

Frascati, 6 November 2017

# Study of quantum electrodynamics and chromodynamics in atomic bound systems

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Seminar organized within the project **Hunt for the Impossible atoms**  
Founded by the **John Templeton Foundation**

# Exotic atomic systems

- Simple atomic systems
  - accurate theoretical predictions
  - simple spectra

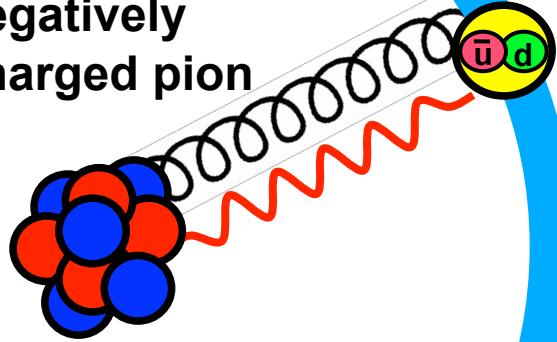
→ accurate test of fundamental interactions:

Quantum Electrodynamics (in strong field)  
and Chromodynamics (at low energy)

Highly charged ions

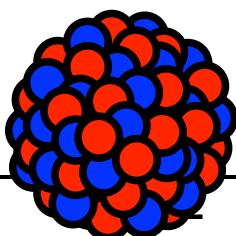
Pionic atoms

Atoms with a negatively charged pion



One-, two- three-electron atoms

$Z \gg 1$



# Summary

- Introduction
  - Test of QED in strong field
  - Study of strong interaction force at low energy
- Heavy highly charged ions
  - Production
  - Lamb shift measurement
  - Vacuum decay experiment
- Pionic atoms
  - Production
  - Pionic hydrogen and deuterium spectroscopy
  - Pion mass measurement
- Conclusions and outlooks

# Summary

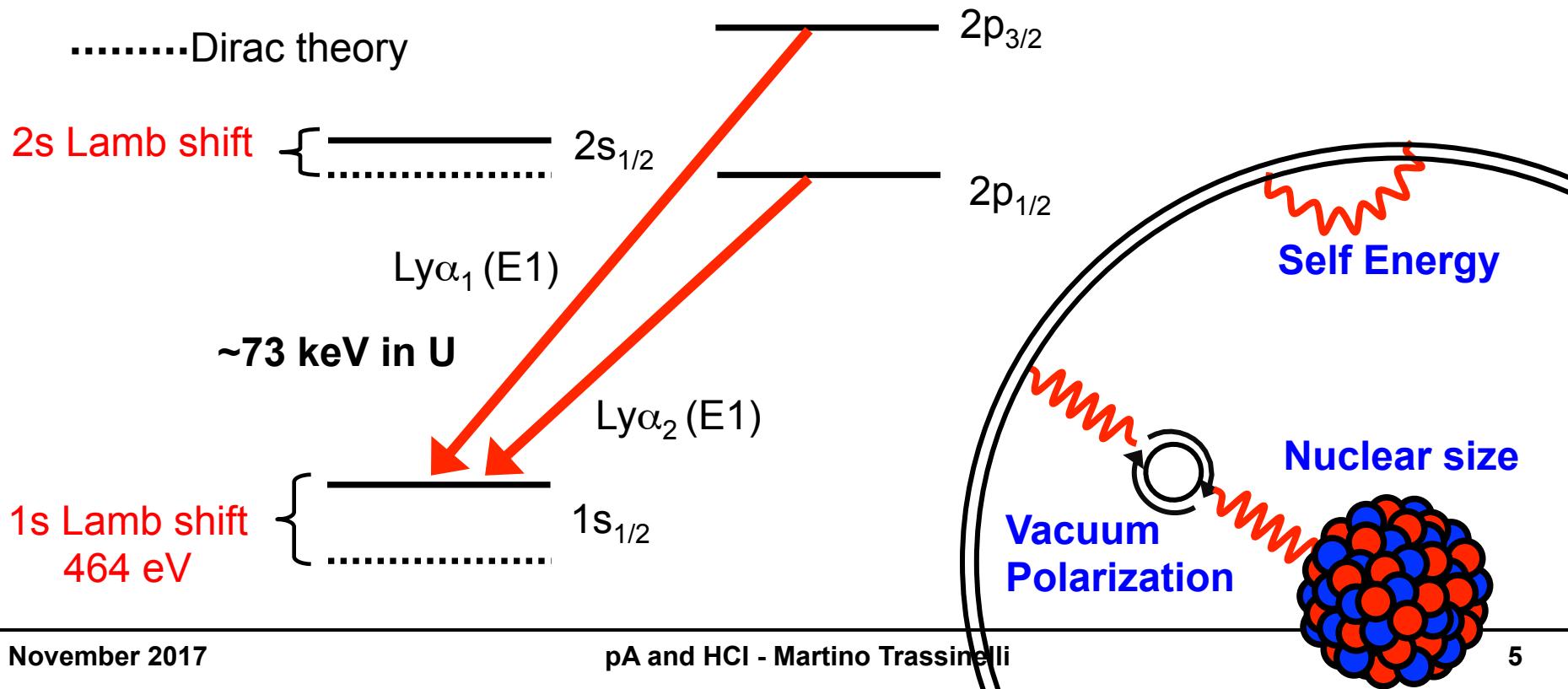
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# Highly charged ions

Dirac equation (spin-1/2 particles) →

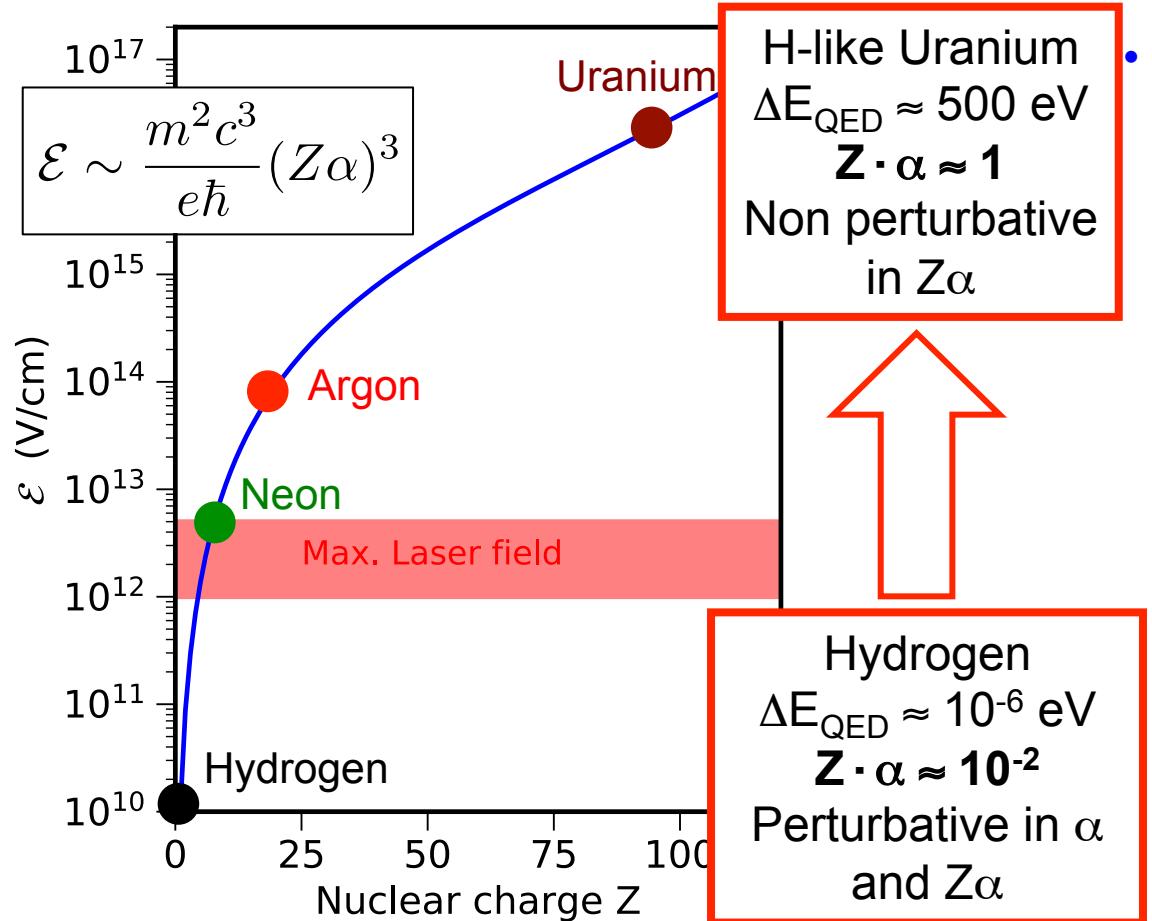
$$E^{nj} = \frac{mc^2}{\sqrt{1 + \frac{(Z\alpha)^2}{\left[n - j - 1/2 + \sqrt{(j + 1/2)^2 - (Z\alpha)^2}\right]^2}}}$$

- Simple atomic systems  
→ accurate theoretical predictions  
→ simple spectra

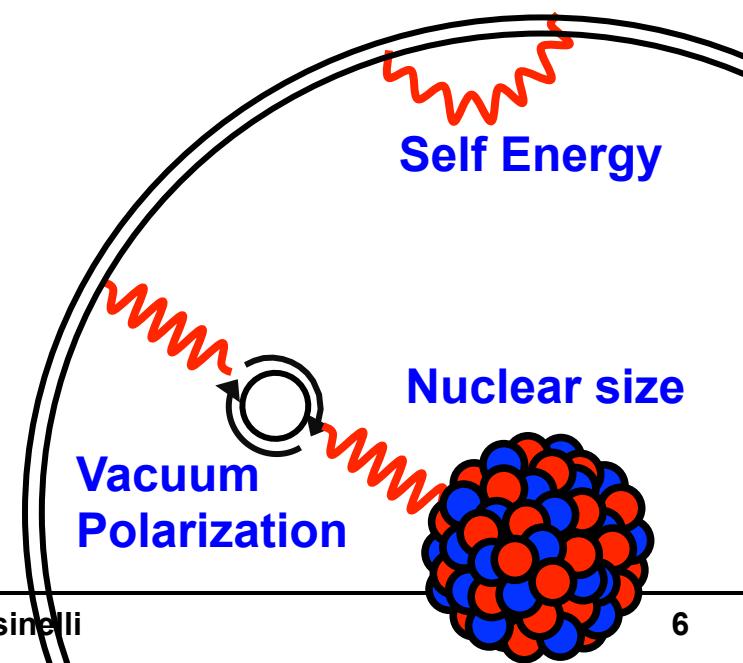


# Few electrons heavy charged ions

$$E_n = mc^2 \frac{(Z\alpha)^2}{2n^2} + \mathcal{O} [(Z\alpha)^4]$$



- Simple atomic systems  
 $\rightarrow$  accurate theoretical predictions  
 $\rightarrow$  simple spectra
- Strong electric field  
 $\rightarrow$  Quantum Electrodynamic effects enhanced  
 $\rightarrow$  Large perturbation during collisions with other atoms



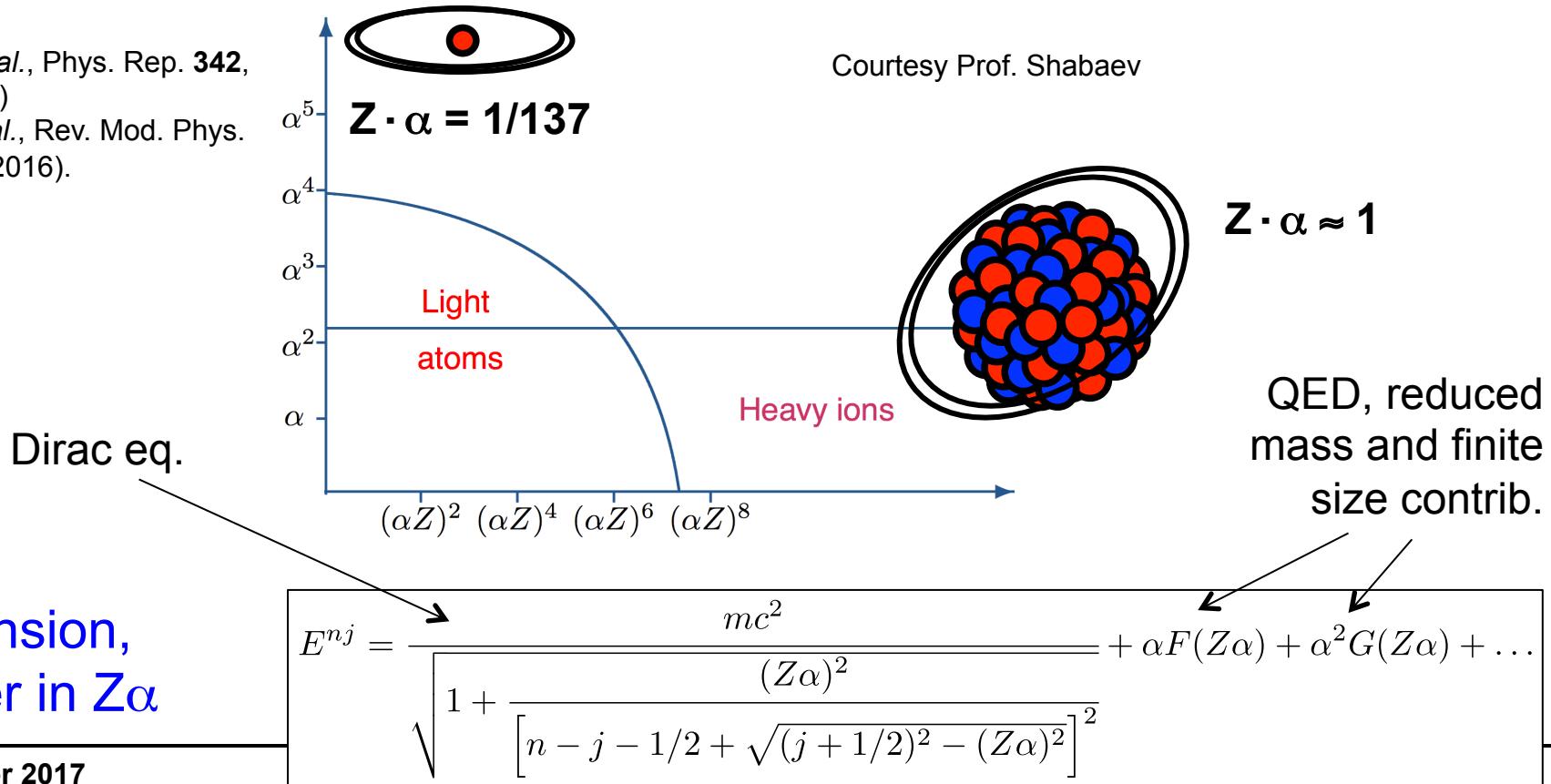
# Tests of QED calculations at strong-coupling regime

## $\alpha$ and $Z\alpha$ expansion

$$E^{nj} = mc^2 - mc^2 \frac{(Z\alpha)^2}{2n^2} + mc^2(Z\alpha)^4 [a(n,j) + \alpha b(n,j) + \alpha^2 c(n,j) + \dots] + \\ + mc^2(Z\alpha)^6 [a'(n,j) + \alpha b'(n,j) + \alpha^2 c'(n,j) + \dots] + \dots$$

M.I. Eides *et al.*, Phys. Rep. **342**, 63-261 (2001)  
 P.J. Mohr *et al.*, Rev. Mod. Phys. **88**, 035009 (2016).

Courtesy Prof. Shabaev



# Non-perturbative bound system QED

## First order in $\alpha$

### Self-energy

P.J. Mohr, Annals of Physics **88**, 26-51 (1974)



### Vacuum polarization

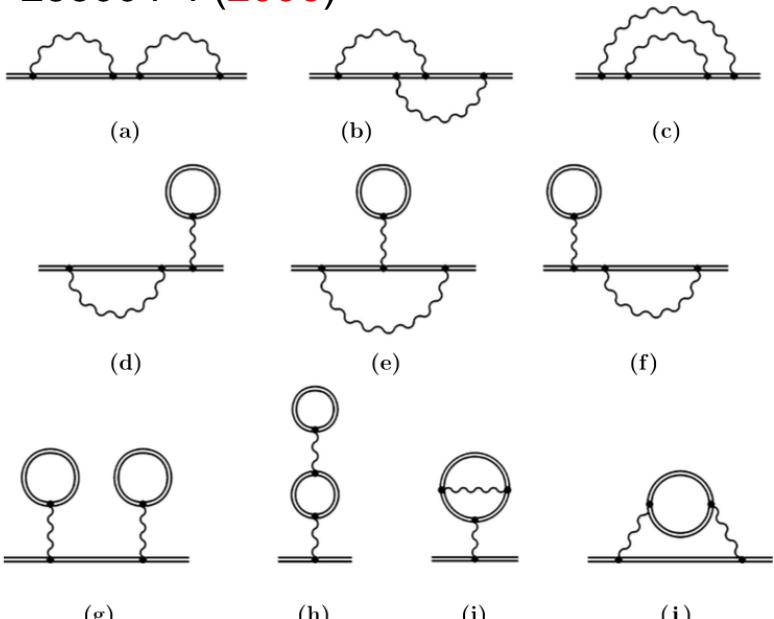
N.L. Manakov *et al.*, Sov. Phys. JETP **68**, 673-679 (1989)

G. Soff *et al.*, Phys. Rev. A **38**, 5066-5075 (1988)



## Second order in $\alpha$

V.A. Yerokhin *et al.*, Phys. Rev. Lett. **97**, 253004-4 (2006)



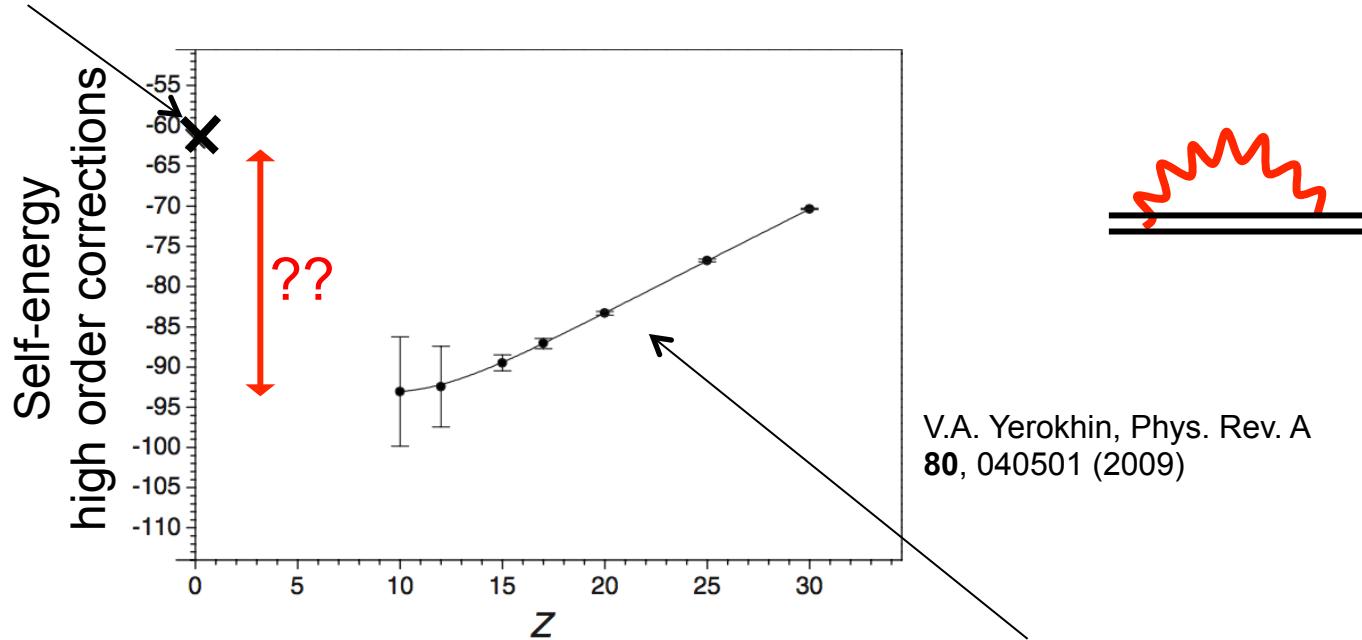
Dirac eq. (1928)

$$E^{nj} = \frac{mc^2}{\sqrt{1 + \left[ n - j - 1/2 + \sqrt{(j + 1/2)^2 - (Z\alpha)^2} \right]^2}} + \alpha F(Z\alpha) + \alpha^2 G(Z\alpha) + \dots$$

# Self-energy predictions

## $\alpha$ and $Z\alpha$ expansion

$$E^{nj} = mc^2 - mc^2 \frac{(Z\alpha)^2}{2n^2} + mc^2(Z\alpha)^4 [a(n,j) + \alpha b(n,j) + \alpha^2 c(n,j) + \dots] + \\ + mc^2(Z\alpha)^6 [a'(n,j) + \alpha b'(n,j) + \alpha^2 c'(n,j) + \dots] + \dots$$

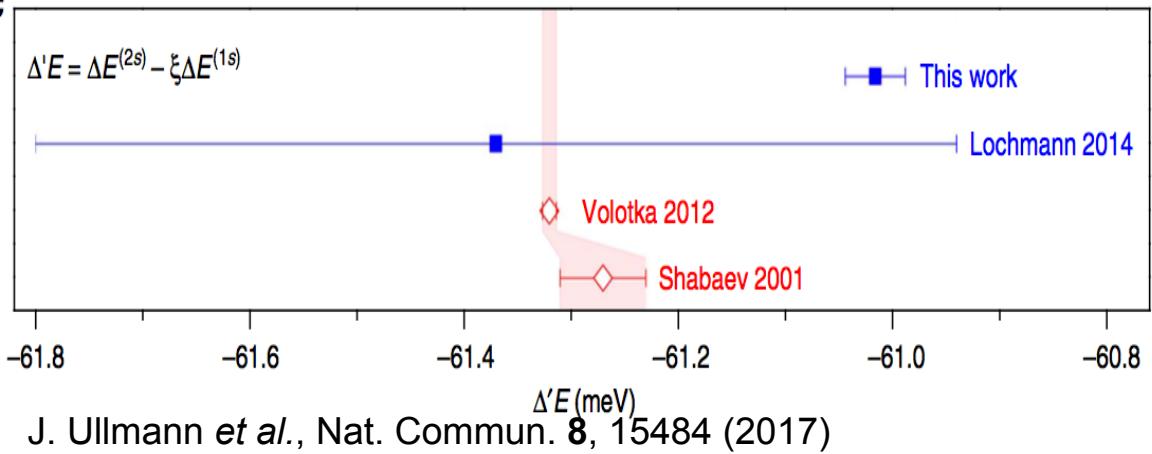


$$E^{nj} = \frac{mc^2}{\sqrt{1 + \left[ n - j - 1/2 + \sqrt{(j + 1/2)^2 - (Z\alpha)^2} \right]^2}} + \alpha F(Z\alpha) + \alpha^2 G(Z\alpha) + \dots$$

$\alpha$  expansion,  
all-order in  $Z\alpha$

# Quantum electrodynamics tests in atomic systems: open questions

## Hyperfine structure of H- and Li-like Bismuth



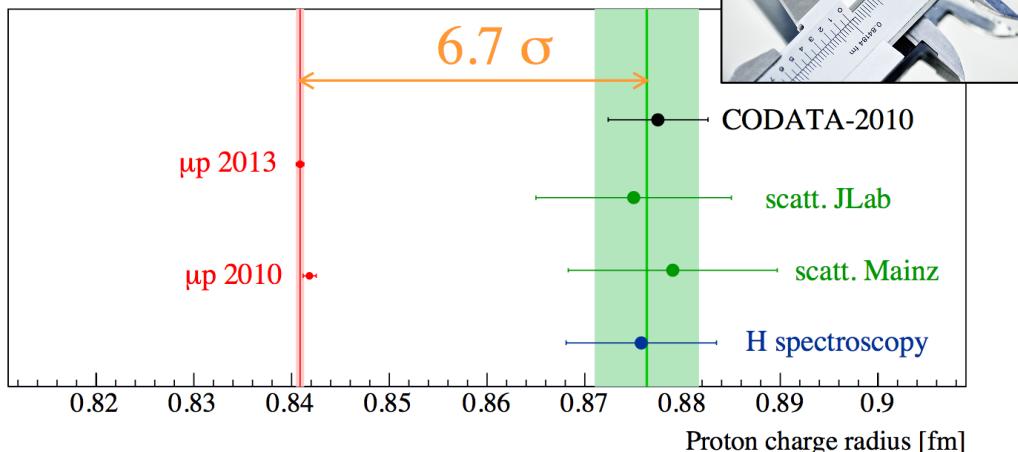
Laser spectroscopy of stored heavy ions

Strong disagreement between hydrogen and muonic hydrogen spectroscopy

$$m_\mu = 200 m_e$$

$$\mathcal{E} \sim \frac{m^2 c^3}{e\hbar} (Z\alpha)^3$$

## Proton radius puzzle



A. Antognini et al., Science 339, 417-420 (2013)  
R. Pohl et al., Nature 466, 213-216 (2010)

# Summary

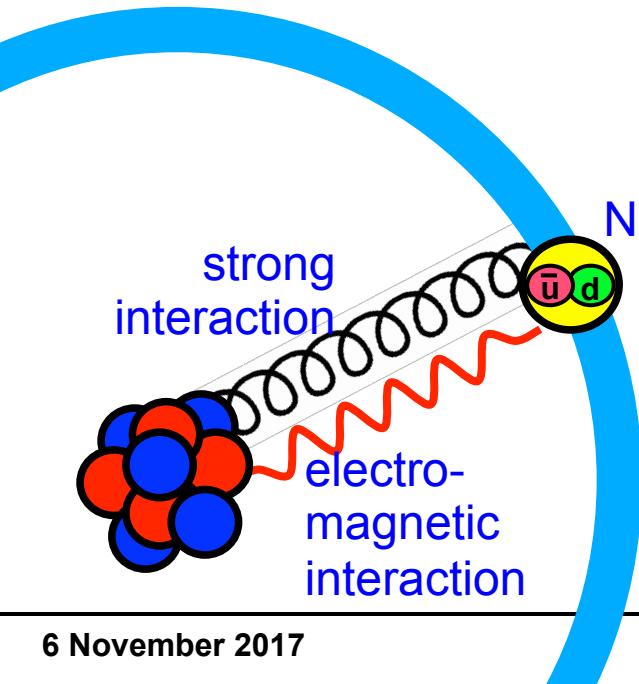
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- Conclusions and outlooks

# Pionic atoms

- Simple atomic systems
  - accurate theoretical predictions
  - simple spectra

**Klein-Gordon equation (spin-0 particles) →**

$$E^{nl} = \frac{mc^2}{\sqrt{1 + \frac{(Z\alpha)^2}{\left[n - l - 1/2 + \sqrt{(l + 1/2)^2 - (Z\alpha)^2}\right]^2}}}$$



Negative charged pion

- $m_\pi = 254 m_e$
- lifetime=26 ns

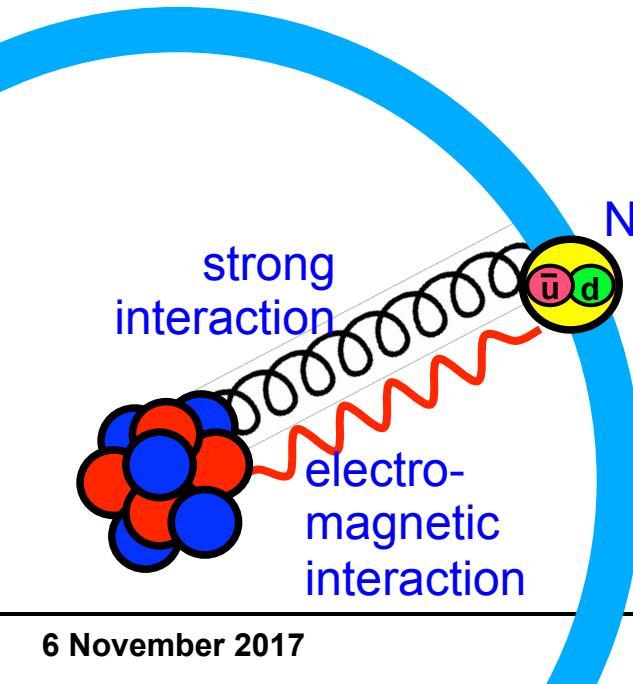
Hydrogen-like atoms

# Pionic atoms

- Simple atomic systems
  - accurate theoretical predictions
  - simple spectra
- Strong electric field
  - Quantum Electrodynamic effects enhanced
- Presence of strong interaction
- Small Bohr radius

$$E^{nl} = \frac{mc^2}{\sqrt{1 + \frac{(Z\alpha)^2}{[n - l - 1/2 + \sqrt{(l + 1/2)^2 - (Z\alpha)^2}]^2}}}$$

$$\mathcal{E} \sim \frac{m^2 c^3}{e\hbar} (Z\alpha)^3$$



Negative charged pion

- $m_\pi = 254 m_e$
- lifetime=26 ns

Hydrogen-like atoms

# Pionic atoms

- Electromagnetic interaction → bound system

- Strong interaction!!

$$E_n = mc^2 \frac{(Z\alpha)^2}{2n^2} + \mathcal{O}[(Z\alpha)^4]$$

# Attraction or repulsion

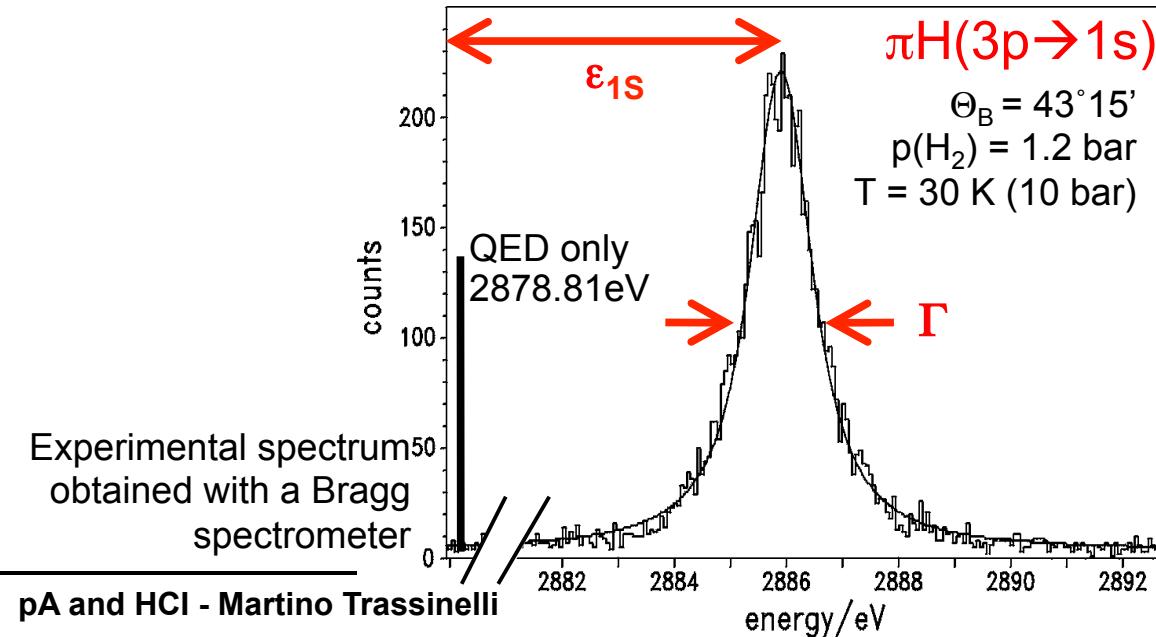
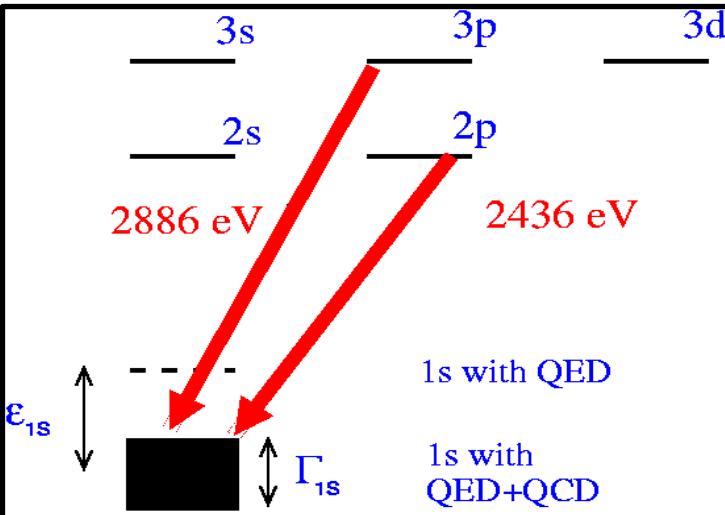
→ shift of the energy transition  $\varepsilon$

## Reaction with the nucleus

→ ground state instable

- lifetime of the atom not infinite
  - non-zero linewidth  $\Gamma$  of the atomic transitions

## Pionic hydrogen transitions

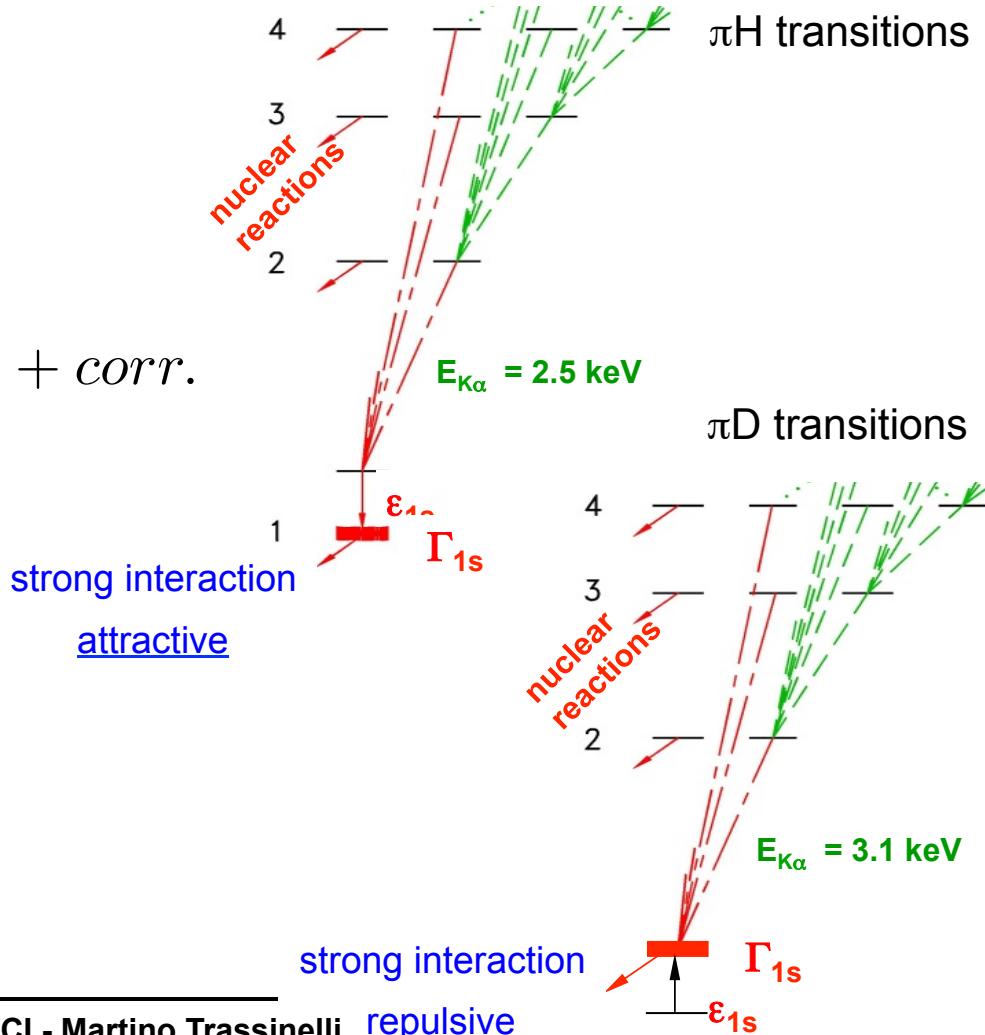


# Strong interaction in simple bound systems

Shift and width related to the pion-nucleus scattering length and cross sections

$$\pi H \left\{ \begin{array}{l} \epsilon_{1s}^{\pi H} \propto a_{\pi^- p \rightarrow \pi^- p} + \text{corr.} \\ \Gamma_{1s}^{\pi H} \propto (a_{\pi^- p \rightarrow \pi^0 n})^2 + \text{corr.} \end{array} \right.$$

$$\pi D \left\{ \begin{array}{l} \epsilon_{1s}^{\pi D} \propto a_{\pi^- p \rightarrow \pi^- p} + a_{\pi^- n \rightarrow \pi^- n} + \text{corr.} \\ \Gamma_{1s}^{\pi D} \propto \Im m(a_{\pi d \rightarrow \pi d}) \end{array} \right.$$

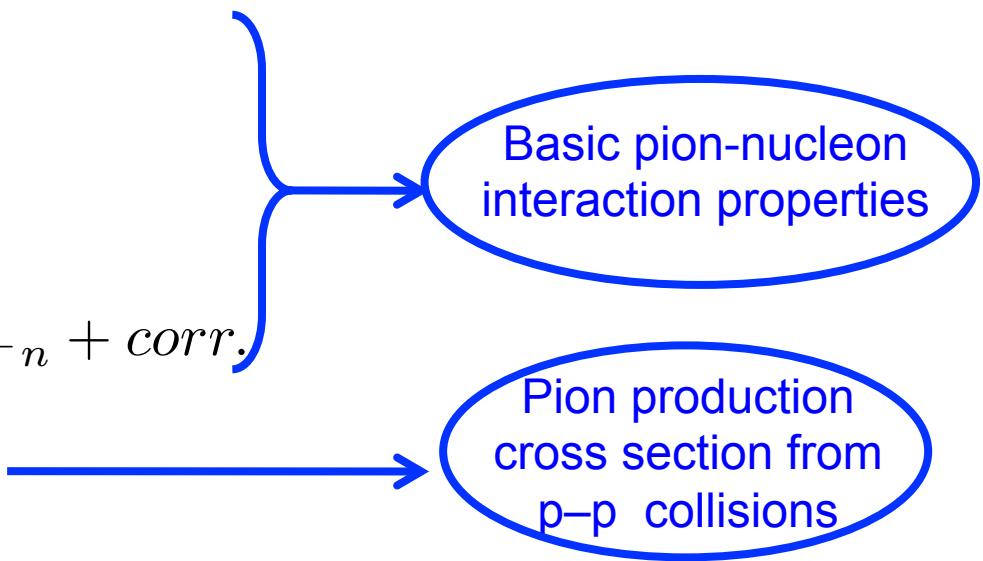


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# Highly charged ions and pionic atoms

- Simple atomic systems

$$E_n = mc^2 \frac{(Z\alpha)^2}{2n^2} + \mathcal{O} [(Z\alpha)^4]$$



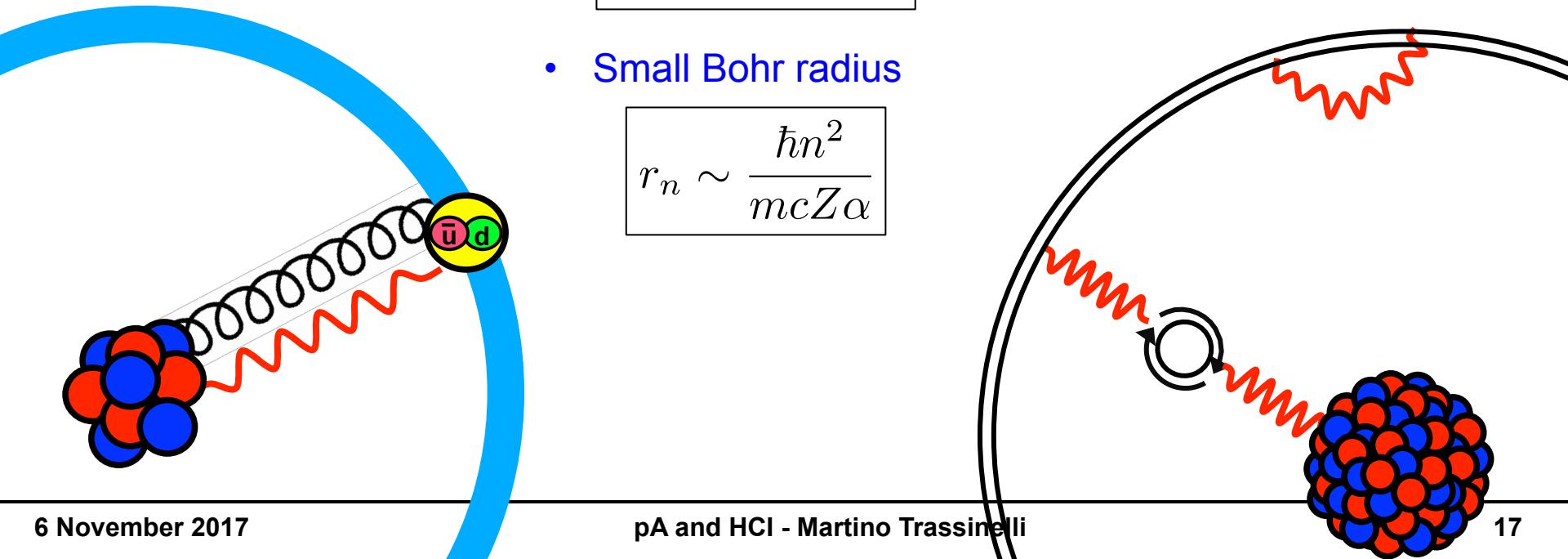
X-ray  
spectroscopy

- Strong electric field

$$\mathcal{E} \sim \frac{m^2 c^3}{e\hbar} (Z\alpha)^3$$

- Small Bohr radius

$$r_n \sim \frac{\hbar n^2}{mcZ\alpha}$$



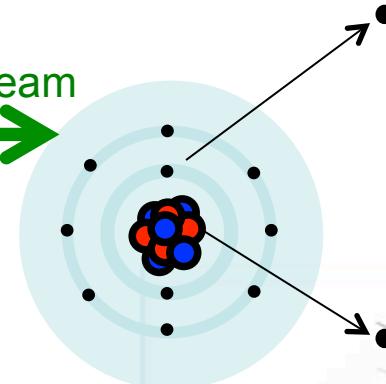
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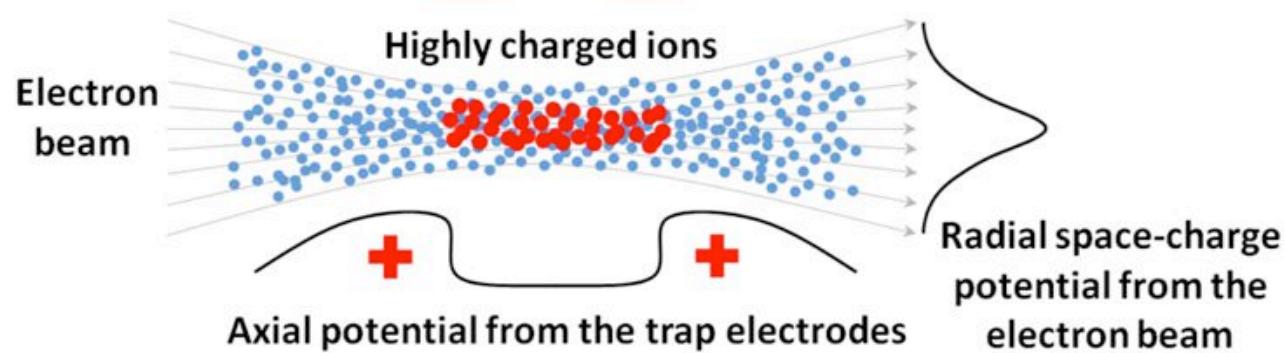
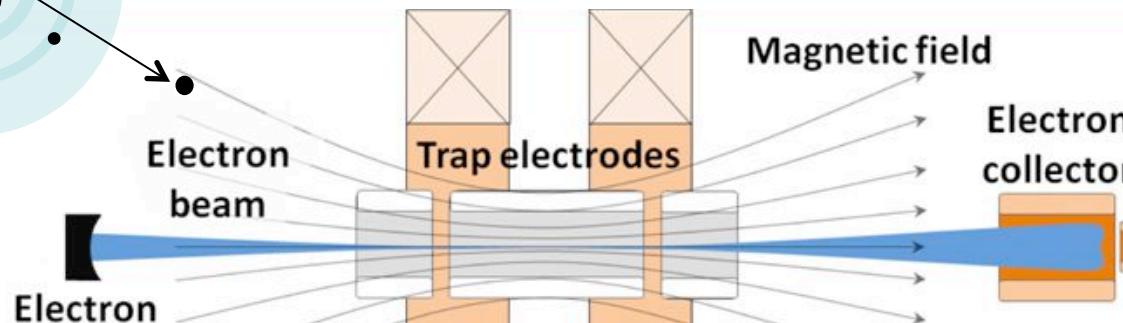
# Highly charged ion production and studies

## Electron impact and trapping

High energy electron beam  
 $V = 200 \text{ kV}$

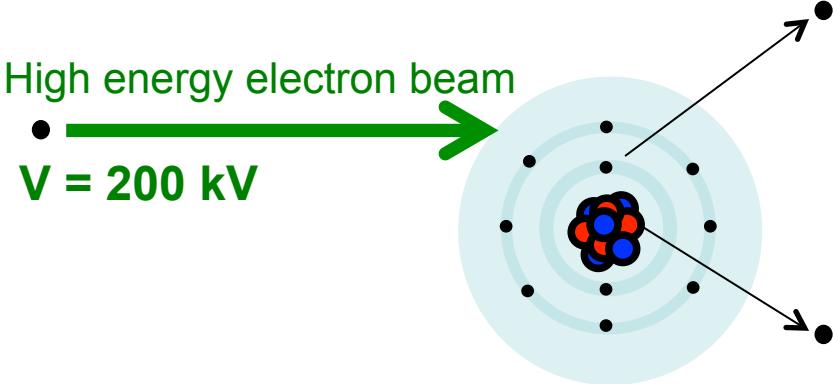


Electron Beam Ion Trap (EBIT) principle

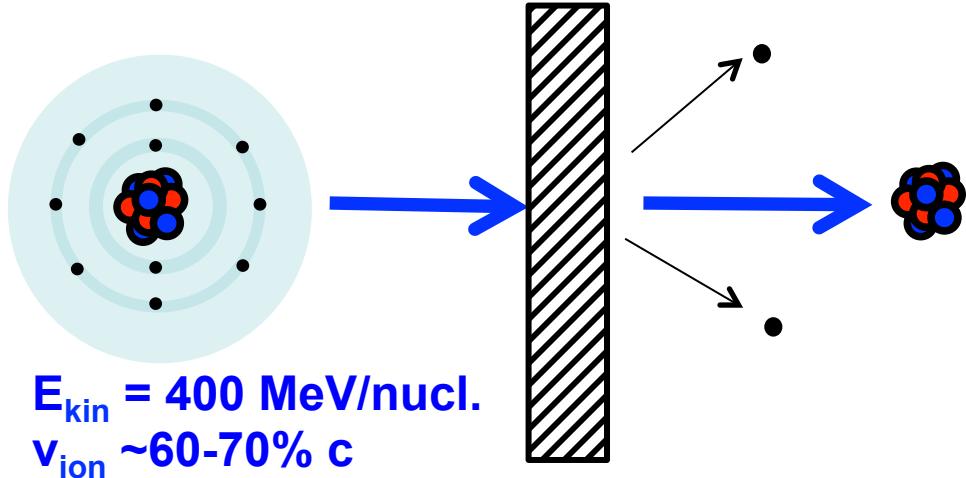


# Highly charged ion production and studies

## Electron impact and trapping



## Acceleration and stripping

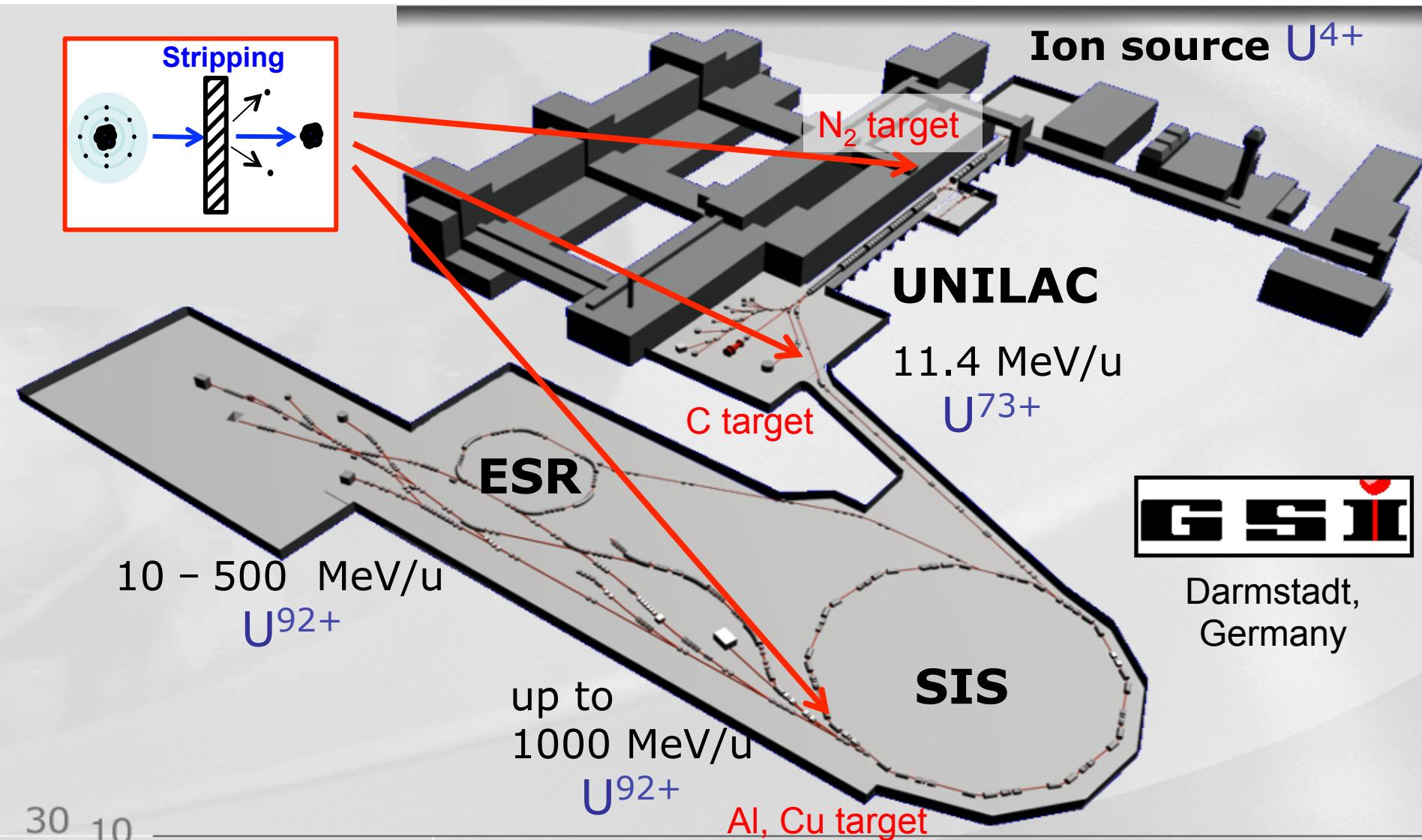


Solid target (graphite, aluminum, copper, ...)  
Thickness  $\sim 100 \text{ mg/cm}^2$

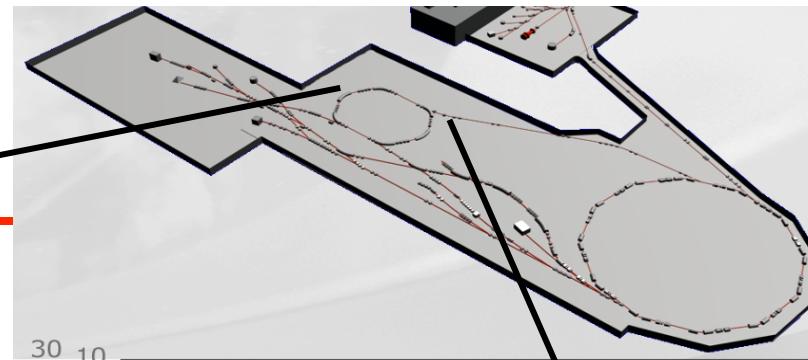
- Max Planck Inst., Heidelberg, Germany
- NIST, Gaithersburg, USA
- ...

- GSI, Darmstadt, Germany
- IMP, Lanzhou, China
- ...

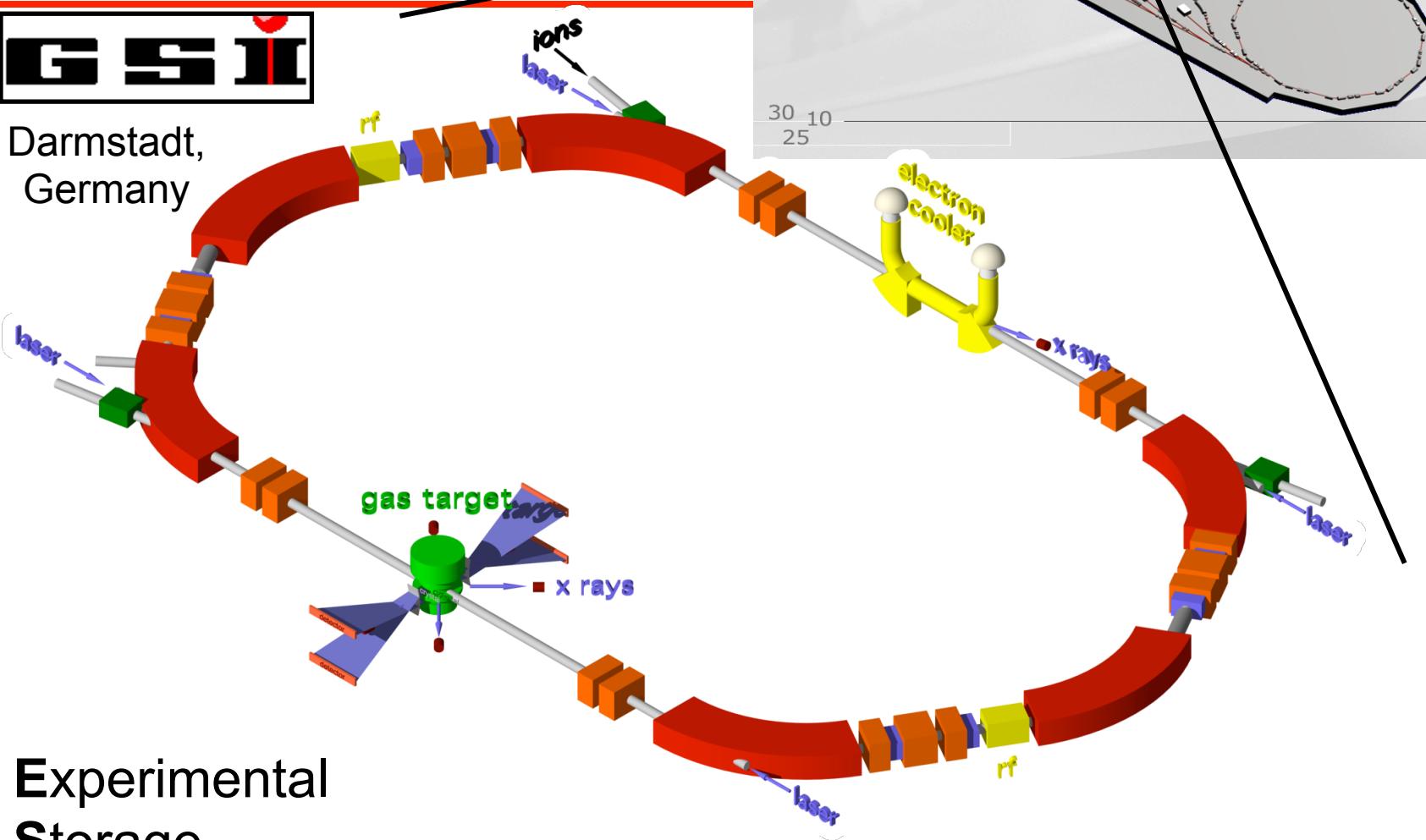
# Highly charged ion production



# ESR storage ring at GSI



Darmstadt,  
Germany

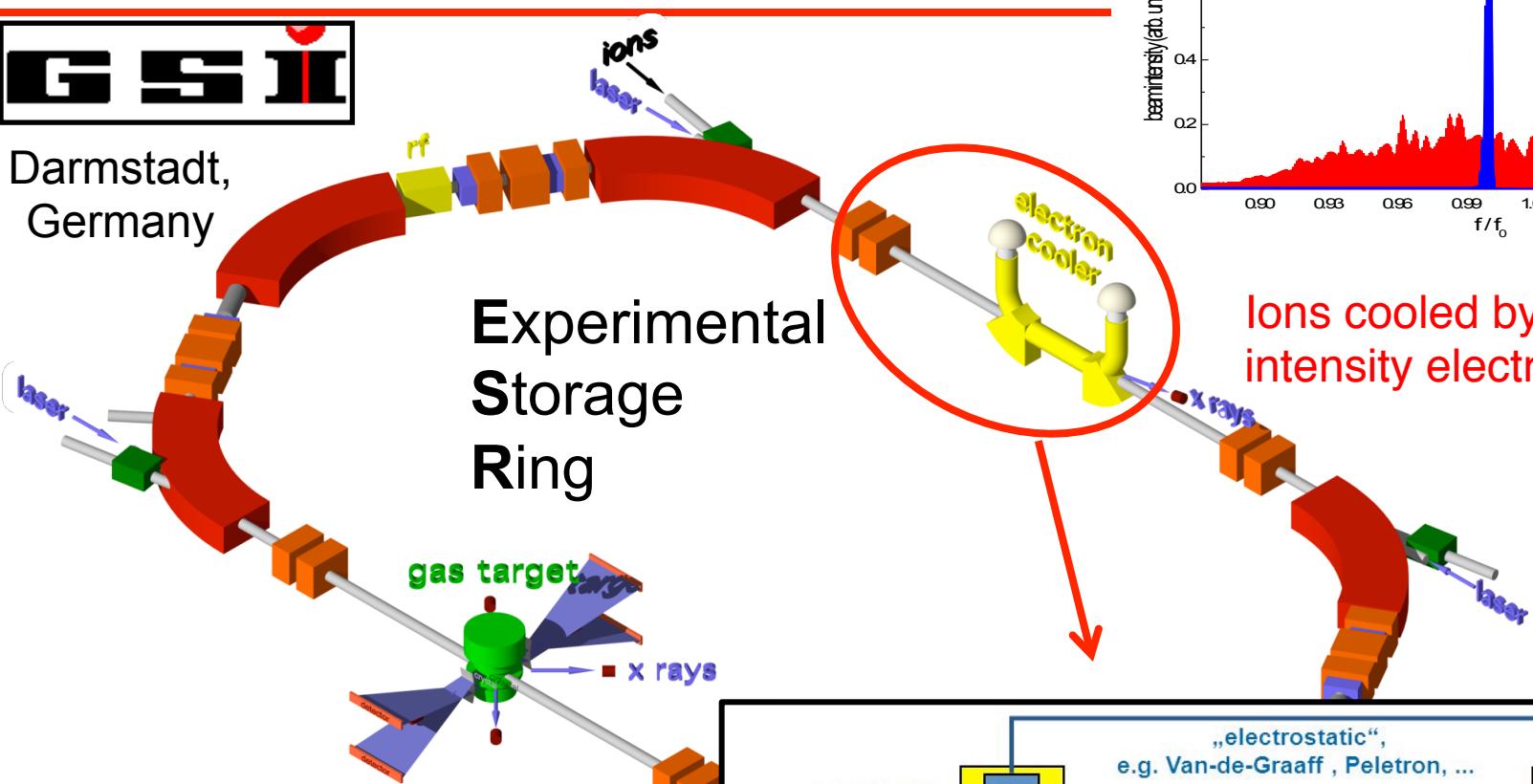


Experimental  
Storage  
Ring

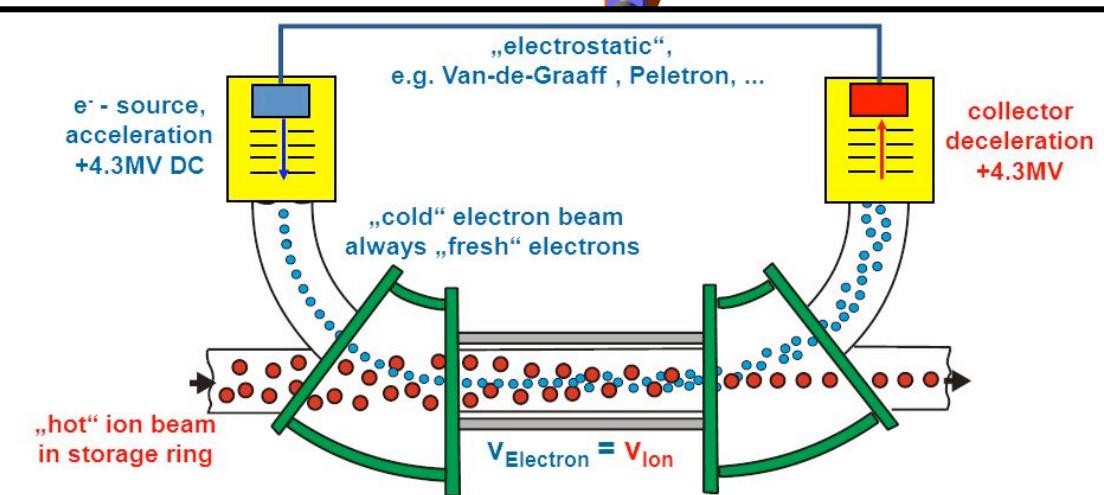
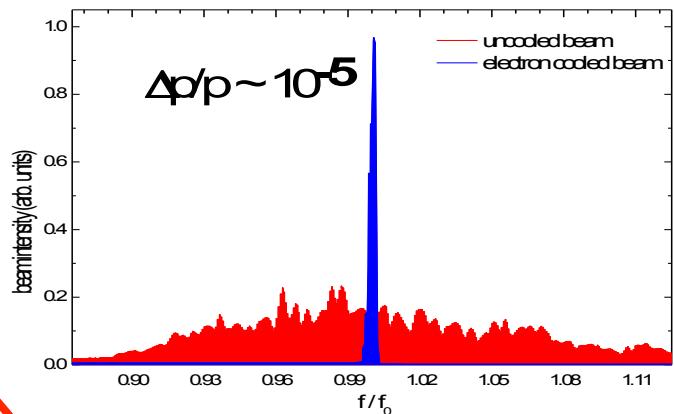
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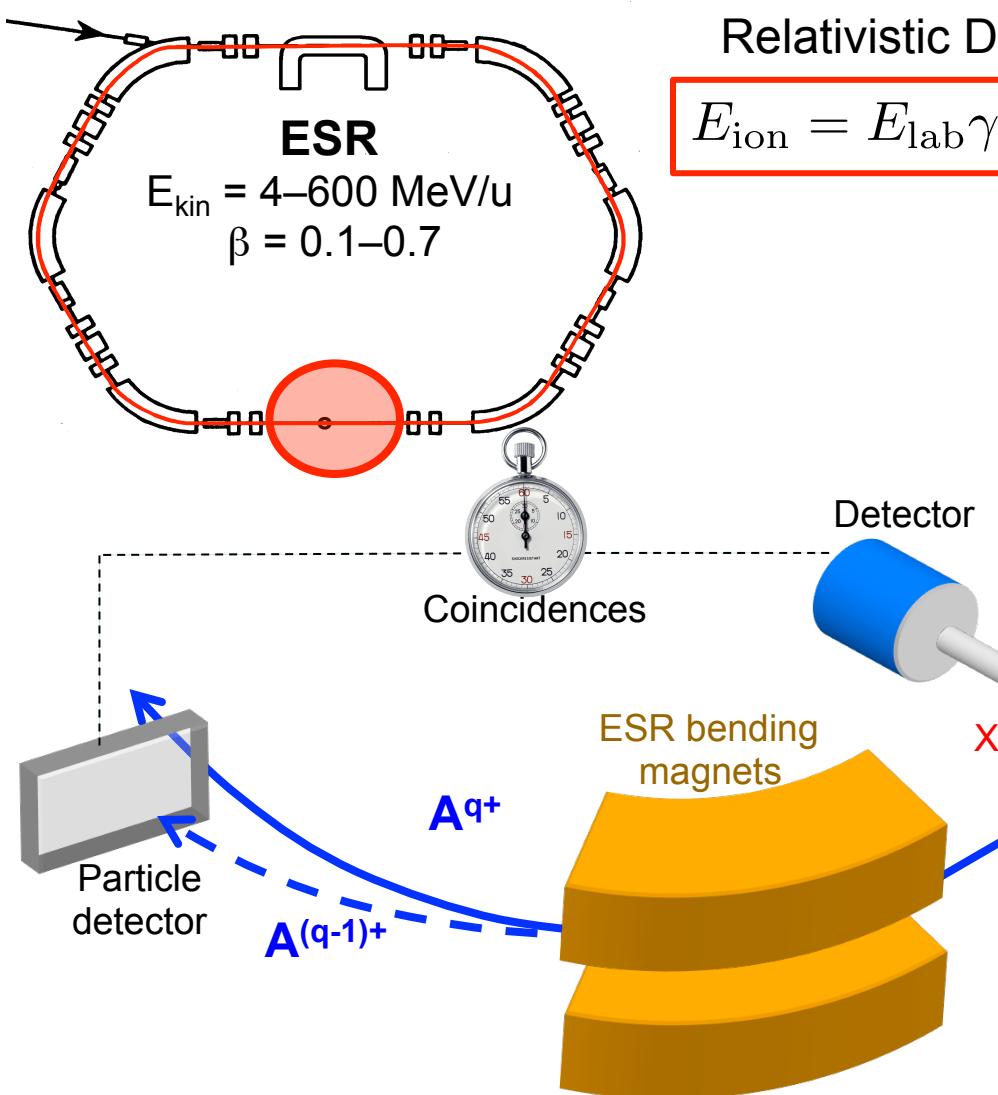
Darmstadt,  
Germany



Circumference: 108 m  
 Injection energy: 400 MeV/u  
 Ion energy: from 4 to 400 MeV/u  
 Revolution frequency: 1 Mhz  
 Stored ions:  $\sim 10^8$   
 Pressure =  $10^{-10-11}$  mbar

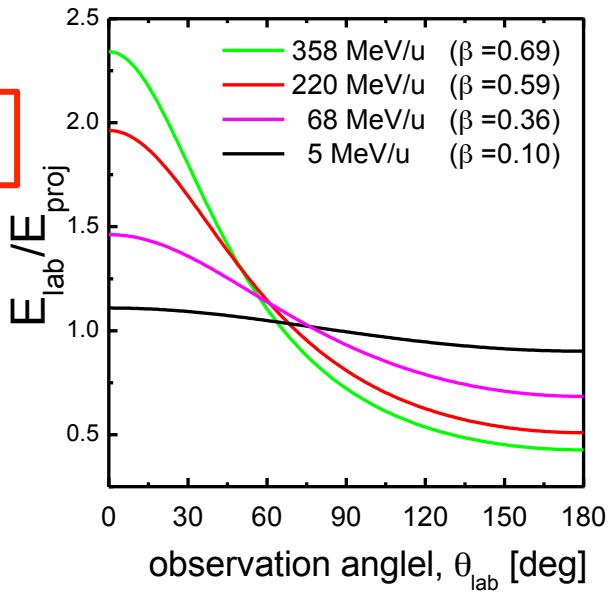


# Experiments at the gas jet-target

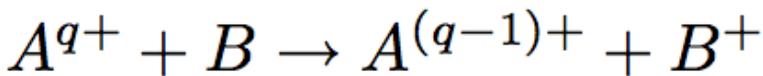


Relativistic Doppler shift

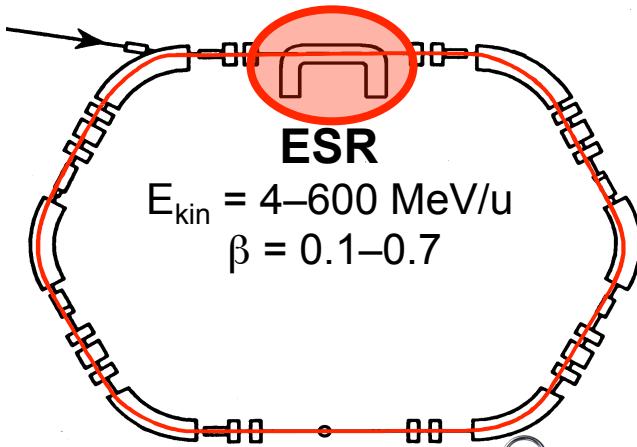
$$E_{\text{ion}} = E_{\text{lab}} \gamma (1 - \beta \cos \theta)$$



Electron transfer from the target atom to the fast ion

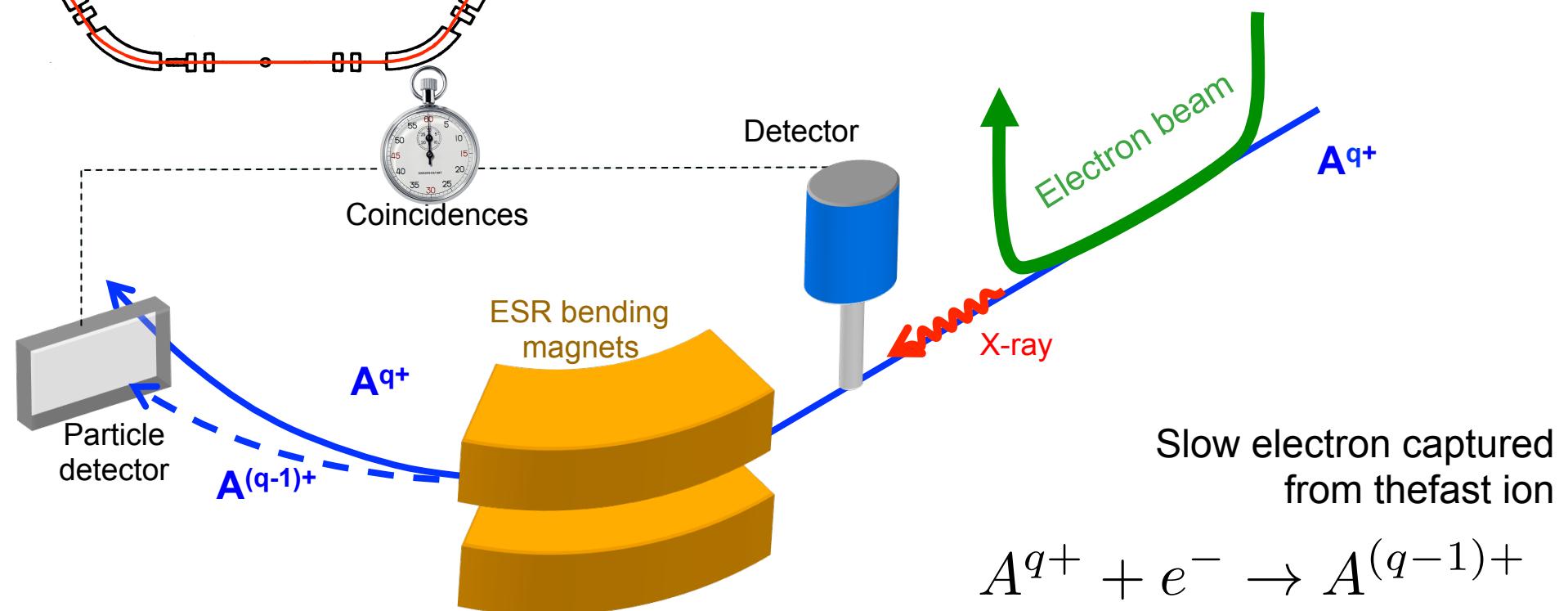
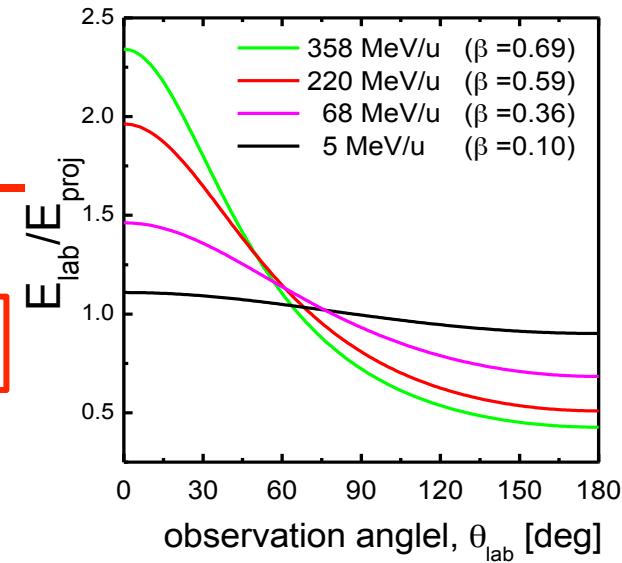


# Experiments at e-cooler



Relativistic Doppler shift

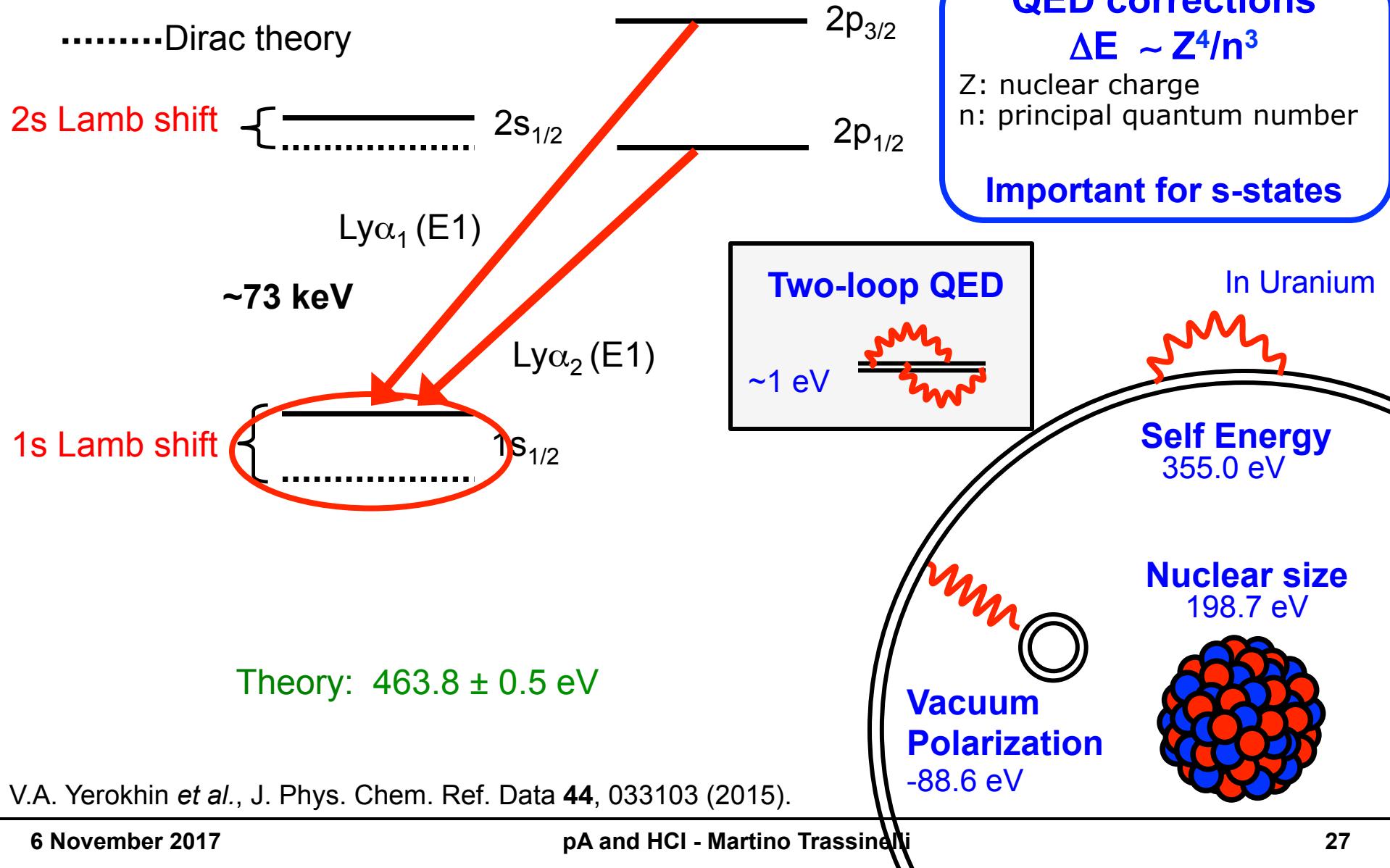
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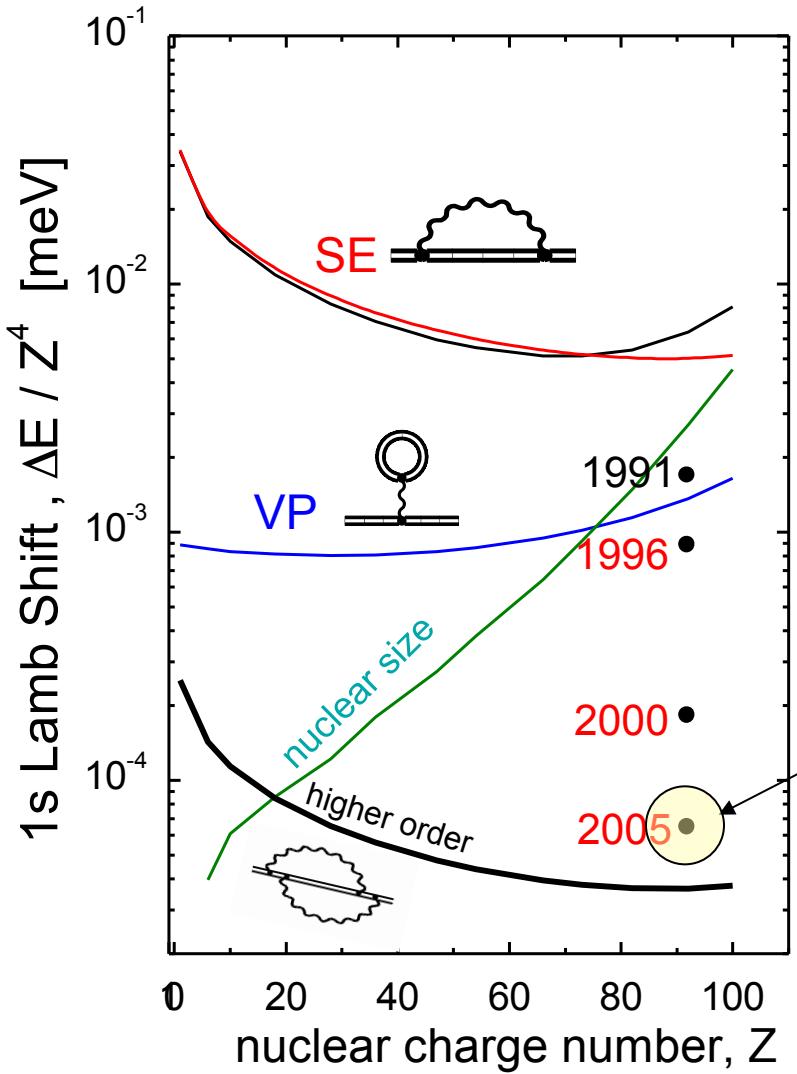
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  - **Lamb shift measurement**
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# Lamb shift of H-like Uranium



# Lamb shift of H-like Uranium



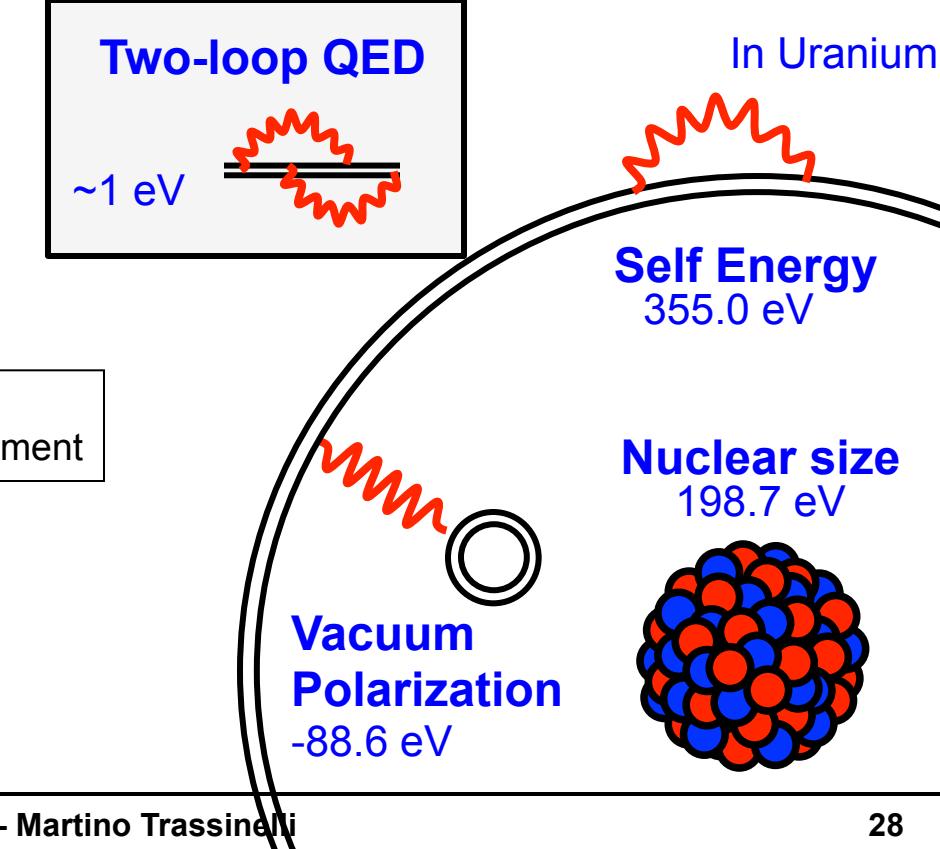
**QED corrections**  
 $\Delta E \sim Z^4/n^3$

$Z$ : nuclear charge  
 $n$ : principal quantum number

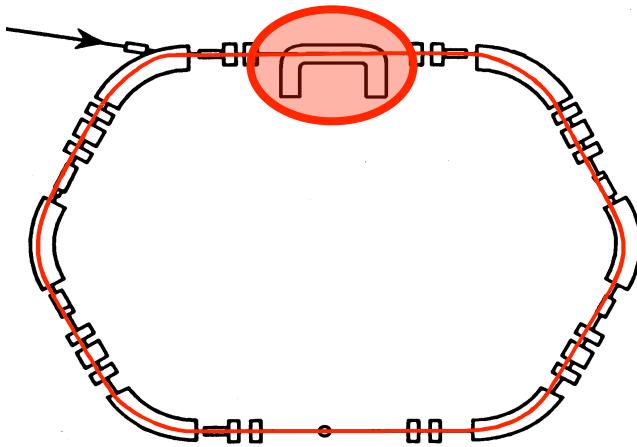
Important for s-states

Two-loop QED

~1 eV

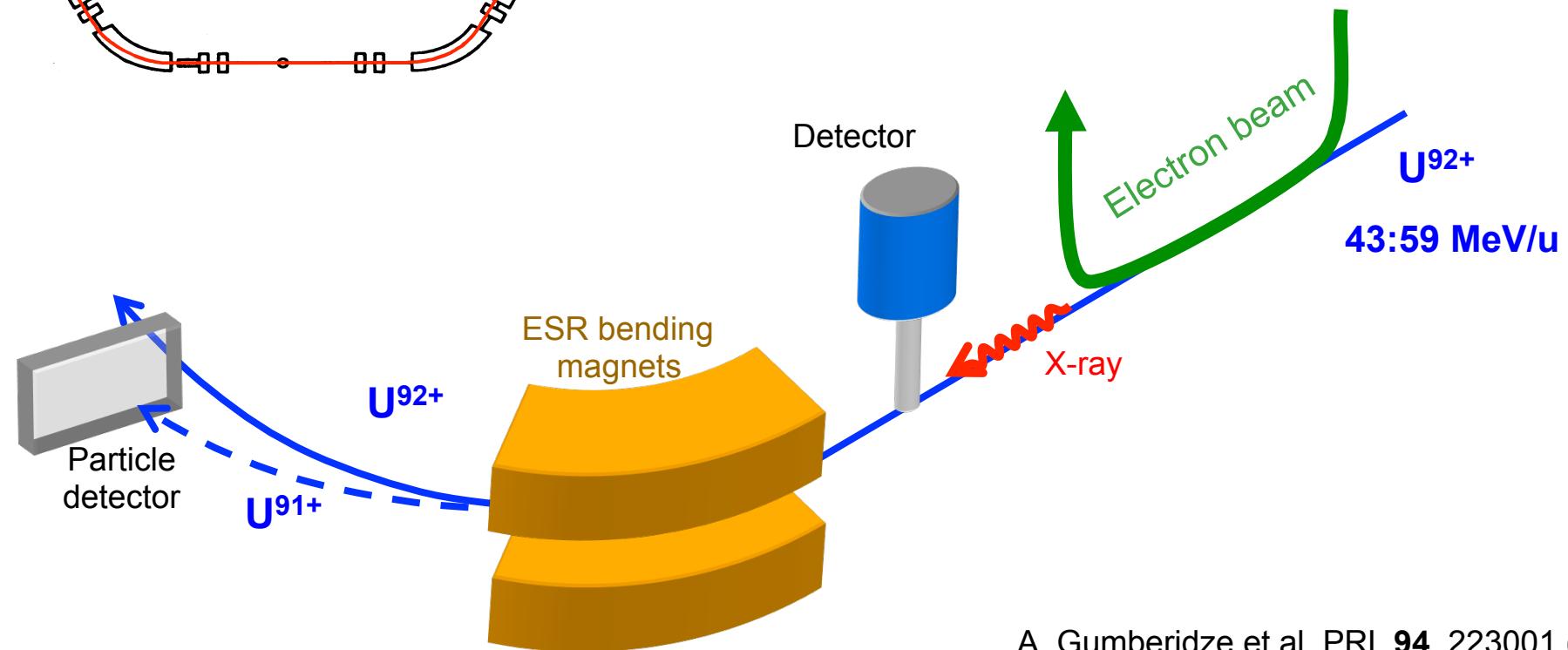
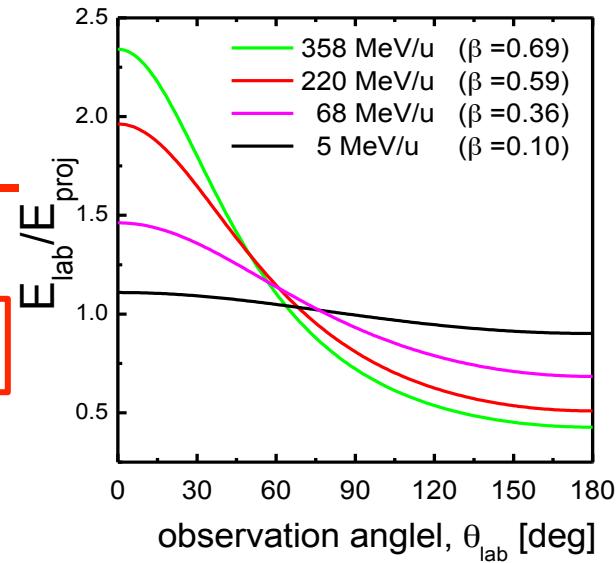


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Relativistic Doppler shift

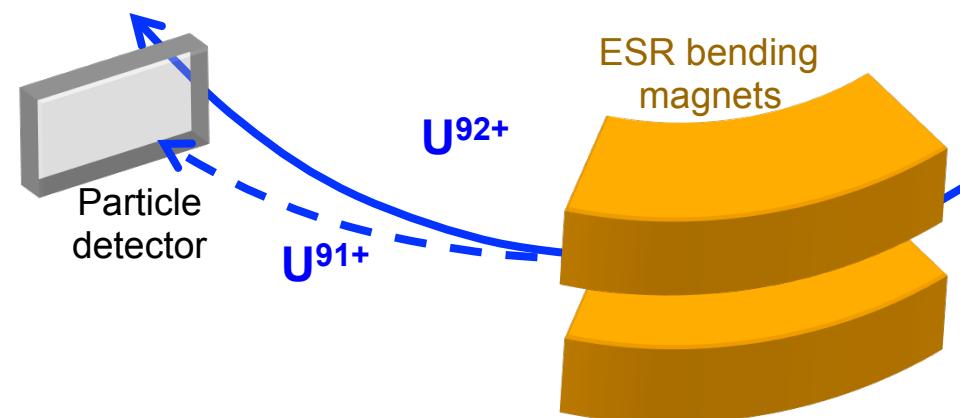
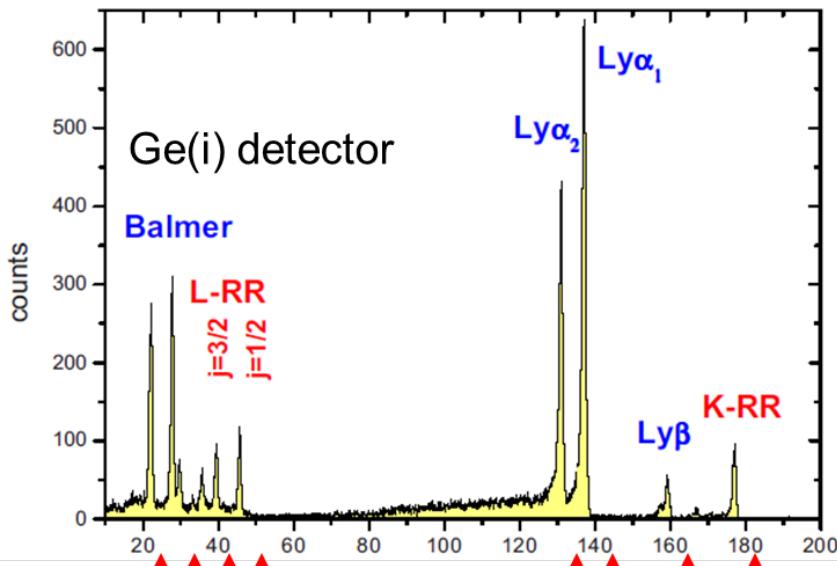
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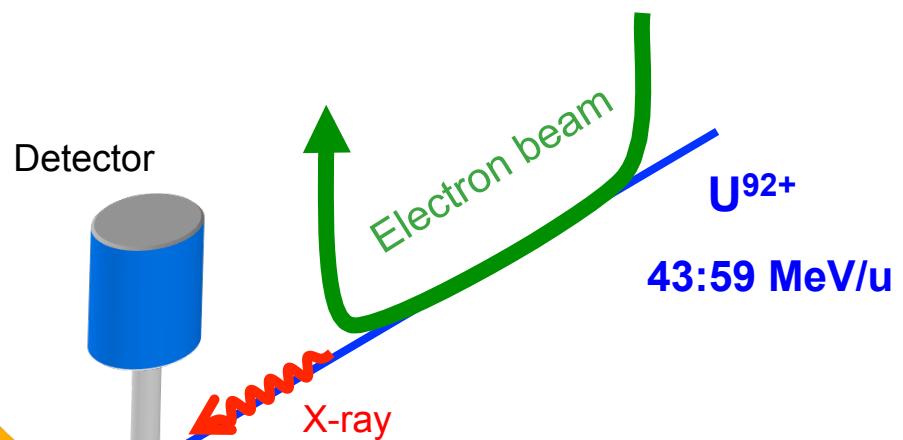
A. Gumberidze et al., PRL 94, 223001 (2005)

# Experiments at e-cooler

Many lines providing intrinsic energy calibration and redundant data.



- decelerated ions
- close to 0-deg observation geometry
- standard germanium detector



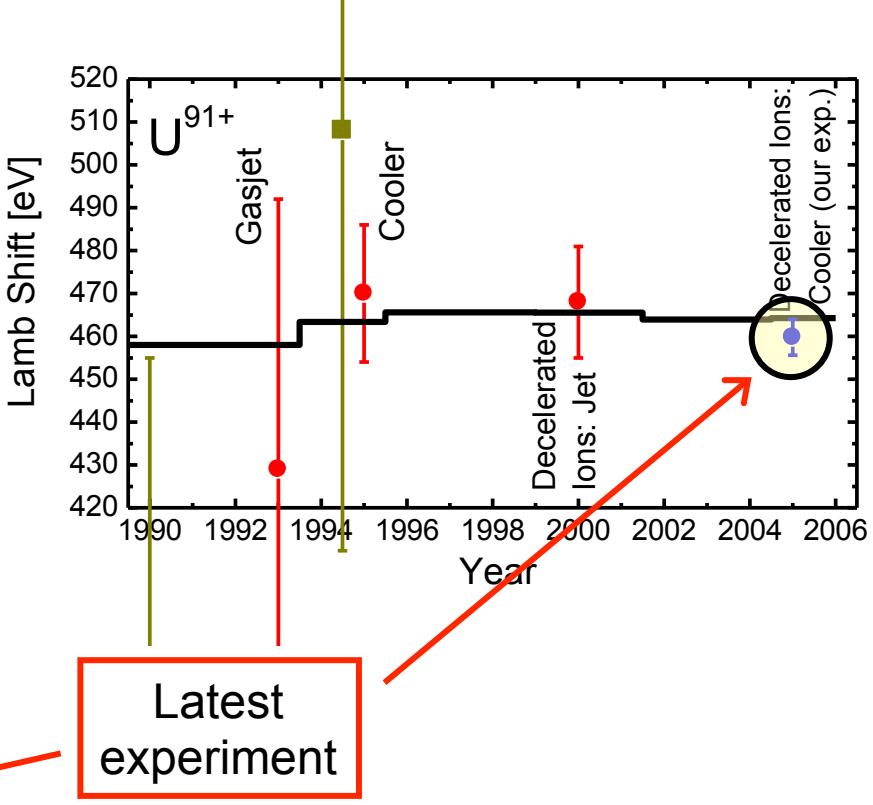
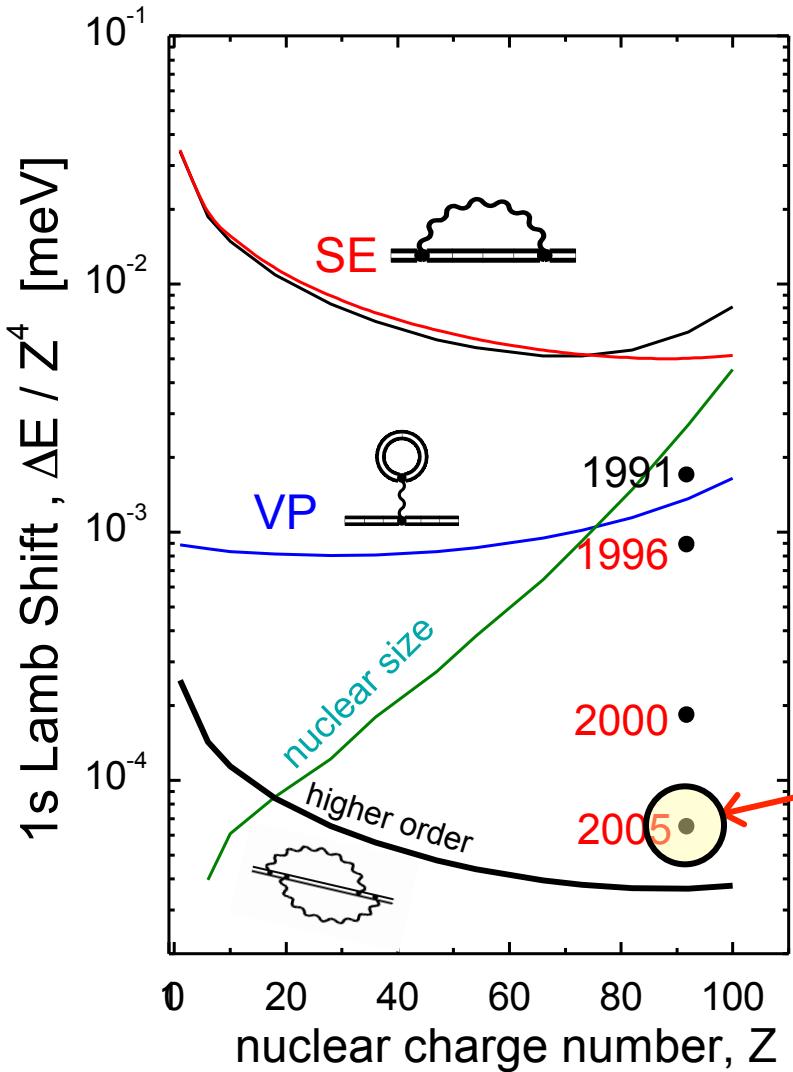
**Experiment :  $460.2 \pm 4.6 \text{ eV}$**

**Theory:  $463.8 \pm 0.5 \text{ eV}$**

**Most stringent test of bound-state QED for one-electron high-Z systems**

A. Gumberidze et al., PRL 94, 223001 (2005)

# Lamb shift of H-like Uranium



Experiment :  $460.2 \pm 4.6$  eV

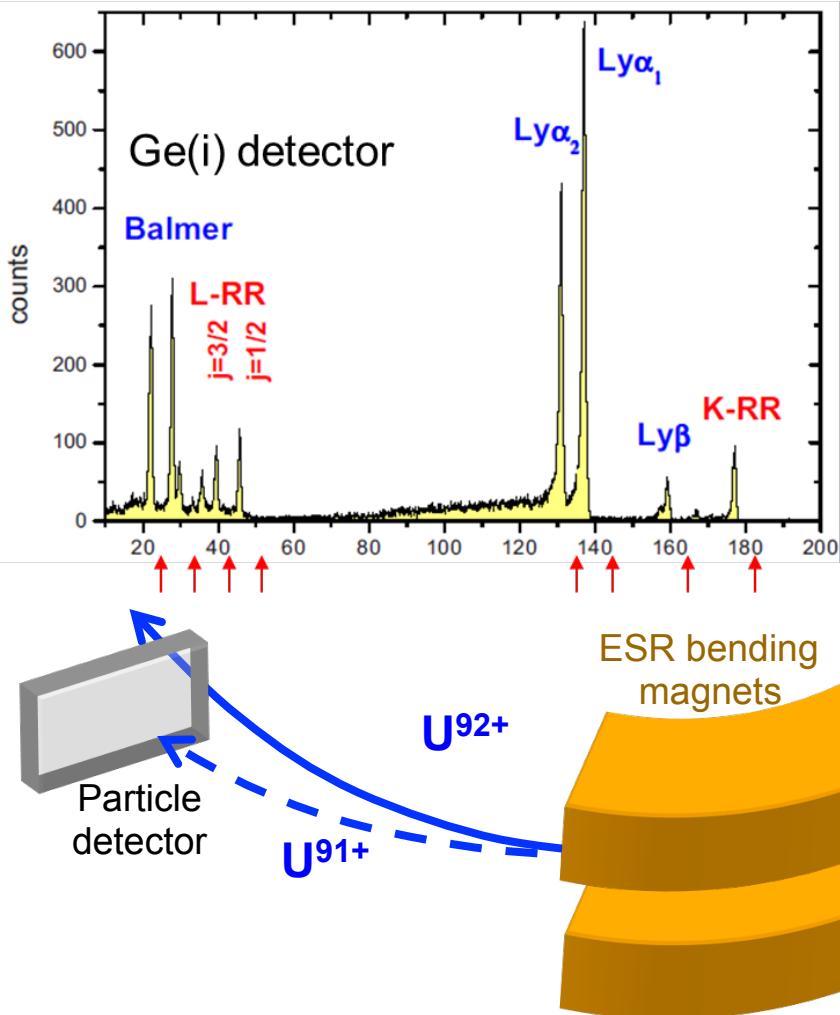
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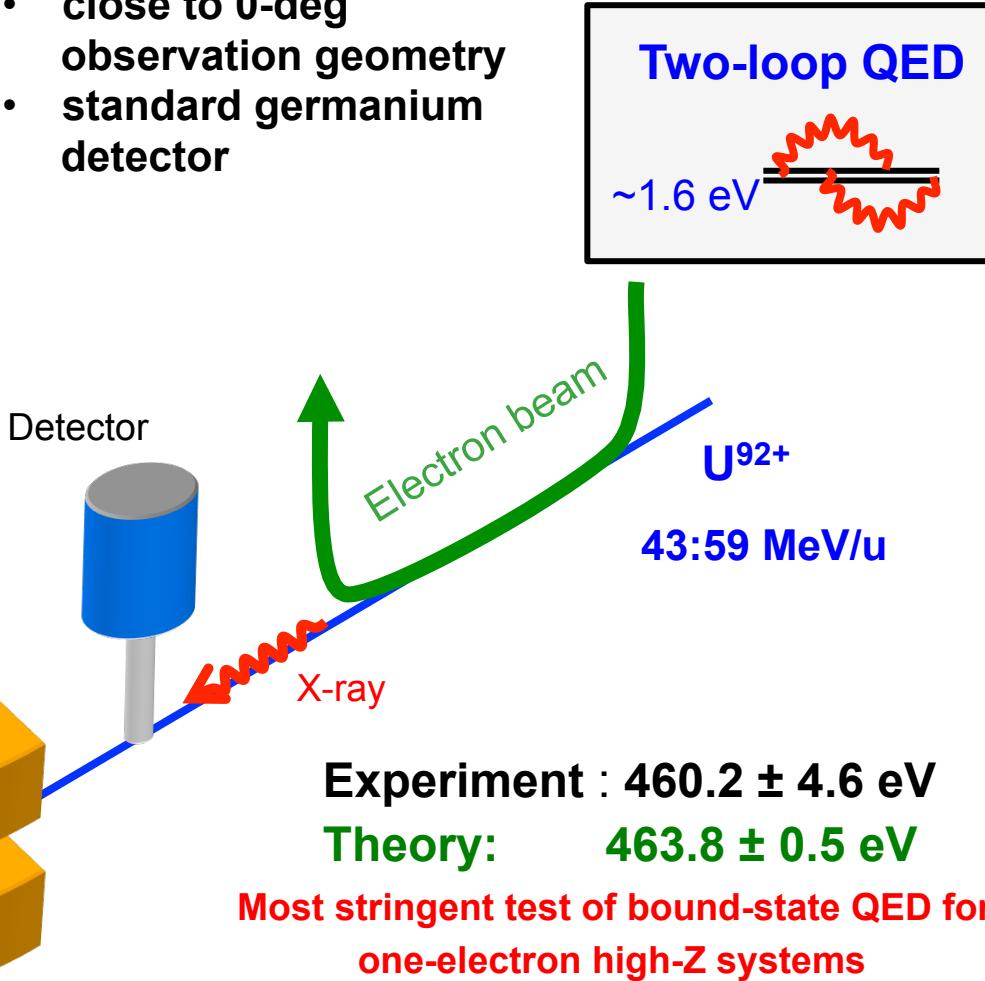
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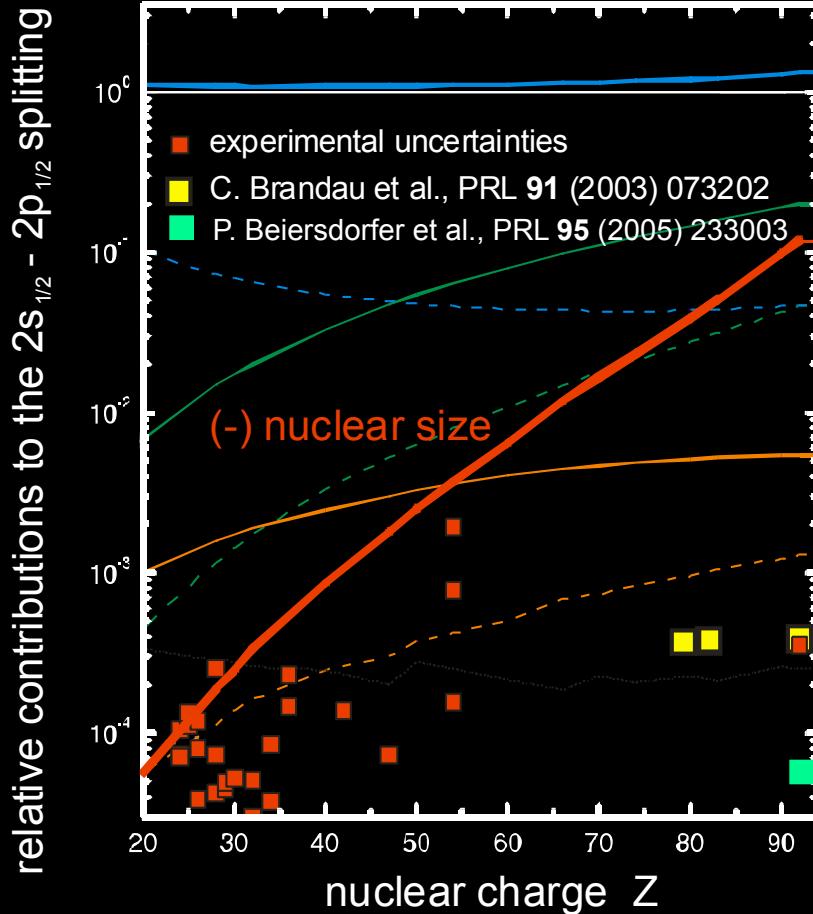


- decelerated ions
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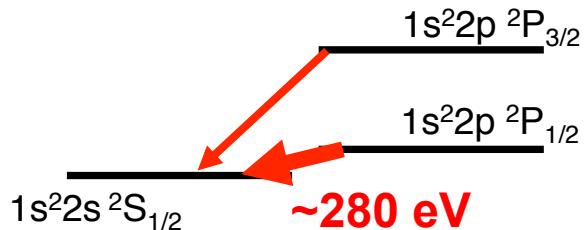


A. Gumberidze et al., PRL 94, 223001 (2005)

# Most precise spectroscopy tests in Li-like systems



Li-like Uranium (3 el.)



XUV spectroscopy

Detailed knowledge about the nucleus is vital for strong field QED studies (nuclear size but also nuclear structure  $\Rightarrow$  nuclear polarization)

# Summary

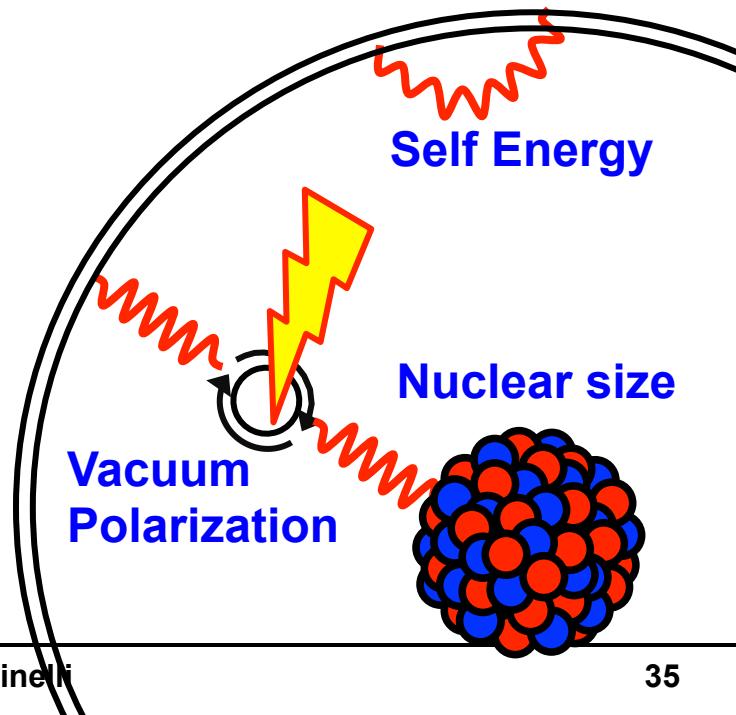
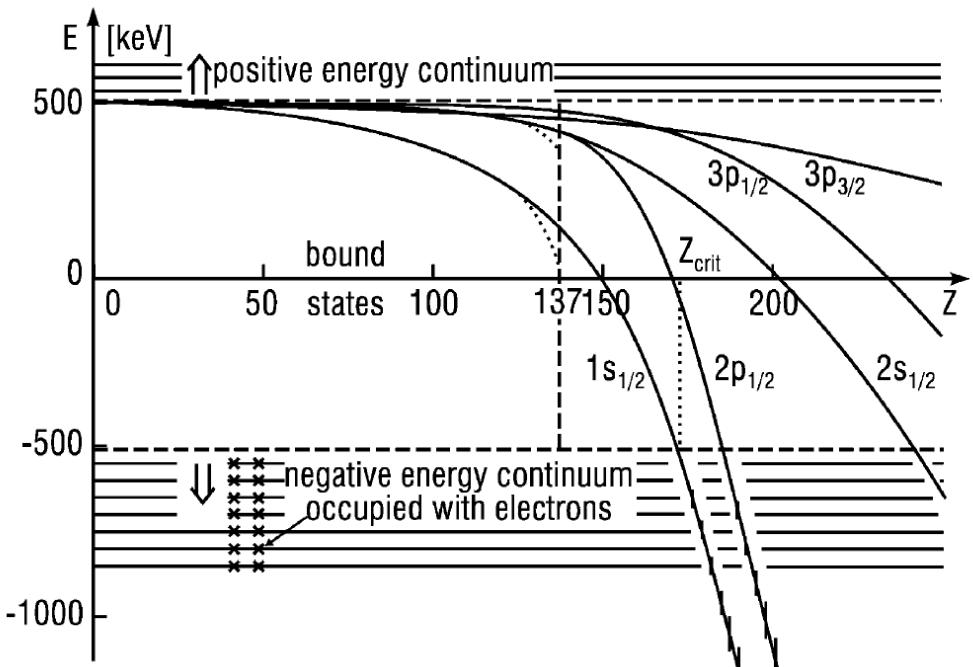
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# Supercritical fields

Dirac equation:  $E_{1s} = mc^2 \sqrt{1 - (Z\alpha)^2}$

$Z > 1/\alpha = 137 \rightarrow$  electron/positron pair creation

Finite nucleus size  $\rightarrow Z_{\text{crit}} = 173$

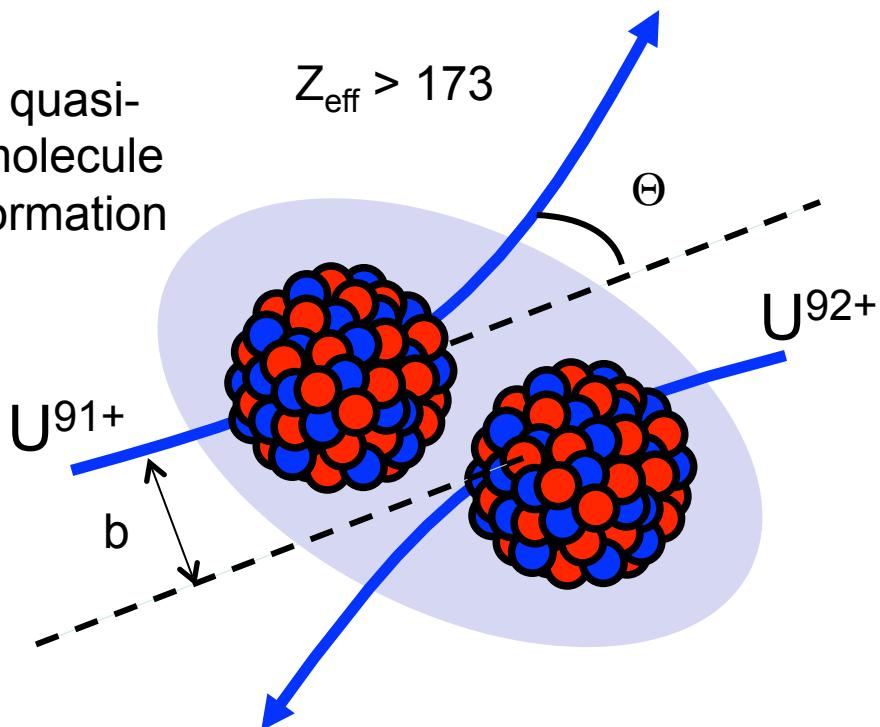
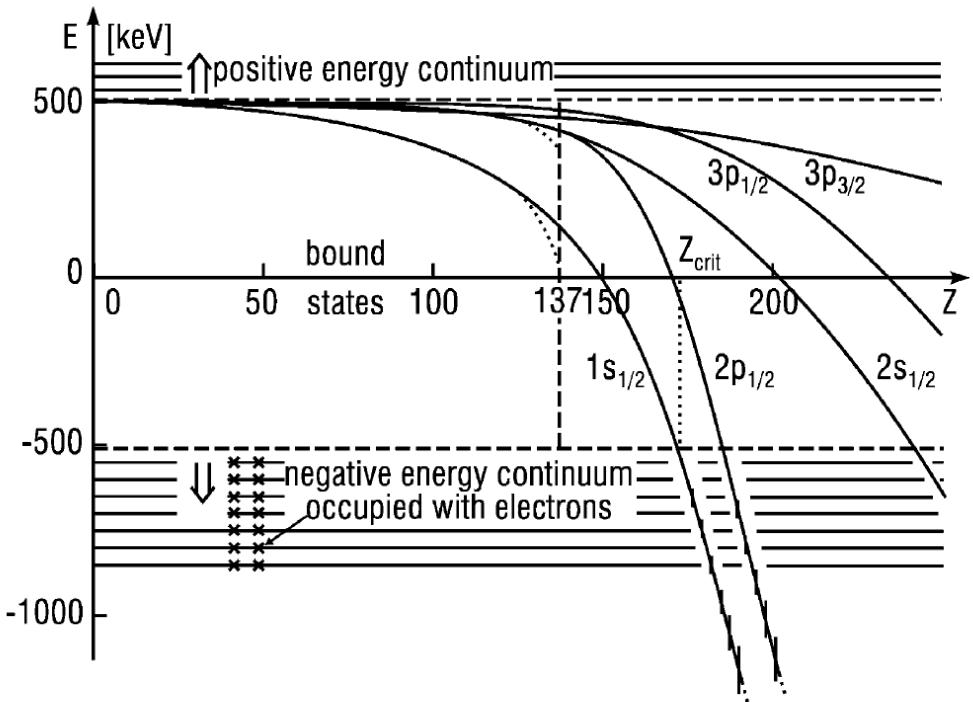


# Supercritical fields

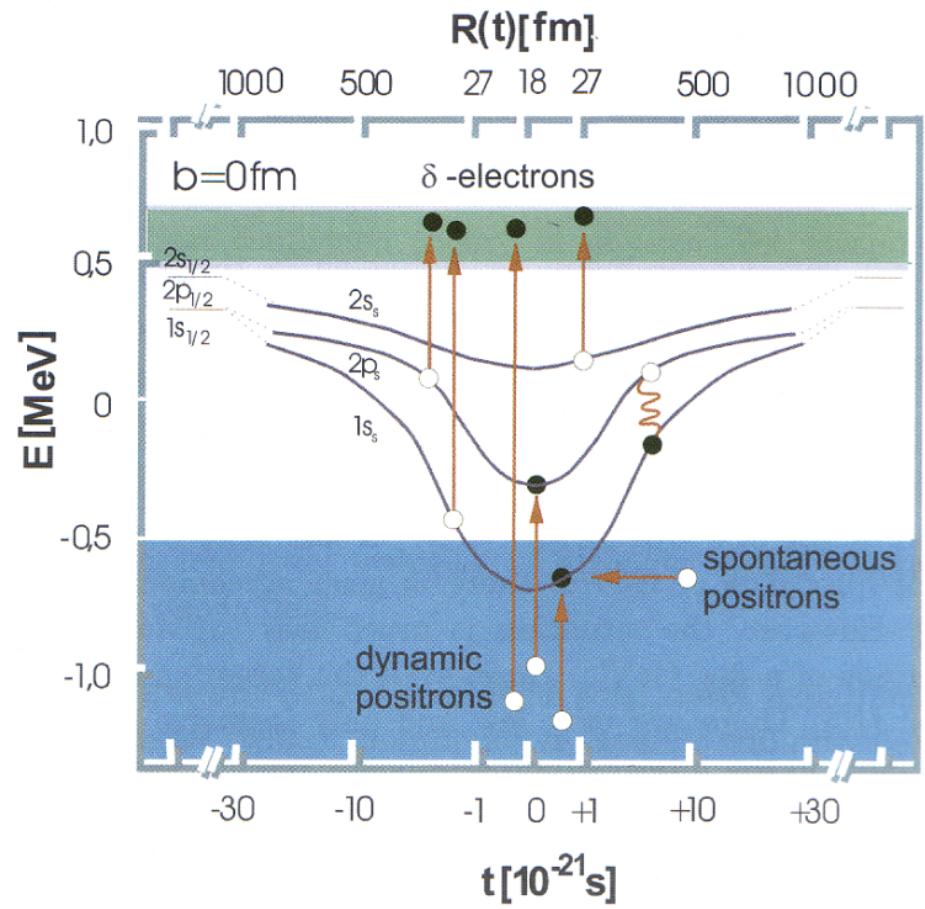
Dirac equation:  $E_{1s} = mc^2 \sqrt{1 - (Z\alpha)^2}$

$Z > 1/\alpha = 137 \rightarrow$  electron/positron pair creation

Finite nucleus size  $\rightarrow Z_{\text{crit}} = 173$

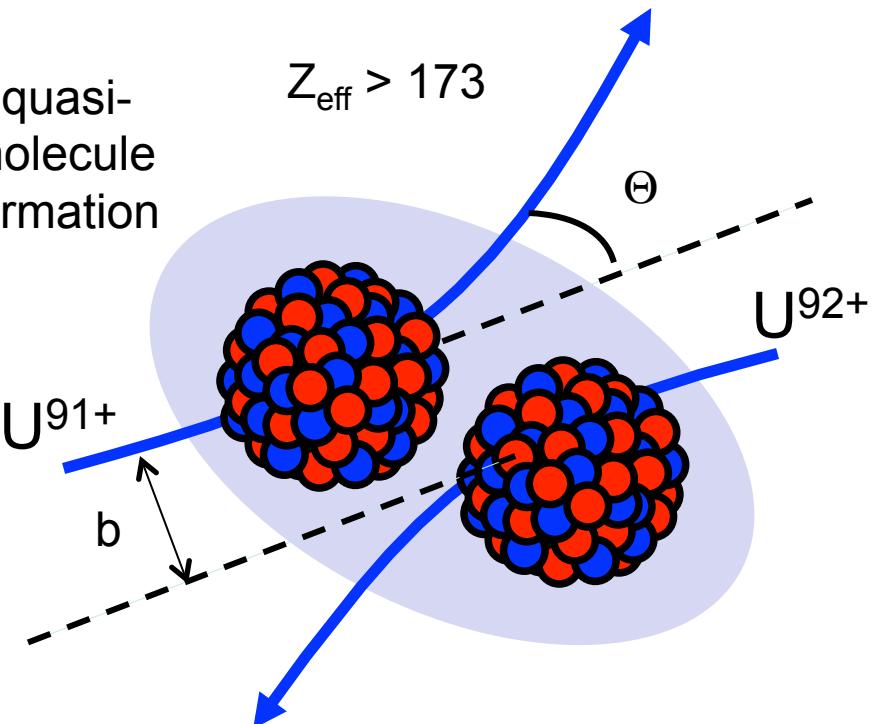


# Supercritical Fields: formation of super heavy quasi-molecules

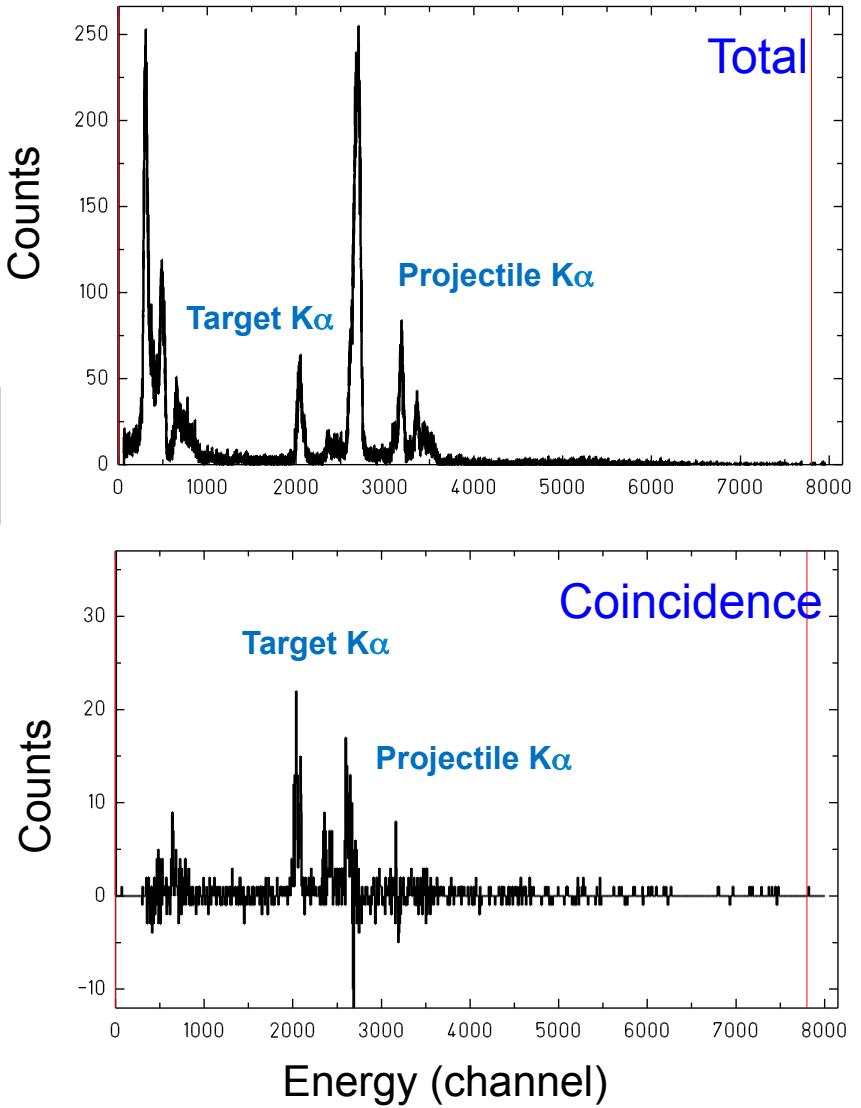
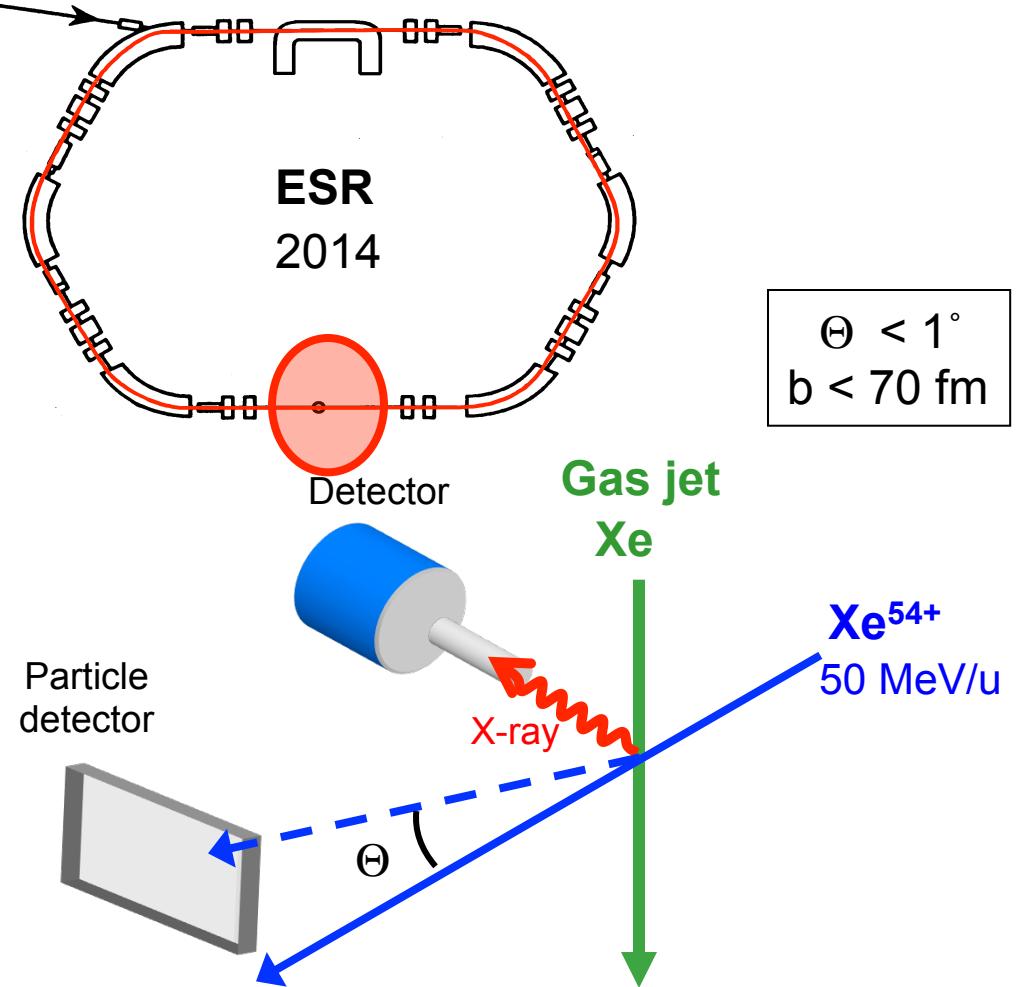


Slow ion – ion collision  
 $\sim 5 \text{ MeV/u}$

quasi-molecule formation



# First steps to supercritical fields



# Summary

- Introduction
  - Test of QED in strong field
  - Study of strong interaction force at low energy
- Heavy highly charged ions
  - Production
  - Lamb shift measurement
  - Vacuum decay experiment
- **Pionic atoms**
  - **Production**
  - Pionic hydrogen and deuterium spectroscopy
  - Pion mass measurement
- Conclusions and outlooks

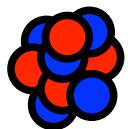
# Pion beam production



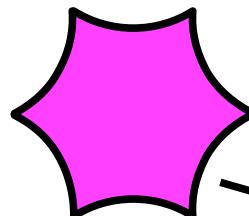
Production at the Paul Scherrer Institut  
(Villigen, Switzerland)

- Proton beam :  $E_{\text{kin}} = 590 \text{ MeV}/c$ ,  $I = 1.9 \text{ mA}$
- Graphite target
- $10^8$  pions/sec,  $E_{\text{kin}} = 110 \text{ MeV}/c$

Accelerate proton



Target (graphite)



Secondary beam of  
charged pions



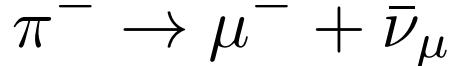
# Pionic and muonic atoms production

- Cyclotron trap to stop the pions:
  - strong magnetic field ( $B_{\max} = 3.5$  Tesla)
  - plastic degraders (energy loss)
- Gaseous target:
  - T: from 14 K to room temperature
  - effective pressure: from ~0 to 40 bars

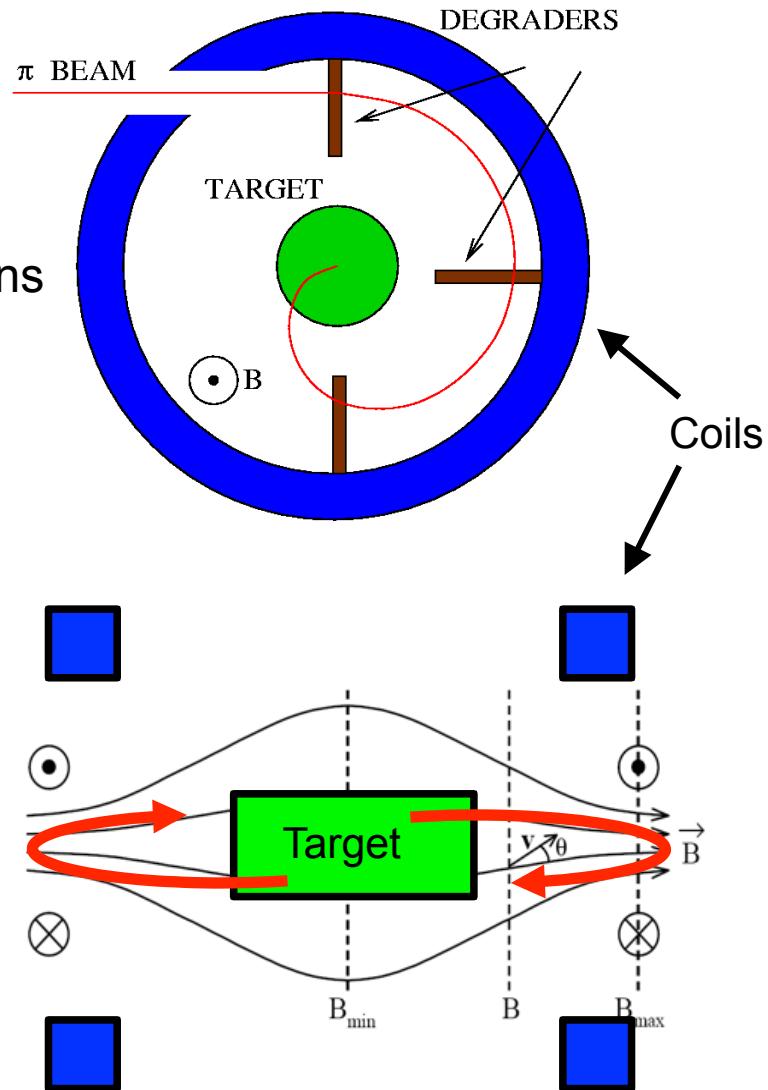


0.5% (per bar) of the incoming pions are stopped inside the target

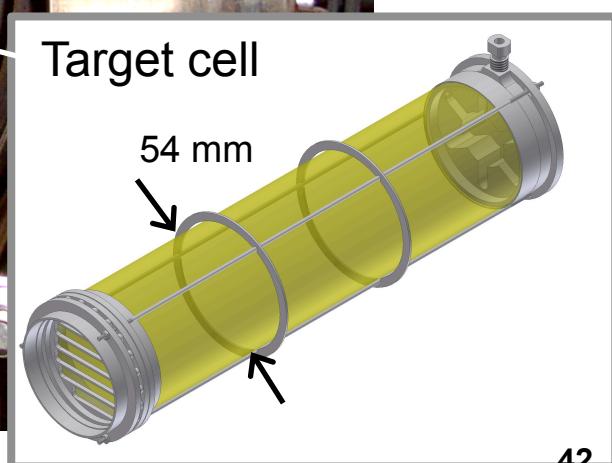
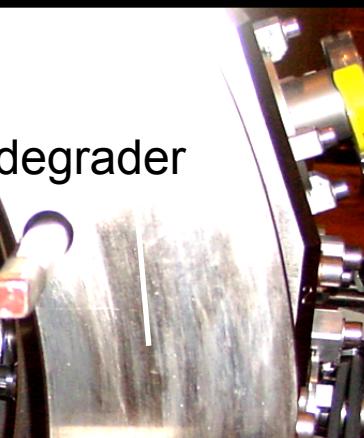
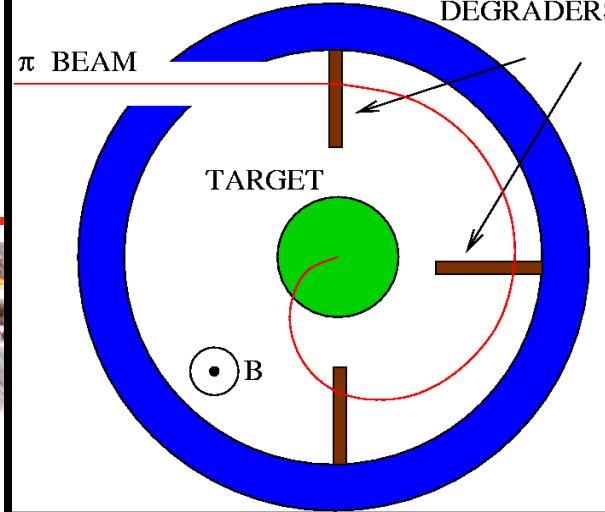
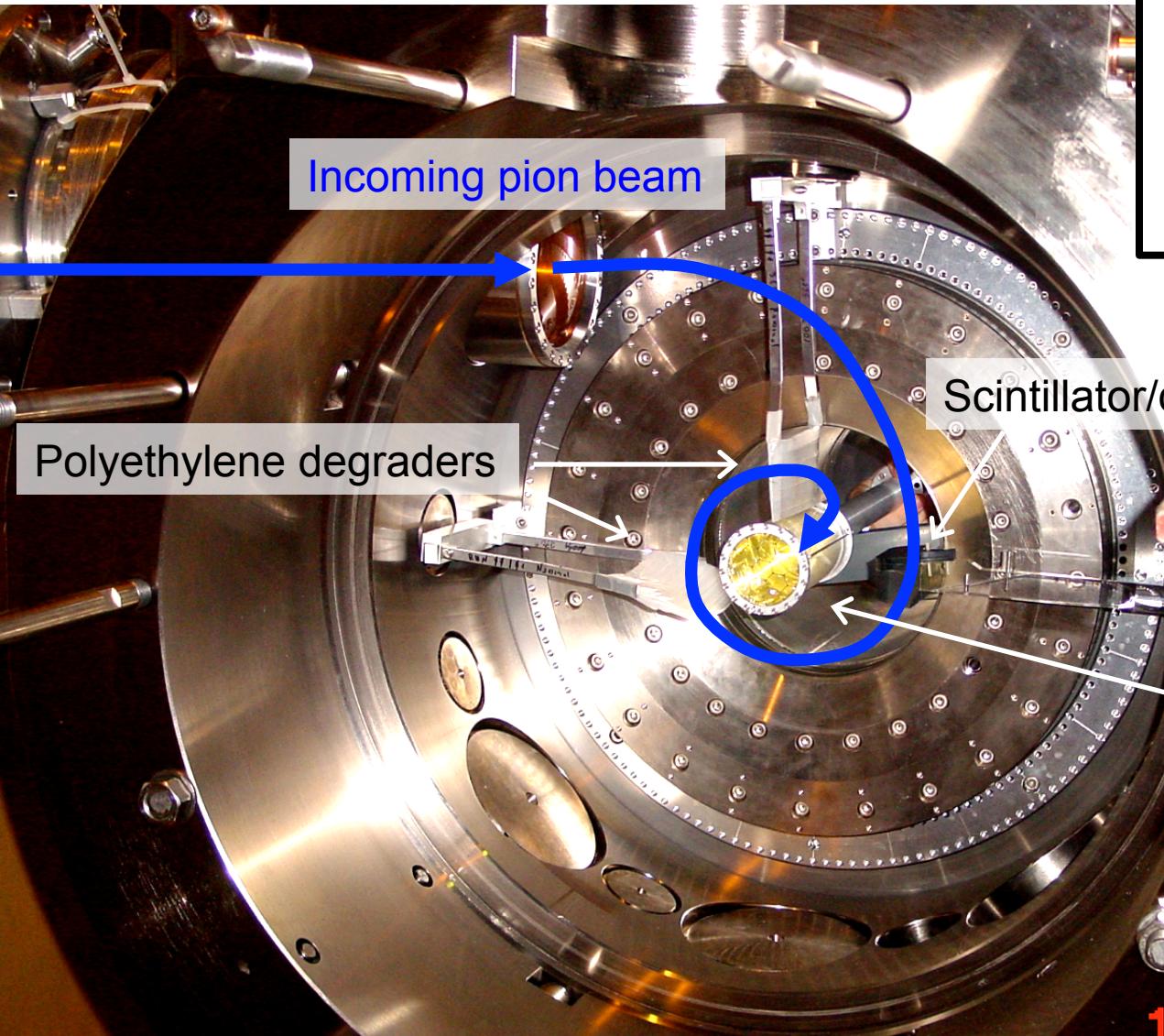
- Production and trapping of the muons



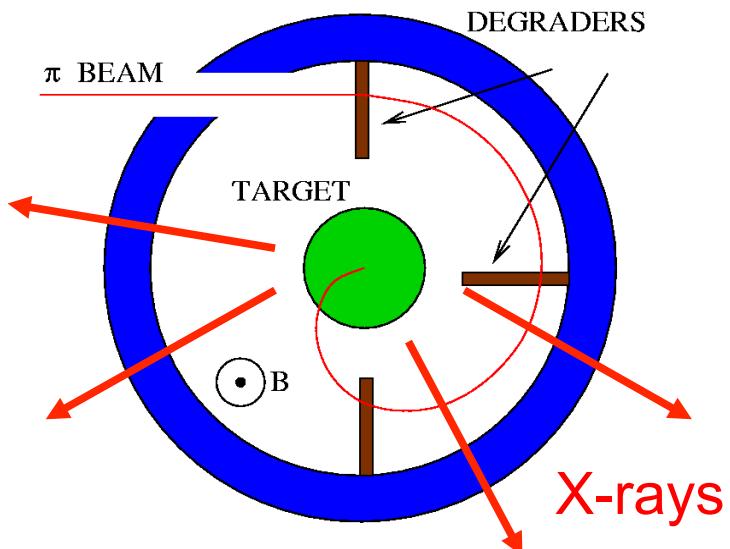
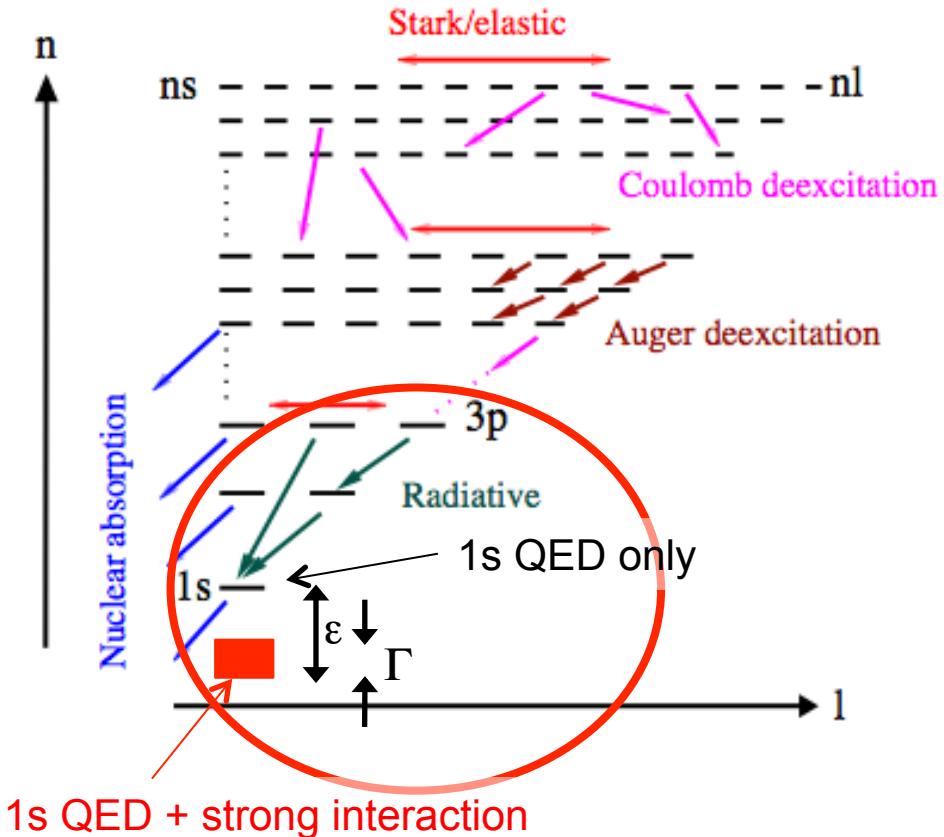
Formation of muonic and pionic atoms



# Cyclotron trap



# X-ray emission and detection



High power resolution for 2-4 keV  
X-ray required

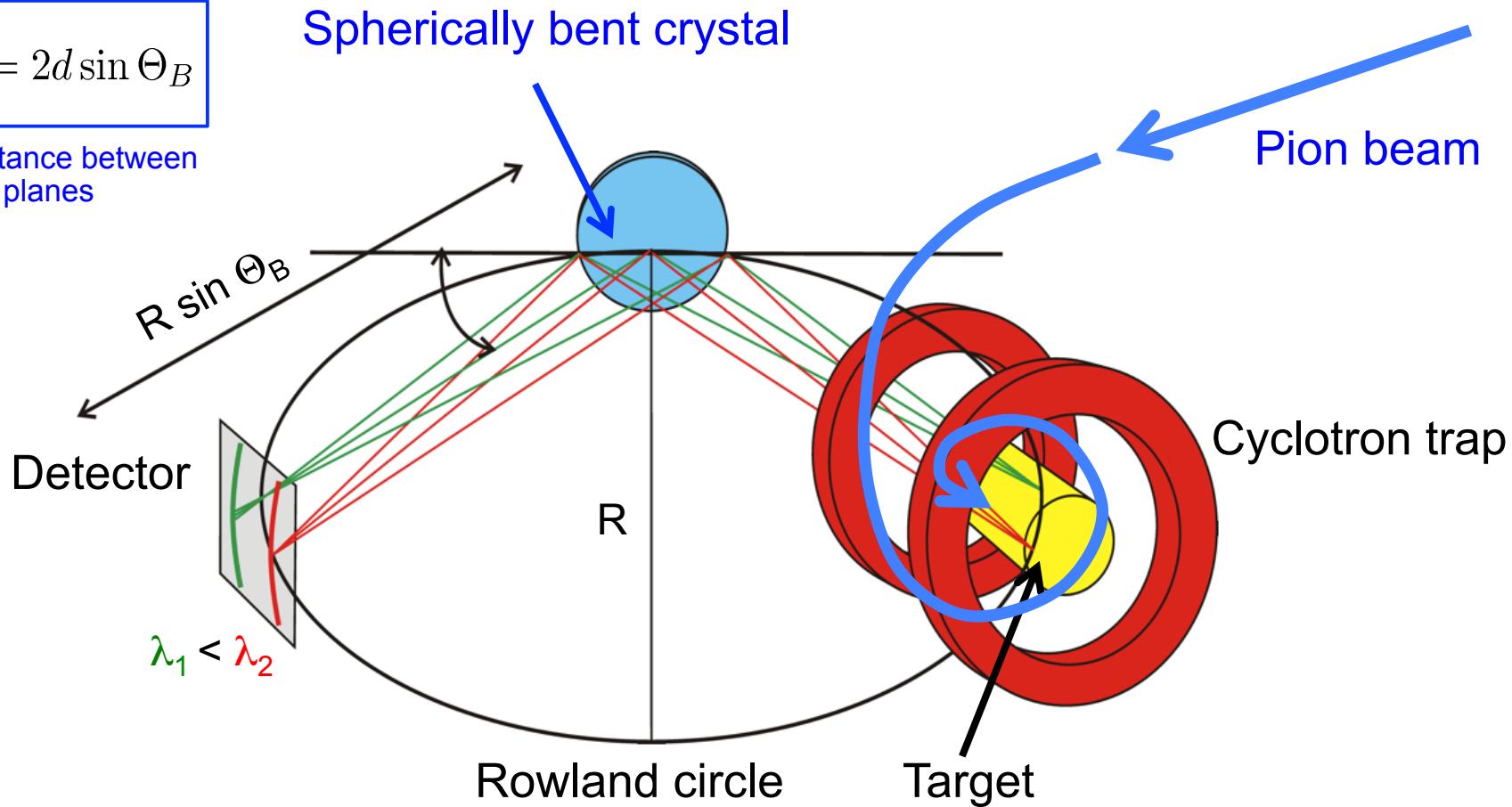


Bragg crystal spectroscopy

# Johann-type Bragg spectrometer

$$\frac{hc}{E} = 2d \sin \Theta_B$$

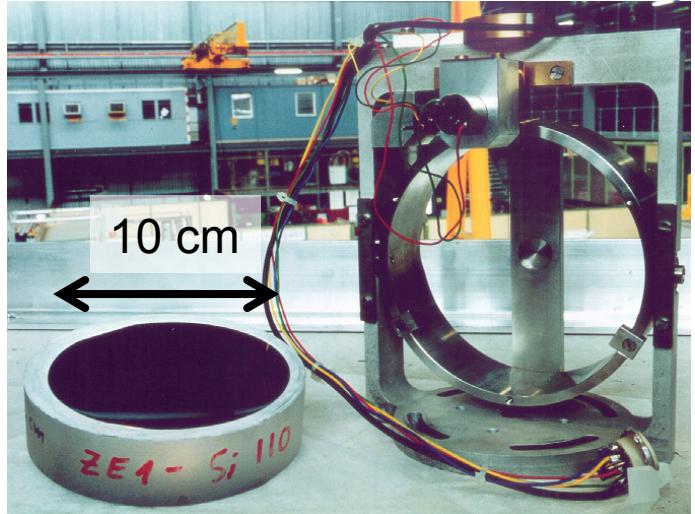
$d$  = distance between  
crystal planes



- [1] H.H. Johann, Zeitschrift für Physik **69**, 185 (1931)
- [2] J. Eggs *et al.*, Zeitschrift für angewandte Physik **20**, 118 (1965)
- [3] D. Gotta, Progress in Particle and Nuclear Physics **52**, 133 (2004)
- [4] D. Gotta *et al.*, Spectrochim. Acta, Part B **120**, 9 (2016)

# Diffraction crystal and position sensitive detector

**Si(110), Si(111), Qz(100), ... crystal [1]**



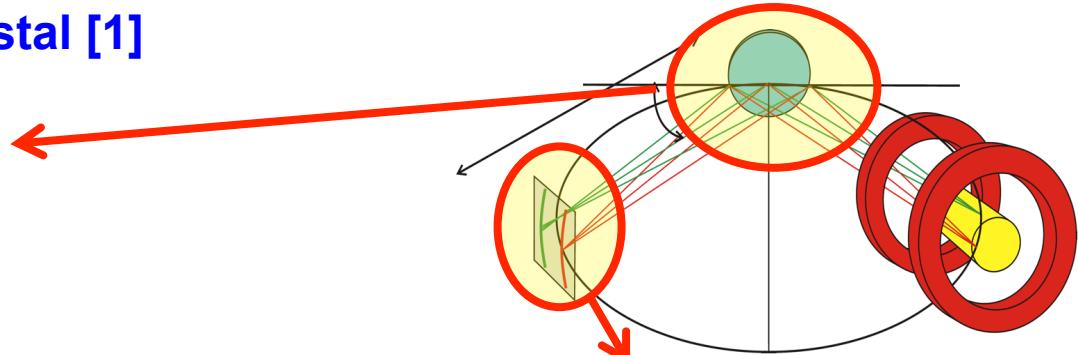
Radius of curvature: ~ 3 m

Diameter: 10 cm

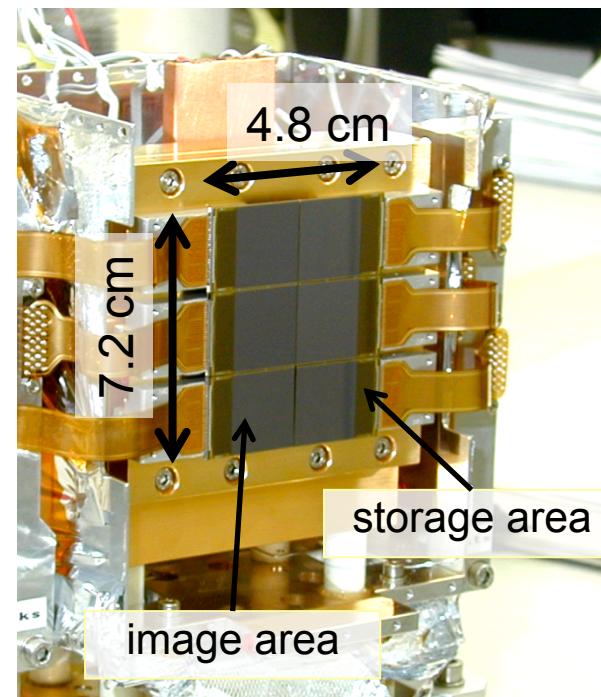
Thickness: 290  $\mu$ m

Support: polished quartz lens

Produced by Zeiss (Oberkochen, Germany)



**2 × 3 X-ray CCD array with frame buffer [2,3]**



pixel size 40  $\mu$ m  $\times$  40  $\mu$ m  
600  $\times$  600 pixels per chip  
frame transfer  $\approx$  10 ms

data processing ~24 s  
operates at  $-100^{\circ}\text{C}$

$\Delta E \approx 150 \text{ eV}$  @ 4 keV  
Efficiency  $\approx$  90%

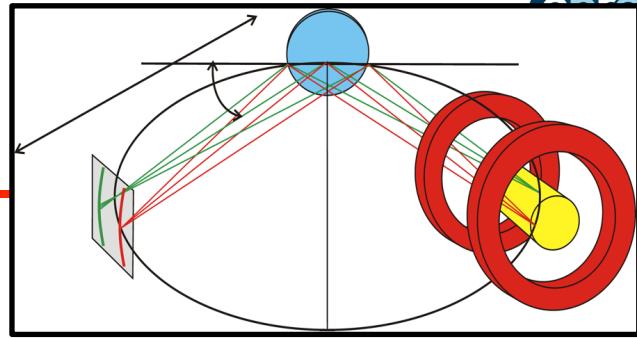
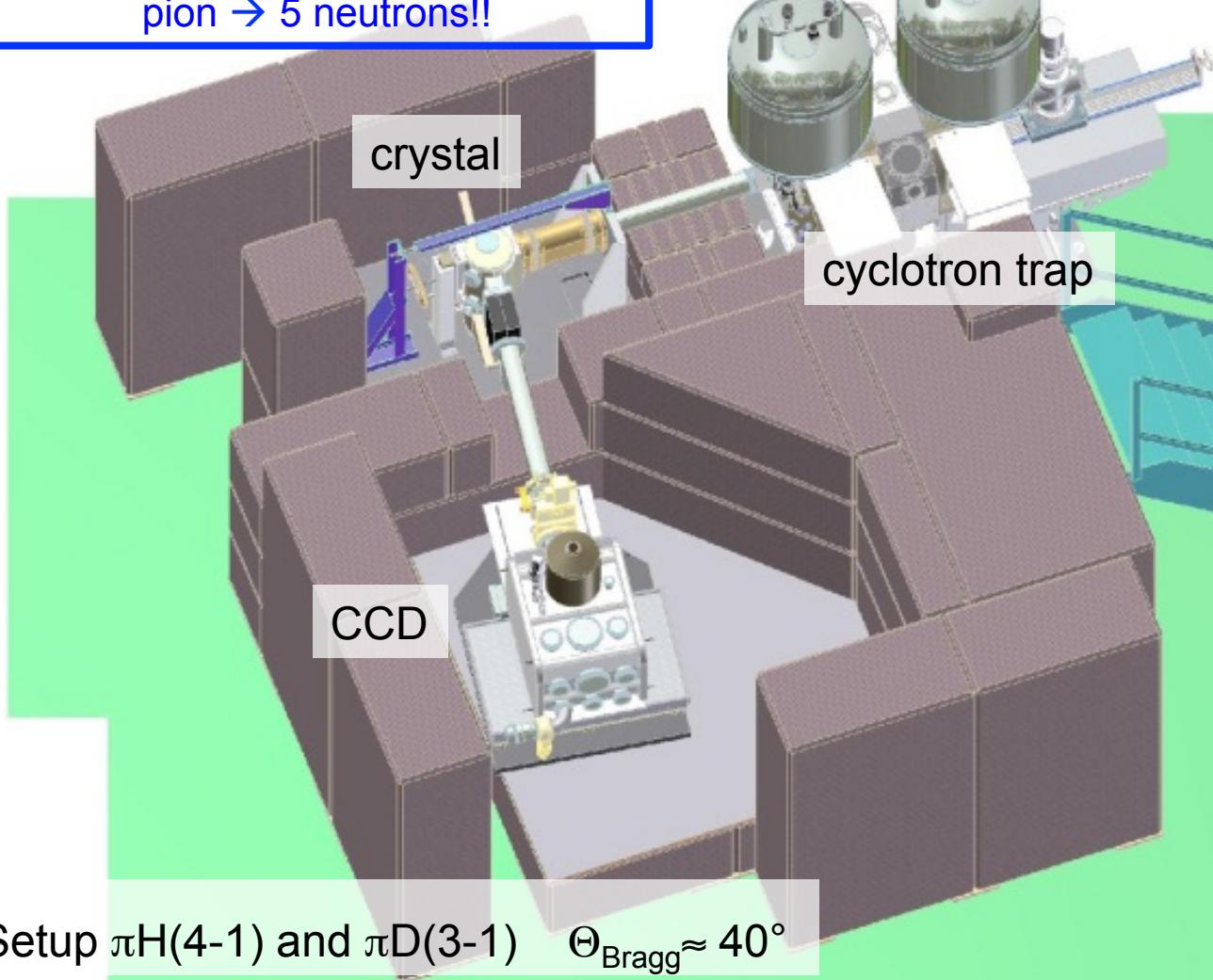
[1] D.S. Covita *et al.*, Rev. Sci. Instum. **79**, 033102-3 (2008)

[2] N. Nelms *et al.*, Nucl. Instrum. Methods A **484**, 419 (2002)

[3] P. Indelicato *et al.*, Rev. Sci. Instum. **77**, 043107 (2006)

# Typical set-up at PSI

Pion stopped in gas: 0.5% per bar.  
 All others produces neutrons: 1 pion → 5 neutrons!!



huge background  
on the CCD



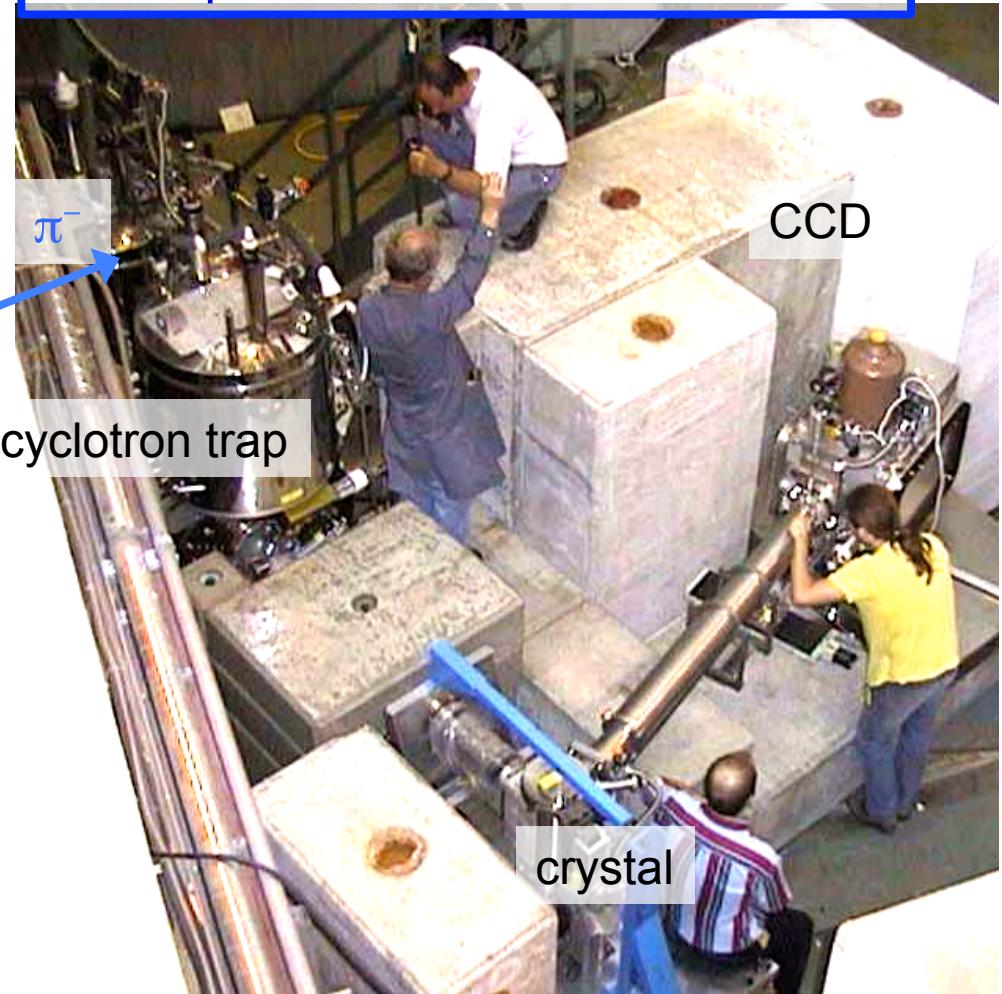
heavy concrete



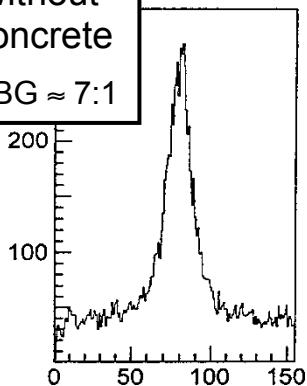
peak-to-background  
reduced by a factor  
of 10

# Typical set-up at PSI

Pion stops in gas: few % all others:  
1 pion makes 5 neutrons!!

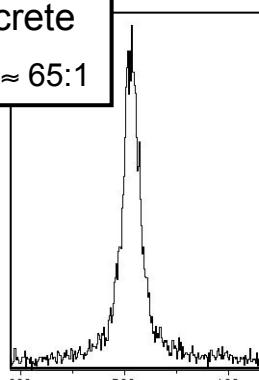


without  
concrete  
 $P/BG \approx 7:1$



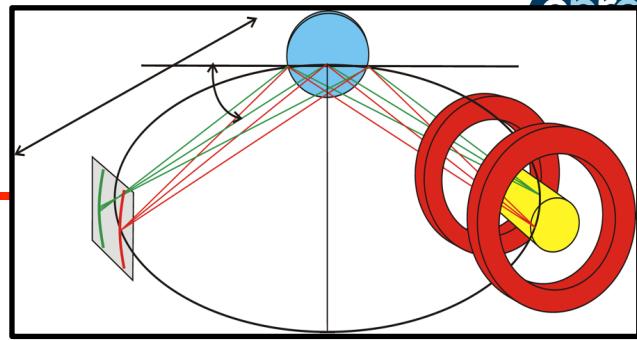
huge background  
on the CCD

with  
concrete  
 $P/BG \approx 65:1$



heavy concrete

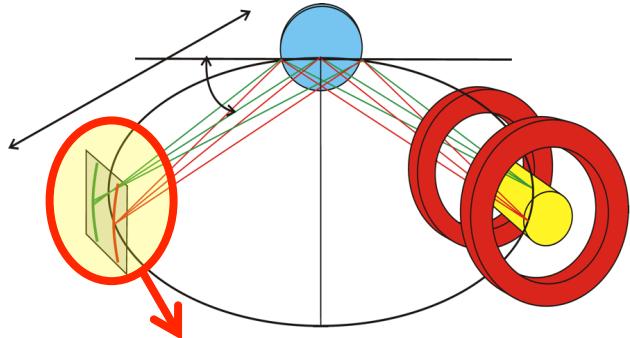
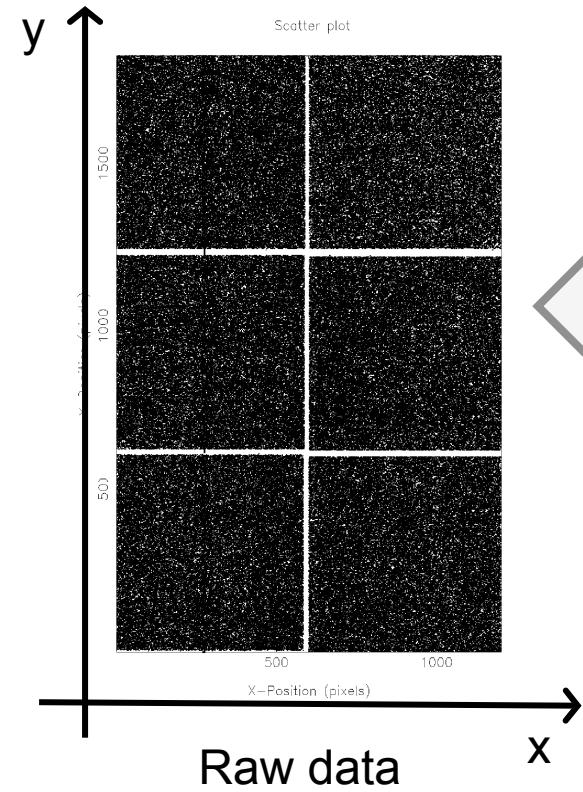
peak-to-background  
reduced by a factor  
of 10



# Data acquisition and pre-analysis

**Several weeks of data collection ...**

Spectrometer transmission:  $\sim 5 \times 10^{-8}$

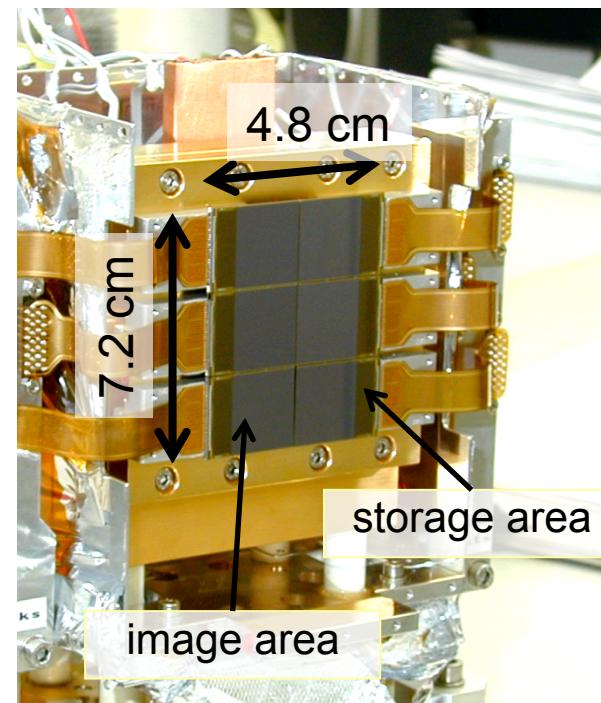


2 × 3 X-ray CCD array with frame buffer [2,3]

pixel size  $40 \mu\text{m} \times 40 \mu\text{m}$   
 600 × 600 pixels per chip  
 frame transfer  $\approx 10 \text{ ms}$

data processing 2.4 s  
 operates at  $-100^\circ\text{C}$

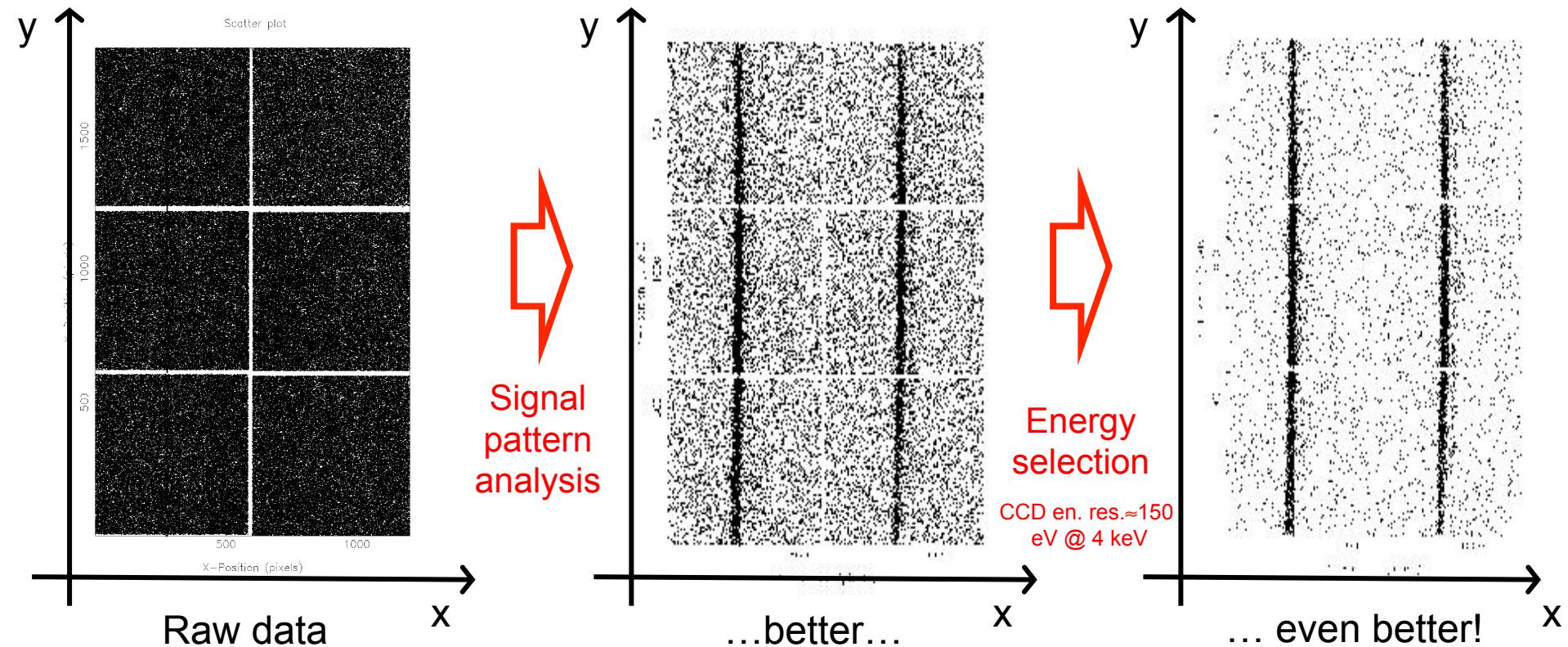
$\Delta E \approx 150 \text{ eV}$  @ 4 keV  
 Efficiency  $\approx 90\%$



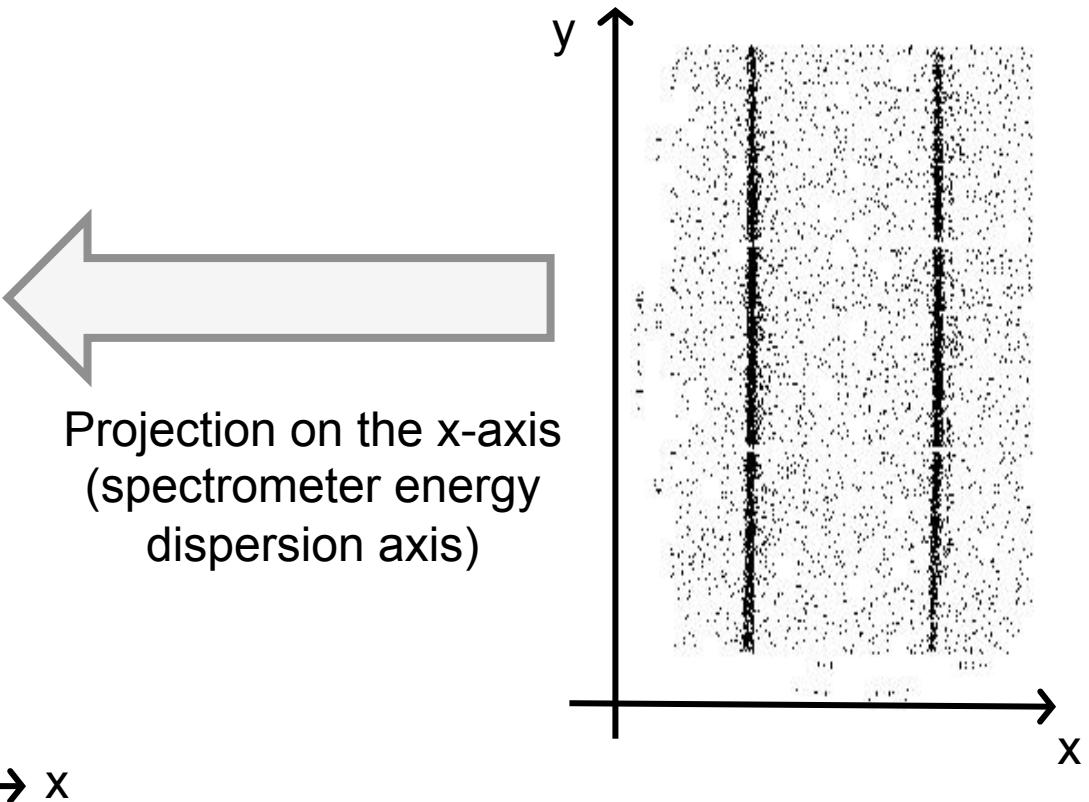
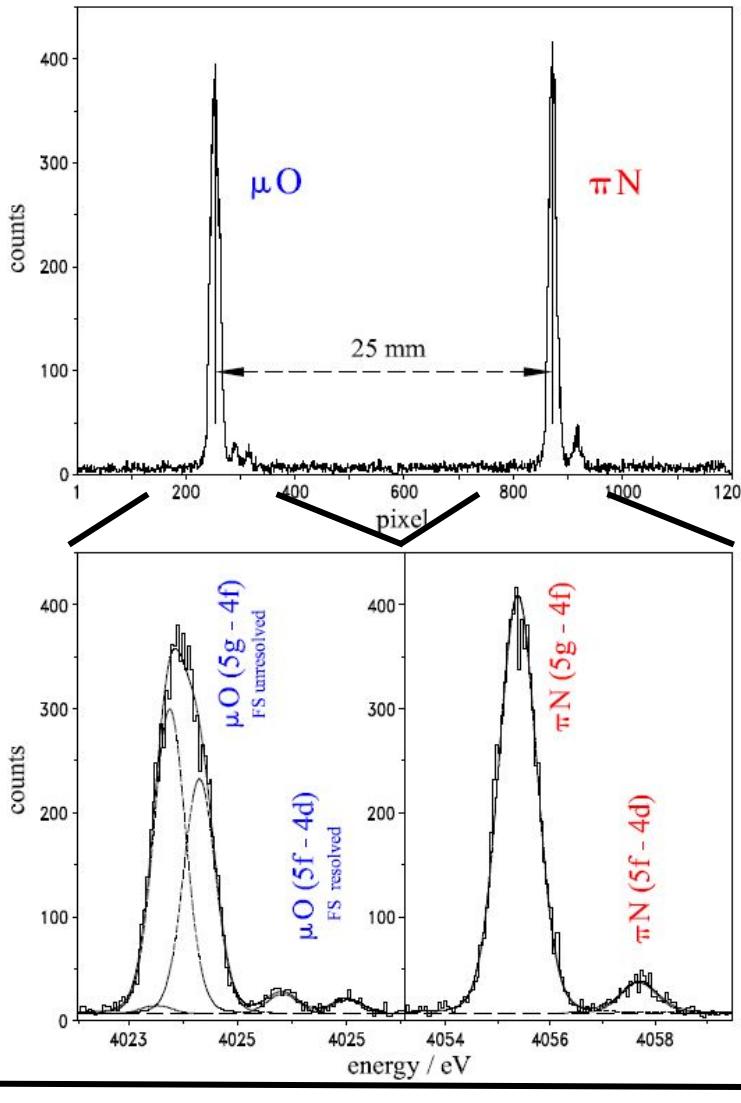
# Data acquisition and pre-analysis

Several weeks of data collection ...

Spectrometer transmission:  $\sim 5 \times 10^{-8}$



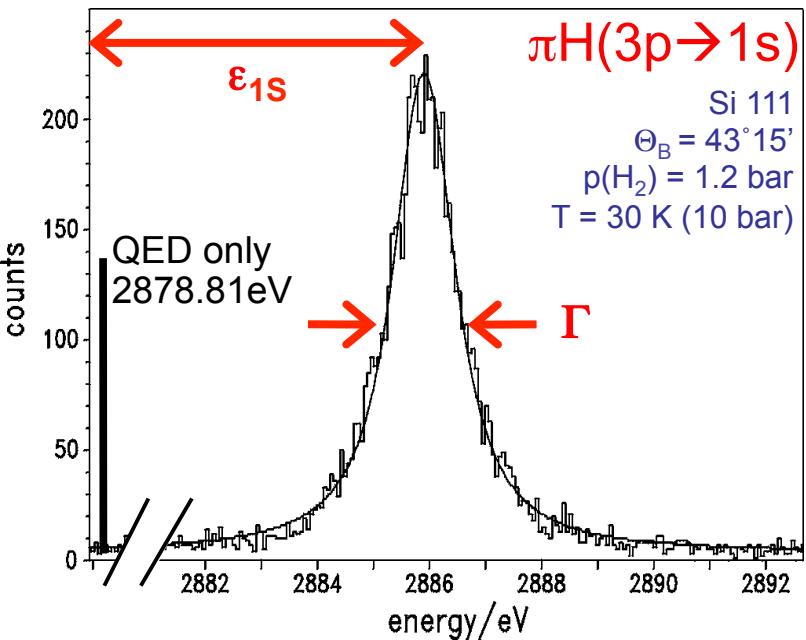
# Data acquisition and pre-analysis



# Summary

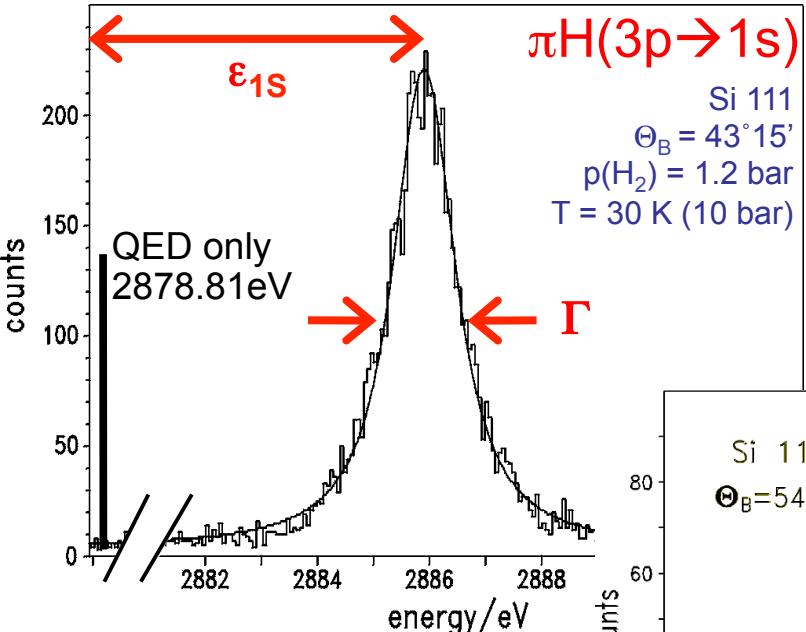
- Introduction
  - Test of QED in strong field
  - Study of strong interaction force at low energy
- Heavy highly charged ions
  - Production
  - Lamb shift measurement
  - Vacuum decay experiment
- Pionic atoms
  - Production
  - **Pionic hydrogen and deuterium spectroscopy**
  - Pion mass measurement
- Conclusions and outlooks

# Pionic hydrogen results



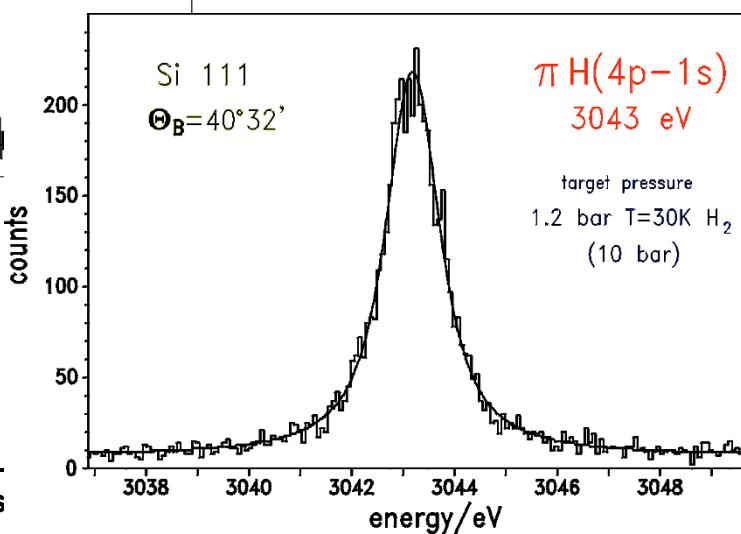
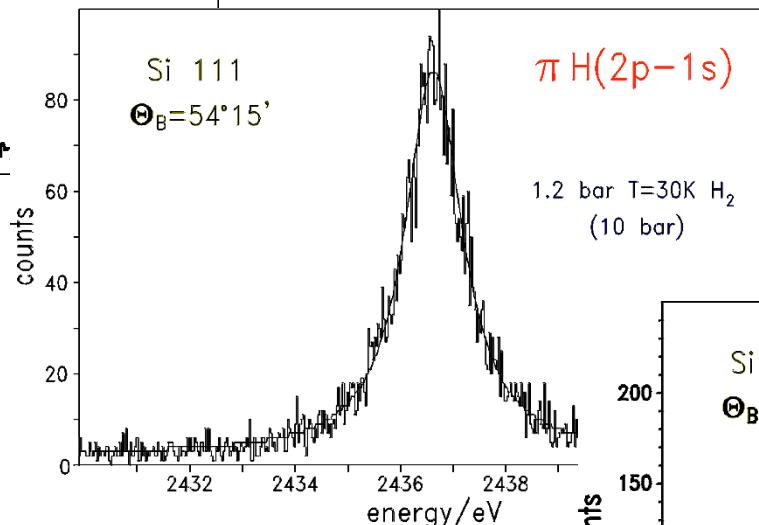
Several weeks of data acquisition for each spectrum

# Pionic hydrogen results



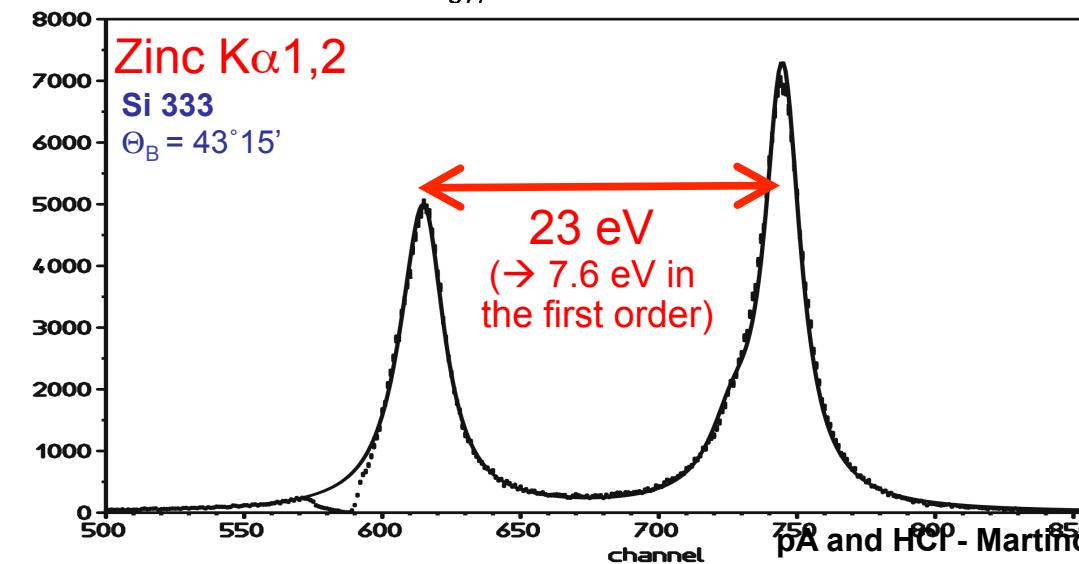
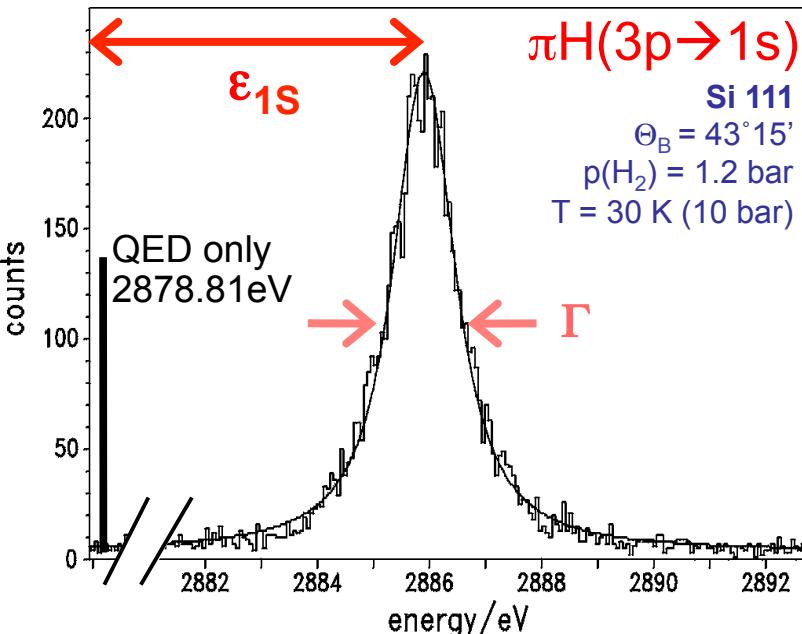
Independent measurement:

- Different transitions
- Different energy calibration
- Different crystals
- **Different target densities**



Several weeks of data acquisition for each spectrum

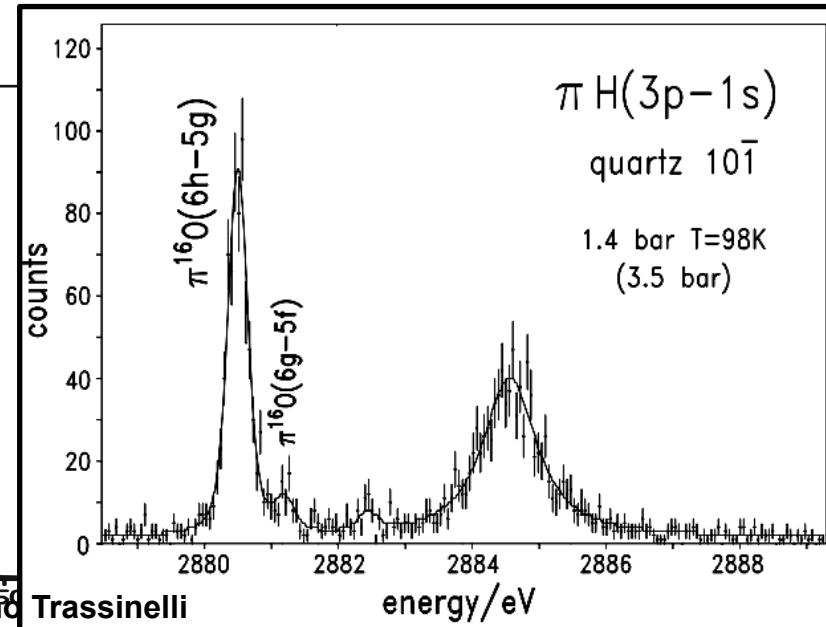
# Pionic hydrogen (and deuterium) shift measurement



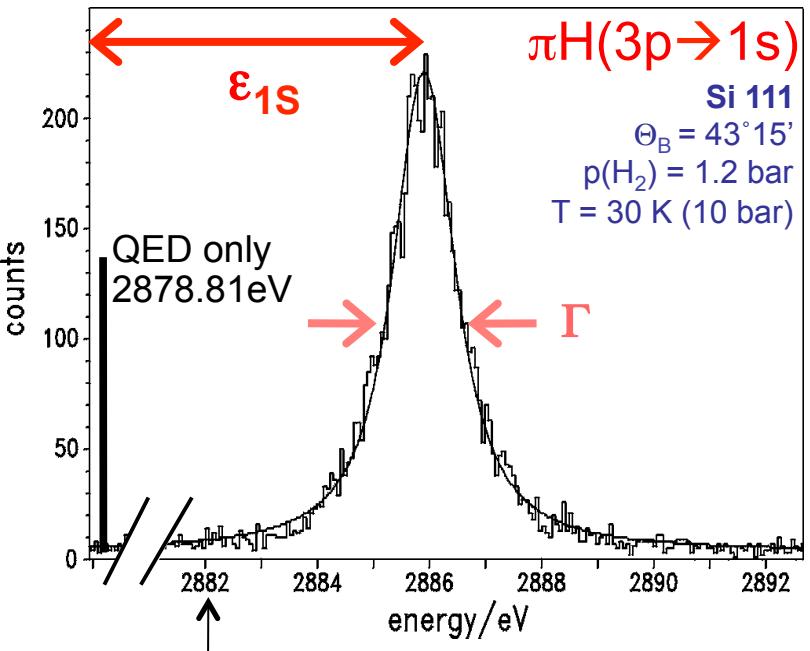
## Calibrations

- $\text{K}\alpha$  fluorescence from selected target (different reflection order)
- from other exotic atom transitions (where strong interaction effects are negligible)
 

smaller systematic errors from crystal spectrometer aberrations and possible chemical shifts and pion mass accuracy



# Pionic hydrogen shift measurement (preliminary result)



Satellite position

## Results

- No satellite from molecular X-ray detected (theoretical predictions [2] not confirmed)
- New value for the strong interaction shift in πH [3] (more 3 times smaller uncertainty)

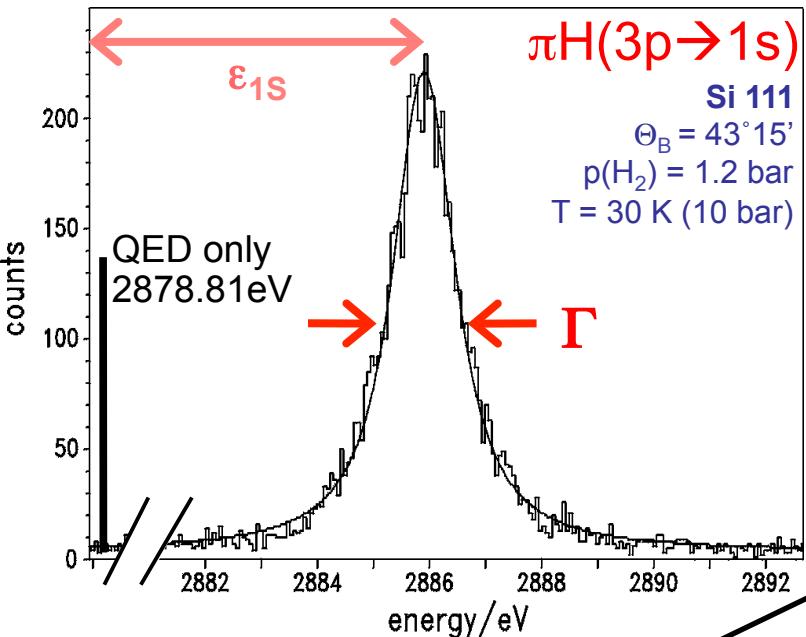
$$\epsilon_{1s} = +7.0869 \pm 0.0071 \pm 0.0064 \text{ eV } (\pm 0.13\%) [1]$$

0.001 eV from QED predictions [4]  
→ from the pion mass

(attractive force)

[1] M. Hennebach *et al.*, Eur. Phys. J. A **50**, 1-10 (2014)  
 [2] S. Kilic *et al.*, Phys. Rev. A **70** 042506 (2004)  
 [3] D. Gotta, *et al.*, Lect. Notes Phys. **745** 165 (2008)  
 [4] J. Schlesser *et al.*, Phys. Rev. C **84**, 015211 (2011)

# Pionic hydrogen (and deuterium) width measurement



from the response function  
of the instrument



- Characterization of the spectrometer [1,2]
- new measurements highly charged ion X-ray transitions
  - simulation of the instrument

Much more complex!!

$$\Gamma_{exp} = \Gamma_{crystal} \otimes \Gamma_{Doppler} \otimes \Gamma_{1s}$$

from the fast movement  
of the ions

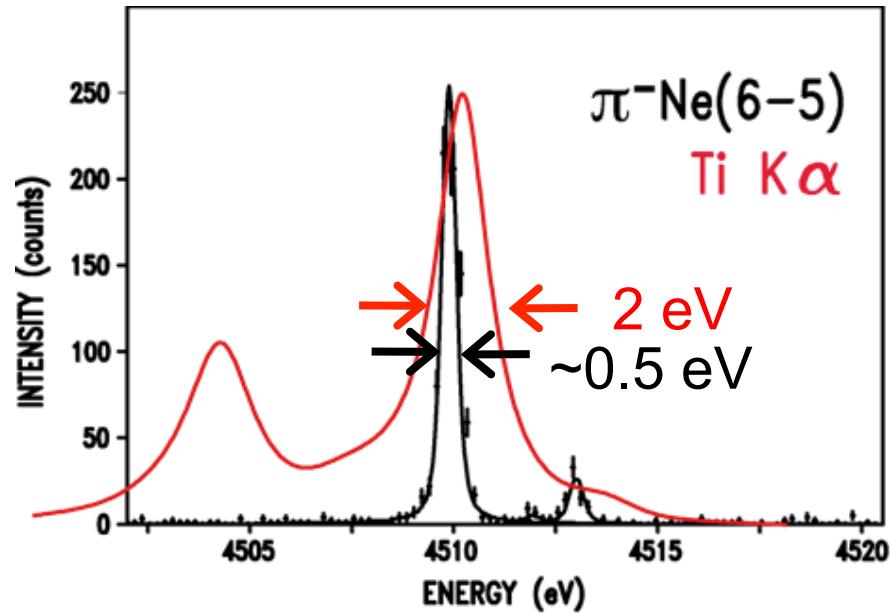
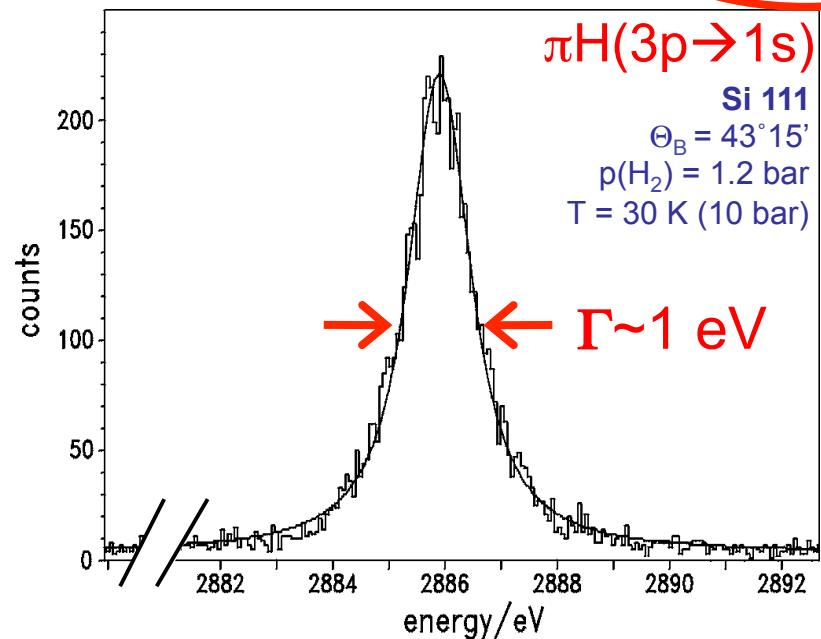


- Accurate investigation to the atomic cascade
- new theoretical approaches
  - new experiment with muonic hydrogen

from the strong  
interaction (goal!!)

# Crystal spectrometer characterization

$$\Gamma_{exp} = \Gamma_{crystal} \otimes \Gamma_{Doppler} \otimes \Gamma_{1s}$$

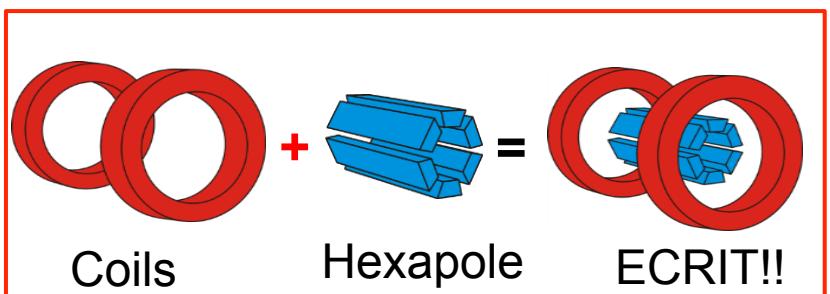
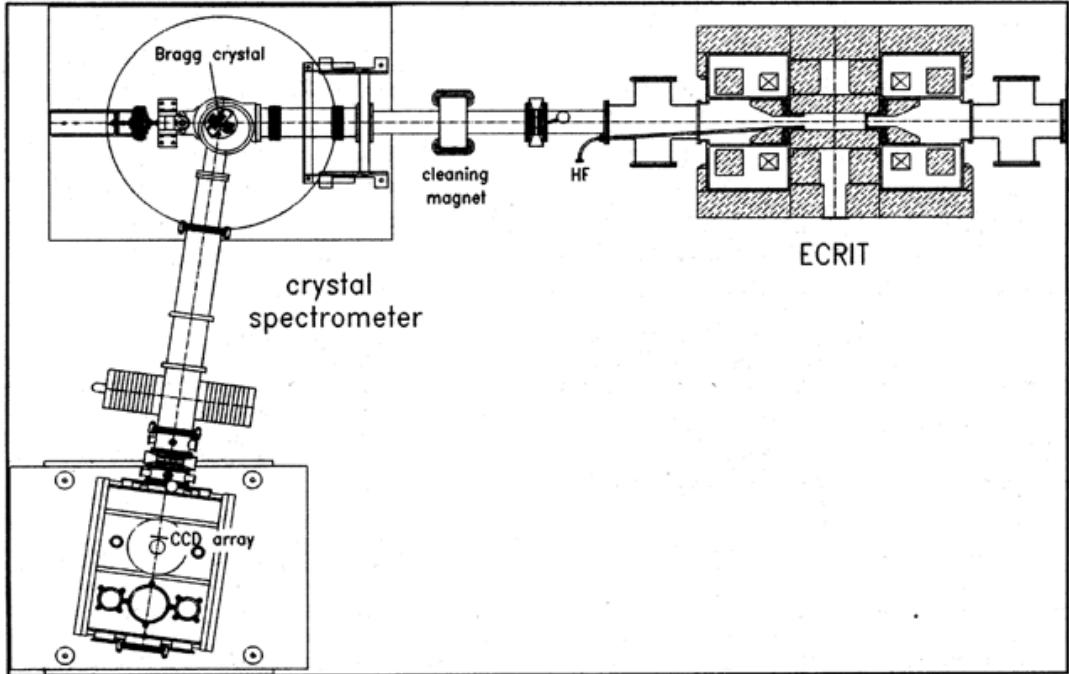


How to characterize the response function of the spectrometer?

Where to find a X-ray line with a  $\Gamma < 0.5$  eV?

- Fluorescence X-ray: **too broad!!**
- Pionic atoms (no Coulomb explosion): too low **count rate!!**
- ... **highly charged ion radiation!!**

# ECRIT X-ray emission

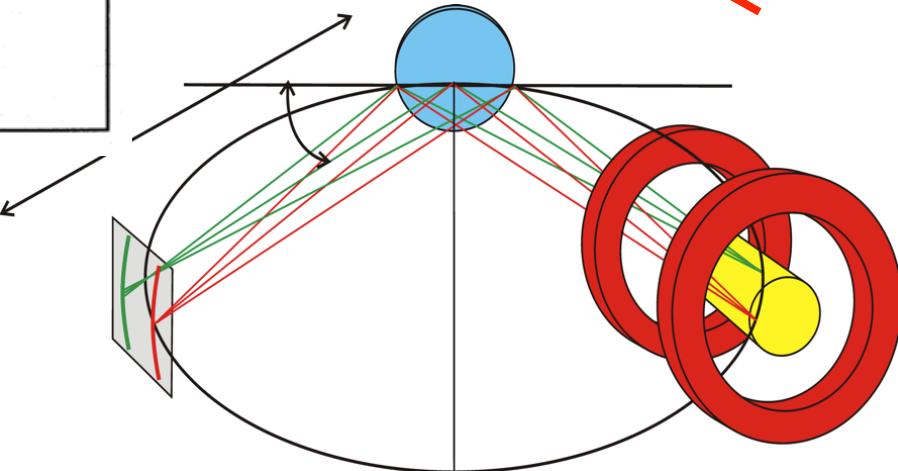


High intense radiation from  
He-like ions



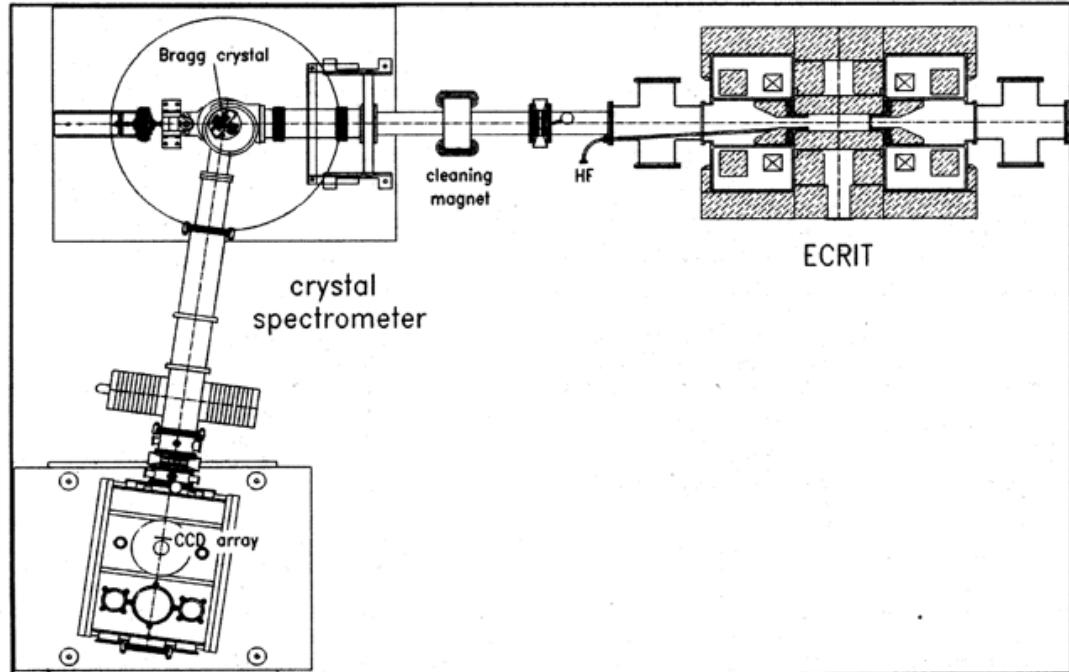
Electron-cyclotron  
resonance ion trap

~~Cyclotron trap~~



Biri et al., Rev. Sci. Instum. **71**, 1116-18 (2000).  
Hitz et al., Nucl. Instrum. Meth. B **205**, 168-172 (2003).

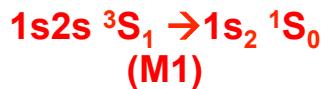
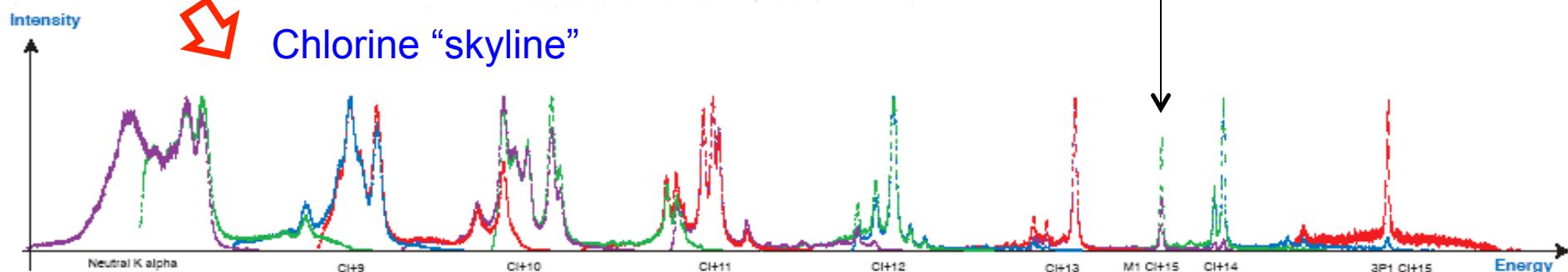
# ECRIT X-ray emission



High intense radiation from  
He-like ions



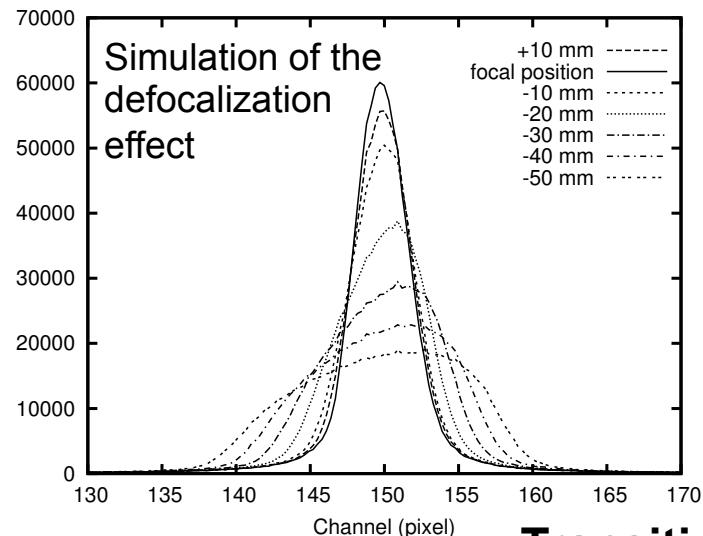
Electron-cyclotron  
resonance ion trap



Anagnostopoulos et al., Nucl. Instrum. Metl  
Anagnostopoulos et al., Nucl. Instrum. Metl  
M.T. et al., J. Phys. CS **58**, 129 (2007)

Covita et al., Rev. Sci. Instum. **79**, 033102 (2008)  
Schlessler et al., Phys. Rev. A **88**, 022503 (2013)  
Gotta and Simons, Spectrochim. Acta, Part B **120**, 9-18 (2016)

# Spectrometer characterization from He-like S, Cl, Ar M1 transitions

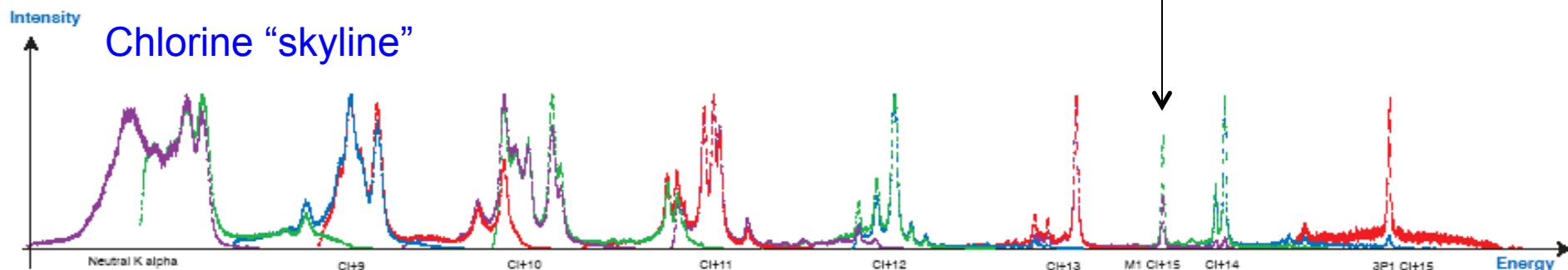
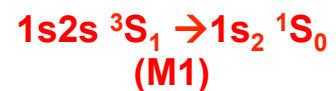


- Transition width << 1 meV
- Doppler broadening < 40 meV

Ideal for spectrometer response function studies

Measurement with:

- Different crystal
- Different crystal aperture
- Different focal position
- Different X-ray energies (Ar, Cl, S)



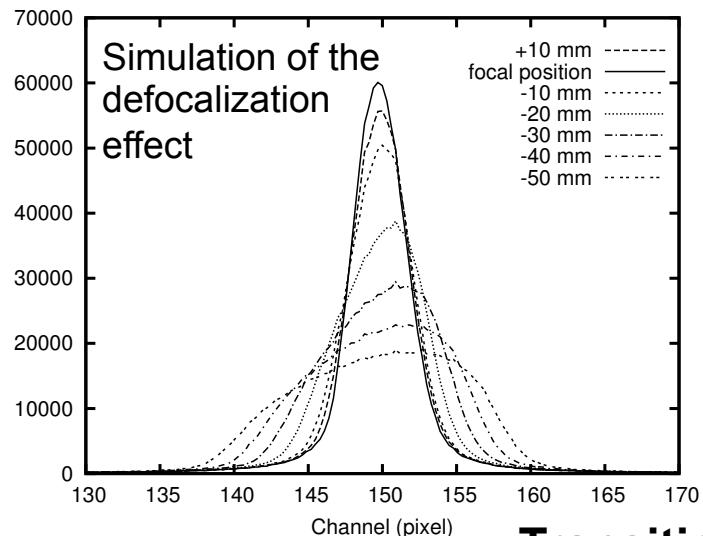
Anagnostopoulos et al., Nucl. Instrum. Metl  
 Anagnostopoulos et al., Nucl. Instrum. Metl  
 M.T. et al., J. Phys. CS **58**, 129 (2007)

Covita et al., Rev. Sci. Instum. **79**, 033102 (2008)

Schlessner et al., Phys. Rev. A **88**, 022503 (2013)

Gotta and Simons, Spectrochim. Acta, Part B **120**, 9-18 (2016)

# Spectrometer characterization from He-like S, Cl, Ar M1 transitions



- Transition width << 1meV
- Doppler broadening < 40 meV

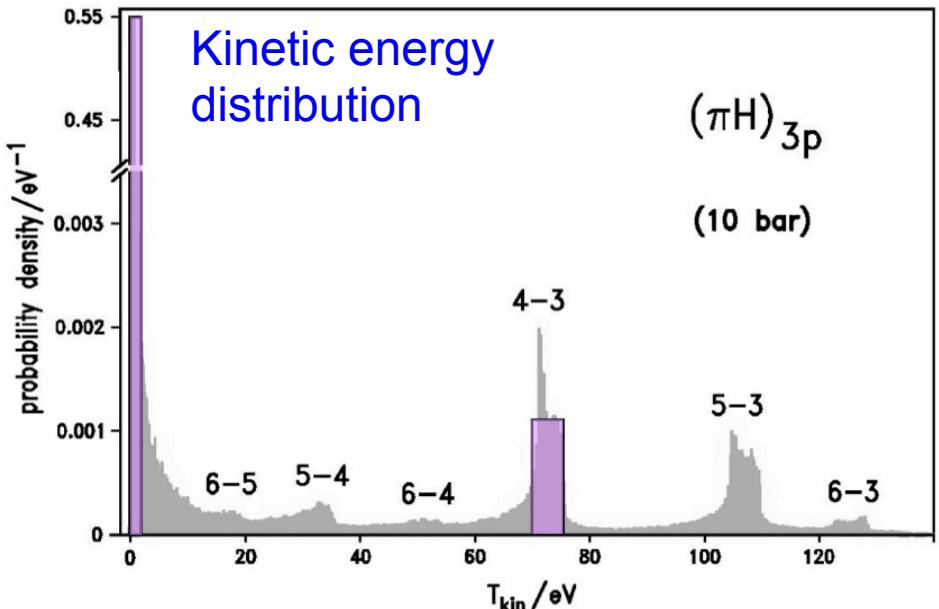
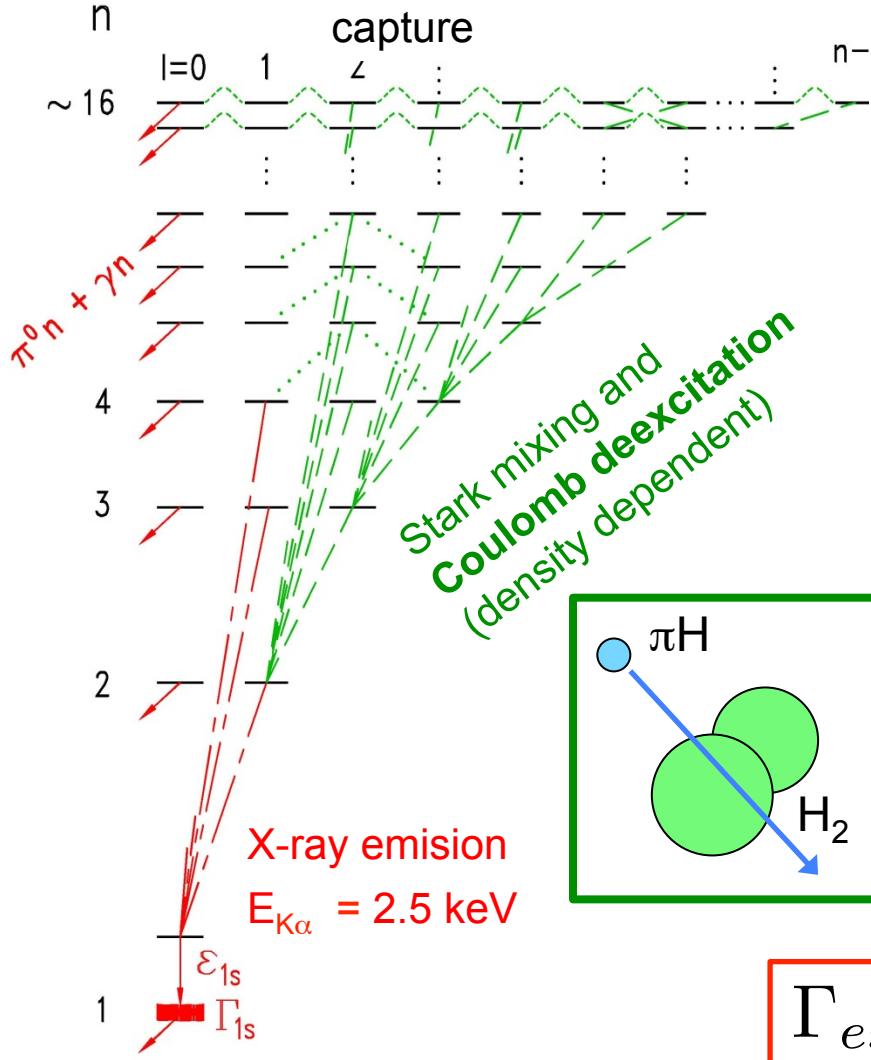
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Measurement with:

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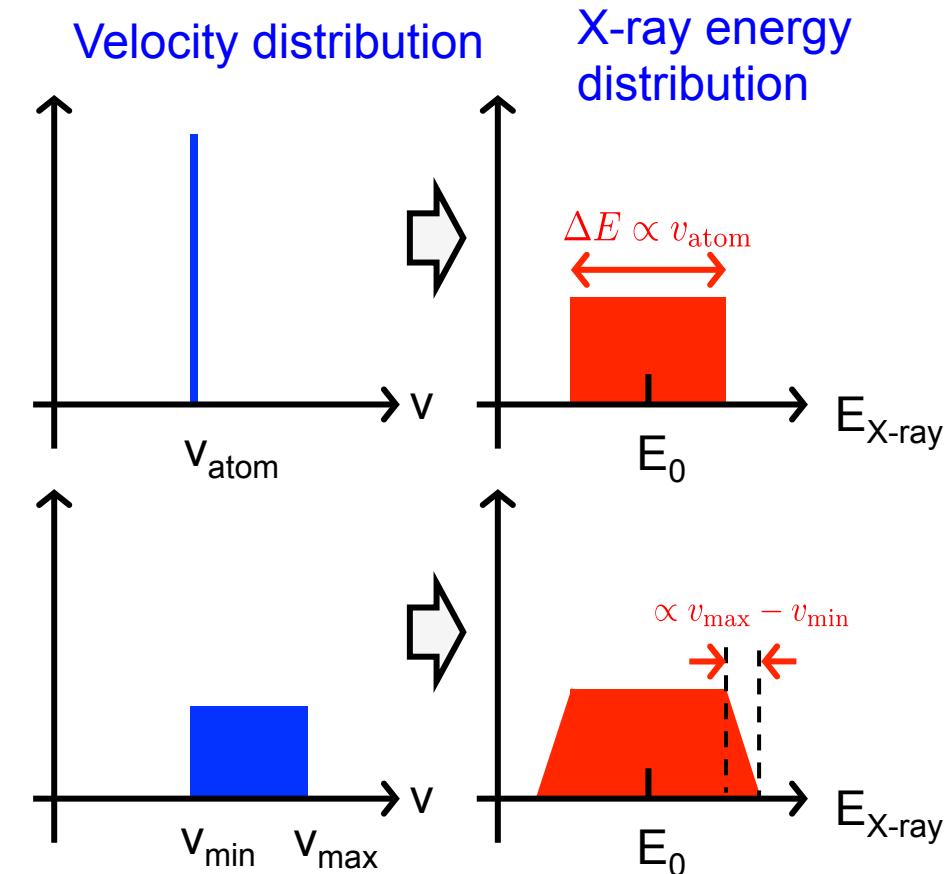
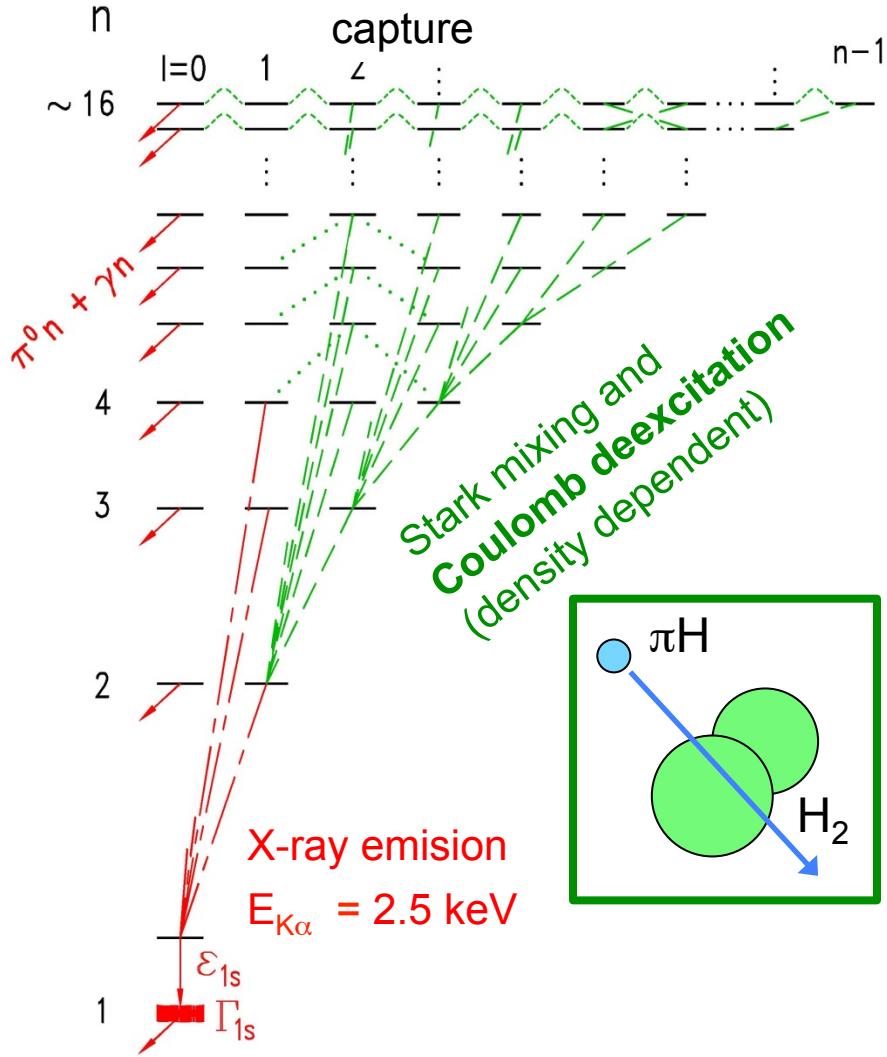
$$\Gamma_{exp} = \Gamma_{crystal} \otimes \Gamma_{Doppler} \otimes \Gamma_{1s}$$

# Transitions induced by collisions in $\pi\text{H}$

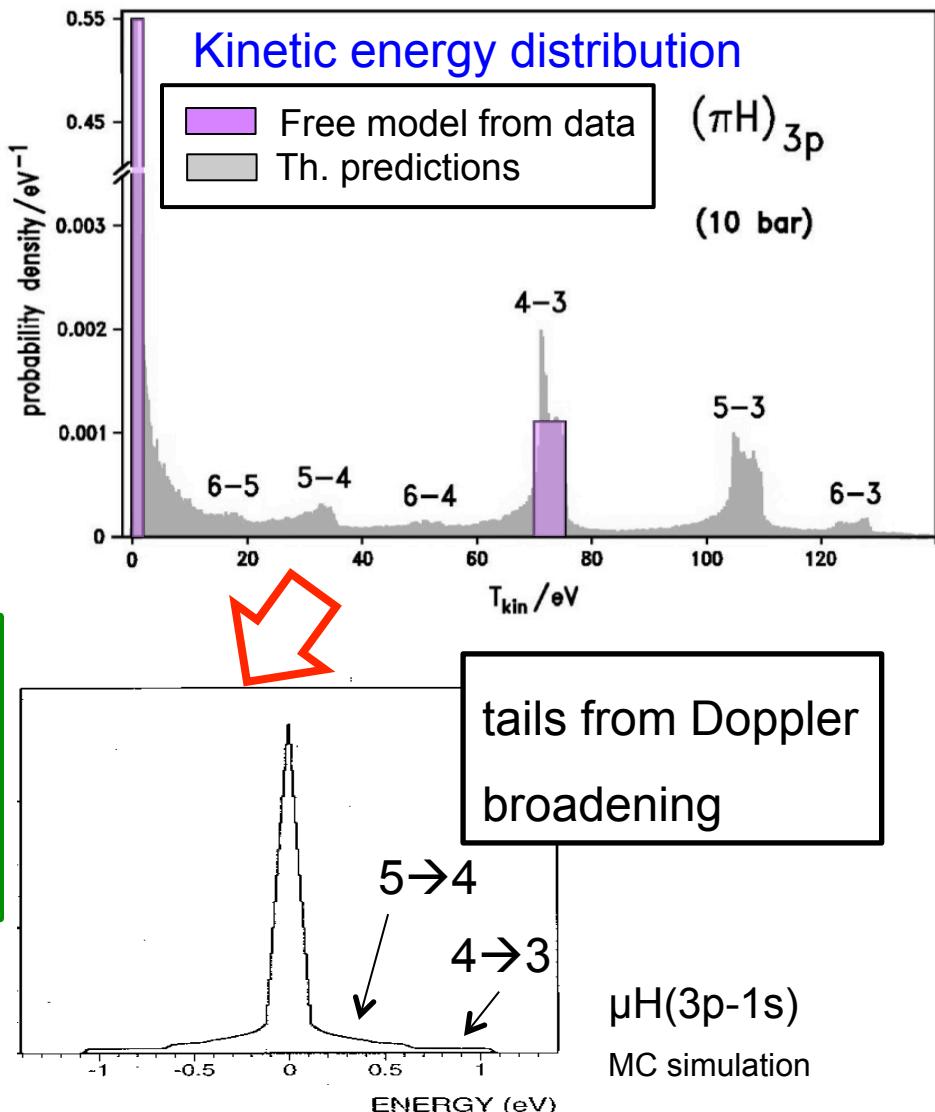
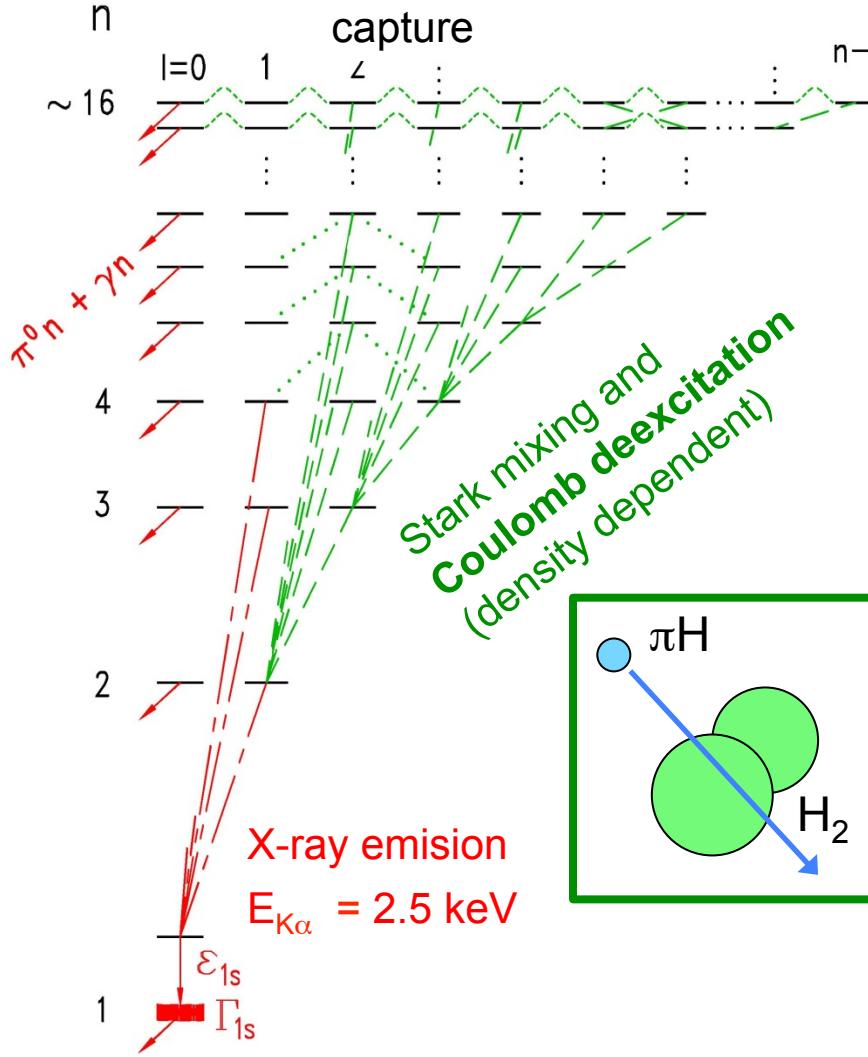


$$\Gamma_{\text{exp}} = \Gamma_{\text{crystal}} \otimes \Gamma_{\text{Doppler}} \otimes \Gamma_{1s}$$

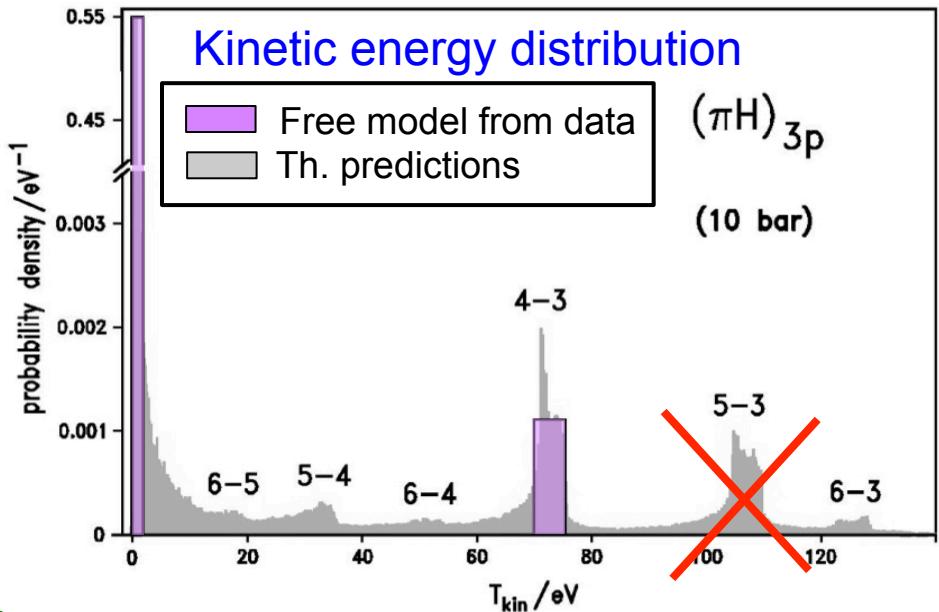
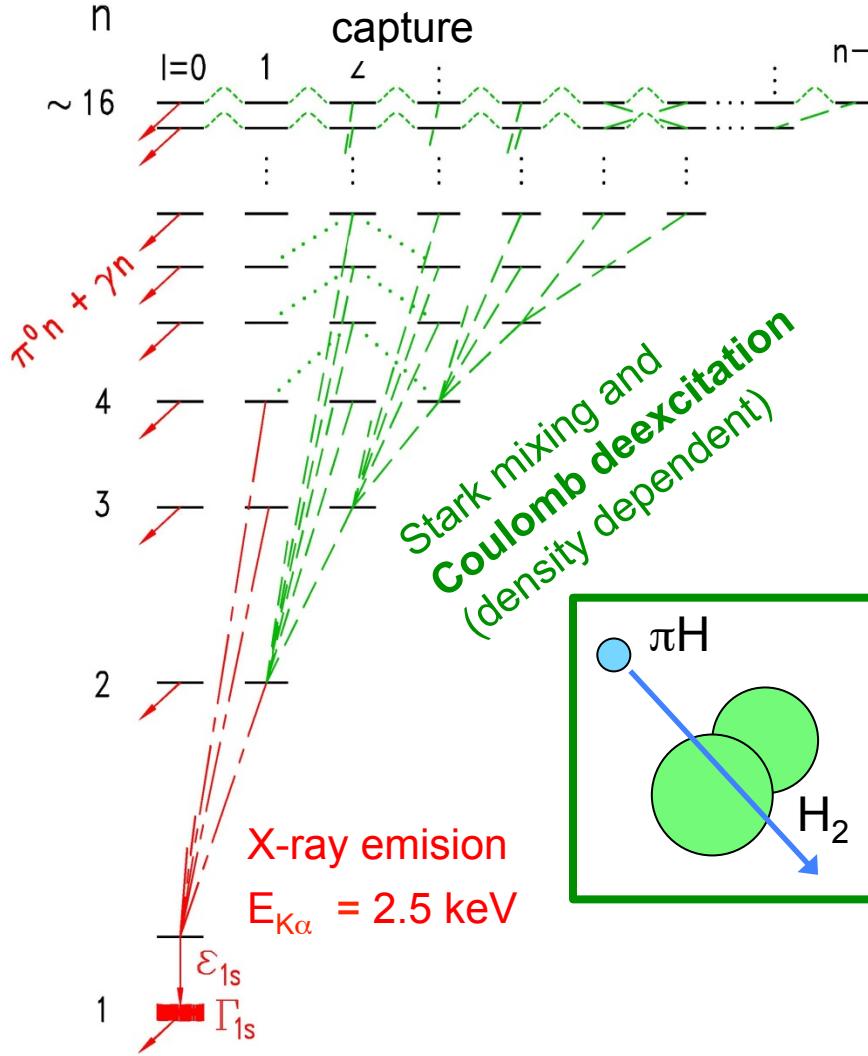
# Transitions induced by collisions in $\pi\text{H}$



# Transitions induced by collisions in $\pi\text{H}$



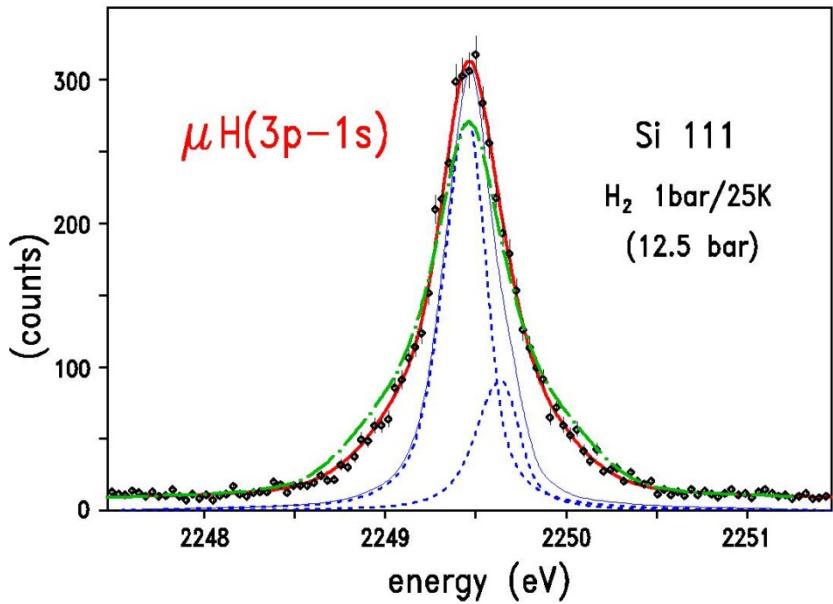
# Transitions induced by collisions in $\pi\text{H}$



Consistency to check!

→ Study of  $\mu\text{H}$ : strong interaction absorption in s-states

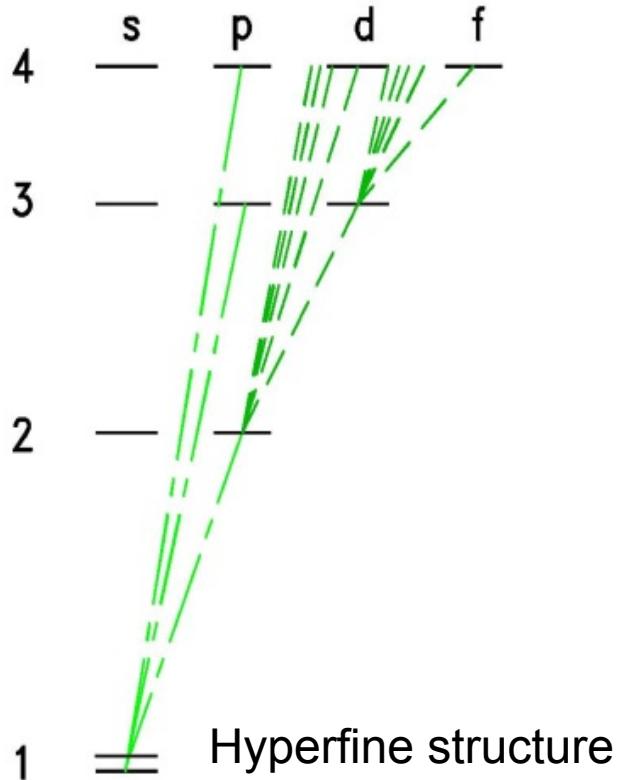
# Simpler: transitions induced by collisions in $\mu\text{H}!!$



High spectroscopy of  $\mu\text{H}$

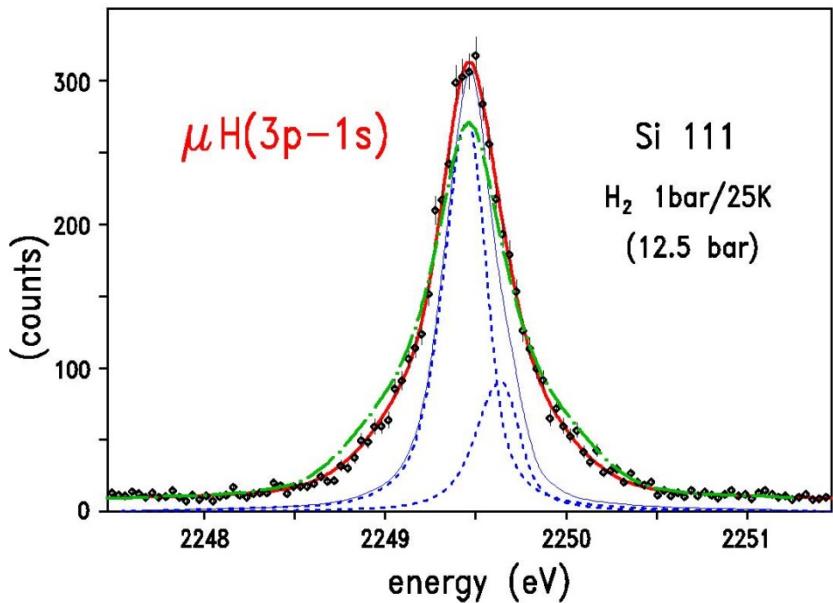


- Test of the cascade model



No strong interaction effects:  
nuclear absorption and energy shift

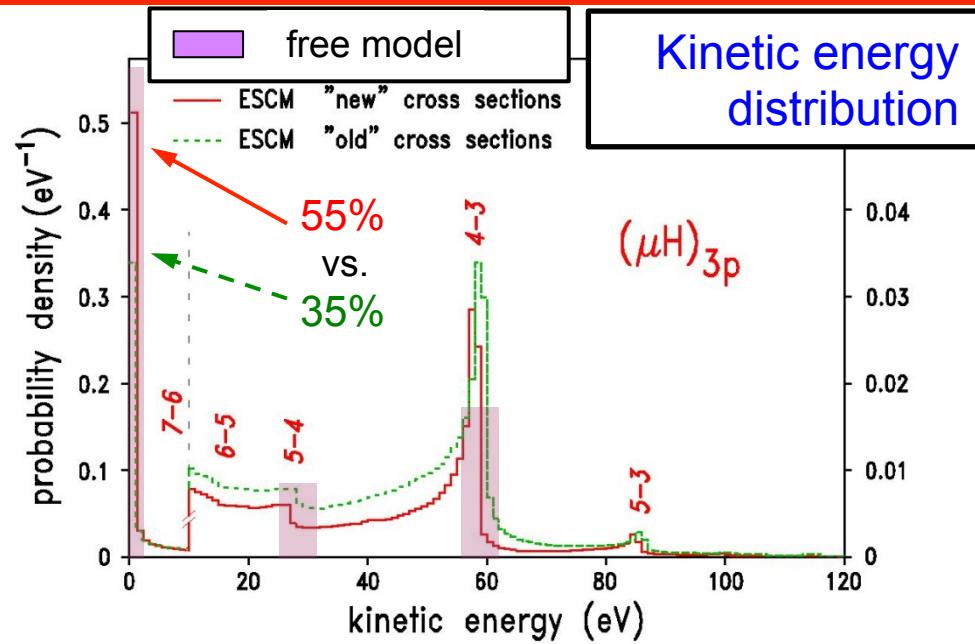
# Simpler: transitions induced by collisions in $\mu\text{H}!!$



High spectroscopy of  $\mu\text{H}$



- Test of the cascade model
- Test of the cross sections  
→ recalculation required
- First measurement of  $\mu\text{H}$  hyperfine (HF) splitting

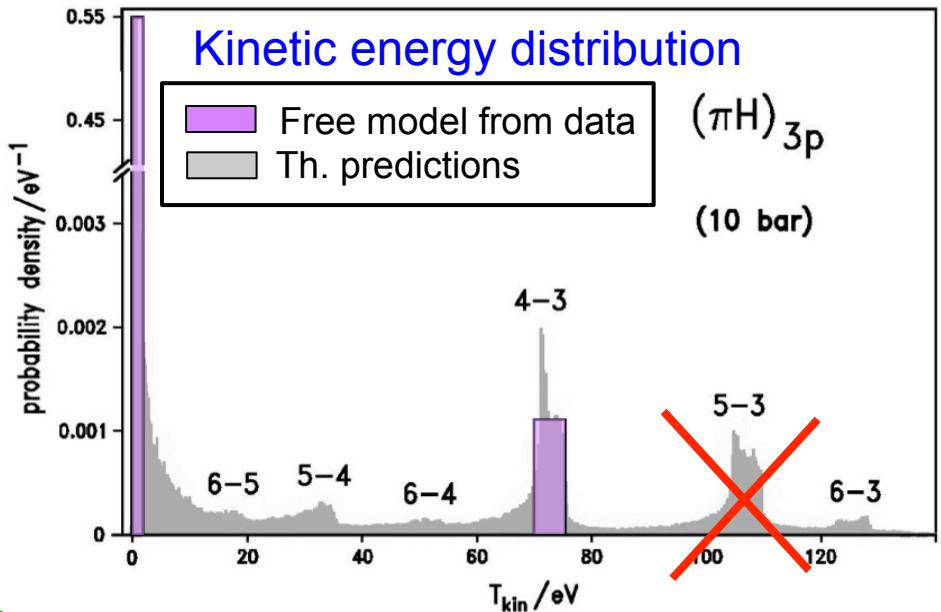
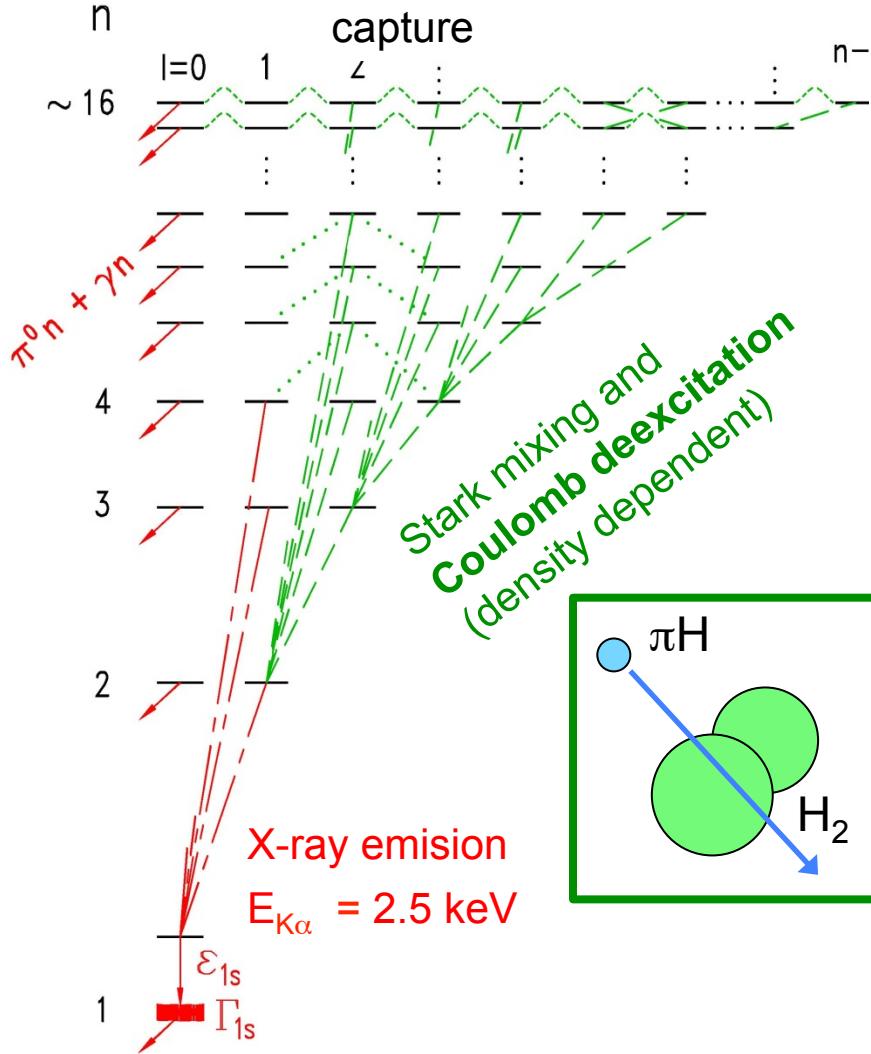


Good agreement with a free model with only 3 "kinetic population boxes"!!!

- {
- HF splitting =  $194 \pm 12 \text{ meV}$
  - Relative intensity ratio =  $3.0 \pm 0.3$   
(HF splitting fixed by theory =  $182:725 \pm 0.062 \text{ meV}$ )

Covita et al., Phys. Rev. Lett. **102**, 023401-4 (2009).

# Transitions induced by collisions in $\pi\text{H}$



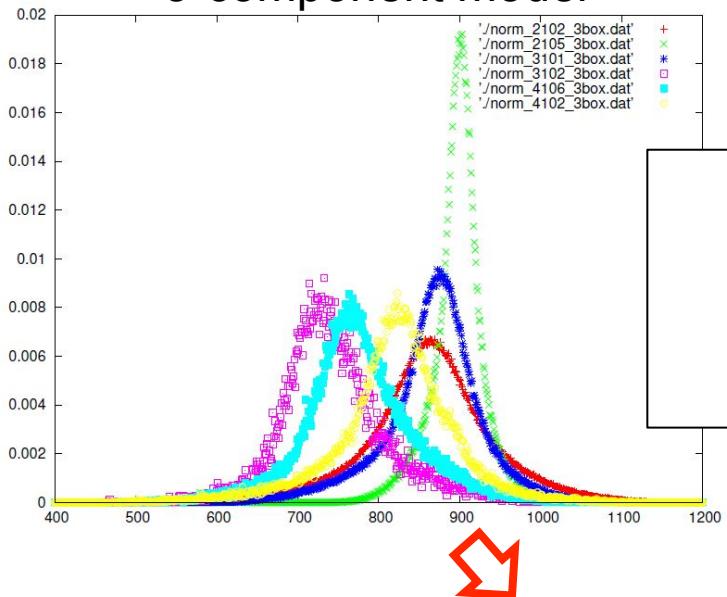
Still inconsistency between empirical findings and theory

# Pionic hydrogen hadronic width summary

Work in progress

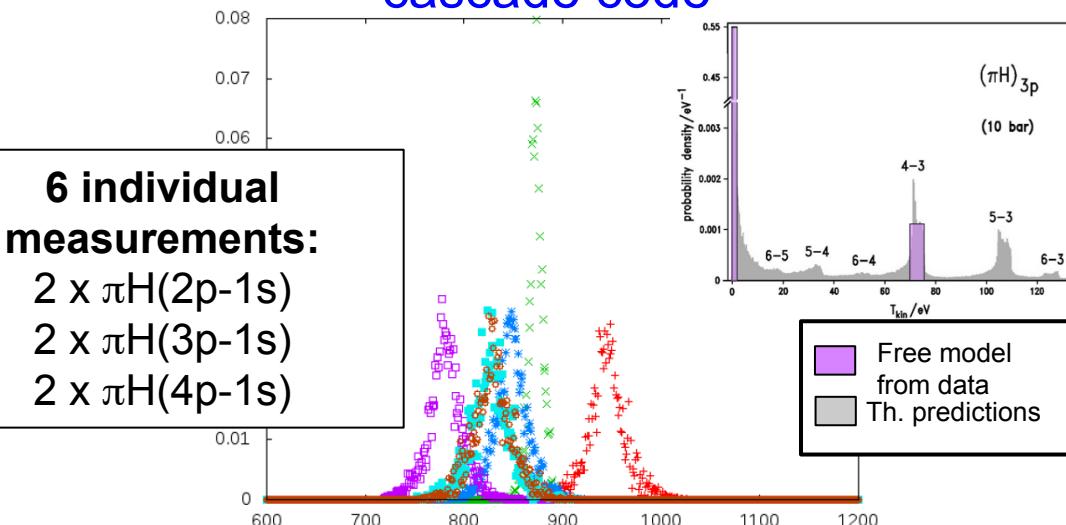
$$\Gamma_{exp} = \Gamma_{crystal} \otimes \Gamma_{Doppler} \otimes \Gamma_{1s}$$

Phenomenological approach  
3-component model



**6 individual measurements:**  
 2 x  $\pi\text{H}(2\text{p}-1\text{s})$   
 2 x  $\pi\text{H}(3\text{p}-1\text{s})$   
 2 x  $\pi\text{H}(4\text{p}-1\text{s})$

Kinetic energy distribution from cascade code



$$\Gamma_{1s} = 0.85^{+0.04}_{-0.05} \text{ eV} (\pm 4-5\%) \text{ preliminary}$$

Already 3-4 times better accuracy than Sigg et al. Phys. Rev. Lett. **75** 3245 (1995)  
 $\Delta\Gamma \rightarrow \Delta\Gamma/2$  with a good cascade understanding

# Strong interaction in simple bound systems

Shift and width related to the pion-nucleus scattering length and cross sections

$$\pi H \left\{ \begin{array}{l} \epsilon_{1s}^{\pi H} \propto a_{\pi^- p \rightarrow \pi^- p} + \text{corr.} \\ \Gamma_{1s}^{\pi H} \propto (a_{\pi^- p \rightarrow \pi^0 n})^2 + \text{corr.} \end{array} \right.$$



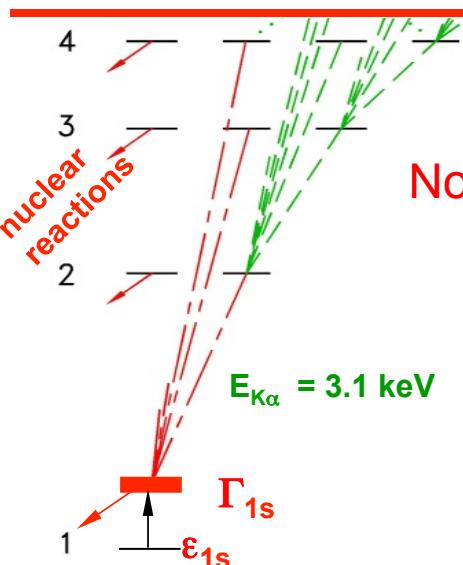
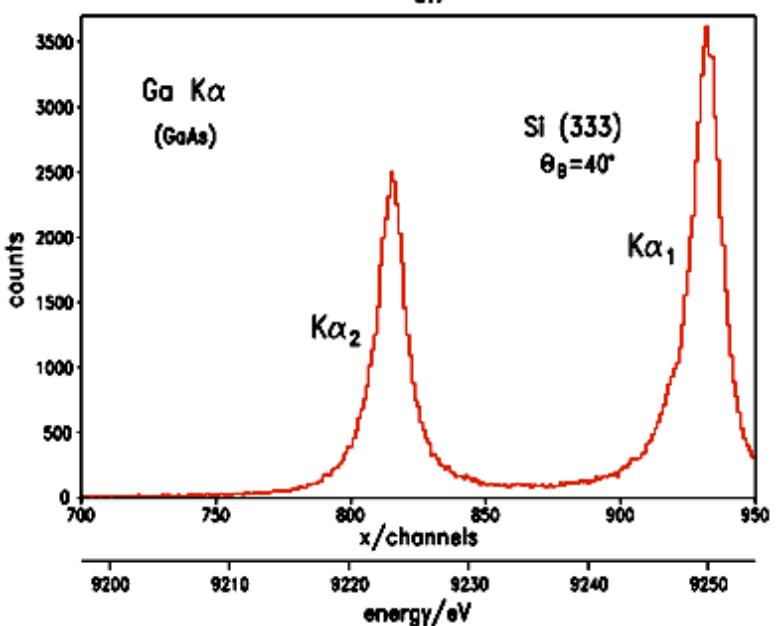
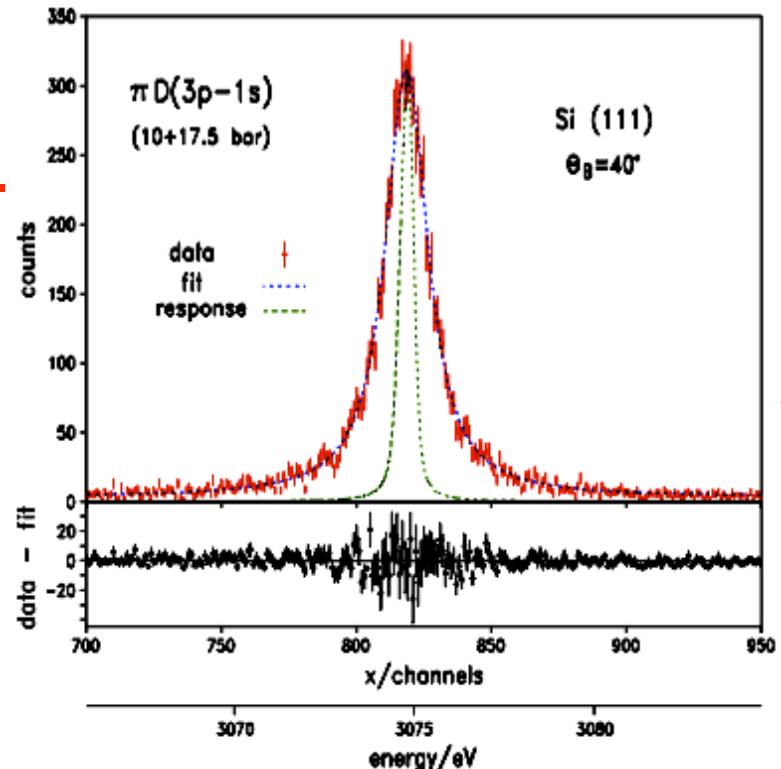
Ok...

$$\pi D \left\{ \begin{array}{l} \epsilon_{1s}^{\pi D} \propto a_{\pi^- p \rightarrow \pi^- p} + a_{\pi^- n \rightarrow \pi^- n} + \text{corr.} \\ \Gamma_{1s}^{\pi D} \propto \Im m(a_{\pi d \rightarrow \pi d}) \end{array} \right.$$



Basic pion-nucleon  
interaction properties

# Pionic deuterium results: shift



No molecular formation observed

## Uncertainty budget

$\pm 27 \text{ meV}$	Ga K $\alpha_2$
$\pm 10 \text{ meV}$	statistics
$\pm 8 \text{ meV}$	pion mass
$\pm 5 \text{ meV}$	systematics
$\pm 2 \text{ meV}$	QED

$$\epsilon_{1s} = -2.356 \pm 0.031 \quad (\pm 1.3\%)$$

(repulsive force)

3 times better accuracy than [2]

- PhD thesis: Th. Strauch, Cologne 2009
- [1] Th. Strauch et al., Phys. Rev. Lett. **104** 142503(2010);  
Eur. Phys. J A **47** 88 (2011)
- [2] Chatellard et al., Phys. Rev. Lett. **74**, 4157 (1995)

# Strong interaction in simple bound systems

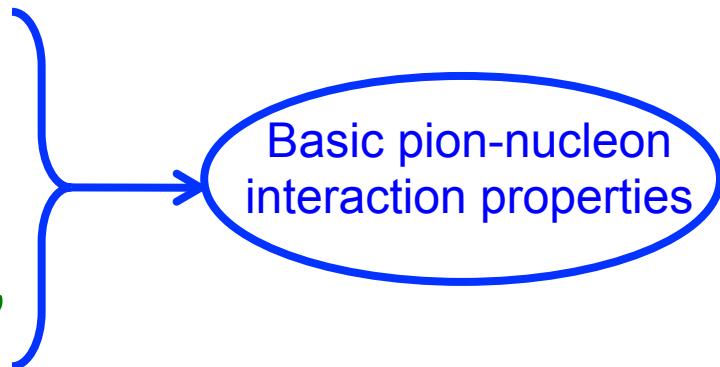
Shift and width related to the pion-nucleus scattering length and cross sections

$$\pi H \left\{ \begin{array}{l} \epsilon_{1s}^{\pi H} \propto a_{\pi^- p \rightarrow \pi^- p} + corr. \\ \Gamma_{1s}^{\pi H} \propto (a_{\pi^- p \rightarrow \pi^0 n})^2 + corr. \end{array} \right.$$

✓      Ok...

$$\pi D \left\{ \begin{array}{l} \epsilon_{1s}^{\pi D} \propto a_{\pi^- p \rightarrow \pi^- p} + a_{\pi^- n \rightarrow \pi^- n} + corr. \\ \Gamma_{1s}^{\pi D} \propto \Im m(a_{\pi d \rightarrow \pi d}) \end{array} \right.$$

✓



# Strong interaction in simple bound systems

Shift and width related to the pion-nucleus scattering length and cross sections

$$\pi H \left\{ \begin{array}{l} \epsilon_{1s}^{\pi H} \propto a_{\pi^- p \rightarrow \pi^- p} + \text{corr.} \\ \Gamma_{1s}^{\pi H} \propto (a_{\pi^- p \rightarrow \pi^0 n})^2 + \text{corr.} \end{array} \right. \quad \begin{array}{l} \propto a^+ + a^- + f_{LEC}(c_1, f_1, f_2) \\ \propto (a^-)^2 + g(c_1, f_2) \end{array}$$

Low energy constants of the effective Chiral Perturbation Lagrangian

$$\pi D \left\{ \begin{array}{l} \epsilon_{1s}^{\pi D} \propto a_{\pi^- p \rightarrow \pi^- p} + a_{\pi^- n \rightarrow \pi^- n} + \text{corr.} \\ \Gamma_{1s}^{\pi D} \propto \Im m(a_{\pi d \rightarrow \pi d}) \end{array} \right. \quad \propto a^+ + h.o.(a^+, a^-) + h_{LEC}(c_1, f_1, f_2)$$

## Isospin cattering lengths $a^\pm$

$\pi N$  isospin symmetry  
(2 quark flavour only)

$$1 \otimes 1/2 \Rightarrow 1/2 \oplus 3/2$$



**$a^+$  isoscalar**  
 **$a^-$  isovector**

# $\pi N$ scattering lengths results

$$\left. \begin{array}{l} \pi H \\ \pi D \end{array} \right\} \begin{array}{l} \epsilon_{1s}^{\pi H} \propto a^+ + a^- + f_{LEC}(c_1, f_1, f_2) \\ \Gamma_{1s}^{\pi H} \propto (a^-)^2 + g(c_1, f_2) \\ \epsilon_{1s}^{\pi D} \propto a^+ + h.o.(a^+, a^-) + h_{LEC}(c_1, f_1, f_2) \end{array}$$

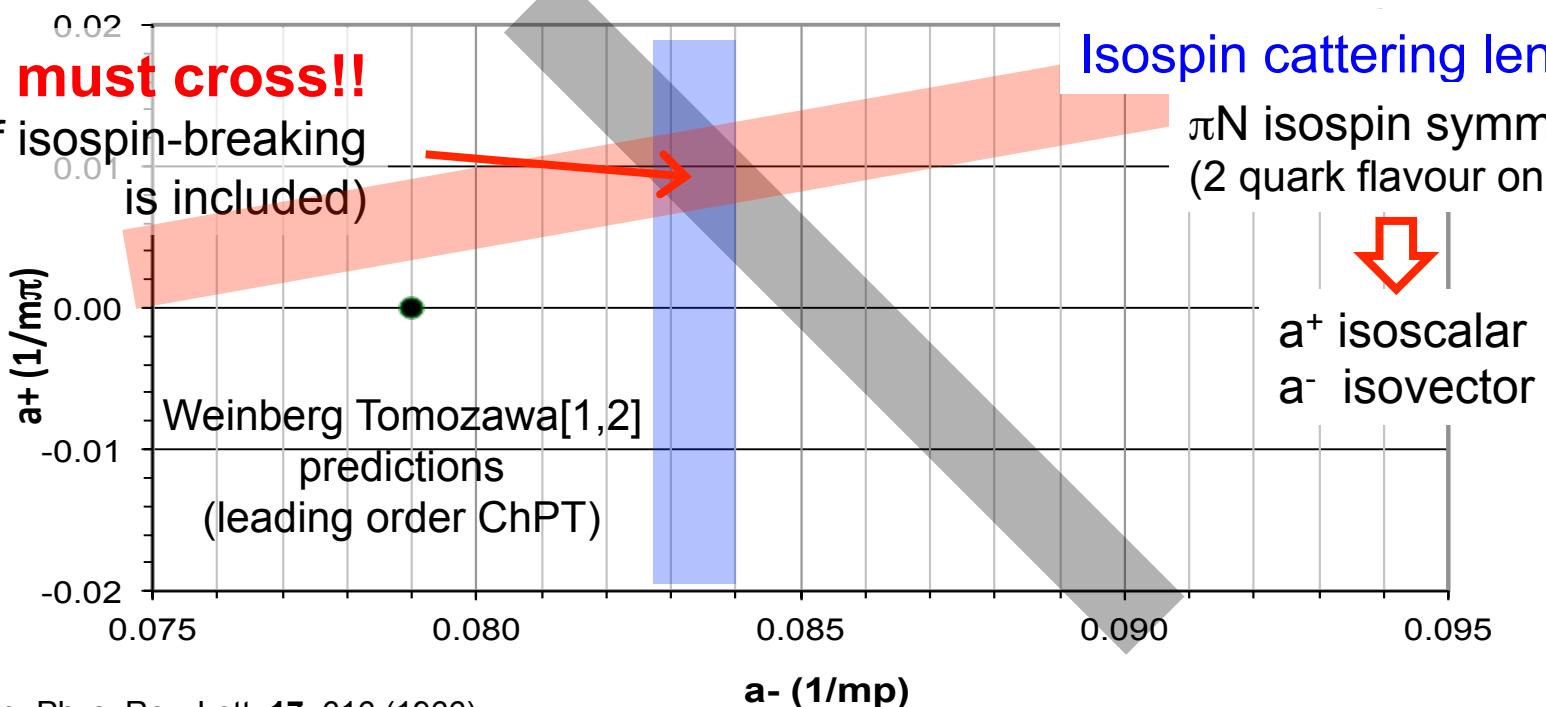
Qualitatively comparison  
with the Chiral Pert. Theory  
predictions

**They must cross!!**

(if isospin-breaking  
is included)

Isospin cattering lengths  $a^\pm$

$\pi N$  isospin symmetry  
(2 quark flavour only)



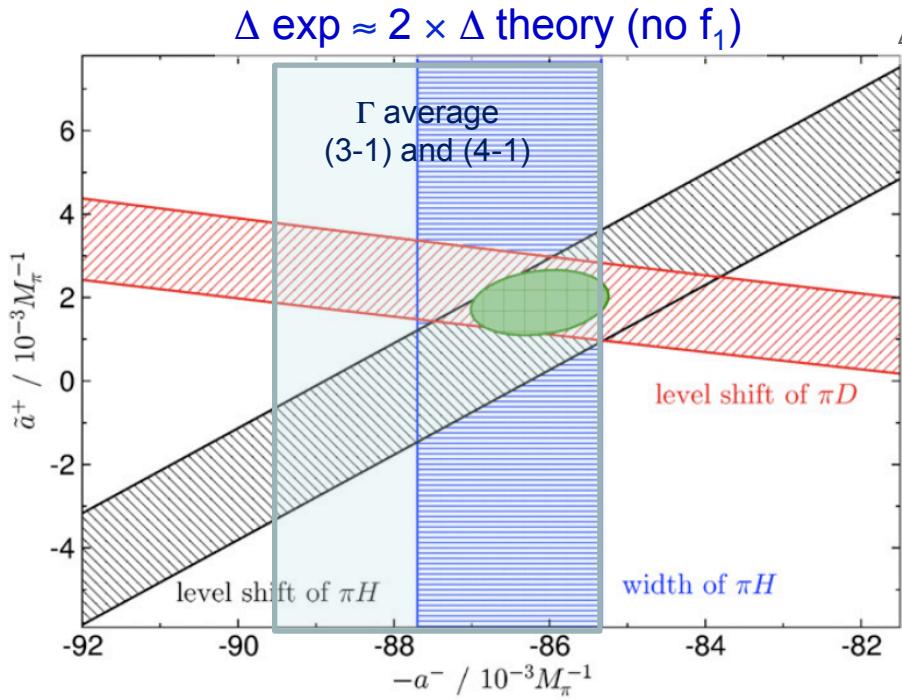
[1] Weinberg, Phys. Rev. Lett. **17**, 616 (1966)

[2] Y. Tomozawa, Nuovo Cim. A **46** 707 (1966)

# $\pi N$ scattering lengths results

$$\left. \begin{array}{l} \pi H \\ \pi D \end{array} \right\} \begin{array}{l} \epsilon_{1s}^{\pi H} \propto a^+ + a^- + f_{LEC}(c_1, f_1, f_2) \\ \Gamma_{1s}^{\pi H} \propto (a^-)^2 + g(c_1, f_2) \\ \epsilon_{1s}^{\pi D} \propto a^+ + h.o.(a^+, a^-) + h_{LEC}(c_1, f_1, f_2) \end{array}$$

Quantitatively comparison  
with the Chiral Pert. Theory  
predictions

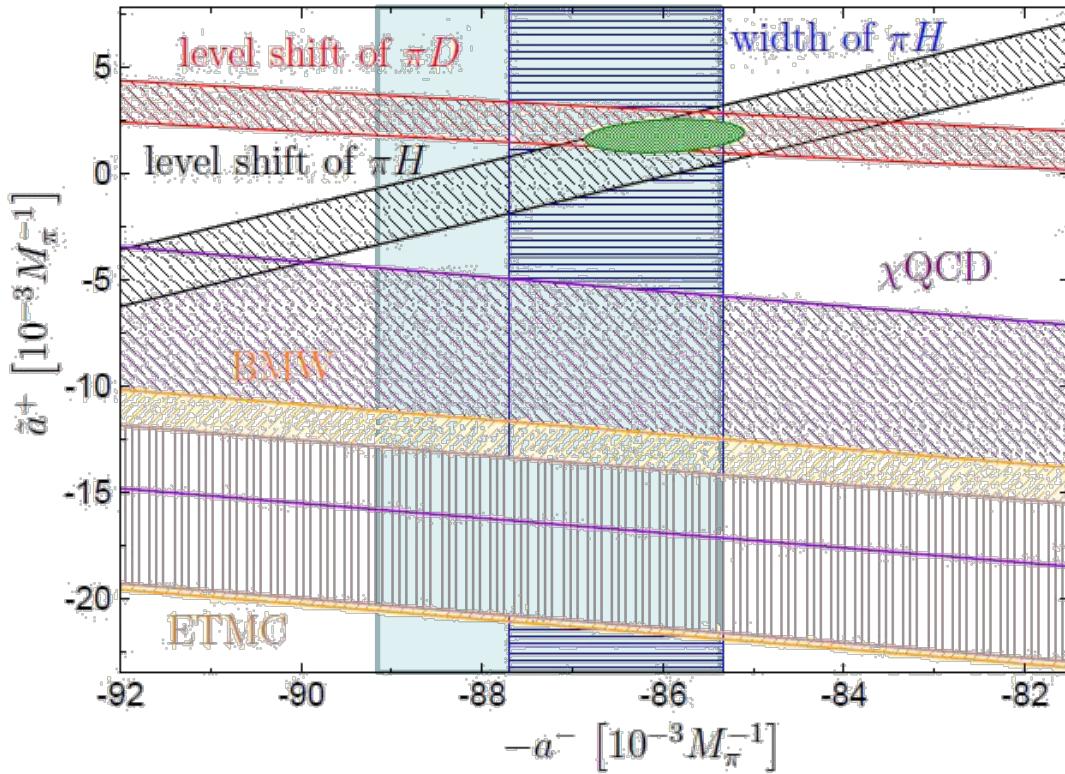


- consistency ✓
- $a^+ > 0 !!$
- Constraints on  $f_1$
- $\pi D$  decisive

Fig. 2. Combined constraints in the  $\tilde{a}^+ - a^-$  plane from data on the width and energy shift of  $\pi H$ , as well as the  $\pi D$  energy shift.

Baru et al., Phys. Lett. B **694**, 473-477 (2011).  
Baru et al., Nucl. Phys. A **872**, 69-116 (2011).

# Beyond chiral perturbation theory, lattice calculations and dark matter detection



← pionic atoms analysis

?

← Lattice predictions of  
the **sigma term**

M. Hoferichter, J. Ruiz de Elvira, B. Kubis,  
and U.-G. Meißner, Phys. Lett. B **760**,  
74-78 (2016)

$$a^+ \rightarrow \text{sigma term } \sigma_{\pi N} = \frac{\mathbf{m}_u + \mathbf{m}_d}{4M} \langle \mathbf{p} | \bar{u}u + \bar{d}d | \mathbf{p} \rangle \leftrightarrow \langle \mathbf{p} | \bar{s}s | \mathbf{p} \rangle \text{ contents} \rightarrow 59.1 \pm 3.5 \text{ MeV}$$

Crucial for the interpretation of dark-matter direct-detection experiments!!

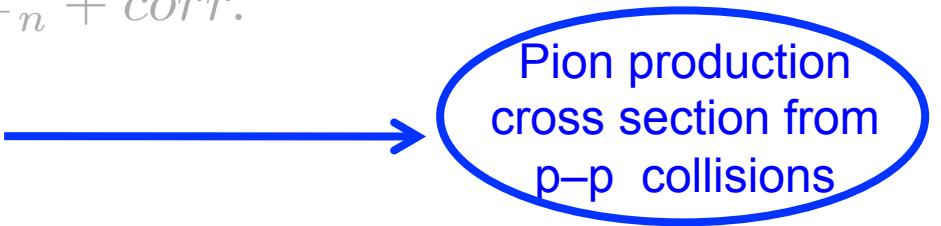
J. Ellis, K.A. Olive, and C. Savage, Phys. Rev. D **77**, 065026 (2008)

$a^- \rightarrow$  pion–nucleus coupling constant via GMO sum rule

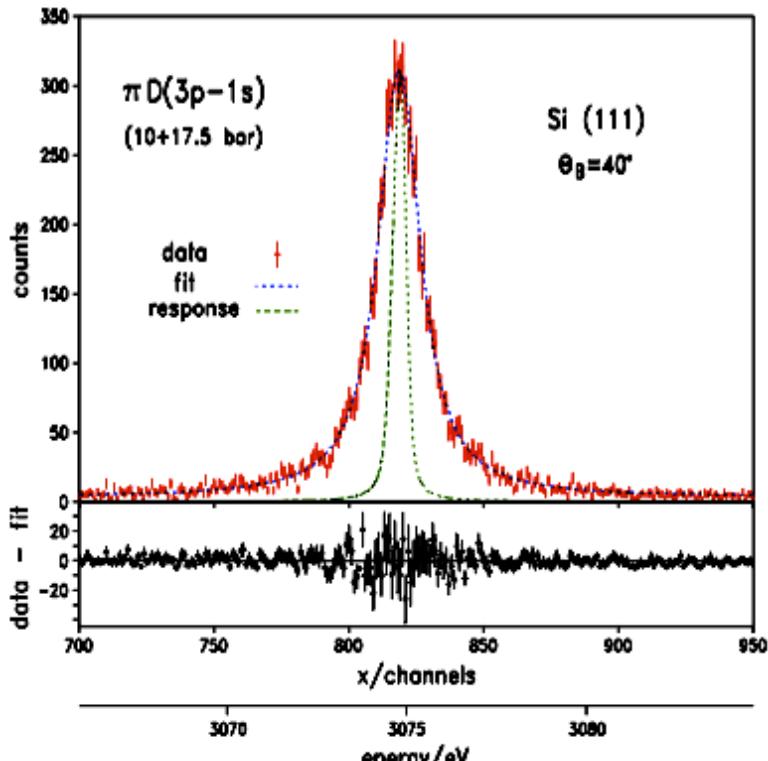
# Pionic deuterium width

$$\pi H \left\{ \begin{array}{l} \epsilon_{1s}^{\pi H} \propto a_{\pi^- p \rightarrow \pi^- p} + corr. \\ \Gamma_{1s}^{\pi H} \propto (a_{\pi^- p \rightarrow \pi^0 n})^2 + corr. \end{array} \right.$$

$$\pi D \left\{ \begin{array}{l} \epsilon_{1s}^{\pi D} \propto a_{\pi^- p \rightarrow \pi^- p} + a_{\pi^- n \rightarrow \pi^- n} + corr. \\ \Gamma_{1s}^{\pi D} \propto \Im m(a_{\pi d \rightarrow \pi d}) \end{array} \right.$$

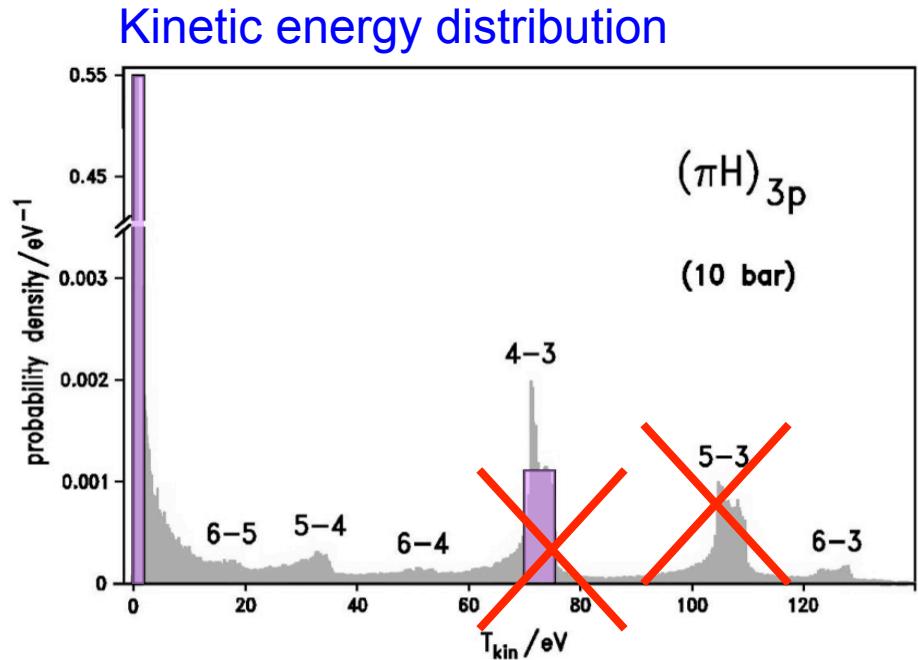


# Pionic deuterium results: width



$$\Gamma_{1s} = 1171^{+23}_{-49} \text{ meV (2-4\%)} [1]$$

4 times better accuracy than [2]



no (small) high-energy components  
due to the isotopic effect [3]

PhD thesis: Th. Strauch, Cologne 2009

[1] Strauch et al., Phys. Rev. Lett. **104** 142503 (2010); Eur. Phys. J. A **47** 88 (2011)

[2] Chatellard et al., Phys. Rev. Lett. **74**, 4157 (1995)

[3] Popov and V.N. Pomerantsev, Phys. Rev. A **95**, 022506 (2017)

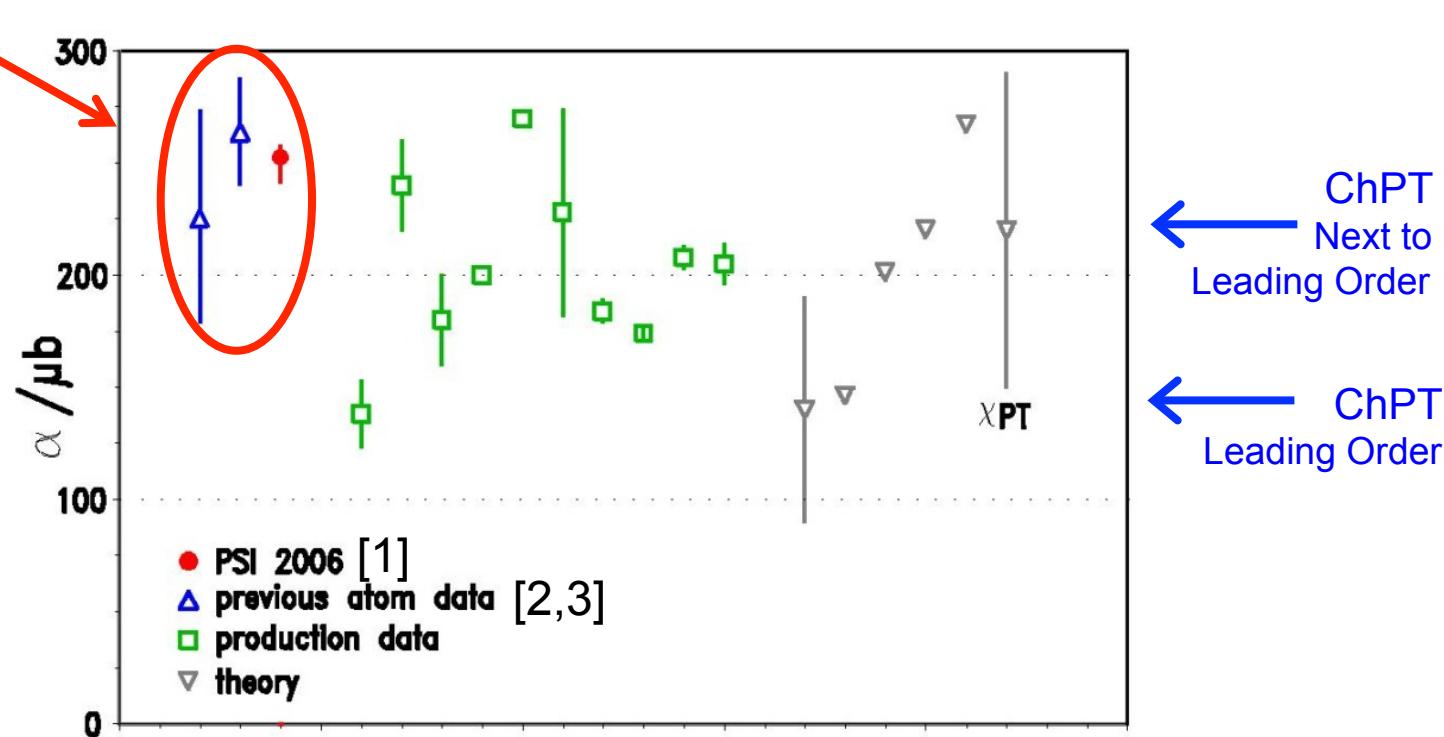
# Pion production cross section

correction factor due to the Coulomb interaction contribution (large uncertainty)

$$\pi D \quad \Gamma_{1s}^{\pi D} \propto \Im m(a_{\pi d \rightarrow \pi d}) \propto \alpha$$

$$\sigma_{pp \rightarrow \pi^+ d} = \alpha C_0^2 \frac{p_\pi}{m_\pi} + \beta C_1^2 \left( \frac{p_\pi}{m_\pi} \right)^3 + \dots$$

Pionic atoms results



[1] Th. Strauch et al.,  
Phys.Rev.Lett.**104** 142503  
(2010) Eur. Phys.J A **47** 88  
(2011) 88

[2] D. Chatellard et al. Phys.  
Rev. Lett. **74** 4157 (1995)  
Nucl. Phys. A **625** (1997) 855  
[3] P. Hauser et al. Phys. Rev. C  
**58** R1869 (1998)

# Summary

- Introduction
  - Test of QED in strong field
  - Study of strong interaction force at low energy
- Heavy highly charged ions
  - Production
  - Lamb shift measurement
  - Vacuum decay experiment
- Pionic atoms
  - Production
  - Pionic hydrogen and deuterium spectroscopy
  - **Pion mass measurement**
- Conclusions and outlooks

# Pion mass measurement from $\pi N$ and $\mu O$ X-ray spectroscopy

Pion mass (unknown) or muon mass (reference)

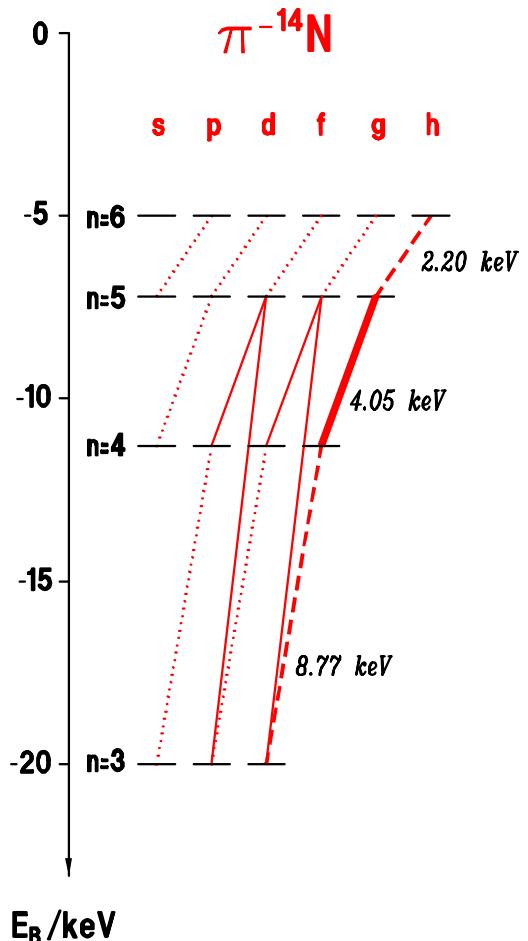
$$E_{\text{X-ray}} = mc^2 \frac{(Z\alpha)^2}{2} \left( \frac{1}{n_f^2} - \frac{1}{n_i^2} \right) + \mathcal{O}(Z^4\alpha^4)$$

QED calculation only

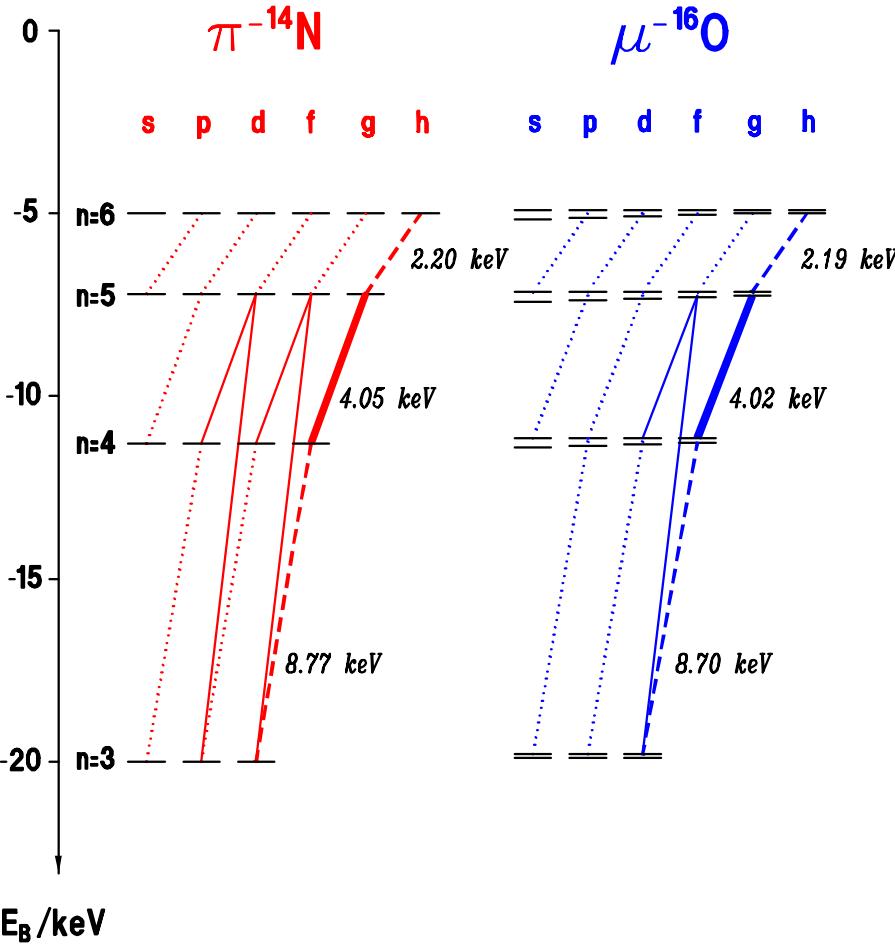
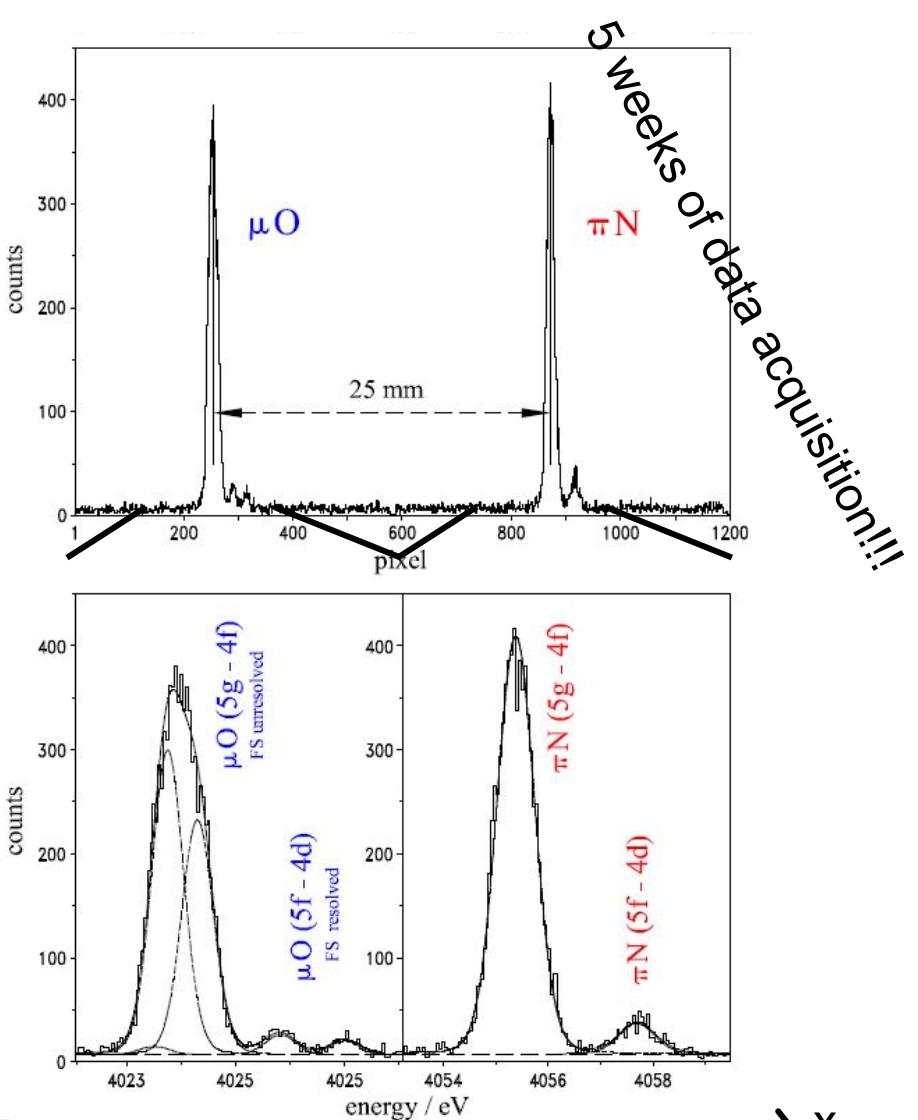
**Circular transition enhanced**

$$|n, \ell = n\rangle \rightarrow |n-1, \ell = n-1\rangle$$

**Strong interaction effects minimized**



# 5g-4f transitions in $\pi N$ and $\mu O$

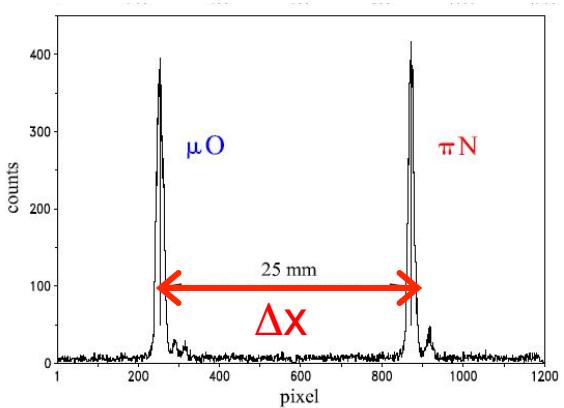


Muon =  $1/2$ -spin particle  
 $\rightarrow$  fine structure in  $\mu O$

# From the line position to the pion mass

From the spatial diff. to the angular position diff.

$$\Delta\Theta = -2 \arctan \left( \frac{\Delta x}{2D} \right)$$



$$\frac{hc}{E} = 2d \sin \Theta_B$$

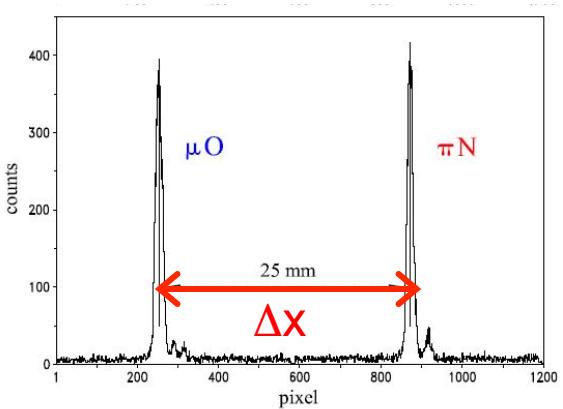
Bragg law

[1] M.T. and P. Indelicato, Phys. Rev. A **76**, 012510(2007)

# From the line position to the pion mass

From the spatial diff. to the angular position diff.

$$\Delta\Theta = -2 \arctan \left( \frac{\Delta x}{2D} \right)$$



From the angular position diff. to the transition energy

$$E_{\pi N} = E_{\mu O} \frac{1}{\cos \Delta\Theta - \frac{\sqrt{1-[hc/(2dE_{\mu O})]^2}}{hc/(2dE_{\mu O})} \sin \Delta\Theta}$$

where

$$E_{\mu O} = f_{\text{QED}_{\text{Dirac}}}(m_\mu) = \tilde{m}_\mu c^2 \frac{(Z\alpha)^2}{2} \left( \frac{1}{n_f^2} - \frac{1}{n_i^2} \right) + \mathcal{O}_{\text{QED}_{\text{Dirac}}}(Z^4 \alpha^4)$$

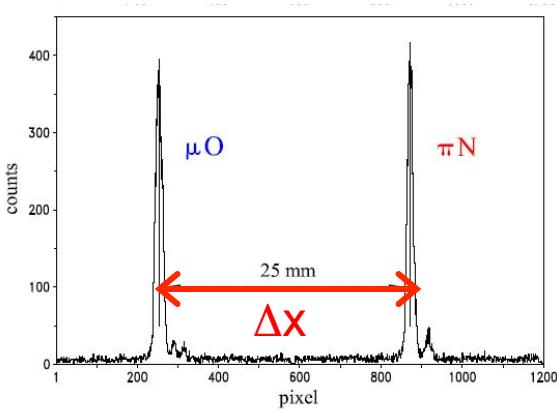
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Bragg law

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$$\frac{hc}{E} = 2d \sin \Theta_B$$

Bragg law

From the transition energy to the pion mass

$$m_\pi = f_{\text{Klein-Gordon}}^{-1}(E_{\pi N})$$



QED calculation (for πN) [1], ....

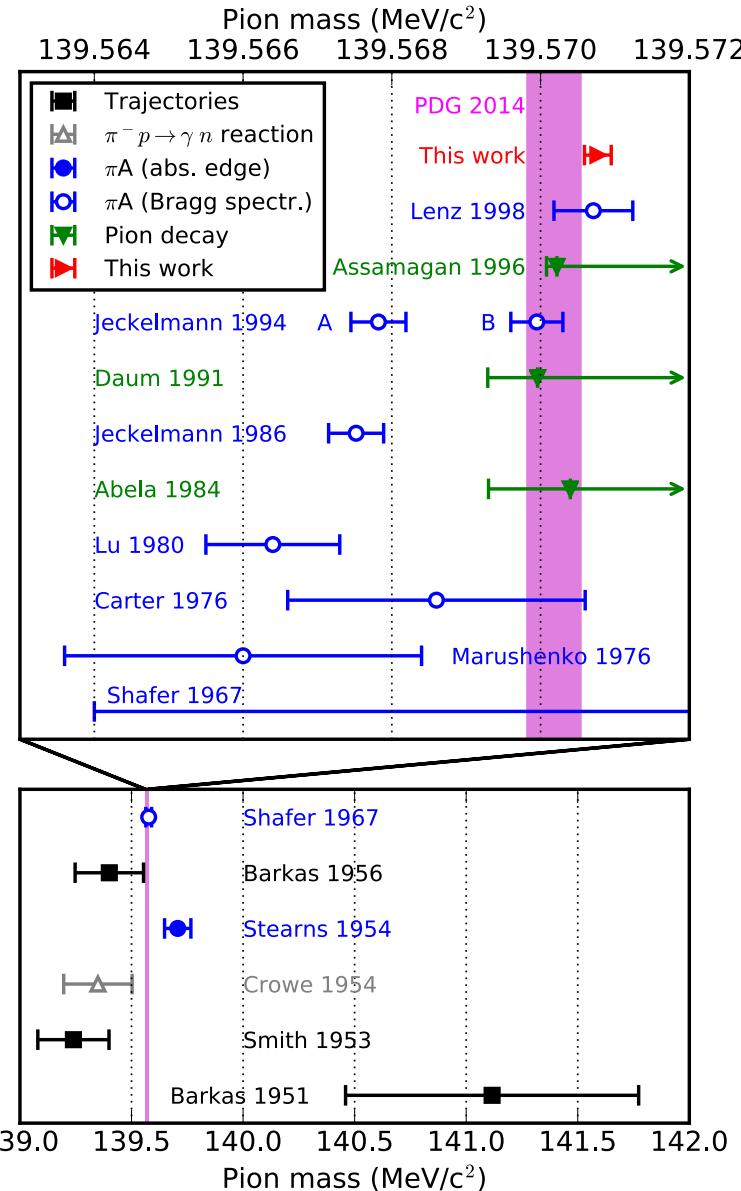
[1] M.T. and P. Indelicato, Phys. Rev. A **76**, 012510(2007)

# List of systematic effects

type of uncertainty	$\mu\Omega$ / arcsec	$\pi N$ / arcsec	total / arcsec	uncertainty / ppb
index of refraction shift	13.22	12.94	- 0.28	$\pm 20$
silicon lattice constant				$\pm 2$
bending correction	14.01	13.71	0.30	$\pm 20$
penetration depth correction	-0.07	-0.07	0	$\pm 4$
focal length				$\pm 670$
CCD alignment				$\pm 340$
pixel distance				$\pm 120$
alignment of detector normal				+ 0 - 30 + 0 - 35
detector height offset				$\pm 100$
shape of target window				$\pm 225$
shape of reflection				$\pm 150$
individual curvature correction				$\pm 30$
temperature correction				+ 290 - 350 + 190 - 290
response function and Doppler broadening				$\pm 15$
line pattern modelling				
fit interval				
QED energy				$\pm 350$
conversion constant $hc$				$\pm 2$
$4f$ strong interaction $45 \mu\text{eV}$	0.003	-0.003		$\pm 10$
$5g$ strong interaction $0.2 \mu\text{eV}$	0.000	0.000		$\pm 0$
K electron screening				$\pm 0$
total systematic error				+ 950 - 1000
statistical error				$\pm 820$

Total uncertainty:  $1.3 \times 10^{-6}$   
 Statistical:  $0.8 \times 10^{-6}$   
 Systematics:  $\sim 1 \times 10^{-6}$

# The new measurement of the pion mass



Particle data group [1]:  
 $139.57018 \pm 0.00035 \text{ MeV}/c^2$   
 →  $2.5 \times 10^{-6}$  accuracy

Our work [2]:  
 $139.57077 \pm 0.00018 \text{ MeV}/c^2$   
 →  $1.3 \times 10^{-6}$  accuracy

- No effect of eventual remaining K-shell electrons ( $< 10^{-9}$ )
- High accuracy calibration line ( $0.25 \times 10^{-6}$  from theory calc.)

→ Improved accuracy for X-ray standards from pionic atoms [3]

- [1] Particle Data Group. Chinese Phys. C **38**, 090001 (2014)  
 [2] M.T. et al., Phys. Lett. B **759**, 583-588 (2016)  
 [3] D.F. Anagnostopoulos et al, Phys. Rev. Lett. **91**, 240801 (2003)

# Summary

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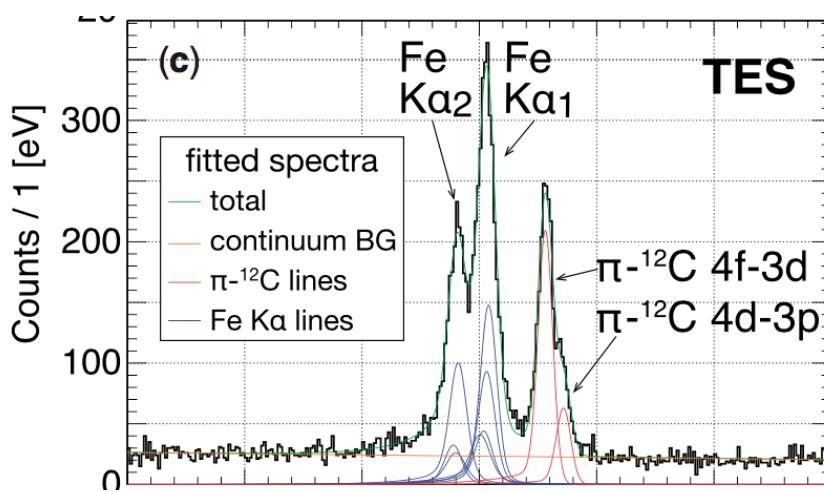
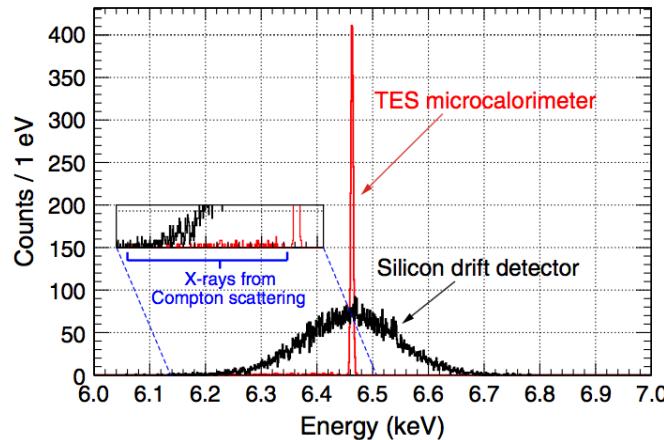
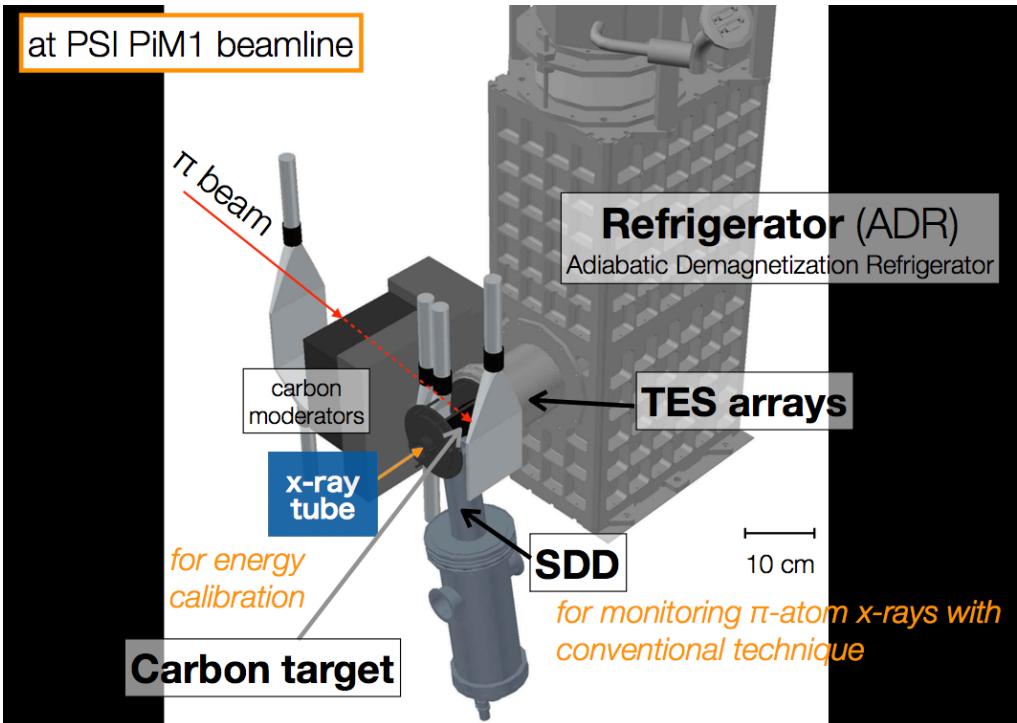
# Conclusions and perspectives for pionic atoms

- End of a long measurement campaign
- New input for investigation on strong interaction at low energy
- Deeper understanding (but not yet complete) of the atomic cascade and cross sections in exotic atomic systems
- New measurement of the pion mass

## Next...

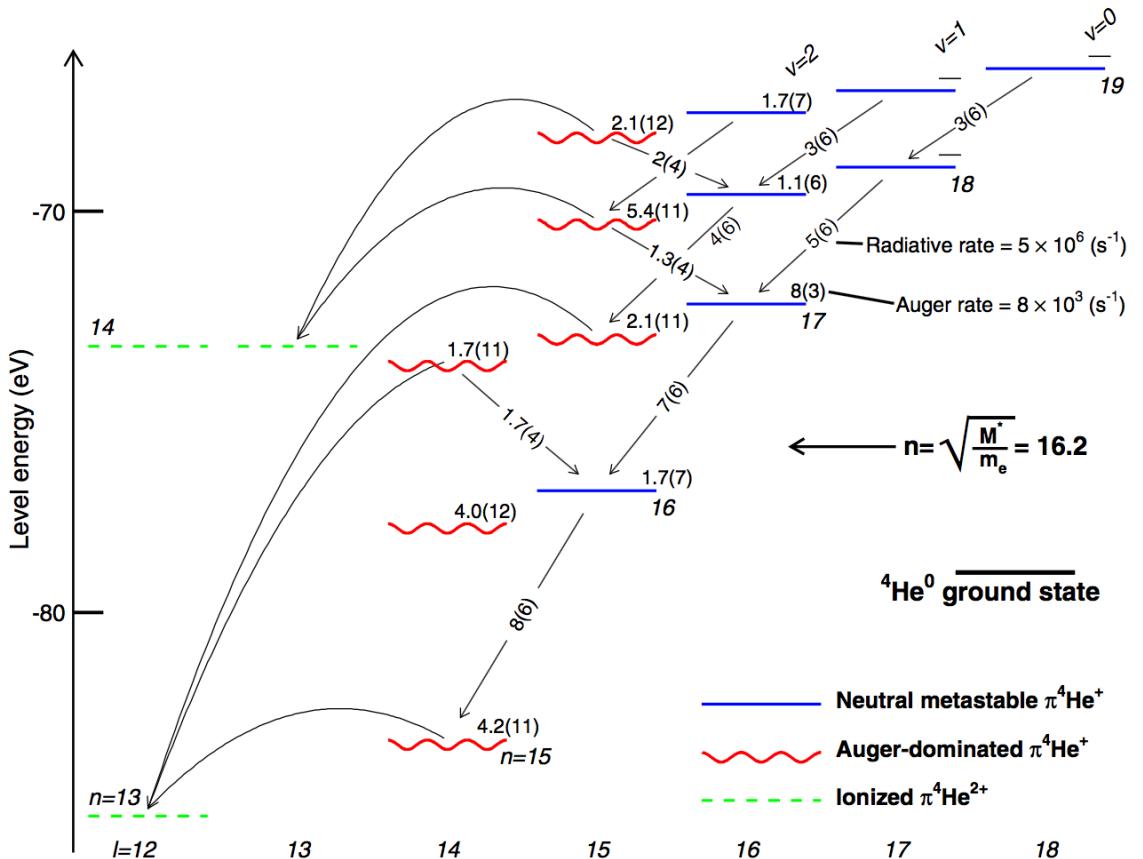
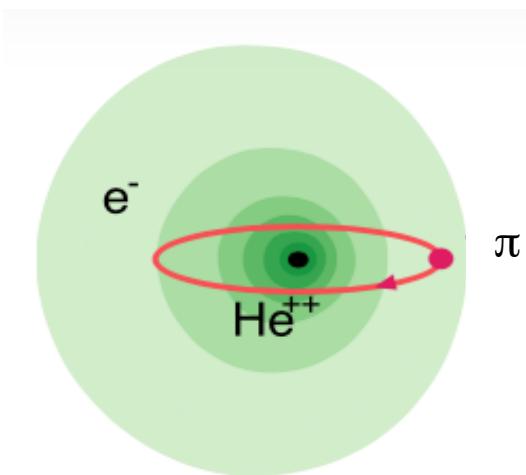
- Atomic cascade and cross sections calculations has to be improved
- New high-resolution experiments with  $\pi T$  and  $\pi He?$  → Additional constraints on  $a^+$  at ...
- Resolution improvement? • Crystal spectrometer:  $0.5 \rightarrow 0.2$  eV?  
• Microcalorimeter [1]? Lower resolution but higher efficiency
- New measurement of the pion mass: laser spectroscopy of  $\pi He^+$   
Proposed experiment at PSI from Hori and co. [2]

# Microcalorimeter measurement of $\pi A$ and $KA$



S. Okada, D.A. Bennett, C. Curceanu *et al.*, Progress of Theoretical and Experimental Physics **2016**, (2016)  
 S. Okada, D.A. Bennett, W.B. Doriese *et al.*, J. Low Temp. Phys. **176**, 1015-1021 (2014)

# Pion mass measurement by laser spectroscopy of $\pi\text{He}^+$



Goal accuracy: better than 1ppm

M. Hori *et al.*, Hyperfine Interact. **233**, 83-87 (2015).  
 M. Hori *et al.*, Phys. Rev. A **89**, 042515 (2014).

# Conclusions and perspectives for heavy highly charged ion

- New QED tests in the strong Coulomb field (non perturbative regime)
- New phenomenon expected (spontaneous emission of positrons from the vacuum decay)
- Two-loop QED not yet tested in hydrogenlike systems

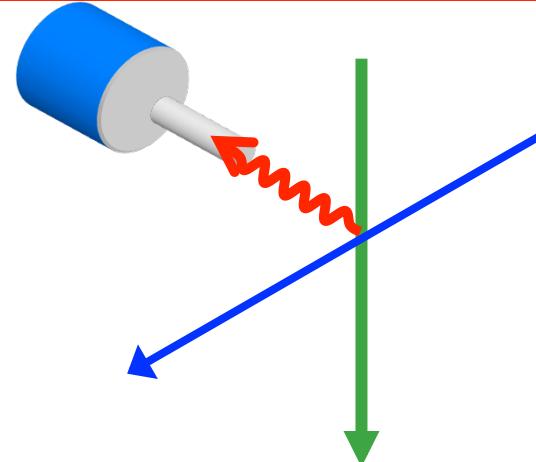
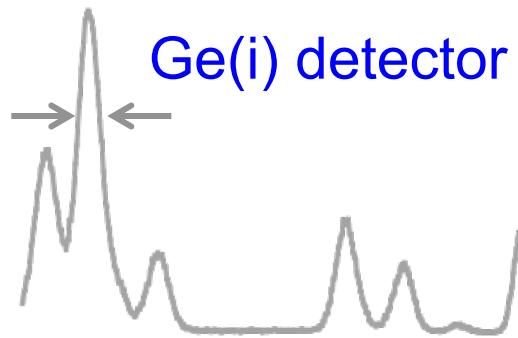
## Next...

- Many new experiments already in preparation for the future
- New experimental methods in development
- New FAIR facility in construction and commissioning

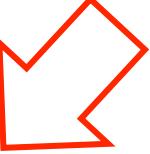
# Towards an accuracy of 1 eV of the 1s level Lamb shift

Resolution:  
**400 eV at 60 keV**

$$\epsilon = 10^{-4}$$

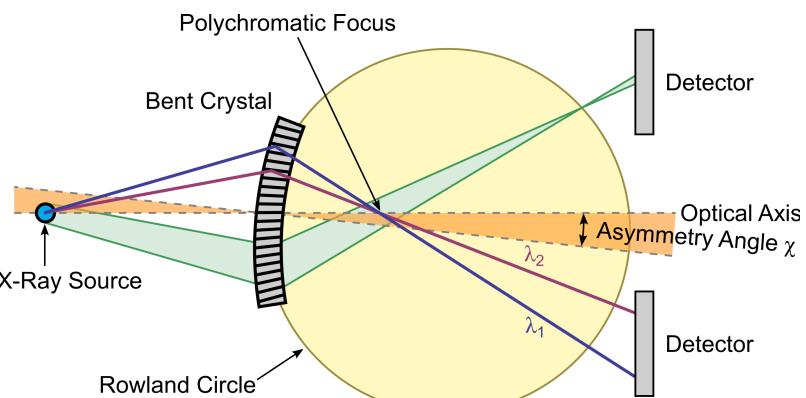


**U<sup>91+</sup> Lamb shift  $\delta E = 4.6 \text{ eV}$**



**Crystal spectroscopy**

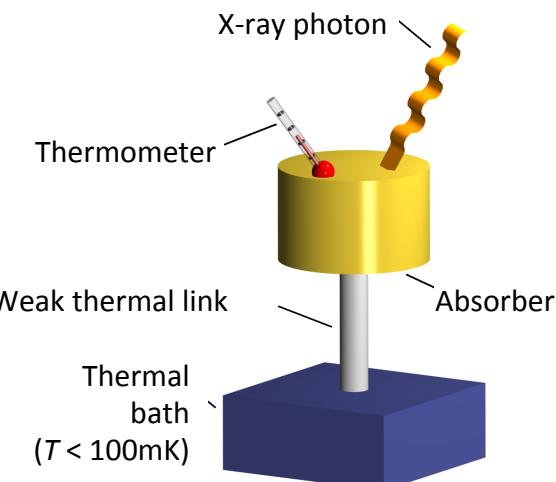
Res:  $\sim 50 \text{ eV}$  at 60 keV  $\epsilon = 10^{-8}$



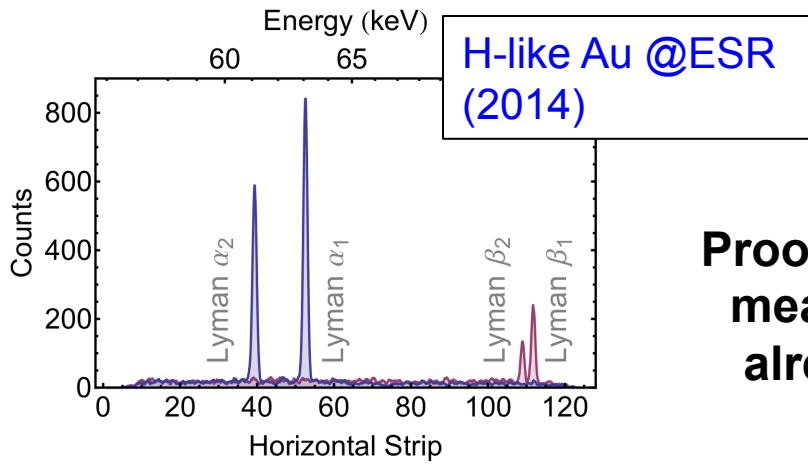
T. Gassner, M.T. et al submitted to PRL

**Resistive and magnetic microcalorimeters**

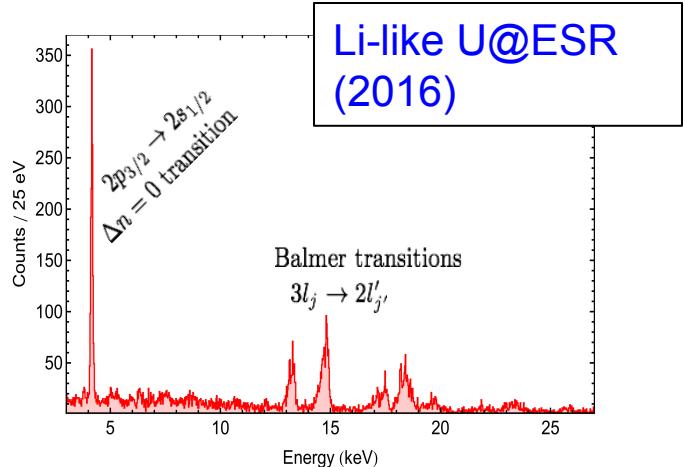
- S. Kraft-Bermuth *et al.*, J. Phys. B **50**, 055603 (2017)  
 C. Pies *et al.*, J. Low Temp. Phys. **167**, 269-279 (2012)



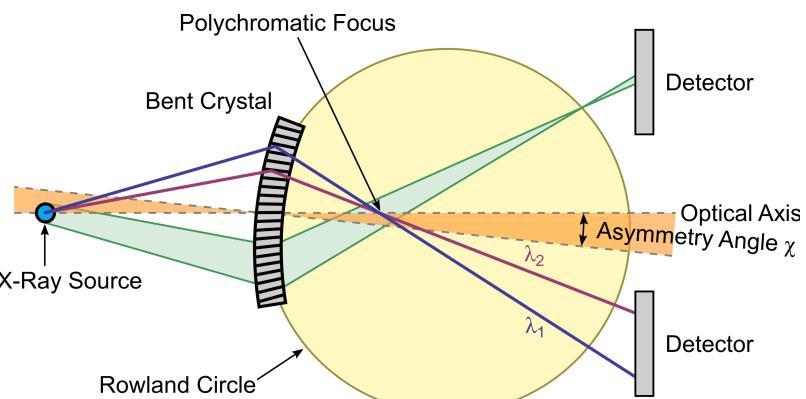
# Towards an accuracy of 1 eV of the 1s level Lamb shift



**Proof of principle measurements already done!**



**Crystal spectroscopy**  
Res:  $\sim 50$  eV at 60 keV  $\epsilon = 10^{-8}$



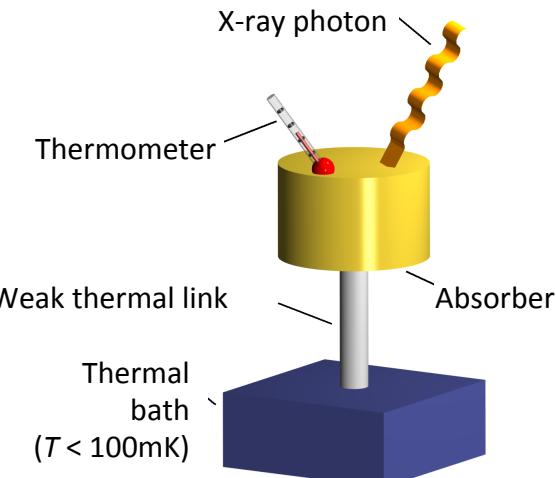
**FOCAL spectrometer**  
T. Gassner, M.T. et al submitted to PRL

6 November 2017

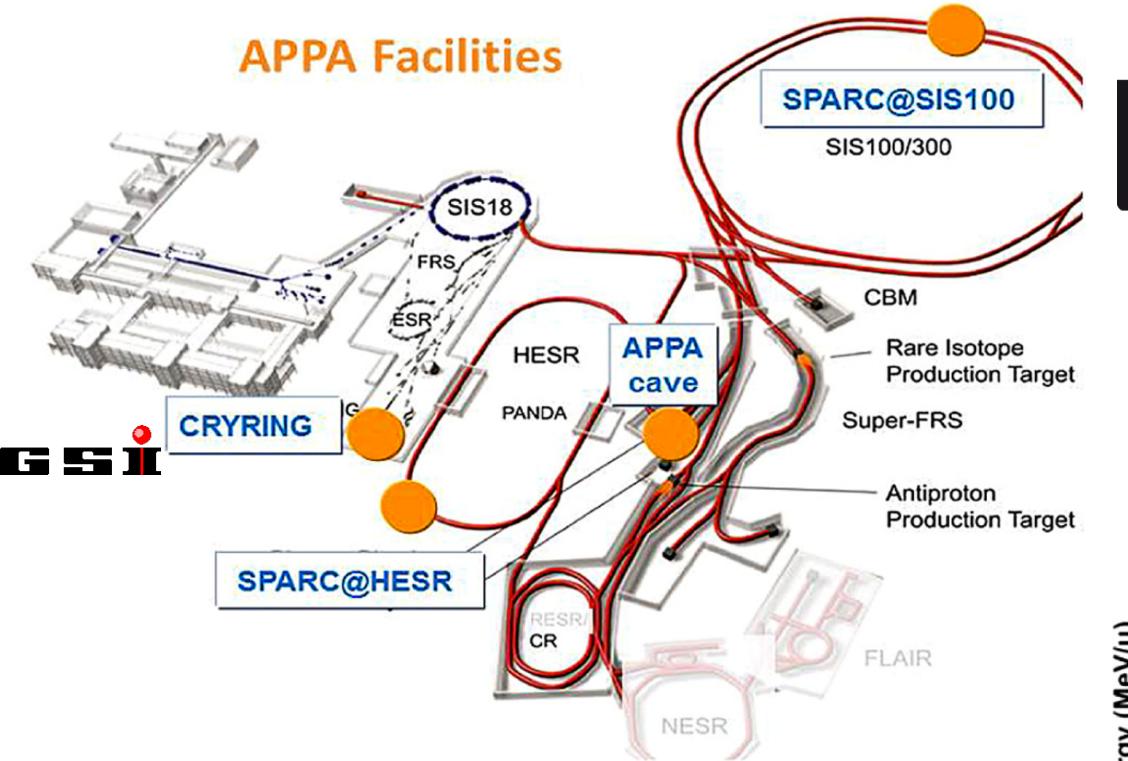
pA and HCl - Martino Trassinelli

- S. Kraft-Bermuth *et al.*, J. Phys. B **50**, 055603 (2017)  
 C. Pies *et al.*, J. Low Temp. Phys. **167**, 269-279 (2012)

**Resistive and magnetic microcalorimeters**

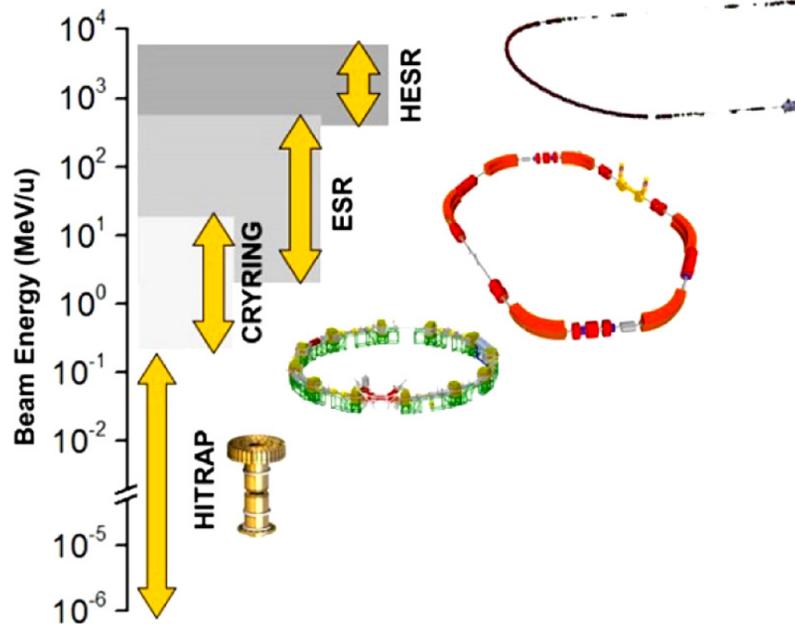


# FAIR facility

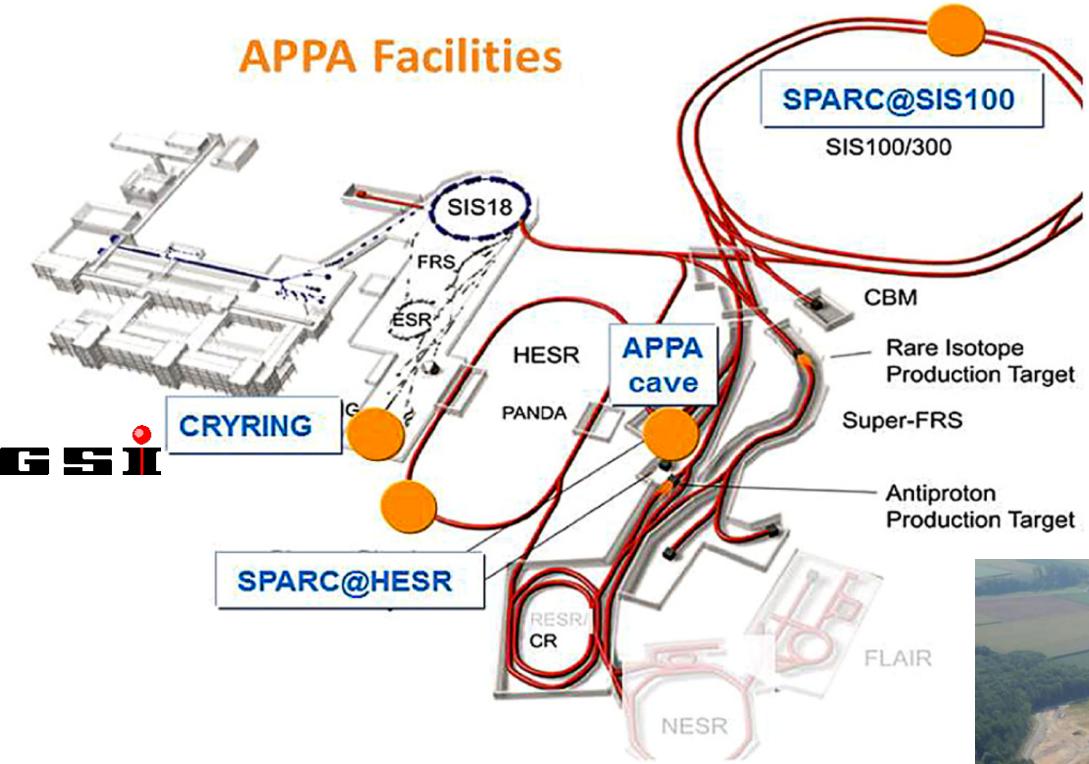


FAIR

Availability of highly charged ions up to bare U with energies between 10 GeV/u to rest



# FAIR facility



**Phase-0: 2018-2019**

**Phase-1: 2024**

Availability of highly charged ions  
up to bare U with energies between  
10 GeV/u to rest



# Thank you!



D. Banas, H.F. Beyer, K.H. Blumenhagen, F. Bosch, C. Brandau, A. Bräuning-Demian, H. Bräuning, W. Chen, Chr. Dimopoulou, E. Förster, T. Gaßner, S. Geyer, A. Gumberidze, S. Hagmann, S. Heß, R. Heß, P.-M. Hillenbrand, P. Indelicato, P. Jagodzinski, T. Kampfer, Chr. Kozuharov, M. Lestinsky, D. Liesen, Yu.A. Litvinov, R. Loetzsches, B. Manil, R. Martin, F. Nolden, N. Petridis, M.S. Sanjari, K.S. Schulze, M. Schwemlein, A. Simionovici, U. Spillmann, M. Steck, Th. Stöhlker, C.I. Szabo, S. Trotsenko, I. Uschmann, G. Weber, O. Wehrhan, N. Winckler, D. Winters, N. Winters, E. Ziegler

F. D. Amaro, D. F. Anagnostopoulos, A. Blechmann, S. Biri, P. Bühler, D. S. Covita, J. M. F. dos Santos, H. Fuhrmann, H. Gorke, D. Gotta, A. Gruber, M. Hennebach, A. Hirtl, T. Ishiwatari, Th. Jensen, E.-O. Le Bigot, V. E. Markushin, J. Marton, M. Nekipelov, V. Pomerantsev, V. Popov, S. Schlessner, A. Schmelzbach, Ph. Schmid, L. M. Simons, Th. Strauch, M. Theisen, J. F. C. A. Veloso, J. Zmeskal

S. Cervera, V. Gafton, T. Kirchner, E.V. Gafton, D. Hannani, S. Hidki, E. Lacaze, E. Lamour, A. Lévy, S. Macé, M. Maranglolo, J. Mérot, F. Mezdari, J.-Y. Pacquet, C. Prigent, J.-M. Ramillon, J.-P. Rozet, A. Salehzadeh, S. Steydli, D. Vernhet

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