

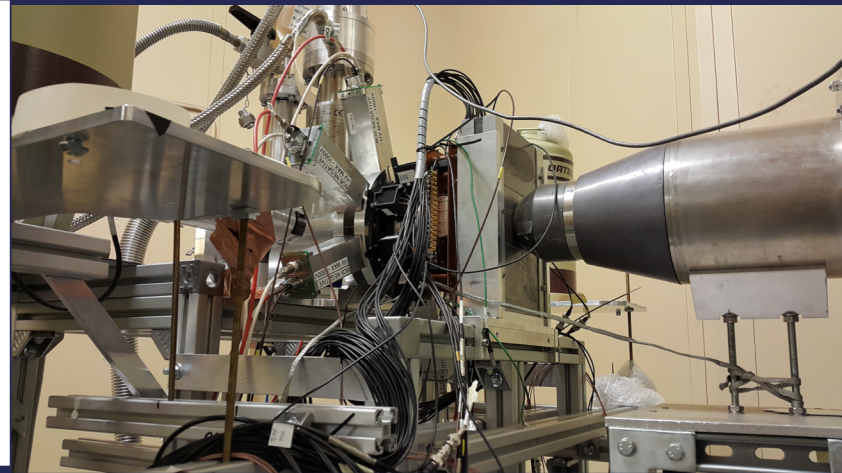
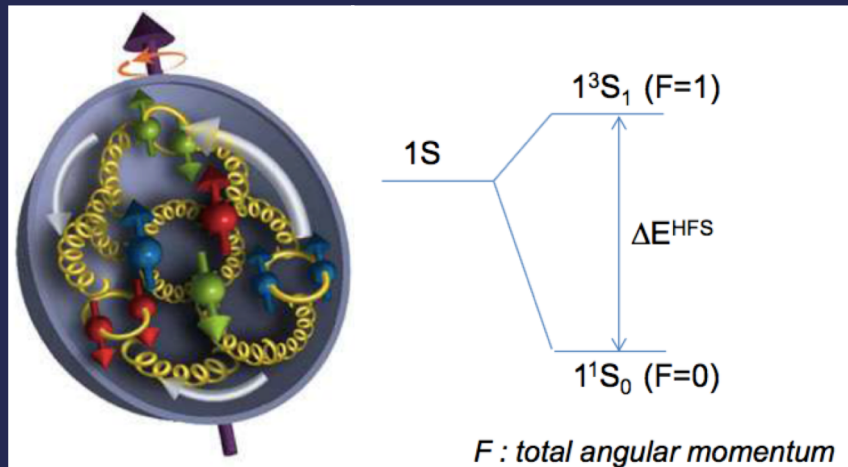
The FAMU experiment:

measuring the ground-state hyperfine splitting in muonic hydrogen

$$\Delta E_{\text{HFS}}(\mu p)_{1S}$$

Determination of the Zemach radius of the proton

Andrea Vacchi for the FAMU Collaboration



FAMU Collaboration



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INFN Roma3: L. Colace, M. De Vincenzi, A. Iaciovano, L. Tortora, F. Somma

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CNR-INO: B. Patrizi, A. Piori, G. Toci, M. Vannini

RIKEN-RAL: K. Ishida

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OUTLINE

- Background & motivations
- FAMU's method to measure the hfs
- 2016 muon transfer rate measurements between 100 and 300 K
- FAMU key ingredients optimization
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- Conclusions

Muonic hydrogen μH

Muon (e^- 's heavier twin) orbiting the proton instead of electron.

$$m_\mu = 207 m_e$$

$$r_\mu = \frac{1}{186} r_e$$

0.511 MeV -1 $\frac{1}{2}$ e electron	105.7 MeV -1 $\frac{1}{2}$ μ muon
--	---

$$m_\mu / m_e \approx 2 \times 10^2$$

- the *radius of the muon orbit* is $\sim a_0/200$ so that the energy levels of muonic hydrogen are orders of magnitude more “sensitive” to the details of the proton structure than the levels of normal hydrogen.
- the binding energy of the ground state of muonic hydrogen is of the order of 200 Ry,

why measuring $\Delta E_{\text{HFS}}(\mu^-p)_{1s}$?

why new independent high precision measurements on μ^-p are needed?

- In eH – “ordinary hydrogen” the hyperfine splitting (HFS) is known to 13 digits – in frequency units
 - $E_{\text{HFS}}^{\text{exp}}(\text{ep}) = 1420,4057517667(9) \text{ MHz}$
- while in μH
 - $E_{\text{HFS}}^{\text{exp}}(\mu p) = 22,8089(51) \text{ meV} \quad [224\text{ppm}]$
- Theory reaches 6 digits of accuracy

muonic hydrogen precision spectroscopy

The muon is tightly bound in hydrogen-like orbits that have very large overlaps with the proton this allows :

- *very high accuracy tests of quantum electrodynamics and the theory of electromagnetic bound states.*
- *verify the theoretical predictions of the nature of quantum mechanics in very strong fields.*
- *precise determination of the values of the fundamental physical constants (particle masses, fine structure constant, proton charge radius, etc.).*
- *point towards physics beyond the Standard Model of particle physics.*

why measuring $\Delta E_{\text{HFS}}(\mu^-p)_{1s}$?

why new independent high precision measurements on μ^-p are needed?

- *surprising Lamb shift measurements points to HFS (next slide)*
- *can check e μ universality*
- *or believing in e μ universality, accurate measurements gives information on the proton structure*
- *accurate data measure the corrections to the leading order*
- *one correction term is sensitive to the magnetic form factor G_M at low momentum transfer, i.e., to the proton magnetic radii R_M*
- *R_M obtained from scattering experiments is a source of controversy*



The proton charge radius can be extracted for each lepton probe from **two** independent methods

Proton radius puzzle

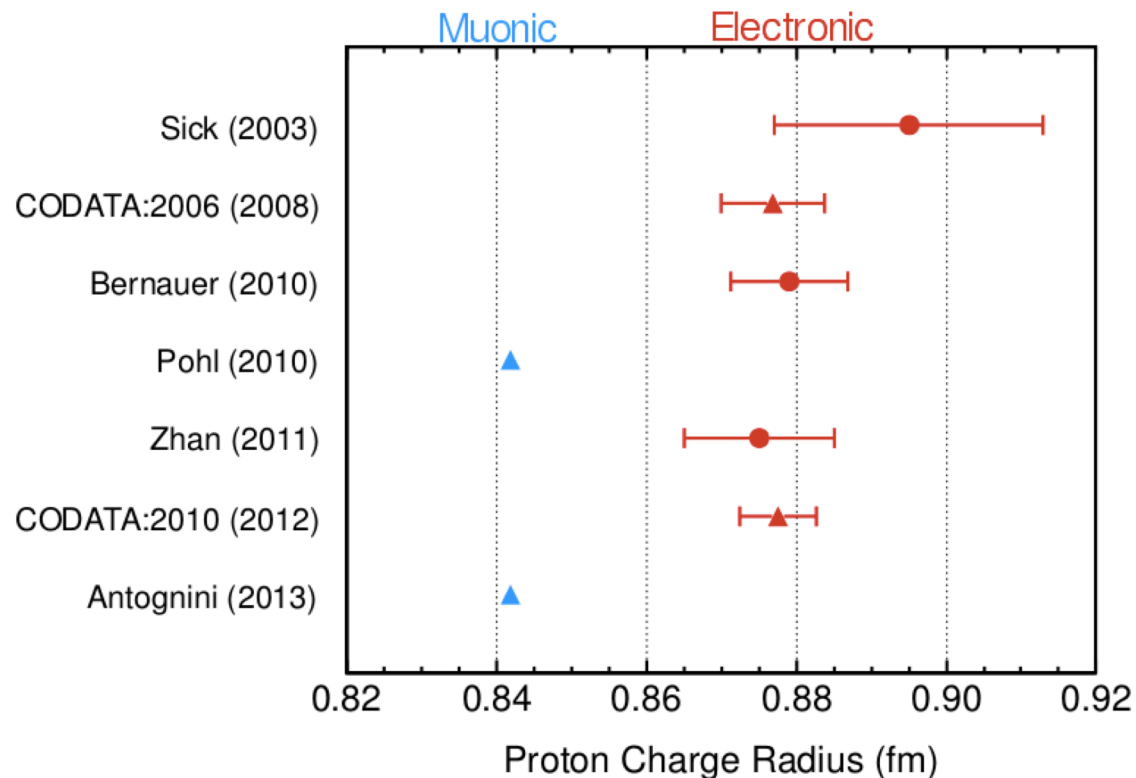
$$[R_{Ep}^{\mu H} = 0.84087(39) \text{ fm}]$$

- [1] R. Pohl, A. Antognini et al., Nature **466**, 213 (2010).
[2] A. Antognini et al., Science **339**, 417 (2013).

↕ **5.6 σ discrepancy**

$$[R_{Ep}^{\text{CODATA 2014}} = 0.8751(61) \text{ fm}]$$

- [3] P. J. Mohr, et al., Rev. Mod. Phys. **84**, 1527 (2012).



The CODATA value of the proton charge radius as obtained from a combination of 24 transition frequency measurements in H and deuterium and several results from elastic electron scattering is **0.88 fm**. However, the **muonic hydrogen Lamb Shift** measurements yield a radius of **0.84 fm**.

why measuring $\Delta E_{\text{HFS}}(\mu^-p)_{1s}$?

why new independent high precision measurements on μ^-p are needed?

$$\Delta E_{\text{HFS}}^{\text{thy}}(ep) = E_F^{ep} (1 + \Delta_{\text{QED}} + \underbrace{\Delta_{hvp}^p + \Delta_{\mu vp}^p + \Delta_{\text{weak}}^p}_{\text{small terms}} + \Delta_S)$$

Fermi Energy

Accurately known

small terms

Proton
structure
term

Structure term ΔS commonly broken into 3 parts

$$\Delta_S = \Delta_Z + \Delta_R + \Delta_{\text{pol}}$$

- Δ_Z = NR limit of the elastic contribution
- Δ_R = relativistic corrections to elastic contribution
- Δ_{pol} = mixture of inelastic with elastic contribution

The Zemach term

$$\Delta_Z = -2\alpha m_r r_Z$$

$$r_Z = \int d^3r_1 \int d^3r_2 \rho_E(r_1) |\vec{r}_1 - \vec{r}_2| \rho_M(r_2)$$

or, using momentum space expression

$$r_Z = -\frac{4}{\pi} \int_0^\infty \frac{dQ}{Q^2} \left(\frac{G_E(Q^2) - G_M(Q^2)}{1 + k_p} - 1 \right)$$

$1+k_p$ is the magnetic moment of the proton (in proton magnetons)

$$G_M/(1 - k_p) = 1 - R_M^2 Q^2/6 \dots$$

shows the dependence on R_M and on R_E

Zemach radius r_Z contains information about both electric and magnetic distributions \rightarrow can help to pin down the magnetic properties of the proton

current status of r_{ch} & r_Z

units fm	rms charge radius r_{ch}	Zemach radius r_Z
e^- -p scattering & spectroscopy	$r_{\text{ch}} = 0.8751(61)$	$r_Z = 1.037(16)$ Dupays&al' 03 $r_Z = 1.086(12)$ s Friar&Sick' 04 $r_Z = 1.047(16)$ Volotka&al' 05 $r_Z = 1.045(4)$ s Distler&al' 11
μ^- -p Lamb shift spectroscopy	$r_{\text{ch}} = 0.84087(39)$	FAMU a 20 years old idea: r_Z from HFS of $(\mu^-p)_{1s}$ Either confirm a e^-p value or admit: e^-p and μ^-p differ

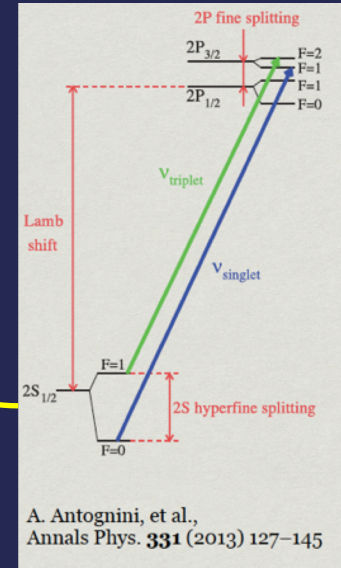
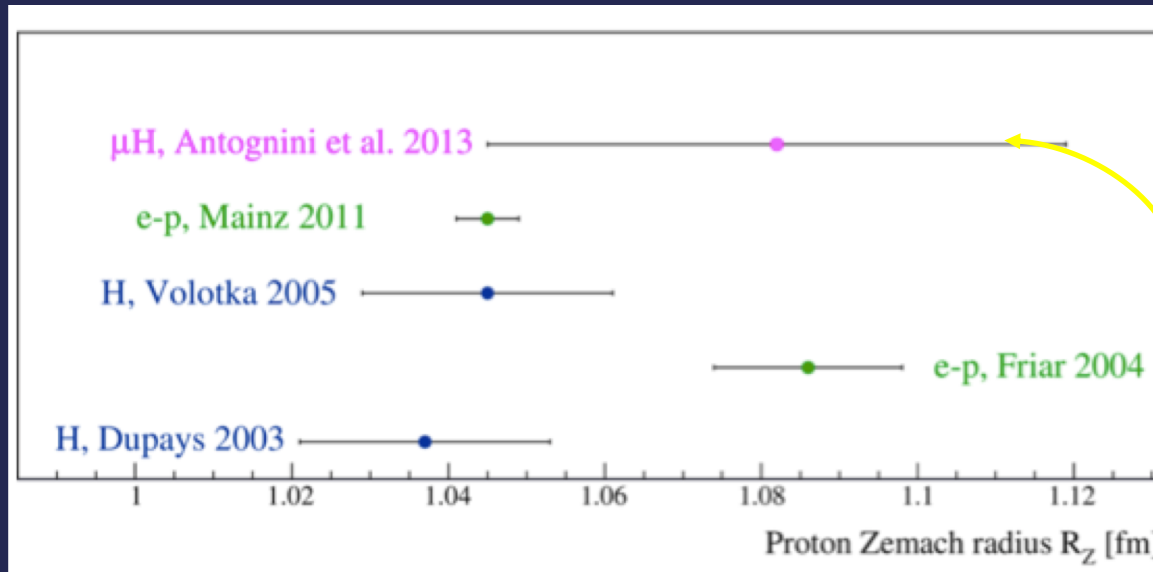
Recently : from hfs of $(\mu^-p)_{2s}$

$r_Z = 1.082(37)$ [PSI'12]

=> we need new independent measurements

r_Z current status

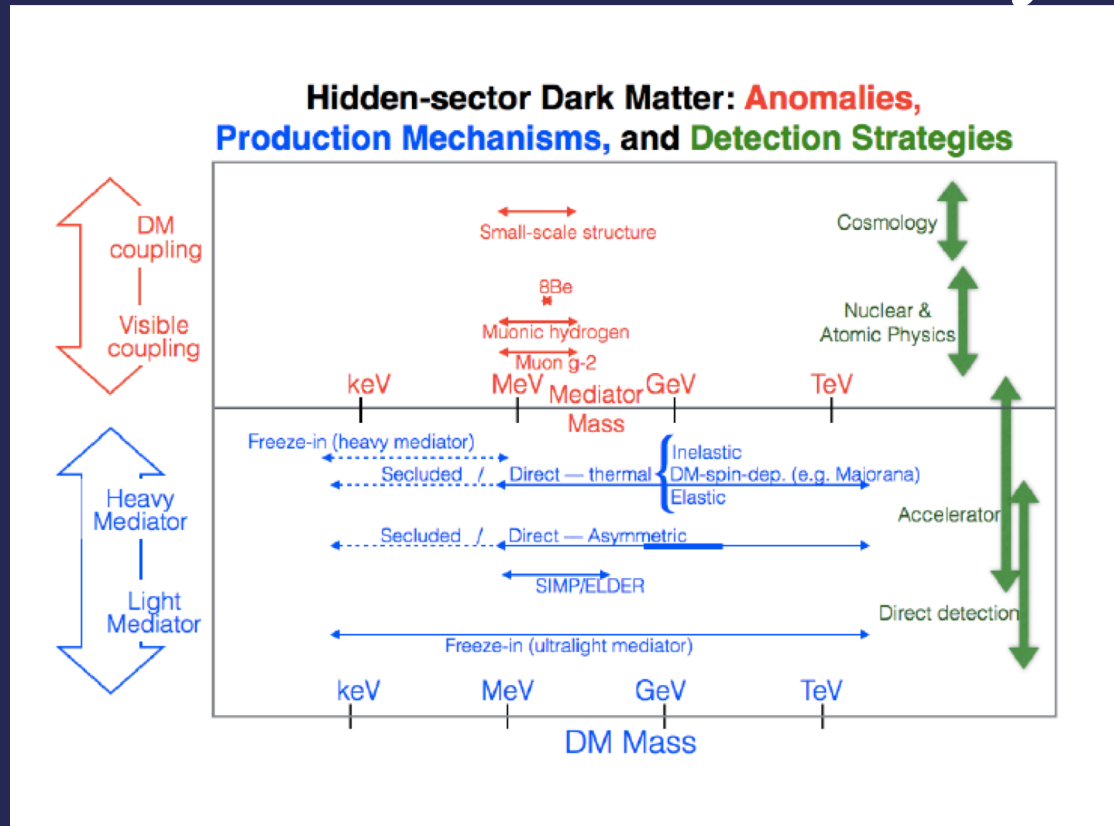
large errors! we need new measurement



The current theoretical uncertainty of r_Z significantly exceeds the experimental one.

The experimental results on the proton Zemach radius may be used as a test for the quality of models of the proton in the limit of low transfer momenta.

Experimental Anomalies and Hints muon-related anomaly



New models, astrophysical observations, and existing experimental anomalies point to the 1 to 100 MeV mass scale as a high value target region for dark matter and dark mediator searches.

The FAMU experiment goals

Currently two other independent experiments plan to measure R_Z

The spectroscopic measurement of $\Delta E_{\text{HFS}}(\mu^-p)_{1S}$, will :

- provide r_Z , the **Zemach radius of the proton**, with high precision to disentangle among discordant theoretical values
 - $\Delta E_{\text{HFS}}^{\text{exp}}(\mu p)$ to 5 – 10 ppm
 - get Zemach radius to < 0.1%, if theory perfect
- quantify any level of discrepancy between values of r_Z as extracted from normal and muonic hydrogen atoms leading to new information on proton structure and muon-nucleon interaction.

The experimental value of r_Z sets important restrictions on the theoretical models of proton electromagnetic structure and on the parametrization of proton form factors, in whose terms the theoretical values are calculated.

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a 25 years old idea and its evolution

Physics Letters A 172 (1993) 277–280
North-Holland

PHYSICS LETTERS A

Experimental method to measure the hyperfine splitting of muonic hydrogen (μ^-p)_{1S}

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Communicated by B. Fricke

We propose an experimental method to measure the hyperfine splitting of the energy level of the muonic hydrogen ground state (μ^-p)_{1S} by inducing a laser-stimulated para-to-ortho transition. The method requires an intense low energy pulsed μ^- beam and a high power tunable pulsed laser.

1. Introduction

The theoretical expression for the hyperfine splitting

A. Werthmüller et al. / Muon transfer to oxygen

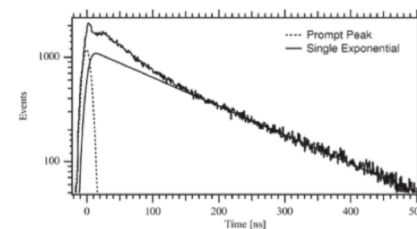


Figure 2. Background subtracted time distribution of muonic oxygen $\mu O(2-1)$ X-rays measured in a gaseous mixture of $H_2 + 0.4\%O_2$ at 15 bar and room temperature. The prompt peak corresponds essentially to muons directly captured in oxygen whereas the delayed part is due to muon transfer from the ground state of the $(\mu p)_{1S}$ atom. The solid line represents a pure exponential function to stress the additional structure.

F. Mulhauser, H. Schneuwly, Hyperfine Interact. 82 (1993).

A. Werthmüller, et al., Hyperfine Interact. 116 (1998).

For few gases the muon-transfer rate λ_{pZ} is energy dependent

Oxygen exhibits a peak in the muon transfer rate λ_{pZ}^{epith} at epithermal energy.

start with H and O gas mixture (around 1% O) at 80K

- I. • μH in $F=0$, $\mu^-p(\uparrow\downarrow)$
- II. • laser photons, at the correct frequency, $\mu^-p(\uparrow\downarrow) \rightarrow \mu^-p(\uparrow\uparrow)$
- III. • $F=1$ revert to $F=0$ by collisional deexcitation, but get kick
- IV. • moving μH have different capture rate on O, see more X-rays
- V. • measure the time distribution of O characteristic X-rays.



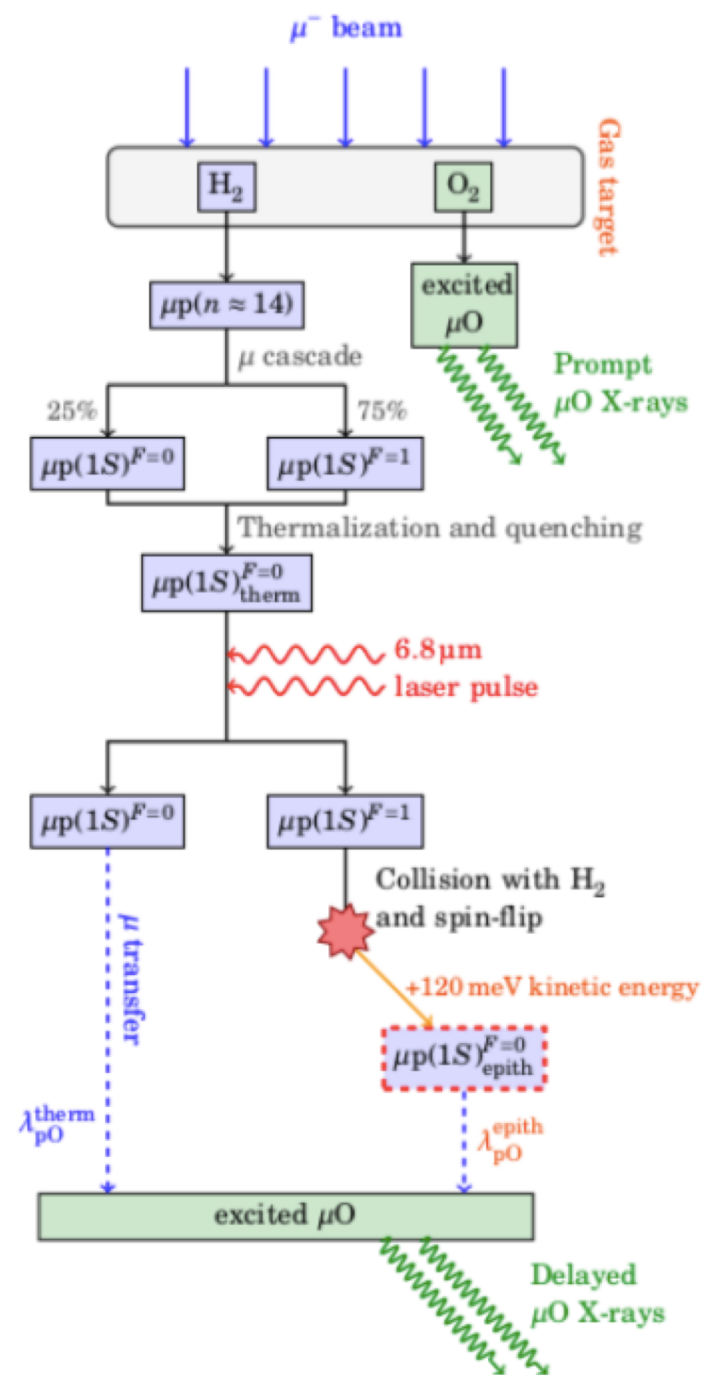
D. Bakalov, A. Adamczak et al., Phys. Lett. A379 (2014).

A. Adamczak et al. Hyperfine Interactions 136: 1–7, 2001.

FAMU Principle of operation

μp formation $\Rightarrow\Rightarrow$

μp thermalization $\Rightarrow\Rightarrow$

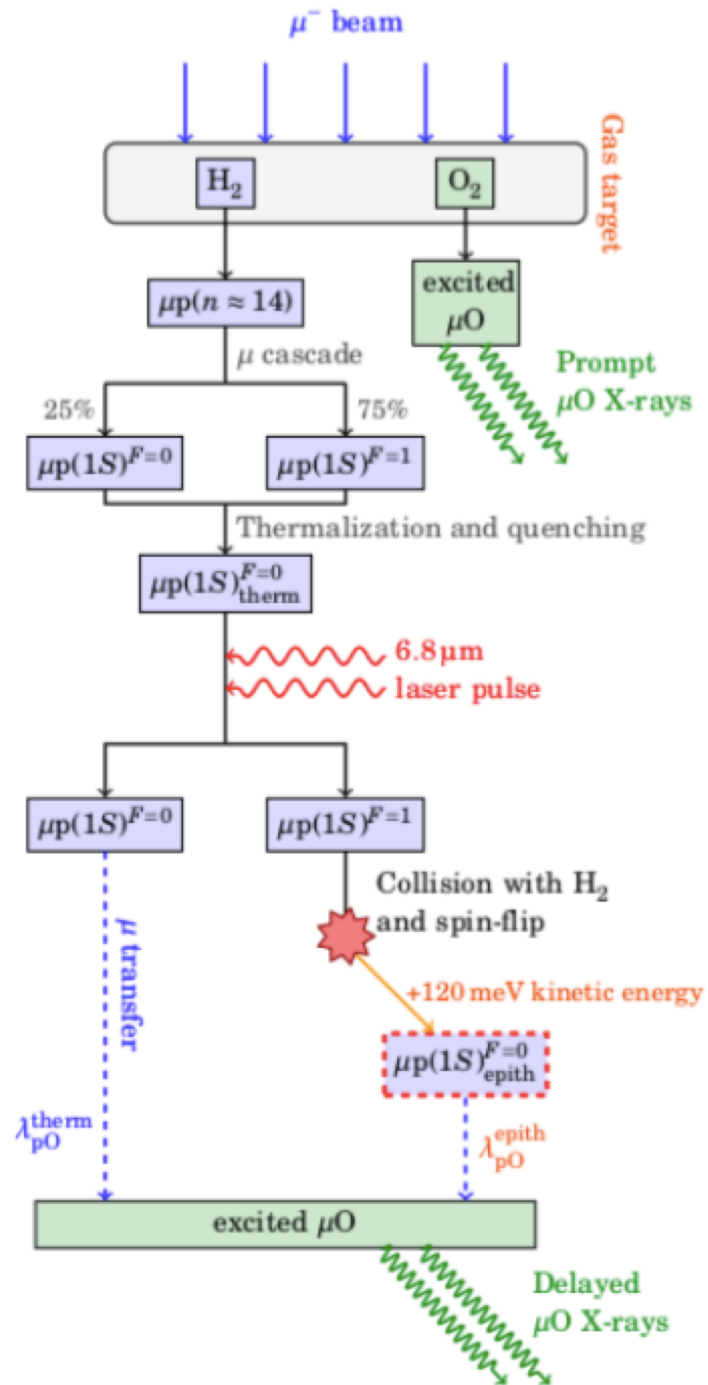


how it works

$\mu^-p(\uparrow\downarrow)$ absorbs a photon

@ *resonance wavelength* $\lambda_0 = hc/\Delta E^{1S}_{\text{HFS}}$
 $\Rightarrow \sim 6.8 \mu \sim 0.183 \text{ eV}$

$\mu^-p(\uparrow\downarrow) \rightarrow \mu^-p(\uparrow\uparrow)$



How it works

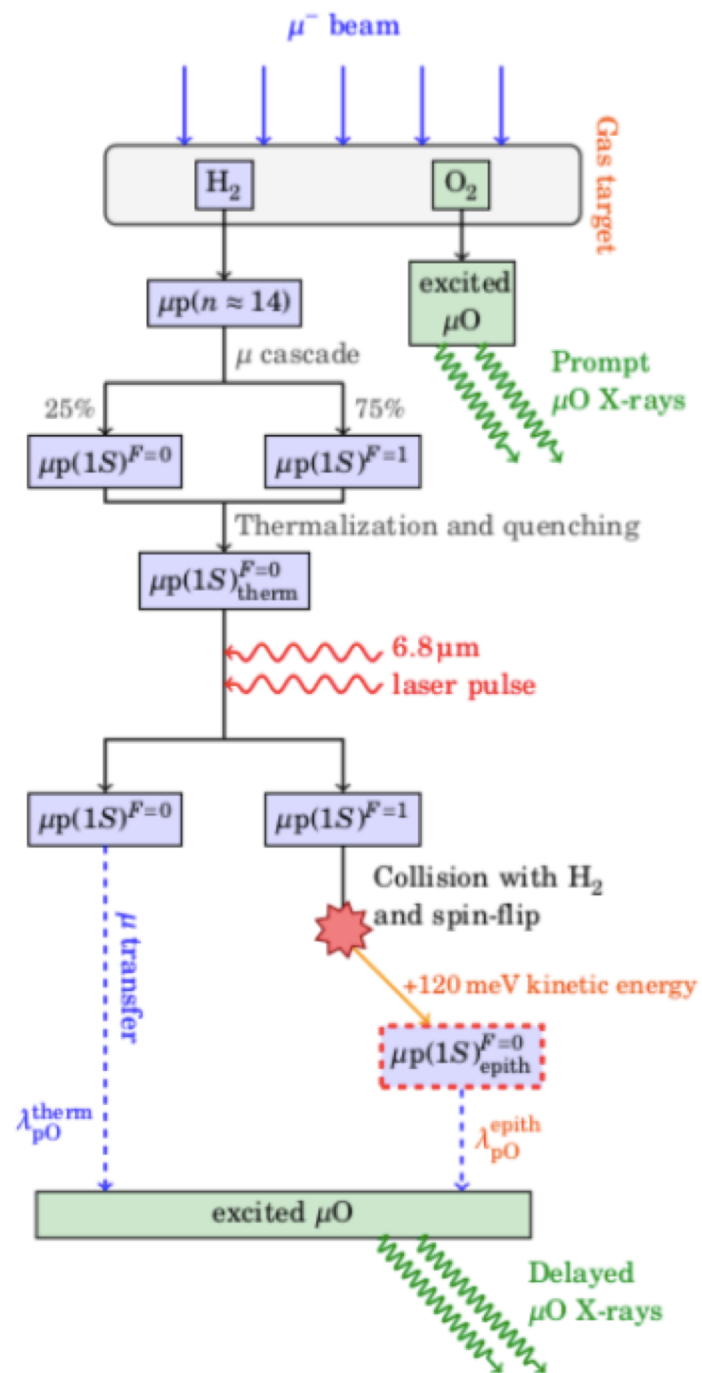
$\mu^-p(\uparrow\uparrow) \ ^3S_1$ atoms
 are collisionally de-excited $\mu^-p(\uparrow\downarrow) \ ^1S_0$
 and accelerated by $\sim 0.12 \text{ eV} \sim \frac{2}{3} \Delta E_{1S}^{\text{HFS}}$

Energy-dependent muon transfer rate

\Rightarrow change the time distribution of the
 cascade X-ray events from μ^-Z^*

\Rightarrow resonance λ_0 is recognized by

\Rightarrow the maximal response in this time
 distribution



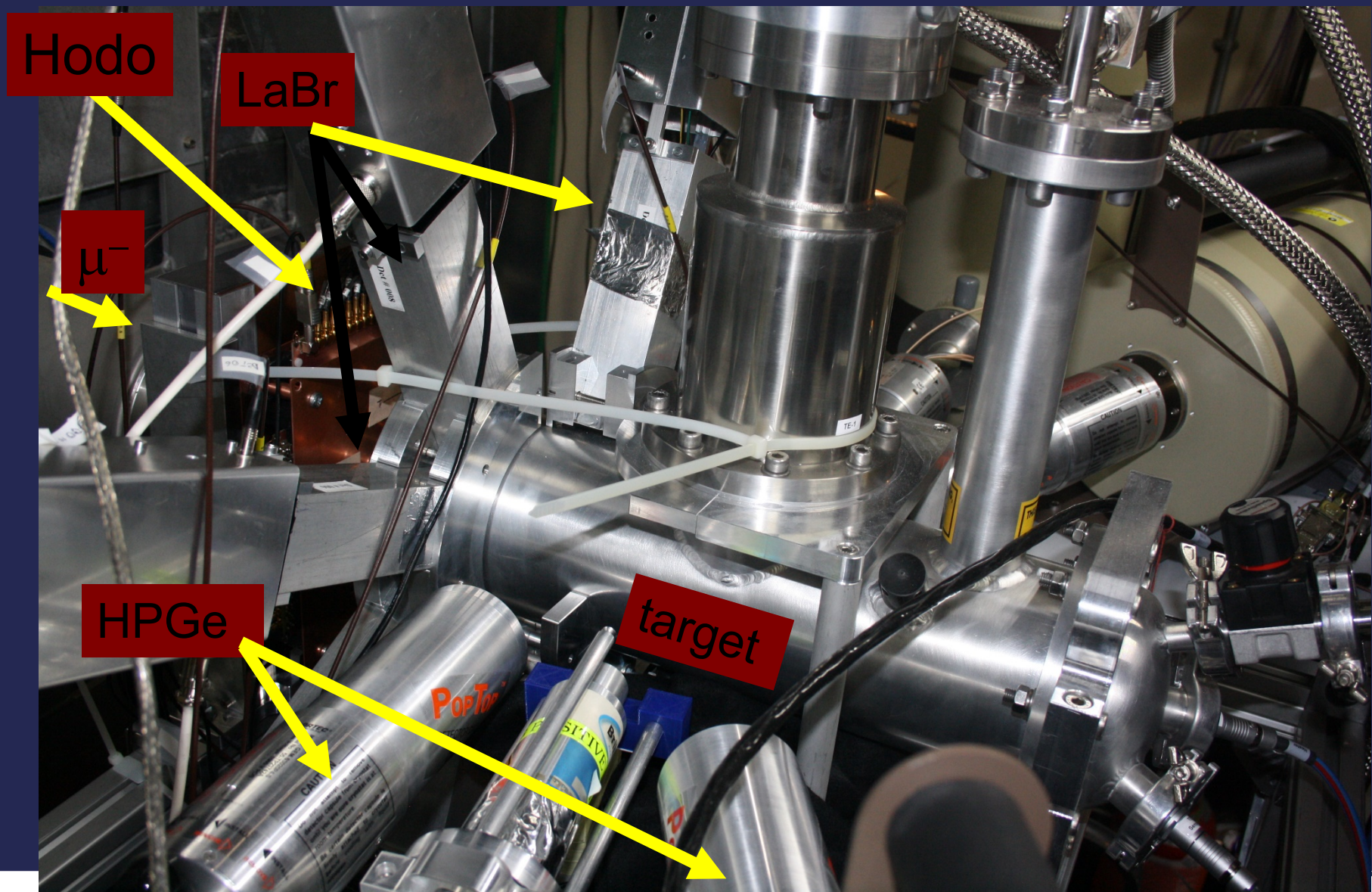
FAMU's activity summary

- 2014 characterisation of beam and detector's noise first measurements of transfer rate at room temperature
- 2015-6
cryogenic target first measurement of transfer rate between 100 and 300 K
laser parts procurement initiated
- 2017-18
laser parts delivery completed assembly and characterization on-going based on the results of the transfer rate measurements at different temperatures optimization studies are on going
 - optimal optic cavity design
 - new cryogenic gas target design study and simulation
 - muon beam optimization

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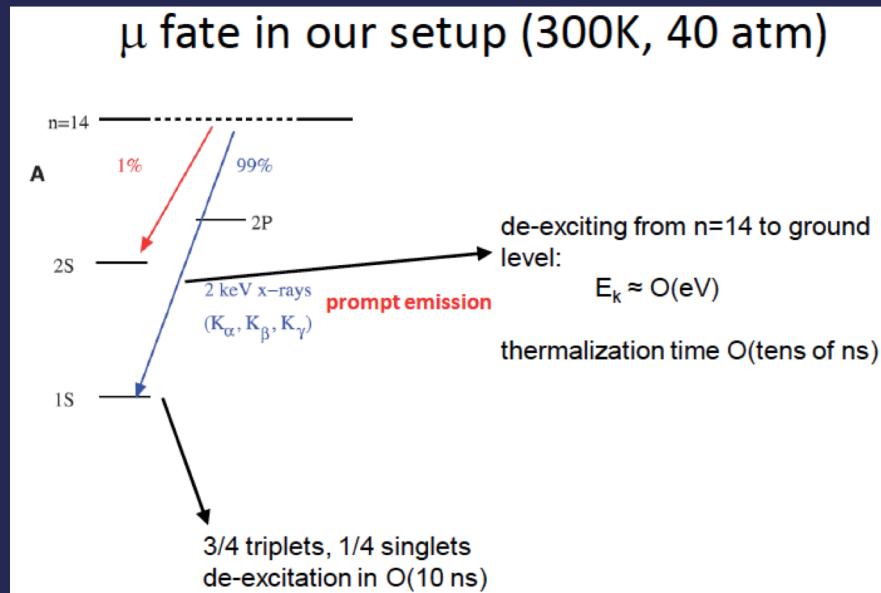
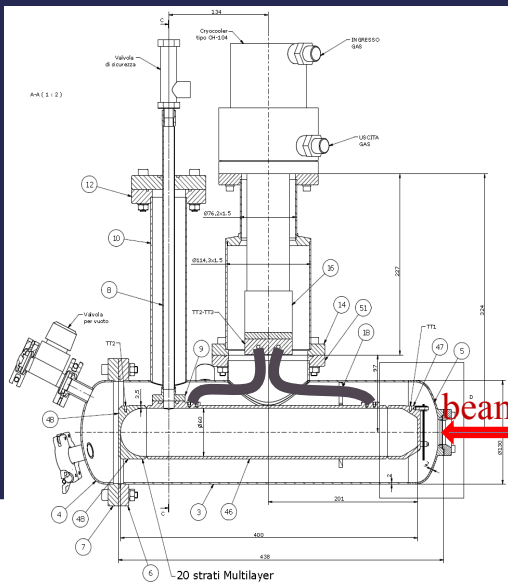
2016: experimental setup



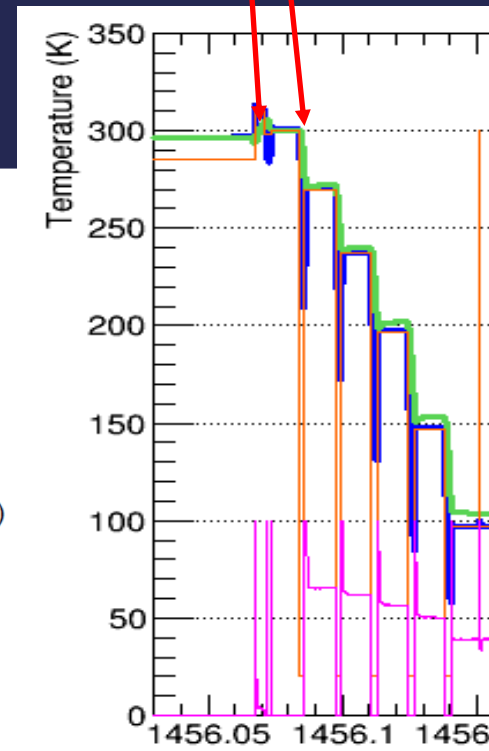
2016: *Energy-dependent muon transfer rate measurement*

Steps:

- 1) **fix a target temperature** (i.e. mean kinetic energy of gas constant)
- 2) produce μ and wait for thermalization
- 3) **study time evolution of Oxygen X-rays**
- 4) repeat with different temperature



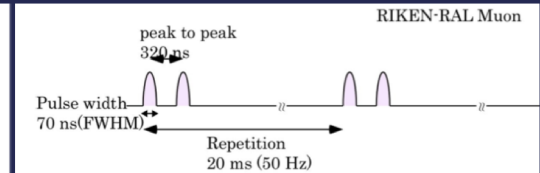
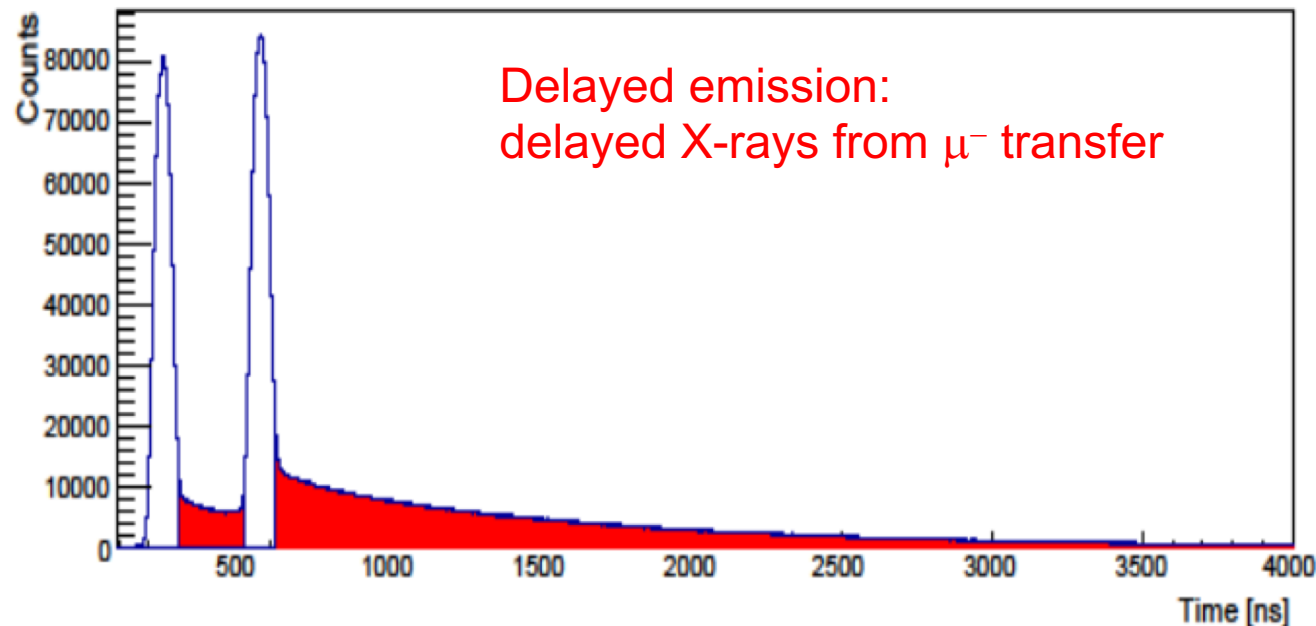
three hours

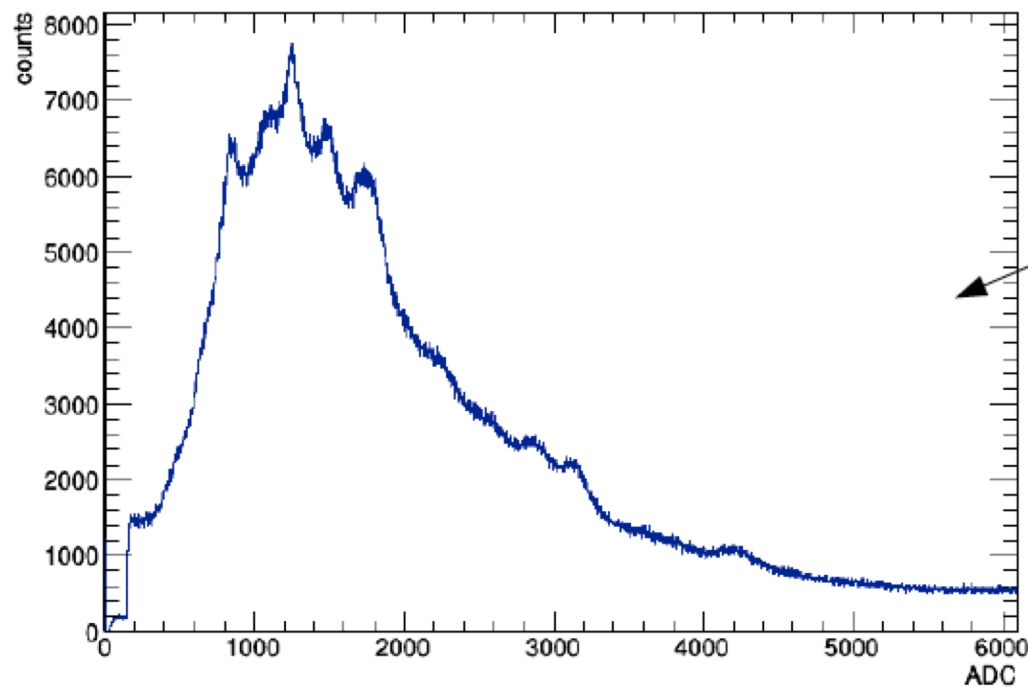


2016: transfer rate measurement

Steps:

- 1) fix a target temperature (i.e. mean kinetic energy of gas constant)
- 2) produce μp and wait for thermalization
- 3) study time evolution of Oxygen X-rays
- 4) repeat with different temperature



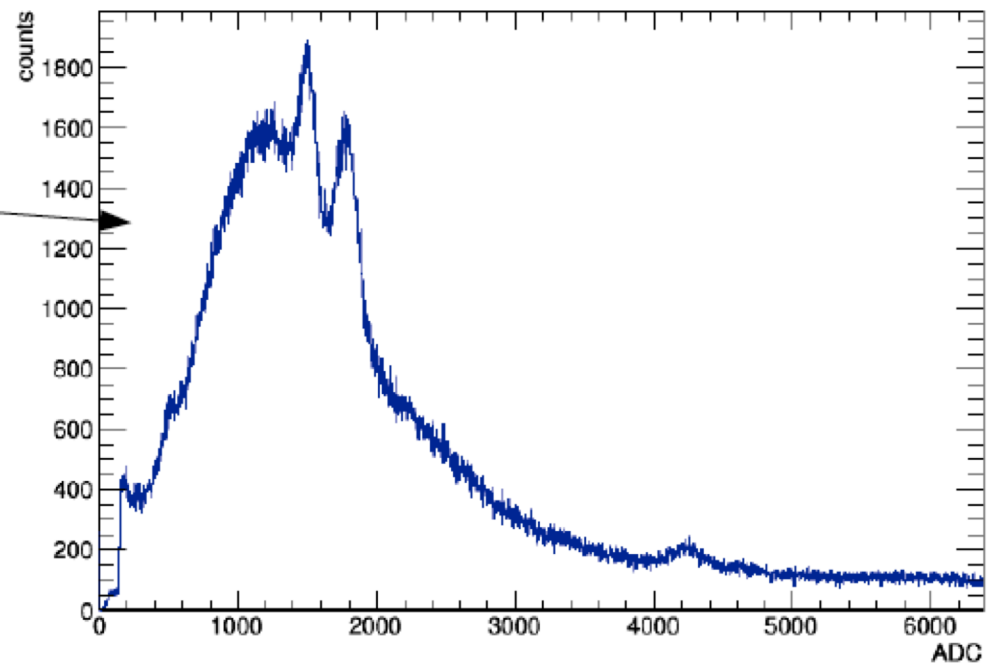


PROMPT SPECTRUM
($t < 1200$ ns)

One detector (LaBr 3)
0.3% oxygen
concentration

DELAYED SPECTRUM
($t > 1200$ ns)

One detector (LaBr 3)
0.3% oxygen
concentration

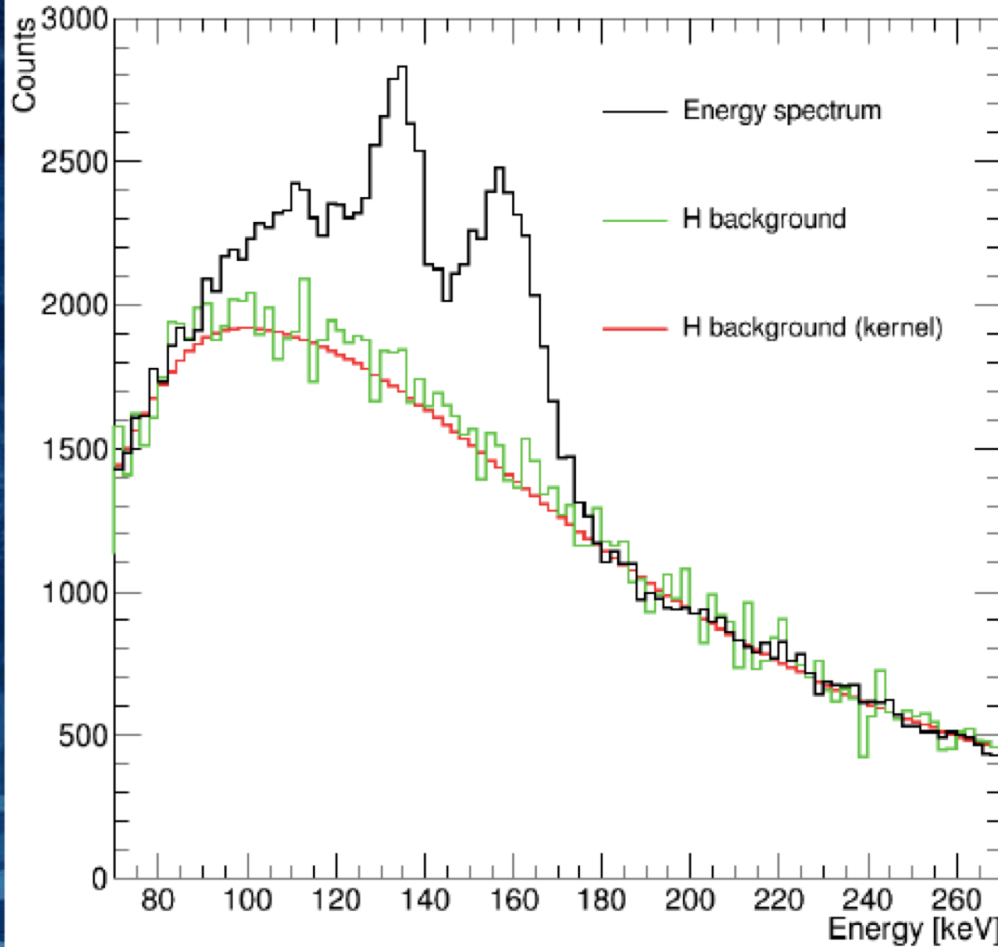


Best solution: pure H smoothing

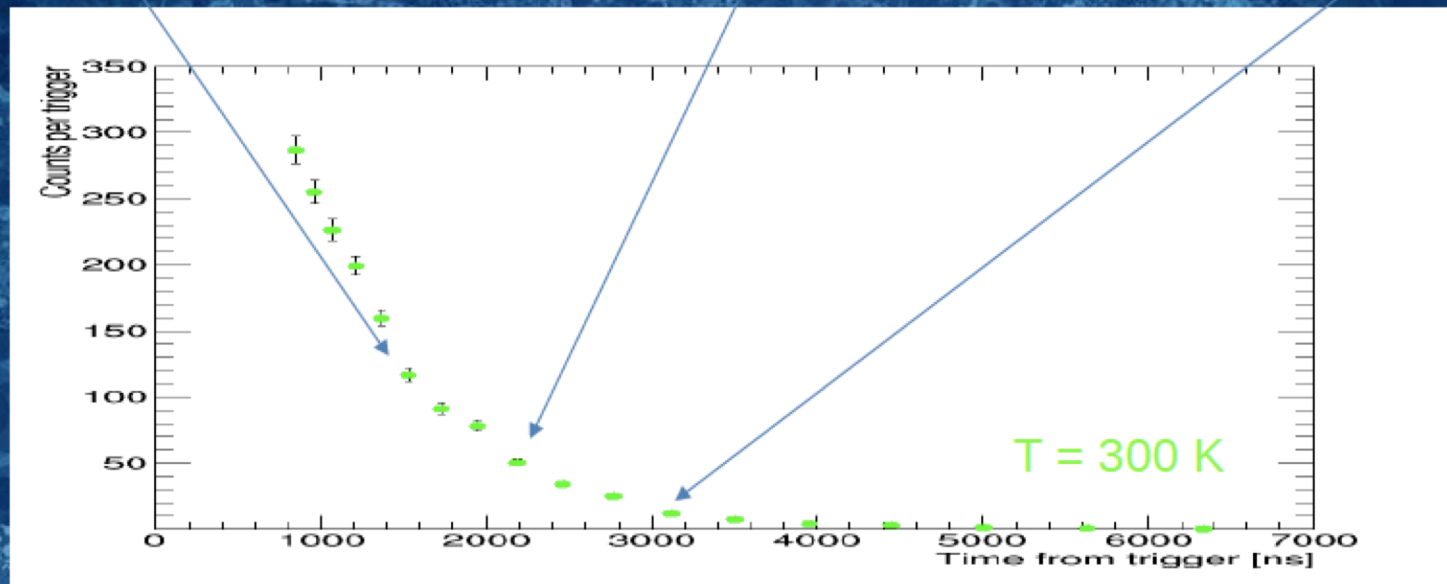
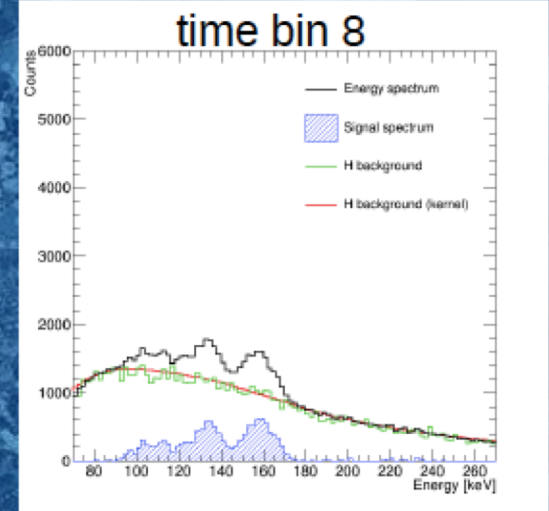
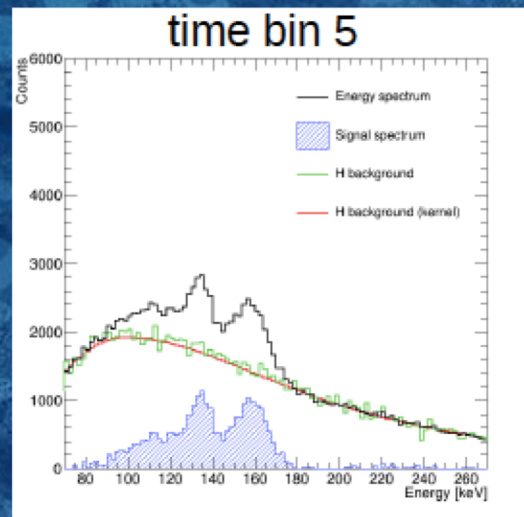
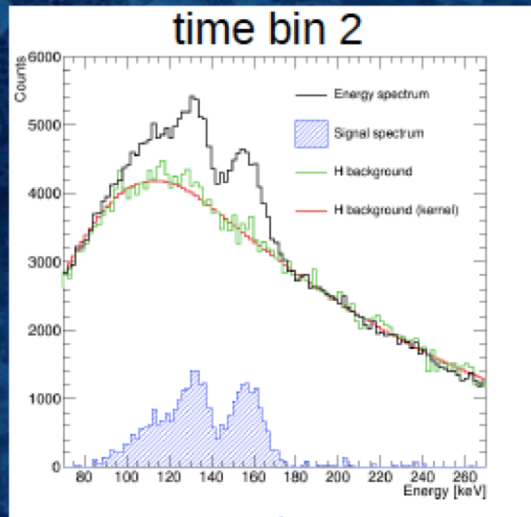
$T = 300 \text{ K}$

Time bin = [1450,1650] ns

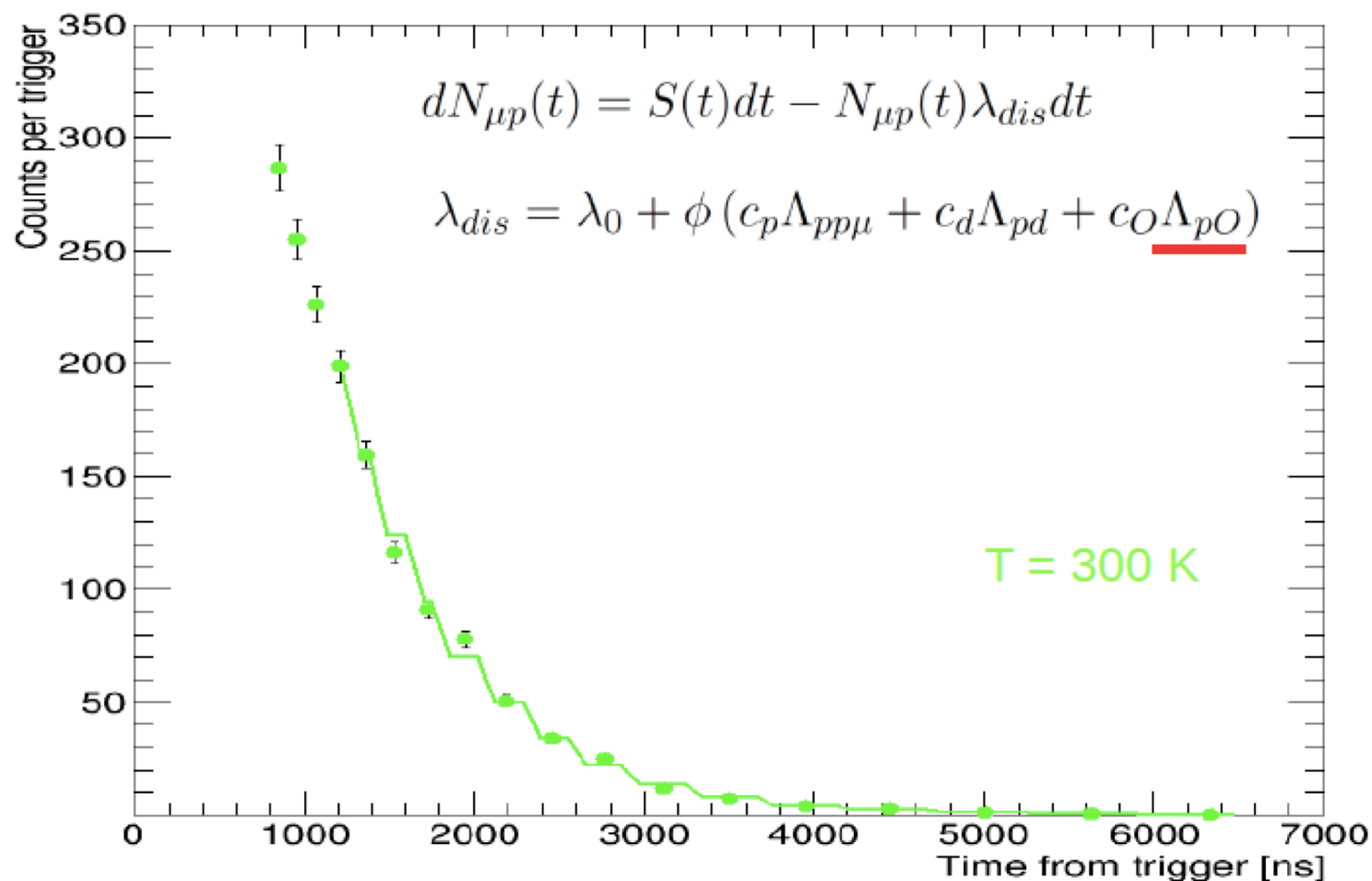
Pure hydrogen data taking within the same beam time and with the same pressure and temperatures.

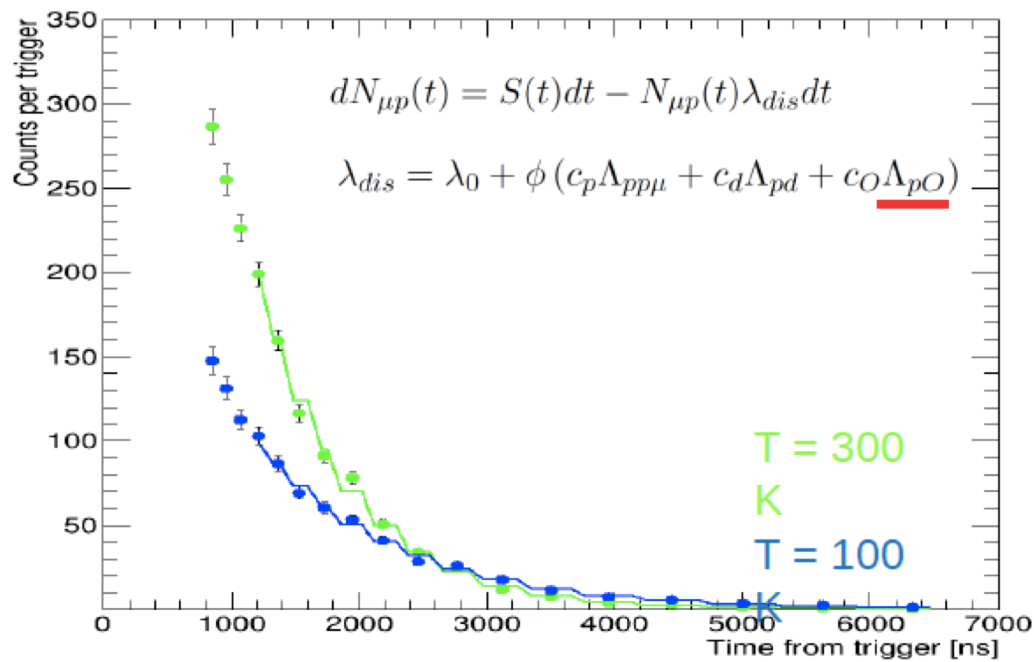


Fixed temperature: time evolution

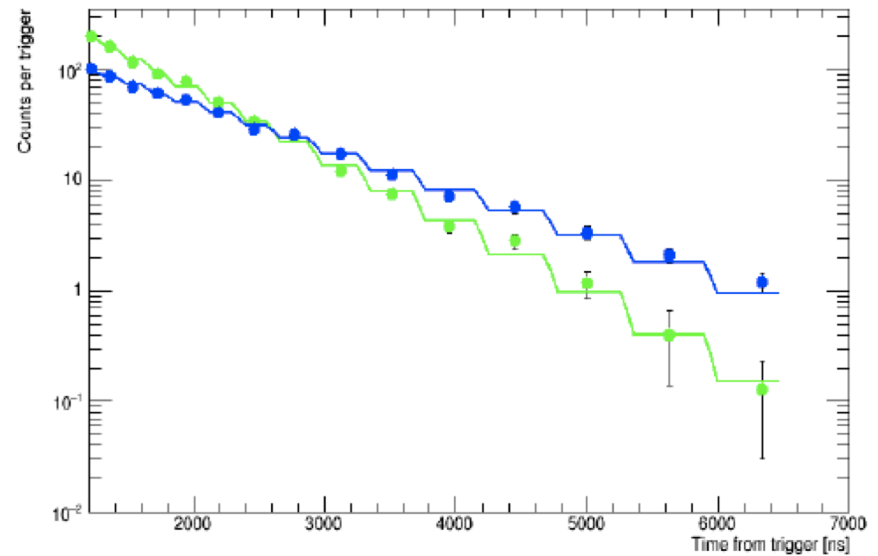


Temperature and time evolution



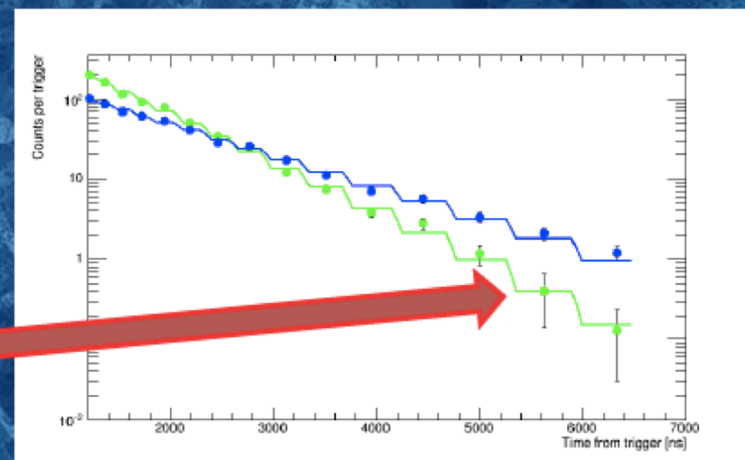
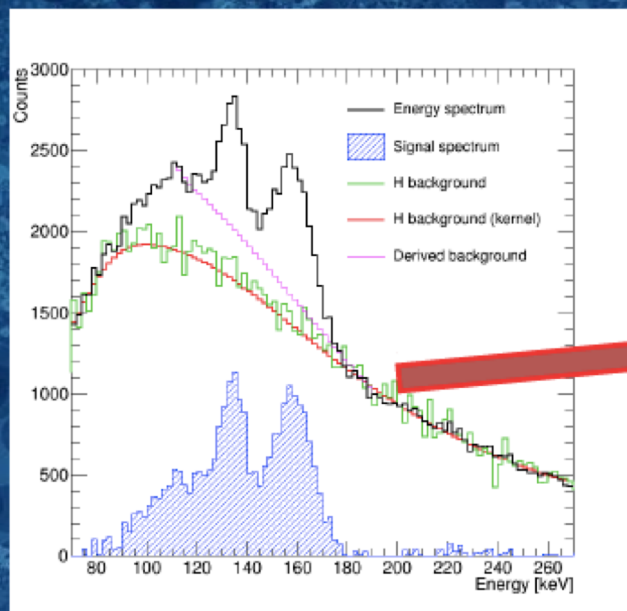


Transfer rate dependence
on temperature



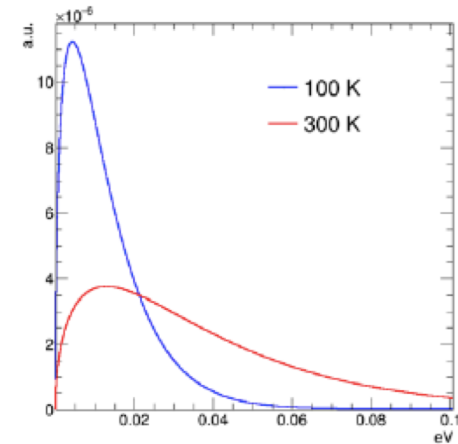
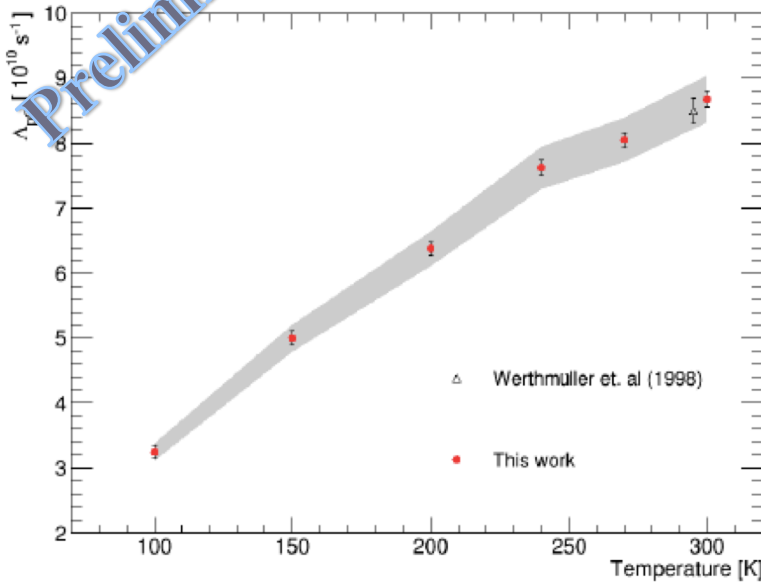
Sistematic errors contributions

- 3% given by the O concentration calculation
- 3% given by the density calculation
- About 5% due to the procedure of the background subtraction

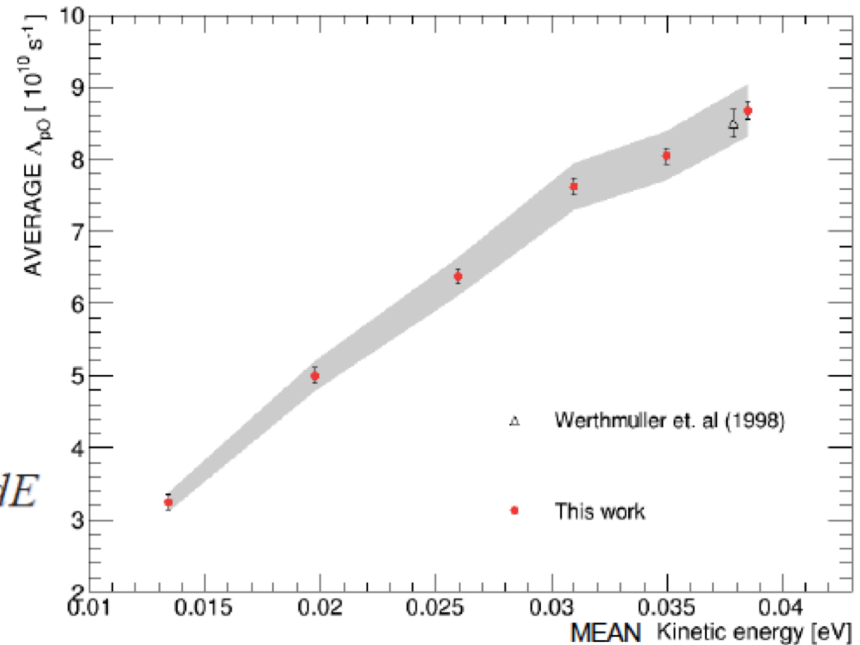


Other uncertainties, negligible (\ll statistical error)

Conversion to kinetic energy



$$\lambda(T) = \int_0^\infty \lambda(E) \sqrt{\frac{4E}{\pi(kT)^3}} \exp(-E/kT) dE$$

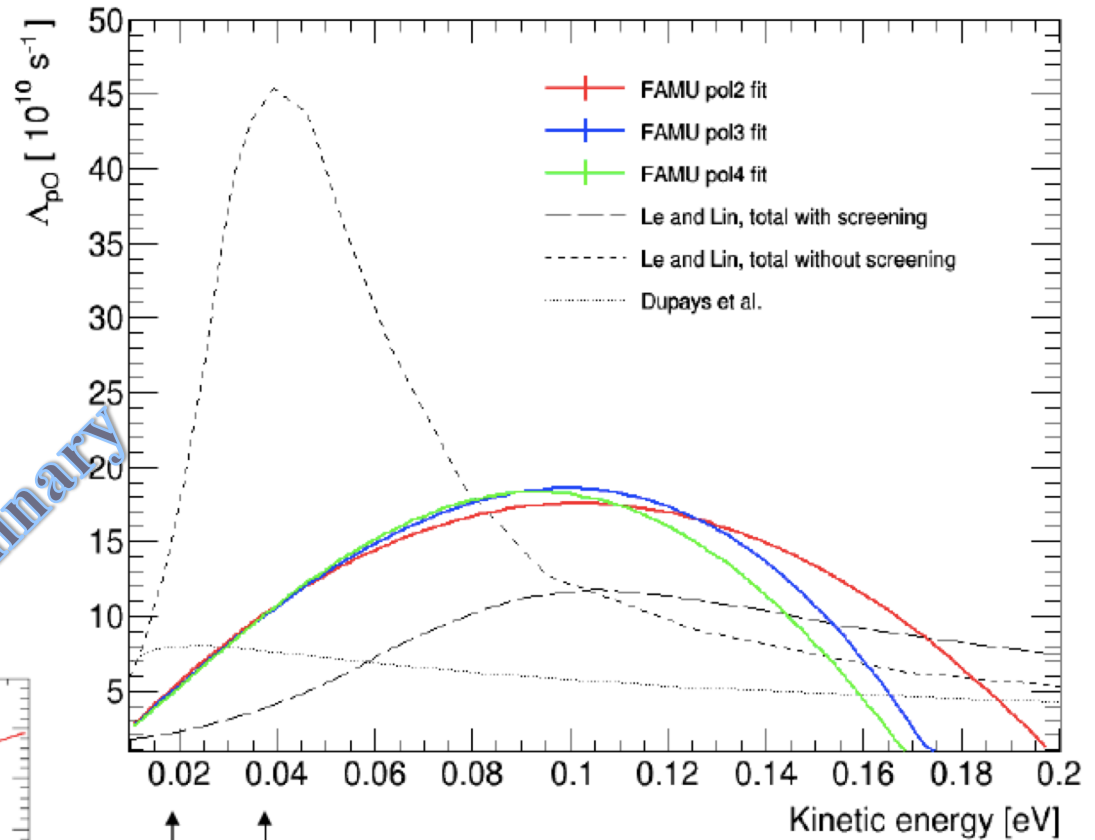
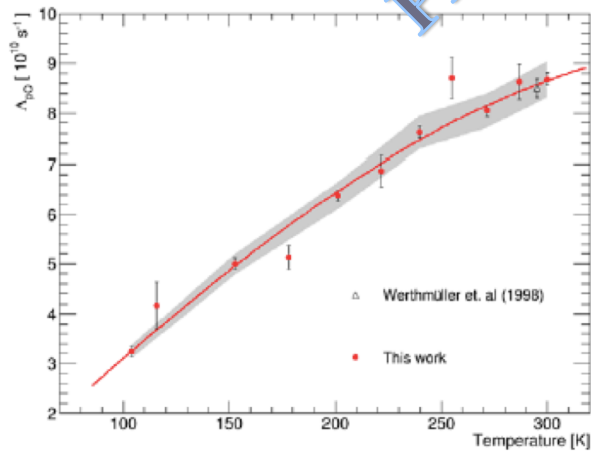


Phenomenological model

$$\lambda(T) = \int_0^\infty \lambda(E) \sqrt{\frac{4E}{\pi(kT)^3}} \exp(-E/kT) dE$$



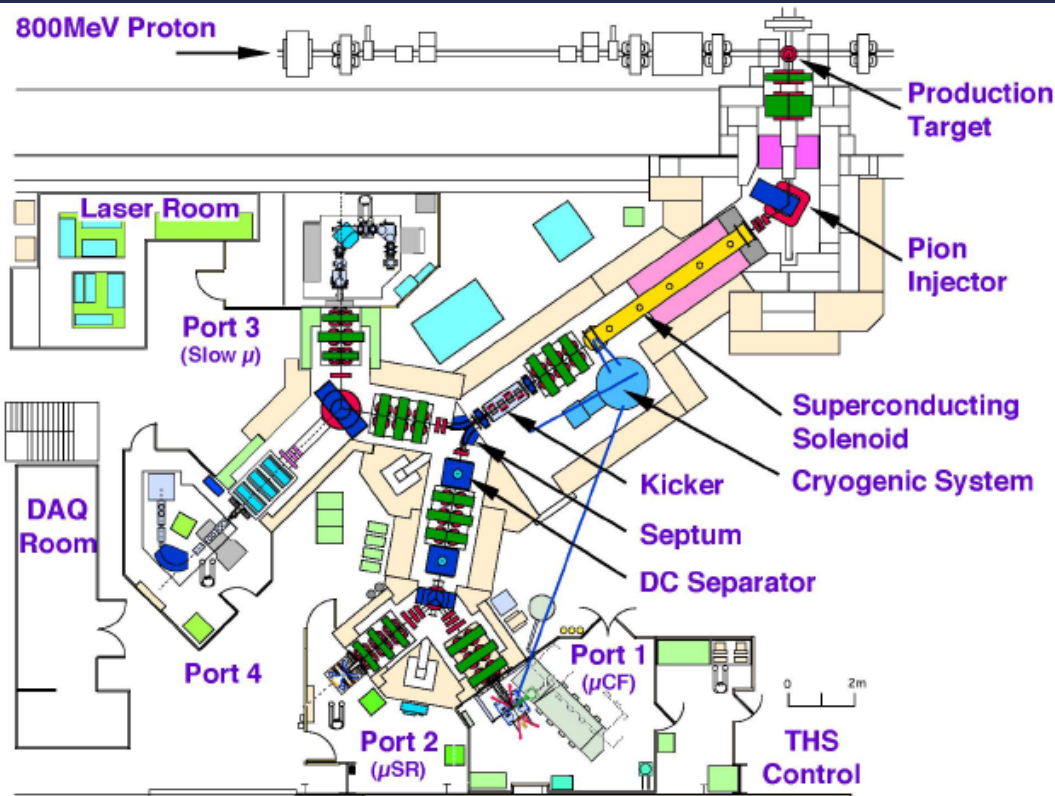
Preliminary



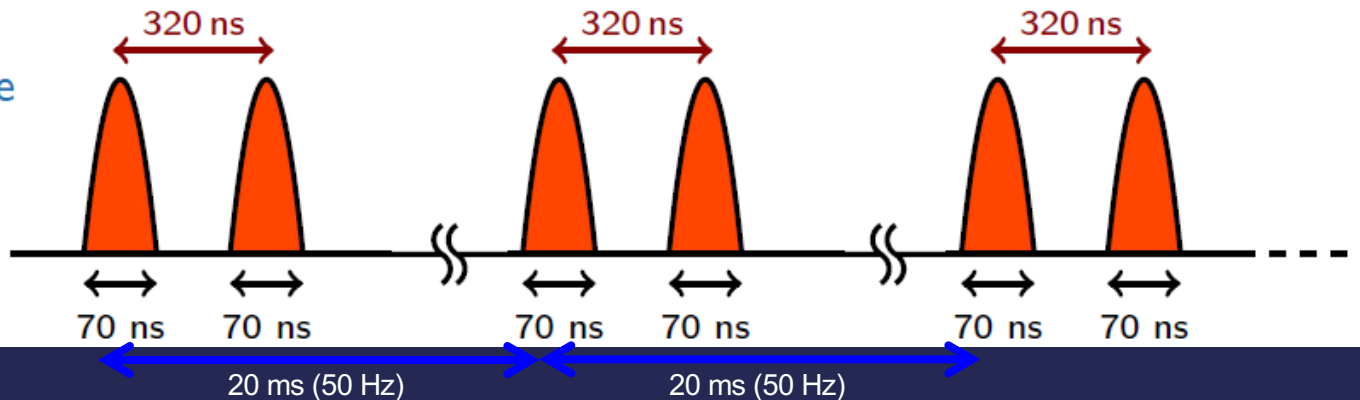
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High intensity muon beam



Beam time structure



FAMU Key elements

Muon Beam at RIKEN-RAL

Beam properties

surface μ^+ (20~30 MeV/c) and
decay μ^+ / μ^- (20~120 MeV/c)

typical beam size 10 cm²

$\bar{x}\Delta p/p$ FWHM 10%(decay), 5%(surface)

Double pulse structure

(Choice of single pulse

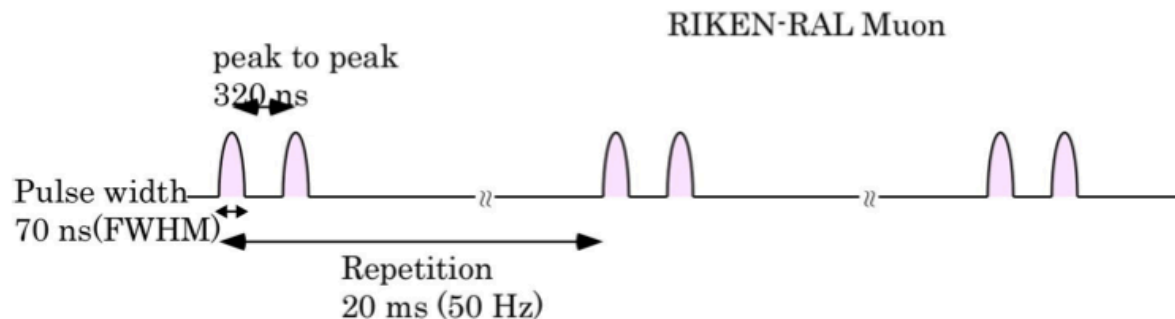
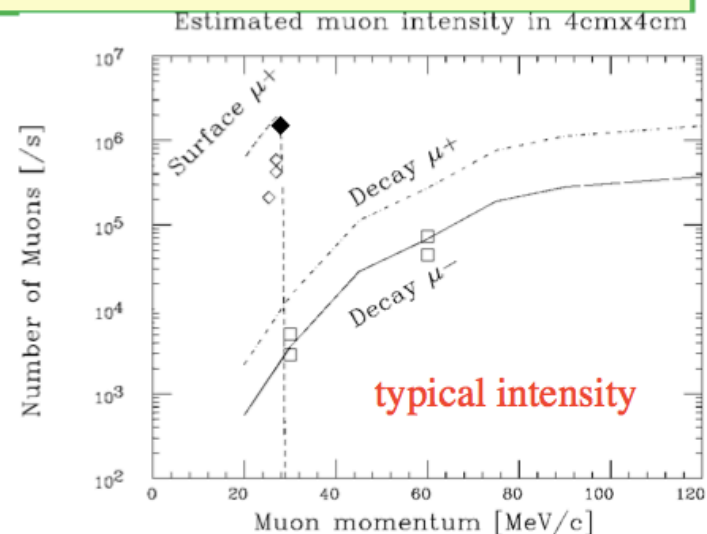
with magnetic kicker (<30 MeV/c))

Operation

160 days/y of ISIS beam time

~40 days for UK

~120 days for RIKEN



Muon beam density enhancement

- Muon beam density enhancement was observed in a number of experiments carried out both at RIKEN-RAL (UK) and at TRIUMF (Canada) laboratories .
- They used several tapered tubes working with muon grazing angle: glass tubes, copper, gold plated copper.

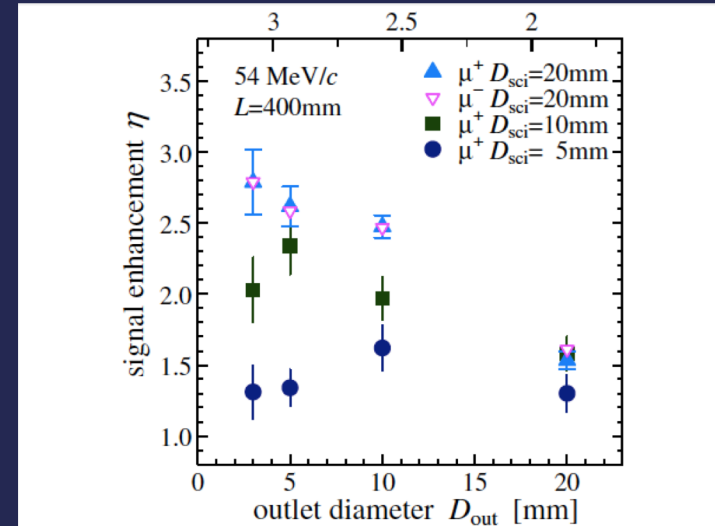


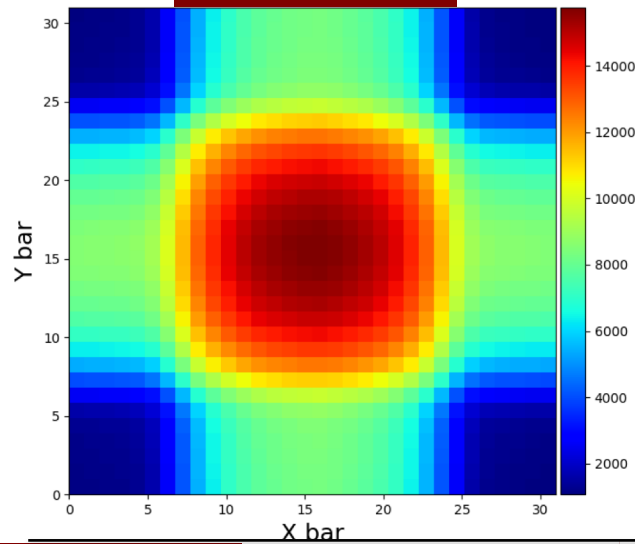
Fig. 2. (Color online) The signal enhancement factor η as a function of outlet diameter D_{out} for 54 MeV/c muons with $L = 400$ mm tubes for $D_{sci} = 5, 10$, and 20 mm. The error bar includes statistical and systematic errors (see text). Data points with “T” shape error bar are the mean of multiple measurements and those with “|” shape error bar are measured only once. Error bars of μ^- data are omitted for clarity.

$$\eta = \begin{cases} V_{with}/V_{without} & \text{for } D_{sci} \leq D_{out}, \\ V_{with}/V_{without, d \leq D_{out}} & \text{for } D_{sci} > D_{out}, \end{cases} \quad (1a)$$

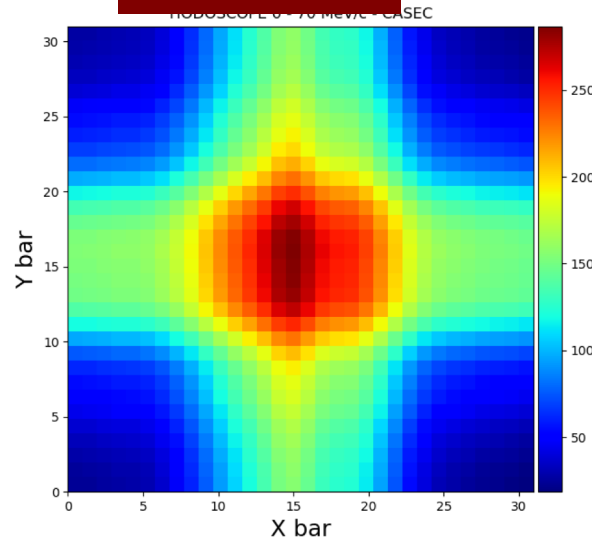
$$(1b)$$

We decided to investigate the possibility to have density enhancement. Several experimental configurations were realized, made of polished copper and of gold plated glass. The analysis is on-going

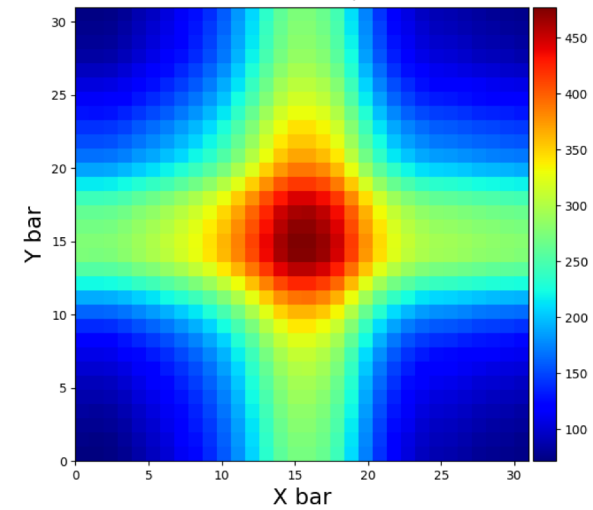
Simulated ODO2



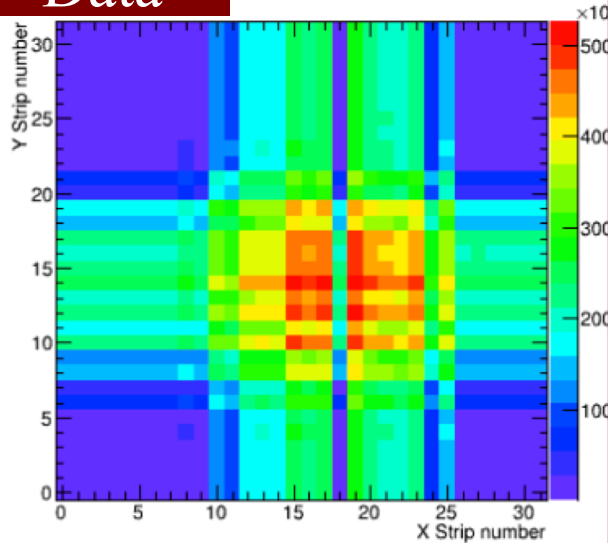
ODO0



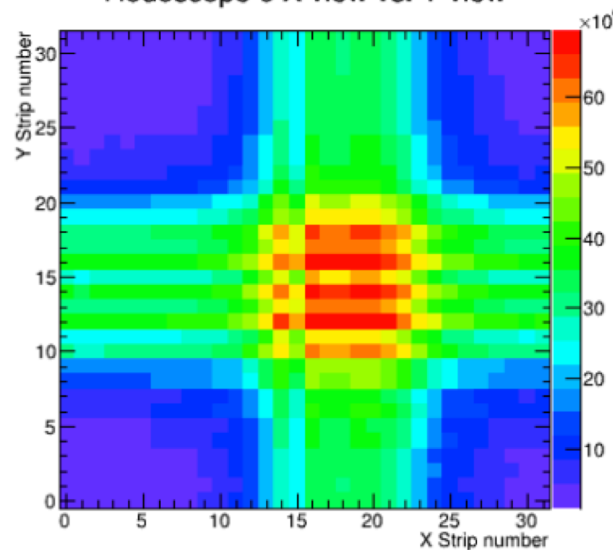
ODO1



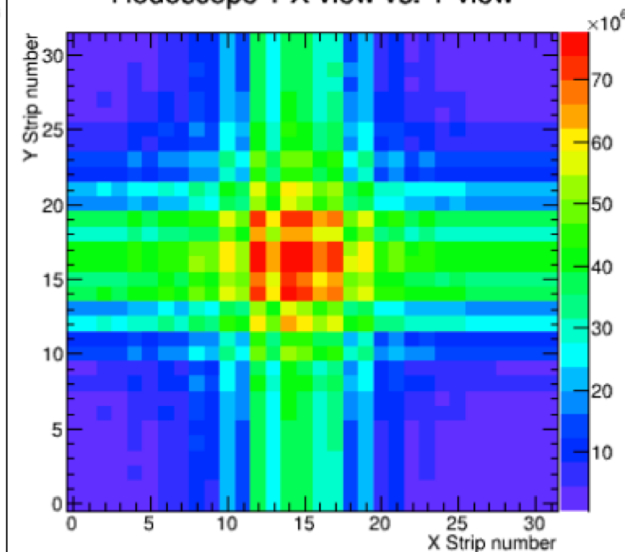
Data Case 2 X view vs. Y view



Hodoscope 0 X view vs. Y view



Hodoscope 1 X view vs. Y view



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FAMU key elements high energy MIR laser

Tunable pulsed MIR laser at $\lambda=6.8\mu$

Direct difference frequency generation
in non-oxide non linear crystals using
single-mode Nd:YAG laser and tunable Cr:forsterite laser

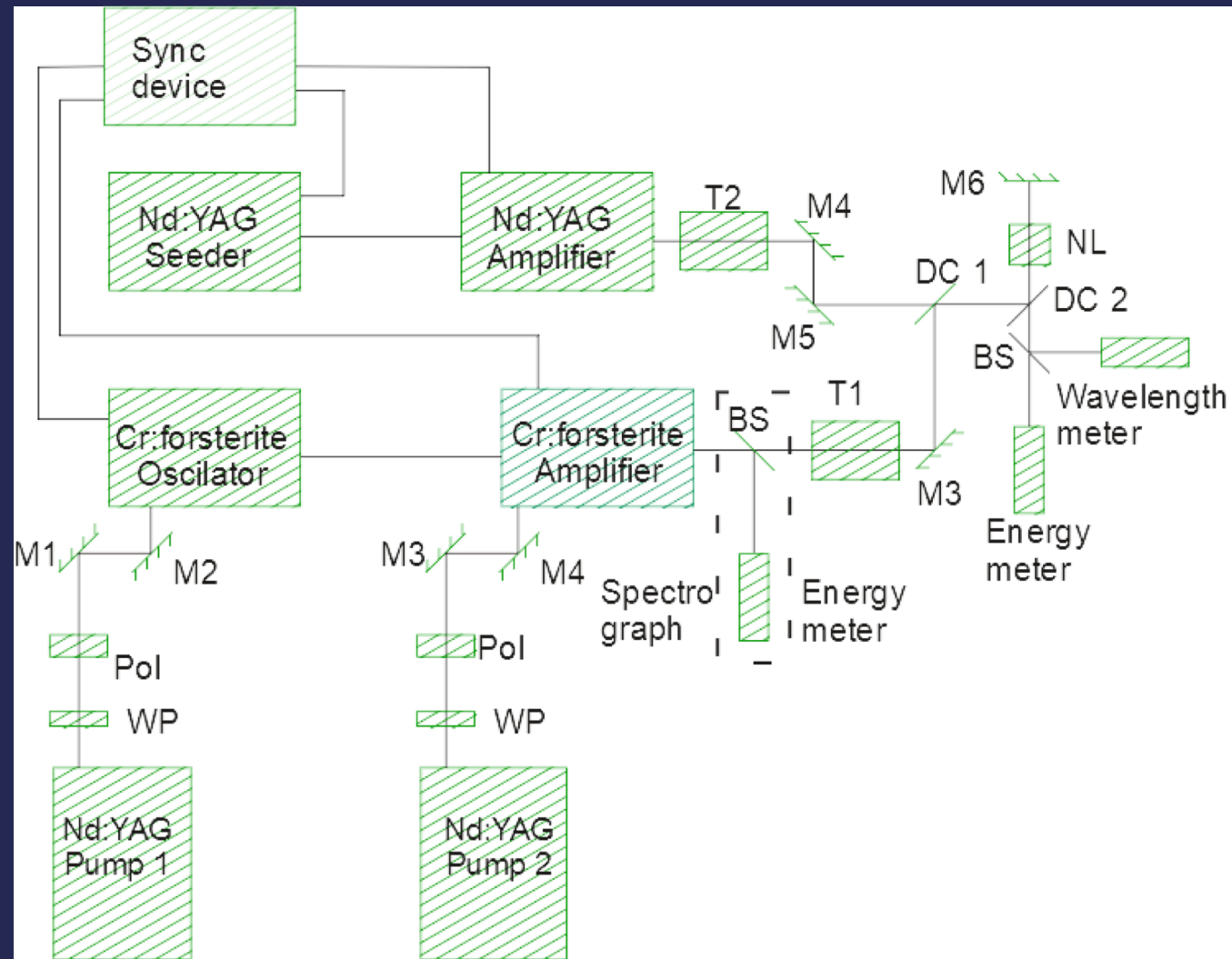
Wavelength:	$\lambda = 6785 \text{ nm}$	44.22 THz
Line width:	$\Delta\lambda = 0.07 \text{ nm}$	450 MHz \Rightarrow 100 MHz
Tunability range:	6785 \pm 10 nm	130 GHz
Tunability step	0.007 nm	45 MHz
Repetition rate:	25 Hz	
Pulse Energy at 6780 nm:	5 mJ	

Final scheme of the DFG based laser system

The Nd:YAG will be at "fixed" wavelength 1064.14nm with linewidth max - 0.34pm (90MHz) and min - 0.11pm (30MHz).

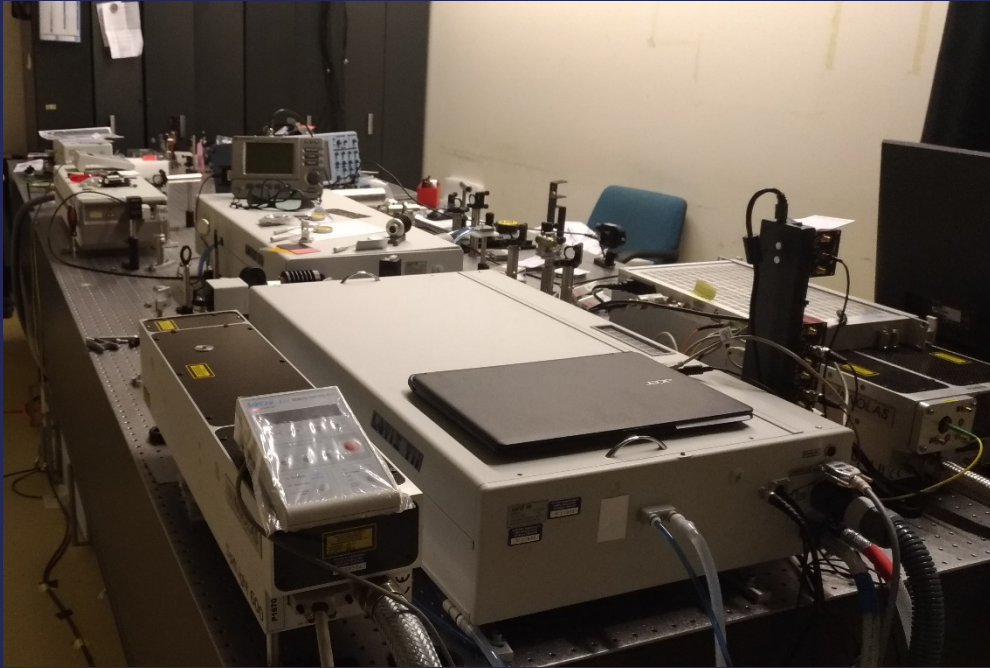
The Cr:forsterite will have linewidth max - 1pm (188MHz) and min - 0.5pm (90MHz).

The Cr:forsterite will be tunable from 1252nm to 1272 nm which corresponds to tunability from 6500nm to 7090nm, which is 3765GHz. The required tunability $6760\text{nm} \pm 3\text{nm}$ corresponds to tunability range $\sim 39\text{GHz}$.

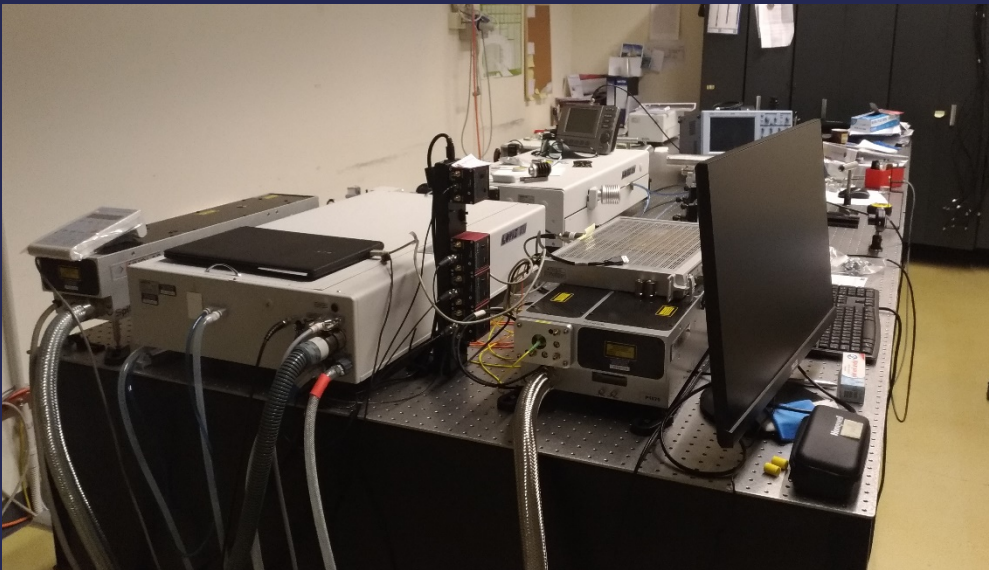


WP - waveplate, Po - polarizer, M1-M5 - mirrors, T1 and T2 - telescopes, BS - beamsplitters, DC1 - dichroic mirror (reflecting 1.26μm, transmitting 1.06μm), DC2 - dichroic mirror (reflecting 1.06 and 1.26 μm, transmitting 6.76μm)

The laser lab



- Available - All lasers
- Available - Most optics and electronics
- Available - Most test and measurement equipment



Laser parameters	Baseline laser source	FAMU laser system
Wavelength λ	6785 nm	6785 nm
Linewidth $\Delta\lambda$	450 MHz	250 MHz
Pump Laser Beam shape	gaussian	flat top
LiInS ₂ crystals	7 x 7 x 20	2 x (10 x 10 x 20)
Nonlinear crystals efficiencies	LiInS ₂ $d_{\text{eff}} = 7,38$ pm/V	LiInSe ₂ $d_{\text{eff}} = 19,5$ pm/V
Cr-Forsterite tot energy	15 mJ	35 mJ
NdYag tot. energy	150 mJ	150 mJ
Available Energy@6785nm	1 mJ	>5 mJ

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2016 Target: a necessary trade-off

Main requirements:

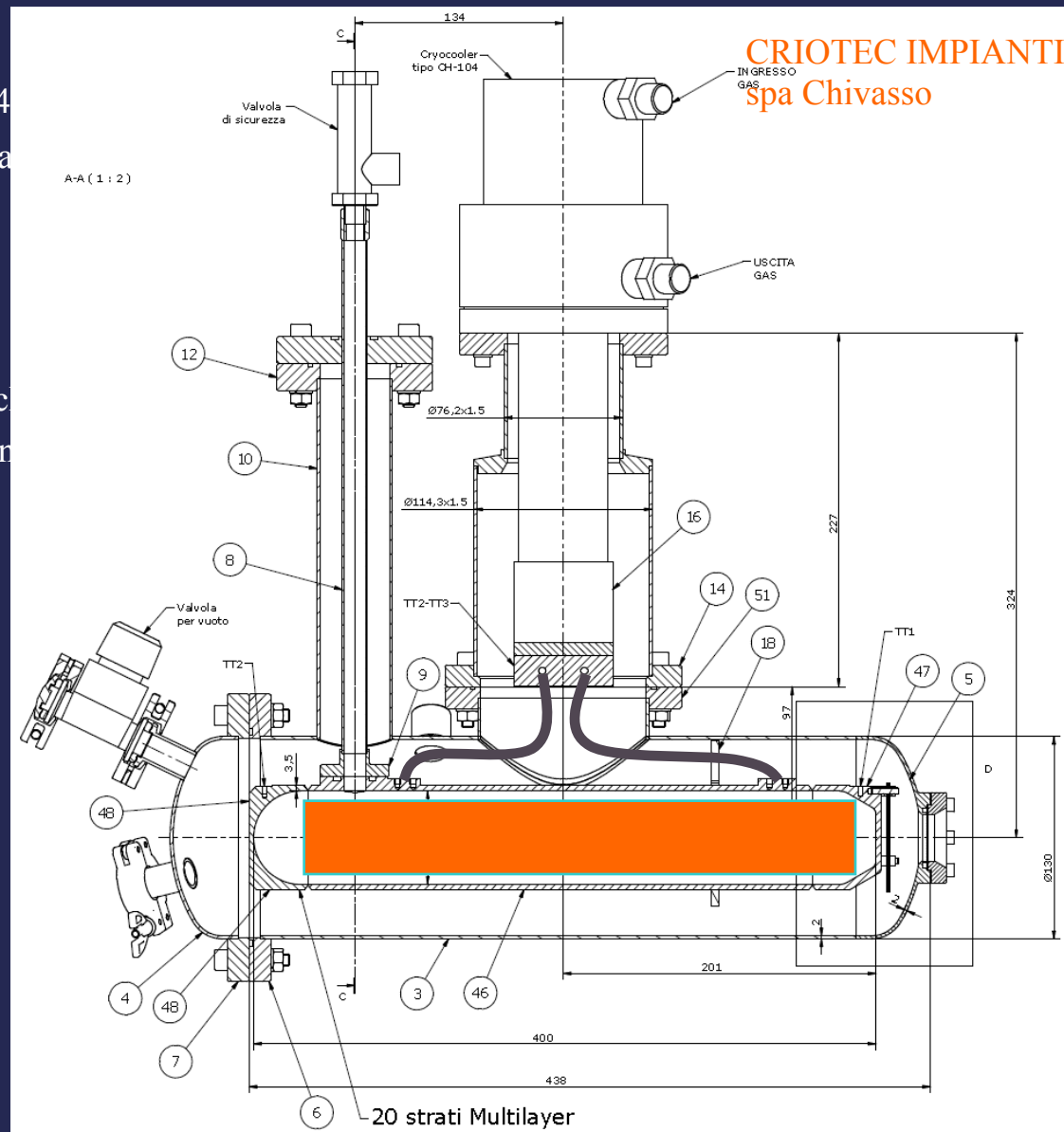
- Operating temperature range: $40\text{ K} \leq T \leq 325\text{ K}$
- Temperature control for measurement runs at fixed T steps from 300 K to 50K
- Gas @ constant density, H_2 charge pressure at room T is $\sim 40\text{ atm}$
- International **safety** certification (Directive 97/23/CE PED)
- Minimize **walls and windows thickness**
- Target shape and dimensions to :
 - **maximize muon stop in gas**
 - **to minimize distance gas – detectors**
 - **to be compliant to allowable volume at Riken Port**

... and, of course, all the above within time and cost constraints!

2016 Best solution

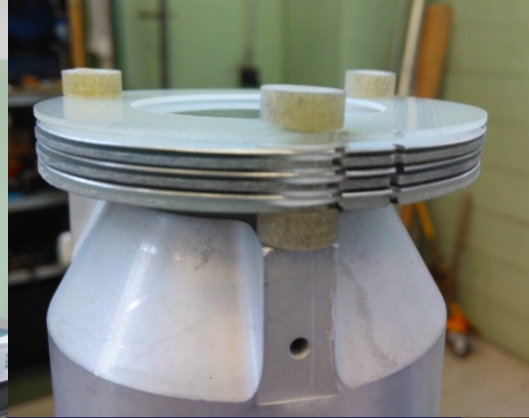
- Target= Inner vessel with high P gas (44 bar)
- Al alloy 6082 T6 cylinder D = 60 mm and L = 400 mm, inner volume of 1.08 l
- Internally Ni/Au plated (L = 280 mm)
- Cylinder side wall thickness = 3.5 mm
- Wrapped in 20 layers of MLI
- Front window D= 30 mm 2.85 mm thick
- Three discs of 0.075 mm Al foil for window radiative shield
- 304L SS gas charging tube
- 304L SS cooler cold-end support
- G10 mechanical strut
- Two Cu straps for cooling

- Vacuum vessel = outer cylinder (P atm)
- Al6060 D=130 mm, 2 mm thick walls
- ≈ 30 mm between inner/outer walls
- Flanged Al window 0.8 mm thick
- Pumping valve & harness feed-throughs



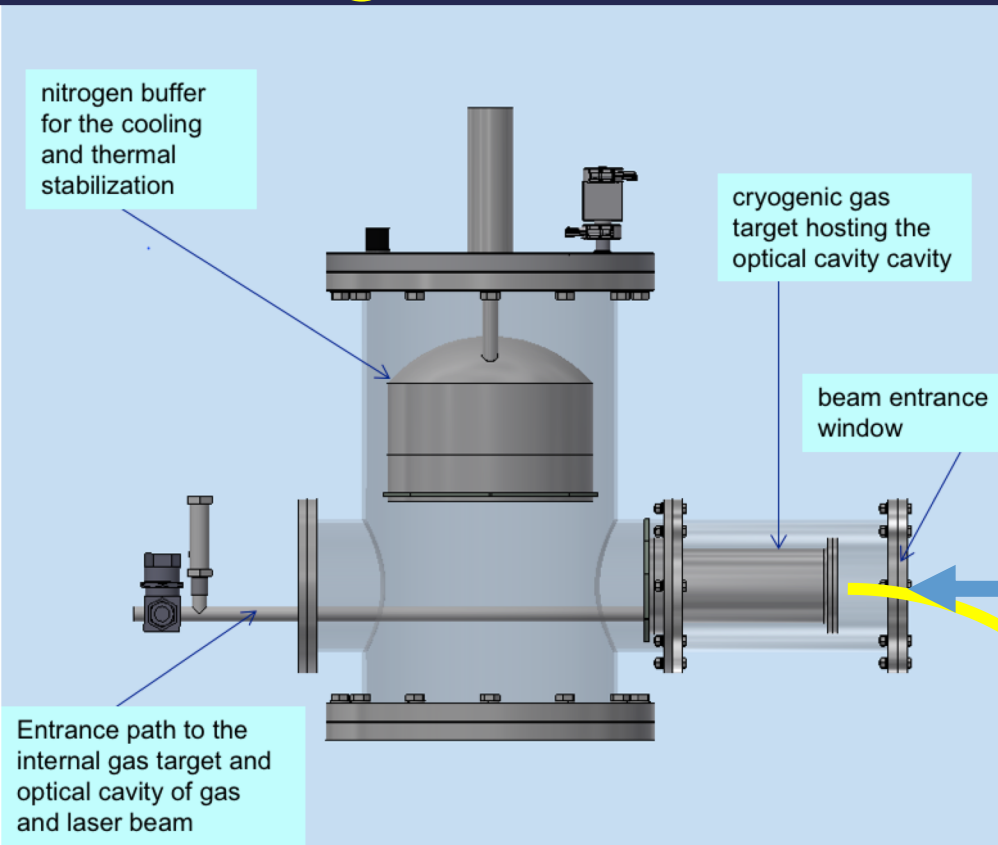
beam

Target in lab

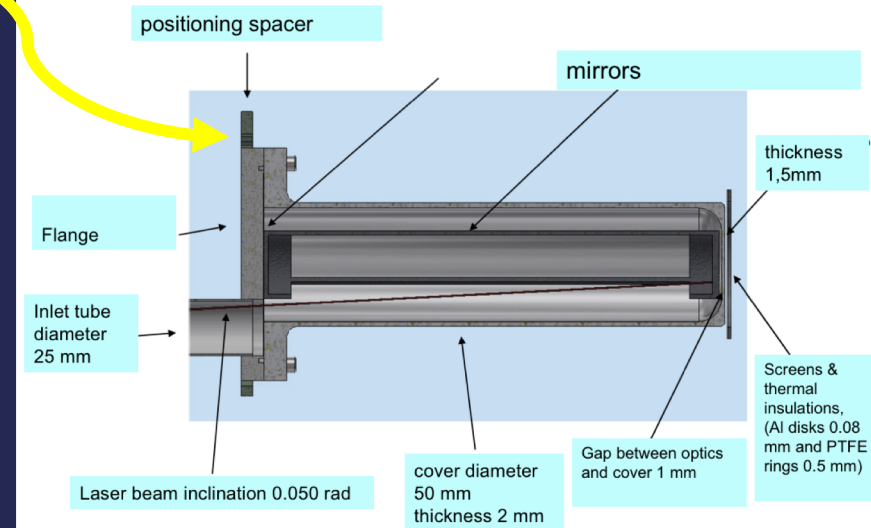


2018 target solution under study

Cryogenic gas target and optical cavity



beam



OUTLINE

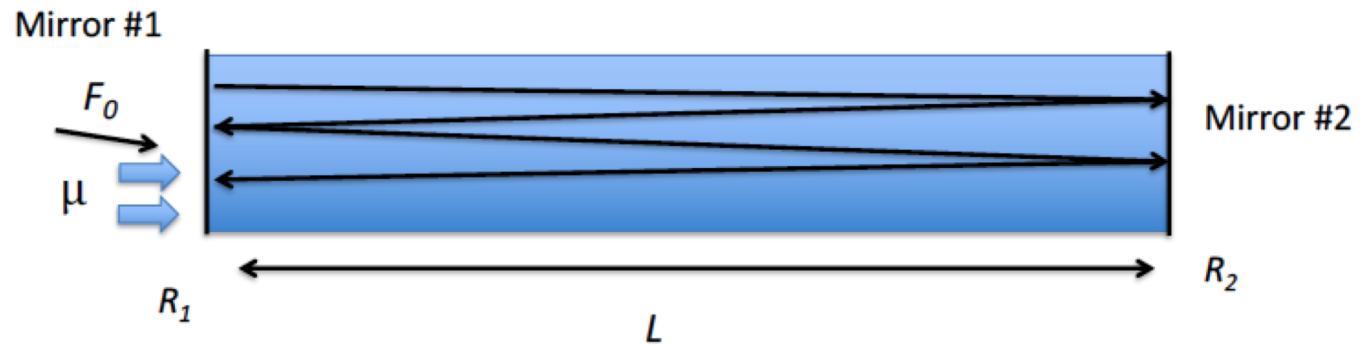
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Multipass Optical Cavity

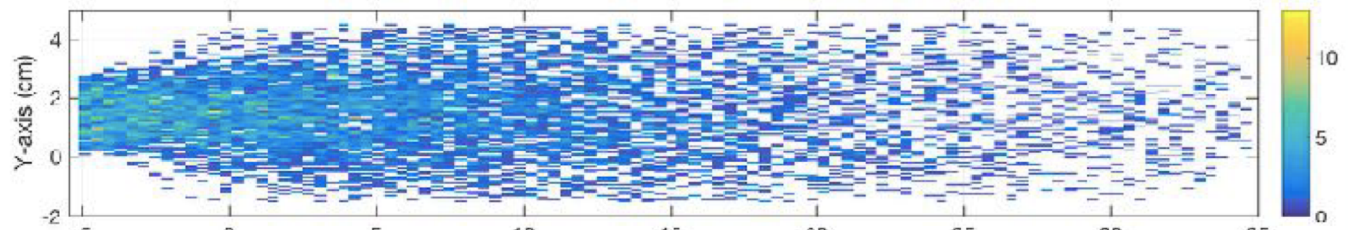
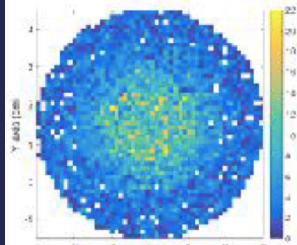
Luigi Moretti, Livio Gianfrani

9497 events

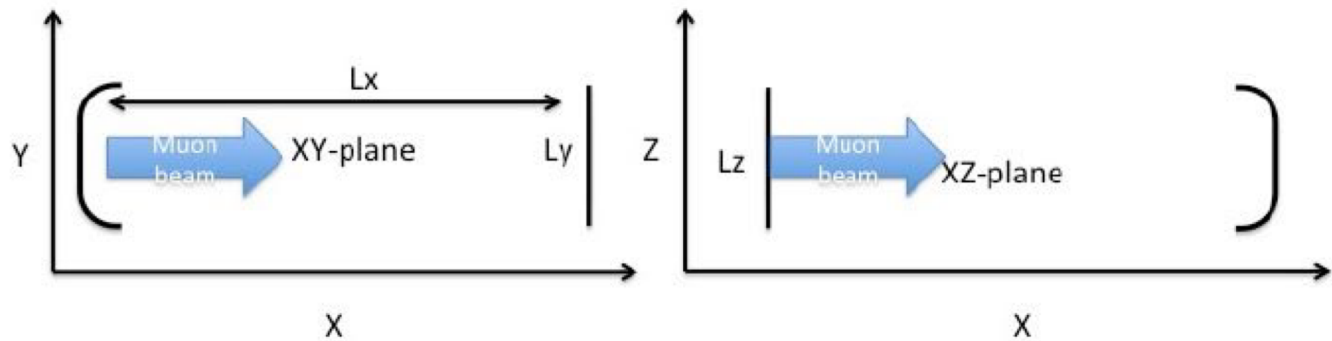
$$V_{\text{est}} = \pi (2 \text{ cm})^2 (15 \text{ cm}) = 94 \text{ cm}^3$$



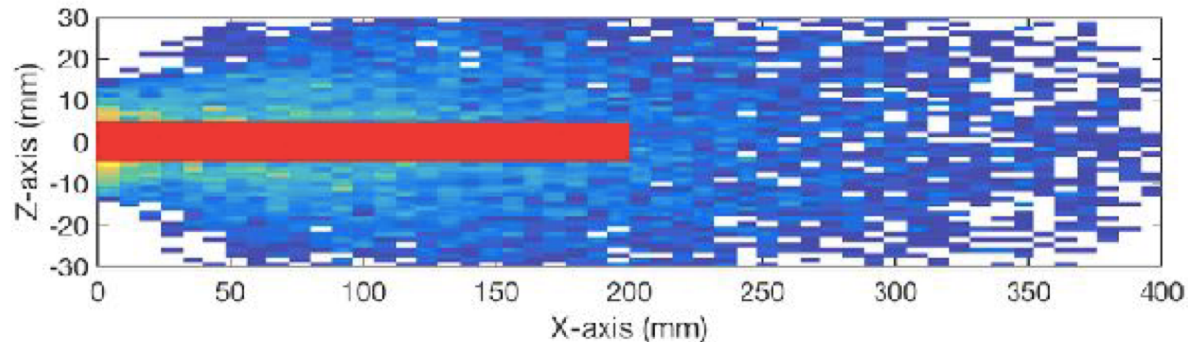
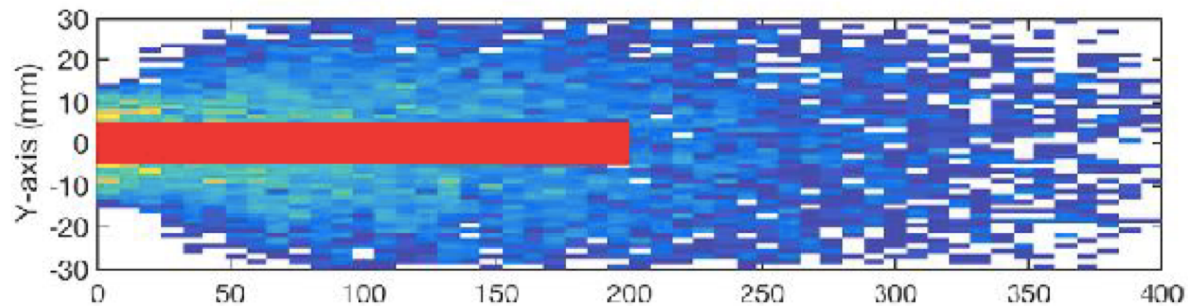
$$L_{\text{eff}} = \frac{L}{\alpha} = \frac{20 \text{ cm}}{12 \times 10^{-4}} \simeq 166 \text{ m}$$



Optical design of cavity



$$L_y = L_z = 2.5 \text{ cm}$$
$$L_x = 20 \text{ cm}$$



Cavity enhancement effect at glance

$$E_l = 2.5 \text{ mJ}$$

$$N_R = 700$$

$$R_1 = R_2 = 0.9989$$

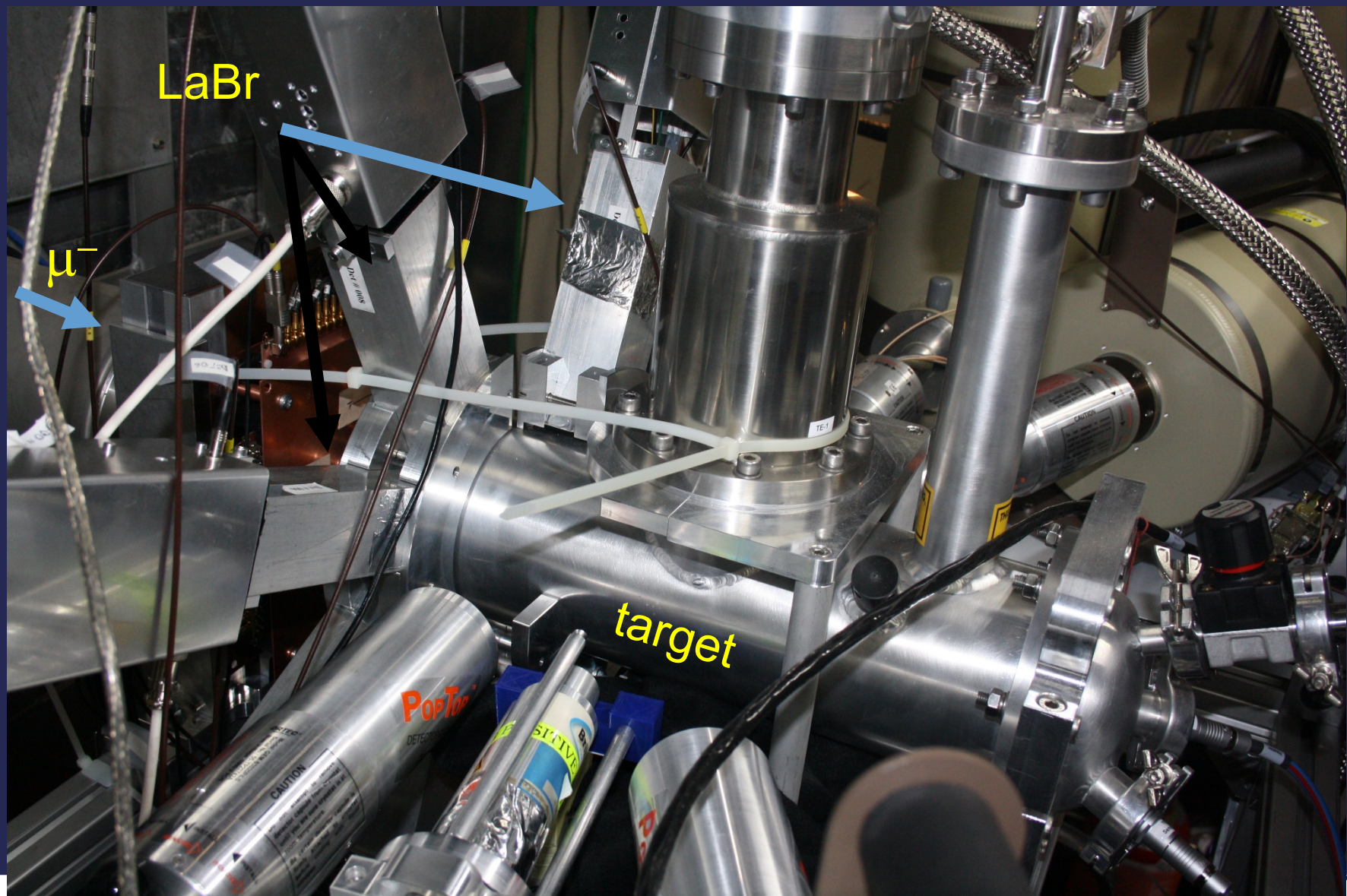
$$\text{New design} \quad S_{ill} \simeq (2 \cdot 2) \text{ cm}^2 \quad (\alpha = 12 \times 10^{-4}) \quad \left. \vphantom{\text{New design}} \right\} \rightarrow D_{cav} = \frac{N_R E_l}{S_{ill}} = 438 \frac{\text{mJ}}{\text{cm}^2}$$

$$\bar{P} = \frac{D_{cav}}{D_{sat}} \simeq 0.01$$

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2016: experimental setup



Detectors: suited for time-resolved X-ray spectroscopy

Germanium HPGe: low energy X-rays spectroscopy

ORTEC GLP:

Energy Range: 0 – 300 keV

Crystal Diameter: 11 mm

Crystal Length: 7 mm

Beryllium Window: 0.127 mm

Resolution Warrented (FWHM):

- at 5.9 keV is 195 eV (T_{sh} 6 μs)

- at 122 keV is 495 eV (T_{sh} 6 μs)

ORTEC GMX:

Energy Range: 10 – 1000 keV

Crystal Diameter: 55 mm

Crystal Length: 50 mm

Beryllium Window: 0.5 mm

Resolution Warrented (FWHM):

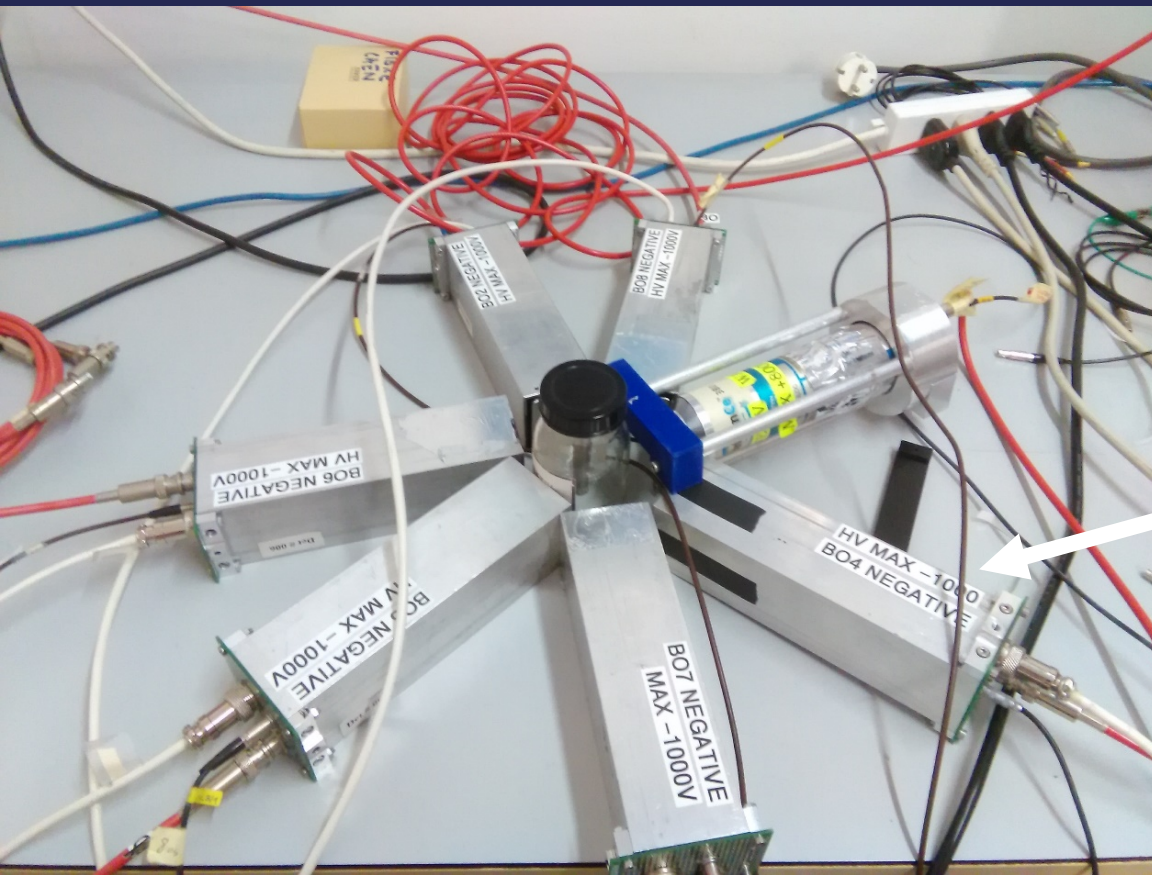
- at 5.9 keV is 600 eV (T_{sh} 6 μs)

- at 122 keV is 800 eV (T_{sh} 6 μs)



Detectors: suited for time-resolved X-ray spectroscopy

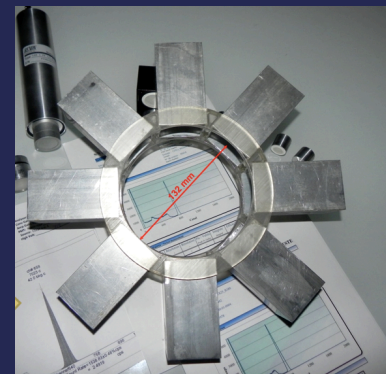
Lanthanum bromide scintillating crystals $[\text{LaBr}_3(\text{Ce})]$:
fast timing X-rays detectors



Lab test

8 cylindrical 1 inch diameter
1 inch long $\text{LaBr}_3(5\%\text{Ce})$
crystals
read by PMTs.

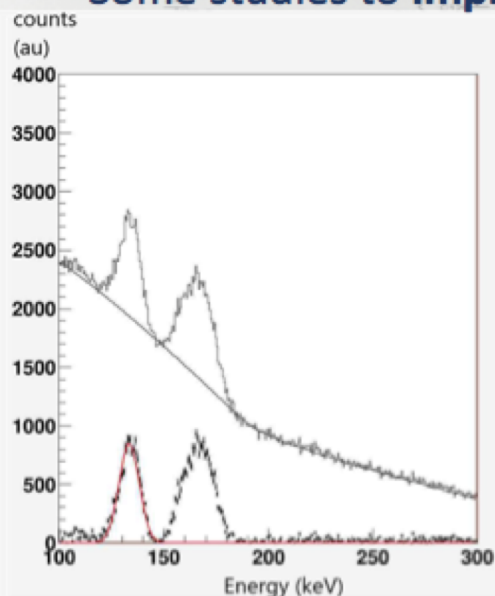
On purpose developed fast
electronics and fast digital
processing signal.



LaBr Bologna detectors

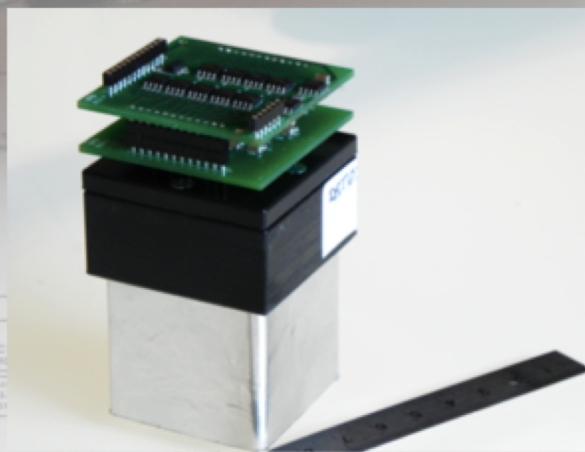
LaBr₃ + (UBA) Hamamatsu photomultiplier

- **Custom active voltage divider** for high rate applications
- **8 built and on beam tested + 8 build ongoing**
- New **high coverage** detector's geometry in order to adapt to the new work in progress target.
- Some studies to **improve energy resolution**



Delayed muonic oxygen lines well resolved.
The 133keV line resolution is 8.5%, slightly worse than the 8.1% predicted

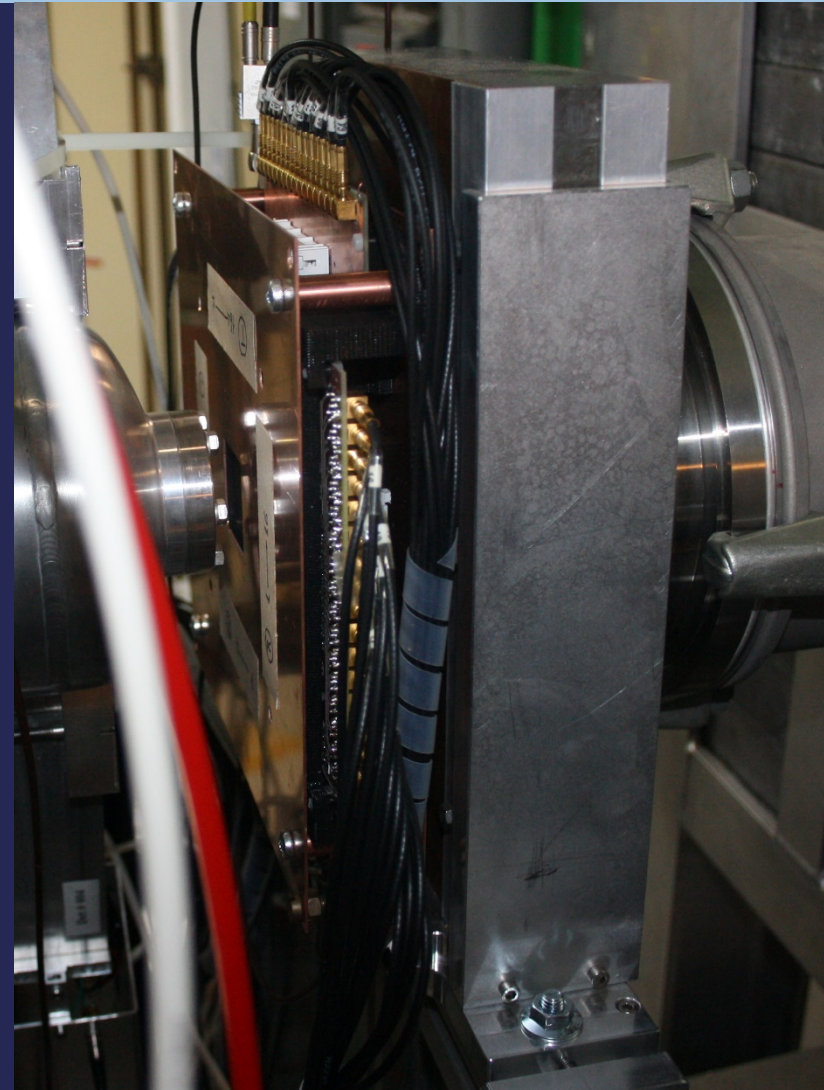
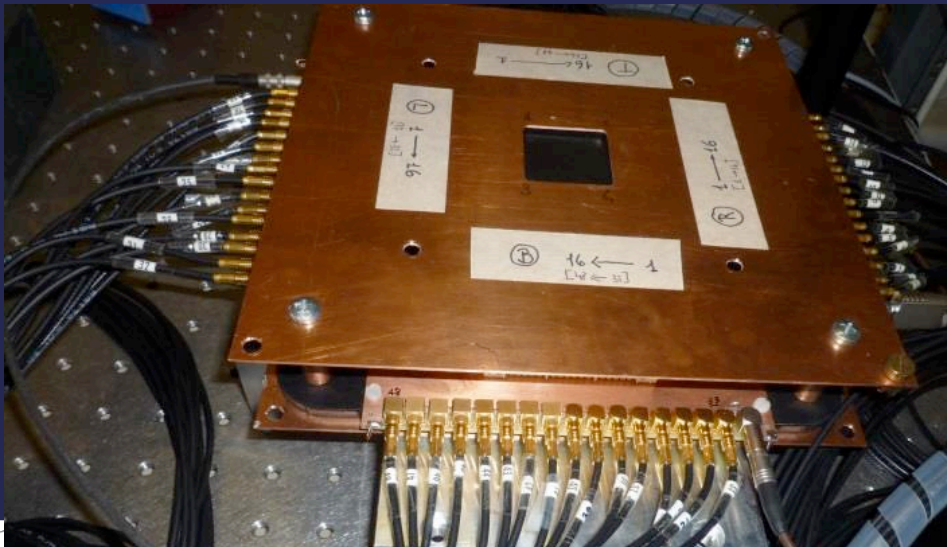
Energy (keV)	Literature resolution	Famu detector
122 keV	7.4%	8.8%
662 keV	2.8%	3.5%



Article: G. Baldazzi and al., The LaBr 3 (Ce) based detection system for the FAMU experiment, Journal of Instrumentation 12 (2017) 03

Hodoscope for beam shape monitoring

Final version:
two planes (X and Y) of 32 scintillating
fibers 1 x 1 mm² square section
SiPM reading with fast electronics
3D printed supports



hodoscope in the 2016 setup

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two competing processes

- the strength of x-ray signal, from mu-p's accelerated via the laser shot, is proportional to
 - the ratio of the muon transfer rate to oxygen and
 - the thermalization rate.
- both of them are proportional to the target density,

Through simulations optimize the relevant parameters

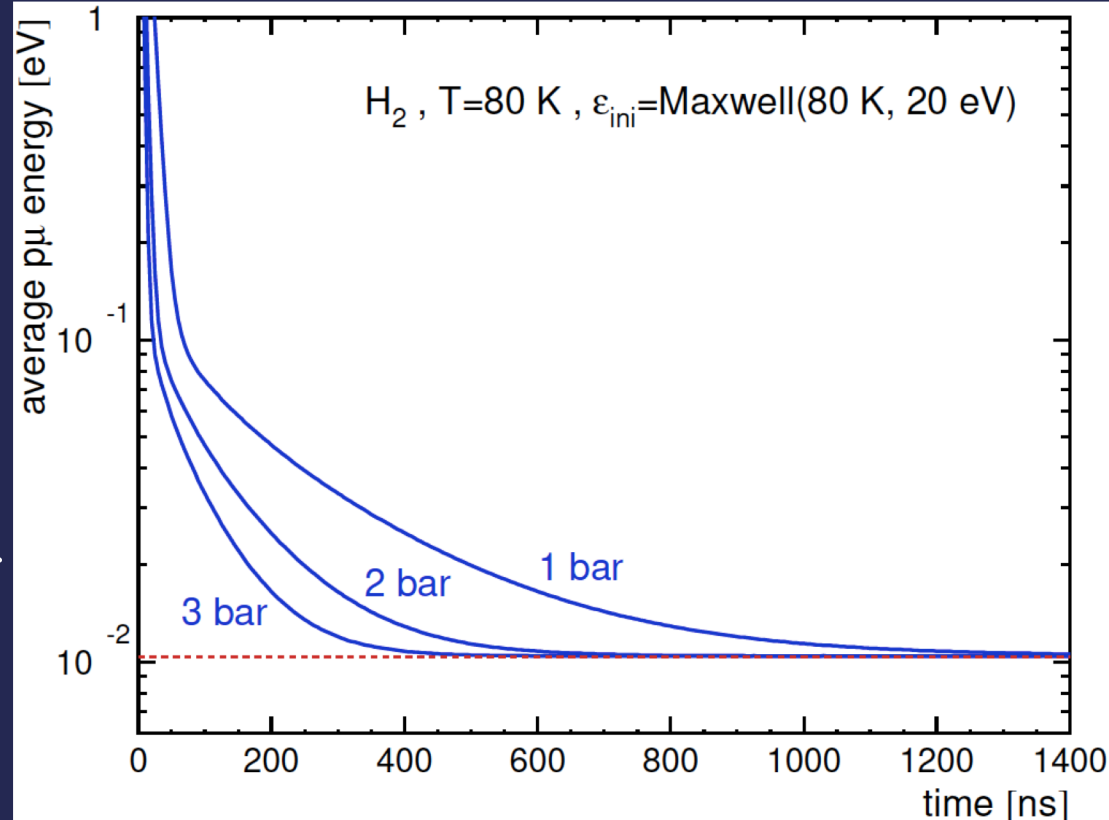
- The only parameter we can use to enhance the signal is the oxygen concentration - the x-ray signal is directly proportional to this concentration.
- The target pressure cannot be too small. We need a reasonable amount of the muon stops within the volume of laser field.
- The overall **optimal condition**, for the HFS measurement is thus a convolution of these two optimization functions, **is going to be determined by the HFS-measurement simulation, which is underway.**

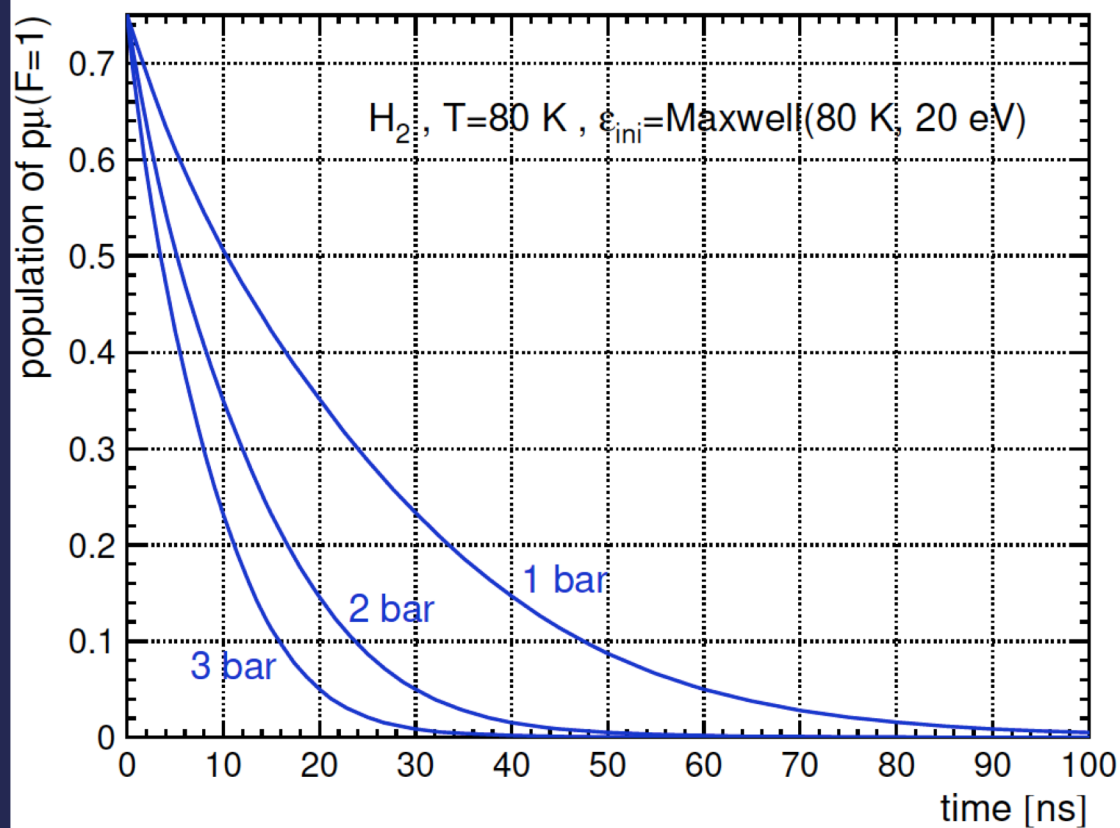
The time evolution of mean kinetic energy, which also illustrates the thermalization time. This indicates the instant of laser ignition when mu-p atoms should be thermalized

Also, this picture shows a mean time of deceleration from about 0.11 eV (mean energy of mu-p's after the laser excitation and downwards spin flip) to about 0.04 eV (lower energy of a relatively high muon transfer rate to oxygen,).

Within this time, the most of muon-transfer events should take place, in order to have a strong signal.

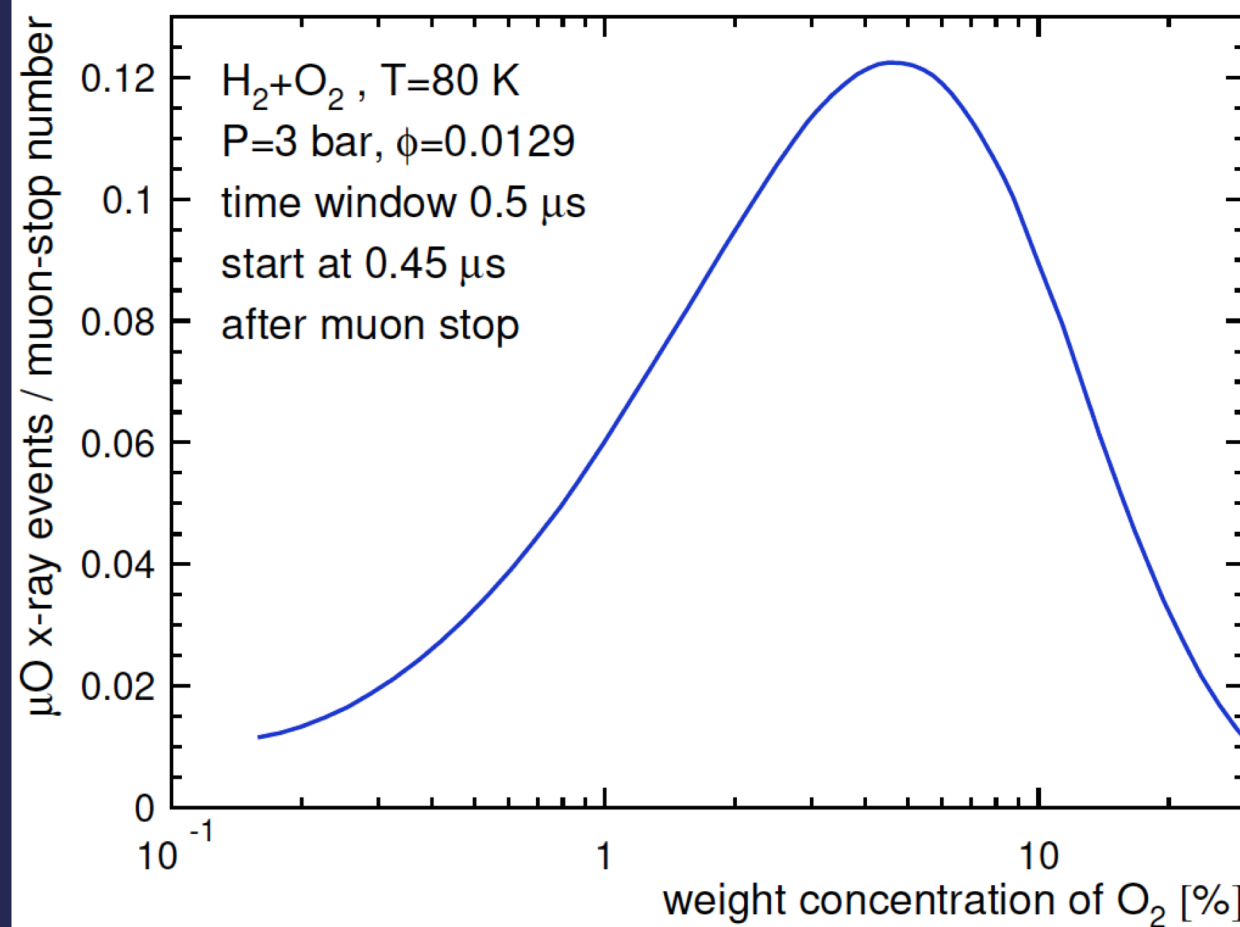
We can increase this signal only by increasing the oxygen concentration, within certain limits.





mu-p spin de-excitation versus time.

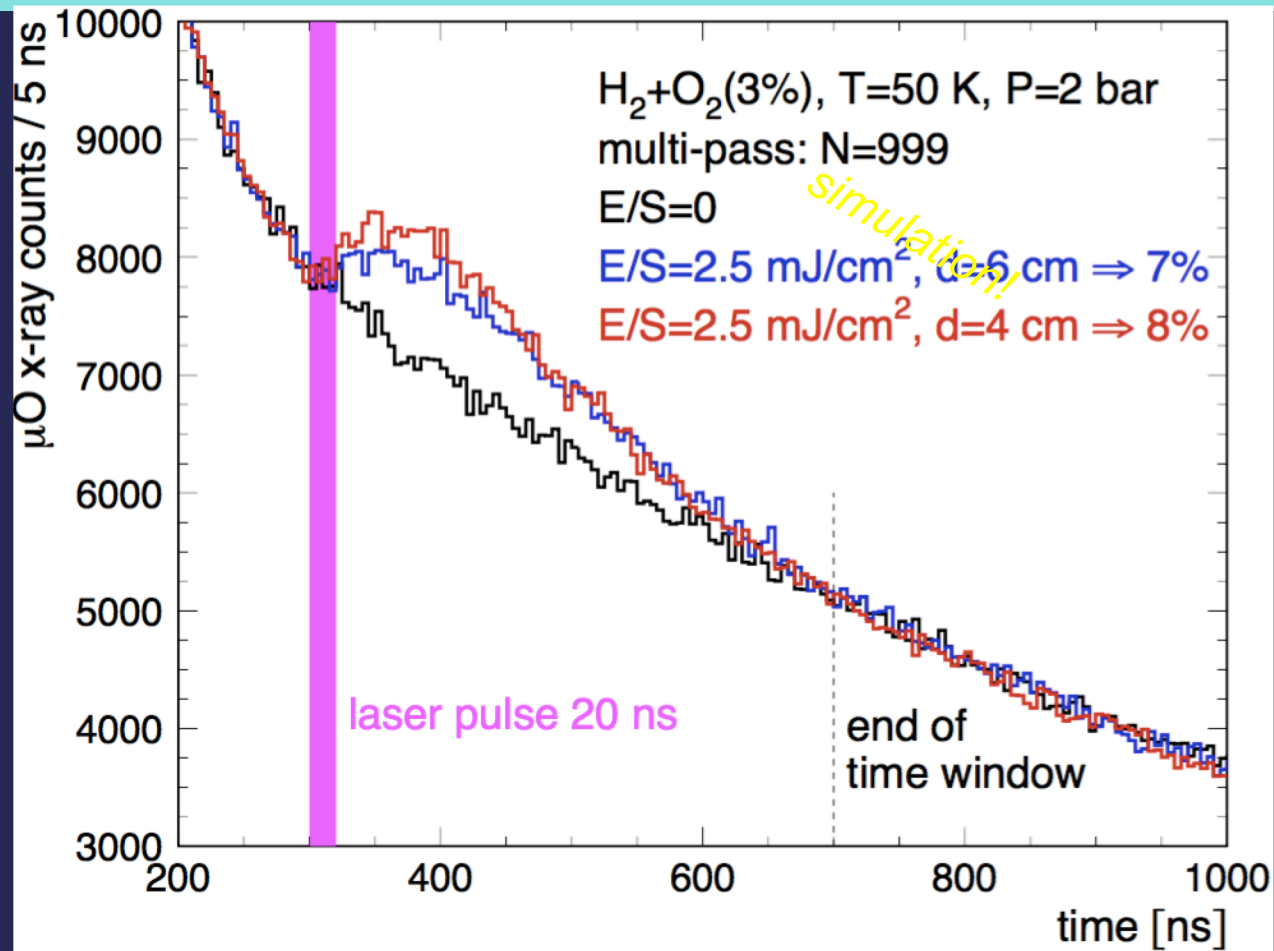
The de-excitation time informs us about how long we should wait for the acceleration of mu-p atom which was excited by a laser photon.



The plotted functions show a number of existing mu-p's in the time window of 500 ns, divided by the number of muon stops. The beginning of the time window corresponds to the moment of full thermalization. The time windows is approximately equal to the time of laser-field presence in the multipass cavity.

Study of best setup to maximize signal

- Shape and orientation of the optical cavity
- Characteristics of the cryo-target
- Pressure and oxygen concentration



Low pressure \Rightarrow New target :

TARGET 2016

vacuum window: 0.8 mm Al
pressure vessel window: 2.84 mm Al
with hodoscope (1mm fibers)
gas: ~cylinder, 6 cm \varnothing 40 cm length
with Ni (100 microns) + Au (10 microns) coating
with multi-layer insulators in front, on sides, on the bottom
lead collimator: wall with hole 3 cm \varnothing

40 BAR @ 300 K

2 BAR @ 80 K

TARGET 2018

vacuum window: 1 mm Kapton
pressure vessel window: 1.5 mm fused Silica
no hodoscope
gas: cylinder 2 cm \varnothing 15 cm length
no coating
with multi-layer insulators in front (same of 2016)
lead collimator: wall with hole 2 cm \varnothing

2 BAR @ 80 K

New target simulations:

@ 300 K

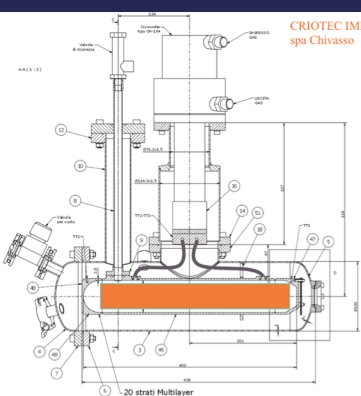
TARGET 2016 vacuum wind
pressure ve
with hodo
gas: ~cy
with Ni
with m
lead co

low pressure :

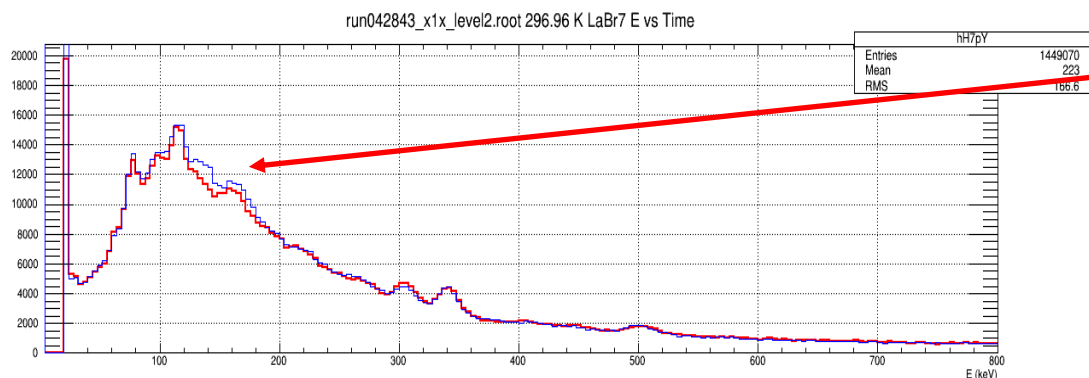
- less stopped muons
- lower momentum = less muons in beam
- & small optical cavity

Need careful optimization
of all elements

TARGET 2018 vacuum
pressure v
no hodoscop
gas: cylinder 2
no coating
with multi-layer insulator
lead collimator: wall with

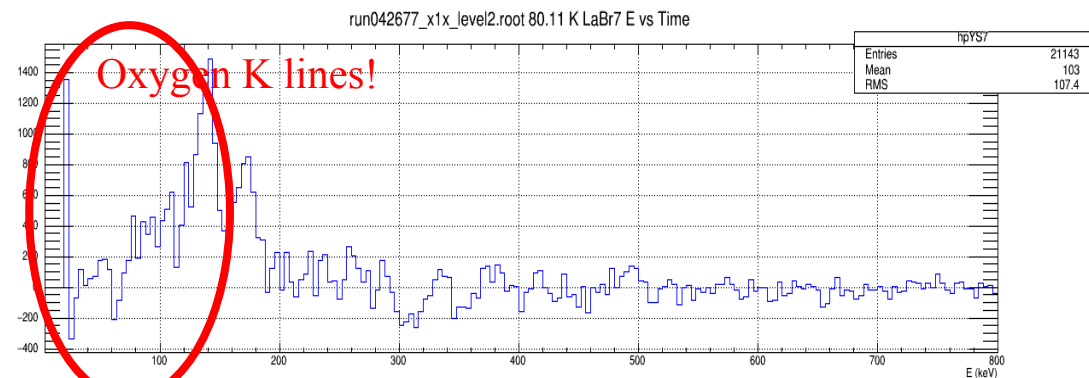


2018 study @low pressure old target

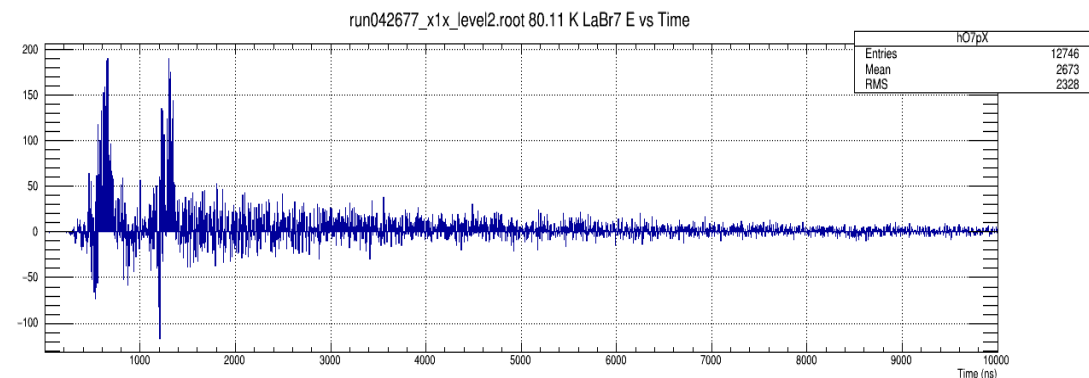


LaBr re-calibrated

Energy spectra
Blue O(3%) mixture
Red pure hydrogen
(3 bar 80 K) (normalized according to acq number of trigger, i.e. time)

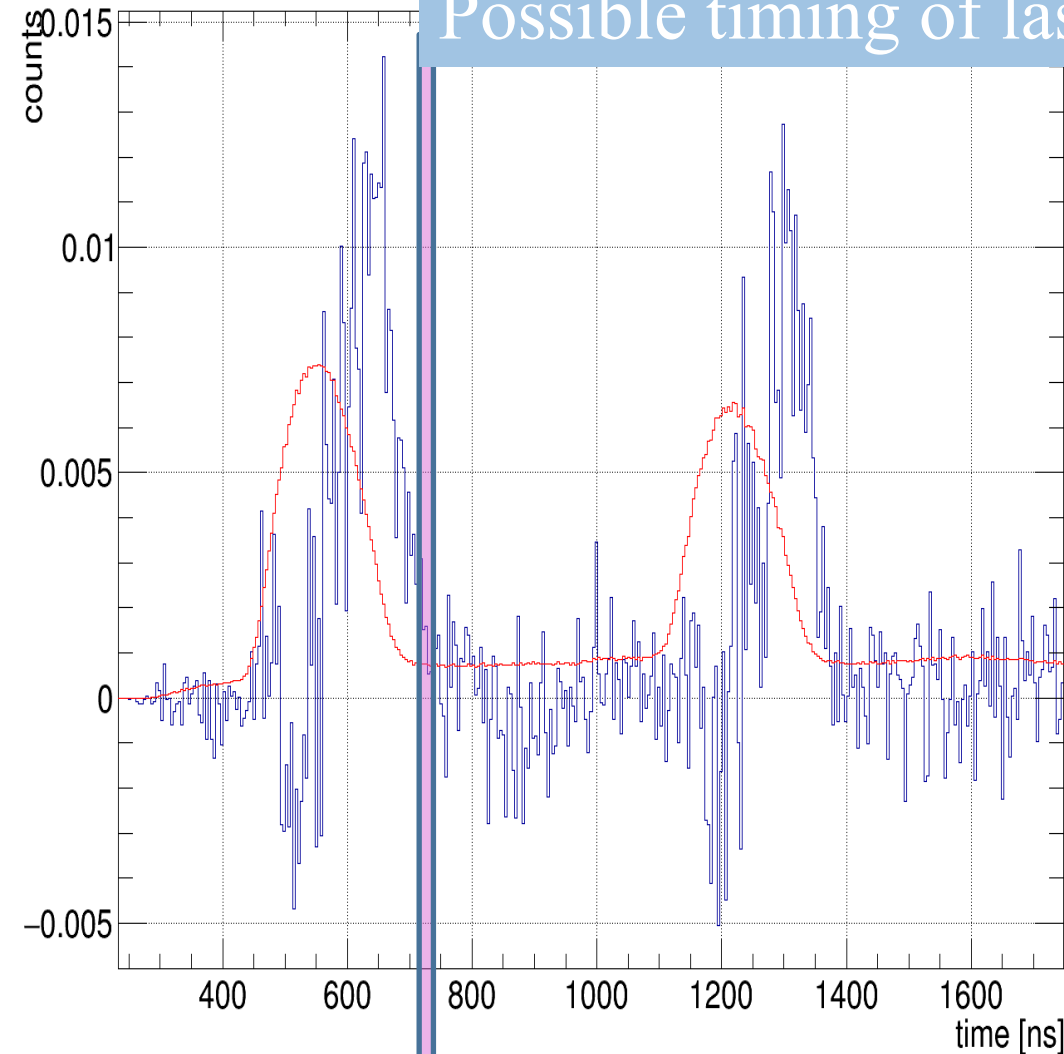


Oxygen mixture
hydrogen subtracted



Time evolution of oxygen mixture – hydrogen in the energy range 110 – 200 keV

Possible timing of laser shot



Oxygen lines time evolution
(very fast due to high oxygen concentration).

Comparison with
muon beam arrival
time (actually prompt
X-ray signal).

Oxygen signal is
delayed but still
overlapping the prompt
signal.

First rough evaluation

For 2.2×10^4 counts:

Statistical fluctuations: $\sqrt{2.2 \times 10^4} = 148$

Expected signal: $2.2 \times 10^4 \times 0.008 = 176$

80 hours = 3.3 days (one frequency measurement). \Rightarrow

\Rightarrow Need careful optimization (beam time reduction):

- 1) Number of detectors (factor 2, 16 LaBr instead of 8)
- 2) Muon focalization (possible factor 2)
- 3) Software reconstruction (probably a factor 2, results presented with quick and dirty “quicklook” analysis)
- 4) laser can be at 8mJ \Rightarrow 4% transition prob (1,6% Signal)
- 5) optimized target.
- 6) gas pressure and concentration

NB2: no systematics taken into account, no background measurement (working at 30/50 Hz but one of the pulses could be used to study the background), no new target materials and momentum.

Summary

The FAMU project has made substantial steps towards the **laser spectroscopy measurement of the hyperfine splitting (hfs) in the 1S state of muonic hydrogen**

$$\Delta E_{\text{hfs}}(\mu^-p)_{1S}$$

preparatory work accomplished :

1. *first measurement* of the temperature dependent muon transfer rate to Oxygen, FAMU method certified!
1. *innovative* and powerful laser system under construction
2. *optimized intense pulsed beam target and optical system*
3. *best detectors* for energy and time observation

expect to initiate the spectroscopic measurements in 2019.

Than you for your attention