

V workshop italiano sulla fisica p-p ad LHC

Perugia, 30 Gennaio - 2 Febbraio

B-Physics: Theoretical Predictions in the LHC Era

- Theoretical Approach and Tools
- State of the art of the theoretical predictions

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Flavour Physics:

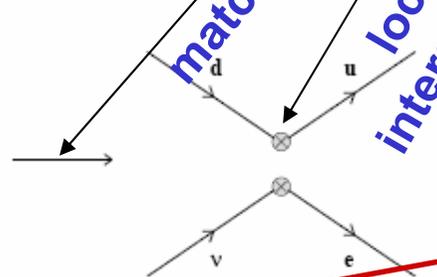
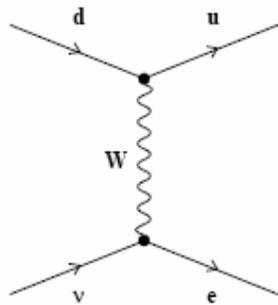
- precision tests of the Standard Model (SM) → Unitarity Triangle (uncert. ~few%)
- search for New Physics (NP) → Interplay with Direct Searches [see Paride's discussion]

Theoretical Approach to Weak Decays of Hadrons (including the effects of strong interactions)

→ occurring well below the electroweak scale

$$H_{\text{eff}} = \frac{G_F}{\sqrt{2}} V_i^{\text{CKM}} C_i(\mu) Q_i(\mu)$$

(e.g. β -decay)



- **perturbative QCD corrections** [up to NNLO (e.g. $b \rightarrow s\gamma$, $b \rightarrow s l^+ l^-$)]
- + Renormalization Group to resum large $\ln^n(M_W/\mu)$
- affected by **NP**

$C_i(\mu)$: **Wilson coefficients** (short-distance)
 $Q_i(\mu)$: **local operators** (long-distance)

- **non-perturbative QCD contributions** [main source of theoretical uncertainty]

Beyond the SM

$$\begin{aligned}
 H_{\text{eff}}^{\text{NP}} = \frac{G_F}{\sqrt{2}} \cdot & \left[V_i^{\text{CKM}} \left(C_i^{\text{NEW}}(\mu) Q_i(\mu) + C_i^{\text{MFV}}(\mu) Q_i^{\text{MFV}}(\mu) \right) \right. \\
 & \left. + V_i^{\text{non-MFV}} C_i^{\text{non-MFV}}(\mu) Q_i^{\text{non-MFV}}(\mu) \right]
 \end{aligned}$$

within MFV

beyond MFV

Minimal Flavour Violation (MFV): supported by the great success of the SM in Flavour Physics!

the SM Yukawa couplings are the only *building-blocks* of flavour violation

[G.D'Ambrosio et al., hep-ph/0207036], [A.J. Buras et al., hep-ph/0007085]

Beyond MFV:

New sources of flavour violation ($V_i^{\text{non-MFV}}$) can appear

New operators (Q_i^{MFV} , $Q_i^{\text{non-MFV}}$) can appear but their (long-distance) matrix elements are not affected by NP

Some Appealing NP Models

MFV

MSSM with MFV

(boson-fermion symmetry, minimal spectrum (sparticles, 2 Higgs doublets, $\tan\beta=v_u/v_d$), R-parity)

Appelquist-Cheng-Dobrescu (ACD) Model

(1 universal extra-dimension \rightarrow SM particles propagate in 5 dimensions, in 4 dimensions Kaluza-Klein modes appear, KK—Parity conservation, only one additional free parameter: $1/R$)

Beyond MFV

MSSM with a general Flavour Structure

27 new Flavour Changing couplings along the squark lines)

Littlest Higgs with T-Parity (LHT)

(Higgs= Goldstone boson of a spontaneously broken global symmetry

$SU(5) \xrightarrow{f} SO(5)$, heavy partners (W_H, Z_H, A_H, T, Φ)

+ a discrete symmetry (T-Parity) \rightarrow heavy particles forbidden at tree-level

(to soften ew precision constraints: $f > 500\text{GeV}$)

new mirror fermions with new flavour interactions)

Theorist's Golden Modes

Suppression within the SM



Sensitivity to NP

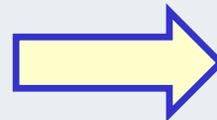
•FCNCs forbidden at tree-level in the SM

(radiative and rare decays: $b \rightarrow (s,d) \gamma$, $b \rightarrow (s,d) t\bar{t}$, $b \rightarrow s\nu\bar{\nu}$, $B_{d,s} \rightarrow t\bar{t}, \dots$)

•CKM-, helicity-suppression

(semileptonic CP-asymmetry: A_{SL}^s, \dots , t-dep. CP-asymmetries: $A_{CP}(B \rightarrow K^* \gamma), \dots$)

Small hadronic uncertainties



Theoretically clean

•At most one hadron in the final state

(leptonic and semileptonic decays: $B_{d,s} \rightarrow t\bar{t}$, $b \rightarrow (s,d) t\bar{t}$, $b \rightarrow s\nu\bar{\nu}, \dots$)

•Smearing of bound-effects in the final state

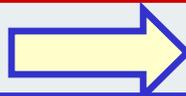
(Inclusive quantities: lifetimes, ΔM_q , $\Delta\Gamma_q/\Gamma_q$, A_{SL}^q , ϕ_s, \dots)

•Suppression/cancellation of some hadronic uncertainties

(clean dominant contributions, peculiar ratios/correlations: $A_{CP}(B \rightarrow J_\psi K_S)$, $\Delta M_s/\Delta M_d, \dots$)

Hadronic Matrix Elements: Theoretical Tools

$\langle Q_i \rangle$: long-distance



Non-perturbative methods

Lattice QCD: True theory (QCD) simulated on a finite and discrete space-time. Physical results require continuum and infinite volume limits, and extrapolations to the physical masses. Recent simulations are unquenched ($N_f=2, 2+1$). Typical uncertainties are of $O(10-15\%)$

Significant improvements are expected thanks to increasing computational power, improved algorithms and theoretical approaches
→ larger volumes, finer lattices, lower masses,...

Sum Rules: based on correlation function analyses and dispersion relations, require phenomenological inputs and model-dependent ansatz.

Useful predictions, mainly for quantities not calculated yet on the Lattice.
Uncertainties difficult to be estimated.

Effective Theories

- ChPT (light hadrons),
- HQET (heavy-light hadrons),
- NRQCD (heavy-heavy hadrons),
- SCET (heavy to light decays)

+

Factorization

approximation for non-leptonic or exclusive matrix elements
 $\langle M_1 M_2 | Q_i | B \rangle \sim \langle M_1 | J_i^a | B \rangle \langle M_2 | J_i^b | 0 \rangle + \text{corr. in } \Lambda_{\text{QCD}}/m_b, \alpha_s$
(pert. kernels, non-pert. distr. amplit. and form factors)

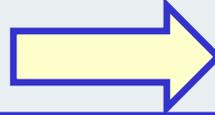
Perturbative QCD (PQCD)

to separate hard perturbative components from non-perturbative ones enclosed in hadron wave functions (from exp.)

B-Physics

Advantages

$$m_b \gg \Lambda_{\text{QCD}}$$



$$\alpha_s(m_b) \sim 10^{-1}$$

Heavy Quark Symmetry (HQS):

soft gluons do not resolve spin and flavour on scales $\sim 1/m_b \rightarrow$
invariance of strong interactions under heavy spin-flavour $SU(2N_h)$

Heavy Quark Effective Theory (HQET):

describes an heavy quark almost on-shell
through an expansion in $p/m_b \sim \Lambda_{\text{QCD}}/m_b$

Heavy Quark Expansion (HQE):

Operator product expansion of physical quantities
in series of Λ_{QCD}/m_b to separate short- and long-distance effects

Soft Collinear Effective Theory (SCET):

describes heavy to light hadron decays,
including both soft and collinear gluon modes

Interest
(at the LHC)

Angles of the UT

α : $B \rightarrow \pi\pi$, $B \rightarrow \rho\rho$, $B \rightarrow \rho\pi$
 β : $B \rightarrow J_\psi K_S$, ...
 γ : $B \rightarrow DK$, $B \rightarrow DK^*$, $B \rightarrow D^*K$

$B_s - \bar{B}_s$ Mixing

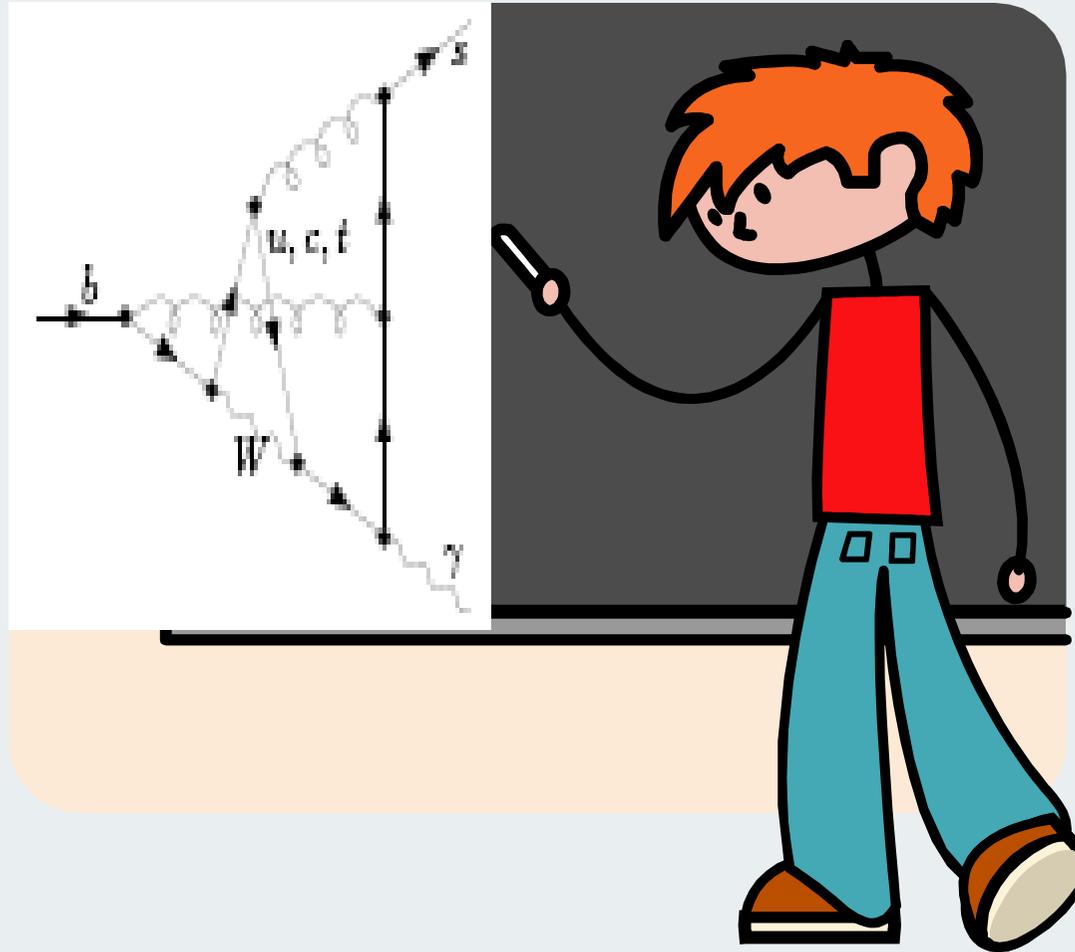
$\Delta\Gamma_s/\Gamma_s$, A_{SL}^s , ϕ_s
 ΔM_s , lifetimes

Radiative and rare decays

$b \rightarrow (s,d) \gamma$ (incl. and excl.)
 $B_{d,s} \rightarrow t\bar{t}$
 $b \rightarrow (s,d) t\bar{t}$ (incl. and excl.)

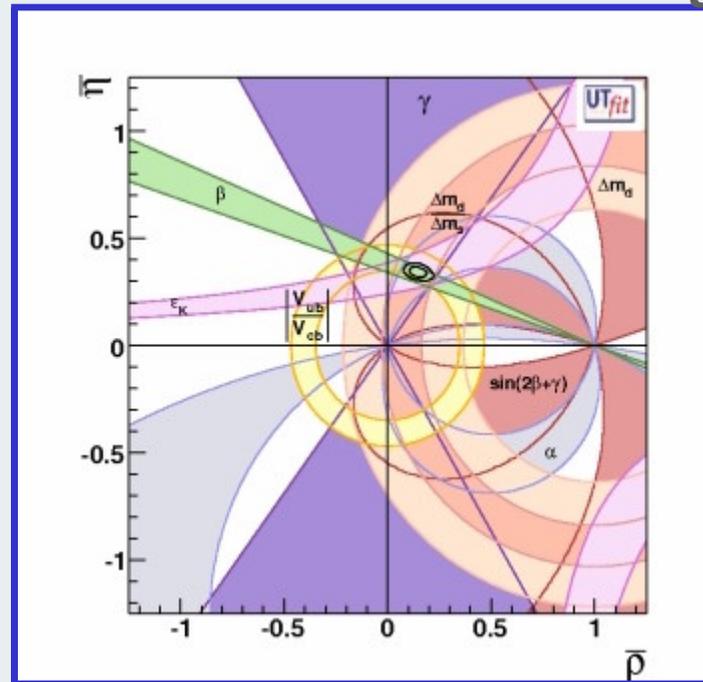
rapid oscillations can be studied
at LHC thanks to large boost!

State of the art of the theoretical predictions in B-Physics



Angles of the Unitarity Triangle

www.utfit.org



- **Great success of the SM**
- **High level of precision (~few %)**
- **Agreement among side and angle measurements**

All 3 angles can be determined from B decays

Improving the (NP-free) determinations of CKM elements is a key ingredient to improve the SM predictions in processes sensitive to NP

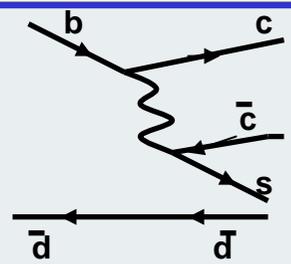
$$\beta(\phi_1)$$

$$V_{td} = |V_{td}| e^{-i\beta}$$

Golden mode: $B \rightarrow J_\psi K_S$

Dominated by one tree-level amplitude $b \rightarrow c\bar{c}s$

Simple expression for the t-dep. CP-asymmetry
 $A_{CP}(t) = -\sin 2\beta \sin(\Delta M_d t)$



Main theoretical uncertainty from the hadronic matrix elements of the CKM-suppressed $b \rightarrow u\bar{u}s$ contribution (irreducible theory error $\sim 1\%$)

- **Similar simplification in other $b \rightarrow c\bar{c}s$ channels:** $\Psi(2S)K_S, \chi_{c1} K_S, \eta_c K_S, J_\psi K_L, J_\psi K^*, B_s \rightarrow \Psi\phi$
- **Alternative determinations (sensitive to NP) from the charmless $b \rightarrow s$ one-loop (penguin) amplitude:** $B \rightarrow \eta' K_{S,L}, B \rightarrow \phi K_S$
- **$\cos 2\beta$ from a time-dep. analysis of $B \rightarrow J_\psi K^*, B \rightarrow D \pi^0$** ($\cos 2\beta > 0$ solving the $\beta \leftrightarrow (\pi/2 - \beta)$ ambiguity)

$$(\sin 2\beta)_{\text{HFAG}} = 0.681 \pm 0.025$$

in slight tension with the result from the UT analysis

$$(\sin 2\beta)_{\text{UTfit}} = 0.744 \pm 0.039$$

from all other INFOS

model-dependence in the non-pert. threshold region

due to the high value

$$|V_{ub}^{\text{incl}}| = 43.1(3.9) \cdot 10^{-4}$$

$$|V_{ub}^{\text{excl}}| = 34.0(4.0) \cdot 10^{-4}$$

[HFAG, 200...]

Recently

[U.Aglietti et al., 0711.0860]:

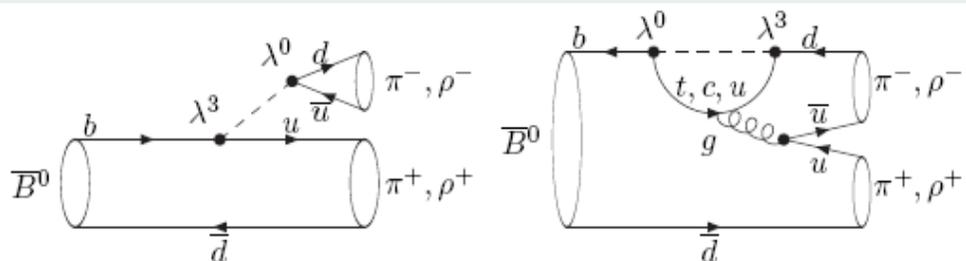
$$|V_{ub}^{\text{incl}}| = 36.9(1.3)(3.1) \cdot 10^{-4}$$

from a different modelling of the threshold region

$\alpha(\phi_2)$

$$\alpha = \arg \left[- \frac{V_{td} V_{tb}^*}{V_{ud} V_{ub}^*} \right]$$

from charmless decays: $B \rightarrow \pi\pi$, $B \rightarrow \rho\rho$, $B \rightarrow \rho\pi$
 (\leftrightarrow tree-level transition $b \rightarrow u\bar{u}d$ carrying V_{ub})



The penguin contribution, introducing different CKM factors, complicate the extraction of α :
tree-penguin disentanglement is required

Analysis of a **large set of observables**:
 Br 's, $A_{CP}(t)$ both in neutral and charged B decays

$B \rightarrow \pi\pi$: isospin analysis [M.Gronau, D.London,1990] + info from $Br(B_s \rightarrow K^+K^-)$ [M.Bona et al (UTfit), hep-ph/0701204]
 $B \rightarrow \rho\rho$: advantage of the suppression of $Br(B \rightarrow \rho^0\rho^0)$ and of the related uncertainty
 $B \rightarrow \rho\pi$: advantage of $\rho^+\pi^-$ and $\rho^-\pi^+$ reachable by both B^0 and \bar{B}^0 , no model-dependance for the strong phase
 [A.E.Snyder, H.R.Quinn,1993]

M.Bona et al. [UTfit coll.],
 hep-ph/0501199

$$(\alpha)_{dir.} = (91 \pm 8)^\circ$$

Main theoretical uncertainty
 from **isospin violations**
 mainly in ew penguins and FSI
 (irreducible theory error few%)

in perfect agreement
 with the result
 from the UT analysis

$$(\alpha)_{UTfit} = (91 \pm 6)^\circ$$

from all
 other INFOS

Similar results from a
 frequentist approach

the unphysical $\alpha \approx 0$ region
 is ruled out by simple arguments
 on the hadronic matrix elements!

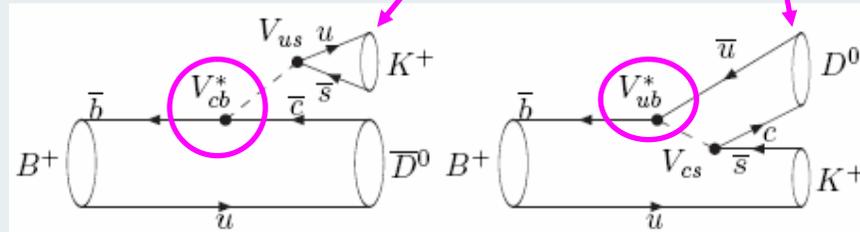
M.Bona et al. [UTfit coll.], hep-ph/0701204

$$\gamma(\phi_3)$$

$$V_{ub} = |V_{ub}| e^{-i\gamma}$$

Determination of γ from $B \rightarrow DK$ decays: [I.I.Y. Bigi, A.I. Sanda, 1988, A.B. Carter, A.I. Sanda, 1988]

- $B^+ \rightarrow DK^+$ can produce both D^0 and \bar{D}^0 , via $\bar{b} \rightarrow \bar{c} u \bar{s}$ and $\bar{b} \rightarrow \bar{u} c \bar{s}$
- D^0 and \bar{D}^0 can decay to a common final state
- The two amplitudes interfere with a relative phase $\delta_B \pm \gamma$, for $B^+(B^-)$



Main contributions from (theoretically clean) tree-level diagrams

Remaining theoretical uncertainty from **simplifying** D-D mixing neglection (irreducible theory error 0.1%)

Various methods consider different final states:

- CP-eigenstates (Gronau, London, Wyler [GLW]) ($\pi^+\pi^-$, K^+K^- , $K_S\pi^0$, $K_S\phi$, $K_S\omega$, ...)
- doubly Cabibbo suppressed D modes (Atwood, Dunietz, Soni [ADS]) ($K^+\pi^-$, $K^+\rho^-$, $K^*\pi^-$, ...)
- three-body D decaying modes (Dalitz plot analysis) ($K_S\pi^+\pi^-$ provides the best estimate at present)

[A. Giri, hep-ph/0303187]

The best strategy is a combined analysis taking into account many D and D* modes

M. Bona et al. [UTfit coll.],
hep-ph/0501199

$$(\gamma)_{\text{dir.}} = (88 \pm 16)^\circ$$

compatible
with the result
from the UT analysis

$$(\gamma)_{\text{UTfit}} = (65.1 \pm 6.5)^\circ$$

from all other INFOS

Similar results from a frequentist approach [CKMfitter]

B_q- \bar{B}_q Mixing

oscillation

$$\hat{H} = \hat{M} - \frac{i}{2} \hat{\Gamma}$$

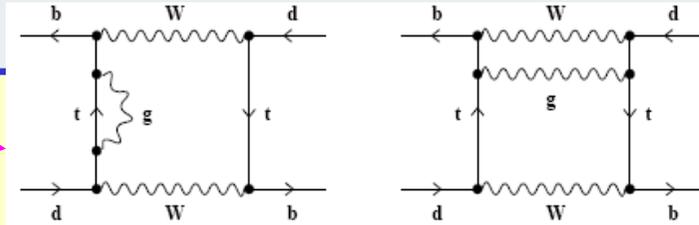
$$\hat{M} = \begin{pmatrix} M_{11} & M_{12} \\ M_{12}^* & M_{11} \end{pmatrix} \quad \hat{\Gamma} = \begin{pmatrix} \Gamma_{11} & \Gamma_{12} \\ \Gamma_{12}^* & \Gamma_{11} \end{pmatrix}$$

decay

Eigenstates:

$$|B_q^{L,H}\rangle = \frac{1}{\sqrt{1 + |(q/p)_q|^2}} \left(|B_q^0\rangle \mp (q/p)_q |\bar{B}_q^0\rangle \right)$$

- **Oscillation** \leftrightarrow **box-diagrams**
- **Wilson coeff. at NLO in QCD** [A.J.Buras et al., 1990]
- **Matrix elements from Lattice QCD**
(f_{Bq} and B_{Bq} with uncert. <15%) [see M.Della Morte, Lattice07 Proceedings]

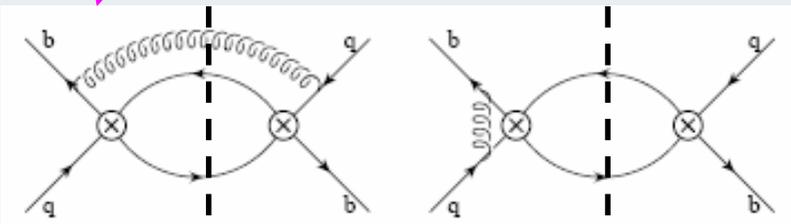


$$\Delta M_q = M_{B_H^q} - M_{B_L^q} = 2 |M_{12}^q|$$

- **Decay** \leftrightarrow **cut diagrams**
- **Wilson coeff. at NLO in QCD and**
 $O(\Lambda_{QCD}/m_b)$ **in the HQE**
- **Matrix elements from Lattice QCD**
+VSA for some subleading operators
(main source of theoretical uncertainty)

$$\Gamma_{B_q} = \Gamma_{11}^q \quad \Delta B=0 \text{ transition}$$

[see C.T., hep-ph/0702235]



$$\Delta \Gamma_q = \Gamma_{B_L^q} - \Gamma_{B_H^q} = -2 |M_{12}^q| \text{Re} \left(\frac{\Gamma_{12}^q}{M_{12}^q} \right)$$

$$A_{SL}^q = -2 \left(\left| \frac{q}{p} \right| - 1 \right) = \text{Im} \left(\frac{\Gamma_{12}^q}{M_{12}^q} \right)$$

$\Delta B=2$ transition

Lifetime Ratios

Theoretical predictions:

$$\frac{\tau(B^+)}{\tau(B_d)} = 1.06 \pm 0.02, \quad \frac{\tau(B_s)}{\tau(B_d)} = 1.00 \pm 0.01, \quad \frac{\tau(\Lambda_b)}{\tau(B_d)} = 0.88 \pm 0.05$$

[E.Franco, V.Lubicz, F.Mescia, C.T. hep-ph/0310241, C.T. hep-ph/0702235]

Experimental averages:

$$\frac{\tau(B^+)}{\tau(B_d)} = 1.071 \pm 0.009, \quad \frac{\tau(B_s)}{\tau(B_d)} = 0.939 \pm 0.021, \quad \frac{\tau(\Lambda_b)}{\tau(B_d)} = 0.921 \pm 0.036$$

[HFAG, 2007]

Larger than the 2006 average
due to the new **CDF** measurement
(3.2 σ above the previous average)

Width Differences and Semileptonic CP-Asymmetries

Theoretical predictions:

$$\frac{\Delta\Gamma_d}{\Gamma_d} = (3.6 \pm 1.0) \cdot 10^{-3}, \quad \frac{\Delta\Gamma_s}{\Gamma_s} = (11 \pm 4) \cdot 10^{-2}$$

[M.Ciuchini, E.Franco, V.Lubicz, F.Mescia, C.T. hep-ph/0308029,
M.Beneke et al. hep-ph/0307344, A.Lenz, U.Nierste hep-ph/0612167,
C.T. hep-ph/0702235]

Experimental averages:

$$\frac{\Delta\Gamma_d}{\Gamma_d} = (9 \pm 37) \cdot 10^{-3}, \quad \frac{\Delta\Gamma_s}{\Gamma_s} = (12.1_{-9.0}^{+8.3}) \cdot 10^{-2}$$

[HFAG, 2007]

- Quite large uncertainties (due to **large NLO** and $O(\Lambda_{\text{QCD}}/m_b)$ contributions that induce strong **cancellations**)
- **Average of results in two operator bases**
(significant differences reflect relevant $O(\alpha_s^2)$ and $O(\alpha_s \Lambda_{\text{QCD}}/m_b)$ corrections)

Theoretical predictions:

$$A_{\text{SL}}^d = -(6.4 \pm 1.6) \cdot 10^{-4}, \quad A_{\text{SL}}^s = (2.7 \pm 0.6) \cdot 10^{-5}$$

[M.Ciuchini, E.Franco, V.Lubicz, F.Mescia, C.T. hep-ph/0308029,
M.Beneke et al. hep-ph/0307344, A.Lenz, U.Nierste hep-ph/0612167,
C.T. hep-ph/0702235]

Experimental averages:

$$A_{\text{SL}}^d = -(5 \pm 56) \cdot 10^{-4}, \quad A_{\text{SL}}^s = -(300 \pm 1010) \cdot 10^{-5}$$

[HFAG, 2007]

Mass Difference

Theoretical prediction:

$$(\Delta M_s)_{\text{dir}}^{\text{SM}} = (17.8 \pm 4.8) \cdot \text{ps}^{-1} \quad [\text{M.Blanke, A.Buras, D.Guadagnoli, C.T. hep-ph/0604057}]$$

$$(\Delta M_s)_{\text{UTfit}} = (17.5 \pm 2.1) \cdot \text{ps}^{-1} \quad [\text{UTfit, www.utfit.org}]$$

Main source of th. unc.

$$f_{B_s} \sqrt{B_{B_s}} = 262(35) \text{ MeV (Lattice)} \quad [\text{S.Hashimoto hep-ph/0411126}]$$

In agreement with the **precise exp. determination**

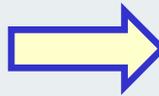
$$f_{B_s} \sqrt{B_{B_s}} = 257(6) \text{ MeV (UTA within SM)} \quad [\text{M.Bona et al. (UTfit), hep-ph/0606167}]$$

Experimental measurement:

$$(\Delta M_s)^{\text{exp.}} = (17.77 \pm 0.10 \pm 0.07) \cdot \text{ps}^{-1} \quad [\text{CDF hep-ex/0609040}]$$

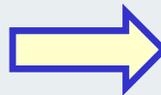
Sensitivity to NP

Γ_{12}^q describes **decay**
(to SM particles only)

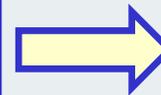


Insensitive to NP

M_{12}^q describes **oscillation**
through box-diagrams



Sensitive to NP



$$M_{12}^q = (M_{12}^q)_{SM} C_{B_q} e^{2i\phi_{B_q}}$$

beyond MFV

$$\frac{\Delta\Gamma_q}{\Gamma_q} = -\left(\frac{\Delta M_q}{\Gamma_q}\right)^{\exp} \left[\text{Re}\left(\frac{\Gamma_{12}^q}{M_{12}^q}\right)^{SM} \frac{\cos 2\phi_{B_q}}{C_{B_q}} - \text{Im}\left(\frac{\Gamma_{12}^q}{M_{12}^q}\right)^{SM} \frac{\sin 2\phi_{B_q}}{C_{B_q}} \right]$$

$$A_{SL}^q = \left[\text{Im}\left(\frac{\Gamma_{12}^q}{M_{12}^q}\right)^{SM} \frac{\cos 2\phi_{B_q}}{C_{B_q}} - \text{Re}\left(\frac{\Gamma_{12}^q}{M_{12}^q}\right)^{SM} \frac{\sin 2\phi_{B_q}}{C_{B_q}} \right]$$

In B_s : $\text{Re} \gg \text{Im}$



Even a small $\phi_{B_s} \equiv \phi_s/2$
can be seen in A_{SL}^s

ϕ_s appears in a clean way
in the t-dep. CP-asymmetry:

$$A_{CP}(B_s \rightarrow J_\psi \phi) \cong \frac{-\eta_f \sin \phi_s \sin(\Delta M_s t)}{\cosh\left(\frac{\Delta\Gamma_s t}{2}\right) - \eta_f \cos \phi_s \sinh\left(\frac{\Delta\Gamma_s t}{2}\right)}$$

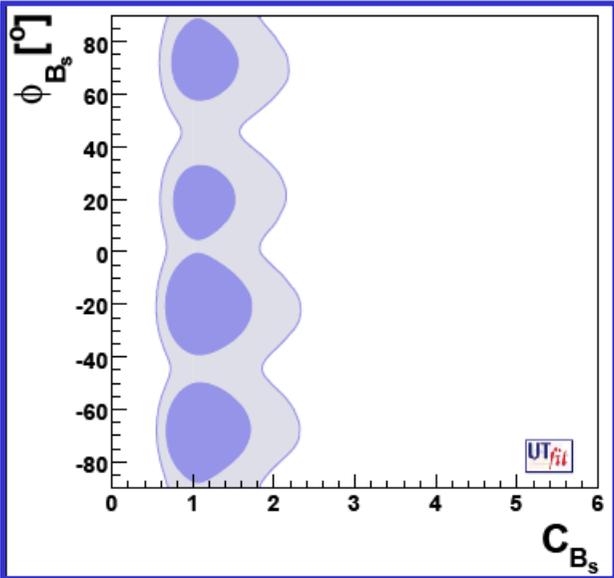
$\beta_s = -1^\circ \approx 0$



Observing a large $A_{CP}(B_s \rightarrow J_\psi \phi)$ at LHC
would be a clear signal of NP, beyond MFV

From a NP (model-indep.) analysis
[M.Bona et al. (UTfit), 0707.0636, hep-ph/0605213]

Contrary to B_d and K systems,
a large NP phase ϕ_{B_s} is still possible

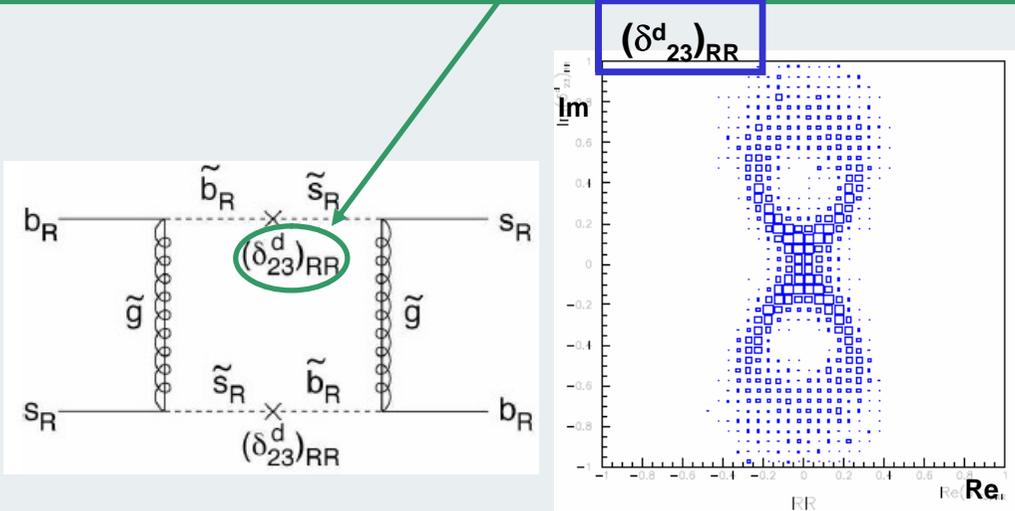


In specific NP models beyond MFV:

MSSM

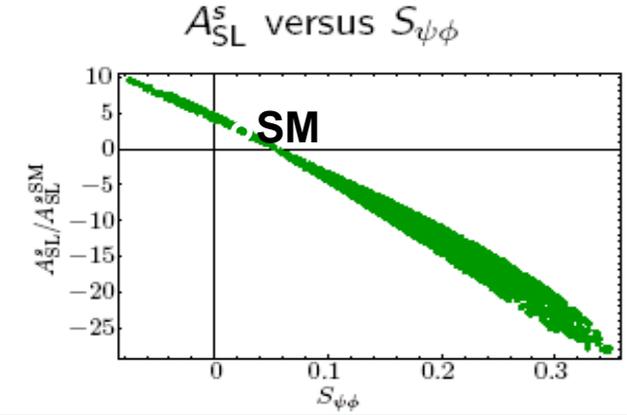
[M.Ciuchini, L.Silvestrini hep-ph/0603114, M.Ciuchini et al., in preparation]

- Constraints on the δ 's (non-diagonal entries of sfermion mass matrices)
- ΔM_s constraints mainly $(\delta_{23}^d)_{RR}$ ($|\delta_{23}^d| < 7 \cdot 10^{-1}$, with $\tan\beta=3$)



Littlest Higgs model with T-Parity

$$S_{\psi\phi} = \sin(2|\beta_s| - 2\phi_{B_s})$$



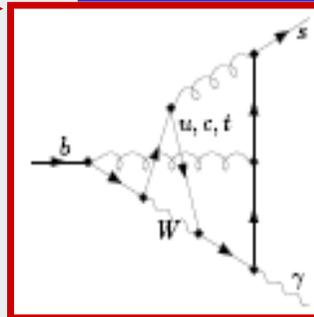
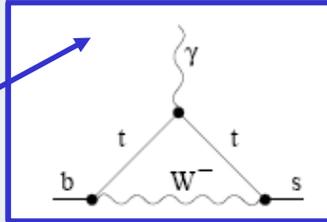
- A_{SL}^s can be enhanced by 10-20
- $S_{\psi\phi}$ can be as high as +0.3

[Blanke, Buras, Poschenrieder, CT, Uhlig, Weiler, hep-ph/0605214]

Radiative and Rare Decays

$b \rightarrow s \gamma$ (inclusive)

- highly sensitive to NP (loop FCNC)
- theoretically well under control
- with a small experimental error



$$\text{Br}(B \rightarrow X_s \gamma)_{E_\gamma > 1.6\text{GeV}}^{\text{exp}} = (3.55 \pm 0.24) 10^{-4}$$

[HFAG, 2007]

NNLO QCD correct. to Wilson coefficients
+ RG resummation of large logs $\ln(M_W^2/m_b^2)$
[M.Misiak et al., hep-ph/0609232]

$$\text{Br}(B \rightarrow X_s \gamma)_{E_\gamma > 1.6\text{GeV}}^{\text{SM}} = (3.15 \pm 0.23) 10^{-4}$$

Main theoretical uncertainty:
unknown $\mathcal{O}(\alpha_s \Lambda_{\text{QCD}}/m_b)$ non-pert.
effects in 4-quark operators

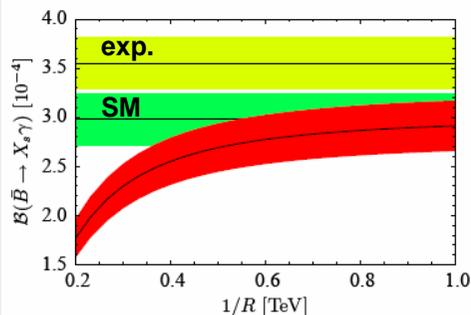
A small positive NP
effect is still allowed

Significant constraint on NP models

1 Universal Extra Dimension

$\text{Br}(B \rightarrow X_s \gamma)$ now represents
the **strongest constraint**:
 $1/R > 600\text{GeV}$

[U.Haisch, A.Weiler, hep-ph/0703064]



mSUGRA (MSSM with MFV)

$b \rightarrow s \gamma$ indicates for the
light Higgs mass $m_h \approx 110\text{GeV}$
compatible with the LEP limit

[O.Buchmuller et al. 0707.3447]

MSSM beyond MFV

Strong constraint on the
non-diagonal entry $(\delta_{23}^d)_{LR} (< 5 \cdot 10^{-3})$

[M.Ciuchini, L.Silvestrini hep-ph/0603114,
M.Ciuchini et al., in preparation]

Littlest Higgs model with T-Parity

Small (~4%) effects
are possible

[M.Blanke et al., hep-ph/0605214]

$b \rightarrow s \gamma$ (exclusive)

$$\langle V \gamma | Q_i | B \rangle = \left[T_1^{B \rightarrow V}(0) T_i^I + \int_0^1 d\xi du T_i^{II}(\xi, u) \phi_B(\xi) \phi_{2;V}^\perp(v) \right] \cdot \epsilon$$

Theoretical predictions require **QCD factorization**:

- **pert. hard scattering kernels**
- **non-pert. form factors**
- **non-pert. light cone distribution amplitudes**

from **Lattice QCD**
[D.Becirevic et al.,
hep-ph/0611295]

from quark models and

from **QCD sum rules on the light cone**
[P.Ball et al., hep-ph/0612081]

$\text{Br}(B \rightarrow K^* \gamma)$ is theoretically **cleaner** than $\text{Br}(B \rightarrow \rho \gamma)$,
where $\mathcal{O}(\Lambda_{\text{QCD}}/m_b)$ corrections turn out to be relevant

$|V_{td}|/|V_{ts}|$ can be extracted
from their BR ratios

[P.Ball, R.Zwicky, hep-ph/0603232]

Interesting exclusive observables

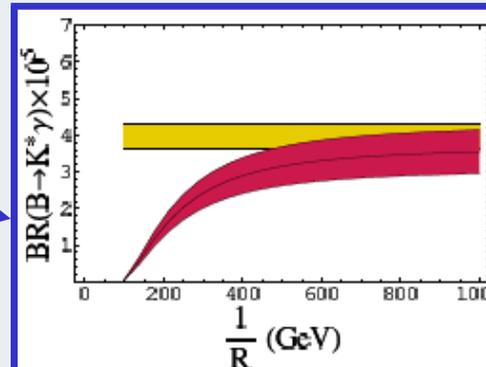
are the t-dep. **CP-asymmetries** $A_{\text{CP}}(B \rightarrow V \gamma)$:

- they are (helicity) **suppressed within the SM** $\sim \mathcal{O}(1\%)$
- their **observation would be a clear signal of NP**

In 1 Universal Extra Dimensions

$B \rightarrow K^* \gamma$ represents a **stringent constraint**

[P.Colangelo et al., hep-ph/0604029, hep-ph/0610044]



(with form factors
from light-cone
QCD sum rules)

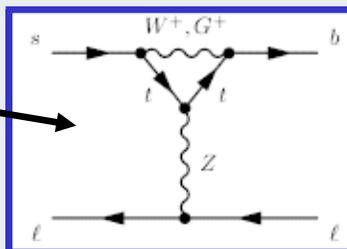
$$B_q \rightarrow l^+ l^-$$

The $\mu^+\mu^-$ modes are **experimentally the best**:

- e^+e^- is m_e^2/m_μ^2 suppressed
- $\tau^+\tau^-$ has at least other two missing ν from decaying τ 's

Upper bounds have been recently obtained

- **Highly sensitive to NP**
(loop FCNC: Z-penguin dominated)
- **Theoretically clean** (purely leptonic)



$$\text{Br}(B_d \rightarrow \mu^+\mu^-) < 1.8 \cdot 10^{-8} \quad (95\% \text{ C.L.})$$

$$\text{Br}(B_s \rightarrow \mu^+\mu^-) < 5.8 \cdot 10^{-8} \quad [\text{CDF}, 0712.1708]$$

$$Q_A = (\bar{b}_L \gamma^\mu q_L) (\bar{l} \gamma^\mu \gamma^5 l)$$

Wilson coeff. at NLO in QCD
[Misiak, J.Urban hep-ph/9901278,
G.Buchalla, A.J.Buras hep-ph/9901288]

$$\text{Br}(B_d \rightarrow \mu^+\mu^-)^{\text{SM}} = (1.03 \pm 0.09) 10^{-10}$$

$$\text{Br}(B_s \rightarrow \mu^+\mu^-)^{\text{SM}} = (3.35 \pm 0.32) 10^{-9}$$

[M.Blanke, A.J.Buras, D.Guadagnoli, C.T.,
hep-ph/0604057]

There is still a lot of room for NP

Within the SM or MFV without new operators,
there are clean correlations
(with ΔM_q and between B_d and B_s systems):

$$\text{Br}(B_q \rightarrow \mu^+\mu^-) = C \frac{\tau(B_q) Y^2(x_t)}{\hat{B}_{B_q} S(x_t)} \Delta M_q$$

$$\frac{\text{Br}(B_s \rightarrow \mu^+\mu^-)}{\text{Br}(B_d \rightarrow \mu^+\mu^-)} = \frac{\hat{B}_{B_d} \tau(B_s) \Delta M_s}{\hat{B}_{B_s} \tau(B_d) \Delta M_d} = 32.4 \pm 1.9$$

[M.Blanke, A.J.Buras, D.Guadagnoli, C.T.,
hep-ph/0604057]

A deviation would signal NP with new operators
and/or new sources of flavour violation

MSSM with large $\tan\beta$

New (Higgs-generated) scalar and pseudoscalar
operators yield $\text{Br} \propto \tan^6\beta$
 $\rightarrow B_q \rightarrow l^+ l^-$ is a smoking gun for Higgs effects in MSSM

[K.S.Babu, C.F.Kolda, hep-ph/9909476,
G.Isidori, A.Retico, hep-ph/0110121,
A.J.Buras et al., hep-ph/0210145,
hep-ph/0207241, hep-ph/0107048,
G.Isidori, P.Paradisi, hep-ph/0605012]

$b \rightarrow (s, d) l^+ l^-$

- Highly sensitive to NP (loop FCNC)
- Main SM contribution from em dipole operator (Q_7^γ), and ew penguin operators (Q^9, Q^{10})

Close to the charm threshold (long-distance) $c\bar{c}$ resonances appear

Two approaches can be used:
• appropriate exp. cuts are introduced
• models (for resonances) + disp. relations
[A.Ali et al., hep-ph/9910221]

In certain phase-space regions some incl. and excl. observables have hadronic uncert. under control

Inclusive: $B \rightarrow X_s l^+ l^-$

- Wilson coefficients at NNLO in QCD
[C. Bobeth et al., hep-ph/0312090, M. Gorban, U. Haisch, hep-ph/0411071]
- HQE at $O(\Lambda_{\text{QCD}}^2/m_c^2), O(\Lambda_{\text{QCD}}^2/m_b^2), O(\Lambda_{\text{QCD}}^3/m_b^3)$
- QED corrections
- bremsstrahlung effects

[see the WG2 CERN-report 0801.1833]

[T. Huber et al., hep-ph/0512066]

$$\text{Br}(\bar{B} \rightarrow X_s \mu^+ \mu^-)^{\text{SM}} = (1.59 \pm 0.11) \cdot 10^{-6} \quad 1 \text{ GeV}^2 < m_{ll}^2 < 6 \text{ GeV}^2$$
$$\text{Br}(\bar{B} \rightarrow X_s e^+ e^-)^{\text{SM}} = (1.64 \pm 0.11) \cdot 10^{-6}$$

Sensitive to the interference of the Wilson coefficients C_7 and C_9

The forward-backward asymmetry (A_{FB}) is sensitive to $C_7 C_{10}$ and $C_9 C_{10}$

Exclusive: $B \rightarrow K^* \ell^+ \ell^-$

The most interesting observables are:

- $d\Gamma^2 / (dq^2 d\cos\theta)$ → extraction of C_9/C_7 and C_{10}/C_7 [Belle, hep-ex/0603018]
 - $\ell^+ \ell^-$: Invariant mass
 - $\ell^+ B$: angle
 - sensitive to NP in $C_{9,10}$ and eventual NP (chirally flipped) $C'_{9,10}$

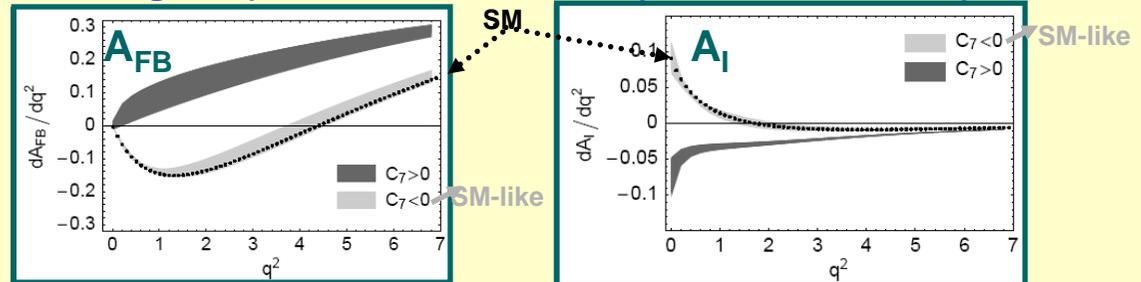
Theoretical study in terms of transversity amplitudes [K.J.M.Lee et al., hep-ph/0612156], based on QCD factorization + SCET [A.Ali et al., hep-ph/0601034] and HQET [B.Grinstein and D.Pirjol, hep-ph/0404250] (main source of uncertainty: Λ_{QCD}/m_b corrections)

- A_{FB} and its zero q_0^2 : main source of uncertainty → hadronic inputs
 - from QCD sum rules [M.Beneke et al., hep-ph/0106067] or exp. results on $B \rightarrow K^* \gamma$ [A.Ali et al., hep-ph/0601034]
 - Significant deviations from the SM in the MSSM [A.Ali et al., hep-ph/9910221, T.Feldmann, J.Matias, hep-ph/0212158]

A_1 (isospin asymmetry between neutral and charged B): Small within the SM (=0 in factorization)

[T.Feldmann and J.Matias, hep-ph/0212158]

MSSM with MFV



- Muon to electron ratio:**

$$R_H \equiv \int_{q_1}^{q_2} dq^2 \frac{d\Gamma(B \rightarrow H \mu^+ \mu^-)}{dq^2} / \int_{q_1}^{q_2} dq^2 \frac{d\Gamma(B \rightarrow H e^+ e^-)}{dq^2}, \quad H = \{ k^* \}$$

=0.991±0.002 within the SM, ~13% NP effects are possible [G.Hiller and F.Krüger, hep-ph/0310219] [model indep.(combined $R_{H \leftrightarrow B_s} \rightarrow \mu^+ \mu^-, \dots$) analysis within MFV, neglecting RightHanded contributions, assuming $C_{S,P} \propto m_l$ (as due to $\tan\beta$ enhanced Higgs couplings in the MSSM)]

Other exclusive channels:

$B \rightarrow K \ell^+ \ell^-$, ($A_{\text{FB}}=0$ in the SM, a deviation would be a smoking gun of NP with scalar and pseudoscalar operators) [M.Beneke et al., hep-ph/0106067]

$B_s \rightarrow \phi \ell^+ \ell^-$, $B_s \rightarrow \eta' \ell^+ \ell^-$ (larger hadronic uncertainties in meson wave functions)

$\Lambda_b \rightarrow \Lambda^0 \ell^+ \ell^-$ (theoretically more complicated)

Conclusions

- There is plenty of interesting B-observables sensitive to NP and accessible at LHC
- A combined analysis, including clean correlations, plays an important role to identify a SM breakdown and its sources
- The NP flavour structure can only be determined with improved measurements in the flavour sector

- see Paride's discussion of:
- Interplay with Direct Searches
 - Lepton flavour violation
 - ...

THANKS!



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