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# Propagation of information in turning flocks of starlings

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# Flocks of starlings vs Physics

Typical flocking model:

attraction, repulsion, alignment

e.g. Vicsek et al.  
1995



$$\vec{v}_i(t+1) = \vec{v}_i(t) + J \sum_{k \in i} \vec{v}_k(t) + \vec{\xi}_i$$

Langevin equation:

$$\frac{d\vec{v}_i}{dt} = -\frac{\partial H}{\partial \vec{v}_i} + \vec{\xi}_i$$

$$H = -J \sum_{\langle ij \rangle} \vec{v}_i(t) \cdot \vec{v}_j(t)$$

Heisenberg  
ferromagnet

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Heisenberg  
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## EMPIRICAL RESULTS ?

The first set of large-scale data on 3D animal aggregations:

**2008: Rome group** up to **2700 starlings** in the field

3D positions  $\mathbf{r}_i$  and velocities  $\mathbf{v}_i$  of all birds in a compact flock  
at *one moment of time* are obtained using stereoscopy



Static properties

**Dynamics?**

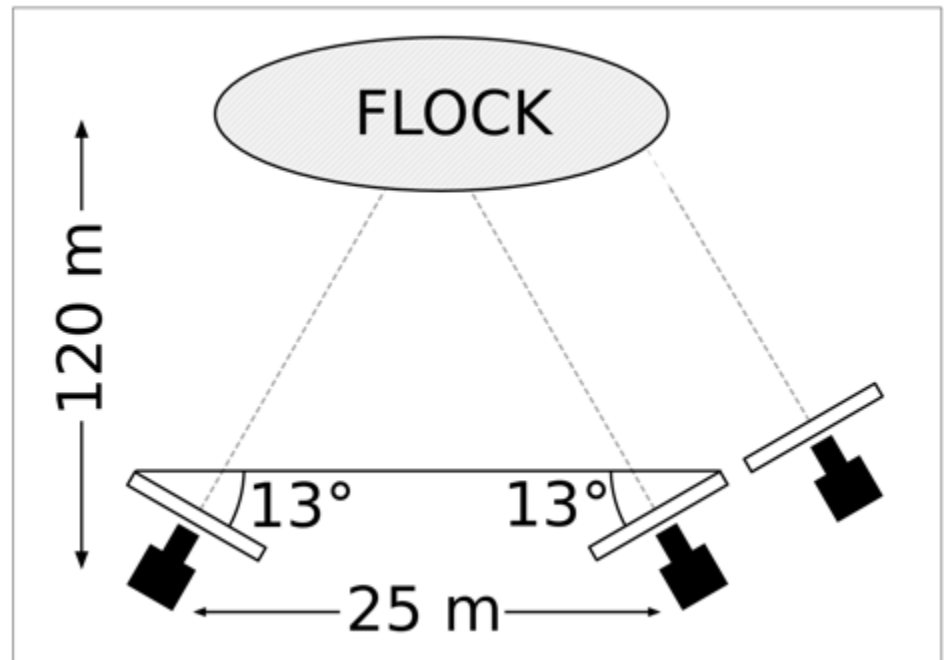
Synchronized and rapid changes  
of direction of the whole group?



# Experiments

- Natural flocks of starlings making turns above a roosting place in Rome
- Experiments are performed using **stereo photography** with three different view points

## Experimental setup



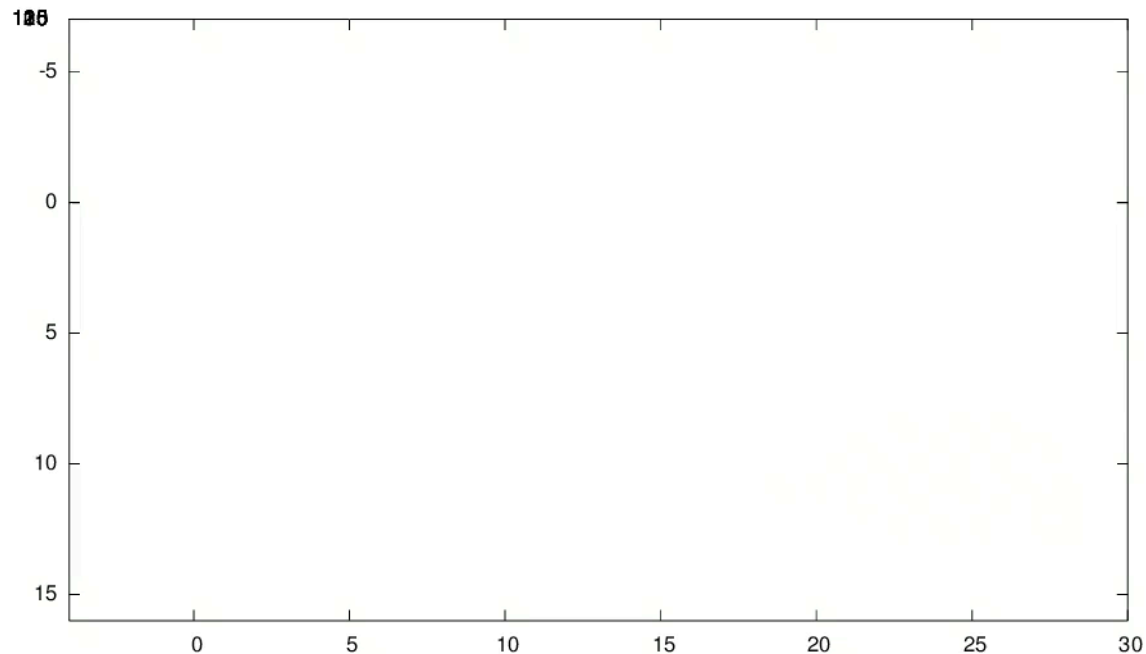
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## 3D trajectories of collective turns

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- 12 turning flocks of 50 to 600 starlings above a roosting place in Rome
- 3D trajectories of **individual** birds for the **entire duration** of a turning event (>5s)

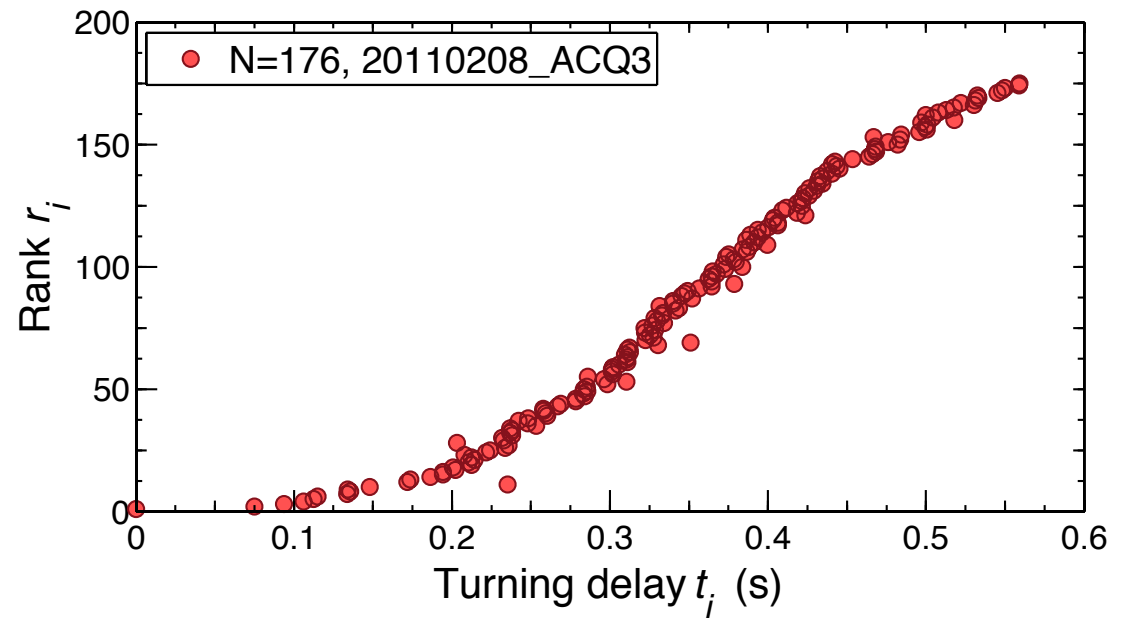
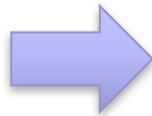
GReTA – tracking algorithm, IEEE trans. Pattern anal. Mach. Intell. (2015)



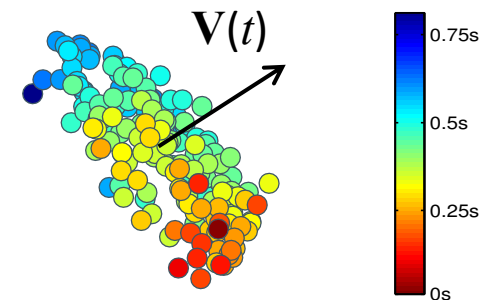
# Birds ranking

Rank birds according to their mutual turning delays  $\tau_{ij}$

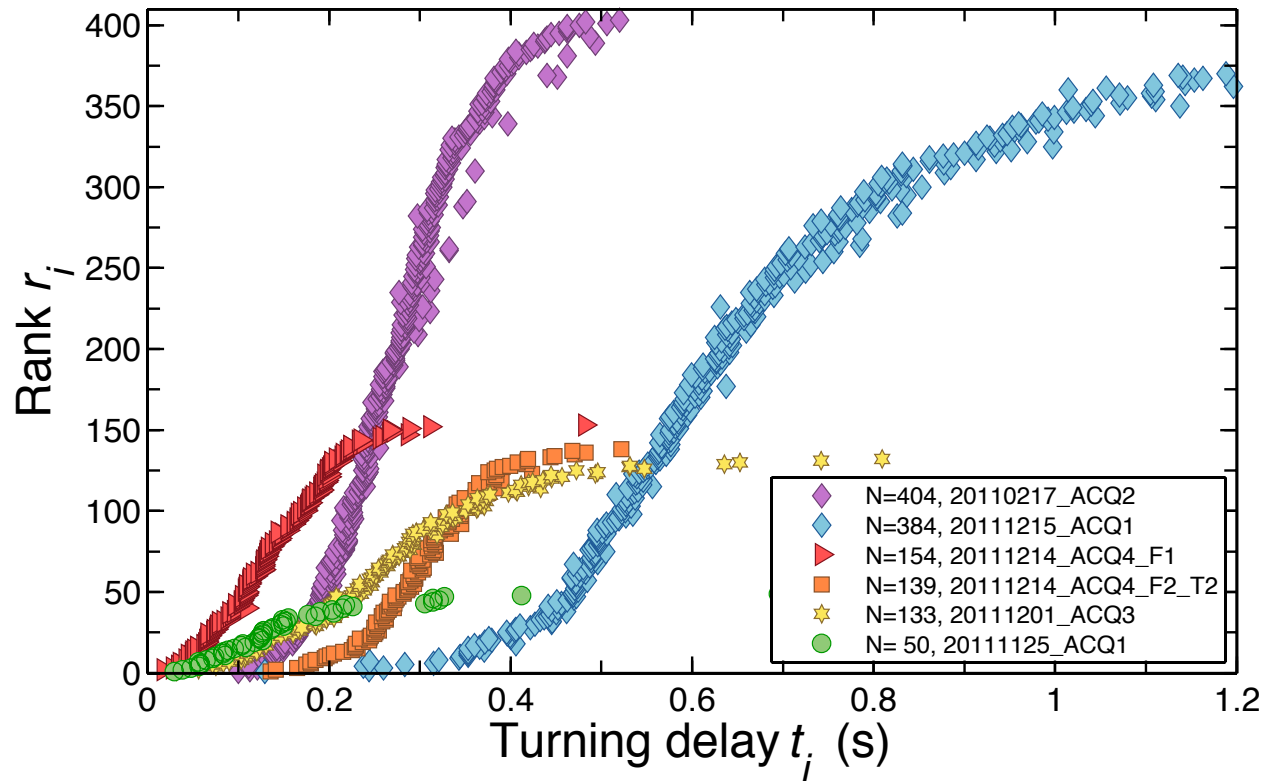
rank	delay
1	0 ms
2	35ms
3	44 ms
4	50 ms
5	52 ms
6	54 ms
7	63 ms
8	64 ms
9	68 ms
10	70 ms
11	71 ms
...	...



Turn starts localized and then it propagates across the flock



# Ranking curves



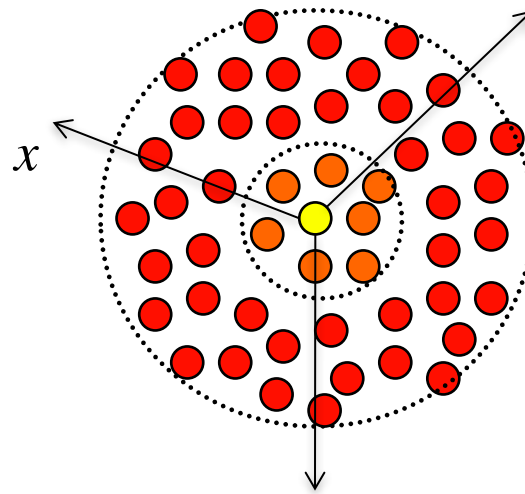


# Ranking and propagation in space ([searching for dispersion law](#))

If the turn starts localized then:

rank	delay
1	0 ms
2	35ms
3	44 ms
4	50 ms
5	52 ms
6	54 ms
7	63 ms
8	64 ms
9	68 ms
10	70 ms
11	71 ms
...	...

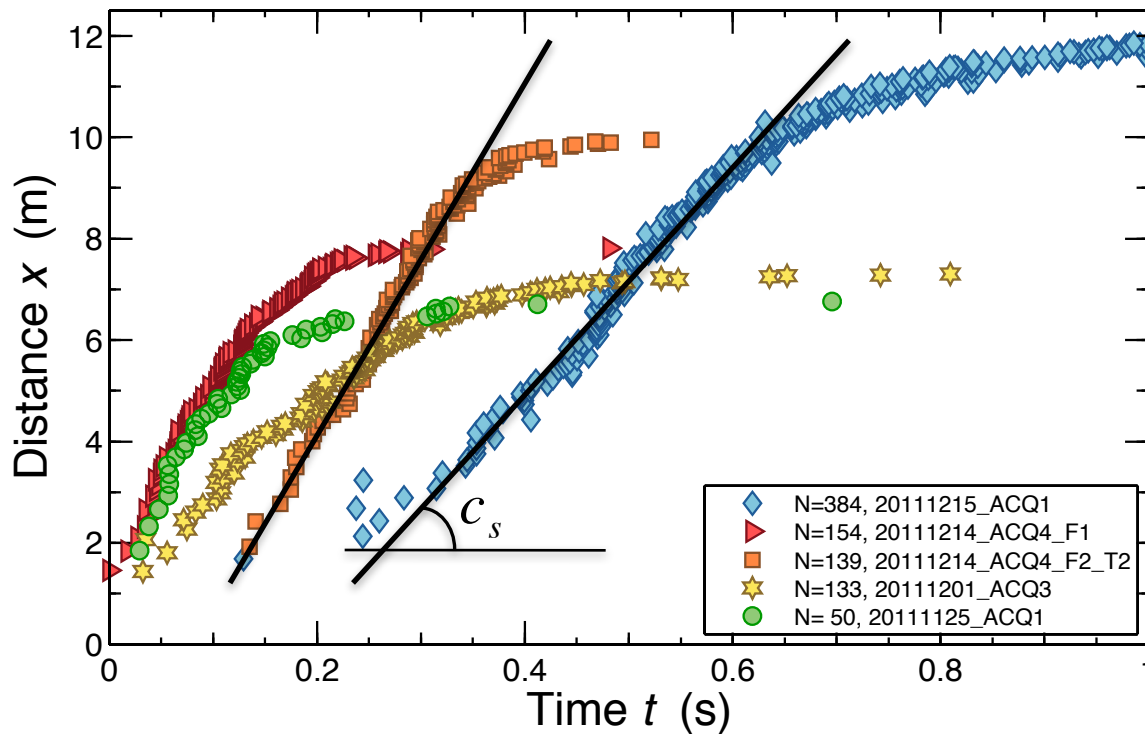
$$\text{rank} = (\text{density } \rho) \times (\text{distance traveled by the turn } x)^3$$



- rank: 1
- rank: 2-8
- rank: 9-38

$$x(t) = \left[ \frac{\text{rank}(t)}{\rho} \right]^{1/3}$$

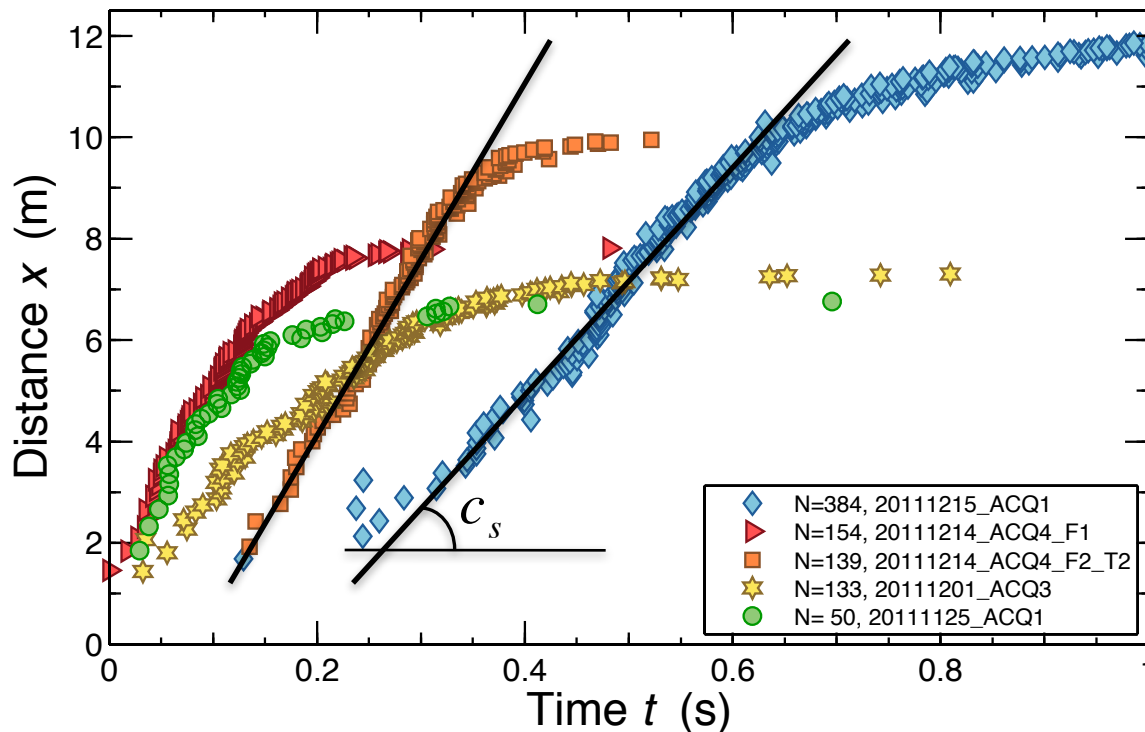
## Dispersion law : linear propagation of the turn



$$x = c_s t$$

$c_s$  = speed of propagation of the turn across the flock

## Dispersion law : linear propagation of the turn



$$x = c_s t$$

$c_s$  = speed of propagation of the turn across the flock

- Linear (sound-like) propagation of the turn (direction)
- Very weak attenuation of the turning signal (no damping)
- Variability of the speed of propagation  $c_s$  (20-40 ms<sup>-1</sup>)

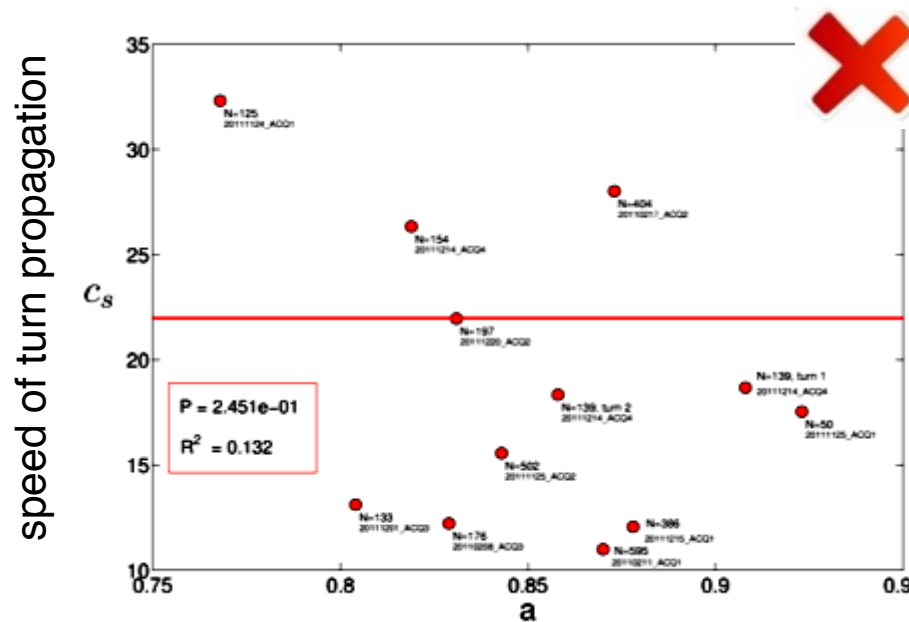
**Not explained by the standard theory of flocking!!**

( predicts diffusive and damped spread of information )

# Flock-to-flock variability of $c_s$

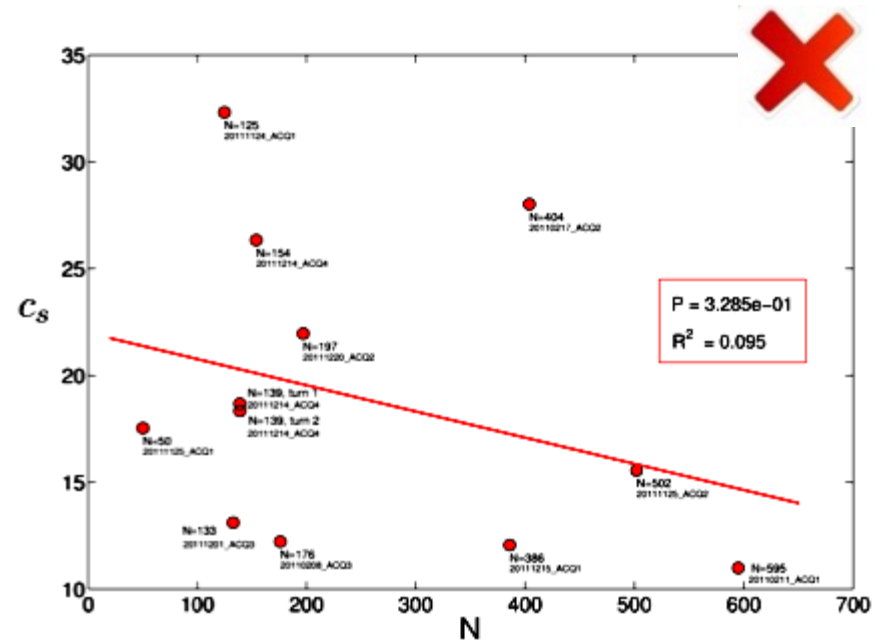
Making sense of the variability of  $c_s$  ...

attempt #1:



nearest neighbors distance  
( density )

attempt #2:



number of birds in the flock

# Standard theory of flocking

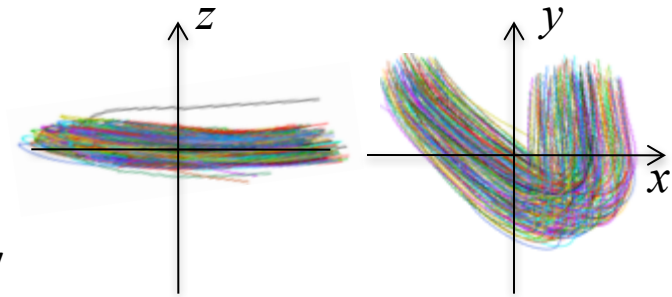
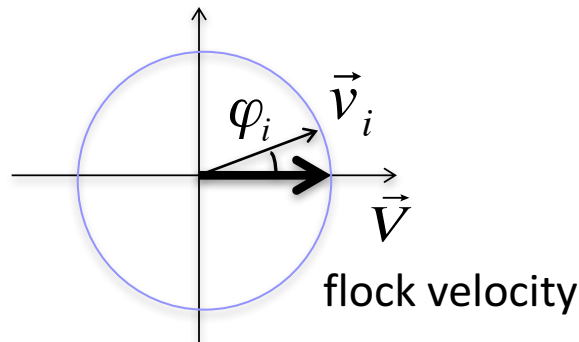
$$\vec{v}_i(t+1) = \vec{v}_i(t) + J \sum_{k \in i} \vec{v}_k(t) + \vec{\xi}_i$$

typical flocking model

$$\frac{d\vec{v}_i}{dt} = -\frac{\partial H}{\partial \vec{v}_i} + \vec{\xi}_i \quad H = -J \sum_{\langle ij \rangle} \vec{v}_i(t) \cdot \vec{v}_j(t)$$

- Planar order parameter:

$$v_i^x + i v_i^y = v e^{i\varphi_i}$$



- High polarization (low T) – spin wave expansion:

$a =$  lattice spacing

$$\varphi \sim 0 \quad \Rightarrow \quad H = \frac{1}{2} J \sum_{\langle ij \rangle} (\varphi_i - \varphi_j)^2 = \frac{1}{2a} J \int d^3x \left[ \vec{\nabla} \varphi(x,t) \right]^2$$

equation for the orientation  
angle change during the turn

$$\frac{\partial \varphi}{\partial t} = -\frac{\delta H}{\delta \varphi} = a^2 J \nabla^2 \varphi$$



$$x \sim \sqrt{t}$$

diffusive propagation



$$\omega = i k^2$$

damping



# What is wrong?

## 1) Missing conservation law

Rotational symmetry of the Hamiltonian  
(all flight directions are equivalent)

$$v_i = v e^{i\varphi_i} \quad \varphi_i \rightarrow \varphi_i + d\varphi$$

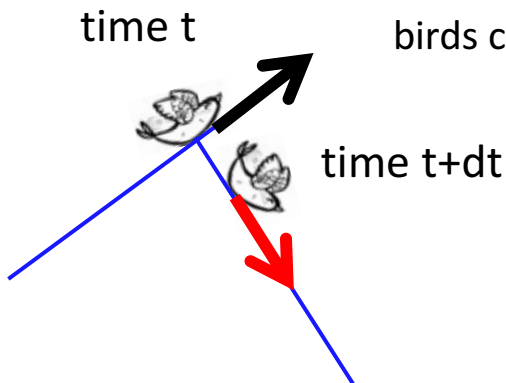
➡ Conservation law which affects the dynamics ! ( *and dispersion law!* )

## 2) No inertia

○ Standard theory:

$$\frac{\partial \varphi}{\partial t} = a^2 J \nabla^2 \varphi + \xi = -\frac{\delta H}{\delta \varphi} + \xi$$

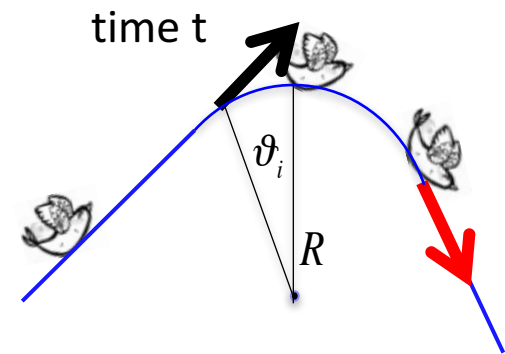
The force acts on velocity,  
birds can turn instantaneously



*but turns are smooth!*

○ Real bird:

To change direction, the bird has some constraints: mass, size, wings, etc.



# New (superfluid) theory of flocking

$$H = \int \frac{d^3x}{a^3} \left\{ \frac{1}{2} \rho_s [\vec{\nabla} \varphi(x,t)]^2 + \frac{s_z^2(x,t)}{2\chi} \right\}$$

$\rho_s \equiv a^2 J$  : rescaled alignment coupling

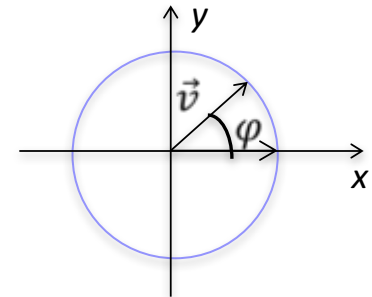
$\varphi(x,t)$  = parametrizes rotations of velocities

$s_z(x,t)$  = momentum conjugated to  $\varphi(x,t)$ , i.e. generator of the rotations around z-axis (**SPIN**)

$\chi$  = generalized moment of inertia

$$\vec{v} = v_x + i v_y = v e^{i\varphi}$$

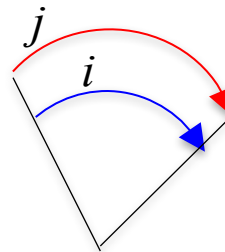
$$\{\vec{v}, s_z\} = \frac{\partial \vec{v}}{\partial \varphi} = i \vec{v}$$



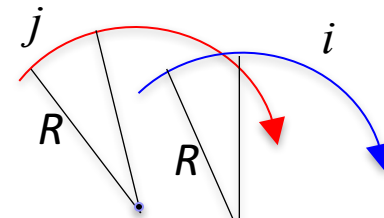
Biological motivation:

$R \approx \text{const.}$

$v \approx \text{const.}$



parallel paths trajectories



equal radius trajectories

# Predictions of the superfluid theory

Equations of motion:

$$\left\{ \begin{array}{l} \frac{\partial \varphi}{\partial t} = \frac{\delta H}{\delta s_z} = \frac{1}{\chi} s_z \\ \frac{\partial s_z}{\partial t} = -\frac{\delta H}{\delta \varphi} = \rho_s \nabla^2 \varphi \end{array} \right.$$



$$\frac{\partial^2 \varphi}{\partial t^2} - \frac{\rho_s}{\chi} \nabla^2 \varphi = 0$$

equation for the orientation  
angle change during the turn

$$x = c_s t$$

linear dispersion law



$$\omega = c_s k$$

no damping



Speed of propagation:  $c_s = \sqrt{\frac{a^2 J}{\chi}}$

The alignment coupling  $J$  has been related to the polarization  $\Phi$

Bialek et al. PNAS (2012)

$$J \propto \frac{1}{1 - \Phi}$$

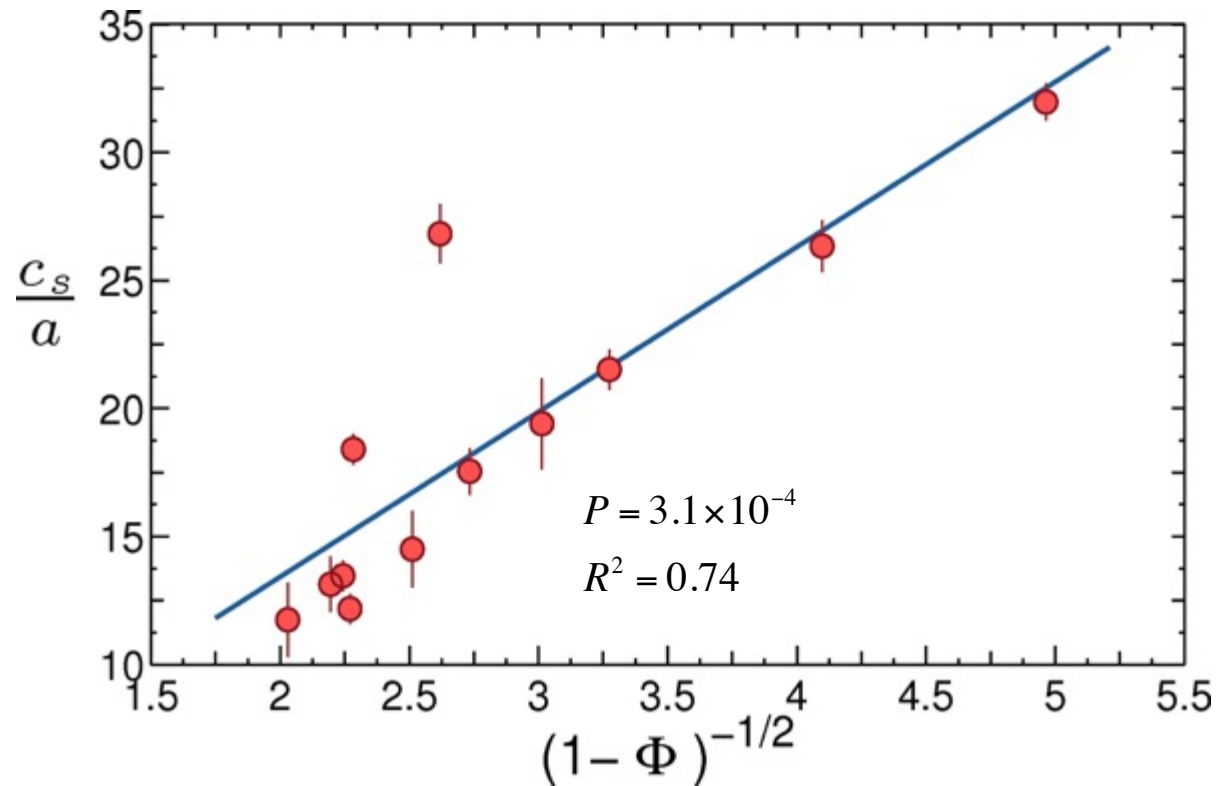
And  $\Phi = \left\| \frac{1}{N} \sum_i \frac{\vec{v}_i}{\|\vec{v}_i\|} \right\|$  is experimentally accessible!

$$c_s \propto \frac{1}{\sqrt{1 - \Phi}}$$

the speed of propagation of the turn across the flock  
must be larger in more ordered flocks



## Experimental test of the prediction



$$c_s \propto \frac{1}{\sqrt{1 - \Phi}} \quad \checkmark$$

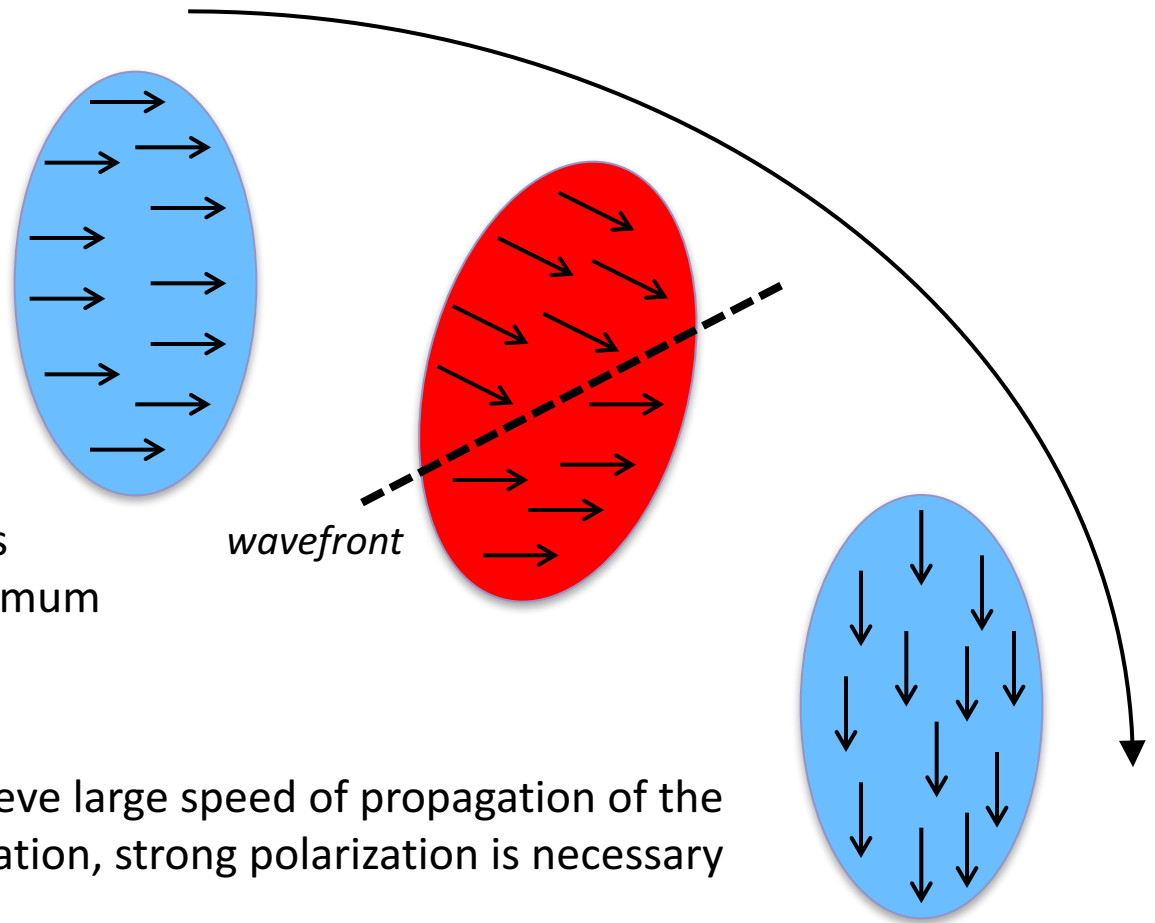
# Why natural groups are so polarized?

The group is fragile  
during the decision

fast information transfer keeps  
group's decoherence to a minimum

$$c_s \propto \frac{1}{\sqrt{1-\Phi}}$$

to achieve large speed of propagation of the  
information, strong polarization is necessary



The link between swift decision-making and large polarization may be the evolutionary drive behind the strong ordering observed in many living groups

# The Inertial Spin Model

A new model for self-organized collective motion  
(from phases to velocities, full 3D rotation)

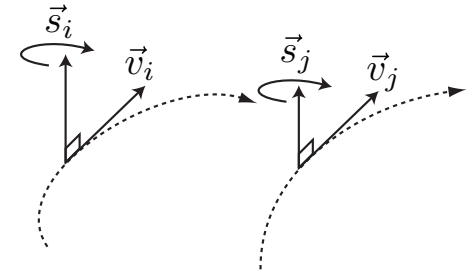
$$\begin{aligned}\frac{d\vec{v}_i}{dt} &= \frac{1}{\chi} \vec{s}_i \times \vec{v}_i; & \frac{d\vec{r}_i}{dt} &= \vec{v}_i \\ \frac{d\vec{s}_i}{dt} &= \vec{v}_i \times \left[ \frac{J}{v_0^2} \sum_j n_{ij} \vec{v}_j - \frac{\eta}{v_0^2} \frac{d\vec{v}_i}{dt} + \frac{\vec{\xi}_i}{v_0} \right]\end{aligned}$$

rotational  
dissipation

noise

$$\langle \vec{\xi}_i(t) \cdot \vec{\xi}_j(t') \rangle = 2d\eta T \delta_{ij} \delta(t - t')$$

Model G



Connection between inertial terms and symmetry is automatically implemented  
giving [correct information propagation](#)

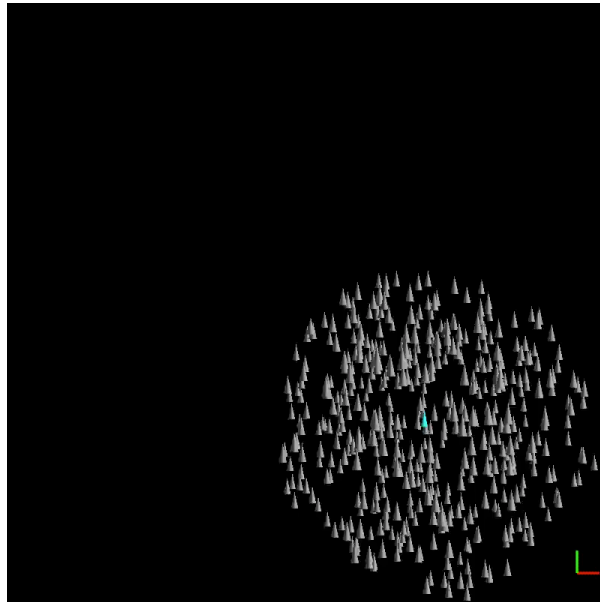
$$\chi \frac{d^2 \vec{v}_i}{dt^2} + \chi \frac{\vec{v}_i}{v_0^2} \left( \frac{d\vec{v}_i}{dt} \right)^2 + \eta \frac{d\vec{v}_i}{dt} = J \left( \sum_j n_{ij} \vec{v}_j \right)^\perp + v_0 \vec{\xi}_i^\perp$$

inertial term
centripetal term
dissipation
social force
noise

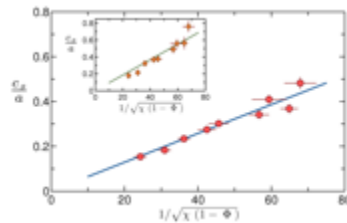
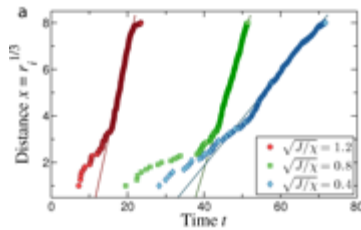
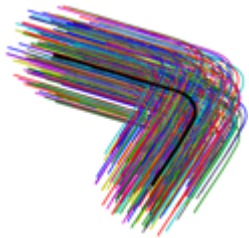
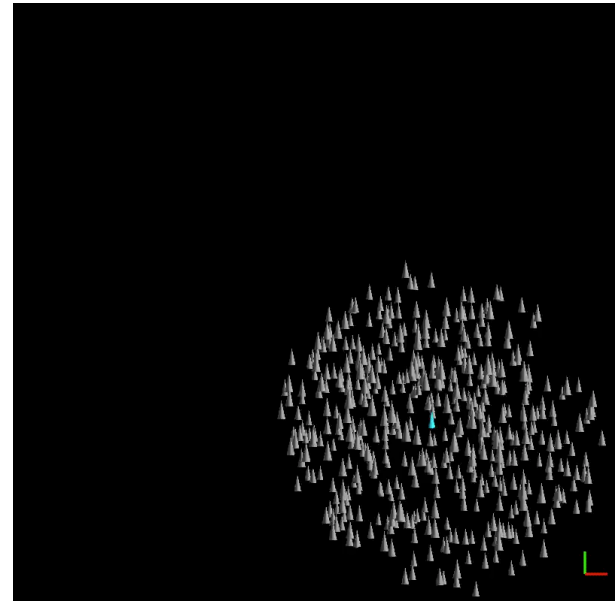
overdamped limit  $\rightarrow$  Vicsek model

# Inertial Spin Model - simulations

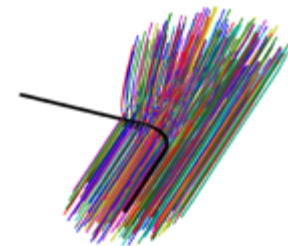
Underdamped regime



Overdamped regime



correct information propagation

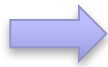


Vicsek model

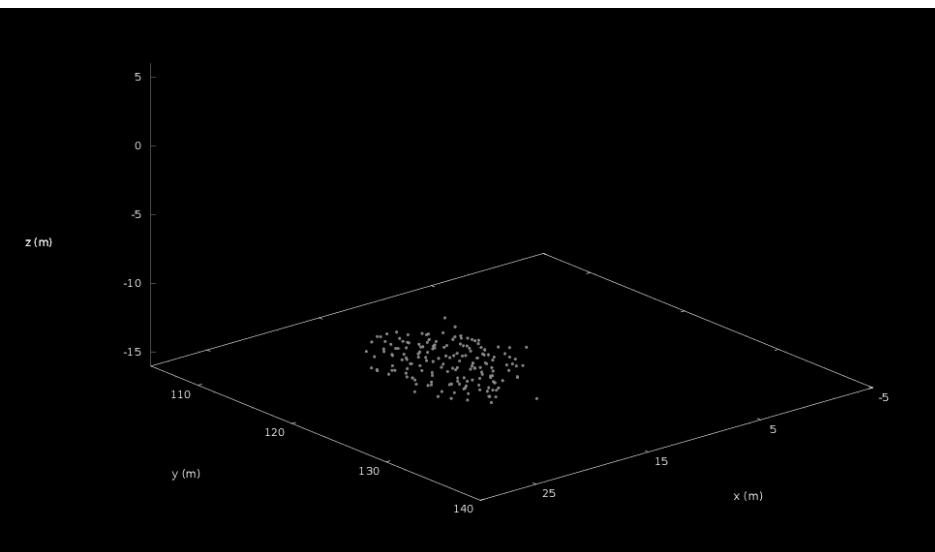
# Why and how did the turn start?

As a response to an external alarm cue? **Not necessarily**

- ✧ **locusts** - in the lab and in the field Buhl et al. Science (2006)
- ✧ **fish schools** - collective evasion maneuvers (lab) Rosenthal et al. PNAS (2015)
- ✧ **starlings aerial display** - flocks keep changing their direction of motion even in the absence of predators or obstacles



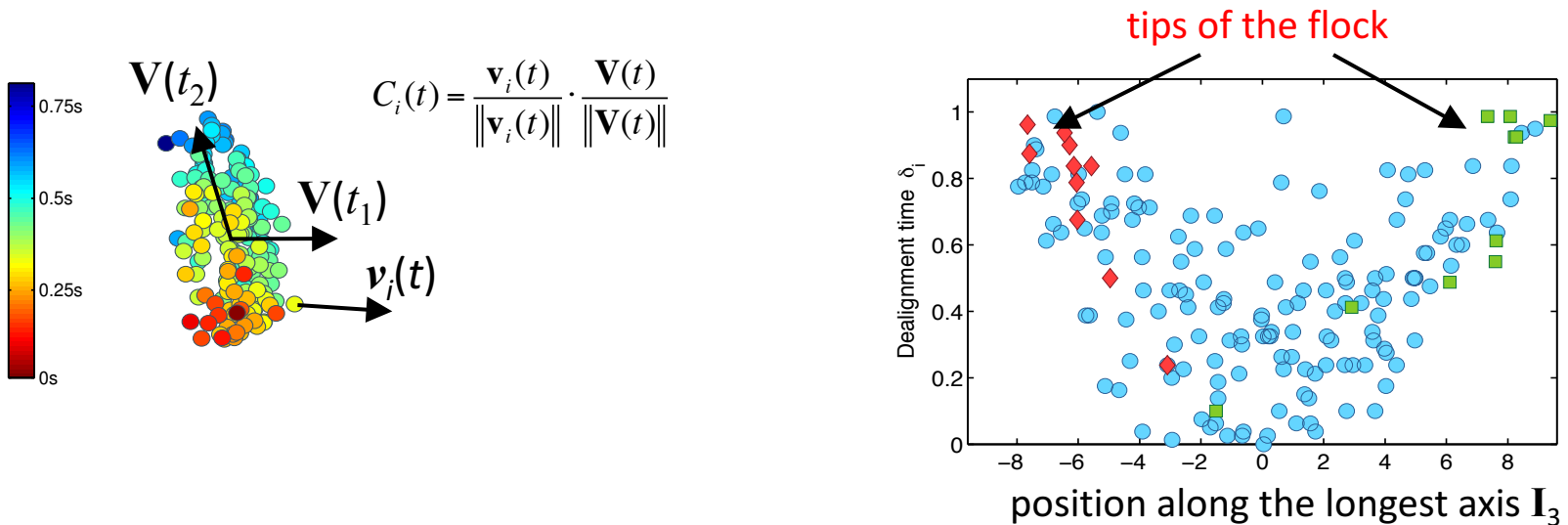
Collective directional switching can be triggered *spontaneously* without changes in the external environment



- ✧ Where it starts?  
**individuals close to the border**
- ✧ What triggers the turn?  
**internal behavioural fluctuations**

# What triggers spontaneous turns?

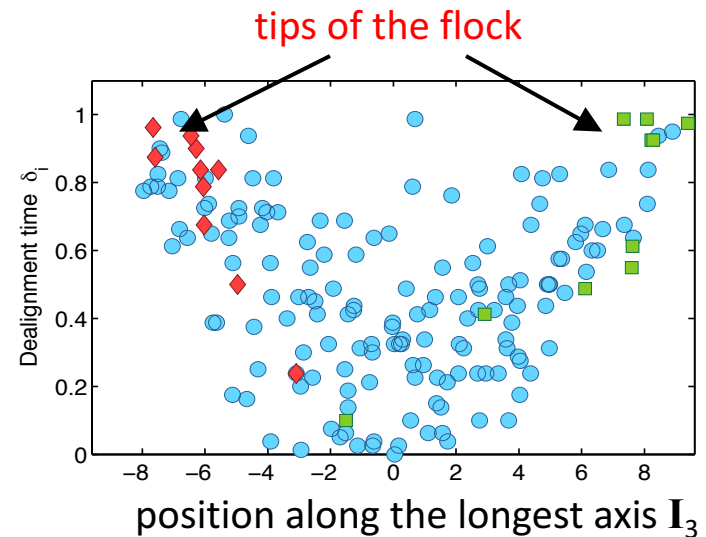
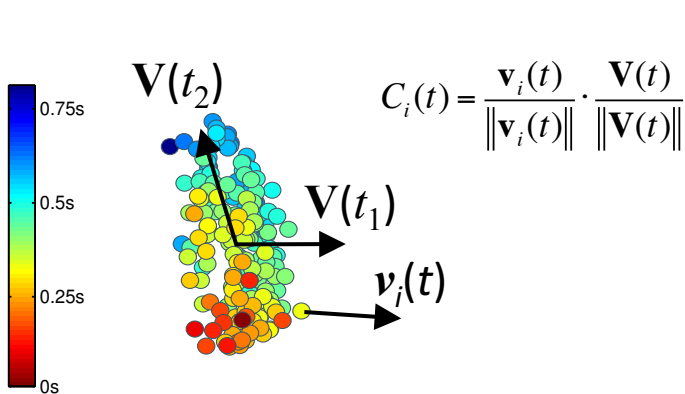
Individual deviations from the global flock's direction of motion prior to the turn:



There is a correlation between the location of an individual in the flock and **how persistently** it deviates

# What triggers spontaneous turns?

Individual deviations from the global flock's direction of motion prior to the turn:



## Why turns occur spontaneously and often?

Standard Heisenberg model on a lattice:

$\tau^{rel} \sim L^{d-2}$  the system changes global state on large scales

What is different in flocks?

the network is random  
interactions are NOT symmetric



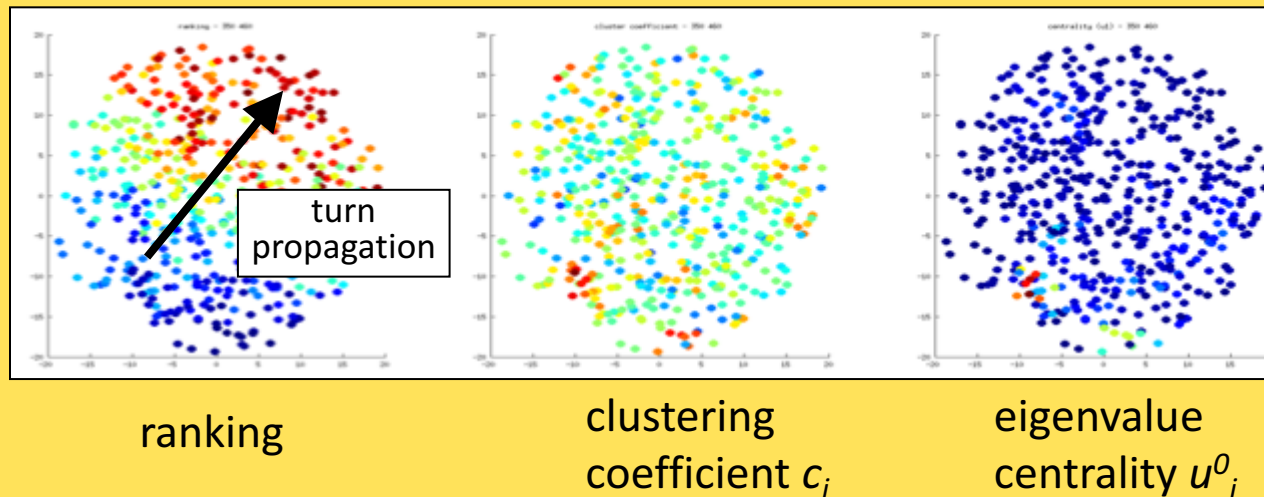
peripheral clusters are more sensitive to noise  
leading to collective changes to state

# Spontaneous turns determined by interaction network

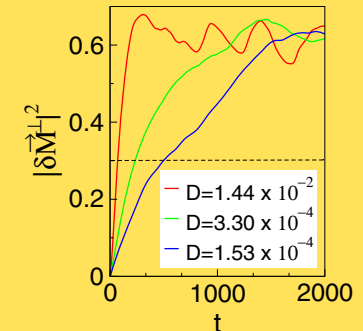
## Dynamics on a random Euclidean network?

Phys. Rev. Lett. (2017)

- points drawn uniformly in Euclidean space instead on a regular lattice
- place the birds/spins and let them interact with their  $n_c$  nearest neighbours



turns start at the boundary where both  $c_i$  and  $u_i^0$  are large



## Experimental confirmation:

- ✧ **fish**: large  $c_i$  of initiators of collective evasion waves in fish schools
- ✧ **starlings**: turns start from the tips; initiators exhibit systematic fluctuations

Rosenthal et al. PNAS (2015)

Attanasi et al. Roy. Soc. Interface (2015)



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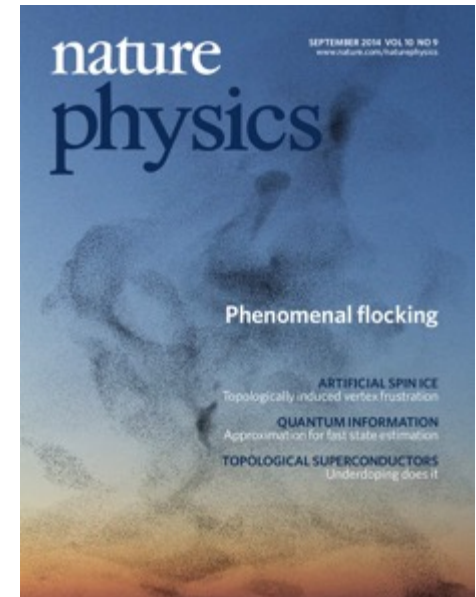
# Conclusions

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- Turns start localized, then spread through the flock fast and accurate
  - ✧ **linear propagation** of orientational information, **no damping**
- New superfluid theory for turns
  - ✧ **symmetries** and **conservation laws** ideas work **in biology** too
- High order in the group grants a more efficient propagation of information
  - ✧ why natural groups are so polarized?
- Non-symmetric random interaction network and inertial dynamics can produce **spontaneous changes** of collective state on short scales

# Based on

- ✧ Information transfer and behavioural inertia in starling flocks  
*Nature Physics*, 2014
- ✧ GReTA -- a novel Global and Recursive Tracking Algorithm in three dimensions  
*IEEE Trans. Pattern Anal. Mach. Intell.*, 2015
- ✧ Flocking and turning: a new model for self-organized collective motion  
*J. Stat. Phys.*, 2015
- ✧ Silent flocks: : Constraints on Signal Propagation Across Biological Groups  
*Phys.Rev.Lett.*, 2015
- ✧ Emergence of collective changes in travel direction of starling flocks from individual birds' fluctuations  
*Roy.Soc. Interface*, 2015
- ✧ Nonsymmetric Interactions Trigger Collective Swings in Globally Ordered Systems  
*Phys.Rev.Lett.*, 2017



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## In collaboration with

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