
Relevance of neutron excess in nuclear matter to proton-induced composite-particle pre-equilibrium emission

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Outline

- some general ideas about the equation of state (EOS)
- relevance of light clusters in formulation of EOS
- α -cluster trend with mass asymmetry in Sn isotopes
- pre-equilibrium reactions and relevance of neutron asymmetry
- experiment to verify influence α -clustering variation in Sn isotopes

Equation of State of Nuclear Matter

$$e(\rho, \delta) = e(\rho, 0) + S(\rho)\delta^2 + \mathcal{O}(\delta^4)$$

$$\delta = \frac{\rho_n - \rho_p}{\rho} \quad \rho = \rho_n + \rho_p$$

symmetry energy

$$S(\rho) = \frac{1}{2} \left. \frac{\partial^2 e(\rho, \delta)}{\partial \delta^2} \right|_{\delta=0}$$

range of interest

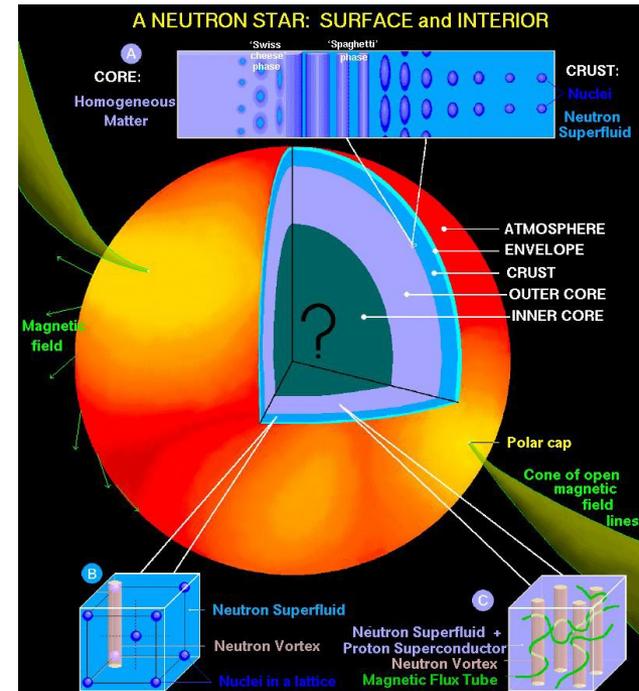
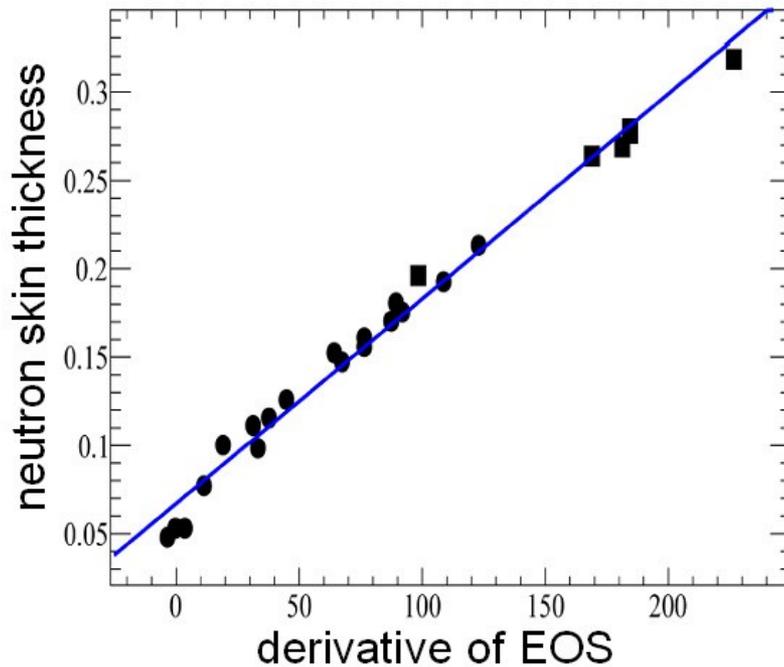
$$10^{-8} \leq \rho / \rho_0 \leq 10$$

$$0 \leq T \leq 100 \text{ MeV}$$

$$0 \leq Y_p \leq 0.6 \quad \text{proton fraction}$$

Symmetry energy vs neutron skin thickness

F Schindler PoS (Bormio 2014)



neutron skin thickness of, for example, ^{208}Pb has implications for properties of neutron star !!

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PHYSICAL REVIEW C **81**, 015803 (2010)

Composition and thermodynamics of nuclear matter with light clusters

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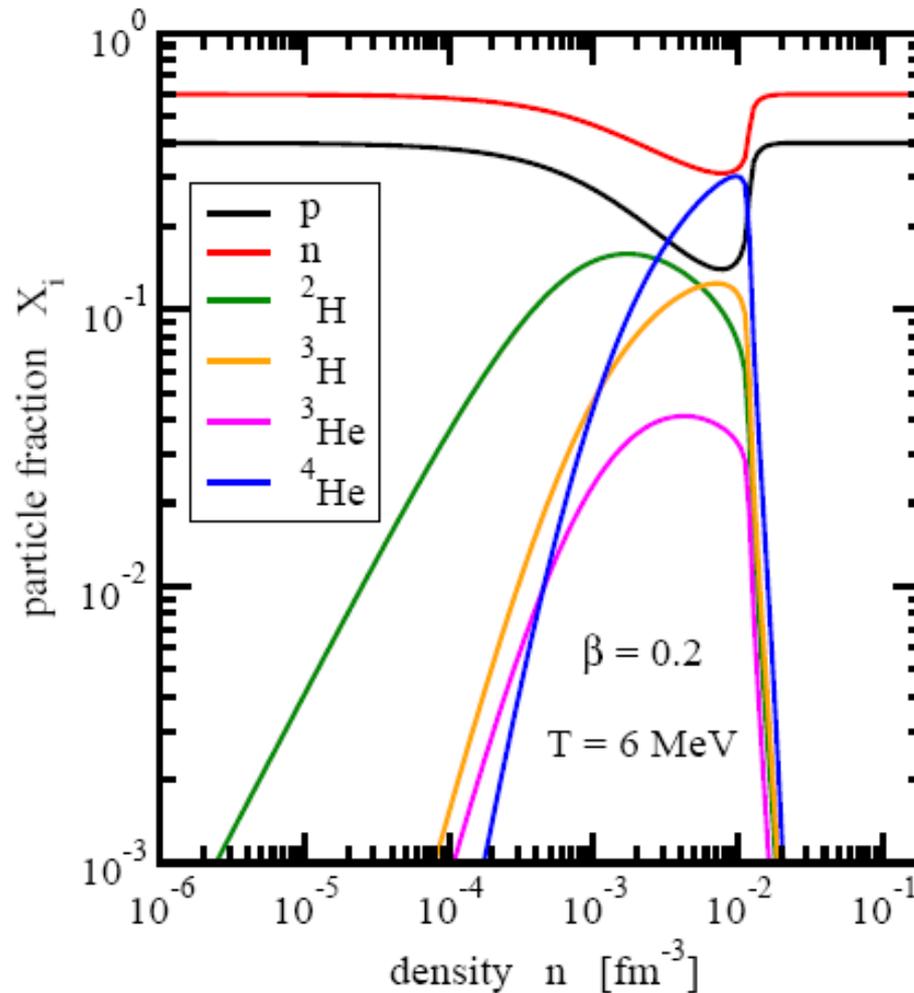
Equation-of-State (EOS) of Nuclear Matter with Light Cluster Correlations
Hermann Wolter
Ludwig-Maximilians-Universität München

28th Internat. Workshop on Nuclear Theory, Rila Mountains, Bulgaria, June 22-27, 2009

Symmetry Energy: Importance at different density ranges
 $E(\rho_B, I)/A = E(\rho_B) + E_{\text{sym}}(\rho_B)I^2 + O(I^4) + \dots$
 $I = \frac{N-Z}{N+Z}$

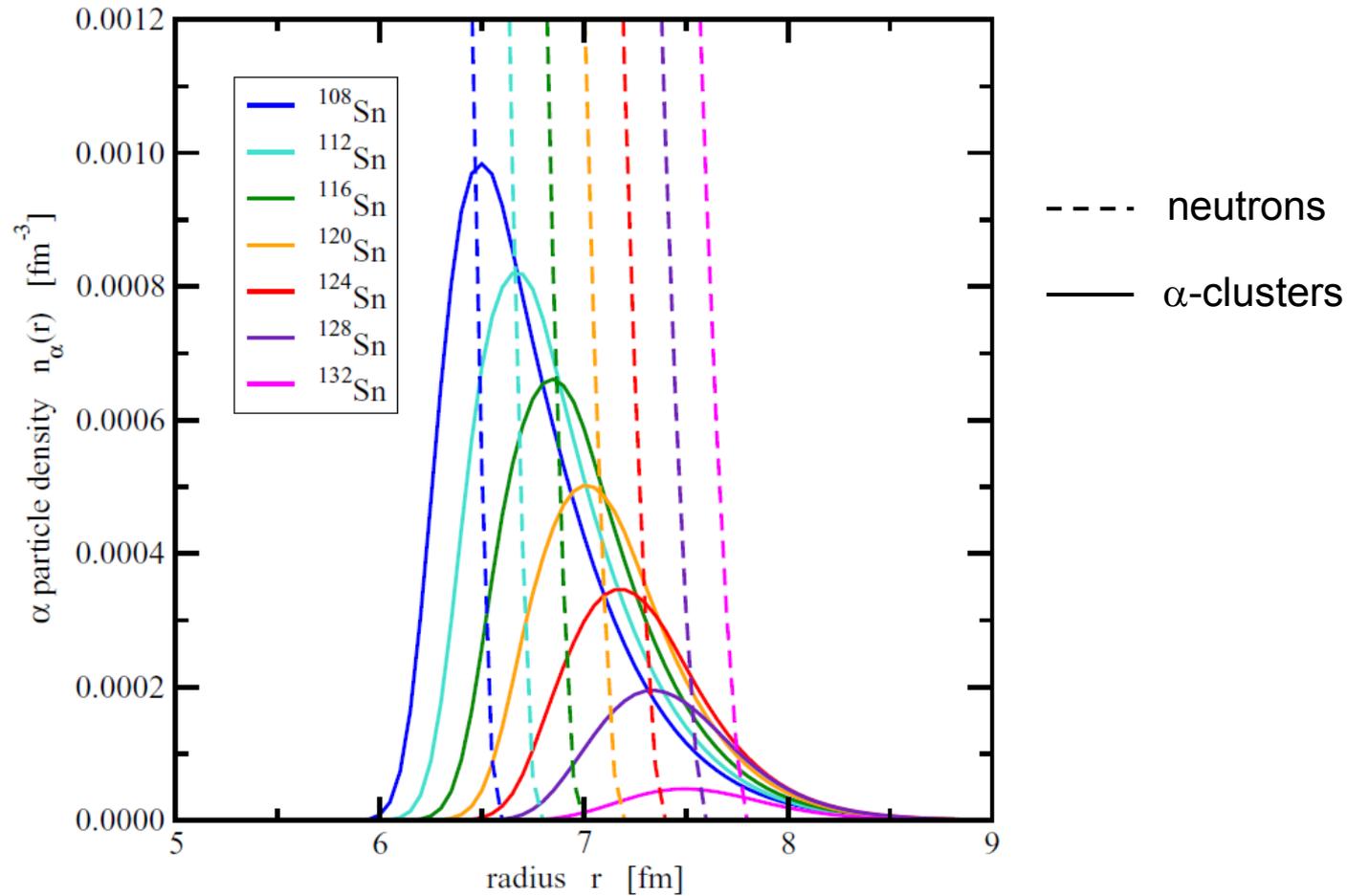
Neutron star structure
heavy ion collisions in the Fermi energy regime
Supernova simulations
neutron skin thickness
differential flow, particle production in HIC

Light Cluster Correlations

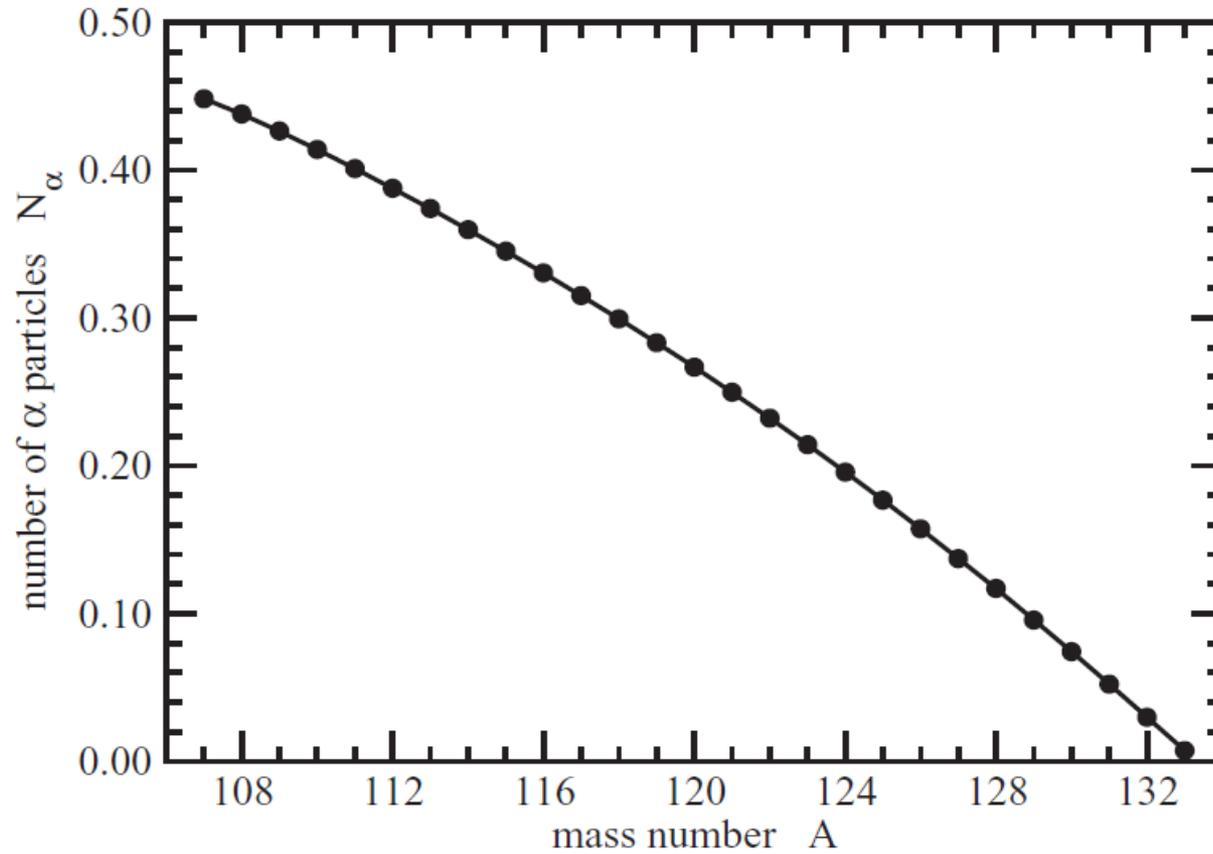


Hermann Wolter 28th Int. Workshop on Nuclear Theory,
Rila Mountains, Bulgaria, June 2009

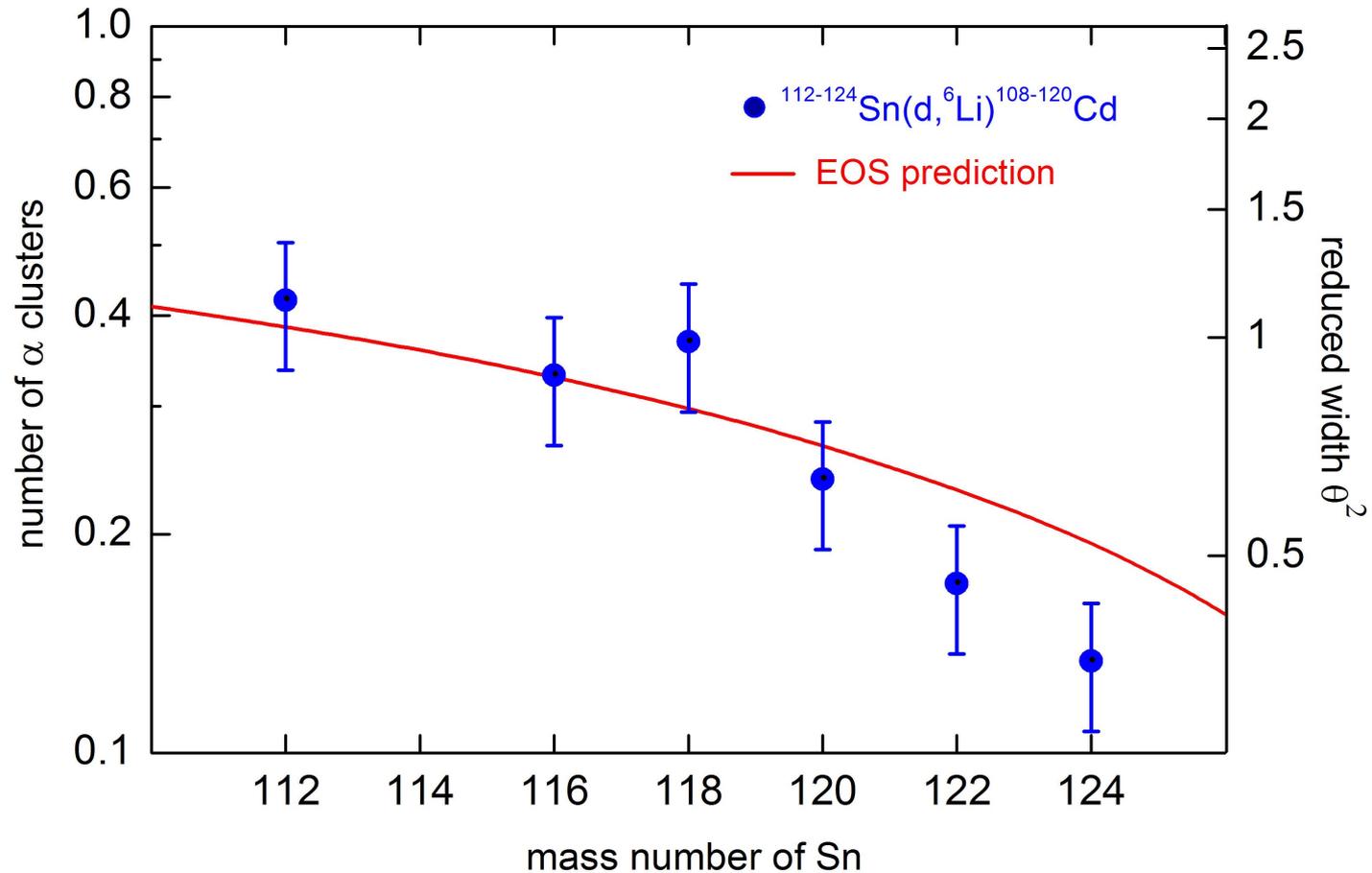
Predicted α -clustering with different mass asymmetry



Total number of α -cluster variation with Sn target mass

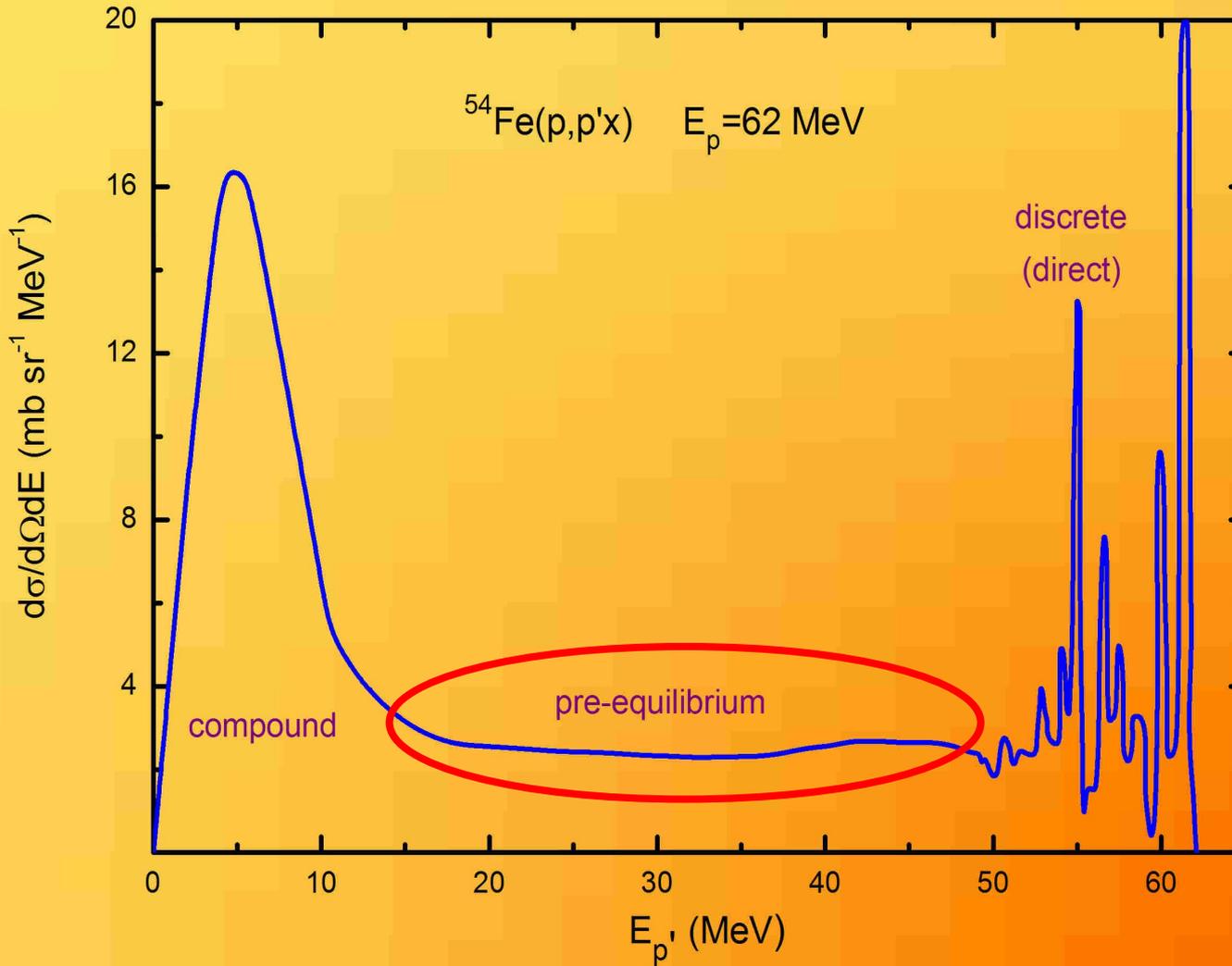


α – cluster pickup vs equation – of –state prediction



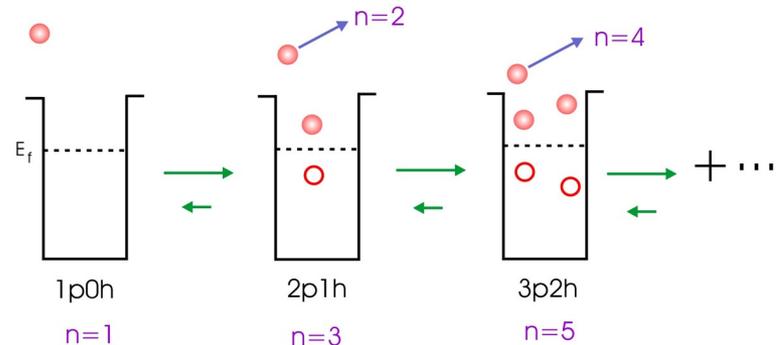
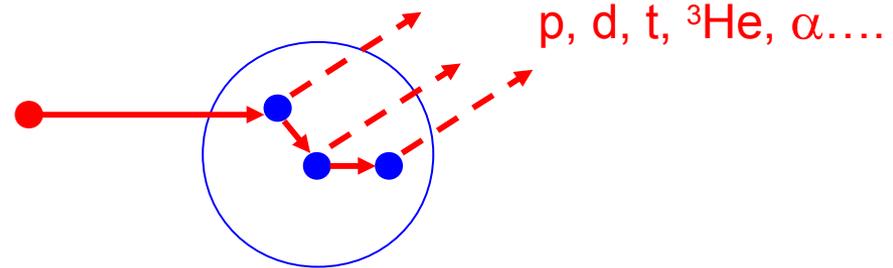
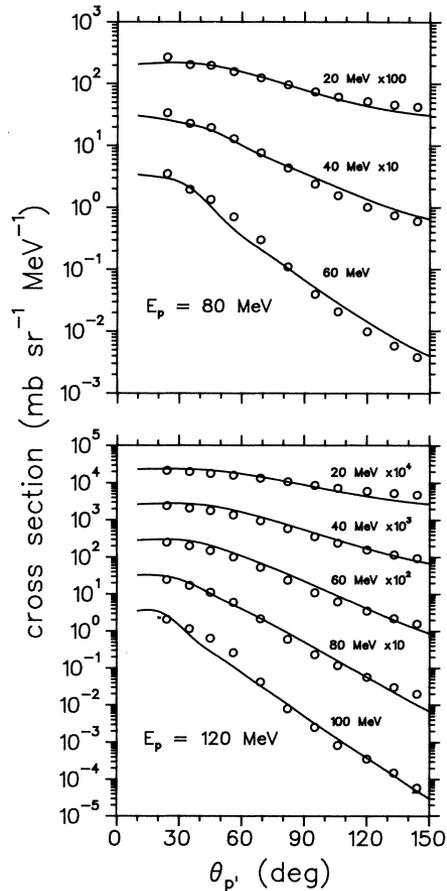
Pre-equilibrium (inclusive) reactions

Bertrand & Peele Phys Rev C 8 (1973) 1045



Mechanism pre-equilibrium (inclusive) reactions

$^{90}\text{Zr}(p,p')$ $E_p = 80, 100 \text{ MeV}$

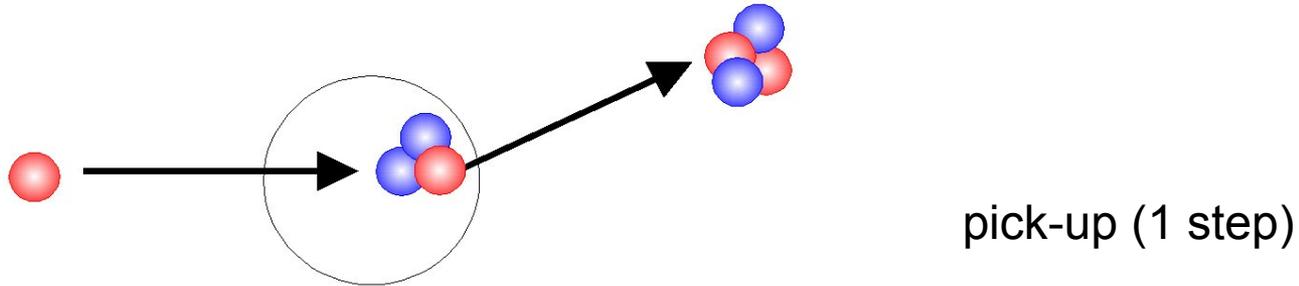


$$\left. \frac{d^2\sigma}{dE d\Omega} \right|_{\text{multistep}} = \sum_{n=2}^{n_{\max}} \sum_{m=n-1}^{n+1} \int d\mathbf{k}_1 \cdots \int d\mathbf{k}_n \left[\frac{d^2W_{m,n}(\mathbf{k}_f, \mathbf{k}_n)}{dE_f d\Omega_f} \right] \left[\frac{d^2W_{n,n-1}(\mathbf{k}_n, \mathbf{k}_{n-1})}{dE_n d\Omega_n} \right] \times \cdots \times \left[\frac{d^2W_{2,1}(\mathbf{k}_2, \mathbf{k}_1)}{dE_2 d\Omega_2} \right] \left[\frac{d^2\sigma_{1,i}(\mathbf{k}_1, \mathbf{k}_i)}{dE_1 d\Omega_1} \right]$$

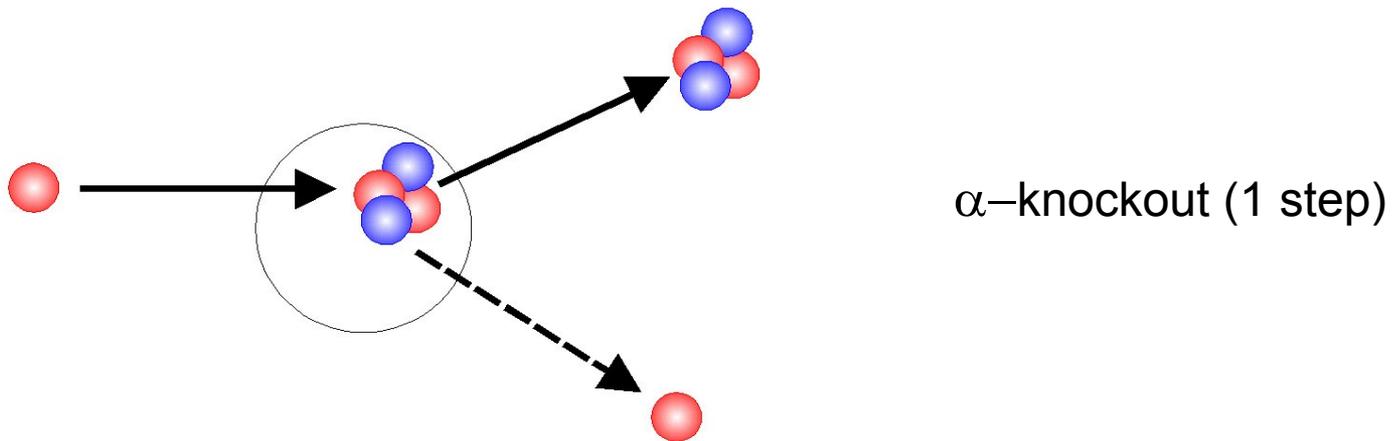
Curves: Predictions of statistical multistep direct reaction mechanism (Feshbach, Kerman, and Koonin)

(p,α) pre-equilibrium reaction

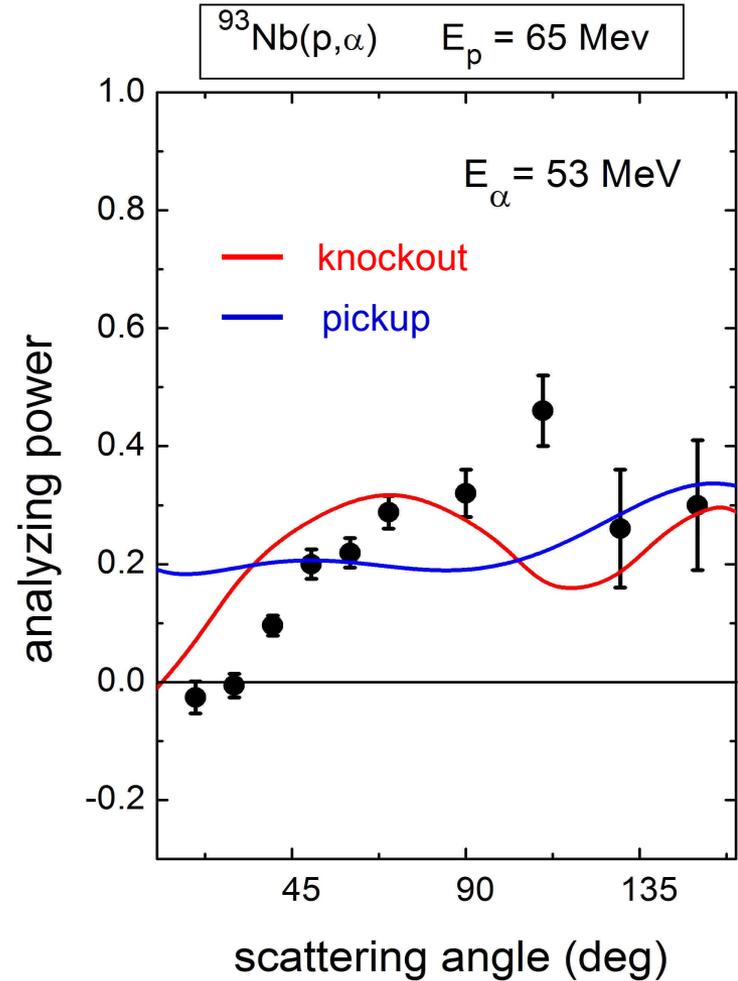
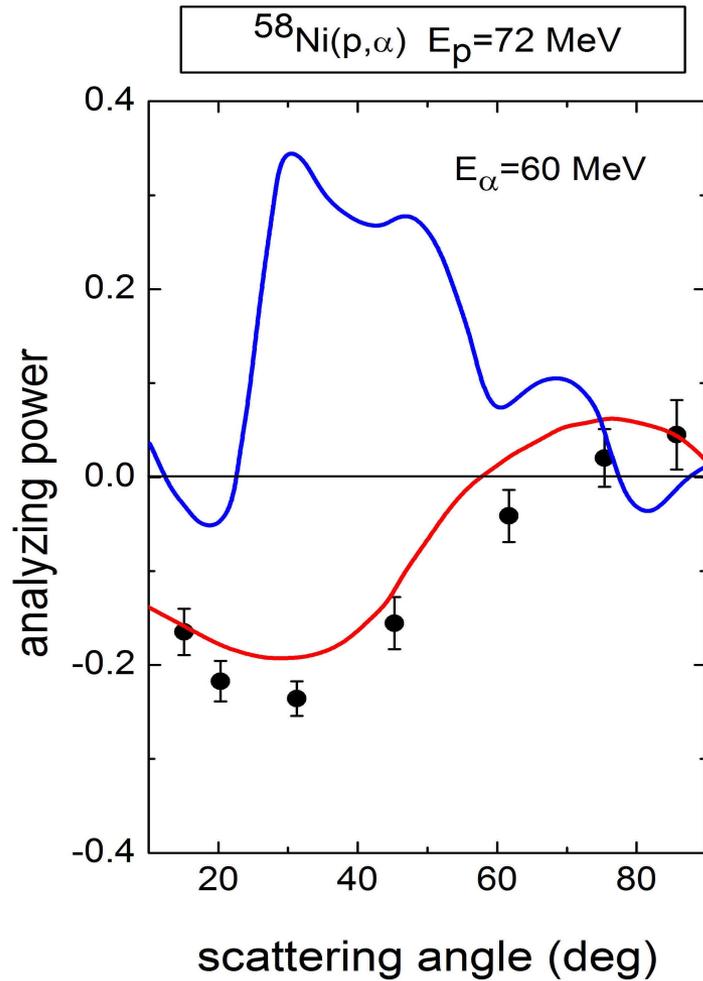
- competition between knockout and pickup



and

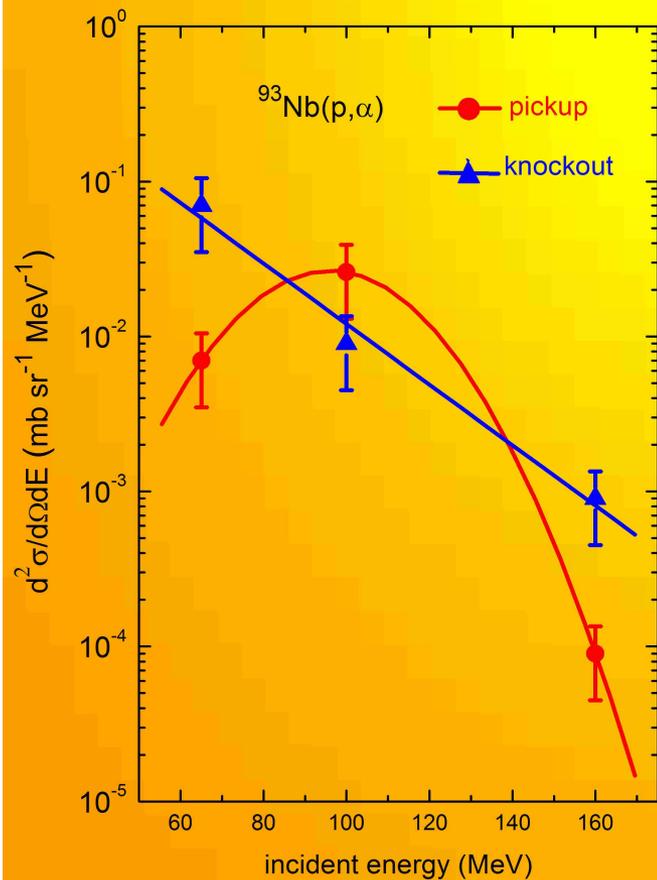


Sensitivity to reaction mechanism



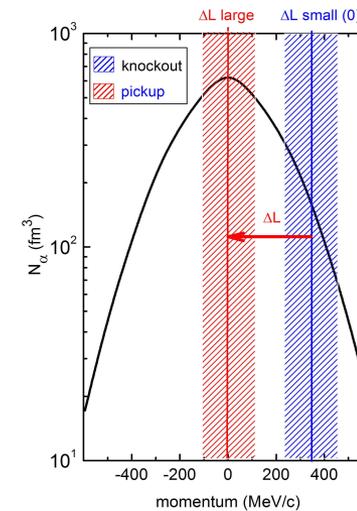
Change of dominant mechanism with incident energy

$^{93}\text{Nb}(p,\alpha)$ $E_p = 65 \rightarrow 160$ MeV



Reasons for incident-energy trend

- target structure
- kinematics
- DWBA sensitivity to the above

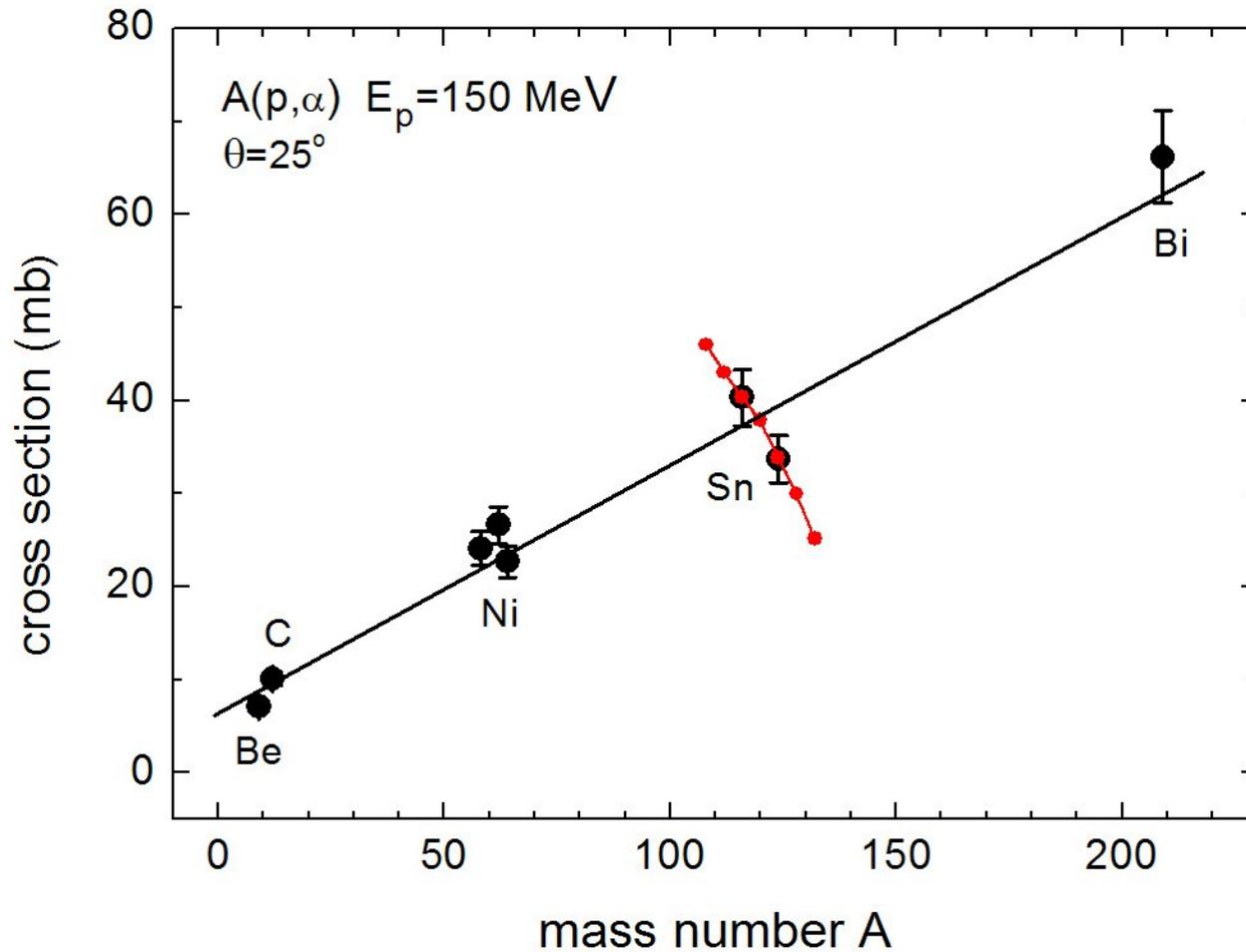


RADIAL INTEGRAL I where $\frac{d^2\sigma}{d\Omega} (DWBA) \sim |I|^2$

reaction: $A(a,b)B$

$$\begin{aligned}
 I &= \int dr_c \chi^{(-)(k_b, \frac{B}{A}r_a)} \phi_C(r_c) \chi^{(+)(k_a, r_a)} && \text{distorted-wave expression} \\
 &\approx \int dr e^{-i(k_b - k_a)r} \phi_C(r) && \text{plane waves; } B \approx A \\
 &\equiv \psi_C(k_b - k_a) && \text{Bound state Fourier transformation}
 \end{aligned}$$

Sensitivity of pre-equilibrium cross section to clustering?



Summary

- light ion clustering is probably a crucial component of the EOS
- (d,⁶Li) pickup consistent with predicted α -clustering trend in Sn isotopes
- decreasing α -clustering on the surface of Sn with growing mass asymmetry is predicted to have a prominent influence on pre-equilibrium reactions

Acknowledgement

- Funding from the National Research Foundation (NRF) of South Africa (grant number 115020)

Thank you