

Quarkonia in nuclear collisions

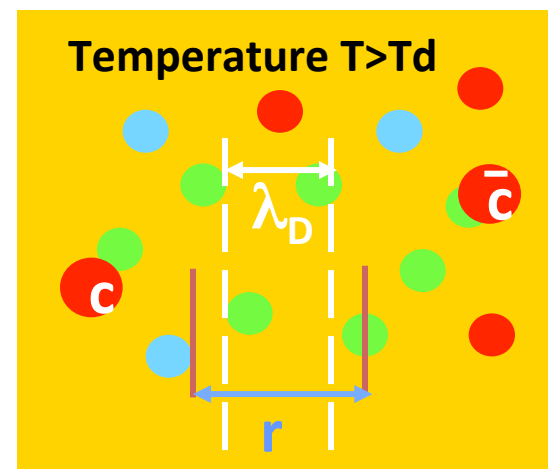
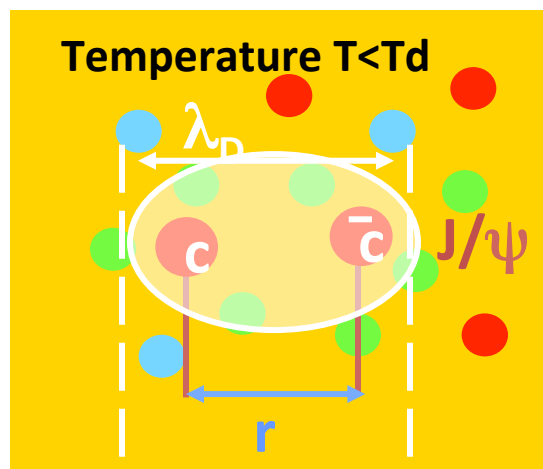
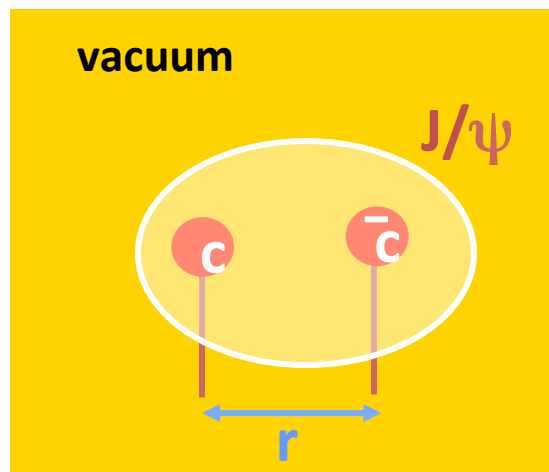
Elena G. Ferreiro

IGFAE, Universidade de Santiago de Compostela, Spain

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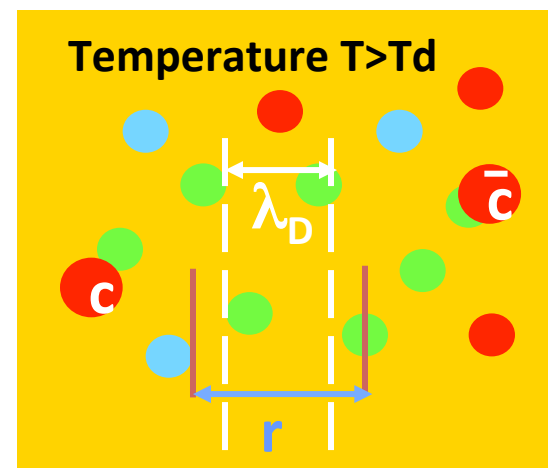
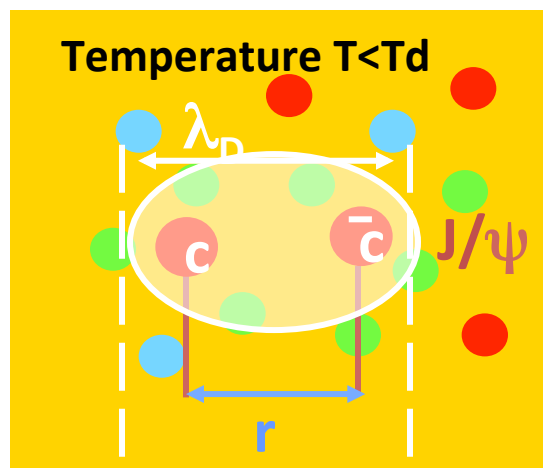
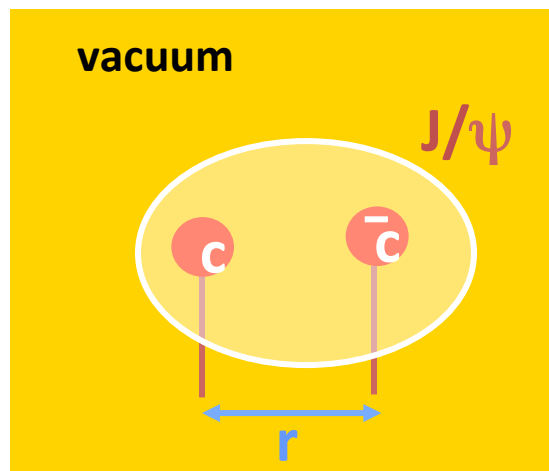
Why quarkonium?

The usual introduction: Debye screening $\lambda_D(T)$

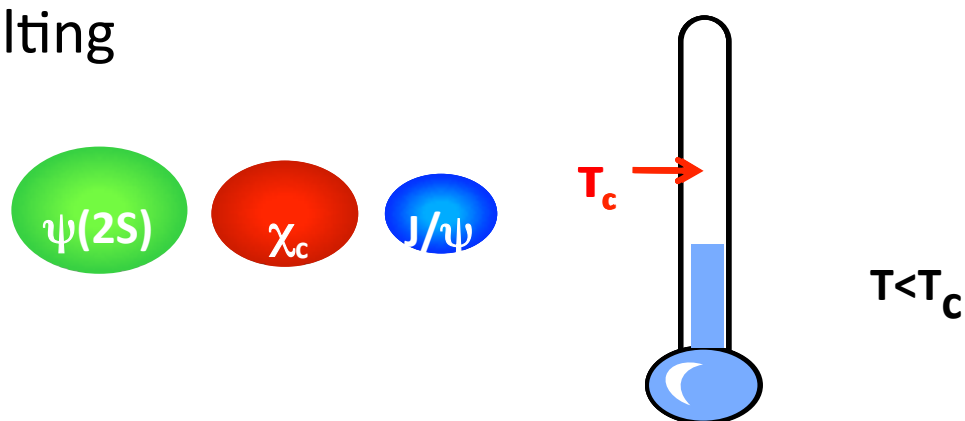


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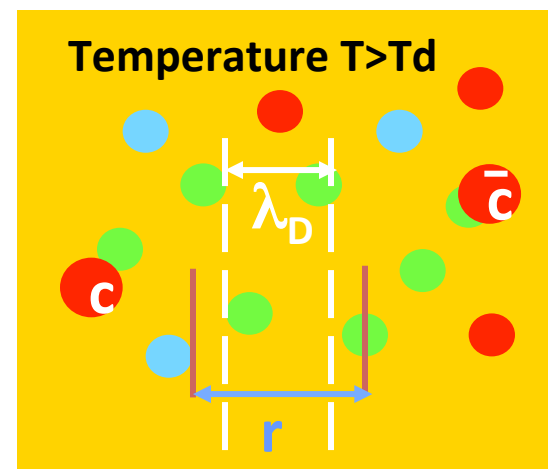
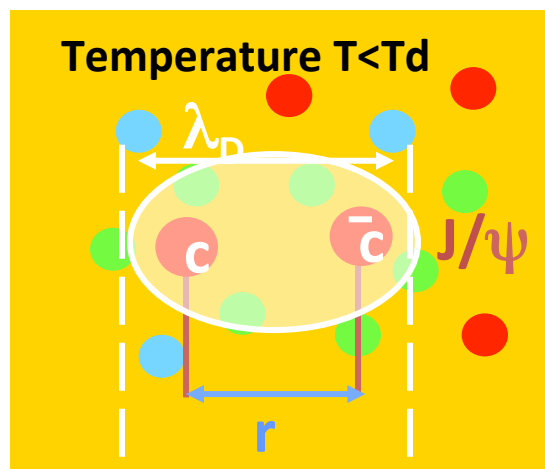
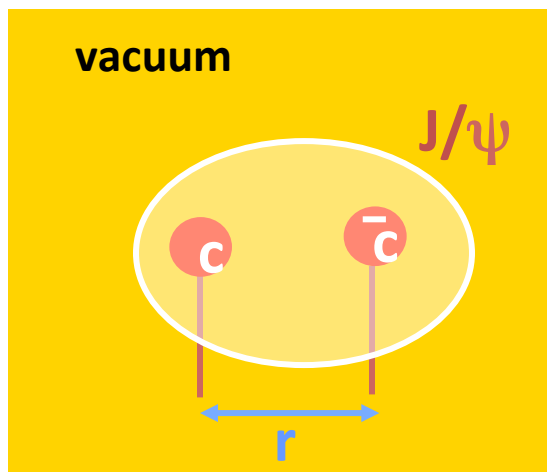


Sequential melting

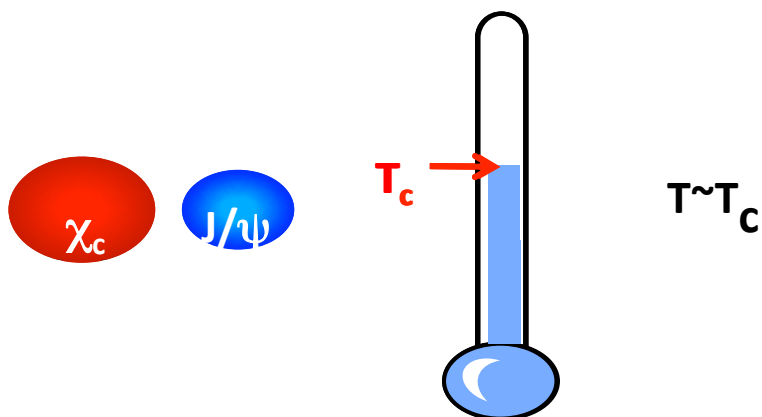


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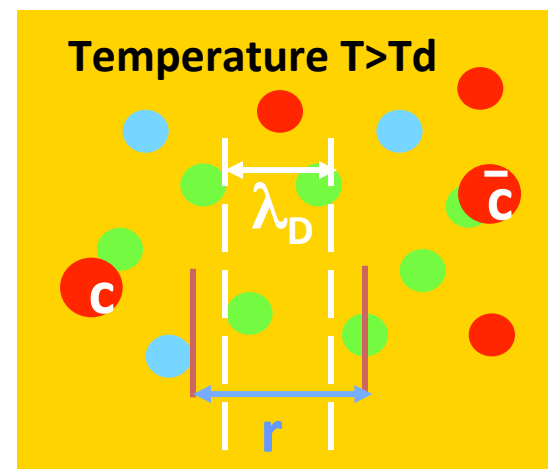
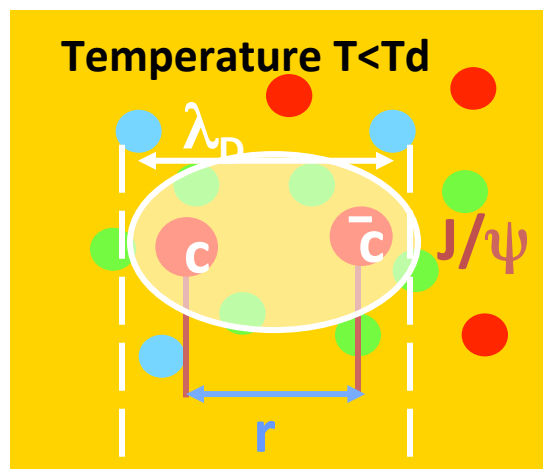
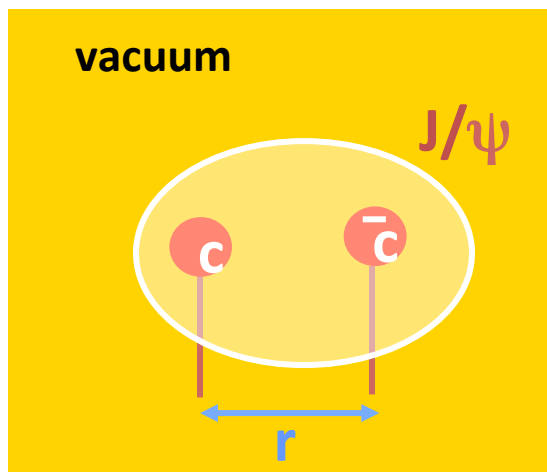


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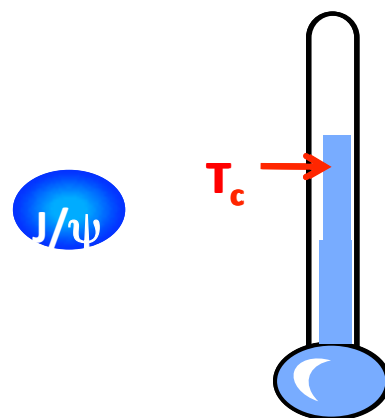


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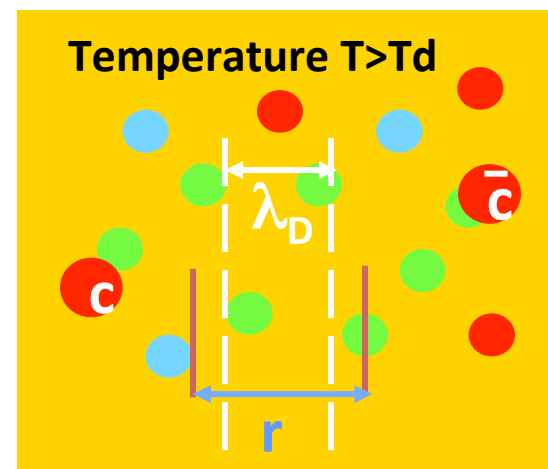
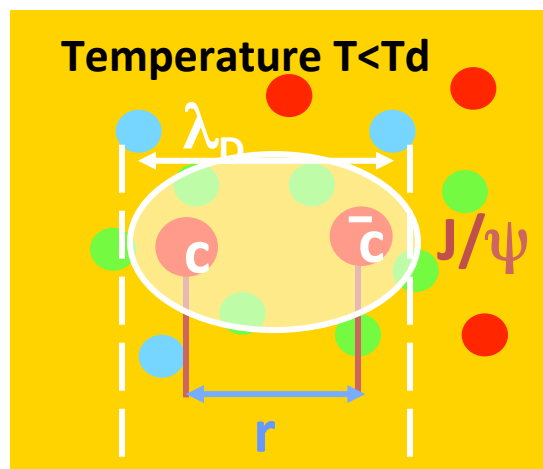
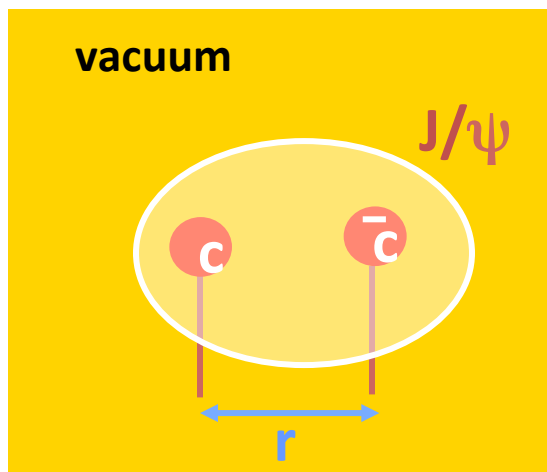
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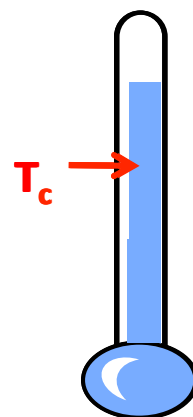
$$T \sim 1.1 T_c$$

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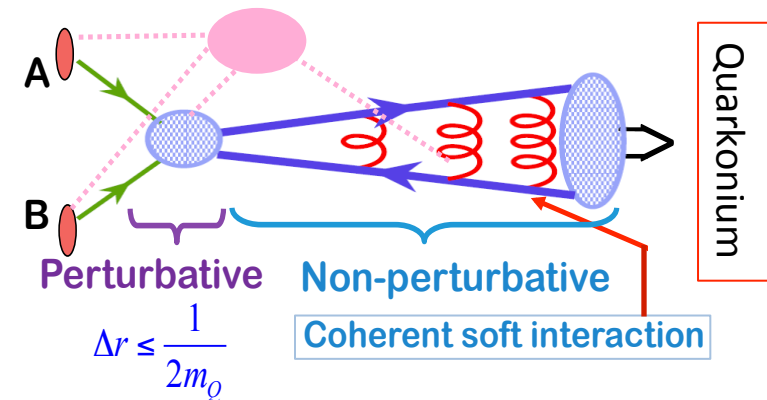


$T \gg T_c$

Quarkonium production schemes in pp: A long history

Quarkonium production involves perturbative and non perturbative QCD

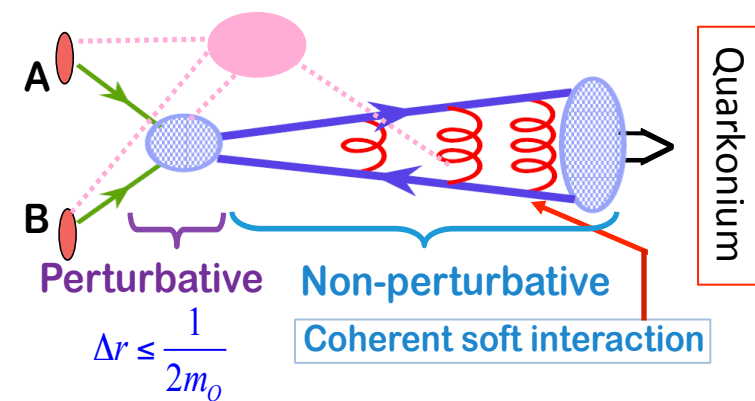
- Production of the heavy-quark pair, $Q\bar{Q}$: **perturbative**
- Evolution of the $Q\bar{Q}$ pair into the physical quarkonium state: **non-perturbative**



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Different approaches to hadronization:

Color singlet model (CSM): 1975 -

Einhorn, Ellis (1975), Chang (1980), Berger & Jone (1981), ...

- Assume physical color singlet state, quantum numbers are conserved
- Only the pair with right quantum numbers

Effectively no free parameter

Color evaporation model (CEM): 1977 -

Fritsch (1977), Halzen (1977), ...

- Does not distinguish states with respect to their color and spin
- All pairs with mass less than open heavy flavor threshold

One parameter per quarkonium state

Nonrelativistic QCD (NRQCD): 1986 -

Caswell, Lapage (1986) Bodwin, Braaten, Lepage (1995), ...

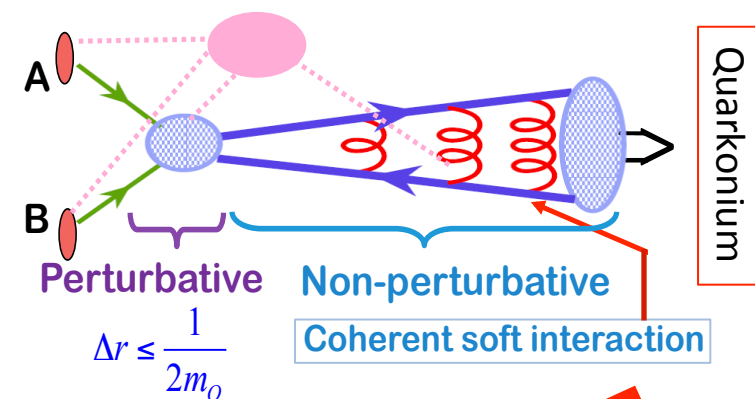
- Rigorous effective field theory based on factorization of soft and hard scales
- All pairs with various probabilities – NRQCD matrix elements

Infinite parameters – organized in powers of v and α_s

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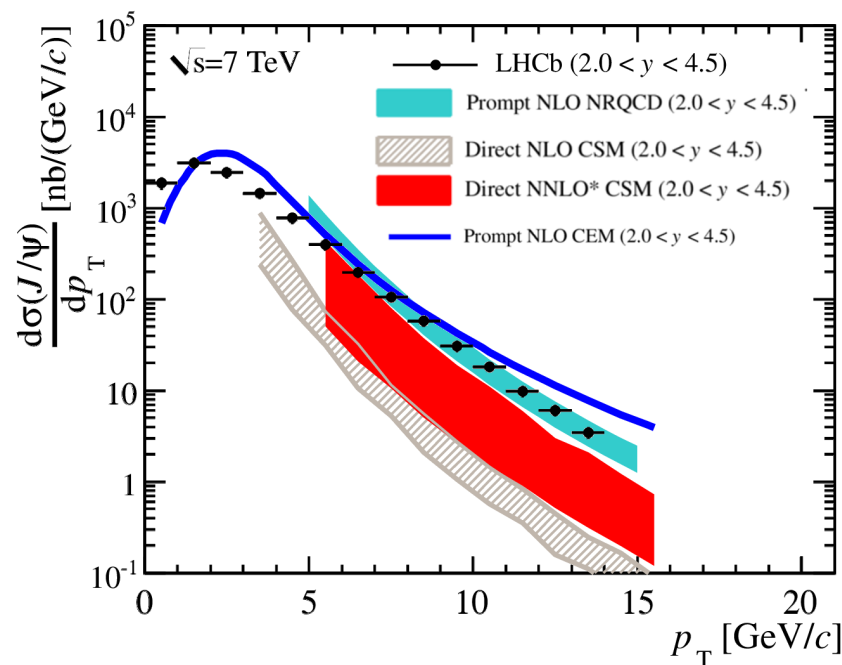
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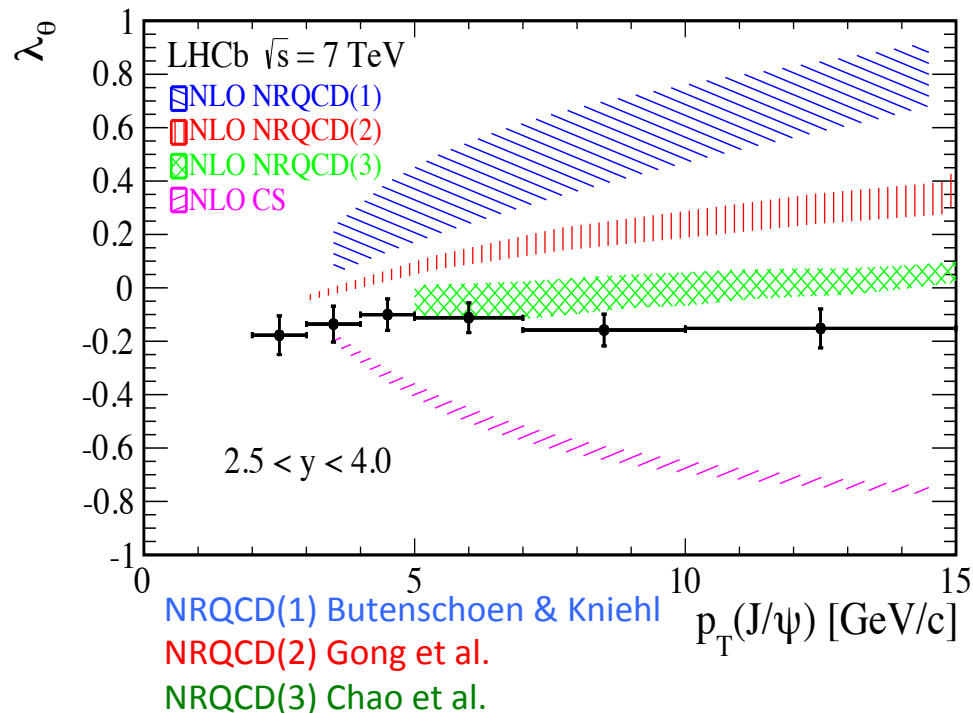
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Production models: state of the art for the J/ψ



Sapores Gravis Review arXiv:1506.03981



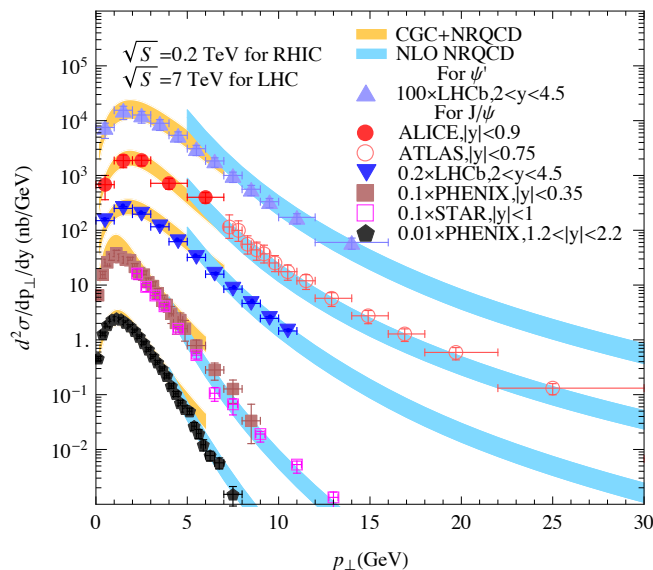
- **CSM** still in the game: Large NLO and NNLO* corrections in p_T ; need a full NNLO
 - **NRQCD**: COM helps in describing the p_T spectrum
- Yet, fits differ in their conclusions owing to their assumptions
(data set, p_T cut, polarization fitted or not)
- At low and mid p_T –region where quarkonium heavy-ion studies are mainly carried out– none of the models can simply be ruled out due to theoretical uncertainties

Recent developments may be helpful

- **Color Evaporation Model (CEM) Improved**
- Explicit charmonium mass dependence
=> ψ'/ψ ratio no longer p_T independent
- Relates $\langle p_\psi \rangle$ to the $c\bar{c}$ pair momentum
=> explain the high p_T data better
- LO calculation of quarkonium polarization in the CEM, longitudinal polarized @ LHC

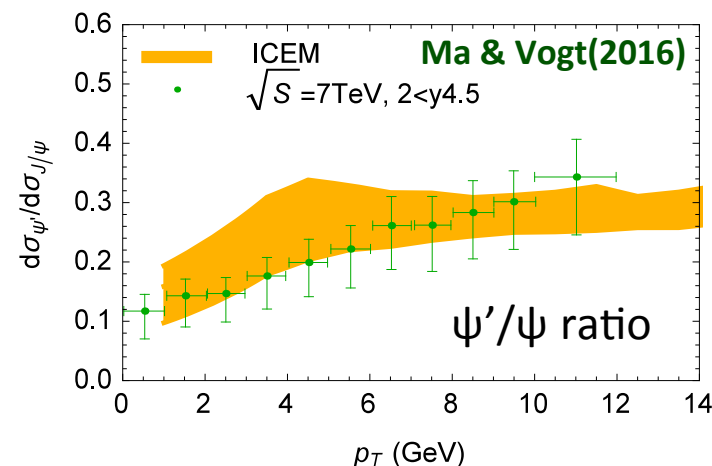
Cheung & Vogt(2017)

- **Saturation meets NRQCD**



$$\sigma_Q^{(N)LO} = F_Q \int_{2m_Q}^{2m_H} \frac{d\sigma_{Q\bar{Q}}^{(N)LO}}{dm_{Q\bar{Q}}} dm_{Q\bar{Q}}$$

changes to M_ψ



- Uses **Color Glass Condensate** saturation model of gluon distributions in the proton with NLO NRQCD matrix elements
- Saturation physics at low p_T ,
normal collinear factorization at high p_T ,
matching at intermediate p_T

Ma, Venugopalan & Zhang (2015)

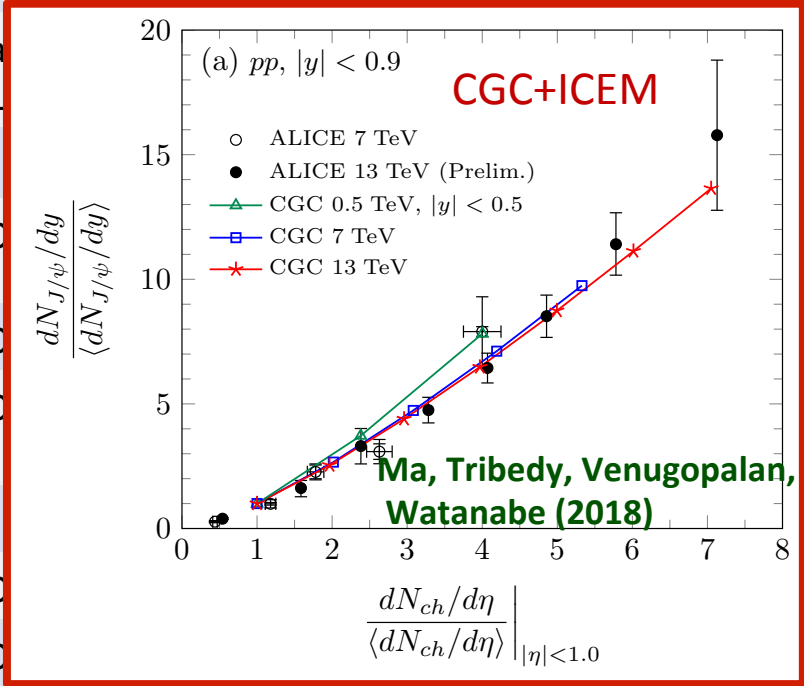
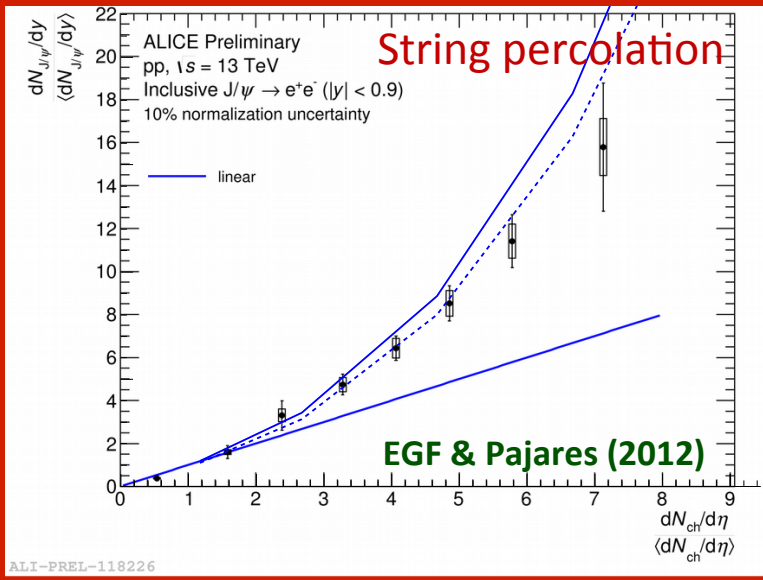
New observables can help

Observables	Experiments	CSM	CEM	NRQCD	Interest
$J/\psi + J/\psi$	LHCb, CMS, ATLAS, D0 (+NA3)	NLO, NNLO*	LO ?	LO	Prod. Mechanism (CS dominant) + DPS + gluon TMD
$J/\psi + D$	LHCb	LO	LO ?	LO	Prod. Mechanism (c to J/psi fragmentation) + DPS
$J/\psi + \Upsilon$	D0	(N)LO	LO ?	LO	Prod. Mechanism (CO dominant) + DPS
$J/\psi + \text{hadron}$	STAR	LO	--	LO	B feed-down; Singlet vs Octet radiation
$J/\psi + Z$	ATLAS	NLO	NLO	Partial NLO	Prod. Mechanism + DPS
$J/\psi + W$	ATLAS	LO	LO ?	Partial NLO	Prod. Mechanism (CO dominant) + DPS
J/ψ vs mult.	ALICE, CMS (+UA1)	--	--	--	Density effects (Saturation/Hydro)
$J/\psi + b$	-- (LHCb, D0, CMS ?)	--	--	LO	Prod. Mechanism (CO dominant) + DPS
$\Upsilon + D$	LHCb	LO	LO ?	LO	DPS
$\Upsilon + \gamma$	--	NLO, NNLO*	LO ?	LO	Prod. Mechanism (CO LDME mix) + gluon TMD/PDF
Υ vs mult.	CMS	--	--	--	Density effects (Saturation/Hydro)
$\Upsilon + Z$	--	NLO	LO ?	LO	Prod. Mechanism + DPS
$\Upsilon + \Upsilon$	CMS	NLO?	LO?	LO?	Prod. Mechanism + DPS + gluon TMD

Lansberg (2018)

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J/ψ vs mult.	ALICE, CMS (+UA1)	--	--	--	
$J/\psi + b$	-- (LHCb, D0, CMS ?)	--	--	LO	
<div>Events at different energies with the same ρ_{strings} or Q_s are identical</div> <div>Saturation in high multiplicity pp?</div>					
$\Upsilon + Z$	--	NLO	LO ?	LO	
$\Upsilon + \Upsilon$	CMS	NLO?	LO?	LO	



Lansberg (2018)

Quarkonium in proton-nucleus: Motivations and expected effects

In such reactions, many physics effects of specific interest are involved:

- **Modification of the gluon flux** *initial-state effect*
 - ♦ Modification of **PDF in nuclei** nPDF shadowing
 - ♦ Gluon **saturation** at low x CGC
- **Parton propagation in medium** *initial/final effect* Coherent energy loss
- **Quarkonium-hadron interaction** *final-state effect*
 - ♦ Break up in the **nuclear matter** Nuclear absorption
 - ♦ Break up by **comoving particles** Comover interaction

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In addition of quantifying nuclear effects, quarkonium production in pA may be able to:

- Test **QCD factorization** in media
- Test the **quarkonium production mechanisms**: octet vs. singlet
- Test the dynamics of **hadronization** and time evolution of the $Q\bar{Q}$ pair

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- **QGP-like** effects?

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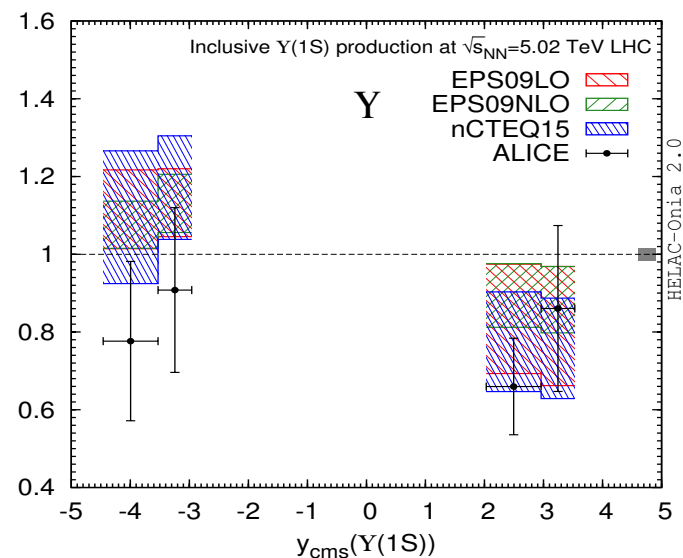
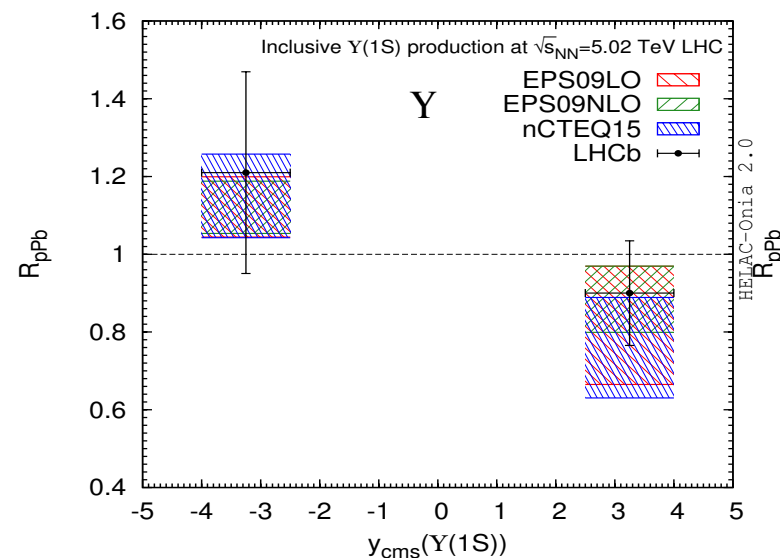
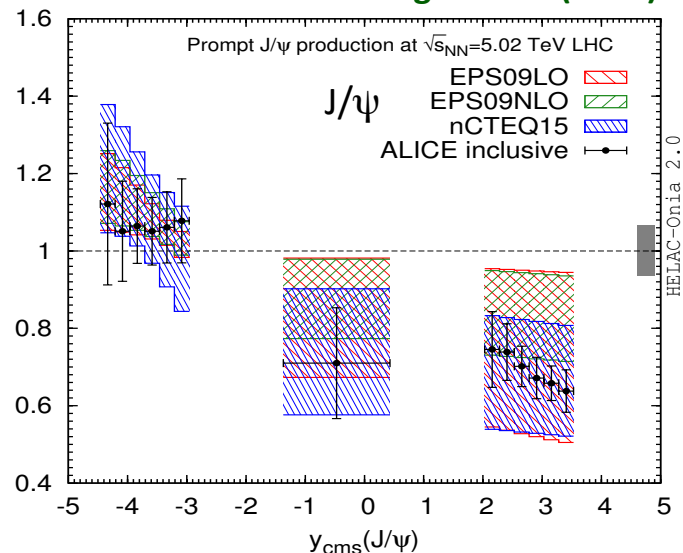
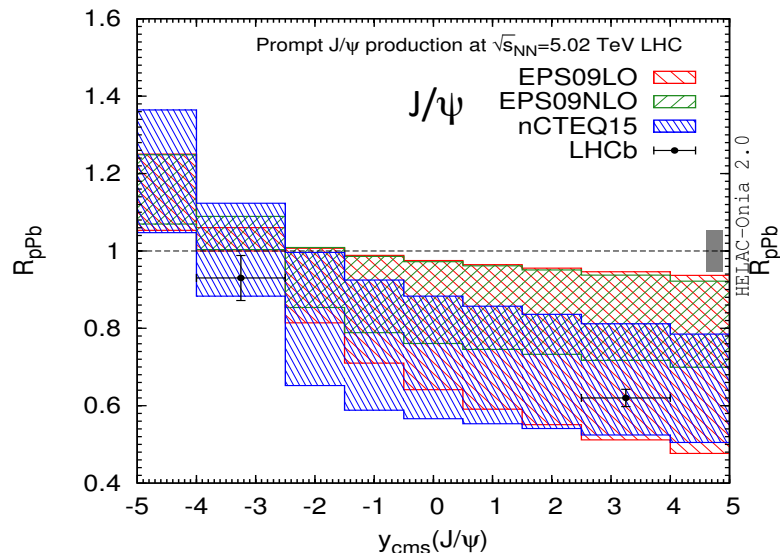
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Obviously relevant if one wishes to use quarkonia
as probes of the QGP => baseline

Comparison of nPDFs with LHC data

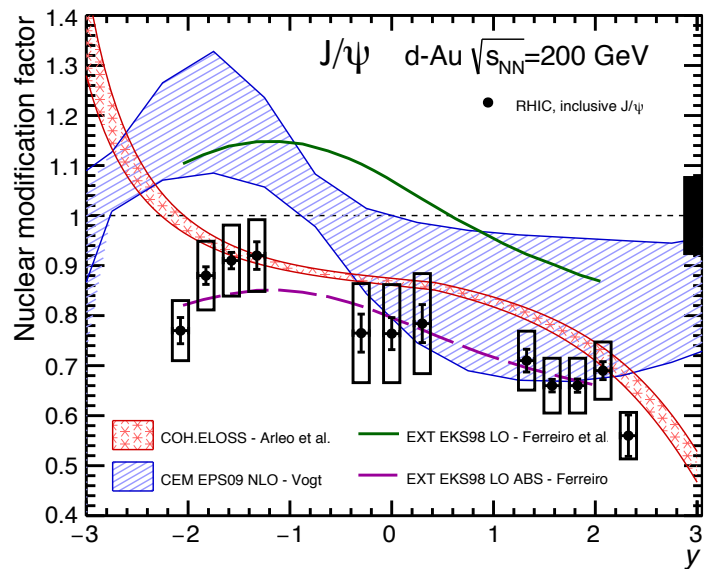
- Several nPDF sets available (using various data, LO/NLO, etc)
- Nuclear break-up neglected at LHC energies

Lansberg & Shao (2016)



- Data is compatible with strong shadowing
- The precision of the current data is already much better than the nPDF uncertainties
- It may offer hints for constraining the gluon density in Pb

Comparison of nPDFs & E_{loss} with RHIC & LHC d/p+A data

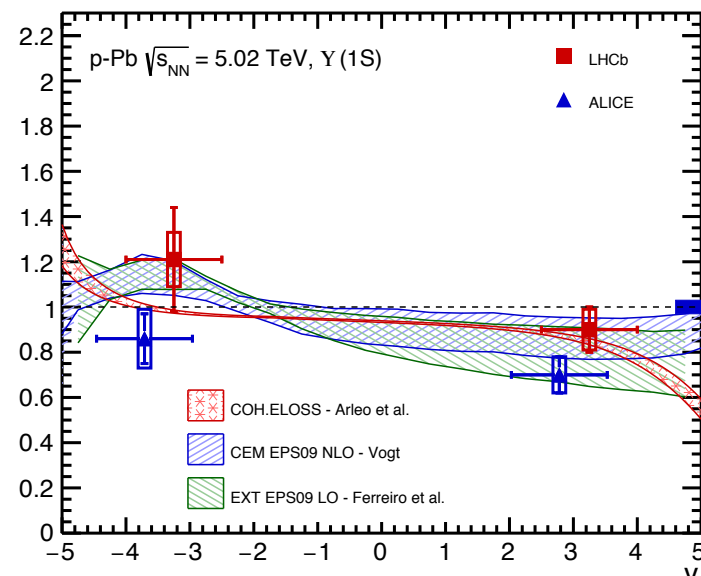
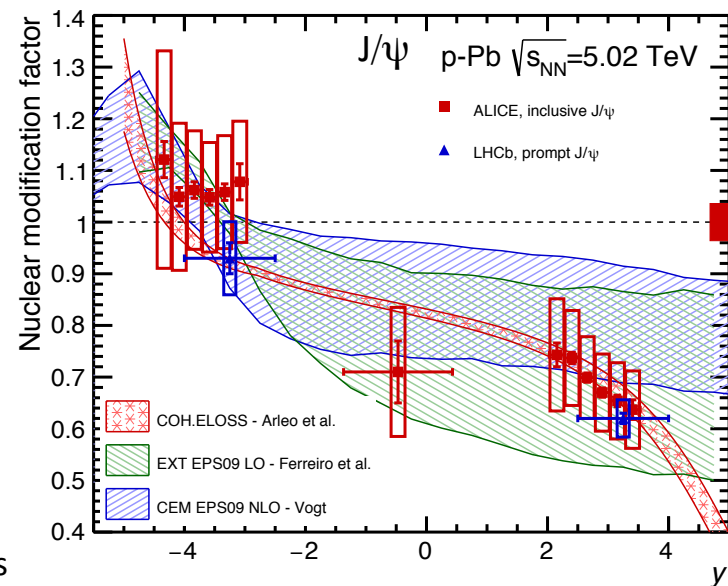
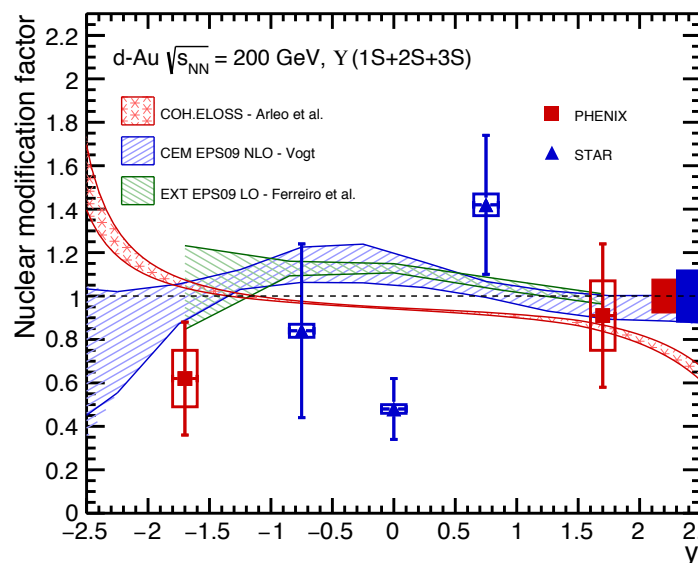


Coherent E_{loss}

$$\Delta E \propto E$$

Interference
terms initial/final
state for $t_f \gg R$
Arleo *et al.* (2014)

nPDF modifi-
cation &/or E_{loss}
fairly agree
with data

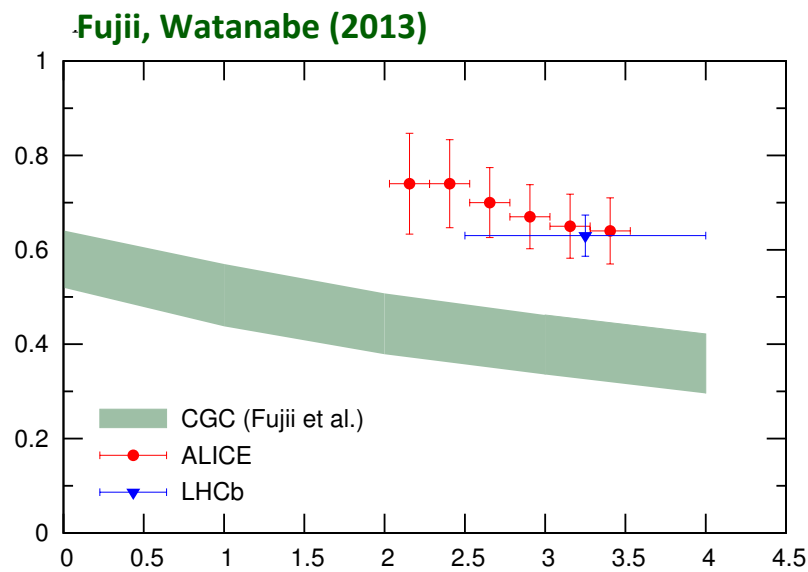


Do data show
energy increase
of suppression?

More precise
data needed

CGC computations: not just gluon saturation

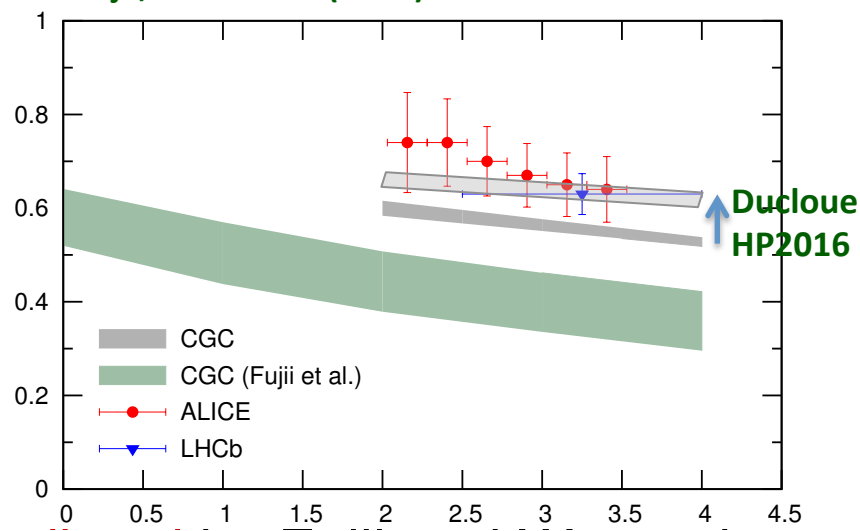
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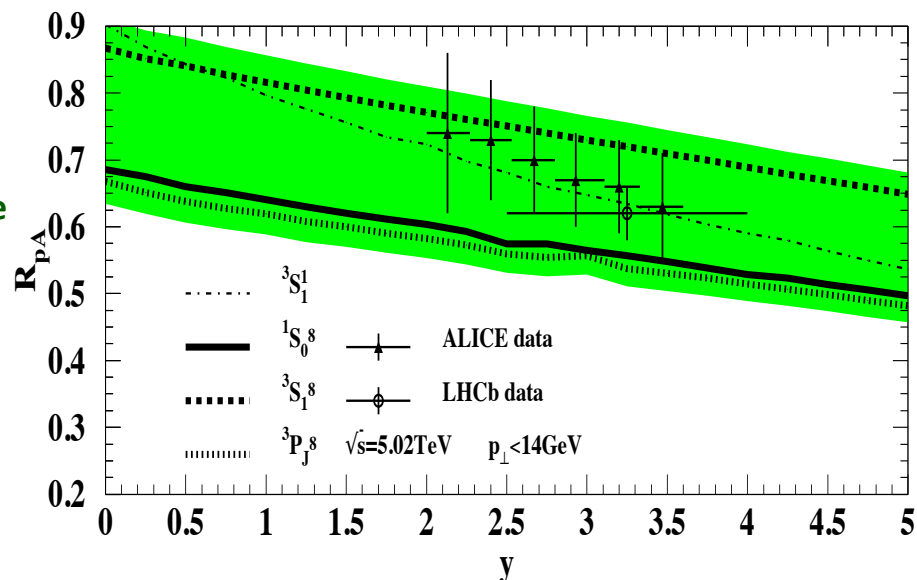
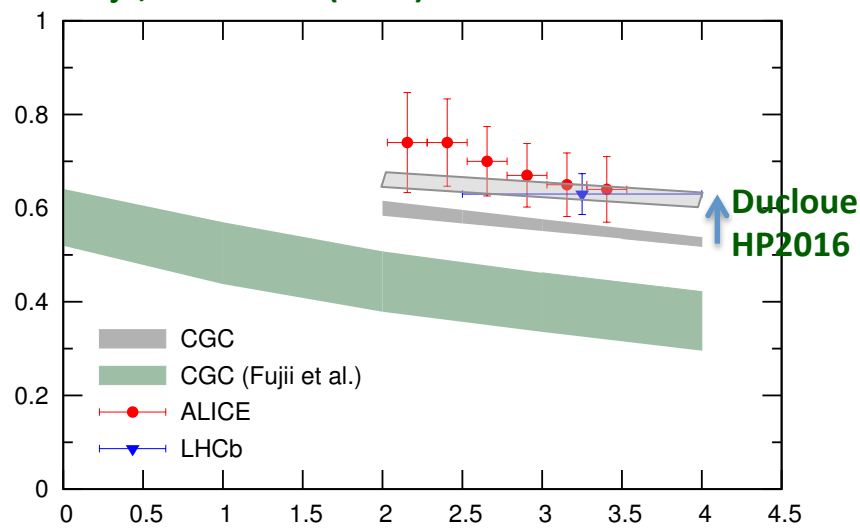


- Improved **postdictions**:
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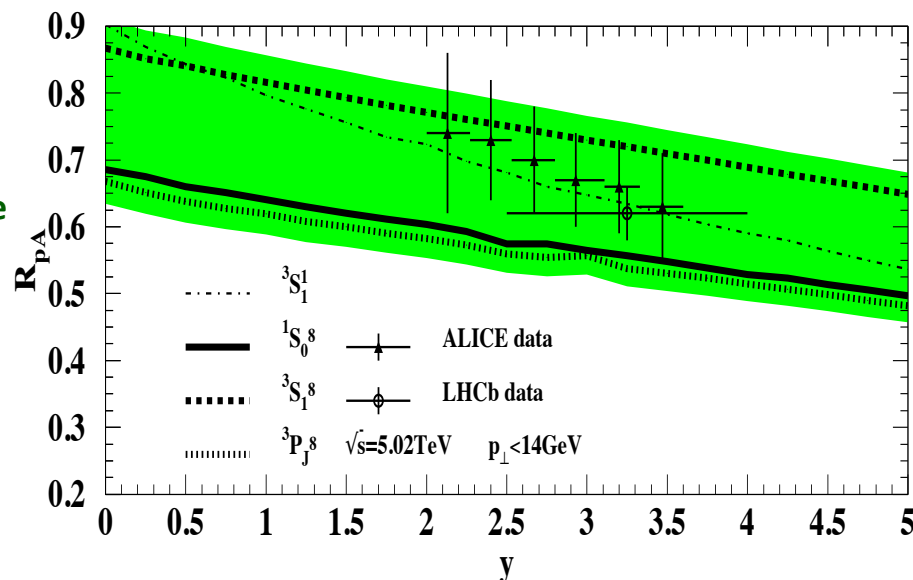
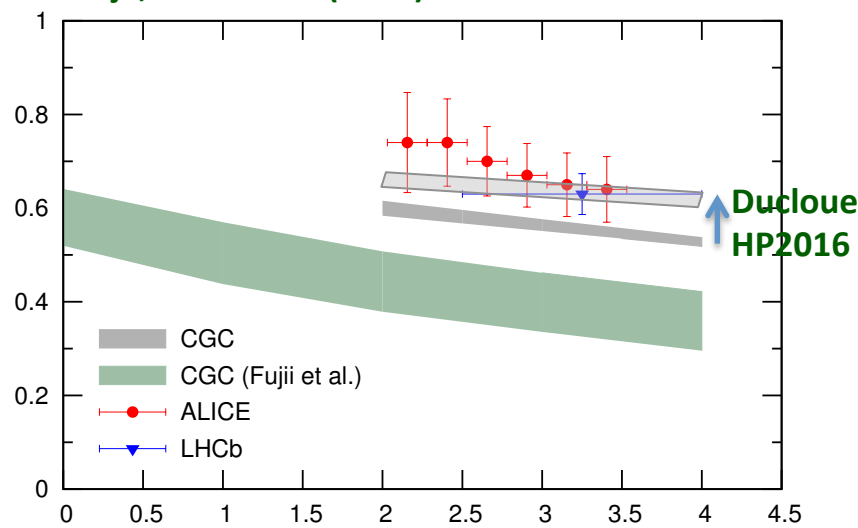


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contribution of CS channel relatively small 10% in pp, 15-20% in pA at low p_T

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- **Issue**: CGC results very much widespread (as those from nPDFs)
- **Note**: CGC on J/ψ suppression applies at forward y (not backward)

Excited states: An intriguing relative suppression in pA

The facts: **data from RHIC & LHC**

- PHENIX: **relative $\psi(2S)/J/\psi$ suppression** in **dAu** collisions @ 200 GeV
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- At low E: the relative suppression can be explained by nuclear absorption

$$\sigma_{\text{breakup}} \propto r_{\text{meson}}^2$$

At high E: too long formation times $t_f = \gamma \tau_f \gg R \Rightarrow$

the quantum state does not matter!

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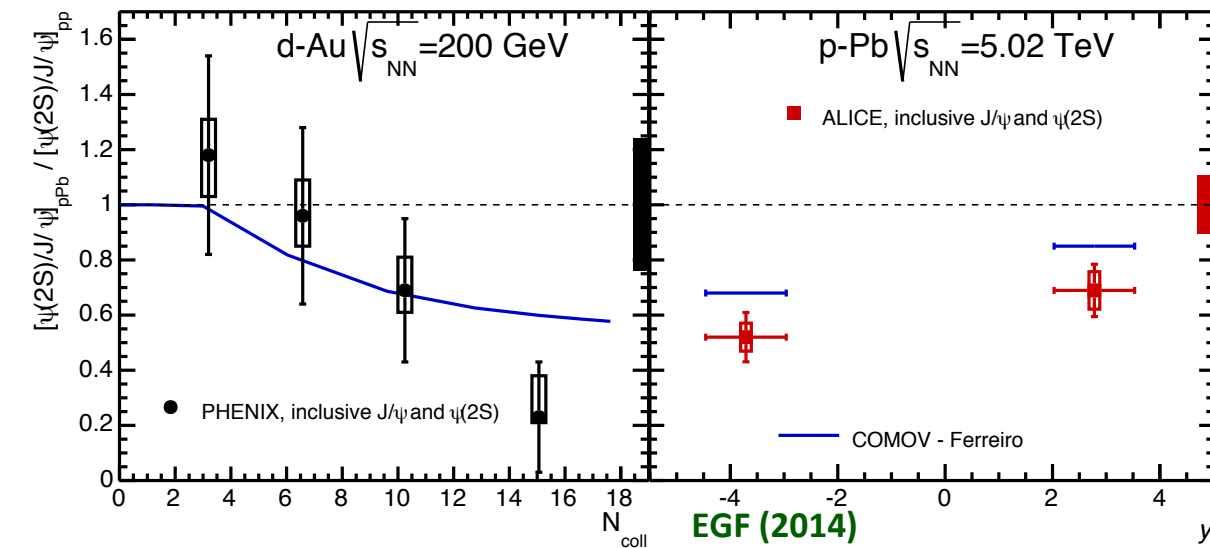
A natural explanation would be a final-state effect acting over sufficiently long time
 \Rightarrow interaction with a comoving medium?

Excited states: Comover interaction

- In a comover model: suppression from scatterings of the nascent ψ with comoving medium of partonic/hadronic origin Gavin, Vogt, Capella, Armesto, EGF, Tywoniuk...
- Stronger comover suppression where the comover densities are larger. For asymmetric collisions as proton-nucleus, **stronger in the nucleus-going direction**
- Rate equation governing the charmonium density:

$$\tau \frac{d\rho^\psi}{d\tau}(b, s, y) = -\sigma^{co-\psi} \rho^{co}(b, s, y) \rho^\psi(b, s, y)$$

$\sigma^{co-\psi}$ originally fitted from SPS data



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$$\tau \frac{d\rho^\psi}{d\tau}(b, s, y) = -\sigma^{co-\psi} \rho^{co}(b, s, y) \rho^\psi(b, s, y)$$
- $\sigma^{co-\psi}$

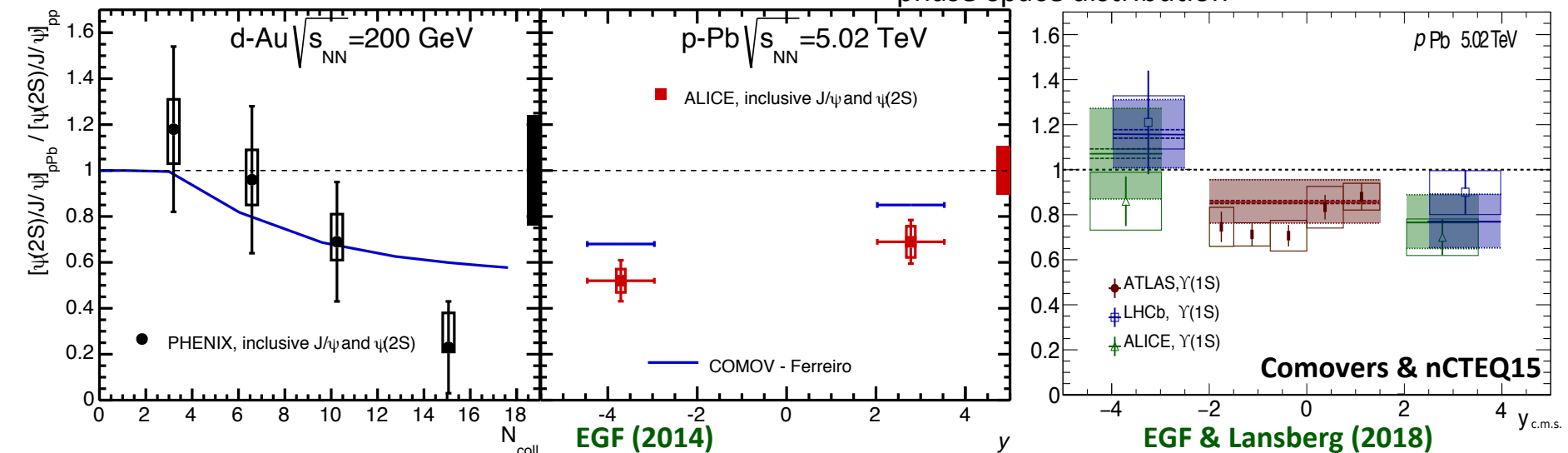
originally fitted from SPS data

$$\sigma^{co-Q_{b\bar{b}}} = \sigma_{\text{geom}} \left(1 - \frac{E_{\text{Binding}}}{\langle E_{co} \rangle}\right)^n$$

New: $\sigma^{co-\psi}$ can be parametrized: n & T_{eff}

averaged over comover phase-space distribution

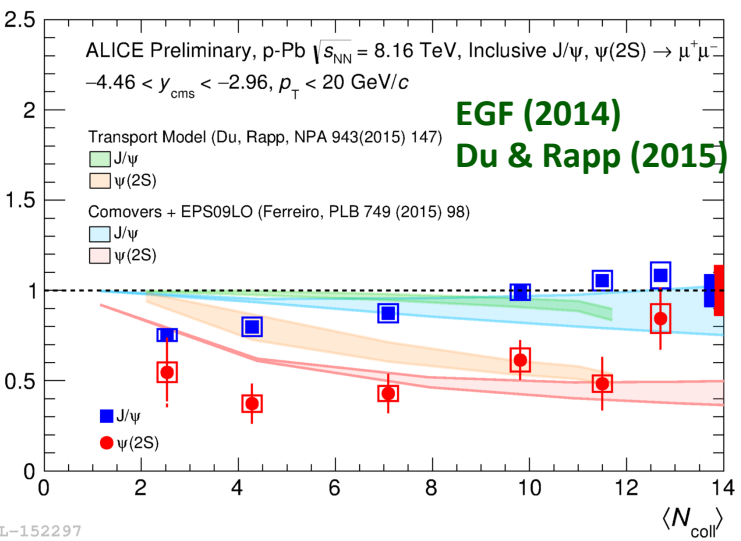
$1/(e^{E_{co}/T_{\text{eff}}} - 1)$



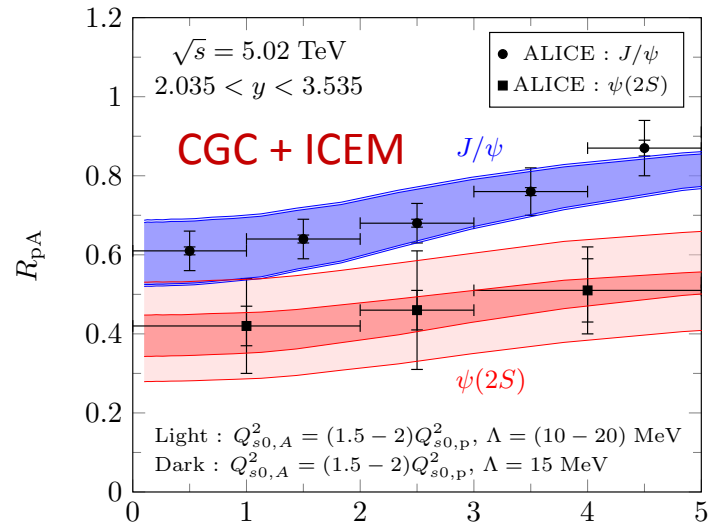
Excited states: Comover interaction

Transport model with final interactions
“similar in spirit to *comover* suppression”

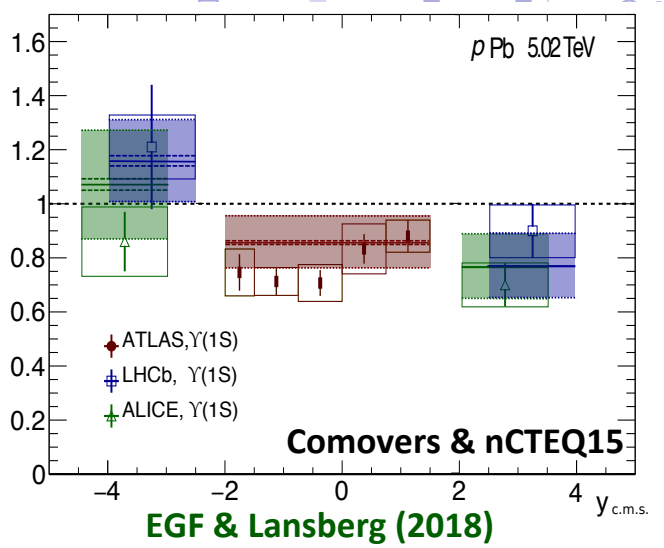
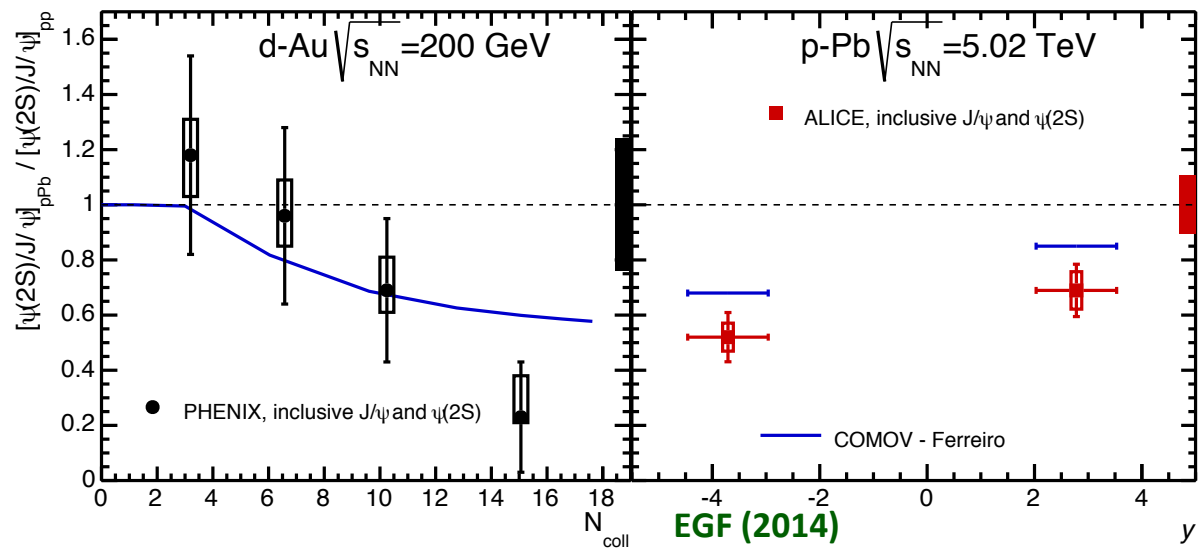
Soft color exchanges between cc & *co-movers* at later stage => effect on $\psi(2S)$



→ New results on $\psi(2S)$ confirm stronger suppression w.r.t. to J/ψ in the Pb-going direction.
→ Final state effects are needed to reproduce the $\psi(2S)$ suppression.
→ Still problems for a quantitative description of the data.



Ma, Venugopalan, Zhang, Watanabe (2018)

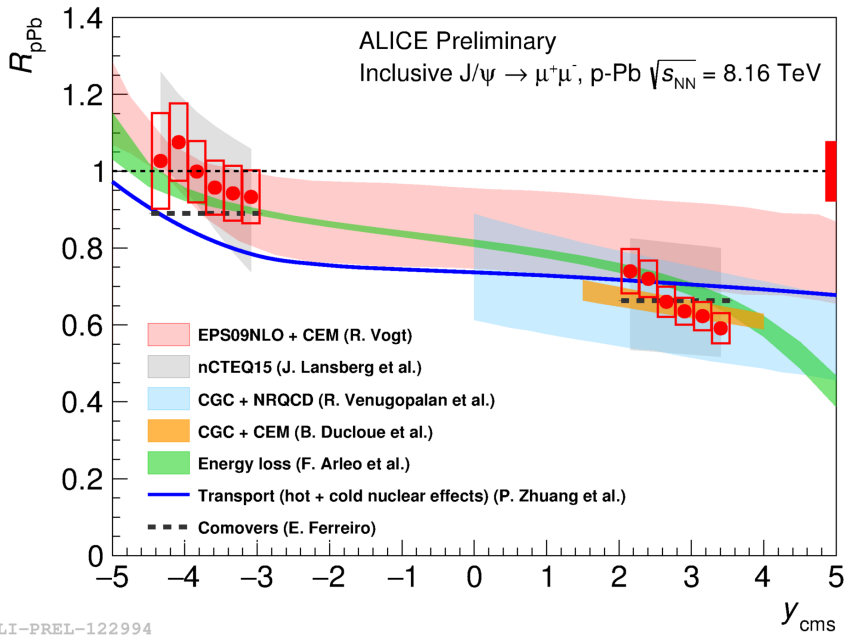
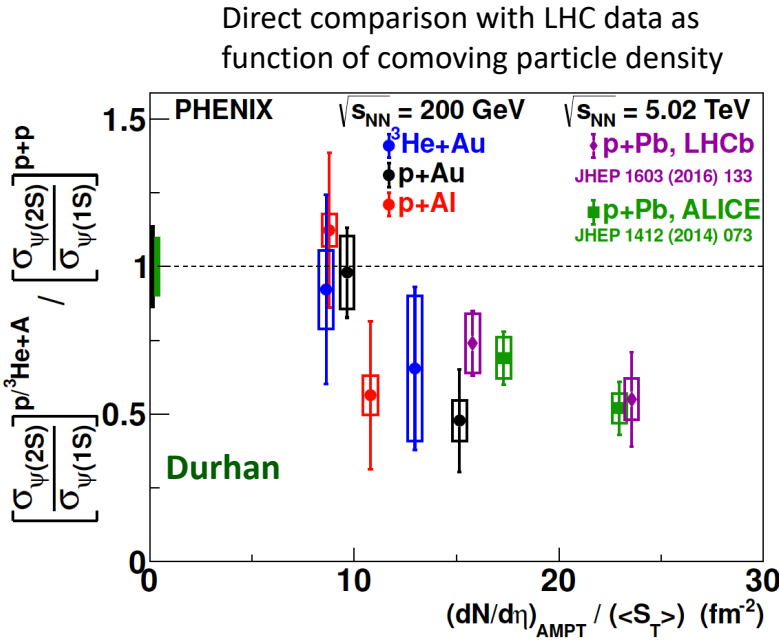


Some comments on proton-nucleus collisions

- Initial-state effects are required to explain pA data from RHIC and LHC
=> Modification of the gluon flux, either by modified nPDF or CGC, needs to be taken into account

Issues:

- Huge uncertainty of nPDFS
- Widespread CGC results
- Coherent Eloss mechanism can also reproduce ground state data



- Final-state effects as comover interaction, are good candidates to reproduce excited to ground state data EGF & Lansberg (2018)

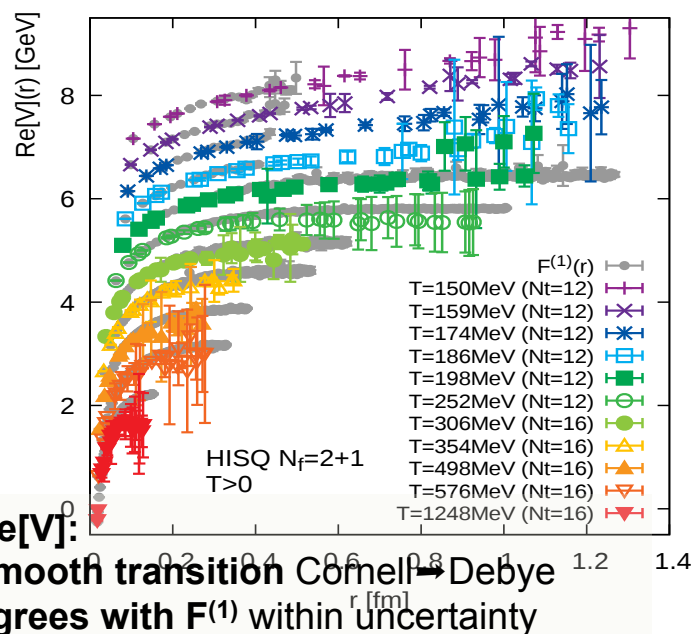
$p\text{Pb } 5.02 \text{ TeV}$	Comover model	CMS data $-1.93 < y < 1.93$
	$-1.93 < y < 1.93$	CMS data
$\Upsilon(2S)/\Upsilon(1S)$	0.91 ± 0.03	$0.83 \pm 0.05 \text{ (stat.)} \pm 0.05 \text{ (syst.)}$
$\Upsilon(3S)/\Upsilon(1S)$	0.72 ± 0.02	$0.71 \pm 0.08 \text{ (stat.)} \pm 0.09 \text{ (syst.)}$

Think bigger: quarkonium in nucleus-nucleus collisions

- Matsui and Satz: suppression of quarkonium as a signature of the QGP
Debye screened potential above the deconfinement temperature
- Time-independent notion of the melting process, **purely real model potentials**
Popular candidates: free energies $F^1(r)$ &/or internal energies $U^1(r)$ **Static**
- An essential step: heavy quark potential not only shows Debye screening but also features an **imaginary part** **Laine et al. (2007)**
Intuitive idea: **Re[V]** captures the screened $Q\bar{Q}$ interaction **Dynamic**
Im[V] captures dissociation by Landau damping & singlet \Leftrightarrow octet

Think bigger: quarkonium in nucleus-nucleus collisions

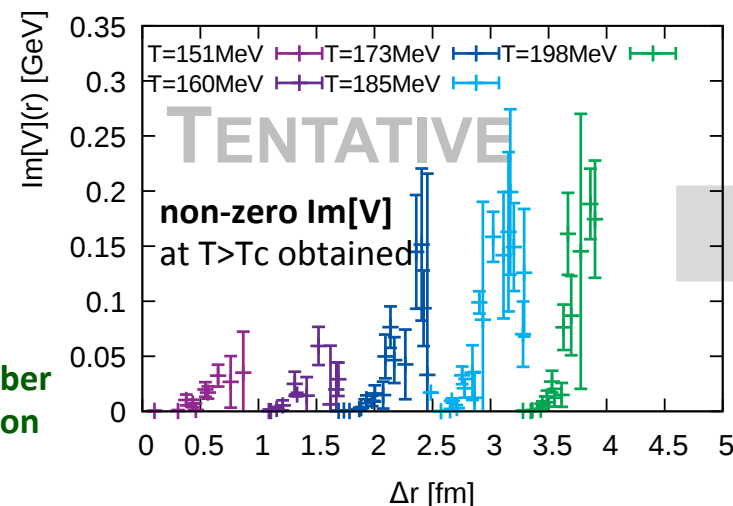
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Current efforts:

- lattice QCD calculation of complex in-medium HQ potential

Petreczky, Rothkopf, Weber
[TUM-QCD] in preparation



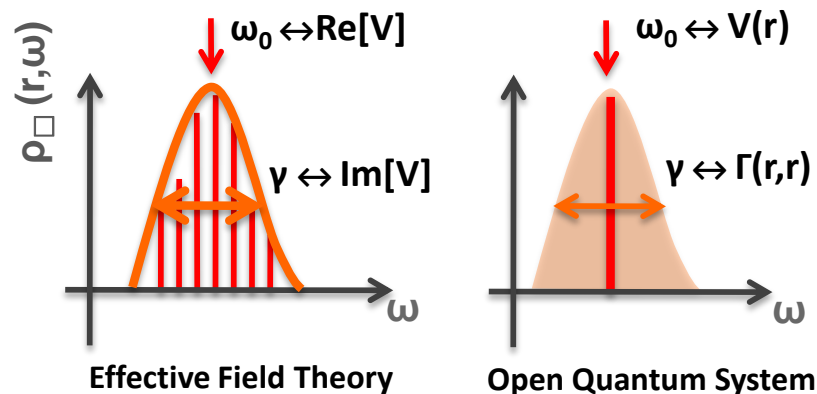
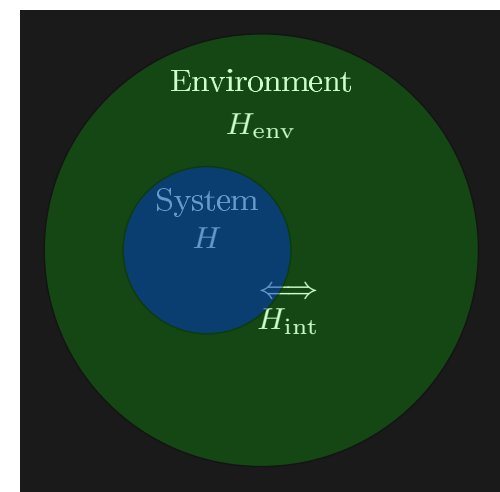
- understand the origin and physics implications of $\text{Im}[V]$

Thinking big: quarkonium in nucleus-nucleus collisions

- To formalize the idea of decoherence in the language of QM and to see how the imaginary part arises from the thermal fluctuations in the medium:

Theory of open quantum systems:

- solution of a stochastic Schrodinger equation
Asakawa& Rothkopf; Katz & Gossiaux,
Kajimoto, Akamatsu, Asakawa, Rothkopf
- computation of the evolution of the density matrix
Borghini, Dutta, Gombeaud;
Brambilla, Escobedo, Soto, Vairo;
Blaizot; De Boni



The real and imaginary parts of the in-medium HQ potential can be related to the stochastic evolution of the in-medium wave function which is perturbed by the thermal medium:

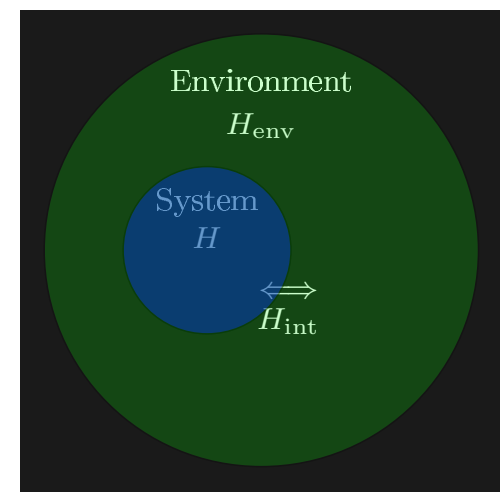
- Stochastic term = thermal noise
- $\text{Im}[V]$ related to the strength of the thermal noise

Thinking big: quarkonium in nucleus-nucleus collisions

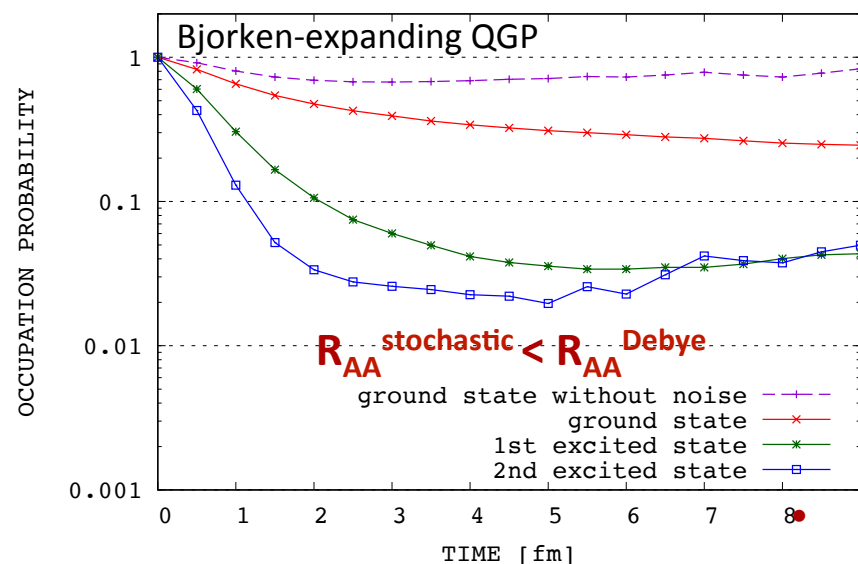
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CHARMONIUM



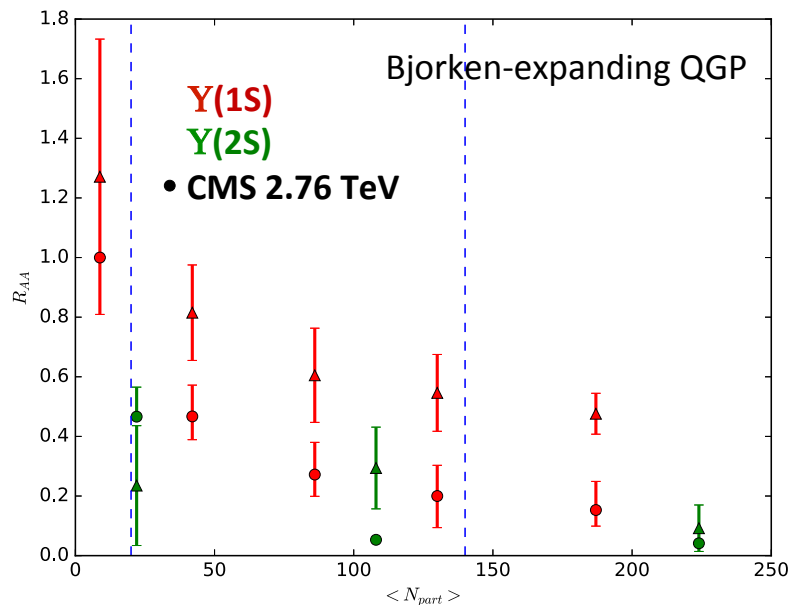
Kajimoto, Akamatsu, Asakawa, Rothkopf (2018)

The real and imaginary parts of the in-medium HQ potential can be related to the stochastic evolution of the in-medium wave function which is perturbed by the thermal medium:

- Stochastic term = thermal noise
- $\text{Im}[V]$ related to the strength of the thermal noise

Noise provides a dynamical dissociation mechanism

Recent developments on open quantum systems for quarkonia



Time evolution of HQ states in an expanding hot QCD medium by implementing EFT –pNRQCD- in the framework of open quantum systems

=> **Lindblad equation**

- non-Abelian nature of QCD: color transitions
- conserves the total number of heavy quarks
- avoids classical approximations

Brambilla, Escobedo, Soto & Vairo (2017)

In the same line: equations for the time evolution of the HQ reduced-density matrix in a non-Abelian QGP

Blaizot & Escobedo (2017)

- treat the relative motion of the heavy quarks semi-classically
- take into account the color transitions within 2 strategies:
 - instantaneously, perturbation theory => **Langevin equation**, analogous to QED
 - as collisions => **Boltzmann equation**

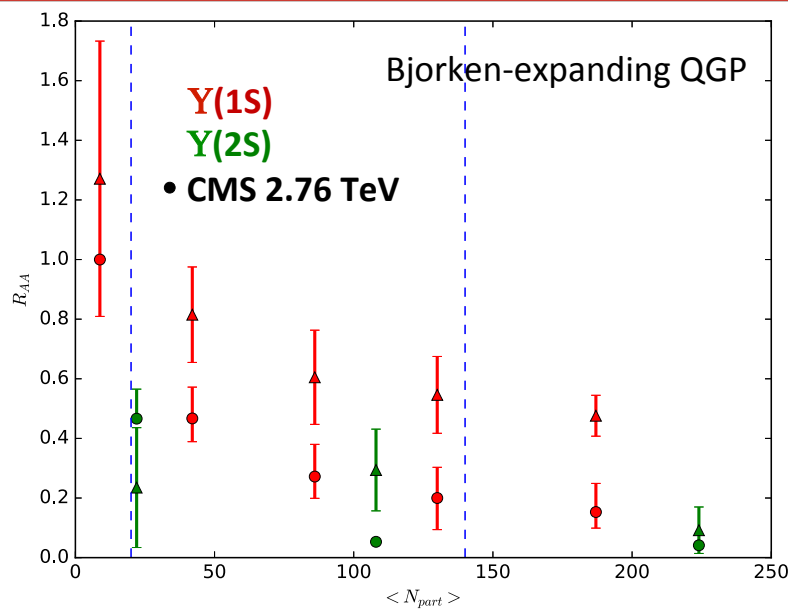
De Boni (2017)

Also: **Schrödinger-Langevin equation**

Gossiaux & Katz (2016)

- interesting framework but not derived from first QCD principles
- QCD features enter in the parameters (similarly to Langevin dynamics in HF physics)

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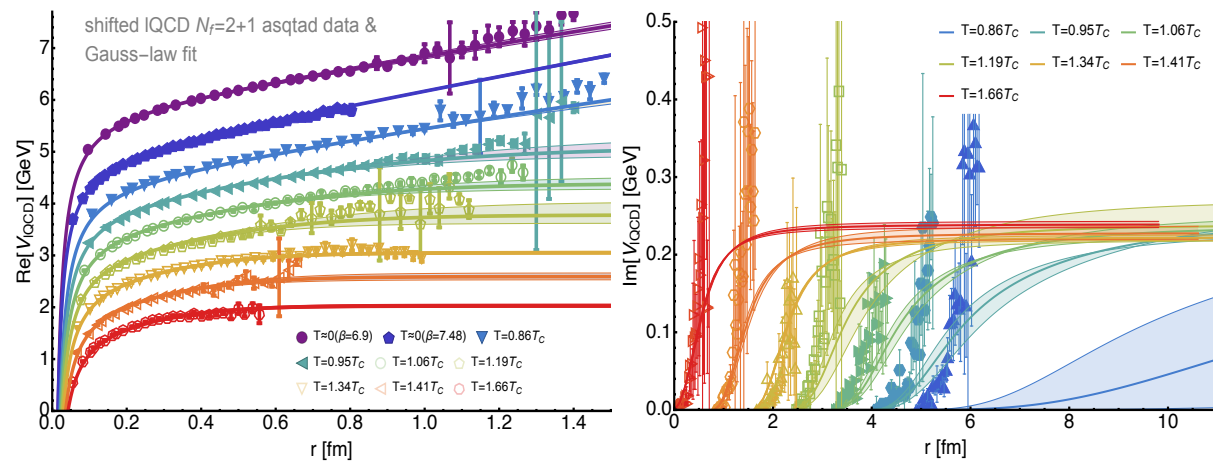
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- QCD features enter in the parameters (similarly to Langevin dynamics in HF physics)

Master equation with time evolution of the HQ states

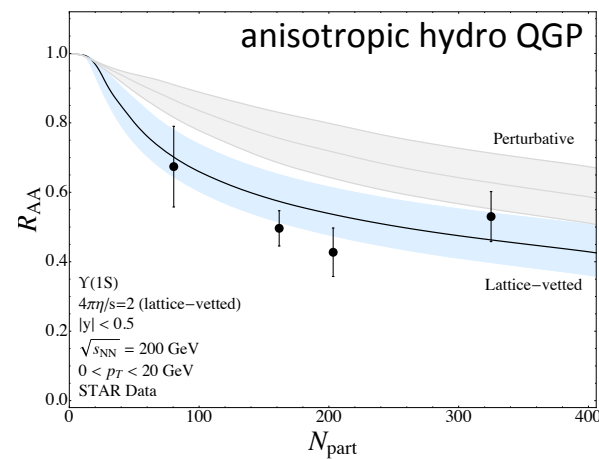
Recent developments on phenomenology for quarkonia

Anisotropic QGP with lattice potential

- lattice QCD vetted HQ potential: complex values at high T
- Y states more easily dissociated



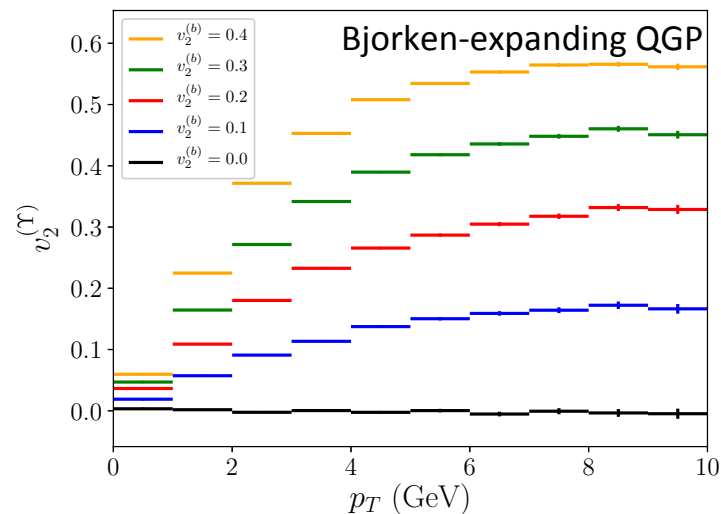
Krouppa, Strickland, Rothkopf (2018)



Dynamical in-medium transport model:

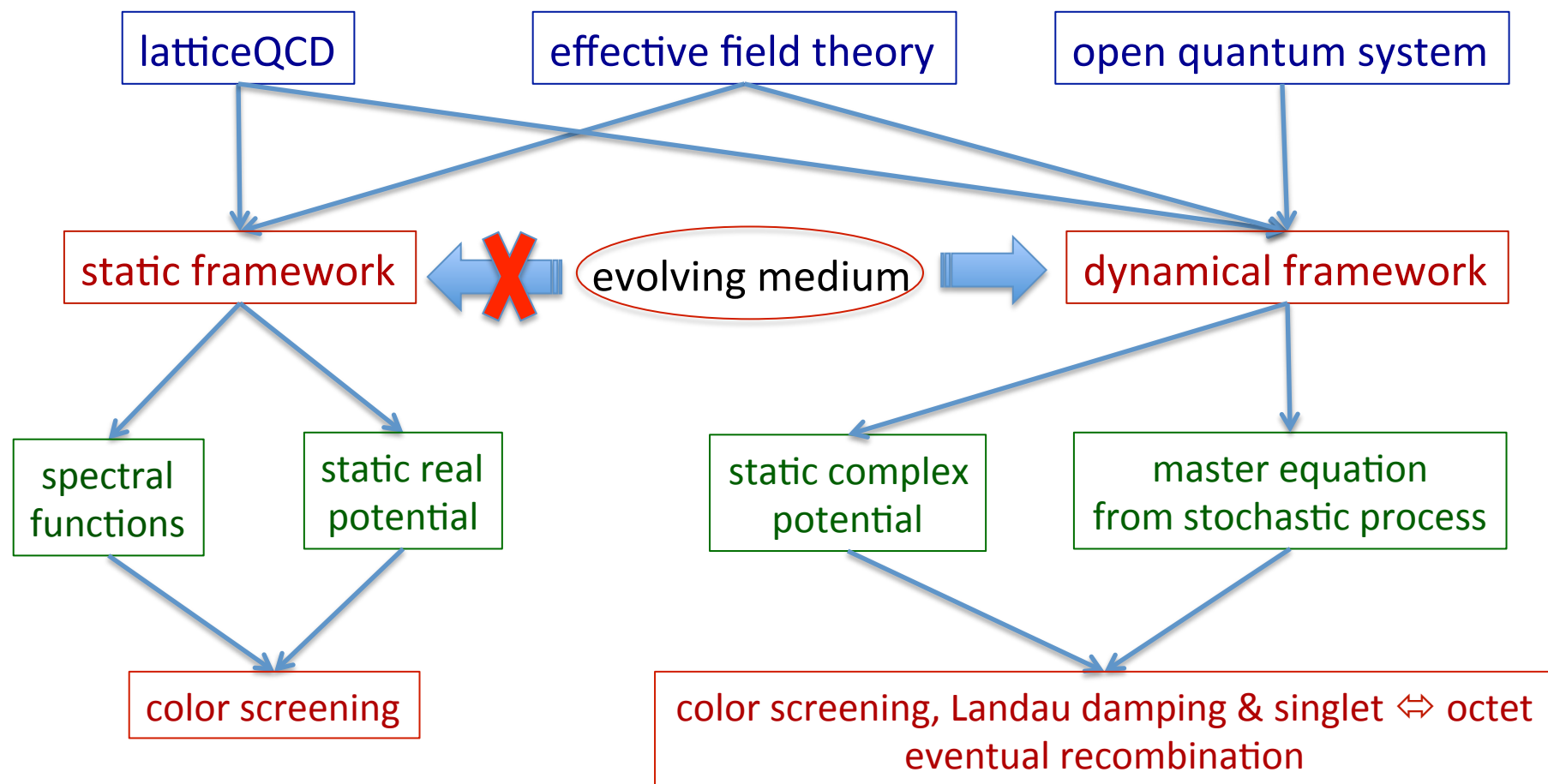
- pNRQCD in a thermal QGP
- Stochastic Boltzmann equations
- HQ diffusion in the medium: necessary for the system to reach equilibrium

Yao & Muller (2018)



Summarizing: theory elements on quarkonia in a QGP

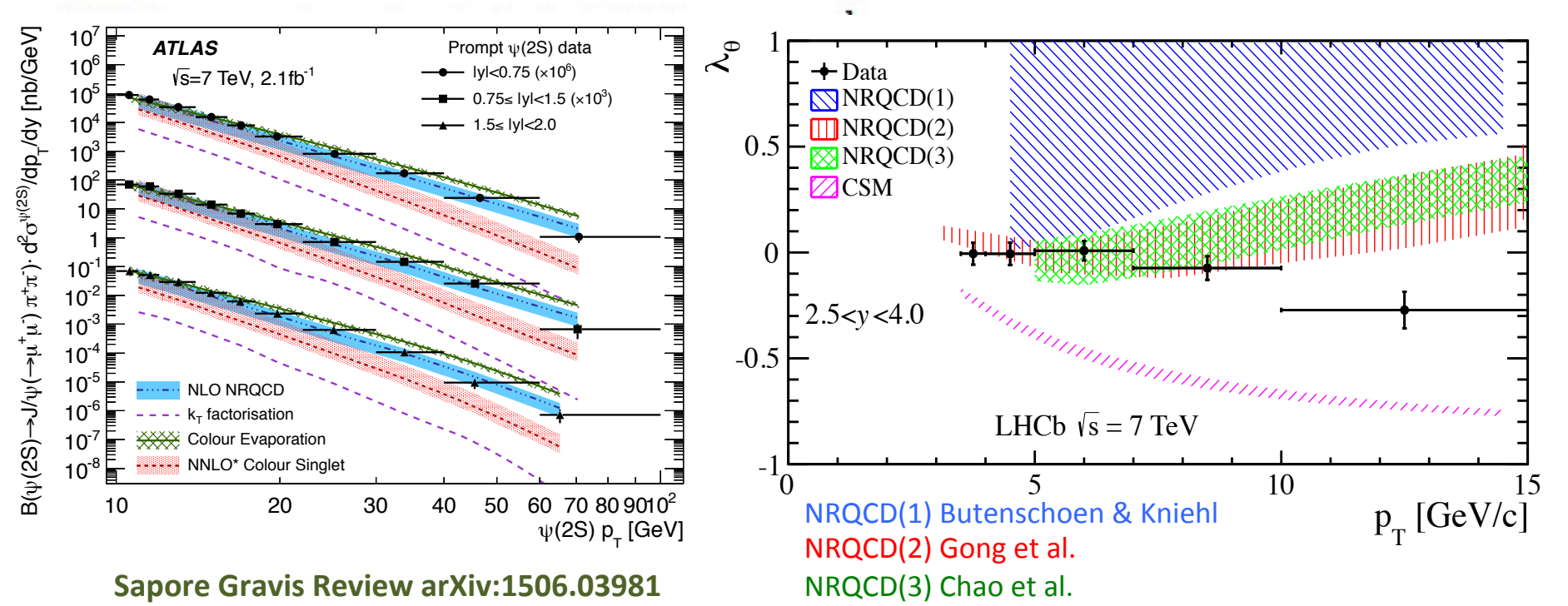
Caveat I: we need firm theoretical understanding of quarkonium production in pp collisions



Caveat II: how to extrapolate **pA** effects –initial & **final**- to AA? Factorization?
If yes... nature of the medium in pA?

BACKUP PROTON-PROTON

Production model: state of the art for the $\psi(2S)$



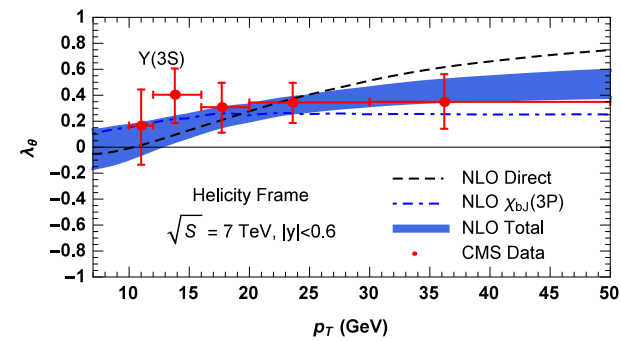
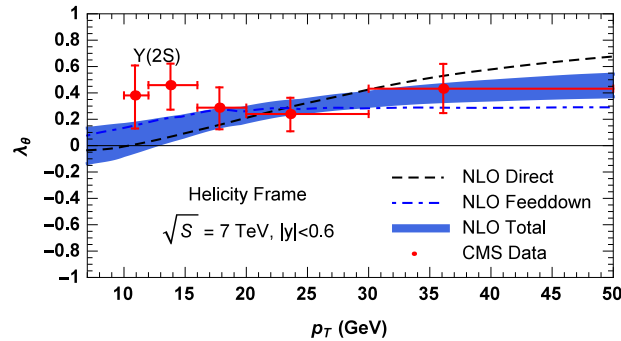
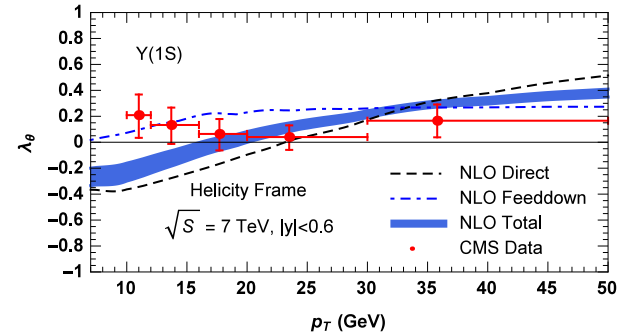
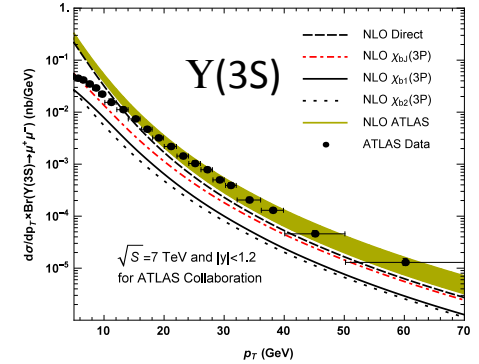
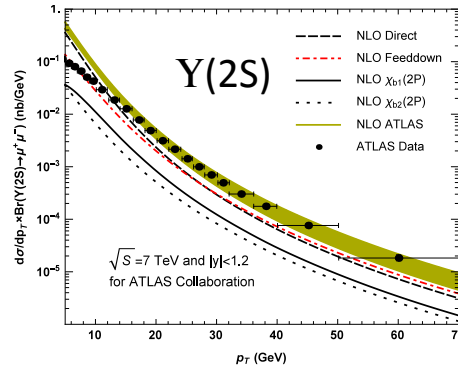
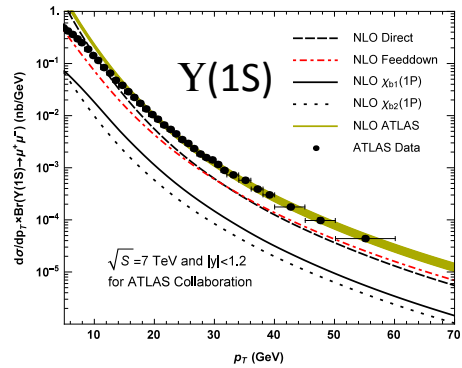
At low and mid p_T –region where quarkonium heavy-ion studies are mainly carried out– none of the models can simply be ruled out due to theoretical uncertainties (heavy-quark mass, scales, non-perturbative parameters, unknown QCD and relativistic corrections, ...)

- New recent developments on may be helpful:
- CEM improved
 - CGC meets NRQCD

Production model: state of the art for the Y

- Larger mass, higher scale and slower velocity could make Y a better candidate for NRQCD

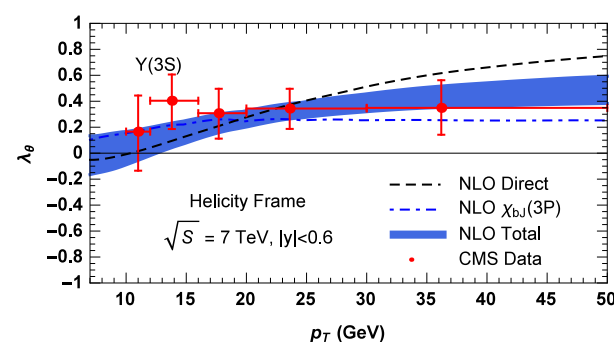
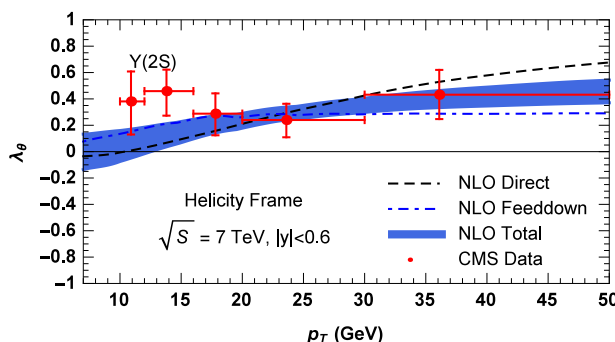
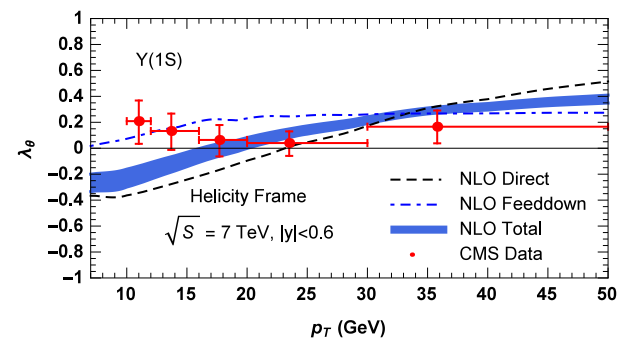
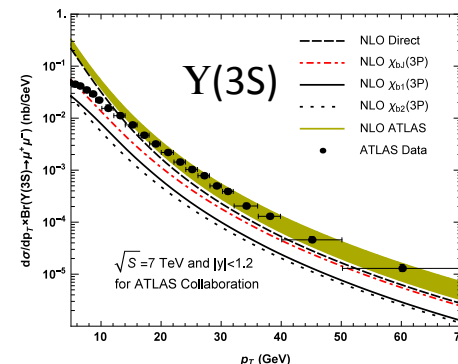
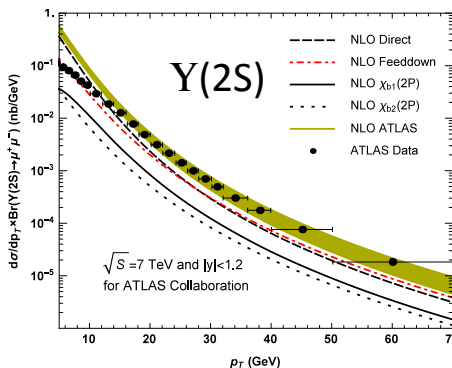
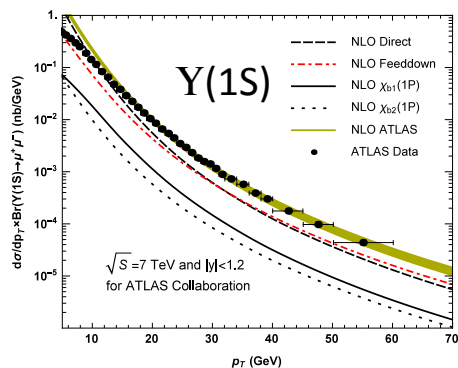
Hang et al.



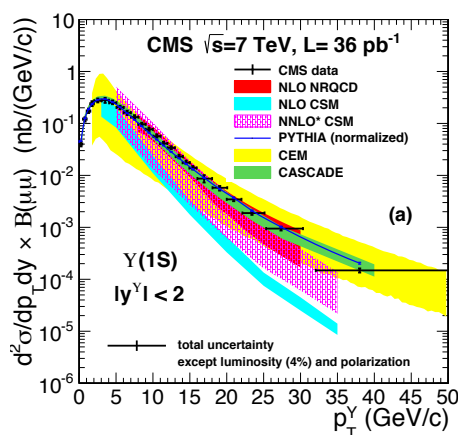
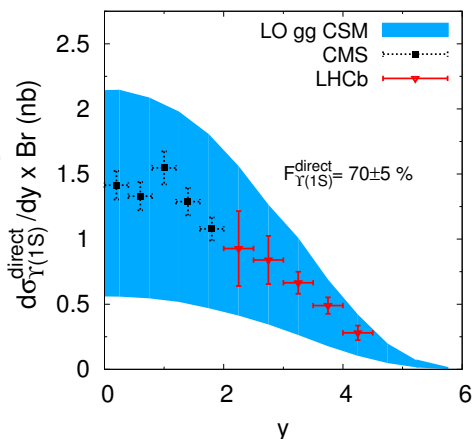
Production model: state of the art for the Υ

- Larger mass, higher scale and slower velocity could make Υ a better candidate for NRQCD

Hang et al.



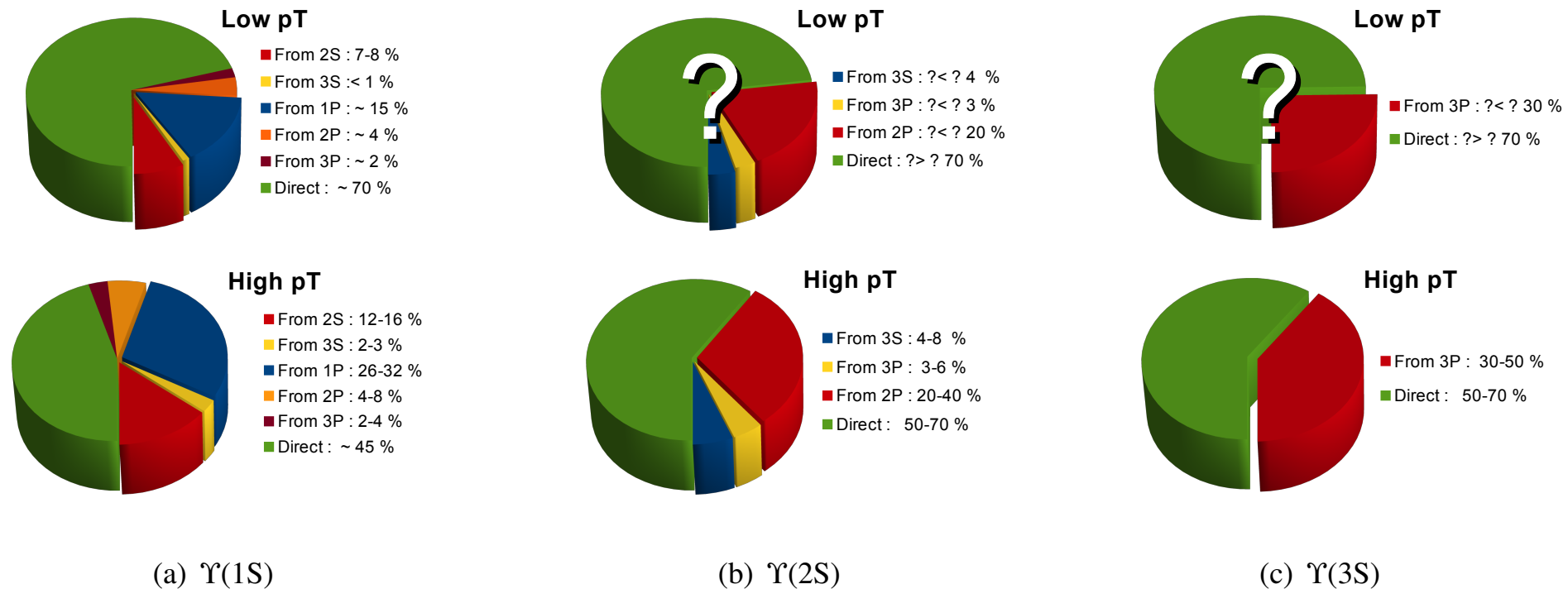
Lansberg



- None of the models can simply be ruled out due to their theoretical uncertainties
- In general, LHC data are much more precise than theory
- Caveat:** Important feeddown contributions -6 states- to be taken into account for interpretations of their possible sequential suppression

News from feed-down

Feed-down structure at low p_T -where quarkonium heavy-ion measurements are mostly carried out- is quite different than that commonly accepted ten years ago based on the CDF measurement, with a $p_T > 8$ GeV



Sapore Gravis Review arXiv:1506.03981 from LHCb data

This information is fundamental to use bottomonia as probes of QGP, especially for the interpretation of their possible sequential suppression

BACKUP PROTON-NUCLEUS

Baseline: nPDFs & nuclear absorption in a collinear pQCD framework

- Parton densities in nuclei are modified

Nuclear PDF assumed to be factorizable in terms of the nucleon PDFs :

$$\mathcal{F}_g^A(x_1, \mu_f) = g(x_1; \mu_f) \times R_g^A(x, \mu_f)$$

In presence of nuclear effects: $R_g^A(x, \mu_f) \neq 1$

- Mesons may scatter inelastically with nucleons in the nuclear matter

Survival probability for a $Q\bar{Q}$ to pass through the target unscathed:

$$S_A(\vec{r}_A, z_A) = \exp \left(-A \sigma_{\text{break-up}} \int_{z_A}^{\infty} d\tilde{z} \rho_A(\vec{r}_A, \tilde{z}) \right)$$

- Any differential cross section can then be obtained from the partonic one:

$$\frac{d\sigma_{pA \rightarrow QX}}{dy dP_T d\vec{b}} = \int dx_1 dx_2 g(x_1, \mu_f) \int dz_A \mathcal{F}_g^A(x_2, \vec{b}, z_B, \mu_f) \mathcal{J} \frac{d\sigma_{gg \rightarrow Q+g}}{d\hat{t}} S_A(\vec{b}, z_A)$$

From any model (CSM, COM, CEM)

Nuclear absorption: Generalities on the break-up cross section

The **bound states** may be destroyed by inelastic scatterings with nucleons if they are formed in the nuclear medium. One expects

$$\sigma_{\text{break-up}} \propto r_{\text{meson}}^2$$

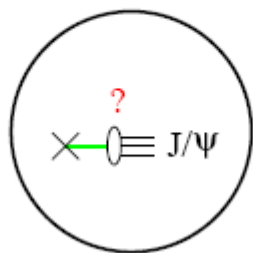
- In order to interact with nuclear matter => $t_f \leq R$

- In the meson rest frame: $\tau_f = \frac{2M_{c\bar{c}}}{(M_{2S}^2 - M_{1S}^2)} \approx 0.3 \div 0.4 \text{ fm}$

- t_f has to be considered in the rest frame of the target nucleus => $t_f = \gamma \tau_f$

Low energy: $t_f = \gamma(x_2) \tau_f \ll R$

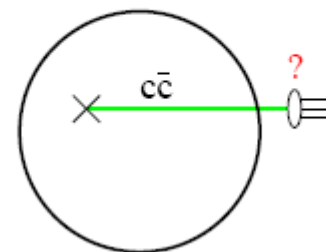
High energy: $t_f = \gamma(x_2) \tau_f \gg R$



Formation time depends on the boost

$$\gamma = \cosh(y - y_{\text{beam}}^A) \Rightarrow \text{At } y=0:$$

$$\gamma_{\text{RHIC}}=107 \text{ and } \gamma_{\text{LHC}}=2660$$



It takes $t_f=30 \text{ fm}/c$ at RHIC and $t_f=800\text{-}1000 \text{ fm}/c$ at LHC for a quarkonium to form and to become distinguishable from its excited states

$$t_f \gg R$$

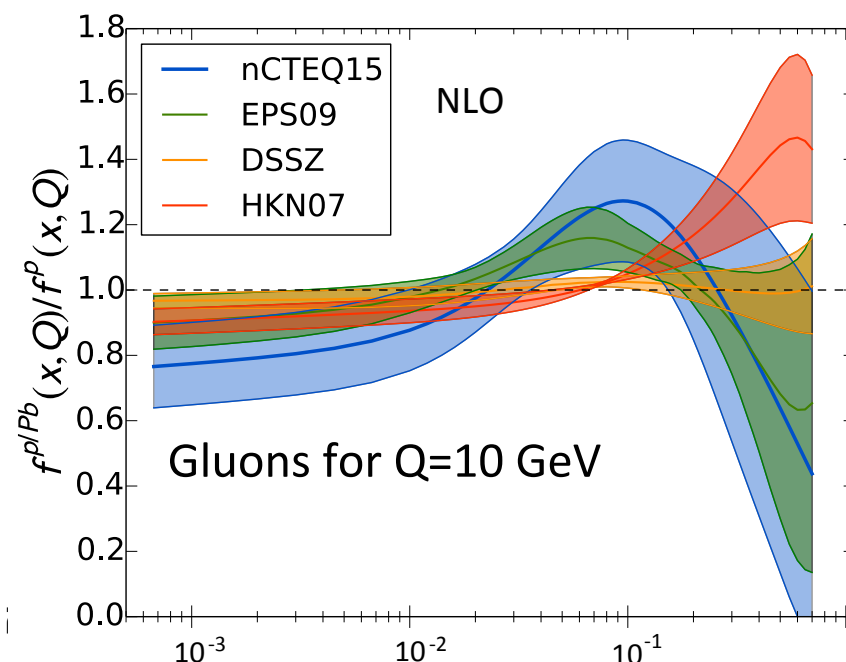
Consensus: $\sigma_{\text{break-up}}$ is getting small at high energies and may be the same for ground and excited states

Typical gluon nuclear PDFs

There are several nPDF sets available (using various data, LO/NLO, etc)

Typical gluon nPDFs: 4 regions

- $x \leq 10^{-2}$: shadowing
- $x \approx 10^{-1}$: anti-shadowing
- $0.3 \leq x \leq 0.7$: EMC effect
- $x \geq 0.7$: Fermi motion

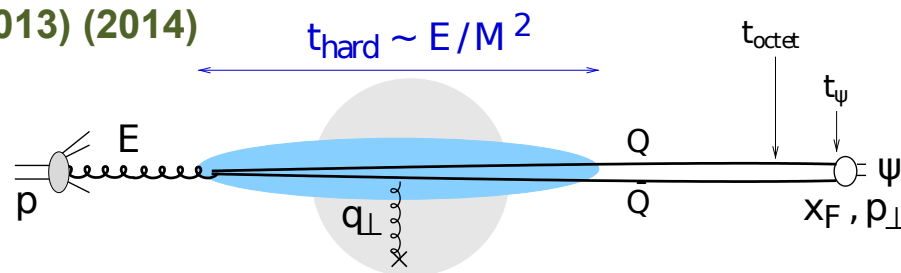


- For the gluons, only the **shadowing** depletion is established although its magnitude is still discussed
- The gluon **antishadowing** not yet observed although used in many studies; absent in some nPDF fits
- The gluon **EMC effect** is even less known, hence the uncertainty there

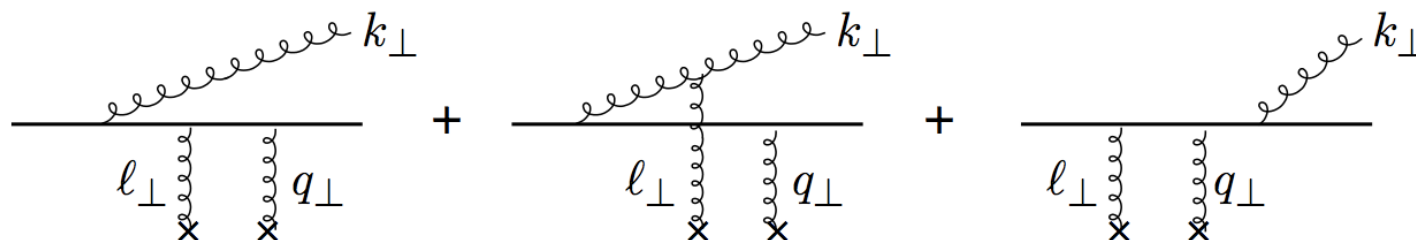
Going further: Coherent energy loss

Arleo, Kolevatov, Peigné, Rustamova (2012) (2013) (2014)

This approach is based on the fact that for large formation times all scattering centers in the medium act coherently.



- Coherent radiation (interference) in the initial/final state crucial for $t_f \gg R$



IS and FS radiation cancels out in the induced spectrum

Interference terms does not cancel in the induced spectrum!

- Leads to a behaviour $\Delta E \propto E$

$$\Delta E = \int d\omega \omega \frac{dI}{d\omega} \Big|_{\text{ind}} = N_c \alpha_s \frac{\sqrt{\Delta q_{\perp}^2}}{m_T} E$$

- $\sqrt{\Delta q_{\perp}^2}$ related to the transport coefficient \hat{q}

- \hat{q} related to the saturation scale by

$$Q_s^2(x, L) = \hat{q}(x) L$$

$$\hat{q}(x) \simeq \hat{q}_0 \left(\frac{10^{-2}}{x} \right)^{0.3}$$

\hat{q}_0 is the only fitted parameter of the approach+the option to switch on/off the shadowing

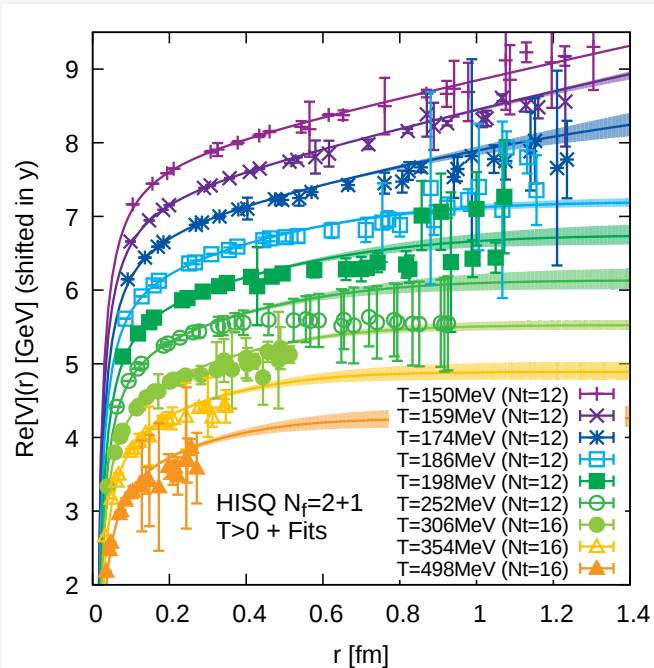
BACKUP NUCLEUS-NUCLEUS

In-medium Quarkonium properties from first principles

Realistic **lattice QCD**
calculation of the complex in-
medium **heavy quark potential**

P. Petreczky, A. Rothkopf, J. Weber
[TUM-QCD] in preparation

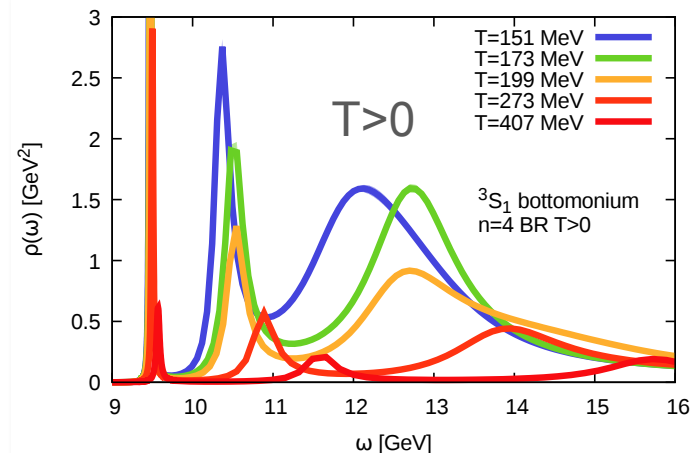
Re[V]:
smooth transition Cornell→**Debye**
agrees with $F^{(1)}$ within uncertainty



non-zero Im[V] at $T > T_c$ obtained

In-medium quarkonium **spectral properties** from
a lattice **effective field theory (NRQCD)**

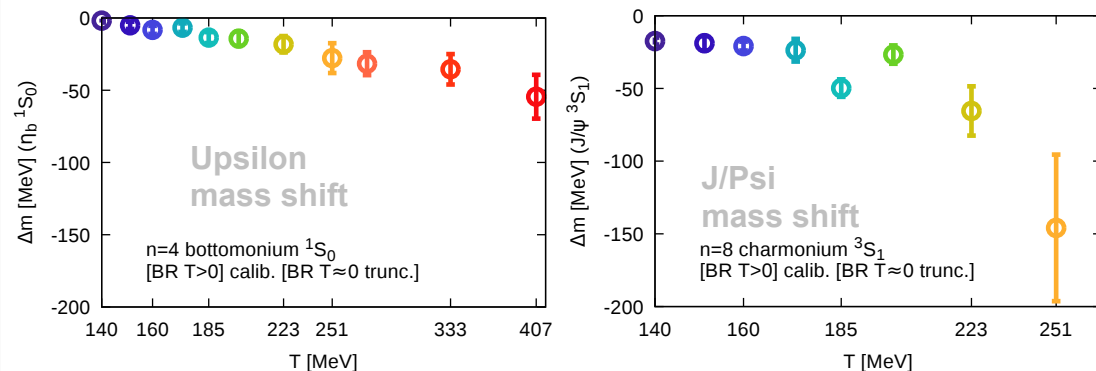
Improved spectral function extraction **algorithm**,
higher statistics, **larger temperature range**



S. Kim, P. Petreczky,
A. Rothkopf,
in preparation

more accurate
melting
temperatures

Heavy $Q\bar{Q}$ becomes **lighter** before melting

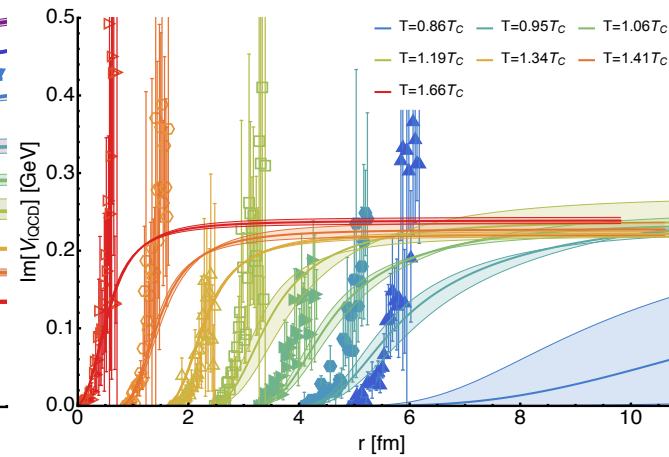
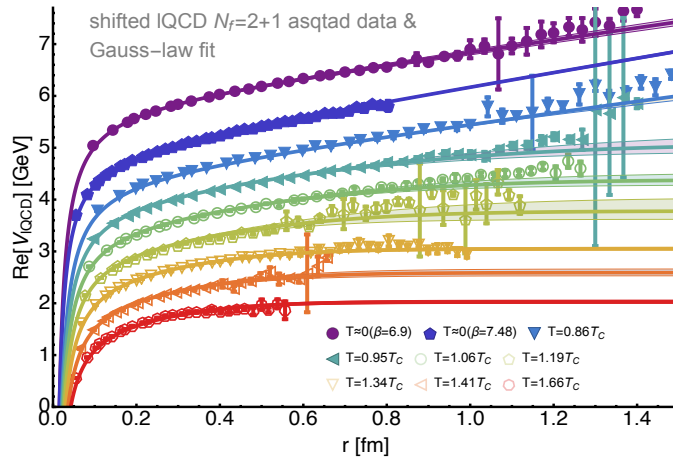


$\Delta m < 0$ consistent with potential based results

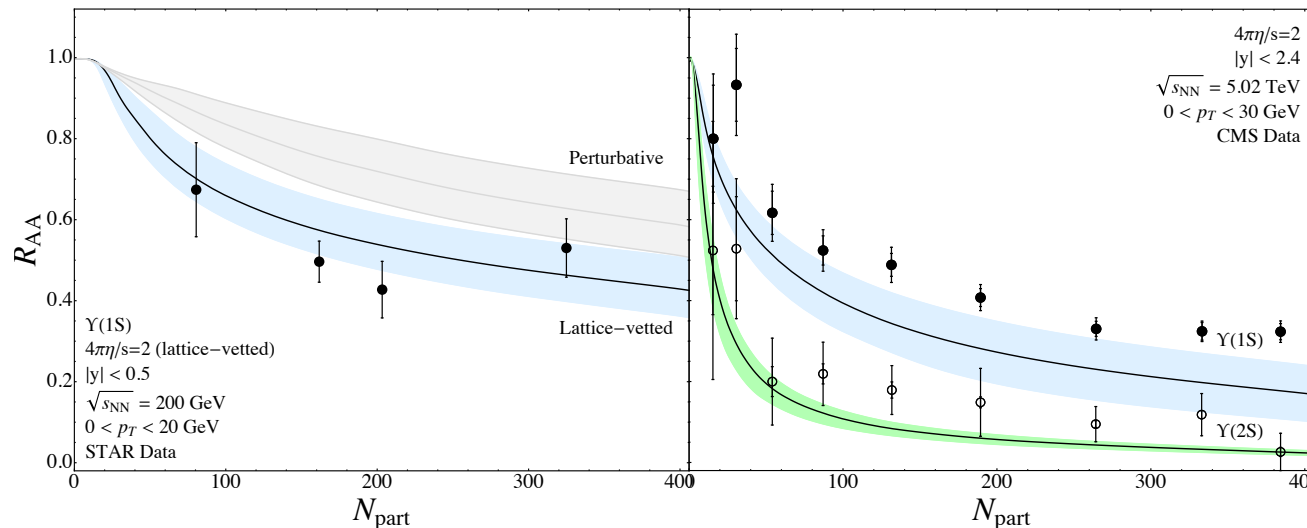
Pheno: Υ suppression in anisotropic QGP with lattice potential

- lattice QCD vetted in-medium heavy-quark potential with anisotropic hydro QGP
- in-medium potential: complex values at high temperatures
- discrete values of the potential obtained from lattice QCD

Krouppa, Strickland, Rothkopf (2018)



- a single T -dependent parameter remains, the Debye mass m_D

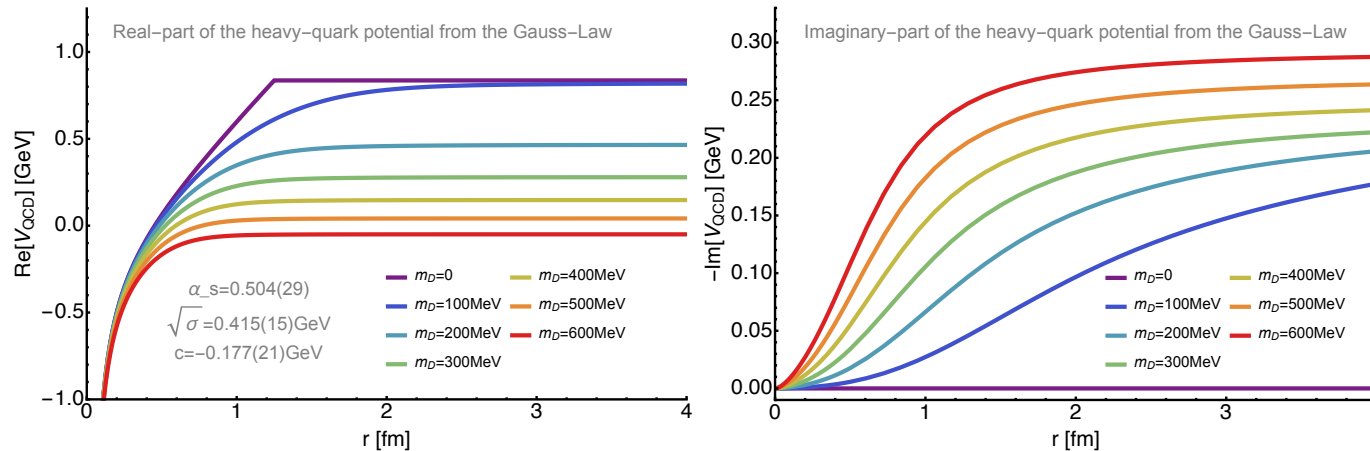


- feed down taken into account
- stronger imaginary part present in the lattice-vetted potential \Rightarrow Υ states more easily dissociated
- space for recombination?

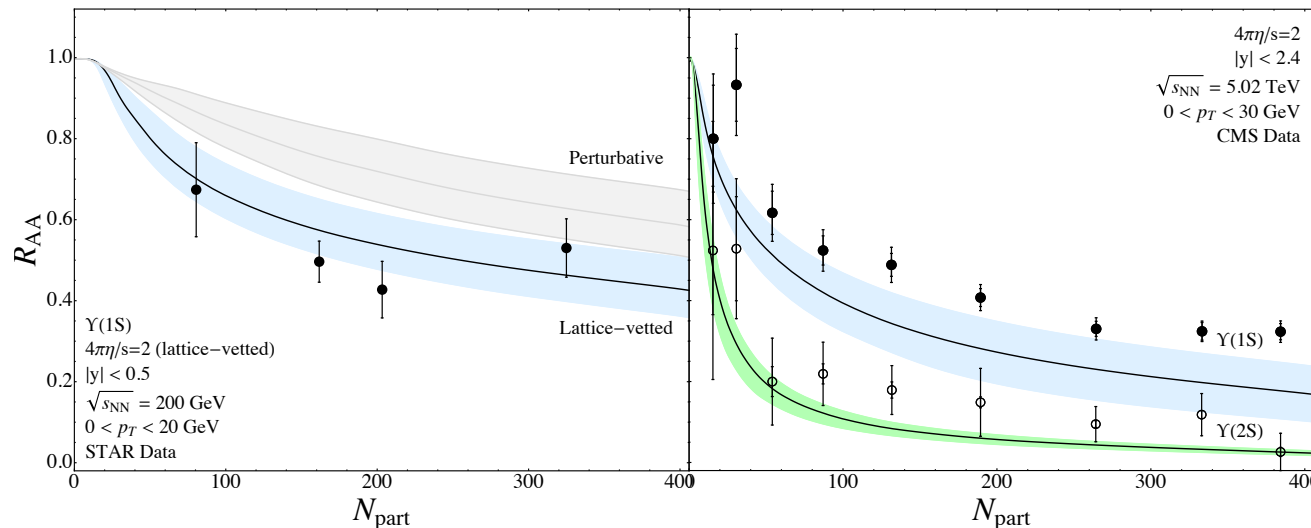
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- in-medium potential: complex values at high temperatures
- discrete values of the potential obtained from lattice QCD

Krouppa, Strickland, Rothkopf (2018)



- a single T-dependent parameter remains, the Debye mass m_D

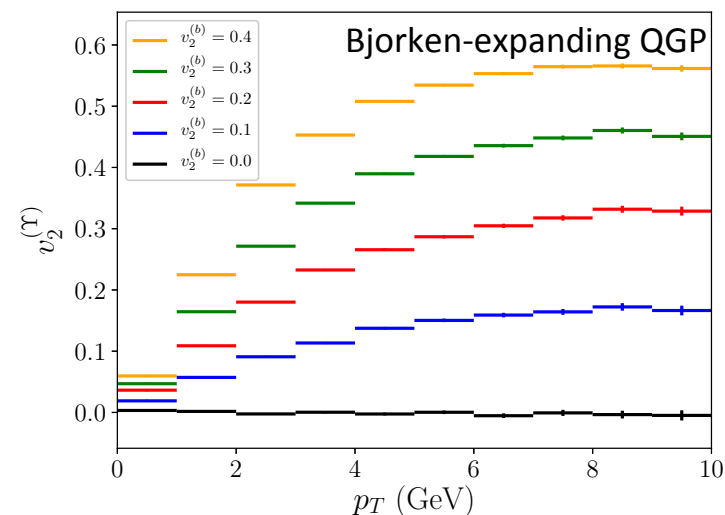


- feed down taken into account
- stronger imaginary part present in the lattice-vetted potential => Υ states more easily dissociated
- space for recombination?

Phenomenology: recent developments

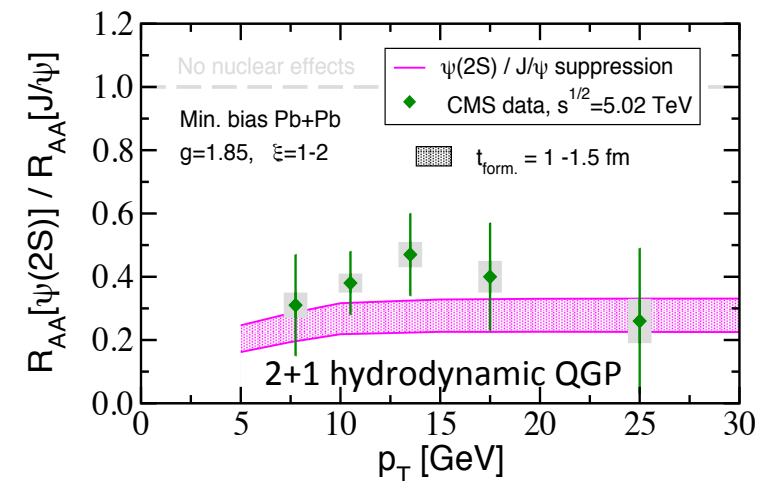
Dynamical in-medium transport model:

- pNRQCD in a thermal QGP
- Stochastic Boltzmann equations
- HQ diffusion in the medium: necessary for the system to reach equilibrium
- Predicts v_2 from recombination **Yao & Muller (2018)**



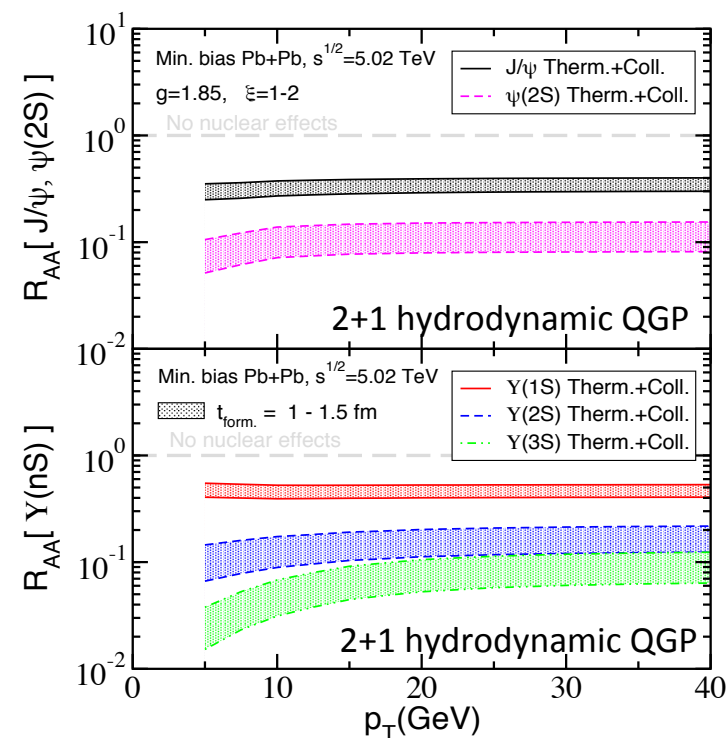
Collisional and thermal dissociation at high p_T :

- Collisional dissociation by p_T broadening
- Debye screening, no $\text{Im}[V]$ **Vitev & Sharma (2017)**



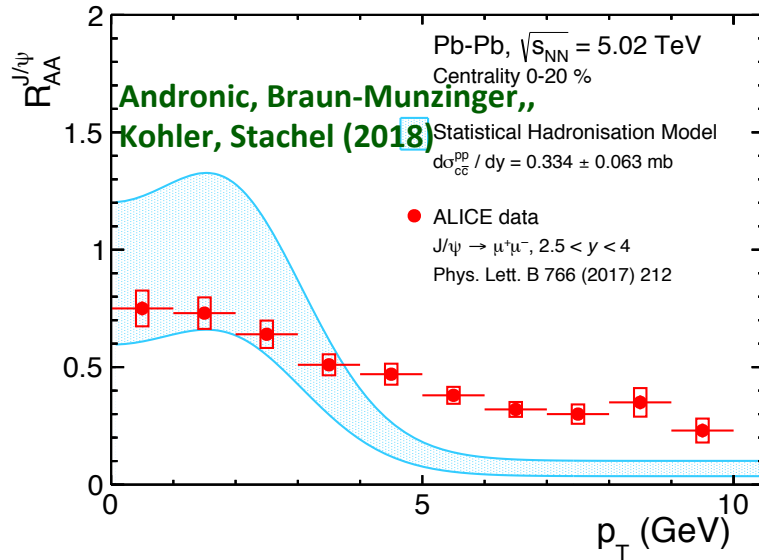
Quarkonium
formation time
 ~ 1 fm

NRQCD for
nucleon-nucleon
baseline

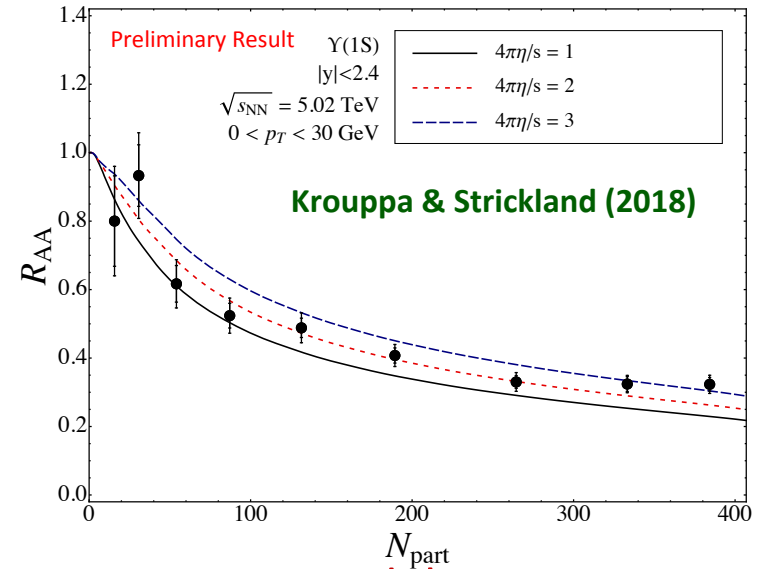


Recent results from some long-lasting phenomenology models

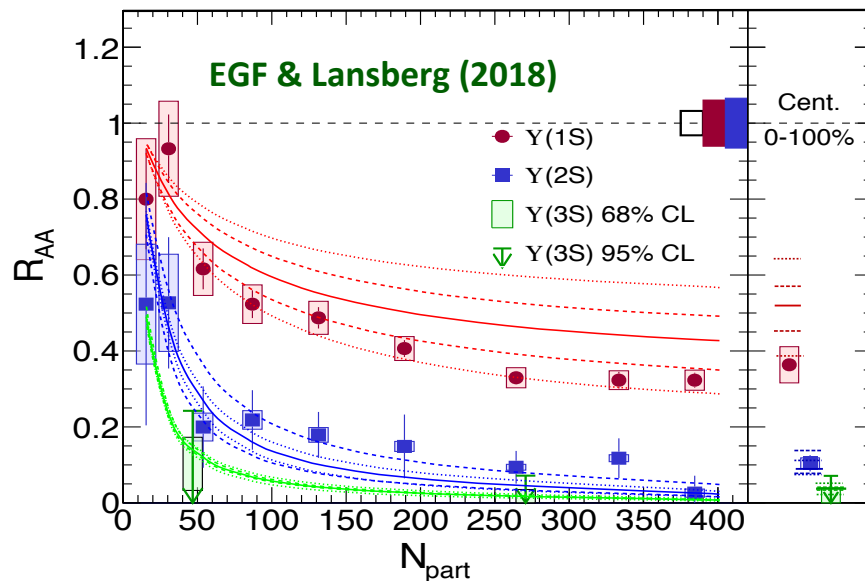
Statistical hadronisation model



a-hydro model



Comover model



Transport model

