

Nuclear Structure Solving Problems of Fundamental Physics

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Contents:

- The g_A problem of weak decays:
- allowed β decays
- forbidden β decays
- Are there sterile neutrinos?
The Ga and reactor- $\bar{\nu}$ anomalies

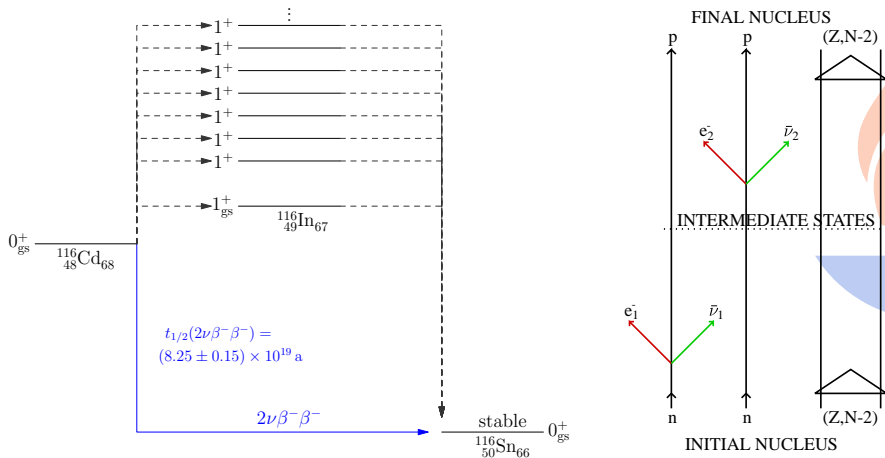
PART 1: Study of the effective value of the weak axial coupling

Motivation:

The **effective value of g_A** is involved in all weak processes, and thus has impact on

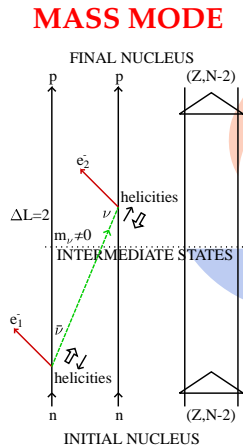
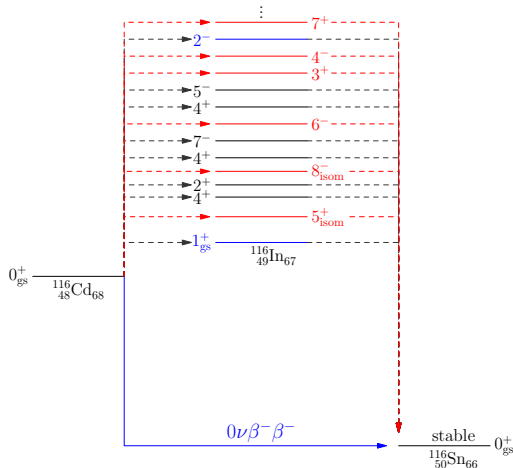
- **studies of rare β decays**
- **processes in neutrino physics** ($\beta\beta$ decay, low-energy (anti)neutrino-nucleus scattering, . . .)
- **processes in astrophysics** (β decays, (anti)neutrino-nucleus scattering cross sections, . . .)

Example: Two-Neutrino Double Beta Decay of ^{116}Cd



$$2\nu\beta\beta - \text{rate} \sim \left| M_{\text{GTGT}}^{(2\nu)} \right|^2 = (g_A)^4 \left| \sum_{m,n} \frac{M_L(1^+_1)M_R(1^+_1)}{D_m} \right|^2$$

Example: Neutrinoless Double Beta Decay of ^{116}Cd



$$0\nu\beta\beta - \text{rate} \sim \left| M_{\text{GTGT}}^{(0\nu)} \right|^2 = (g_{A,0\nu})^4 \left| \sum_{J\pi} \langle 0^+ | \mathcal{O}_{\text{GTGT}}^{(0\nu)}(J\pi) | 0_i^+ \rangle \right|^2$$

Definitions

See also: “Value of the axial-vector coupling strength in β and $\beta\beta$ decays: A review” published in **Frontiers in Physics** 5 (2017) 55.

Nucleon weak current in a nucleus:

$$j_N^\mu = g_V \gamma^\mu - g_A \gamma^\mu \gamma^5$$

Quenching:

$$q = g_A / g_A^{\text{free}}$$

Free value of g_A (Particle Data Group 2016) from the decay of free neutron:

$$g_A^{\text{free}} = 1.2723(23)$$

Effective value of g_A :

$$g_A^{\text{eff}} = q g_A^{\text{free}}$$

Gamow-Teller β decays

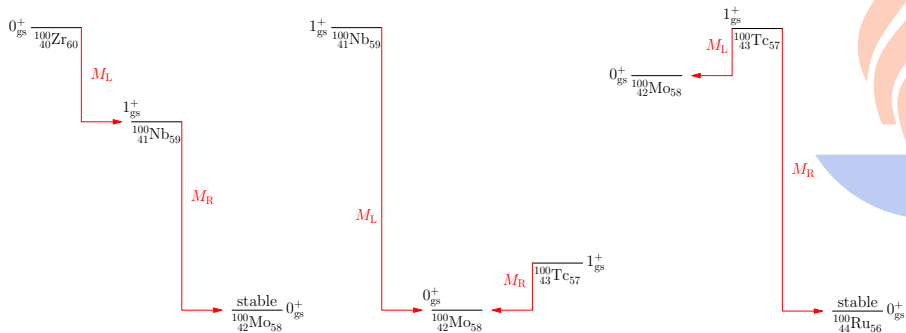
There are data on:

Gamow-Teller β TRANSITIONS

Theoretical approaches:

ISM (Interacting Shell Model)
pnQRPA (proton-neutron QRPA)

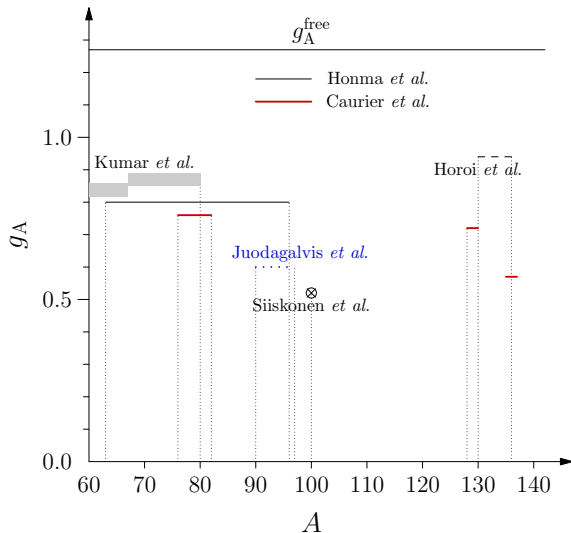
Typical Gamow-Teller β transitions



Results from:

Quenching of g_A in the ISM calculations

Results from the ISM



- Kumar *et al.*: J. Phys. G 43 (2016) 105104
- Honma *et al.*: J. Phys. Conf. Ser. 49 (2006) 45
- Caurier *et al.*: Phys. Lett. B 711 (2012) 62
- Horoi *et al.*: Phys. Rev. C 93 (2016) 024308
- Juodagalvis *et al.*: Phys. Rev. C 72 (2005) 024306
- Siiskonen *et al.*: Phys. Rev. C 63 (2001) 055501

Proton-neutron Quasiparticle Random-Phase Approximation (pnQRPA)

Results from:

Quenching of g_A in the pnQRPA calculations

Results from the pnQRPA analyses

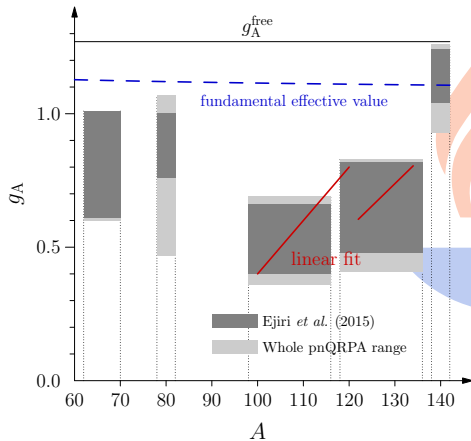
A	pn Conf.	\bar{g}_A^{eff} [1]
62 – 70	$1p_{3/2} - 1p_{1/2}$	0.81 ± 0.20
78 – 82	$0g_{9/2} - 0g_{7/2}$	0.88 ± 0.12
98 – 116	$0g_{9/2} - 0g_{7/2}$	0.53 ± 0.13
118 – 136	$1d_{5/2} - 1d_{5/2}$	0.65 ± 0.17
138 – 142	$1d_{5/2} - 1d_{3/2}$	1.14 ± 0.10

[1] H. Ejiri, J. S., J. Phys. G 42 (2015)
055201

Other analyses in the whole range:

[2] P. Pirinen, J. S., Phys. Rev. C 91
(2015) 054309

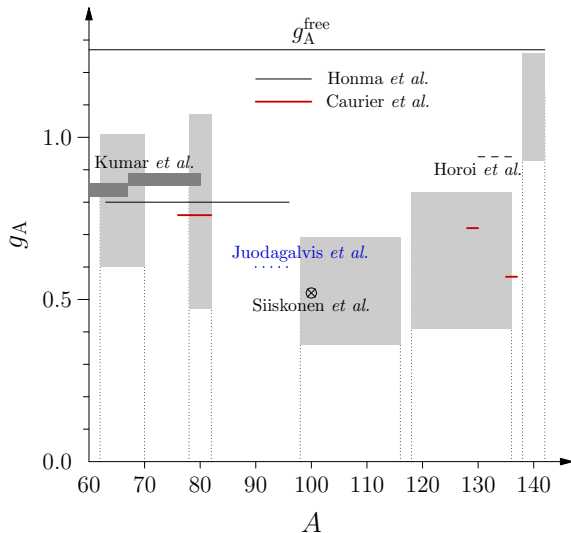
[3] F. Deppisch, J. S., Phys. Rev. C 94
(2016) 055501



Fundamental quenching: M. Ericson (1971); M. Ericson *et al.* (1973);
M. Rho (1974); D. H. Wilkinson (1974)

(Meson-exchange currents \rightarrow effective two-body operators)

Results from the ISM on top of the pnQRPA ranges

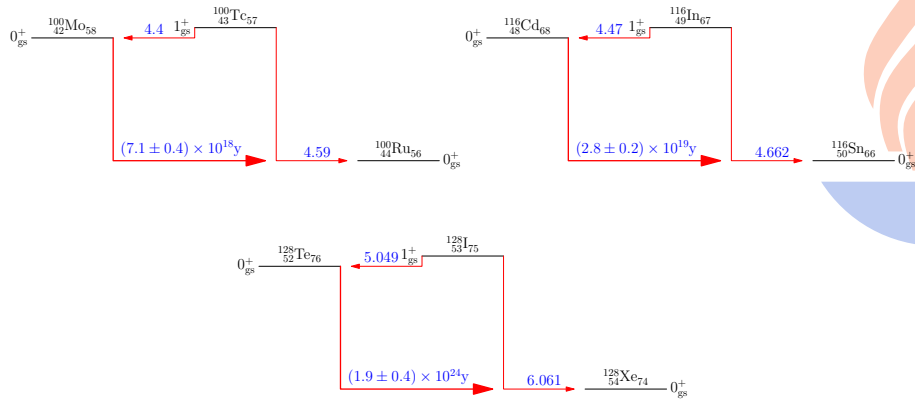


- **Kumar et al.:** J. Phys. G 43 (2016) 105104
- **Honma et al.:** J. Phys. Conf. Ser. 49 (2006) 45
- **Caurier et al.:** Phys. Lett. B 711 (2012) 62
- **Horoi et al.:** Phys. Rev. C 93 (2016) 024308
- **Juodagalvis et al.:** Phys. Rev. C 72 (2005) 024306
- **Siiskonen et al.:** Phys. Rev. C 63 (2001) 055501

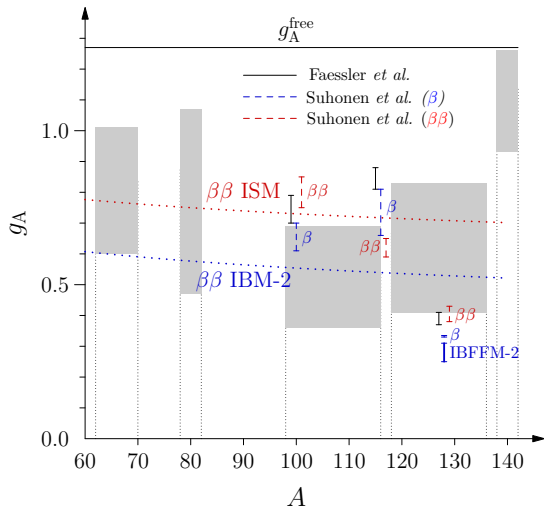
Results from:

Quenching of g_A
in the pnQRPA-based,
ISM-based and
IBM-based calculations
of β decays and $\beta\beta$ decays

The studied cases



Results from the $\beta+\beta\beta$ calculations against the pnQRPA ranges from Gamow-Teller β decays



- **pnQRPA: Faessler *et al.***, A. Faessler, G. L. Fogli, E. Lisi, V. Rodin, A. M. Rotunno, F. Šimkovic, arXiv 0711.3996v1 [Nucl-th]
- **pnQRPA: Suhonen *et al.***, J. Suhonen, O. Civitarese, Nucl. Phys. A 924 (2014) 1
- **$\beta\beta$ ISM and IBM-2:** J. Barea, J. Kotila, F. Iachello, Phys. Rev. C 87 (2013) 014315
- **IBFFM-2:** N. Yoshida, F. Iachello, Prog. Theor. Exp. Phys. 2013 (2013) 043D01

Results from:

Effective value of g_A
as derived from
electron spectra of
forbidden non-unique β decays

Spectrum shape of higher-forbidden non-unique β decays

Half-life:

$$t_{1/2} = \kappa / \tilde{C}.$$

Dimensionless integrated shape function:

$$\tilde{C} = \int_1^{w_0} C(w_e) p w_e (w_0 - w_e)^2 F_0(Z_f, w_e) dw_e.$$

Shape factor:

$$C(w_e) = \sum_{k_e, k_\nu, K} \lambda_{k_e} \left[M_K(k_e, k_\nu)^2 + m_K(k_e, k_\nu)^2 - \frac{2\gamma_{k_e}}{k_e w_e} M_K(k_e, k_\nu) m_K(k_e, k_\nu) \right],$$

where

$$\lambda_{k_e} = \frac{F_{k_e-1}(Z, w_e)}{F_0(Z, w_e)}; \quad \gamma_{k_e} = \sqrt{k_e^2 - (\alpha Z_f)^2},$$

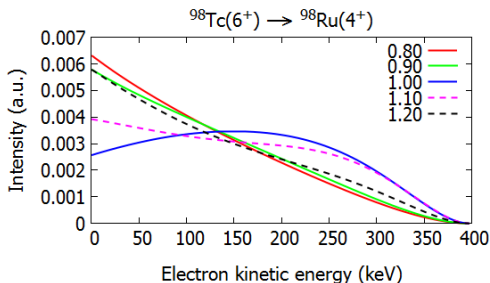
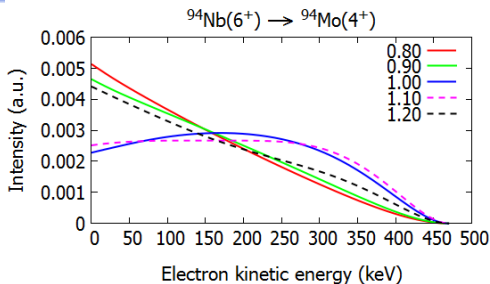
$F_{k-1}(Z, w_e)$ being the generalized Fermi function.

Decomposition of the shape factor:

$$C(w_e) = g_V^2 C_V(w_e) + g_A^2 C_A(w_e) + g_V g_A C_{VA}(w_e).$$

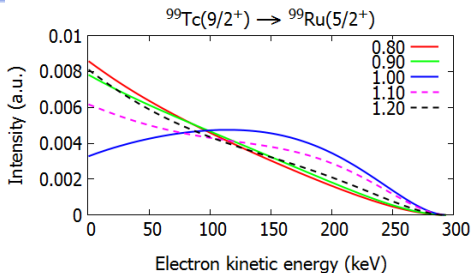
ISM-computed β spectra for different values of g_A

Normalized
ISM-computed
electron spectra for
the $2nd$ -forbidden
nonunique β^-
decays of ^{94}Nb and
 ^{98}Tc ($g_V = 1.0$).

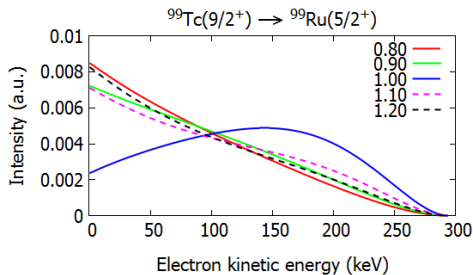


Example: ISM- and MQPM-computed electron spectra

Normalized ISM-
and
MQPM-computed
electron spectra for
the 2nd-forbidden
nonunique β^- decay
of ^{99}Tc ($g_V = 1.0$)
using different
values of g_A .



(ISM)



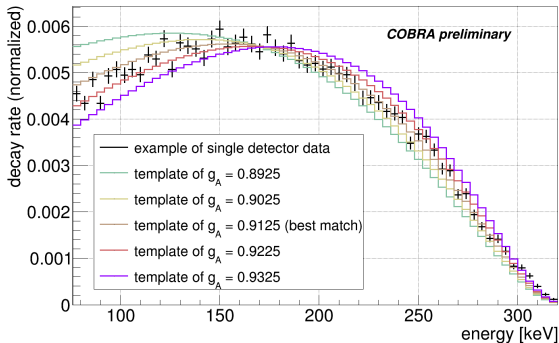
(MQPM)

Example: Decay of ^{113}Cd – Comparison with data

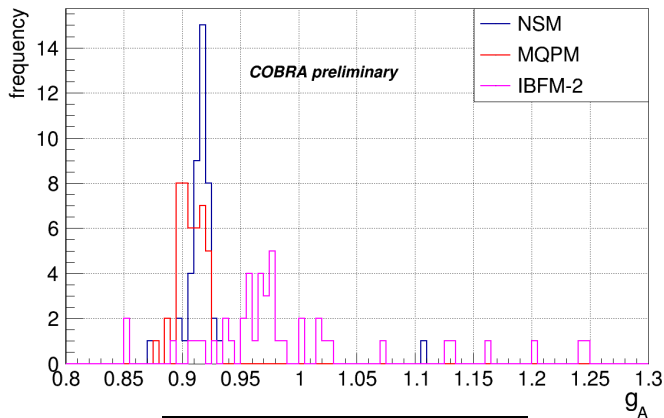
Normalized electron spectra
for the 4th-forbidden
nonunique β^- decay
 $^{113}\text{Cd}(1/2^+) \rightarrow ^{113}\text{In}(9/2^+)$
($g_V = 1.0$).

Experimental data from:

The **COBRA** collaboration,
L. Bodenstern-Dresler *et al.*, arXiv:1806.02254
[nucl-ex] 6 Jun 2018



Distribution of the best-match g_A values from 44 detector units



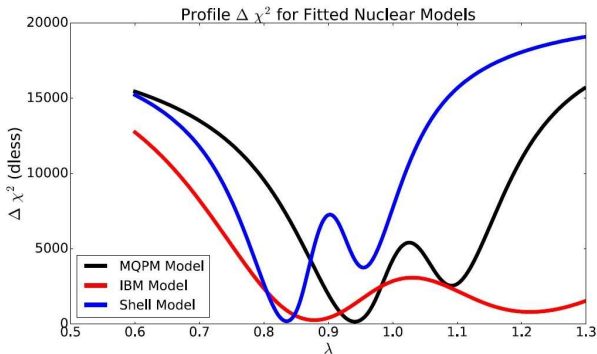
$$\begin{aligned}\bar{g}_A(\text{ISM}) &= 0.92 \pm 0.02 \\ \bar{g}_A(\text{MQPM}) &= 0.91 \pm 0.01 \\ \bar{g}_A(\text{IBFM-2}) &= 0.94 \pm 0.09\end{aligned}$$

Example: Decay of ^{115}In – Comparison with data

Normalized electron spectra
for the 4th-forbidden
nonunique β^- decay
 $^{115}\text{In}(9/2^+) \rightarrow ^{115}\text{Sn}(1/2^+)$
($g_V = 1.0$).

Result from:

The MIT-CSNSM-Jyväskylä
collaboration, A. Leder *et al.*,
to be submitted.



$$\begin{aligned}\bar{g}_A(\text{ISM}) &= 0.83 \pm 0.03 \\ \bar{g}_A(\text{IBFM-2}) &= 0.88 \pm 0.06 \\ \bar{g}_A(\text{MQPM}) &= 0.94^{+0.03}_{-0.04}\end{aligned}$$

Summary of the exploratory work on β spectra

Transition	$J_i^{\pi_i}$ (gs)	$J_f^{\pi_f}$ (n_f)	Branching	K	Sensitivity	Nucl. model
$^{36}\text{Cl} \rightarrow ^{36}\text{Ar}$	2+	0+ (gs)	98%	2	None	ISM
$^{48}\text{Ca} \rightarrow ^{48}\text{Sc}$	0+	4+ (2)	$\sim 0\%$	4	None	ISM
$^{48}\text{Ca} \rightarrow ^{48}\text{Sc}$	0+	6+ (gs)	$\sim 0\%$	6	None	ISM
$^{50}\text{V} \rightarrow ^{50}\text{Cr}$	6+	2+ (1)	$\sim 0\%$	4	Weak	ISM
$^{60}\text{Fe} \rightarrow ^{60}\text{Co}$	0+	2+ (1)	100%	2	None	ISM
$^{85}\text{Br} \rightarrow ^{85}\text{Kr}$	3/2-	9/2+ (gs)	$\sim 0\%$	3	Moderate	MQPM
$^{87}\text{Rb} \rightarrow ^{87}\text{Sr}$	3/2-	9/2+ (gs)	100%	3	Moderate	MQPM, ISM
$^{92}\text{Rb} \rightarrow ^{92}\text{Sr}$	0-	0+ (gs)	95%	1	Weak	ISM
$^{93}\text{Zr} \rightarrow ^{93}\text{Nb}$	5/2+	9/2+ (gs)	$5 \leq \%$	2	Weak	MQPM
$^{93}\text{Y} \rightarrow ^{93}\text{Zr}$	1/2-	1/2+ (1)	2%	1	Moderate	ISM
$^{94}\text{Nb} \rightarrow ^{94}\text{Mo}$	6+	4+ (2)	100%	2	Strong	NSM
$^{95}\text{Sr} \rightarrow ^{95}\text{Y}$	1/2+	1/2- (gs)	56%	1	Weak	ISM
$^{96}\text{Zr} \rightarrow ^{96}\text{Nb}$	0+	4+ (2)	$\sim 0\%$	4	None	ISM
$^{96}\text{Zr} \rightarrow ^{96}\text{Nb}$	0+	6+ (gs)	$\sim 0\%$	6	Strong	ISM
$^{96}\text{Y} \rightarrow ^{96}\text{Zr}$	0-	0+ (gs)	96%	1	weak	ISM
$^{97}\text{Zr} \rightarrow ^{97}\text{Nb}$	1/2+	9/2+ (gs)	$\sim 0\%$	4	Strong	MQPM
$^{97}\text{Y} \rightarrow ^{97}\text{Zr}$	1/2+	1/2- (gs)	40%	1	Weak	ISM
$^{98}\text{Tc} \rightarrow ^{98}\text{Ru}$	6+	4+ (3)	100%	2	Strong	ISM
$^{99}\text{Tc} \rightarrow ^{99}\text{Ru}$	9/2+	5/2+ (gs)	100%	2	Strong	MQPM, ISM

Summary on β spectra continues . . .

Transition	$J_i^{\pi_i}$ (gs)	$J_f^{\pi_f}$ (n_f)	Branching	K	Sensitivity	Nucl. model
$^{101}\text{Mo} \rightarrow ^{101}\text{Tc}$	1/2 ⁺	9/2 ⁺ (gs)	~0%	4	Strong	MQPM
$^{113}\text{Cd} \rightarrow ^{113}\text{In}$	1/2 ⁺	9/2 ⁺ (gs)	100%	4	Strong	MQPM, ISM, IBFM-2
$^{115}\text{Cd} \rightarrow ^{115}\text{In}$	1/2 ⁺	9/2 ⁺ (gs)	~0%	4	Strong	MQPM
$^{115}\text{In} \rightarrow ^{115}\text{Sn}$	9/2 ⁺	1/2 ⁺ (gs)	100%	4	Strong	MQPM, ISM, IBFM-2
$^{117}\text{Cd} \rightarrow ^{117}\text{In}$	1/2 ⁺	9/2 ⁺ (gs)	~0%	4	Strong	MQPM
$^{119}\text{In} \rightarrow ^{119}\text{Sn}$	9/2 ⁺	1/2 ⁺ (gs)	~0%	4	Strong	MQPM
$^{123}\text{Sn} \rightarrow ^{123}\text{Sb}$	11/2 ⁻	1/2 ⁺ (4)	~0%	5	Weak	MQPM
$^{125}\text{Sb} \rightarrow ^{125}\text{Te}$	7/2 ⁺	9/2 ⁻ (3)	7.2%	1	None	MQPM
$^{126}\text{Sn} \rightarrow ^{126}\text{Sb}$	0 ⁺	2 ⁺ (5)	100%	2	None	ISM
$^{133}\text{Sn} \rightarrow ^{133}\text{Sb}$	7/2 ⁻	7/2 ⁺ (gs)	85%	1	Weak	ISM
$^{134}\text{Sb} \rightarrow ^{134}\text{Te}$	0 ⁻	0 ⁺ (gs)	98%	1	Weak	ISM
$^{135}\text{Cs} \rightarrow ^{135}\text{Ba}$	7/2 ⁺	3/2 ⁺ (gs)	100%	2	None	MQPM
$^{135}\text{Te} \rightarrow ^{135}\text{I}$	7/2 ⁻	7/2 ⁺ (gs)	62%	1	Weak	ISM
$^{137}\text{Cs} \rightarrow ^{137}\text{Ba}$	7/2 ⁺	3/2 ⁺ (gs)	5.4%	2	None	MQPM, ISM
$^{137}\text{Xe} \rightarrow ^{137}\text{Cs}$	7/2 ⁻	7/2 ⁺ (gs)	67%	1	Weak	ISM
$^{138}\text{Cs} \rightarrow ^{138}\text{Ba}$	3 ⁻	3 ⁺ (1)	44%	1	Strong	ISM
$^{139}\text{Ba} \rightarrow ^{139}\text{La}$	7/2 ⁻	7/2 ⁺ (gs)	70%	1	Weak	ISM
$^{139}\text{Cs} \rightarrow ^{139}\text{Ba}$	7/2 ⁺	7/2 ⁻ (gs)	85%	1	Weak	ISM

Summary on β spectra continues . . .

Transition	$J_i^{\pi_i}$ (gs)	$J_f^{\pi_f}$ (n_f)	Branching	K	Sensitivity	Nucl. model
$^{141}\text{Ce} \rightarrow ^{141}\text{Pr}$	$7/2^-$	$5/2^+$ (gs)	31%	1	Weak	MQPM
$^{142}\text{Pr} \rightarrow ^{142}\text{Nb}$	2^-	2^+ (1)	3.7%	1	Weak	ISM
$^{143}\text{Pr} \rightarrow ^{143}\text{Nb}$	$7/2^+$	$7/2^-$ (gs)	100%	1	Weak	ISM
$^{159}\text{Gd} \rightarrow ^{159}\text{Tb}$	$3/2^-$	$5/2^+$ (1)	26%	1	None	MQPM
$^{161}\text{Tb} \rightarrow ^{161}\text{Dy}$	$3/2^+$	$5/2^-$ (1)	$\sim 0\%$	1	None	MQPM
$^{169}\text{Er} \rightarrow ^{169}\text{Tm}$	$1/2^-$	$3/2^+$ (1)	45%	1	None	MQPM
$^{210}\text{Bi} \rightarrow ^{210}\text{Po}$	1^-	0^+ (gs)	100%	1	Strong	ISM
$^{211}\text{Pb} \rightarrow ^{211}\text{Bi}$	$9/2^+$	$9/2^-$ (gs)	91%	1	Weak	ISM
$^{213}\text{Bi} \rightarrow ^{213}\text{Po}$	$9/2^-$	$9/2^+$ (gs)	66%	1	Weak	ISM

Conclusions about the effective g_A

Conclusion 1:

The long chain of ISM calculations and the recent pnQRPA and IBM-2 calculations of Gamow-Teller β decays and $2\nu\beta\beta$ decays are (surprisingly!) **consistent with each other** and clearly point to a **A -dependent quenched g_A**

Conclusion 2:

The **spectrum-shape method (SSM)** for forbidden non-unique β decays is a **robust tool** (largely independent of the nuclear model, the assumed Hamiltonian and mean field) to search for the **effective value of g_A** and to try to solve other problems, like those related to the **reactor- $\bar{\nu}_e$ spectra**

PART 2: Neutrino-related anomalies imply oscillations to sterile neutrinos

Sterile neutrinos:

The gallium anomaly

The reactor antineutrino anomaly

imply oscillations of the “ordinary” neutrinos (ν_e, ν_μ, ν_τ) to

STERILE NEUTRINO

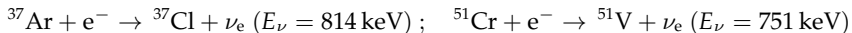
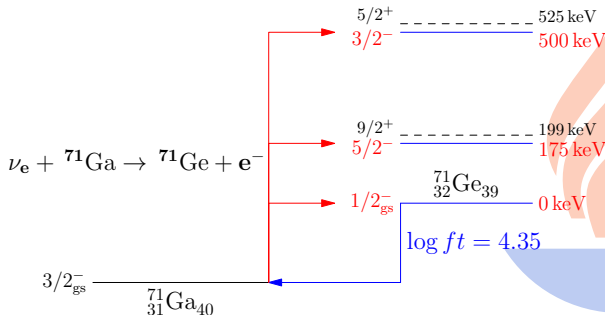
in the mass range of a few eV

But what are these anomalies?

The ^{71}Ga anomaly (has pestered us for some 20 years!)

Charged-current
neutrino- ^{71}Ga scattering
via Gamow-Teller type of
transitions.

Monoenergetic ν_e from
artificial neutrino sources
via
Electron captures:



The **scattering cross sections** σ have been measured by the **GALLEX experiment** [Phys. Lett. B 342 (1995) 440 ; ibid B 420 (1998) 114 ; ibid B 685 (2010) 47] and the **SAGE experiment** [Phys. Rev. Lett. 77 (1996) 4708 ; Phys. Rev. C 59 (1999) 2246 ; ibid C 73 (2006) 045805 ; ibid C 80 (2009) 015807]

Estimation of the scattering cross section

The cross sections can be deduced from neutrino kinematics, as first done by J. N. Bahcall, Phys. Rev. C 56 (1997) 3391 (verified by our more complete calculations)

$$\sigma(^{37}\text{Ar}) = 6.62 \times 10^{-45} \text{ cm}^2 \left(1 + 0.695 \frac{\text{BGT}_{175}}{\text{BGT}_{\text{gs}}} + 0.263 \frac{\text{BGT}_{500}}{\text{BGT}_{\text{gs}}} \right).$$

$$\sigma(^{51}\text{Cr}) = 5.53 \times 10^{-45} \text{ cm}^2 \left(1 + 0.667 \frac{\text{BGT}_{175}}{\text{BGT}_{\text{gs}}} + 0.218 \frac{\text{BGT}_{500}}{\text{BGT}_{\text{gs}}} \right),$$

where BGT_{gs} can be normalized by the $\log ft$ of the Gamow-Teller EC transition $^{71}\text{Ge}(1/2_{\text{gs}}^-) \rightarrow ^{71}\text{Ga}(3/2_{\text{gs}}^-)$, and $\text{BGT} = (g_A)^2 (f \| \mathcal{O}_{\text{GT}} \| i)^2 / (2J_i + 1)$, J_i being the angular momentum of the initial state.

BGT ratios can be taken from D. Frekers *et al.*, The $^{71}\text{Ga}(^3\text{He}, t)$ reaction and the low-energy neutrino response, Phys. Lett B 706 (2011) 134:

$$\frac{\text{BGT}_{175}}{\text{BGT}_{\text{gs}}} = 0.039 \pm 0.030; \quad \frac{\text{BGT}_{500}}{\text{BGT}_{\text{gs}}} = 0.202 \pm 0.016,$$

or from our shell-model calculations with the JUN45 interaction:

$$\frac{\text{BGT}_{175}}{\text{BGT}_{\text{gs}}} = 0.033; \quad \frac{\text{BGT}_{500}}{\text{BGT}_{\text{gs}}} = 0.016,$$

Quantitative statement of the gallium anomaly

$$R = \frac{\sigma_{\text{measured}}(\text{GALLEX,SAGE})}{\sigma_{\text{estimated}}}$$

It seems that **experiments measure a reduced neutrino flux:**

Estimate	GALLEX 1	GALLEX 2	SAGE 1	SAGE 2
$R(\text{Frekers } et al.)$	0.93 ± 0.11	0.79 ± 0.11	0.93 ± 0.11	0.77 ± 0.08
$R(\text{SM, JUN45})$	0.98 ± 0.11	0.83 ± 0.11	0.97 ± 0.12	0.81 ± 0.09

?
⇒ Oscillations to STERILE NEUTRINOS

Questions raised:

- Are there problems with the cross-section measurements (GALLEX 1 vs. GALLEX 2, SAGE 2)?
- Why the BGT of Frekers *et al.* deviate from the shell-model computed BGTs?

Problems with the analysis of the $^{71}\text{Ga}(^3\text{He}, t)$ reaction?

$$\text{BGT}_{\text{reaction}} = \frac{(g_A)^2}{2j_i+1} [(f\|\mathcal{O}_{\text{GT}}\|i) + \delta(f\|\mathcal{O}_{\text{T}}\|i)]^2,$$

where $\mathcal{O}_{\text{T}} \sim [\sigma Y_2]_1$ is the **tensor part** entering the reaction analysis and $\delta = 0.097$ is the mixing strength (From the analysis of Gamow-Teller transitions in the sd shell: W.C. Haxton, Phys. Lett. B 431 (1998) 110.).

We find **interference of the GT and tensor terms**:

Transition	$(f\ \mathcal{O}_{\text{GT}}\ i)$	$(f\ \mathcal{O}_{\text{T}}\ i)$	$\text{BGT}_{\beta}(\text{SM})$	$\text{BGT}_{\text{reaction}}(\text{SM})$
$3/2^- (\text{Ga}) \rightarrow 1/2^- (\text{Ge, gs})$	-0.795	0.465	0.158	0.141
$3/2^- (\text{Ga}) \rightarrow 5/2^- (\text{Ge, 175 keV})$	0.144	-1.902	0.0052	0.0004
$3/2^- (\text{Ga}) \rightarrow 3/2^- (\text{Ge, 500 keV})$	0.100	0.048	0.0025	0.0027

The charge-exchange reactions assume always a **constructive interference of the GT and tensor terms**!

Conclusions about the ^{71}Ga anomaly

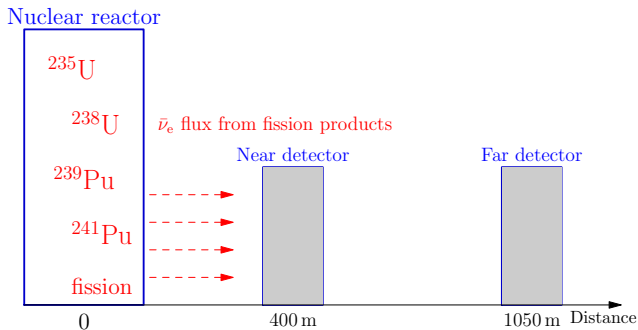
Conclusions:

NONE YET!

The work continues. . .

The reactor antineutrino anomaly

The $\bar{\nu}_e$ flux from reactors has been measured in **short-baseline neutrino-oscillation experiments**¹: **Daya Bay** (in Daya Bay, China; 6 reactors, 8 detectors), **RENO** (South Korea; 2 detectors 294m and 1383 m from 6 reactors) and **Double Chooz** (Chooz, France, 2 detectors 400m and 1050 m from 2 reactors, schematic figure below).



¹RENO: Phys. Rev. Lett. 108 (2012) 191802; Double Chooz: J. High Energy Phys. 2014 (2014) 86; Daya Bay: Phys. Rev. Lett. 116 (2016) 061801.

The neutrino-flux measurements find:

The reactor $\bar{\nu}_e$ anomaly:

The measured flux is some **5% smaller** than that predicted from the β decays of the fission yields of the reactor fuel

\Rightarrow ?
 \Rightarrow Oscillations to STERILE NEUTRINOS

The bump anomaly:

There is an unexpected **bump at 4 – 6 MeV (spectral shoulder)** in the measured $\bar{\nu}_e$ spectrum.

\Rightarrow ???

Novel application of calculated electron spectra

Implement:

machinery to compute
the spectral shapes of
key first-forbidden transitions
making up some 50% of the total flux
and even more at the spectral bump

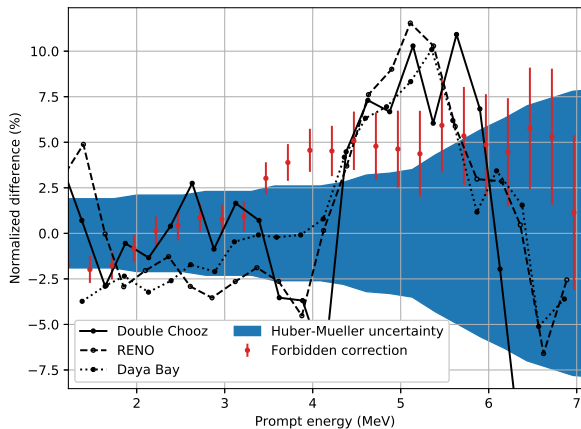
See: L. Heyen, J. Kostensalo, N. Severijns, J.S., First forbidden transitions in the reactor anomaly, arXiv:1805.12259 [nucl-th] 30 May 2018

Results from the analysis

Taking into account the first-forbidden (non-unique) decays of

$^{86}\text{Br}(0^+)$, $^{86}\text{Br}(2^+)$, ^{87}Se ,
 $^{89}\text{Br}(3/2^+)$, $^{89}\text{Br}(5/2^+)$, ^{90}Rb ,
 $^{91}\text{Kr}(5/2^-)$, $^{91}\text{Kr}(3/2^-)$, ^{92}Rb ,
 ^{92}Y , ^{93}Rb , $^{94}\text{Y}(0^+)$, $^{95}\text{Rb}(7/2^+)$,
 $^{95}\text{Rb}(3/2^+)$, ^{95}Sr , ^{96}Y , ^{97}Y , ^{98}Y ,
 ^{133}Sn , $^{134m}\text{Sb}(6^+)$, $^{134m}\text{Sb}(6^+?)$,
 ^{135}Te , ^{136m}I , ^{137}I , ^{138}I , ^{140}Cs ,
 ^{142}Cs

decreases the computed $\bar{\nu}$ flux by 5%
!



The spectral sholder appears due to forbidden spectral corrections !

Conclusions about the reactor $\bar{\nu}_e$ anomaly

Conclusions:

Proper account of the **spectral shapes** of

(first) forbidden β decays

is instrumental in the quest of the solution

to the anomaly

The work still continues. . .

The end

THANKS FOR PATIENCE!