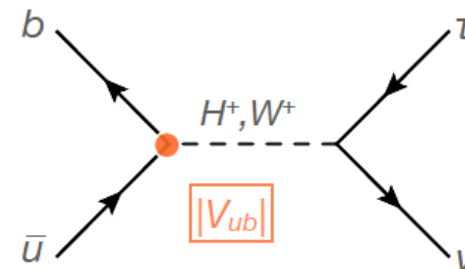
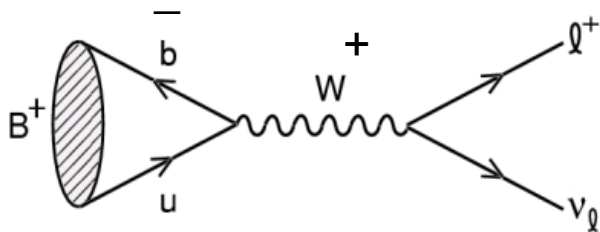


Study of $B \rightarrow \tau \nu$

Mario Merola, Elisa Manoni, Claudia Cecchi, Guglielmo De Nardo

Belle II Italia

Pisa, 20/11/17





Outline



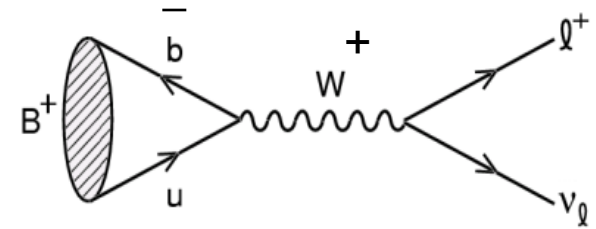
2

*new w.r.t.
last meeting*

- Theory introduction and recent results overview
- Analysis status (as of B2TiP report)
- **Impact of new extra clusters selection**
- **Physics validation – performances comparison MC8 / MC9**
- Conclusions and future plans

- Helicity suppressed

$$BR_{SM}(B \rightarrow l \nu) = \frac{G_F^2 m_B \tau_B}{8\pi} f_B^2 |V_{ub}|^2 m_\ell^2 \left[1 - \frac{m_\ell^2}{m_B^2}\right]^2$$

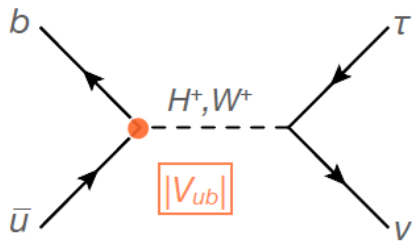


$\tau: \mu: e \rightarrow 1 : 10^{-3} : 10^{-7}$

- The SM predicts a branching ratio of $\mathcal{B}(B^+ \rightarrow \tau^+ \nu_\tau) = 0.817^{+0.054}_{-0.031} \times 10^{-4}$

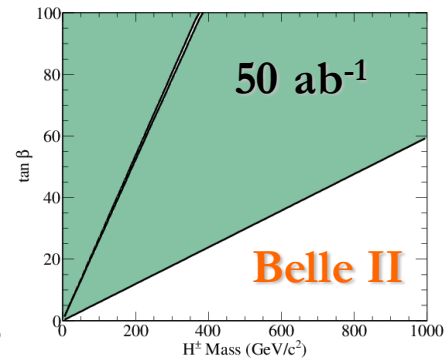
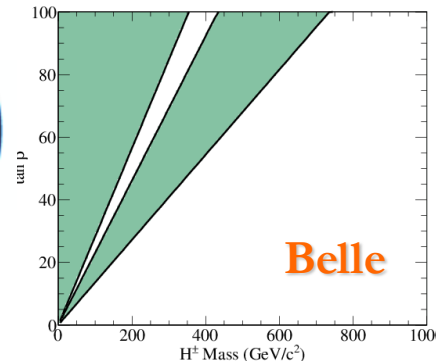
<http://ckmfitter.in2p3.fr/>

Higgs doublet models predict interference with SM decay with a modification of the branching ratio [[PhysRevD.86.054014](#)]

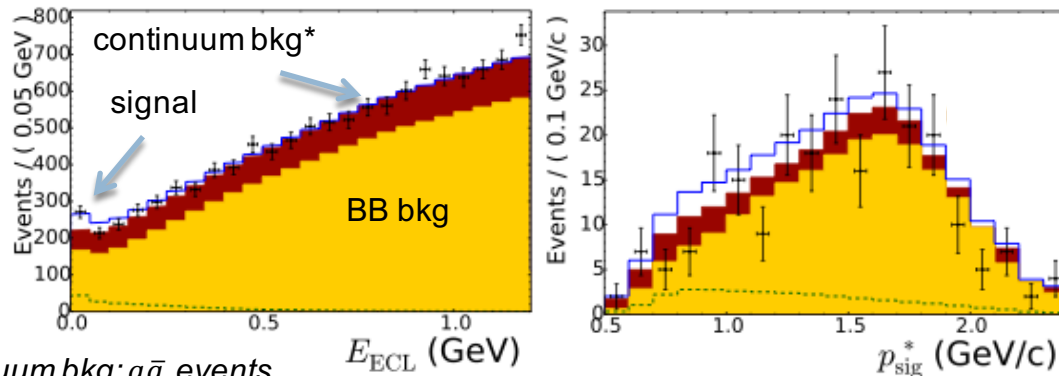


$$B = B_{SM} \times \left(1 - m_B^2 \frac{\tan^2 \beta}{m_{H^\pm}^2}\right)$$

ratio of the two Higgs vacuum expectation values



- First **evidence at Belle** (2006) and **Babar** (2012)
- Most recent measurement (Belle – 2015, using semileptonic tag):
 - use of **multivariate techniques** (neural network) **to reconstruct the tag side**
 - the **signal side** is reconstructed in four modes: $\tau \rightarrow \mu \nu \nu, e \nu \nu, \pi \nu, \rho \nu$
 - the signal is extracted through a **two-dimensional maximum likelihood fit** to the E_{ECL} and p_{sig}^* distributions



*continuum bkg: $q\bar{q}$ events

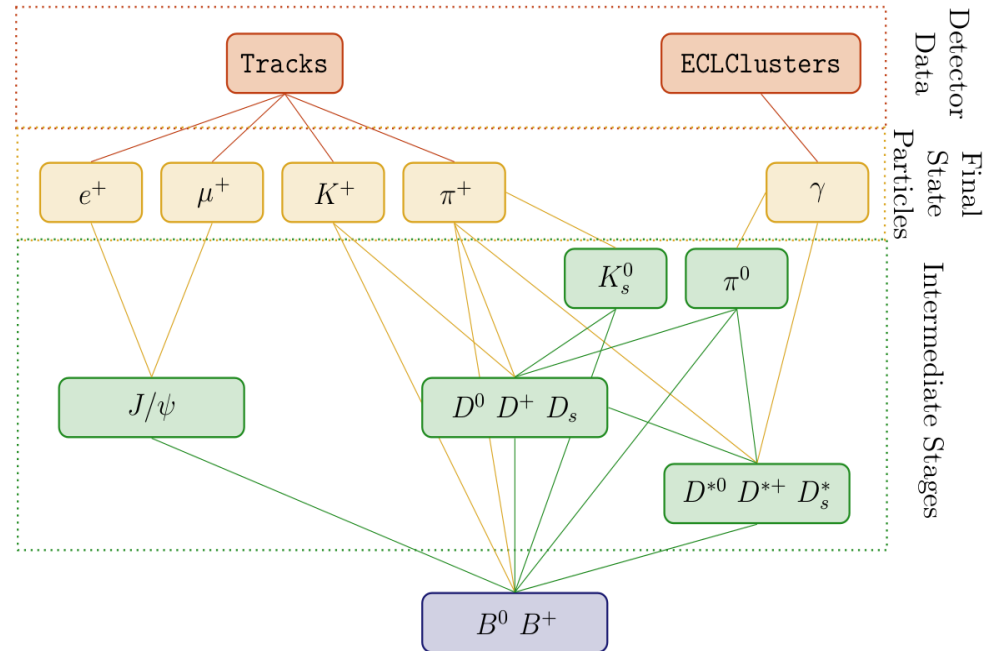
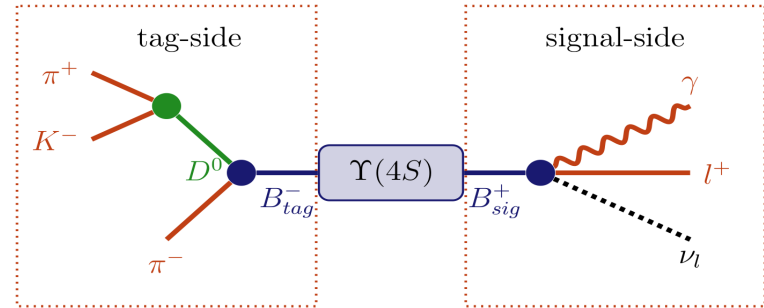
- E_{ECL} (later on called E_{extra}) is the sum of the energies of clusters in the ECL not associated to reconstructed B mesons
- p_{sig}^* is the momentum of the signal side particle in the CM

$$\mathcal{B} = [0.91 \pm 0.19(\text{stat.}) \pm 0.11(\text{syst.})] \times 10^{-4} \quad (\text{evidence at } \sim 4.6 \sigma \text{ level})$$

- Developed by Thomas Keck*, it's an extension of the Full Reconstruction used in Belle, and uses a **multivariate technique to reconstruct the B-tag side** through lots of decay modes in a $\Upsilon(4S)$ decay.

- Hierarchical approach:** first train multivariate classifiers (MVC) on FSP, then reconstruct intermediate particles and build new dedicated MVC. For each candidate a signal probability is defined, which represents the "goodness" of its reconstruction.

- Training performed on $B^+ B^- / B^0 \bar{B}^0$ events with beam background at KEKCC



*<https://ekp-invenio.physik.uni-karlsruhe.de/record/48602/files/EKP-2015-00001.pdf>



Analysis status (B2TiP)

<https://docs.belle2.org/record/389/files/BELLE2-PUB-DRAFT-2016-008.pdf>

B tag side

Hadronic tag using FEI

- 1) Pre-selection on B-tag kinematics*
- 2) Cut on FEI output discriminant
- 3) Pick the highest sigprob B candidate

* Beam-constrained mass: $M_{bc} = \sqrt{E_{beam}^{*2} - p_B^{*2}}$

* Energy difference: $\Delta E = E_B^* - E_{beam}^*$

B sig side

$B \rightarrow \tau \nu$

- 4 tau modes: $\mu \nu \nu, e \nu \nu, \pi \nu, \pi \pi^0 \nu$
- PID, ECL cluster cleaning (see next slide)
- $110 < M(\pi^0) < 160$ MeV
- $625 < M(\rho) < 925$ MeV

Require full reconstruction of tag side and *only one additional track* in the event

Run on MC5 production:

- $100 \cdot 10^6$ events of $B \rightarrow \tau \nu \rightarrow$ generic with beam background
- 1 ab^{-1} of $B^+ B^- / B^0 \bar{B}^0$ and continuum with beam background

<https://confluence.desy.de/display/BI/Computing+MC5Release4Physics>

PID selection

- Likelihood function based on E/p and dE/dx
- Cut on the LR = $L(\text{particle}) / (L(e) + L(\mu) + L(\pi))$

Photon and π^0 selection

Cluster cleaning (to reject photons from beam background) with cuts on photon energy, cluster timing and $E9/E25$ (separately in forward, barrel and backward detector regions). Details at the confluence page:

<https://confluence.desy.de/display/BI/Physics+Pi0+and+extra+clusters+cleaning>

Continuum rejection

- MVA with boosted decision trees to separate back-to-back topology from events with spherical symmetry (BB). See backup for details

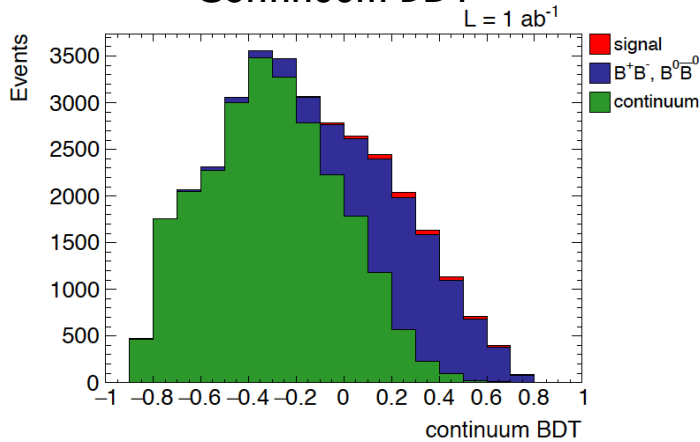
In the post-B2TiP analysis:

Follow PID recommendations:

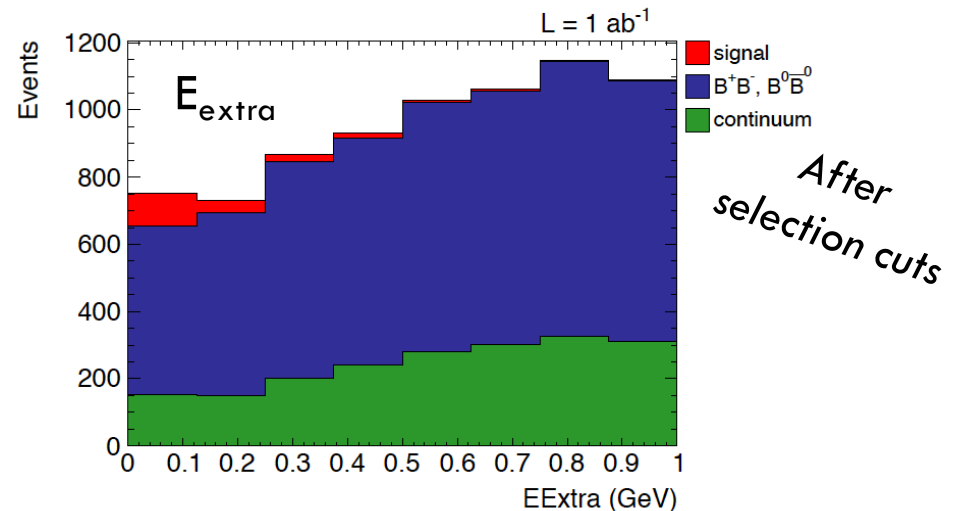
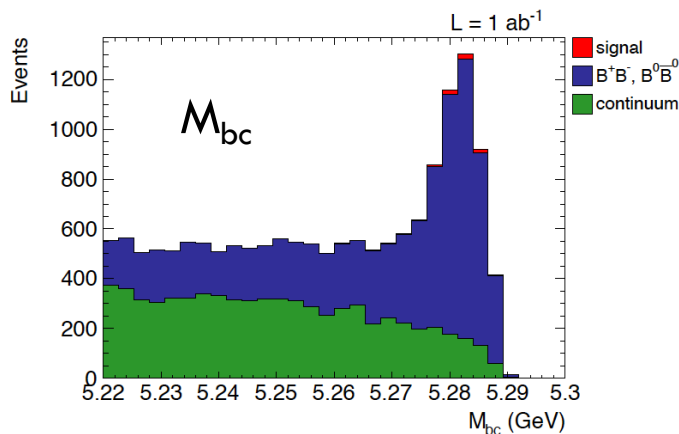
<https://confluence.desy.de/display/BI/Physics+StandardParticles>

New extra energy and π^0 selection (see my talk in the tools session this morning)

Continuum BDT



Cuts on the BDT, M_{bc} , ΔE , missing mass, and signal side track momentum are optimized maximizing the FOM* in the M_{bc} and E_{extra} signal windows (respectively 5.275-5.29 GeV/c^2 and 0-0.2 GeV). Optimization for hadronic and leptonic tau decay modes separately



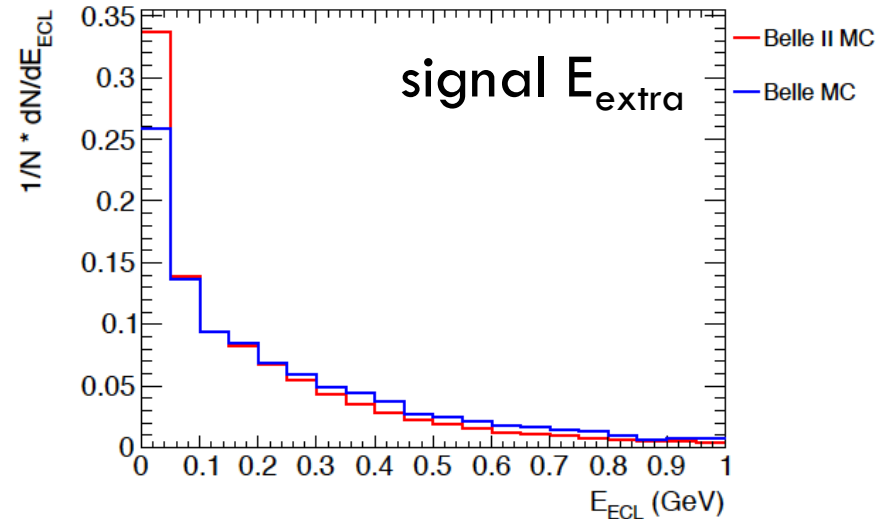
In the plots shown here and in the next slides signal and bkg are normalized to 1 ab^{-1}

* $S/\sqrt{S+B}$ where S is $B \rightarrow \tau \nu$ and B is $BB + \text{continuum bkg}$, normalized to 1 ab^{-1}

Signal and background event yields in 1 ab^{-1}

	E_{ECL}	$< 1 \text{ GeV}$	$< 0.25 \text{ GeV}$
Belle II	# background events	7420	1348
	# signal events	188	136
	signal efficiency (‰)	2.2	1.6
Belle*	# background events	2160	365
	# signal events	97	60
	signal efficiency (‰)	1.2	0.7

[*PRL 110, 131801 \(2013\)](#)



- In Belle II we have **higher bkg** contamination and **higher signal efficiency**
- Statistical improvement ($S/\sqrt{S+B}$), but we **need to evaluate the systematics impact** (e.g. uncertainty on the peaking background)
- E_{extra} has a narrow peak at 0 for Belle II MC \rightarrow better extra clusters reconstruction despite higher beam background

- **Branching ratio:** fit to the E_{extra} distribution for toy MC pseudo-datasets and take mean and width of the results
- **p-value determination:** use the test statistics $Q = L(s+b)/L(b)$ evaluated on pseudo-datasets sampled from $S+B$ and B only E_{extra} distributions.

$$\text{BR}(B \rightarrow \tau\nu) = 0.82 \pm 0.24 \times 10^{-4} \sim 30\% \text{ precision}$$

$$\text{p-val} = 0.000385 \rightarrow \text{significance: } 3.4 \sigma$$

in 1 ab^{-1}

- The main **systematic uncertainties** are: signal and background E_{Extra} PDFs, branching fractions of the peaking backgrounds, tagging efficiency, and K_L^0 veto efficiency (followed by the signal efficiency and others)

Systematics extrapolation based on Belle II note*

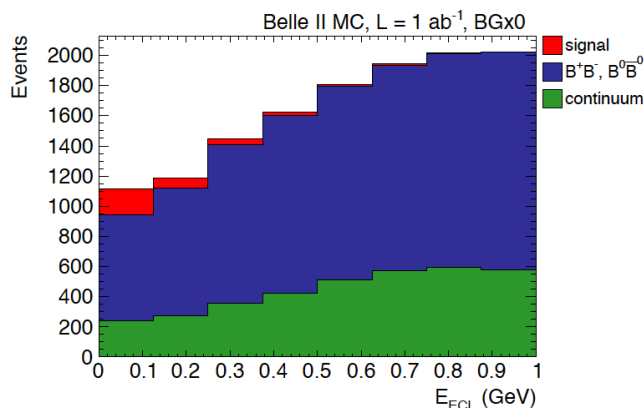
Integrated Luminosity (ab^{-1})	1	5	50
statistical uncertainty (%)	29.2	13.0	4.1
systematic uncertainty (%)	12.6	6.8	4.6
total uncertainty (%)	31.6	14.7	6.2

luminosity needed for $B \rightarrow \tau\nu$ 5σ
 observation is 2.6 ab^{-1}

* Belle2-note-0021

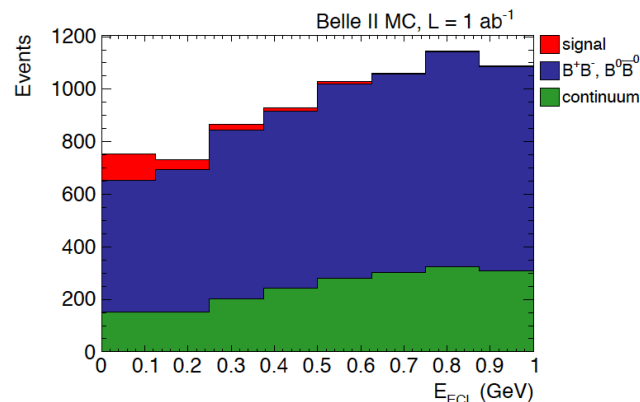
- Impact of beam background evaluated re-performing the study described above on MC5 samples without beam background

BGx0



E_{ECL}	< 1 GeV	< 0.25 GeV
# background events	12835	2062
# signal events	332	238
signal efficiency (%)	3.8	2.7

BGx1



E_{ECL}	< 1 GeV	< 0.25 GeV
# background events	7420	1348
# signal events	188	136
signal efficiency (%)	2.2	1.6

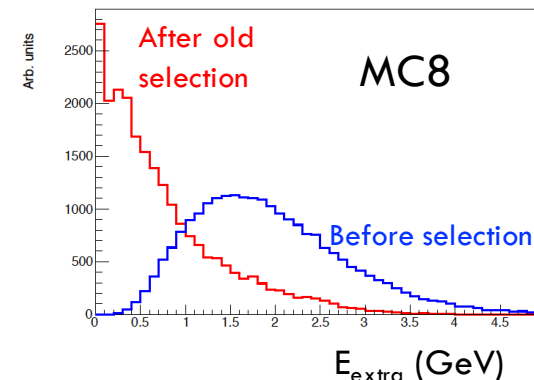
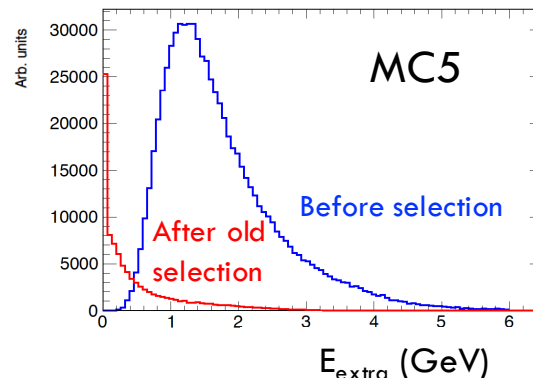
- Toy MC: expected precision for BGx0 is 20% (30% for BGx1) with a significance $> 5\sigma$ in 1 ab^{-1}



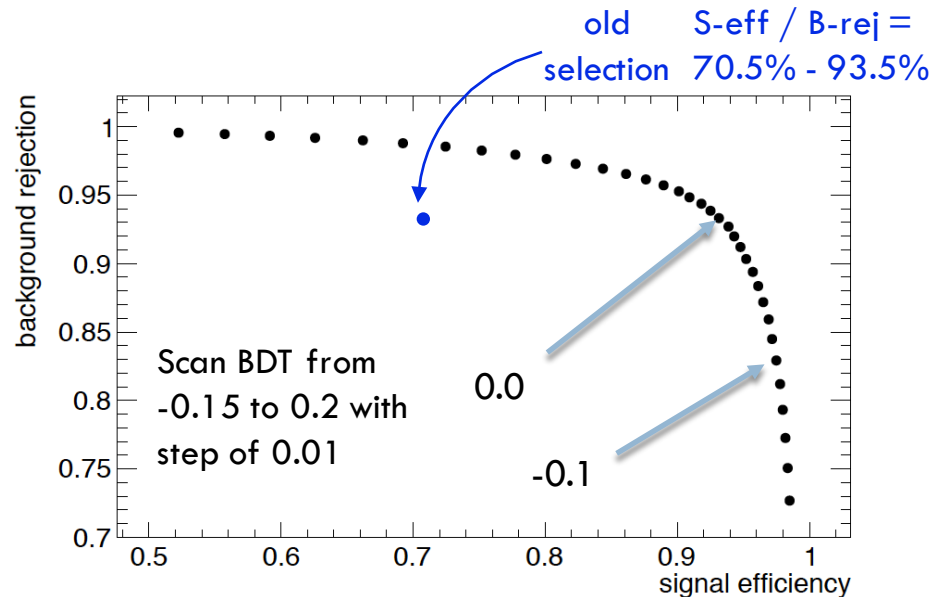
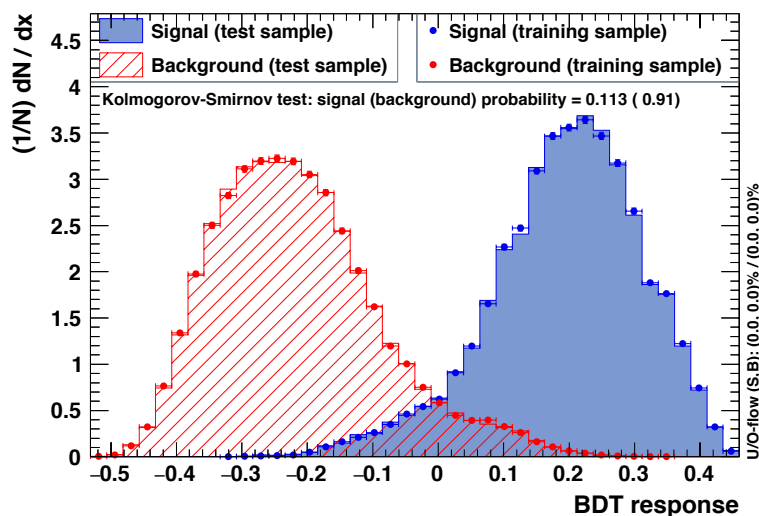
Analysis update

- **PID selection**
 - Use the release-09 recommended working points (95-99% efficiencies)
<https://confluence.desy.de/display/BI/Physics+StandardParticles>
- **Extra clusters and pi0 selection**
 - See presentation at the tools session this morning: **MVA classifiers** trained for the extra clusters and pi0s
 - The selection used in the analysis presented before performs much worse with the increased level of background of the last MC campaigns (MC8 and MC9)

E_{extra} in $B \rightarrow \tau \nu$ events
with the old selection



TMVA overtraining check for classifier: BDT

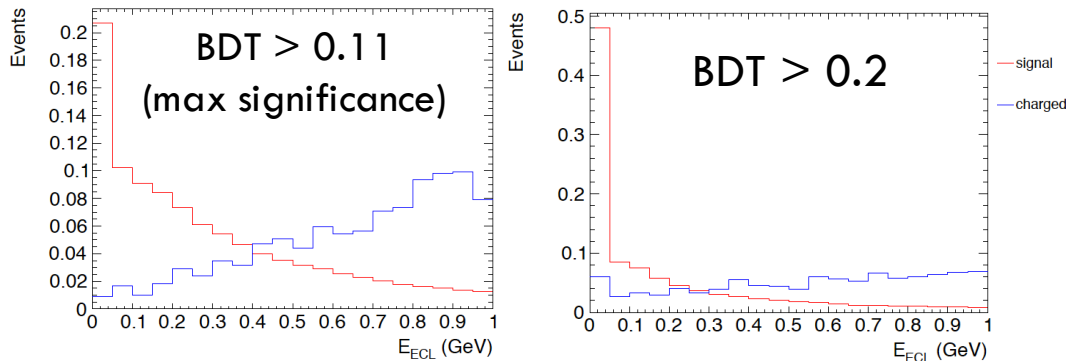
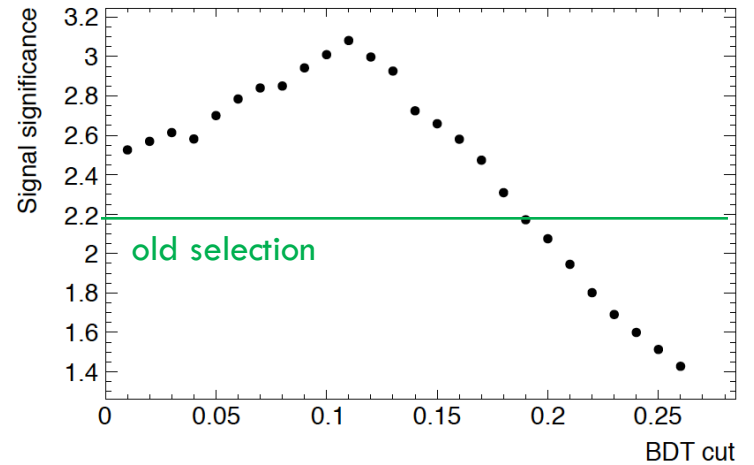
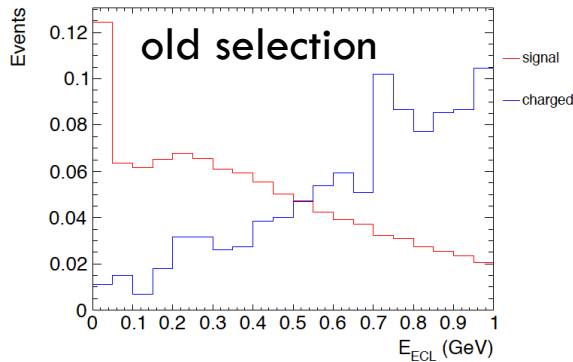


- Consider **cluster variables**: energy, timing and cluster shape
- Train a BDT with $B \rightarrow \tau\nu$ events from MC9 production b \times 1 (using TMVA)

At same signal efficiency level, we have $\epsilon_{\text{bkg}}=1.5\%$ with respect to 6.5% of old selection \rightarrow ~80% more bkg rejected

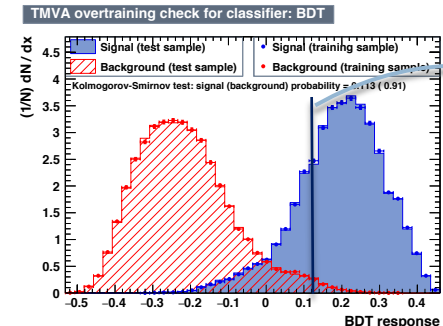
To choose the optimal cut point look at the E_{extra} distributions for $B \rightarrow \tau\nu$ and generic BB (next slide)

- E_{extra} distribution for tau nu signal and B^+B^- background with $M_{bc} > 5.27$ GeV



Better signal shape but increasing background yield in signal region ($E_{\text{extra}} < 0.2$ GeV)

Significance evaluated as $S/\sqrt{S+B}$ in $E_{\text{extra}} < 0.2$ GeV, where S is tau nu and B is B^+B^- . Normalized to 1 ab^{-1}



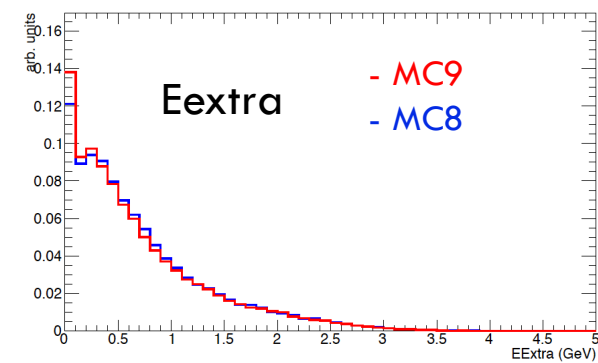
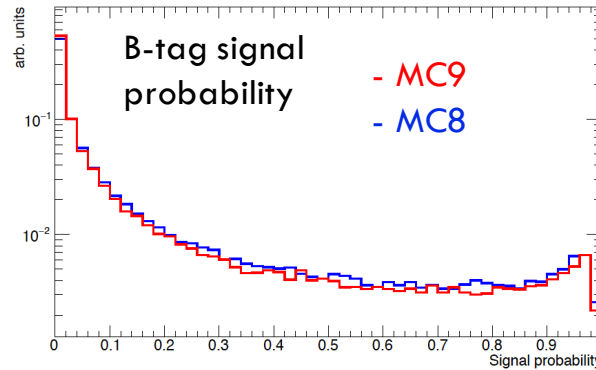
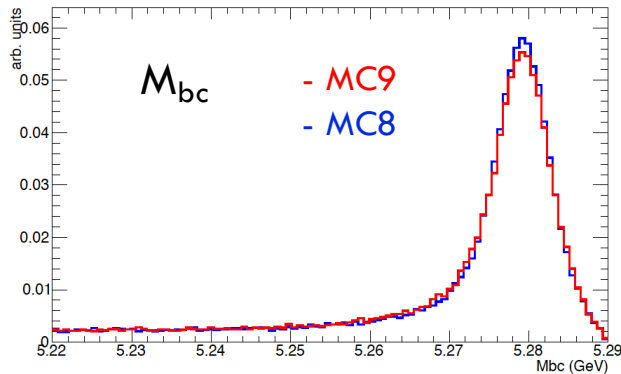
S-eff / B-rej = 80% / 97.5%

WG1 validation

<https://confluence.desy.de/display/BI/Data+Production+Validation>

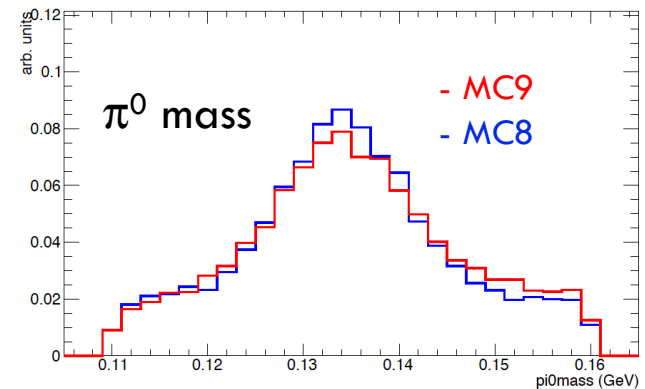
- Within the leptonic, semi-leptonic and missing energy B decays working group we have four modes for analysis validation: $B \rightarrow \tau \nu$, $B \rightarrow \pi l \nu$, $B \rightarrow D^* l \nu$, $B \rightarrow D^* \tau \nu$
- The basic idea is set up a simple analysis for each mode and check the effect of the changes from a software release to an other

- Comparison between MC8 and MC9 (bgx1)

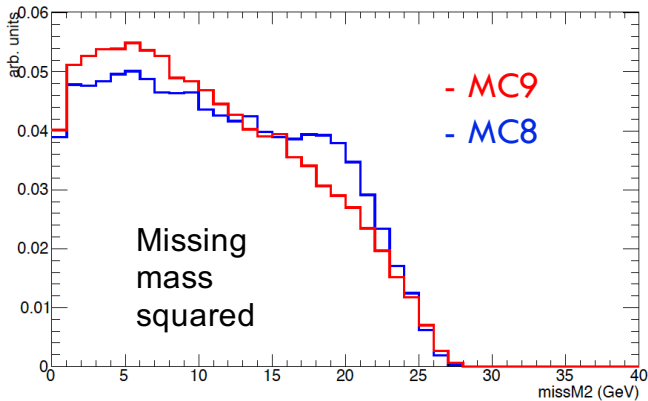


Brief summary of the reconstruction steps:

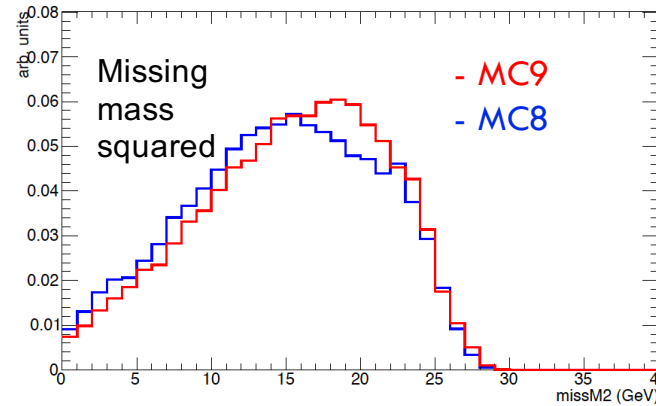
- Reconstruct the B-tag with Full Event Interpretation and pick the best candidate per event
- Require only 1 track on the signal side, PID (four τ decay channels considered: $\mu\nu\nu$, $e\nu\nu$, $\pi\nu$, $\pi\pi^0\nu$) and neutrals quality criteria



hadronic modes



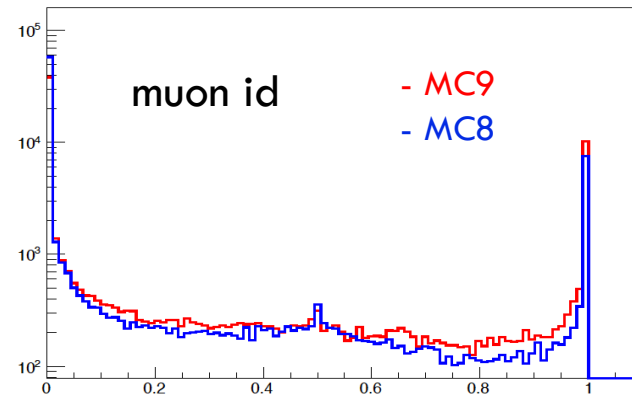
leptonic modes



$$M_{miss}^2 = \left(2E_{beam} - E_{B_{tag}} - E_{B_{sig}} \right)^2 - \left| \vec{p}_{B_{tag}} + \vec{p}_{B_{sig}} \right|^2$$

efficiency	MC9/MC8
TOT	84%
Lep modes (mu/ele)	99% (135% / 81%)
Had modes ($\pi\nu$ / $\pi\pi^0\nu$)	75% (76% / 73%)

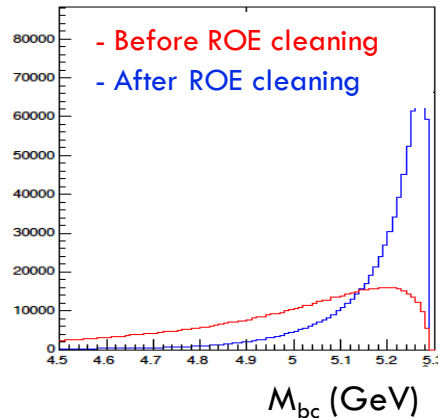
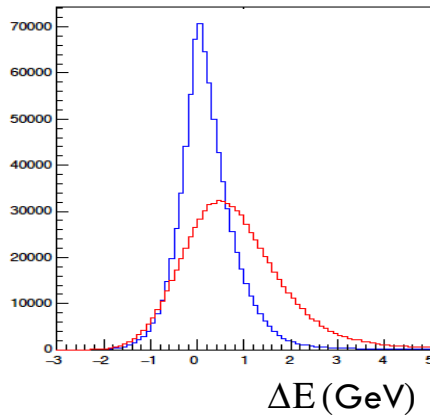
electron: eid; muon: muid and !(eid)
 pion: piid and !(muid) and !(eid)



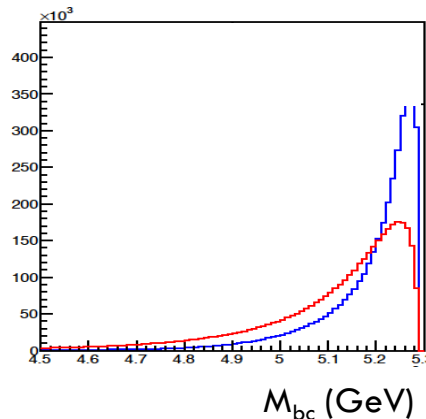
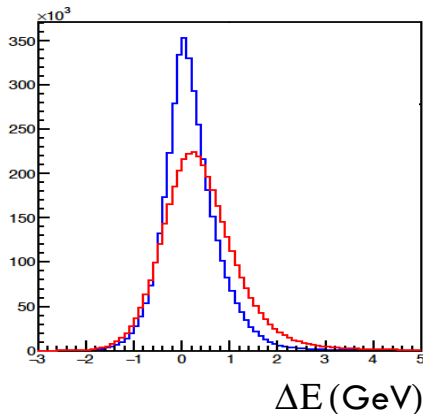
Improvement of muid in MC9

Comparison between MC8 and MC9

MC8



MC9



- Reconstruct the signal $B \rightarrow \pi l \nu$
- Apply tracks and cluster cleaning* to the Rest of Event (ROE) of the signal

*remove tracks originating far from the IP and remove low energetic / out-of-time clusters

MC9/MC8 \sim 82%

“Before ROE” distribution looks better in MC9: from release 09 we have a new 99% efficient cut on the cluster timing at mdst level ($|t|/dt99 < 1$ for $E < 50$ MeV, where $dt99$ is the time containing the 99% of the signal)

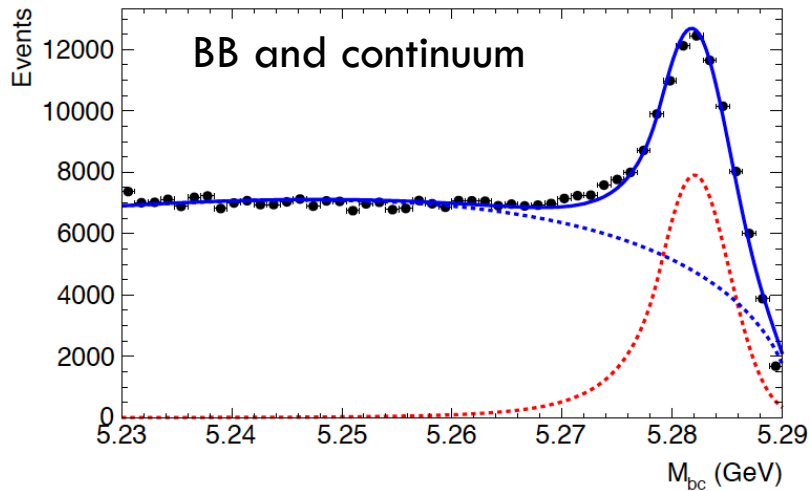
- $B \rightarrow \tau \nu$ sensitivity study on 1 ab^{-1} of MC5 production: precision on the branching ratio measurement found to be 30% (3.4σ stat. only) with beam bkg, and 20% ($>5\sigma$ stat. only) without beam bkg. Including systematic uncertainties the observation (5σ) is expected at 2.6 ab^{-1}
- Analysis update with last MC9 campaign
 - New MVA selection for extra clusters and π^0 - improvement of signal / BB separation in E_{extra}
 - **To do list:**
 - Evaluate the impact of the MVA on the branching ratio measurement (after continuum suppression and selection cuts)
 - Study the peaking background - KL veto
 - Signal extraction: 2D fit with E_{extra} and missing mass
- Validation studies comparing MC8 and MC9 show improved PID and robust reconstruction against beam background



Backup

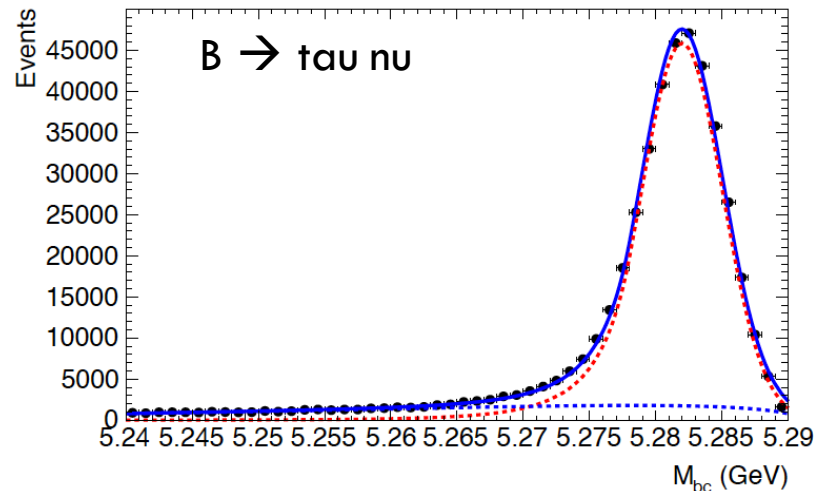


- Purity of the background and signal samples is evaluated via fit to M_{bc} distribution with Argus (combinatorics) + double gaussian (true B candidates)



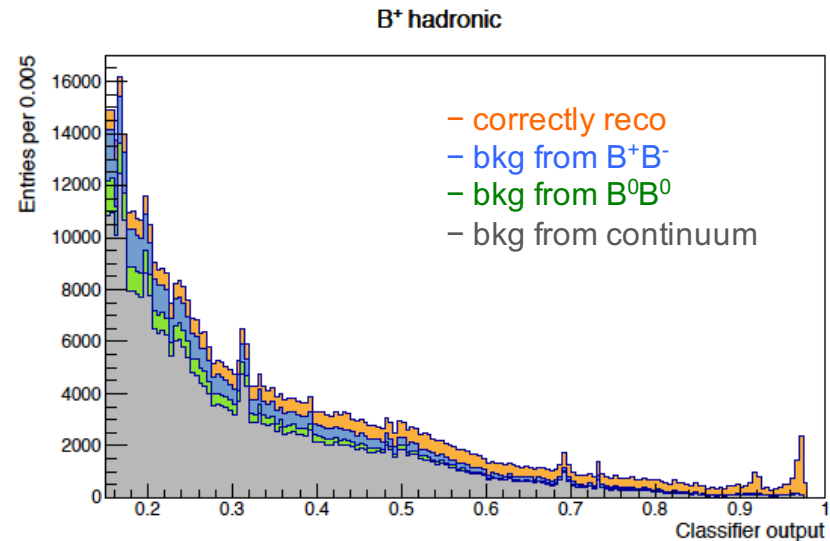
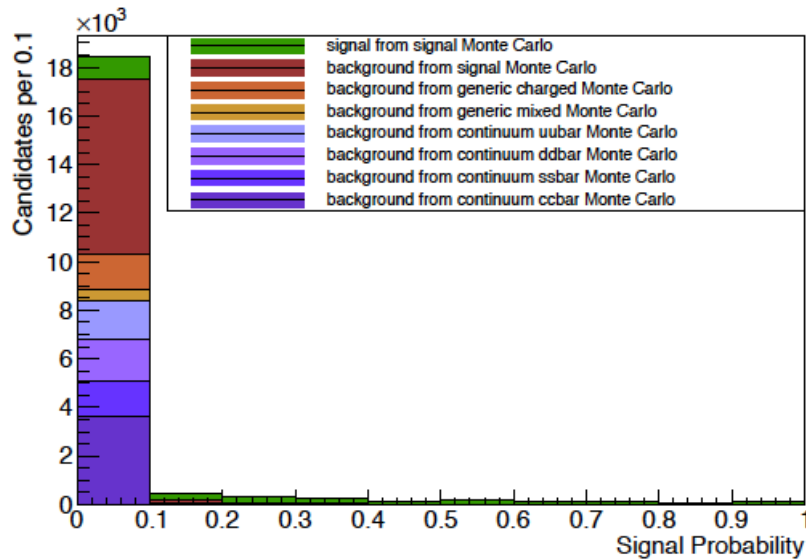
Purity ~50%

continuum rejection applied



Purity ~93%

- Input variables used to train the multivariate classifiers:
 - PID, tracks momenta, impact parameters (**charged FS particles**);
 - cluster info, energy and direction (**photons**);
 - invariant mass, angle between photons, energy and direction (π^0);
 - released energy, invariant mass, daughter momenta and vertex quality ($D^{(*)}_{(s)}$, J/ψ);
 - the same as previous step plus vertex position, ΔE (**B**);
 - additionally, for each particle the **classifier output of the daughters** are also used as discriminating variables.



from Christian Pulvermacher PhD thesis

Total reconstruction efficiency compared with Belle I

Belle II

B^+ (hadronic)	0.78 %	B^+ (semileptonic)	1.05 %
B^0 (hadronic)	0.59 %	B^0 (semileptonic)	1.17 %

Belle I

B^+ (hadronic)	0.39 %	B^+ (semileptonic)	0.80 %
B^0 (hadronic)	0.28 %	B^0 (semileptonic)	0.86 %

Belle paper, hadronic tag,
PRL 110, 131801 (2013)

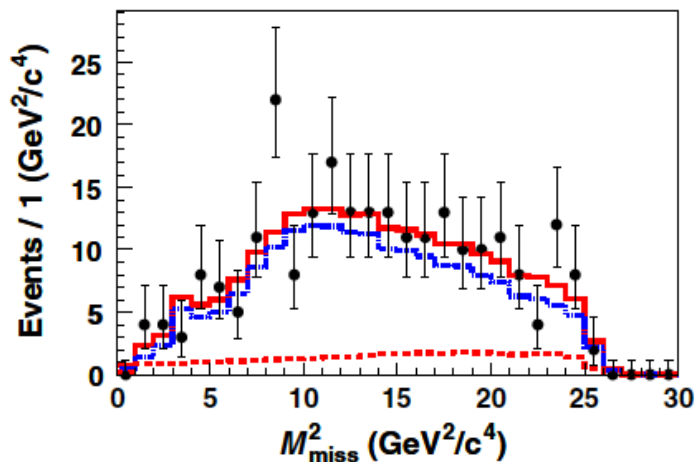
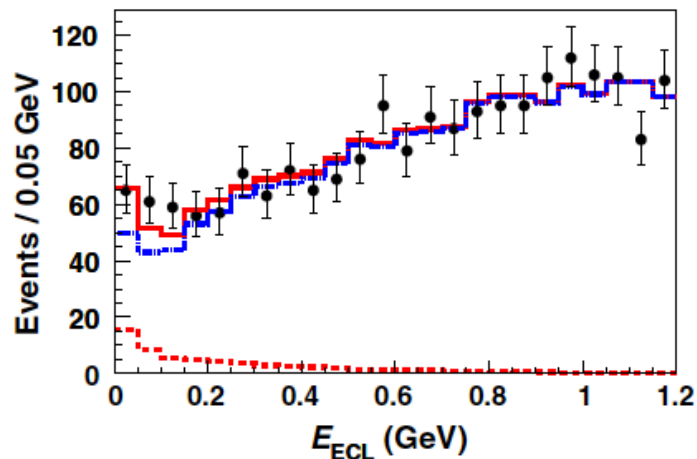
Entire Belle data sample $\sim 700 \text{ fb}^{-1}$

TABLE I. Results of the fit for $B^- \rightarrow \tau^- \bar{\nu}_\tau$ yields (N_{sig}), detection efficiencies (ϵ), and branching fractions (\mathcal{B}). The efficiencies include the branching fractions of the τ^- decay modes. The errors for N_{sig} and \mathcal{B} are statistical only.

Submode	N_{sig}	ϵ (10^{-4})	\mathcal{B} (10^{-4})
$\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau$	16_{-9}^{+11}	3.0	$0.68_{-0.41}^{+0.49}$
$\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau$	26_{-14}^{+15}	3.1	$1.06_{-0.58}^{+0.63}$
$\tau^- \rightarrow \pi^- \nu_\tau$	8_{-8}^{+10}	1.8	$0.57_{-0.59}^{+0.70}$
$\tau^- \rightarrow \pi^- \pi^0 \nu_\tau$	14_{-16}^{+19}	3.4	$0.52_{-0.62}^{+0.72}$
Combined	62_{-22}^{+23}	11.2	$0.72_{-0.25}^{+0.27}$

$$\mathcal{B}(B^- \rightarrow \tau^- \bar{\nu}_\tau) = [0.72_{-0.25}^{+0.27}(\text{stat}) \pm 0.11(\text{syst})] \times 10^{-4}$$

Significance: 3.0σ



Y4S photons

- $E > 72 \text{ MeV}$, $-114 < \text{clusterTiming} < -46$, $E9E25 > 0.800$, $\text{minC2HDist} > 39 \text{ cm}$ – forward
- $E > 71 \text{ MeV}$, $-112 < \text{clusterTiming} < -48$, $E9E25 > 0.805$, $\text{minC2HDist} > 29 \text{ cm}$ – barrel
- $E > 66 \text{ MeV}$, $-142 < \text{clusterTiming} < -18$, $E9E25 > 0.710$, $\text{minC2HDist} > 23 \text{ cm}$ – backward

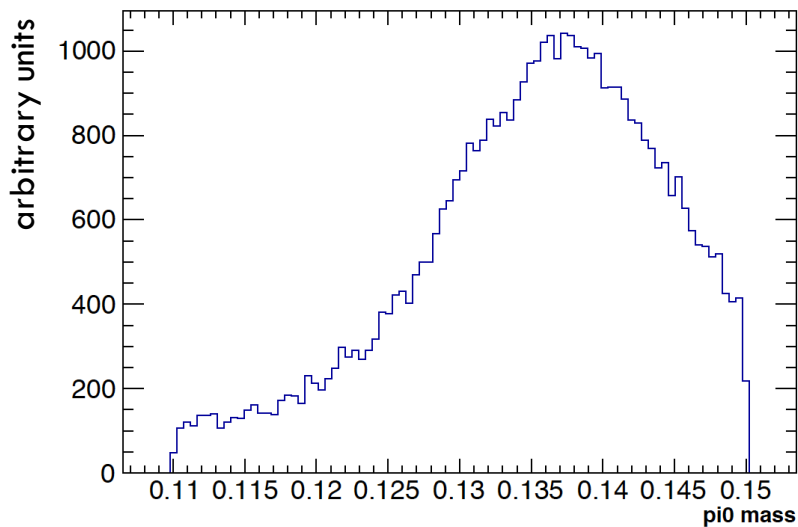
Each cut corresponds to an efficiency of photons from physics of 95%

Extra photons

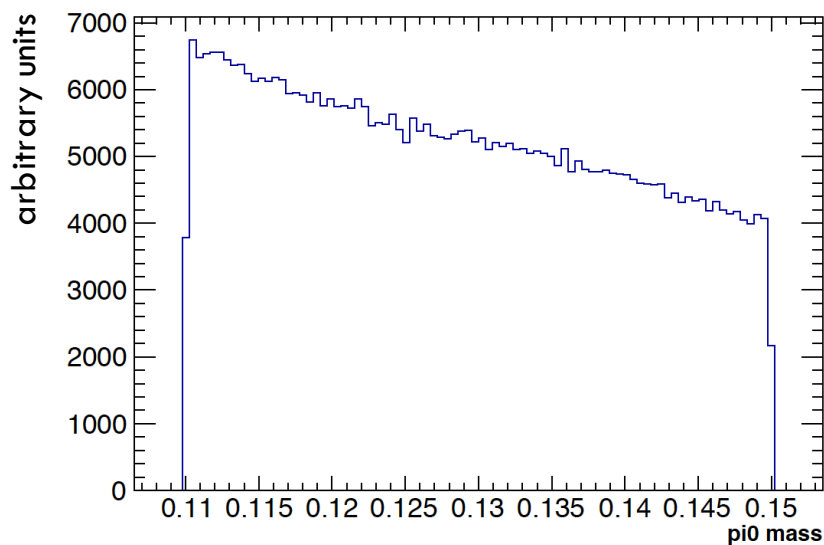
- $E > 48 \text{ MeV}$, $-121 < \text{clusterTiming} < -39$, $E9E25 > 0.665$, $\text{minC2HDist} > 32 \text{ cm}$ – forward
- $E > 51 \text{ MeV}$, $-123 < \text{clusterTiming} < -37$, $E9E25 > 0.685$, $\text{minC2HDist} > 22 \text{ cm}$ – barrel
- $E > 49 \text{ MeV}$, $-151 < \text{clusterTiming} < -9$, $E9E25 > 0.650$, $\text{minC2HDist} > 24 \text{ cm}$ – backward

Each cut corresponds to an efficiency of photons from physics of 90%

After selection



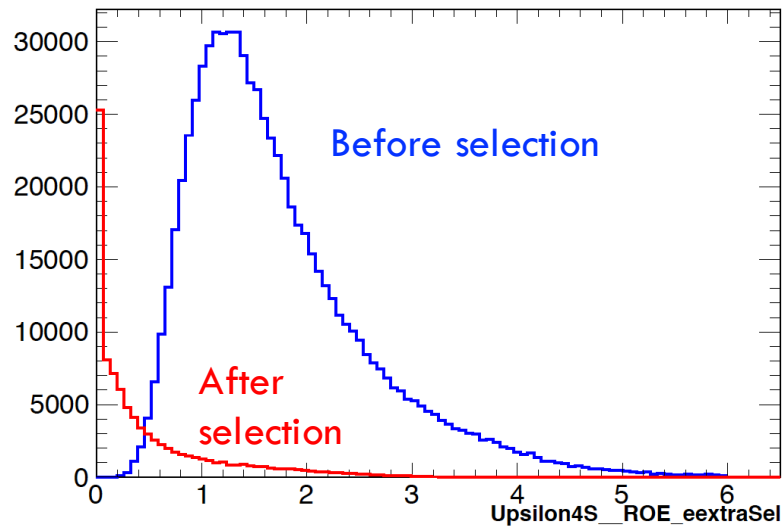
Before selection



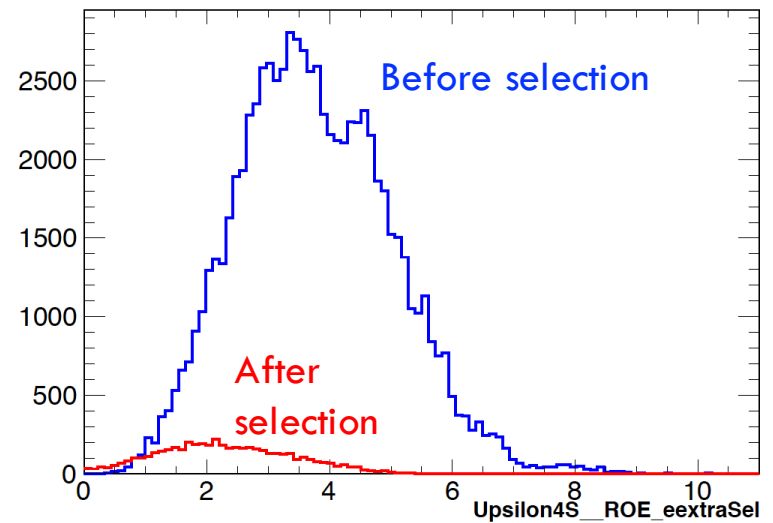
Signal $B \rightarrow \tau \nu$ sample

Extra cluster cleaning selection

signal $B \rightarrow \tau \nu$



B^+B^- bkg



Photon and PID selection eff: 12.2 %

N.B. before PID selection we have a lot of multiple candidates (particle reconstructed as mu and ele and pi)

- Input Variables:** R_2 , $\text{Cos}\theta_{th}$, Cleo Cones and Kakuno Super Fox-Wolfram (KSFW) moments: 30 variables

- R2:** $R_2 = H_2/H_0$ where $H_l = \sum_j \frac{|\vec{p}_i||\vec{p}_j|}{W^2} P_l(\cos\vartheta_{ij})$ are the Fox-Wolfram moments

- Cos θ_{th} :** $|\cos(\vartheta_{thrust})| = \frac{|\vec{p}_B \cdot \hat{T}|}{|\vec{p}_B|}$ where T is the thrust axis of the rest of the event

- Cleo Cones:** momentum flow around the B thrust axis in 9 angular bins

- KSFW:**
$$KSFW = \sum_{l=0}^4 R_l^{so} + \sum_{l=0}^4 R_l^{oo} + \gamma \sum_{n=1}^{N_t} |(P_t)_n|$$

so: particles from b-tag
and ROE are considered
oo: particles from ROE
only are considered

c: charged,
n: neutral,
m: missing

$$R_l^{so} = \frac{\alpha_{cl} H_{cl}^{so} + \alpha_{nl} H_{nl}^{so} + \alpha_{ml} H_{ml}^{so}}{E_{beam}^* - \Delta E}$$

scalar sum of the transverse
momentum of each particle

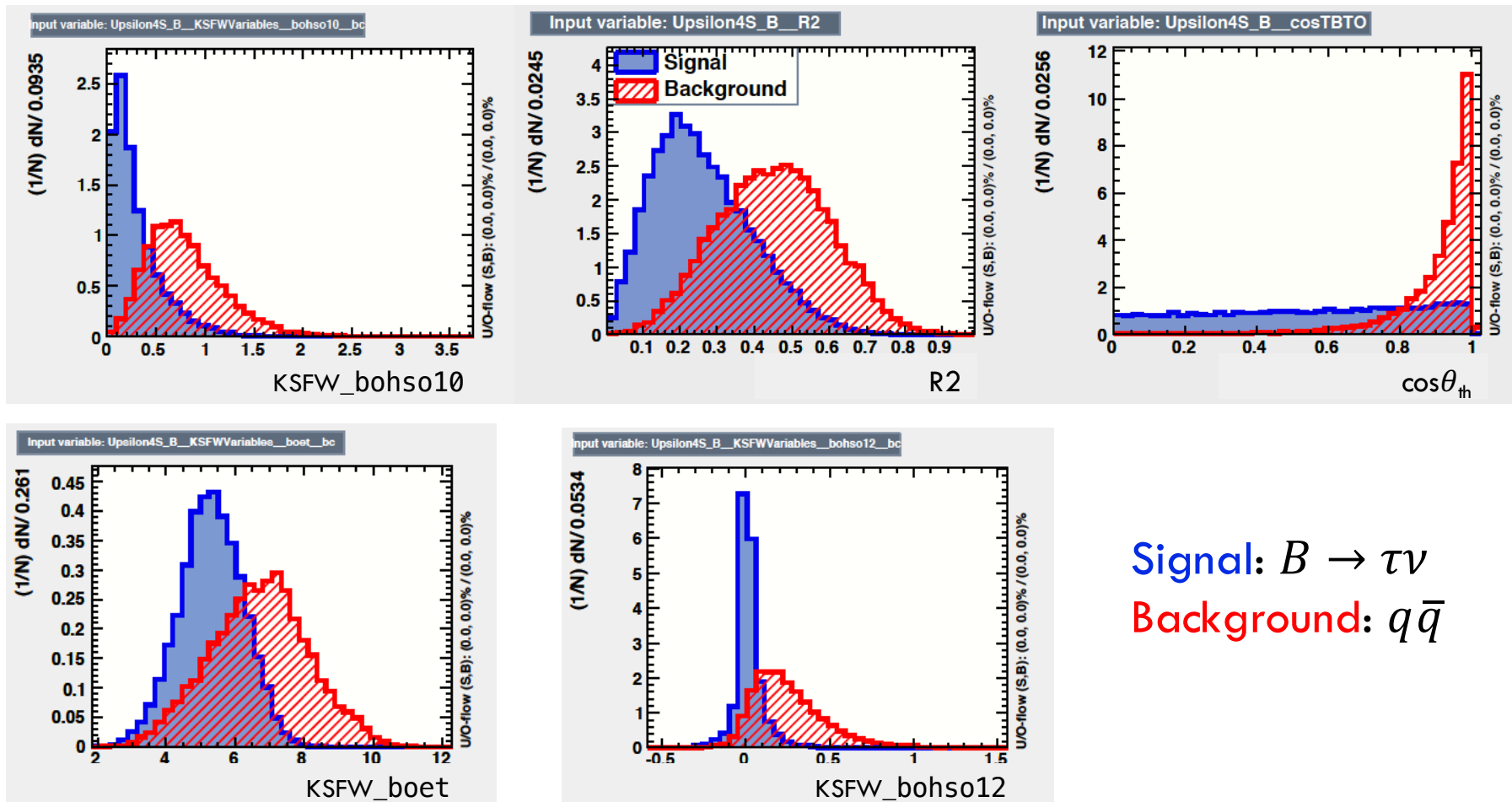
$$l \text{ odd} \quad H_{cl}^{so} = \sum_i \sum_{jx} Q_i Q_{jx} |p_{jx}| P_l(\cos\theta_{i,jx})$$

$$l \text{ odd} \quad R_l^{oo} = \sum_j \sum_k \beta_l Q_j Q_k |p_j| |p_k| P_l(\cos\theta_{j,k})$$

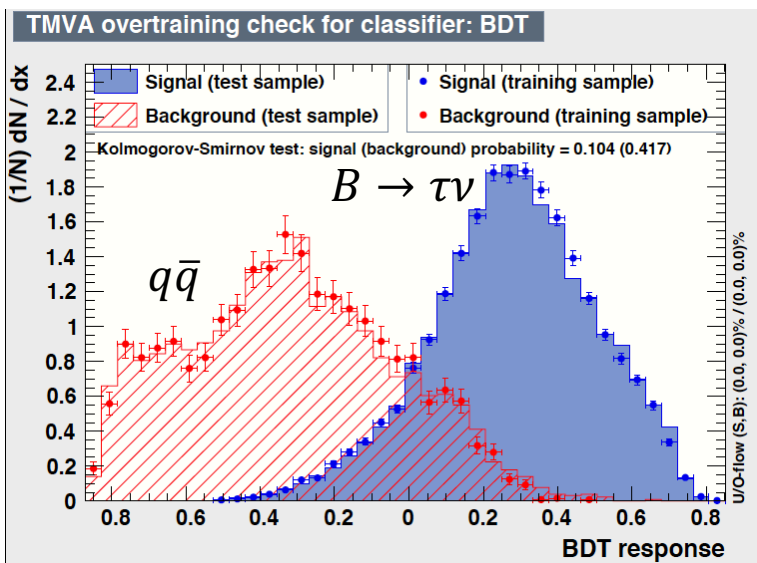
$$l \text{ even} \quad H_{xl}^{so} = \sum_i \sum_{jx} |p_{jx}| P_l(\cos\theta_{i,jx})$$

$$l \text{ even} \quad R_l^{oo} = \sum_j \sum_k \beta_l |p_j| |p_k| P_l(\cos\theta_{j,k})$$

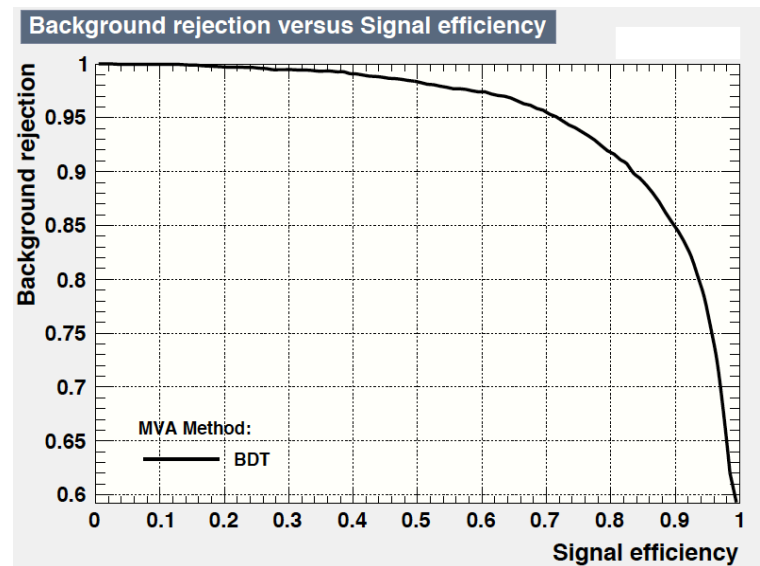
- **BDT training**
 - Preselection cuts on M_{bc} (5.27-5.29 GeV/c²) and E_{extra} (< 0.3 GeV)
 - 20000/3000 events used for signal/background training (~3/10% of the entire samples)
 - Remove the “less powerful” (according to the BDT variable ranking) and highly correlated variables → 20 variables left with a negligible degradation of the BDT performances (i.e. ROC curve integral)



Signal: $B \rightarrow \tau\nu$
 Background: $q\bar{q}$



Overtraining under control
 Limited statistics for the backgrounds



ROC curve

- Good separation power

Hadronic tag

Integrated Luminosity (ab^{-1})	1	5	50
statistical uncertainty (%)	29.2	13.0	4.1
systematic uncertainty (%)	12.6	6.8	4.6
total uncertainty (%)	31.6	14.7	6.2

Semileptonic tag

Integrated Luminosity (ab^{-1})	1	5	50
statistical uncertainty (%)	19.0	8.5	2.7
systematic uncertainty (%)	17.9	8.7	4.5
total uncertainty (%)	26.1	12.2	5.3