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JOHANNES GUTENBERG UNIVERSITÄT MAINZ

# Search for New Physics with Pion Decays

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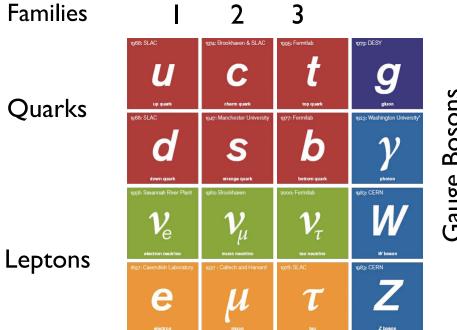


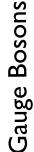
## Outline

- General Context
- Motivation
- Experimental Technique
- Data Analysis
- Results
- Conclusions & Outlook



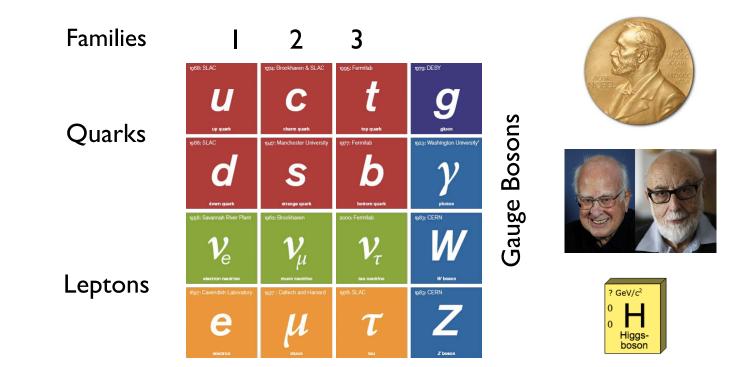






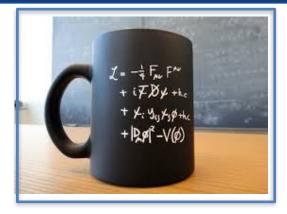
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### The Standard Model



S.L. Glashow, Nucl. Phys. 22, 519 (1961) S. Weinberg, Phys. Rev. Lett. 19, 1264 (1967) A. Salam and J. C. Ward, Phys. Lett. 13, 168 (1964). P. Higgs: Phys.Rev.Lett, 13, 508 (1964) F.Englert, R. Brout: Phys.Rev.Lett, 13, 321 (1964) G. Guralnik, C. Hagen, T. Kibble: Phys.Rev.Lett. 13, 585 (1964)







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+ iFDY +kc

+ X: Yux Xyp the

 $+|\mathbf{p}_{\mathbf{p}}|^{2}-V(\mathbf{p})$ 

### The Standard Model

 $\mathcal{L}_{SM} = -\frac{1}{2}\partial_{\nu}g^{a}_{\mu}\partial_{\nu}g^{a}_{\mu} - g_{s}f^{abc}\partial_{\mu}g^{a}_{\nu}g^{b}_{\mu}g^{c}_{\nu} - \frac{1}{4}g^{2}_{s}f^{abc}f^{ade}g^{b}_{\mu}g^{c}_{\nu}g^{d}_{\mu}g^{e}_{\nu} - \partial_{\nu}W^{+}_{\mu}\partial_{\nu}W^{-}_{\mu} - \frac{1}{2}g^{2}_{\mu}g^{a}_{\nu}g^{b}_{\mu}g^{c}_{\nu}g^{d}_{\mu}g^{e}_{\nu} - \frac{1}{2}g^{2}_{\mu}g^{a}_{\nu}g^{c}_{\mu}g^{d}_{\nu}g^{e}_{\nu} - \frac{1}{2}g^{2}_{\mu}g^{a}_{\nu}g^{c}_{\mu}g^{d}_{\nu}g^{e}_{\nu} - \frac{1}{2}g^{2}_{\mu}g^{a}_{\nu}g^{c}_{\mu}g^{d}_{\nu}g^{e}_{\nu} - \frac{1}{2}g^{2}_{\mu}g^{c}_{\nu}g^{d}_{\mu}g^{e}_{\nu} - \frac{1}{2}g^{2}_{\mu}g^{c}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{e}_{\nu} - \frac{1}{2}g^{2}_{\mu}g^{c}_{\mu}g^{d}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{d}$  $M^{2}W_{\mu}^{+}W_{\mu}^{-} - \frac{1}{2}\partial_{\nu}Z_{\mu}^{0}\partial_{\nu}Z_{\mu}^{0} - \frac{1}{2c^{2}}M^{2}Z_{\mu}^{0}Z_{\mu}^{0} - \frac{1}{2}\partial_{\mu}A_{\nu}\partial_{\mu}A_{\nu} - igc_{w}(\partial_{\nu}Z_{\mu}^{0}(W_{\mu}^{+}W_{\nu}^{-} - W_{\mu}^{-}W_{\mu}^{-}))$  $W_{\nu}^{+}W_{\mu}^{-}) - Z_{\nu}^{0}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\mu}^{-}\partial_{\nu}W_{\mu}^{+}) + Z_{\mu}^{0}(W_{\nu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\nu}^{-}\partial_{\nu}W_{\mu}^{+}))$  $igs_w(\partial_\nu A_\mu(W^+_\mu W^-_\nu - W^+_\nu W^-_\mu) - A_\nu(W^+_\mu \partial_\nu W^-_\mu - W^-_\mu \partial_\nu W^+_\mu) + A_\mu(W^+_\nu \partial_\nu W^-_\mu - W^-_\mu \partial_\nu W^+_\mu) + A_\mu(W^+_\mu \partial_\nu W^-_\mu - W^-_\mu \partial_\nu W^-_\mu) + A_\mu(W^+_\mu \partial_\nu W^-_\mu - W^-_\mu \partial_\mu W^-_\mu) + A_\mu(W^+_\mu \partial_\mu W^-_\mu - W^-_\mu \partial_\mu W^-_\mu) + A_\mu(W^+_\mu \partial_\mu$  $W^{-}_{\nu}\partial_{\nu}W^{+}_{\mu})) - \frac{1}{2}g^{2}W^{+}_{\mu}W^{-}_{\nu}W^{+}_{\nu}W^{-}_{\nu} + \frac{1}{2}g^{2}W^{+}_{\mu}W^{-}_{\nu}W^{+}_{\mu}W^{-}_{\nu} + g^{2}c^{2}_{w}(Z^{0}_{\mu}W^{+}_{\mu}Z^{0}_{\nu}W^{-}_{\nu} - G^{0}_{\mu}W^{+}_{\mu}W^{-}_{\nu}W^{+}_{\nu}W^{-}_{\nu}) + \frac{1}{2}g^{2}W^{+}_{\mu}W^{-}_{\nu}W^{-}_{\nu}W^{-}_{\mu}W^{-}_{\nu}W^{-}_{\mu}W^{-}_{\nu}W^{-}_{\mu$  $Z_{\mu}^{0}Z_{\mu}^{0}W_{\nu}^{+}W_{\nu}^{-}) + g^{2}s_{w}^{2}(A_{\mu}W_{\mu}^{+}A_{\nu}W_{\nu}^{-} - A_{\mu}A_{\mu}W_{\nu}^{+}W_{\nu}^{-}) + g^{2}s_{w}c_{w}(A_{\mu}Z_{\nu}^{0}(W_{\mu}^{+}W_{\nu}^{-} - A_{\mu}A_{\mu}W_{\nu}^{-})) + g^{2}s_{w}c_{w}(A_{\mu}Z_{\nu}^{0}(W_{\mu}^{+}W_{\nu}^{-} - A_{\mu}A_{\mu}W_{\nu}^{-})) + g^{2}s_{w}c_{w}(A_{\mu}Z_{\nu}^{0}(W_{\mu}^{+}W_{\nu}^{-} - A_{\mu}A_{\mu}W_{\nu}^{-})) + g^{2}s_{w}c_{w}(A_{\mu}Z_{\mu}^{0}(W_{\mu}^{+}W_{\mu}^{-} - A_{\mu}A_{\mu}W_{\mu}^{-})) + g^{2}s_{w}c_{w}(A_{\mu}Z_{\mu}^{0}(W_{\mu}^{+}W_{\mu}^{-} - A_{\mu}A_{\mu}W_{\mu}^{-})) + g^{2}s_{w}c_{w}(A_{\mu}Z_{\mu}^{0}(W_{\mu}^{+}W_{\mu}^{-})) + g^{2}s_{w}c_{w}(A_{\mu}Z_{\mu}^{-})) + g^{2}s_{w}c_{w}(A_{\mu}Z_{\mu}^{0}(W_{\mu}^{+}W_{\mu}^{-})) + g^{2}s_{w}c_{w}(A_{\mu}Z_{\mu}^{-})) + g^{2}s_{w}c_{w}(A_{\mu}Z_{\mu}^{-})) + g^{2}s_{w}c_{w}(A_{\mu}Z_{\mu}^{-})) + g^{2}s_{w}c_{w}(A_{\mu}Z_{\mu}^{-})) + g^{2}s_{w}c_{w}(A_{\mu}Z_{\mu}^{-})) + g^{2}s_{w}c_{w}(A_{\mu}Z_{\mu}^{-})) + g^{2}s_{w}c_{w}(A$  $W_{\nu}^{+}W_{\mu}^{-}) - 2A_{\mu}Z_{\mu}^{0}W_{\nu}^{+}W_{\nu}^{-}) - \frac{1}{2}\partial_{\mu}H\partial_{\mu}H - 2M^{2}\alpha_{h}H^{2} - \partial_{\mu}\phi^{+}\partial_{\mu}\phi^{-} - \frac{1}{2}\partial_{\mu}\phi^{0}\partial_{\nu}\phi^{0} - \frac{1}{2}\partial_{\mu}\phi^{0}\partial_{\mu}\phi^{0} - \frac{1}{2}\partial_{\mu}\phi^{0} - \frac{1}{2}\partial_{\mu}\phi^{0}\partial_{\mu}\phi^{0} - \frac{1}{2}\partial_{\mu$  $\beta_h \left( \frac{2M^2}{a^2} + \frac{2M}{a}H + \frac{1}{2}(H^2 + \phi^0\phi^0 + 2\phi^+\phi^-) \right) + \frac{2M^4}{a^2}\alpha_h$  $q\alpha_{h}M(H^{3} + H\phi^{0}\phi^{0} + 2H\phi^{+}\phi^{-}) \frac{1}{8}g^{2}\alpha_{h}\left(H^{4}+(\phi^{0})^{4}+4(\phi^{+}\phi^{-})^{2}+4(\phi^{0})^{2}\phi^{+}\phi^{-}+4H^{2}\phi^{+}\phi^{-}+2(\phi^{0})^{2}H^{2}\right)$  $gMW^+_{\mu}W^-_{\mu}H - \frac{1}{2}g\frac{M}{c^2}Z^0_{\mu}Z^0_{\mu}H \frac{1}{2}iq\left(W^+_{\mu}(\phi^0\partial_{\mu}\phi^--\phi^-\partial_{\mu}\phi^0)-W^-_{\mu}(\phi^0\partial_{\mu}\phi^+-\phi^+\partial_{\mu}\phi^0)\right)+$  $\frac{1}{2}g\left(W^+_{\mu}(H\partial_{\mu}\phi^- - \phi^-\partial_{\mu}H) + W^-_{\mu}(H\partial_{\mu}\phi^+ - \phi^+\partial_{\mu}H)\right) + \frac{1}{2}g\frac{1}{c_{\mu}}(Z^0_{\mu}(H\partial_{\mu}\phi^0 - \phi^0\partial_{\mu}H) + W^-_{\mu}(H\partial_{\mu}\phi^+ - \phi^+\partial_{\mu}H))$  $M\left(\frac{1}{c}Z_{\mu}^{0}\partial_{\mu}\phi^{0}+W_{\mu}^{+}\partial_{\mu}\phi^{-}+W_{\mu}^{-}\partial_{\mu}\phi^{+}\right)-ig\frac{s_{w}^{2}}{c}MZ_{\mu}^{0}(W_{\mu}^{+}\phi^{-}-W_{\mu}^{-}\phi^{+})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}$  $\begin{array}{l} W^{-}_{\mu}\phi^{+}) - ig\frac{1-2c_{w}^{2}}{2c_{w}}Z^{0}_{\mu}(\phi^{+}\partial_{\mu}\phi^{-}-\phi^{-}\partial_{\mu}\phi^{+}) + igs_{w}A_{\mu}(\phi^{+}\partial_{\mu}\phi^{-}-\phi^{-}\partial_{\mu}\phi^{+}) - \\ \frac{1}{4}g^{2}W^{+}_{\mu}W^{-}_{\mu}(H^{2}+(\phi^{0})^{2}+2\phi^{+}\phi^{-}) - \frac{1}{8}g^{2}\frac{1}{c_{w}^{2}}Z^{0}_{\mu}Z^{0}_{\mu}(H^{2}+(\phi^{0})^{2}+2(2s_{w}^{2}-1)^{2}\phi^{+}\phi^{-}) - \end{array}$  $\frac{1}{2}g^{2}\frac{s_{w}^{2}}{c_{w}}Z_{\mu}^{0}\phi^{0}(W_{\mu}^{+}\phi^{-}+W_{\mu}^{-}\phi^{+}) - \frac{1}{2}ig^{2}\frac{s_{w}^{2}}{c_{w}}Z_{\mu}^{0}H(W_{\mu}^{+}\phi^{-}-W_{\mu}^{-}\phi^{+}) + \frac{1}{2}g^{2}s_{w}A_{\mu}\phi^{0}(W_{\mu}^{+}\phi^{-}+W_{\mu}^{-}\phi^{+}) - \frac{1}{2}ig^{2}\frac{s_{w}^{2}}{c_{w}}Z_{\mu}^{0}H(W_{\mu}^{+}\phi^{-}-W_{\mu}^{-}\phi^{+}) + \frac{1}{2}g^{2}s_{w}A_{\mu}\phi^{0}(W_{\mu}^{+}\phi^{-}+W_{\mu}^{-}\phi^{+}) - \frac{1}{2}ig^{2}\frac{s_{w}^{2}}{c_{w}}Z_{\mu}^{0}H(W_{\mu}^{+}\phi^{-}-W_{\mu}^{-}\phi^{+}) + \frac{1}{2}g^{2}s_{w}A_{\mu}\phi^{0}(W_{\mu}^{+}\phi^{-}+W_{\mu}^{-}\phi^{+}) + \frac{1}{2}g^{2}s_{w}A_{\mu}\phi^{0}(W_{\mu}^{+}\phi^{-}+W_{\mu}^{-}\phi^{-}) + \frac{1}{2}g^{2}s_{w}A_{\mu}\phi^{0}(W_{\mu}^{+}\phi^{-}) + \frac{1}{2}g^{2}s_{w}A_{\mu}\phi^{0}(W_{\mu}^{+}\phi^{-}+W_{\mu}^{-}\phi^{-}) + \frac{1}{2}g^{2}s_{w}A_{\mu}\phi^{0}(W_{\mu}^{+}\phi^{-}) + \frac{1}{2}g^{2}s_{w}A_{\mu}\phi^{0}$  $g^{2}s_{w}^{2}A_{\mu}A_{\mu}\phi^{+}\phi^{-} + \frac{1}{2}ig_{s}\lambda_{ii}^{a}(\bar{q}_{i}^{\sigma}\gamma^{\mu}q_{j}^{\sigma})g_{\mu}^{a} - \bar{e}^{\lambda}(\gamma\partial + m_{e}^{\lambda})e^{\lambda} - \bar{\nu}^{\lambda}(\gamma\partial + m_{\nu}^{\lambda})\nu^{\lambda} - \bar{u}_{i}^{\lambda}(\gamma\partial + m_{\nu}^{\lambda})e^{\lambda} - \bar{\nu}^{\lambda}(\gamma\partial + m_{\nu}^$  $m_u^{\lambda} u_j^{\lambda} - \bar{d}_i^{\lambda} (\gamma \partial + m_d^{\lambda}) d_i^{\lambda} + igs_w A_{\mu} \left( -(\bar{e}^{\lambda} \gamma^{\mu} e^{\lambda}) + \frac{2}{3} (\bar{u}_i^{\lambda} \gamma^{\mu} u_j^{\lambda}) - \frac{1}{3} (\bar{d}_i^{\lambda} \gamma^{\mu} d_j^{\lambda}) \right) +$  $\frac{ig}{4c}Z_{\mu}^{0}\{(\bar{\nu}^{\lambda}\gamma^{\mu}(1+\gamma^{5})\nu^{\lambda})+(\bar{e}^{\lambda}\gamma^{\mu}(4s_{w}^{2}-1-\gamma^{5})e^{\lambda})+(\bar{d}_{i}^{\lambda}\gamma^{\mu}(\frac{4}{3}s_{w}^{2}-1-\gamma^{5})d_{i}^{\lambda})+$  $(\bar{u}_{i}^{\lambda}\gamma^{\mu}(1-\frac{8}{3}s_{w}^{2}+\gamma^{5})u_{i}^{\lambda})\}+\frac{ig}{2\sqrt{2}}W_{\mu}^{+}\left((\bar{\nu}^{\lambda}\gamma^{\mu}(1+\gamma^{5})U^{lep}{}_{\lambda\kappa}e^{\kappa})+(\bar{u}_{i}^{\lambda}\gamma^{\mu}(1+\gamma^{5})C_{\lambda\kappa}d_{i}^{\kappa})\right)+$  $\frac{ig}{2\sqrt{2}}W^{-}_{\mu}\left((\bar{e}^{\kappa}U^{lep^{\dagger}}_{\kappa\lambda}\gamma^{\mu}(1+\gamma^{5})\nu^{\lambda})+(\bar{d}^{\kappa}_{i}C^{\dagger}_{\kappa\lambda}\gamma^{\mu}(1+\gamma^{5})u^{\lambda}_{i})\right)+$  $\frac{ig}{2M_{\prime}/2}\phi^{+}\left(-m_{e}^{\kappa}(\bar{\nu}^{\lambda}U^{lep}{}_{\lambda\kappa}(1-\gamma^{5})e^{\kappa})+m_{\nu}^{\lambda}(\bar{\nu}^{\lambda}U^{lep}{}_{\lambda\kappa}(1+\gamma^{5})e^{\kappa})+\right.$  $\frac{ig}{2M\sqrt{2}}\phi^{-}\left(m_{e}^{\lambda}(\bar{e}^{\lambda}U^{lep}_{\lambda\kappa}^{\dagger}(1+\gamma^{5})\nu^{\kappa})-m_{\nu}^{\kappa}(\bar{e}^{\lambda}U^{lep}_{\lambda\kappa}^{\dagger}(1-\gamma^{5})\nu^{\kappa}\right)-\frac{g}{2}\frac{m_{\nu}^{\lambda}}{M}H(\bar{\nu}^{\lambda}\nu^{\lambda}) \frac{g}{2}\frac{m_e^{\lambda}}{M}H(\bar{e}^{\lambda}e^{\lambda}) + \frac{ig}{2}\frac{m_{\nu}^{\lambda}}{M}\phi^0(\bar{\nu}^{\lambda}\gamma^5\nu^{\lambda}) - \frac{ig}{2}\frac{m_e^{\lambda}}{M}\phi^0(\bar{e}^{\lambda}\gamma^5e^{\lambda}) - \frac{1}{4}\bar{\nu}_{\lambda}M_{\lambda\kappa}^R(1-\gamma_5)\hat{\nu}_{\kappa} \frac{1}{4}\overline{\nu_{\lambda}}\frac{m_{\lambda}^{R}(1-\gamma_{5})\hat{\nu}_{\kappa}}{M_{\lambda\kappa}^{R}(1-\gamma_{5})\hat{\nu}_{\kappa}} + \frac{ig}{2M\sqrt{2}}\phi^{+}\left(-m_{d}^{\kappa}(\bar{u}_{i}^{\lambda}C_{\lambda\kappa}(1-\gamma^{5})d_{i}^{\kappa}) + m_{u}^{\lambda}(\bar{u}_{i}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{i}^{\kappa}) + m_{u}^{\lambda}(\bar{u}_{i}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{i}^{\kappa})\right) + \frac{ig}{4}\overline{\nu_{\lambda}}\frac{m_{\lambda}^{R}(1-\gamma_{5})\hat{\nu}_{\kappa}}{M_{\lambda\kappa}^{R}(1-\gamma_{5})\hat{\nu}_{\kappa}} + \frac{ig}{2M\sqrt{2}}\phi^{+}\left(-m_{d}^{\kappa}(\bar{u}_{i}^{\lambda}C_{\lambda\kappa}(1-\gamma^{5})d_{i}^{\kappa}) + m_{u}^{\lambda}(\bar{u}_{i}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{i}^{\kappa})\right) + \frac{ig}{4}\overline{\nu_{\lambda}}\frac{m_{\lambda}^{R}(1-\gamma_{5})\hat{\nu}_{\kappa}}{M_{\lambda\kappa}^{R}(1-\gamma_{5})\hat{\nu}_{\kappa}} + \frac{ig}{2M\sqrt{2}}\phi^{+}\left(-m_{d}^{\kappa}(\bar{u}_{i}^{\lambda}C_{\lambda\kappa}(1-\gamma^{5})d_{i}^{\kappa}) + m_{u}^{\lambda}(\bar{u}_{i}^{\lambda}C_{\lambda\kappa}(1-\gamma^{5})d_{i}^{\kappa})\right) + \frac{ig}{4}\overline{\nu_{\lambda}}\frac{m_{\lambda}^{R}(1-\gamma_{5})\hat{\nu}_{\kappa}}{M_{\lambda\kappa}^{R}(1-\gamma_{5})\hat{\nu}_{\kappa}} + \frac{ig}{2M\sqrt{2}}\phi^{+}\left(-m_{d}^{\kappa}(\bar{u}_{i}^{\lambda}C_{\lambda\kappa}(1-\gamma^{5})d_{i}^{\kappa}) + m_{u}^{\lambda}(\bar{u}_{i}^{\lambda}C_{\lambda\kappa}(1-\gamma^{5})d_{i}^{\kappa})\right) + \frac{ig}{4}\overline{\nu_{\lambda}}}\frac{m_{\lambda}^{R}(1-\gamma_{5})\hat{\nu}_{\kappa}}{M_{\lambda}^{R}(1-\gamma_{5})\hat{\nu}_{\kappa}} + \frac{ig}{2M\sqrt{2}}\phi^{+}\left(-m_{d}^{\kappa}(\bar{u}_{i}^{\lambda}C_{\lambda\kappa}(1-\gamma^{5})d_{i}^{\kappa}) + m_{u}^{\lambda}(\bar{u}_{i}^{\lambda}C_{\lambda\kappa}(1-\gamma^{5})d_{i}^{\kappa})\right) + \frac{ig}{4}\overline{\nu_{\lambda}}}\frac{m_{\lambda}^{R}(1-\gamma_{5})\hat{\nu}_{\kappa}}{M_{\lambda}^{R}(1-\gamma_{5})\hat{\nu}_{\kappa}}} + \frac{ig}{4}\overline{\nu_{\lambda}}\frac{m_{\mu}^{R}(1-\gamma_{5})\hat{\nu}_{\kappa}}{M_{\lambda}^{R}(1-\gamma_{5})\hat{\nu}_{\kappa}}} + \frac{ig}{4}\overline{\nu_{\lambda}}}\frac{m_{\mu}^{R}(1-\gamma_{5})\hat{\nu}_{\kappa}}{M_{\lambda}}} + \frac{ig}{4}\overline{\nu_{\lambda}}}\frac{m_{\mu}^{R}(1-\gamma_{5})\hat{\nu}_{\kappa}}{M_{\lambda}}} + \frac{ig}{4}\overline{\nu_{\lambda}}}\frac{m_{\mu}^{R}(1-\gamma_{5})\hat{\nu}_{\kappa}}{M_{\lambda}}} + \frac{ig}{4}\overline{\nu_{\lambda}}}\frac{m_{\mu}^{R}(1-\gamma_{5})\hat{\nu}_{\kappa}}{M_{\lambda}}} + \frac{ig}{4}\overline{\nu_{\lambda}}}\frac{m_{\mu}^{R}(1-\gamma_{5})\hat{\nu}}{M_{\lambda}}} + \frac{ig}{4}\overline{\nu_{\lambda}}\frac{m_{\mu}^{R}(1-\gamma_{5})\hat{\nu}}{M_{\lambda}}} + \frac{ig}{4}\overline{\nu_{\lambda}}}\frac{m_{\mu}^{R}(1-\gamma_{5})\hat{\nu}}{M_{\lambda}}} + \frac{ig}{4}\overline{\nu_{\lambda}}\frac{m_{\mu}^{R}(1-\gamma_{5})\hat{\nu}}{M_{\lambda}}} + \frac{ig}{4}\overline{\nu_{\lambda}}\frac{m_{\mu}^{R}(1-\gamma_{5})\hat{\nu}}{M_{\lambda}}} + \frac{ig}{4}\overline{\nu_{\lambda}}\frac{m_{\mu}^{R}(1-\gamma_$  $\frac{ig}{2M\sqrt{2}}\phi^{-}\left(m_{d}^{\lambda}(\bar{d}_{j}^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^{5})u_{j}^{\kappa})-m_{u}^{\kappa}(\bar{d}_{j}^{\lambda}C_{\lambda\kappa}^{\dagger}(1-\gamma^{5})u_{j}^{\kappa})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\right.$  $\frac{g}{2}\frac{m_{d}^{\lambda}}{M}H(\bar{d}_{i}^{\lambda}d_{i}^{\lambda}) + \frac{ig}{2}\frac{m_{u}^{\lambda}}{M}\phi^{0}(\bar{u}_{i}^{\lambda}\gamma^{5}u_{i}^{\lambda}) - \frac{ig}{2}\frac{m_{d}^{\lambda}}{M}\phi^{0}(\bar{d}_{i}^{\lambda}\gamma^{5}d_{i}^{\lambda}) + \bar{G}^{a}\partial^{2}G^{a} + g_{s}f^{abc}\partial_{\mu}\bar{G}^{a}G^{b}g_{\mu}^{c} + \frac{ig}{2}\frac{m_{u}^{\lambda}}{M}\phi^{0}(\bar{u}_{i}^{\lambda}\gamma^{5}u_{i}^{\lambda}) - \frac{ig}{2}\frac{m_{d}^{\lambda}}{M}\phi^{0}(\bar{d}_{i}^{\lambda}\gamma^{5}d_{i}^{\lambda}) + \bar{G}^{a}\partial^{2}G^{a} + g_{s}f^{abc}\partial_{\mu}\bar{G}^{a}G^{b}g_{\mu}^{c} + \frac{ig}{2}\frac{m_{u}^{\lambda}}{M}\phi^{0}(\bar{u}_{i}^{\lambda}\gamma^{5}u_{i}^{\lambda}) - \frac{ig}{2}\frac{m_{d}^{\lambda}}{M}\phi^{0}(\bar{d}_{i}^{\lambda}\gamma^{5}d_{i}^{\lambda}) + \bar{G}^{a}\partial^{2}G^{a} + g_{s}f^{abc}\partial_{\mu}\bar{G}^{a}G^{b}g_{\mu}^{c} + \frac{ig}{2}\frac{m_{u}^{\lambda}}{M}\phi^{0}(\bar{u}_{i}^{\lambda}\gamma^{5}u_{i}^{\lambda}) - \frac{ig}{2}\frac{m_{d}^{\lambda}}{M}\phi^{0}(\bar{d}_{i}^{\lambda}\gamma^{5}d_{i}^{\lambda}) + \bar{G}^{a}\partial^{2}G^{a} + \frac{ig}{2}\frac{ig}{M}\frac{ig}{M}g^{a} + \frac{ig}{2}\frac{ig}{M}g^{a} + \frac{ig}{2}\frac$  $\bar{X}^{+}(\partial^{2}-M^{2})X^{+}+\bar{X}^{-}(\partial^{2}-M^{2})X^{-}+\bar{X}^{0}(\partial^{2}-\frac{M^{2}}{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}X^{-}+\bar{Y}\partial^{2}X^$  $\partial_{\mu}\bar{X}^{+}X^{0}$ )+ $igs_{w}W^{+}_{\mu}(\partial_{\mu}\bar{Y}X^{-}-\partial_{\mu}\bar{X}^{+}\bar{Y})$ + $igc_{w}W^{-}_{\mu}(\partial_{\mu}\bar{X}^{-}X^{0} \partial_{\mu}\bar{X}^{0}X^{+})+igs_{w}\bar{W}_{\mu}^{-}(\partial_{\mu}\bar{X}^{-}Y-\partial_{\mu}\bar{Y}X^{+})+igc_{w}Z_{\mu}^{0}(\partial_{\mu}\bar{X}^{+}X^{+} \partial_{\mu} \bar{X}^- X^-) + igs_w A_{\mu} (\partial_{\mu} \bar{X}^+ X^+ \partial_{\mu}\bar{X}^{-}X^{-}) - \frac{1}{2}gM\left(\bar{X}^{+}X^{+}H + \bar{X}^{-}X^{-}H + \frac{1}{c^{2}}\bar{X}^{0}X^{0}H\right) + \frac{1-2c^{2}_{w}}{2c_{w}}igM\left(\bar{X}^{+}X^{0}\phi^{+} - \bar{X}^{-}X^{0}\phi^{-}\right) +$  $\frac{1}{2a}igM(\bar{X}^{0}X^{-}\phi^{+}-\bar{X}^{0}X^{+}\phi^{-})+igMs_{w}(\bar{X}^{0}X^{-}\phi^{-})+igMs_{w}(\bar{X}^{0}X^{+}\phi^{-})+igMs_{w}(\bar{X}^{0}X^{+}\phi^{-})+igMs_{w}(\bar{X}^{0}X^{+}\phi^{-})+igMs_{w}(\bar{X}^{0}X^{+}\phi^{-})+igMs_{w}(\bar{X}^{0}X^{+}\phi^{-})+igMs_{w}(\bar{X}^{0}X^{+}\phi^{-})+igMs_{w}(\bar{X}^{0}X^{+}\phi^{-})+igMs_{w}(\bar{X}^{0}X^{+}\phi^{-})+igMs_{w}(\bar{X}^{0}X^{+}\phi^{-})+igMs_{w}(\bar{X}^{0}X^{+}\phi^{-})+igMs_{w}(\bar{X}^{0}X^{+}\phi^{-})+igMs_{w}(\bar{X}^{0}X^{+}\phi^{-})+igMs_{w}(\bar{X}^{0}X^{+}\phi^{-})+igMs_{w}(\bar{X}^{0}X^{+}\phi^{-})+igMs_{w}(\bar{X}^{0}X^{+}\phi^{-})+igMs_{w}(\bar{X}^{0}X^{+}\phi^{-})+igMs_{w}(\bar{X$  $\frac{1}{2}iqM\left(\bar{X}^{+}X^{+}\phi^{0}-\bar{X}^{-}X^{-}\phi^{0}\right)$ 



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### The Standard Model

 $\mathcal{L}_{SM} = -\frac{1}{2}\partial_{\nu}g^{a}_{\mu}\partial_{\nu}g^{a}_{\mu} - g_{s}f^{abc}\partial_{\mu}g^{a}_{\nu}g^{b}_{\mu}g^{c}_{\nu} - \frac{1}{4}g^{2}_{s}f^{abc}f^{ade}g^{b}_{\mu}g^{c}_{\nu}g^{d}_{\mu}g^{e}_{\nu} - \partial_{\nu}W^{+}_{\mu}\partial_{\nu}W^{-}_{\mu} - \frac{1}{2}g^{2}_{\mu}g^{a}_{\nu}g^{b}_{\mu}g^{c}_{\nu}g^{d}_{\mu}g^{e}_{\nu} - \frac{1}{2}g^{2}_{\mu}g^{a}_{\nu}g^{c}_{\mu}g^{d}_{\nu}g^{e}_{\nu} - \frac{1}{2}g^{2}_{\mu}g^{a}_{\nu}g^{c}_{\mu}g^{d}_{\nu}g^{e}_{\nu} - \frac{1}{2}g^{2}_{\mu}g^{a}_{\nu}g^{c}_{\mu}g^{d}_{\nu}g^{e}_{\nu} - \frac{1}{2}g^{2}_{\mu}g^{c}_{\nu}g^{d}_{\mu}g^{e}_{\nu} - \frac{1}{2}g^{2}_{\mu}g^{c}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{e}_{\nu} - \frac{1}{2}g^{2}_{\mu}g^{c}_{\mu}g^{d}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{d}_{\nu}g^{d}_{\mu}g^{d}$  $M^{2}W_{\mu}^{+}W_{\mu}^{-} - \frac{1}{2}\partial_{\nu}Z_{\mu}^{0}\partial_{\nu}Z_{\mu}^{0} - \frac{1}{2c^{2}}M^{2}Z_{\mu}^{0}Z_{\mu}^{0} - \frac{1}{2}\partial_{\mu}A_{\nu}\partial_{\mu}A_{\nu} - igc_{w}(\partial_{\nu}Z_{\mu}^{0}(W_{\mu}^{+}W_{\nu}^{-} - W_{\mu}^{-}))$  $W_{\nu}^{+}W_{\mu}^{-}) - Z_{\nu}^{0}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\mu}^{-}\partial_{\nu}W_{\mu}^{+}) + Z_{\mu}^{0}(W_{\nu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\nu}^{-}\partial_{\nu}W_{\mu}^{+}))$  $igs_w(\partial_\nu A_\mu(W^+_\mu W^-_\nu - W^+_\nu W^-_\mu) - A_\nu(W^+_\mu \partial_\nu W^-_\mu - W^-_\mu \partial_\nu W^+_\mu) + A_\mu(W^+_\nu \partial_\nu W^-_\mu - W^-_\mu \partial_\nu W^+_\mu) + A_\mu(W^+_\mu \partial_\nu W^-_\mu - W^-_\mu \partial_\nu W^-_\mu) + A_\mu(W^+_\mu \partial_\nu W^-_\mu - W^-_\mu \partial_\mu W^-_\mu) + A_\mu(W^+_\mu \partial_\mu W^-_\mu - W^-_\mu \partial_\mu W^-_\mu) + A_\mu(W^+_\mu \partial_\mu$  $W^{-}_{\nu}\partial_{\nu}W^{+}_{\mu})) - \frac{1}{2}g^{2}W^{+}_{\mu}W^{-}_{\nu}W^{+}_{\nu}W^{-}_{\nu} + \frac{1}{2}g^{2}W^{+}_{\mu}W^{-}_{\nu}W^{+}_{\mu}W^{-}_{\nu} + g^{2}c^{2}_{w}(Z^{0}_{\mu}W^{+}_{\mu}Z^{0}_{\nu}W^{-}_{\nu} - G^{0}_{\mu}W^{+}_{\mu}W^{-}_{\nu}W^{+}_{\nu}W^{-}_{\nu}) + \frac{1}{2}g^{2}W^{+}_{\mu}W^{-}_{\nu}W^{-}_{\nu}W^{-}_{\mu}W^{-}_{\nu}W^{-}_{\mu}W^{-}_{\nu}W^{-}_{\mu$  $Z^{0}_{\mu}Z^{0}_{\mu}W^{+}_{\nu}W^{-}_{\nu}) + g^{2}s^{2}_{w}(A_{\mu}W^{+}_{\mu}A_{\nu}W^{-}_{\nu} - A_{\mu}A_{\mu}W^{+}_{\nu}W^{-}_{\nu}) + g^{2}s_{w}c_{w}(A_{\mu}Z^{0}_{\nu}(W^{+}_{\mu}W^{-}_{\nu} - A_{\mu}A_{\mu}W^{+}_{\nu}W^{-}_{\nu}))$  $W_{\nu}^{+}W_{\mu}^{-}) - 2A_{\mu}Z_{\mu}^{0}W_{\nu}^{+}W_{\nu}^{-}) - \frac{1}{2}\partial_{\mu}H\partial_{\mu}H - 2M^{2}\alpha_{h}H^{2} - \partial_{\mu}\phi^{+}\partial_{\mu}\phi^{-} - \frac{1}{2}\partial_{\mu}\phi^{0}\partial_{\nu}\phi^{0} - \frac{1}{2}\partial_{\mu}\phi^{0}\partial_{\mu}\phi^{0} - \frac{1}{2}\partial_{\mu}\phi^{0} - \frac{1}{2}\partial_{\mu}\phi^{0}\partial_{\mu}\phi^{0} - \frac{1}{2}\partial_{\mu$  $\beta_h \left( \frac{2M^2}{a^2} + \frac{2M}{a}H + \frac{1}{2}(H^2 + \phi^0\phi^0 + 2\phi^+\phi^-) \right) + \frac{2M^4}{a^2}\alpha_h$  $q\alpha_{h}M(H^{3} + H\phi^{0}\phi^{0} + 2H\phi^{+}\phi^{-}) \frac{1}{8}g^{2}\alpha_{h}\left(H^{4}+(\phi^{0})^{4}+4(\phi^{+}\phi^{-})^{2}+4(\phi^{0})^{2}\phi^{+}\phi^{-}+4H^{2}\phi^{+}\phi^{-}+2(\phi^{0})^{2}H^{2}\right)$  $gMW^+_{\mu}W^-_{\mu}H - \frac{1}{2}g\frac{M}{c^2}Z^0_{\mu}Z^0_{\mu}H \frac{1}{2}iq\left(W^+_{\mu}(\phi^0\partial_{\mu}\phi^--\phi^-\partial_{\mu}\phi^0)-W^-_{\mu}(\phi^0\partial_{\mu}\phi^+-\phi^+\partial_{\mu}\phi^0)\right)+$  $\frac{1}{2}g\left(W^+_{\mu}(H\partial_{\mu}\phi^- - \phi^-\partial_{\mu}H) + W^-_{\mu}(H\partial_{\mu}\phi^+ - \phi^+\partial_{\mu}H)\right) + \frac{1}{2}g\frac{1}{c_{\mu}}(Z^0_{\mu}(H\partial_{\mu}\phi^0 - \phi^0\partial_{\mu}H) + W^-_{\mu}(H\partial_{\mu}\phi^+ - \phi^+\partial_{\mu}H))$  $M\left(\frac{1}{c}Z_{\mu}^{0}\partial_{\mu}\phi^{0}+W_{\mu}^{+}\partial_{\mu}\phi^{-}+W_{\mu}^{-}\partial_{\mu}\phi^{+}\right)-ig\frac{s_{w}^{2}}{c}MZ_{\mu}^{0}(W_{\mu}^{+}\phi^{-}-W_{\mu}^{-}\phi^{+})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}$  $\begin{array}{c} W_{\mu}^{-}\phi^{+}) - ig\frac{1-2c_{w}^{2}}{2c_{w}}Z_{\mu}^{0}(\phi^{+}\partial_{\mu}\phi^{-} - \phi^{-}\partial_{\mu}\phi^{+}) + igs_{w}A_{\mu}(\phi^{+}\partial_{\mu}\phi^{-} - \phi^{-}\partial_{\mu}\phi^{+}) - i\frac{1}{4}g^{2}W_{\mu}^{+}W_{\mu}^{-}(H^{2} + (\phi^{0})^{2} + 2\phi^{+}\phi^{-}) - \frac{1}{8}g^{2}\frac{1}{c_{w}^{2}}Z_{\mu}^{0}Z_{\mu}^{0}(H^{2} + (\phi^{0})^{2} + 2(2s_{w}^{2} - 1)^{2}\phi^{+}\phi^{-}) - \frac{1}{8}g^{2}\frac{1}{c_{w}^{2}}Z_{\mu}^{0}Z_{\mu}^{0}(H^{2} + (\phi^{0})^{2}) + \frac{1}{8}g^{2}\frac{1}{c_{w}^{2}}Z_{\mu}^{0}Z_{\mu}^{0}(H^{2} + (\phi^{0})^{2}) + \frac{1}{8}g^{2}\frac{1}{c_{w}^{2}}Z_{\mu}^{0}Z_{\mu}^{0}(H^{2} + (\phi^{0})^{2}) + \frac{1}{8}g^{2}\frac{1}{c_{w}^{2}}Z_{\mu}^{0}(H^{2} + (\phi^{0})^{2}) + \frac{1}{8}g^{2}\frac{1}{c_{w}^{2}$  $\frac{1}{2}g^{2}\frac{s_{w}^{2}}{c_{w}}Z_{\mu}^{0}\phi^{0}(W_{\mu}^{+}\phi^{-}+W_{\mu}^{-}\phi^{+}) - \frac{1}{2}ig^{2}\frac{s_{w}^{2}}{c_{w}}Z_{\mu}^{0}H(W_{\mu}^{+}\phi^{-}-W_{\mu}^{-}\phi^{+}) + \frac{1}{2}g^{2}s_{w}A_{\mu}\phi^{0}(W_{\mu}^{+}\phi^{-}+W_{\mu}^{-}\phi^{+}) - \frac{1}{2}ig^{2}\frac{s_{w}^{2}}{c_{w}}Z_{\mu}^{0}H(W_{\mu}^{+}\phi^{-}-W_{\mu}^{-}\phi^{+}) + \frac{1}{2}g^{2}s_{w}A_{\mu}\phi^{0}(W_{\mu}^{+}\phi^{-}+W_{\mu}^{-}\phi^{+}) - \frac{1}{2}ig^{2}\frac{s_{w}^{2}}{c_{w}}Z_{\mu}^{0}H(W_{\mu}^{+}\phi^{-}-W_{\mu}^{-}\phi^{+}) + \frac{1}{2}g^{2}s_{w}A_{\mu}\phi^{0}(W_{\mu}^{+}\phi^{-}+W_{\mu}^{-}\phi^{+}) + \frac{1}{2}g^{2}s_{w}A_{\mu}\phi^{0}(W_{\mu}^{+}\phi^{-}+W_{\mu}^{-}\phi^{-}) + \frac{1}{2}g^{2}s_{w}A_{\mu}\phi^{0}(W_{\mu}^{+}\phi^{-}) + \frac{1}{2}g^{2}s_{w}A_{\mu}\phi^{0}(W_{\mu}^{+}\phi^{-}+W_{\mu}^{-}\phi^{-}) + \frac{1}{2}g^{2}s_{w}A_{\mu}\phi^{0}(W_{\mu}^{+}\phi^{-}) + \frac{1}{2}g^{2}s_{w}A_{\mu}\phi^{0}$  $g^{2}s_{w}^{2}A_{\mu}A_{\mu}\phi^{+}\phi^{-} + \frac{1}{2}ig_{s}\lambda_{ii}^{a}(\bar{q}_{i}^{\sigma}\gamma^{\mu}q_{i}^{\sigma})g_{\mu}^{a} - \bar{e}^{\lambda}(\gamma\partial + m_{k}^{\lambda})e^{\lambda} - \bar{\nu}^{\lambda}(\gamma\partial + m_{\mu}^{\lambda})\nu^{\lambda} - \bar{u}_{i}^{\lambda}(\gamma\partial + m_{\mu}^{\lambda})e^{\lambda} - \bar{u}_{i}$  $m_u^{\lambda} u_j^{\lambda} - \bar{d}_i^{\lambda} (\gamma \partial + m_d^{\lambda}) d_i^{\lambda} + igs_w A_{\mu} \left( -(\bar{e}^{\lambda} \gamma^{\mu} e^{\lambda}) + \frac{2}{3} (\bar{u}_i^{\lambda} \gamma^{\mu} u_j^{\lambda}) - \frac{1}{3} (\bar{d}_i^{\lambda} \gamma^{\mu} d_j^{\lambda}) \right) +$  $\frac{ig}{4c}Z_{\mu}^{0}\{(\bar{\nu}^{\lambda}\gamma^{\mu}(1+\gamma^{5})\nu^{\lambda})+(\bar{e}^{\lambda}\gamma^{\mu}(4s_{w}^{2}-1-\gamma^{5})e^{\lambda})+(\bar{d}_{i}^{\lambda}\gamma^{\mu}(\frac{4}{3}s_{w}^{2}-1-\gamma^{5})d_{i}^{\lambda})+$  $(\bar{u}_{i}^{\lambda}\gamma^{\mu}(1-\frac{8}{3}s_{w}^{2}+\gamma^{5})u_{i}^{\lambda})\}+\frac{ig}{2\sqrt{2}}W_{\mu}^{+}\left((\bar{\nu}^{\lambda}\gamma^{\mu}(1+\gamma^{5})U^{lep}{}_{\lambda\kappa}e^{\kappa})+(\bar{u}_{i}^{\lambda}\gamma^{\mu}(1+\gamma^{5})C_{\lambda\kappa}d_{i}^{\kappa})\right)+$  $\frac{ig}{2\sqrt{2}}W^{-}_{\mu}\left((\bar{e}^{\kappa}U^{lep^{\dagger}}_{\kappa\lambda}\gamma^{\mu}(1+\gamma^{5})\nu^{\lambda})+(\bar{d}^{\kappa}_{i}C^{\dagger}_{\kappa\lambda}\gamma^{\mu}(1+\gamma^{5})u^{\lambda}_{i})\right)+$  $\frac{ig}{2M_{\lambda}/2}\phi^{+}\left(-m_{e}^{\kappa}(\bar{\nu}^{\lambda}U^{lep}_{\lambda\kappa}(1-\gamma^{5})e^{\kappa})+m_{\nu}^{\lambda}(\bar{\nu}^{\lambda}U^{lep}_{\lambda\kappa}(1+\gamma^{5})e^{\kappa})+\right.$  $\frac{ig}{2M\sqrt{2}}\phi^{-}\left(m_{e}^{\lambda}(\bar{e}^{\lambda}U^{lep}_{\lambda\kappa}^{\dagger}(1+\gamma^{5})\nu^{\kappa})-m_{\nu}^{\kappa}(\bar{e}^{\lambda}U^{lep}_{\lambda\kappa}^{\dagger}(1-\gamma^{5})\nu^{\kappa}\right)-\frac{g}{2}\frac{m_{\nu}^{\lambda}}{M}H(\bar{\nu}^{\lambda}\nu^{\lambda}) \frac{g}{2}\frac{m_e^{\lambda}}{M}H(\bar{e}^{\lambda}e^{\lambda}) + \frac{ig}{2}\frac{m_{\nu}^{\lambda}}{M}\phi^0(\bar{\nu}^{\lambda}\gamma^5\nu^{\lambda}) - \frac{ig}{2}\frac{m_e^{\lambda}}{M}\phi^0(\bar{e}^{\lambda}\gamma^5e^{\lambda}) - \frac{1}{4}\bar{\nu}_{\lambda}M_{\lambda\kappa}^R(1-\gamma_5)\hat{\nu}_{\kappa} \frac{1}{4}\overline{\nu_{\lambda}}\frac{M_{\lambda\kappa}^{R}\left(1-\gamma_{5}\right)\hat{\nu}_{\kappa}}+\frac{ig}{2M\sqrt{2}}\phi^{+}\left(-m_{d}^{\kappa}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1-\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+\frac{ig}{2M\sqrt{2}}\phi^{+}\left(-m_{d}^{\kappa}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1-\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+\frac{ig}{2M\sqrt{2}}\phi^{+}\left(-m_{d}^{\kappa}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1-\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+\frac{ig}{2M\sqrt{2}}\phi^{+}\left(-m_{d}^{\kappa}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1-\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+\frac{ig}{2M\sqrt{2}}\phi^{+}\left(-m_{d}^{\kappa}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1-\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+\frac{ig}{2M\sqrt{2}}\phi^{+}\left(-m_{d}^{\kappa}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1-\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+\frac{ig}{2M\sqrt{2}}\phi^{+}\left(-m_{d}^{\kappa}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1-\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+\frac{ig}{2M\sqrt{2}}\phi^{+}\left(-m_{d}^{\kappa}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+\frac{ig}{2M\sqrt{2}}\phi^{+}\left(-m_{d}^{\kappa}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+\frac{ig}{2M\sqrt{2}}\phi^{+}\left(-m_{d}^{\kappa}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\overline{u_{j}}\overset{\lambda}{C}_{\lambda\kappa}(1+\gamma^{$  $\frac{ig}{2M\sqrt{2}}\phi^{-}\left(m_{d}^{\lambda}(\bar{d}_{j}^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^{5})u_{j}^{\kappa})-m_{u}^{\kappa}(\bar{d}_{j}^{\lambda}C_{\lambda\kappa}^{\dagger}(1-\gamma^{5})u_{j}^{\kappa})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\right.$  $\frac{g}{2}\frac{m_A^\lambda}{M}H(\bar{d}_i^\lambda d_i^\lambda) + \frac{ig}{2}\frac{m_A^\lambda}{M}\phi^0(\bar{u}_i^\lambda\gamma^5 u_i^\lambda) - \frac{ig}{2}\frac{m_A^\lambda}{M}\phi^0(\bar{d}_i^\lambda\gamma^5 d_j^\lambda) + \bar{G}^a\partial^2 G^a + g_s f^{abc}\partial_\mu \bar{G}^a G^b g^c_\mu +$  $\bar{X}^{+}(\partial^{2}-M^{2})X^{+}+\bar{X}^{-}(\partial^{2}-M^{2})X^{-}+\bar{X}^{0}(\partial^{2}-\frac{M^{2}}{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}Y+iqc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-}-M^{2})X^{0}+\bar{Y}\partial^{2}X^{-}+\bar{Y}\partial^{2}X^$  $\partial_{\mu}\bar{X}^{+}X^{0}$ )+ $igs_{w}W^{+}_{\mu}(\partial_{\mu}\bar{Y}X^{-}-\partial_{\mu}\bar{X}^{+}\bar{Y})$ + $igc_{w}W^{-}_{\mu}(\partial_{\mu}\bar{X}^{-}X^{0} \partial_{\mu}\bar{X}^{0}X^{+})+igs_{w}\bar{W}_{\mu}^{-}(\partial_{\mu}\bar{X}^{-}Y-\partial_{\mu}\bar{Y}X^{+})+igc_{w}Z_{\mu}^{0}(\partial_{\mu}\bar{X}^{+}X^{+} \partial_{\mu}\tilde{X}^{-}X^{-})+igs_{w}A_{\mu}(\partial_{\mu}\bar{X}^{+}X^{+} \partial_{\mu}\bar{X}^{-}X^{-}) - \frac{1}{2}gM\left(\bar{X}^{+}X^{+}H + \bar{X}^{-}X^{-}H + \frac{1}{c^{2}}\bar{X}^{0}X^{0}H\right) + \frac{1-2c^{2}_{w}}{2c_{w}}igM\left(\bar{X}^{+}X^{0}\phi^{+} - \bar{X}^{-}X^{0}\phi^{-}\right) + \frac{1}{2c_{w}}igM\left(\bar{X}^{+}X^{0}\phi^{+} - \bar{X}^{0}\phi^{+}\right) + \frac{1}{2c_{w}}igM\left(\bar{X}^{+}X^{0}\phi^{+$  $\frac{1}{2c_{w}}igM(\dot{X}^{0}X^{-}\phi^{+}-\bar{X}^{0}X^{+}\phi^{-})+igMs_{w}(\dot{X}^{0}X^{-}\phi^{+}-\bar{X}^{0}X^{+}\phi^{-})+$  $\frac{1}{2}igM(\bar{X}^{+}X^{+}\phi^{0}-\bar{X}^{-}X^{-}\phi^{0})$ 

Now verified up to the ~TeV range and working very well, but...



### **Open Questions**

#### Theoretical Issues:

- Gravity
- Neutrino Masses
- Hierarchy Problem
- Flavour Problem (3 families)
- ...

Standard Model  $\mathcal{L} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + i \overline{\psi} \mathcal{D} \psi + h.c. + (D_{\mu} \phi)^2 - \langle \phi \rangle$  $+ \psi_{i} \mathcal{U}_{j} \mathcal{U}_{j} \phi + h.c. + (D_{\mu} \phi)^2 - \langle \phi \rangle$ 



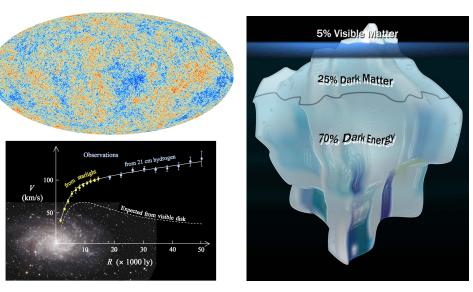
### **Open Questions**

#### Theoretical Issues:

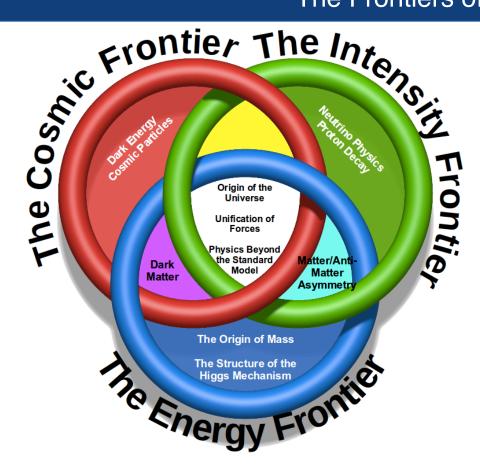
- Gravity
- Neutrino Masses
- Hierarchy Problem
- Flavour Problem (3 families)
- **-** ...

#### **Cosmological Issues**

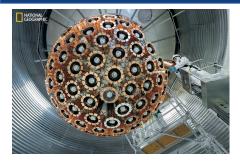
- Dark Energy
- Dark Matter
- Inflation
- Matter/Antimatter Asymmetry
- CP violation
- ...



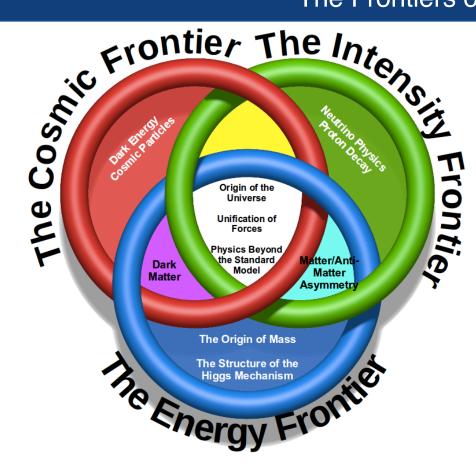




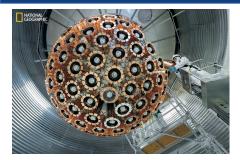




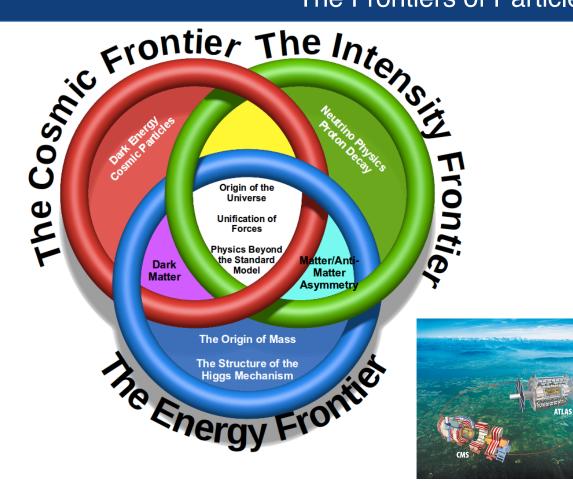








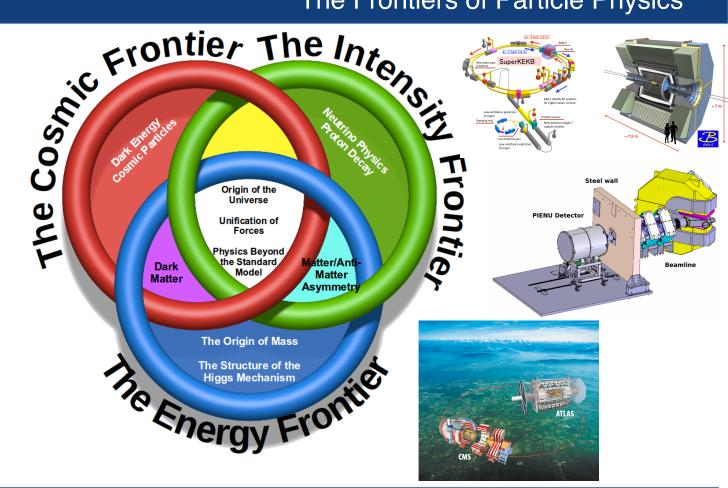










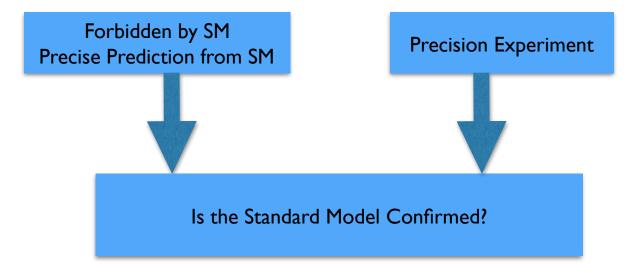




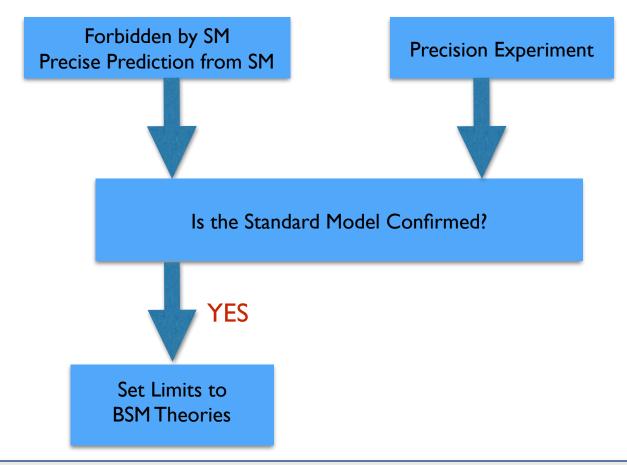
Forbidden by SM Precise Prediction from SM

Precision Experiment

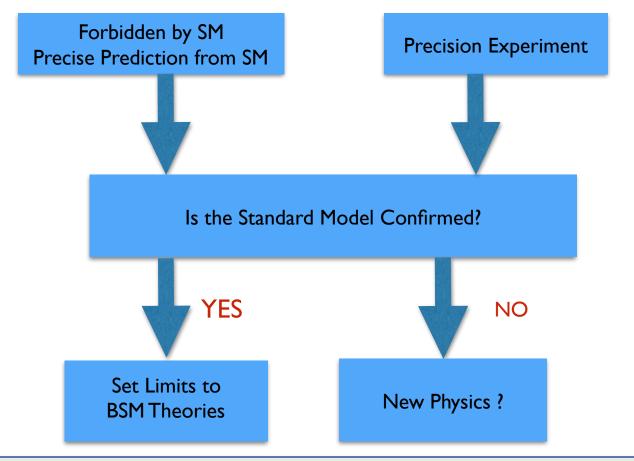














# The Early History of Pions



Early History

1935: H. Yukawa predicts a new particle

1936: Discovery of the Muon



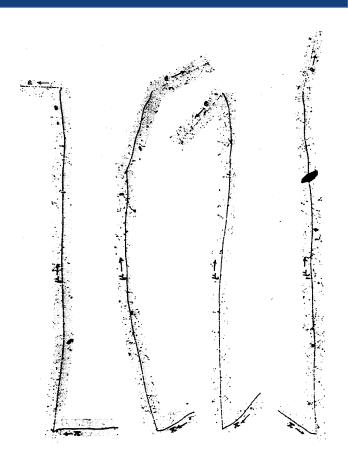
1947: C. Powell and collaborators discover the Pion M.Lattes, H.Muirhead, G.Occhialini, C.Powell: Nature, 159:694-697 (1947)



**1949**: H.Yukawa awarded the Nobel Prize.

**1950**: C. Powell awarded the Nobel Prize







- Pion discovered with 
$$\pi^+ \to \mu^+ \nu$$

- But:  $m_e=0.511~{
m MeV}$ 

 $m_{\mu} = 105 \text{ MeV}$ 

- Why don't we see  $\ \pi^+ 
  ightarrow e^+ 
  u$  ?
- 1950s: Many experimental indications that the weak interactions were violating parity. "V-A" structure:

$$H_w \sim \left(\frac{g^2 V_{ud}}{8m_W^2}\right) \bar{l}\gamma_\lambda (1-\gamma_5) \bar{\nu}_l \bar{u}\gamma^\lambda \gamma_5 d$$



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#### Note on the Decay of the $\pi$ -Meson

M. RUDERMAN AND R. FINKELSTEIN California Institute of Technology, Pasadena, California (Received July 25, 1949)

Assuming the symmetric coupling scheme proposed by Wheeler and Tiomno, and others, we have calculated the ratio of the decay rate  $\pi$ -meson-electron+neutrino to the decay rate of  $\pi$ -meson- $\mu$ -meson +neutrino. The electron-neutrino decay proceeds faster, in disagreement with experiment, unless the  $\pi$ -meson is pseudoscalar and the  $\beta$ -decay coupling is pseudovector. Hence if the symmetric coupling scheme is corect and no other direct couplings are introduced, the  $\pi$ -meson must be pseudoscalar and  $\beta$ -decay must be at least partially pseudovector. If symmetric coupling is not assumed, no conclusion of this kind can be drawn.

Scalar <i>P</i> -scalar Vector <i>P</i> -vector	f f f f	f 5.1 f f	f f 4.0 f	$\begin{pmatrix} f\\ 1.0 \times 10^{-4}\\ f\\ f \end{pmatrix}$	$ \begin{array}{c} f \\ f \\ 2.4 \\ 2.4 \end{array} $
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### The Pion and the Standard Model

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Scalar P-scalar Vector P-vector	f f f	f 5.1 f f	$\begin{array}{c}f\\f\\4.0\\f\end{array}$	$\begin{pmatrix} f\\ 1.0 \times 10^{-4}\\ f\\ f \end{pmatrix}$	$\begin{array}{c}f\\f\\2.4\\2.4\end{array}$
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JANUARY 1, 1958

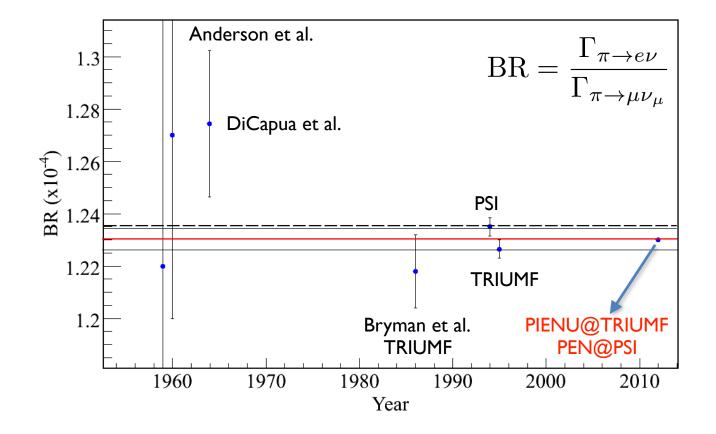
#### Theory of the Fermi Interaction

R. P. FEYNMAN AND M. GELL-MANN California Institute of Technology, Pasadena, California (Received September 16, 1957)

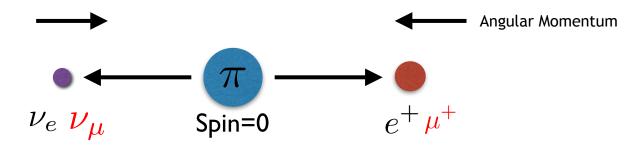
Experimentally<sup>16</sup> no  $\pi \rightarrow e + \nu$  have been found, indicating that the ratio is less than 10<sup>-5</sup>. This is a very serious discrepancy. The authors have no idea on how it can be resolved.





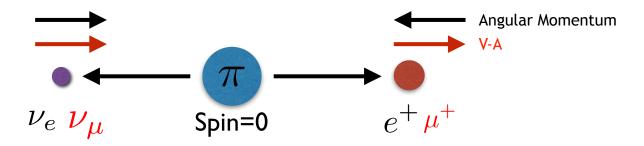




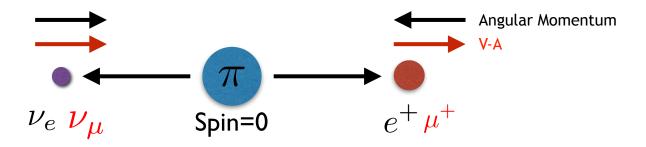




### Helicity Suppression



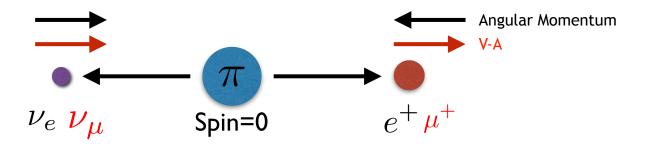




#### Neutrinos produced only by weak interactions:

Neutrinos: left-handed helicity Antineutrinos: right-handed helicity



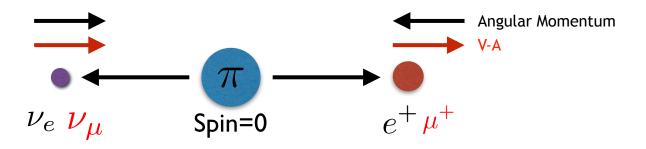


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Weak interaction forces the electron into the "wrong" helicity state





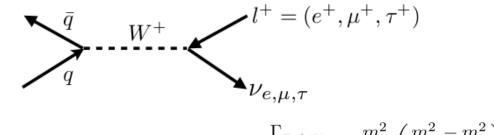
Neutrinos produced only by weak interactions:

Neutrinos: left-handed helicity Antineutrinos: right-handed helicity

Weak interaction forces the electron into the "wrong" helicity state

The V-A structure of the weak interactions explains why the muon decay mode is favoured!

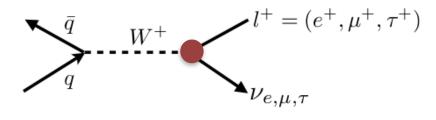
# 



$$\Gamma_{\pi \to l\nu_l} = G_{e,\mu,\tau}^2 \frac{m_\pi f_\pi^2 m_l^2}{8\pi} \left( 1 - \frac{m_l^2}{m_\pi^2} \right)^2$$

$$R_0 = \frac{\Gamma_{\pi \to e\nu_e}}{\Gamma_{\pi \to \mu\nu_\mu}} = \frac{m_e^2}{m_\mu^2} \left(\frac{m_\pi^2 - m_e^2}{m_\pi^2 - m_\mu^2}\right)^2 = 1.28336(2) \times 10^{-4}$$

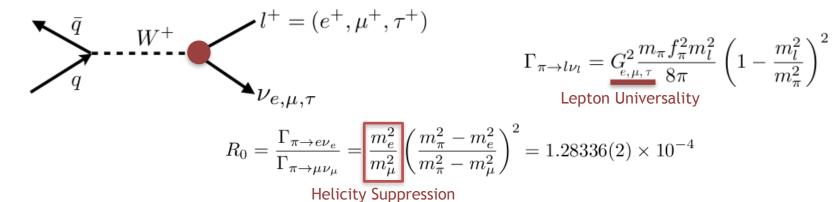
# 



$$\Gamma_{\pi \to l\nu_l} = \frac{G_{e,\mu,\tau}^2 m_\pi f_\pi^2 m_l^2}{8\pi} \left(1 - \frac{m_l^2}{m_\pi^2}\right)^2$$
Lepton Universality

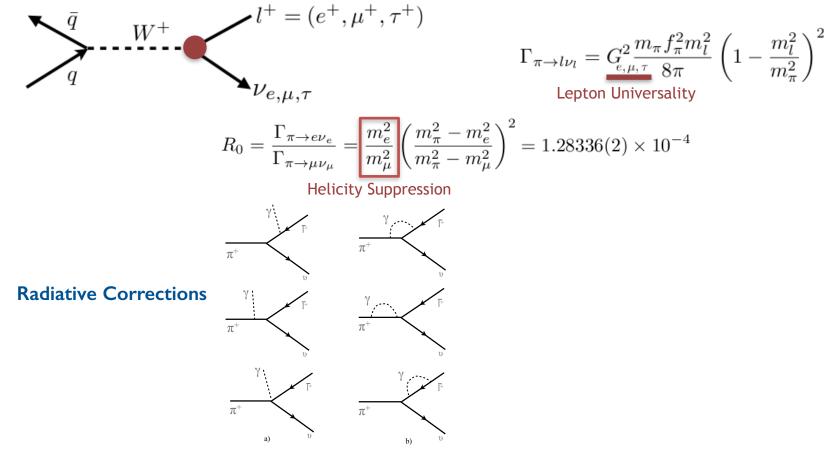
$$R_0 = \frac{\Gamma_{\pi \to e\nu_e}}{\Gamma_{\pi \to \mu\nu_\mu}} = \frac{m_e^2}{m_\mu^2} \left(\frac{m_\pi^2 - m_e^2}{m_\pi^2 - m_\mu^2}\right)^2 = 1.28336(2) \times 10^{-4}$$



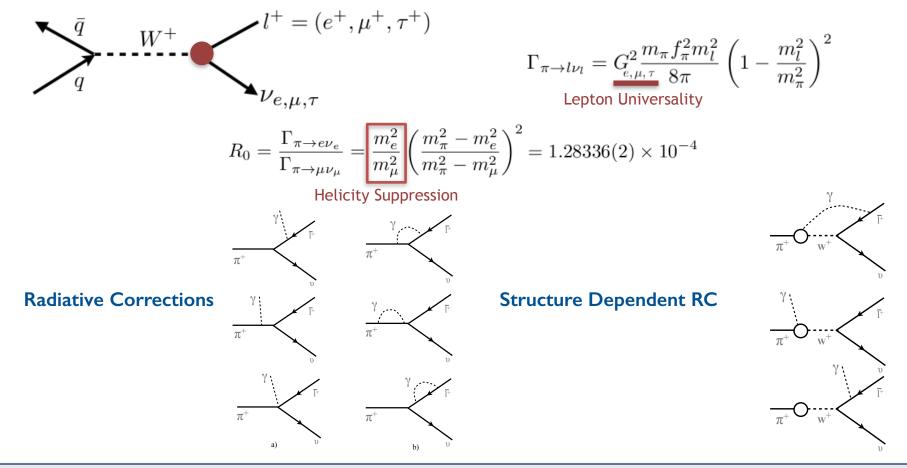


Napoli, Oct 2017

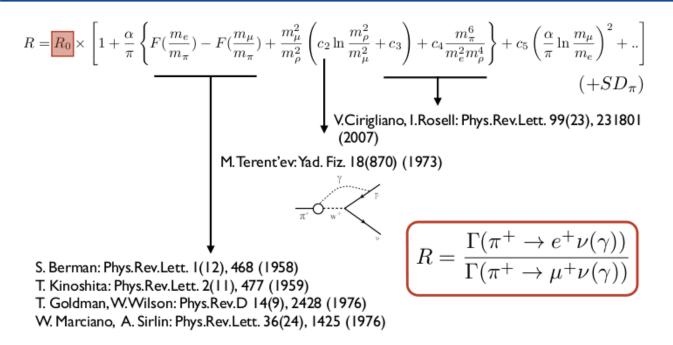




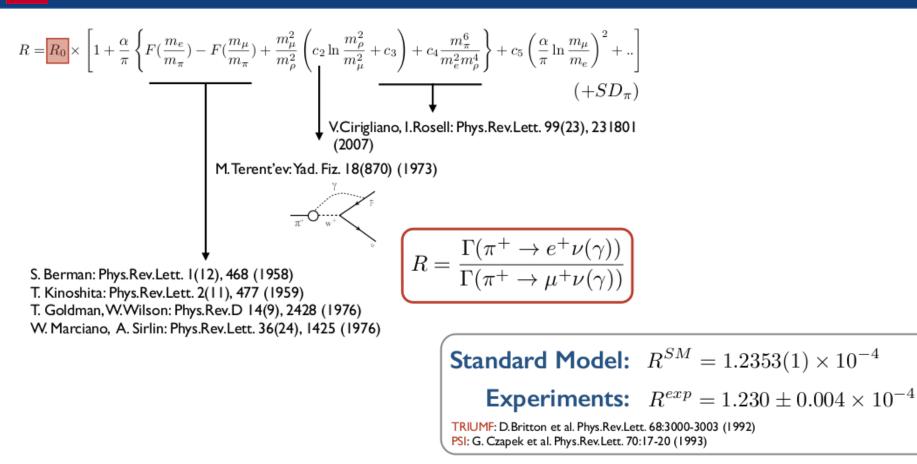




### Precision Calculation and Experimental Situation



### Precision Calculation and Experimental Situation





#### New pseudo-scalar interactions (no helicity suppression) B.Campbell, D. Maybury: Nucl.Phys. B709, 419 (2005)

$$1 - \frac{R^{exp}}{R^{SM}} \sim \mp \frac{\sqrt{2}\pi}{G_{\mu}} \frac{1}{\Lambda^2} \frac{m_{\pi}^2}{m_e(m_d + m_u)} \sim (\frac{1\text{TeV}}{\Lambda})^2 \times 10^3 \quad \Rightarrow 1000\text{TeV}$$

Charged Higgs (with non-SM couplings) O. Shanker: Nucl. Phys. B204(3), 375 (1982)

Relevant for SUSY models, Changes the BR through loop contributions

$$1 - \frac{R^{exp.}}{R^{SM}} \sim \mp \frac{2m_{\pi}^2}{m_e(m_d + m_u)} \frac{m_W^2}{m_{H^{\pm}}} \lambda_{ud} (\lambda_{e\nu} - \frac{m_e}{m_{\mu}} \lambda_{\mu\nu}) \qquad M_H^{\pm} \sim 400 \text{GeV}$$

R-parity violating SUSY affects the BR already at tree-level!

And More: Leptoquarks, new scalar interactions, massive neutrinos,...



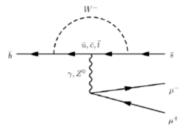
## Lepton Universality Violation ???

#### LHCb Collaboration,

R. Aaij et al., "Test of lepton universality using  $B^+ \rightarrow K^+l^+l^-$  decays," arXiv:1406.6482.

- Previously measured by Belle and BaBar at 20-50% precision level
- $R_K$  = 1 expected from SM
- Theoretically clean observable with small corrections
- Analysis :  $1 < q^2 < 6 \text{ GeV}^2/c^4$

$$R_K = \frac{B^+ \to K^+ \mu^+ \mu^-}{B^+ \to K^+ e^+ e^-} = 0.745^{+0.090}_{-0.074} (\text{stat}) \pm 0.036 (\text{cyst})$$
  
$$2.6\sigma \text{ deviation from the SM value}$$



Feruglio, Paradisi, Pattori, Phys. Rev. Lett. 118, 011801 (2017)

$$\begin{split} R_{D^{(*)}}^{\tau/\ell} &= \frac{\mathcal{B}(\bar{B} \to D^{(*)}\tau\bar{\nu})_{\rm exp}/\mathcal{B}(\bar{B} \to D^{(*)}\tau\bar{\nu})_{\rm \scriptscriptstyle SM}}{\mathcal{B}(\bar{B} \to D^{(*)}\ell\bar{\nu})_{\rm \scriptscriptstyle exp}/\mathcal{B}(\bar{B} \to D^{(*)}\ell\bar{\nu})_{\rm \scriptscriptstyle SM}},\\ R_D^{\tau/\ell} &= 1.37 \pm 0.17, \qquad R_{D^*}^{\tau/\ell} = 1.28 \pm 0.08\,. \end{split}$$

J. P. Lees et al. [BaBar Collaboration], Phys. Rev. D 88 (2013) 7, 072012 [arXiv:1303.0571].
M. Huschle et al. [Belle Collaboration], Phys. Rev. D 92 (2015) 7, 072014 [arXiv:1507.03233].
R. Aaij et al. [LHCb Collaboration], Phys. Rev. Lett. 115 (2015) 15, 159901 [arXiv:1506.08614].

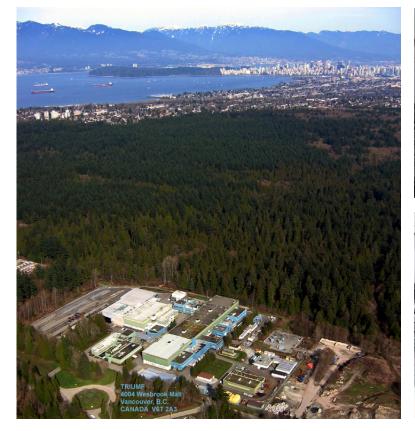
 $3.9\sigma$  deviation from the SM value



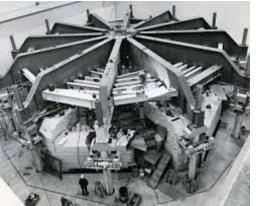
# The PIENU Experiment at TRIUMF



## The TRIUMF Cyclotron







First Beam: 1974 Total magnet weight: 4000 Tons Magnet diameter: 18m Magnetic field: Up to 5600 gauss Electric Field Frequency: 23MHz

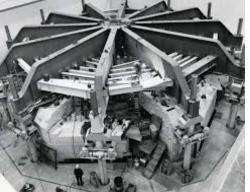
Proton Beam: Energy: 500 MeV Max Extr. Current: 140 uA.



## The TRIUMF Cyclotron

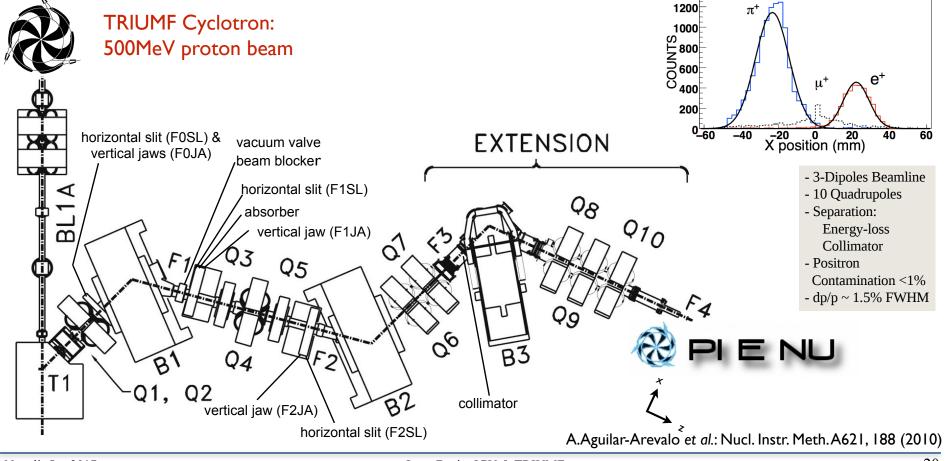


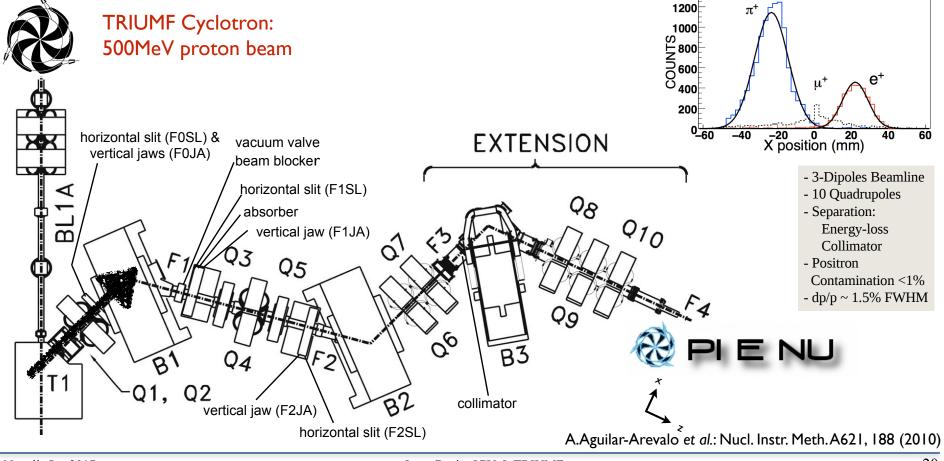


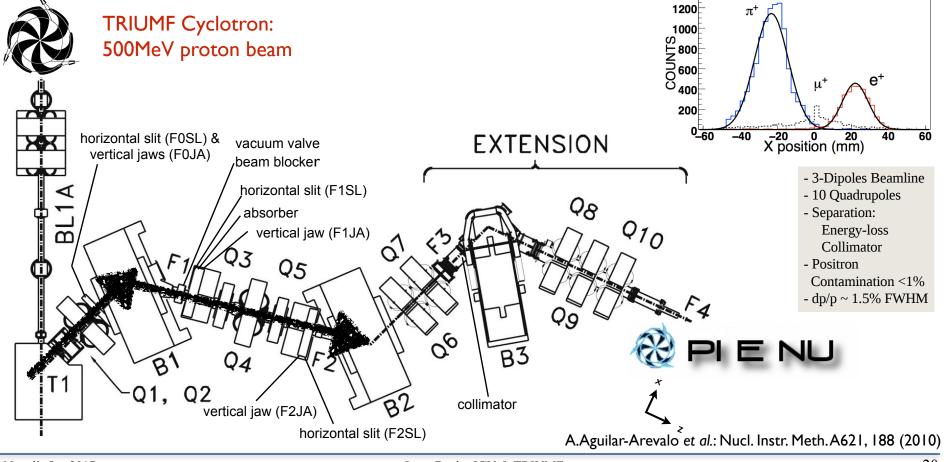


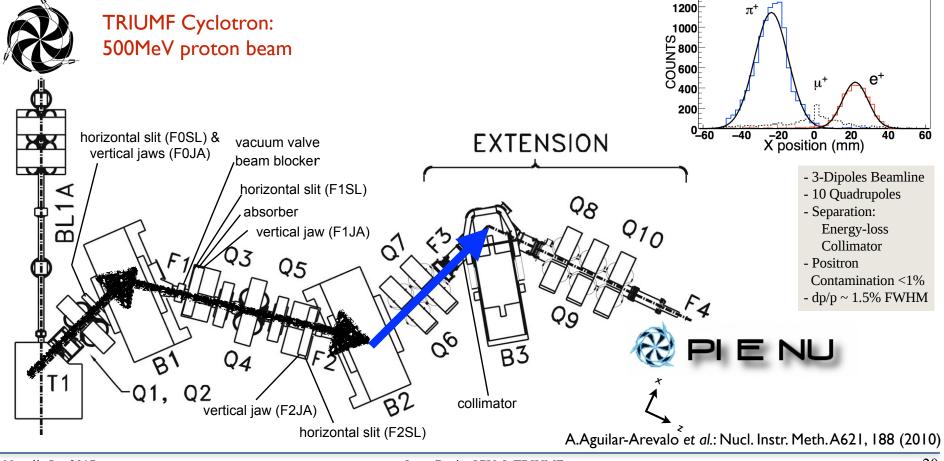
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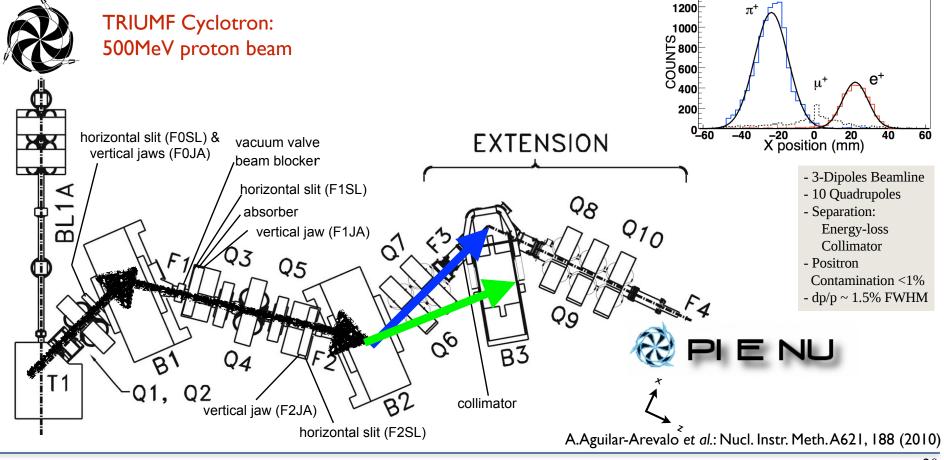
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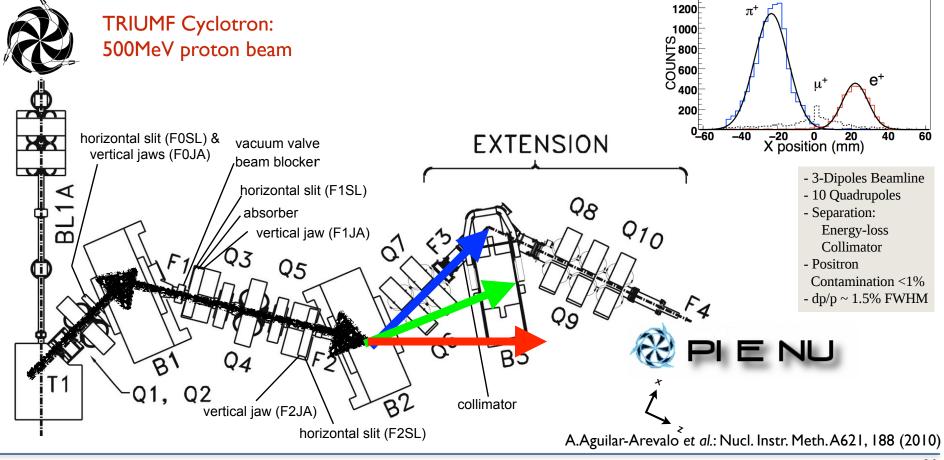


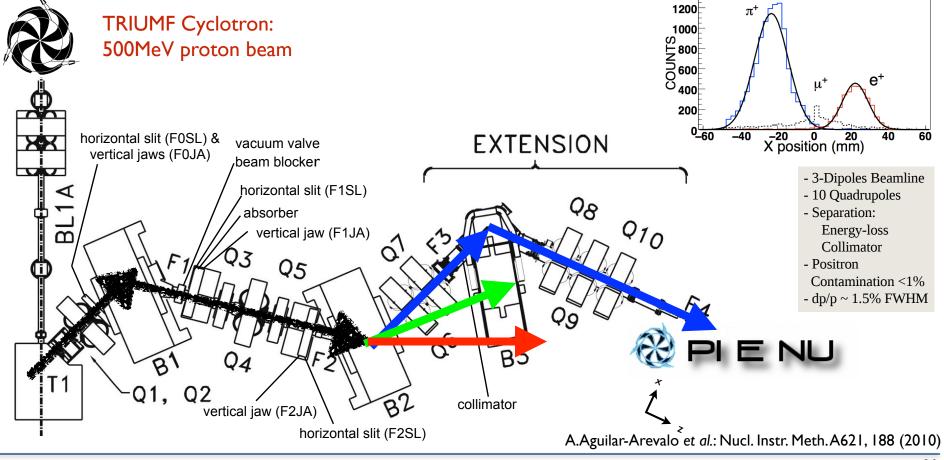






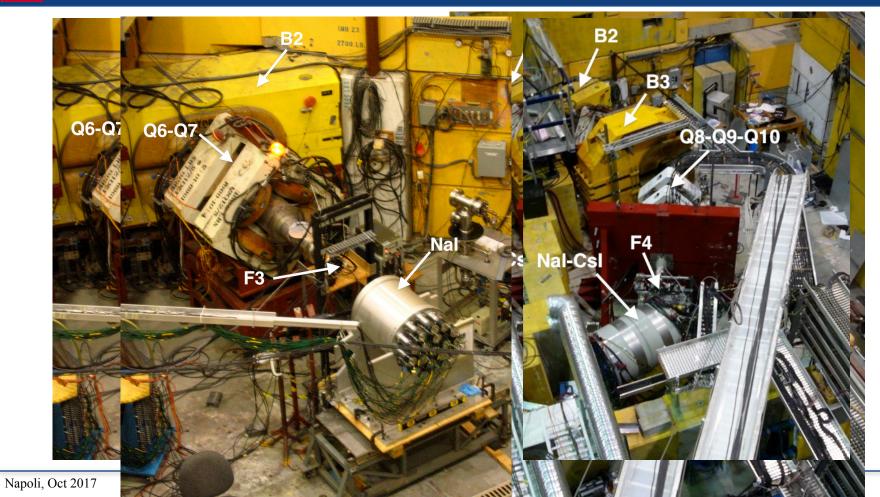








## The Pion Beam



21



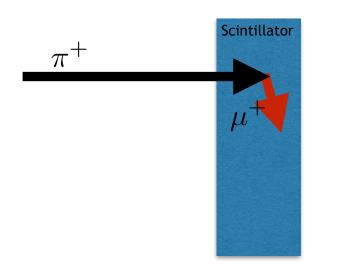
- Simultaneous measurement (energy and time)
- Same acceptance and conditions
- Systematic uncertainties cancel in the BR







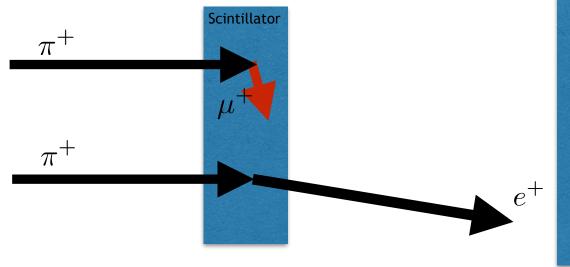
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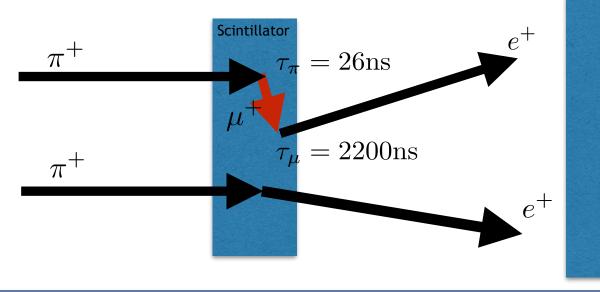
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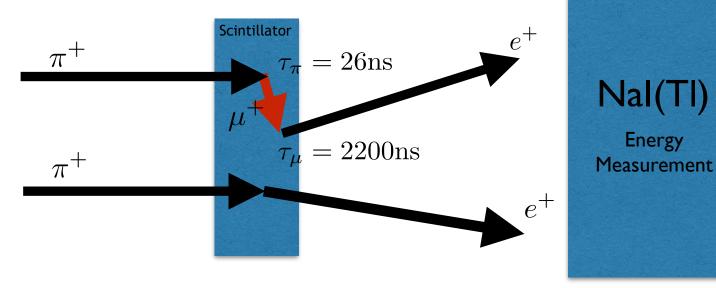


- Simultaneous measurement (energy and time)
- Same acceptance and conditions
- Systematic uncertainties cancel in the BR



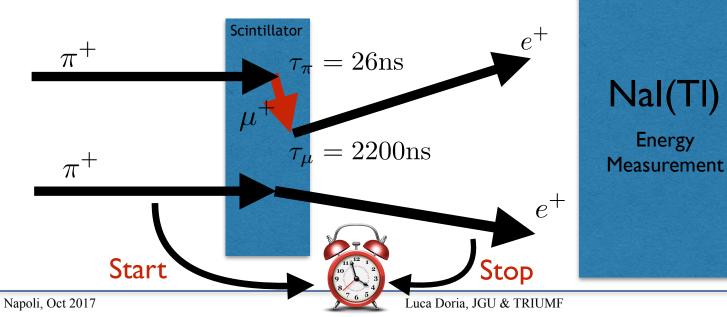


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- Simultaneous measurement (energy and time)
- Same acceptance and conditions
- Systematic uncertainties cancel in the BR





#### Beam:

60kHz pions @ 75 MeV/c  $\pi: \mu: e = 85: 14: 1$ 

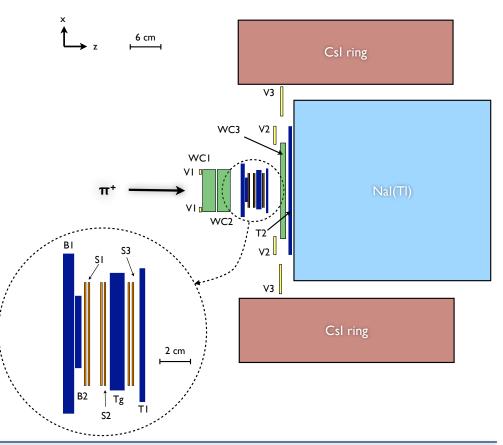
#### Detector:

Acceptance: 20% Plastic Scintillators Nal(TI) + Csl Calorimeter Wire Chambers Silicon Strips

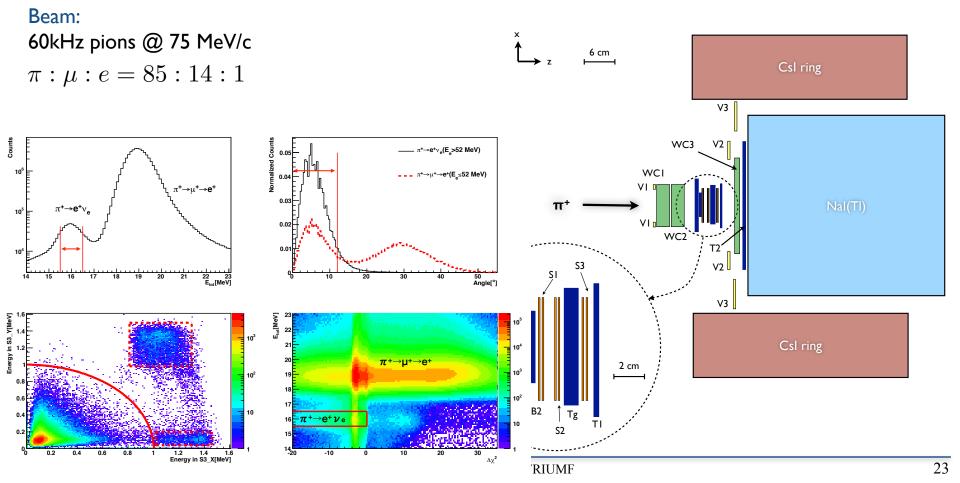
Energy resolution: 2.2% FWHM @ 70MeV

**Temperature Stabilization** 

Data taking: 2009-2012









## Experimental Setup: Target Region

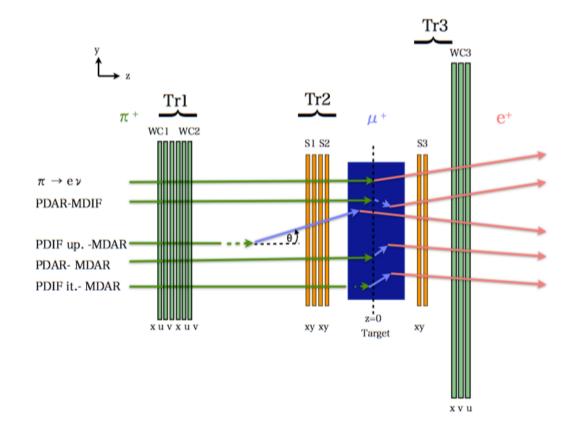
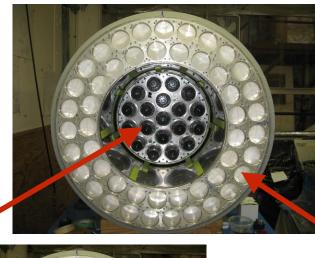


Figure from C.Malbrunot, PhD thesis (2012)





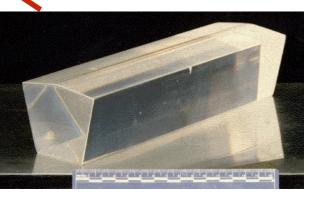
"BiNa": Monolithic 48x48cm Nal(TI) crystal I9-PMTs readout



97 pure Csl crystals single PMT readout





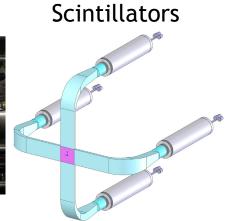




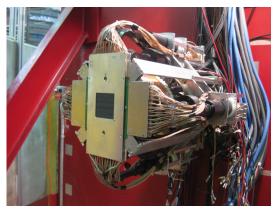
## Tracking and Time/Energy Detectors

### Wire Chambers









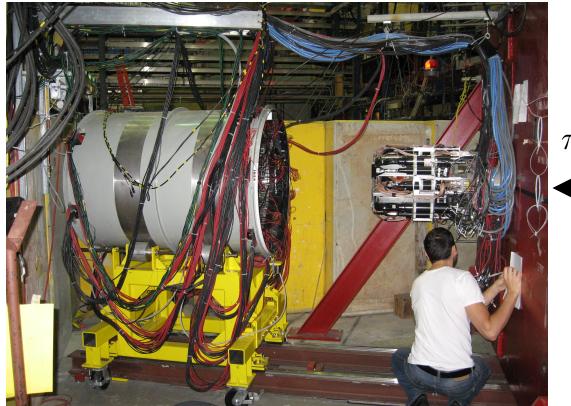
#### **Silicon Detectors**







## **Experimental Setup**



 $\pi^+$  Beam

A.Aguilar-Arevalo et al: Nucl. Instr. Meth. A79, 38-46 (2015)

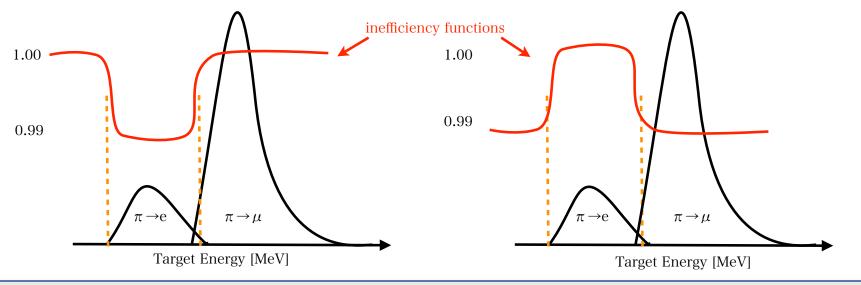


## **Data Analysis**

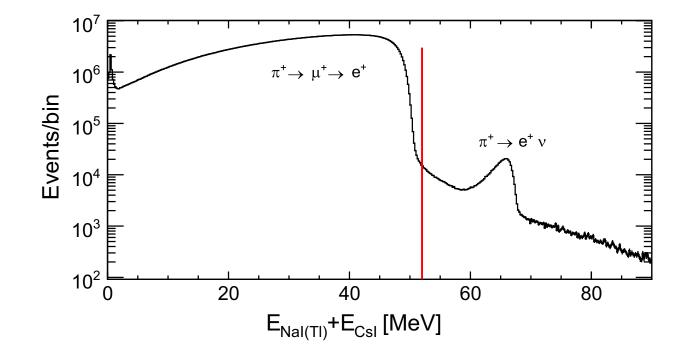


- Avoid biases in precision experiments!

- Blinding procedure done before starting the analysis.
- One of the two decays is slightly suppressed: BR changes.
- Random and unknown inefficiency factor
- "Unblinding" only when the Collaboration agrees on the analysis procedure and systematic error estimates.

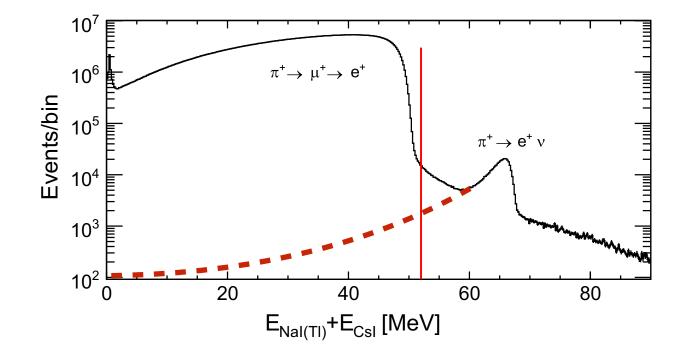






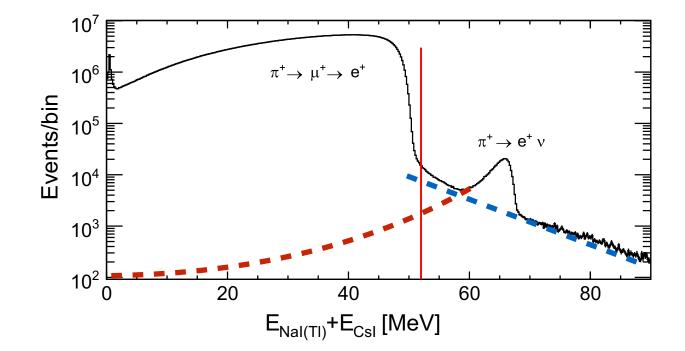
Low Energy TailPileup



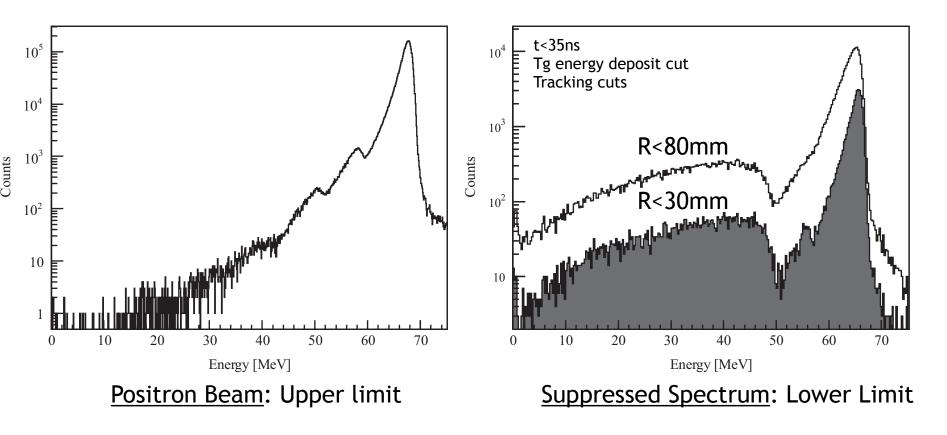


Low Energy TailPileup

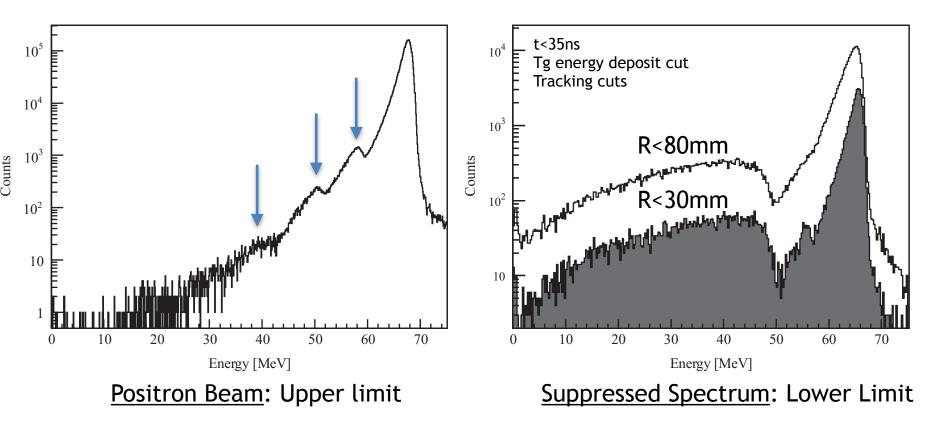




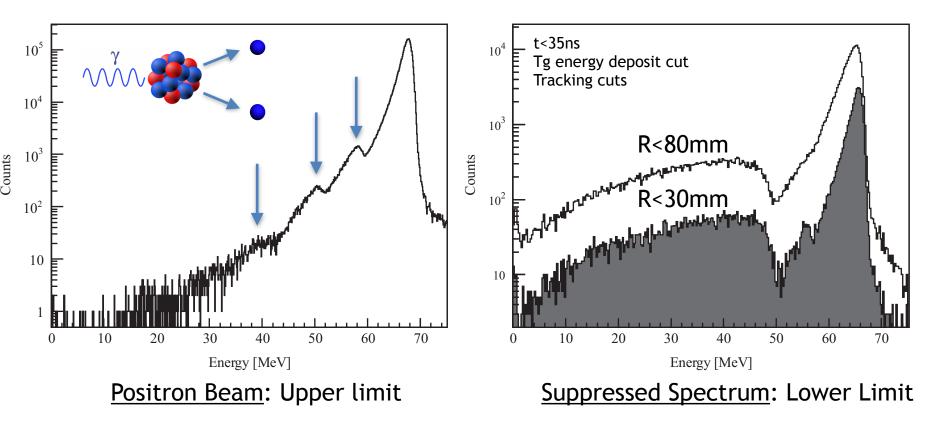
Low Energy TailPileup



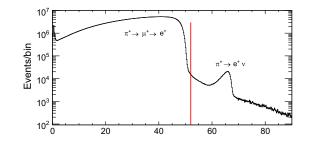




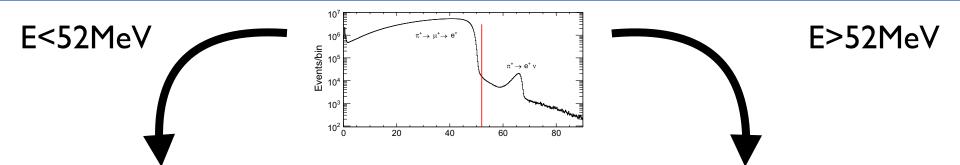


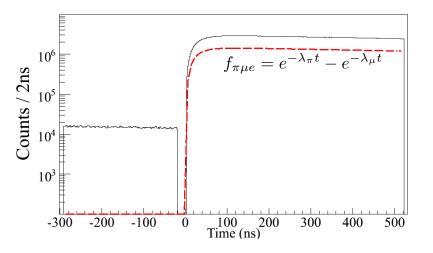




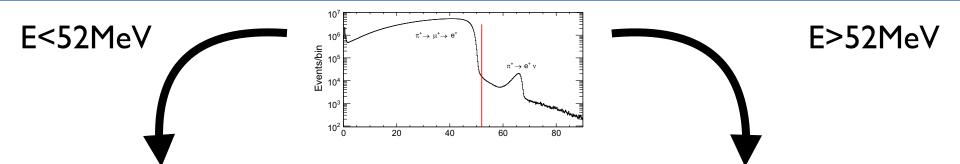


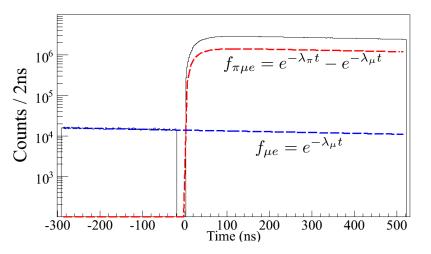




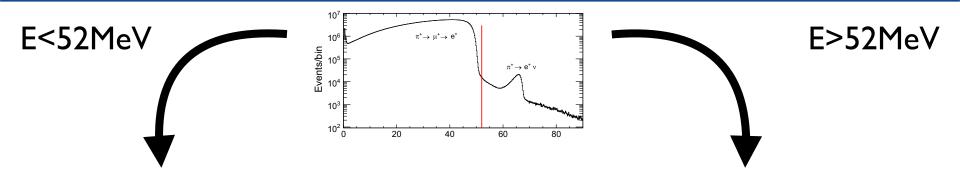


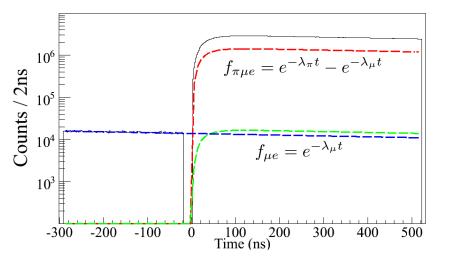






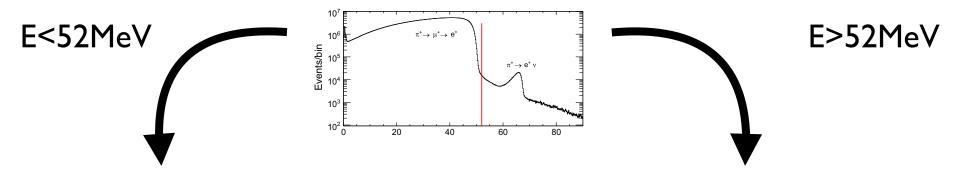


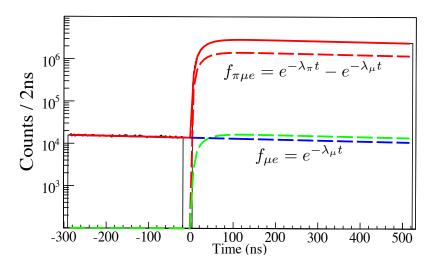






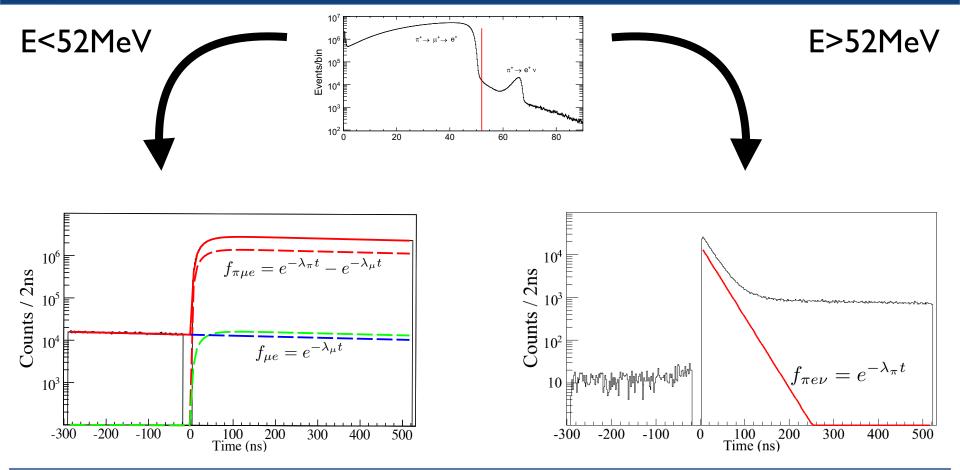






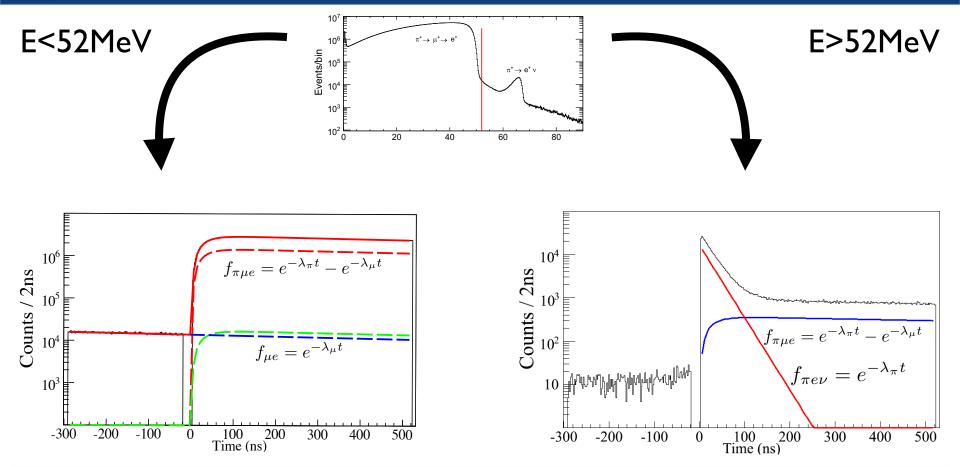


Time Spectrum Fit



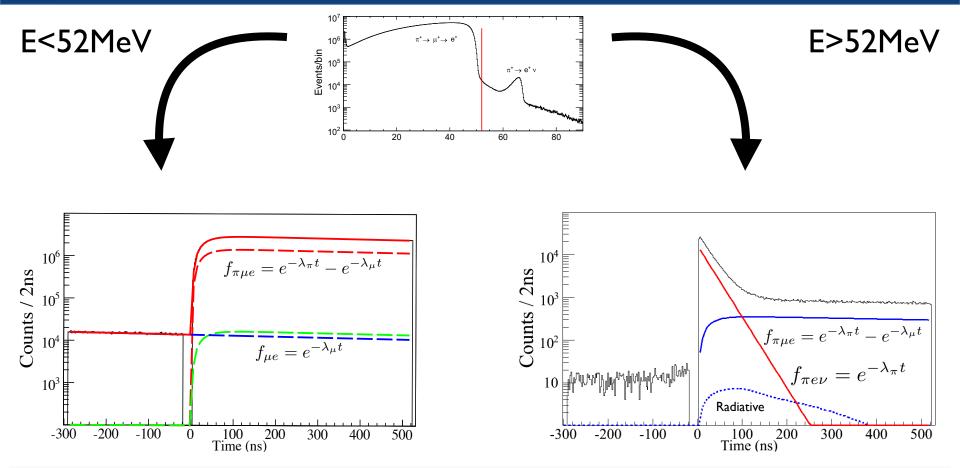


## Time Spectrum Fit



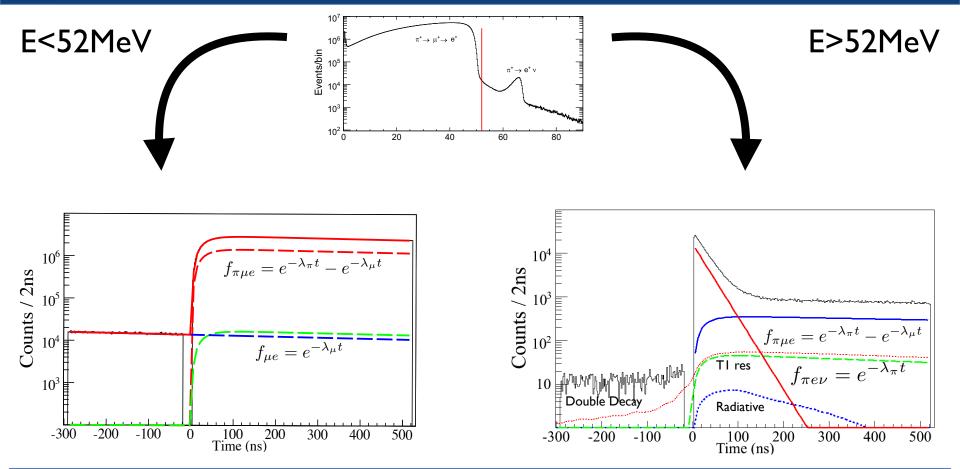


## Time Spectrum Fit



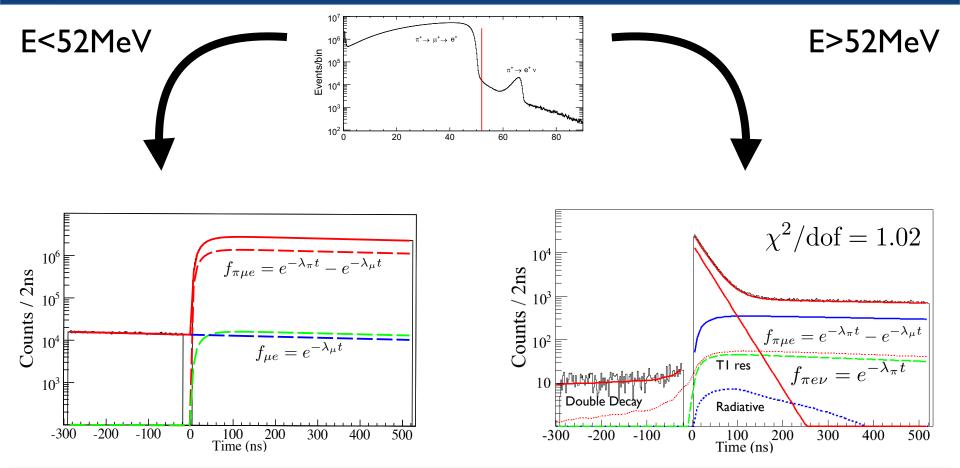


Time Spectrum Fit





Time Spectrum Fit





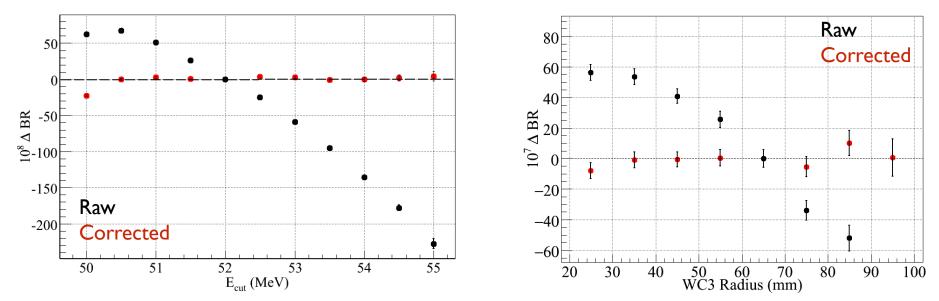
### Acceptance Radius Dependence

- R= 60 mm
- Errors adjusted to statistics change
- Maximum R investigated

with e<sup>+</sup> beam

### **Energy cut dependence**

Tail/muDIF corrections applied





# **Results**



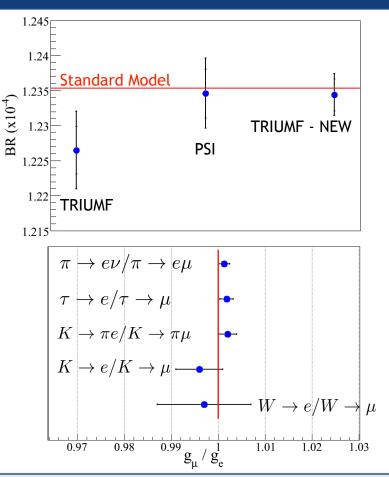
## 2010 Dataset Results

### Phys. Rev. Lett. 115, 071801 (2015)

	Values	Uncertainties	
		Stat	Syst
$R_{e/\mu}^{Raw} (10^{-4})$	1.1972	0.0022	0.0005
$\pi, \mu$ lifetimes			0.0001
other parameters			0.0003
excluded components			0.0005
Corrections			
Acceptance	0.9991		0.0003
Low energy tail	1.0316		0.0012
Other	1.0004		0.0008
$R_{e/\mu}^{Exp} (10^{-4})$	1.2344	0.0023	0.0019

 $R_{e/\mu}^{Th} (10^{-4}) = 1.2352(2)$ 

$$e - \mu$$
 Universality:  $g_e/g_\mu = 0.9996 \pm 0.0012$ 





Dataset	BR	Status
2010	$1.2344 \pm 0.0023 \pm 0.0012$	Published
2011	$1.2XX \pm 0.0018 \pm 0.0013$	Completed, blind
2012	$1.2XX \pm 0.0009 \pm 0.00X$	In progress



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## Final Goal: 0.1% precision

## Massive Neutrino Search



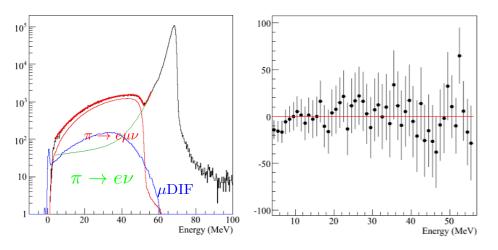
 $\pi 
ightarrow e 
u$  is a two-body decay

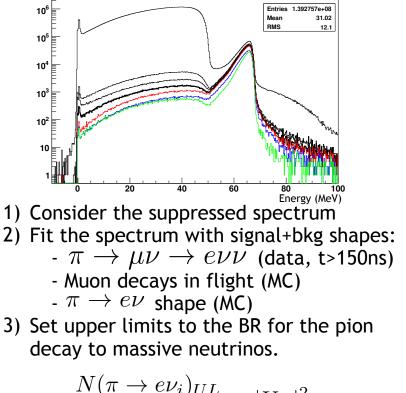
The pion decays at rest

-> Kinematics fully known if e<sup>+</sup> is measured:

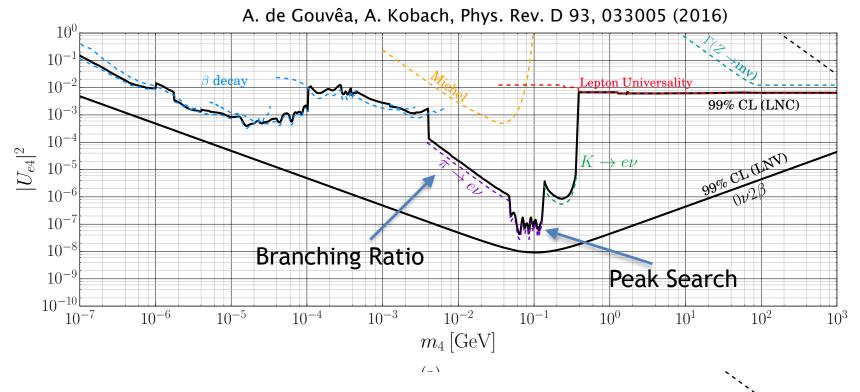
$$m_{\nu} = \sqrt{m_{\pi}^2 + m_e^2 - 2m_{\pi}E_e}$$

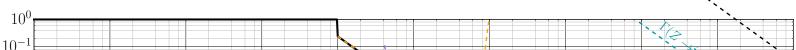
If a massive neutrino can be produced, it will show up as a peak in the energy spectrum.













D.I. Britton et al., Phys. Rev. D46, R885 (1992). M. Aoki et al., Phys. Rev. D84, 052002 (2011).

Plot showed only at the talk and then removed for distributing the slides. Waiting for publication, sorry!

Obtained upper limits at about 10<sup>-8</sup> level



- Best limit on lepton universality violation established
- Work ongoing towards full dataset analysis
- Massive neutrino searches in the MeV range in pion and muon decays
- More BSM decay searches possible: Majorons, Z', ...



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### Final results coming soon: stay tuned!



#### JOHANNES GUTENBERG UNIVERSITÄT MAINZ

## Thank You! Merci!



TRIUMF: Alberta I British Columbia I Calgary I Carleton I Guelph I Manitoba I McGill I McMaster I Montréal I Northern British Columbia I Queen's I Regina I Saint Mary's I Simon Fraser I Toronto I Victoria I Western I Winnipeg I York



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TRIUMF: Alberta I British Columbia I Calgary I Carleton I Guelph I Manitoba I McGill I McMaster I Montréal I Northern British Columbia I Queen's I Regina I Saint Mary's I Simon Fraser I Toronto I Victoria I Western I Winnipeg I York Thank You! Merci! Danke!



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TRIUMF: Alberta I British Columbia I Calgary I Carleton I Guelph I Manitoba I McGill I McMaster I Montréal I Northern British Columbia I Queen's I Regina I Saint Mary's I Simon Fraser I Toronto I Victoria I Western I Winnipeg I York Thank You! Merci! Danke! Grazie!

