

# Flavor hierarchies from dynamical scales

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based on GP and A. Pomarol 1603.06609

GP, M. Riembau and T. Vantalón 1712.06337

# The SM and BSM flavor puzzle

The SM has a **peculiar flavor structure**: where does it come from?

... so far several ideas, but no compelling scenario

Moreover strong theoretical considerations (naturalness problem) suggest the necessity of **new physics** related to the EW scale

big effects are typically expected in **flavor physics** and **CP violation**  
(sensitive to energy scales much higher than TeV)

... but basically **no deviations** seen experimentally!

How can we explain this?

# The SM and BSM flavor puzzle

## Popular solutions:

- ◆ Very high BSM scale  $\sim 10^3$  TeV  $\rightarrow$  give up on naturalness
- ◆ BSM flavor structure similar to SM:
  - flavor symmetries
  - CP invariance

# The SM and BSM flavor puzzle

## Popular solutions:

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  - flavor symmetries
  - CP invariance

**This seems a step back from SM!**

in the SM global symmetries are **accidental!**

*“[symmetries] are not fundamental at all, but they are just accidents, approximate consequences of deeper principles.”*

*S. Weinberg, referring to isospin  
in “Symmetry: ‘A ‘Key to Nature’s Secrets’”*

# Looking for a dynamical flavor structure

Is it possible to obtain the **flavor structure**  
as an **emergent feature**?

In this talk I will try to address this question in the context of  
**composite Higgs scenarios**

# **The basic picture**

# Higgs compositeness and flavor

Higgs compositeness forces flavor structure to be explained at “low” energy scales

◆ Higgs associated to a composite operator:

$$\mathcal{O}_H \sim \bar{\psi}\psi \quad \Rightarrow \quad \dim[\mathcal{O}_H] > 1$$

→ Yukawa's  $\bar{f}\mathcal{O}_H f$  are irrelevant couplings reduced by running

Sizable **top** Yukawa can only be generated at **low scale!**

$$\dim[\mathcal{O}_H] \gtrsim 2 \quad \Rightarrow \quad \Lambda_t \lesssim 10 \text{ TeV}$$

# Anarchic partial compositeness

The standard **anarchic partial compositeness** flavor picture:

- ◆ Yukawa's from linear mixing to operators from the strong sector

$$\mathcal{L}_{lin} \sim \varepsilon_i \bar{f}_i \mathcal{O}_{f_i}$$

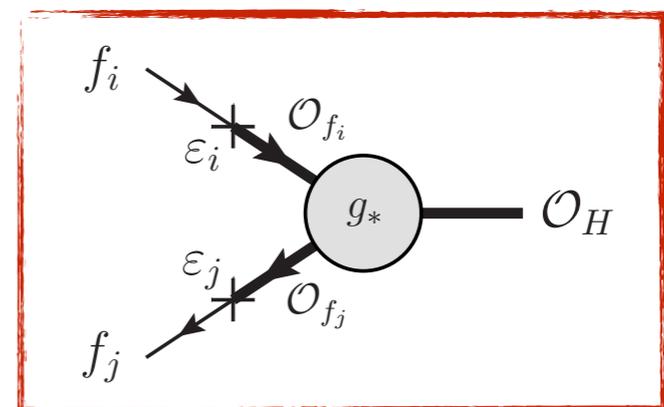
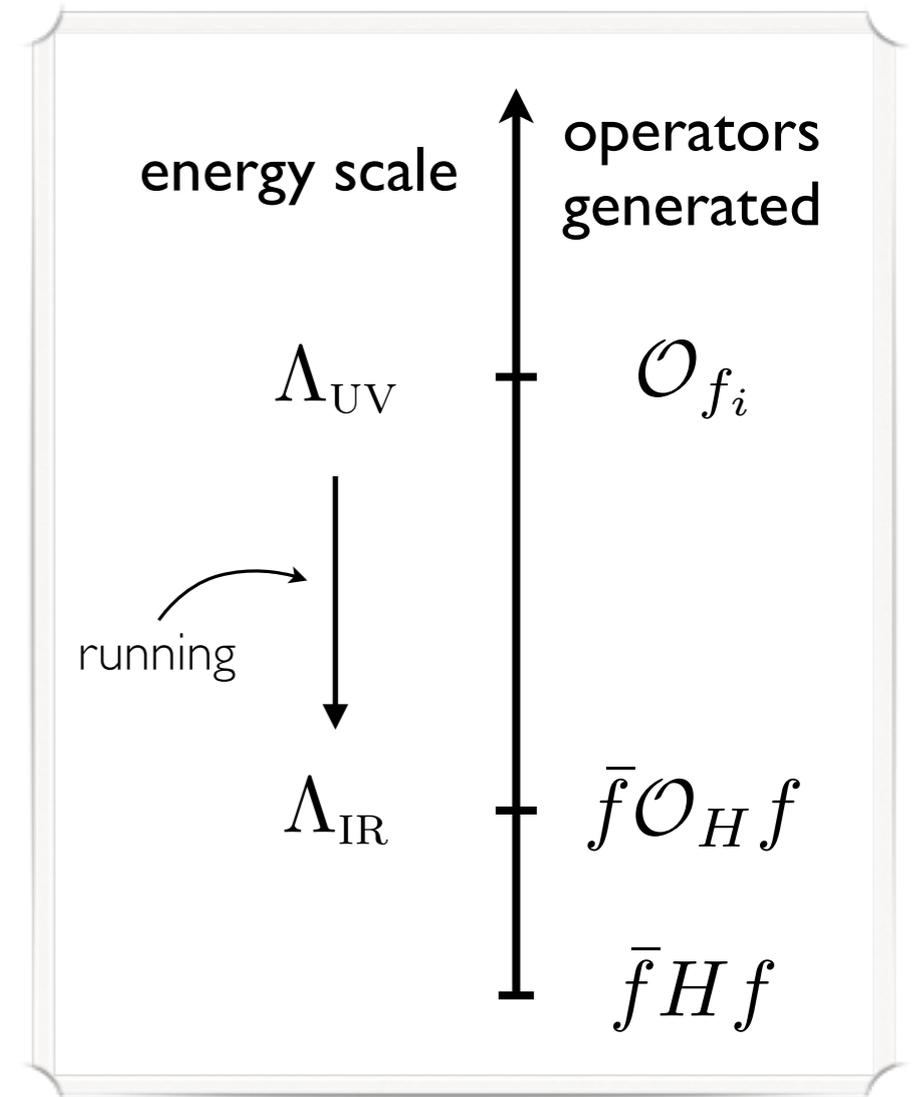
- ◆ size of IR mixings related to  $dim[\mathcal{O}_{f_i}]$

$$\varepsilon_{f_i}(\Lambda_{IR}) \sim \left( \frac{\Lambda_{IR}}{\Lambda_{UV}} \right)^{dim[\mathcal{O}_{f_i}] - 5/2}$$

→ smaller mixings give smaller Yukawa's

$$\mathcal{Y}_f \sim g_* \varepsilon_{f_i} \varepsilon_{f_j}$$

strong sector coupling

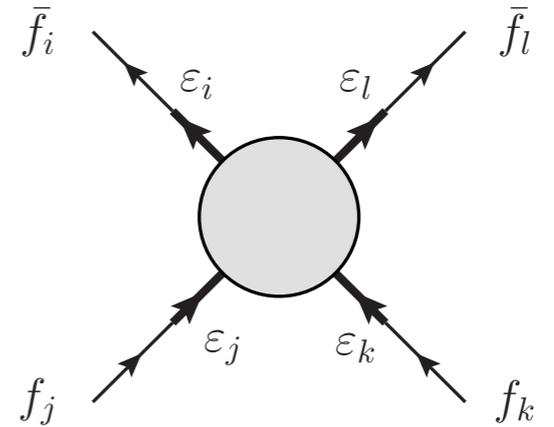


# Flavor and CP-violation constraints

Strong bounds from  $\Delta F = 2$  transitions

$$\mathcal{O}_{\Delta F=2} \sim \frac{g_*^2}{\Lambda_{\text{IR}}^2} \varepsilon_i \varepsilon_j \varepsilon_k \varepsilon_l \bar{f}_i \gamma^\mu f_j \bar{f}_k \gamma_\mu f_l$$

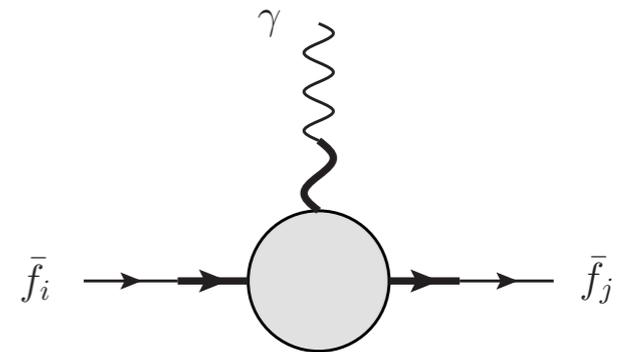
- ♦ bound from  $\varepsilon_K$ :  $\Lambda_{\text{IR}} \gtrsim 10 \text{ TeV}$



... and especially from **CP-violation** and **lepton flavor violation**

$$\mathcal{O}_{dipole} \sim \frac{g_*}{16\pi^2} \frac{g_* v}{\Lambda_{\text{IR}}^2} \varepsilon_i \varepsilon_j \bar{f}_i \sigma_{\mu\nu} f_j g F^{\mu\nu}$$

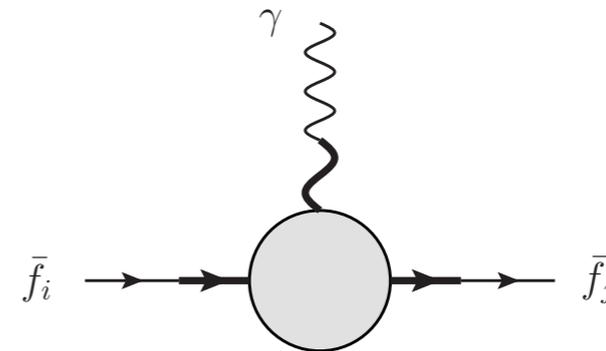
- ♦ bound from  $n$  EDM:  $\Lambda_{\text{IR}} \gtrsim 10 \text{ TeV}(g_*/3)$
- ♦ bound from  $e$  EDM:  $\Lambda_{\text{IR}} \gtrsim 100 \text{ TeV}(g_*/3)$
- ♦ bound from  $\mu \rightarrow e \gamma$ :  $\Lambda_{\text{IR}} \gtrsim 100 \text{ TeV}(g_*/3)$



# How to suppress EDM's

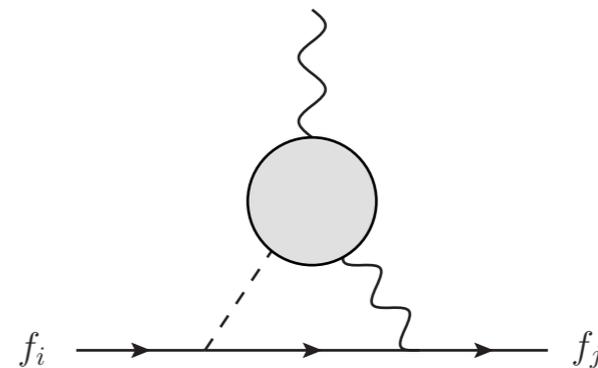
Large EDM's come from linear partial-compositeness mixings of light fermions

$$\mathcal{L}_{lin} \sim \varepsilon_i \bar{f}_i \mathcal{O}_{f_i}$$



Significant improvement if mixing through **bilinear operators!**

$$\mathcal{L}_{bilin} \sim \bar{f}_i \mathcal{O}_H f_j$$



- ◆ EDM's generated only at two loops

# An explicit implementation

Portal interaction for light fermions “decouples” at high energy

[GP and A. Pomarol '16]

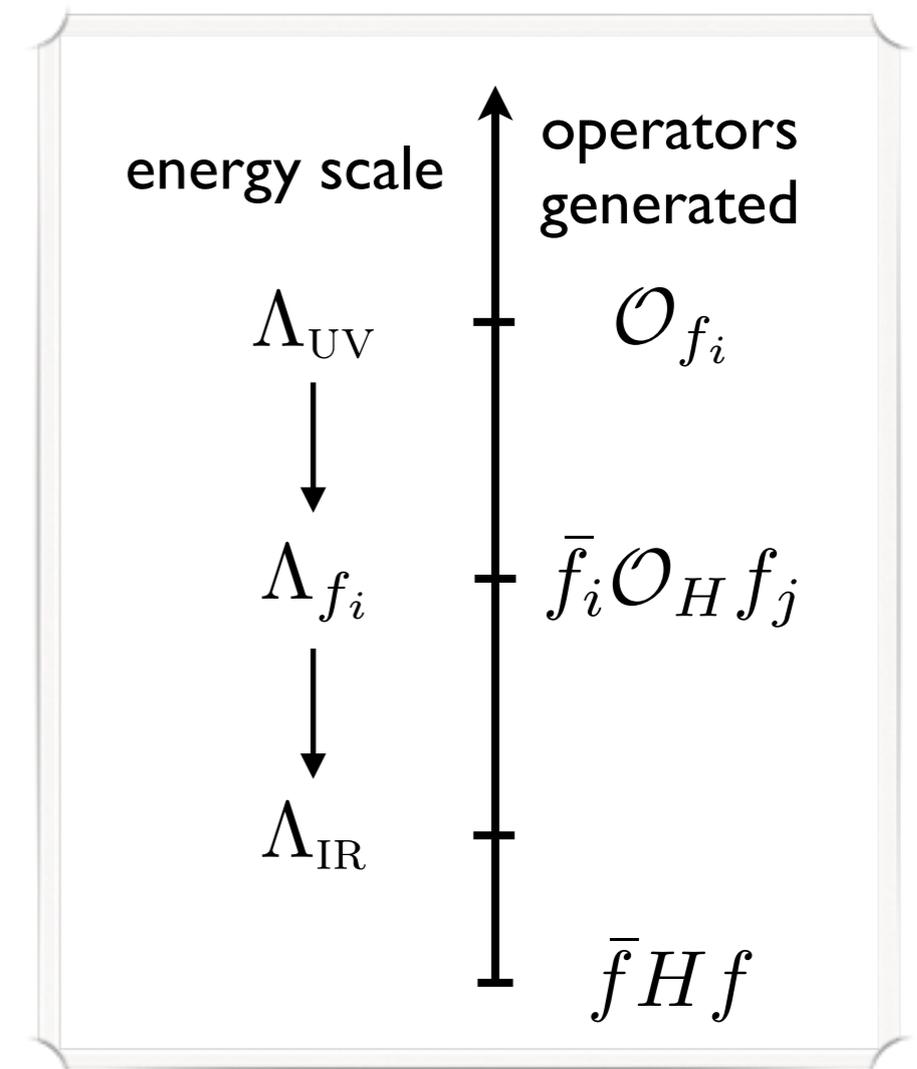
[see also: Vecchi '12; Matsedonskyi '15; Cacciapaglia et al. '15]

$$\mathcal{L}_{lin} \sim \varepsilon_i \bar{f}_i \mathcal{O}_{f_i}$$



Bilinear mixing generated at scale  $\Lambda_f$

$$\mathcal{L}_{bilin} \sim \bar{f}_i \mathcal{O}_H f_j$$

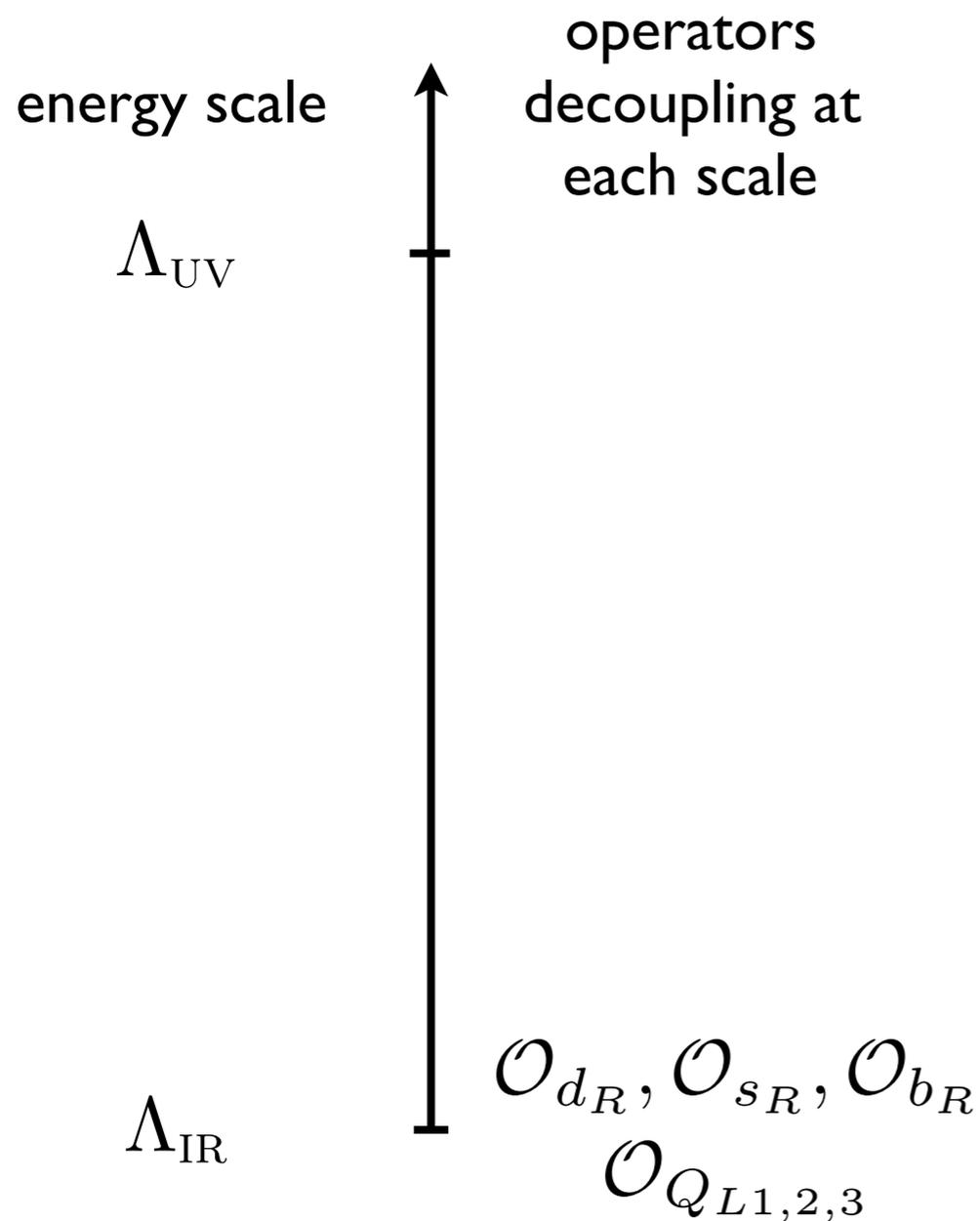


larger **decoupling scales** correspond to smaller fermion **masses**

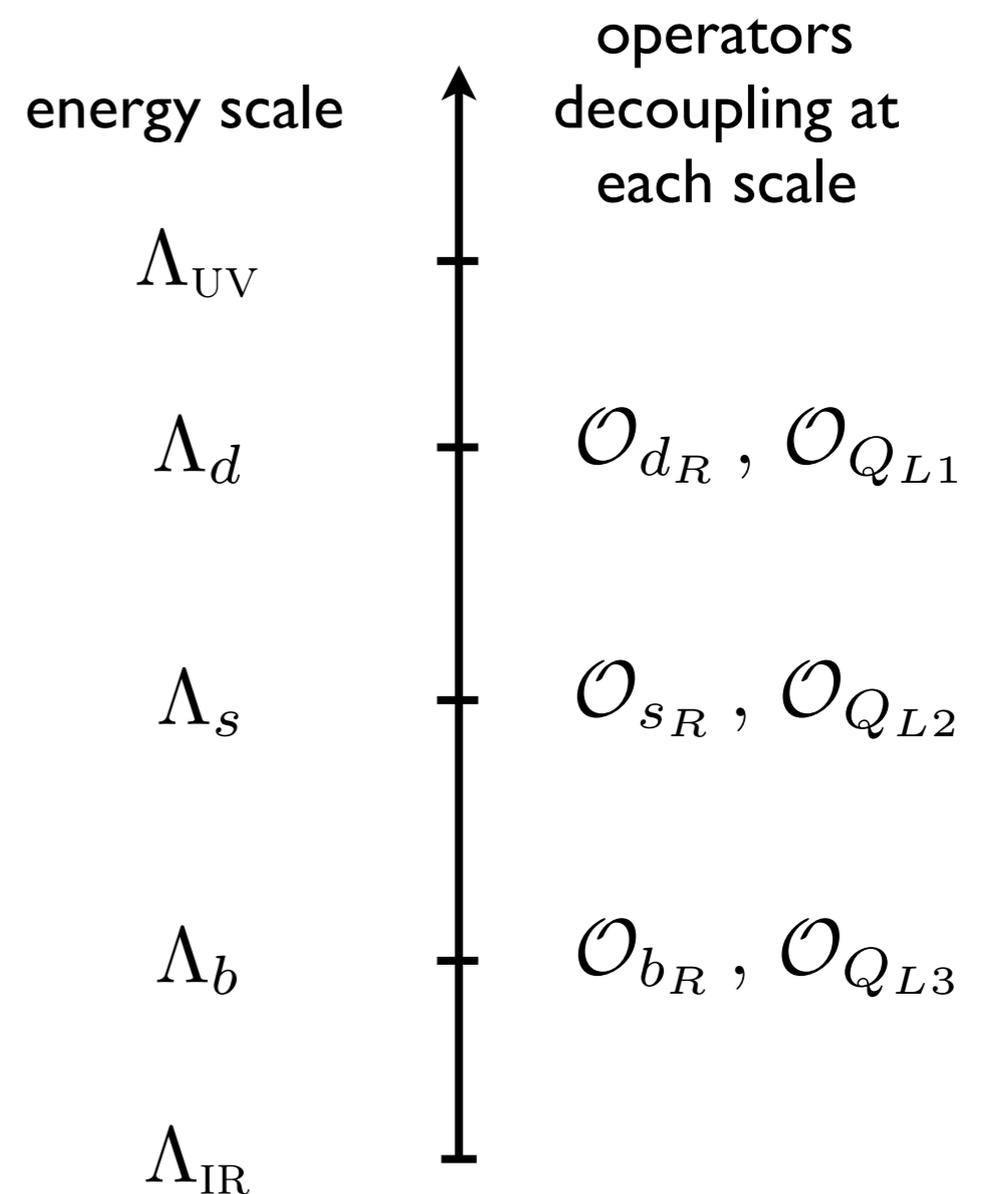
# Anarchic vs Dynamical scales

Explicit example: The down-quark sector

## Anarchic scenario



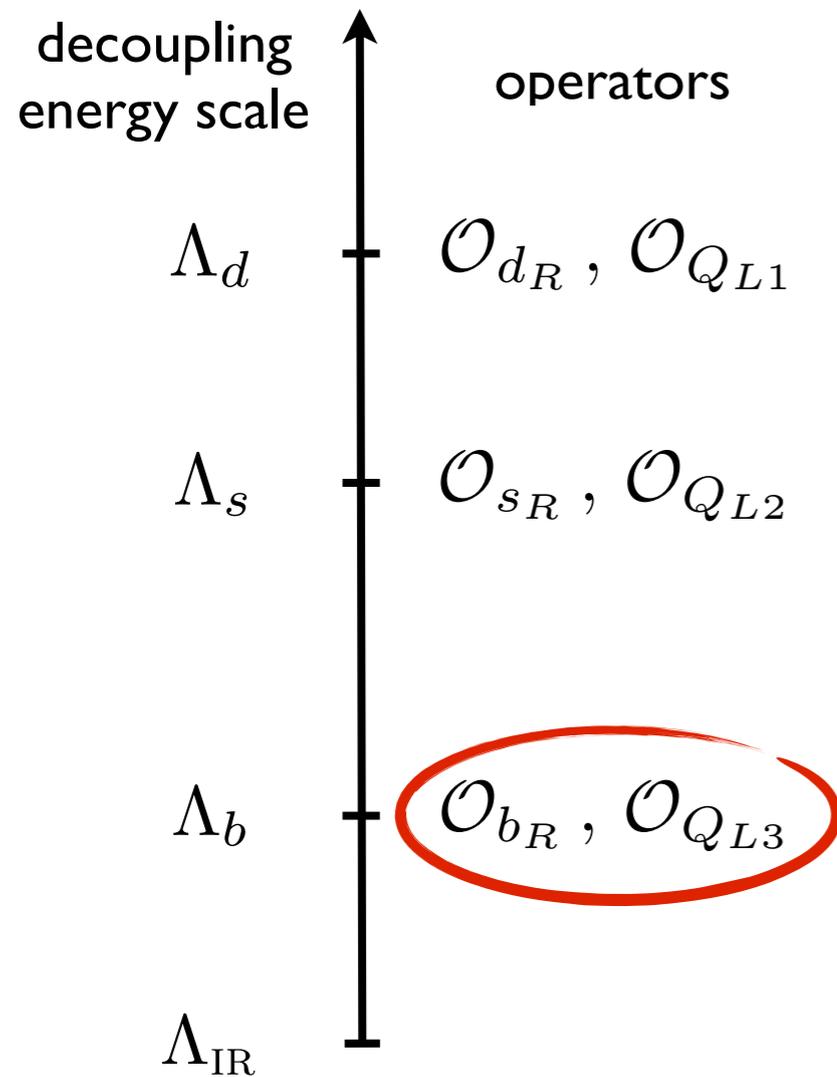
## Dynamical scales



# **The emergent flavor structure**

# The emergent flavor structure

down-quark sector



partial compositeness mixings

$$\mathcal{L}_{lin}^{(3)} = \varepsilon_{b_L}^{(3)} \bar{Q}_{L3} \mathcal{O}_{Q_{L3}} + \varepsilon_{b_R}^{(3)} \bar{b}_R \mathcal{O}_{b_R}$$



below  $\Lambda_b$

$$\mathcal{L}_{bilin}^{(3)} = \frac{1}{\Lambda_b^{d_H-1}} (\varepsilon_{b_L}^{(3)} \bar{Q}_{L3}) \mathcal{O}_H (\varepsilon_{b_R}^{(3)} b_R)$$



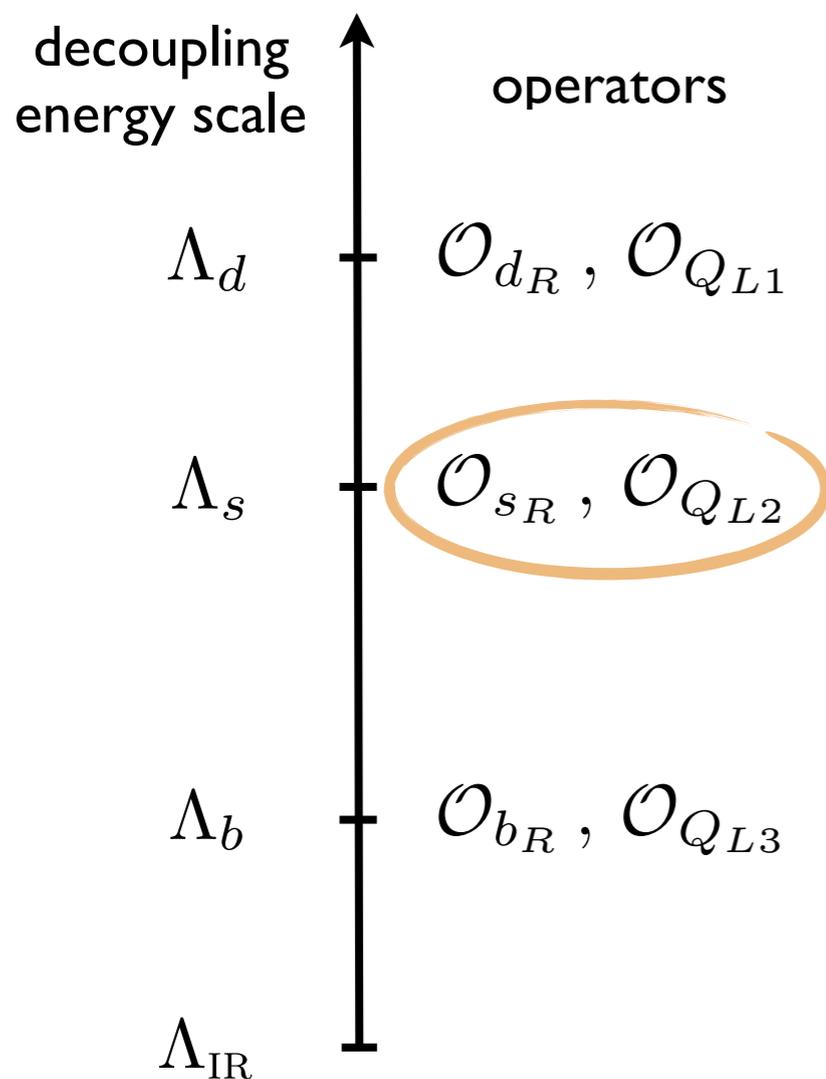
below  $\Lambda_{IR}$

$$\mathcal{Y}_{down} = g_* \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & \varepsilon_{b_L}^{(3)} \varepsilon_{b_R}^{(3)} \end{pmatrix} \left( \frac{\Lambda_{IR}}{\Lambda_b} \right)^{d_H-1}$$

# The emergent flavor structure

partial compositeness mixings

down-quark sector



$$\mathcal{L}_{lin}^{(2)} = (\varepsilon_{b_L}^{(2)} \bar{Q}_{L3} + \varepsilon_{s_L}^{(2)} \bar{Q}_{L2}) \mathcal{O}_{Q_{L2}} + (\varepsilon_{b_R}^{(2)} \bar{b}_R + \varepsilon_{s_R}^{(2)} \bar{s}_R) \mathcal{O}_{s_R}$$



below  $\Lambda_s$

$$\mathcal{L}_{bilin}^{(2)} = \frac{1}{\Lambda_d^{d_H-1}} (\varepsilon_{b_L}^{(2)} \bar{Q}_{L3} + \varepsilon_{s_L}^{(2)} \bar{Q}_{L2}) \mathcal{O}_H (\varepsilon_{b_R}^{(2)} b_R + \varepsilon_{s_R}^{(2)} s_R)$$



below  $\Lambda_{IR}$

$$\mathcal{Y}_{down} = g_* \begin{pmatrix} 0 & 0 & 0 \\ 0 & \varepsilon_{s_L}^{(2)} \varepsilon_{s_R}^{(2)} & \varepsilon_{s_L}^{(2)} \varepsilon_{b_R}^{(2)} \\ 0 & \varepsilon_{b_L}^{(2)} \varepsilon_{s_R}^{(2)} & 0 \end{pmatrix} \left( \frac{\Lambda_{IR}}{\Lambda_s} \right)^{d_H-1}$$

# The emergent flavor structure

partial compositeness mixings

down-quark sector

decoupling  
energy scale

operators

$\Lambda_d$

$\mathcal{O}_{d_R}, \mathcal{O}_{Q_{L1}}$

$\Lambda_s$

$\mathcal{O}_{s_R}, \mathcal{O}_{Q_{L2}}$

$\Lambda_b$

$\mathcal{O}_{b_R}, \mathcal{O}_{Q_{L3}}$

$\Lambda_{IR}$

$$\mathcal{L}_{lin}^{(1)} = (\varepsilon_{b_L}^{(1)} \bar{Q}_{L3} + \varepsilon_{s_L}^{(1)} \bar{Q}_{L2} + \varepsilon_{d_L}^{(1)} \bar{Q}_{L1}) \mathcal{O}_{Q_{L1}} \\ + (\varepsilon_{b_R}^{(1)} \bar{b}_R + \varepsilon_{s_R}^{(1)} \bar{s}_R + \varepsilon_{d_R}^{(1)} \bar{d}_R) \mathcal{O}_{d_R}$$



below  $\Lambda_d$



below  $\Lambda_{IR}$

$$\mathcal{Y}_{down} = g_* \begin{pmatrix} \varepsilon_{d_L}^{(1)} \varepsilon_{d_R}^{(1)} & \varepsilon_{d_L}^{(1)} \varepsilon_{s_R}^{(1)} & \varepsilon_{d_L}^{(1)} \varepsilon_{b_R}^{(1)} \\ \varepsilon_{s_L}^{(1)} \varepsilon_{d_R}^{(1)} & & \\ \varepsilon_{b_L}^{(1)} \varepsilon_{d_R}^{(1)} & & \end{pmatrix} \left( \frac{\Lambda_{IR}}{\Lambda_d} \right)^{d_H-1}$$

# The emergent flavor structure

The Yukawa matrix has an “onion” structure

$$\mathcal{Y}_{down} \simeq \begin{pmatrix} Y_d & \alpha_R^{ds} Y_d & \alpha_R^{db} Y_d \\ \alpha_L^{ds} Y_d & Y_s & \alpha_R^{sb} Y_s \\ \alpha_L^{db} Y_d & \alpha_L^{sb} Y_s & Y_b \end{pmatrix}$$

where the Yukawa's are given by

$$Y_f \equiv g_* \varepsilon_{fLi}^{(i)} \varepsilon_{fRi}^{(i)} \left( \frac{\Lambda_{\text{IR}}}{\Lambda_f} \right)^{d_H - 1} \simeq m_f / v$$

- smaller Yukawa's for larger decoupling scale
- mixing angles suppressed by Yukawa's:  $\theta_{ij} \sim Y_i / Y_j$ 
  - CKM mostly the rotation in the down-quark sector

# Comparison with anarchic

bilinears

$$\begin{pmatrix} Y_d & \alpha_R^{ds} Y_d & \alpha_R^{db} Y_d \\ \alpha_L^{ds} Y_d & Y_s & \alpha_R^{sb} Y_s \\ \alpha_L^{db} Y_d & \alpha_L^{sb} Y_s & Y_b \end{pmatrix}$$

anarchic

$$\begin{pmatrix} Y_d & \sqrt{Y_d Y_s} & \sqrt{Y_d Y_b} \\ \sqrt{Y_d Y_s} & Y_s & \sqrt{Y_s Y_b} \\ \sqrt{Y_d Y_b} & \sqrt{Y_s Y_b} & Y_b \end{pmatrix}$$

The bilinear scenario predicts **smaller off-diagonal elements**

- ▶ particularly relevant for R rotations: suppressed w.r.t. anarchic

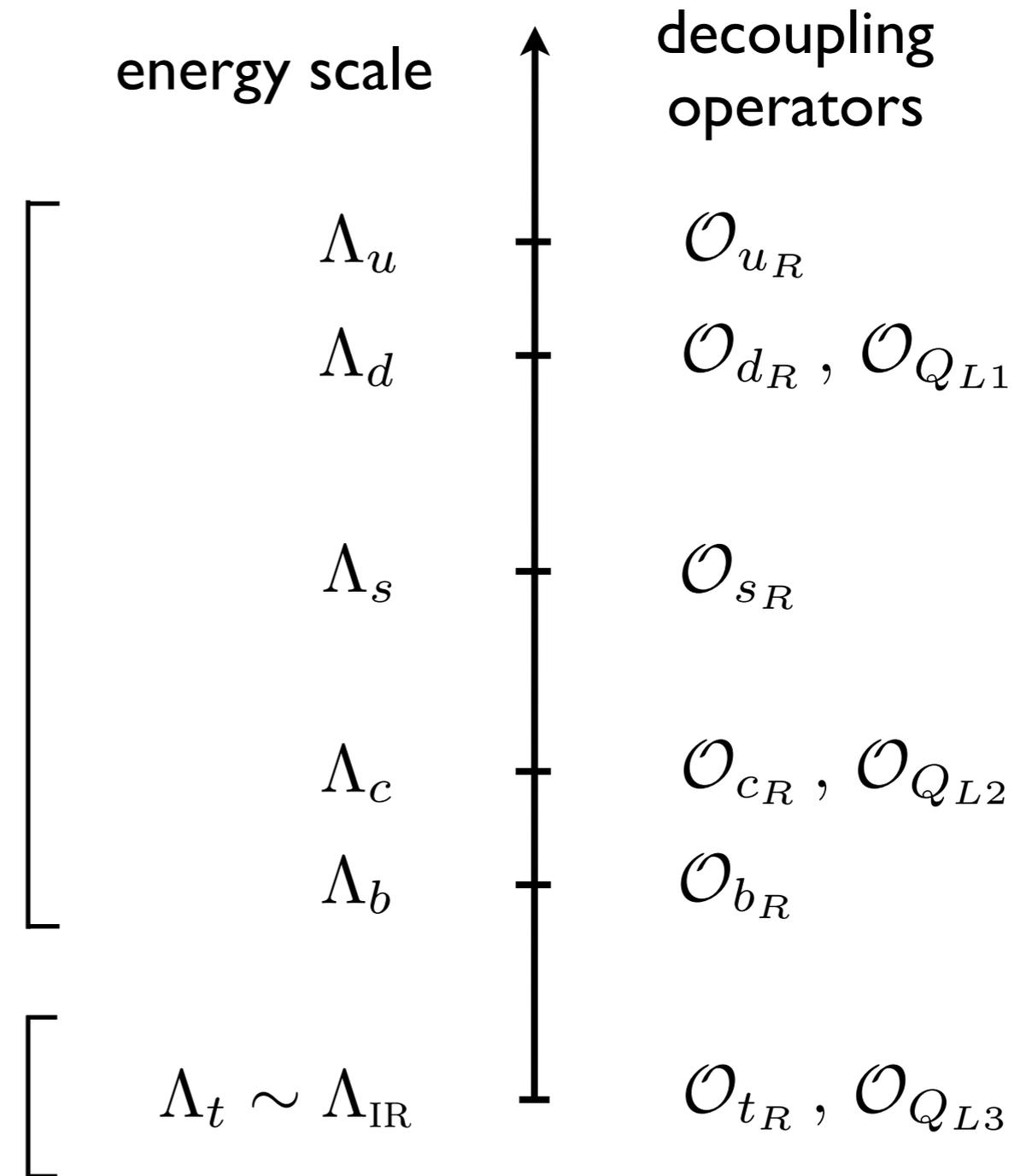
# The hierarchy of scales

High scale suppresses flavor effects

- ◆ small contributions to FCNC's
- ◆ negligible EDM's

Main flavor effects from top

- ◆ unavoidable if top is composite!



# **Flavor and CP-violating effects**

# $\Delta F = 1$ transitions

Top partial compositeness at  $\Lambda_{\text{IR}}$  gives rise to flavor effects

$\Delta F = 1$  operators

$$\sim \frac{g_* Y_t}{\Lambda_{\text{IR}}} \bar{Q}_{L3} \gamma^\mu Q_{L3} i H^\dagger \overleftrightarrow{D}_\mu H$$



rotation to physical basis

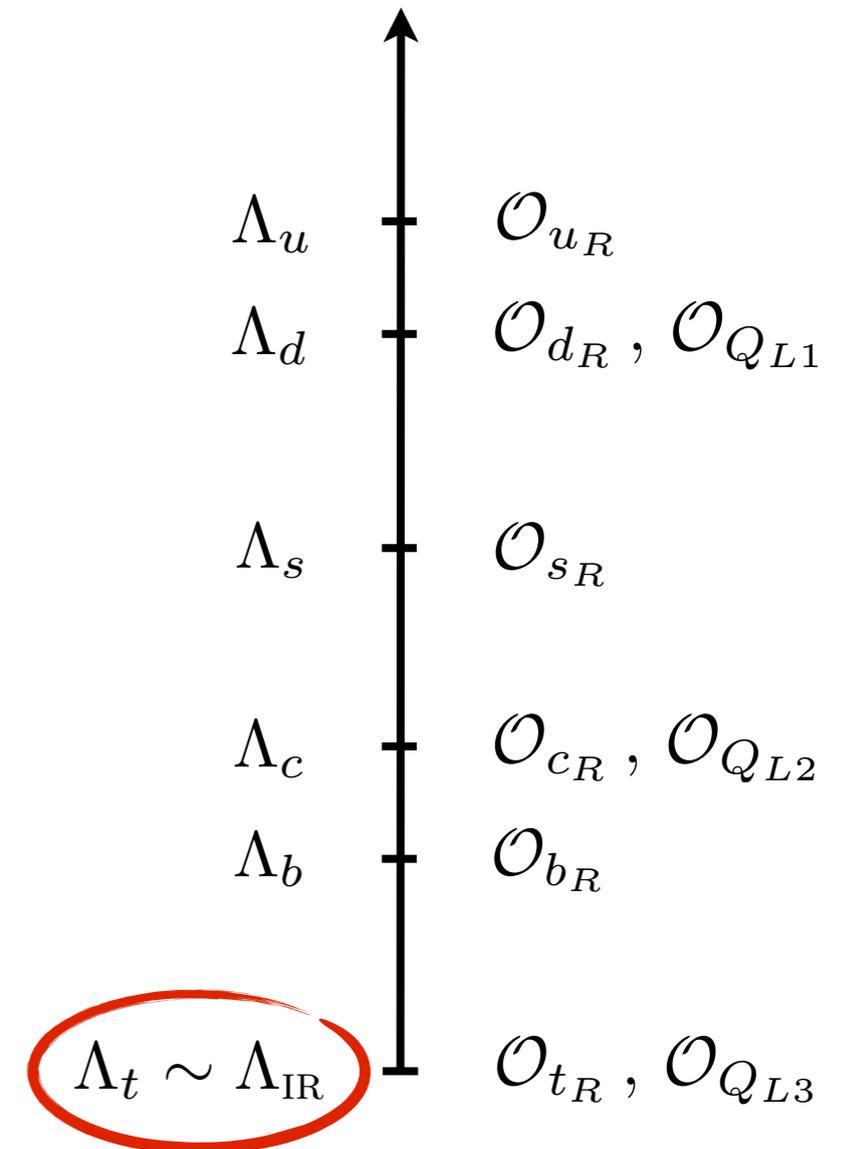
$$V_L \sim V_{\text{CKM}}$$

corrections to  $K \rightarrow \mu\mu, \varepsilon'/\varepsilon, B \rightarrow X\ell\ell, Z \rightarrow bb$

- correlated and close to experimental bounds

$$\Lambda_{\text{IR}} \gtrsim 4 - 5 \text{ TeV}$$

- can be suppressed by left-right symmetry



# $\Delta F = 2$ transitions

Top partial compositeness at  $\Lambda_{\text{IR}}$  gives rise to flavor effects

$\Delta F = 2$  operators

$$\sim \frac{Y_t^2}{\Lambda_{\text{IR}}^2} (\bar{Q}_{L3} \gamma^\mu Q_{L3})^2$$



rotation to physical basis  
 $V_L \sim V_{\text{CKM}}$

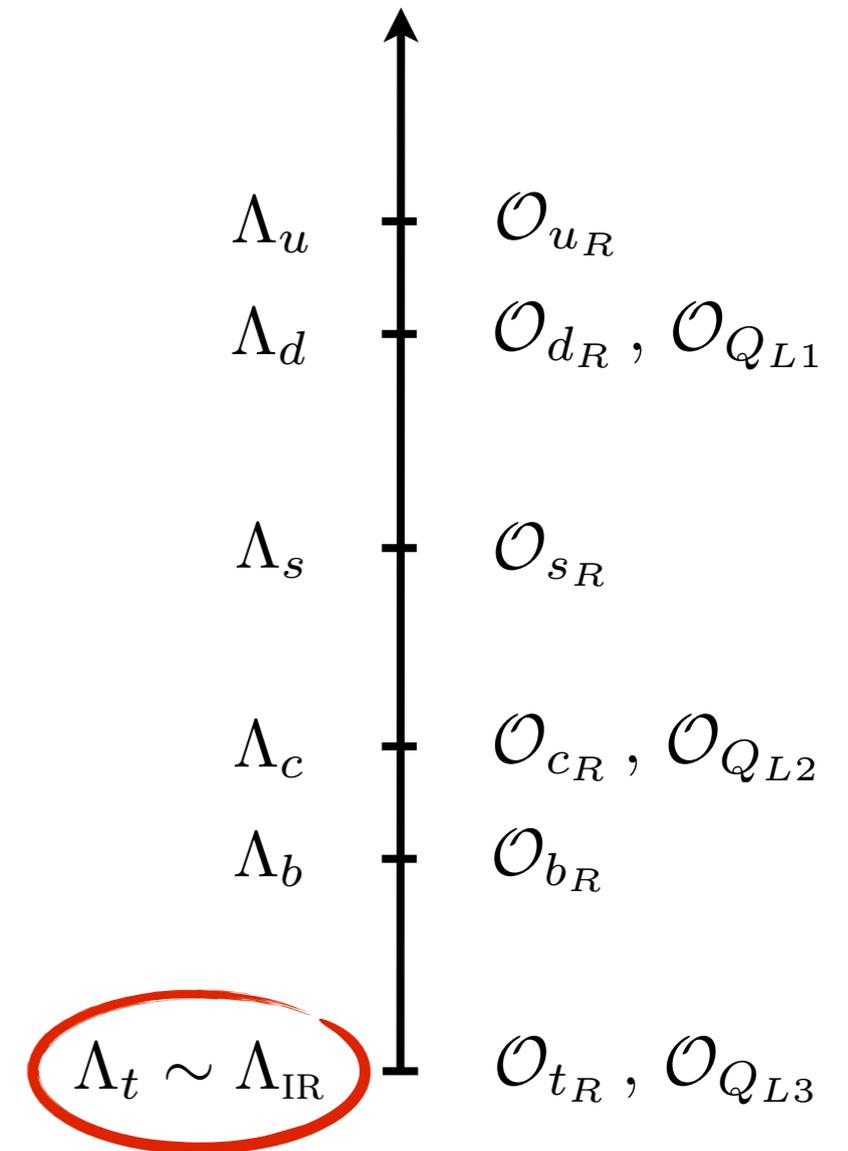
corrections to  $\varepsilon_K$ ,  $\Delta M_{B_d}$ ,  $\Delta M_{B_s}$

- correlated: interesting prediction

$$\frac{\Delta M_{B_d}}{\Delta M_{B_s}} \simeq \frac{\Delta M_{B_d}}{\Delta M_{B_s}} \Big|_{\text{SM}}$$

- close to experimental bounds

$$\Lambda_{\text{IR}} \gtrsim 2 - 3 \text{ TeV}$$



# Effects at higher scales

Top partial compositeness at  $\Lambda_{\text{IR}}$  gives rise to flavor effects

$$\Delta F = 2 \text{ operators}$$

$$\sim \frac{g_*^2}{\Lambda_s^2} (\bar{Q}_{L2} s_R) (\bar{s}_R Q_{L2})$$

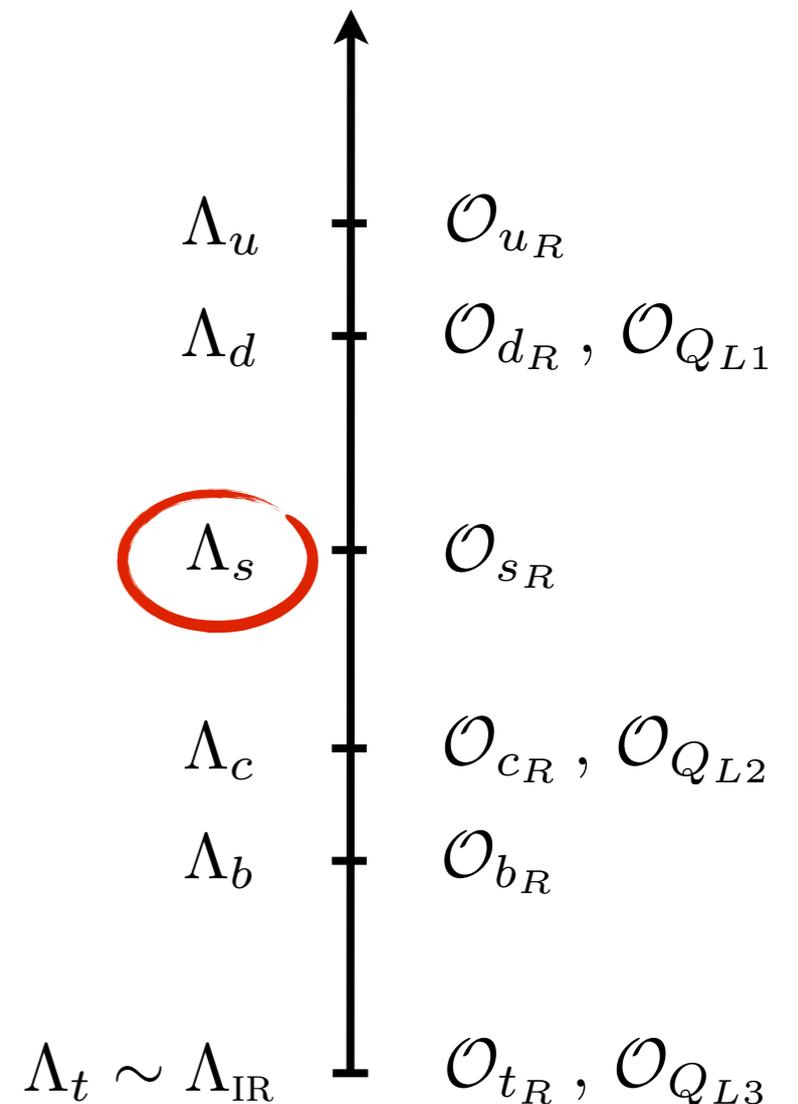


rotation to physical basis  
 $V_L \sim V_{\text{CKM}}$

corrections to  $\varepsilon_K$

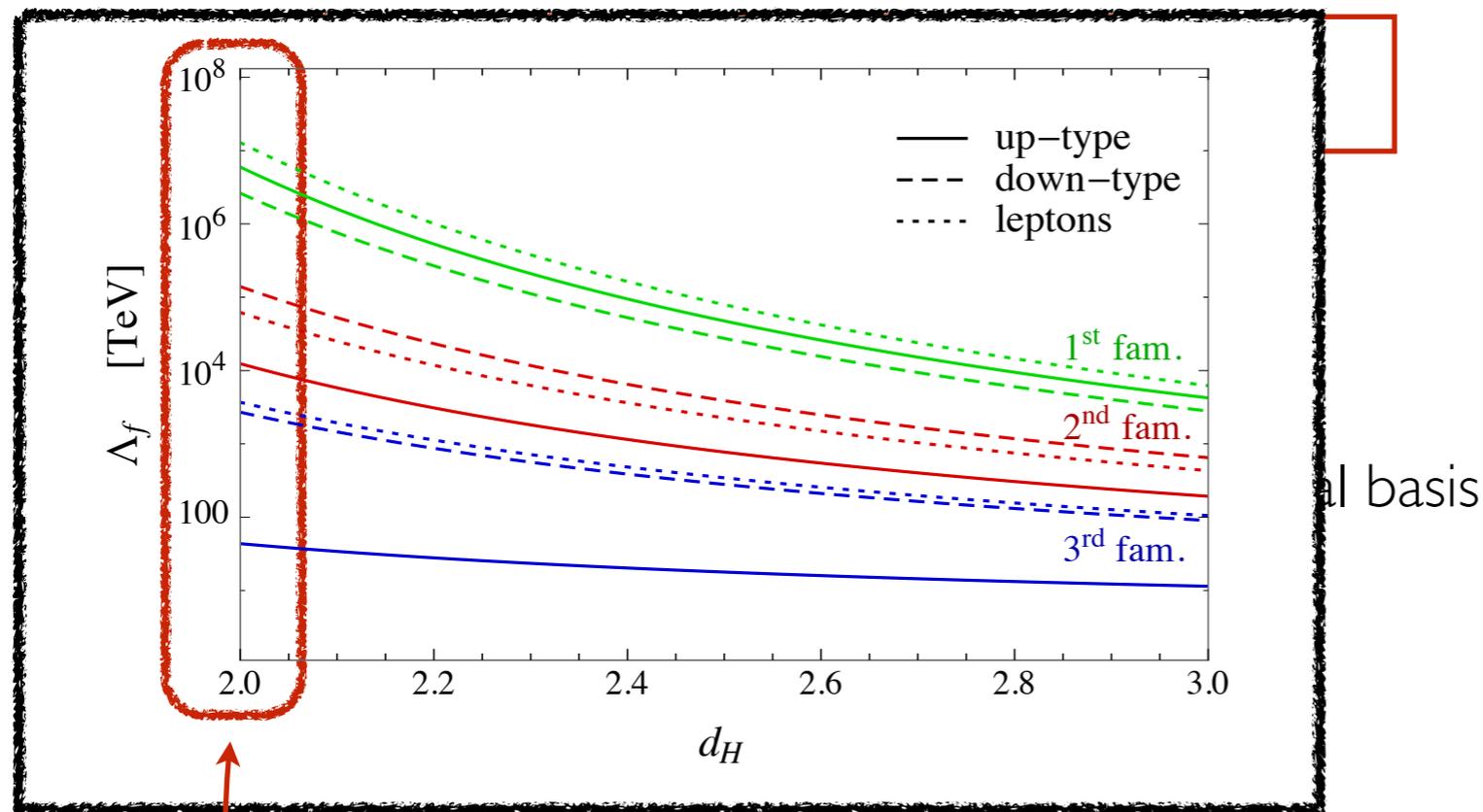
- close to experimental bounds for

$$\Lambda_s \sim 10^5 \text{ TeV}$$



# Effects at higher scales

Top partial compositeness at  $\Lambda_{\text{IR}}$  gives rise to flavor effects

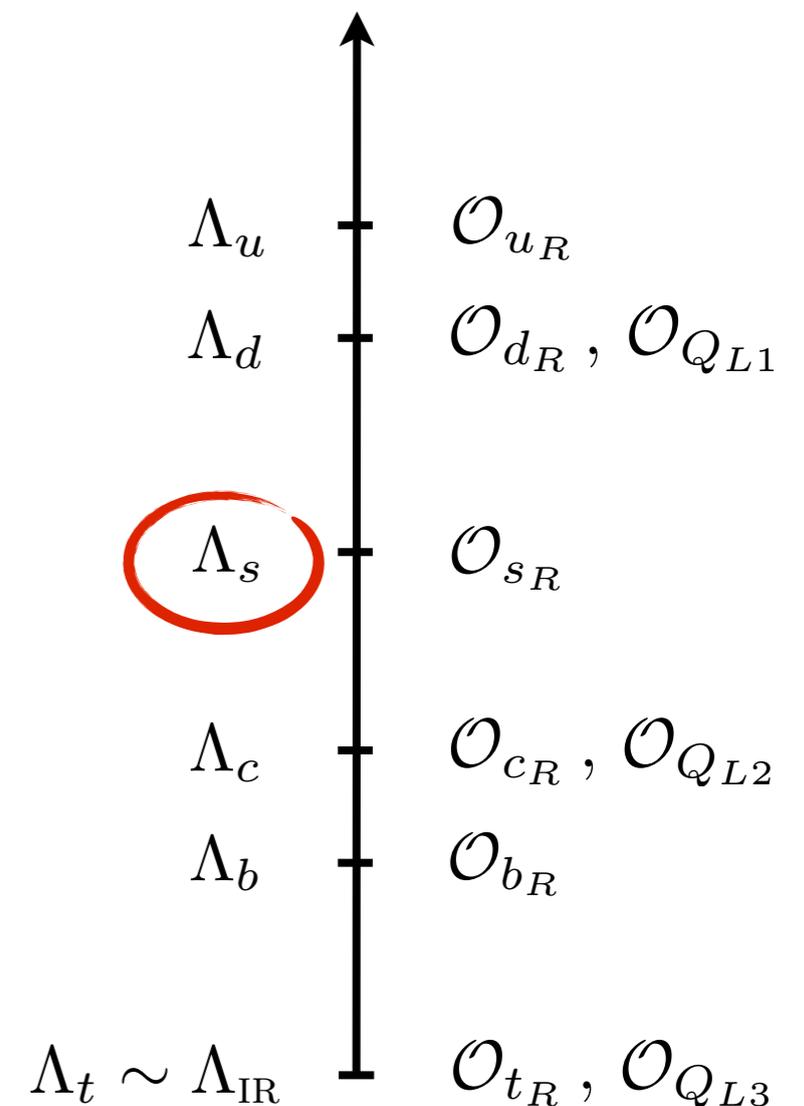


- close to experimental bounds for

$$\Lambda_s \sim 10^5 \text{ TeV}$$



realized if Higgs dimension  $d_H \sim 2$



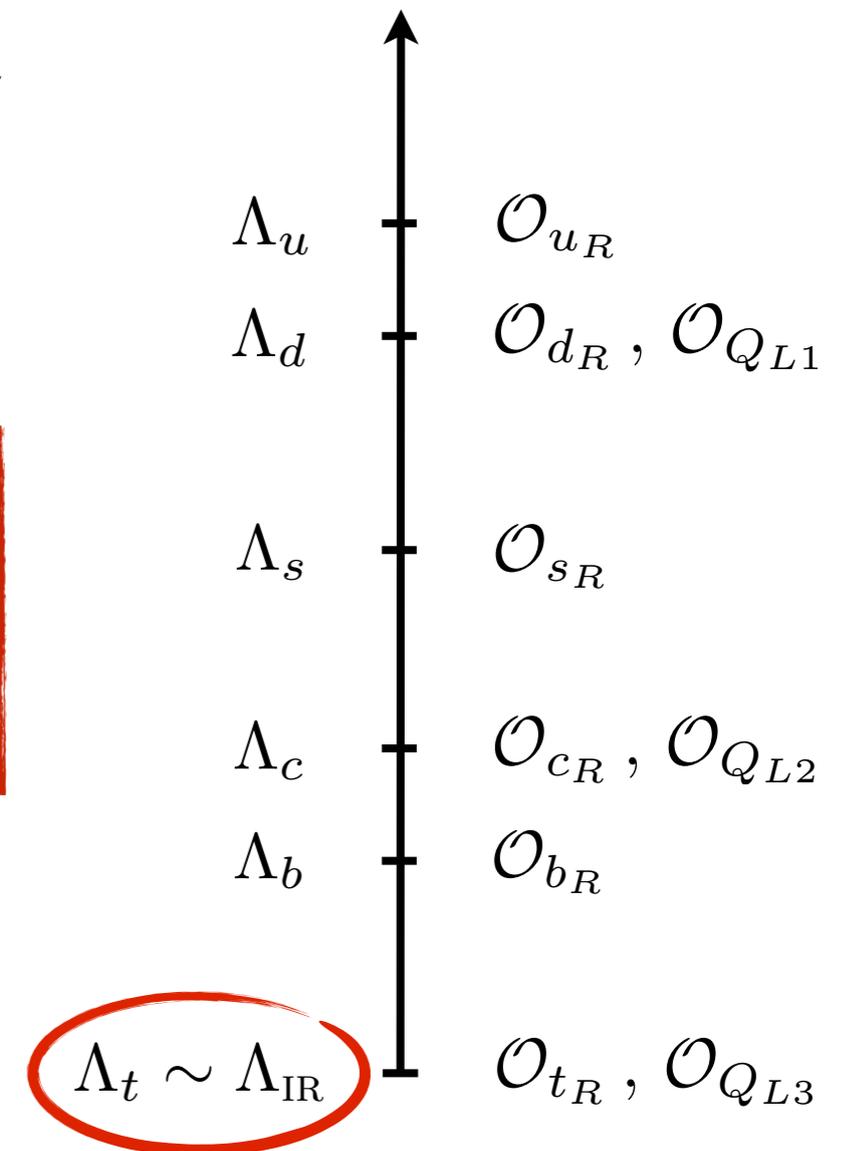
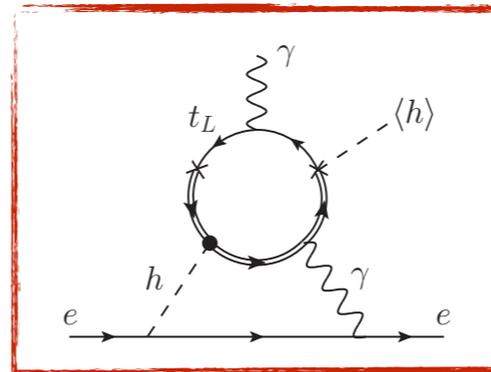
# EDMs

Top partial compositeness at  $\Lambda_{\text{IR}}$  gives rise to EDM's

- ♦ one-loop EDMs for light fermions suppressed by

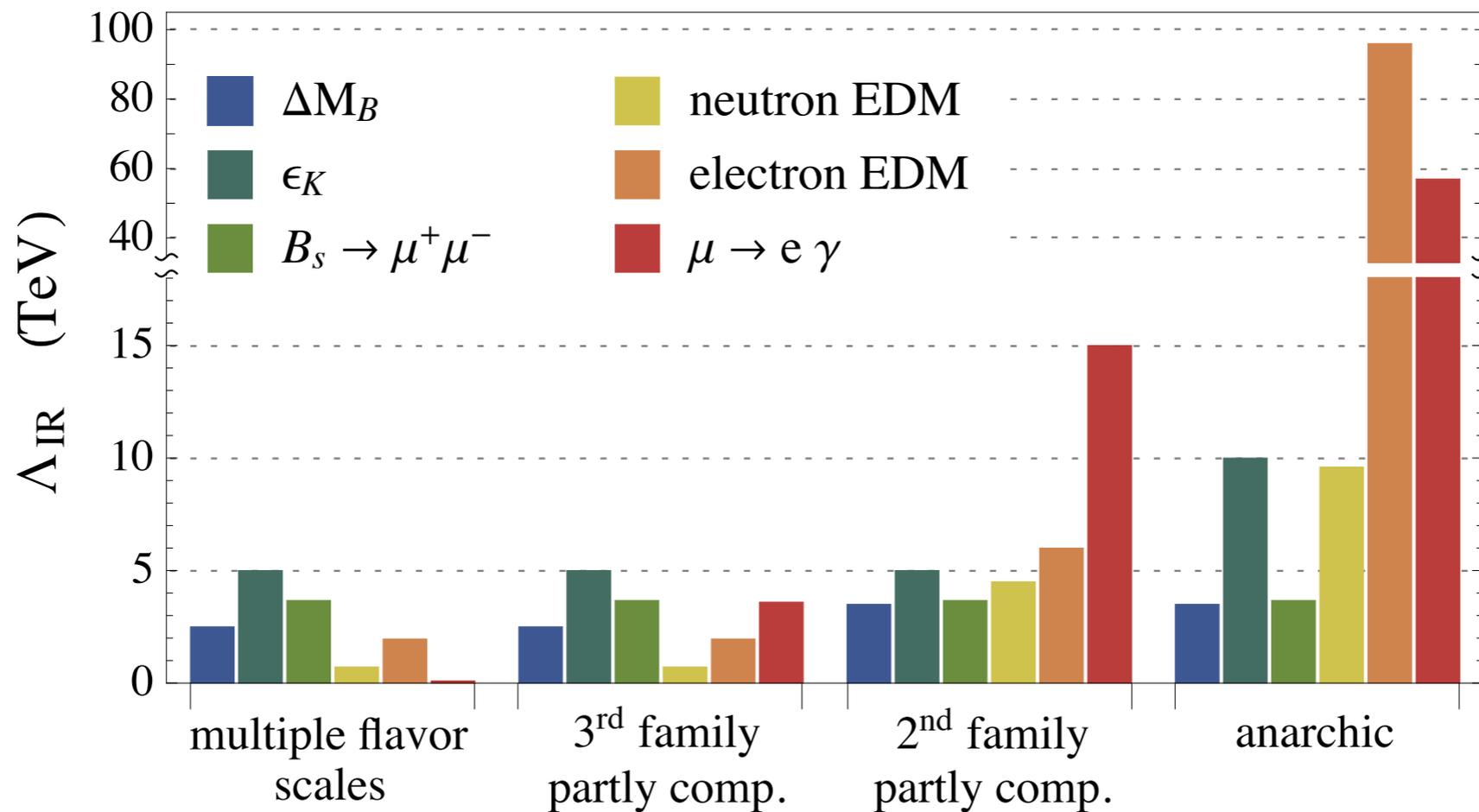
$$\Lambda_{u,d,e} > 10^6 \text{ TeV}$$

... but sizable **neutron** and **electron EDM** from two-loop Barr-Zee diagrams



$n$  and  $e$  EDMs lead to the bound  $\Lambda_{\text{IR}} \gtrsim \text{TeV}$

# Summary of the bounds



- ◆ huge improvement with respect to the anarchic case (especially in the lepton sector)
- ◆ several effects close to experim. bounds for  $\Lambda_{\text{IR}} \sim \text{few TeV}$

# Next generation EDM bounds

Experimental bounds on EDMs will soon greatly improve

## ◆ electron EDM

$$\begin{array}{ccccc} & \text{ACME} & & \text{ACME II} & & \text{ACME III} \\ |d_e| < 9.4 \cdot 10^{-29} e \text{ cm} & \longrightarrow & |d_e| \lesssim 0.5 \cdot 10^{-29} e \text{ cm} & \longrightarrow & |d_e| \lesssim 0.3 \cdot 10^{-30} e \text{ cm} \end{array}$$

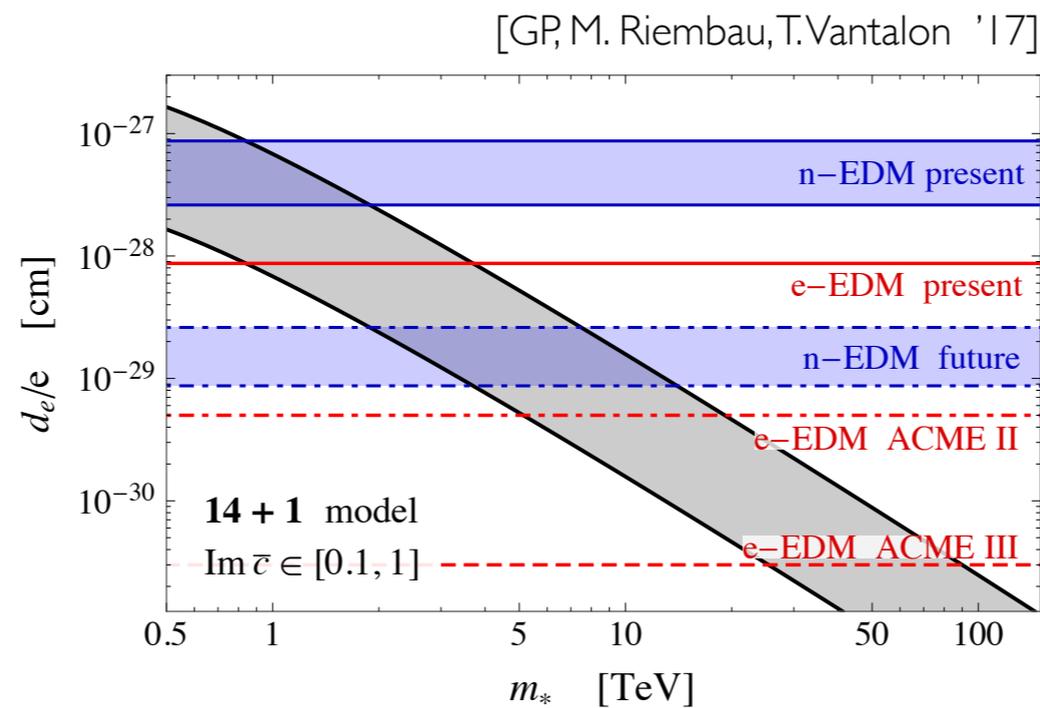
## ◆ neutron EDM

$$|d_n| < 2.9 \cdot 10^{-26} e \text{ cm} \longrightarrow |d_n| \lesssim 10^{-27} e \text{ cm}$$

- ▶ EDMs will become some of the strongest bounds on BSM, indirectly probing new physics well above the 10 TeV scale

# EDM probes of top partners

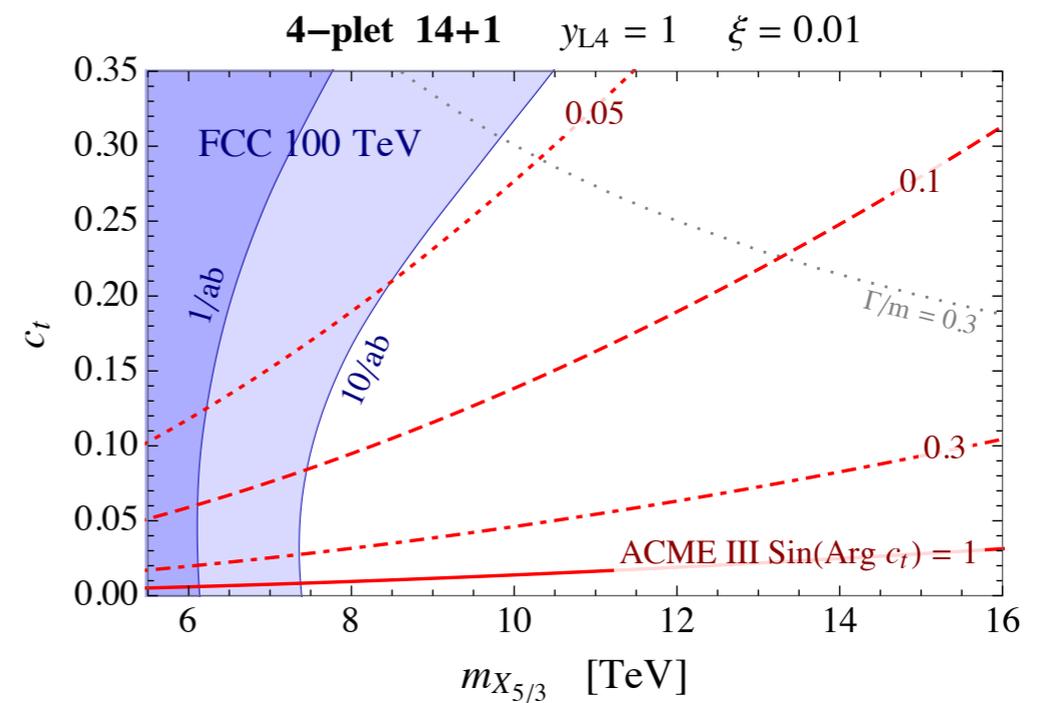
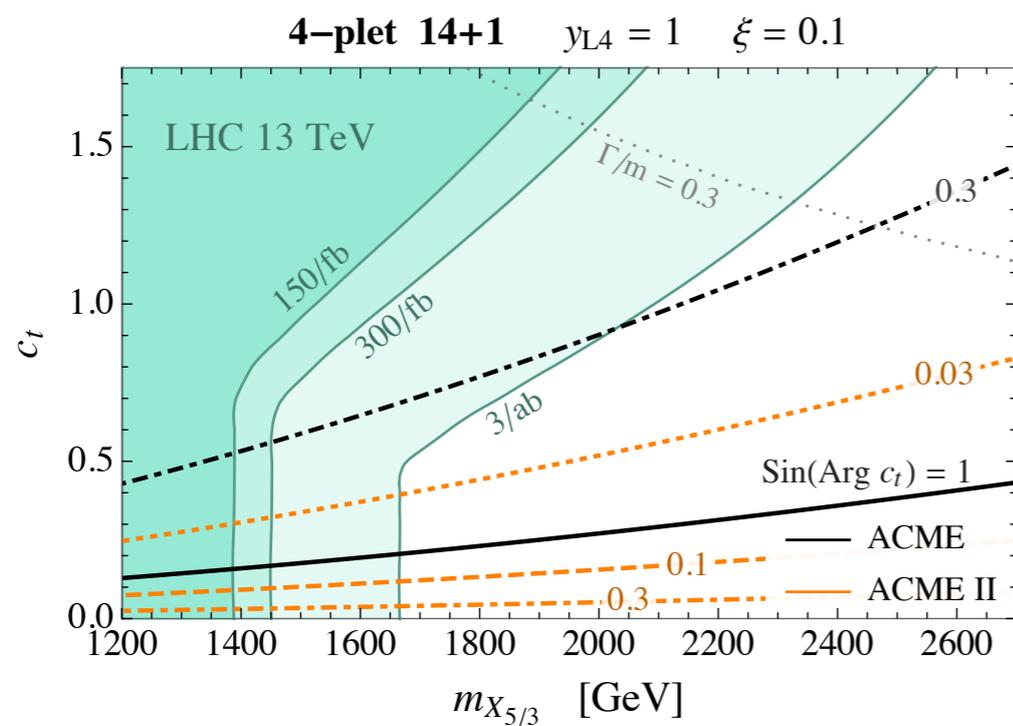
Near-future bounds could probe partner masses well above 10 TeV



# EDM probes of top partners

EDM bounds competitive with direct searches at LHC and even FCC<sub>100</sub>

[GP, M. Riembau, T. Vantalou '17]



# **Conclusions**

# Conclusions

The **flavour structure** of the SM could be an **emergent feature**:

- ◆ Yukawa hierarchies linked to dynamically generated mass scales

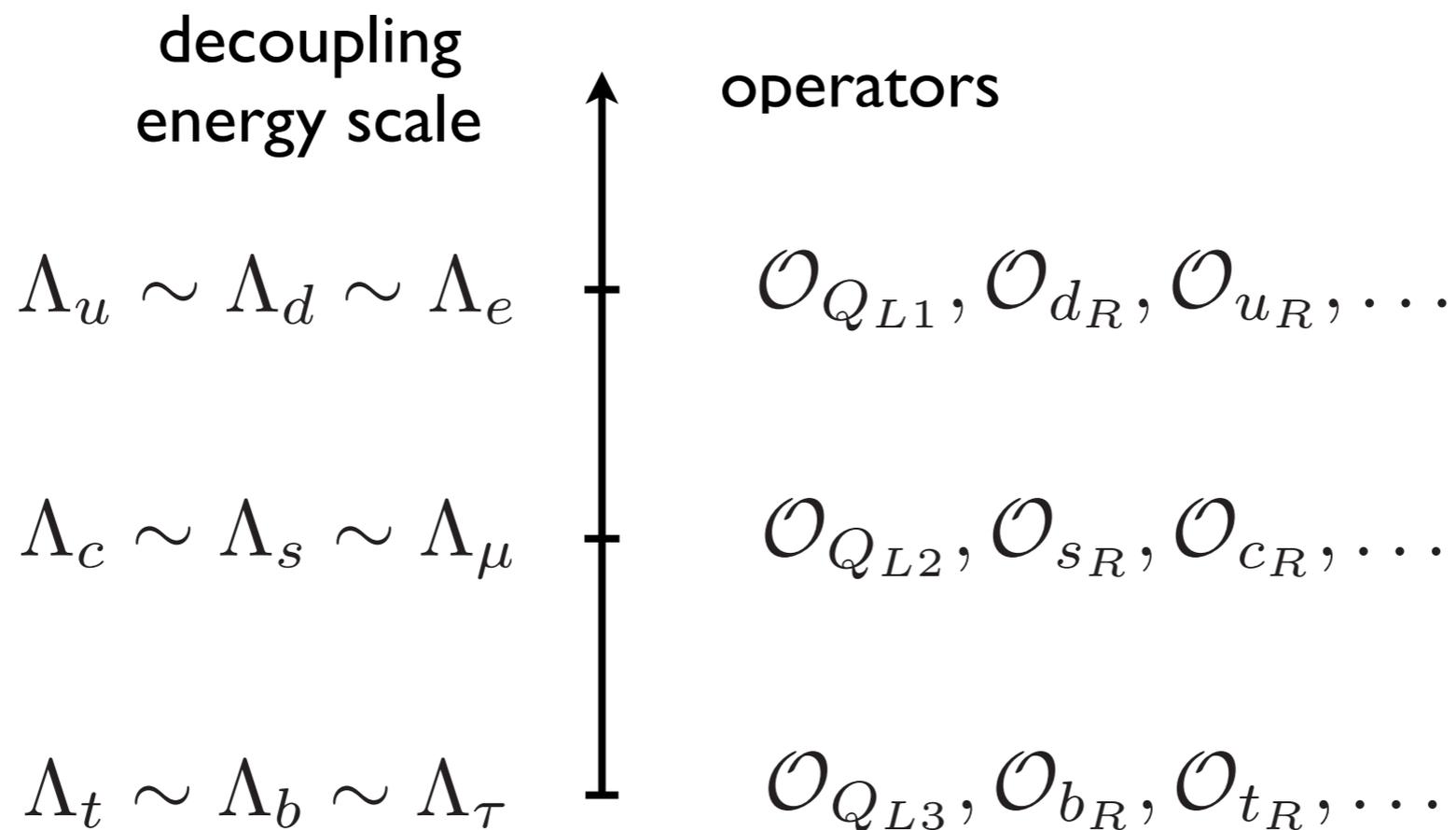
Successful implementation in composite Higgs scenarios

- ◆ modification of partial compositeness
- ◆ flavor from mixing with the composite dynamics at different scales (at low energy equivalent to bilinear mixings)
- ◆ compatibility with flavour bounds + several new physics effects around the corner

**Backup**

# One scale for each family

More economical construction by associating one scale to each generation



- ◆ Yukawa differences within each generation due to different mixings
- ◆ Only main difference:  $\mu \rightarrow e\gamma$  close to exp. bounds

# Neutrino masses

◆ **Majorana masses** realization:

$$\frac{1}{\Lambda_\nu^{2d_H-1}} \bar{L}^c \mathcal{O}_H \mathcal{O}_H L \quad \longrightarrow \quad m_\nu \simeq \frac{g_*^2 v^2}{\Lambda_{\text{IR}}} \left( \frac{\Lambda_{\text{IR}}}{\Lambda_\nu} \right)^{2d_H-1}$$

for  $d_H \sim 2$  dimension-7 operators:

$$m_\nu \sim 0.1 - 0.01 \text{ eV} \quad \Rightarrow \quad \Lambda_\nu \sim 0.8 - 1.5 \times 10^8 \text{ GeV} \sim \Lambda_e$$

◆ **Dirac masses** realization:

$$\frac{1}{\Lambda_\nu^{d_H-1}} \mathcal{O}_H \bar{L} \nu_R$$

for  $d_H \sim 2$  dimension-5 operators as in SM