



# Lepton Flavor Violating Processes in the Left-Right Symmetric Model

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# Left-Right Symmetric Model Basics

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$$G_{EW} = SU(2)_L \times SU(2)_R \times U(1)' \rightarrow SU(2)_L \times U(1)_Y$$

- Right-handed neutrinos Pati, Salam '74
- New gauge fields Mohapatra, Pati '75
  - »  $W_R$  &  $Z_R$  with couplings  $\kappa = g_R/g_L$
- New Higgs fields with vev  $v_R$ 
  - » Doublet Higgs:
    - Dirac neutrinos
    - Strong constraints from  $W_R \rightarrow l\nu$  LHC searches (5.2 TeV for  $\kappa=1$ )
  - » Triplet Higgs:  $(\Delta_L^\pm, \Delta_{R,L}^{\pm\pm})$ 
    - Majorana right-handed neutrinos w/ mass  $N_l \sim$  mass  $W_R$
    - $W_R \rightarrow l N_l$  avoided if mass  $N_l >$  mass  $W_R$
    - $U(1)'$  can be identified as  $U(1)_{B-L}$
  - » Bi-Doublet Higgs to generate fermion masses with vevs  $k_{1,2}$
- Right-handed CKM, PMNS matrix

# Left-Right Symmetric Model Basics

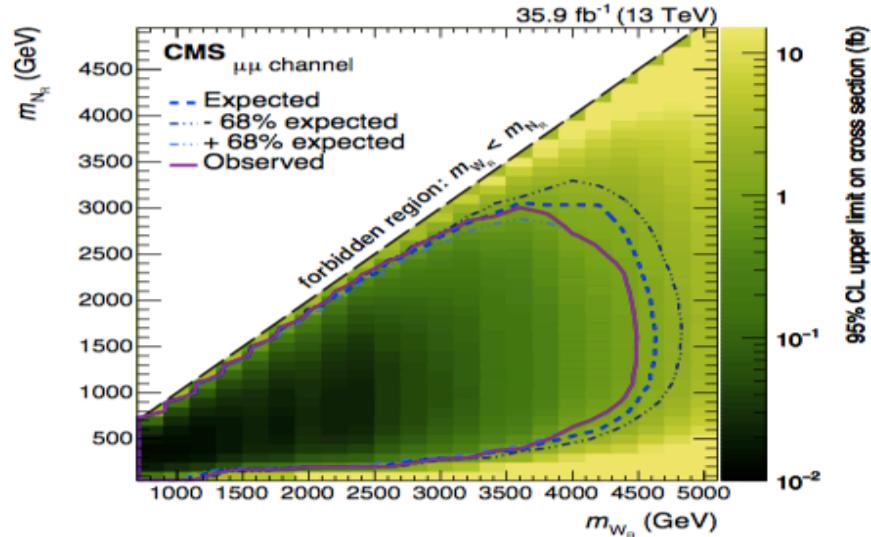
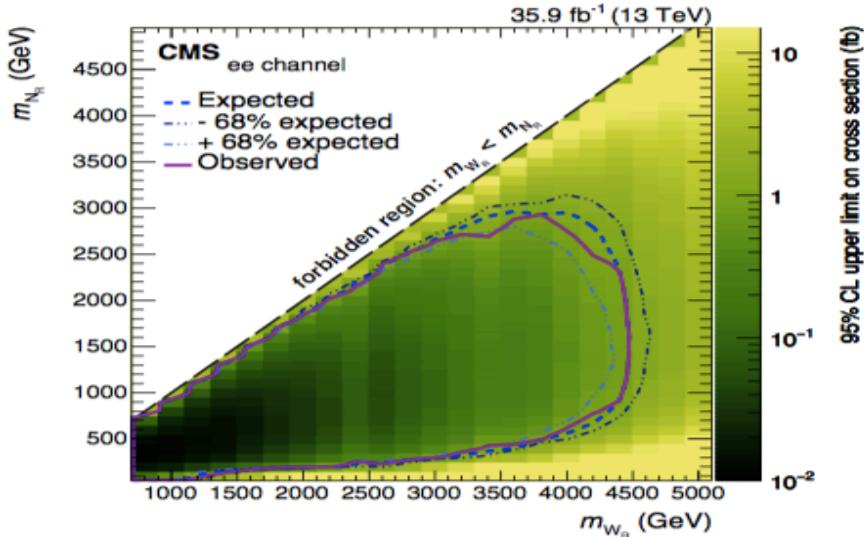
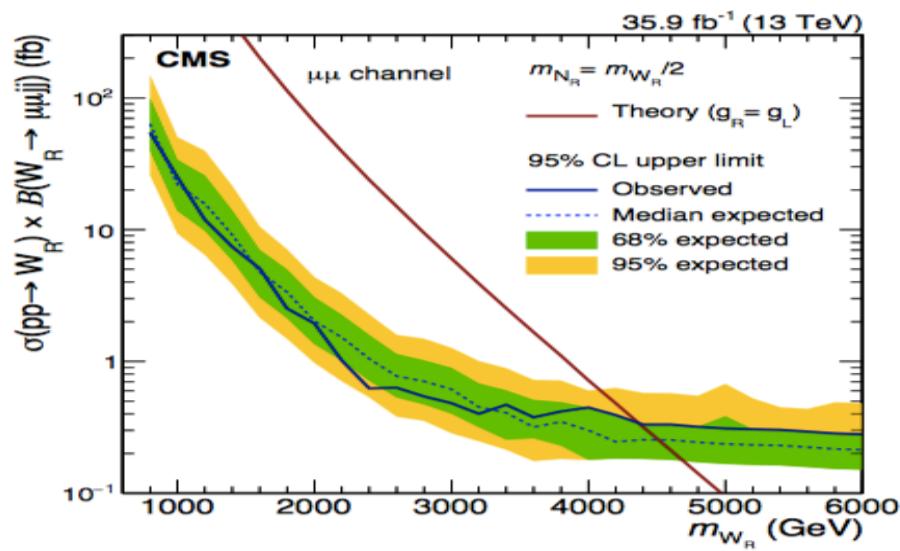
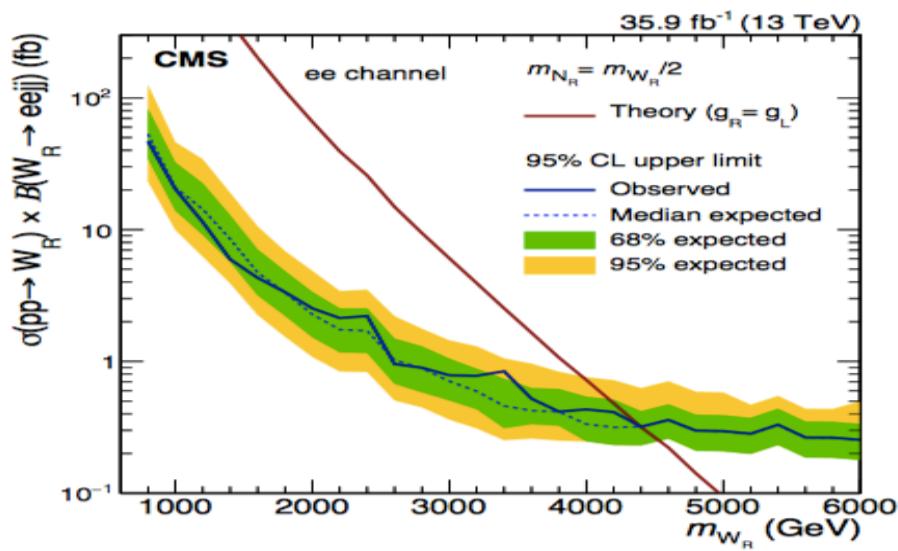
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# Bounds from Direct LHC Searches: $W_R \rightarrow N_R l$ Channel

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# Right-handed gauge sector

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- $W_L - W_R$  mass matrix

$$\mathcal{M}_W^2 = \begin{pmatrix} m_W^2 & \beta_w m_W^2 \\ \beta_w m_W^2 & m_{W_R}^2 \end{pmatrix}$$

- Diagonalized by mixing

$$\tan 2\phi_w = \frac{-2\beta_w m_W^2}{m_{W_R}^2 - m_W^2}$$

- $W_R/Z_R$  mass ratio set by theory

$$\frac{m_{Z_R}^2}{m_{W_R}^2} = \frac{\kappa^2(1-x_w)\rho_R}{\kappa^2(1-x_w) - x_w} > 1$$

where  $\kappa > 0.55$  is physical region

- Lepton Yukawa couplings to triplet Higgs

$$y_R \left[ \left( \Delta_R^0 + \frac{v_R}{\sqrt{2}} \right) \overline{N^c} P_R N + \frac{\Delta_R^+}{\sqrt{2}} \overline{N} P_R \ell + \frac{\Delta_R^{++}}{2} \overline{\ell^c} P_R \ell \right] + \text{h.c.},$$

$$(h_R)_{ij} = \sum_n (V_R)_{ni} (V_R)_{nj} \frac{M_{N_n}}{M_{W_R}}$$

$$\mathcal{L}_{\Delta^\pm \nu \ell} = \frac{g_L \kappa}{\sqrt{2}} \left\{ \tilde{h}_{ij} \Delta_L^\pm \overline{\nu_L^{i c}} \ell_L^j + \text{h.c.} \right\},$$

$$\mathcal{L}_{\Delta^{\pm\pm} \ell \ell} = \frac{g_L \kappa}{2} h_{ij} \left\{ \Delta_L^{++} \overline{\ell_L^{c i}} \ell_L^j + \Delta_R^{++} \overline{\ell_R^{c i}} \ell_R^j + \text{h.c.} \right\}$$

# Scan of parameter space

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- Perform a scan of parameter space, two distinct model sets
  - » Gauge sector parameters
    - Fix  $W_R$  mass = 5, 10 TeV,
    - $\kappa = 1$ ,
    - $V_{CKM}^R = V_{CKM}^L$
  - » Right-handed neutrinos
    - assign  $m_1 < m_2 < m_3$  w/ signed  $m_{2,3}$   
 $100 \text{ GeV} \leq M_{N_R^i} \leq 20 \text{ TeV.}$
  - » Right-handed PMNS matrix
    - $0 \leq s_{12}, s_{13}, s_{23} \leq 1$
  - » Charged scalars  $\Delta_L^\pm, \Delta_{R,L}^{\pm\pm}$   
 $400 \text{ GeV} \lesssim M_{\Delta_L^\pm, \Delta_{L,R}^{\pm\pm}} \leq 20 \text{ TeV.} \quad 0.5 \leq \tan \beta \leq 50$

Generated  $3 \times 10^8$  models per set

# Consistency with current LFV/LNV constraints

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Subject parameter space to constraints:

Rare processes:  $0\nu\beta\beta$ ,  $\mu \rightarrow e\gamma$ ,  $\tau \rightarrow l\gamma$ ,  $\mu \rightarrow eee$ ,  $\tau \rightarrow lll'$ ,  $\mu \rightarrow e$  conversion

Muonium oscillations

Observable	Experimental bound		Future limit	
$B(\mu^- \rightarrow e^-\gamma)$	$< 4.2 \times 10^{-13}$	[72]	$< 6 \times 10^{-14}$	[96]
$B(\tau^- \rightarrow \mu^-\gamma)$	$< 4.4 \times 10^{-8}$	[73]	$< 10^{-9}$	[86]
$B(\tau^- \rightarrow e^-\gamma)$	$< 3.3 \times 10^{-8}$	[73]	$< 10^{-9}$	[86]
$B(\mu^- \rightarrow e^-e^+e^-)$	$< 10^{-12}$	[74]	$< 10^{-15} - 10^{-16}$	[95]
$B(\tau^- \rightarrow e^-e^+e^-)$	$< 2.7 \times 10^{-8}$	[75]	$< 10^{-9} - 10^{-10}$	[86]
$B(\tau^- \rightarrow \mu^-\mu^+\mu^-)$	$< 2.1 \times 10^{-8}$	[75]	$< 10^{-9} - 10^{-10}$	[86]
$B(\tau^- \rightarrow e^-\mu^+\mu^-)$	$< 2.7 \times 10^{-8}$	[75]	$< 10^{-9} - 10^{-10}$	[86]
$B(\tau^- \rightarrow e^+\mu^-\mu^-)$	$< 1.7 \times 10^{-8}$	[75]	$< 10^{-9} - 10^{-10}$	[86]
$B(\tau^- \rightarrow \mu^-e^+e^-)$	$< 1.8 \times 10^{-8}$	[75]	$< 10^{-9} - 10^{-10}$	[86]
$B(\tau^- \rightarrow \mu^+e^-e^-)$	$< 1.5 \times 10^{-8}$	[75]	$< 10^{-9} - 10^{-10}$	[86]
$CR(\mu^- \rightarrow e^-)$ [Au]	$< 7 \times 10^{-13}$	[76]		
$CR(\mu^- \rightarrow e^-)$ [Ti]	$< 4.3 \times 10^{-12}$	[77]	$< 10^{-18}$	[84, 85]
$CR(\mu^- \rightarrow e^-)$ [Pb]	$< 4.6 \times 10^{-11}$	[78]		
$CR(\mu^- \rightarrow e^-)$ [Al]	—		$< 10^{-16} - 10^{-18}$	[80, 85]
$P(M \rightarrow \bar{M})$	$< 8.2 \times 10^{-11}$	[79]		
$T_{1/2}^{\beta\beta_{0\nu}}$ [ $^{136}\text{Xe}$ ]	$> 1.07 \times 10^{26}$ yr	[89]		
$\langle m_{ee} \rangle$	$< 61 - 165$ meV		$< 3-12$ meV)	[92, 93]

Note large improvement in future expt's!!

# Consistency with Lepton Flavor Conserving Processes

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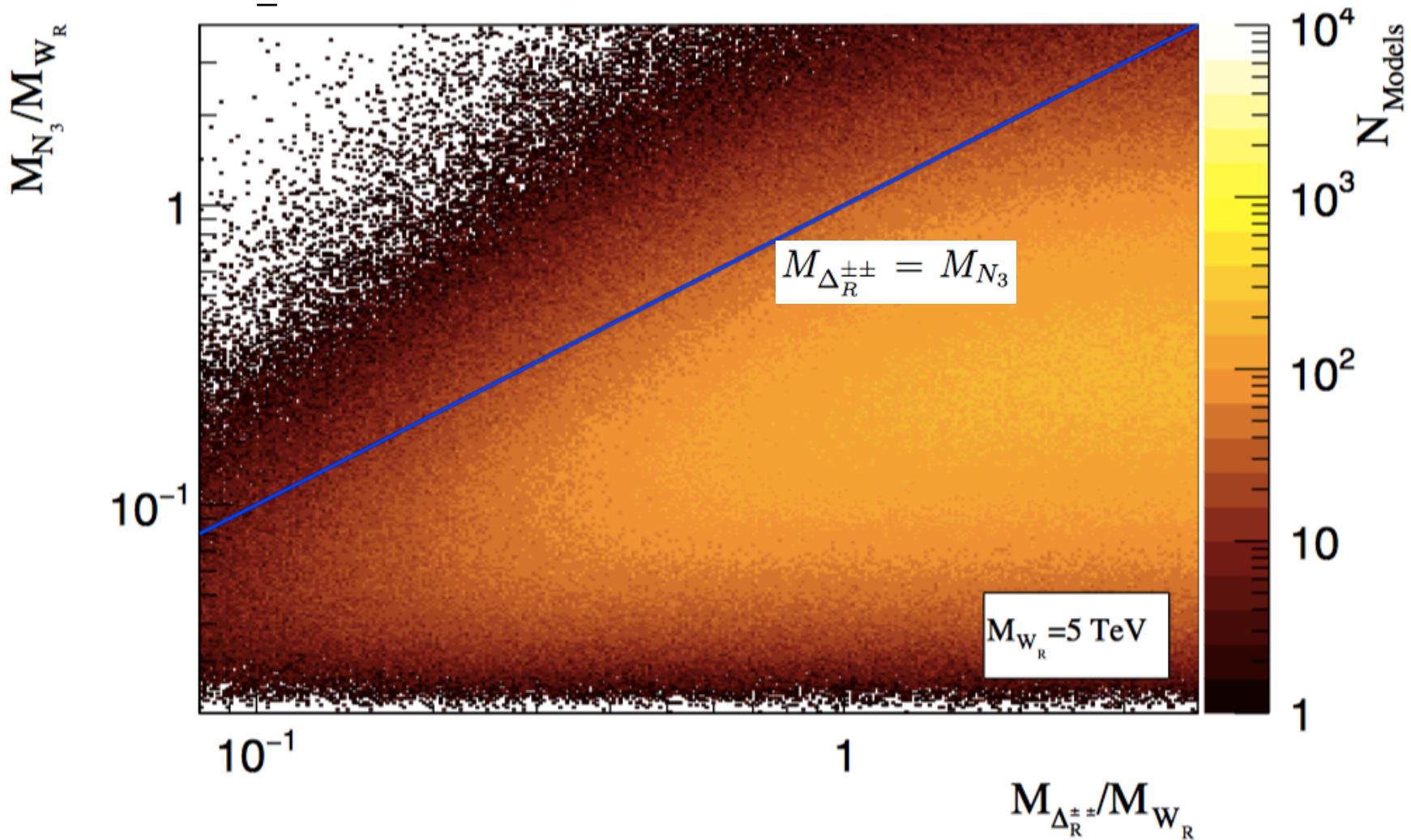
- Subject parameter space to LFC constraints
  - »  $e^+e^- \rightarrow l^+l^-$  from LEP2, cross sections and asymmetries
  - » Low-energy parity-violating asymmetry in Moller scattering
  - » Neutrino-electron scattering observables
  - » Muon decay
- 4-Fermion interaction

$$\mathcal{L}_{\text{Eff}} \supset a_\ell \frac{g_R^2}{4} \frac{|h_{e\ell}|^2}{M_{\Delta_\alpha^{\pm\pm}}^2} (\bar{e}_\alpha \gamma^\mu e_\alpha) (\bar{\ell}_\alpha \gamma^\mu \ell_\alpha), \quad \alpha = L, R,$$

- Surviving model set after LFV/LNV & LFC Constraints:
  - »  $6.6 \times 10^5$  models;  $M_{W_R} = 5 \text{ TeV}$
  - »  $2.7 \times 10^6$  models;  $M_{W_R} = 10 \text{ TeV}$

# Distribution of Models

$M_{W_R} = 5 \text{ TeV}$



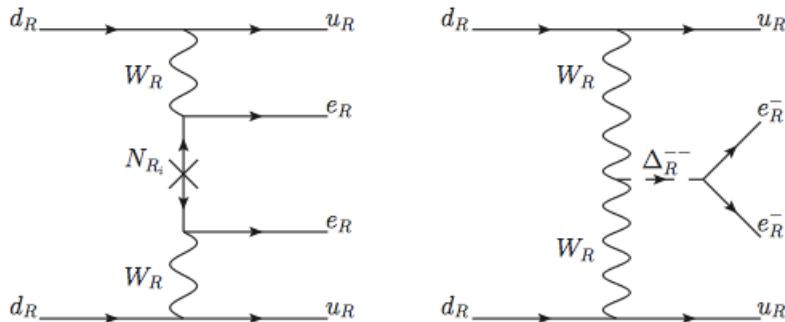
# Neutrinoless double-beta decay

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- Current limits in  $\text{Ge}^{76}$  and  $\text{Xe}^{136}$  (Gerda, EXO-200, Kamland-Zen)
- Probes effective Majorana neutrino mass

$$|m_{ee}|^2 = |m_{ee_L}|^2 + |m_{ee_R}|^2$$

- Tree-level LNV diagrams with N and  $\Delta_R^{\pm\pm}$  exchange



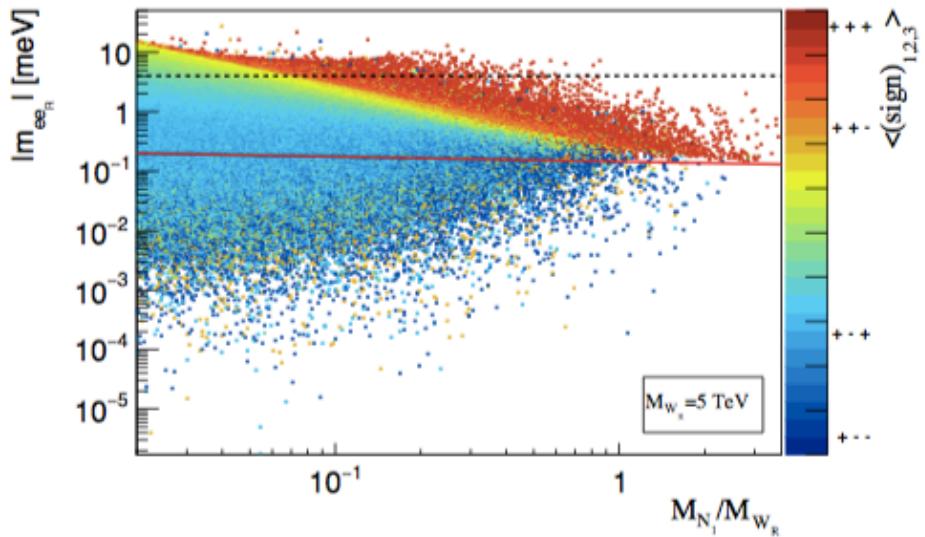
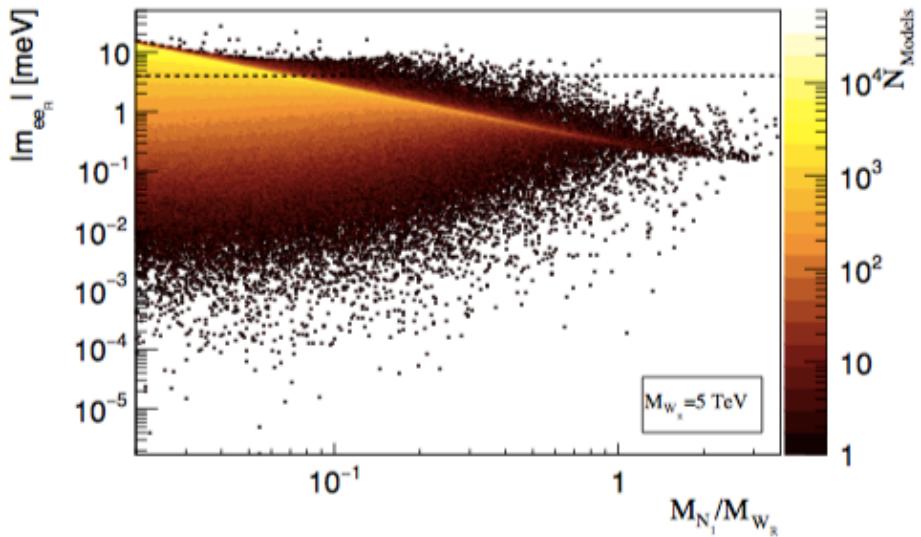
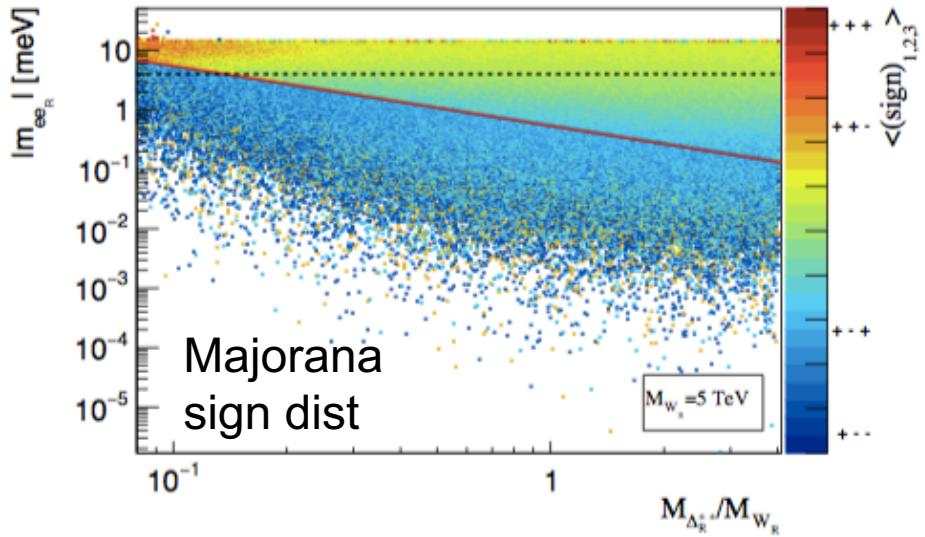
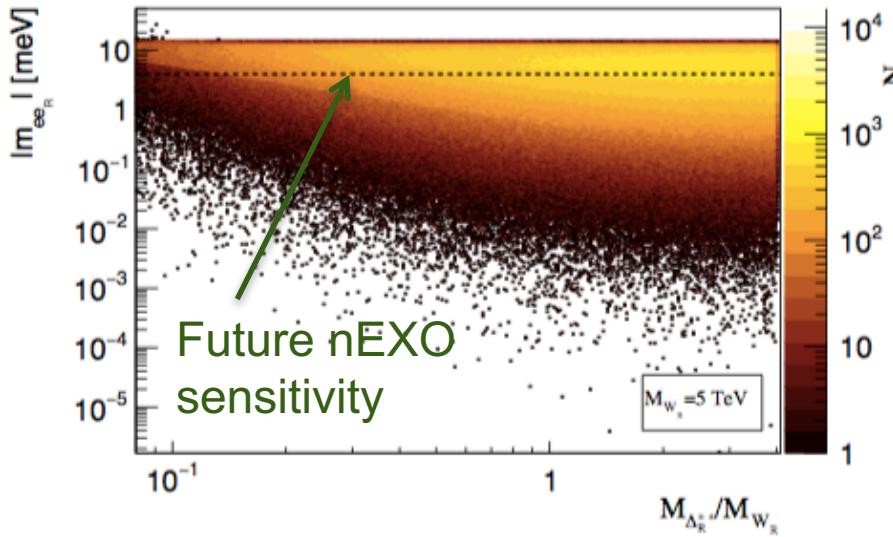
$$x_i = M_{N_i}^2 / M_{W_R}^2$$

$$x_{\Delta_R^{\pm\pm}} \equiv M_{\Delta_R^{\pm\pm}}^2 / M_{W_R}^2$$

$$\eta_R = \frac{m_p}{M_{W_R}} \left( \frac{\kappa M_W}{M_{W_R}} \right)^4 \sum_i (\text{sign})_i V_{ei}^2 \left( \frac{1}{\sqrt{x_i}} + \frac{\sqrt{x_i}}{x_{\Delta_R^{\pm\pm}}} \right)$$

# Neutrinoless Double-Beta Decay Results

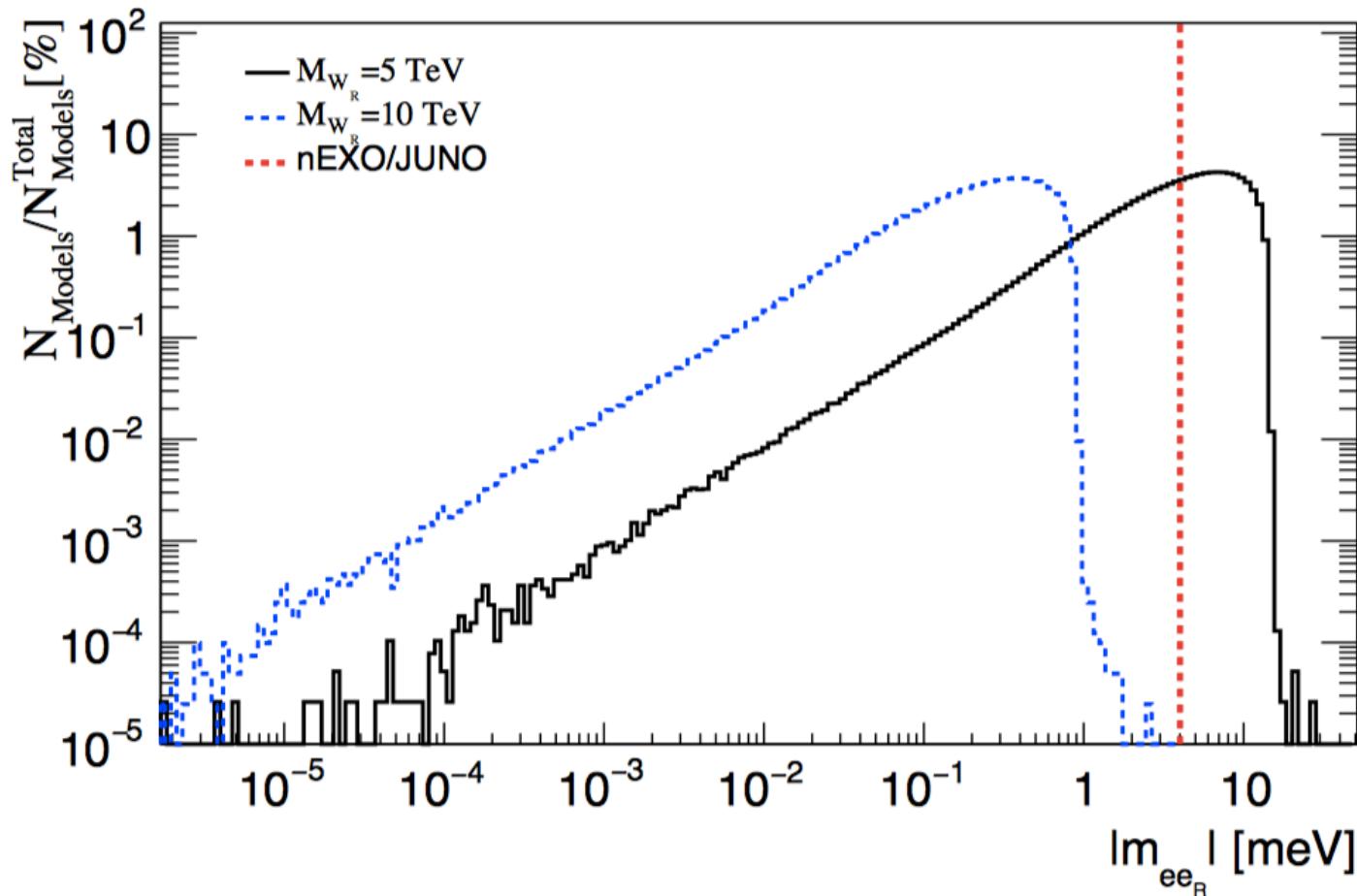
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# Neutrinoless double-beta decay: histogram of predictions

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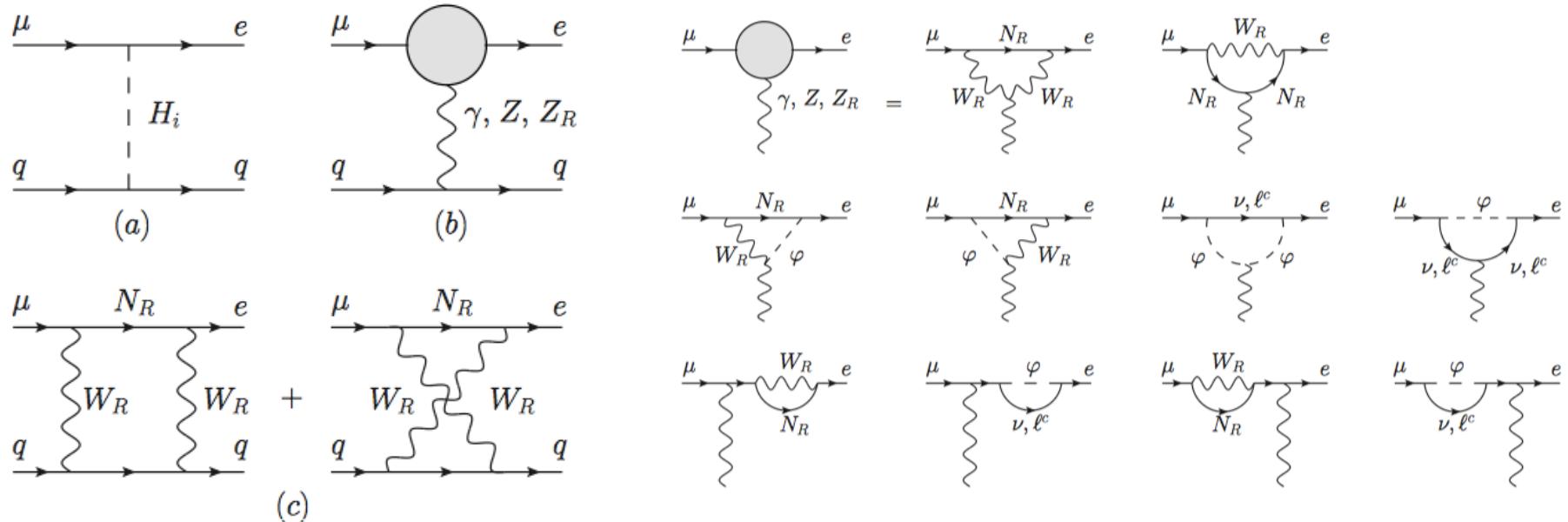
0v $\beta\beta$  has sensitivity to  $M_{W_R} = 5 \text{ TeV}$



# Mu2e conversion ( $\mu N \rightarrow e N$ )

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- Current limits for Pb, Ti, Au (SINDRUM II)
- LRM contributions
  - » Tree-level neutral Higgs exchange (small)  $y_D/(\alpha/4\pi) \ll 1$
  - » 1-loop  $W_R$ ,  $\Delta_L^\pm$ ,  $\Delta_{R,L}^{\pm\pm}$  exchange to anapole/dipole vertices
    - Log enhanced  $\sim \log(-q^2/M_{\Delta_{L,R}^{\pm\pm}}^2)$
  - » 1-loop  $W_R$  exchange in  $\mu e Z_i$  vertices
  - » 1-loop  $W_R$  box diagrams

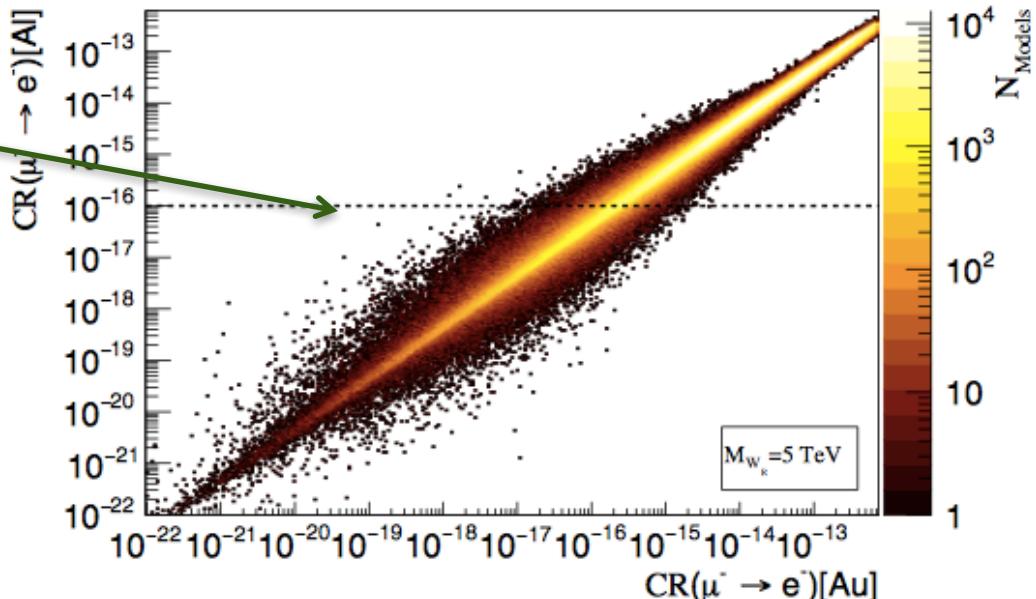
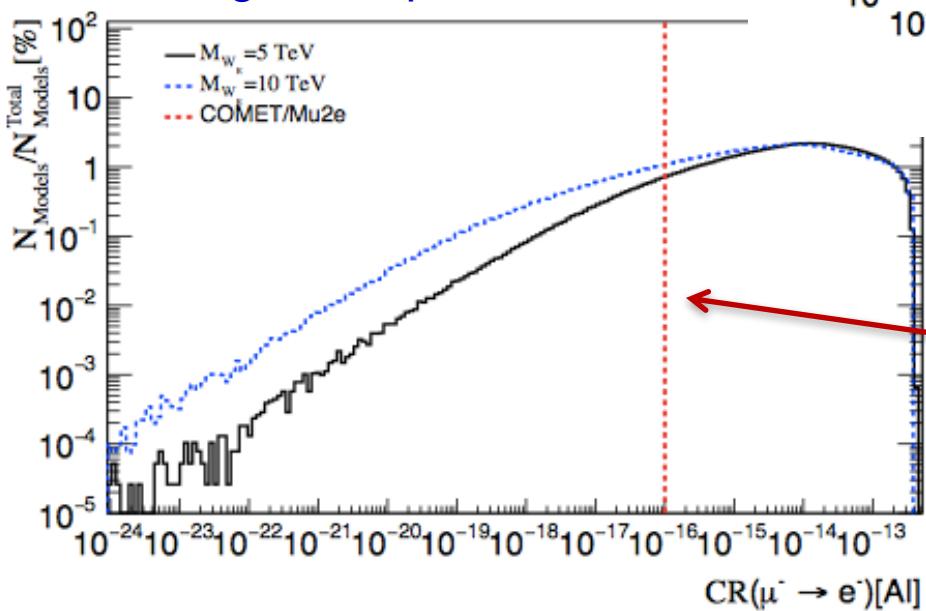


# Mu2e Conversion in Al: Results

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Future  
Mu2e/COMET  
sensitivity

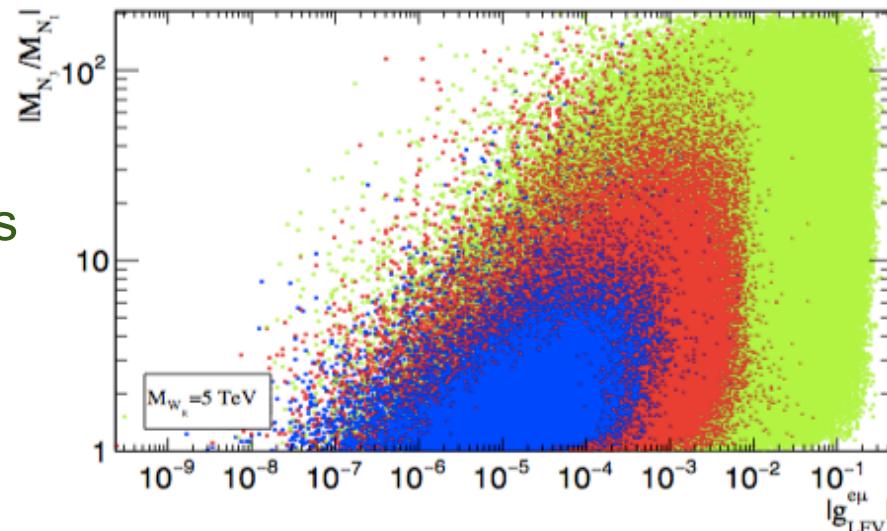
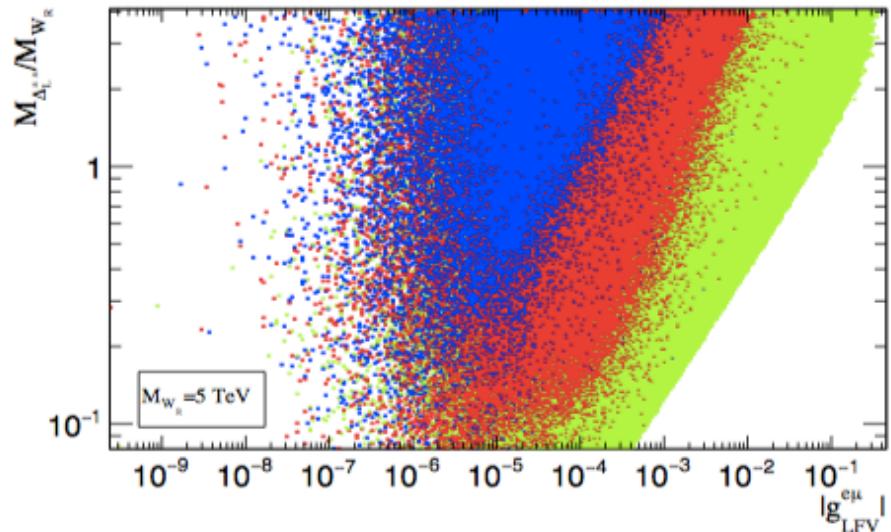
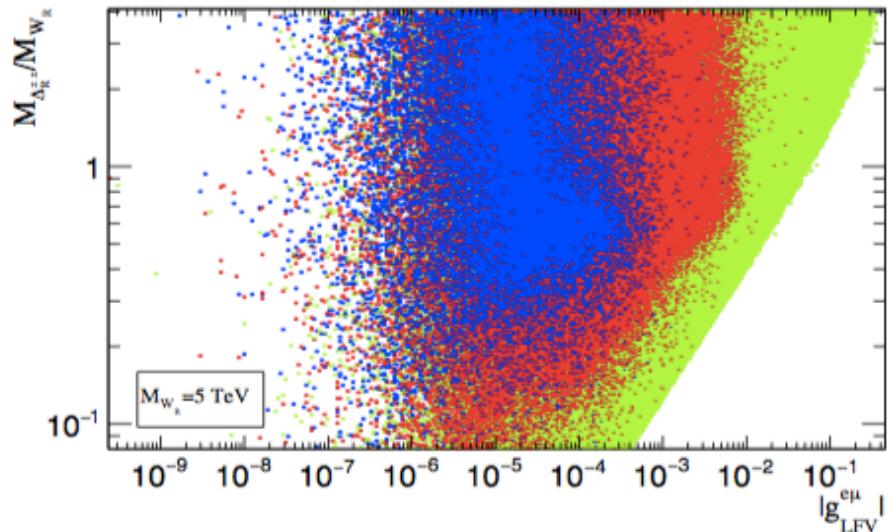
Histogram of predictions



Large fraction of  
models covered!

# Strong Constraints from Mu2e

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Current Constraints  
 $\text{CR}(\mu \rightarrow e) < 10^{-16}$   
 $\text{CR}(\mu \rightarrow e) < 10^{-18}$

# Rare Muon Decays

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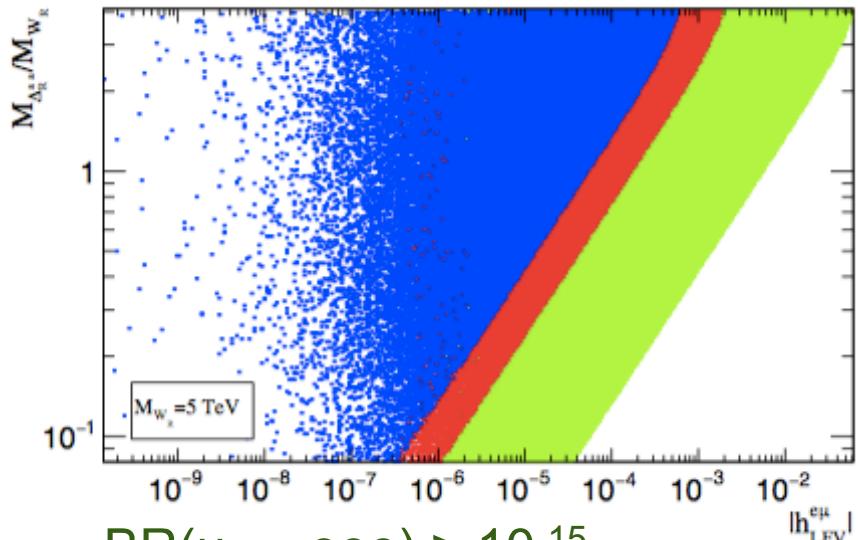
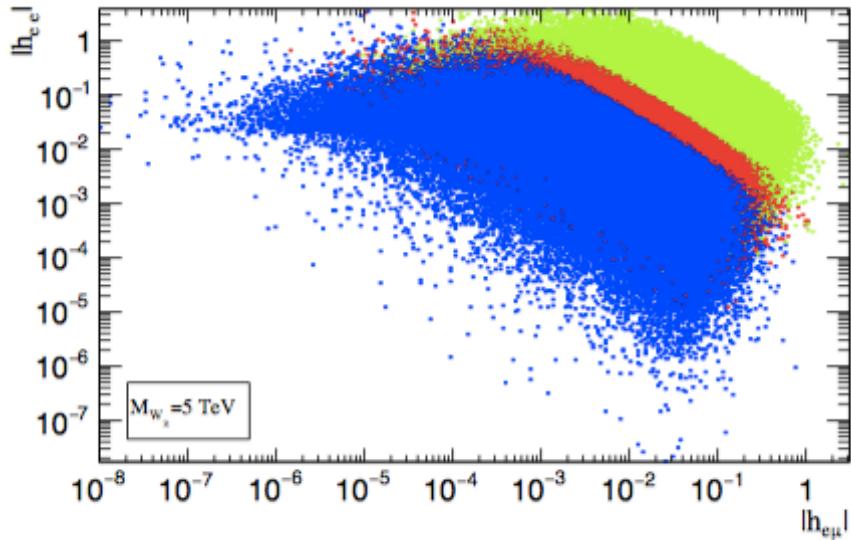
- Strong current bounds on  $\mu \rightarrow e\gamma$  &  $\mu \rightarrow eee$  (MEG, SINDRUM)
- LRM contributions to  $\mu \rightarrow e\gamma$ 
  - » 1-loop  $W_R$  exchange
  - » 1-loop  $\Delta_L^\pm, \Delta_{R,L}^{\pm\pm}$  exchange
- LRM contributions to  $\mu \rightarrow eee$ 
  - » Leading contributions: Tree-level  $\Delta_{R,L}^{\pm\pm}$  exchange

$$B(\mu^- \rightarrow e^- e^+ e^-) = \frac{1}{2} \left( \frac{\kappa M_W}{M_{W_R}} \right)^4 |h_{\mu e} h_{ee}^*|^2 \left( \frac{1}{x_{\Delta_L^{\pm\pm}}} + \frac{1}{x_{\Delta_R^{\pm\pm}}} \right)$$

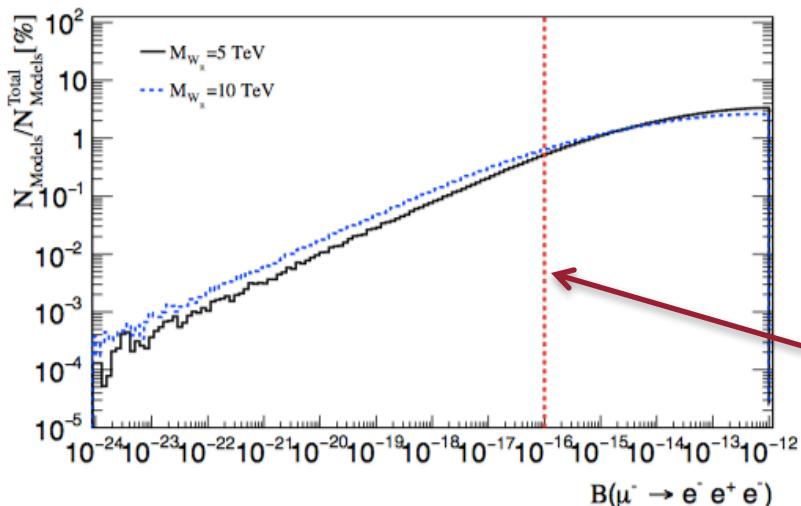
$$x_{\Delta_{L,R}^{\pm\pm}} = M_{\Delta_{L,R}^{\pm\pm}}^2 / M_{W_R}^2 \quad (h_R)_{ij} = \sum_n (V_R)_{ni} (V_R)_{nj} \frac{M_{N_n}}{M_{W_R}}$$

# $\mu \rightarrow \text{eee}$ Results

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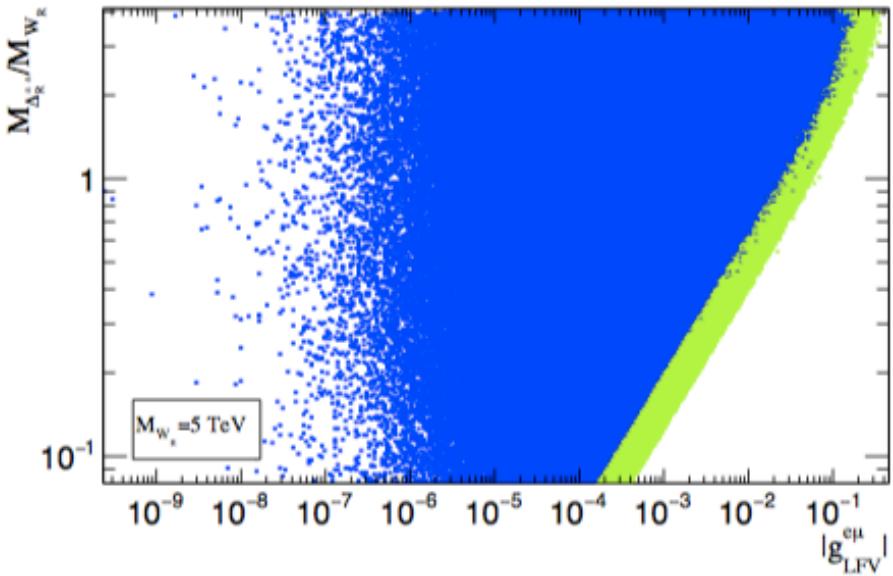
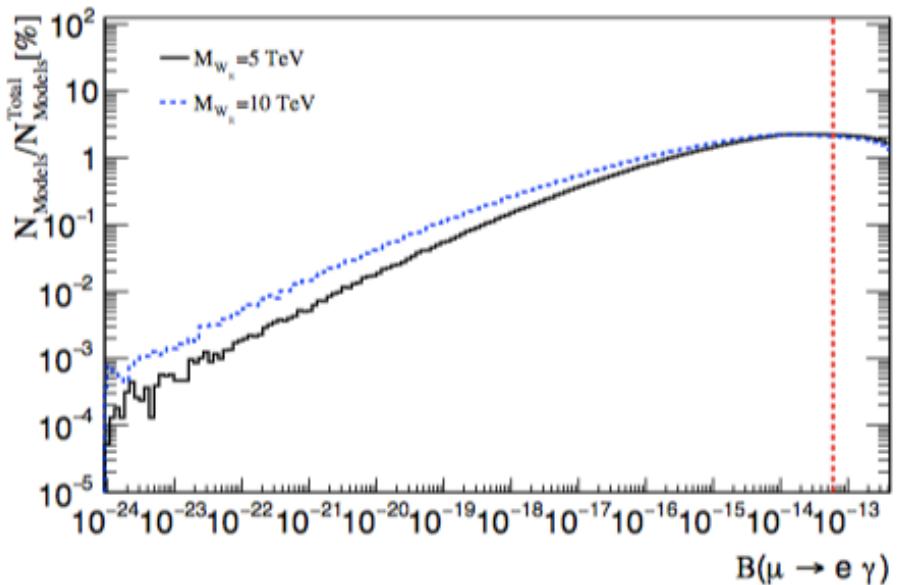
$\text{BR}(\mu \rightarrow \text{eee}) > 10^{-15}$   
 $\text{BR}(\mu \rightarrow \text{eee}) > 10^{-16}$   
 $\text{BR}(\mu \rightarrow \text{eee}) < 10^{-16}$



Mu3e would have good sensitivity

# $\mu \rightarrow e\gamma$ Results

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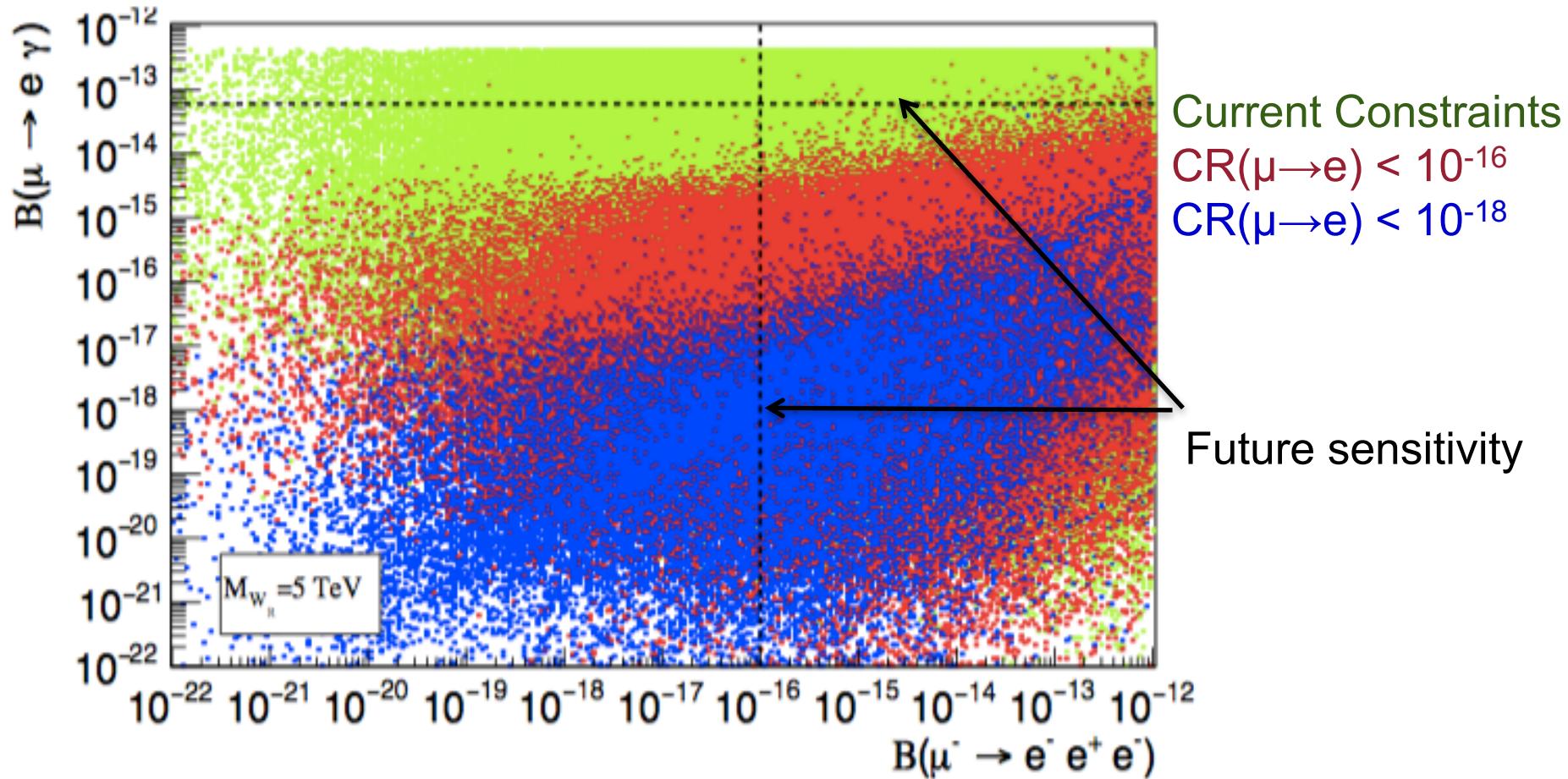


Consistent with current limits  
 $\text{BR}(\mu \rightarrow e\gamma) < 6 \times 10^{-14}$

$\mu \rightarrow e\gamma$  not a strong probe

# Comparison of LFV in the muon sector

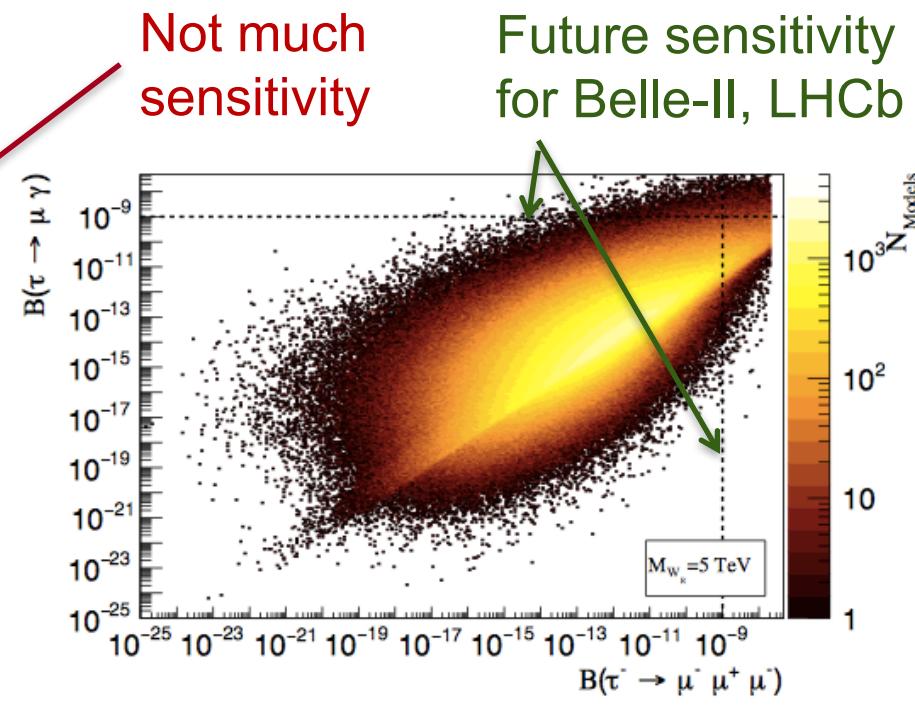
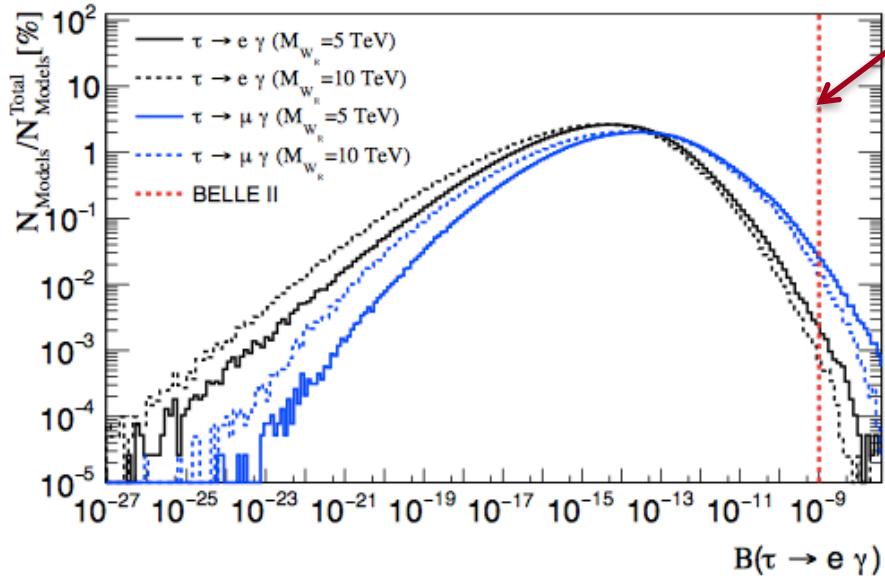
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# Rare tau decays

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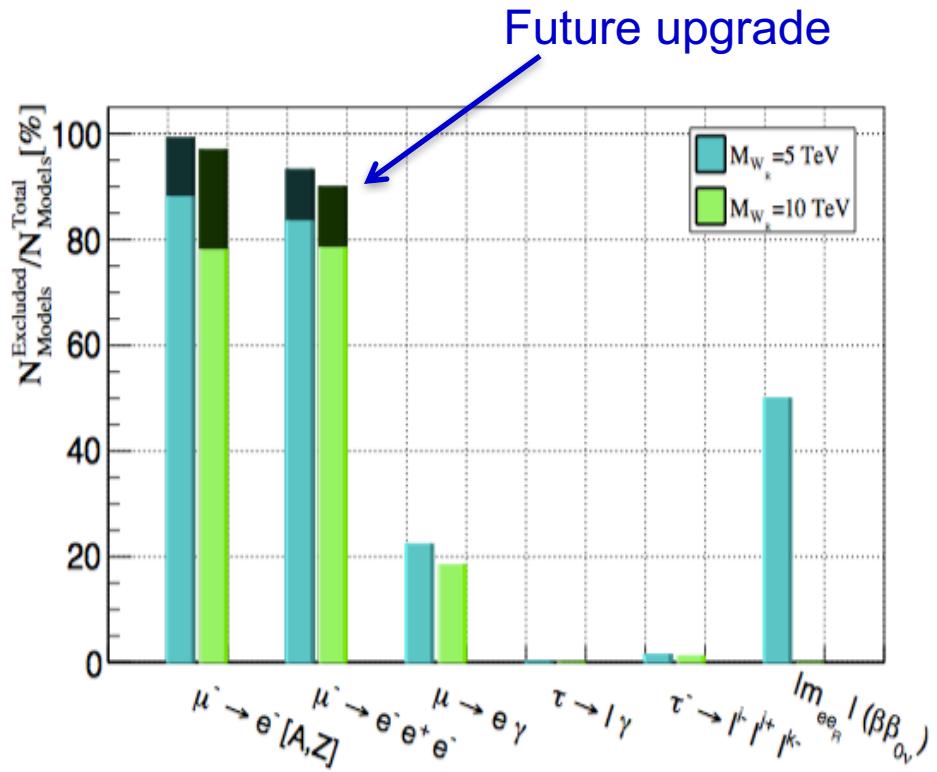
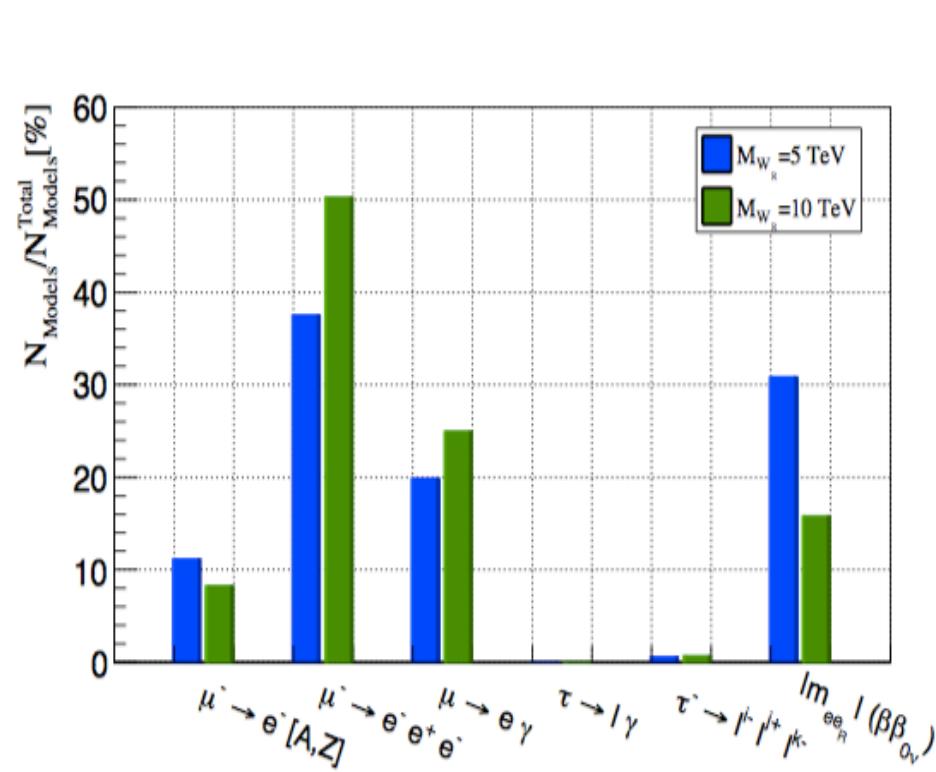
- Current limits from BaBar/Belle
- LRM contributions to  $\tau \rightarrow e\gamma, \mu\gamma$ 
  - » 1-loop  $W_R$  exchange
  - » 1-loop  $\Delta_L^\pm, \Delta_{R,L}^{\pm\pm}$  exchange
- LRM contributions to  $\tau \rightarrow \text{III}$ 
  - » Tree-level  $\Delta_{R,L}^{\pm\pm}$  exchange



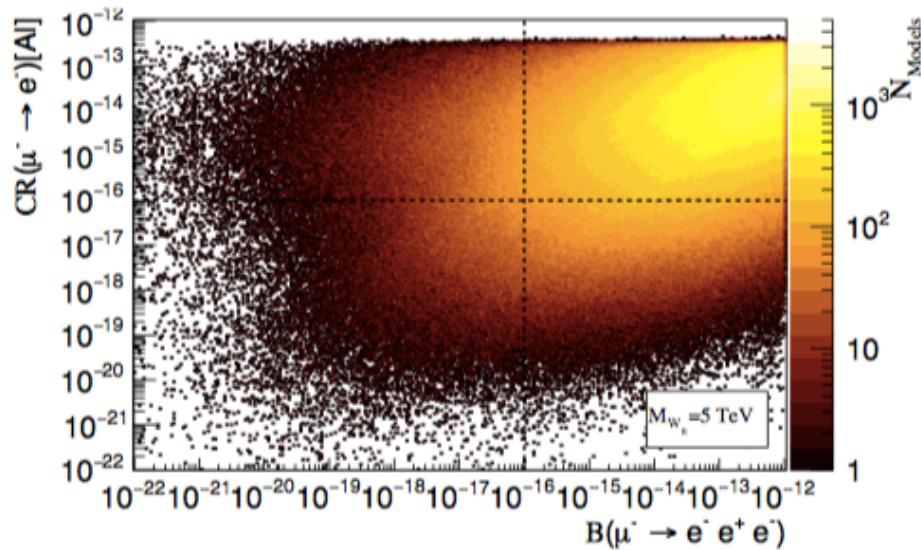
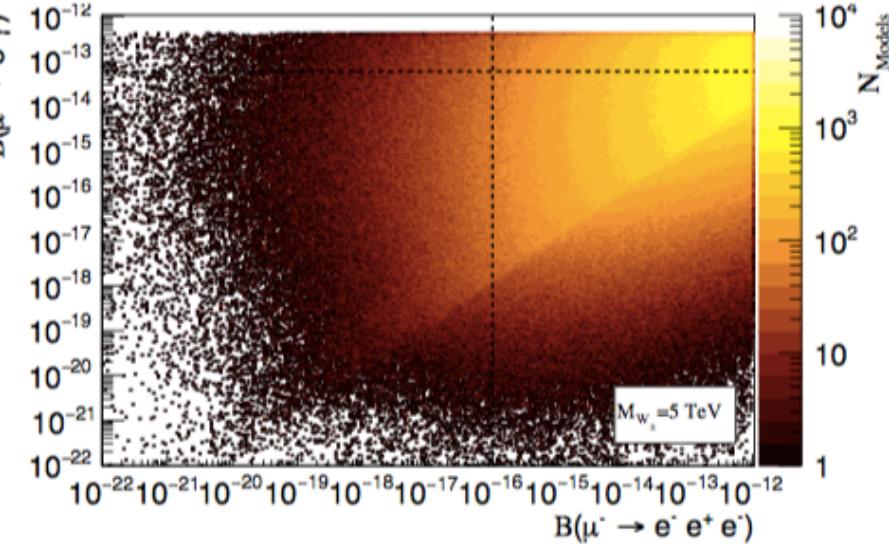
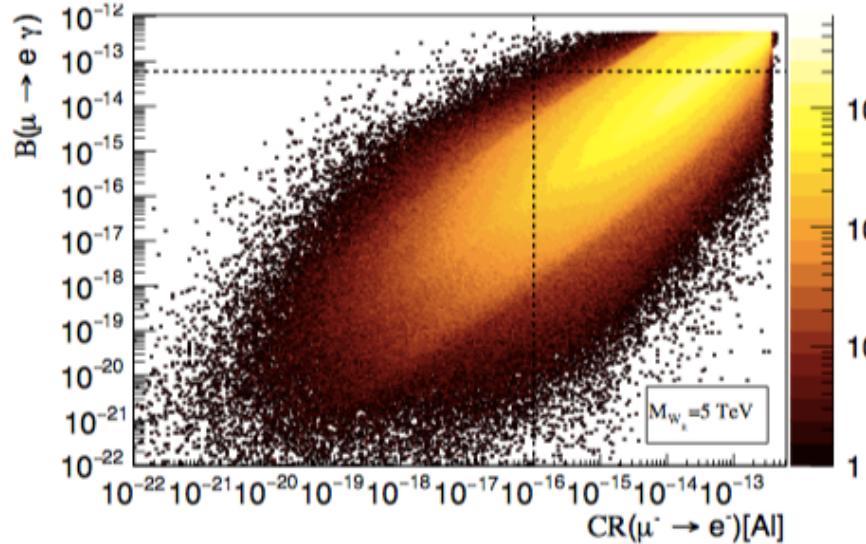
# LFV Reach Comparison

- Quantify relative importance of each variable by

$$R_i \equiv \frac{B_i}{B_i^{\text{exp}}}, \frac{\text{CR}_i}{\text{CR}_i^{\text{exp}}},$$



# Correlations Between Observables



# Correlations Between Observables

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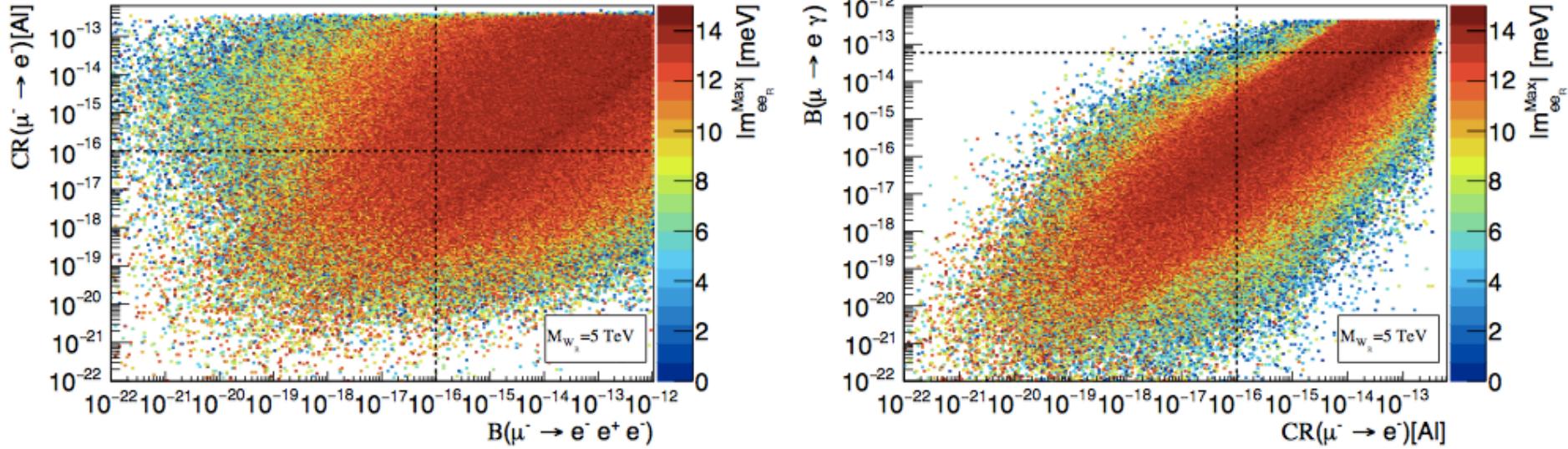


Figure 20: (Left) The maximum effective Majorana mass  $|m_{ee_R}^{\text{Max}}|$  in meV as a function of  $\mu^- \rightarrow e^-$  [Al] and  $\mu \rightarrow e^- e^+ e^-$ . (Right) The maximum effective Majorana mass  $|m_{ee_R}^{\text{Max}}|$  in meV as a function of  $\mu^- \rightarrow e^-$  [Al] and  $\mu \rightarrow e\gamma$ . In both panels the dashed lines indicate the expected future sensitivities to each LFV observable.

# Summary

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- LRM is a highly predictive scenario impacts the other frontiers
- Strong influence in LFV/LNV processes
- Mu2e &  $\mu \rightarrow eee$  have significant reach in this parameter space, outpassing direct collider sensitivity
- $0\nu\beta\beta$  has sensitivity to  $M_{W_R} = 5 \text{ TeV}$