

# $Z'$ , $Z_{KK}$ , $Z^*$ and all that:

---

current bounds and theoretical prejudices  
on a heavy neutral vector boson

Roberto Contino - CERN

# The case of a “standard” Z'

$$\begin{aligned}\mathcal{L} = & \mathcal{L}_{SM} - \frac{1}{4} Z'_{\mu\nu} Z'^{\mu\nu} + g_{Z'}^{[\Psi]} \sum_a Z'_\mu \bar{\Psi}_a z_a \gamma^\mu \Psi_a \\ & + g_{Z'}^{[H]} H^\dagger z_H Z'_\mu i D^\mu H + h.c. + \dots\end{aligned}$$

# The case of a “standard” Z'

$$\mathcal{L} = \mathcal{L}_{SM} - \frac{1}{4} Z'_{\mu\nu} Z'^{\mu\nu} + g_{Z'}^{[\Psi]} \sum_a Z'_\mu \bar{\Psi}_a z_a \gamma^\mu \Psi_a$$

+  $g_{Z'}^{[H]} H^\dagger z_H Z'_\mu i D^\mu H + h.c. + \dots$

couplings to the  
SM fermions

The diagram shows the Lagrangian  $\mathcal{L}$  as a sum of terms. The first term is the standard model Lagrangian  $\mathcal{L}_{SM}$ . The second term is a kinetic term for the Z' boson:  $-\frac{1}{4} Z'_{\mu\nu} Z'^{\mu\nu}$ . The third term is a coupling between the Z' boson and SM fermions, represented by a yellow circle labeled  $g_{Z'}^{[\Psi]}$  and a green circle labeled  $\bar{\Psi}_a z_a \gamma^\mu \Psi_a$ . A red bracket groups this term, and a red arrow points from it to the text "couplings to the SM fermions". The fourth term is a coupling between the Z' boson and the Higgs field  $H$ , represented by a yellow circle labeled  $g_{Z'}^{[H]}$  and  $H^\dagger z_H Z'_\mu i D^\mu H$ . The text "h.c." indicates the hermitian conjugate of the previous term.

# The case of a “standard” Z'

$$\mathcal{L} = \mathcal{L}_{SM} - \frac{1}{4} Z'_{\mu\nu} Z'^{\mu\nu} + g_{Z'}^{[\Psi]} \sum_a Z'_\mu \bar{\Psi}_a z_a \gamma^\mu \Psi_a$$

$+ g_{Z'}^{[H]} H^\dagger z_H Z'_\mu i D^\mu H + h.c. + \dots$

couplings to the  
SM fermions

Z' - Z mixing after EWSB

# The case of a “standard” $Z'$

$$\mathcal{L} = \mathcal{L}_{SM} - \frac{1}{4} Z'_{\mu\nu} Z'^{\mu\nu} + g_{Z'}^{[\Psi]} \sum_a Z'_\mu \bar{\Psi}_a z_a \gamma^\mu \Psi_a$$
$$+ g_{Z'}^{[H]} H^\dagger z_H Z'_\mu i D^\mu H + h.c. + \dots$$

couplings to the  
SM fermions

$\xrightarrow{\hspace{10em}}$

$\xleftarrow{\hspace{10em}}$   $Z' - Z$  mixing after EWSB

- common assumptions:

- same strength for the coupling to the SM fermions and the Higgs:

$$g_{Z'}^{[\Psi]} = g_{Z'}^{[H]} = g_{Z'}$$

- couplings are flavor universal (so as to avoid large FCNC)

- most popular models: **heavy Z, Left-Right, E<sub>6</sub>, (B-L), etc ...**

**example:**

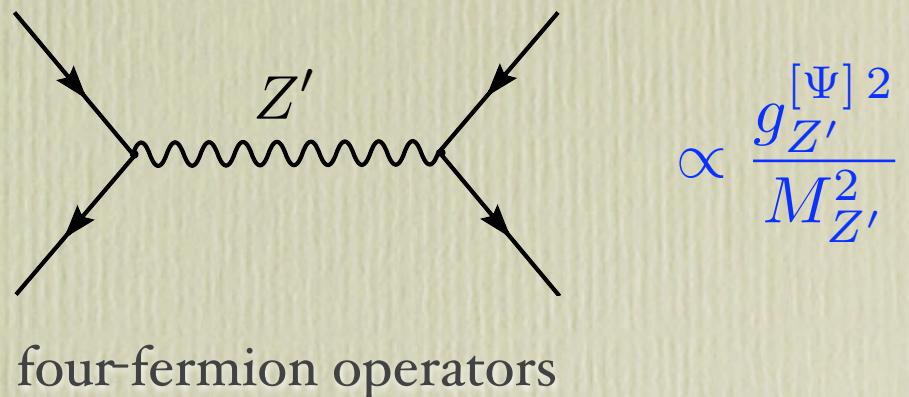
$$E_6 \rightarrow SO(10) \times U(1)_\psi$$

|  | Heavy $Z$ (SSM)  | $Z_\psi$ from $E_6$          |
|--|--|------------------------------|
| $g_{Z'}$                                     | $g_2 / \cos \theta_W$  | $g_2 \tan \theta_W$          |
| charges                                      | $(T_{3_L} - Q \sin \theta_W^2)$  | $\sqrt{\frac{72}{5}} Q_\psi$ |
| $\begin{pmatrix} \nu_L \\ e_L \end{pmatrix}$ | $+\frac{1}{2}$<br>$-\frac{1}{2} + s_W^2$                               | +1                           |
| $\nu_R$                                      | 0  | -1                           |
| $e_R$  | $s_W^2$  | -1                           |
| $\begin{pmatrix} u_L \\ d_L \end{pmatrix}$   | $+\frac{1}{2} - \frac{2}{3}s_W^2$<br>$-\frac{1}{2} + \frac{1}{3}s_W^2$ | +1                           |
| $u_R$  | $-\frac{2}{3}s_W^2$  | -1                           |
| $d_R$  | $\frac{1}{3}s_W^2$   | -1                           |
| $H$  | $-\frac{1}{2}$   | -2                           |

# Bounds from LEP precision tests

- A heavy  $Z'$  affects:

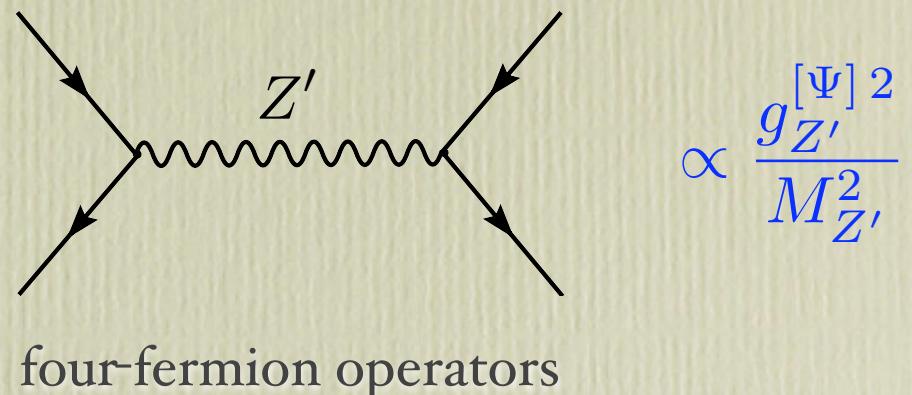
1. LEP**2** (off-pole) observables



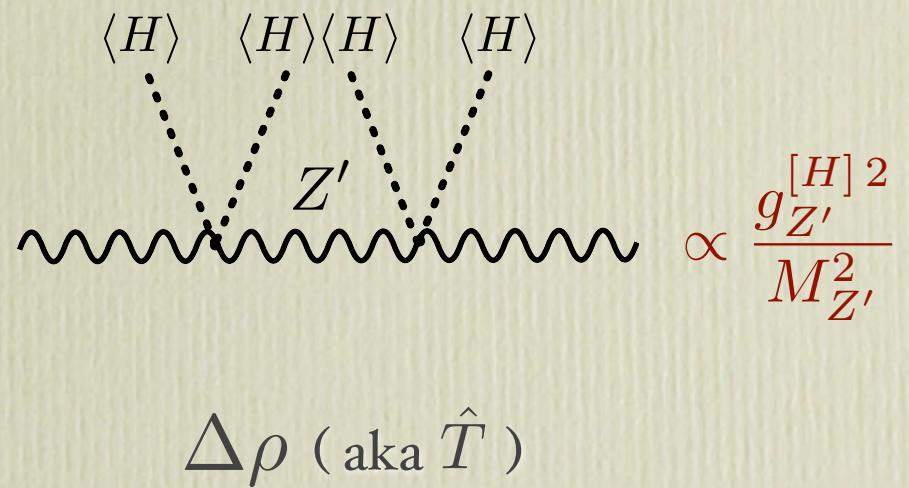
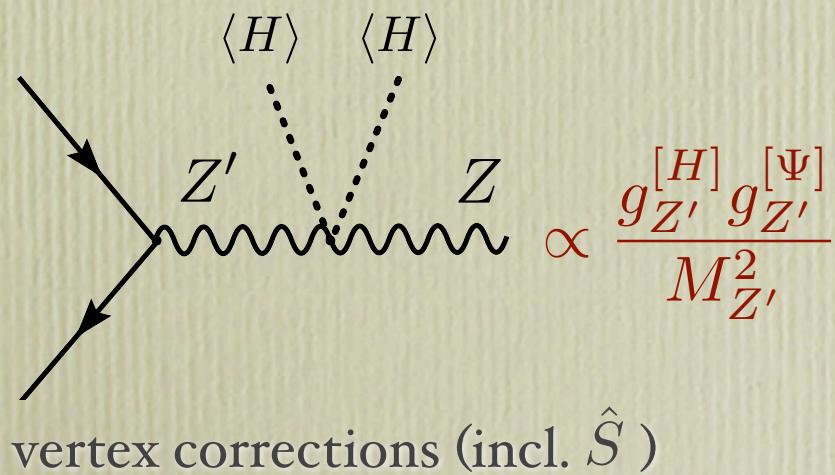
# Bounds from LEP precision tests

- A heavy  $Z'$  affects:

i. LEP2 (off-pole) observables

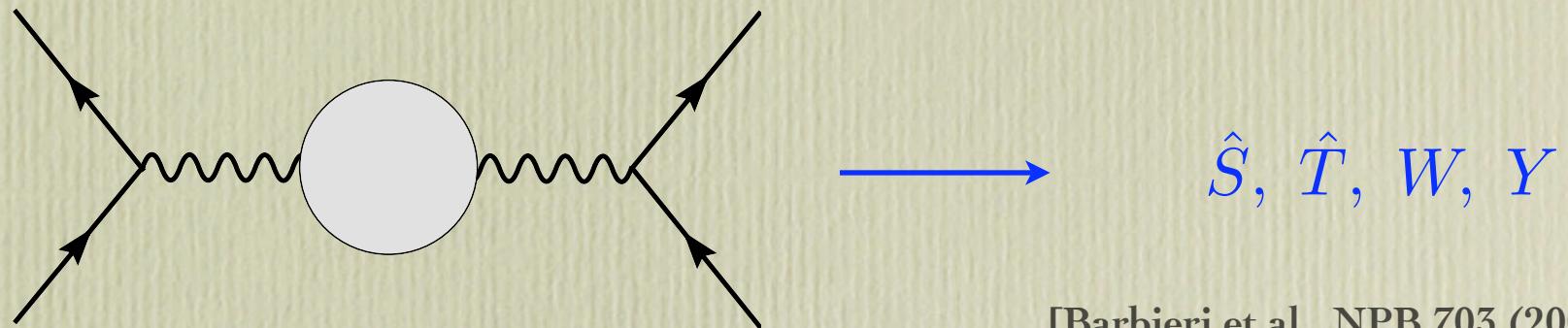


i. LEP1 Z-pole observables only via the  $Z'$ - $Z$  mixing (i.e.  $g_{Z'}^{[H]}$ )



- A universal (**oblique**)  $Z'$ :

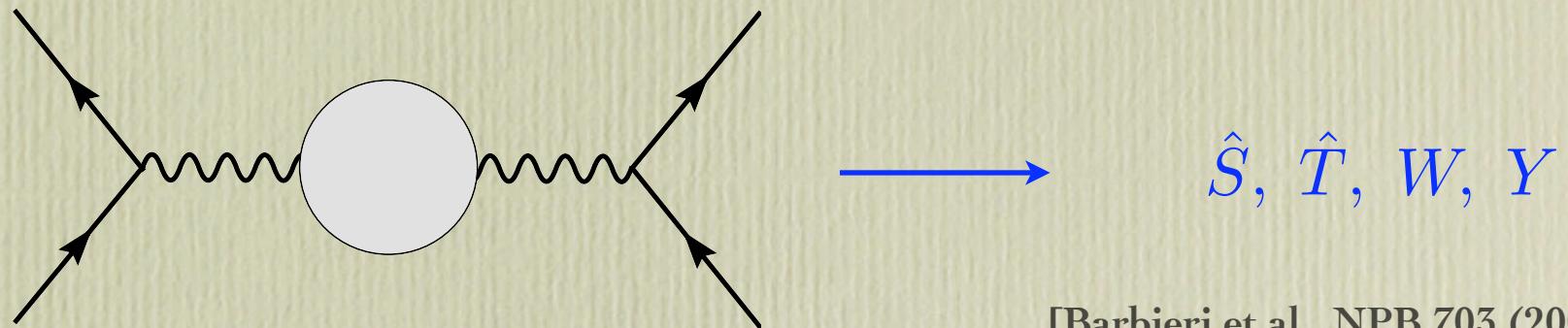
one whose corrections can be recast purely as modifications of the SM gauge boson self-energies



[Barbieri et al. NPB 703 (2004) 127]

- A universal (**oblique**)  $Z'$ :

one whose corrections can be recast purely as modifications of the SM gauge boson self-energies



[Barbieri et al. NPB 703 (2004) 127]

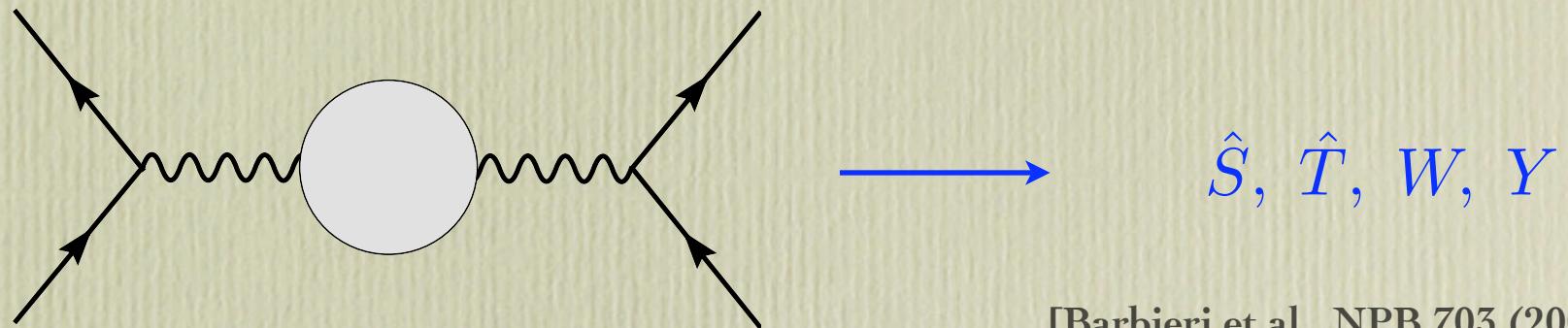
Examples:

✓ heavy hypercharge: universal

- heavy  $Z, (B - L), Z_\psi$ : not universal

- A universal (**oblique**)  $Z'$ :

one whose corrections can be recast purely as modifications of the SM gauge boson self-energies



[Barbieri et al. NPB 703 (2004) 127]

Examples:

✓ heavy hypercharge: universal

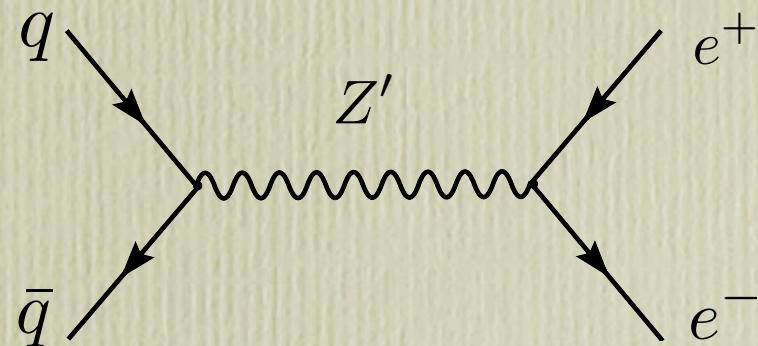
- heavy  $Z, (B - L), Z_\psi$ : not universal

☞ Notice:

the oblique basis usually does not coincide with the mass-eigenstates basis

# Tevatron exclusion limits

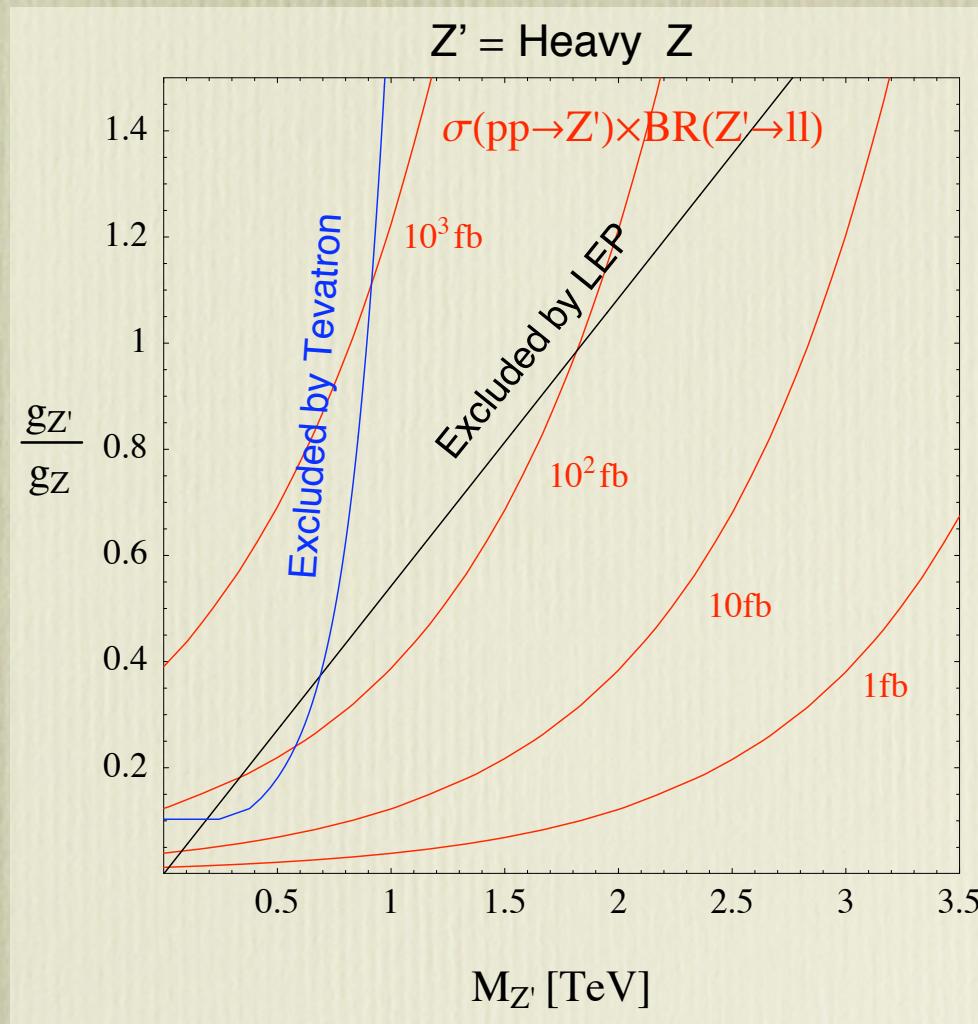
D $\emptyset$  and CDF search for  $Z'$   
production in Drell-Yan scattering:



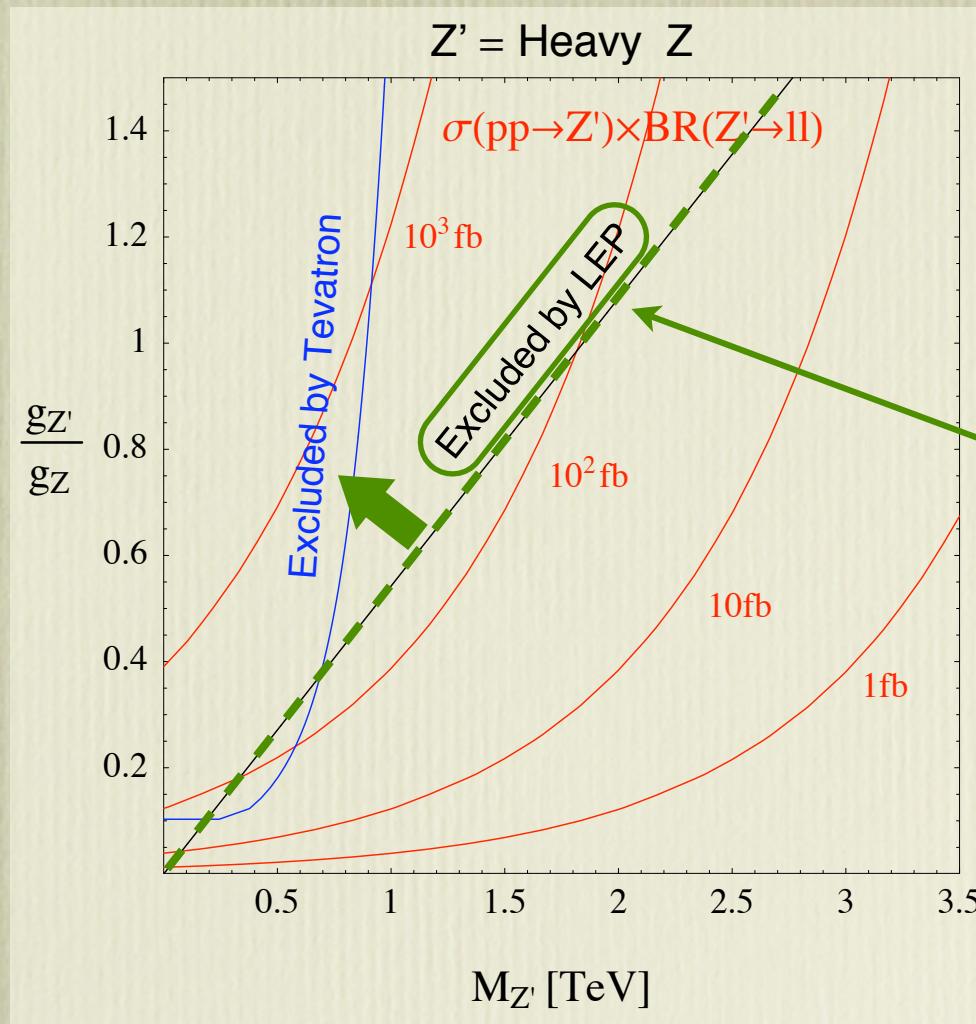
☞ I will use the bounds from CDF RunII with  $1.3 \text{ fb}^{-1}$ :

[ Phys Rev Lett 99 (2007) 171802 ; arXiv:0707.2524 ]

# The case of a heavy Z (SSM)

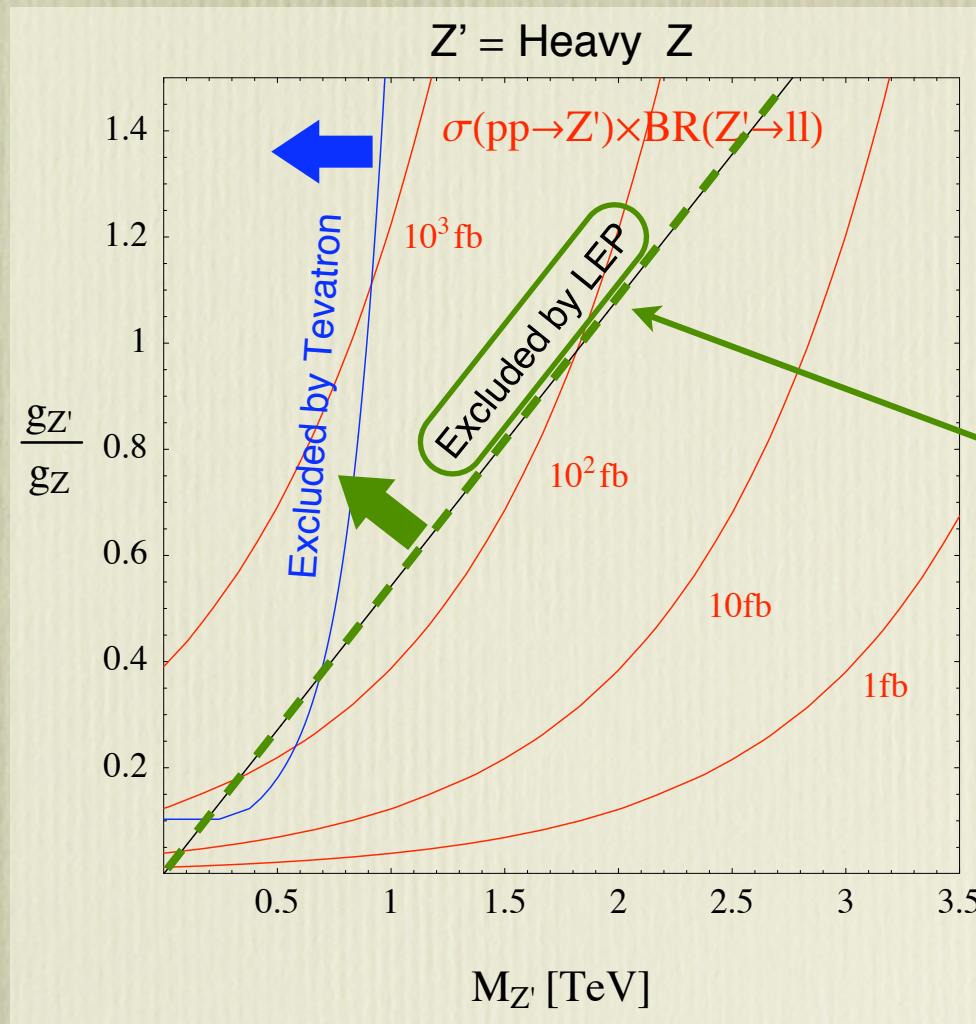


# The case of a heavy Z (SSM)



fit from:  
Cacciapaglia et al.  
hep-ph/0604111

# The case of a heavy Z (SSM)



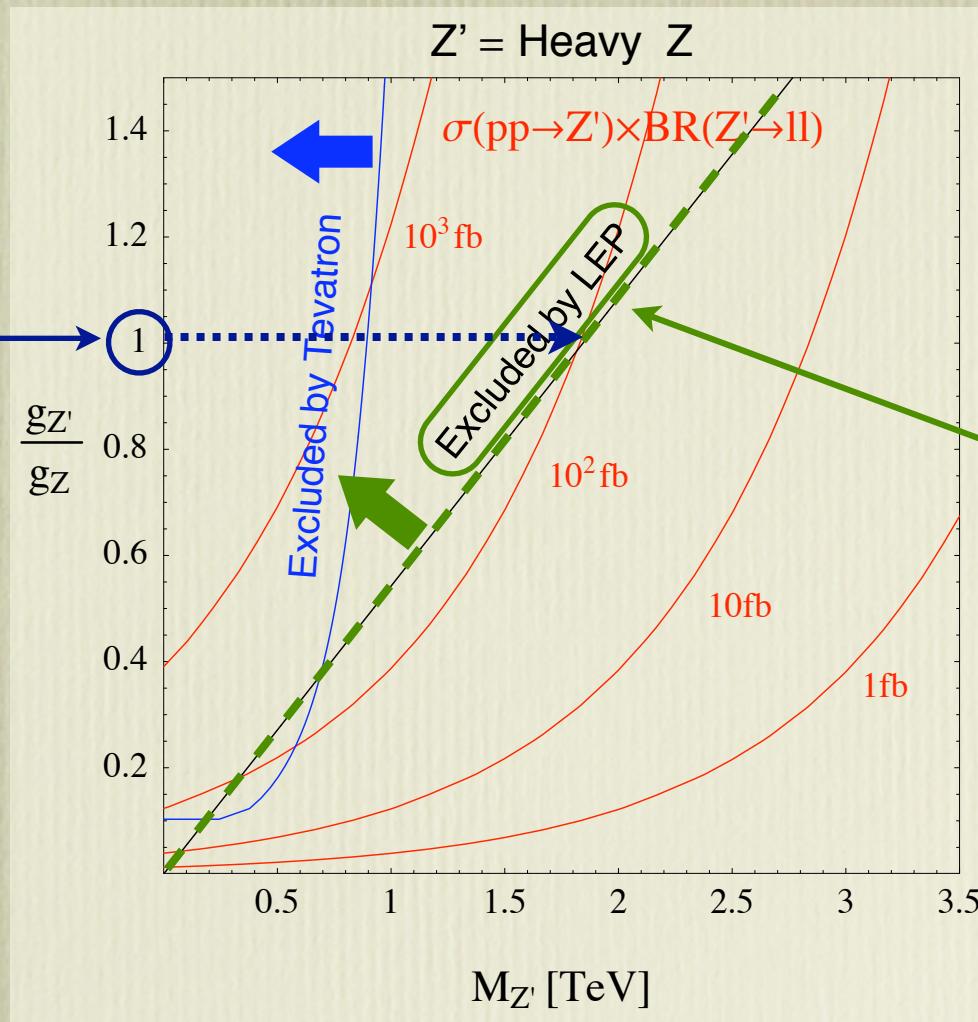
99% CL exclusion limit  
from LEP precision tests

fit from:  
Cacciapaglia et al.  
hep-ph/0604111

# The case of a heavy Z (SSM)

SM coupling  
implies a bound

$M_{Z'} \lesssim 1.8 \text{ TeV}$



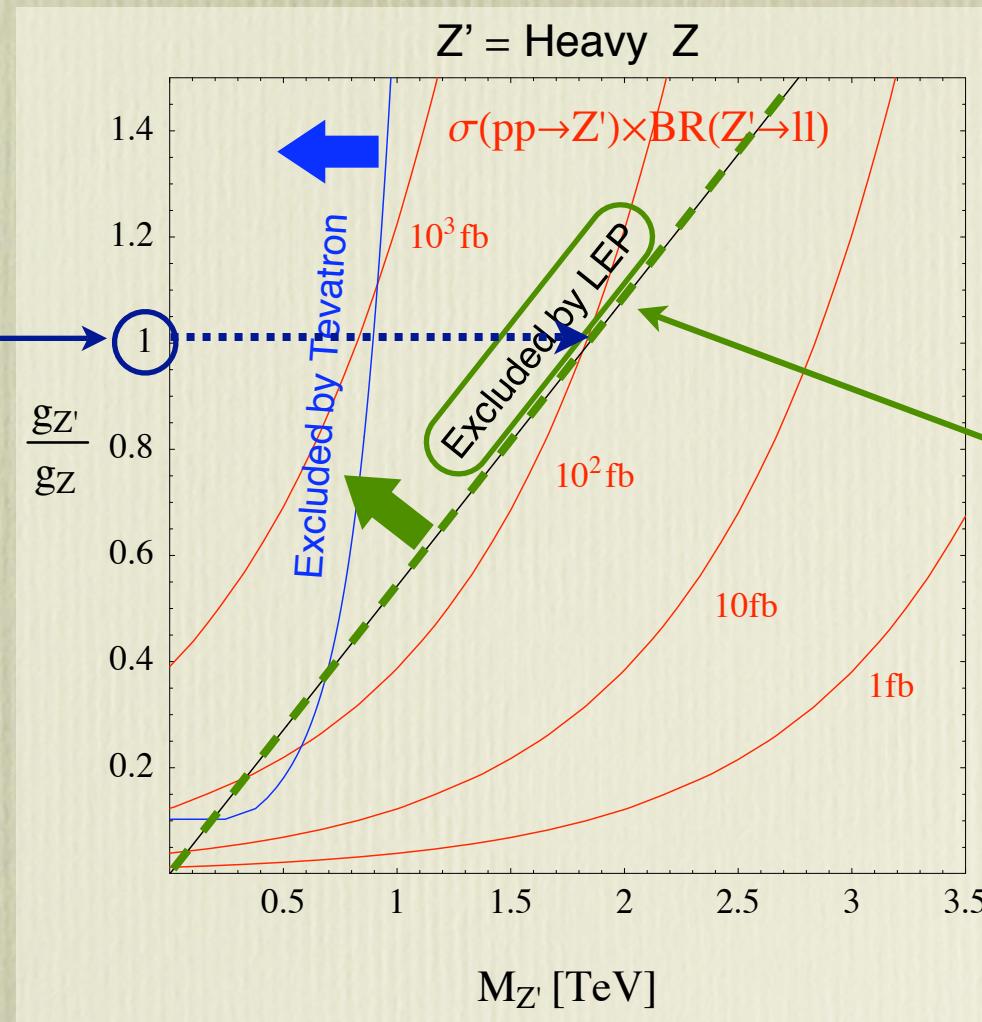
99% CL exclusion limit  
from LEP precision tests

fit from:  
Cacciapaglia et al.  
hep-ph/0604111

# The case of a heavy Z (SSM)

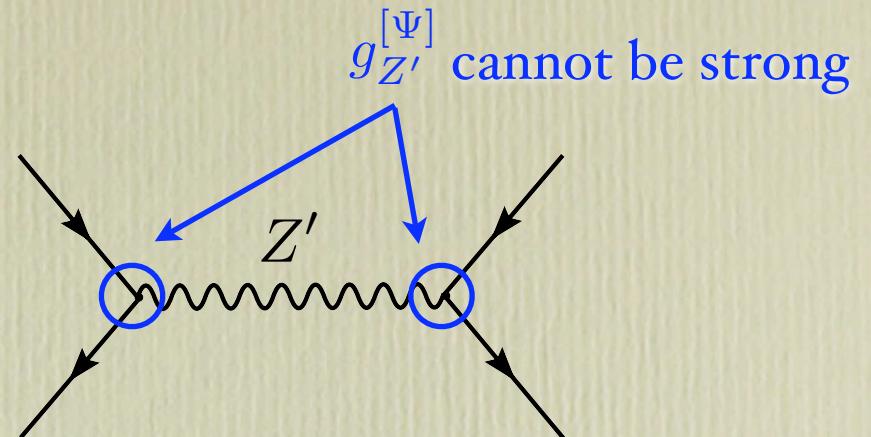
SM coupling  
implies a bound

$M_{Z'} \lesssim 1.8 \text{ TeV}$



Moral: strong couplings seem excluded... ... really true ?

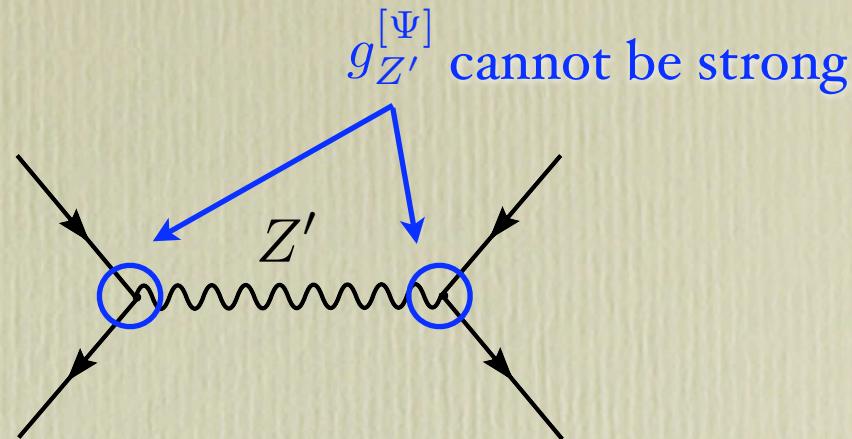
Bounds on contact interactions  
from LEP**2** quite robust :



Bounds on contact interactions  
from LEP2 quite robust :

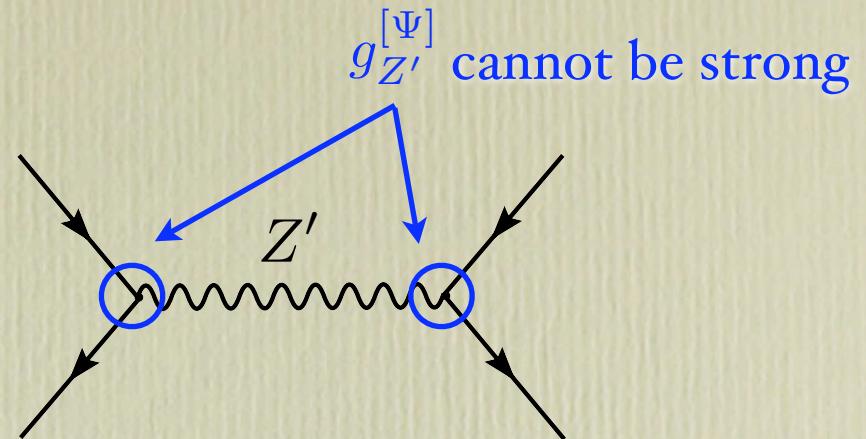
$$\langle H \rangle \quad \langle H \rangle \langle H \rangle \quad \langle H \rangle \\ \text{---} \quad \text{---} \quad \text{---} \\ \text{wavy line} \quad \text{dotted line} \quad \text{wavy line} \\ \text{---} \quad \text{---} \quad \text{---} \\ Z' \quad Z' \quad Z'$$

$$\propto \frac{g_{Z'}^{[H]2}}{M_{Z'}^2}$$



the strong bound on  
 $\Delta\rho \propto [\Pi_{11}(0) - \Pi_{33}(0)]$   
 can be avoided with a  
 custodial symmetry

Bounds on contact interactions  
from LEP**2** quite robust :



$$\langle H \rangle \quad \langle H \rangle \langle H \rangle \quad \langle H \rangle$$

$$\propto \frac{g_{Z'}^{[H] 2}}{M_{Z'}^2}$$

the strong bound on  
 $\Delta\rho \propto [\Pi_{11}(0) - \Pi_{33}(0)]$   
 can be avoided with a  
 custodial symmetry

$g_{Z'}^{[H]}$  strong is compatible with  
LEP**1** bounds if  $g_{Z'}^{[\Psi]}$  is weaker

$$\propto \frac{g_{Z'}^{[H]} g_{Z'}^{[\Psi]}}{M_{Z'}^2}$$

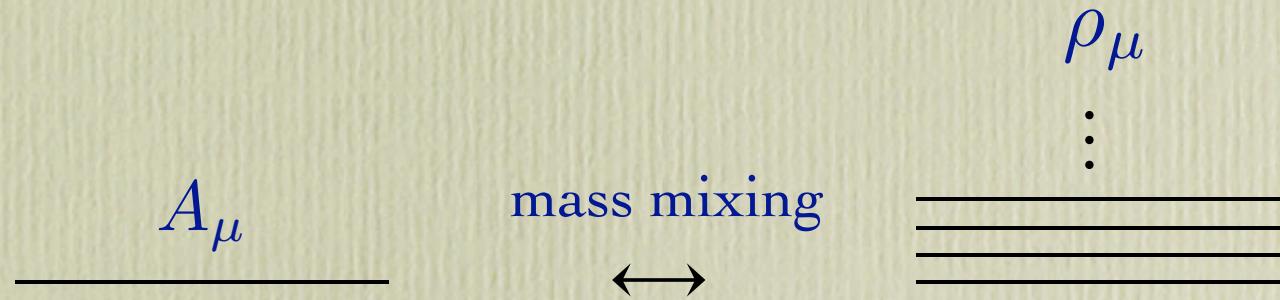
# An alternative scheme: partial compositeness

# An alternative scheme: partial compositeness

the SM gauge bosons could be  
the admixture of an  
elementary with a composite

$$G_{el} \supset [SU(2)_L \times U(1)_Y]_{el}$$

$$G_{comp} \supset [SU(2)_L \times SU(2)_R \times U(1)_X]_{comp}$$



# An alternative scheme: partial compositeness

the SM gauge bosons could be  
the admixture of an  
elementary with a composite

$$G_{el} \supset [SU(2)_L \times U(1)_Y]_{el}$$

$$G_{comp} \supset [SU(2)_L \times SU(2)_R \times U(1)_X]_{comp}$$

$$A_\mu$$

mass mixing



$$\rho_\mu$$

⋮

$$\overbrace{\hspace{1cm}}^{\hspace{1cm}}$$

same as ρ-photon  
mixing in QCD

$$\mathcal{L}_{mix} = \frac{M_*^2}{2} \left( \frac{g_{el}}{g_*} A_\mu - \rho_\mu \right)^2$$

$$= \frac{M_*^2}{2} \rho_\mu^2 - M_*^2 \frac{g_{el}}{g_*} A_\mu \rho_\mu + \frac{M_*^2}{2} \left( \frac{g_{el}}{g_*} \right)^2 A_\mu^2$$

# An alternative scheme: partial compositeness

the SM gauge bosons could be  
the admixture of an  
elementary with a composite

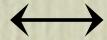
$\longleftrightarrow$  ! Randall-Sundrum are of this type

$$G_{el} \supset [SU(2)_L \times U(1)_Y]_{el}$$

$$G_{comp} \supset [SU(2)_L \times SU(2)_R \times U(1)_X]_{comp}$$

$$A_\mu$$

mass mixing



$$\rho_\mu$$

:

$$\overbrace{\hspace{1cm}}^{\vdots}$$

same as  $\rho$ -photon  
mixing in QCD



$$\mathcal{L}_{mix} = \frac{M_*^2}{2} \left( \frac{g_{el}}{g_*} A_\mu - \rho_\mu \right)^2$$

$$= \frac{M_*^2}{2} \rho_\mu^2 - M_*^2 \frac{g_{el}}{g_*} A_\mu \rho_\mu + \frac{M_*^2}{2} \left( \frac{g_{el}}{g_*} \right)^2 A_\mu^2$$

# Diagonalization:

from the composite/elementary basis  
to the mass eigenstates (KK) basis

$$\begin{pmatrix} A_\mu \\ \rho_\mu \end{pmatrix} \rightarrow \begin{pmatrix} \cos \theta & \sin \theta \\ \sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} A_\mu \\ \rho_\mu \end{pmatrix}$$

$$\tan \theta = \frac{g_{el}}{g_*}$$

$$g_{SM} = \frac{g_{el} g_*}{\sqrt{g_{el}^2 + g_*^2}} \simeq g_{el}$$

$$|\text{SM}\rangle = \cos \theta |A_\mu\rangle + \sin \theta |\rho_\mu\rangle$$

$$|\text{heavy}\rangle = -\sin \theta |A_\mu\rangle + \cos \theta |\rho_\mu\rangle$$

☞  $\theta$  parametrizes the degree of partial compositeness

# Diagonalization:

from the composite/elementary basis  
to the mass eigenstates (KK) basis

$$\begin{pmatrix} A_\mu \\ \rho_\mu \end{pmatrix} \rightarrow \begin{pmatrix} \cos \theta & \sin \theta \\ \sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} A_\mu \\ \rho_\mu \end{pmatrix}$$

$$\tan \theta = \frac{g_{el}}{g_*}$$

$$g_{SM} = \frac{g_{el} g_*}{\sqrt{g_{el}^2 + g_*^2}} \simeq g_{el}$$

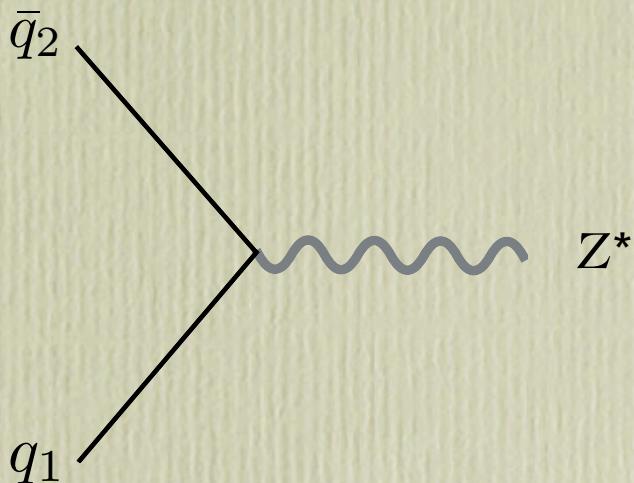
$$\begin{aligned} |\text{SM}\rangle &= \cos \theta |A_\mu\rangle + \sin \theta |\rho_\mu\rangle \\ |\text{heavy}\rangle &= -\sin \theta |A_\mu\rangle + \cos \theta |\rho_\mu\rangle \end{aligned}$$

☞  $\theta$  parametrizes the degree of partial compositeness

- the Higgs is a full composite (= solution to the Hierarchy Problem)
- LEP bounds imply light fermions (almost completely) elementary
- top (and bottom) can have a sizable composite component

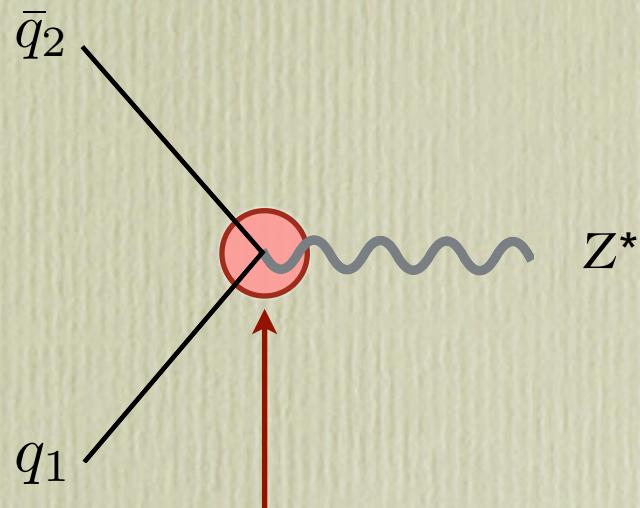
## Consequences of Partial Compositeness: **Z\* PRODUCTION & DECAY**

Drell-Yan production has  
the largest cross section:



## Consequences of Partial Compositeness: **Z\* PRODUCTION & DECAY**

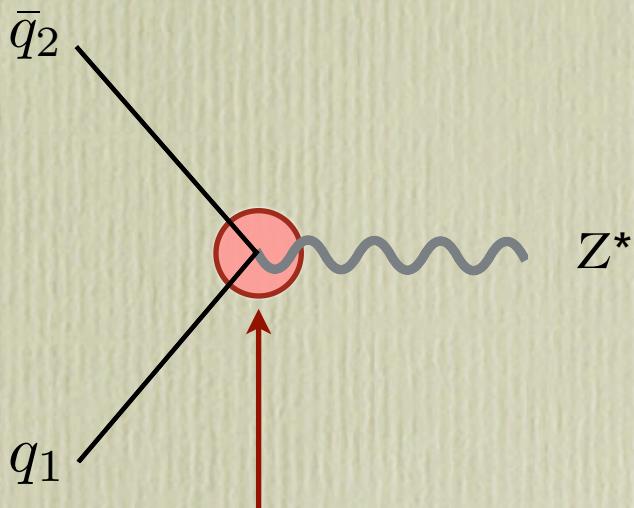
Drell-Yan production has the largest cross section:



$$g_* \sin \varphi_1 \sin \varphi_2 \cos \theta_2 + g_{2\,el} \cos \varphi_1 \cos \varphi_2 \sin \theta_2 \simeq g_2 \tan \theta_2$$

## Consequences of Partial Compositeness: **Z\* PRODUCTION & DECAY**

Drell-Yan production has the largest cross section:



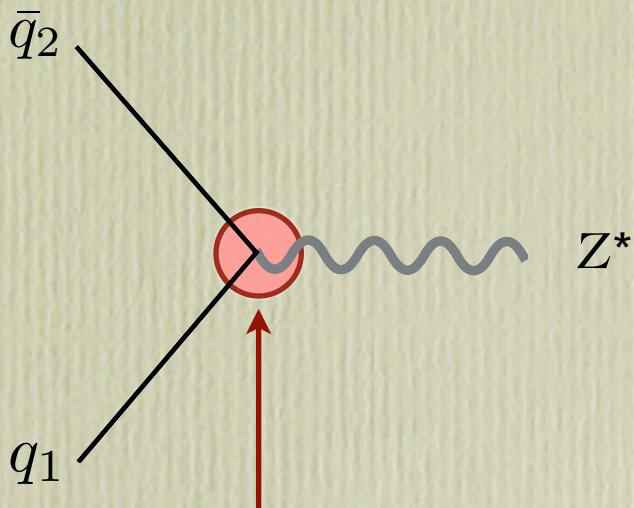
$$g_* \sin \varphi_1 \sin \varphi_2 \cos \theta_2 + g_{2\,el} \cos \varphi_1 \cos \varphi_2 \sin \theta_2 \simeq g_2 \tan \theta_2$$

interaction among the composite components

interaction among the composite components

## Consequences of Partial Compositeness: **Z\* PRODUCTION & DECAY**

Drell-Yan production has the largest cross section:



$$g_* \sin \varphi_1 \sin \varphi_2 \cos \theta_2 + g_{2\,el} \cos \varphi_1 \cos \varphi_2 \sin \theta_2 \simeq g_2 \tan \theta_2$$

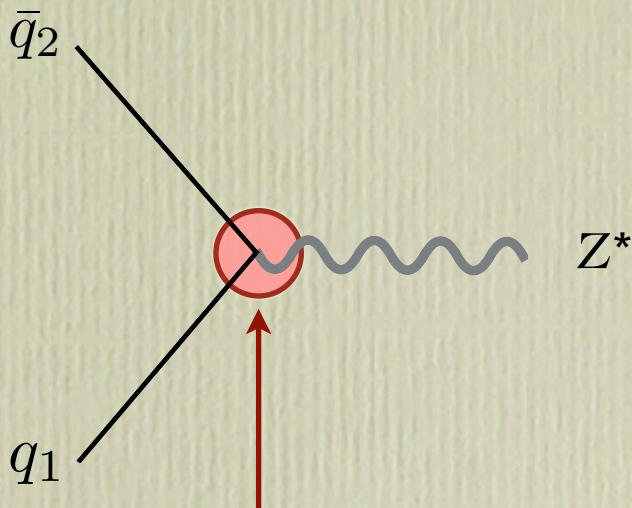


interaction among the composite components

**SUPPRESSED**

# Consequences of Partial Compositeness: $Z^*$ PRODUCTION & DECAY

Drell-Yan production has the largest cross section:



$$g_* \sin \varphi_1 \sin \varphi_2 \cos \theta_2 + g_{2\,el} \cos \varphi_1 \cos \varphi_2 \sin \theta_2 \simeq g_2 \tan \theta_2$$

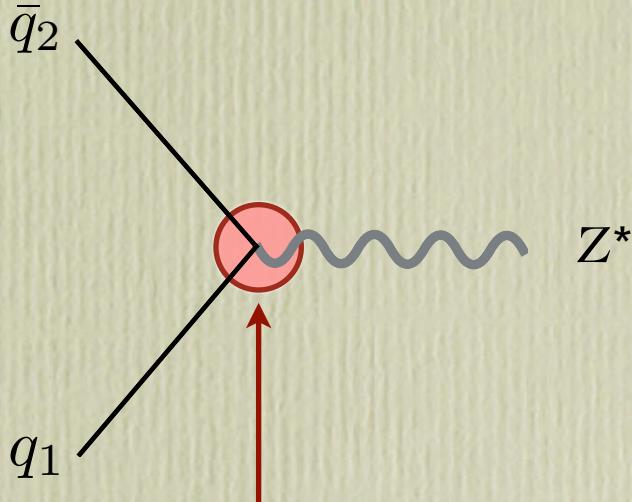
interaction among the composite components

interaction among the elementary components

**SUPPRESSED**

# Consequences of Partial Compositeness: $Z^*$ PRODUCTION & DECAY

Drell-Yan production has the largest cross section:



$$g_* \sin \varphi_1 \sin \varphi_2 \cos \theta_2 + g_{2\,el} \cos \varphi_1 \cos \varphi_2 \sin \theta_2 \simeq g_2 \tan \theta_2$$

interaction among the composite components

**SUPPRESSED**

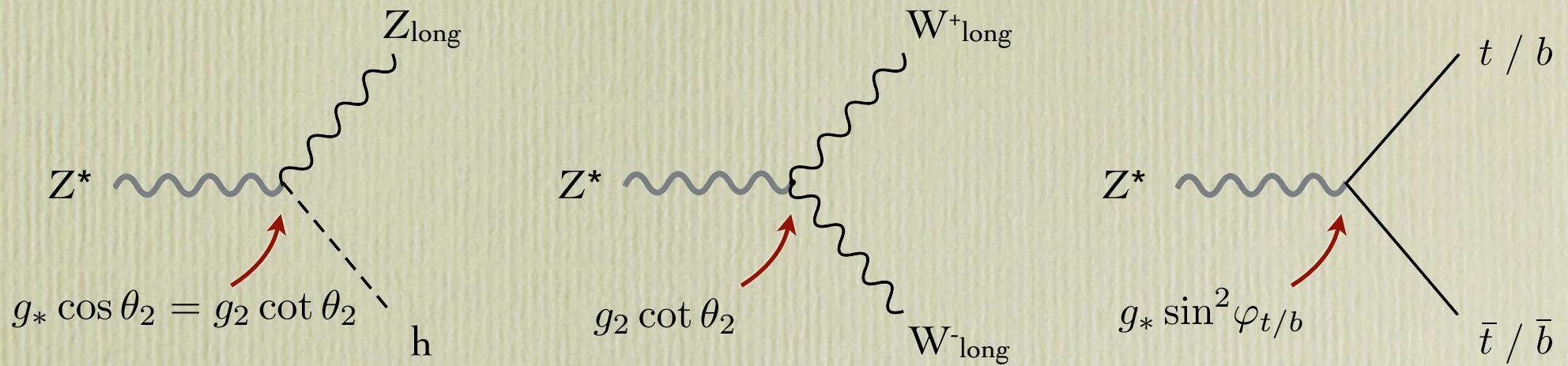
$$\tan \theta_2 = \frac{g_{2\,el}}{g_*} \ll 1$$

suppression compared to SM strength:

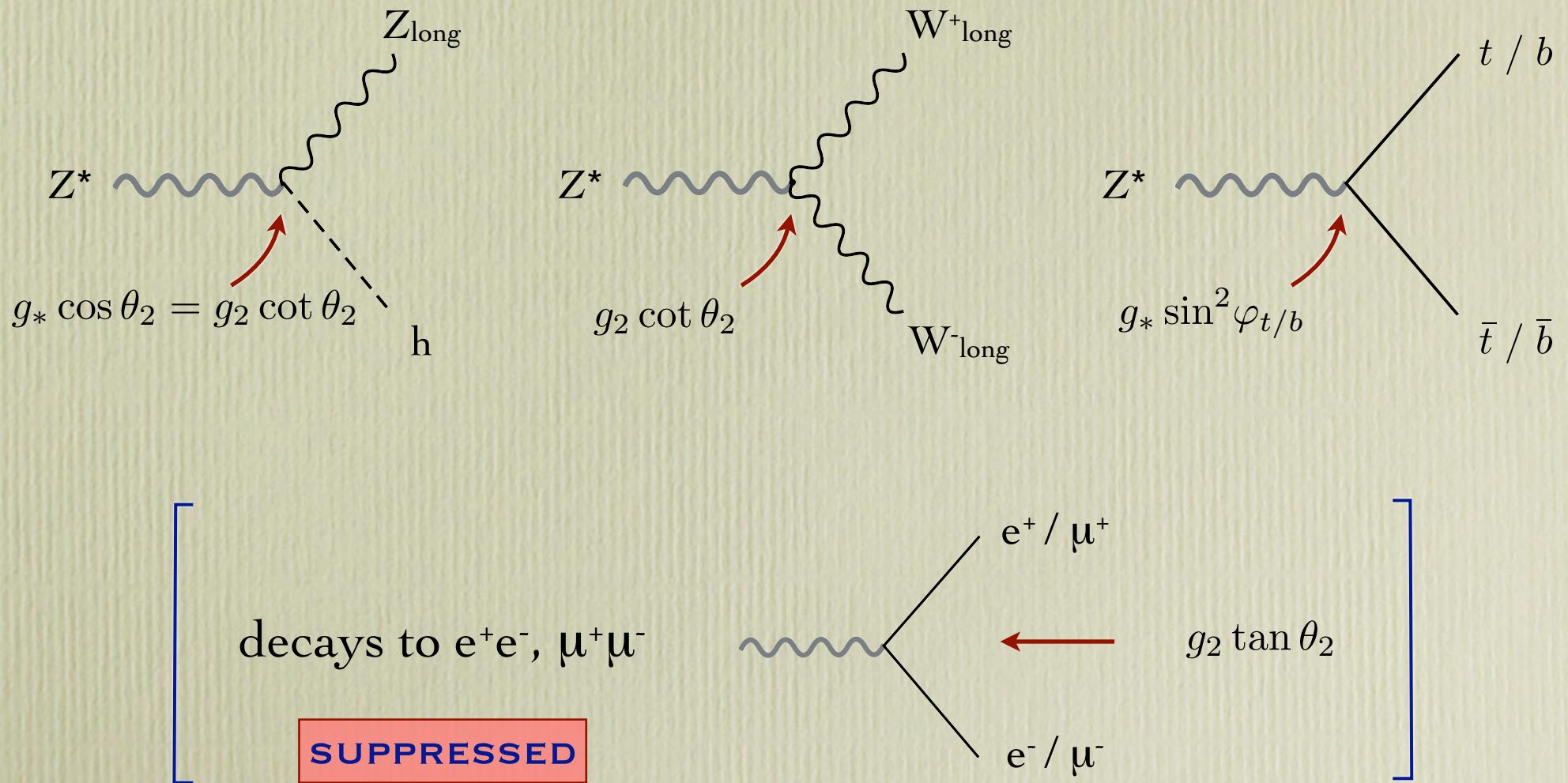


interaction among the elementary components

Largest BR's to the SM particles with the largest composite component:  $H$ ,  $W_{\text{long}}$ ,  $Z_{\text{long}}$ , top, bottom



Largest BR's to the SM particles with the largest composite component:  $H$ ,  $W_{\text{long}}$ ,  $Z_{\text{long}}$ , top, bottom



## example: the case of $W^{*3}$

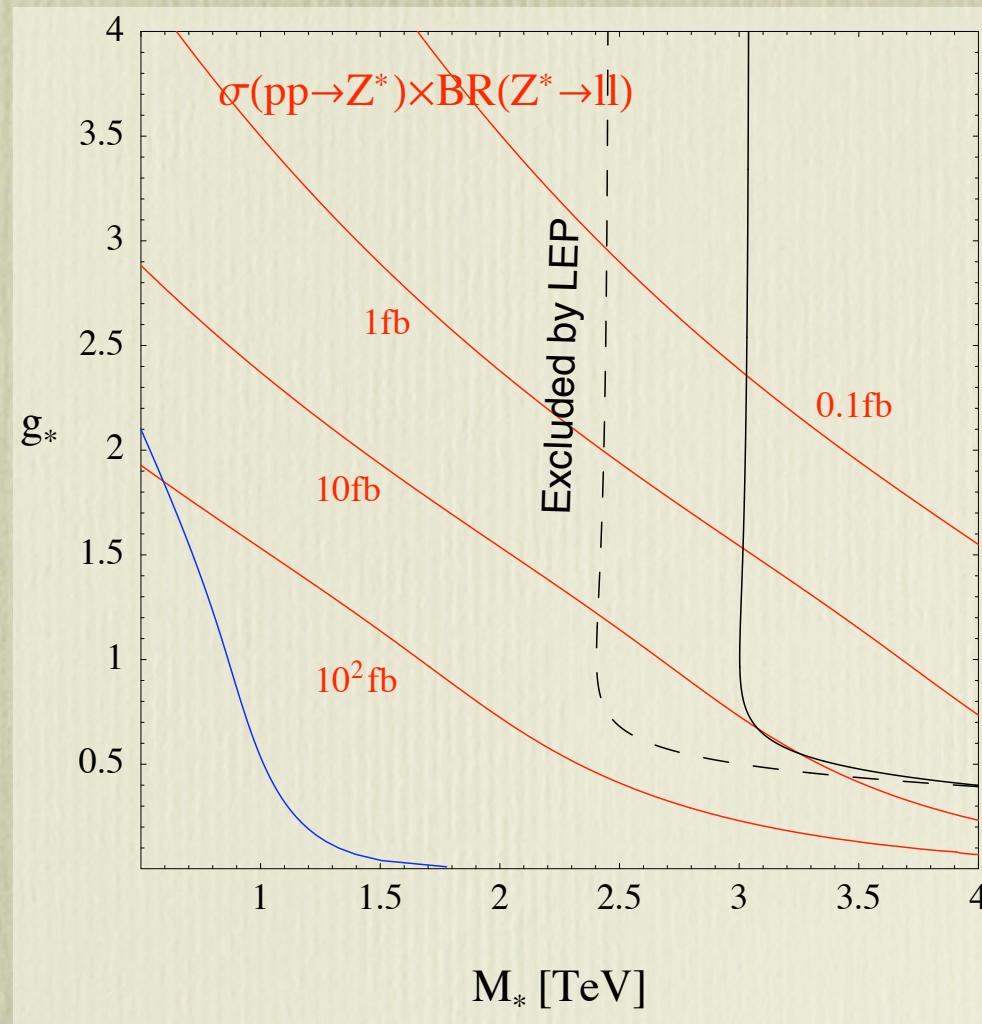
$$\Gamma(W^{*3} \rightarrow q\bar{q}) = 3 \Gamma(W^{*3} \rightarrow l\bar{l}) \simeq \frac{g_2^2 \tan^2 \theta_2}{32\pi} M_*$$

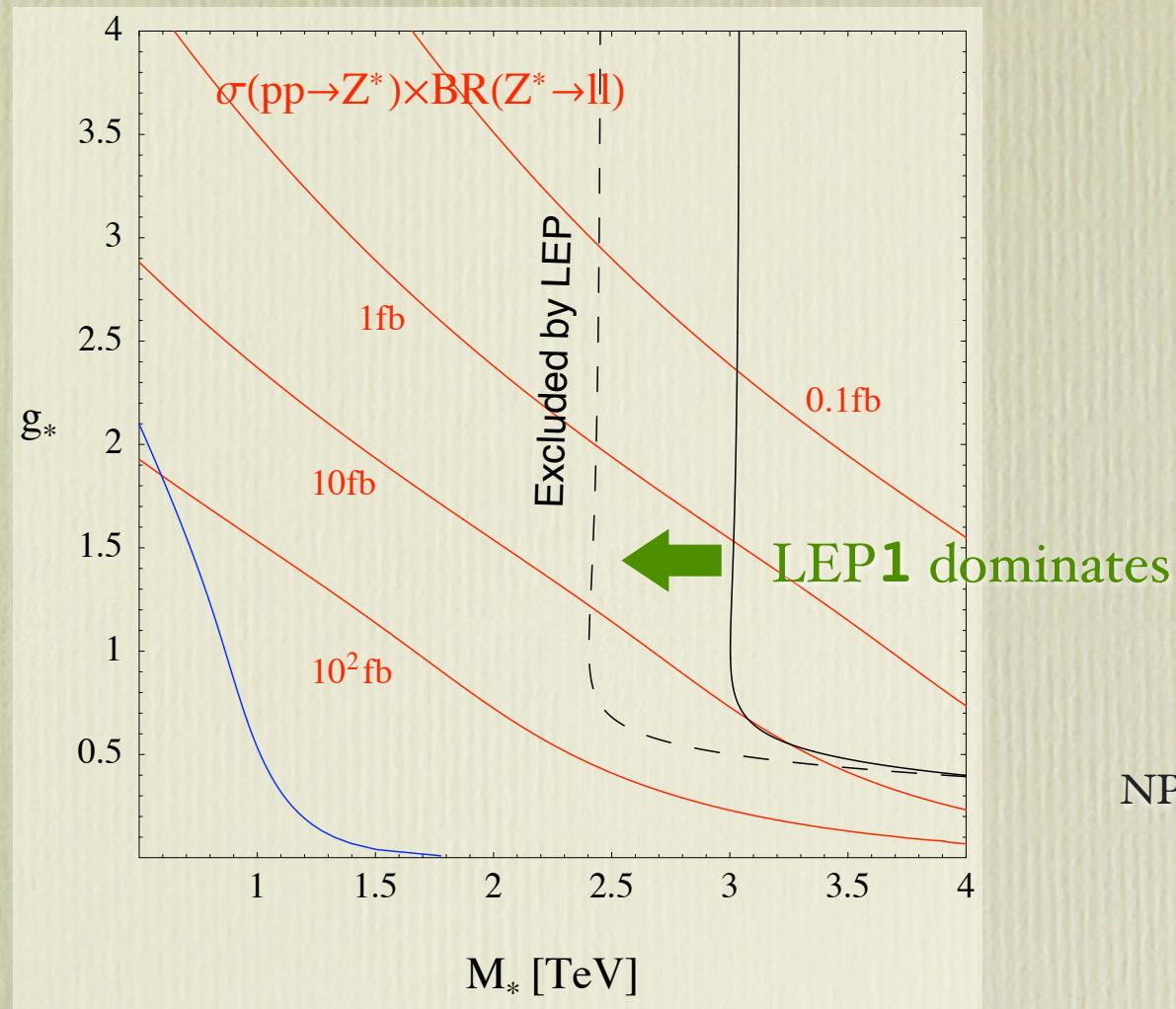
$$\Gamma(W^{*3} \rightarrow t\bar{t}) = \Gamma(W^{*3} \rightarrow b\bar{b}) = (\sin^2 \varphi_{t_L} \cot \theta_2 - \cos^2 \varphi_{t_L} \tan \theta_2)^2 \frac{g_2^2}{32\pi} M_*$$

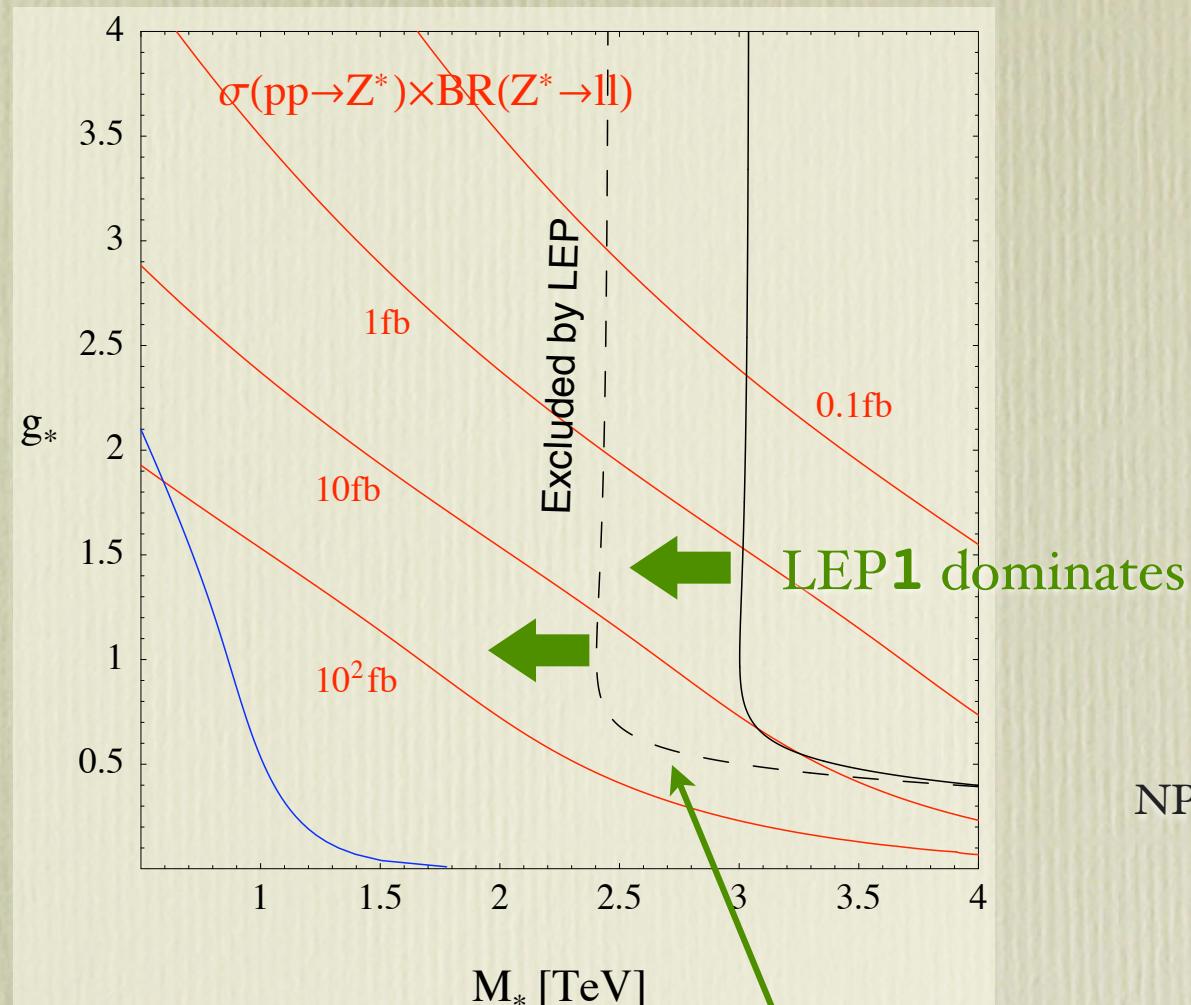
$$\Gamma(W^{*3} \rightarrow ZH) = \Gamma(W^{*3} \rightarrow W^+W^-) = \frac{g_2^2 \cot^2 \theta_2}{192\pi} M_*$$

for  $\begin{cases} M_* = 3 \text{ TeV} \\ \tan \theta_2 = 1/6 \\ \sin \varphi_{t_L} = 0.4 \end{cases}$

$\Gamma_{tot} = 170 \text{ GeV}$ 
  
 $BR(ee, \mu\mu) = 0.1\%$ 
  
 $BR(t\bar{t}, b\bar{b}) = 5\%$

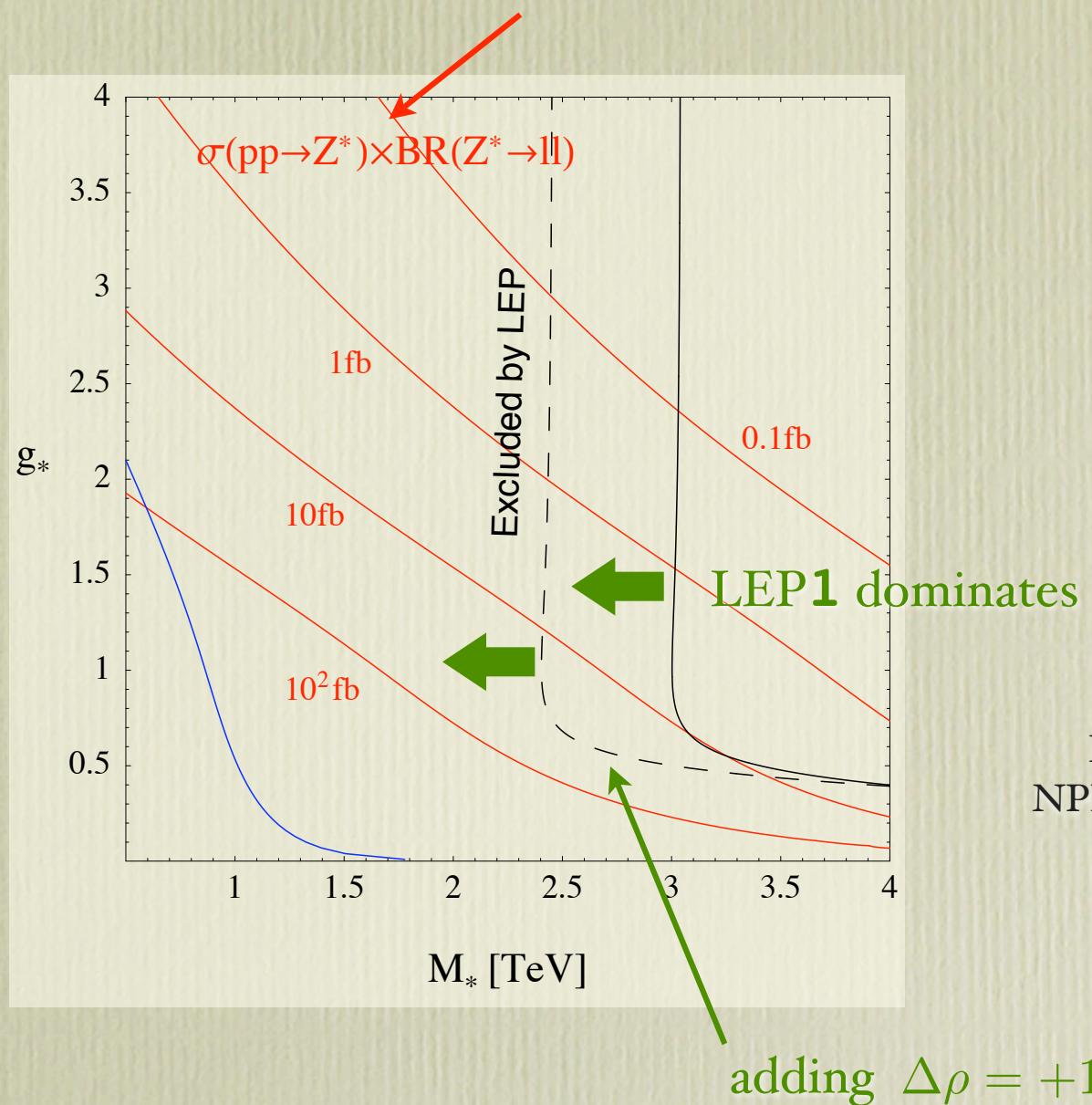






fit from:  
 Barbieri et al.  
 NPB 703 (2004) 127

cross section refers to heavy  $W_{3L}$



# LHC discovery potential

**Z<sup>\*</sup>:**     $M = 2(3) \text{ TeV}$     with     $L = 100(10^3) \text{ fb}^{-1}$     [ Agashe et al., PRD 76 (2007) 115015 ]

$$Z^* \rightarrow W^+W^- \rightarrow l^+l^-\nu\nu$$

$$l\nu jj$$

$$Z^* \rightarrow Zh \rightarrow l^+l^- b\bar{b}$$

$$jj W^+W^- \rightarrow jj l\nu jj$$

**G<sup>\*</sup> (heavy gluon):**     $M = 4 \text{ TeV}$     with     $L = 100 \text{ fb}^{-1}$     [ Agashe et al., hep-ph/0612015 ]

$$G^* \rightarrow t\bar{t}$$

- use of a LR asymmetry
- exploit the highly-boosted tops

# Backup slides

