

Physics with muon collider

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Muon based Colliders

- A $\mu^+\mu^-$ collider offers an ideal technology to extend lepton high energy frontier in the multi-TeV range:
 - No synchrotron radiation (limit of e^+e^- circular colliders)
 - No beamstrahlung (limit of e^+e^- linear colliders)
 - but muon lifetime is 2.2 μs (at rest)
- Best performances in terms of luminosity and power consumption
- Great potentiality if the technology proves its feasibility:
 - cooled muon source
 - fast acceleration
 - μ Collider
 - radiation Safety (muon decay in accelerator and detector)

The strength of a μ -beam facility lies in its richness:

- Muon rare processes
- Neutrino physics
- Higgs factory
- Multi-TeV frontier

Focus here

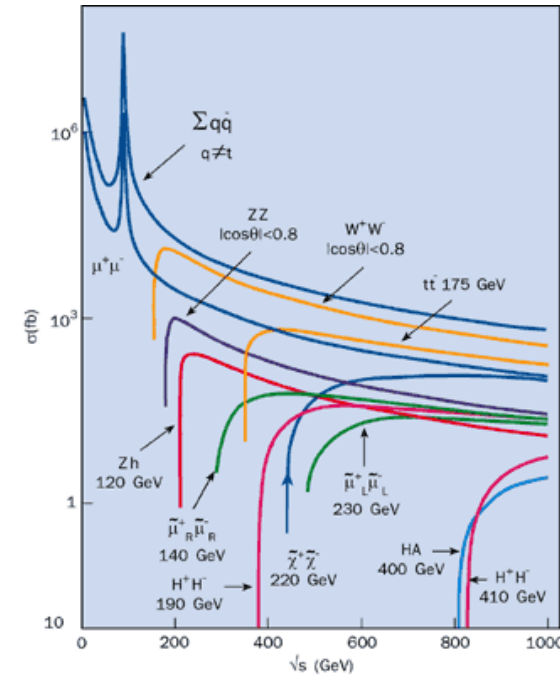
Take 1

Get 4 !

μ -colliders can essentially do the HE program of e^+e^- colliders with added bonus (and some limitations)

TeV/Multi-TeV Lepton Collider Basics

- At $\sqrt{s}=M_H$ resonant Higgs production
 - For $\sqrt{s}<500\text{GeV}$
 - SM threshold region: top pairs; W^+W^- ; ZZ ; Zh ; ...
 - For $\sqrt{s}>500\text{GeV}$
 - For SM pair production
- $R = \sigma/\sigma_{\text{QED}}(\mu^+\mu^- \rightarrow e^+e^-) \sim \text{flat}$
- High luminosity required

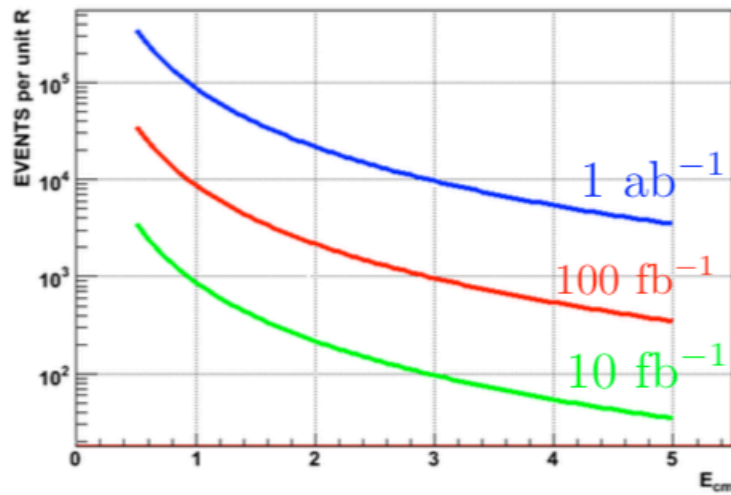




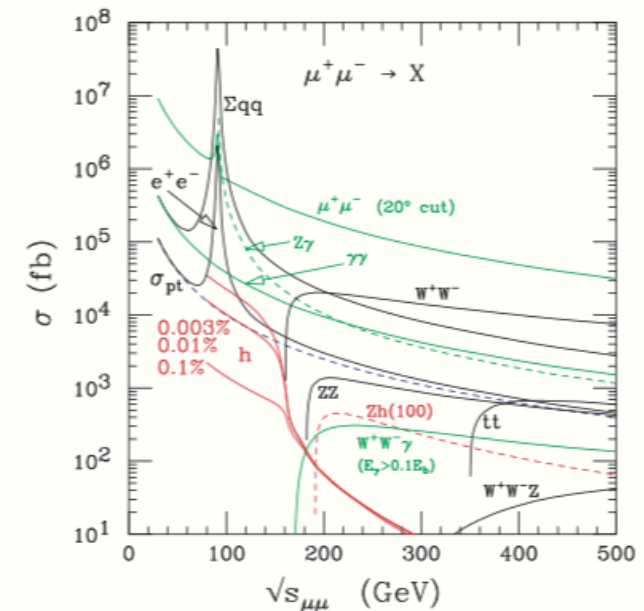
MultiTeV Lepton Collider Basics

- For $\sqrt{s} < 500 \text{ GeV}$
 - SM threshold region: top pairs; W^+W^- ; Z^0Z^0 ; Z^0h ; ...
- For $\sqrt{s} > 500 \text{ GeV}$
 - For SM pair production ($|\theta| > 10^\circ$)
 $R = \sigma / \sigma_{\text{QED}}(\mu^+\mu^- \rightarrow e^+e^-) \sim \text{flat}$

$$\sigma_{\text{QED}}(\mu^+\mu^- \rightarrow e^+e^-) = \frac{4\pi\alpha^2}{3s} = \frac{86.8 \text{ fb}}{s(\text{TeV}^2)}$$
 - High luminosity required



Standard Model Cross Sections



$$\sqrt{s} = 3.0 \text{ TeV} \quad \mathcal{L} = 10^{34} \text{ cm}^{-2}\text{sec}^{-1}$$

$$\rightarrow 100 \text{ fb}^{-1}\text{year}^{-1}$$

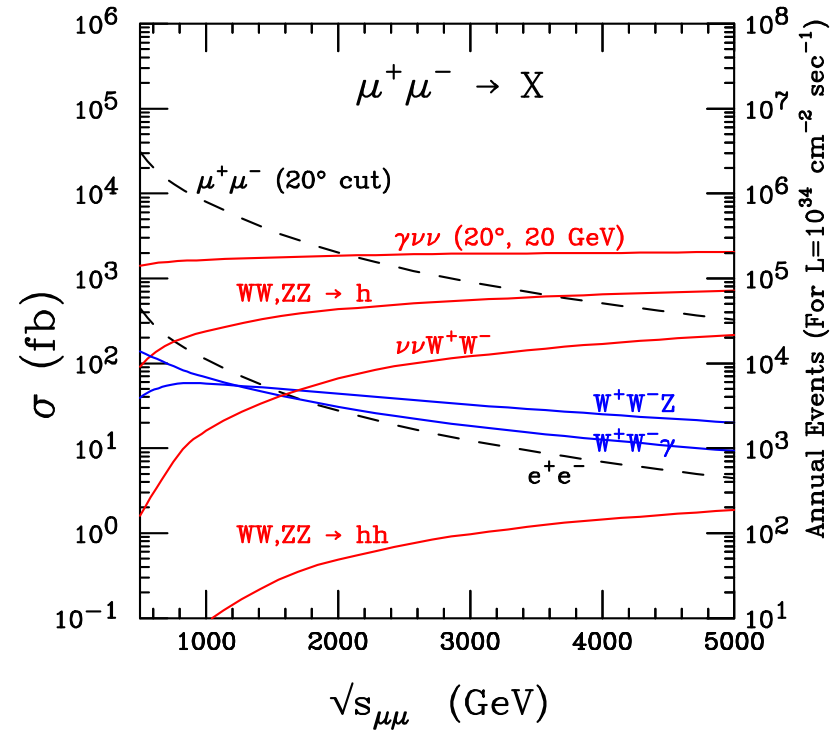
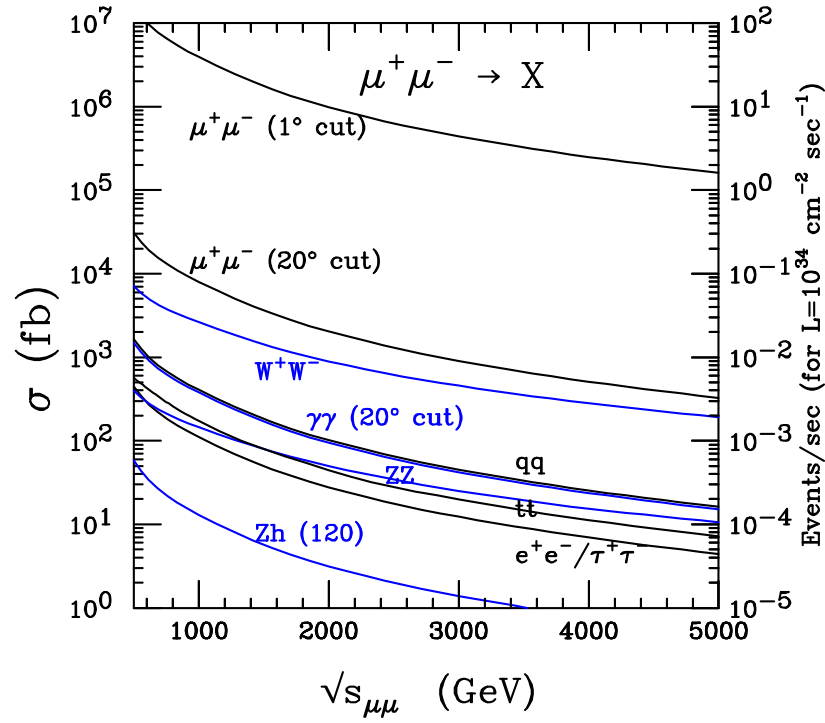
\Rightarrow 965 events/unit of R

Processes with $R \geq 0.1$ can be studied

Total - 540 K SM events per year

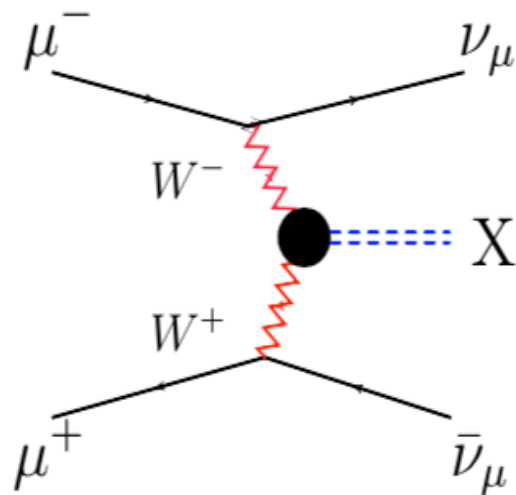
$$= 10^{36} \text{ cm}^{-2}\text{s}^{-1} @ \sqrt{s} 30 \text{ TeV}$$

SM at a muon collider:



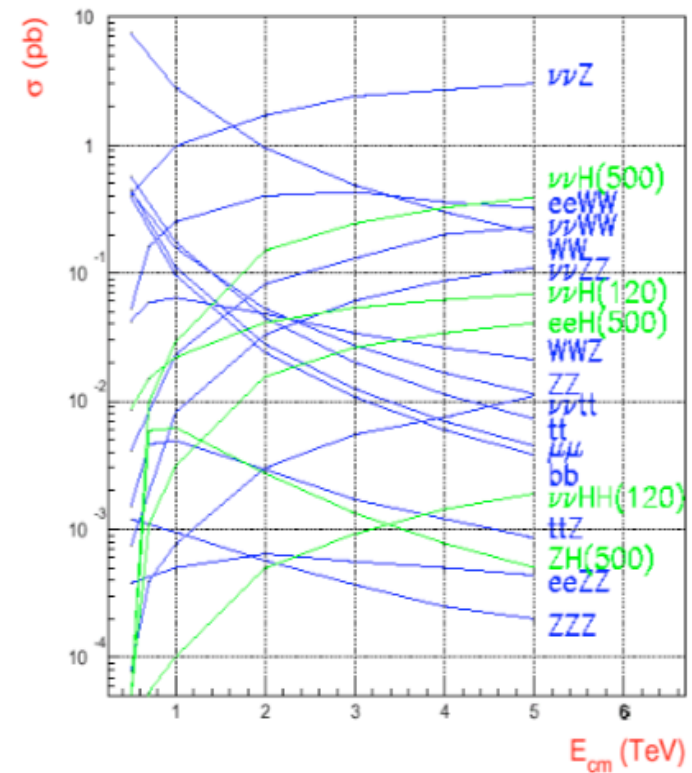
Vector boson fusion

- For $\sqrt{s} > 1 \text{ TeV}$ - Fusion Processes
 - Large cross sections
 - Increase with s .
 - Important at multi-Tev energies
 - $M_X^2 < s$
- Backgrounds for SUSY processes
- t-channel processes sensitive to angular cuts



$$\sigma(s) = C \ln\left(\frac{s}{M_X^2}\right) + \dots$$

CLIC (or MC $e^- \rightarrow \mu$)

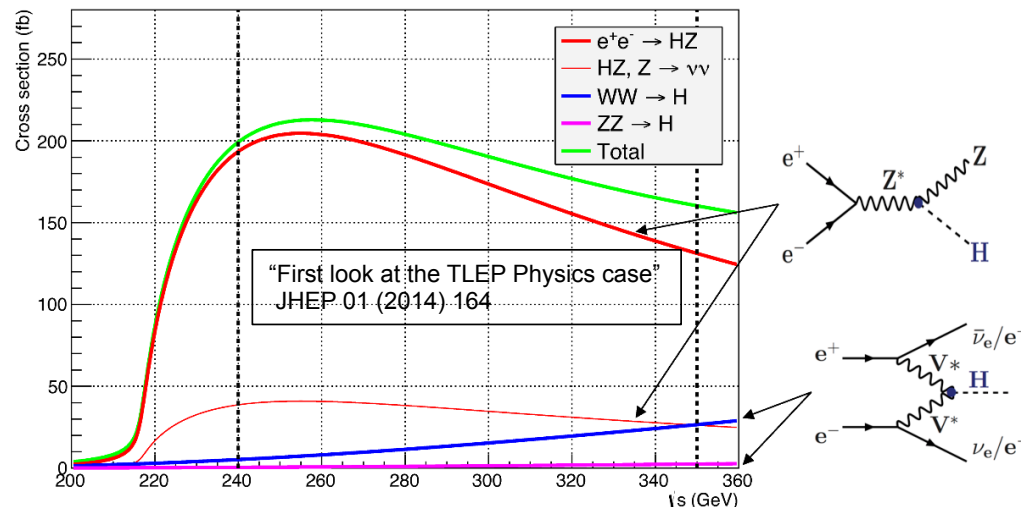


Higgs Physics

M. Antonelli, Padova, July 16th 2015

Higgs boson production

- Muons are leptons, like electrons
 - Muon colliders can a priori do everything that e^+e^- colliders can do, e.g.:



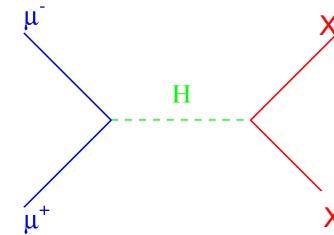
- FCC-ee luminosity: $0.5 - 1.1 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$ / IP and up to 4 IPs
- Muon collider luminosity: $\text{few} \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$ / IP
- Precision on branching ratios, couplings, width, mass, etc. , with 2 IPs
 - A factor 10 better at FCC-ee (and twice better at ILC) than at a muon collider

SM Higgs resonance

- Resonant production

$$\sigma(\mu^+\mu^- \rightarrow H^0) = \frac{4\pi\Gamma_H^2 Br(H^0 \rightarrow \mu^+\mu^-)}{(\hat{s} - M_H^2)^2 + \Gamma_H^2 M_H^2}$$

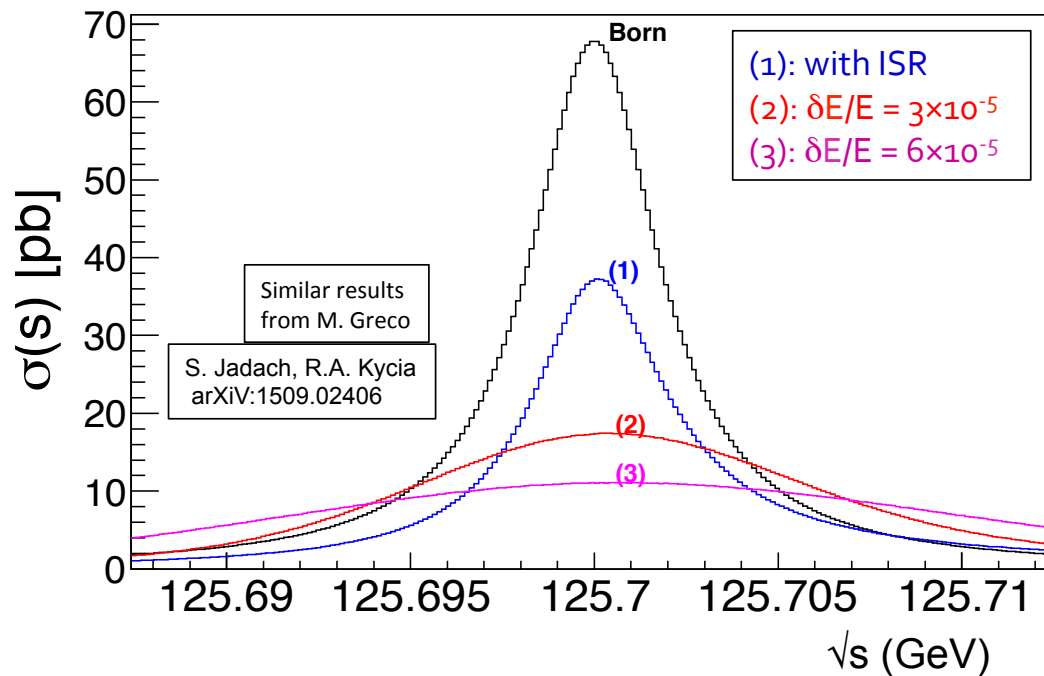
- Convolved with
 - Beam energy spectrum
 - Initial state radiation (ignored in most studies)
- The measurement of the lineshape gives access to
 - The Higgs mass, m_H
 - The Higgs width, Γ_H
 - The branching ratio into $\mu^+\mu^-$, $BR(H \rightarrow \mu\mu)$
 - Hence, the coupling of the Higgs to the muon, $g_{H\mu\mu}$
 - Some branching fractions and couplings, with exclusive decays



Major background:
 $\mu^+\mu^- \rightarrow Z/\gamma^* \rightarrow XX$

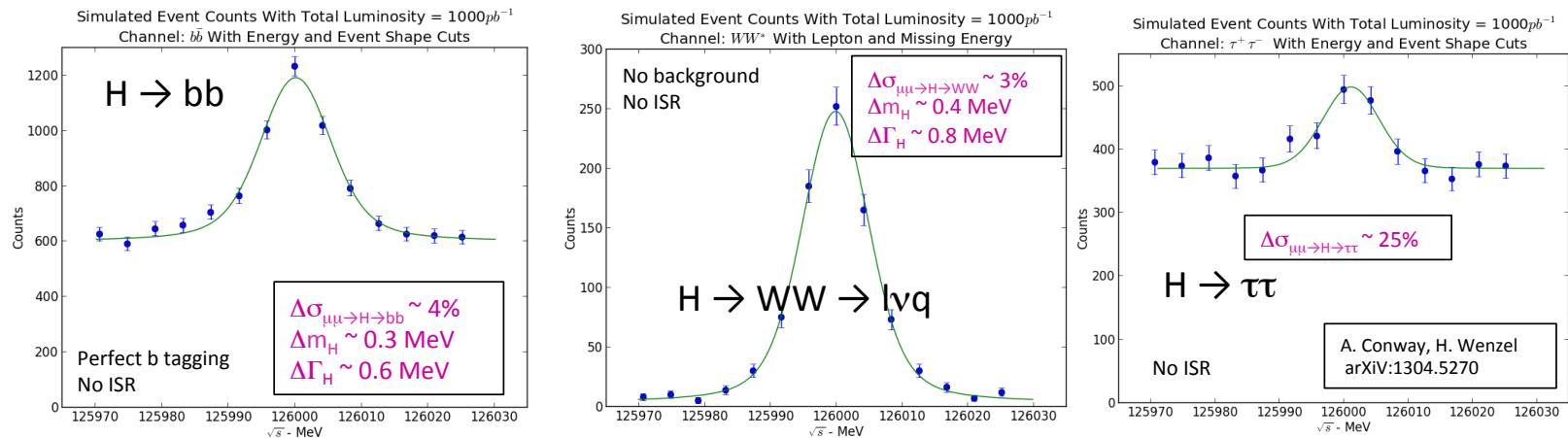
SM Higgs resonance

- Muons are heavy, unlike electrons: $m_\mu/m_e \sim 200$
 - Large direct coupling to the Higgs boson: $\sigma(\mu^+\mu^- \rightarrow H) \sim 40,000 \times \sigma(e^+e^- \rightarrow H)$
 - Much less synchrotron radiation, hence potentially superb energy definition
 - $\delta E/E$ can be reduced to $3-4 \times 10^{-5}$ with more longitudinal cooling
 - Albeit with equivalent reduction of luminosity: $2 - 8 \times 10^{31} \text{ cm}^{-2}\text{s}^{-1}$



- $\sigma(\mu^+\mu^- \rightarrow H) \sim 15 \text{ pb}$
(ISR often forgotten...)
- $200 - 800 \text{ pb}^{-1}/\text{yr}$
- $3000 - 12000 \text{ Higgs}/\text{yr}$

Scan of the SM Higgs resonance



– Notes

- Some optimism in these numbers (perfect b tag, only Z bkgd, no beam bkgd...)
- Errors to be increased to account for ISR
- A better scan strategy should be designed (less in the sides, more in the peak)
- The numbers are for 5 years at low luminosity, and 1.2 year after lumi upgrade
 - Combined numbers (next slide) given for 5 (low lumi) + 5 (upgrade) years.

Possible results with 1 fb^{-1}

- Simulated results with backgrounds and cuts
 - $1 \text{ fb}^{-1} = 1 \text{ yr} (10^7 \text{ sec}) @ 1 \times 10^{32}$

Channel		$\Gamma_{H \rightarrow X} (\text{MeV})$	$\Delta M_H (\text{MeV})$	$Br(H^0 \rightarrow X)$
Total	Raw	4.56 ± 1.52	0.13 ± 0.16	0.96 ± 0.04
	Cut	5.57 ± 1.33	-0.02 ± 0.14	0.65 ± 0.01
$b\bar{b}$	Raw	3.49 ± 1.83	-0.06 ± 0.19	0.67 ± 0.05
	Cut	4.78 ± 0.48	0.01 ± 0.05	0.271 ± 0.001
WW^*	Raw	4.06 ± 0.24	0.00 ± 0.07	0.217 ± 0.001
	Cut	3.96 ± 0.17	-0.16 ± 0.04	0.1271 ± 0.0002
$\tau^+\tau^-$	Raw	4.82 ± 4.46	-0.54 ± 0.47	0.0623 ± 0.0005
	Cut	0.84 ± 2.97	1.07 ± 0.30	0.24 ± 0.23
$\gamma\gamma$	Raw	2.85 ± 5.73	-0.6 ± 0.9	0.0035 ± 0.0001
	Cut	—	—	—

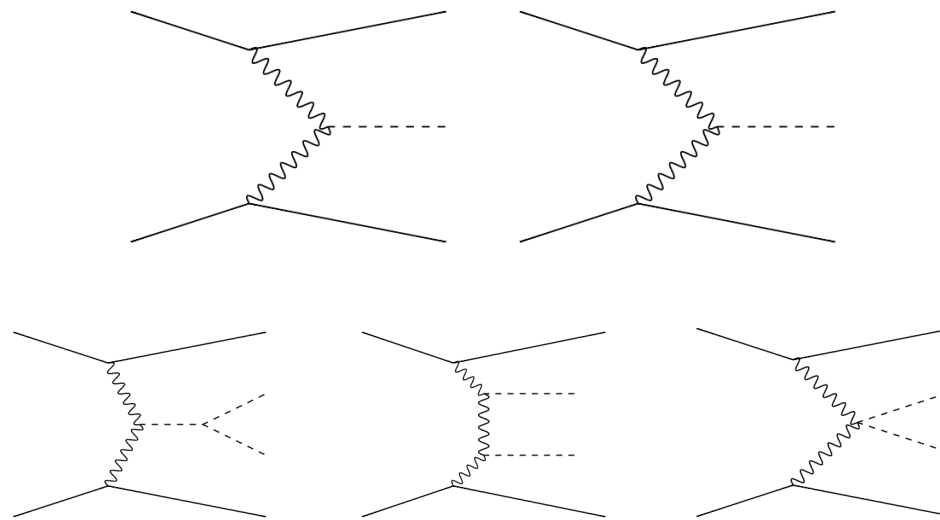
– Combined:

- $\sigma(M_H) \sim 0.03 \text{ MeV} (< \sim 100 \text{ MeV @ ILC-500})$
- $\sigma(\Gamma_H) \sim 0.16 \text{ MeV} (\sim 0.08 \text{ MeV @ ILC-500})$

YKK FNAL study
arxiv1308.2143

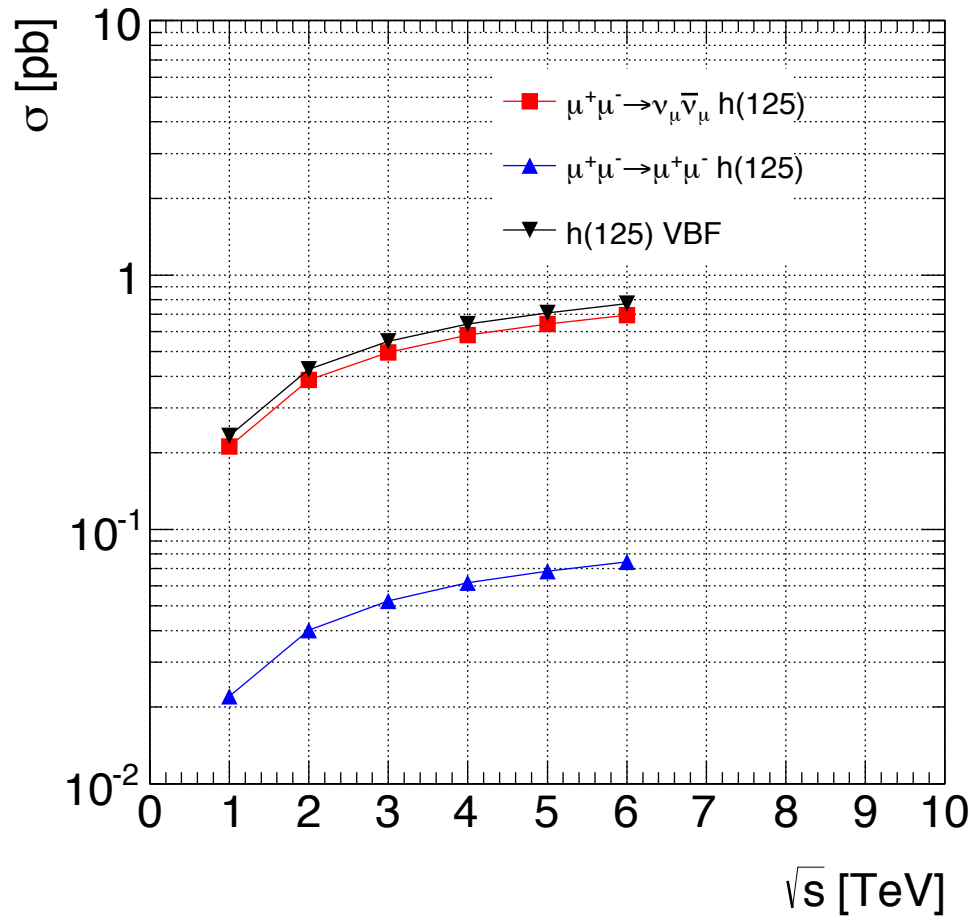
Higgs production for multiTev muon collider

- VBF dominant production mode



- WHIZARD event generator for cross section computation
 - <http://whizard.hepforge.org/>

VBF Higgs production



@sqrt(s) = 3 TeV

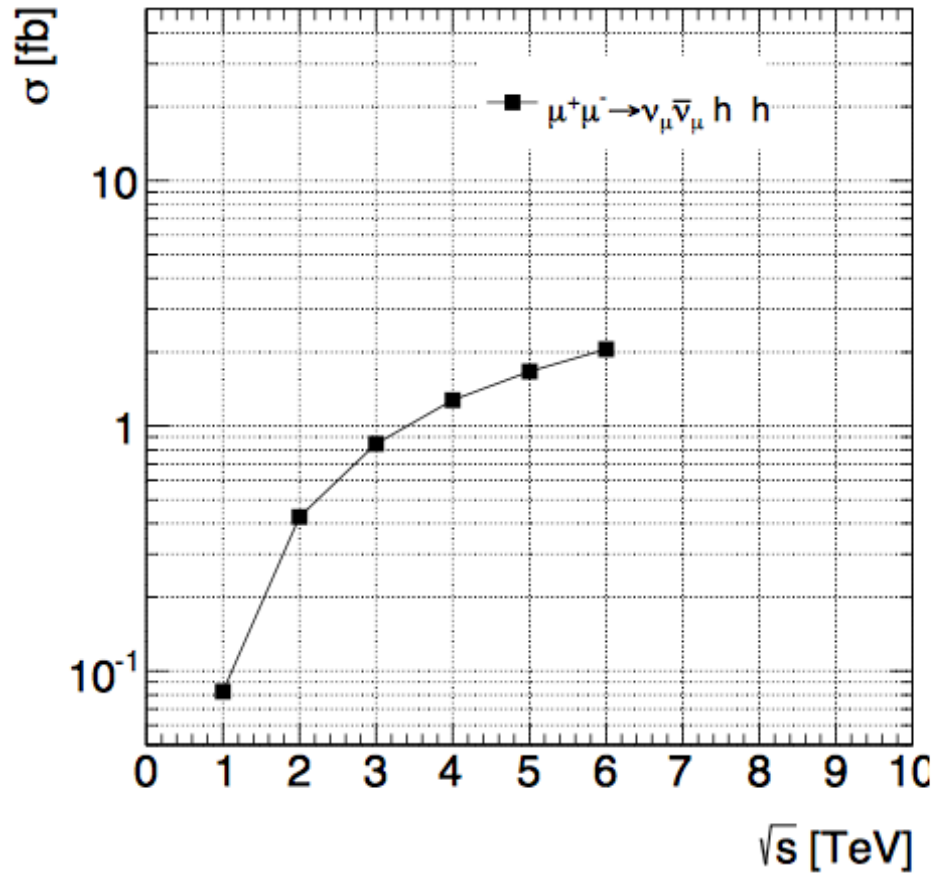
$\mu\mu \rightarrow \nu\nu H$: 495 fb

$\mu\mu \rightarrow \mu\mu h$: 52 fb

R Di Nardo, M Rotondo,
G Simi

Analysis study
to be performed

VBF HH production

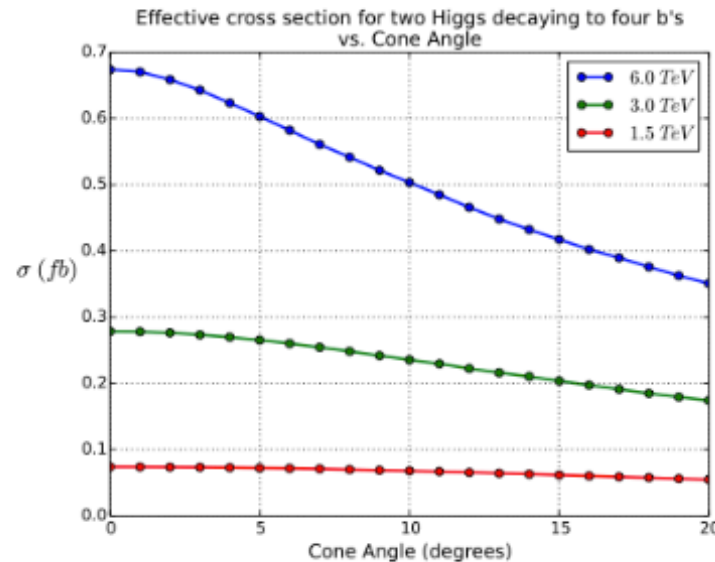


Not yet detailed studies

@sqrt(s) = 3 TeV
 $\mu\mu \rightarrow \nu\nu HH$: 0.9 fb

@sqrt(s) = 6 TeV
 $\mu\mu \rightarrow \nu\nu HH$: 2.1 fb

Machine bkg limitations:
 xs with 4b in det. acceptance



A.Conway, H.Wenzel, R.Lipton and E.Eichten,
 arXiv:1405.5910

SM Higgs

- Resonant Higgs production:

- Unique measurements of mh and Γh
($mh \sim 0.1$ MeV, $\Gamma h \sim 0.2$ MeV)
- Best test of 2nd generation Higgs couplings ($h \rightarrow \mu+\mu-$)

- HZ production:

- Similar to e^+e^- measurements but lower statistics factor 10 (ILC/CEPC) 100 FCC-ee

- VBF at multiTeV

- High $x_s(O(1\text{Pb})@6\text{TeV})$ & high lumi better statistics than FCC-ee ?
- Competitive (probably best) measurement of HH production

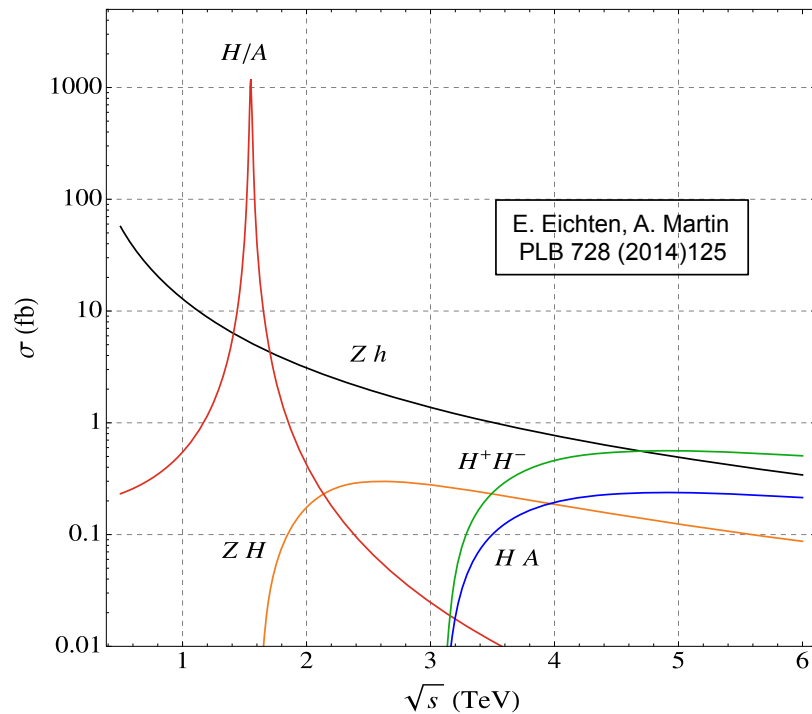
Error on	$\mu\mu$ resonance	ILC	FCC-ee
m_H (MeV)	0.06	30	8
Γ_H (MeV)	0.17	0.16	0.04
g_{Hbb}	2.3%	1.5%	0.4%
g_{HWW}	2.2%	0.8%	0.2%
$g_{H\tau\tau}$	5%	1.9%	0.5%
$g_{H\gamma\gamma}$	10%	7.8%	1.5%
$g_{H\mu\mu}$	2.1%	20%	6.2%
g_{HZZ}	–	0.6%	0.15%
g_{Hcc}	–	2.7%	0.7%
g_{HGG}	–	2.3%	0.8%
BR_{Invis}	–	<0.5%	<0.1%

P. Janot

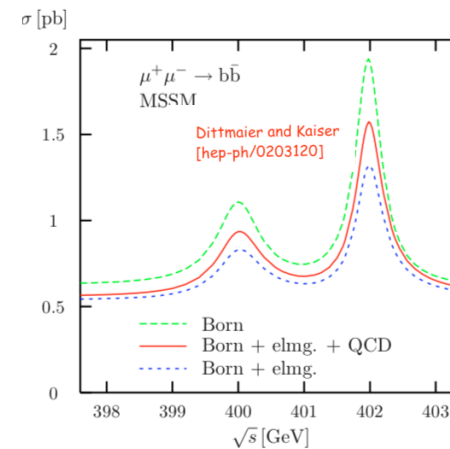
BSM Higgs Physics

M. Antonelli, Padova, July 16th 2015

BSM Higgs boson production



- Resonant H/A production
 $\mu^+ \mu^- \rightarrow H, A$
 2 states separation $\sqrt{s} < 900$ GeV

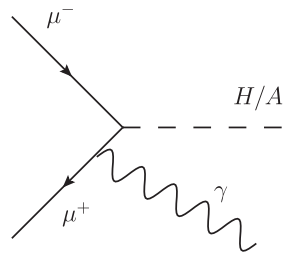


- Pair production like $e^+ e^-$

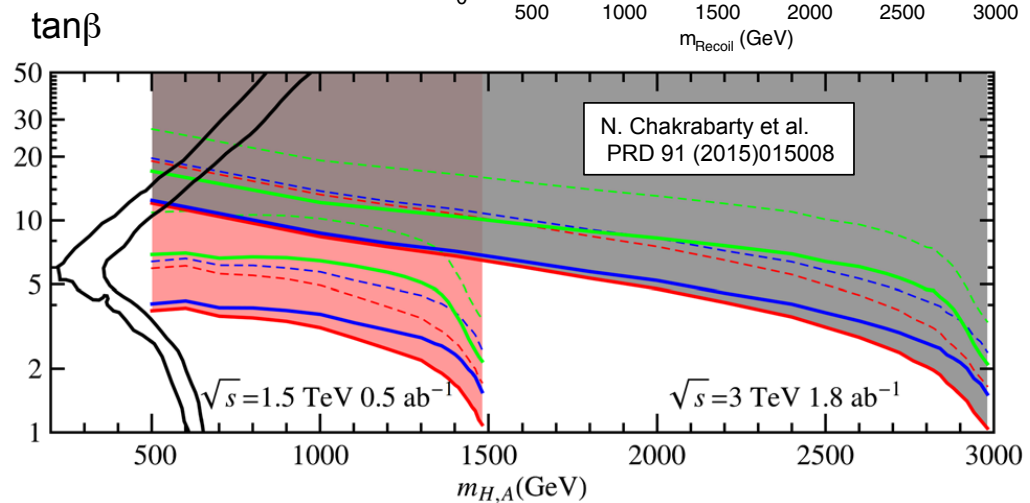
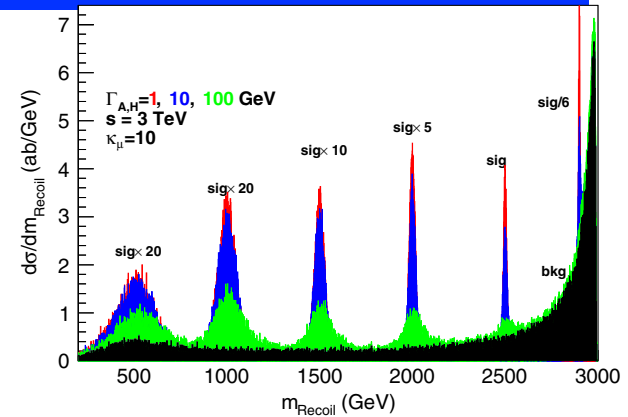
Radiative return H/A production

- Automatic mass scan with radiative returns in $\mu\mu$ collisions

- Select event with an energetic photon
 - Check the recoil mass $m_{\text{Recoil}} = [s - 2E_\gamma\sqrt{s}]^{1/2}$



- Can “see” H and A
 - If $\tan\beta > 5$

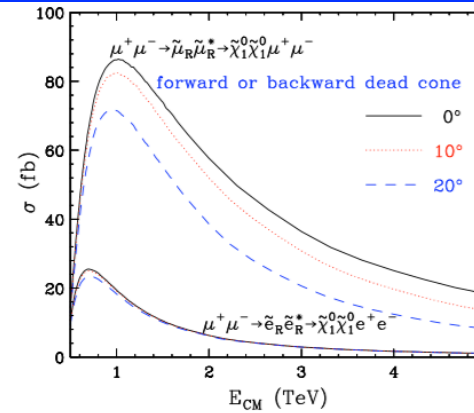


BSM Physics

SUSY

- $\mu^+ \mu^- \rightarrow \tilde{e}_1^+ \tilde{e}_1^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 e^+ e^-$
 - Angular cut at 20° from beam direction:
 - 50% reduction for smuon pairs
 - 20% reduction for selectron pairs
 - Mass measurements using edge method better for MC than CLIC:

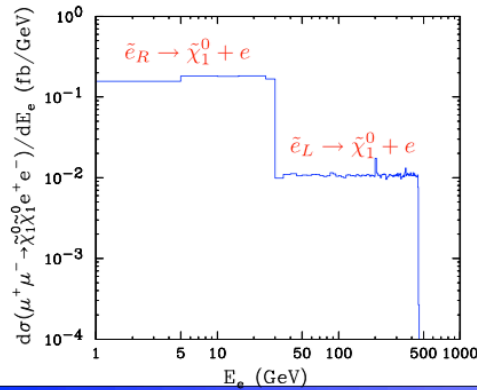
$$E_{\max/\min} = \frac{1}{2} M_{\tilde{e}} \left[1 - \frac{M_{\tilde{\chi}_1^0}^2}{M_{\tilde{e}}^2} \right] \gamma (1 \pm \beta)$$



Effect of beamstrahlung

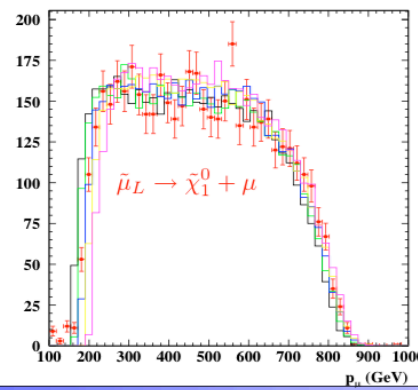
Kong, Winter (MC)

$m_{\tilde{\chi}_1^0} = 212$; $m_{\tilde{e}_R} = 222$; $m_{\tilde{e}_L} = 374$ GeV

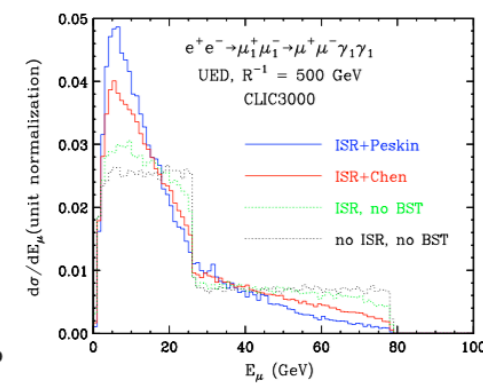


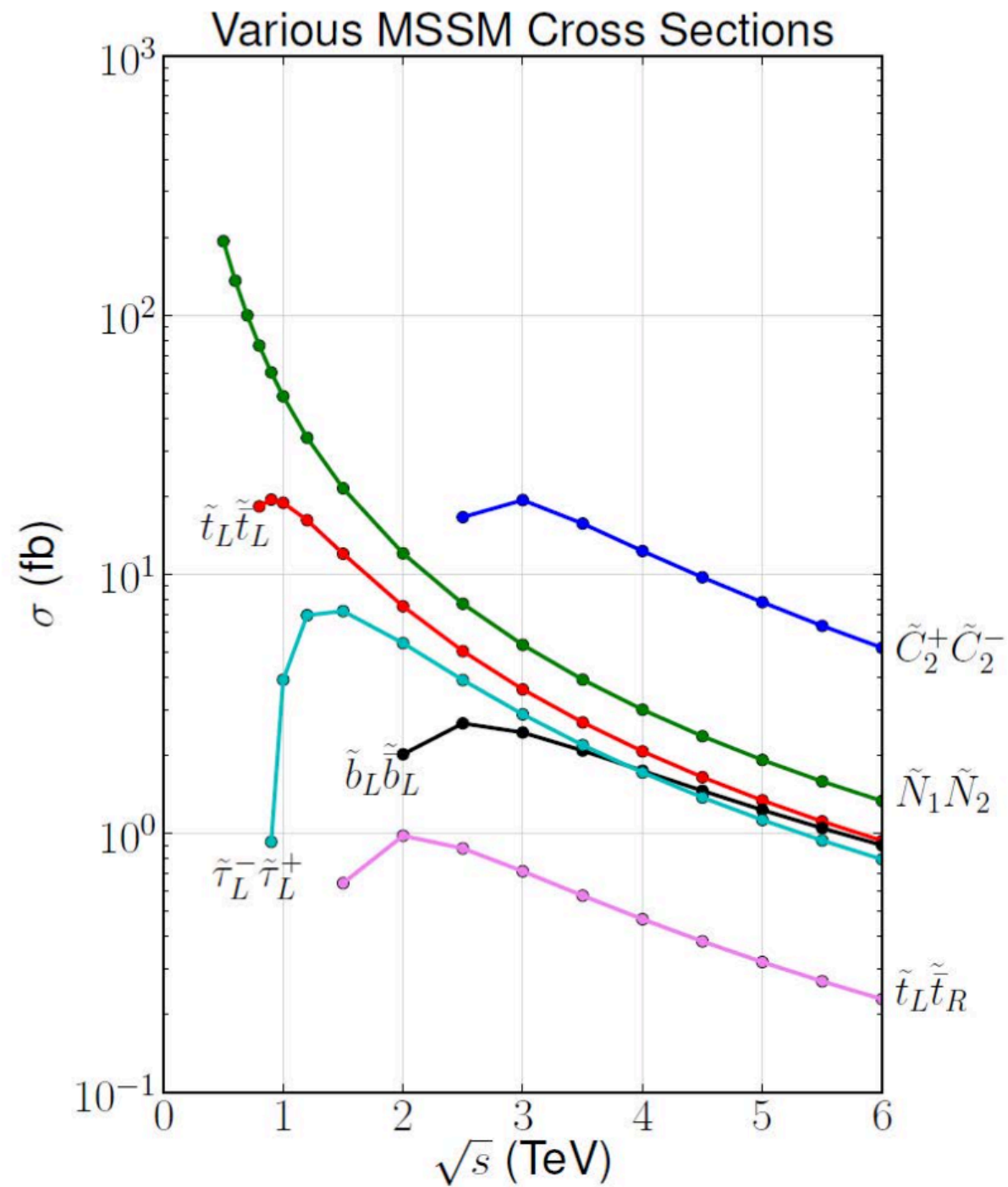
CLIC report (2004)

$m_{\tilde{\chi}_1^0} = 660$ GeV; $m_{\tilde{\mu}_L} = 1150$ GeV



Datta, Kong and Matchev [arXiv:hep-ph/0508161]





Resonances

□ Universal behavior for s-channel resonance

$$\sigma(E) = \frac{2J+1}{(2S_1+1)(2S_2+1)} \frac{4\pi}{k^2} \left[\frac{\Gamma^2/4}{(E-E_0)^2 + \Gamma^2/4} \right] B_{in} B_{out}$$

Convolute with beam resolution ΔE .

If $\Delta E \ll \Gamma$

$$R_{\text{peak}} = (2J+1) 3 \frac{B(\mu^+\mu^-) B(\text{visible})}{\alpha_{\text{EM}}^2}$$

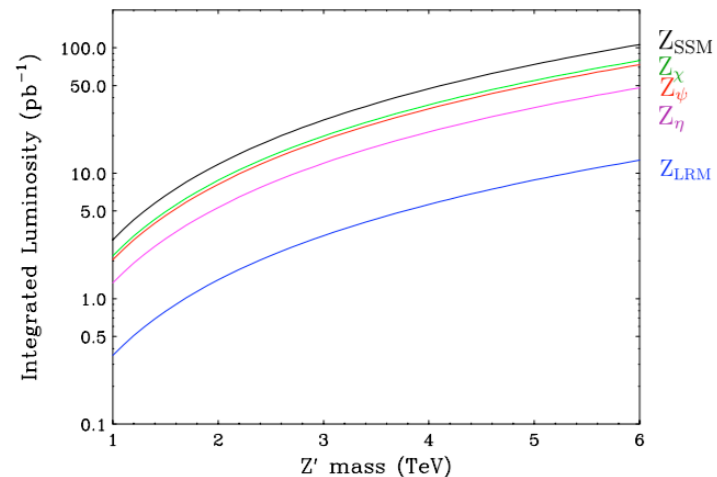
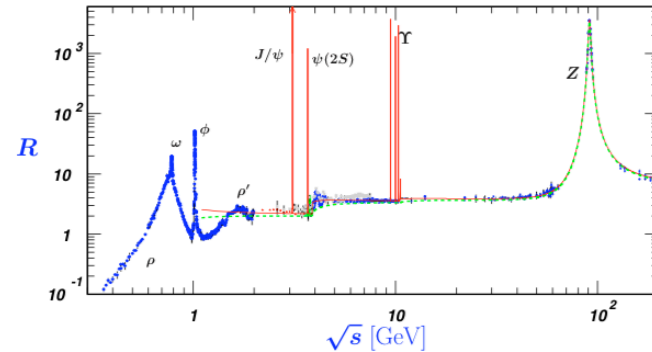
□ Can use to set minimum required luminosity for a muon collider:

- Likely new physics candidates:
 - scalars: h, H^0, A^0, \dots
 - gauge bosons: Z'
 - new dynamics: bound states
 - ED: KK modes
- Example - new gauge boson: Z'
 - SSM, E6, LRM
 - 5σ discovery limits: 4-5 TeV at LHC (@ 300 fb^{-1})

Minimum luminosity at Z' peak:

$$\mathcal{L} = 0.5\text{-}5.0 \times 10^{30} \text{ cm}^{-2} \text{ sec}^{-1}$$

for $M(Z') \rightarrow 1.5\text{-}5.0 \text{ TeV}$



The integrated luminosity required to produce 1000 $\mu^+\mu^- \rightarrow Z'$ events on the peak

Strong dynamics

- Solves the Naturalness Problem: Electroweak Symmetry Breaking is generated dynamically at a nearby scale. May or may not be a light Higgs boson.

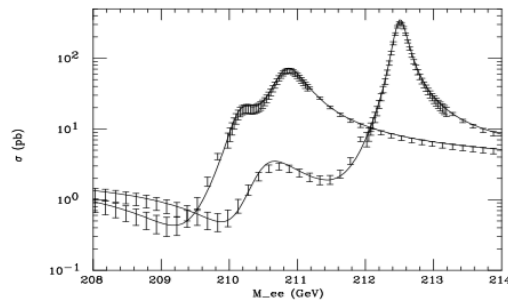
- Theoretical issues**
- What is the spectrum of low-lying states?
 - What is the ultraviolet completion? Gauge group? Fermion representations?
 - What is the energy scale of the new dynamics?
 - Any new insight into quark and/or lepton flavor mixing and CP violation?
 - ...

Technicolor, ETC, Walking TC, Topcolor , ...

For example with a new strong interaction at TeV scale expect:

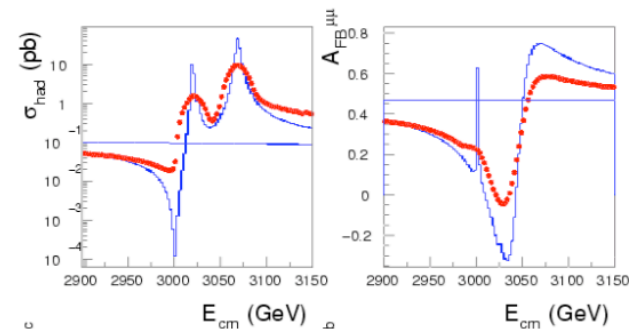
- Technipions - s channel production (Higgs like)
- Technirhos - Nearby resonances (ρ_T, ω_T)- need fine energy resolution of muon collider.

Eichten, Lane, Womersley PRL 80, 5489 (1998)
 $M(\rho_T) = 210 \text{ GeV}$ $M(\omega_T) = 211, 209 \text{ GeV}$
 MC 40 steps (total 1 fb^{-1})



good benchmark processes

CLIC - D-BESS model (resolution 13 GeV)



Extradimensions

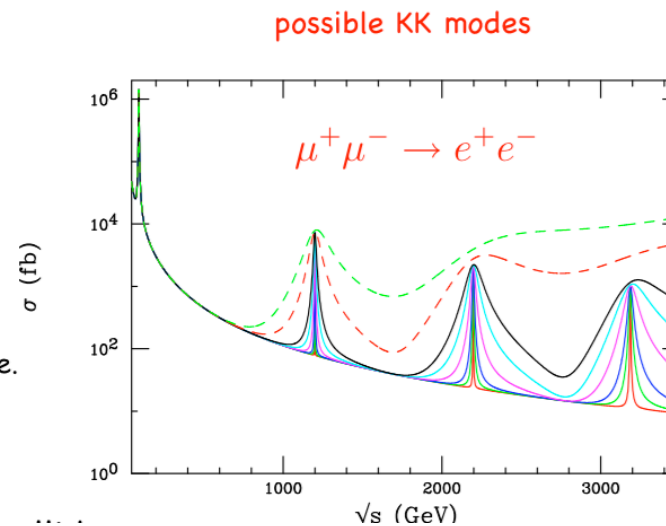
- Solves the Naturalness Problem: The effective GUT scale is moved closer.

Theoretical issues

- How many dimensions?
- Which interactions (other than gravity) extend into the extra dimensions?
- At what scale does gravity become a strong interaction?
- What happens above that scale?
- ...

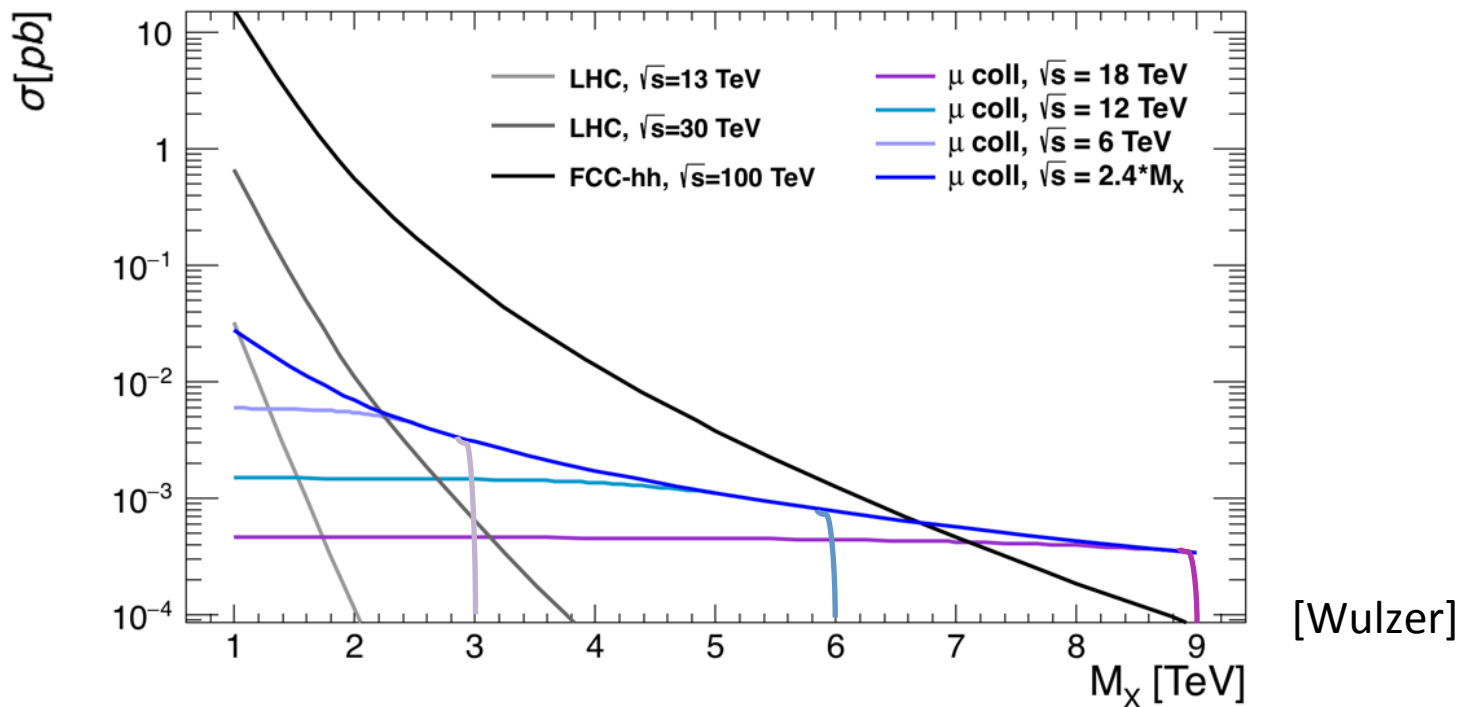
Randall-Sundrum model: warped extra dimensions

- two parameters:
 - ▶ mass scale \propto first KK mode;
 - ▶ width \propto 5D curvature / effective 4D Planck scale.



Muon collider vs hadron collider

- Study the same benchmark used for White Paper:
 - New heavy particles, both colored and EW charged (\sim vector like quarks) \rightarrow xsec can be predicted
 - FCC reach stops at $M_x = 7$ TeV
- Hadron machine pays the price of the exponentially falling PDF \rightarrow multi-TeV muon machine can be competitive!



Experimental environment

1. the luminosity and frequency of crossings are such that
pile-up will not be a problem. Situation better than LHC/CLIC/FCC-hh
2. the main background arises from $\mu \rightarrow e\nu\nu$ decays with off momentum/axis electron radiate or hit material around the detector (low beta point is most achromatic)
 10^{12} muons $\rightarrow 10^9 e^\pm$ produced per turn \rightarrow produce lots of photons and neutrons.

Shielding against these backgrounds is necessary. 10^{-15} cones of tungsten have been proposed seems OK. Never worse than the background at HL-LHC! But much lower physics rates

Much work to do. Situation worse than e^+e^- colliders.

much reduced with the e^+e^- muon source option

3. luminosity measurement with $\mu\mu \rightarrow \mu\mu$ (muon equivalent to Bhabha scattering) has to be done through this shielding (probably OK, needs to be demonstrated)
4. HF design similar to that of ILC/CLIC detectors (beam constraint is more constraining)
5. High energy collider more similar to LHC

U.S. Muon Accelerator Program

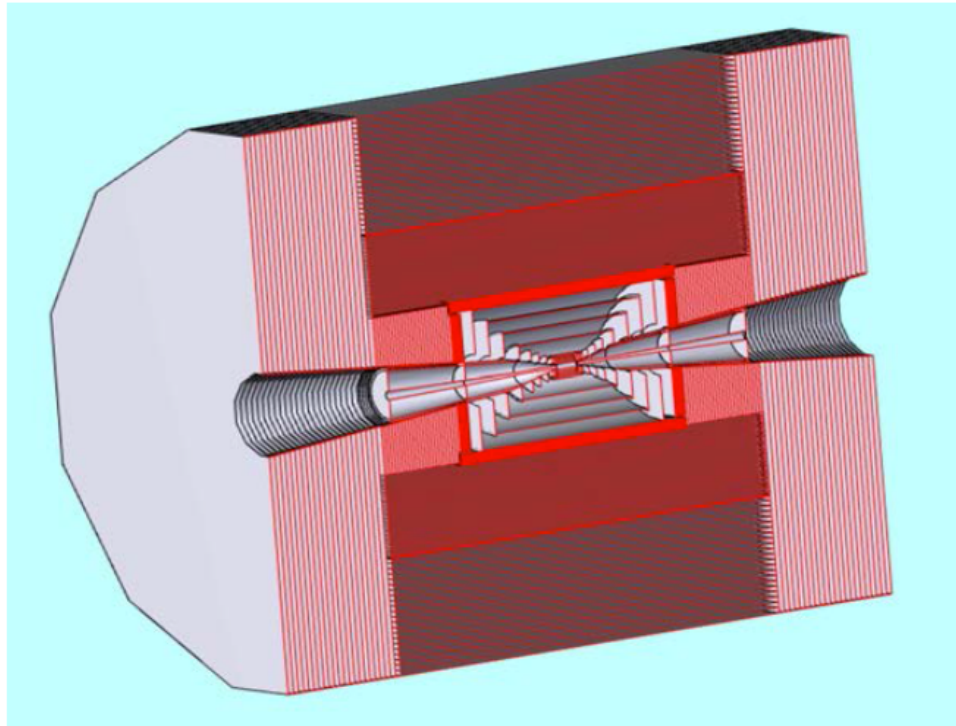
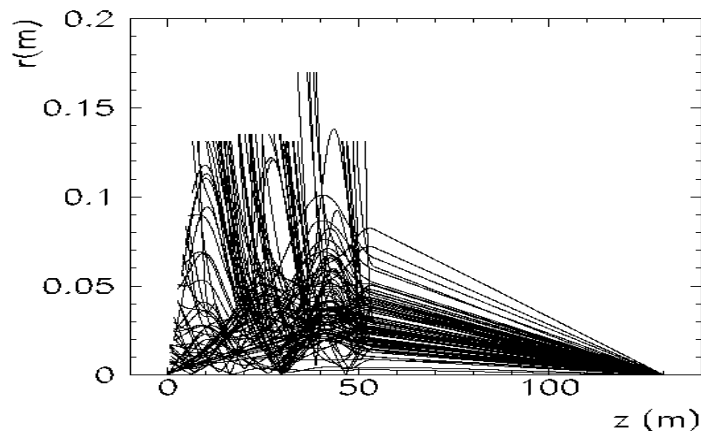
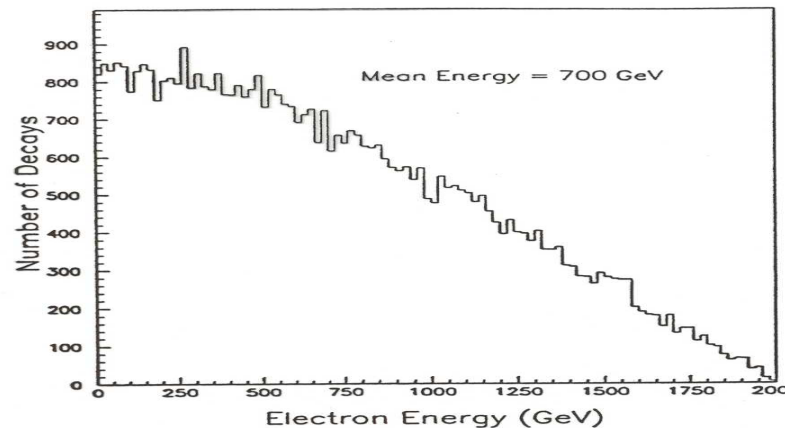


Figure 23: Cross sectional view of a possible Higgs Factory Muon Collider detector showing the tungsten cones shielding the detector from beam related backgrounds.

Background Sources

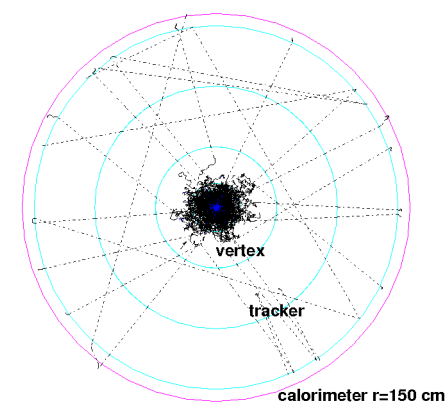
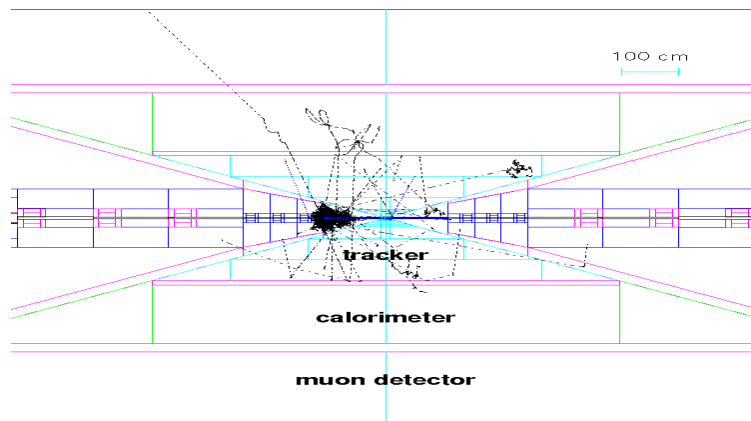
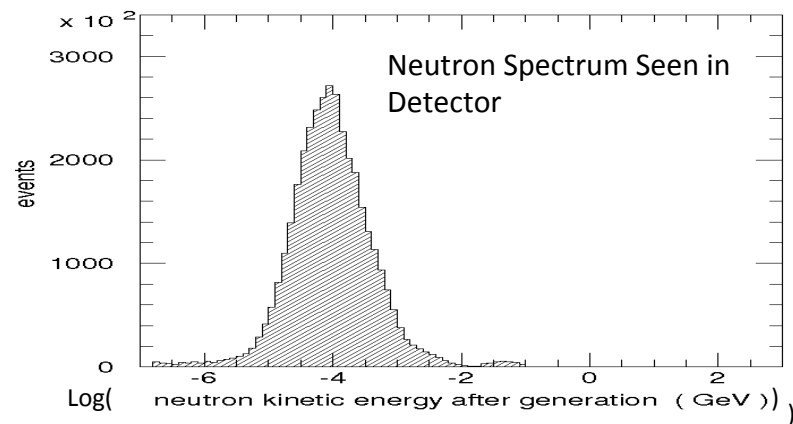
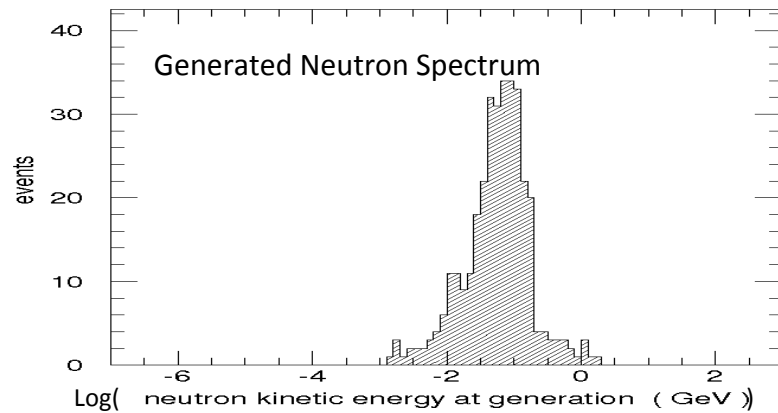
- Muon Decay Background
 - Electron Showers from high energy electrons.
 - Bremsstrahlung Radiation for decay electrons in magnetic fields.
 - Photonuclear Interactions
 - Source of hadrons background.
 - Bethe-Heitler muon production.
- Beam Halo
 - Beam Scraping at 180° from IP to reduce halo. Could it cause some?
 - Collider sources such as magnet misalignments.
- Beam-Beam Interactions.
 - Believed to be small.

Muon Decay Background

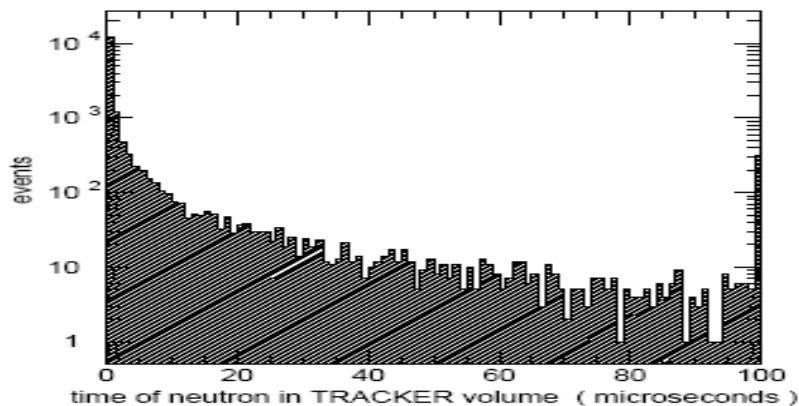
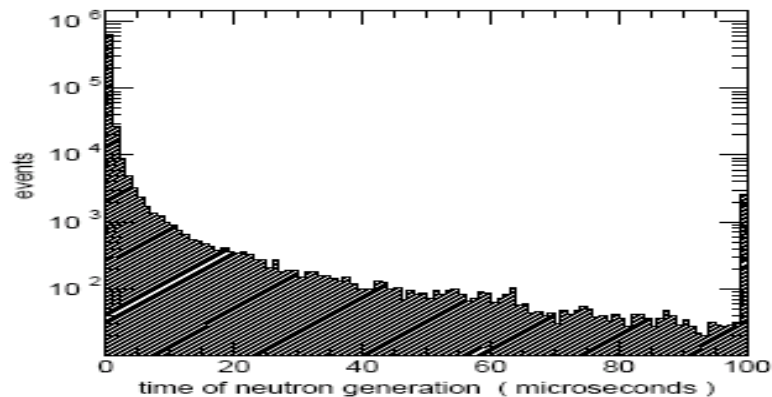


- Upper figure shows electron energy spectrum from decay of 2 TeV muons.
 - 2×10^{12} Muons/bunch in each beam
 - 2.6×10^5 decays/meter
 - Mean Decay Electron energy = 700 GeV
- Lower figure shows trajectories of decay electrons.
 - Electron decay angles are of the order of ~ 10 microradians.
 - In the final focus section, the decay electrons tend to stay in the beam pipe until they see the final focus quad fields.

Neutron Background

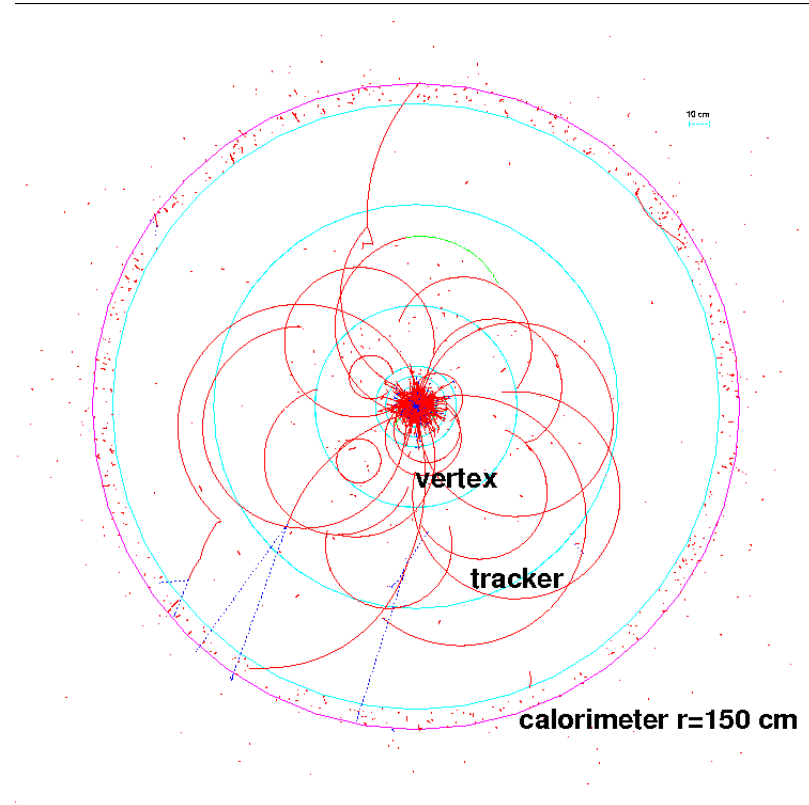
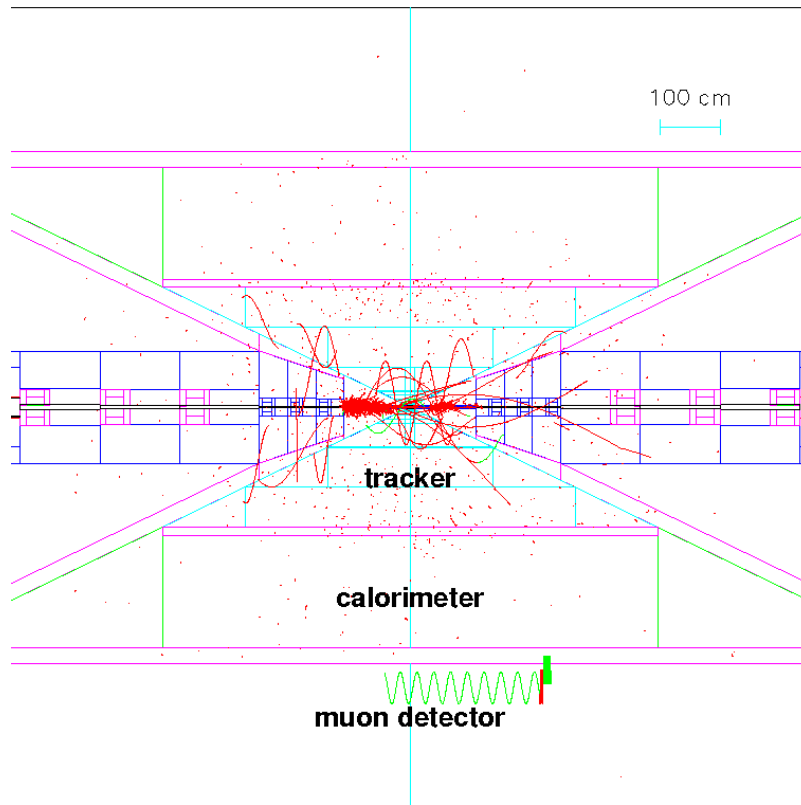


Time Distribution of Neutron Background

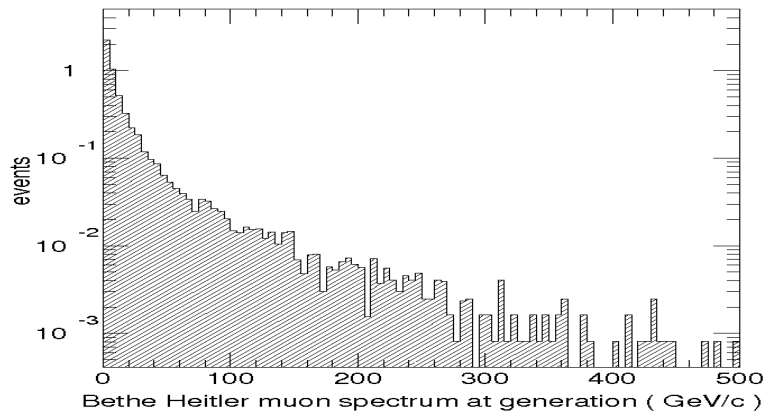


- The top distribution shows the time distribution of the neutron background generated.
- The lower distribution shows the time distribution of the neutron background that is seen in the tracker.
- The neutron flux has fallen by two orders of magnitude before the next bunch crossing (10 μ s later).

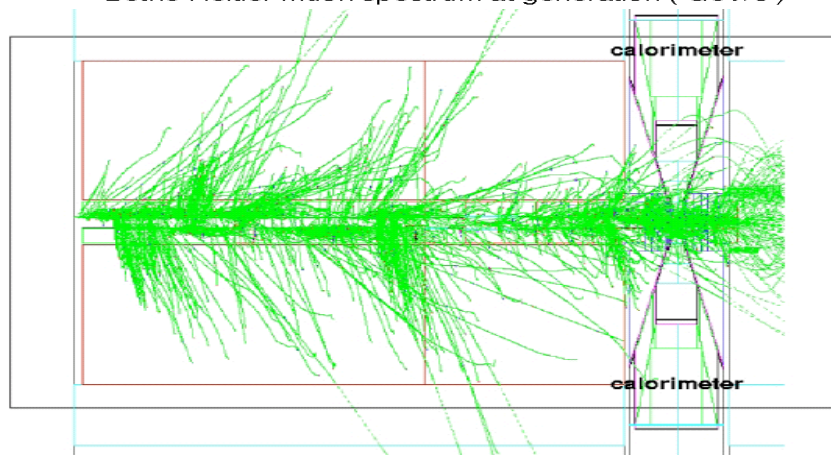
Pion Background in the Detector



Bethe-Heitler Muon Trajectories for the 2x2 TeV Collider



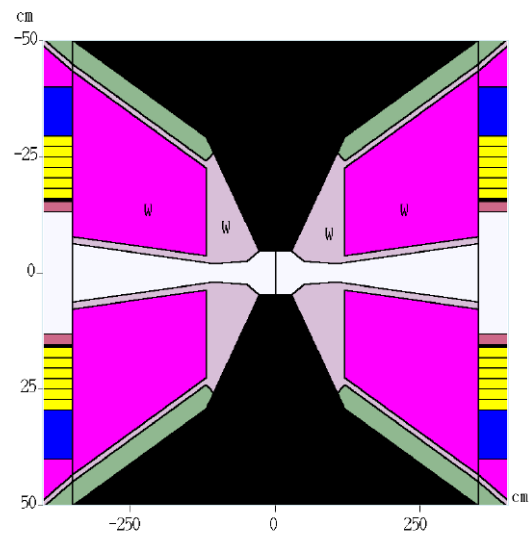
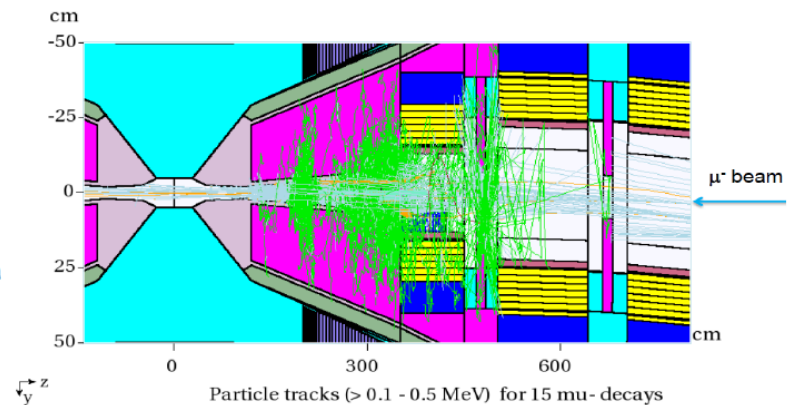
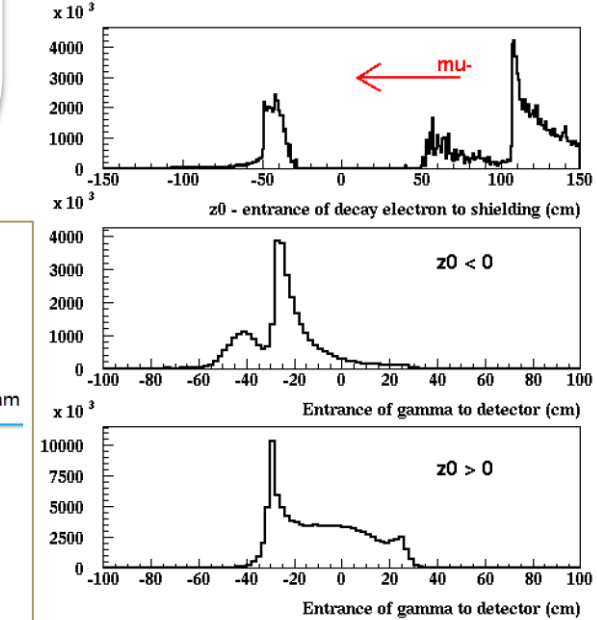
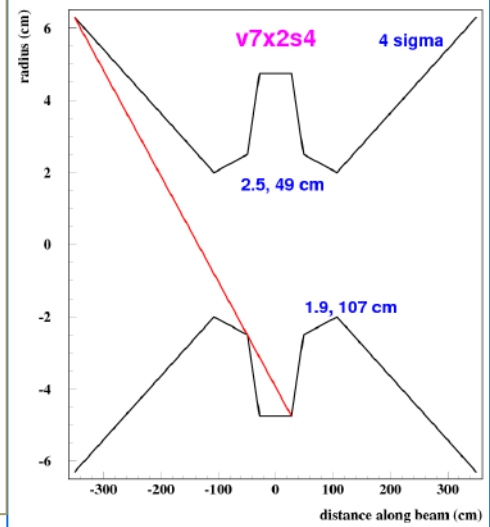
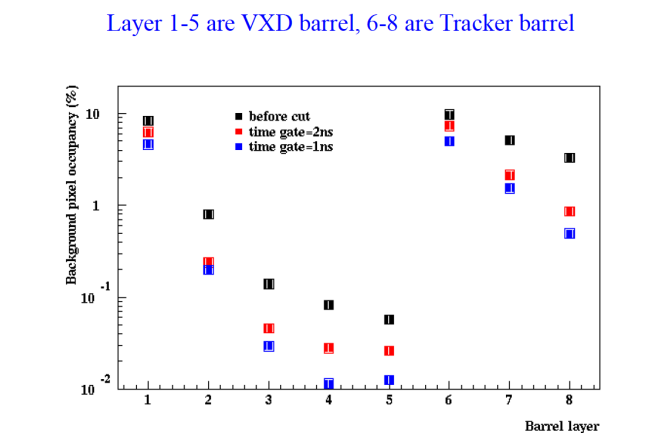
Muon pair production at beam pipe
for example
 $\mu N \rightarrow \mu\mu^+\mu^-N$
 $eN \rightarrow e\mu^+\mu^-N$
(electrons are more likely to hit beam pipe).



Machine Detector Interface

- ✓ Backgrounds appear manageable with suitable detector pixelation and timing rejection
- ✓ Recent study of hit rates comparing MARS, EGS and FLUKA appear consistent to within factors of <2
- ⇒ Significant improvement in our confidence of detector performance

Pixel occupancy in barrel vs timing cuts.
Pixel - 20x20 μm in VXD and 1000x100 μm in Tracker



Conclusion

- **Higgs Factory (~125 GeV)**
 - Very precise determinations of mh and Γ_h
 - Test of Higgs $\mu\mu$ coupling
- **Higgs physics at higher energies**
 - ZH \sim factor 10 in accuracy worse wrt FCCee (2 wrt ILC/CEPC)
 - Very promising H and HH σ values at MultiTeV
(need to be studied)
- **BSM physics**
 - Explore very high energy frontier with pair production (provided sufficient luminosity) up to ?
 - Best for new resonances (negligible beamstrahlung, reduced ISR) additional Higgs bosons in particular
 - BSM in VBF not studied yet