



# The Properties of Parsec-Scale Blazar Jets

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# Basic Idea

*Using the Blandford-Konigl jet model and five observables, one can determine a number of properties of blazar jets*

## Observables:

1. Redshift
2. core flux density
3. extended flux density
4. core shift
5. apparent opening angle

## Nuisance parameters:

1. electron distribution parameters ( $\gamma_1$ ,  $\gamma_2$ ,  $p$ )
2. equipartition parameters ( $\xi_e$ ,  $\xi_p$ )

## Blandford-Konigl jet model

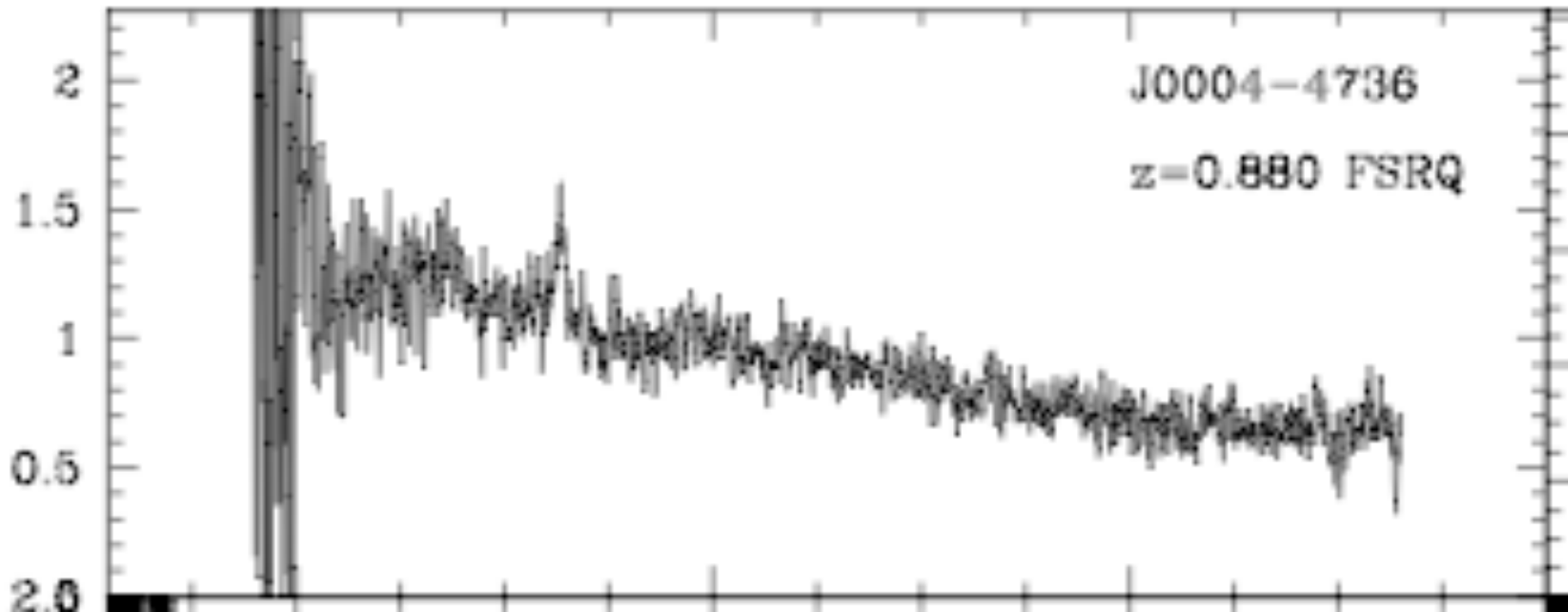
## Results (jet parameters):

1. Lorentz factor ( $\Gamma$ )
2. angle to line of sight ( $\theta$ )

## Other parameters:

1. Doppler factor ( $\delta$ )
2. jet opening angle ( $\alpha$ )
3. Magnetic field  $B(1 \text{ pc})$

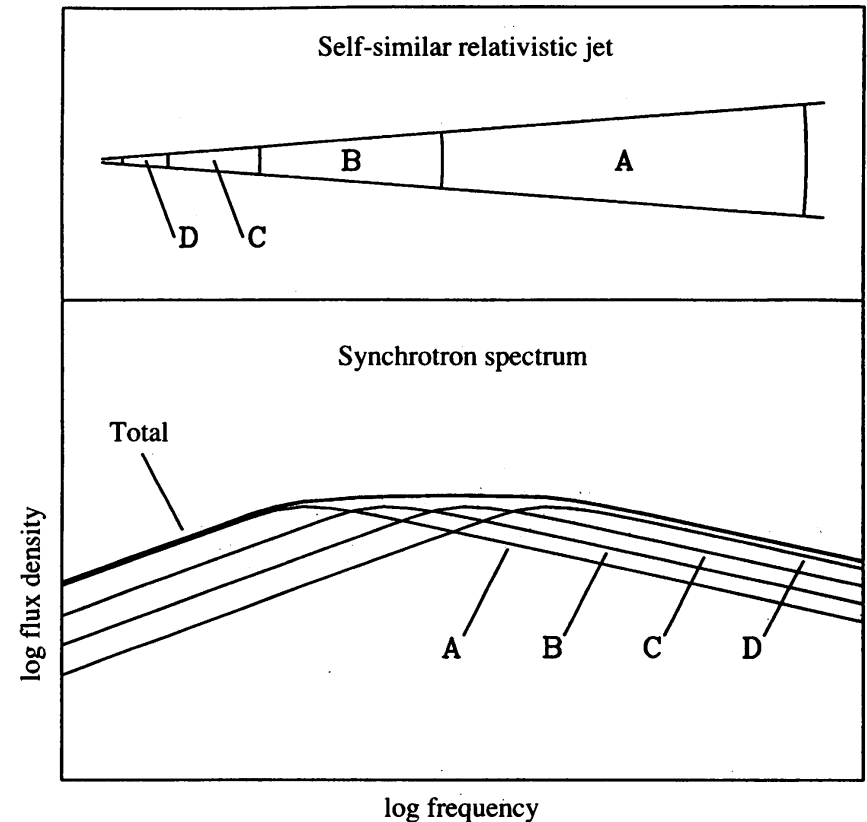
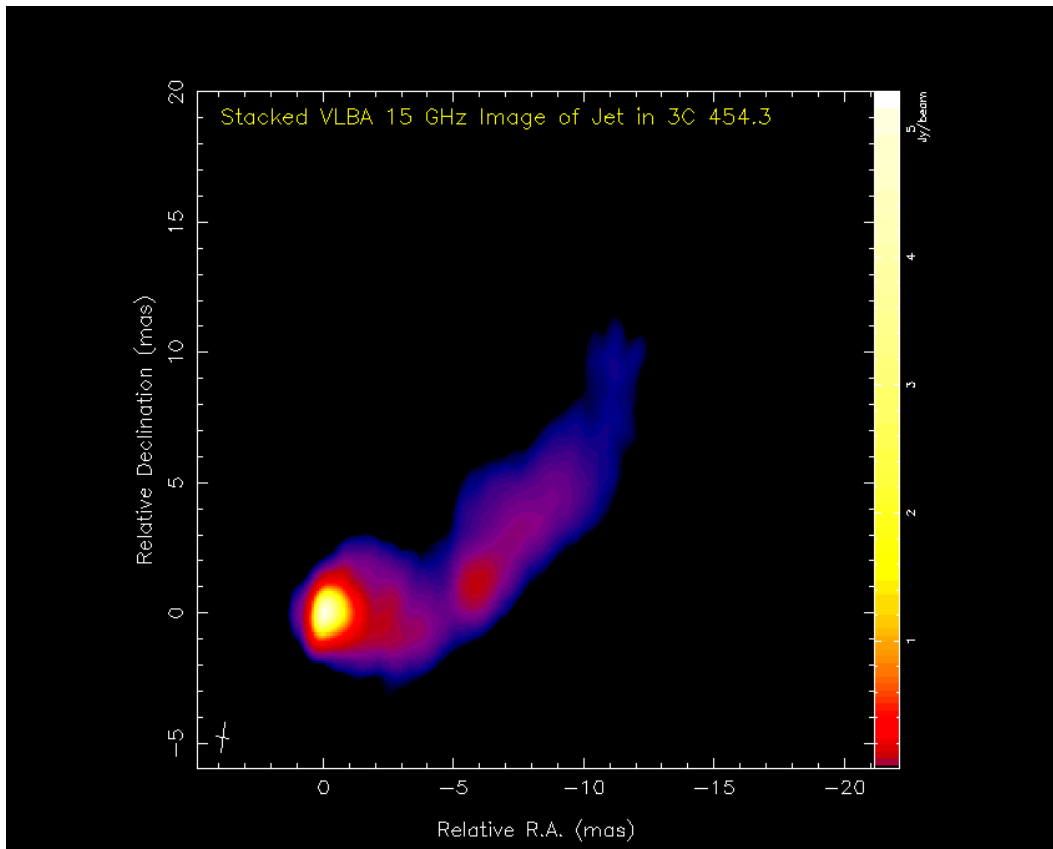
Gives distance to source, determines luminosities from fluxes



Shaw et al. (2012)

# Core Flux Density

Core radio spectra seen in VLBI images are flat. BK model explains this as the superposition of several self-absorbed components.  $F_\nu(\Gamma, \theta, \alpha, P_j)$ . Also depends on electron distribution  $N_e(\gamma) = N_{e0} \gamma^{-p}$ .

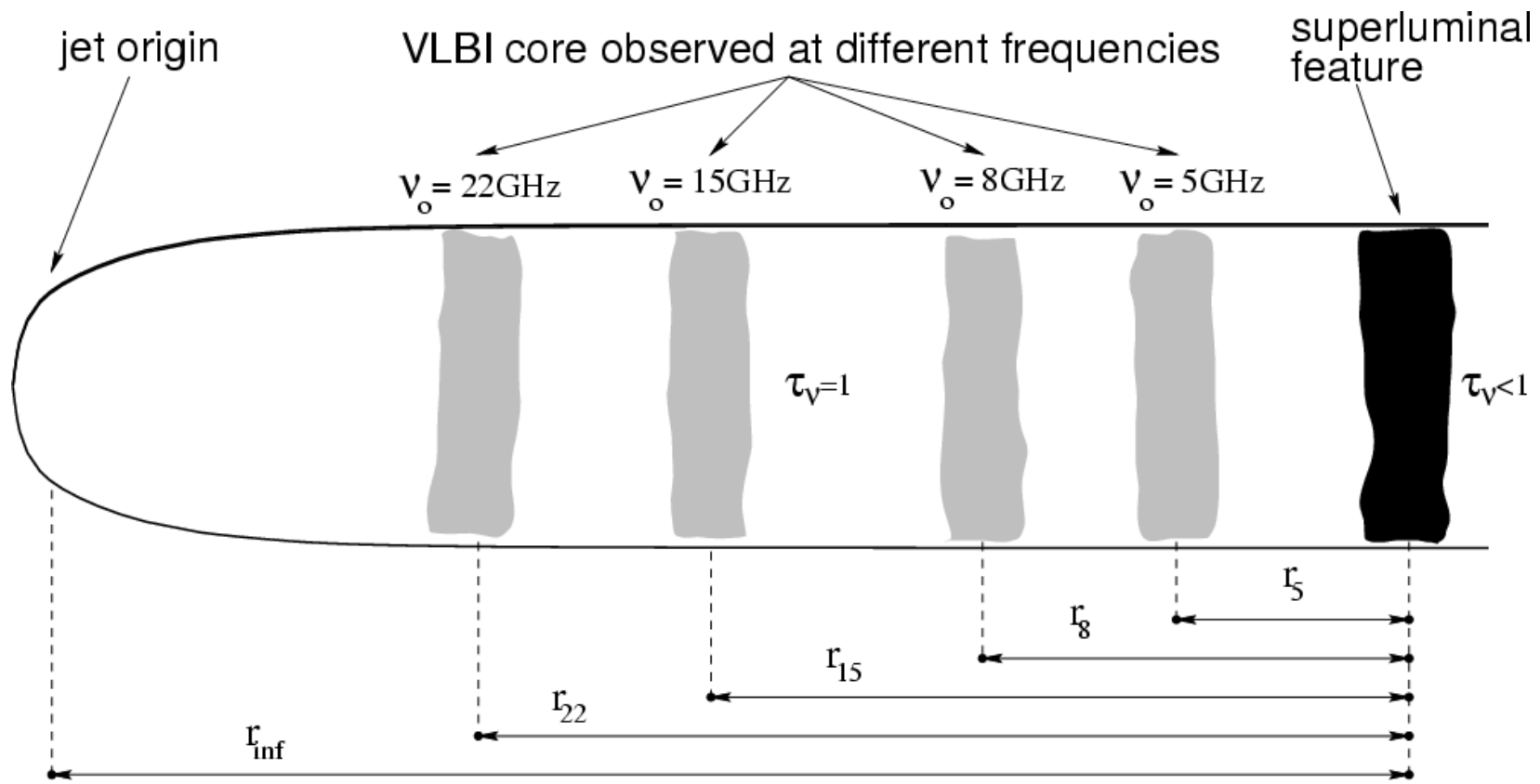


MOJAVE website  
<http://www.physics.purdue.edu/astro/MOJAVE/>

Marscher (1995)

# Core Shift

VLBI core position is dependent on frequency. Core's position "shifts" when viewed at different frequencies.  $\Delta\phi(\Gamma, \theta, \alpha, P_j)$ . Also depends on electron distribution  $N_e(\gamma) = N_{e0} \gamma^{-p}$ .



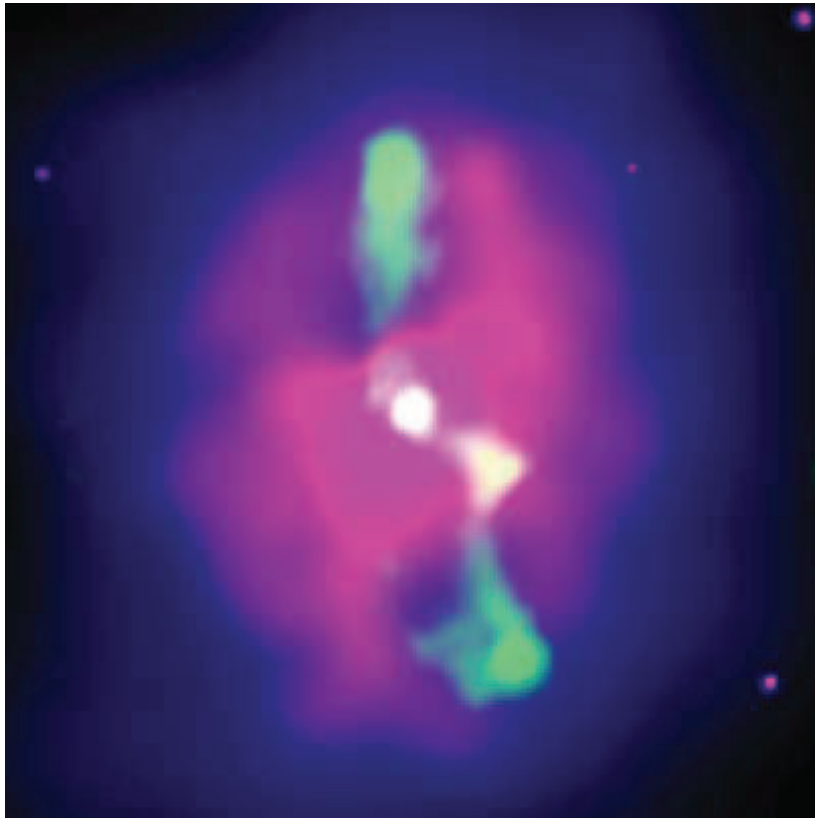
Kovalev et al. (2008)

# Extended Radio Flux and Jet Power

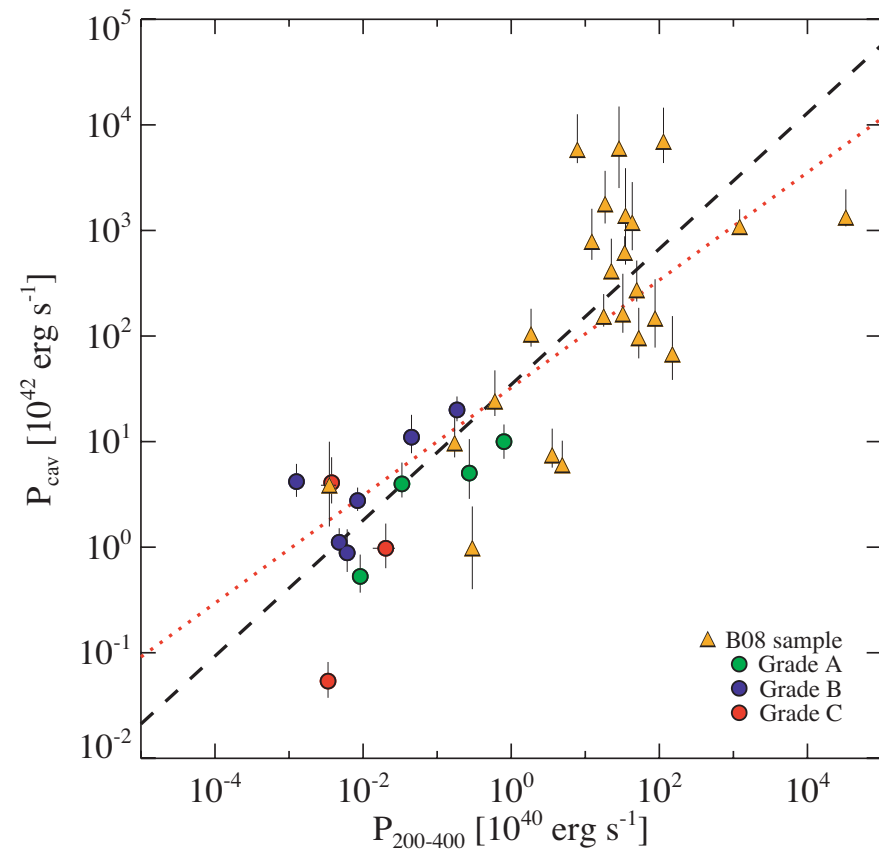
The Power needed to inflate cavities in hot ICM is well-correlated with extended radio luminosity. So measuring extended radio flux gives jet power.

MS 0735+7421

327 MHz



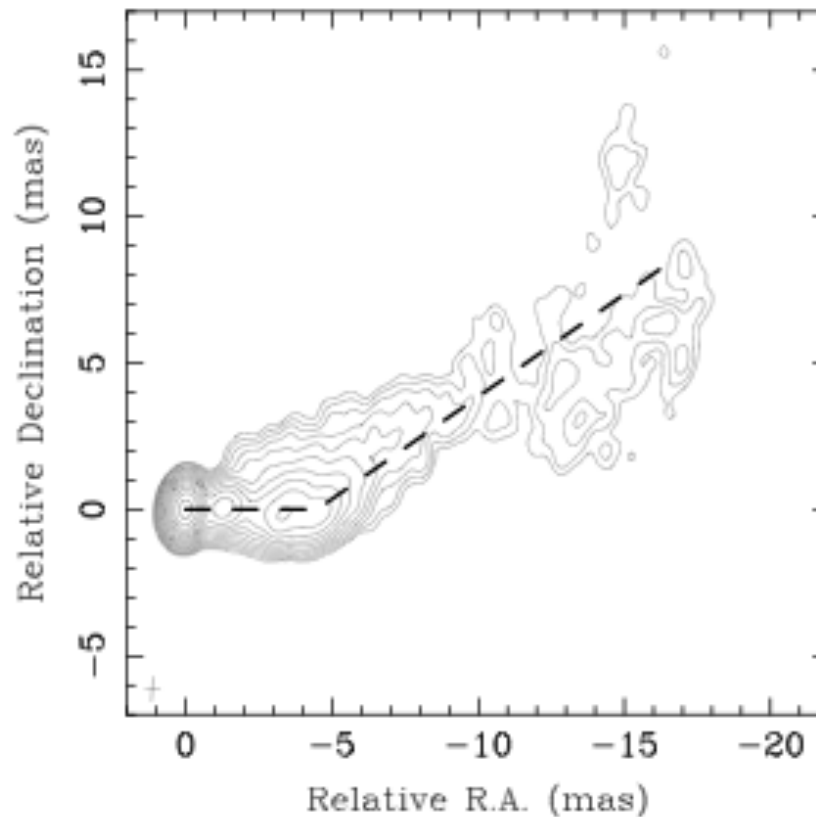
Birzan et al. (2008)



Cavagnolo et al. (2010)

# Apparent Jet Opening Angle

Jet opening angle projected on the sky can be measured by analyzing transverse jet profiles from VLBI images.  $\alpha = \alpha_{\text{app}} \sin \theta$



Pushkarev et al. (2009)

# Finding Jet Parameters

Using observables, we can get two equations:

$$F_v(\Gamma, \theta, \alpha, P_j) \rightarrow F_v(\Gamma, \theta, \alpha_{app}, L_{ext})$$

$$\Delta\phi(\Gamma, \theta, \alpha, P_j) \rightarrow \Delta\phi(\Gamma, \theta, \alpha_{app}, L_{ext})$$

Two equations, two unknowns, can be solved for  $\Gamma$  and  $\theta$ .

Once these are known, one can find:

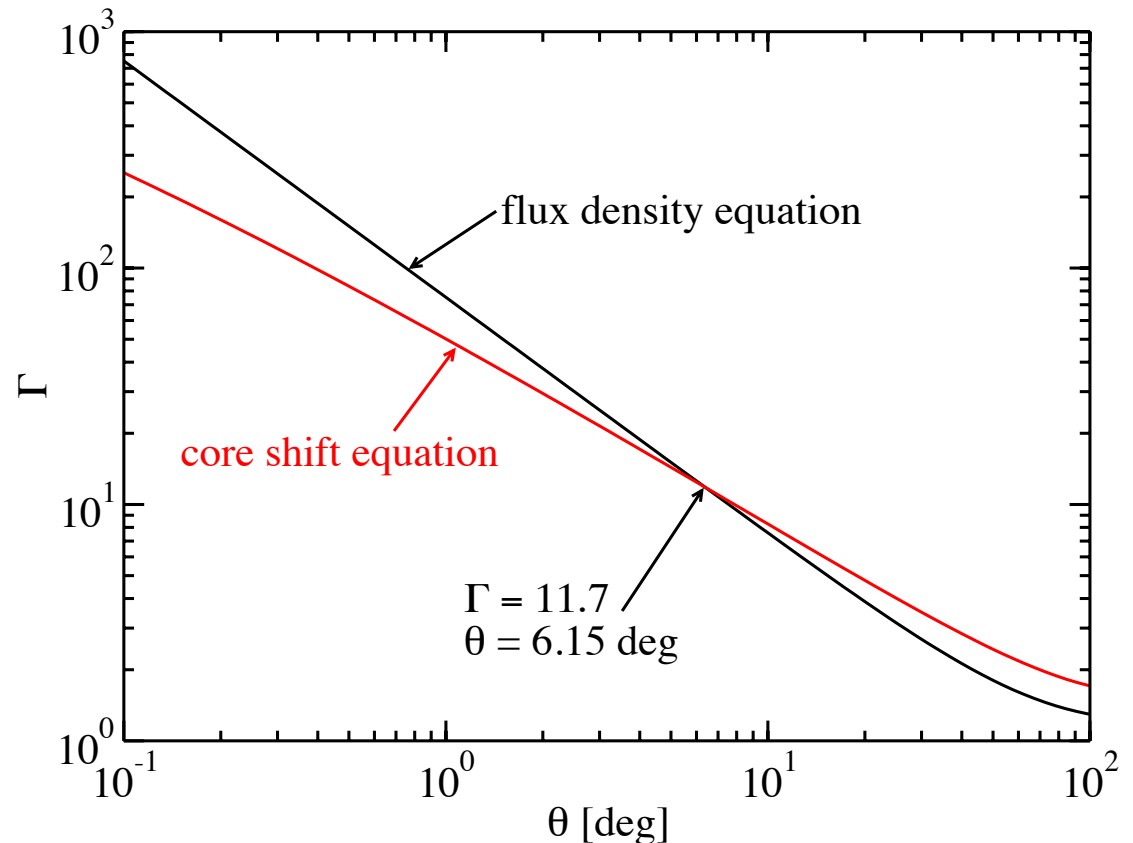
$$\delta_D = [\Gamma(1 - \beta \cos \theta)]^{-1}$$

$$\alpha = \alpha_{app} \sin \theta$$

$$\beta_{app} = (2\delta_D \Gamma - \delta_D^2 - 1)^{1/2}$$

$$B(1 \text{ pc}) \sim P_j^{1/2}$$

[  $B \sim r^{-1}$  in BK model ]

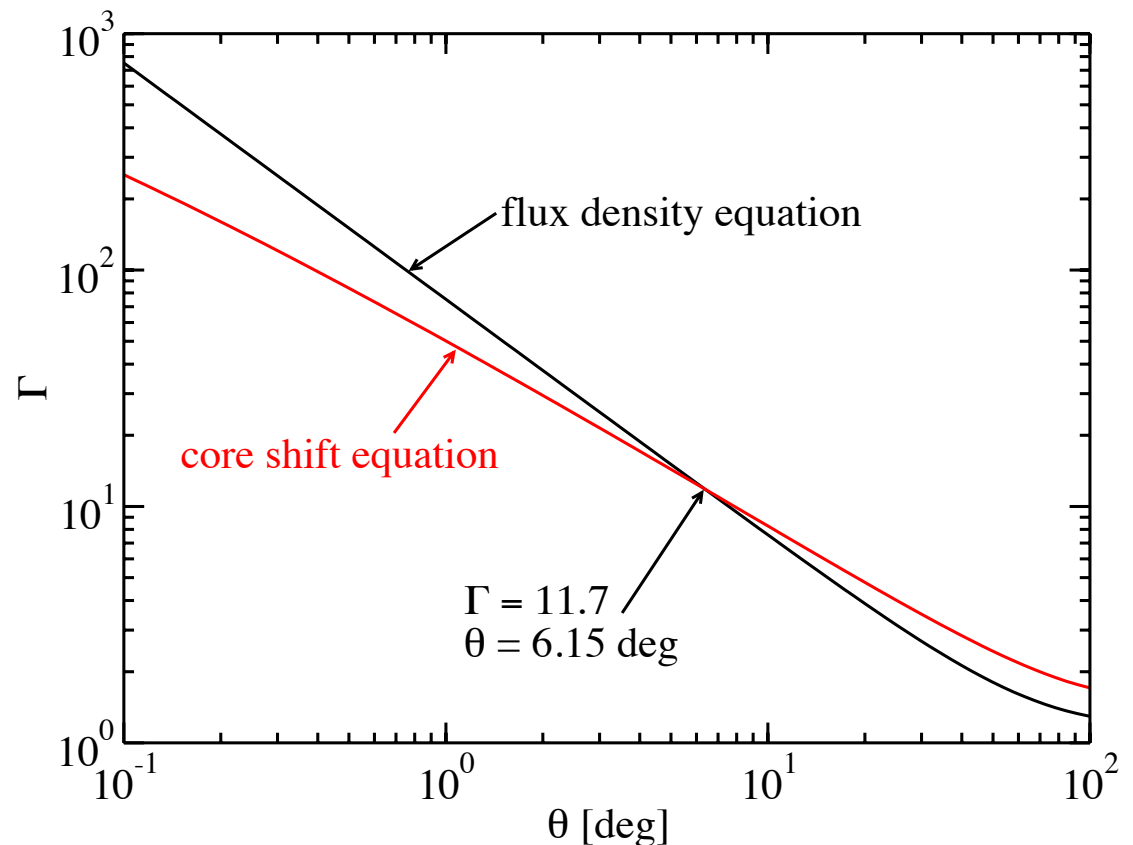




# Finding Jet Parameters

*Nuisance parameters drawn from flat priors:*

1. electron distribution parameters
  1.  $\log(\gamma_1)$ : between 0 and 4.
  2.  $\log(\gamma_2)$ : between 3 and 7.
  3.  $p$ : between 1 and 5.
2. equipartition parameters
  1.  $\log(\xi_e) = \log(u_e/u_B)$ : between -1 and 1.
  2.  $\log(\xi_p) = \log(u_p/u_B)$ : between -4 and 1.



*Observables taken from literature:*

1. core flux density → MOJAVE website (e.g. Lister et al. 2009)
2. extended flux density → Meyer et al. (2011)
3. core shift → Pushkarev et al. (2012)
4. apparent opening angle → Pushkarev et al. (2009).

64 sources: 11 BL Lacs, 52 FSRQs, 1 NLSy1

TABLE 1  
BLAZAR RADIO MEASUREMENTS

Source	Alias	Type <sup>a</sup>	$z$	$\log_{10} \left[ \frac{L_{\text{ext}}}{\text{erg s}^{-1}} \right]$	$F_{\nu}(\text{core})$ [Jy]	$2\alpha_{\text{app}}$ [°]	$\Delta\phi$ [mas]
0133+476	DA 55	Q	0.859	41.93	1.781	21.7	0.099
0202+149	4C +15.05	Q	0.405	41.39	0.921	16.4	0.113
0212+735	S5 0212+73	Q	2.367	42.30	3.281	16.4	0.143
0215+015	OD 026	Q	1.715	43.52	1.170	36.7	0.111
0234+285	4C 28.07	Q	1.207	43.21	2.944	19.8	0.239
0333+321	NRAO 140	Q	1.259	42.98	1.343	8.0	0.276
0336-019	4C 28.07	Q	0.852	42.36	2.311	26.8	0.105

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TABLE 2  
BLAZAR JET PARAMETER RESULTS

Source	Alias	$\Gamma$	$\theta$ [°]	$\alpha$ [°]	$B(1 \text{ pc})$ [G]	$\delta_D$	$\beta_{\text{app}}$
0133+476	DA 55	$7.5^{+36.6}_{-5.8}$	$3.6^{+12.6}_{-2.9}$	$0.7^{+2.4}_{-0.6}$	$0.7^{+3.1}_{-0.4}$	$8.2^{+25.7}_{-6.0}$	$4.6^{+28.5}_{-4.2}$
0202+149	4C +15.05	$5.4^{+20.2}_{-3.7}$	$9.1^{+23.2}_{-7.2}$	$1.3^{+3.1}_{-1.0}$	$0.4^{+0.9}_{-0.2}$	$4.2^{+10.6}_{-2.7}$	$3.8^{+14.5}_{-3.1}$
0212+735	S5 0212+73	$8.9^{+34.3}_{-6.8}$	$1.5^{+4.2}_{-1.2}$	$0.2^{+0.6}_{-0.2}$	$2.5^{+15.7}_{-1.9}$	$12.7^{+28.7}_{-9.3}$	$3.8^{+30.6}_{-3.7}$
0215+015	OD 026	$5.8^{+22.1}_{-4.1}$	$9.3^{+24.4}_{-7.5}$	$3.0^{+7.3}_{-2.4}$	$0.7^{+1.8}_{-0.4}$	$4.0^{+10.7}_{-2.6}$	$4.0^{+14.9}_{-3.2}$
0234+285	4C 28.07	$4.0^{+8.9}_{-2.5}$	$14.0^{+23.2}_{-10.2}$	$2.4^{+3.7}_{-1.7}$	$1.2^{+2.9}_{-0.7}$	$2.9^{+4.6}_{-1.6}$	$2.8^{+6.3}_{-2.2}$
0333+321	NRAO 140	$5.4^{+12.1}_{-3.4}$	$14.6^{+24.6}_{-9.7}$	$1.0^{+1.5}_{-0.7}$	$1.7^{+2.5}_{-0.9}$	$2.7^{+4.6}_{-1.5}$	$3.9^{+7.1}_{-2.7}$
0336-019	4C 28.07	$7.7^{+35.1}_{-5.9}$	$4.3^{+13.7}_{-3.5}$	$1.0^{+3.2}_{-0.8}$	$0.6^{+2.4}_{-0.4}$	$7.6^{+22.8}_{-5.5}$	$5.1^{+27.2}_{-4.5}$

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Results for all 64 sources.

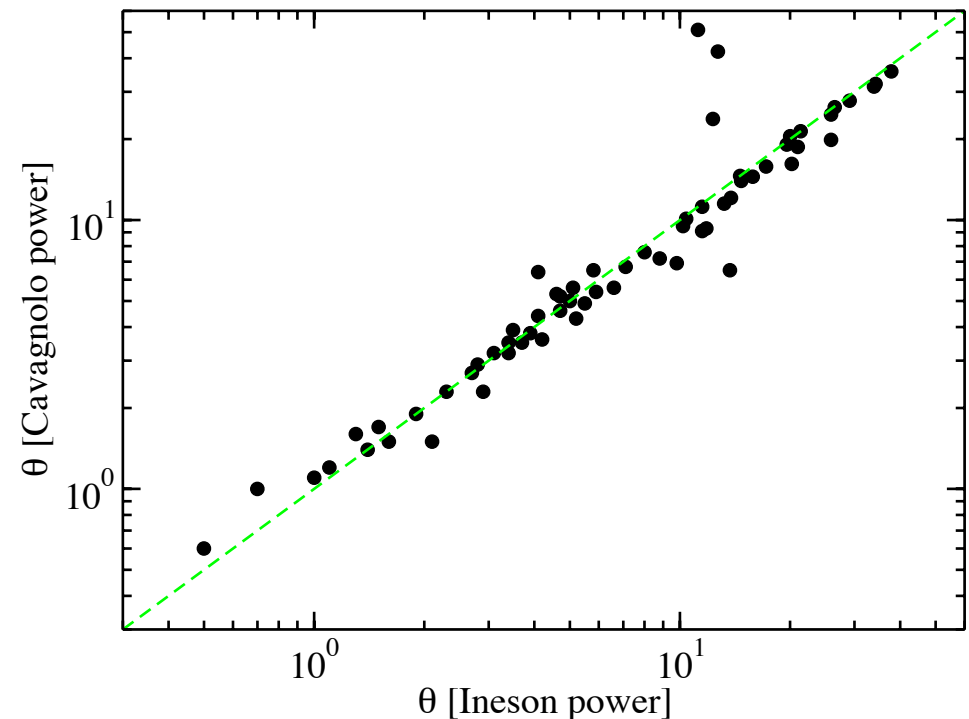
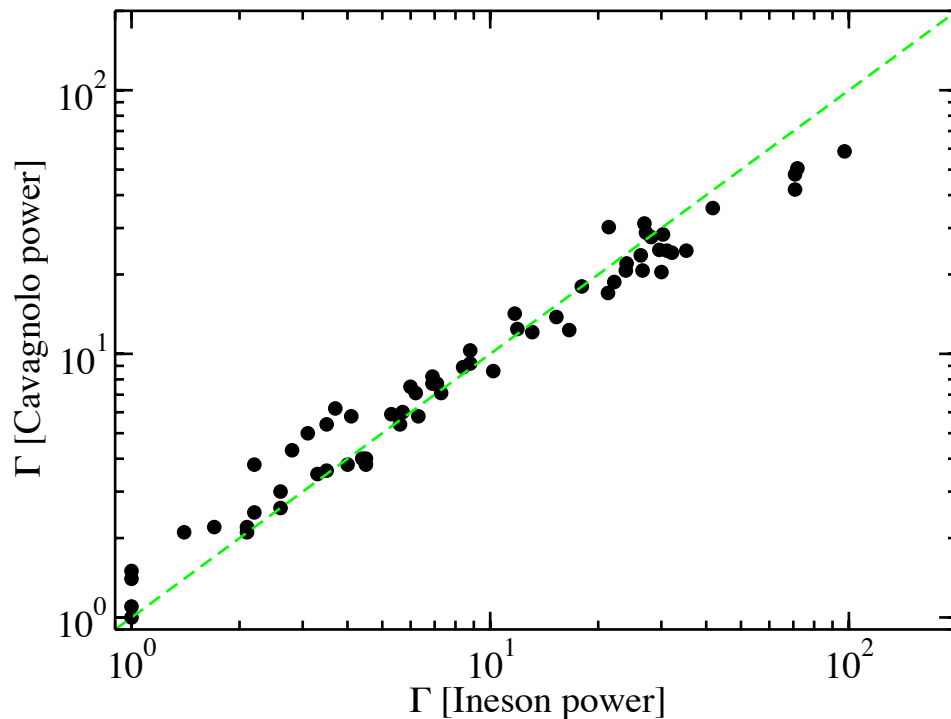
Errors are quite large. Dominated by errors on core shift and unknown electron spectral index.

TABLE 2  
BLAZAR JET PARAMETER RESULTS

Source	Alias	$\Gamma$	$\theta$ [°]	$\alpha$ [°]	$B(1 \text{ pc})$ [G]	$\delta_D$	$\beta_{\text{app}}$
0133+476	DA 55	$7.5^{+36.6}_{-5.8}$	$3.6^{+12.6}_{-2.9}$	$0.7^{+2.4}_{-0.6}$	$0.7^{+3.1}_{-0.4}$	$8.2^{+25.7}_{-6.0}$	$4.6^{+28.5}_{-4.2}$
0202+149	4C +15.05	$5.4^{+20.2}_{-3.7}$	$9.1^{+23.2}_{-7.2}$	$1.3^{+3.1}_{-1.0}$	$0.4^{+0.9}_{-0.2}$	$4.2^{+10.6}_{-2.7}$	$3.8^{+14.5}_{-3.1}$
0212+735	S5 0212+73	$8.9^{+34.3}_{-6.8}$	$1.5^{+4.2}_{-1.2}$	$0.2^{+0.6}_{-0.2}$	$2.5^{+15.7}_{-1.9}$	$12.7^{+28.7}_{-9.3}$	$3.8^{+30.6}_{-3.7}$
0215+015	OD 026	$5.8^{+22.1}_{-4.1}$	$9.3^{+24.4}_{-7.5}$	$3.0^{+7.3}_{-2.4}$	$0.7^{+1.8}_{-0.4}$	$4.0^{+10.7}_{-2.6}$	$4.0^{+14.9}_{-3.2}$
0234+285	4C 28.07	$4.0^{+8.9}_{-2.5}$	$14.0^{+23.2}_{-10.2}$	$2.4^{+3.7}_{-1.7}$	$1.2^{+2.9}_{-0.7}$	$2.9^{+4.6}_{-1.6}$	$2.8^{+6.3}_{-2.2}$
0333+321	NRAO 140	$5.4^{+12.1}_{-3.4}$	$14.6^{+24.6}_{-9.7}$	$1.0^{+1.5}_{-0.7}$	$1.7^{+2.5}_{-0.9}$	$2.7^{+4.6}_{-1.5}$	$3.9^{+7.1}_{-2.7}$
0336-019	4C 28.07	$7.7^{+35.1}_{-5.9}$	$4.3^{+13.7}_{-3.5}$	$1.0^{+3.2}_{-0.8}$	$0.6^{+2.4}_{-0.4}$	$7.6^{+22.8}_{-5.5}$	$5.1^{+27.2}_{-4.5}$
1101+384	Mrk 421	$1.4^{+2.7}_{-0.4}$	$51.0^{+26.5}_{-41.1}$	$6.7^{+1.9}_{-5.2}$	$0.1^{+0.9}_{-0.1}$	$1.1^{+0.4}_{-0.6}$	$0.8^{+0.8}_{-0.7}$
1652+398	Mrk 501	$1.5^{+2.1}_{-0.5}$	$42.4^{+30.1}_{-38.2}$	$6.3^{+2.8}_{-5.6}$	$0.1^{+1.3}_{-0.1}$	$1.1^{+0.7}_{-0.5}$	$0.8^{+1.0}_{-0.8}$

For Mrk 421, Mrk 501 and other TeV blazars,  $\Gamma$ ,  $\delta_D$  and  $\beta_{\text{app}}$  are low, consistent with observations of jet components.

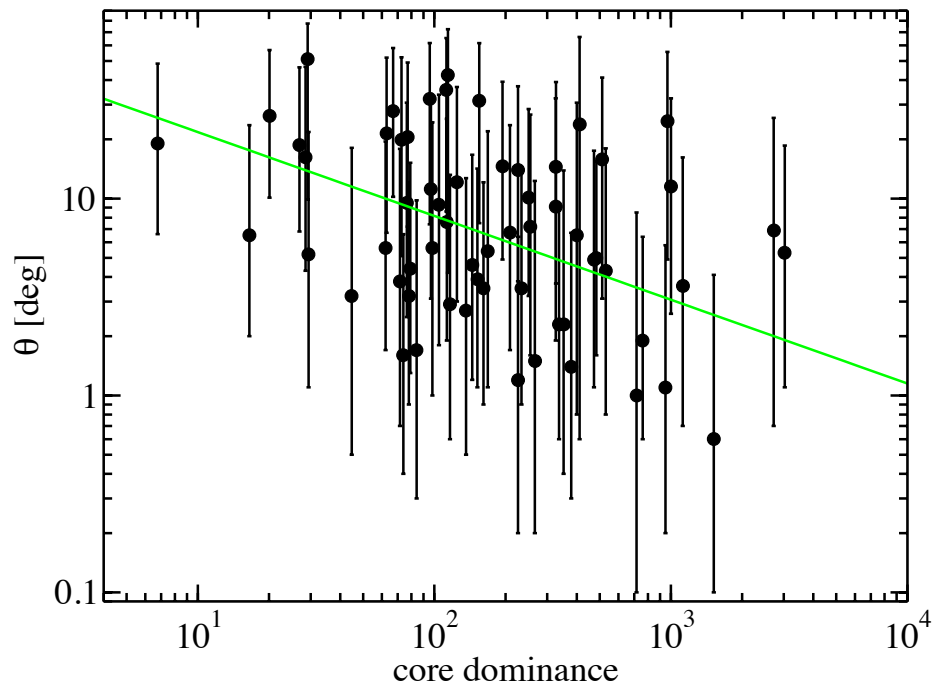
# Expressions for Jet Power



Relation between jet power and extended radio luminosity is controversial (e.g., Godfrey & Shabala 2016). Different expressions for jet power don't have strong effect on results.

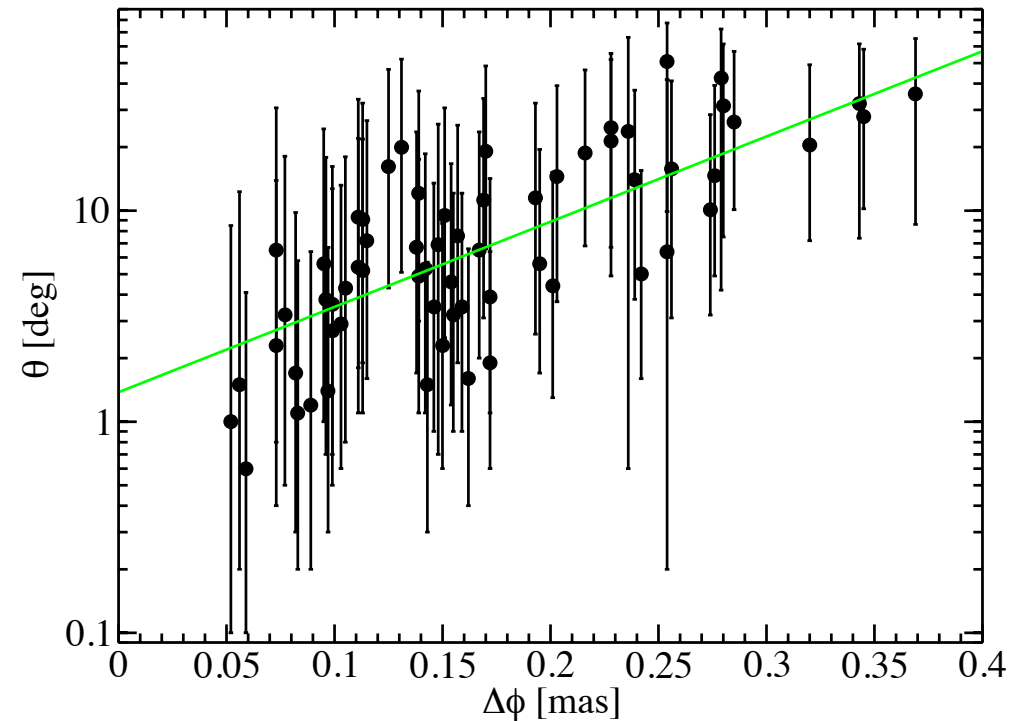
Cavagnolo et al. (2010) versus Ineson et al. (2017).

# Proxies for jet angle



Core dominance: ratio of core to extended radio flux.

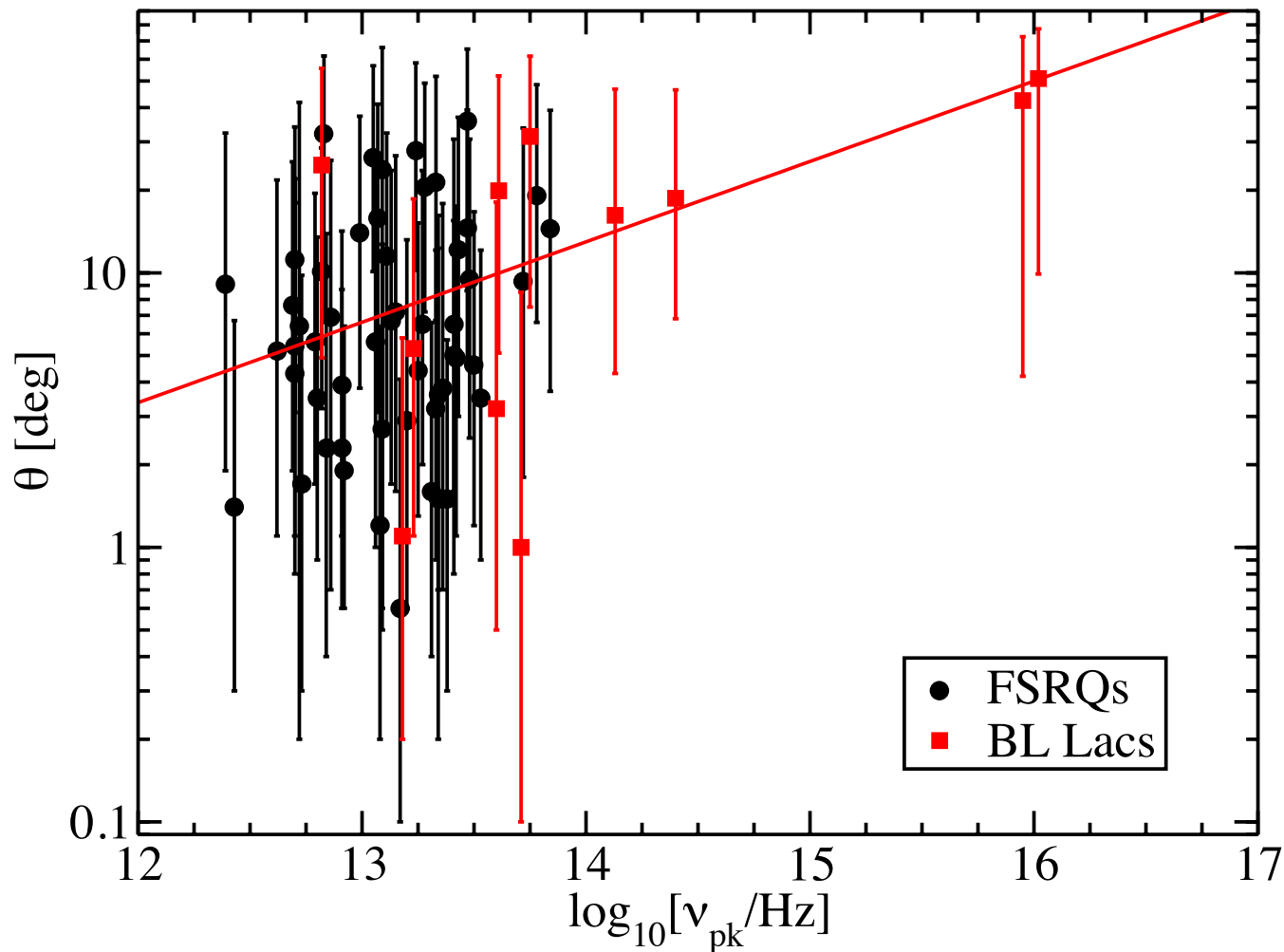
Not significantly correlated with observing angle ( $< 4\sigma$ ).



Core Shift

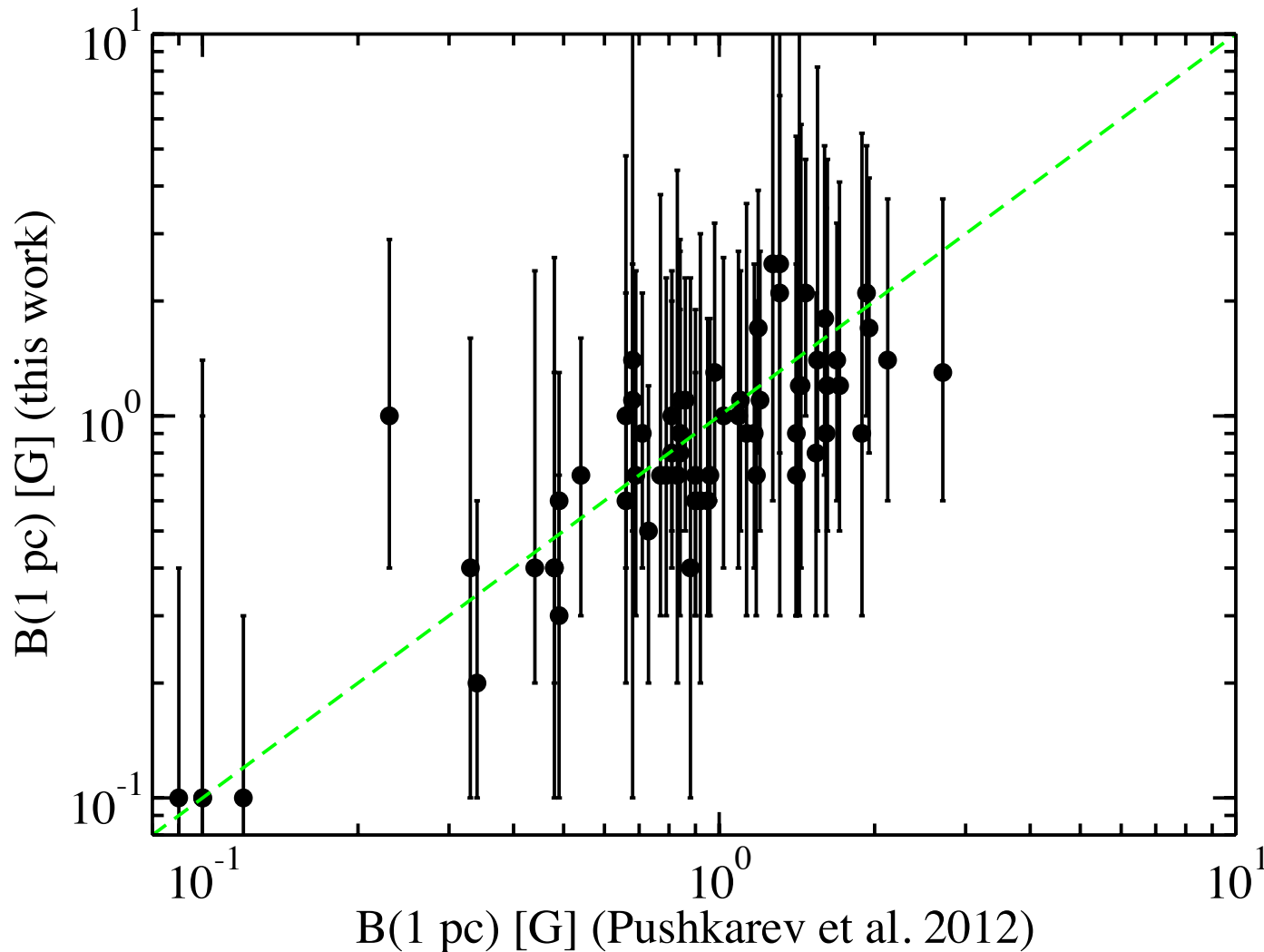
Significantly correlated with observing angle. ( $> 5\sigma$ )

# $\theta$ and $v_{pk}$



Some expectation that  $\theta$  and  $v_{pk}$  are correlated for BL Lacs (Meyer et al. 2011). Did not find significant evidence for this (but large errors and few sources).

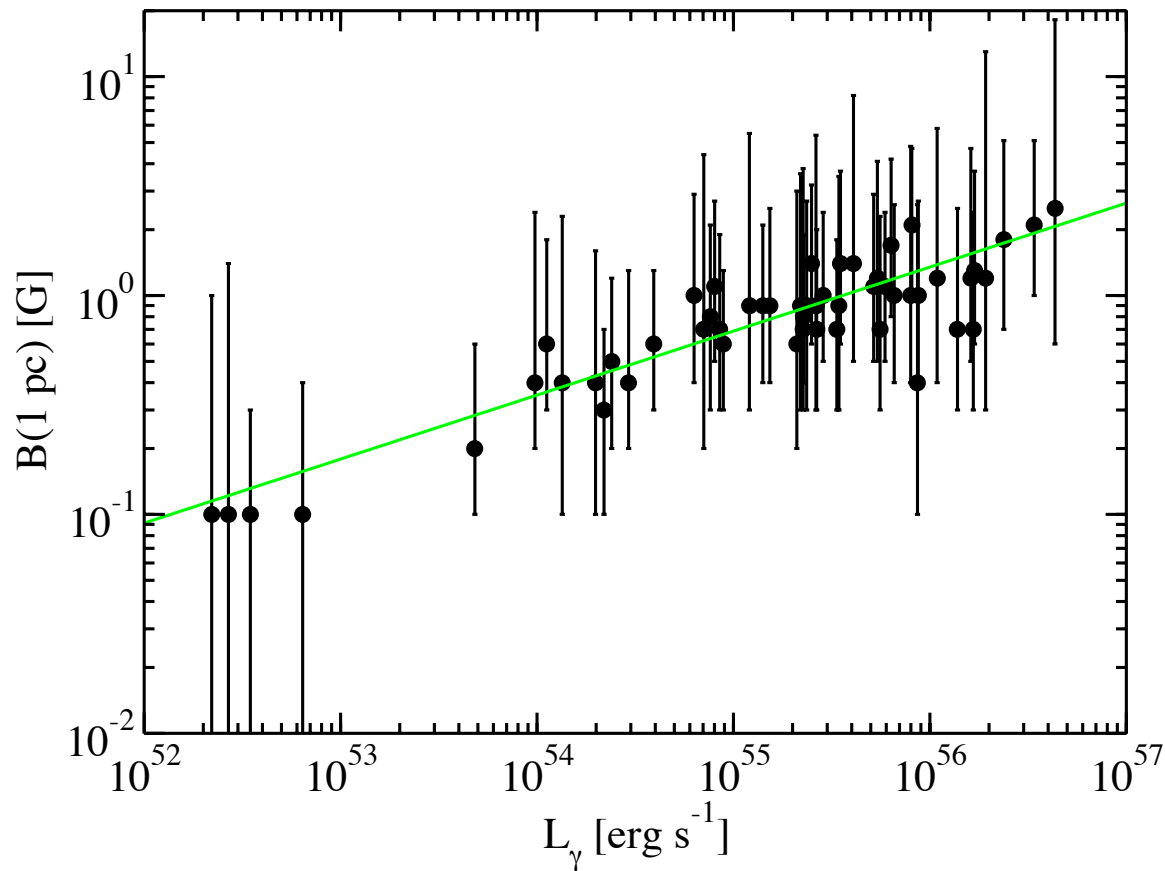
# Magnetic Field



My magnetic field values are consistent with values found by Pushkarev et al. (2012) using a different method.

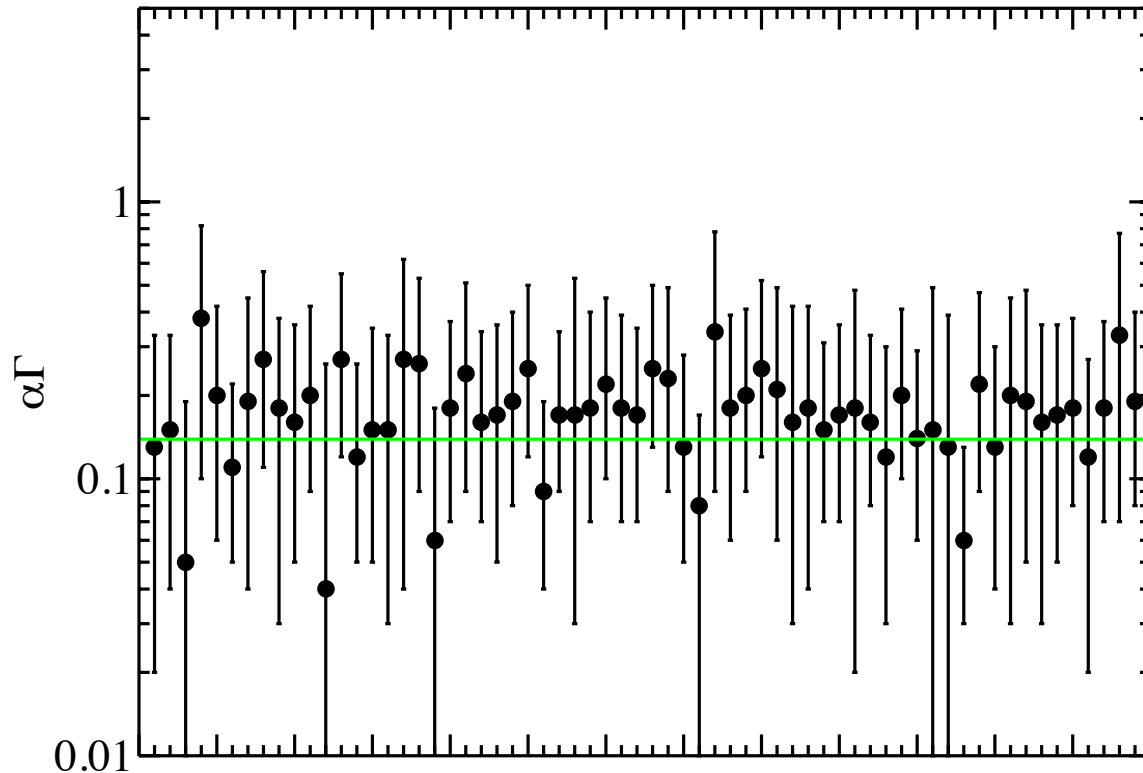


# $\gamma$ -ray luminosity



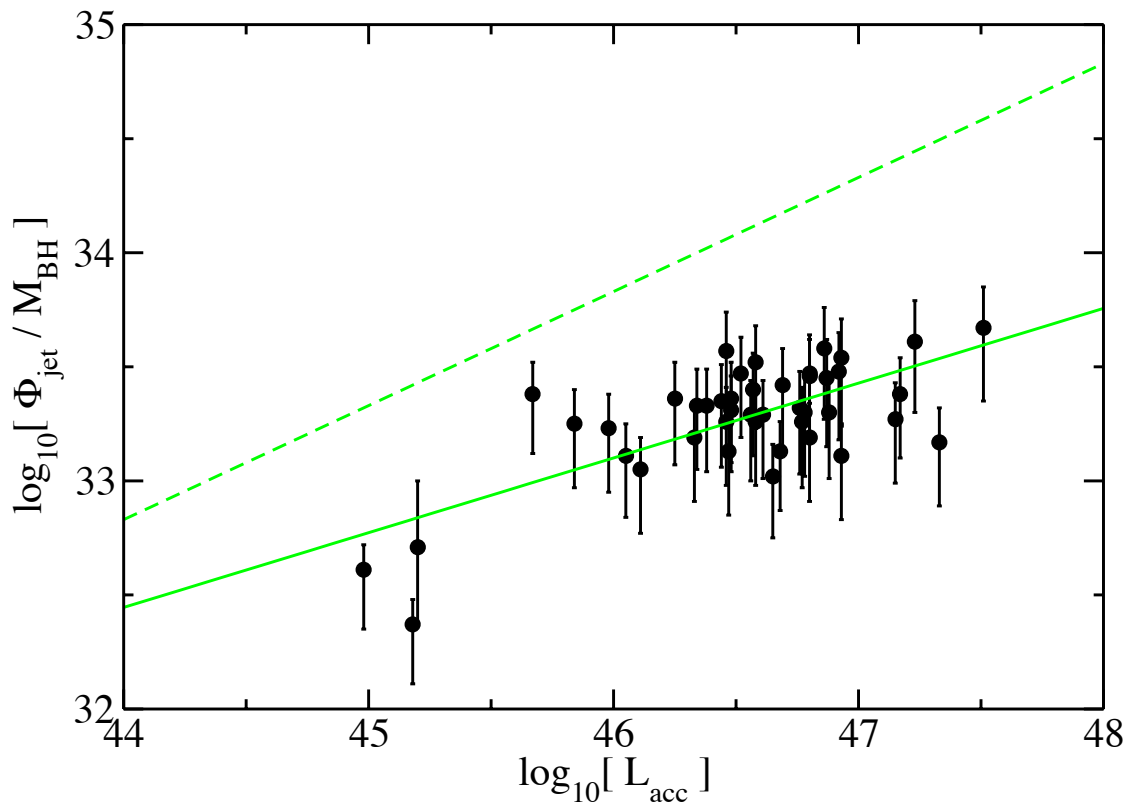
Of all the parameters I determine, magnetic field is best-correlated with  $\gamma$ -ray luminosity ( $> 5\sigma$ ).

But is this a selection effect?  
 $P_j \sim \alpha \Gamma B^2$



My results are consistent with a constant  $\alpha\Gamma$ , i.e.,  $\alpha \sim 1/\Gamma$ .  
Similar results found by others (e.g., Jorstad et al. 2005, 2017; Clausen-Brown et al. 2013; Pushkarev et al. 2009, 2017) .

# Jets from Magnetically-Arrested Disks



Following Zamaninasab et al. (2014)

Parsec-scale magnetic flux can be computed from:

$$\Phi_{\text{jet}} = 1.2 \times 10^{34} \Gamma \alpha \left[ \frac{M_{\text{BH}}}{10^9 M_{\odot}} \right] \left[ \frac{B(1 \text{ pc})}{1 \text{ G}} \right] \text{ G cm}^2$$

Expectation from jets launched from MADs:

$$\log_{10} [\Phi_{\text{jet}}/M_{\text{BH}}] = 0.5 \log_{10} L_{\text{acc}} + 34.4$$

This is **not** consistent with my results. May be due expression above assuming  $a \sim 1$  and  $\eta = 0.4$  for all sources.

# Summary

- I describe a method to determine parameters of parsec-scale blazar jets from observable quantities.
- I compute properties for 64 sources.
- Errors are large. Errors dominated by error in core shift measurement and uncertainty in electron spectral index ( $p$ ). Variability is another issue.
- Properties are consistent with previous results. Results are consistent with slow  $\beta_{\text{app}}$  for many TeV BL Lacs.
- Find little evidence for MAD-launched jets, or scenario of Meyer et al. (2011) ( $\theta$  and  $v_{\text{pk}}$  correlation for BL Lacs).
- A promising method for studying jets, especially if ways can be found to reduce errors!