

# *Scrutiny of recollimation shock in BL Lacertae on sub-pc scales*

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*in collaboration with  
the MOJAVE team*

(<http://www.physics.purdue.edu/MOJAVE>)

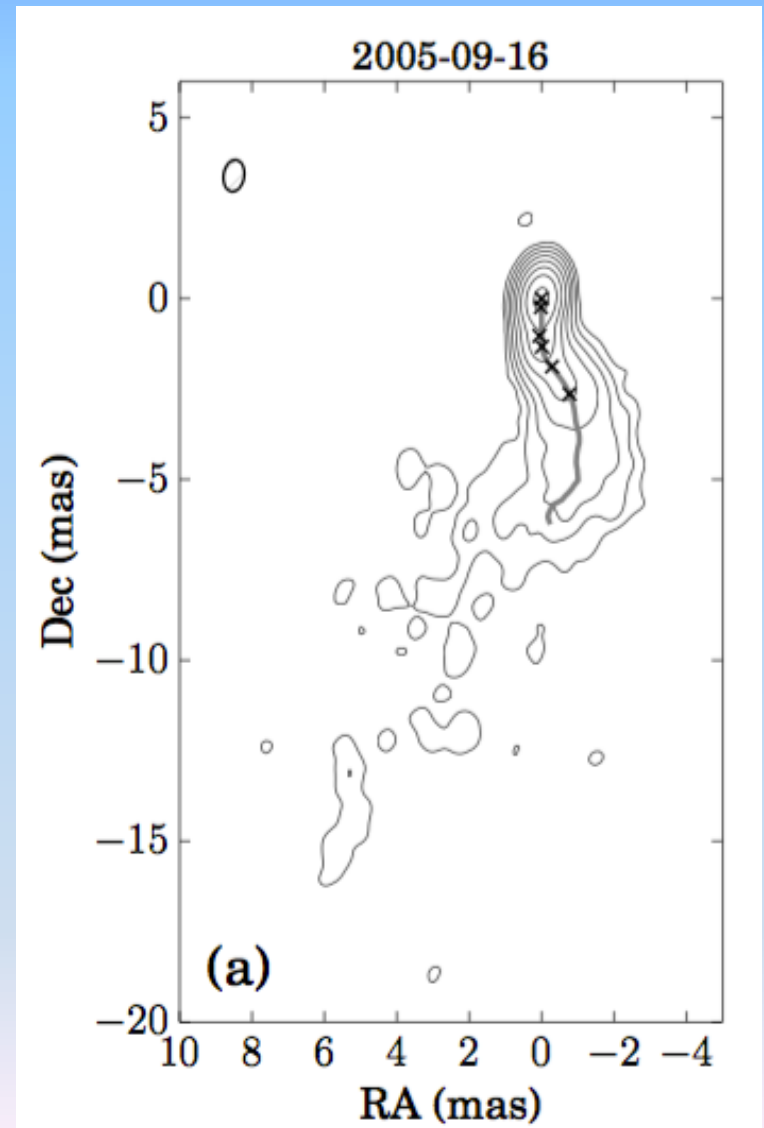
# *Outline*

- Observations and motivation to study a quasi-stationary component (QSC) of the jet.
- Errors of positions and flux leakage effects.
- Trajectory and kinematics of QSC.
- On-sky flux density distribution of QSC.
- Toy emission model.
- Follow-ups and summary.

# Monitoring of BL Lac at 15 GHz

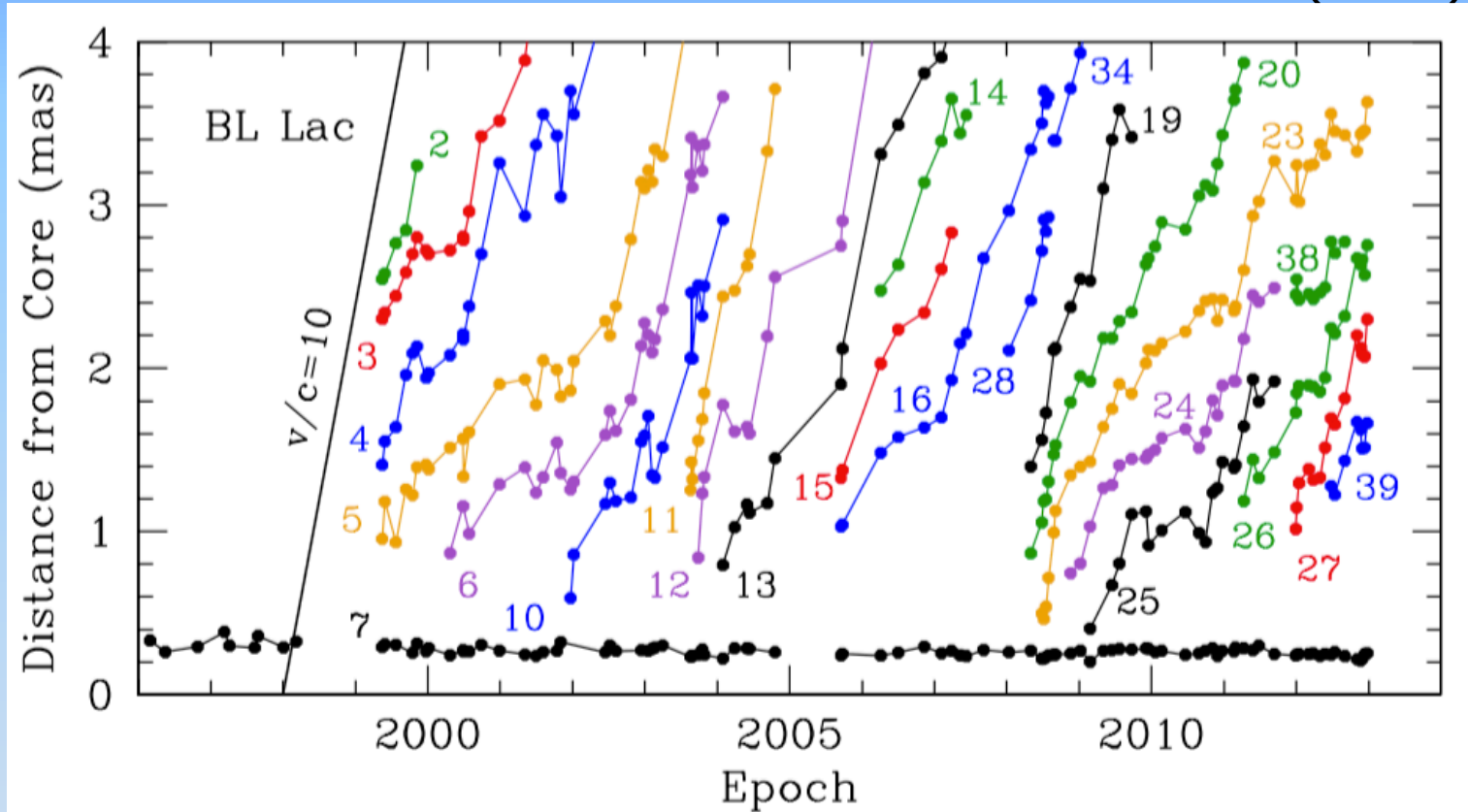
- VLBA monitoring at 15 GHz (1995-2012) in the frame of the MOJAVE program
- Beam size:  $\sim 0.9$  mas
- 1 mas = 1.29 pc
- Jet viewing angle: 4-12 deg

Cohen et al. (2014)



# Core separation

Cohen et al. (2014)

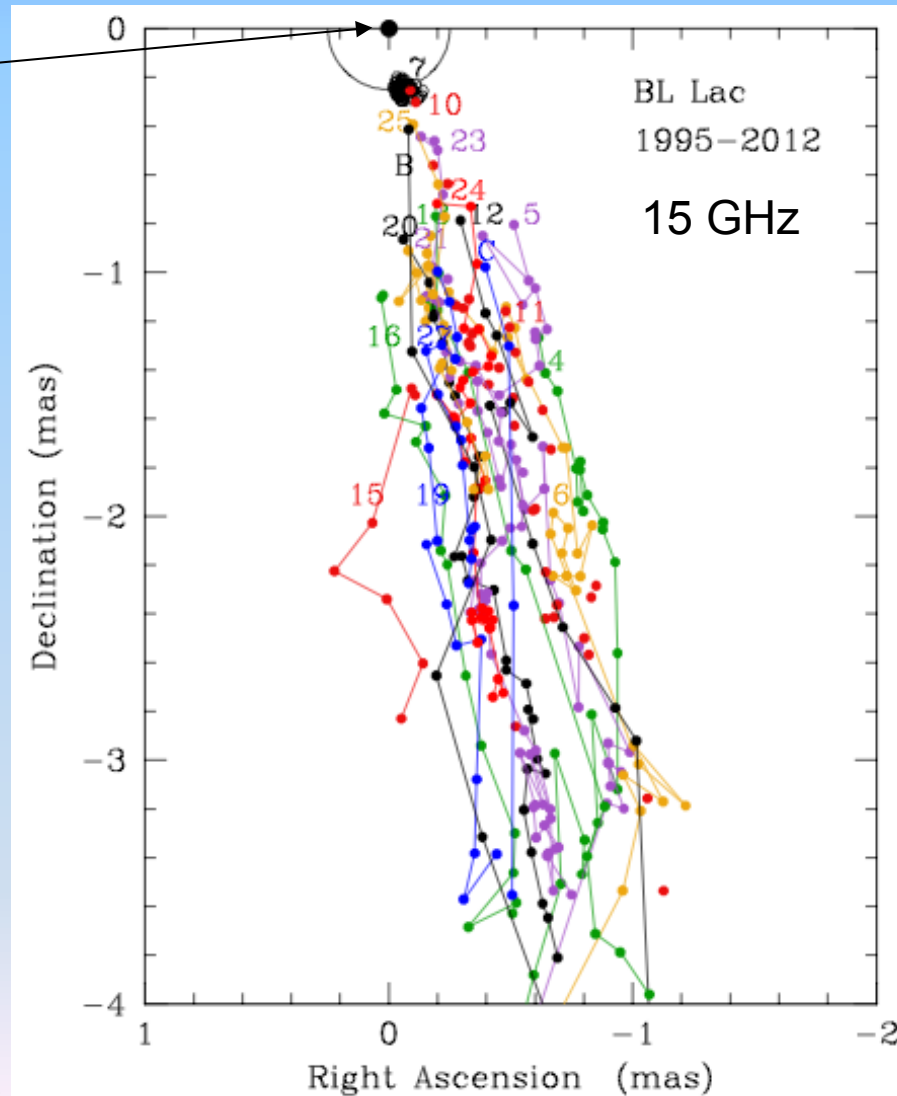


- **D**: radio core
- **C7**: stationary feature
- **[D-C7]**:  $\sim 0.26$  mas (0.34 pc)
- **C2-C8**: moving features  $\sim (3-10)c$ , max. Lorentz factor  $\sim 10$

# Radio core at 15 GHz

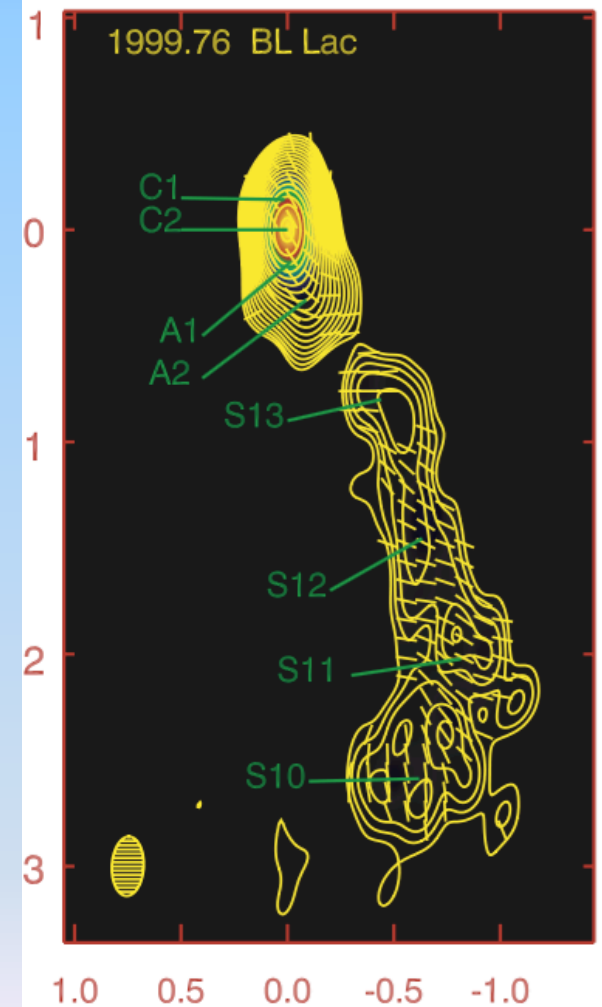
Radio core:  
- flat spectrum  
- reference point  
- compound str.

C7 component:  
- Quasi-stationary  
recollimation shock  
- A2 at 43 GHz  
- tightness of points



Cohen et al. (2014)

Jorstad et al. (2005)

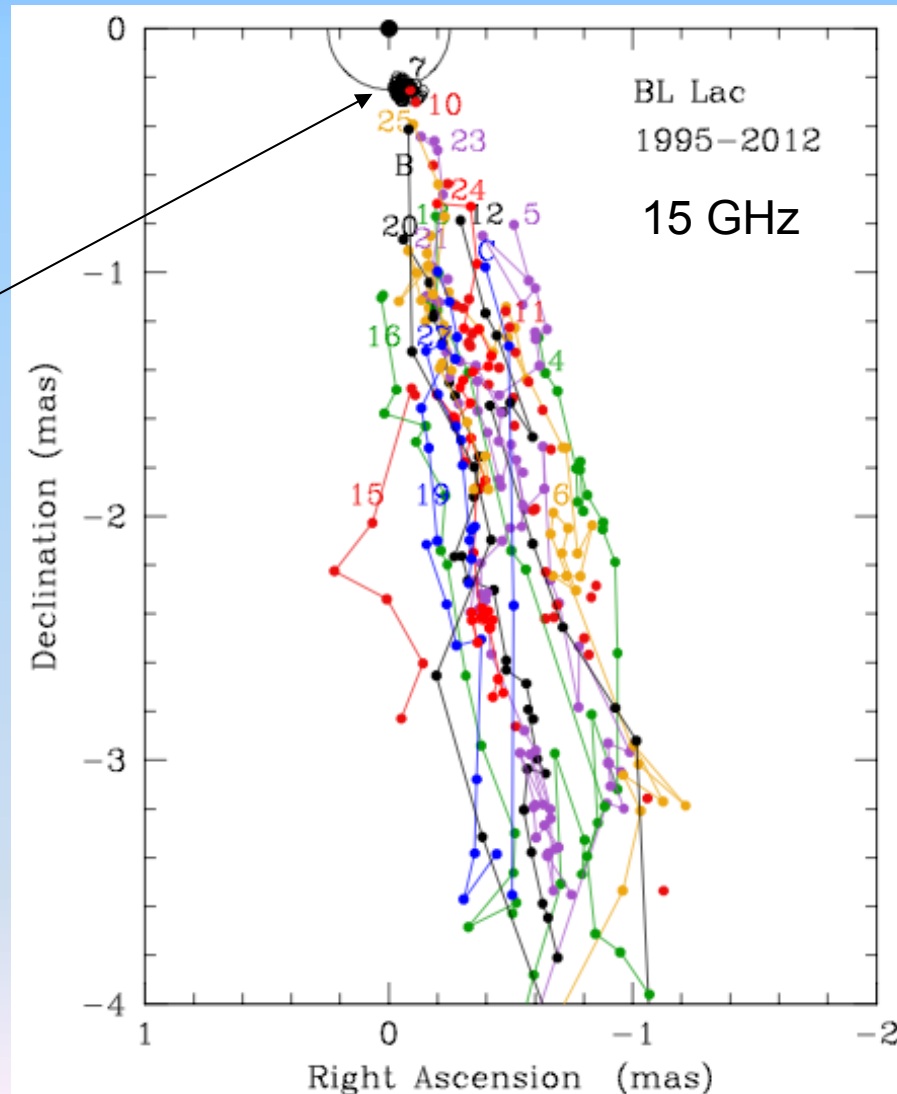


# Recollimation shock and moving features

Radio core:  
- flat spectrum  
- reference point  
- compound str.

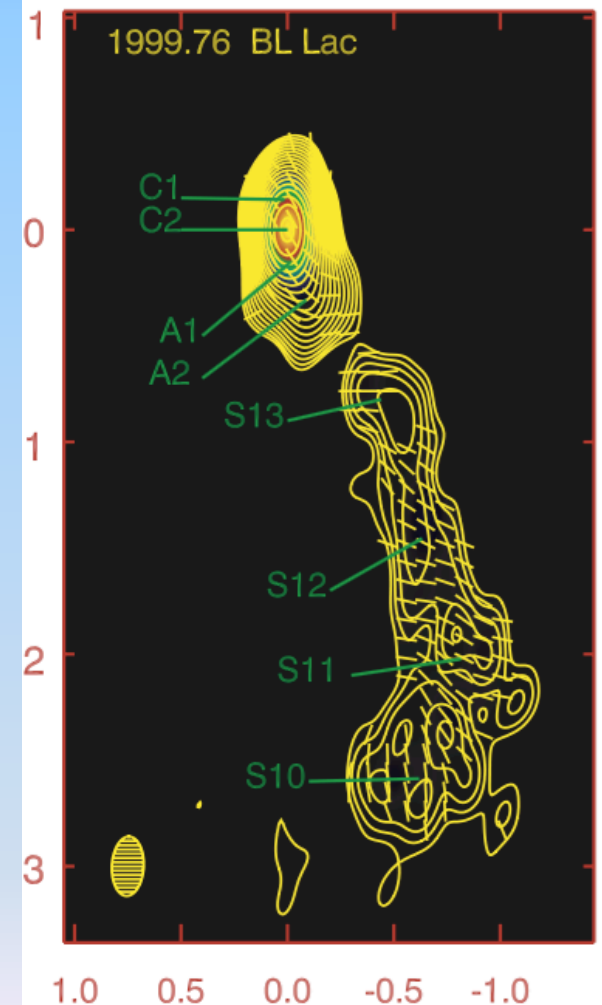
C7 component:  
- Quasi-stationary  
recollimation shock  
- A2 at 43 GHz  
- tightness of points

Moving radio  
components  
emanate from C7:  
- 19 comp.  
- speed  $< 10c$



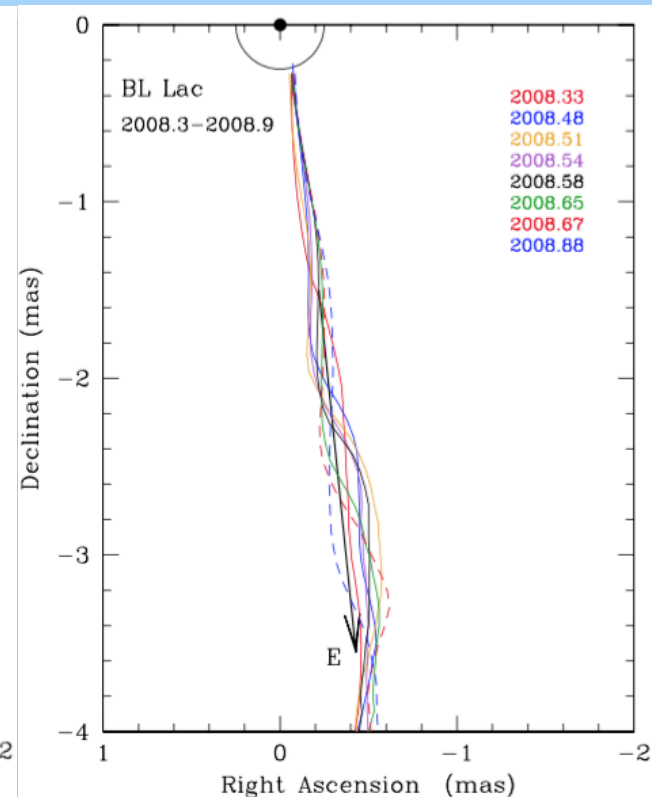
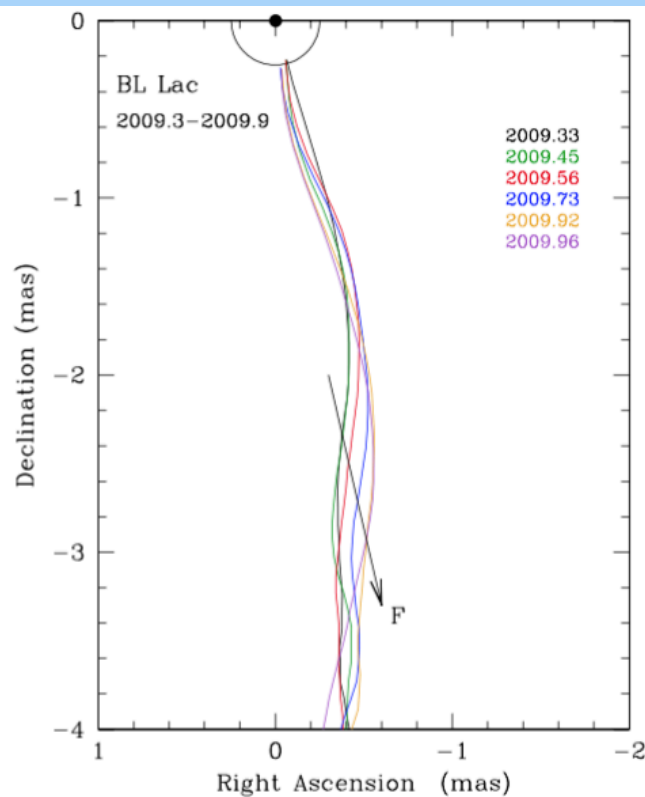
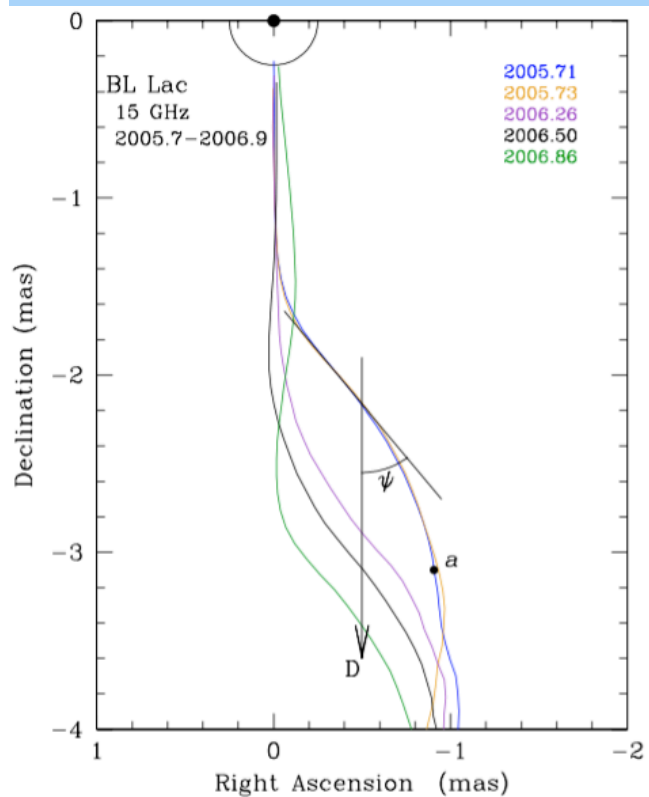
Cohen et al. (2014)

Jorstad et al. (2005)

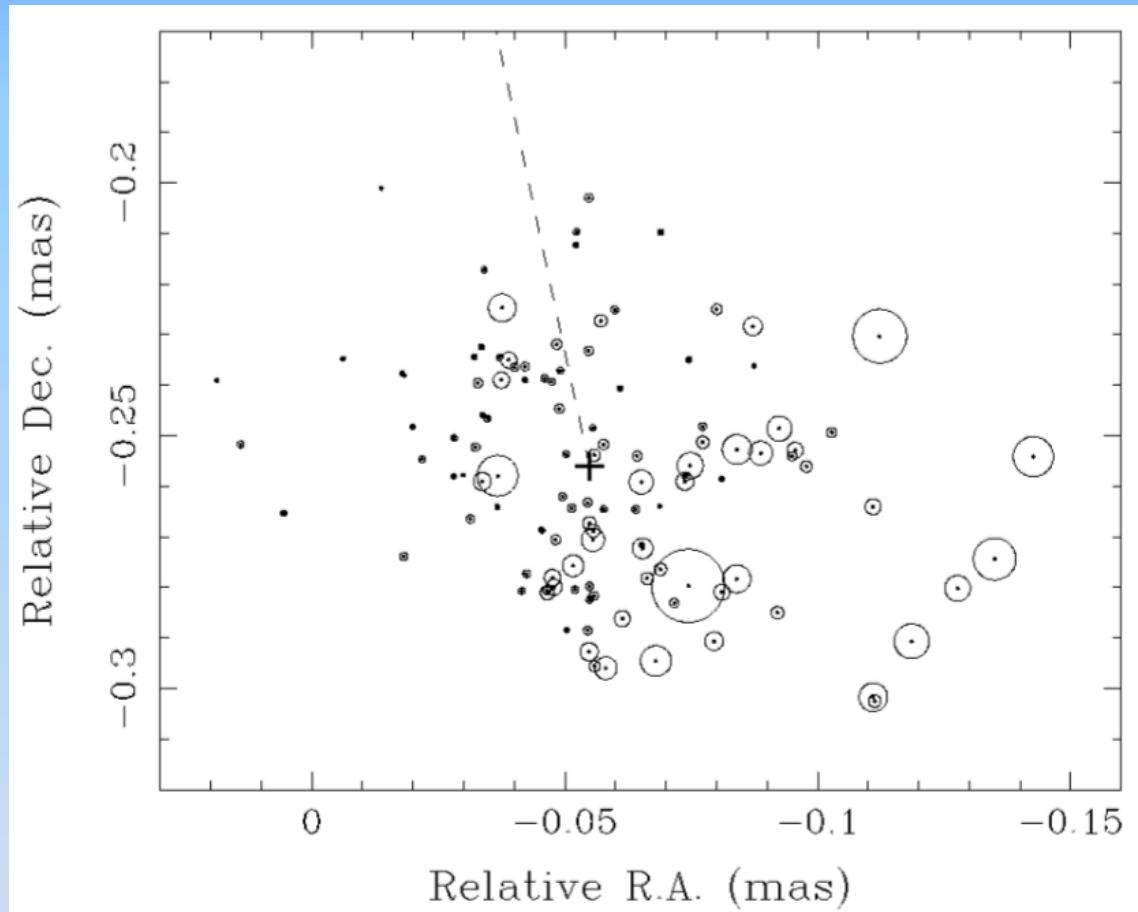


# Motivation

- Comp. C7 is a recollimation shock (RCS)
- Link between position angle of RCS and position angle of jet
- RCS drives the shape of the jet on ps-scales
- “Whip” jet model: relativistic, rapidly shaken RCS generates transverse Alfvén waves propagating downstream on helical magnetic field (Cohen et al. 2014,2015).



# RCS scatter



**Data:** 116 epochs between 1999-2016

Data reduction as in Cohen et al. (2014)

## Reasons of scatter:

- Dynamical/geometry reasons.
- Moving of the core as a result of changes of a pressure/density.
- Intrinsic error of RCS.

## Positional uncertainties:

- Fomalont (1999):  $\sim 1 \mu\text{as}$
- Lobanov (2005):  $\sim 4 \mu\text{as}$

## Limitations:

- Methods apply to an isolated Gaussian  $\rightarrow$  positional error represents the lower limit.



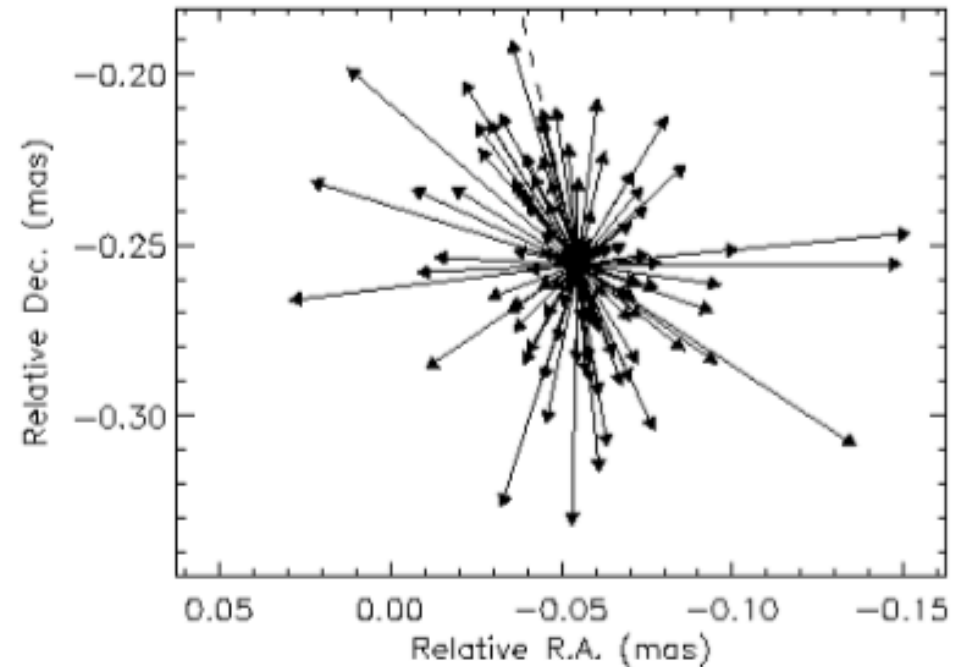
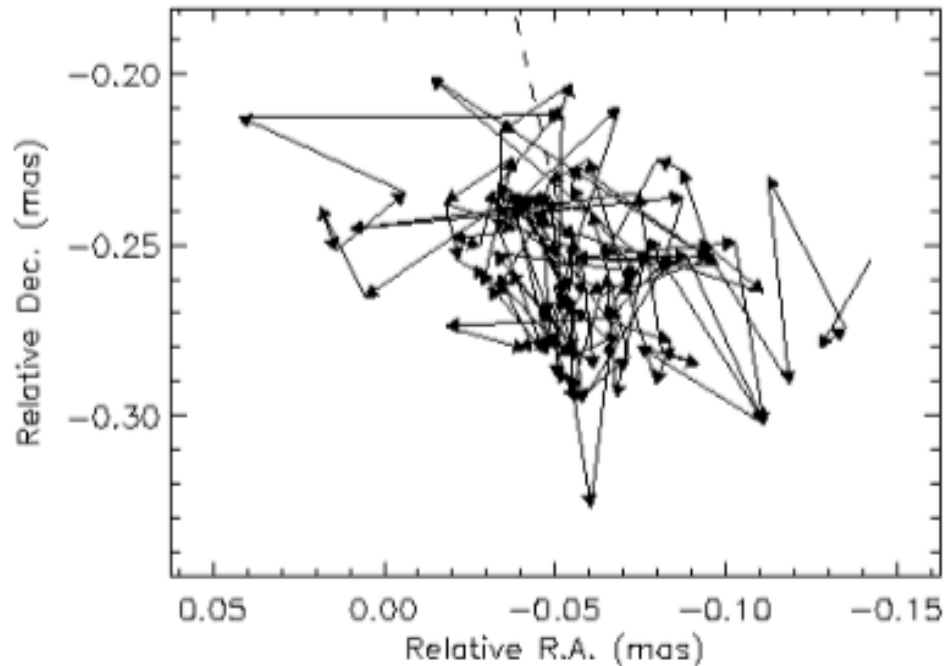
# *RCS: Flux leakage effect*

Effects of flux leakage between bright core and RCS:

- Simulate 116 “observed” (u,v) data sets with constant fluxes of radio core and RCS (2 Jy and 1Jy)
- Add a noise corresponding to the actual data weights.
- Model fit simulated data sets to check (a) dependence between position of RCS and its flux and (b) flux leakage between radio core and RCS:
  - 110/116:  $S_{\text{core}}=1.99 \pm 0.02$  Jy and  $S_{\text{C7}}=1.01 \pm 0.02$  Jy,

We find no dependence between RCS position and flux. Flux leakage is typically small (within 10%) but in rare cases can reach to 50%

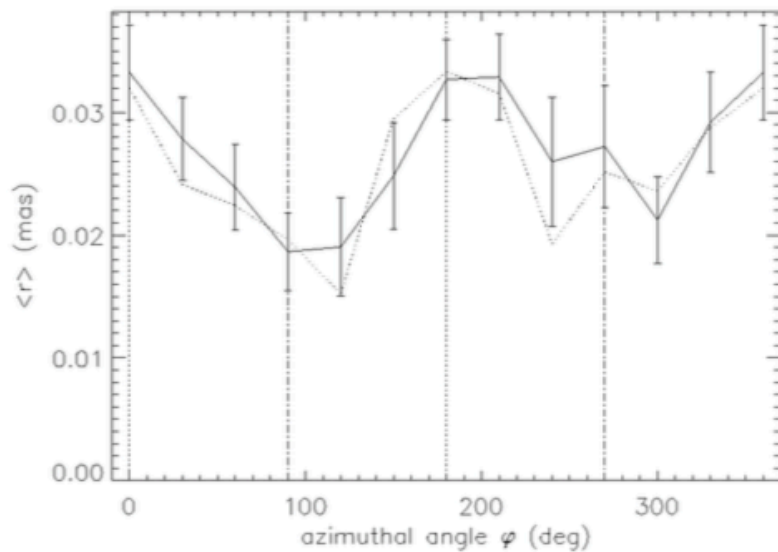
# RCS trajectory



**Motion vector** – motion of RCS between two consequent epochs.

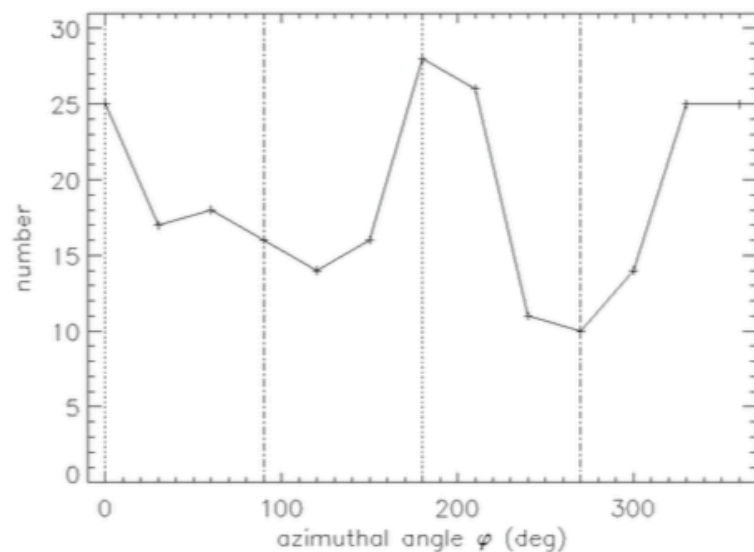
- Six long motion vectors ( $>0.08$  mas) have random orientation – are excluded from further analysis.
- Motion vectors ( $<0.08$  mas) show anisotropy along the jet
- Length of motion vectors are asymmetric wrt the jet axis

# Asymmetry and anisotropy of motion vectors



## Asymmetry:

Mean length of motion vectors along the azimuthal angle (angular beam = 60 deg, step = 30 deg)



## Anisotropy:

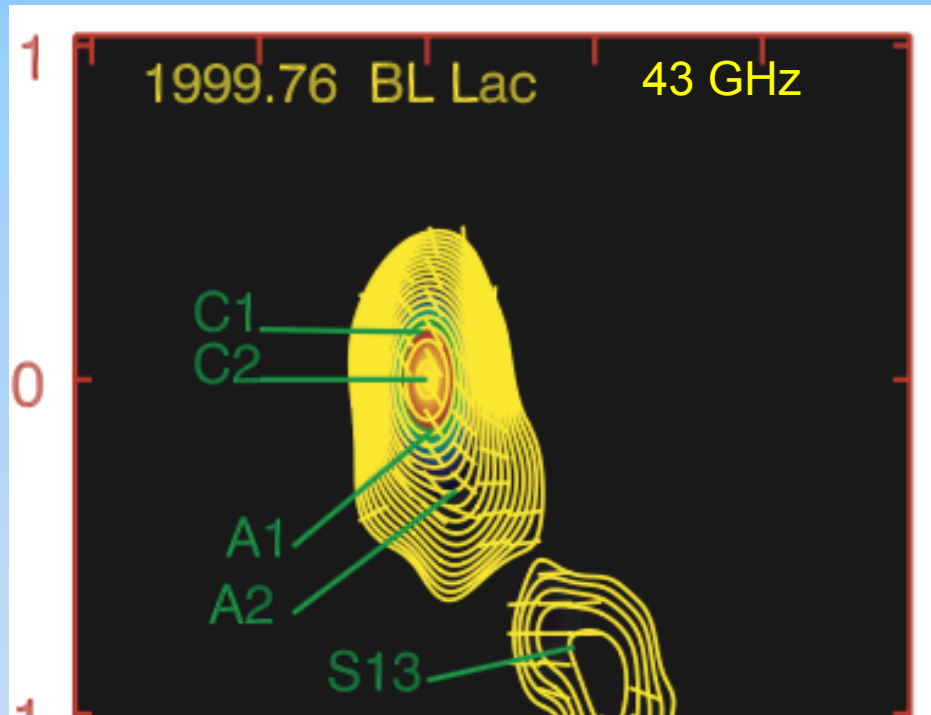
Number of motion vectors along the azimuthal angle (angular beam = 60 deg, step = 30 deg)

# Core „wobbling“

- Resolution-dependent core shift
- Pressure gradient in the external medium (Agudo et al. 2012)
- Binary BH system (e.g., Valtonen et al 2006)
- Variation of flow injection due to changes in the particle density or magnetic field configuration
- ...

# Resolution dependent core-shift

Jorstad et al. (2005)



## 43 GHz:

C1 (weak), C2 (strong), A1 (relatively strong), A2 (intermediate)

## 15 GHz:

- core components C2 and A1
- components observed at 43 GHz
- RCS is identified with A2

Relative brightness of C2 and A1 components will shift the core at 15 GHz along the jet axis

# Estimate of core shift

Apparent (observed) motion-vector of RCS:

$$\vec{r} = -\vec{r}_c + \vec{r}_s + \vec{r}_e$$

$r_c$  – vector of proper motion of the core (along the jet axis)

$r_s$  – vector of proper motion of RCS (random orientation)

$r_e$  – vector of positional error of RCS (random)

$$r_c \gg r_s + r_e \rightarrow \vec{r} \approx -\vec{r}_c$$

$$r_c \ll r_s + r_e \rightarrow \vec{r} \approx \vec{r}_s + \vec{r}_e$$

# Estimate of core shift

Projections of apparent vector-motion on jet axis (j) and transverse to the jet axis (n):

$$r^j = -r_c^j + r_s^j + r_e^j$$

$$r^n = r_s^n + r_e^n$$

**Assumptions:** Motion vectors of RCS and its positional uncertainties are oriented randomly

$$f(r^j) = g * (h * k) = g * p = \int_0^{\infty} \int_0^{\infty} g(r_c^j) p(r^j - r^n) dr_c^j dr^n$$

**f** – observed PDF of apparent motion of RCS

**g** – seeking PDF of core shift

**p** – observed PDF of true motion of RCS

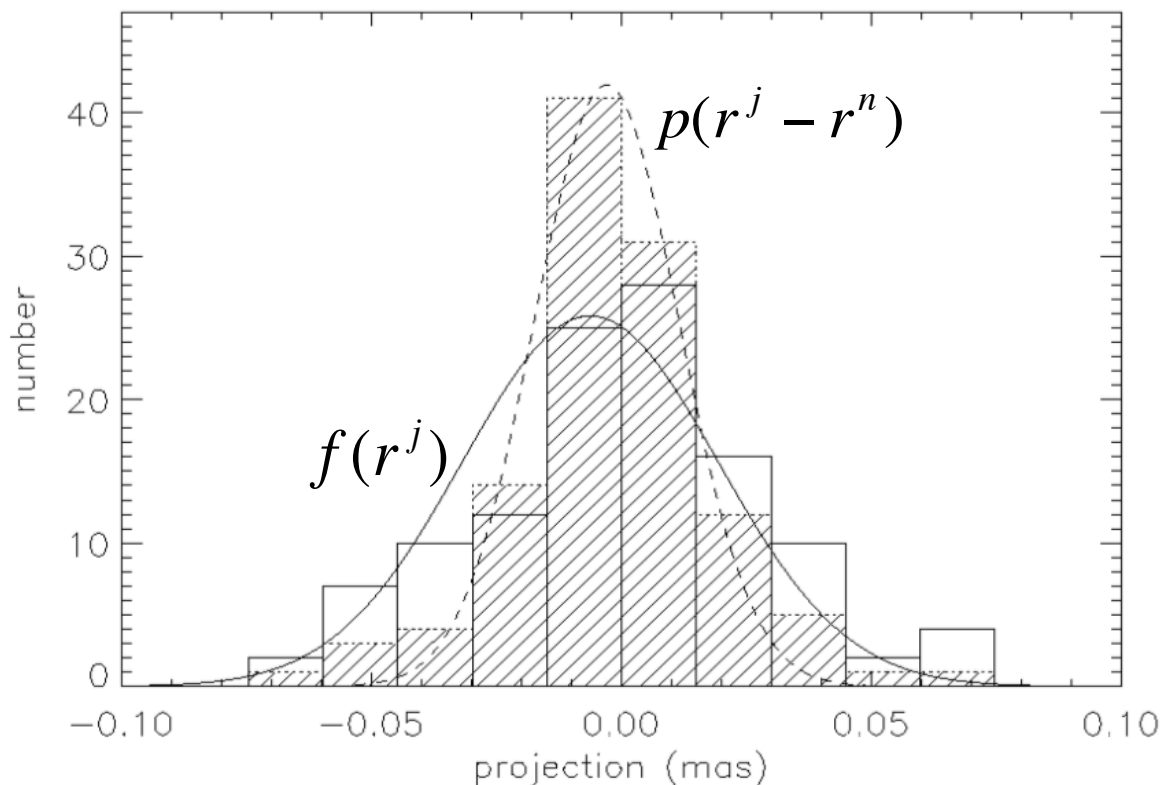
# Estimate of core shift: convolution of Gaussians

$f$  and  $p$  are Gaussian like distributions with

$$\sigma_f = 0.025 \pm 0.002 \text{ mas}$$

$$\sigma_p = 0.015 \pm 0.001 \text{ mas}$$

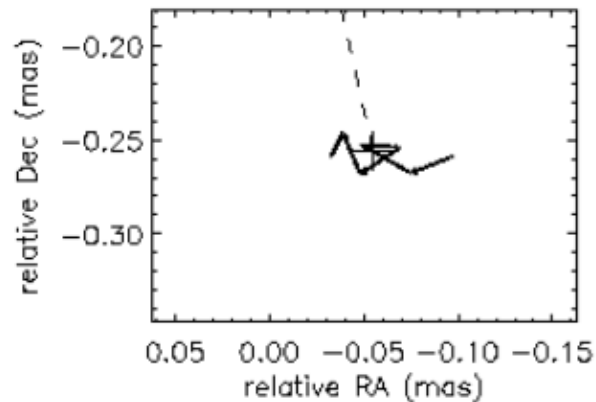
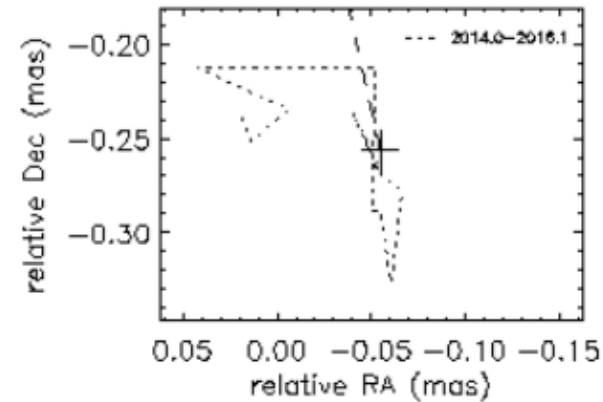
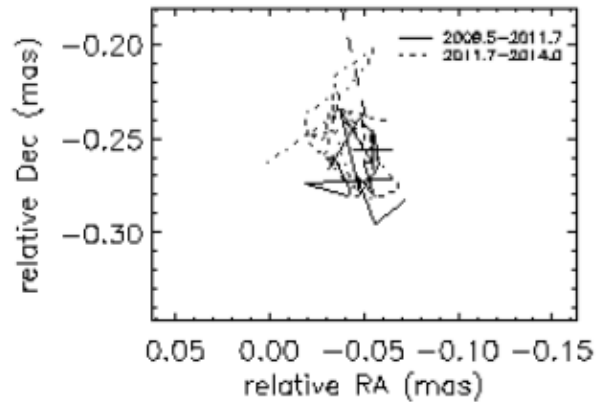
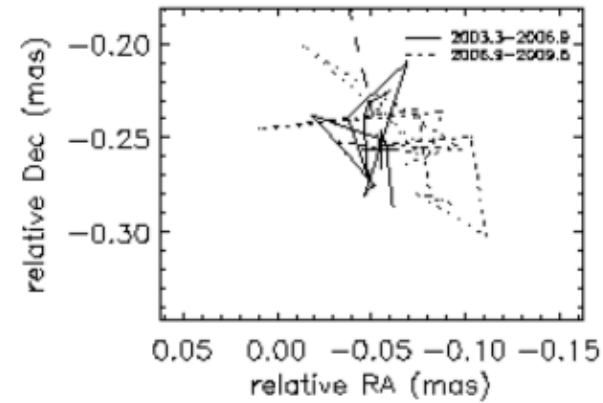
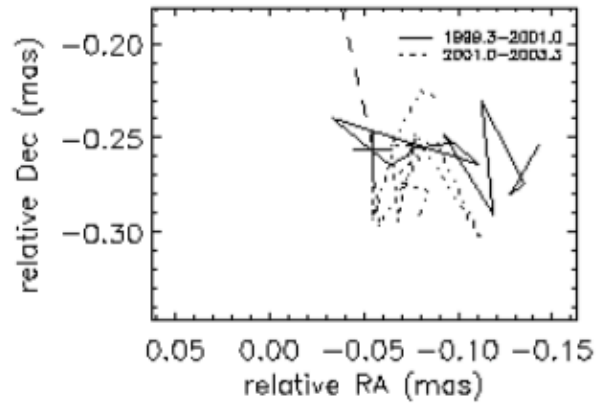
Convolution of two Gaussians ( $f = g * p$ ):  $\sigma_g = (\sigma_f^2 - \sigma_p^2)^{1/2} = 0.021 \pm 0.002 \text{ mas}$



Contribution of core shift  
to apparent motion of RCS  
is significant ( $0.021 \text{ mas} >$   
 $0.015 \text{ mas}$ )



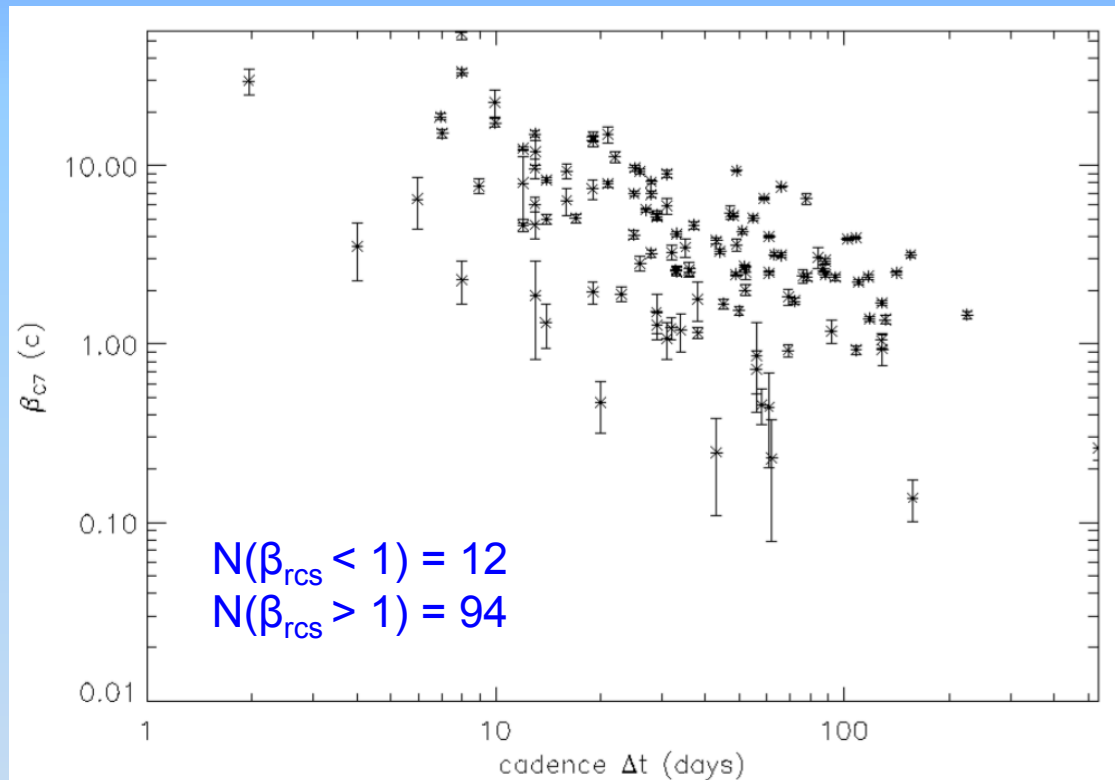
# RCS motion



Time scales of weeks-months: erratic motion

Time scales of years: clock-wise motion (chance prob. 3%)

# RCS kinematics



1. Mean speed measured from observed trajectories:  
 $\langle \beta_{\text{RCS}} \rangle = 4.6 !!!$

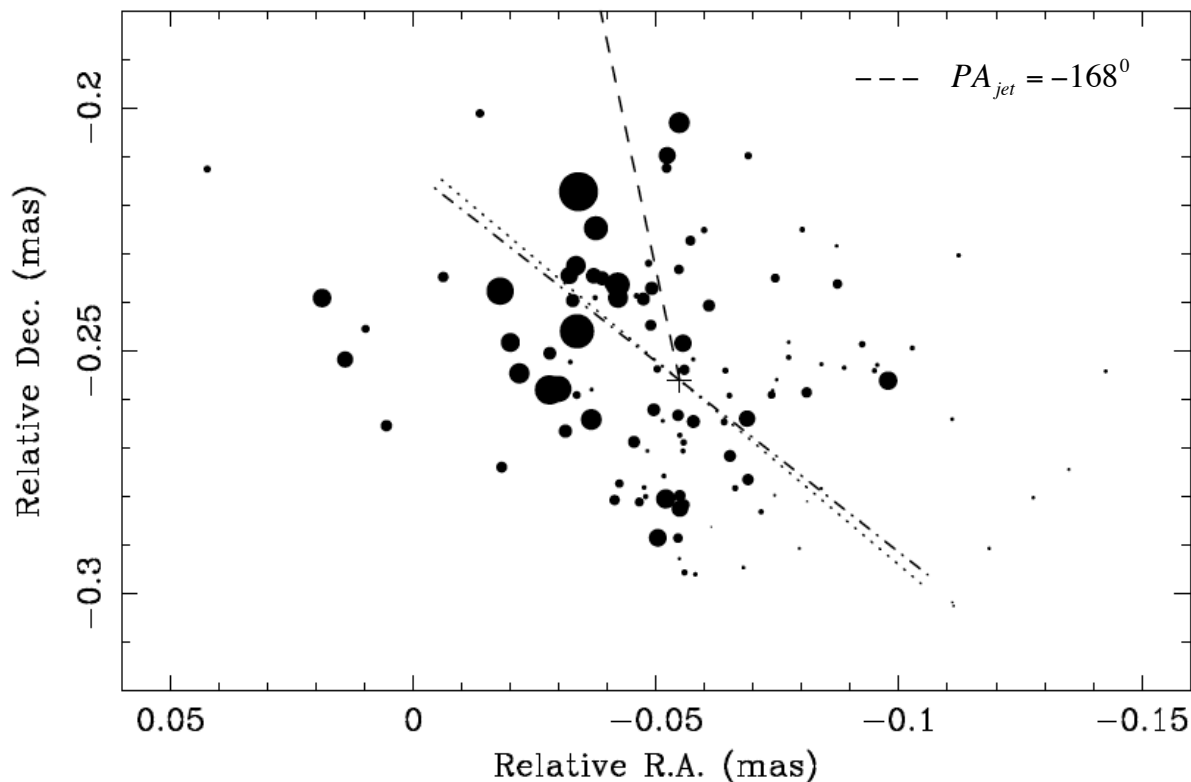
Majority of measured speeds of RCS are superluminal due to resolution-dependent core shift.

2. Mean speed measured from smoothed trajectories:  
 $\langle \beta_{\text{RCS}} \rangle = 0.071 \pm 0.003$

- RCS is a quasi-stationary component
- RCS swings and excites transverse waves propagating downstream the jet (Cohen et al. 2015)
- RCS should move in near face-on plane-like area

RCS should have speeds less than the speed of the light.

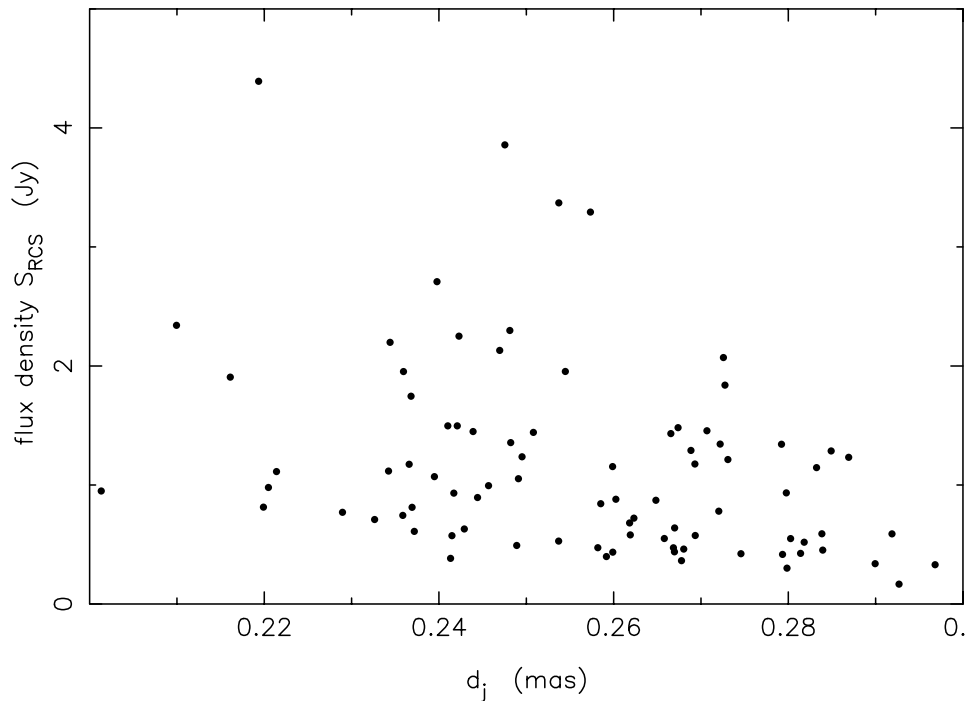
# Distribution of flux density of RCS on sky



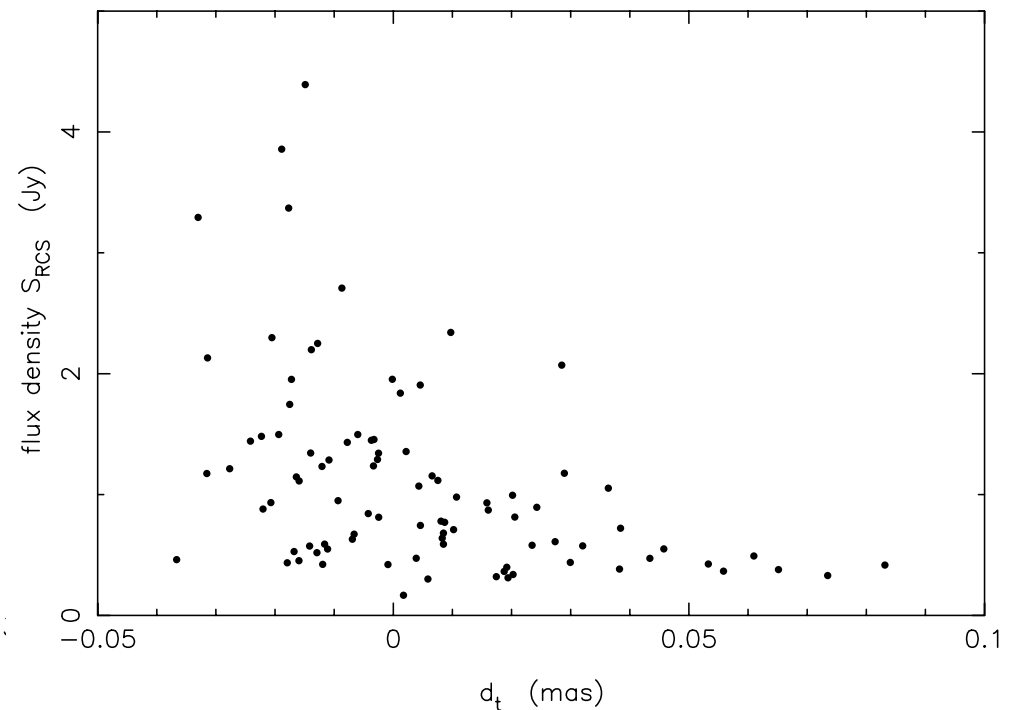
- Flux density range: 0.17-4.4 Jy
- Flux distribution is **asymmetric** along and transverse to the jet central axis ( $PA_{jet} = -168^{\circ}$ , dashed line).

# Asymmetry of flux along and transverse to the jet axis

Along the jet axis



Transverse to the jet axis



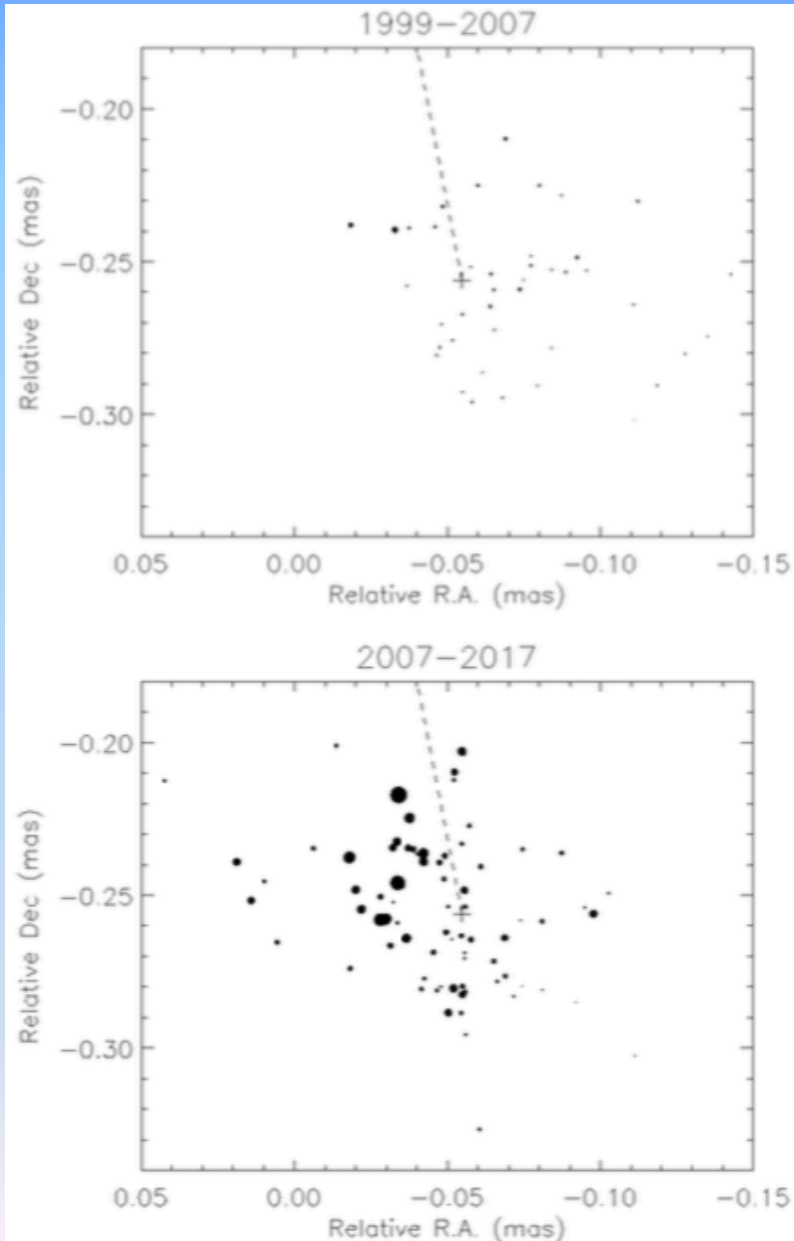
- Kendall's  $\tau$  rank:  $\rho=-0.34$  (c.l. >99.99%).

Significant brightening of RCS close to the core (no flux leakage effect).

- Kendall's  $\tau$ :  $\rho=-0.36$  (c.l. >99.99%)

Significant flux asymmetry with respect to the jet axis.

# *Distribution of flux density*



## **1999-2007**

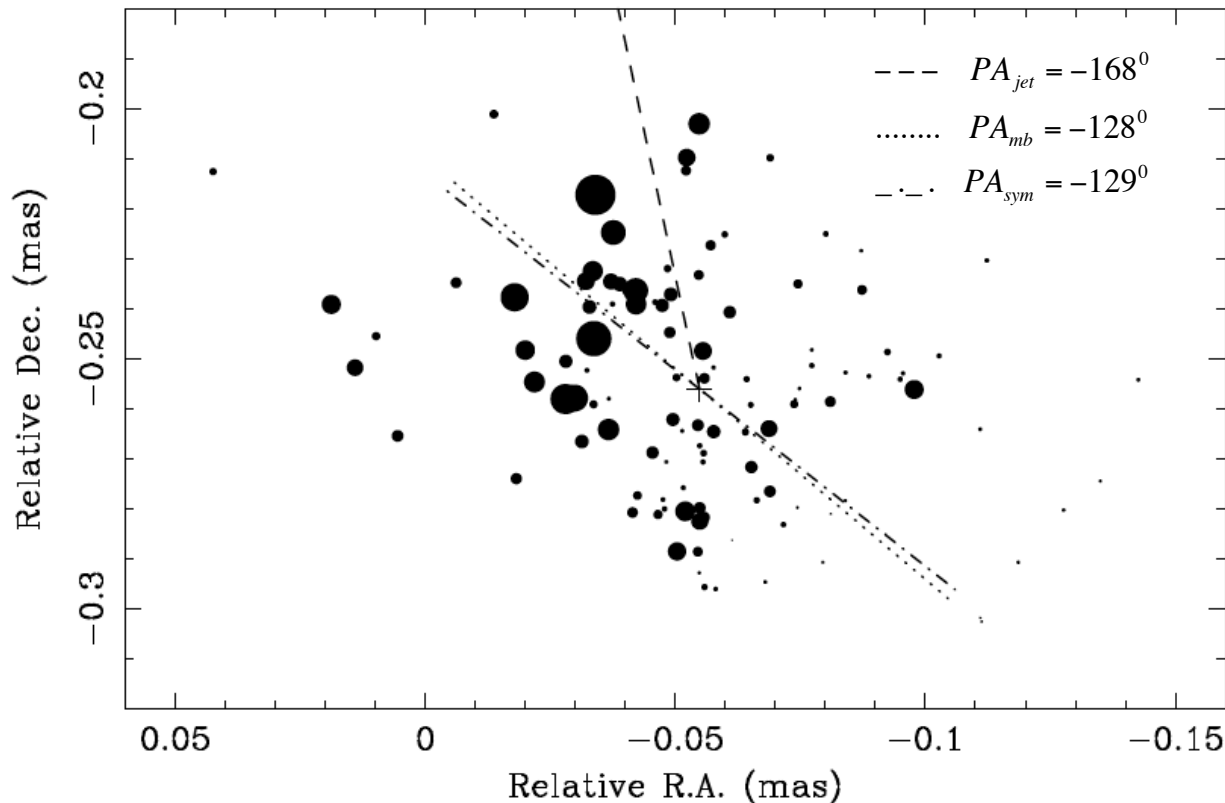
- Asymmetry along the jet:  
Kendall's  $\tau = -0.37$  (c.l. > 99.99%)
- Asymmetry transverse to the jet:  
Kendall's  $\tau$  rank:  $\rho = -0.28$  (c.l. ~ 95%)

## **2007-2017**

- Asymmetry along the jet:  
Kendall's  $\tau = -0.41$  (c.l. > 99.99%)
- Asymmetry transverse to the jet:  
Kendall's  $\tau = -0.31$  (c.l. ~ 96%)

Flux asymmetry is independent of time

# Maximized beaming and flux asymmetry axes



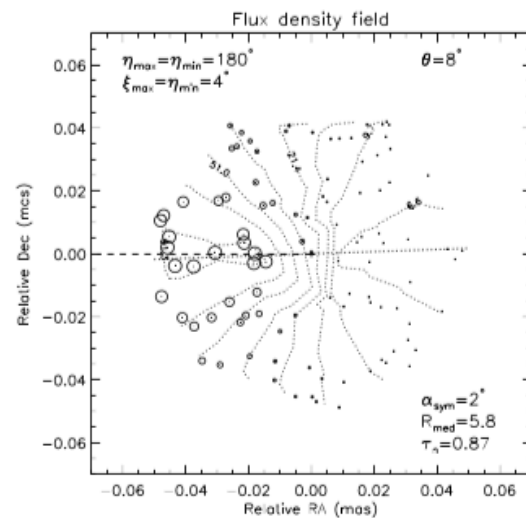
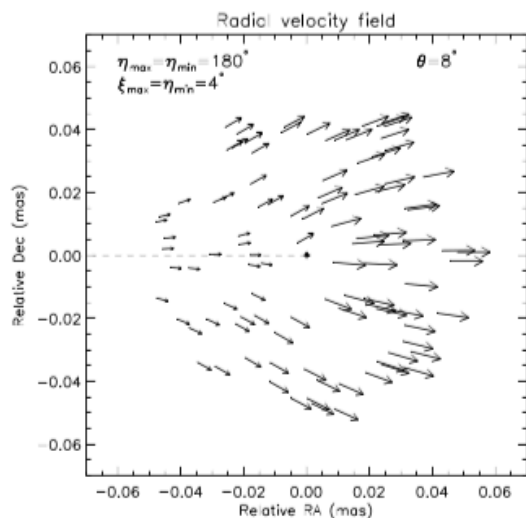
- **Maximized beaming axis:** **Maximum correlation** (Kendall's tau) of the flux happens along the  $PA_{mb} = -128^\circ$  direction (dotted line).

- **Flux asymmetry axis:** This direction represents an axis of reflection symmetry for fluxes transverse to the  $PA_{sym} = -121^\circ$ . **Minimum correlation** of the flux transverse to the direction of  $PA_{sym} = -129^\circ$  (dash-dot line).

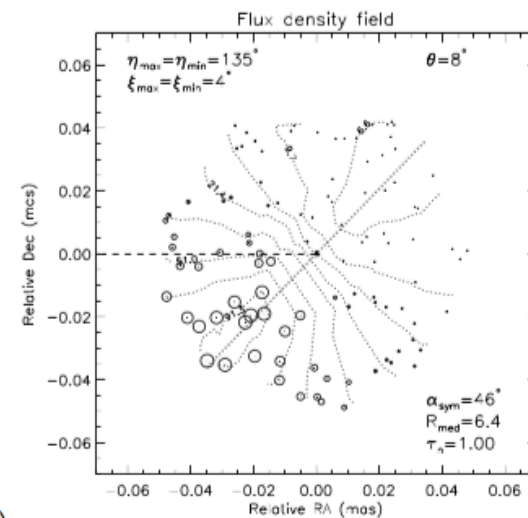
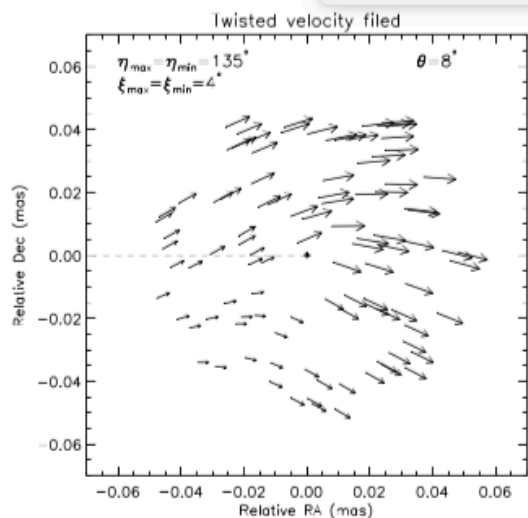
- $PA_{mba} \approx PA_{sym}$ : symmetry axis and maximized beaming axis are aligned!

# Simulations of RCS emission

Radial velocity field



Twisted velocity field



$$S(r, \varphi) = S_0 D(\beta, \theta_j(r, \varphi))^{2-\alpha}$$

Toy model:

- $S_0, \beta$  are constant
- Beaming is due to jet viewing angle  $\theta_j(r, \varphi)$  at RCS's position  $(r, \varphi)$ .

# *Follow-up studies*

## BL Lacertae:

- Trajectory of RCS and origin of transverse waves of jet
- Origin of  $\gamma$ -ray/optical flares.
- Magnetic field structure: polarization properties of RCS.

## RCS data (> 70 epochs) available from the MOJAVE database:

- 0716+714: BL Lac (LAT)
- 0415+379 (3C 111): LSP G (LAT)
- 0851+202 (OJ 287): BL Lac (LAT)
- 1253-055 (3C 279): LSP HPQ (LAT)
- 1641+399 (3C 345): LSP HPQ (LAT)
- 2251+158 (3C 454.3): LSP HPQ (LAT)

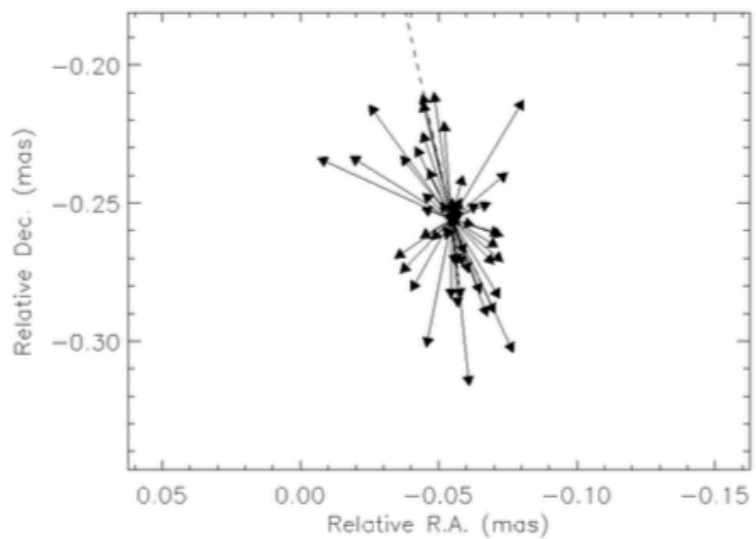
- Use of 43 GHz VLBA data



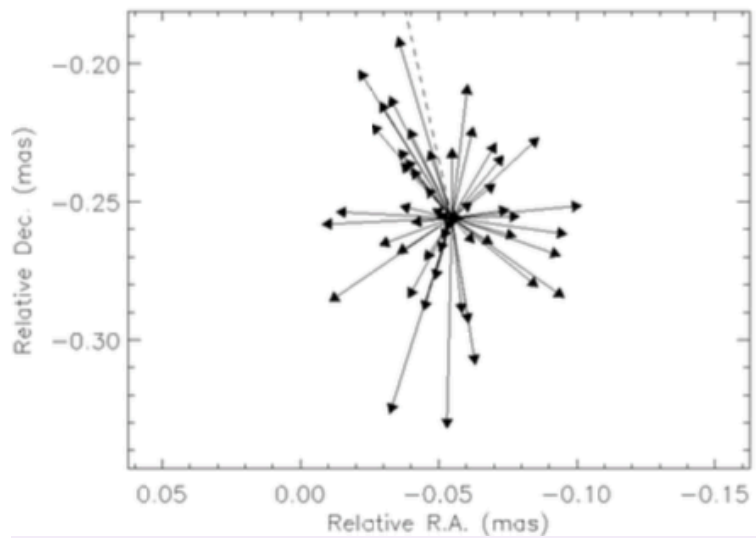
# Summary

- Monitoring of BL Lacertae at 15 GHz:
  - Vector motions of RCS (recollimation shock) are asymmetric along the jet axis – evidence of resolution-dependent core shift.
  - Core motion dominates over intrinsic motion of RCS.
  - RCS moves in clock-wise direction on time scales of few years with subrelativistic speed of about  $0.1c$ .
  - Flux asymmetry along and transverse to the jet axis.
- Simple model of the velocity field of RCS can account for observed flux asymmetry.
- Observations at 43 GHz is important to reveal intrinsic motion of RCS.

# Trajectory of RCS

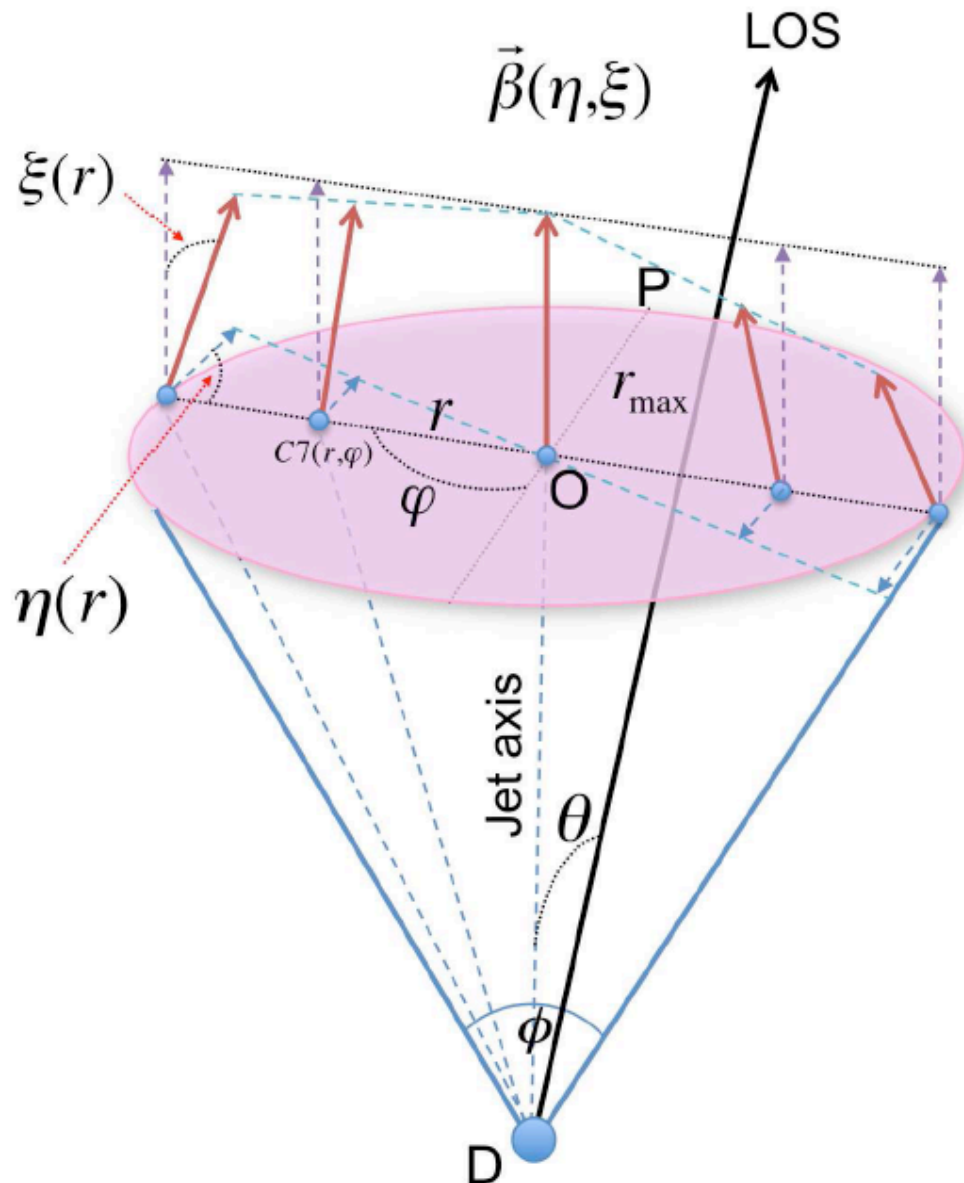


Cadence range:  $\Delta t < 35$  days



Cadence range:  $\Delta t > 35$  days

# RCS model: Velocity field



## Geometry of RCS:

- Plane of RCS motion is normal to the jet axis and within a circle of radius  $r_{\max}$ .
- Location of RCS is given by  $(r, \varphi)$ .
- Jet opening angle:  $\phi = 2\text{atan}^{-1}(R/r_{\max})$ , where  $R$  is a distance between the RCS plane and the core  $D$  (DO).

## Ordered axisymmetric jet velocity field:

- Jet velocity orientation is given by  $\xi(r)$  and  $\eta(r)$ , where  $r$  is a distance of RCS from the jet axis (O).

$$\xi(r) = \frac{\xi_{\max} - \xi_{\min}}{r_{\max}} r + \xi_{\min}$$

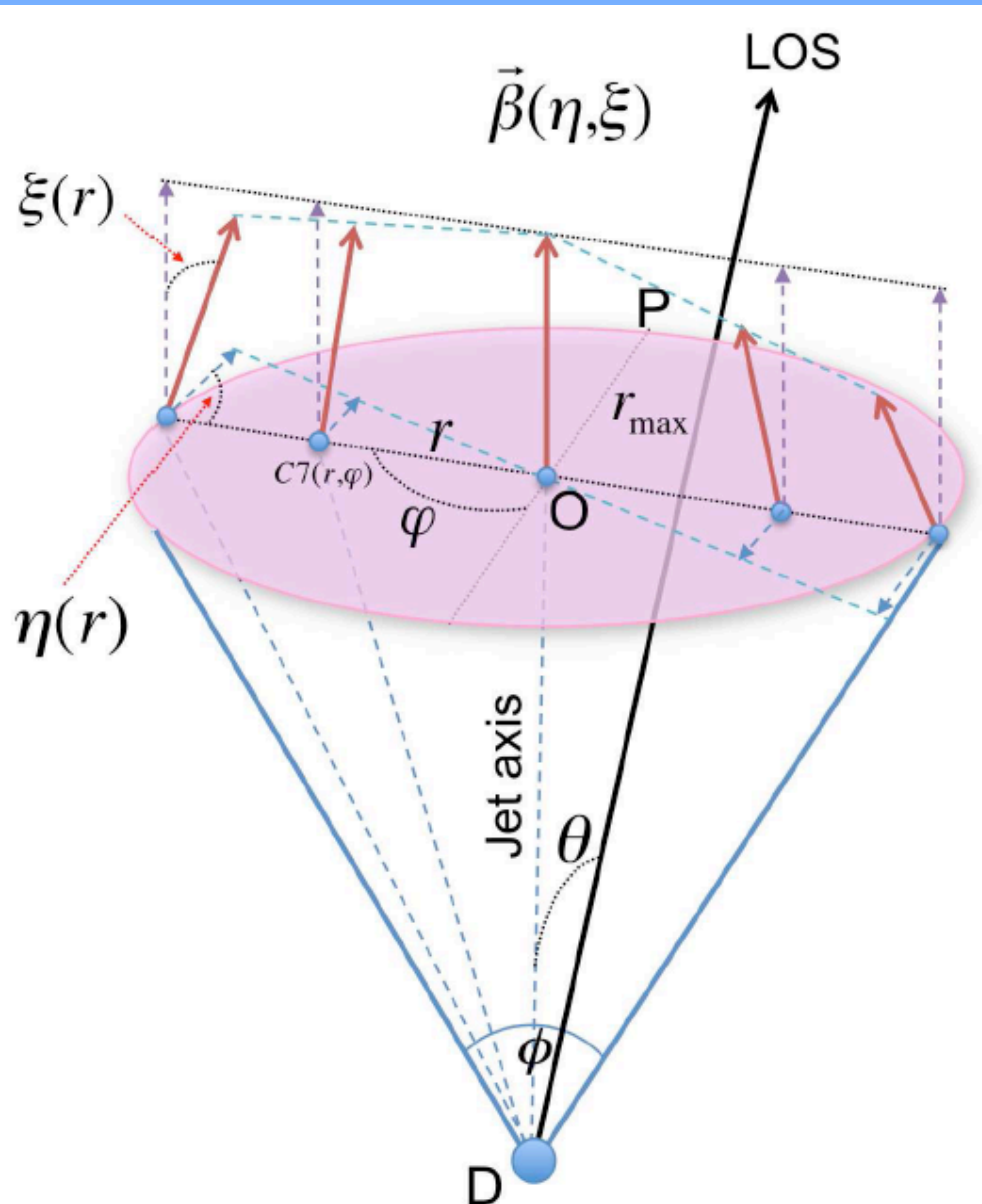
$$\eta(r) = \frac{\eta_{\max} - \eta_{\min}}{r_{\max}} r + \eta_{\min}$$

- Jet speed  $\beta$  at RCS is constant:

$$\vec{\beta}(\xi(r), \eta(r)): \quad \beta = \sqrt{\beta_n^2(r) + \beta_t^2(r)}$$

$$\beta_n(r) = \beta \cos \xi(r), \quad \beta_t(r) = \beta \sin \xi(r)$$

# RCS model: Beaming



**Viewing angle of the jet central axis  $\theta$ :** Angle between the jet central axis and the LOS.

**Viewing angle of the jet,  $\theta_j(r, \varphi)$ , at the location of RCS( $r, \varphi$ ):** Angle between the jet velocity vector at RCS( $r, \varphi$ ) and the LOS.

**Intrinsic flux density of RCS:**  $S_{\text{int}}$  is constant.

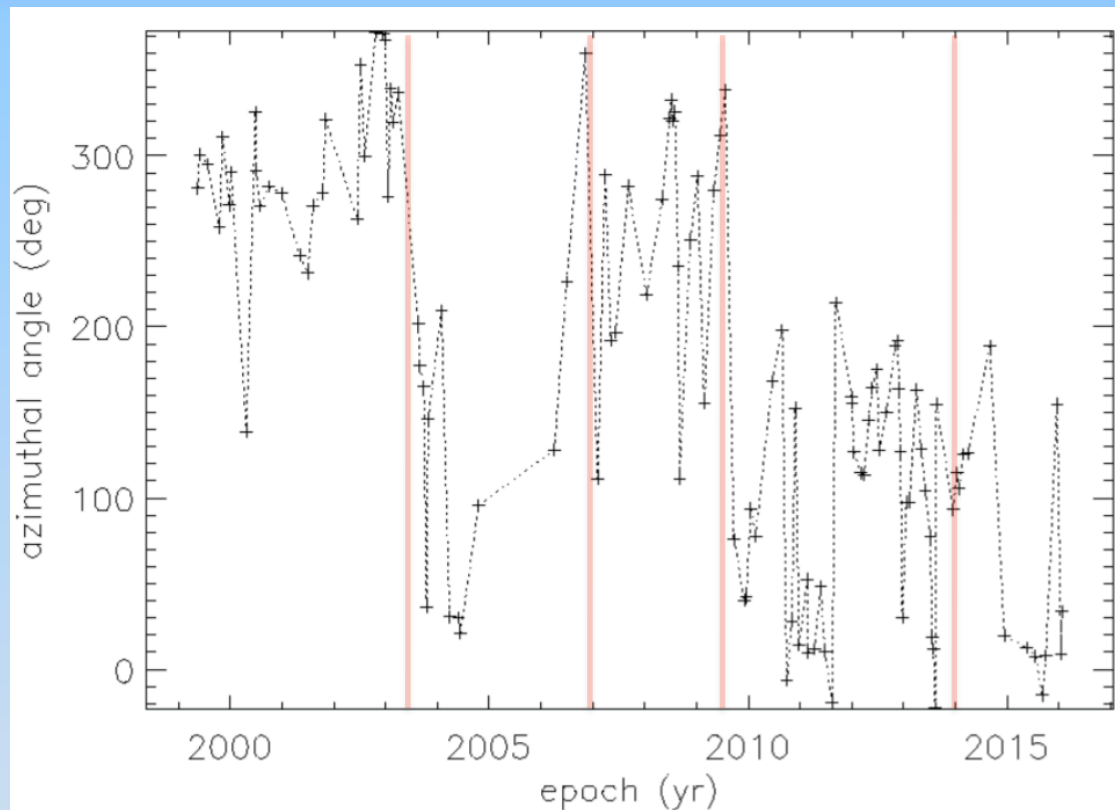
**Simulated flux density of RCS at the location defined by  $r$  and  $\varphi$ :**

$$S_{C7}(r, \varphi) = S_{\text{int}} D^{p-2}(\beta, \theta_{C7}(r, \varphi))$$

$$D(\beta, \theta_{C7}) = \frac{1}{\gamma(1 - \beta \cos(\theta_{C7}(r, \varphi)))}$$

# *RCS motion*

Azimuthal angle – epoch



Clustering of azimuth. angles with epoch:

1.  $< 2003.3$  yr
2. 2003.3-2006.9
3. 2006.9-2009.5
4. 2009.5-2014
5.  $> 2014$