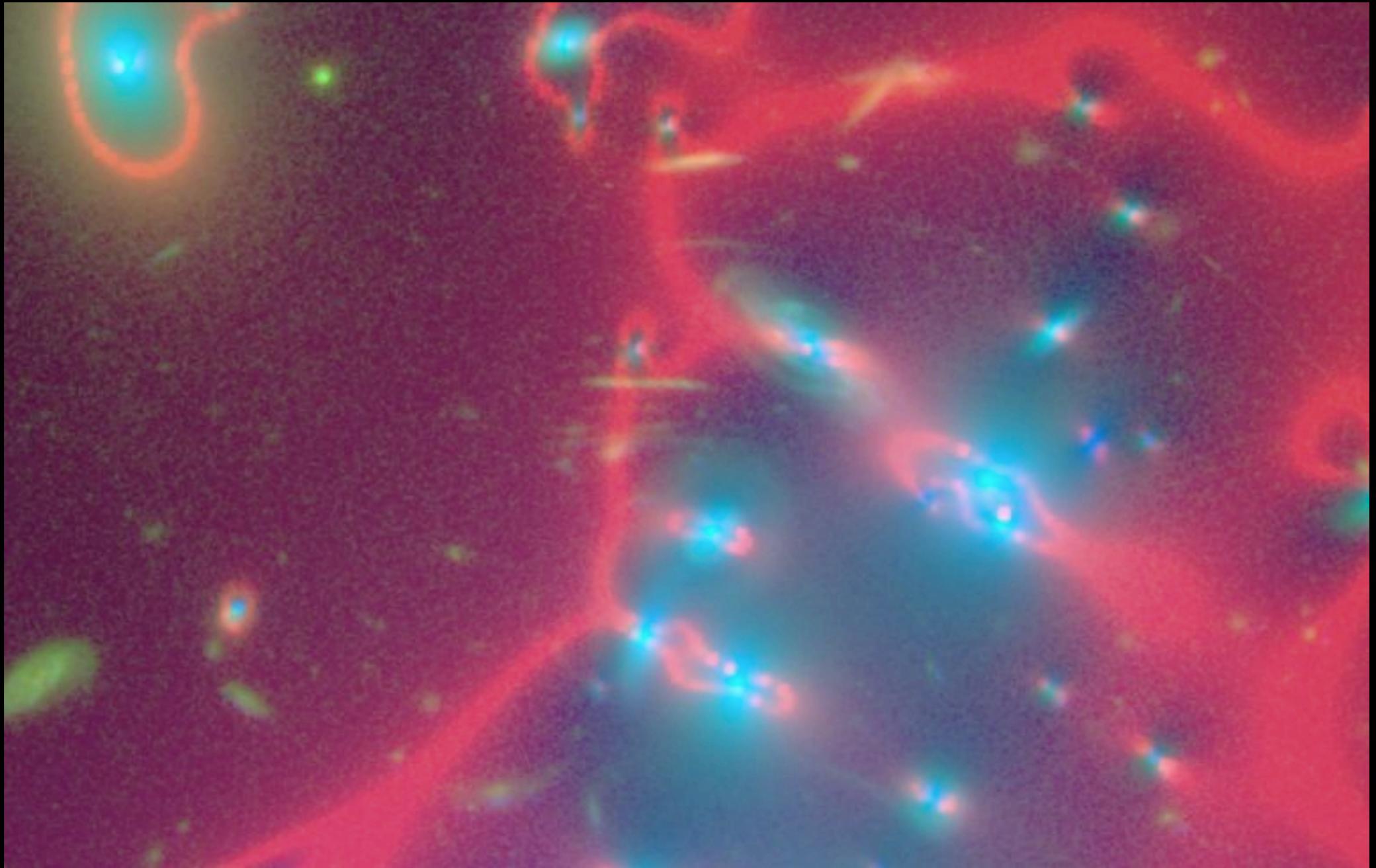


slide by Jennifer Lotz

**Abell 2744  
Cluster**

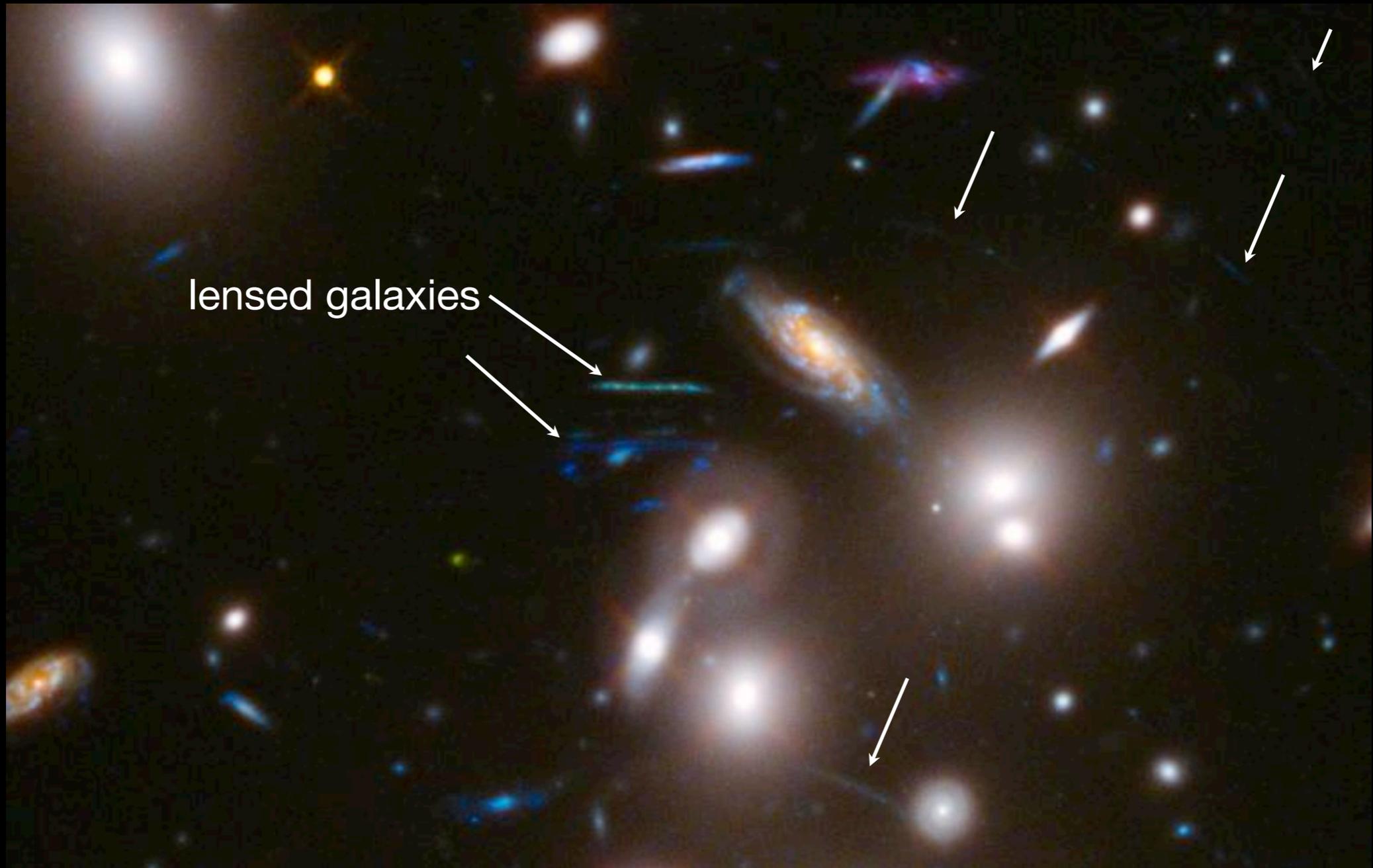


slide by Jennifer Lotz



background galaxies are magnified by factors up to  $\sim 10-20$ ,  
providing the deepest yet view of the universe

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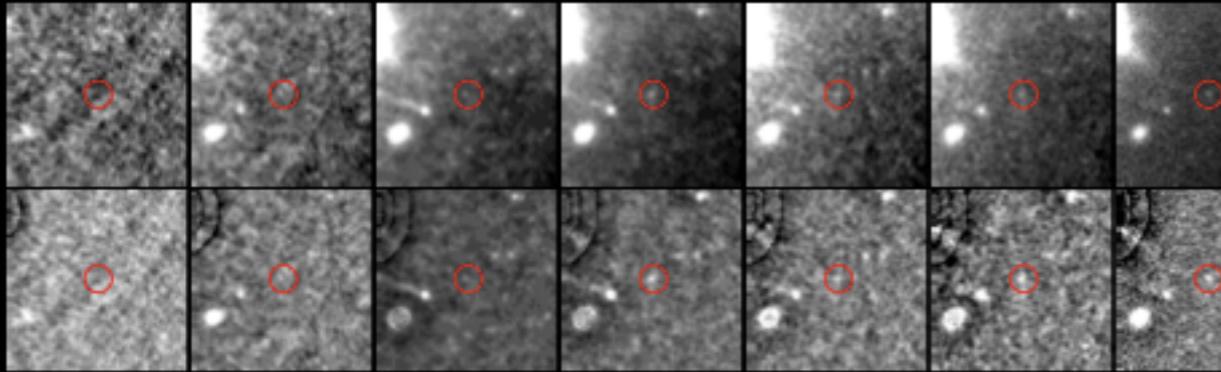


lensed galaxies

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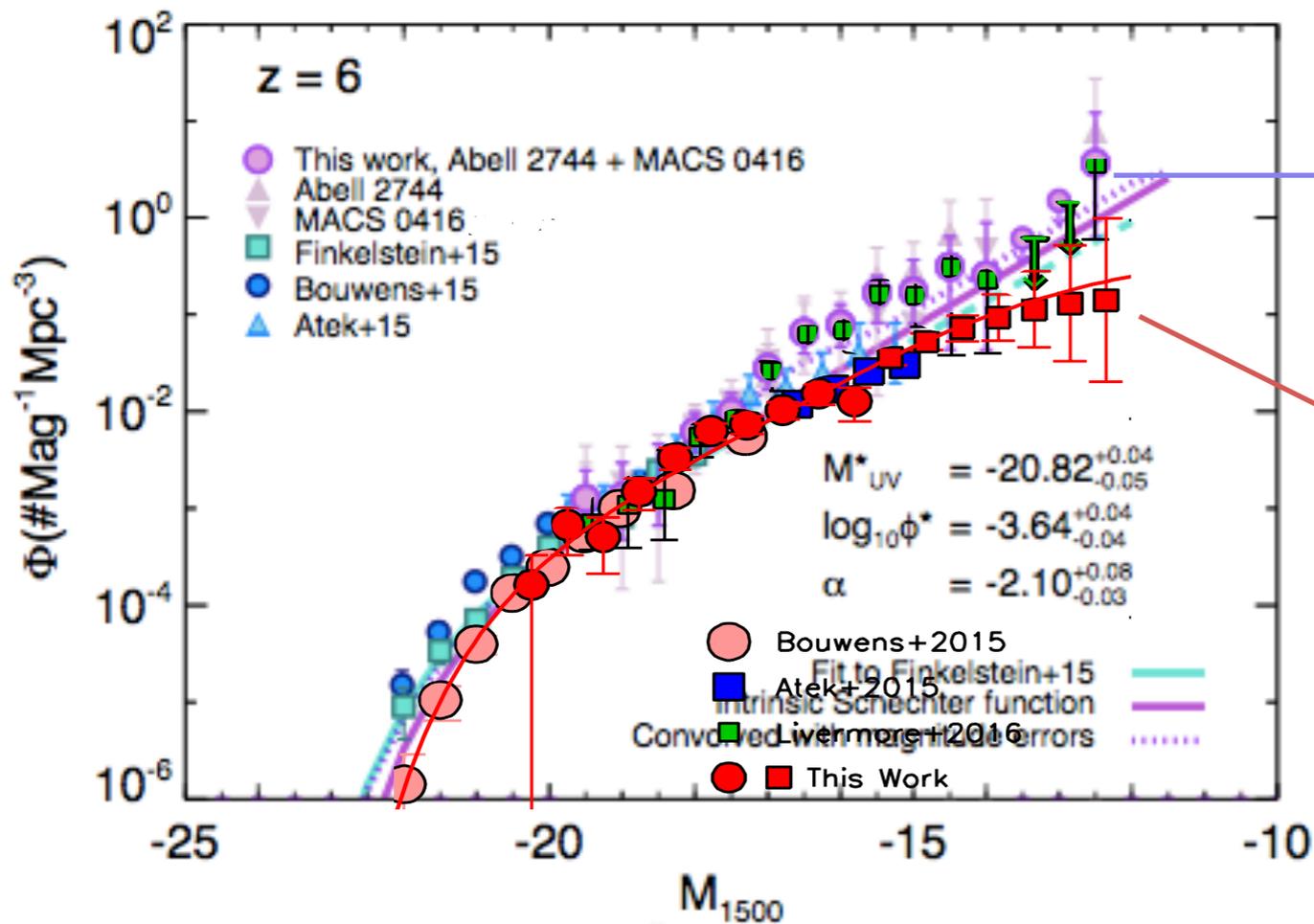
slide by Jennifer Lotz

# Luminosity Functions of $z=6$ Galaxies in the Hubble Frontier Fields: Based on 2 HFF lensing clusters 164 galaxies at $z=6$



Postage stamp image of a2744 z6 3341, from the  $z \sim 6$  sample detected in the Abell 2744 cluster field. The circle shows a  $0.4''$  aperture. This galaxy is magnified by a factor  $\sim 20\times$ , giving it an intrinsic UV magnitude of  $M_{UV}^* = -14.54$ , but was not detected in previous studies due to the bright foreground object close to the line of sight (top row). It is easily detected in the wavelet-subtracted images (lower row)

Integrated number densities of galaxies ( $\#/Mpc^3$ ) down to the faints magnitude: correspond to



Livermore et al. 2017

Best fit	$\log \Phi_{\text{obs}} = 0.54$
$1\sigma$	$\log \Phi_{\text{obs}} = 0.26$
$2\sigma$	$\log \Phi_{\text{obs}} = 0.01$
$3\sigma$	$\log \Phi_{\text{obs}} = -0.36$

Bouwens et al. 2017

Best fit	$\log \Phi_{\text{obs}} = -0.25$
$1\sigma$	$\log \Phi_{\text{obs}} = -0.47$
$2\sigma$	$\log \Phi_{\text{obs}} = -0.62$
$3\sigma$	$\log \Phi_{\text{obs}} = -0.9$

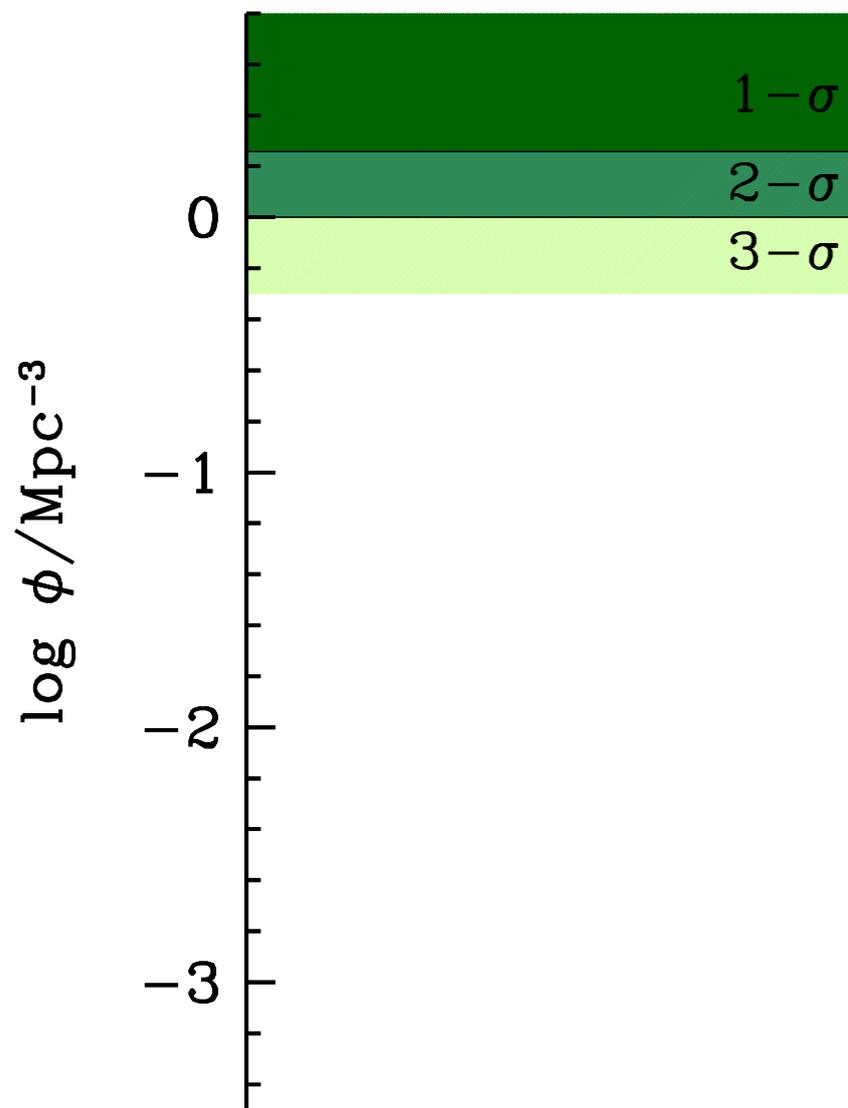
# HFF constraints on thermal WDM models

Based on 2 HFF lensing clusters Abell 2744 and MACS 0416

Menci, Grazian, Castellano & Sanchez 2016

1. Starting from observed luminosity function, we run  $10^7$  Monte Carlo extractions of galaxies according to the observed distribution and with an uncertainty provided by the observed error bars.

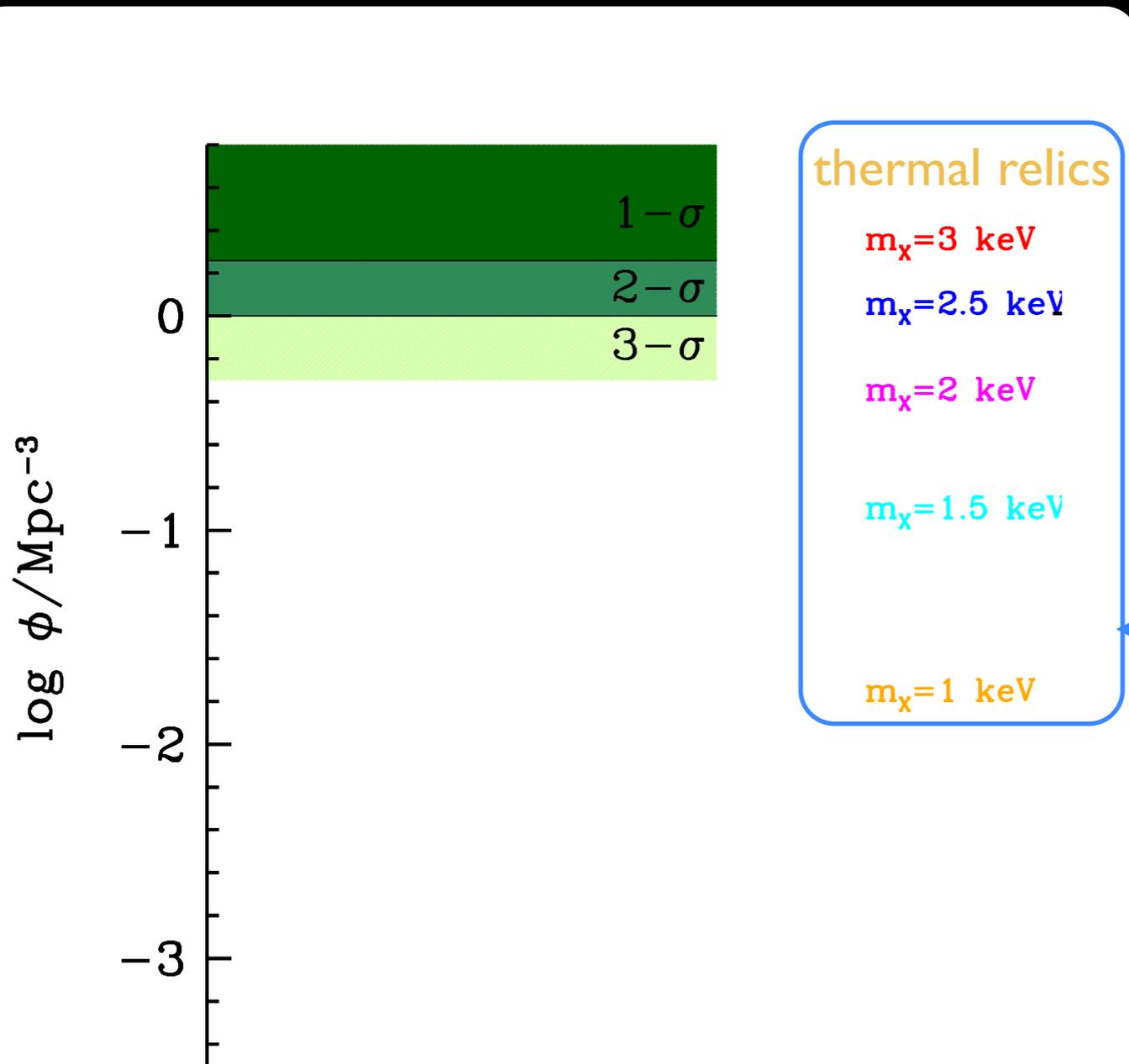
2. Compute the total number density of galaxies down to the faintest magn bin:  
# of galaxies/Mpc<sup>3</sup>  
at different confidence levels:



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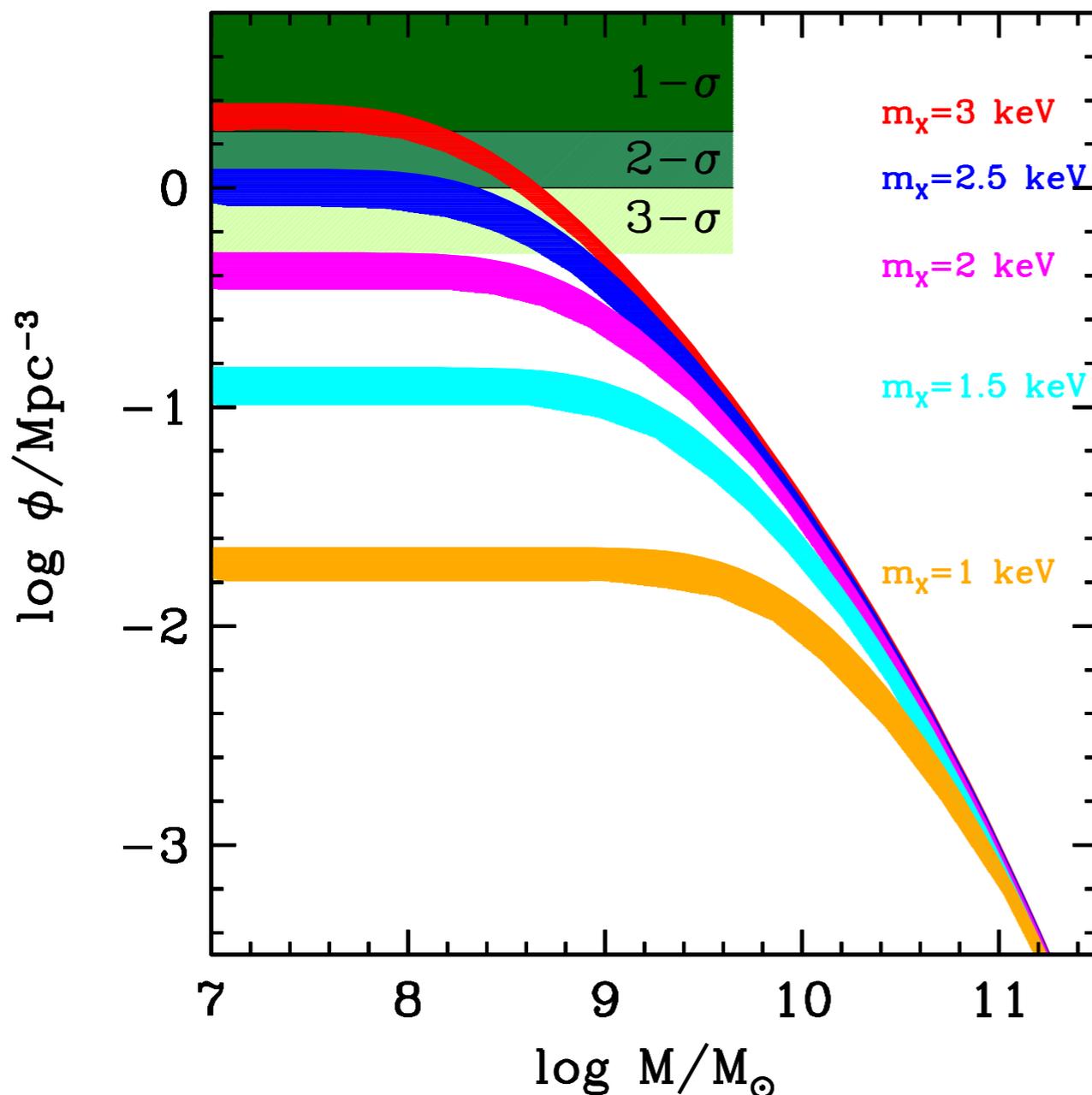
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Menci, Grazian, Castellano & Sanchez 2016

thermal relics

Menci, Grazian, Castellano & Sanchez 2016



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2. Compute the total number density of galaxies down to the faintest magn bin:  
# of galaxies/Mpc<sup>3</sup>  
at different confidence levels:

3. Assume a Power Spectrum  $P(m_\chi, \text{production model})$

4. Compute the associated WDM cumulative mass function and the corresponding maximum number density  $\tilde{\Phi}(m_\chi, \text{production model})$

5. Allowed WDM models are those with  $\Phi_{\text{obs}} \leq \tilde{\Phi}(m_\chi, \text{production model})$   
observed galaxies cannot outnumber the DM halos

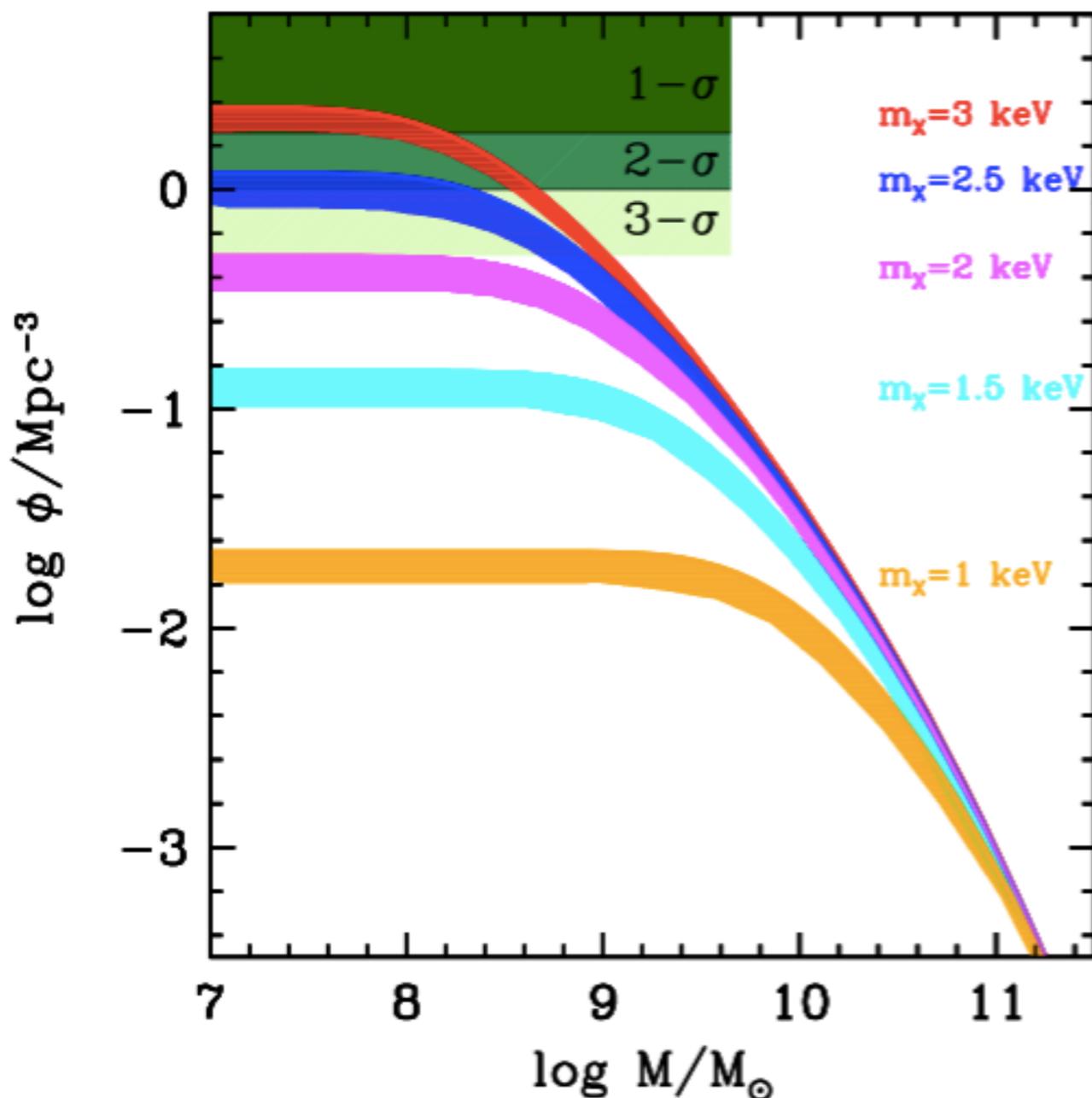
# HFF constraints on thermal WDM models

$m_\chi > 3$  keV ( $1\sigma$ )  $m_\chi > 2.4$  keV ( $2\sigma$ )  
(comparing with Livermore et al)

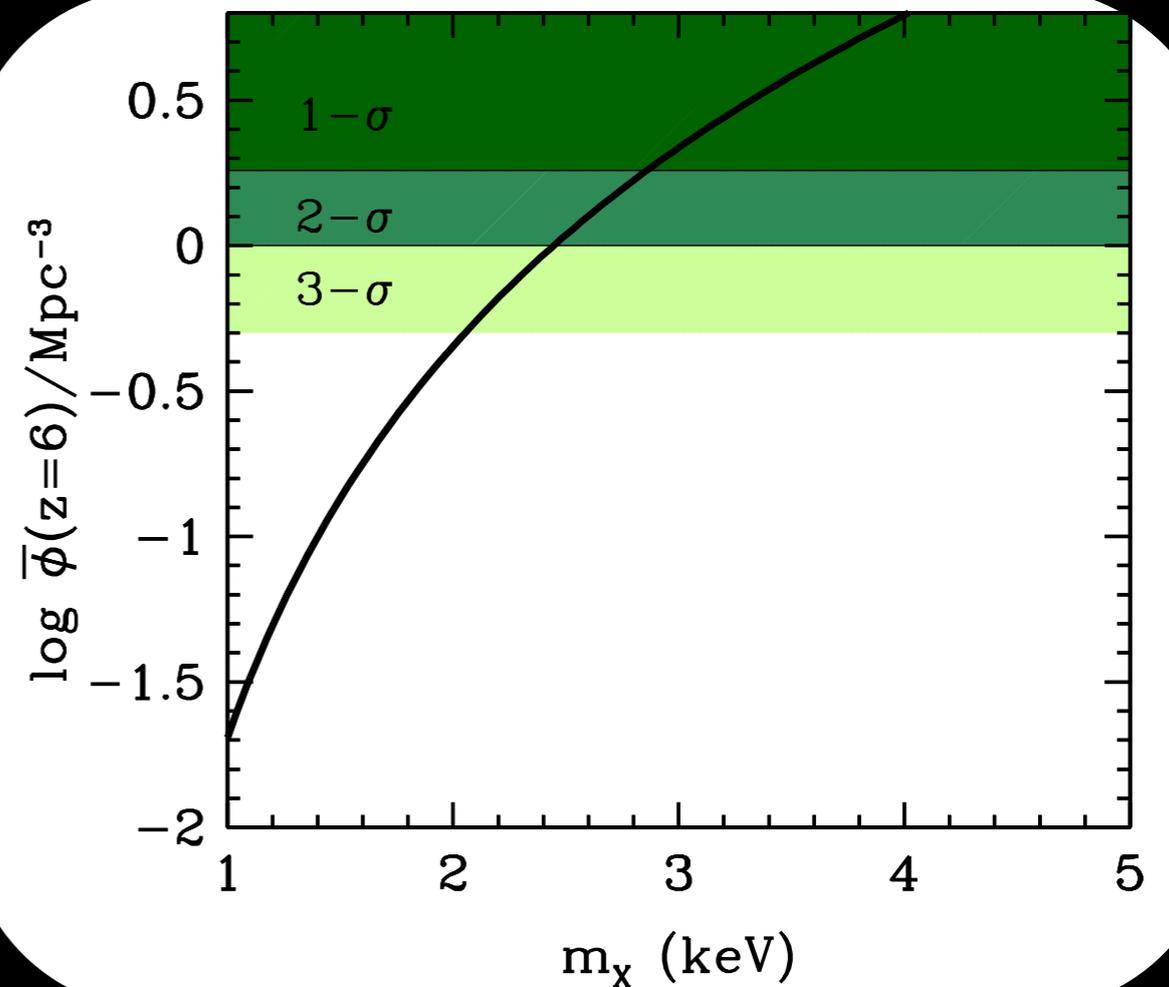
$m_\chi > 2.5$  keV ( $1\sigma$ )  $m_\chi > 2.$  keV ( $2\sigma$ )  
(comparing with Bouwens et al)

The tighter limits derived so far independently of baryon physics visible galaxies cannot outnumber their host DM halos

Menci, Grazian, Castellano & Sanchez 2016



Very Conservative: The observed galaxies cannot outnumber their host DM halo, whose density saturates to a max. value depending on  $m_\chi$



# Sterile Neutrino WDM Production from Active–Sterile Transitions

**Strong physical motivation:** the most natural extension of SM to include mass terms for active neutrinos.

2 parameters: neutrino mass  $m_\nu$   
mixing with active neutrinos  $\sin^2(2\theta)$   
(oscillation probability)

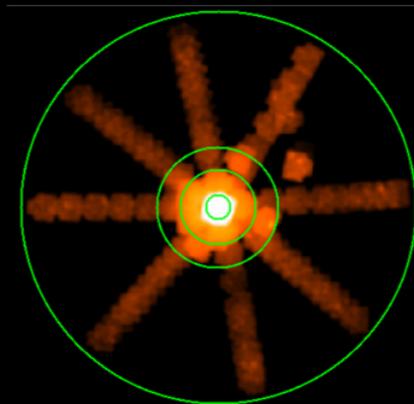
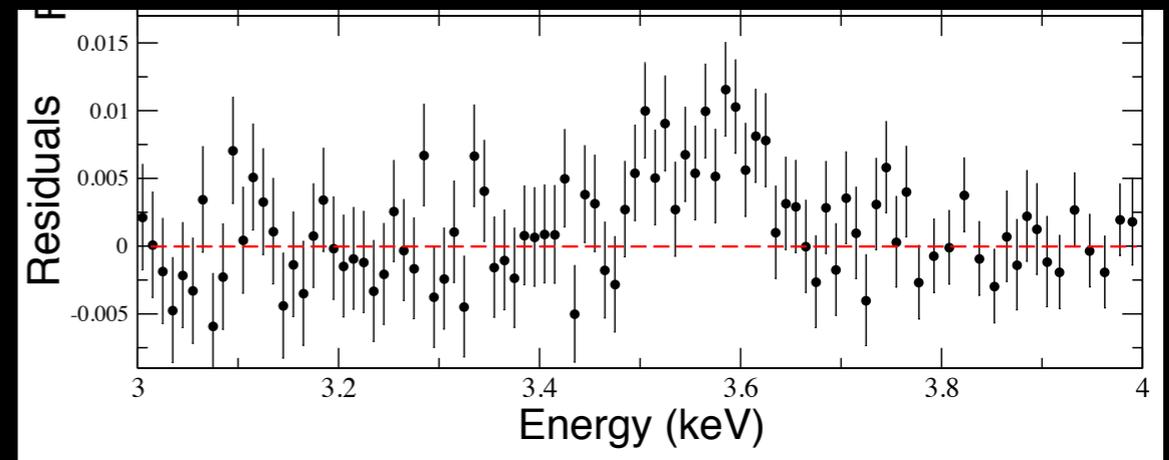
## Not completely Dark !

Stacked XMM spectra (MOS and PN) of 73 bright galaxy

Detected a very weak line at  $E = 3.55\text{--}3.57$  keV rest-frame energy: IF due to WDM corresponds to the decay of

$m_\nu \approx 7$  keV

X-ray line reported in stacked observations of X-ray clusters with the XMM-Newton X-ray Space telescope with both CCD instruments (Bulbul et al. 2014). Consistent line in XMM-Newton observations of M31, Galactic Center (Boyarsky et al. 2015) and M31, Draco (Ruchayskiy 2015), Perseus Cluster (Boyarsky et al. 2014) + 9 individual clusters (Iakubovskiy 2016). Signal from Milky Way detected also by NuSTar (Nerenov et al. 2016)

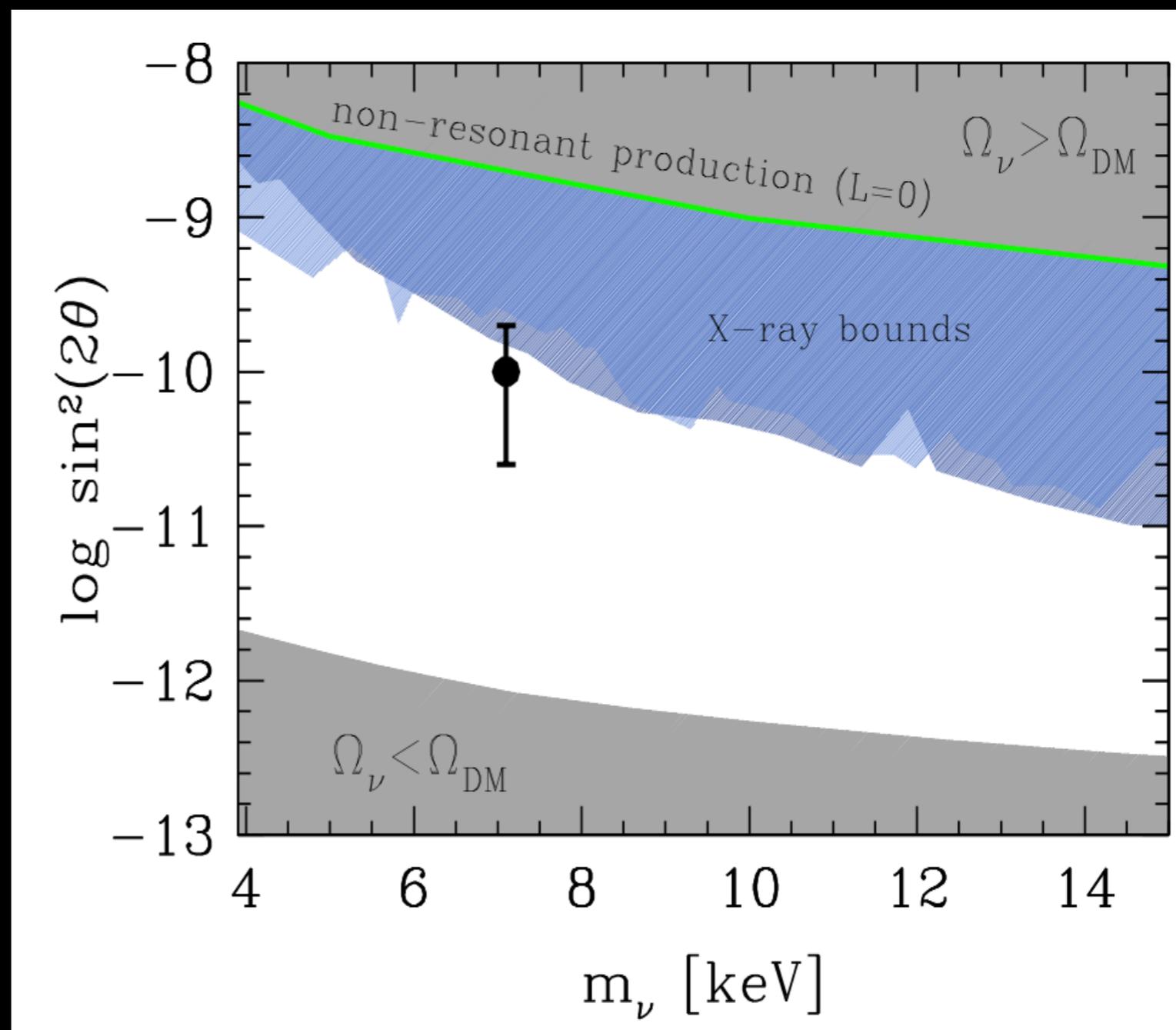


The radial distribution of the signal is consistent with a decay origin (Franse et al. 2016)

# Sterile Neutrino WDM

Exploring the Parameter Space of Sterile Neutrino Models based on resonant production

# Production from Active–Sterile Transitions

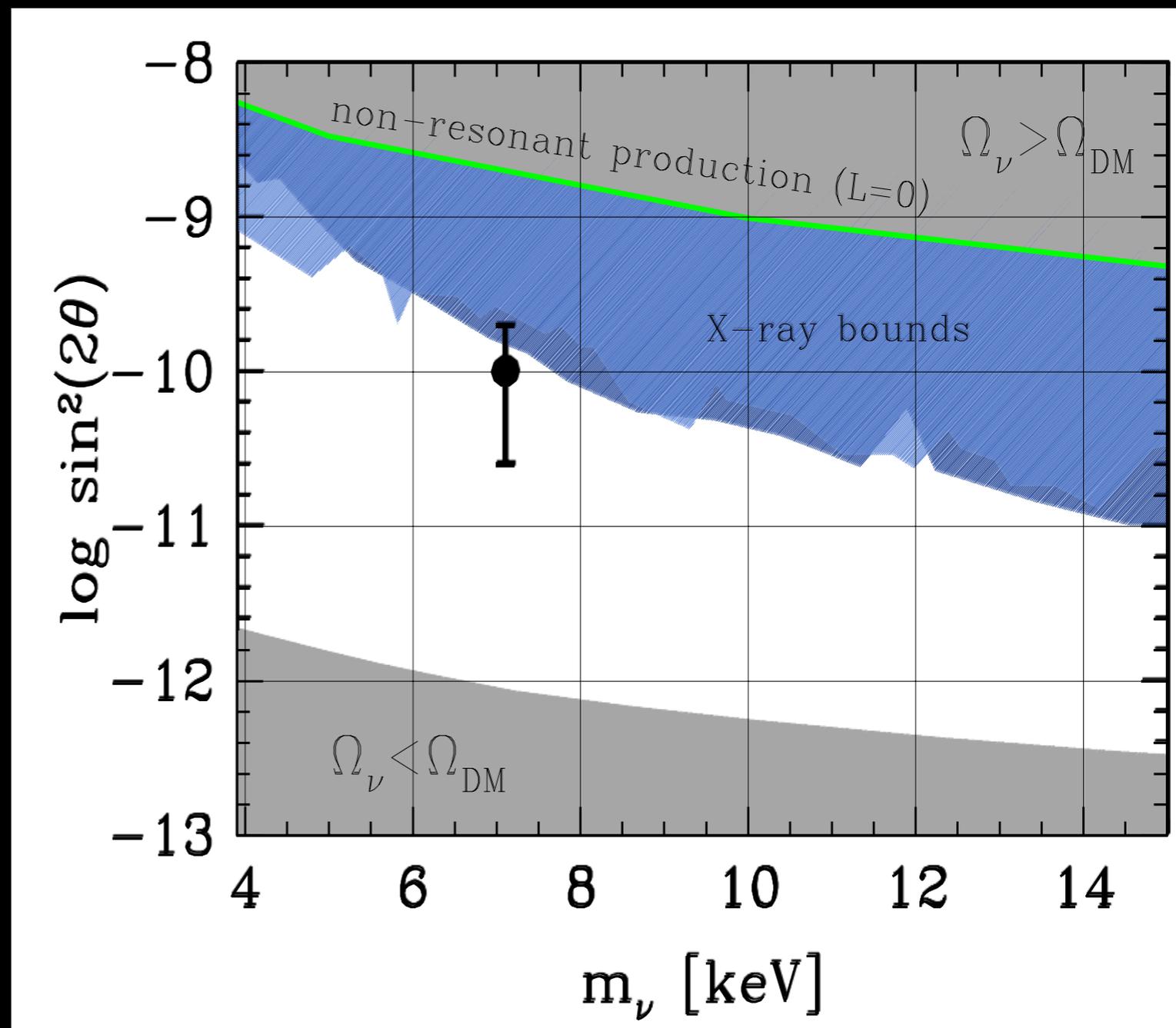


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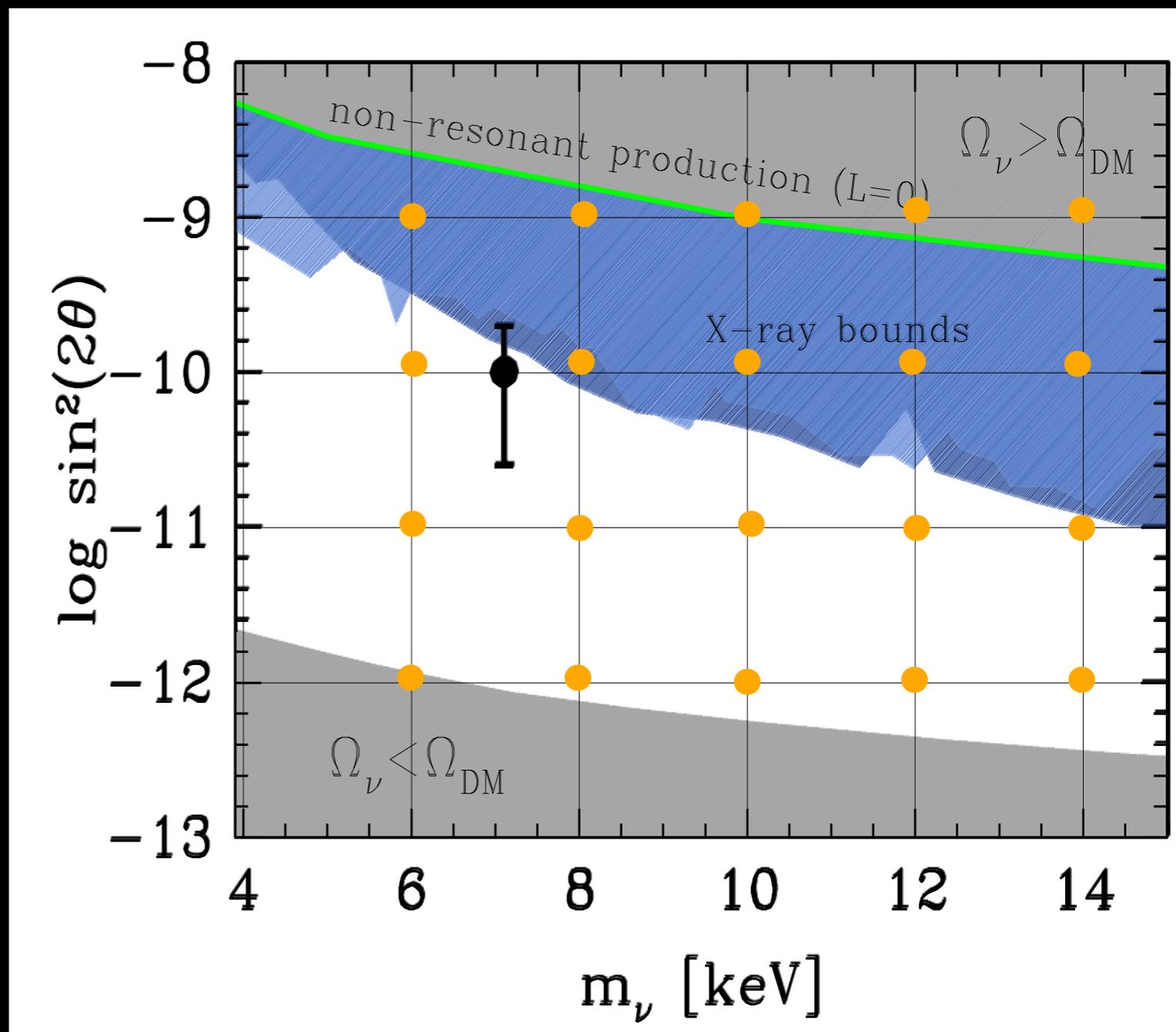
For each point in the grid of parameter space

Compute Power Spectrum  $P(k)$   
(solve Boltzmann equation)

Compute  $\bar{\phi}$

Compare with HFF number density of galaxies at  $z=6$   $\bar{\phi} \geq \phi_{obs}$

Allowed region:



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Grid of Values for  $m_\nu$  and  $\sin^2(2\theta)$

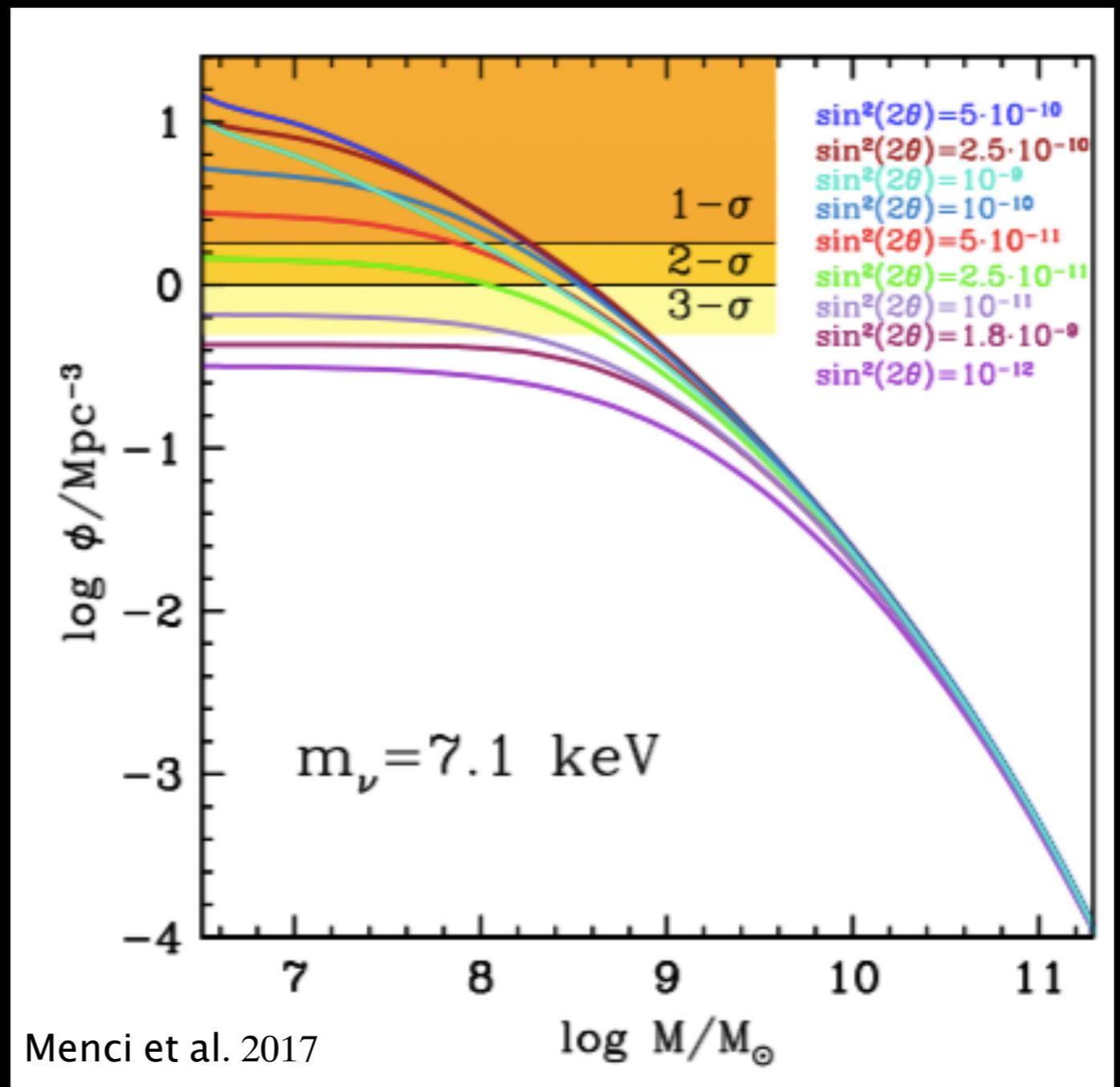
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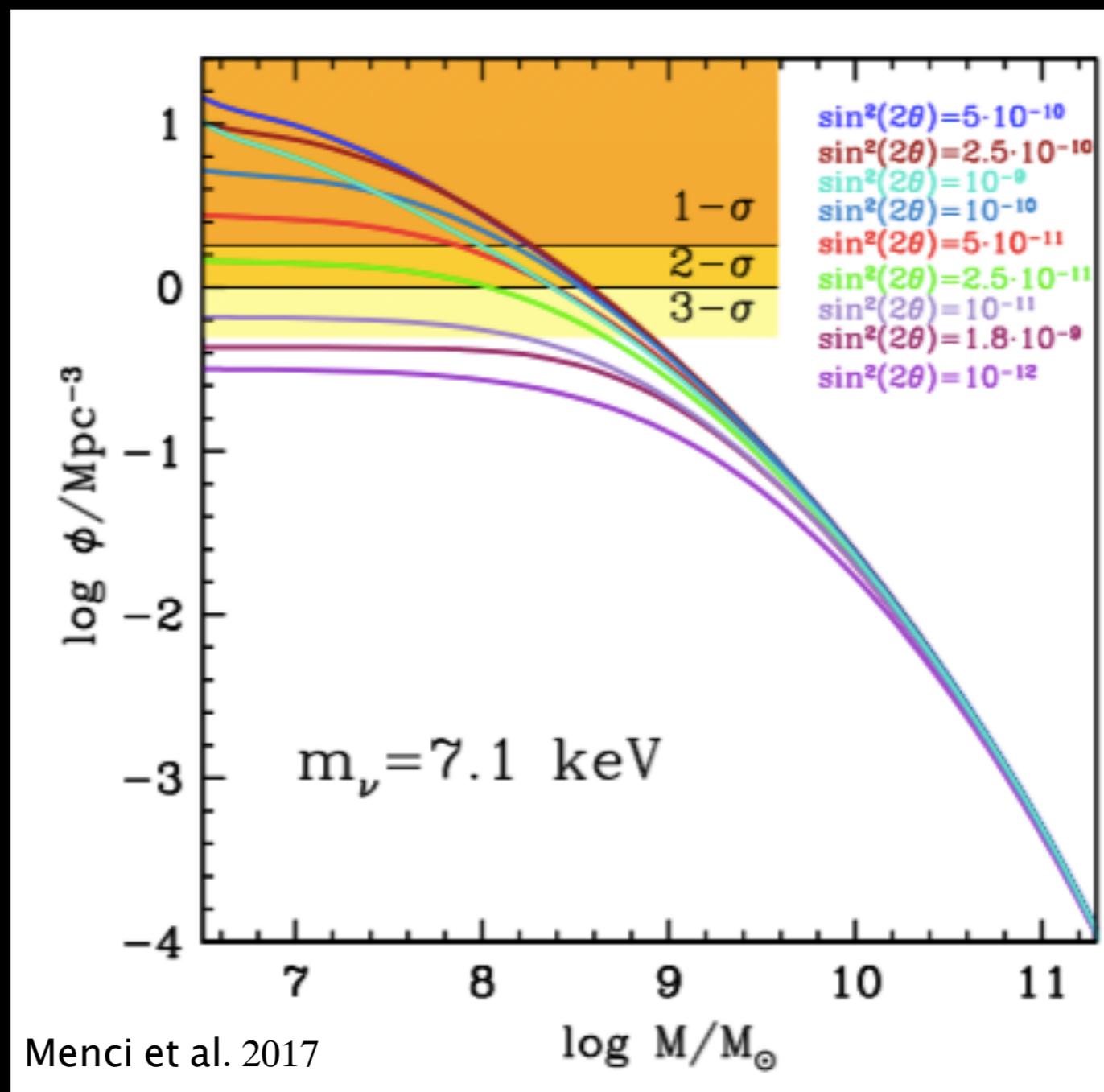
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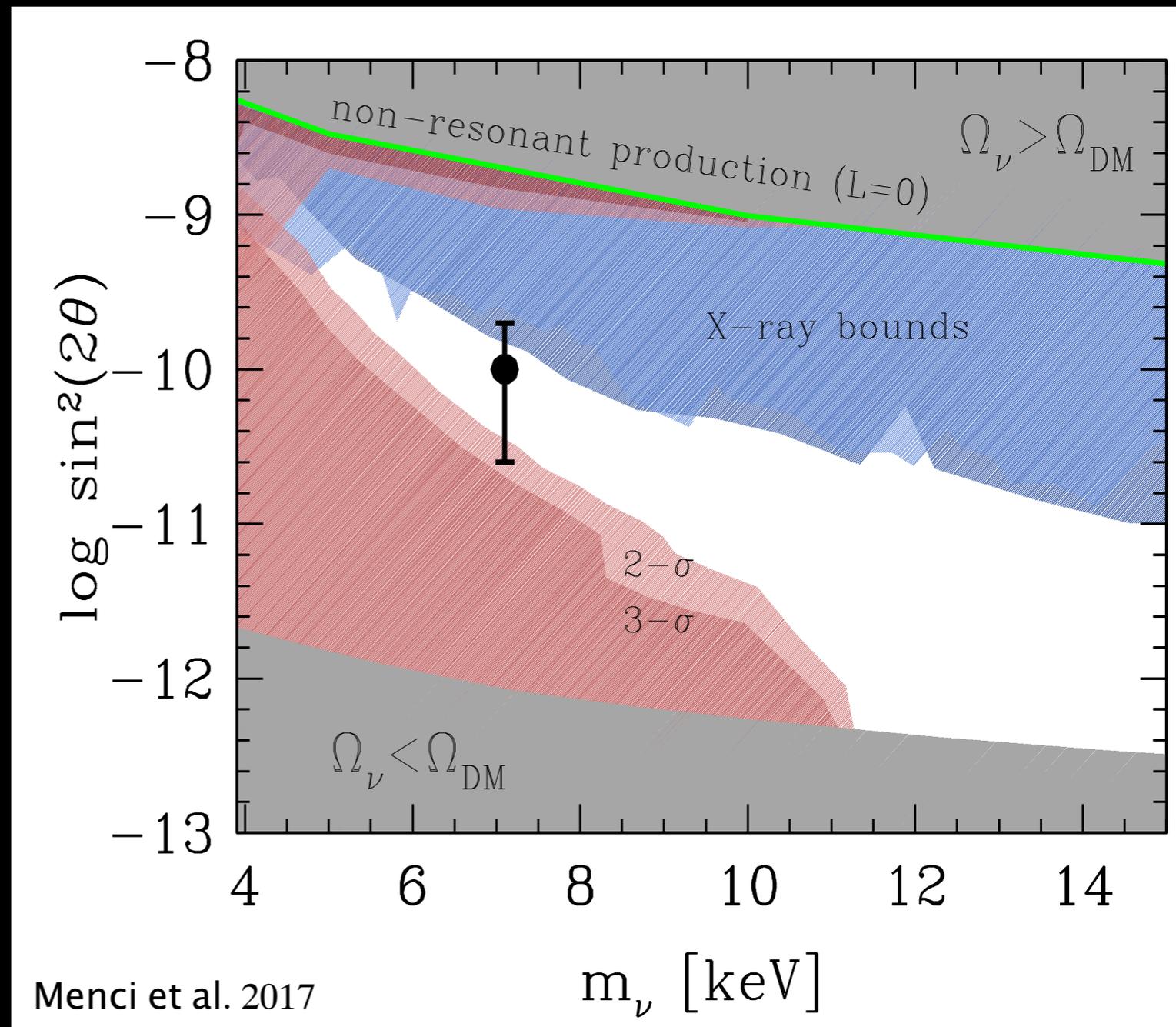
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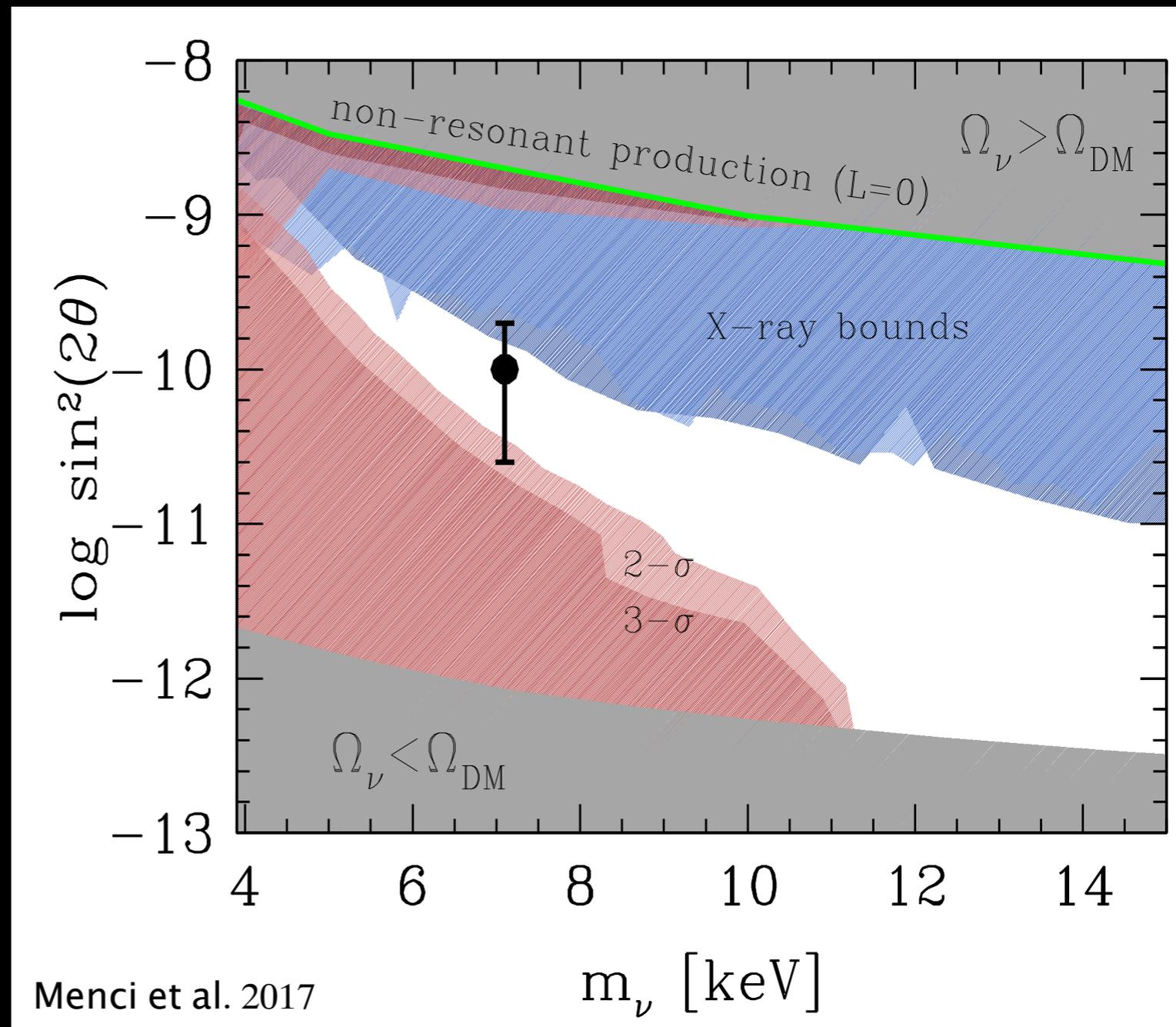
Sets lower bounds for mixing angle which are Independent of baryon physics (L/M ratio) and of the assumed density profile.

Unprecedented constraints on parameter space of such models

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Exploring the Parameter Space of Sterile Neutrino Models based on resonant production

Schneider et al. 2016

Lovell et al. 2015

Limits from Milky Way satellites:

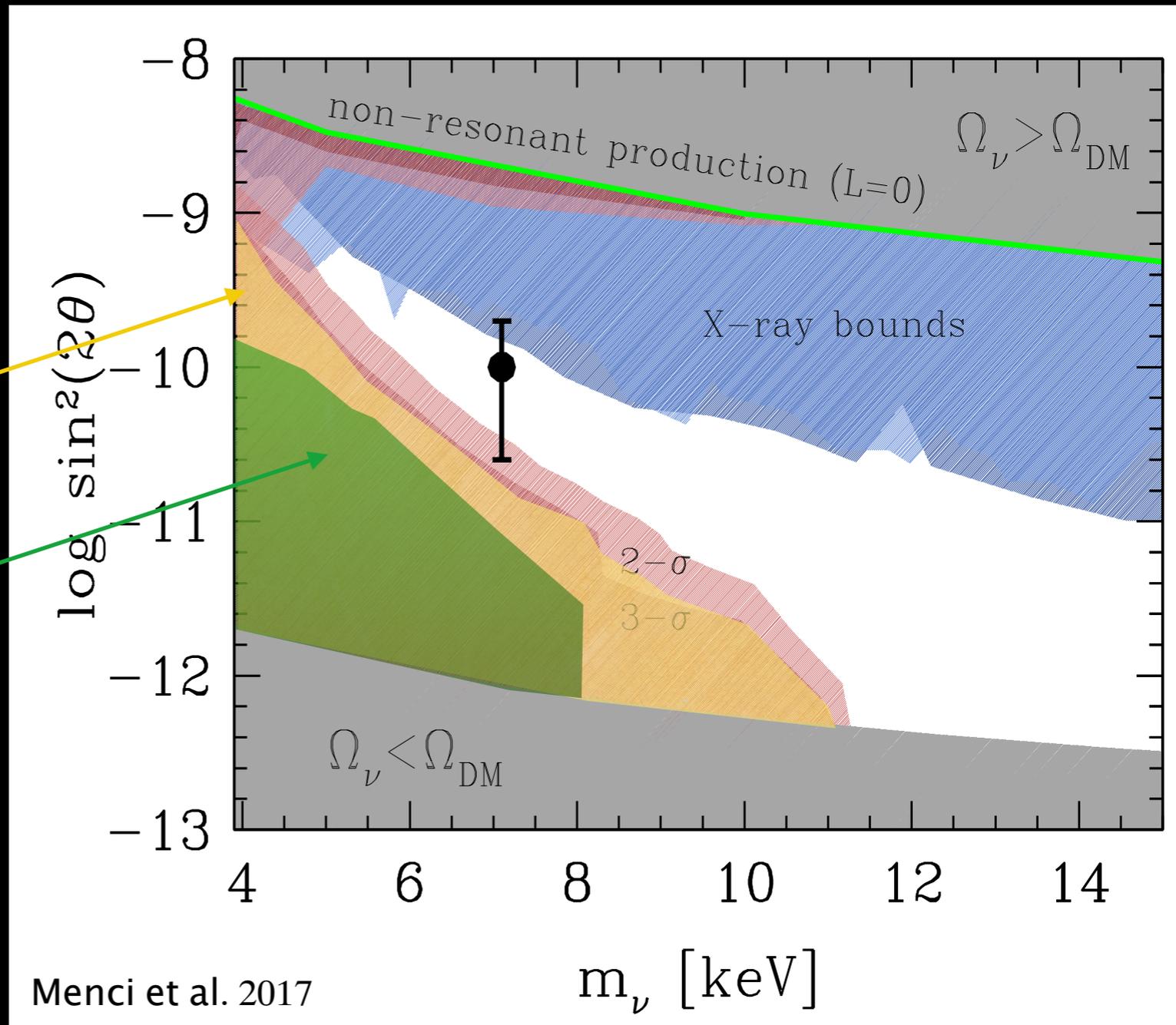
Depend on

assumed upper limit for MW mass

assumed lower limit for satellite masses (based on estimated L/M ratio or stellar velocity dispersion depending on assumed density profile)

assumed isotropic distribution to correct SDSS observations for limited sky coverage

assumed halo-to-halo variance

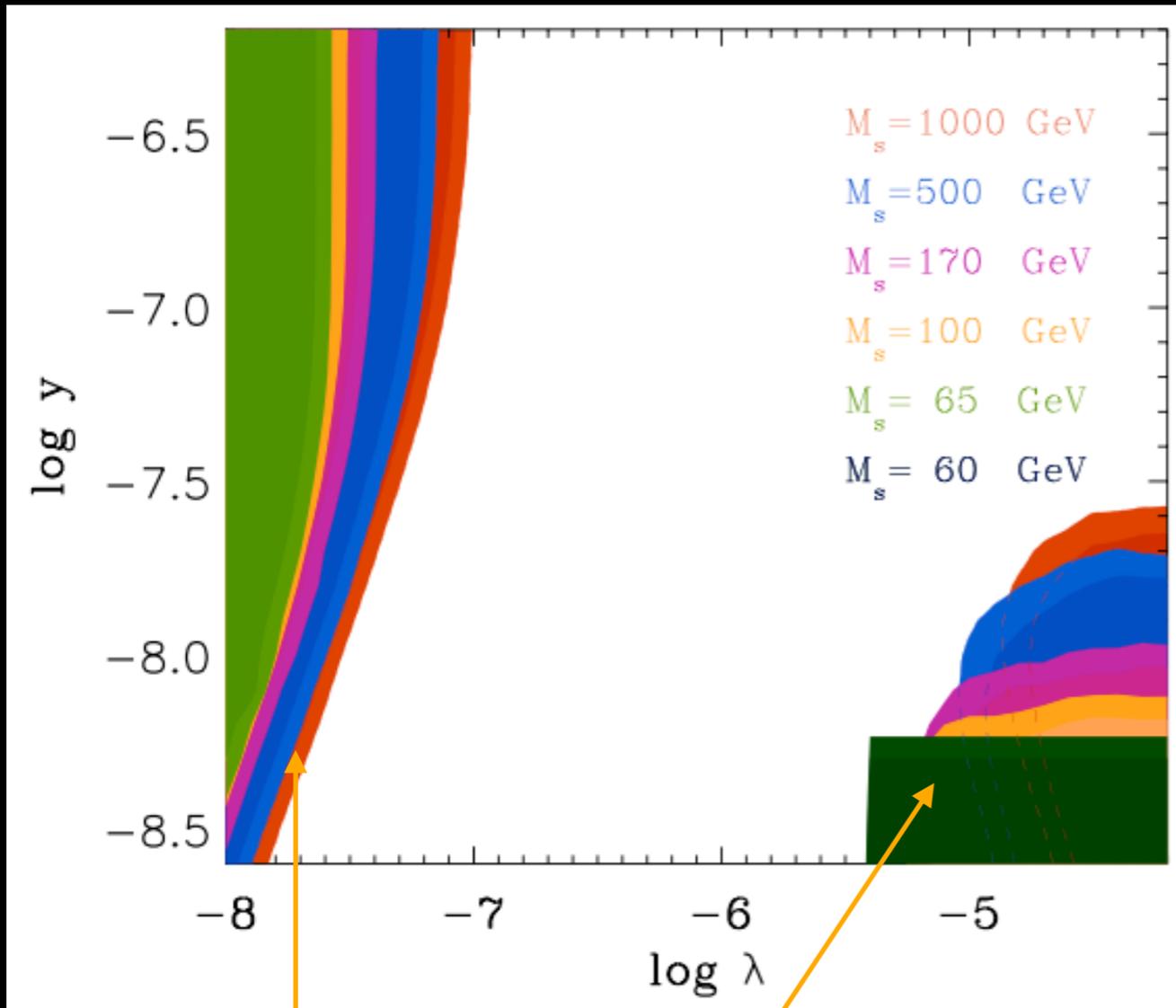


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Unprecedented constraints on parameter space of such models

# Sterile neutrinos from scalar decay (Merle et al. 2013)

Exploring the full parameter space of Sterile Neutrino Models based on scalar decay



3 parameters

$m_s$  mass of scalar  
 $y$  coupling to scalar field  
 $\lambda$  coupling to Higgs

## Special Cases

Small Higgs coupling  $\lambda \ll 10^{-6}$

S is gradually produced, and sterile neutrino production follows.

Freeze-in limit. Model depend only on  $y$

Strong Higgs coupling

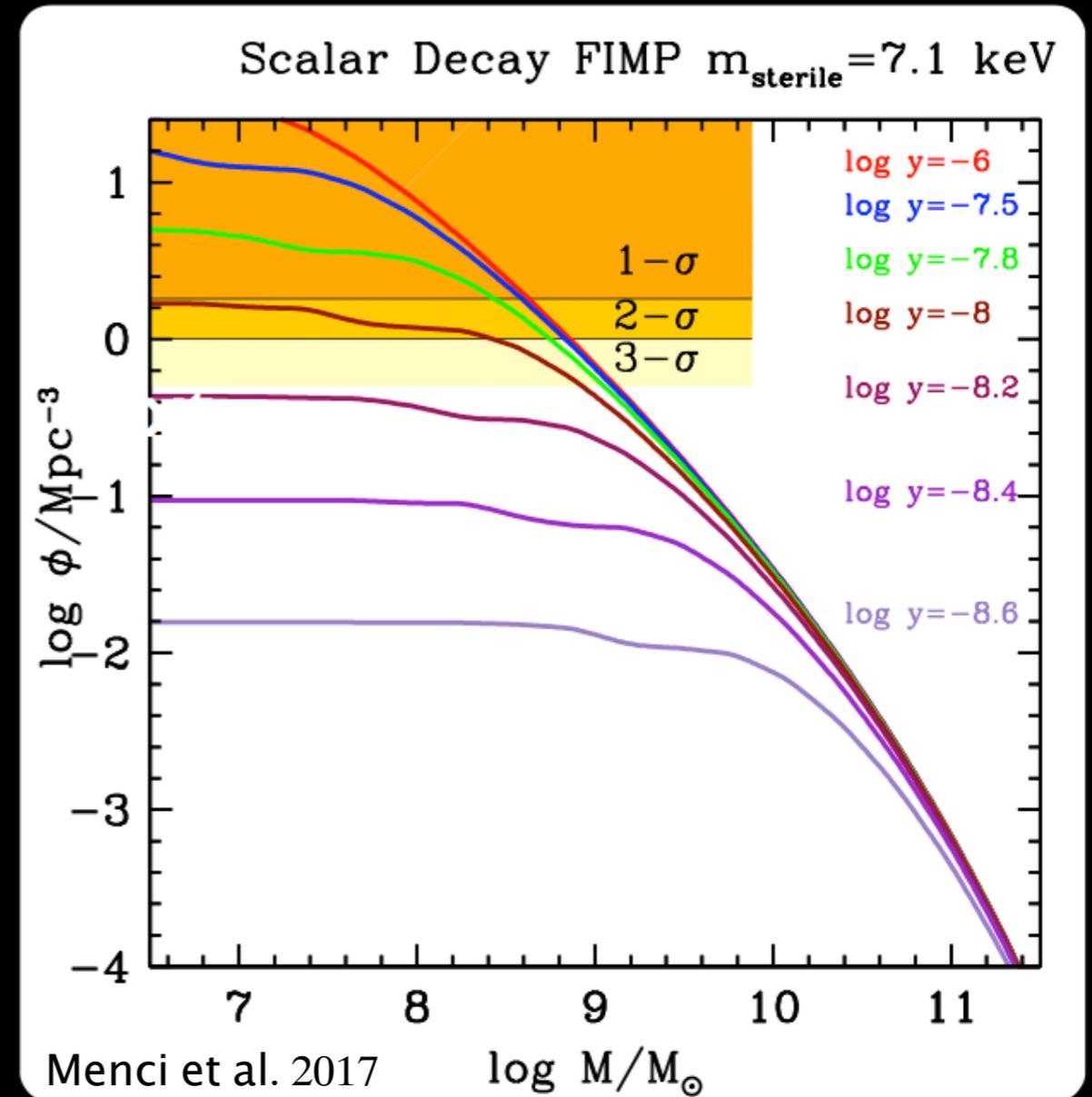
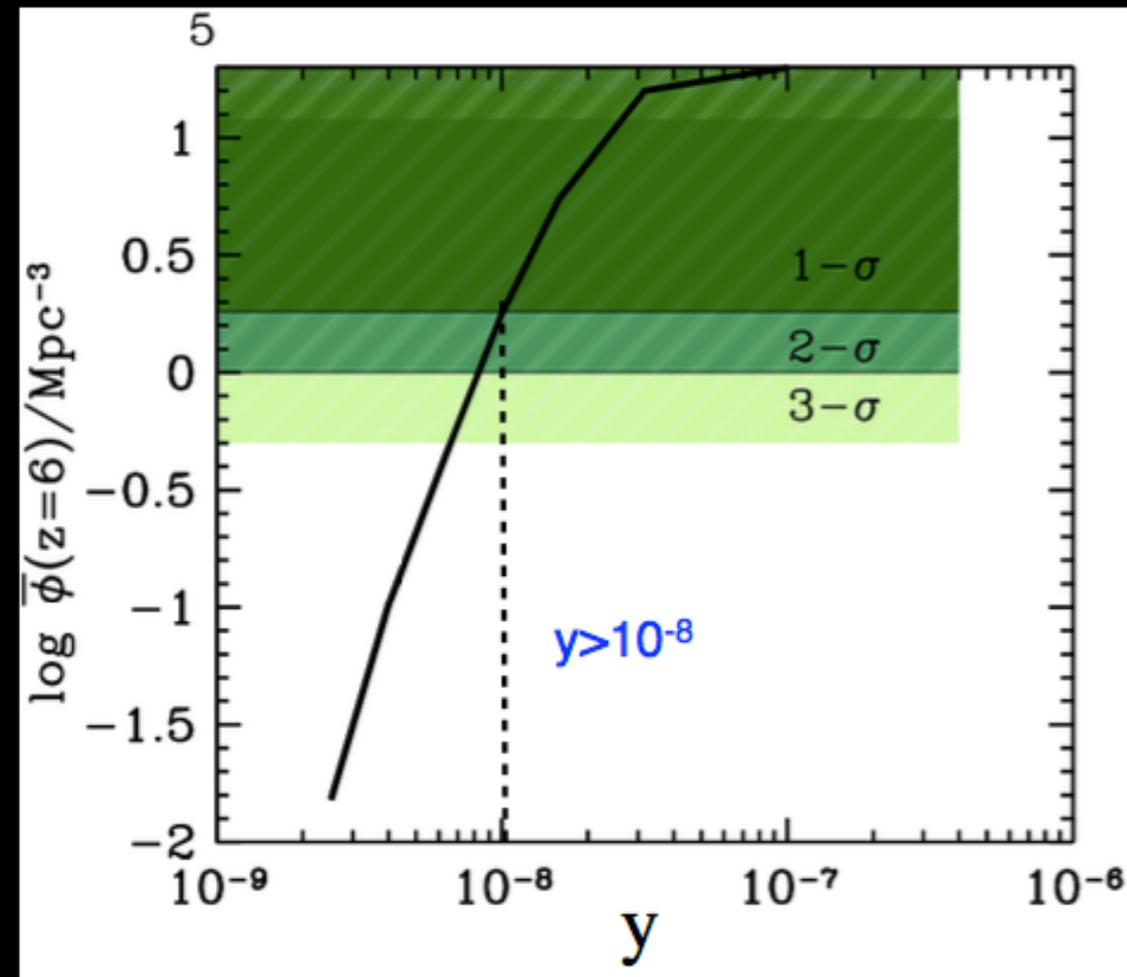
S is abundantly produced at early times. Fast sterile neutrino production follows until freeze-out

Freeze-out limit

# Sterile neutrinos from scalar decay (Merle et al. 2013)

Scalar field  $S$  coupled to the right-handed neutrino. The most general coupling is a Yukawa term with coupling strength  $y$

$y > 10^{-8}$  at 2- $\sigma$  level for  $m_{\text{sterile}} = 7$  keV



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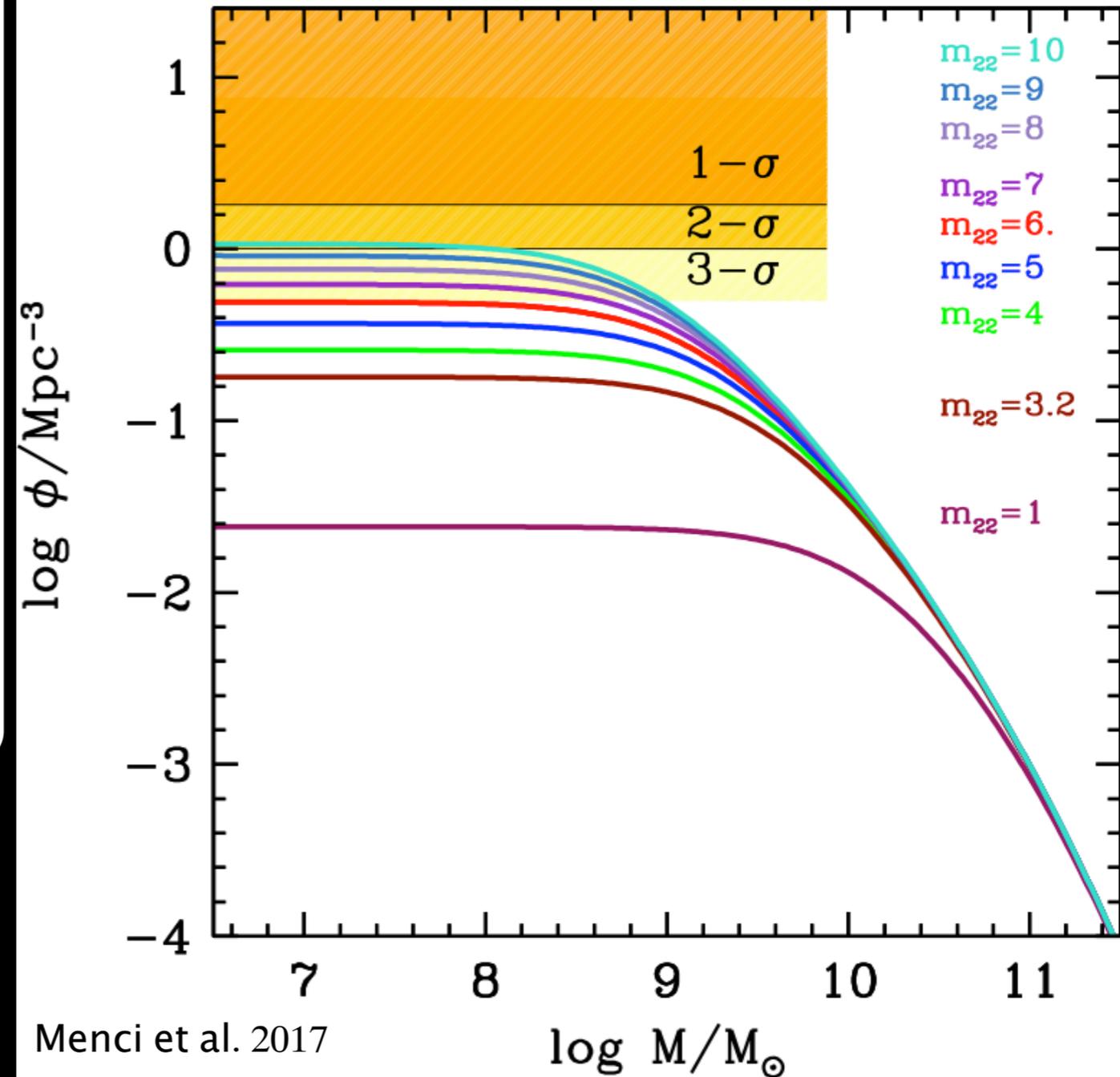
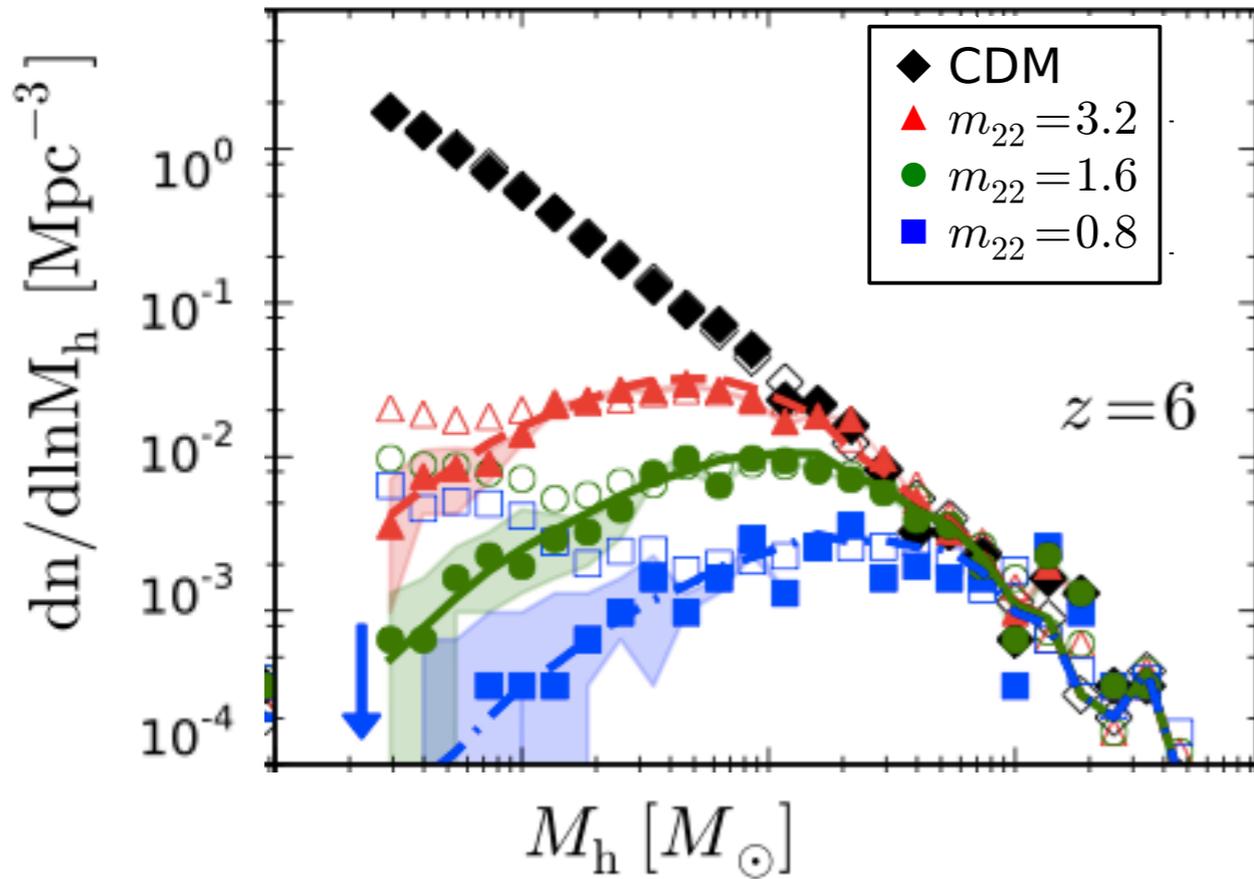
$$\mathcal{L} \supset -\frac{y}{2} S \bar{N}^c N, \quad \lambda \ll 10^{-6} \quad \text{Small Higgs coupling}$$

# Wave DM - Fuzzy Dm: Bose condensate of ultra-light axion $m_\chi \sim 10^{-22}$ eV. Such class of models is ruled out

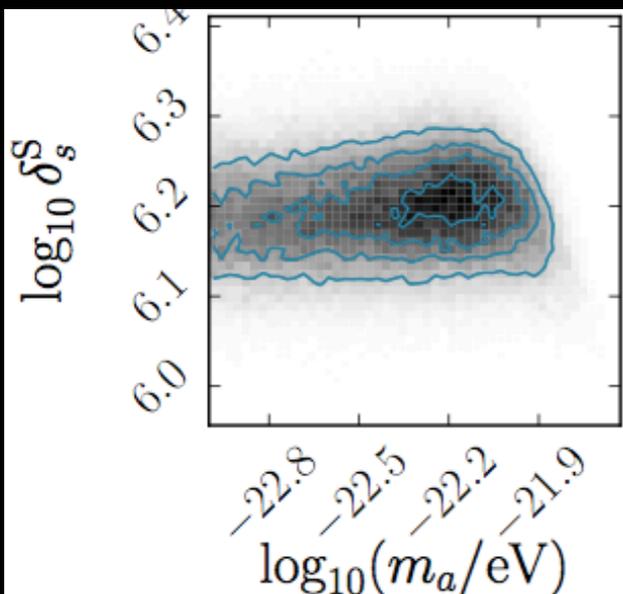
matching observed abundance of  $z=6$  galaxies requires  $m_{22} > 10$

Matching the dwarf profiles requires  $m_{22} < 1.2$

Schive et al. 2016



Menci et al. 2017



Marsch et al. 2015

# Conclusions

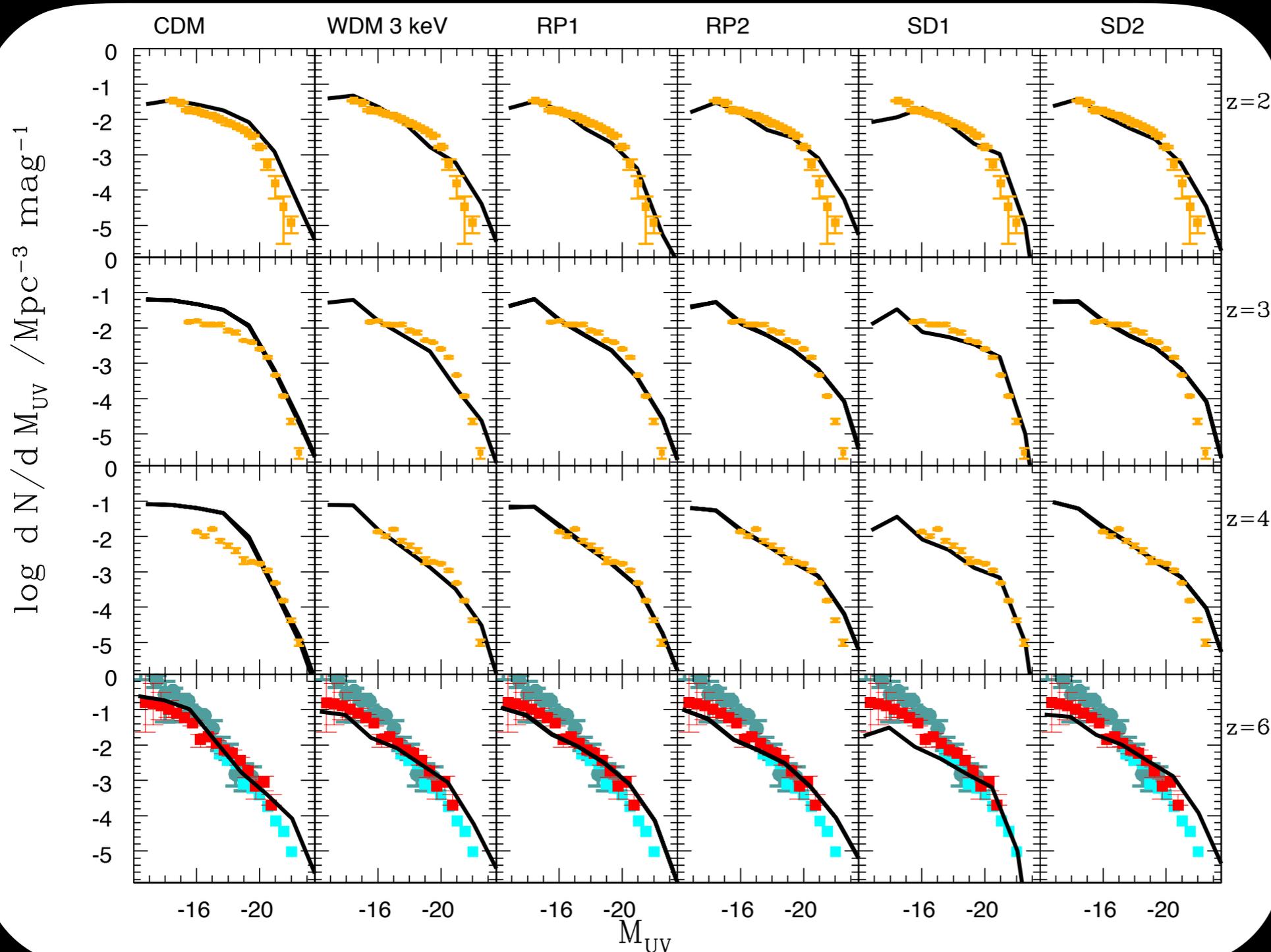
The abundance of faint galaxies at  $z=5-7$  down to  $MUV=-12.5$  yields strong constraints on DM models with suppressed power spectra.

Strongest constraints derived so far independently of baryon physics

- **Thermal Relics:**
  - $m_{\chi} > 2$  keV (abundances in Bouwens et al. 2017) at  $2-\sigma$  level
  - $m_{\chi} > 2.4$  keV (abundances in Livermore et al. 2017) at  $2-\sigma$  level
- **Sterile neutrinos**
  - **Produced through Shi-Fuller mechanism** (resonant production):
    - unprecedented lower limits for  $\sin^2(2\theta)$  as a function of  $m_{\text{sterile}}$ .
    - E.g., for  $m_{\text{sterile}}=7$  keV we obtain  $-10.4 < \log \sin^2(2\theta) < -9.8$  at  $2-\sigma$  level
  - **Produced through scalar decay** (for small Higgs portal coupling)
    - $y > 10^{-8}$  at  $2-\sigma$  level
- **Fuzzy DM** (condensate of ultra-light axions) are ruled out:  $m_{\chi} > 10^{-21}$  eV  
 $2-\sigma$  level

Constraints from maximum abundance of DM halos are **MODEL INDEPENDENT** but **VERY CONSERVATIVE**. The observed galaxies cannot outnumber their host DM halo,

If baryon physics is included in the models (e.g. through SAM models) the predicted abundance of luminous galaxies can provide tighter constraints



UV LF computed from the Rome Semi-analytic model

Feedback tuned so as to match the local stellar mass and the local LFs.

CDM  
3 keV thermal model

4 sterile neutrino models  
Consistent with the tentative 3.5 keV line  
(2 based on resonant production, 2 based on scalar decay)

Observed abundance by Livermore disfavour all WDM and sterile N models.

Scalar decay models are Disfavoured by existing Measurements



# The Nature of DM determines the shape of the power spectrum $P(k)$

CDM: Large power in at small scales yields

Guo et al. 2011

- huge amount of small-scale structures Papastergis et al. 2011
- huge amount of sub-structure Kravtsov, Klypin, Gnedin 2004

Predicted abundance of low-mass halos are much larger than the observed abundances of low-luminosity galaxies

$$N(L) = N(M) \left[ \frac{dM}{dL} \right]$$

## A Possible Solution: Baryon Physics

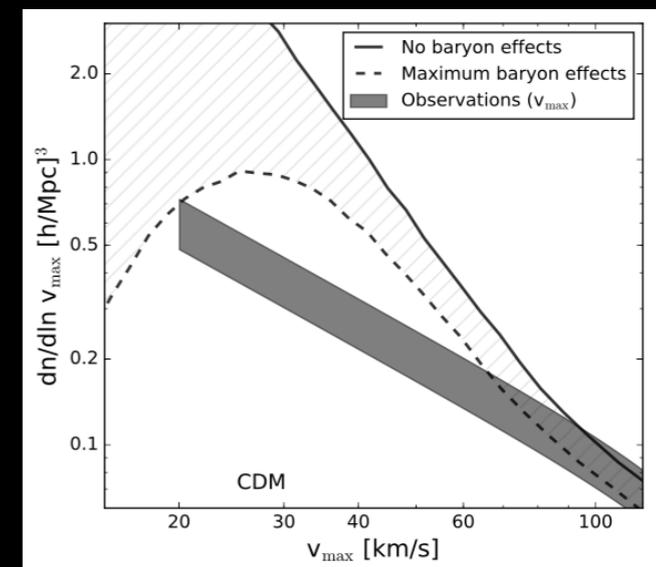
Suppress luminosity (star formation) in low-mass haloes  
Heat - Expell Gas from shallow potential wells

- Enhanced SN feedback
- UV background

Even considering baryonic effects, the comparison with observed abundance of dwarf galaxy is critical

## An Alternative Solution:

The problem is rooted in the power spectrum, i.e., in the assumed DM model: the actual DM Power Spectrum and Mass Function are suppressed with respect to CDM below mass scales  $M \sim 10^8 M_\odot - 10^9 M_\odot$



# Sterile Neutrino WDM Production from Active–Sterile Transitions

## Suppression of Power spectrum with respect to CDM

2 parameters: neutrino mass  $m_\nu$   
mixing with active neutrinos  
(oscillation probability)

Suppression of Power Spectrum is **only approximately** similar to thermal WDM with a rescaled mass

**Approximate** correspondence between thermal relic mass  $m_\chi$  and sterile neutrino mass  $m_\nu$  (yielding the same power spectrum) depends on the assumed production mechanism

E.g. for the Shi-Fuller mechanism  $m_\nu \approx 2.5 m_\chi$

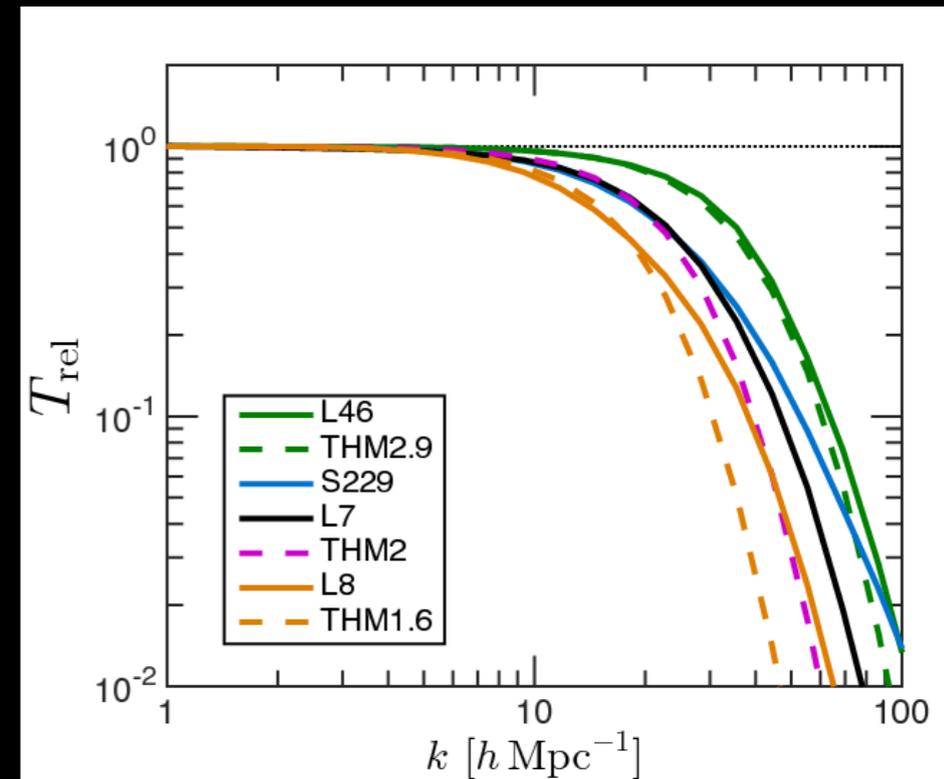
**Deriving Power Spectra in the sterile neutrino case requires complete computations**

For each couple of free parameters  $m_\nu \sin^2(2\theta)$

– Solve the Boltzmann equation to get the momentum distrib.  
[sterile-dm code \(Venumadhav et al. 2016\)](#)

– Compute the Power Spectrum based on obtained  $f(p)$   
[Boltzmann solver CLASS \(Blas et al. 2011; Lesgourgues & Tram 2011\)](#)

## Suppression with respect to CDM



[Bozek et al. 2015](#)

Suppression of the power spectrum of resonantly-produced sterile neutrino models (solid lines) and their best-fit thermal equivalent model (dashed lines) relative to CDM.

The L7 model has an equivalent thermal WDM model of  $m=2$  keV (THM2/dashed; magenta).

The shape and large- $k$  behavior of the WD transfer functions vary among the sterile neutrino models and compared with their thermal equivalent models.

# Sterile Neutrino WDM

# Right-handed neutrino

**Strong physical motivation:** the most natural extension of SM to include mass terms for active neutrinos requires SNs

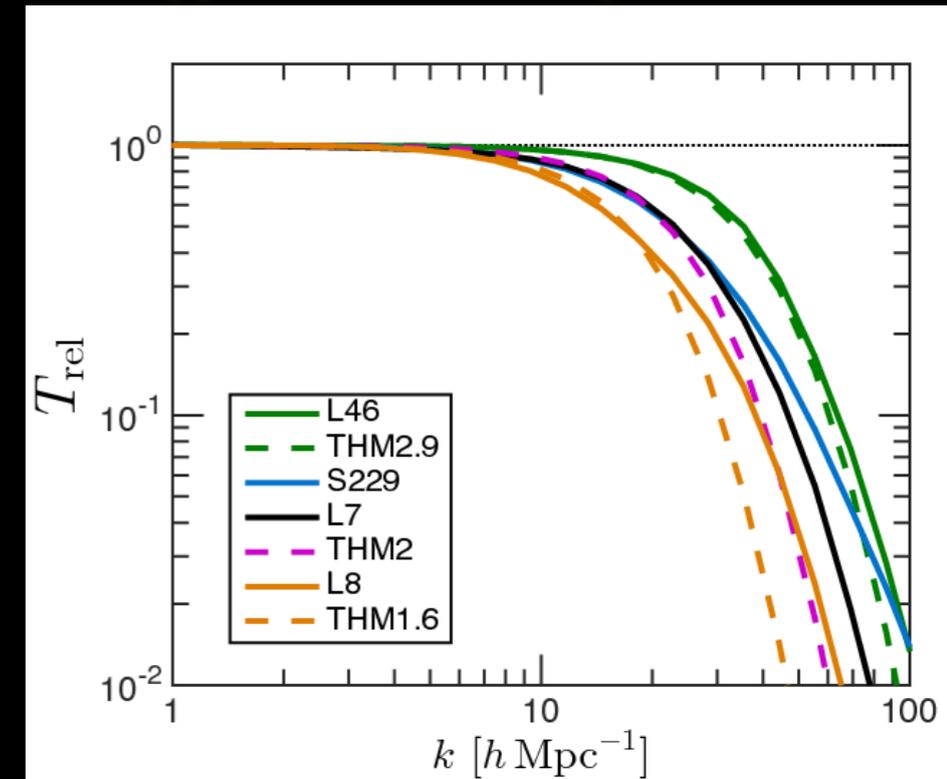
$$\mathcal{L}_{\text{Yuk}} = h_d \bar{Q}_L d_R \Phi + h_u \bar{Q}_L u_R \tilde{\Phi} + h_e \bar{\ell}_L e_R \Phi + \text{H.c.}$$

If **right-handed neutrinos** exist, neutrinos get a mass through a Yukawa term  $h_\nu \bar{\ell}_L \nu_R \tilde{\Phi} \Rightarrow m_D = h_\nu v$ .

$$\ell_L = \begin{pmatrix} \nu_L \\ e_L \end{pmatrix}$$

2 parameters: neutrino mass  $m_\nu$   
 mixing with active neutrinos  $\sin^2(2\theta)$   
 (oscillation probability)

Suppression with respect to CDM



are produced in primordial plasma through

- oscillations with null lepton asymmetry  $L=0$   
 Dodelson, Widrow; Abazajian, Fuller; Dolgov, Hansen; Asaka, Laine, Shaposhnikov et al.
- oscillations on resonance with lepton asymmetry  
 Shi Fuller, Laine Shaposhnikov
- Decay of a scalar field  
 Merle 2015
- production mechanisms which do not involve oscillations
  - inflaton decays directly into sterile neutrinos Shaposhnikov, Tkachev
  - Higgs physics: both mass and production AK, Petraki

- 1 parameter  $m_\nu$   
 $m_\nu \sin^2(2\theta)$  are related to produce the correct abundance
- 2 parameters  $m_\nu \sin^2(2\theta)$   
 $\sin^2(2\theta)$  and lepton asymmetry are related to produce the correct abundance
- 3 parameters  
 $m_S$   
 $y$   
 $\lambda$   
 mass of scalar  
 coupling to scalar field  
 coupling to Higgs

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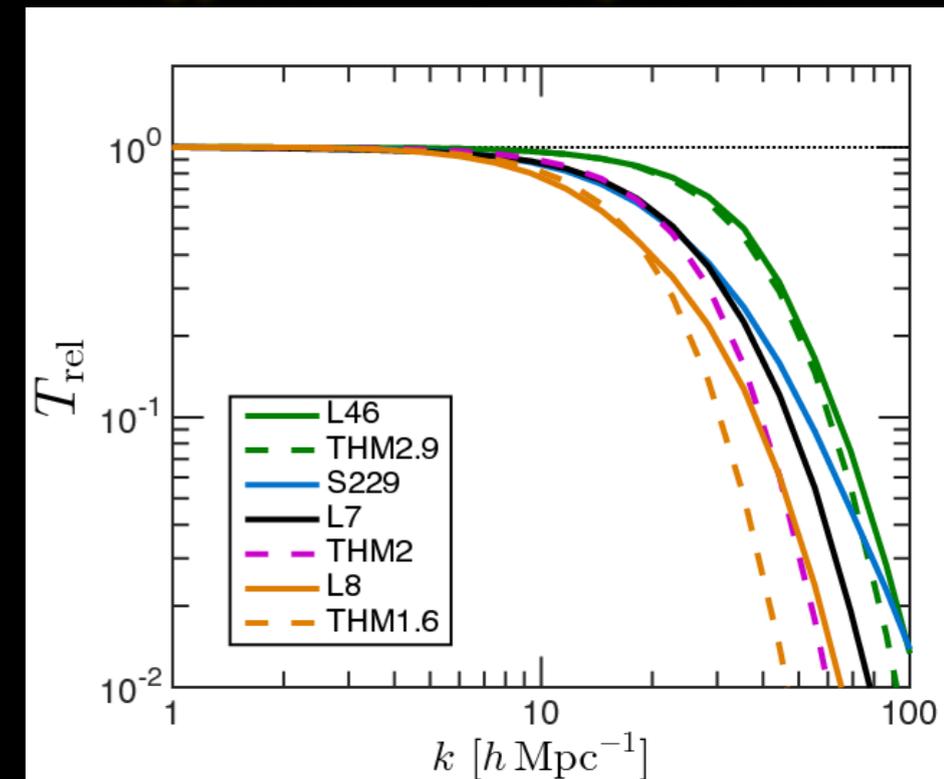
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