



Italian National Agency for New Technologies,  
Energy and Sustainable Economic Development



# Impact of new results of the neutron capture cross section measurements for odd gadolinium isotopes on thermal-spectrum systems

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# Structure of presentation

- Motivation for the use of Gd in thermal fission reactors
- Status of available data
- Performance of available data and necessity of new experiments
- New n\_TOF xs
- Zed-2 benchmark and preliminary assessment of new xs
- Conclusions and future developments
- References

# Importance of Gd odd isotopes in fission reactors

Use as “**burnable neutron poisons**” in nuclear reactors

- To increase the **efficiency** and economic performances of **reactor fuel**, it is necessary to **increase** the initial **enrichment of  $^{235}\text{U}$**  in the fuel itself.
- However high enrichments pose severe safety problems due to the **high initial excess reactivity**.
- This can be **inherently compensated** by loading the fuel with “**burnable neutron poisons**”, i.e. isotopes with very high capture cross section, that are depleted together with the fissile isotopes.

It is very important to assess the **capture behavior of burnable poisons** in order to evaluate:

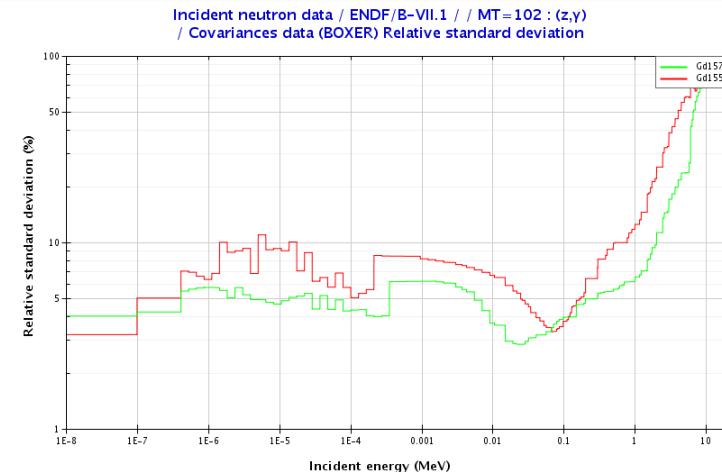
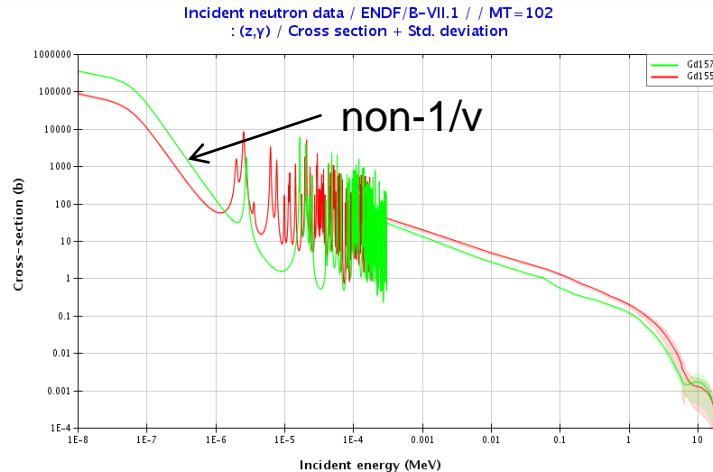
- the **economic gain due to the extension** of fuel life;
- the **residual reactivity penalty** at EOL, in terms of reactor days lost (16 pins Gd-doped FAs for PWRs = 5 full power days lost/year = 8 M€ for the electricity market in France);
- the **reactivity peak** for partially spent fuel for the criticality safety evaluations of Spent Fuel Pools.

# Use in Gen. II & Gen. III Reactors

Current Gen. II and Gen. III nuclear reactors make **extensive use of Gadolinium** as:

- **burnable neutron poison** (Gadolinia:  $\text{Gd}_2\text{O}_3$ ) for **PWR, BWR, VVER** fuels
- **emergency shutdown poison** (Gadolinium nitrate,  $\text{GdNO}_3$ ), for **CANDU**.

The reason of this choice is the **extremely high neutron capture cross sections** of the odd Gd isotopes ( $^{155}\text{Gd}$  and  $^{157}\text{Gd}$ ) for low energy neutrons (thermal to  $\approx 10$  eV).



# 157Gd(n,g) thermal

Despite their importance, the capture cross sections of the odd Gd isotopes have not been so extensively studied and are **not known with the accuracy required** by present-day nuclear industry.

Reference	Year	Thermal xs (kb)	Deviation from ENDF/B-VII
Pattenden <i>2<sup>nd</sup> At. En. Conf. Geneva, 16</i>	1958	264	+3.9%
Tattersall <i>Jour. Nucl. Ener. A 12, 32</i>	1960	213	-20%
Moller <i>Nucl. Sci. Eng. 8, 183</i>	1960	254	=
Sun <i>J. Radioanal. Nucl. Chem. 256, 541</i>	2003	232	-9%
Leinweber <i>Nucl. Sci. Eng. 154, 261</i>	2006	226	-12%
<b>Mughabghab</b> <i>Evaluation (adopted in ENDF/B-VII)</i>	<b>2006</b>	<b><math>254 \pm 0.3\%</math></b>	=
Choi <i>Nucl. Sci. Eng. 177, 219</i>	2014	239	-6%

# Evaluated data vs some experimental benchmarks

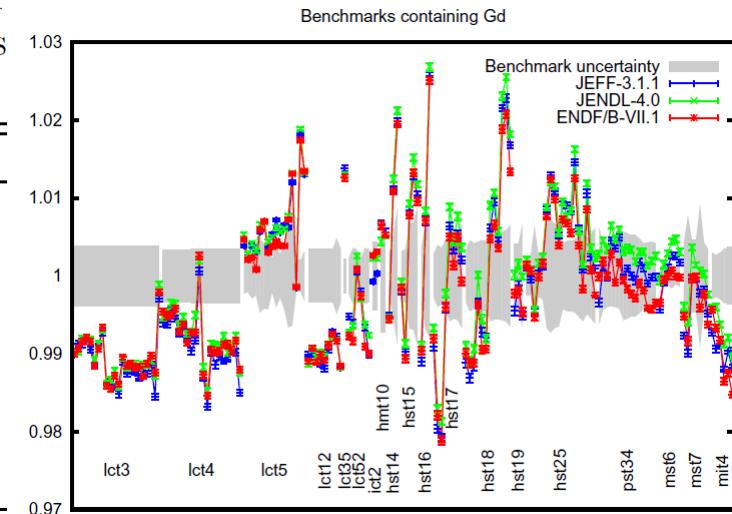
ICSBEP	Config.	K Exp	K ENDF/B-VII	K JEFF-3.1	K Leinweber	Improvement?
HST-014	C2	1.0000	1.00996	1.01304	1.01903	N
	C3	1.0000	1.01827	1.01852	1.02636	N
LCT-035	C3	1.0000	0.99591	0.99556	0.99935	Y
LCT-005	C2	1.0000	1.00029	1.00006	1.00466	N
	C3	1.0000	0.99907	1.00002	1.01651	N
	C4	1.0000	0.99721	0.99846	1.01602	N
	C6	1.0000	1.00684	1.00697	1.00962	N
	C7	1.0000	1.00191	1.00258	1.00846	N
	C8	1.0000	1.00163	1.00295	1.01213	N
	C9	1.0000	1.00257	1.00379	1.01459	N
	C10	1.0000	1.00135	1.00290	1.01474	N
	C11	1.0000	1.00165	1.00342	1.01544	N
	C13	1.0000	1.01309	1.01129	1.01303	N
	C15	1.0000	1.01751	1.01750	1.02436	N

# van der Marck 2012 Analysis

In 2012 S. C. van der Marck published an extensive and comprehensive analysis of **ENDF/B-VII.1**, **JENDL-4.0**, **JEFF-3.1.1** performances using MCNP6 over available benchmarks (mainly ICSBEP). The conclusion about Gd isotopes is that the evaluations above aren't good enough to represent the experimental data, experimental uncertainties included.

TABLE XXXVII: Average values for  $C/E - 1$  (in pcm) for benchmarks containing Gd.  $N$  is the number of benchmarks in the category.

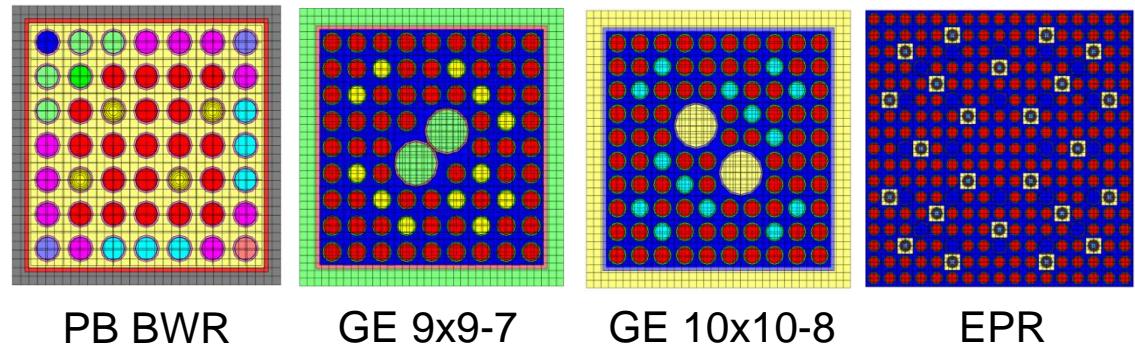
Category	$N$	ENDF/B-VII.1	JENDL-4.0	JEFF-3.1.1
leu-comp-therm	74	-556	-499	-578
ieu-comp-therm	2	285	224	-24
heu-met-therm	2	585	482	614
heu-sol-therm	52	196	421	278
mix-sol-therm	13	-233	75	-185
mix-misc-therm	6	-1009	-690	-982
pu-sol-therm	15	-111	345	82



# ENEA S/U Analysis

- To understand and assess the importance and role of 157Gd and 155Gd in nuclear fuels, a **Sensitivity and Uncertainty (SU) analysis on k** for several different FAs has been performed at BOL, hot-full power (HFP) conditions using the US-NRC reference **SCALE 6.1** code system developed at ORNL.
- Tsunami-2D sequence with **ENDF/B-VII.0** evaluations.

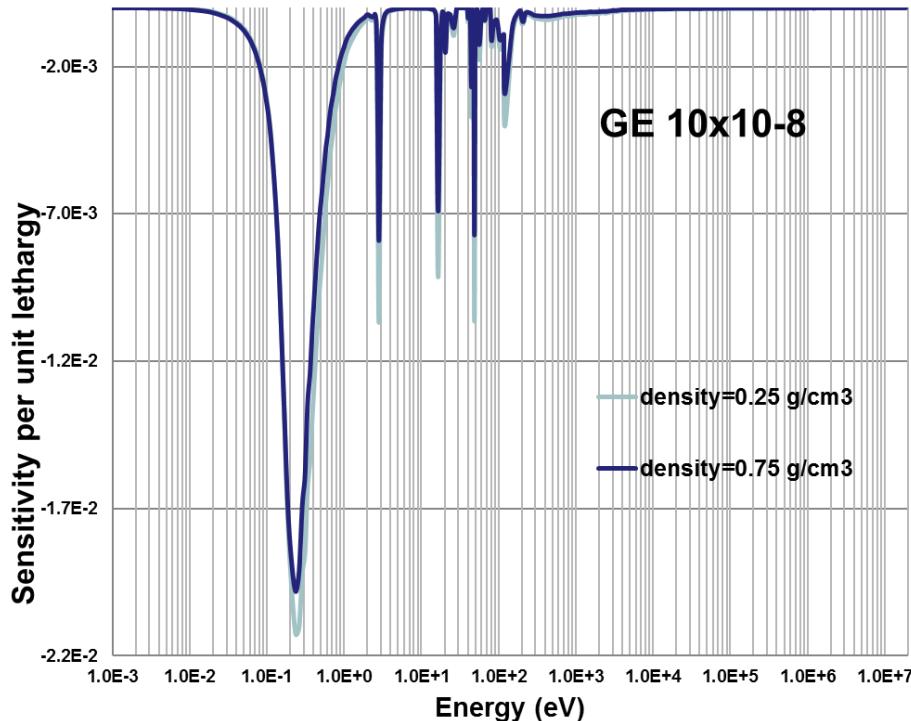
$$S_i(E) = \frac{\sigma_i}{k} \frac{\partial k}{\partial \sigma_i} = \frac{\frac{\partial k}{\partial \sigma_i}}{\frac{\sigma_i}{k}}$$



Covariance Data: 44-group library (based on ENDF/B-VII.0)

# ENEA S/U Analysis

- BWR GE 10x10-8 results.
- Two different moderator densities tested.
- The region of highest sensitivity for  $k$  is **between 0.1 and 1 eV**.



# ENEA S/U Analysis

Nuclide-Reaction	Contrib. to Uncertainty in k (% $\Delta k/k$ )	Rank
$^{235}\text{U} \bar{\nu}$	2.70E-01	1.00
$^{238}\text{U}(n,\gamma)$	1.97E-01	0.81
$^{235}\text{U}(n,\gamma)$	1.43E-01	0.64
$^{235}\text{U}(n,f)$	1.43E-01	0.56
$^{235}\text{U}(n,f) / ^{235}\text{U}(n,\gamma)$	1.21E-01	0.54
$^{238}\text{U}(n,n')$	1.20E-01	0.51
$^{235}\text{U} \chi$	1.13E-01	0.45
$^{238}\text{U} \bar{\nu}$	7.11E-02	0.32
$^{157}\text{Gd}(n,\gamma)$	6.03E-02	0.26
$^{155}\text{Gd}(n,\gamma)$	4.48E-02	0.20
$^{92}\text{Zr}(n,\gamma)$	4.29E-02	0.16
$^1\text{H}(n,\gamma)$	3.67E-02	0.14
$^{91}\text{Zr}(n,\gamma)$	3.48E-02	0.13
$^1\text{H}(n,n)$	3.13E-02	0.12
$^{90}\text{Zr}(n,\gamma)$	2.82E-02	0.10

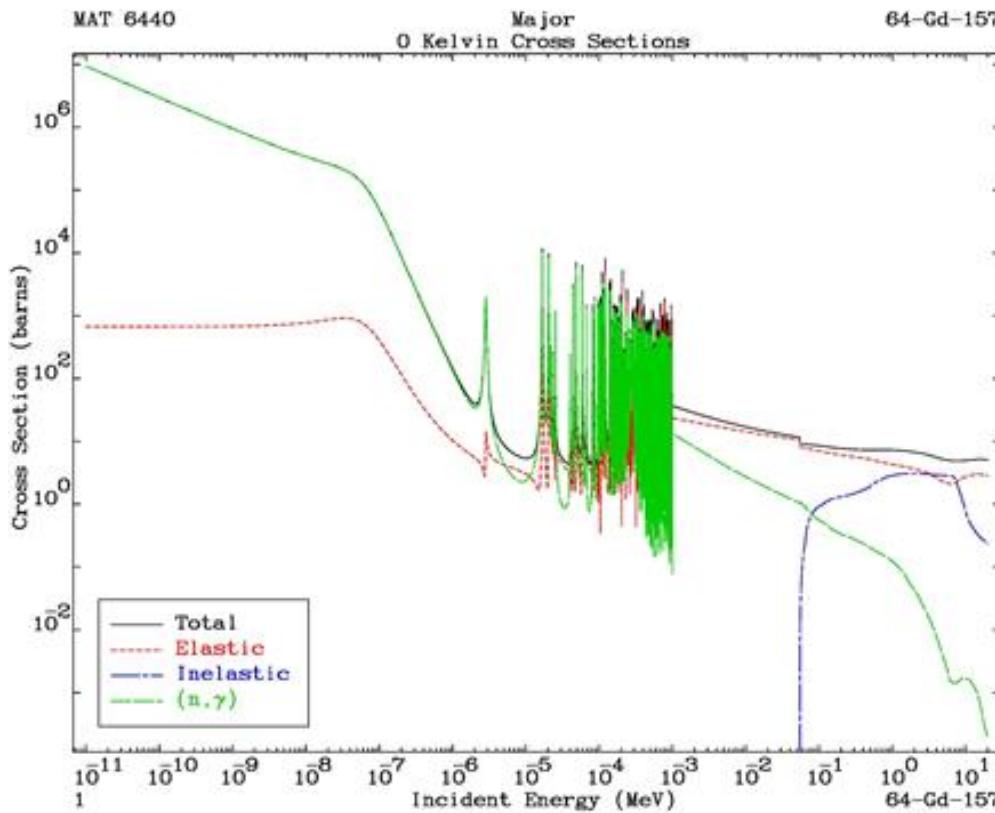
The **uncertainty** on **Gd** cross sections gives the **largest contribution** to the uncertainty on k after  $^{235,238}\text{U}$ .

Several **cross sections** in this list have already been **measured at nTOF**.

# New n\_TOF measurements

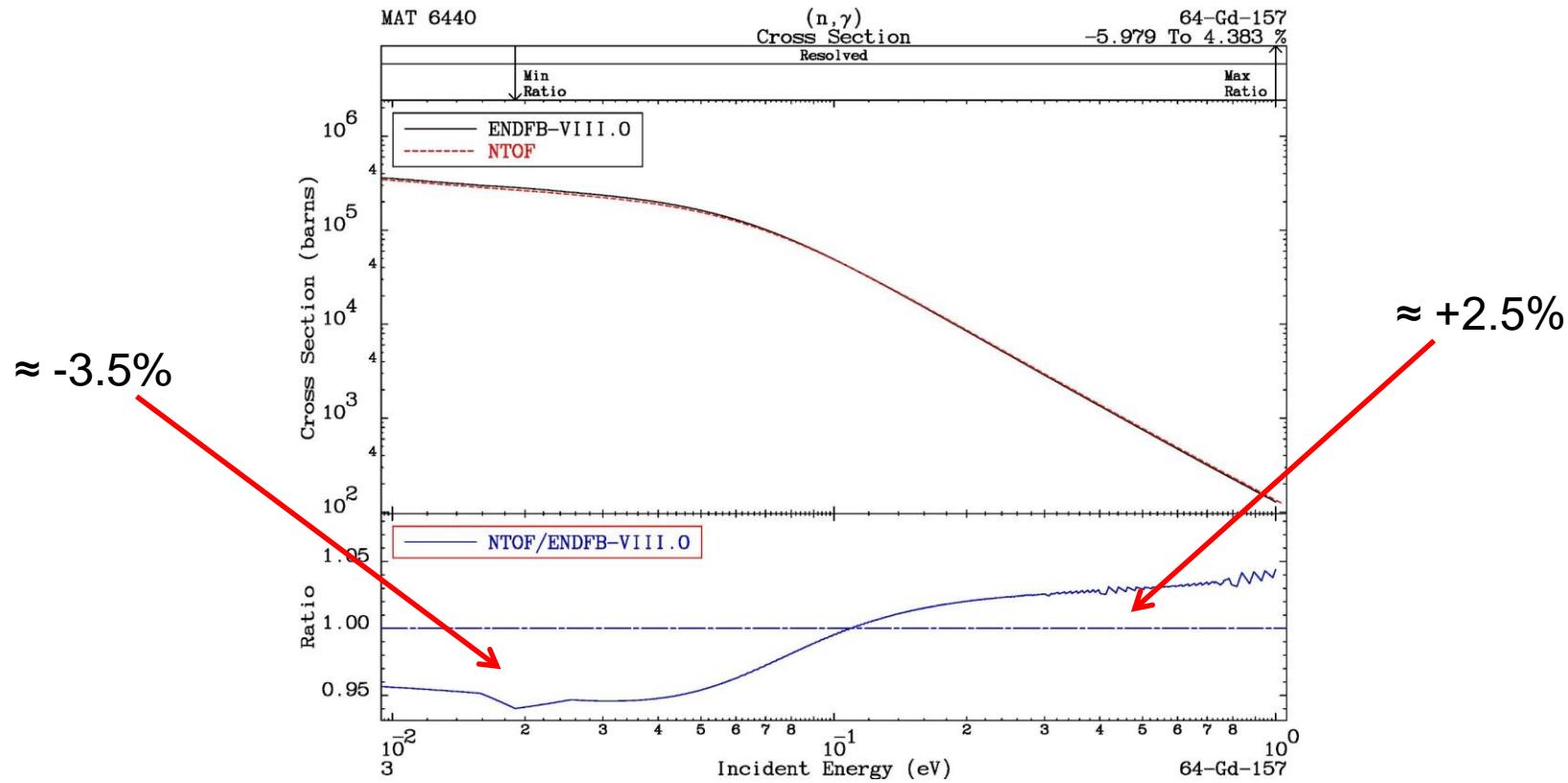
- The n\_TOF Collaboration decided in 2015 to carry out new Gd odd isotopes ( $n,g$ ) xs measurements;
  - Isotopically «pure» samples were acquired from ORNL;
  - Measurements were conducted in July 2016;
  - Results are being published (see also M. Mastromarco presentation at this conference, Thursday 17:30).
- 
- The newly obtained xs @ 0.025 eV results  $239.8 \pm 9.3$  kb;
  - Xs uncertainty @ 0.025 eV about 3.9%;
  - Uncertainty to be reduced to about 3.0% after detailed post-irradiation analysis of the samples (to be accomplished after use at GELINA).

# New n\_TOF 157Gd xsec



# Preliminary cross sections retrieved from ArXiv 1805.04149 (2018)

# New n\_TOF 157Gd(n,g) xsec vs ENDF/B-VIII



# AECL - Chalk River results

## NUCLEAR DATA AND THE EFFECT OF GADOLINIUM IN THE MODERATOR

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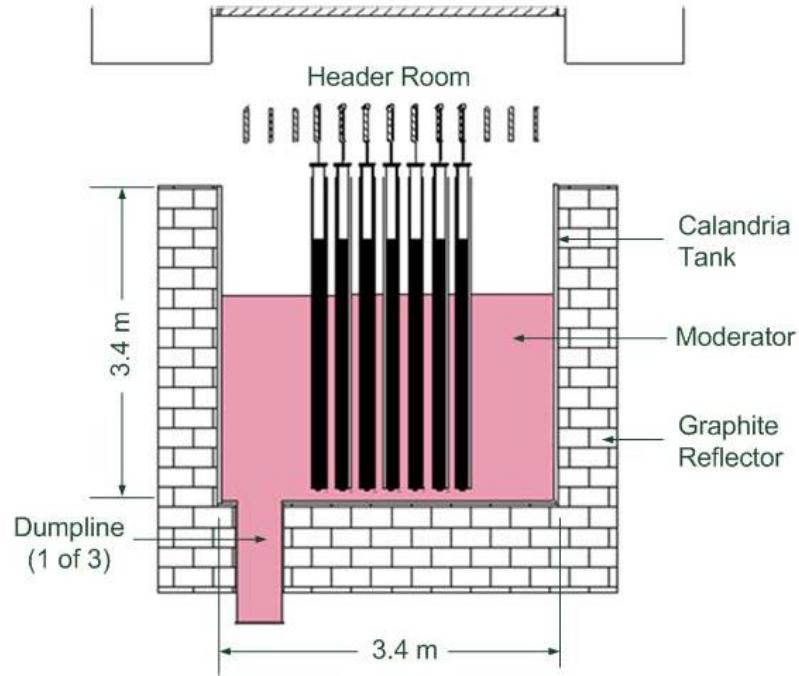
### Article Info

Keywords: gadolinium cross-section, moderator poison, nuclear data, ZED-2

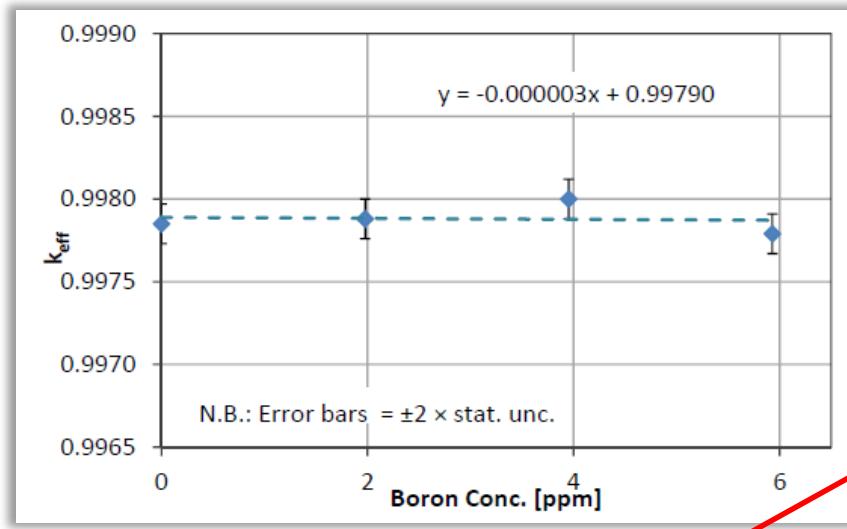
Article history: Received 24 April 2012, Accepted 9 June 2012, Available online 30 June 2012.

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## ZED-II Research Reactor



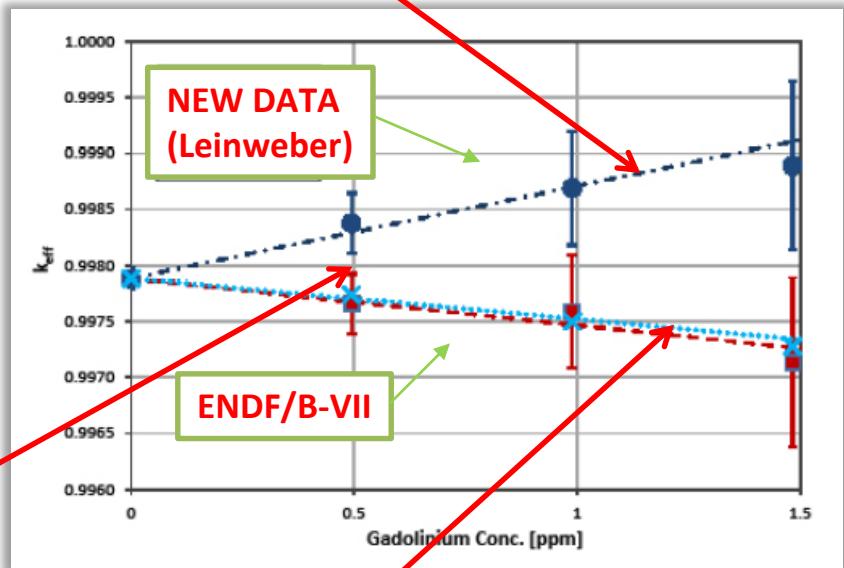
# AECL - Chalk River results



Real thermal xs between  
226 and 254 kb!

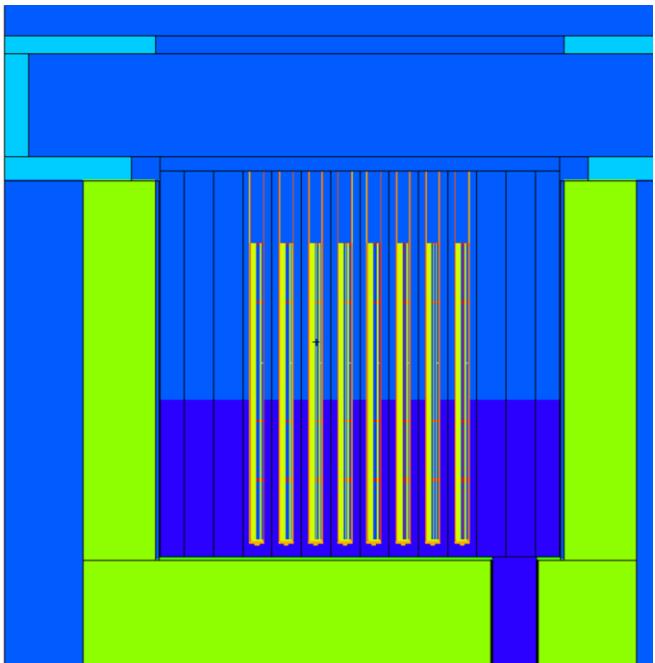
$\approx -22 \text{ pcm}$

$(n,g) @ 0.025 \text{ eV} = 226 \text{ kb}$



$(n,g) @ 0.025 \text{ eV} = 254 \text{ kb}$

# MCNP6 Calculations

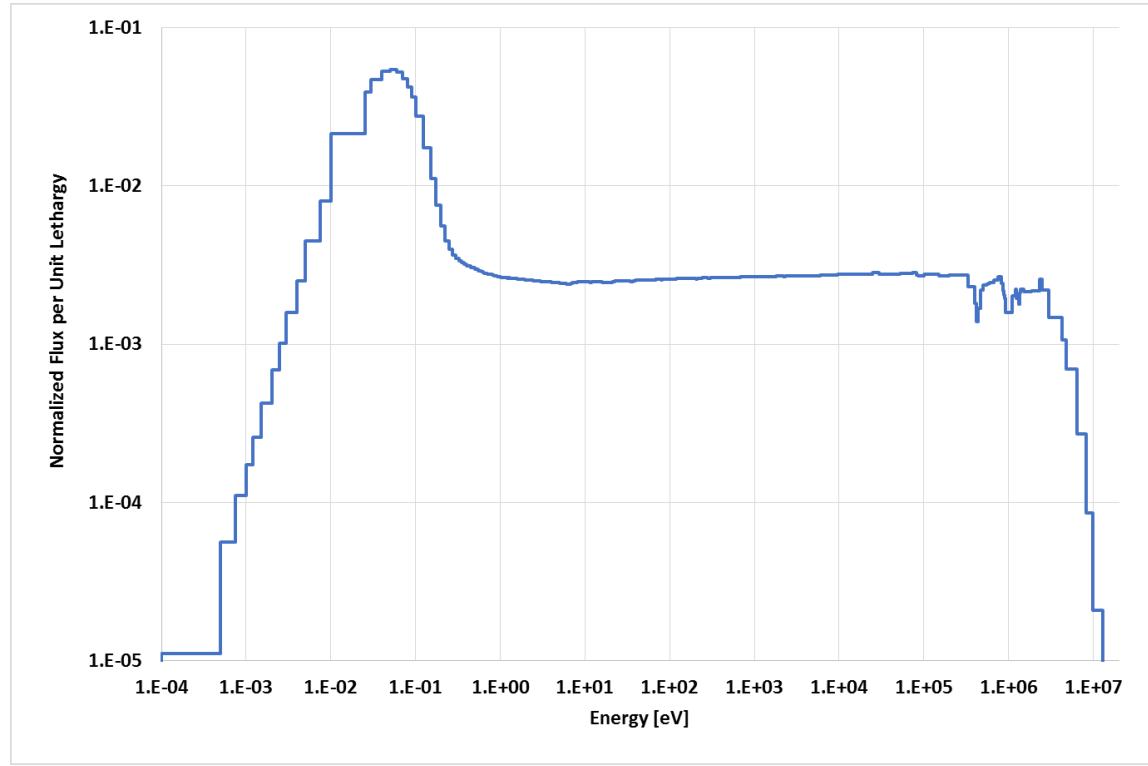


	Lower Energy bound [MeV]	Upper Energy bound [MeV]	Lower Energy bound [eV]	Upper Energy bound [eV]	Spectrum Group Score	Rel Err (1 sd)	Percentage
Case 1	1.00E-11	1.00E-10	1.00E-05	1.00E-04	1.36372E-03	0.0005	0.0005%
	1.00E-10	1.00E-07	1.00E-04	1.00E-01	1.64690E+02	0.0000	63.1422%
	1.00E-07	2.00E+01	1.00E-01	2.00E+07	9.61324E+01	0.0000	36.8572%
			total		2.60824E+02	0.0000	99.9999%
Case 2	1.00E-11	1.00E-10	1.00E-05	1.00E-04	1.33117E-03	0.0005	0.0005%
	1.00E-10	1.00E-07	1.00E-04	1.00E-01	1.61164E+02	0.0000	62.6011%
	1.00E-07	2.00E+01	1.00E-01	2.00E+07	9.62810E+01	0.0000	37.3985%
			total		2.57446E+02	0.0000	100.0001%
Case 3	1.00E-11	1.00E-10	1.00E-05	1.00E-04	1.30079E-03	0.0005	0.0005%
	1.00E-10	1.00E-07	1.00E-04	1.00E-01	1.57696E+02	0.0000	62.0626%
	1.00E-07	2.00E+01	1.00E-01	2.00E+07	9.63953E+01	0.0000	37.9372%
			total		2.54092E+02	0.0000	100.0002%
Case 4	1.00E-11	1.00E-10	1.00E-05	1.00E-04	1.26969E-03	0.0005	0.0005%
	1.00E-10	1.00E-07	1.00E-04	1.00E-01	1.54368E+02	0.0000	61.5284%
	1.00E-07	2.00E+01	1.00E-01	2.00E+07	9.65201E+01	0.0000	38.4712%
			total		2.50889E+02	0.0000	100.0001%

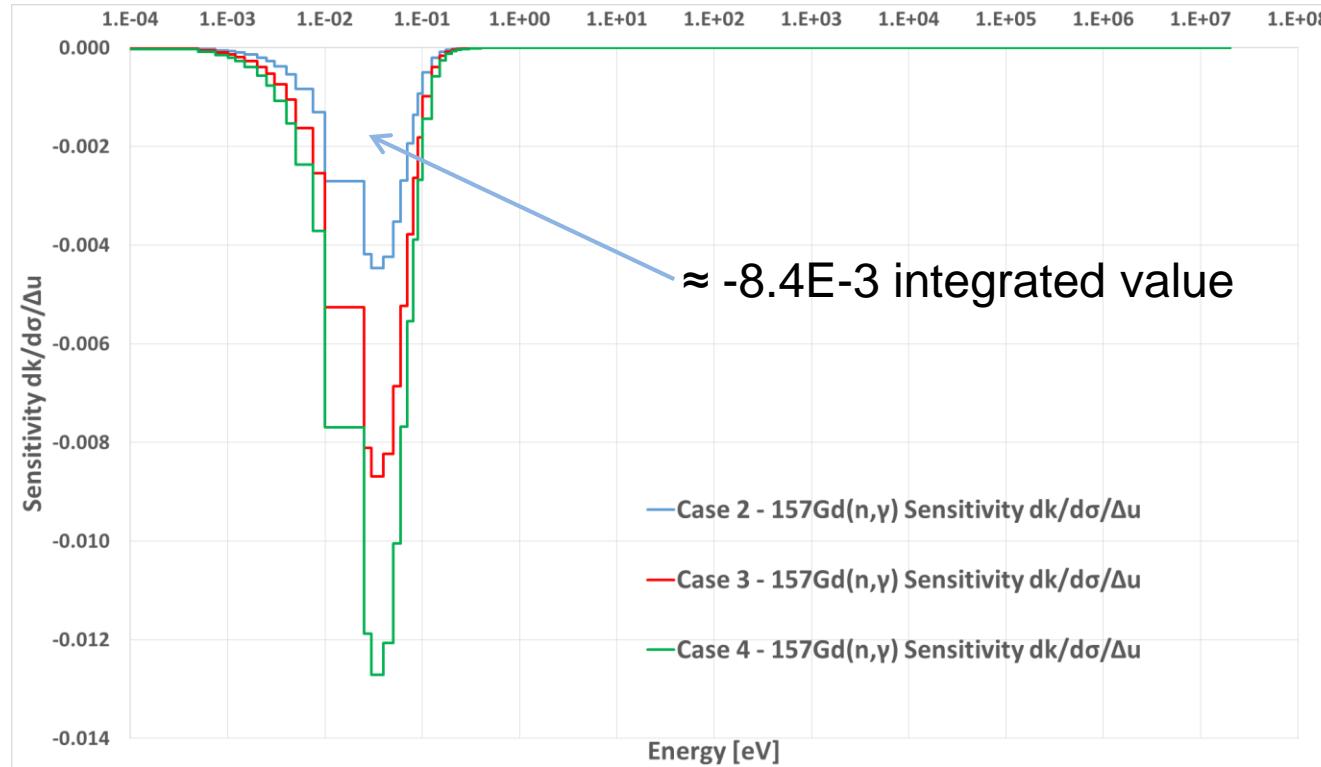
# Zed-2 Flux per unit lethargy in moderator

MCNP6  
calculations

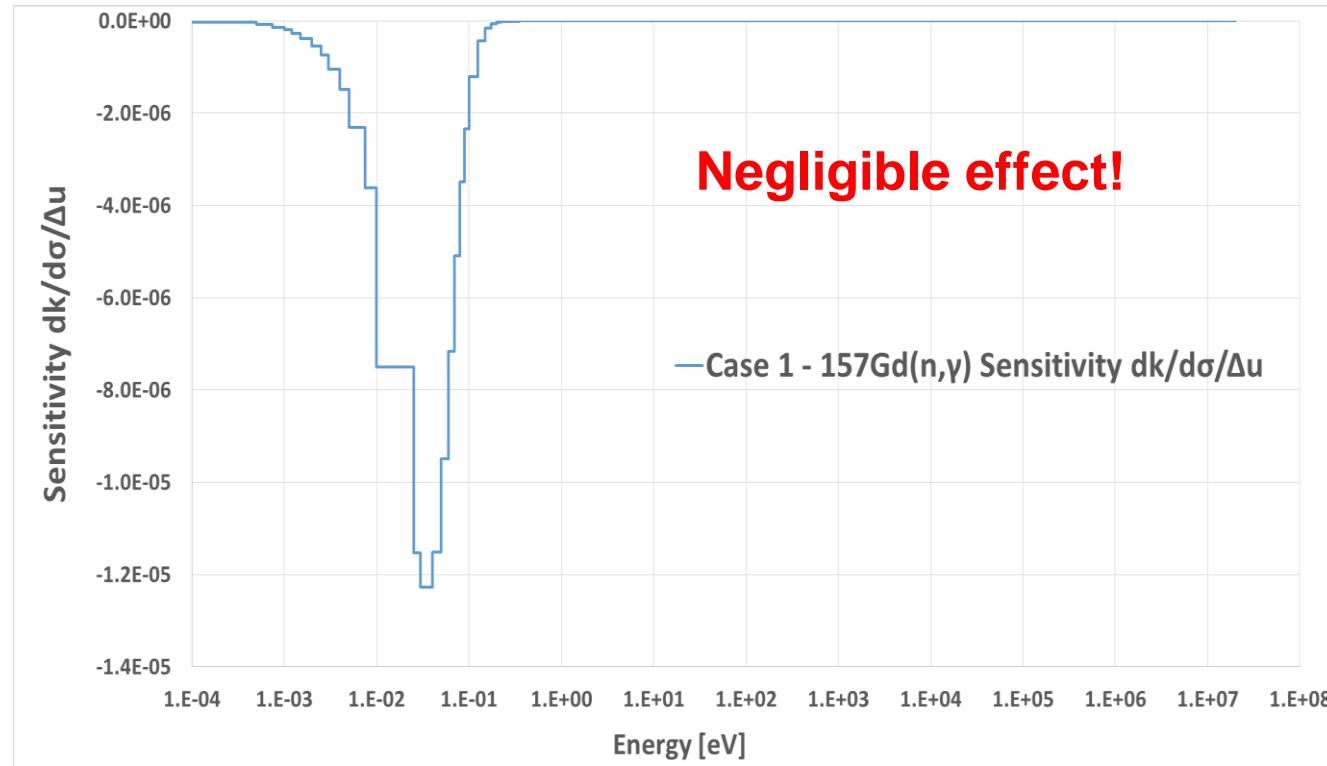
Very well  
thermalized  
specturm!



# Zed-2 k sensitivity per unit lethargy to $^{157}\text{Gd}(n,\gamma)$



# Zed-2 k sensitivity per unit lethargy to $^{157}\text{Gd}(\text{n},\text{g})$ only due to impurities in graphite reflector



# 1&2 groups Zed-2 sensitivities to $^{157}\text{Gd}(\text{n},\gamma)$

	Energy Bounds [eV]		Lethargy Interval [--]	$^{157}\text{Gd}(\text{n},\gamma)$ Sensitivity	Relative Uncertainty	$^{157}\text{Gd}(\text{n},\gamma)$ Sensitivity/ $\Delta u$	Sensitivity/ $\Delta u$ Absolute Uncertainty	$^{155}\text{Gd}(\text{n},\gamma)$ Sensitivity	Relative Uncertainty	$^{155}\text{Gd}(\text{n},\gamma)$ Sensitivity/ $\Delta u$	Sensitivity/ $\Delta u$ Absolute Uncertainty
Case 2	1.00E-04	1.00E-01	6.91E+00	-8.1813E-03	0.0004	-1.1844E-03	-4.7375E-07	-1.8362E-03	0.0004	-2.6582E-04	-1.0633E-07
	1.00E-01	2.00E+07	1.91E+01	-1.7510E-04	0.0003	-9.1609E-06	-2.7483E-09	-3.9074E-05	0.0003	-2.0443E-06	-6.1328E-10
Case 3	sum of 2 groups		2.60E+01	-8.3564E-03	0.0004	-3.2113E-04	-1.2778E-07	-1.8753E-03	0.0004	-7.2066E-05	-2.8676E-08
	1 group integration	calculation	2.60E+01	-8.3577E-03	0.0004	-3.2118E-04	-1.2847E-07	-1.8756E-03	0.0004	-7.2079E-05	-2.8831E-08
Case 4	1.00E-04	1.00E-01	6.91E+00	-1.5901E-02	0.0004	-2.3019E-03	-9.2076E-07	-3.5684E-03	0.0004	-5.1658E-04	-2.0663E-07
	1.00E-01	2.00E+07	1.91E+01	-3.4339E-04	0.0004	-1.7966E-05	-7.1862E-09	-7.6710E-05	0.0003	-4.0133E-06	-1.2040E-09
Case 5	sum of 2 groups		2.60E+01	-1.6244E-02	0.0004	-6.2427E-04	-2.4971E-07	-3.6451E-03	0.0004	-1.4008E-04	-5.5737E-08
	1 group integration	calculation	2.60E+01	-1.6247E-02	0.0004	-6.2437E-04	-2.4975E-07	-3.6457E-03	0.0004	-1.4010E-04	-5.6041E-08
Case 6	1.00E-04	1.00E-01	6.91E+00	-2.3277E-02	0.0004	-3.3697E-03	-1.3479E-06	-5.2231E-03	0.0004	-7.5612E-04	-3.0245E-07
	1.00E-01	2.00E+07	1.91E+01	-5.0723E-04	0.0003	-2.6537E-05	-7.9612E-09	-1.1341E-04	0.0003	-5.9334E-06	-1.7800E-09
Case 7	sum of 2 groups		2.60E+01	-2.3784E-02	0.0004	-9.1402E-04	-3.6366E-07	-5.3365E-03	0.0004	-2.0508E-04	-8.1596E-08
	1 group integration	calculation	2.60E+01	-2.3788E-02	0.0004	-9.1416E-04	-3.6567E-07	-5.3374E-03	0.0004	-2.0511E-04	-8.2046E-08

# 1-grp $\Delta k$

$$\Delta k \cong k \cdot S \cdot \frac{\Delta \sigma}{\sigma}$$

$$k = 0.99766 \quad S \cong -8.36E-3 \quad \Delta \sigma \cong -0.035 \sigma$$

$$\boxed{\Delta k \cong +29.2 \text{ pcm}}$$

The ideal, compensating gain should have been around +22 pcm.

Approximation introduced: total sensitivity attributed solely to thermal group (<0.1 eV)!

## 2-grps $\Delta k$

- 2 groups: 1) 0.0 – 0.1 eV,  
2) 0.1 – 2.0E7 eV
- Second group by far less important than first;
- Correction to  $k$  results now roughly **+ 28.1 pcm**;
- Full MCNP6 calculations with the new xs are needed for a more precise assessment;
- These will be accomplished in the next weeks.

# Conclusions and next steps

From the preliminary and «back of the envelope» analyses conducted so far

- The new xs seems to satisfy the Zed-2 experiments much better than currently available evaluations;
- The new xs, again based on Zed-2 results, seems to underestimate slightly capture by about 0.8%;
- Infinite groups calculations with MCNP6 are needed for better confidence on the performance of the new xs in Zed-2;
- Many other ICSBEP benchmarks are to be used for further validation of the new product;
- Uncertainty in the thermal region needs to be further reduced;
- GELINA experiments with the same samples are underway;
- Possibility to produce new evaluations for JEFF4.

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**Thank you for your attention**

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