

# B decay and CP violation

## *CKM angles and sides*

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For the B Factories

# Outline

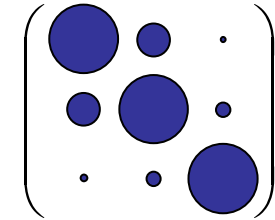
- The CKM matrix and Unitarity Triangle
- The BABAR and BELLE dectectors
- Side measurements
  - $B_d$  and  $B_s$  mixing
  - $V_{cb}$  inclusive & exclusive
  - $V_{ub}$  inclusive & exclusive
  - *No time for Radiative decays !*
- CKM angle measurements
  - $\beta / \phi_1$
  - $\alpha / \phi_2$
  - $\gamma / \phi_3$

# The CKM matrix

quark mixing matrix of charged current interactions

- **CKM matrix definition:**

$$\mathcal{L}_{W^\pm} = -\frac{g}{\sqrt{2}} (\bar{u}_L \quad \bar{c}_L \quad \bar{t}_L) \gamma^\mu \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d_L \\ s_L \\ b_L \end{pmatrix} W_\mu^\pm + h.c.$$



relative element sizes

- Unitary matrix

- 3 real parameters + **1 complex phase**

Only source of ~~CP~~ in SM

- **Wolfenstein parameterization:**

$$V_{CKM} = \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + O(\lambda^4)$$

Annotations:  $|V_{td}|e^{-i\beta}$  points to the bottom-left element  $A\lambda^3(1 - \rho - i\eta)$ ;  $|V_{ub}|e^{-i\gamma}$  points to the top-right element  $A\lambda^3(\rho - i\eta)$ .

- the 4 parameters are  $\lambda \approx 0.22$ ,  $A \approx 0.83$ ,  $\rho$  and  $\eta$ .

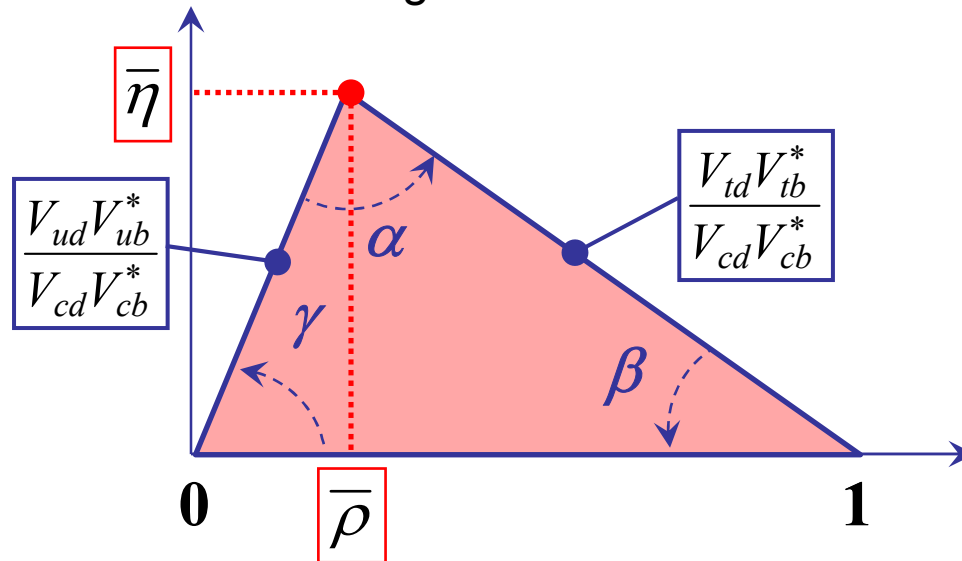
- matrix hierarchy reflected by development in power of  $\lambda$ .

- in this representation CKM angles are carried by  $V_{td} = |V_{td}|e^{-i\beta}$ ,  $V_{ub} = |V_{ub}|e^{-i\gamma}$ , with  $\alpha = \pi - \beta - \gamma$

# The Unitarity Triangle

- Unitary of  $V_{CKM} \rightarrow V_{CKM}^\dagger V_{CKM} = 1 \rightarrow V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$ 
  - unitary triangle of  $B$  sector
  - all terms of the order  $\lambda^3 \rightarrow$  CPV angles sizeable

$\bar{\rho}$  and  $\bar{\eta}$  are slight redefinition of  $\rho$  and  $\eta$  to provide a well defined expansion in  $\lambda$  of  $V_{CKM}$  and its unitarity of to all orders in  $\lambda$ .



Name of angles	
BELLE	BABAR
$\phi_1$	$\beta$
$\phi_2$	$\alpha$
$\phi_3$	$\gamma$

- **Sides of the triangles measurable by non CP violating processes**
  - eg : semileptonic  $B$  decays,  $B^0\bar{B}^0$  mixing frequency
- **Angles measured with CP violating processes**
  - If  $\alpha$  or  $\beta$ :  $B^0\bar{B}^0$  mixing is needed ingredient to access the phase of  $V_{td}$
  - If  $\gamma$  charged  $B$  decays can allow access as well

# Three types of $CP$ violation

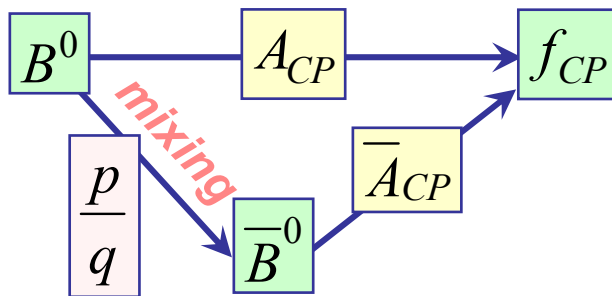
- **$CP$  violation in decay (“direct”  $CPV$ ):**

- $|A(B \rightarrow f)| \neq |\bar{A}(\bar{B} \rightarrow \bar{f})|$
- both charged or neutral  $B$ 's
  - *only possible  $CPV$  for  $B^\pm$ 's*

- **$CP$  violation in mixing:**

- $\langle B^0 | \bar{B}^0 \rangle \neq \langle \bar{B}^0 | B^0 \rangle$
  - $(|p/q| \neq 1) \sim 10^{-3}$  in SM, approaching experimental limits
- $$|B_L\rangle = p|B^0\rangle + q|\bar{B}^0\rangle$$
- $$|B_H\rangle = p|B^0\rangle - q|\bar{B}^0\rangle$$

- **$CP$  violation in interference between mixing and decay:**



$$\lambda_{f_{CP}} = \eta_{f_{CP}} \frac{p \bar{A}_{CP}}{q A_{CP}}$$

Independent of phase convention

depend on final state

- **Time dependent  $CP$  asymmetry:**

$$A_{f_{CP}}(\Delta t) = \frac{N(B^0(\Delta t) \rightarrow f_{CP}) - N(\bar{B}^0(\Delta t) \rightarrow f_{CP})}{N(B^0(\Delta t) \rightarrow f_{CP}) + N(\bar{B}^0(\Delta t) \rightarrow f_{CP})}$$

$$= S_{f_{CP}} \cdot \sin \Delta m_{B^0} \Delta t - C_{f_{CP}} \cdot \cos \Delta m_{B^0} \Delta t$$

$$C_{f_{CP}} = \frac{1 - |\lambda_{f_{CP}}|^2}{1 + |\lambda_{f_{CP}}|^2} = -A_{f_{CP}}$$

if  $\neq 0$ : direct  $CPV$

$$S_{f_{CP}} = \frac{2 \operatorname{Im} \lambda_{f_{CP}}}{1 + |\lambda_{f_{CP}}|^2}$$

I should make clear that :

At  $\Delta t = 0$  the  $B$  meson is a pure  $B^0$  or  $\bar{B}^0$

It decays at  $\Delta t$  in a interference state

On an experimental point of view, the detector has to measure:

→  $B$   $CP$  flavor ( $B^0$  or  $\bar{B}^0$ ) at  $\Delta t = 0$

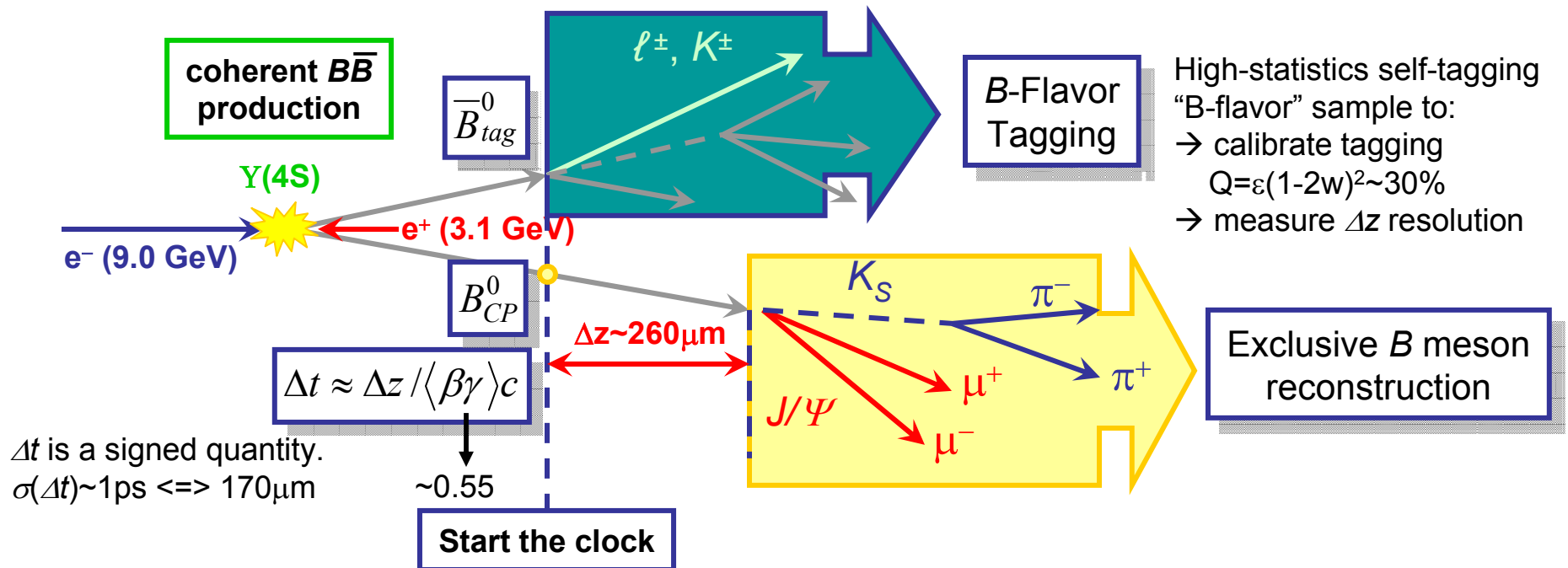
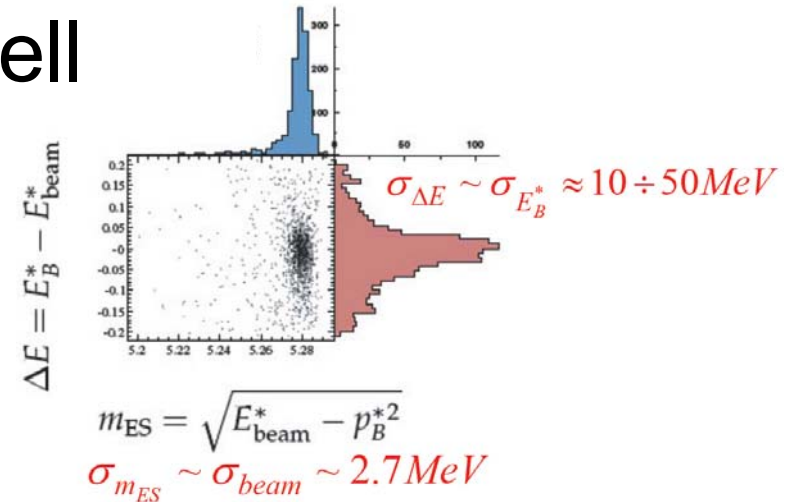
→ The decay time  $\Delta t$  of the  $B$  meson

- Time dependent  $CP$  asymmetry:

$$A_{f_{CP}}(\Delta t) = \frac{N(B^0(\Delta t) \rightarrow f_{CP}) - N(\bar{B}^0(\Delta t) \rightarrow f_{CP})}{N(B^0(\Delta t) \rightarrow f_{CP}) + N(\bar{B}^0(\Delta t) \rightarrow f_{CP})}$$
$$= S_{f_{CP}} \cdot \sin \Delta m_{B^0} \Delta t - C_{f_{CP}} \cdot \cos \Delta m_{B^0} \Delta t$$

# Time dependent measurements at B-factories in a nutshell

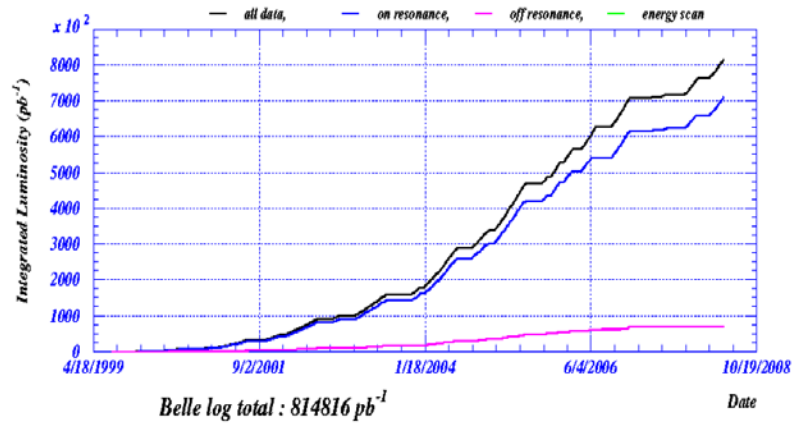
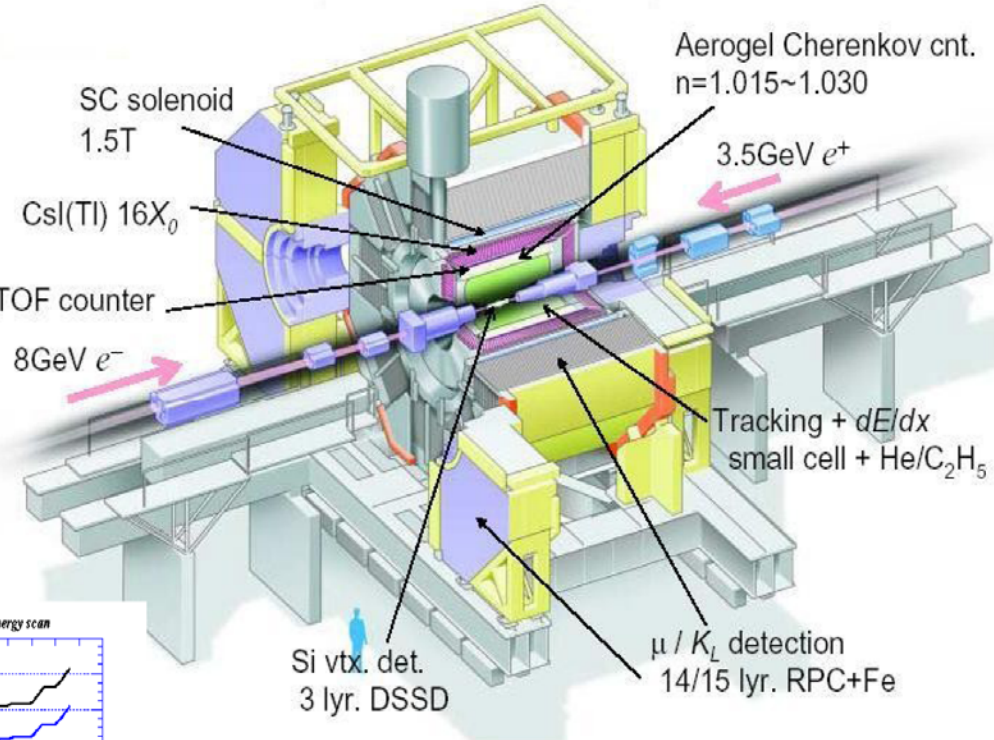
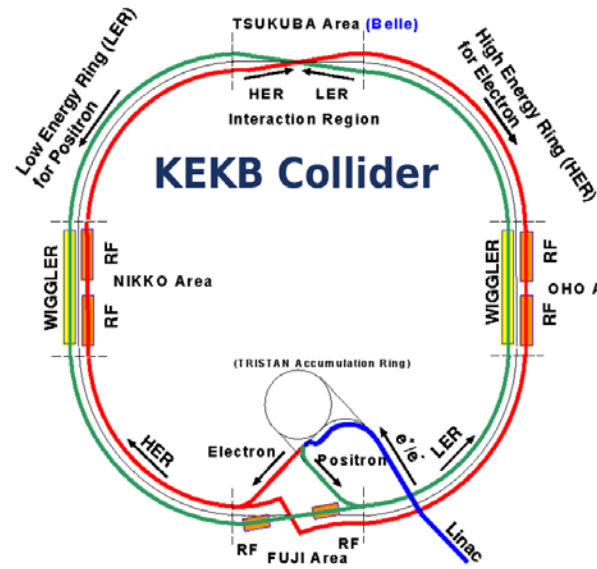
- reconstruct final ( $CP$  eigen)state
- measure distance between decay vertices
- determine  $B^0$  tag flavor at decay time
- fit...



# The BABAR and BELLE detectors

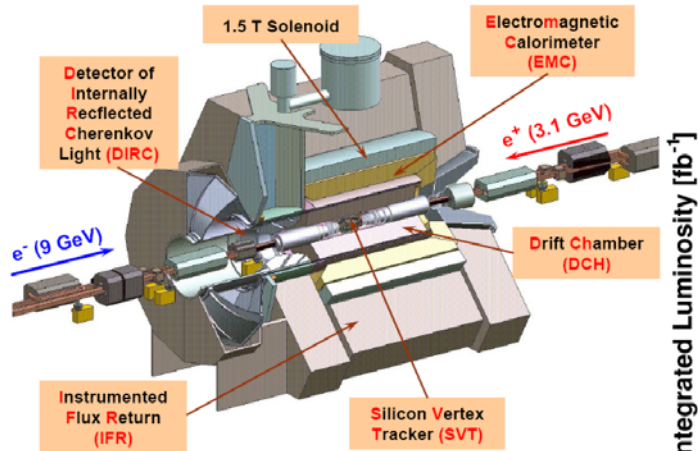


# The BELLE detector

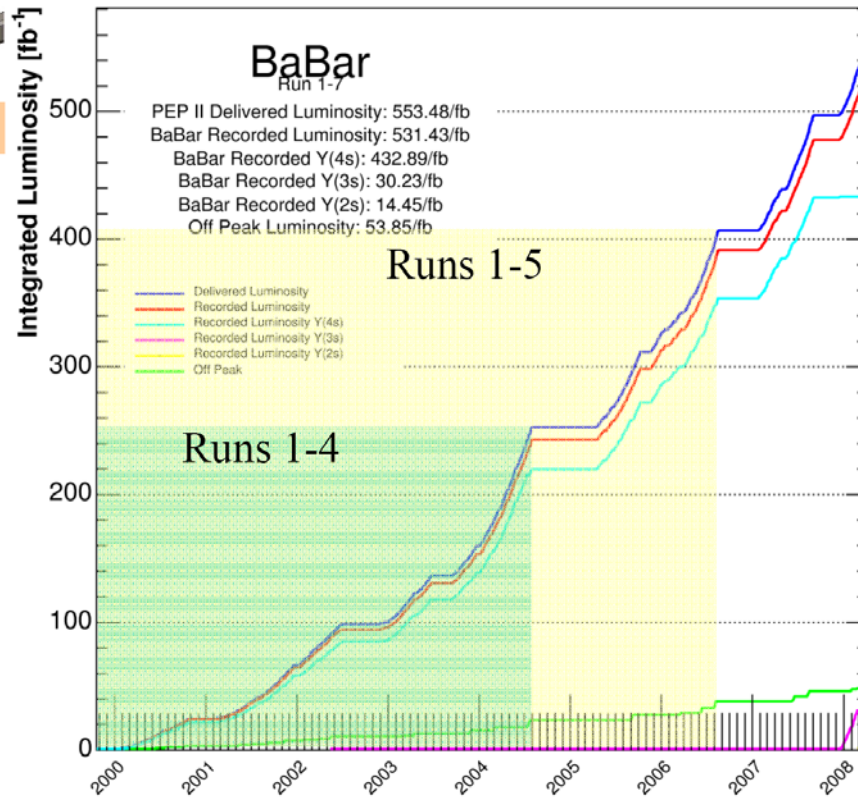


3.5 GeV  $e^+$  & 8 GeV  $e^-$  beams  
 3 km circumference, 11 mrad crossing angle  
 $L = 1.7 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$  (world record)  
 $\int L dt \sim 820 \text{ fb}^{-1} @ \gamma(4S) + \text{off} (\sim 10\%)$

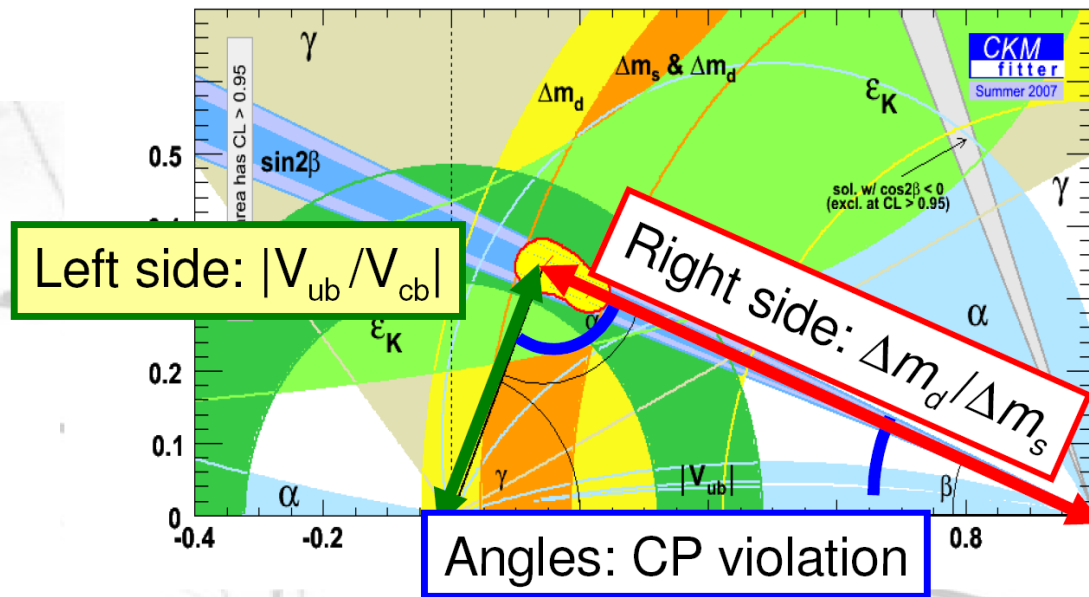
# The BABAR detector



Final collisions 12:43pm,  
Monday 7 Apr 2008



# Side measurements



## $|V_{td}|/|V_{ts}|$ from $\Delta m_s/\Delta m_d$

- $B_d$  and  $B_s$  oscillation frequency controlled by mass difference:

$$\Delta m_q = \frac{G_F^2 m_W^2 \eta S(x_t^2)}{6\pi^2} m_{B_q} f_{B_q}^2 B_{B_q} |V_{tq}^* V_{tb}|^2$$

- Form factor and B-parameters from Lattice calculations known to  $\sim 15\%$   
 $\rightarrow$  uncertainty on  $V_{td}$

- Ratio better controlled (hep-lat/0510113):

$$\xi^2 = \frac{f_d^2 B_d}{f_s^2 B_s} = 1.210^{+0.047}_{-0.035} \quad (\sigma \sim 4\%)$$

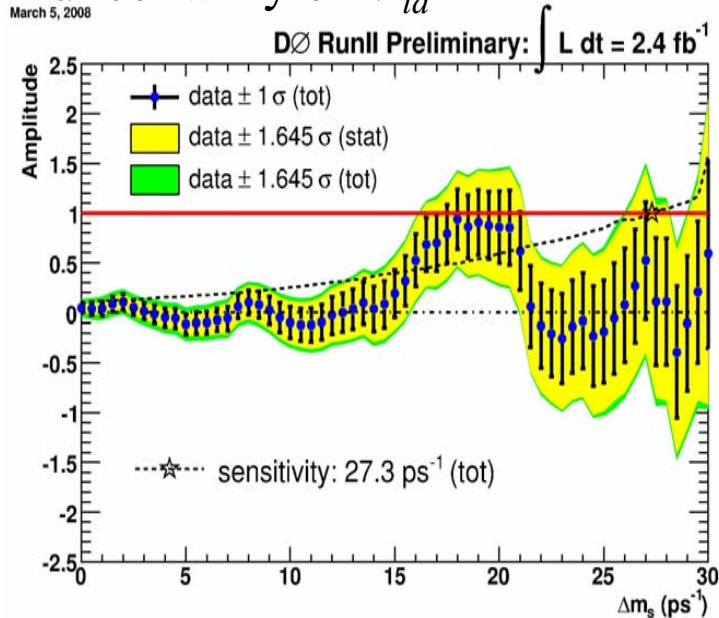
# $|V_{td}|/|V_{ts}|$ from $\Delta m_s/\Delta m_d$

- $B_d$  and  $B_s$  oscillation frequency controlled by mass difference:

$$\Delta m_q = \frac{G_F^2 m_W^2 \eta S(x_t^2)}{6\pi^2} m_{B_q} f_{B_q}^2 B_{B_q} |V_{tq}^* V_{tb}|^2$$

- Form factor and B-parameters from Lattice calculations known to  $\sim 15\%$

→ uncertainty on  $V_{td}$

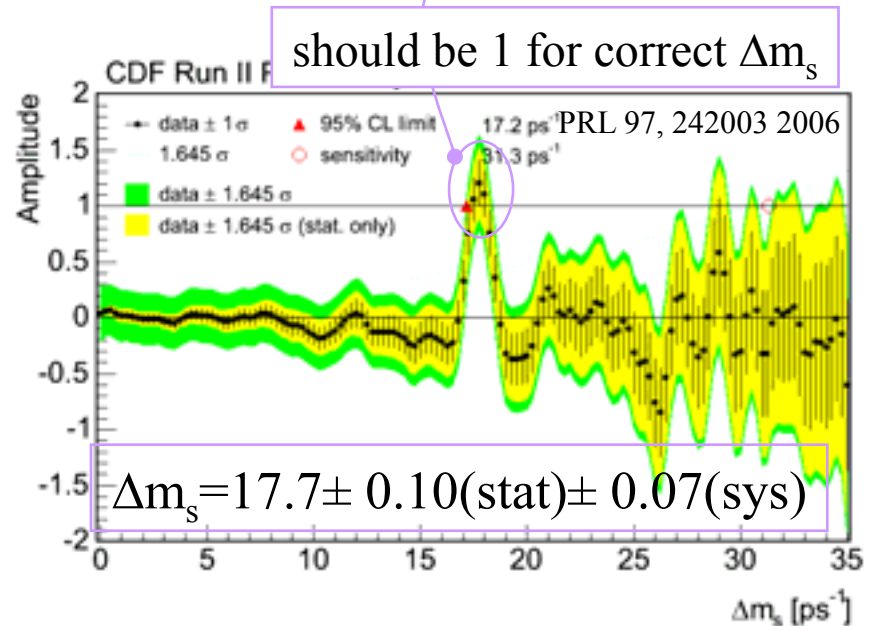


- Ratio better controlled (hep-lat/0510113):

$$\xi^2 = \frac{f_d^2 B_d}{f_s^2 B_s} = 1.210^{+0.047}_{-0.035} \quad (\sigma \sim 4\%)$$

- Performed “amplitude scan”:

$$L_{sig}^t = \frac{1}{\tau} e^{-t/\tau} (1 \pm A \cdot D \cdot \cos(\Delta M \cdot t))$$



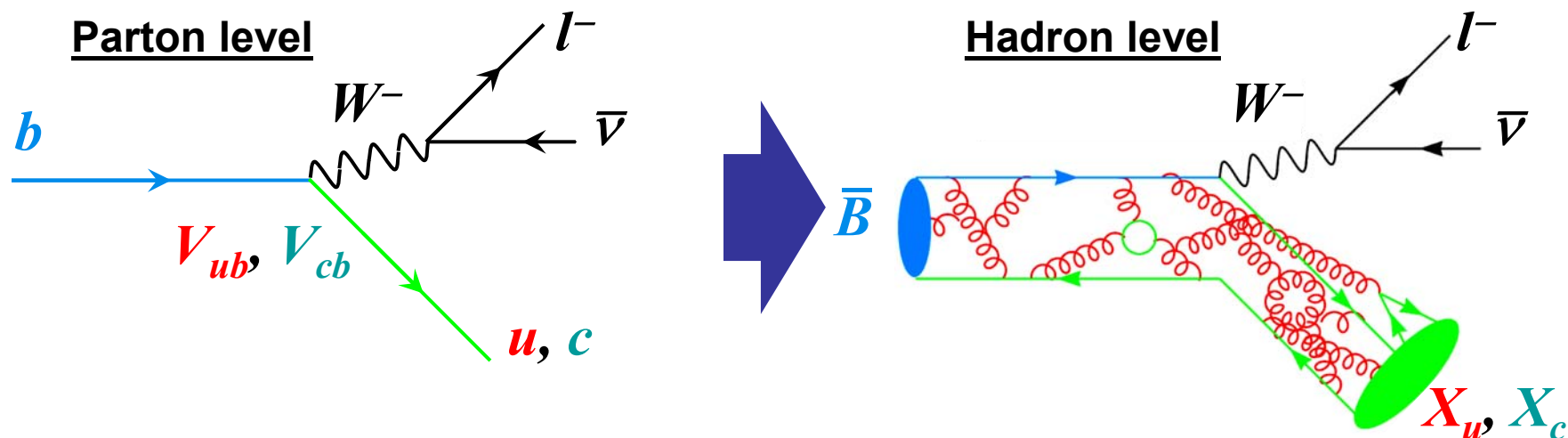
$|V_{td}|/|V_{ts}|$  from  $\Delta m_s/\Delta m_d$

- Together with  $\Delta m_d=0.505\pm 0.005$  (PDG) and  $m(B_d)/m(B_s)=0.98320$  (PDG):

$$\left| \frac{V_{td}}{V_{ts}} \right| = 0.2060 \pm 0.0007 \text{ (exp)} \begin{matrix} +0.0081 \\ -0.0060 \end{matrix} \text{ (theo)}$$

# Semileptonic decays

## from partons to hadrons

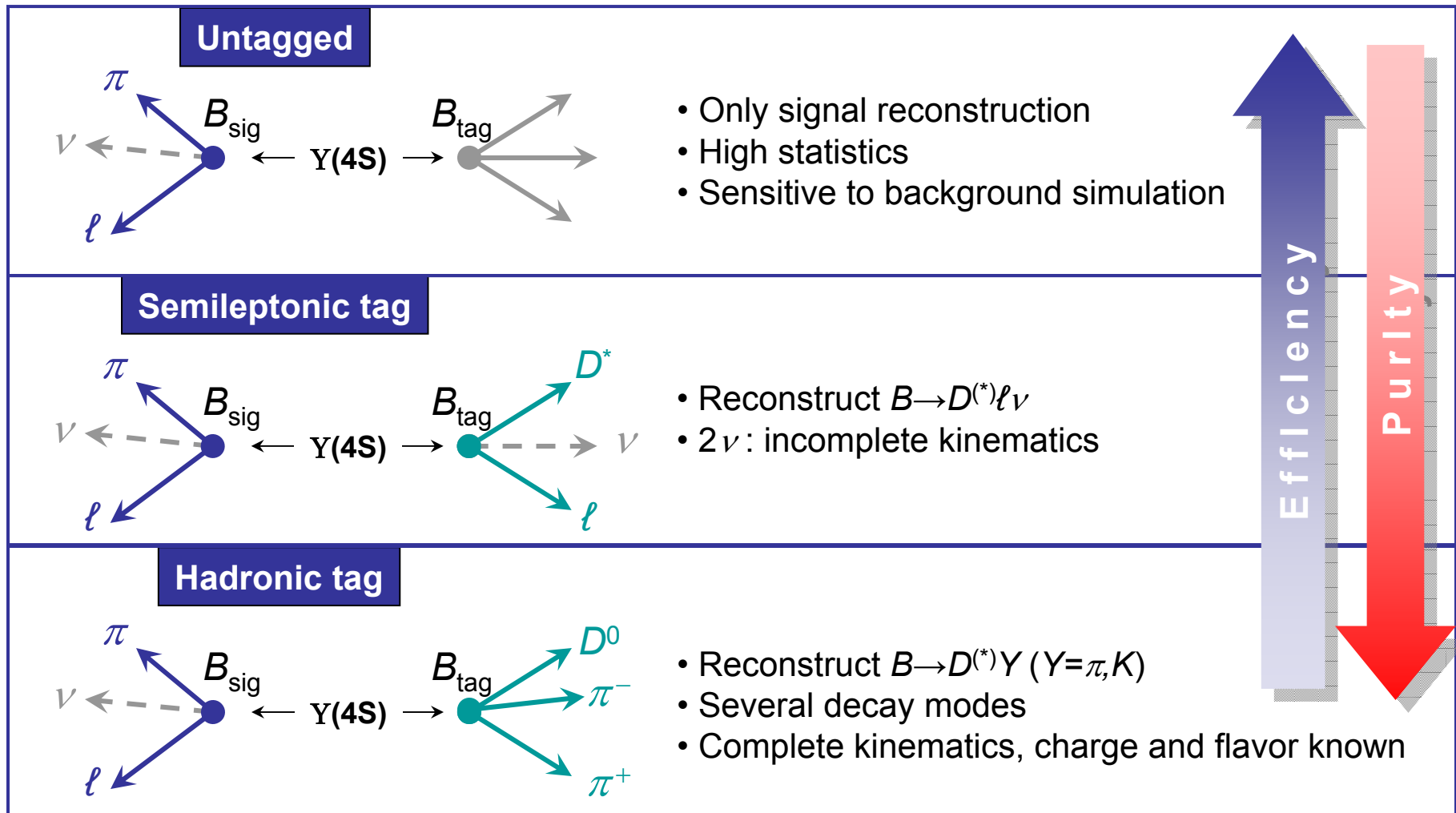


- Quark decay is a tree level, short distance process.
- Decay properties depend directly on  $|V_{c(u)b}|$  and  $m_b$  in **perturbative regime** ( $\alpha_s^n$  expansion).
- But quarks are bound by soft gluons...
- **Non-perturbative** long distance interactions of  $b$  quark with light quarks complicate the situation.

- **Two different approaches are used:**
  - Inclusive : extrapolate by theory phase space measured to the full phase space
  - Exclusive : needs prediction of form factor by theory

# Experimental methods

- Exclusive or inclusive reconstruction are used on the signal side
- In addition, on the other  $B$  (“tag”) side:





# Coping with non-perturbative interactions in $V_{cb}$ extraction (inclusive analysis)

- Total decay rate:

$$\Gamma(B \rightarrow X_{c(u)} l \nu) = \underbrace{\frac{G_F^2 m_b^5}{192\pi^3}}_{\text{free quark decay}} |V_{c(u)b}|^2 \left[ [1 + A_{EW}] A_{\text{pert.}} A_{\text{non pert.}} \right]$$

$\alpha_s^k$  expansion
 $(1/m_b)^n$  expansion

- Non perturbative parameters ***need to be measured***
  - they depend on the expansion, which depends on the  $m_b$  definition
- Can be extracted from ***the moments of lepton energy and hadronic mass spectra: (integration)***

$$\langle E_l^n \rangle_{E > E_{cut}} = \frac{1}{\Gamma_{c(u)}} \int (E_l - \langle E_l \rangle)^n \frac{d\Gamma_{c(u)}}{dE_l} dE_l$$

$$\langle m_X^n \rangle_{E > E_{cut}} = \frac{1}{\Gamma_{c(u)}} \int m_X^n \frac{d\Gamma_{c(u)}}{dm_X} dm_X$$

Calculations are available in “**kinetic**” (Benson & al., Nucl. Phys. B665:367) and “**1S**” (Bauer & al., PRD **70**, 094017 (2004)) schemes.  
They are based on Heavy Quark Expansion (HQE) and Operator Product Expansion (OPE).

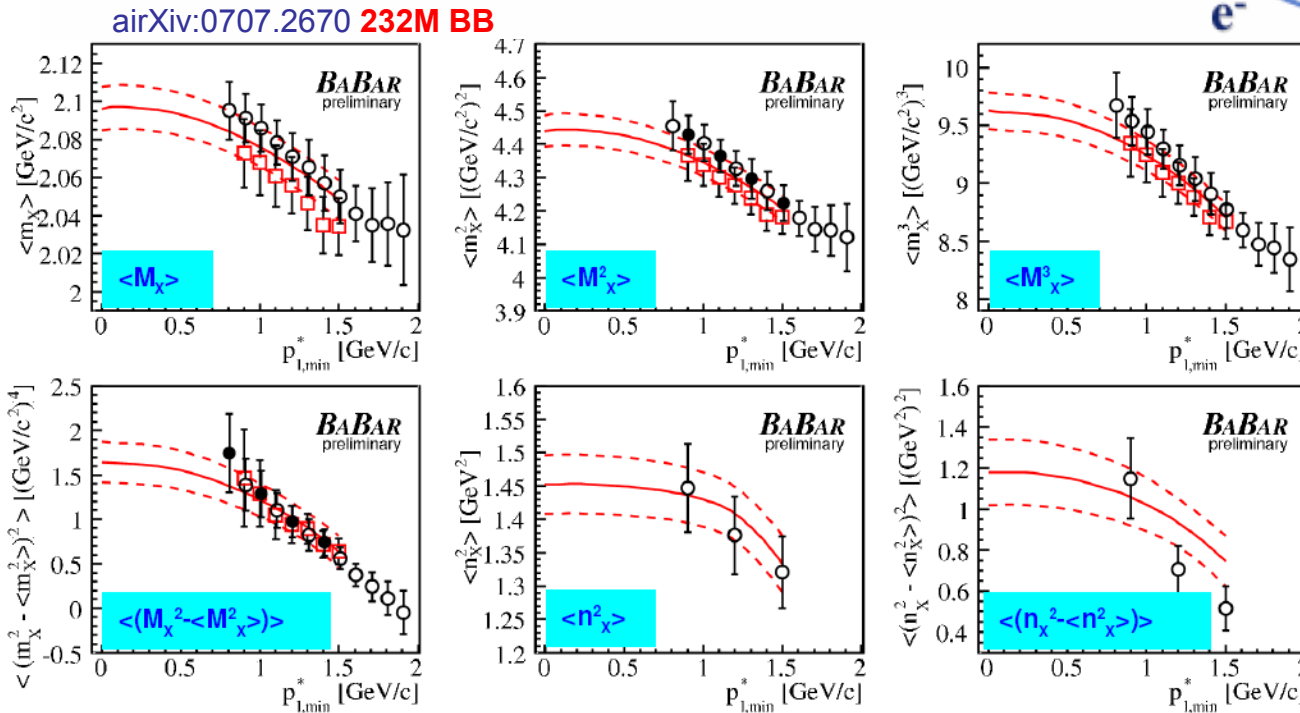
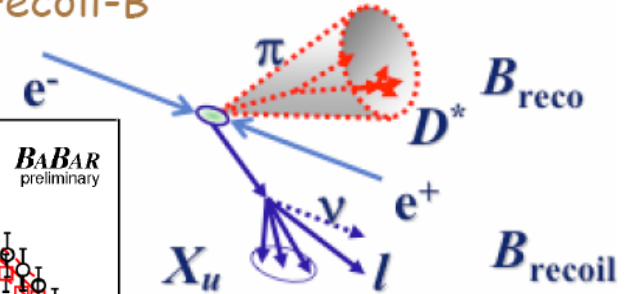
- More than 60 measured moments available from DELPHI, CLEO, BABAR, BELLE, CDF

# Moments in semileptonic decays



fully-reconstructed B meson B flavor and momentum known.

rest of the event contains one "recoil" lepton in the recoil-B



$\langle m_x^n \rangle$  new

$\langle m_x^n \rangle$  old

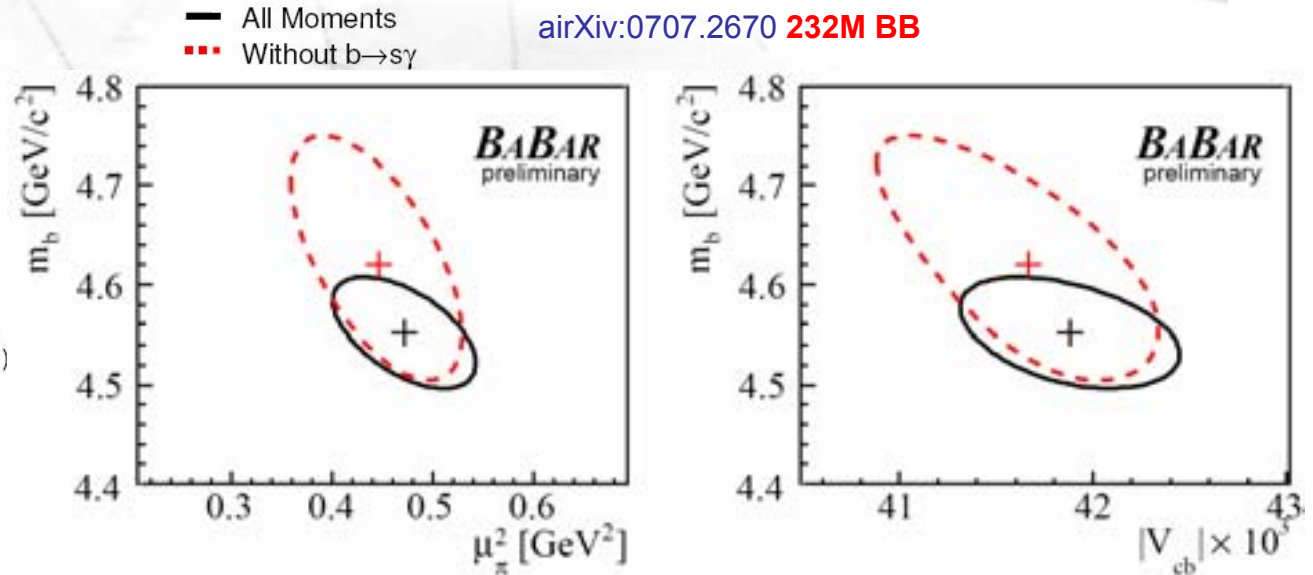
$$n_x = m_x^2 c^4 - 2\tilde{\Lambda} E_x + \tilde{\Lambda}$$

$(\tilde{\Lambda} = 0.65 \text{ GeV})$

Fit moments of these distribution to get  $V_{cb}$  and HQ parameters

# Global OPE fit – Kinetic Scheme

- 27 input moments:
  - 8 mass moments  
(this analysis)
  - 13  $E_1$  moments  
(Phys. Rev. D69 111104 (2004))
  - 6  $E_\gamma$  moments  
(Phys. Rev. D 72, 052004 (2005),  
Phys. Rev. Lett. 97 171803 (2006))
- Further input:  $\tau_B$
- 8 fit parameters:
  - $|V_{cb}|$ ,  $m_b$ ,  $m_c$ ,  $\beta_{sl}$
  - 4 HQE parameters

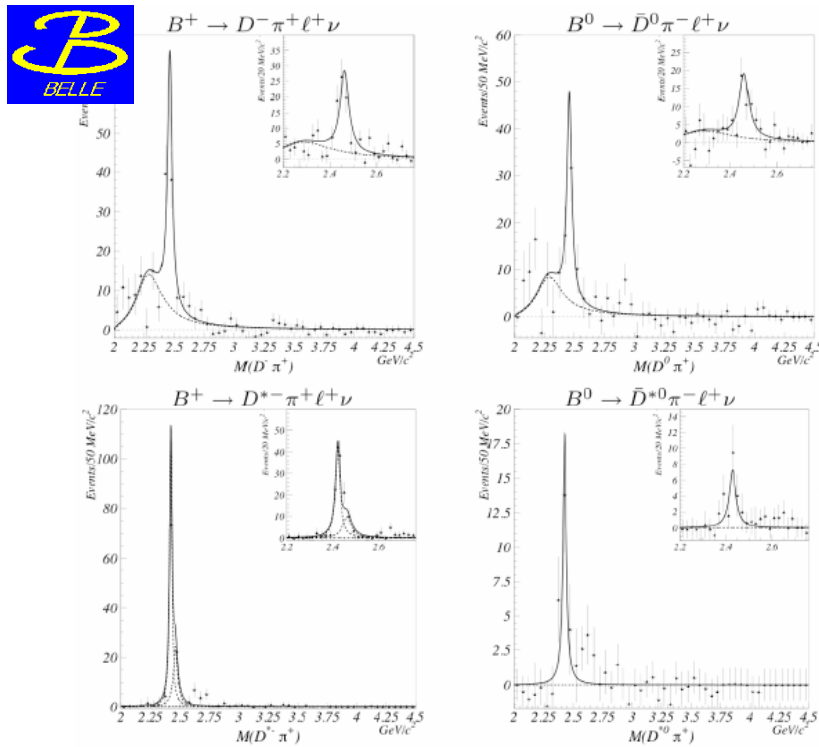


- Fit results:
    - $|V_{cb}| = (41.88 \pm 0.44_{\text{exp}} \pm 0.35_{\text{theo}} \pm 0.59_{\Gamma_{\text{SL}}}) 10^{-3}$  (1.9% total error)
    - $m_b = (4.55 \pm 0.038_{\text{exp}} \pm 0.040_{\text{theo}}) \text{ GeV}$  (1.2% total error)
    - $m_c = (1.070 \pm 0.038_{\text{exp}} \pm 0.040_{\text{theo}}) \text{ GeV}$
    - $\beta_{\text{SL}} = (10.597 \pm 0.171_{\text{exp}} \pm 0.053_{\text{theo}}) \%$
    - $m_\pi^2 = (0.471 \pm 0.034_{\text{exp}} \pm 0.062_{\text{theo}}) \text{ GeV}^2$
    - $m_G^2 = (0.330 \pm 0.042_{\text{exp}} \pm 0.043_{\text{theo}}) \text{ GeV}^2$
    - $\rho_D^3 = (0.220 \pm 0.021_{\text{exp}} \pm 0.042_{\text{theo}}) \text{ GeV}^3$
    - $\rho_{\text{LS}}^3 = -(0.159 \pm 0.081_{\text{exp}} \pm 0.050_{\text{theo}}) \text{ GeV}^3$
- } non-perturbative  
params

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# BR measurements of $B \rightarrow D^{**} \ell \nu$

- Measurement to control  $D^{**}$  background in  $V_{cb}$  analyses:



HQET predicts the rate of broad  $D_0^*$   
 $\sim 10$  times smaller than narrow  $D_2^*$

Belle measure comparable branchings  
 fractions

$$\mathcal{B}(\text{mode}) \equiv \mathcal{B}(B \rightarrow D^{**} \ell \nu) \times \mathcal{B}(D^{**} \rightarrow D^{(*)} \pi^+)$$

$D\pi$  invariant mass study

Mode	Yield	$\mathcal{B}$ , %	Signif.
$B^+ \rightarrow D_0^{*0} \ell^+ \nu$	$102 \pm 19$	$0.24 \pm 0.04 \pm 0.06$	5.4
$B^+ \rightarrow \bar{D}_2^{*0} \ell^+ \nu$	$94 \pm 13$	$0.22 \pm 0.03 \pm 0.04$	8.0
$B^0 \rightarrow D_0^{*-} \ell^+ \nu$	$61 \pm 22$	$0.20 \pm 0.07 \pm 0.05$	2.6
$B^0 \rightarrow D_2^{*-} \ell^+ \nu$	$68 \pm 13$	$0.22 \pm 0.04 \pm 0.04$	5.5

$D^* \pi$  invariant mass study

Mode	Yield	$\mathcal{B}$ , %	Signif.
$B^+ \rightarrow \bar{D}_1^{\prime 0} \ell^+ \nu$	$-5 \pm 11$	$< 0.07$ @ 90% C.L.	
$B^+ \rightarrow \bar{D}_1^0 \ell^+ \nu$	$81 \pm 13$	$0.42 \pm 0.07 \pm 0.07$	6.7
$B^+ \rightarrow \bar{D}_2^{\prime 0} \ell^+ \nu$	$35 \pm 11$	$0.18 \pm 0.06 \pm 0.03$	3.2
$B^0 \rightarrow D_1^{\prime -} \ell^+ \nu$	$4 \pm 8$	$< 0.5$ @ 90% C.L.	
$B^0 \rightarrow D_1^- \ell^+ \nu$	$20 \pm 7$	$0.54 \pm 0.19 \pm 0.09$	2.9
$B^0 \rightarrow D_2^{\prime -} \ell^+ \nu$	$1 \pm 6$	$< 0.3$ @ 90% C.L.	

$$\begin{aligned} \mathcal{B}(B^- \rightarrow D_1^0 \ell \nu) &= 0.42 \pm 0.04 \pm 0.04 \% \\ \mathcal{B}(B^- \rightarrow D_1^{\prime 0} \ell \nu) &= 0.47 \pm 0.06 \pm 0.06 \% \\ \mathcal{B}(B^- \rightarrow D_2^* \ell \nu) &= 0.29 \pm 0.05 \pm 0.03 \% \\ \mathcal{B}(B^- \rightarrow D_0^* \ell \nu) &= 0.52 \pm 0.07 \pm 0.06 \% \end{aligned}$$

BABAR confirms large BR for  $D_0^*$ , and finds large BR for  $D_1^{\prime}$  ( $6\sigma$  difference will BELLE !)

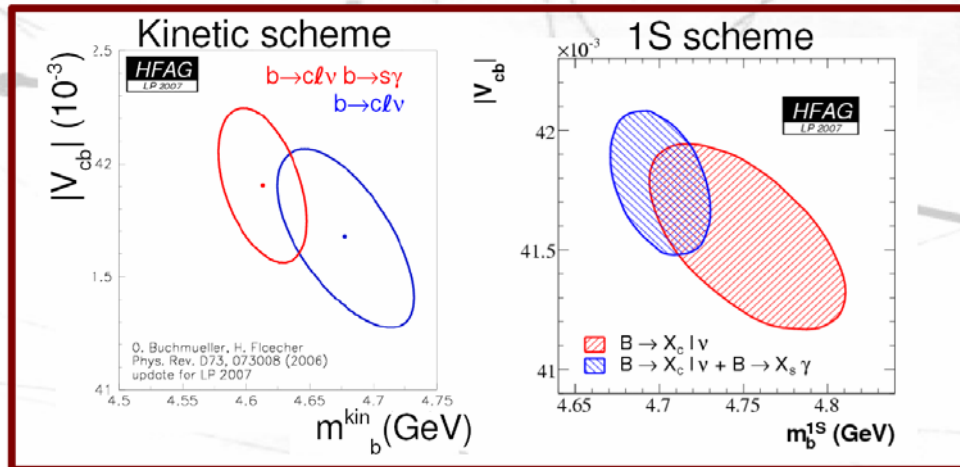
arXiv:0711.3252



# $V_{cb}$ and HQE parameters

- More results from global fits in the kinetic and 1S schemes are available. Recent averages performed by the HFAG
- A pattern is present: results with  $b \rightarrow c\ell\nu$  and  $b \rightarrow s\gamma$  moments differ from results with  $b \rightarrow c\ell\nu$  moments only (except in hep-ex/0611047, but larger errors).
- HFAG results for Lepton Photon:

	$m_b$ (GeV)	$m_b$ (GeV)
	$b \rightarrow c\ell\nu$ $b \rightarrow s\gamma$	$b \rightarrow c\ell\nu$
Kinetic scheme	$4.613 \pm 0.035$	$4.677 \pm 0.053$
1S scheme	$4.701 \pm 0.030$	$4.751 \pm 0.058$



- Large uncertainties due to the ansatz and missing terms
- Different values of  $m_b$  impact the determination of  $|V_{ub}|$  from inclusive decays

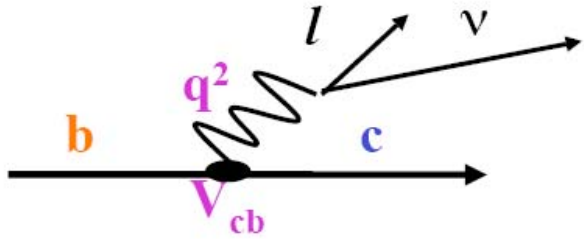
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# $V_{cb}$ exclusive $B^- \rightarrow D^{*0} e^- \bar{\nu}$



$$B^- \rightarrow D^{*0} e^- \bar{\nu}; D^* \rightarrow \pi^0 D^0$$

$$\frac{d\Gamma(B \rightarrow D | \nu)}{dw} = K(w) F^2(w) |V_{cb}|^2$$



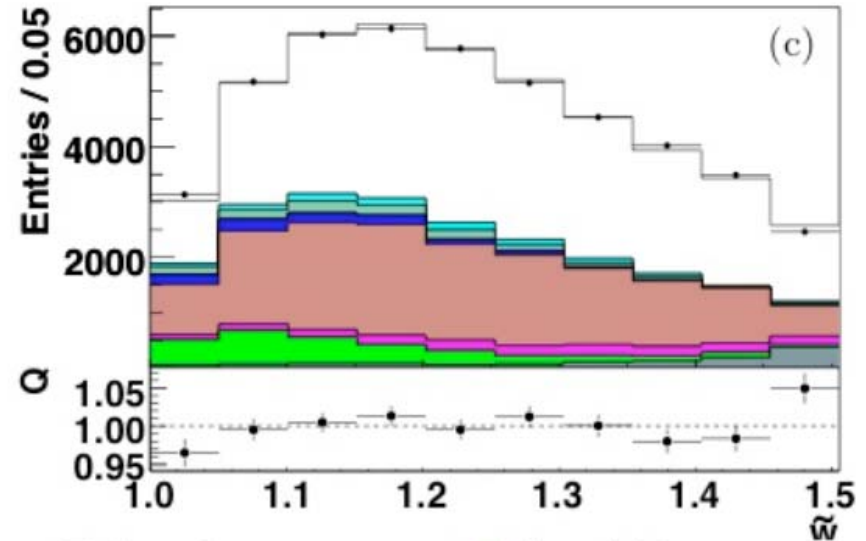
$$w = \frac{m_B^2 + m_{D^*}^2 - q^2}{2m_B m_{D^*}}$$

$$F(1) \cdot |V_{cb}| = (35.9 \pm 0.6 \pm 1.4) \cdot 10^{-3},$$

$$\rho_{A_1}^2 = 1.16 \pm 0.06 \pm 0.08,$$

$$\mathcal{B}(B^- \rightarrow D^{*0} e^- \bar{\nu}_e) = (5.56 \pm 0.08 \pm 0.41)\%.$$

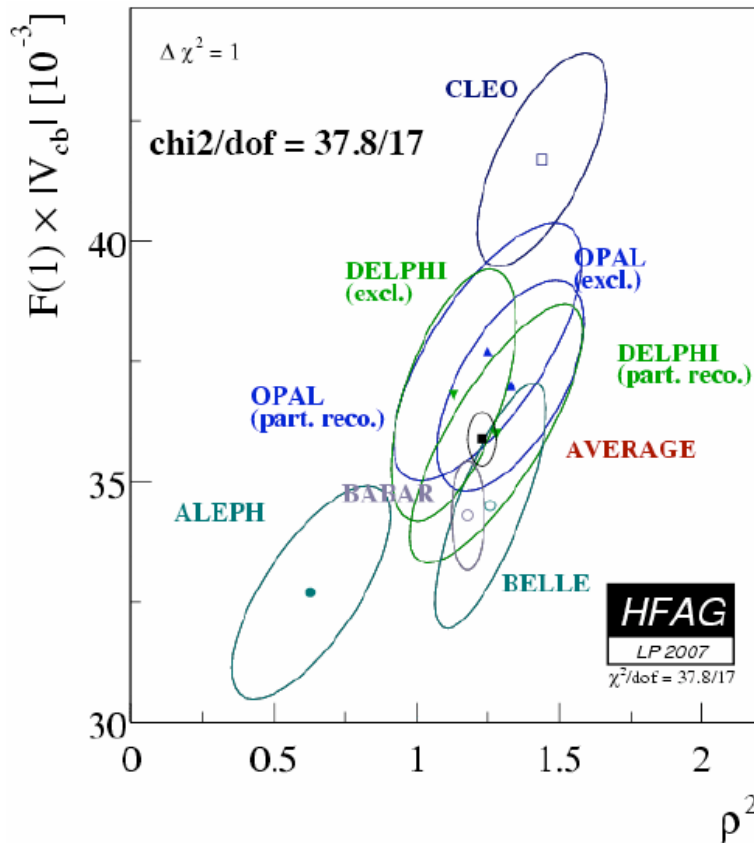
PRL 100 231803 (2008) 226M BB



- |  |   |
|--|---|
| <input type="checkbox"/> Signal                          | <input type="checkbox"/> Signal-like            |
| <input type="checkbox"/> $D^{**}$ ( $\Delta m$ -peaking) | <input type="checkbox"/> $D^0 e \nu$            |
| <input type="checkbox"/> $D^{**}$ ( $\Delta m$ -flat)    | <input type="checkbox"/> Combinatorial $D^{*0}$ |
| <input type="checkbox"/> Correlated                      | <input type="checkbox"/> $c\bar{c}$ events      |
| <input type="checkbox"/> Uncorrelated                    |   |

Main physics background  $B \rightarrow D^{**} l \nu$

# $F(1)|V_{cb}|$



$$F(1)|V_{cb}| = (35.9 \pm 0.6) 10^{-3} \quad \rho_A^2 = 1.23 \pm 0.05$$

From  $F(1) = 0.919 \pm 0.033$ :

$$|V_{cb}| = (39.1 \pm 0.65 \pm 1.4) 10^{-3}$$

error is dominated by the lattice calculation

$B \rightarrow D^0 l \nu$  has a small theoretical error but it's more difficult experimentally and very few measurement

HFAG average uses  $R_1, R_2$  from BaBar

this decrease  $F(1)|V_{cb}|$

→ PRL 77, 032002 (2007)  
**79fb<sup>-1</sup>+9.6fb<sup>-1</sup> offpeak**

# $V_{ub}$ from inclusive semileptonic decays

$$\Gamma(\bar{B} \rightarrow X_u \ell \bar{\nu}) = \underbrace{\frac{G_F^2 |V_{ub}|^2 m_b^5}{192\pi^3}}_{\text{free quark decay}} \left[ 1 + \underbrace{\mathcal{O}(\alpha_s)}_{\text{perturbative correction}} + \underbrace{\mathcal{O}(1/m_b^2)}_{\text{non perturbative correction}} + H.C. \right] \quad \begin{array}{l} \text{O.P.E.} \\ \sim 5\% \text{ uncertainty} \end{array}$$

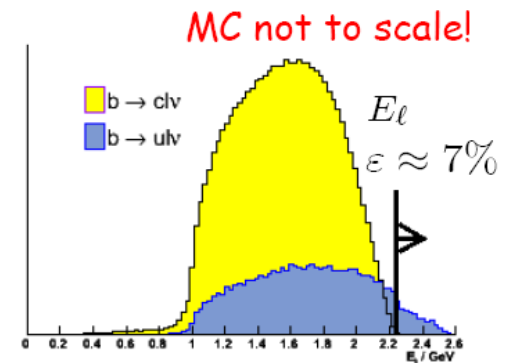
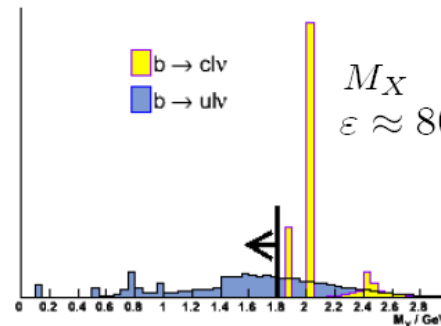
$$\frac{\Gamma_u}{\Gamma_c} \approx \frac{1}{50}$$

free quark decay     perturbative correction     non perturbative correction

$m_u \ll m_c$  different kinematics

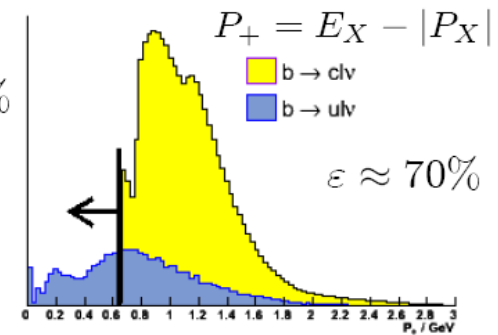
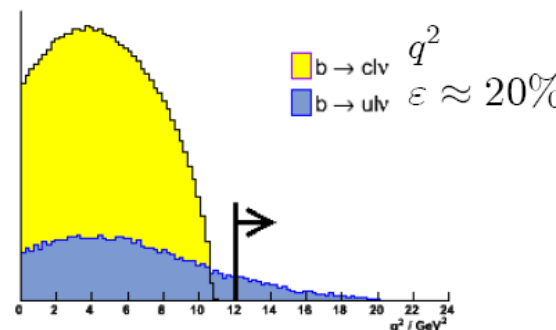
phase space cuts  
to exclude  $b \rightarrow c$  transition

this breaks the OPE convergence



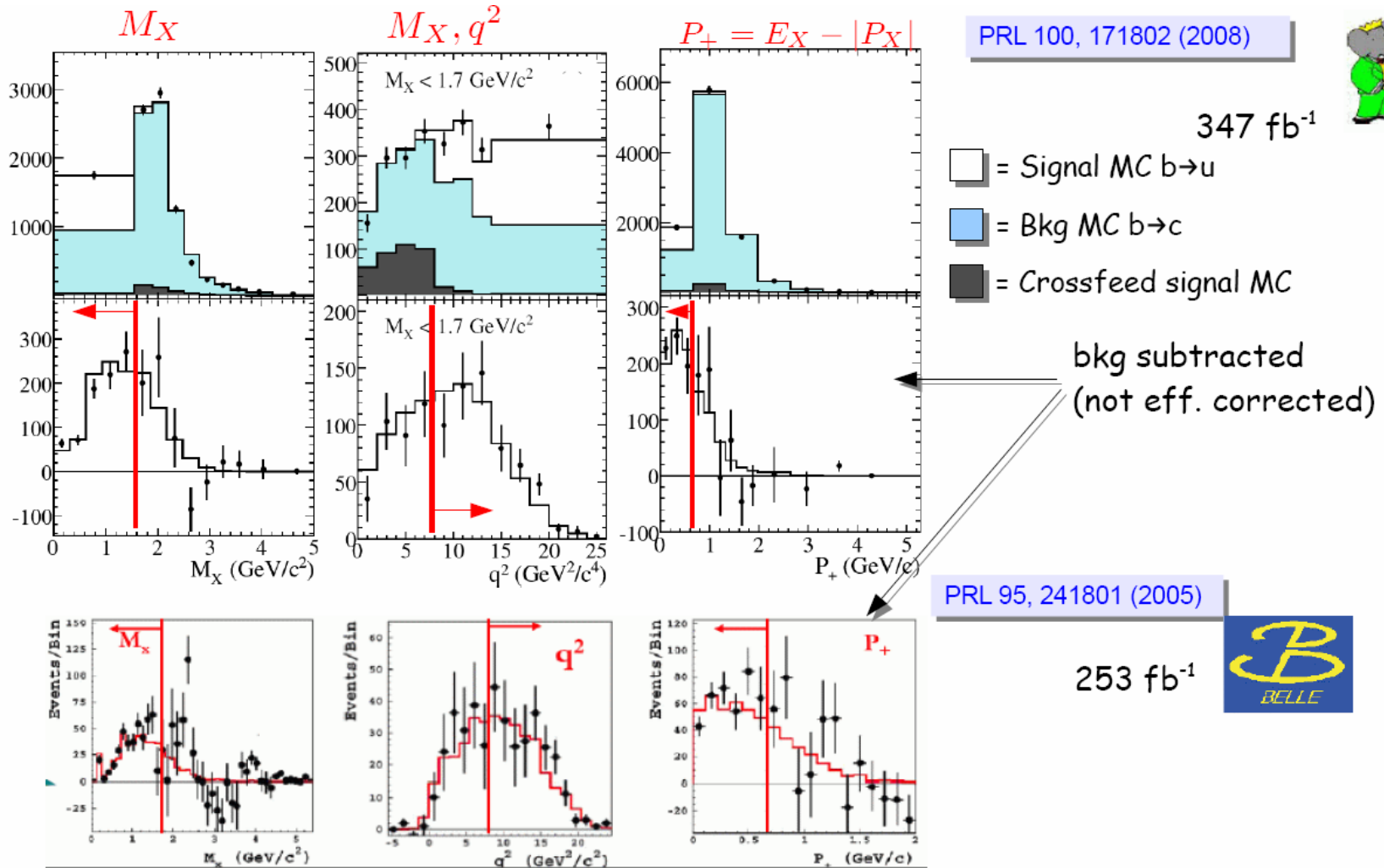
theoretical acceptances  
are sensitive to b quark  
motion (Fermi motion)  
parametrized by **Shape Function**

(Leading) Shape Function  
can be measured by  $E_\gamma$   
spectrum in  $B \rightarrow X_s \gamma$  decays





# Inclusive $V_{ub}$ with hadronic tag





## Hadronic tag: results

Kinematic region	N	$\Delta\mathcal{B}(\bar{B} \rightarrow X_u \ell \bar{\nu}) \cdot 10^{-3}$ (stat. syst. theo.)	$ V_{ub}  \cdot 10^{-3}$ (stat. syst. theo.)	theoretical framework
$m_X < 1.55 \text{ GeV}/c^2$	$803 \pm 60$	$1.18 \pm 0.09 \pm 0.07 \pm 0.01$	$4.27 \pm 0.16 \pm 0.13 \pm 0.30$	BLNP
			$4.56 \pm 0.17 \pm 0.14 \pm 0.32$	DGE
$P_+ < 0.66 \text{ GeV}/c$	$633 \pm 63$	$0.95 \pm 0.10 \pm 0.08 \pm 0.01$	$3.88 \pm 0.19 \pm 0.16 \pm 0.28$	BLNP
			$3.99 \pm 0.20 \pm 0.16 \pm 0.24$	DGE
$m_X < 1.7 \text{ GeV}/c^2$ $q^2 > 8 \text{ GeV}^2/c^4$	$562 \pm 55$	$0.81 \pm 0.08 \pm 0.07 \pm 0.02$	$4.57 \pm 0.22 \pm 0.19 \pm 0.30$	BLNP
			$4.64 \pm 0.23 \pm 0.19 \pm 0.25$	DGE
			$4.93 \pm 0.24 \pm 0.20 \pm 0.36$	BLL

Largest uncertainty: theoretical error 6-7.5%



How predictive is theory?

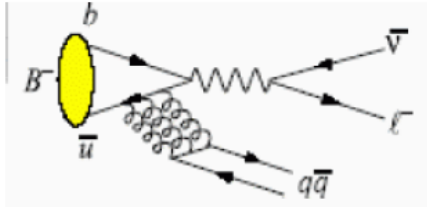
$\Phi_1/\Phi_2$	Data ( $\Delta\mathcal{B}$ )	$\Gamma_{thy}$ (BLNP)	double ratio $\Gamma_{thy}/\Delta\mathcal{B}$
$M_X/M_x, q^2$	$1.46 \pm 0.13$	$1.67 \pm 0.05$	$1.14 \pm 0.11$
$P_+/M_X$	$0.81 \pm 0.07$	$0.98 \pm 0.03$	$1.21 \pm 0.11$
$P_+/M_X, q^2$	$1.18 \pm 0.14$	$1.63 \pm 0.05$	$1.38 \pm 0.17$

$$|V_{ub}| = \sqrt{\frac{\Delta\mathcal{B}(\bar{B} \rightarrow X_u \ell \bar{\nu})}{\tau_B \cdot \Gamma_{thy}}}$$

$$\frac{\Delta\mathcal{B}(\Phi_1)}{\Delta\mathcal{B}(\Phi_2)} = \frac{\Gamma_{thy}(\Phi_1)}{\Gamma_{thy}(\Phi_2)}$$

# Weak Annihilation

arXiv: 0708.1753



- introduces differences between  $B^0$  and  $B^+$  decays
- small contribution: 3% of the total decay rate
- **But would sit in the high  $q^2$  region, where  $V_{ub}$  meas. is performed.**
- compare  $B^0$  partial rate to the charge averaged rate in region where WA contribution is greater (high  $q^2$  and large  $p_l$ )



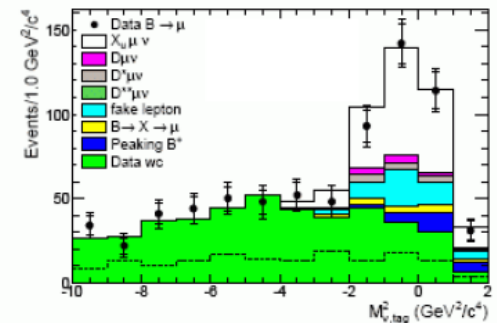
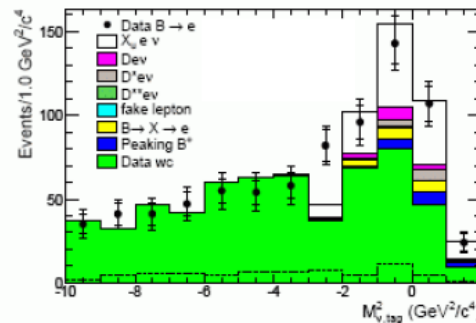
347 fb<sup>-1</sup>

· Study charmless semileptonic decays on recoil of partial reconstructed  $B^0 \rightarrow D^{*+} l \bar{\nu}$

· neutrino mass  $m_\nu^2 = (P_B - P_{D^*} - P_\ell)^2$  **131.1 ± 36.9**

**172.0 ± 32.2**

$$A^{+/-0} = \frac{\Delta\Gamma^+ - \Delta\Gamma^0}{\Delta\Gamma^+ + \Delta\Gamma^0}$$



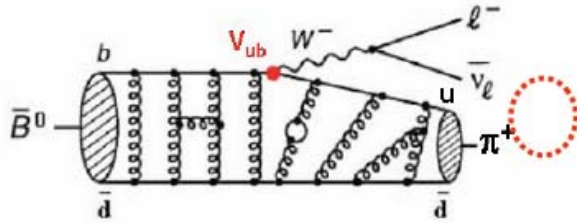
$\Delta p$	$\Delta\mathcal{B}(B) \cdot 10^4 [s]$	$\Delta\mathcal{B}(B^0) \cdot 10^4$	$A^{+/-0}$
2.2 – 2.6 GeV/c	2.31±0.10±0.18	2.62±0.33±0.16	-0.17±0.15±0.11
2.3 – 2.6 GeV/c	1.46±0.06±0.10	1.30±0.21±0.07	0.08±0.15±0.08
2.4 – 2.6 GeV/c	0.75±0.04±0.06	0.76±0.15±0.05	-0.05±0.20±0.10

A. Petrella HQ&L 2008

**No evidence of weak annihilation**

$\Gamma_{wa}/\Gamma_{B \rightarrow ul\nu} < 8\% @90\% CL$   
consistent with CLEO  $q^2$  studies  
PRL 96, 121801 (2006)

# $V_{ub}$ measurement with exclusive decays



Experimentally clean

$$\frac{d\Gamma(B \rightarrow \pi l \nu)}{dq^2} = \frac{G_F^2}{24\pi^2} |V_{ub}|^2 p_\pi^3 |f_+(q^2)|^2$$

Currently only  $B \rightarrow \pi l \nu$  for  $|V_{ub}|$  - one dominant form factor ( $q^2$  shape and normalization needed)

- Form factor calculations from various methods:
  - "unquenched" lattice QCD (HPQCD, Fermilab, ...)
  - Light-Cone Sum Rules (Ball & Zwicky, ...)
  - quark models (ISGW2, ...)

**FF dominates  $|V_{ub}|$  error**

ISGW2 quark-model incompatible (Prob<0.06%).

E. Barberio

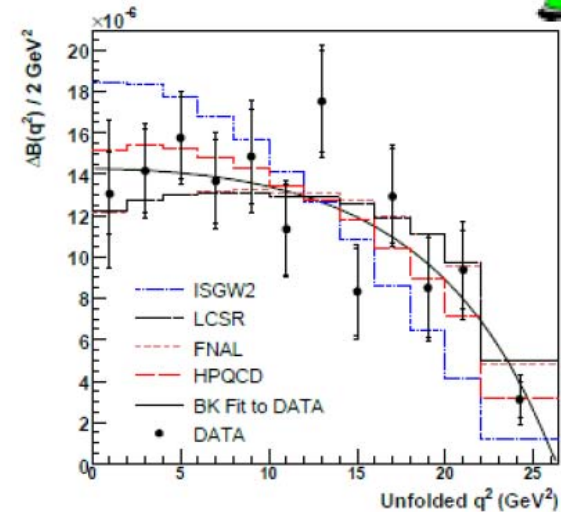
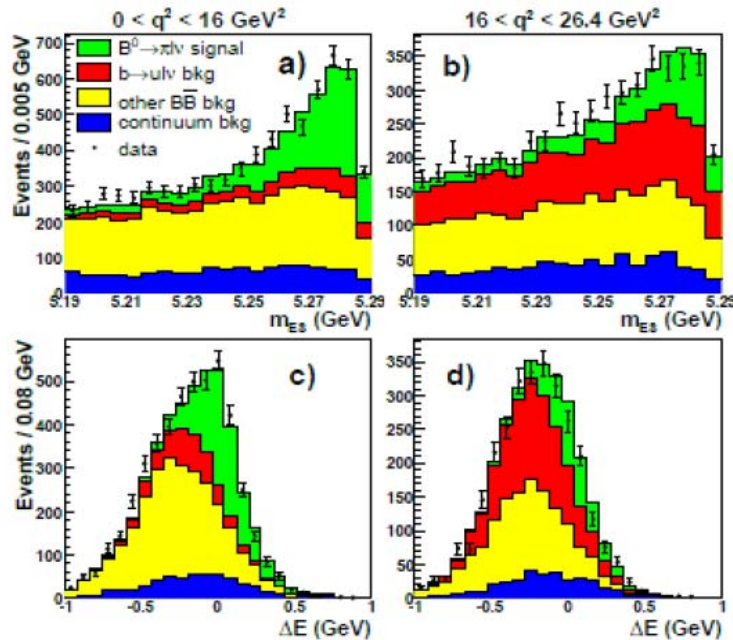
30

# $V_{ub}$ measurement with exclusive decays

## $B \rightarrow \pi l \nu$ : untagged method

BaBar 227MBB

Loose neutrino reconstruction



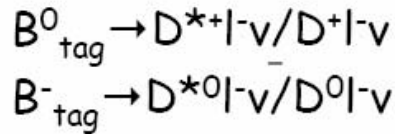
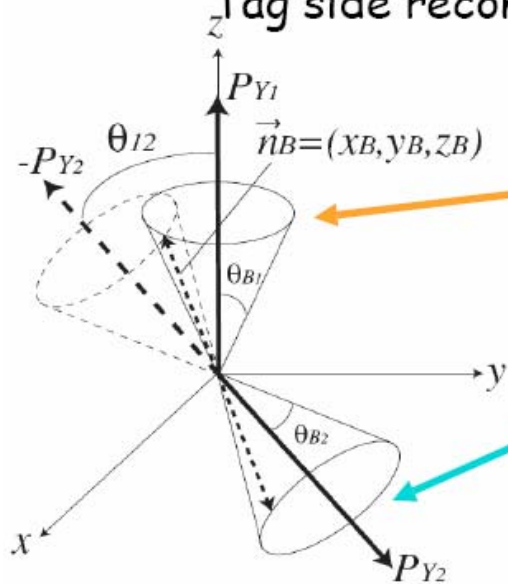
	$q^2$ (GeV <sup>2</sup> )	$\Delta\zeta$ (ps <sup>-1</sup> )	$ V_{ub} $ (10 <sup>-3</sup> )
HPQCD [3]	> 16	$1.46 \pm 0.35$	$4.1 \pm 0.2 \pm 0.2$ $^{+0.6}_{-0.4}$
FNAL [4]	> 16	$1.83 \pm 0.50$	$3.7 \pm 0.2 \pm 0.2$ $^{+0.6}_{-0.4}$
LCSR [5]	< 16	$5.44 \pm 1.43$	$3.6 \pm 0.1 \pm 0.1$ $^{+0.6}_{-0.4}$
ISGW2 [6]	0–26.4	$9.6 \pm 4.8$	$3.2 \pm 0.1 \pm 0.1$ $^{+1.3}_{-0.6}$

Phys. Rev. Lett. 98:091801 (2007)

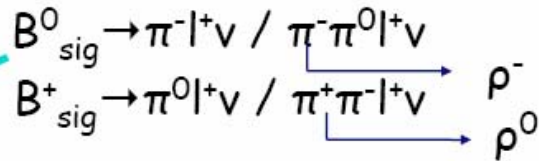
# Exclusive $\rho$ and $\pi$ decay, with $D^*/\nu$ tag



Tag side reconstruction

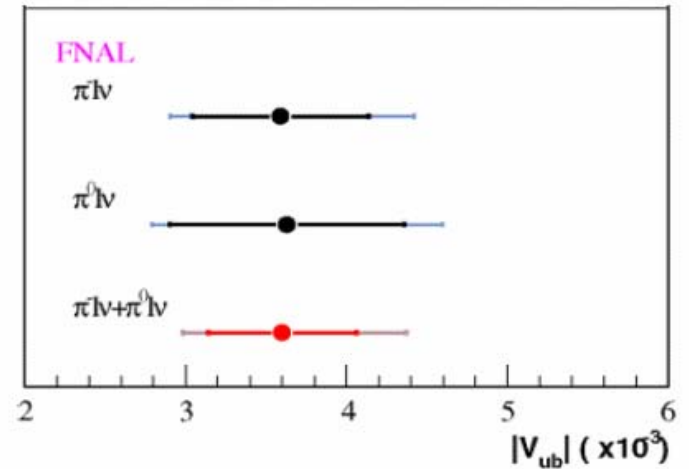
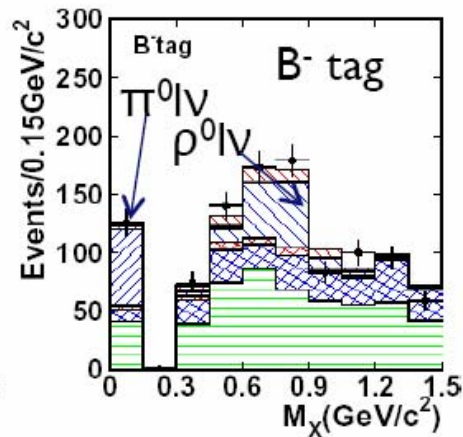
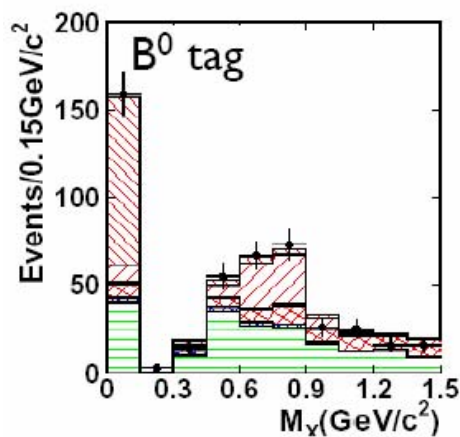


Signal



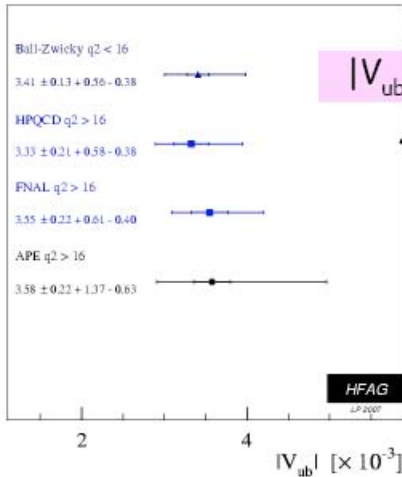
253 fb<sup>-1</sup>  
(275M BB pairs)

Full  $q^2$  region



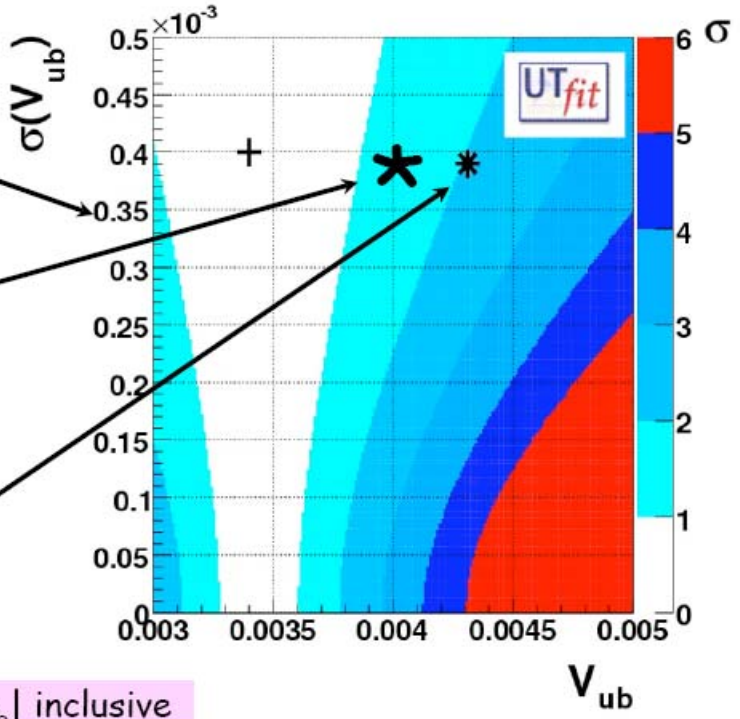
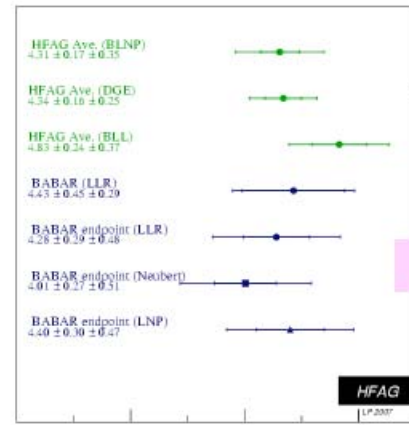
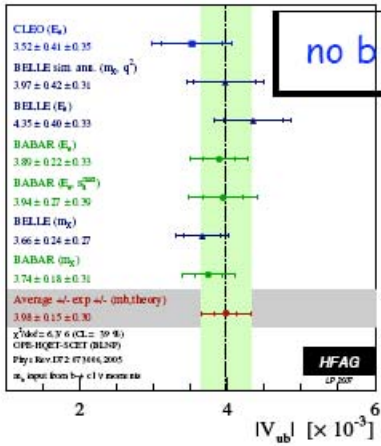
# $|V_{ub}|$ : inclusive vs exclusive

Most probable value of  $V_{ub}$  from measurements of other CKM parameters



$|V_{ub}|$  exclusive

$|V_{ub}|$  inclusive

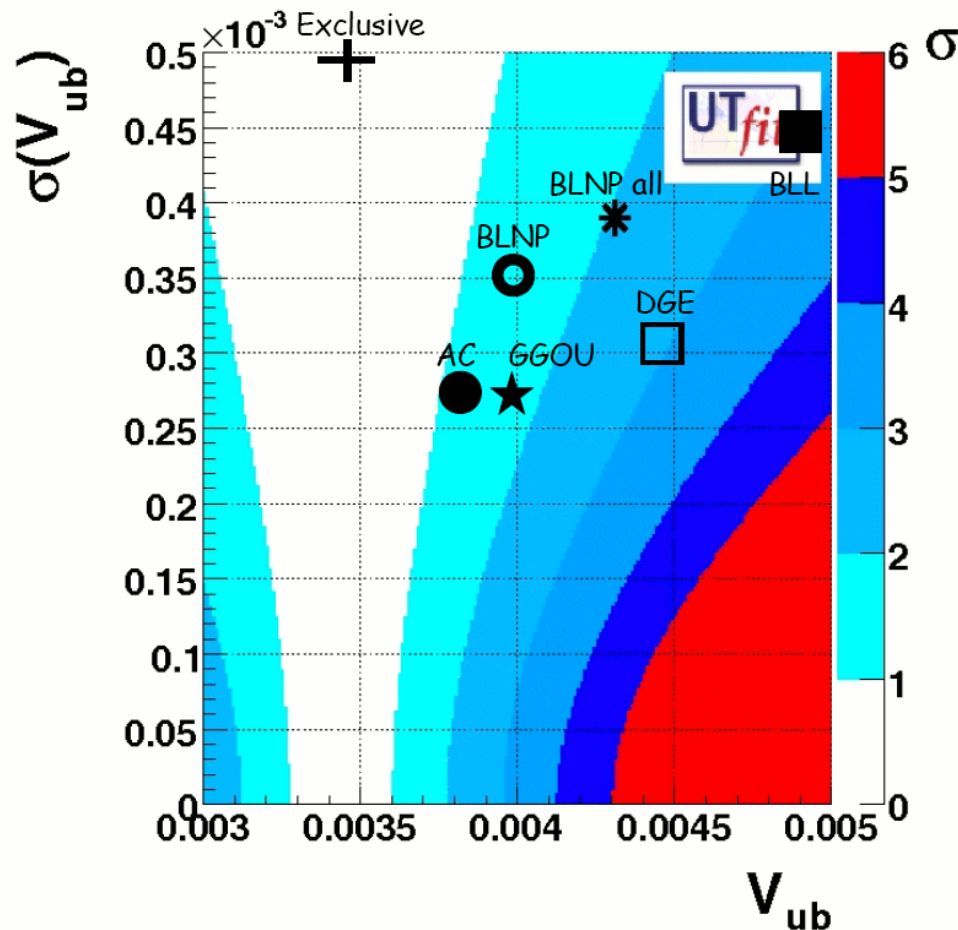


$|V_{ub}|$  inclusive

$b \rightarrow sy$

E. Barberio

# $V_{ub}$ : inclusive versus exclusive



- small "tension" with exclusive for some calculations

- measurements still dominated by theory  
great effort to improve: measurements can help as well

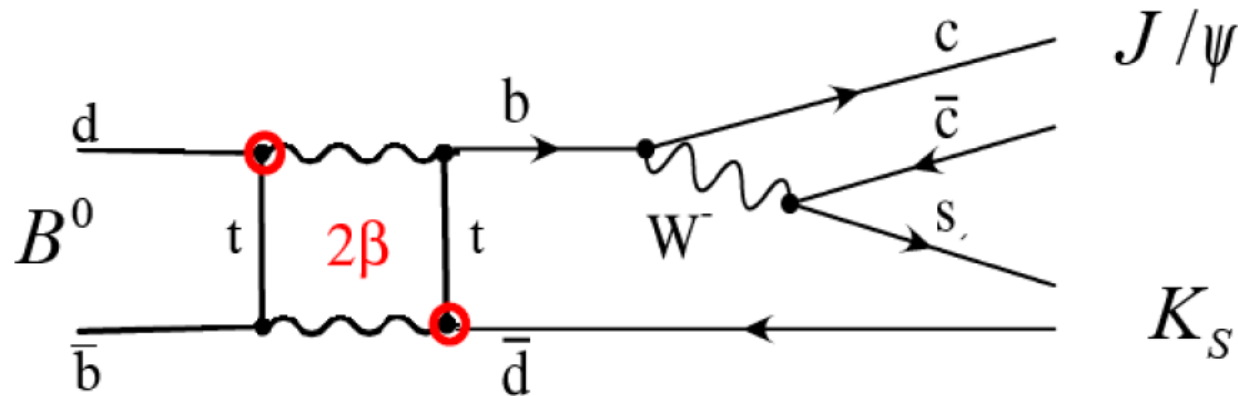
- error on  $|V_{ub}| \sim 9\%$ ; expected to push down to 5%



# CKM angle measurements

# Measurement of $\beta$

- The measurement of  $\beta$  is to “collect” the phase of the  $B^0\bar{B}^0$  mixing:



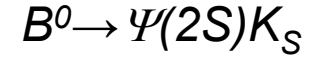
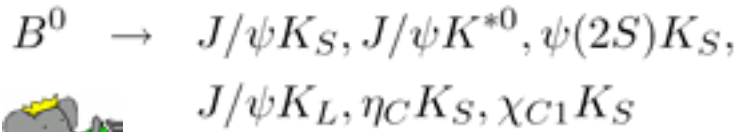
$$A(\Delta t) = S_{f_{CP}} \sin(\Delta m_d \Delta t) - C_{f_{CP}} \cos(\Delta m_d \Delta t)$$

$$\lambda_{f_{CP}} = \frac{q}{p} \frac{\bar{A}}{A} = \eta_{f_{CP}} e^{-i2\beta}$$

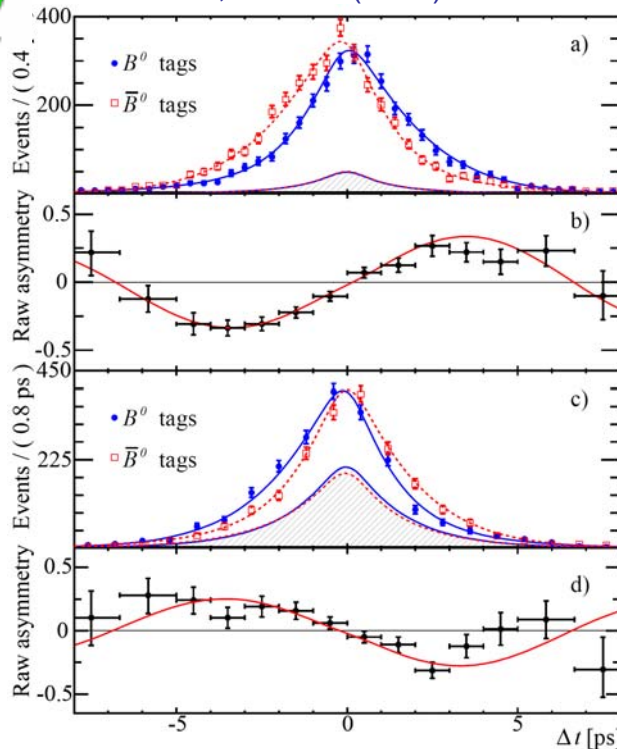
$$|\lambda_{f_{CP}}| = 1, C_{f_{CP}} = 0 \quad S_{f_{CP}} = -\eta_{f_{CP}} \sin 2\beta$$

Uncertainty  $\sim 1\%$

# $\sin(2\beta)$ in $b \rightarrow c\bar{c}s$ decays : “golden modes”

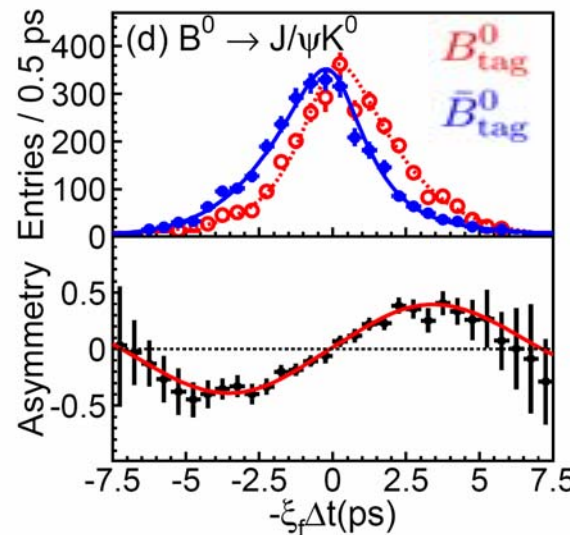


PRL 99, 171803 (2007) 383M BB



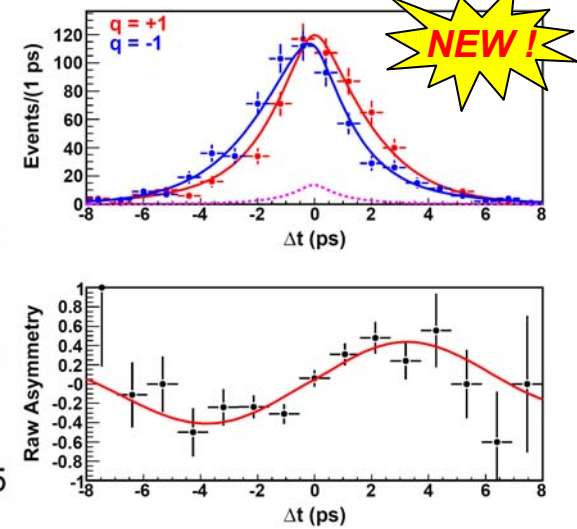
$\sin 2\beta = 0.714 \pm 0.032 \pm 0.018$   
 $|\lambda| = 0.952 \pm 0.022 \pm 0.017$

PRL 98, 031802 (2007) 535 BB



$\sin 2\phi_1 = +0.642 \pm 0.031 \pm 0.017$      $S = +0.72 \pm 0.09 \pm 0.03$   
 $A = -0.018 \pm 0.021 \pm 0.014$      $A = +0.04 \pm 0.07 \pm 0.05$

PRD(R) 77, 091103 (2008) 657M BB



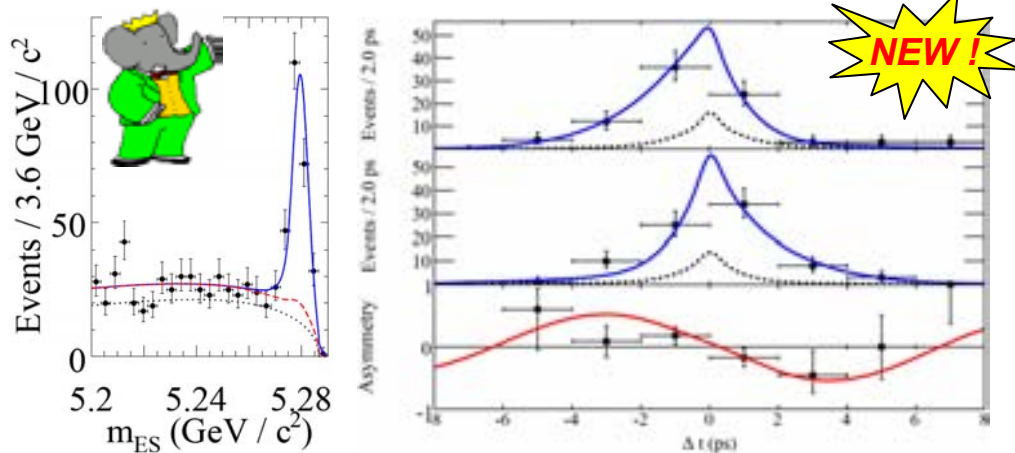
**New BELLE average**

$\sin 2\beta = +0.650 \pm 0.029 \pm 0.018$   
 $A = -0.019 \pm 0.020 \pm 0.015$

# $b \rightarrow c\bar{c}d$ decays : $B^0 \rightarrow J/\Psi\pi^0$

- Penguins with different phases could contribute
- If not, SM predicts  $S = -\sin 2\beta$ ,  $C = 0$
- Can constrain penguin pollution in  $J/\Psi K^0$ , by SU(3)  
(see PRL **95**, 221804 (2005) : uncertainties may be larger than considered)

arXiv:0804.0896, accepted by PRL **466M BB**



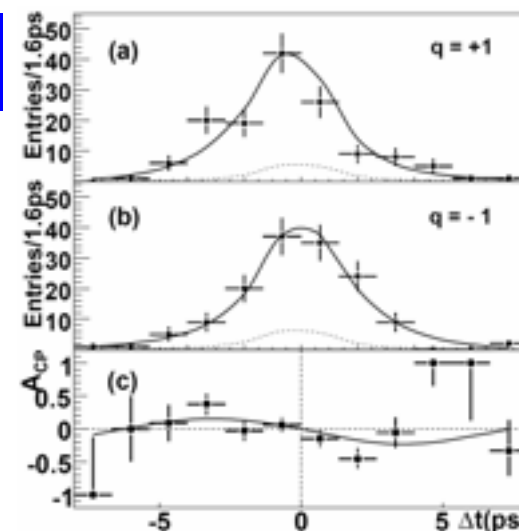
$$S = -1.23 \pm 0.21 \pm 0.04$$

$$C = -0.20 \pm 0.19 \pm 0.03$$

$$BF = (1.69 \pm 0.14 \pm 0.07) \cdot 10^{-5}$$

4 $\sigma$  evidence for CPV !

PRD(RC) **77**, 071101 (2008) **535M BB**

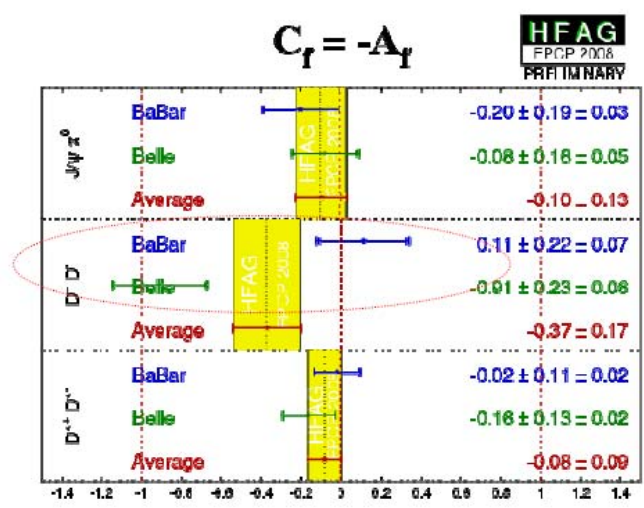
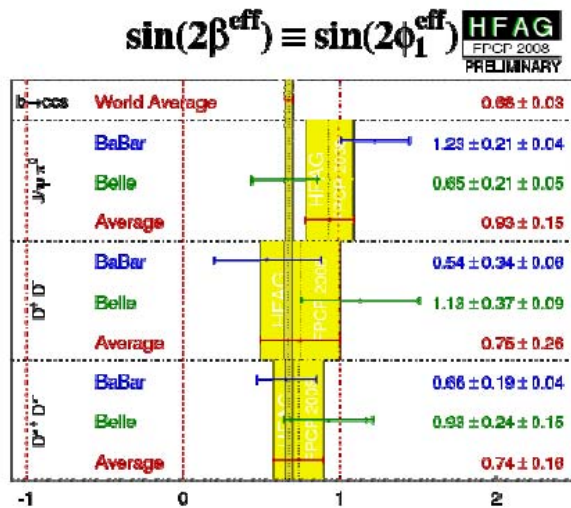
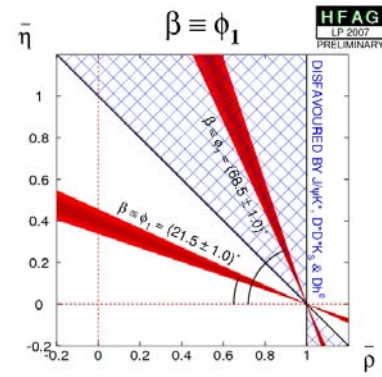
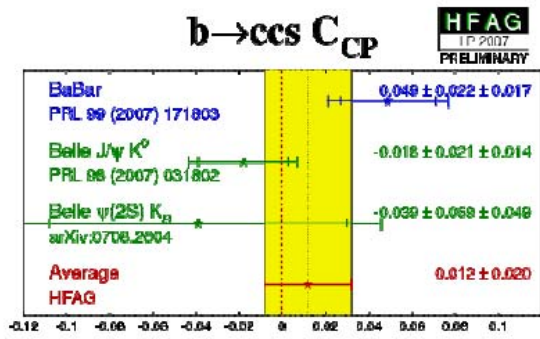
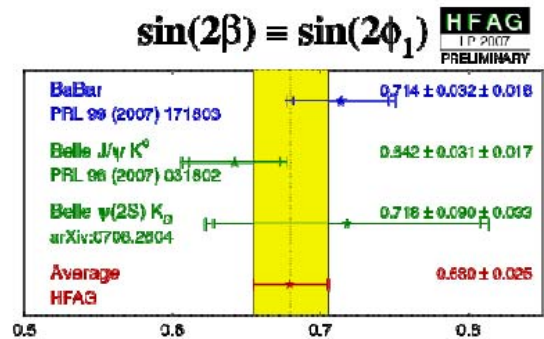


$$S = -0.65 \pm 0.21 \pm 0.05$$

$$C = -0.08 \pm 0.16 \pm 0.05$$

S is 2.4 $\sigma$  from 0

# sin2β from b→c $\bar{c}$ s, c $\bar{c}$ d decays: summary

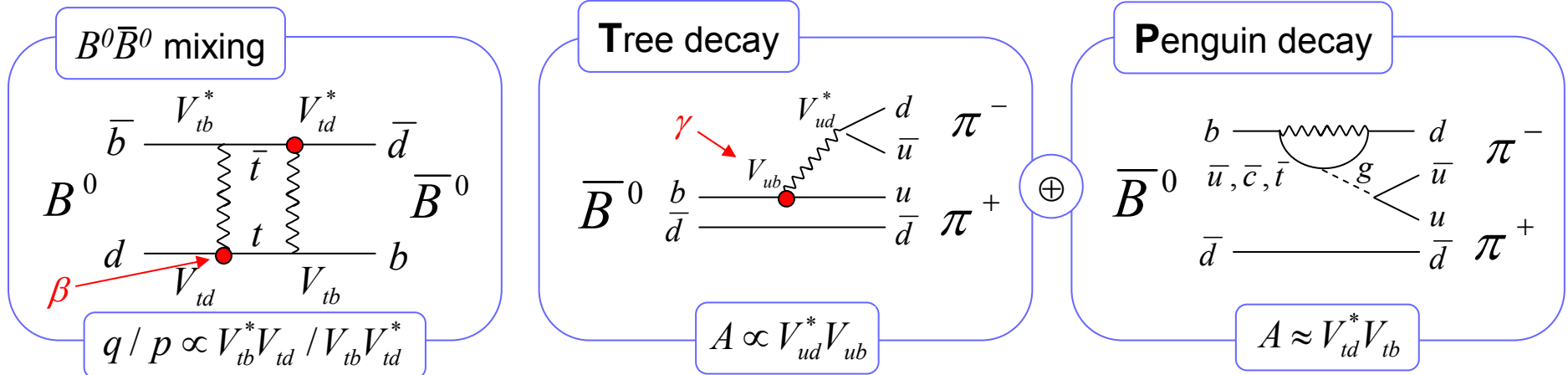


BEACH 2008, 22-28 June, 2008

F. Martínez-Vidal, Unitarity Triangle angles at BaBar

26

# Measuring $\alpha$ : penguin pollution



$$A(\Delta t) = S_{f_{CP}} \sin(\Delta m_d \Delta t) - C_{f_{CP}} \cos(\Delta m_d \Delta t) \quad |P/T| \sim 30-60\% \text{ in } \pi^+\pi^-$$

$$\lambda_{f_{CP}} = \frac{q}{p} \frac{\bar{A}}{A} = \eta_{f_{CP}} e^{-i2\beta} e^{-i2\gamma} = \eta_{f_{CP}} e^{i2\alpha}$$

$$S_{f_{CP}} = -\eta_{f_{CP}} \sin 2\alpha$$

$$C_{f_{CP}} = 0$$

$\Rightarrow$

penguin pollution

$$\lambda_{f_{CP}} = \eta_{f_{CP}} e^{i2\alpha} \frac{T + P e^{+i\gamma} e^{i\delta}}{T + P e^{-i\gamma} e^{i\delta}} = \eta_{f_{CP}} \left| \lambda_{f_{CP}} \right| e^{i2\alpha_{eff}}$$

$$S_{f_{CP}} = \eta_{f_{CP}} \sqrt{1 - C_{f_{CP}}^2} \sin 2\alpha_{eff}$$

$$C_{f_{CP}} \propto \sin \delta, \quad \delta = \delta_P - \delta_T \text{ strong phase diff.}$$

How to obtain  $\alpha$  from  $\alpha_{eff}$ ?  $\rightarrow$  need additional information

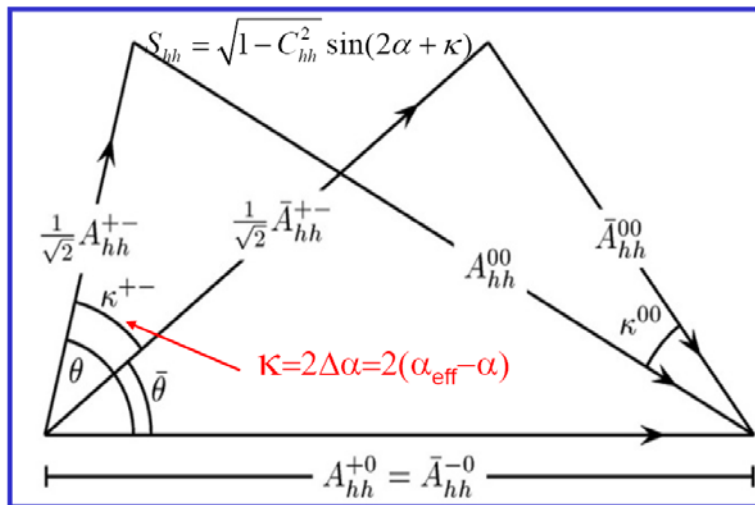
# Coping with penguins

- Gronau & London analysis:**

- According to SU(2):
  - Tree amplitude is I=0 and I=2
  - Gluonic penguin is pure I=0
  - $B^+ \rightarrow h^+ h^0$  is pure I=2 (neglecting EW penguins) so :  $A^{+0} = \bar{A}^{-0}$

- Decay amplitudes are related by:

$$A^{+0} = \frac{1}{\sqrt{2}} A^{+-} + A^{00}; \bar{A}^{-0} = \frac{1}{\sqrt{2}} \bar{A}^{+-} + \bar{A}^{00}$$



- Allows estimation of penguin-induced shift in  $\alpha$ :

$$\kappa^{+-} = 2(\alpha_{eff} - \alpha)$$

- But 4-fold ambiguity

$$\kappa^{+-} = \pm(\theta \pm \bar{\theta})$$

- And 2-fold ambiguity in  $2\alpha$

- Measurement of 6 amplitudes needed, on 6 tagged samples

- time dependent analyses needed for  $B^0$  amplitudes.

- Grossman/Quinn bound:**

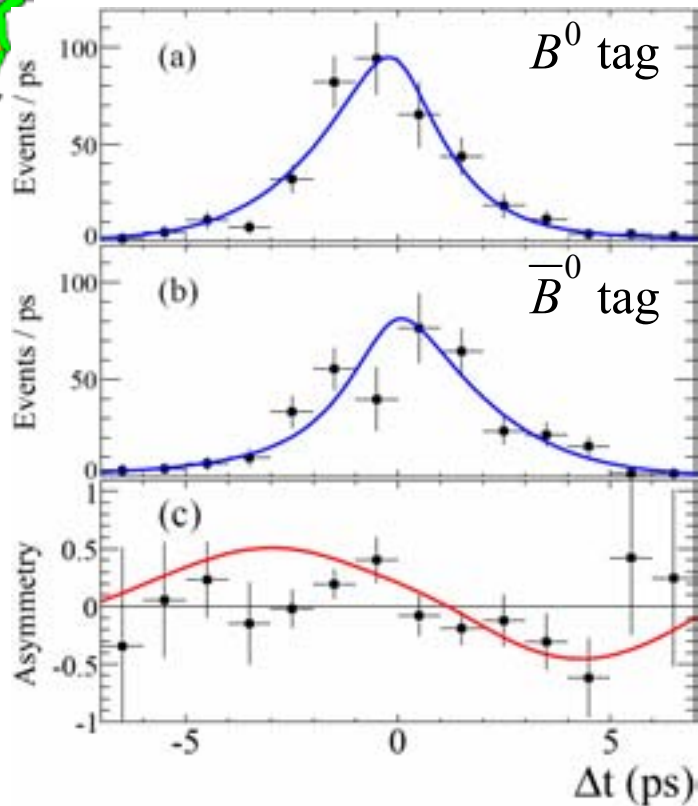
$$\sin^2(\alpha_{eff} - \alpha) \leq \frac{BF(B \rightarrow h^0 h^0)}{BF(B^\pm \rightarrow h^\pm h^0)}$$

- don't need to tag B flavor
- useful if  $BF(B \rightarrow h^0 h^0)$  is small

# CP asymmetries in $B^0 \rightarrow \pi^+ \pi^-$



PRL 99, 021603 (2007) **383M BB**



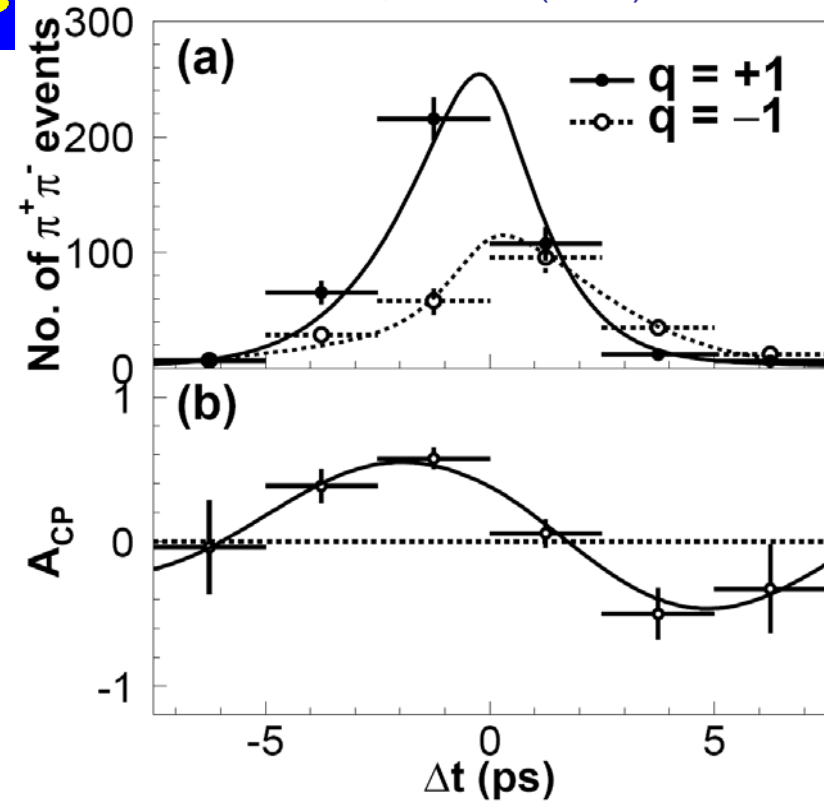
**$1139 \pm 49$  signal events**

**$S_{+-} = -0.60 \pm 0.11 \pm 0.03$  ( $5.1\sigma$ )**

**$C_{+-} = -0.21 \pm 0.09 \pm 0.02$  ( $2.2\sigma$ )**



PRL 98, 211801 (2007) **535M BB**



**$1464 \pm 65$  signal events**

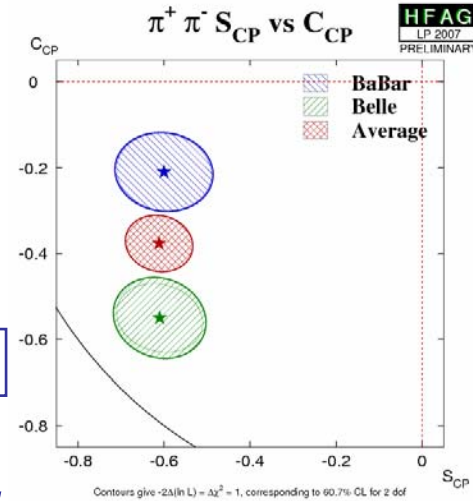
**$S_{+-} = -0.61 \pm 0.10 \pm 0.04$  ( $5.3\sigma$ )**

**$C_{+-} = -0.55 \pm 0.08 \pm 0.05$  ( $5.5\sigma$ )**



# $\alpha$ from $B \rightarrow \pi\pi$

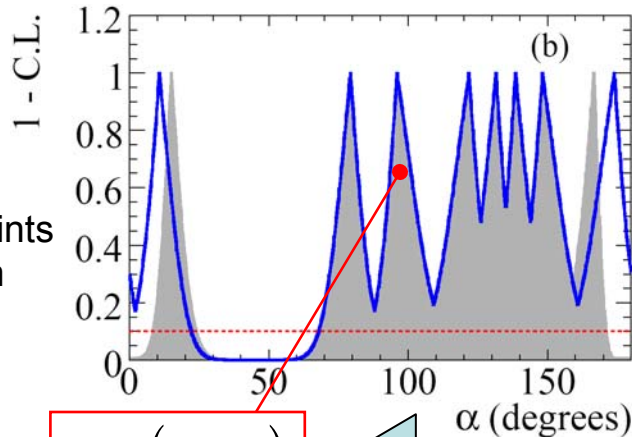
- CPV well established in  $B^0 \rightarrow \pi^+ \pi^-$ 
  - still some  $2.1\sigma$  difference in direct CPV between BABAR and BELLE



$\pi^0 \pi^0$  time dependent asymmetry!      Time integrated asymmetry

- Isospin analysis to extract  $\alpha$ 
  - use/measure  $S_{+-}, C_{+-}, S_{00}, C_{00}, BF_{+-}, BF_{00}$

PRD 76, 091102 (2007) 383M BB



■ SU(3) constraints on penguin from  $B_s \rightarrow K^+ K^-$

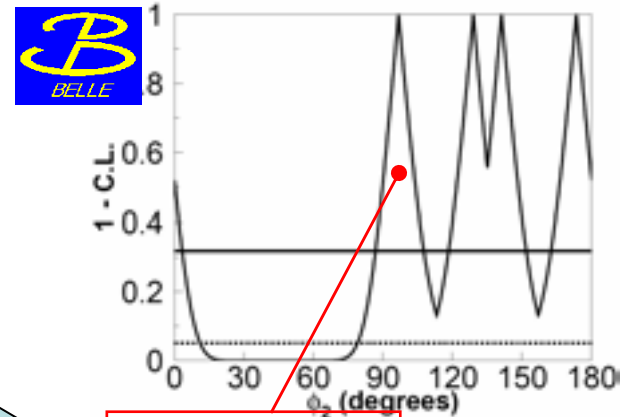


$$\alpha = (96^{+11}_{-6})^\circ$$

SM compatible solutions

$$\alpha = (96 \pm 11)^\circ$$

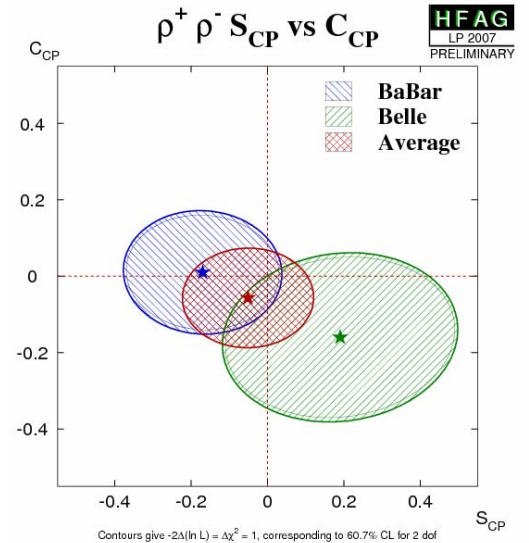
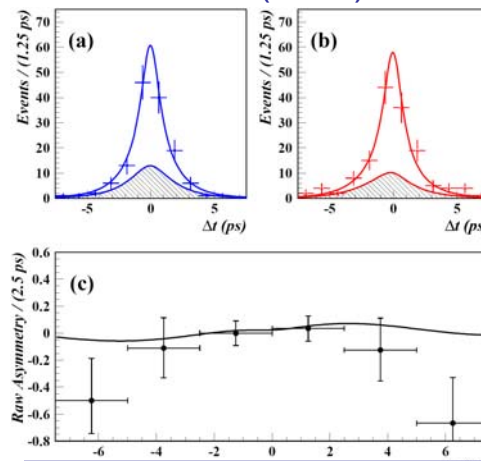
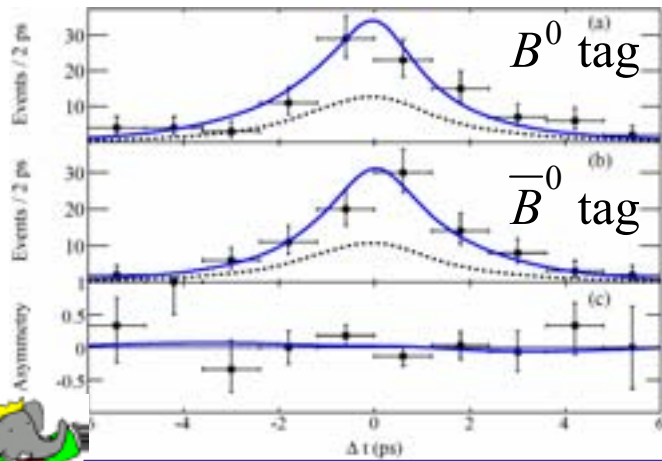
PRL 98, 211801 (2007) 535M BB



# CP asymmetries in $B^0 \rightarrow \rho^+ \rho^-$

- Vector Vector final state
  - but almost pure  $CP$  even ( $f_L \sim 1$ )
- Large BF, small penguin pollution
  - $\rho$  is wide
- Experimentally challenging
  - up to  $2\pi_0$  in final state

PRD 76 052007 (2007) 383M BB PRL 96 171801 (2006) 265M BB  
 PRD 76 011104 (2007) 535M BB



HFAG  
 LP 2007  
 PRELIMINARY



$$BF^{+-} = (25.5 \pm 2.1^{+3.6}_{-3.9}) \times 10^{-6}$$

$$f_L^{+-} = 0.992 \pm 0.024^{+0.026}_{-0.013}$$

$$C_L^{+-} = +0.01 \pm 0.15 \pm 0.06$$

$$S_L^{+-} = -0.17 \pm 0.20^{+0.05}_{-0.06}$$

$$BF^{+-} = (22.8 \pm 3.8^{+2.3}_{-2.6}) \times 10^{-6}$$

$$f_L^{+-} = 0.941^{+0.034}_{-0.040} \pm 0.30$$

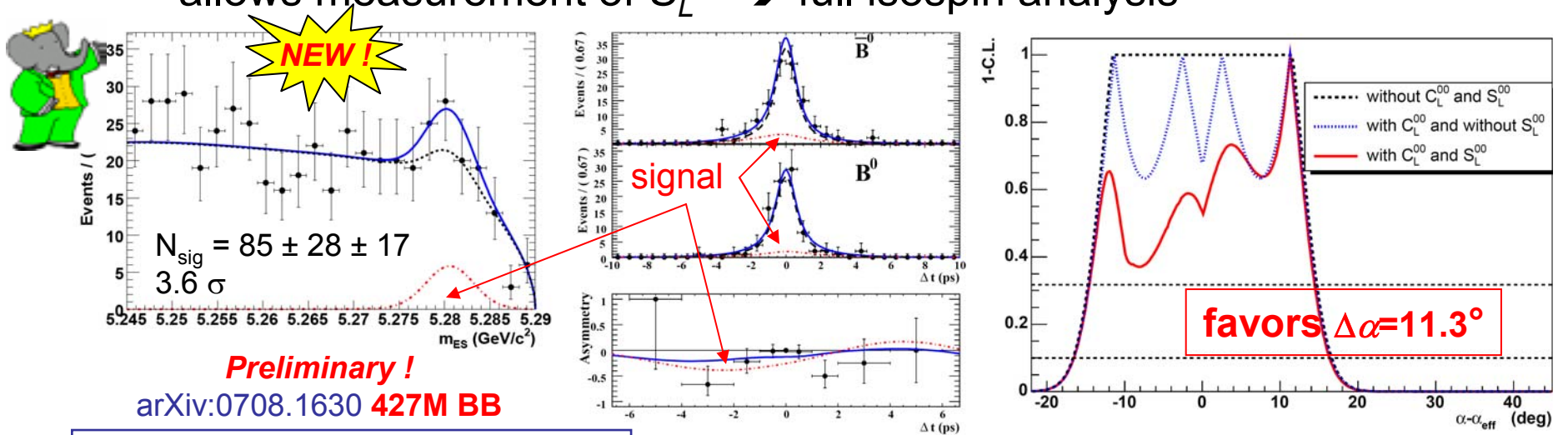
$$C_L^{+-} = -0.16 \pm 0.21 \pm 0.08$$

$$S_L^{+-} = +0.19 \pm 0.30 \pm 0.08$$

World average:  
 $S_{+-} = -0.05 \pm 0.17$   
 $C_{+-} = -0.06 \pm 0.13$

# $B^0 \rightarrow \rho^0 \rho^0$ and isospin analysis

- **First measurement of time dependent asymmetries in  $\rho^0 \rho^0$** 
  - in contrast with  $\pi^0 \pi^0, \rho^0 \rho^0$  vertex can be reconstructed  $\rightarrow$  TD possible
  - allows measurement of  $S_L^{00} \rightarrow$  full isospin analysis



$$BF^{00} = (0.84 \pm 0.29 \pm 0.17) \times 10^{-6}$$

$$f_L^{00} = 0.70 \pm 0.14 \pm 0.05$$

$$C_L^{00} = +0.4 \pm 0.9 \pm 0.2$$

$$S_L^{00} = +0.5 \pm 0.9 \pm 0.2$$

$BF^{00}$  low  $\rightarrow$  penguin small

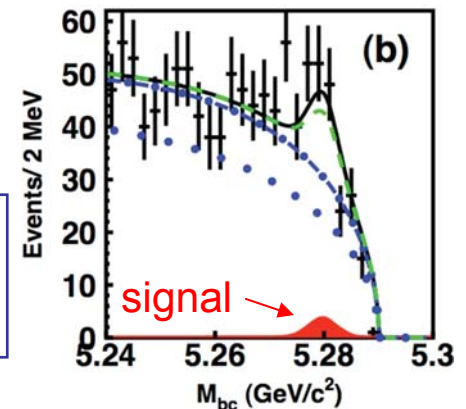


LaThuile, Italy 657M BB



$$BF^{00} = (0.4 \pm 0.4 \pm 0.2) \times 10^{-6}$$

$$< 1.0 \times 10^{-6} @ 90\% \text{ CL}$$



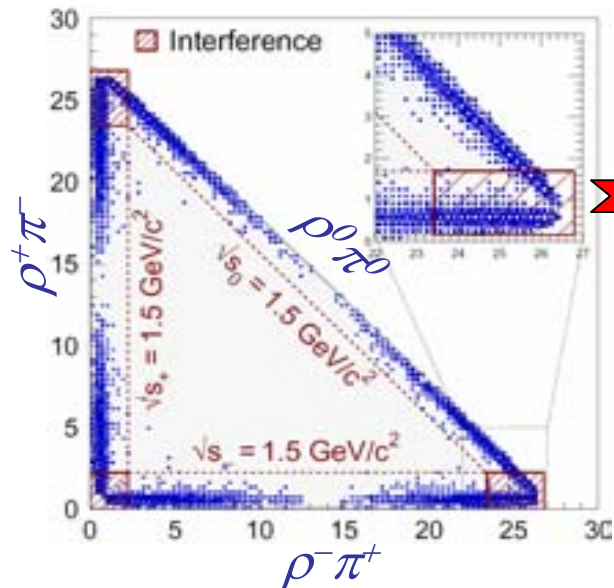
# Dalitz analysis of $B^0 \rightarrow (\rho\pi)^0 \rightarrow \pi^+ \pi^- \pi^0$

- Dominant  $B^0 \rightarrow \rho^+ \pi^-$  is not a **CP eigenstate**
- 5 amplitudes involved :  $B^0 \rightarrow \rho^+ \pi^-, \rho^- \pi^+, \rho^0 \pi^0$  and  $B^+ \rightarrow \rho^+ \pi^0, \rho^0 \pi^+$   
 –  $\rightarrow$  Isospin pentagon !
- Better approach  $\rightarrow$  TD Dalitz analysis assuming isospin symmetry:

$$A(B^0 \rightarrow \pi^+ \pi^- \pi^0) = f_+ A(\rho^+ \pi^-) + f_- A(\rho^- \pi^+) + f_0 A(\rho^0 \pi^0)$$

$$\bar{A}(\bar{B}^0 \rightarrow \pi^+ \pi^- \pi^0) = f_+ \bar{A}(\rho^+ \pi^-) + f_- \bar{A}(\rho^- \pi^+) + f_0 \bar{A}(\rho^0 \pi^0)$$

A. Snyder and H. Quinn,  
PRD 48, 2139 (1993)



Interferences at equal masses provides information on **strong phases** between resonances

# Dalitz analysis of $B^0 \rightarrow (\rho\pi)^0 \rightarrow \pi^+ \pi^- \pi^0$

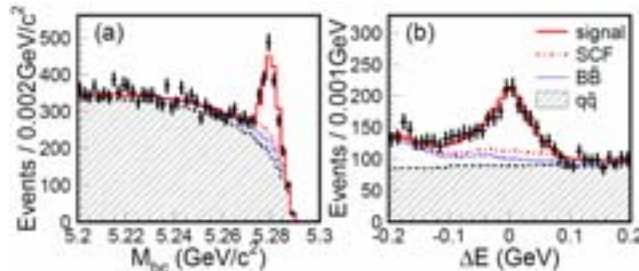
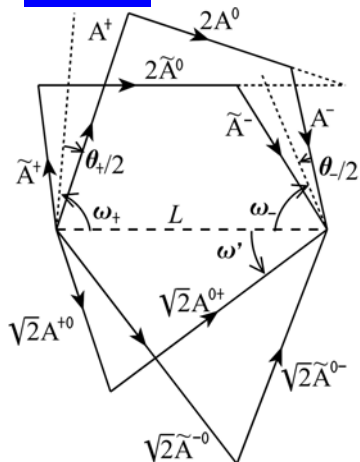
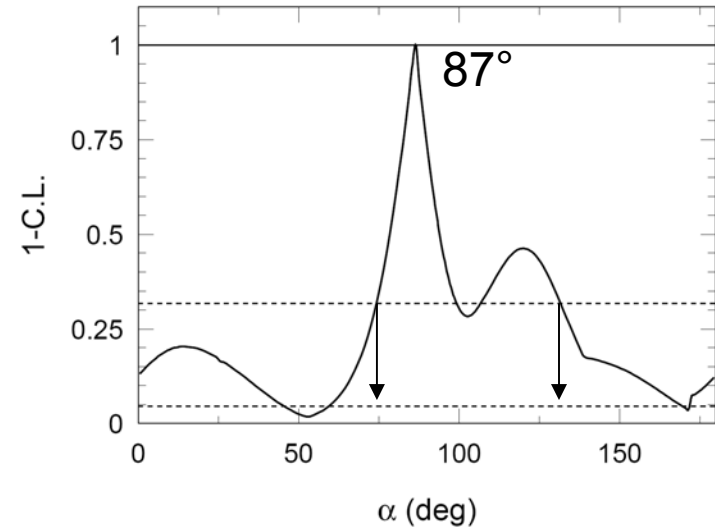


2067 ± 86 signal events

$$\alpha = (87^{+45}_{-13})^\circ$$

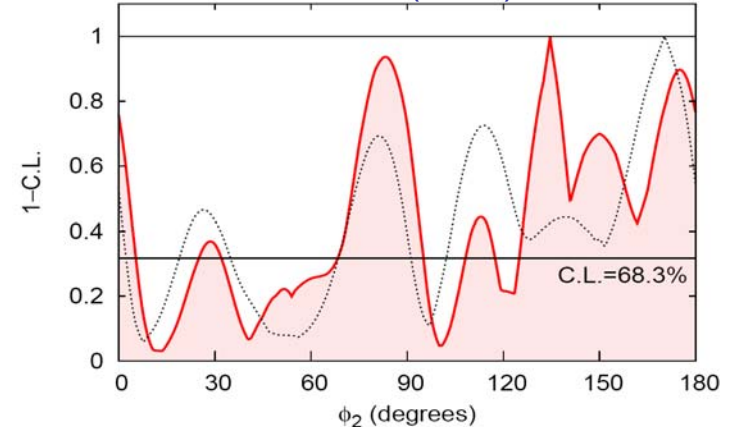
(+ mirror solution at  $\alpha + 180^\circ$ )

PRD 76 012004 (2007) 375M BB



$68 < \alpha < 95^\circ$  at 68% CL

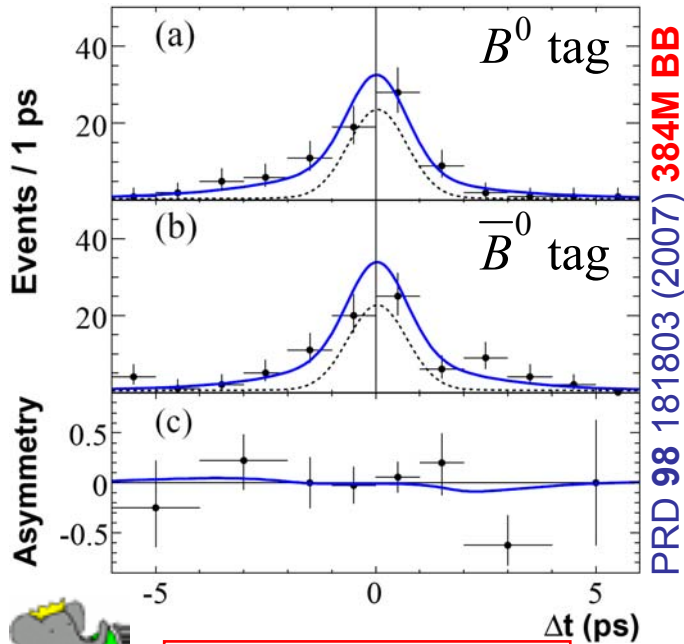
PRD 77 072001 (2008) 349M BB



Dalitz

Dalitz+pentagon

# $B^0 \rightarrow a_1 \pi$



$$\alpha_{eff}^{a_1\pi} = (78.6 \pm 7.3)^\circ$$

- SU(3) related modes ( $\pi \leftrightarrow K$ ,  $a_1 \leftrightarrow K_1$ ) to constrain  $\alpha$ - $\alpha_{eff}$ :
  - $B \rightarrow a_1 K$ : PRL **100**, 051802 (2008)
  - $B \rightarrow K_1 \pi$ : ongoing

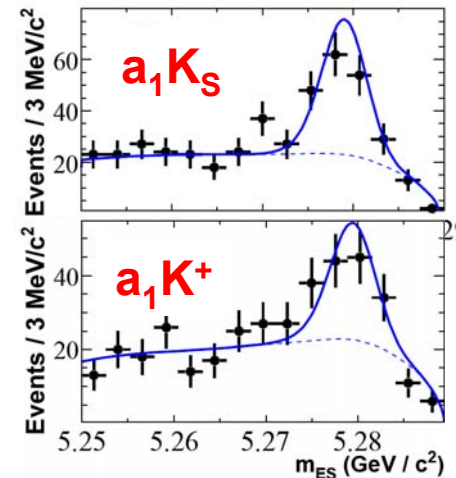
- Decay  $B^0 \rightarrow a_1 \pi$  has same quark diagram than  $B \rightarrow \pi\pi, \rho\pi, \dots$ 
  - and is similar to  $B \rightarrow \rho\pi$ : not a CP eigenstate, quasi-2 body approach
- High branching fraction:

$$BR = (33.2 \pm 3.2 \pm 3.2) \times 10^{-6}$$

PRL **97**, 051802 (2006)

$$BR = (29.8 \pm 3.2 \pm 4.6) \times 10^{-6}$$

hep-ex 0706.3279



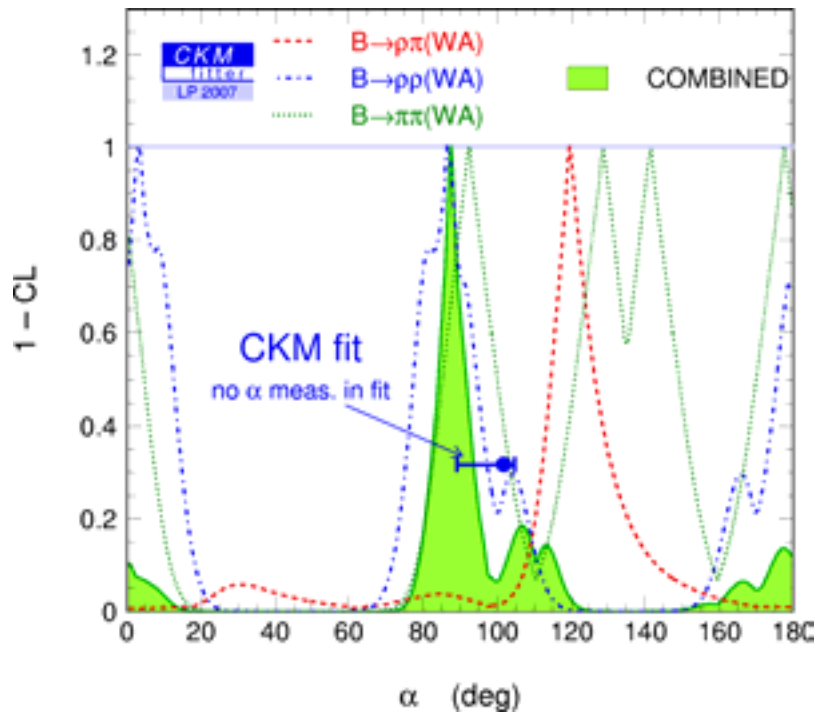
$$BF(B^0 \rightarrow a_1^- K^+) = (16.3 \pm 2.9 \pm 2.3) \times 10^{-6}$$

$$BF(B^0 \rightarrow a_1^- K^0) = (34.9 \pm 5.0 \pm 4.4) \times 10^{-6}$$

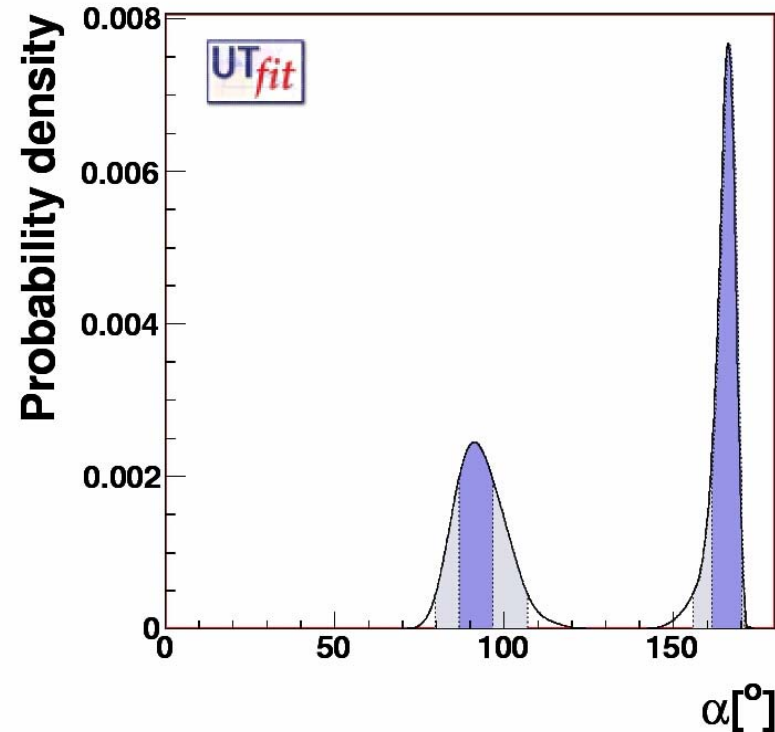


# Combined constraints on $\alpha$

- Frequentist versus Bayesian treatment of constraints



$1\sigma$  interval for  $\alpha$  [82.2 ; 93.7] $^\circ$



- Excluded regions are common.
- Situation should clarify with more data.

# Measurement of $\gamma$ : methods overview

- Measure relative phase ( $\gamma$ ) between  $b \rightarrow \bar{c} \bar{u} s$  and  $b \rightarrow \bar{u} \bar{c} s$  decay processes
- **For final states common to  $D^0$  and  $\bar{D}^0 \Rightarrow$  interferences  $\Rightarrow \gamma$  accessible**

$A \sim \lambda^3$

Color favored

Color suppr.

### Three methods

GLW $D^0$ CP modes	ADS DCSD mode	GGSZ Dalitz
$K^+K^-, \pi^+\pi^-$ [CP+] $K_S\pi^0, K_S\omega, K_S\phi$ [CP-]	$K^+\pi^-$ $D^0 \rightarrow K^+\pi^-$ suppr. $\bar{D}^0 \rightarrow K^+\pi^-$ fav.	<div style="border: 1px solid gray; padding: 5px; text-align: center;"> <math>K_S\pi^+\pi^-</math> <math>K_S K^+K^-</math> <math>\pi^0\pi^+\pi^-</math> </div>

$A \sim \lambda^3 r_B^{(*)} e^{-i\gamma} e^{i\delta}$

**Theoretically clean: no penguin contributions.**

- $\delta$  = relative (unknown) strong phase
- $\gamma$  = weak phase
- $r_B^{(*)}$  = (critical) ratio of suppr./fav. amplitudes:

$$r_B^{(*)} \equiv \left| \frac{A(B^- \rightarrow \bar{D}^{(*)0} K^-)}{A(B^- \rightarrow D^{(*)0} K^-)} \right| \sim 0.1 - 0.2$$



# Updated $B^+ \rightarrow D^* K^+$ and $B^+ \rightarrow DK$ GLW

- Based on triangle relations of amplitudes

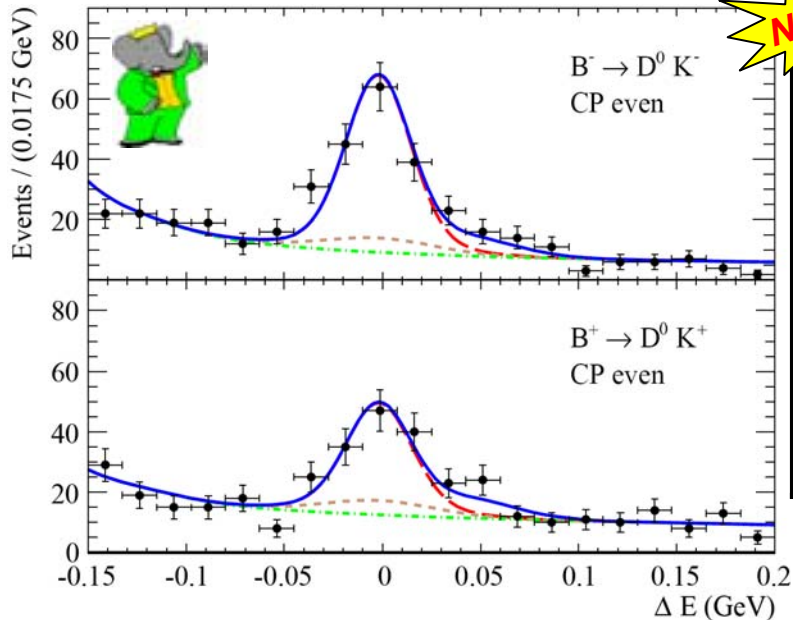
$$R_{CP\pm} \equiv \frac{\Gamma(B^- \rightarrow D_{CP\pm}^0 K^-) + \Gamma(B^+ \rightarrow D_{CP\pm}^0 K^+)}{[(B^- \rightarrow D^0 K^-) + \Gamma(B^+ \rightarrow \bar{D}^0 K^+)]/2} = 1 + r_B^2 \pm 2r_B \cos \delta \cos \gamma$$

$$A_{CP\pm} \equiv \frac{\Gamma(B^- \rightarrow D_{CP\pm}^0 K^-) - \Gamma(B^+ \rightarrow D_{CP\pm}^0 K^+)}{\Gamma(B^- \rightarrow D_{CP\pm}^0 K^-) + \Gamma(B^+ \rightarrow D_{CP\pm}^0 K^+)} = \pm 2r_B \sin \delta \sin \gamma / R_{CP\pm}$$

8-fold ambiguity on  $\gamma$

$$A_{CP+} R_{CP+} = -A_{CP-} R_{CP-}$$

2.8 $\sigma$  from no CPV



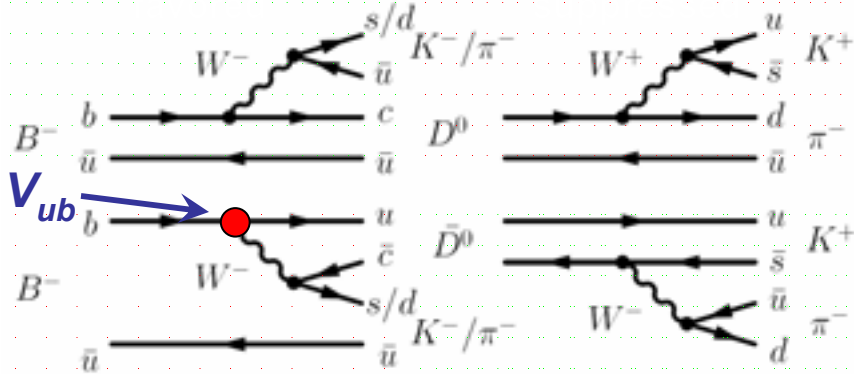
	$B^+ \rightarrow DK^+$	$B^+ \rightarrow D^* K^+$
$A_{CP+}$	$+0.27 \pm 0.09 \pm 0.04$	$-0.11 \pm 0.09 \pm 0.01$
$A_{CP-}$	$-0.09 \pm 0.09 \pm 0.02$	$+0.06 \pm 0.10 \pm 0.02$
$R_{CP+}$	$1.06 \pm 0.10 \pm 0.05$	$1.31 \pm 0.13 \pm 0.04$
$R_{CP-}$	$1.03 \pm 0.10 \pm 0.05$	$1.10 \pm 0.12 \pm 0.04$

arXiv:0802.4052 **383M BB**  
accepted by PRD

preliminary **383M BB**  
(hot topic FPCP 08)

Results consistent with  $\gamma = (67.6 \pm 4.0)^\circ$  from SM fit

# Updated $B^+ \rightarrow DK^+$ ADS

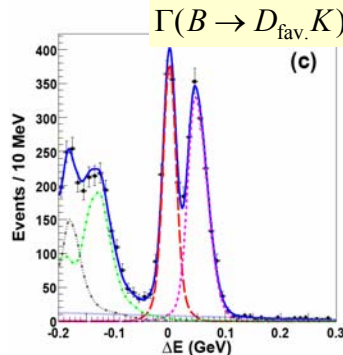
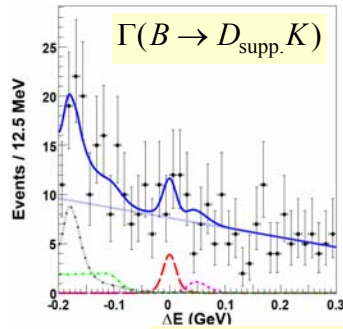


$$r_D = 0.0578 \pm 0.0008$$

$$R_{ADS} \equiv \frac{\Gamma(B \rightarrow D_{\text{supp.}} K)}{\Gamma(B \rightarrow D_{\text{fav.}} K)} = r_D^2 + r_B^2 + 2r_B r_D \cos \gamma \cos \delta$$

$$A_{ADS} \equiv \frac{\Gamma(B^- \rightarrow D_{\text{supp.}} K^-) - \Gamma(B^+ \rightarrow D_{\text{supp.}} K^+)}{\Gamma(B^- \rightarrow D_{\text{supp.}} K^-) + \Gamma(B^+ \rightarrow D_{\text{supp.}} K^+)} = 2r_B r_D \sin \gamma \sin \delta / R_{ADS}$$

$\delta = \delta_B + \delta_D$  : relative strong phases for B and D decays



arXiv:0804.2063, submitted to PRD(RC) 657M BB

No significant signal observed in the suppressed mode:

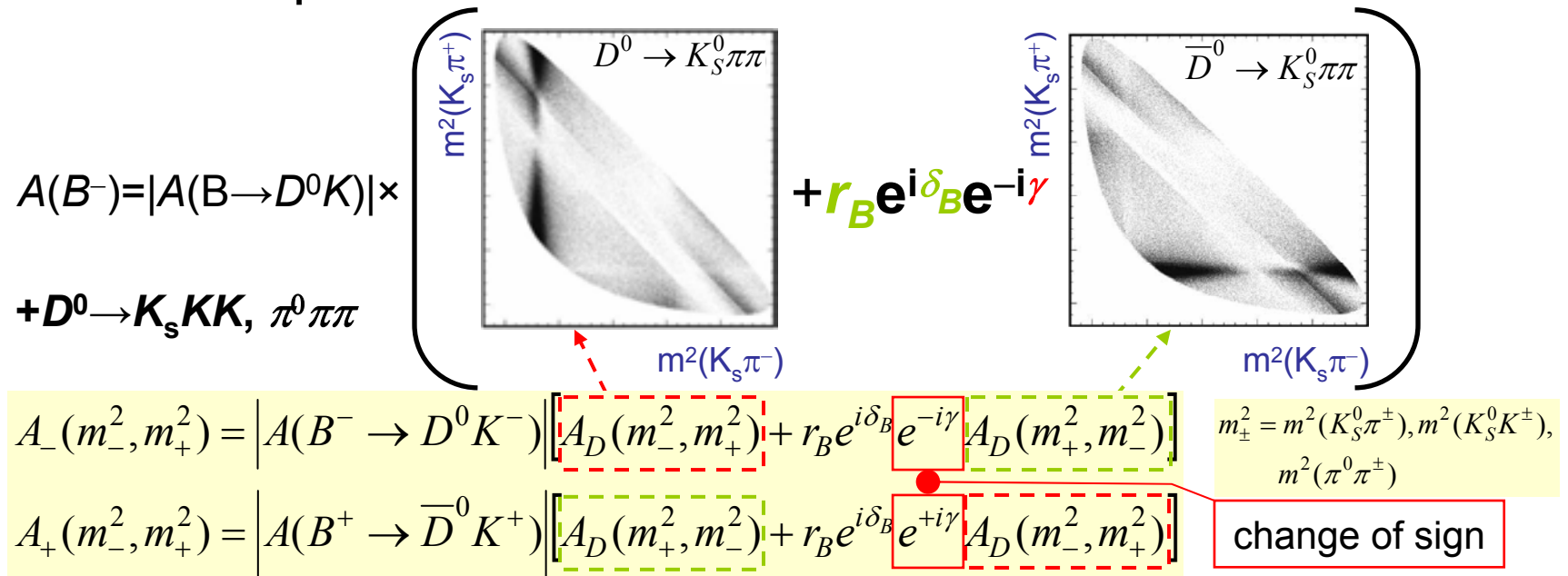
$$\text{BF}(B \rightarrow D_{\text{supp.}} K) < 2.8 \cdot 10^{-7} \text{ @ } 90\% \text{ CL}$$

$$r_B < 0.19 \text{ @ } 90\% \text{ CL}$$

# B<sup>+</sup> → D<sup>(\*)</sup>K<sup>+</sup> Dalitz

Giri et al. PRD **68**, 054018 (2003)  
Bondar, PRD **70**, 072003 (2004)

- The idea in pictures:



- Extract  $\gamma, r_B, \delta_B$  using cartesian coordinates  $x_\pm$  and  $y_\pm$

$$\Gamma_\pm(m_-^2, m_+^2) \propto |A_{D^\pm}|^2 + r_B^2 |A_{D^\mp}|^2 + 2\eta \left\{ x_\pm \Re[A_{D^\pm} A_{D^\mp}^*] + y_\pm \Im[A_{D^\pm} A_{D^\mp}^*] \right\}$$

$$\begin{aligned} x_\pm &= \kappa r_B \cos(\delta_B \pm \gamma) \\ y_\pm &= \kappa r_B \sin(\delta_B \pm \gamma) \end{aligned}$$

– makes likelihood Gaussian and unbiased

$\kappa$  account for natural width of K<sup>\*</sup>

$\eta$  accounts for parities  $D^0 \rightarrow D^0 \gamma$  wrt  $D^0 \pi^0$

- Two-fold ambiguity  $(\delta_B, \gamma) \rightarrow (\delta_B + \pi, \gamma + \pi)$

# Dalitz plot analysis of $D^0/\bar{D}^0$ decays

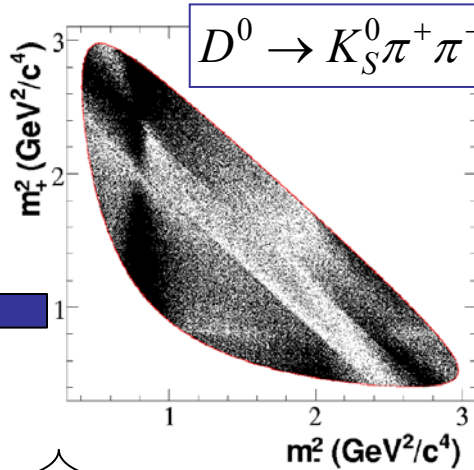
- Extract  $D^0/\bar{D}^0$  decay amplitudes from high statistics samples of  $D^{*+} \rightarrow D^0 \pi^+$ , tagging  $D^0$  flavor with pion charge



arXiv:0802.4052 **383M BB**  
accepted by PRD

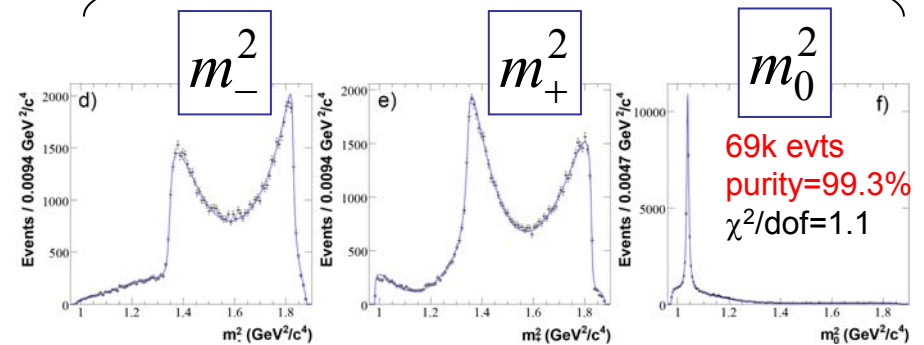
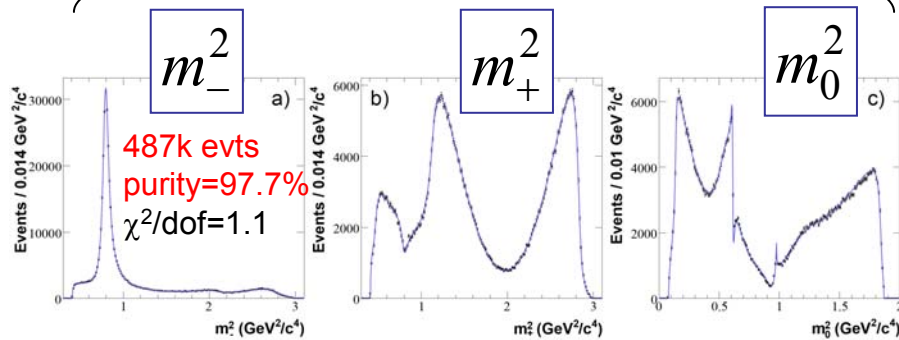
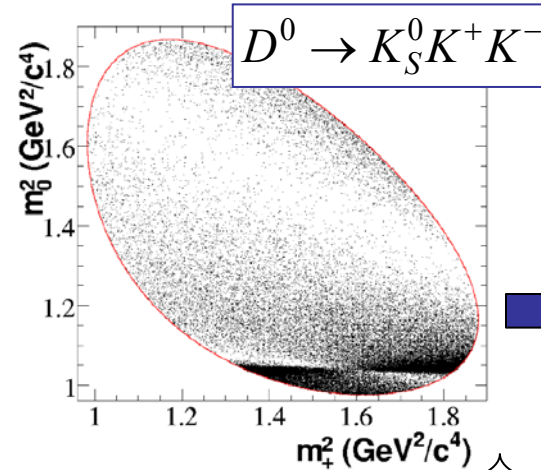
parameterization

$K^*(892)^\pm, K_0^*(1430)^\pm,$   
 $K_2^*(1430)^\pm, K^*(1680)^-,$   
 $\rho(770), \omega(782), f_2(1270),$   
 $K$ -matrix for  $\pi\pi$  S-wave  
and running phase,  
non-resonant for  
 $K\pi$  S-wave



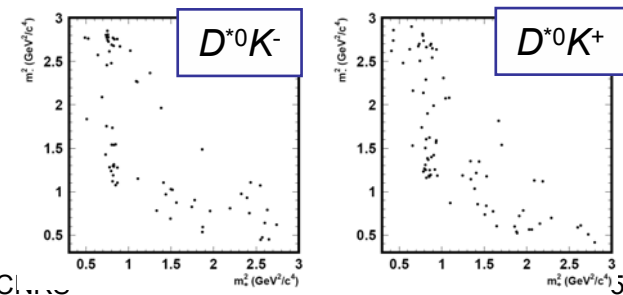
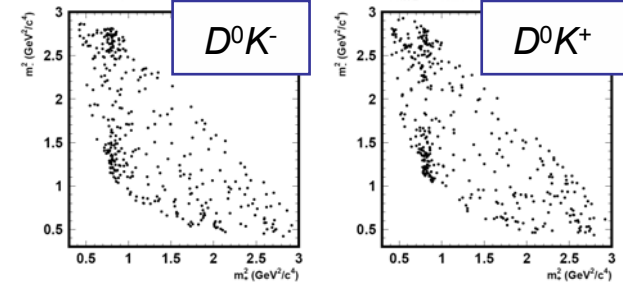
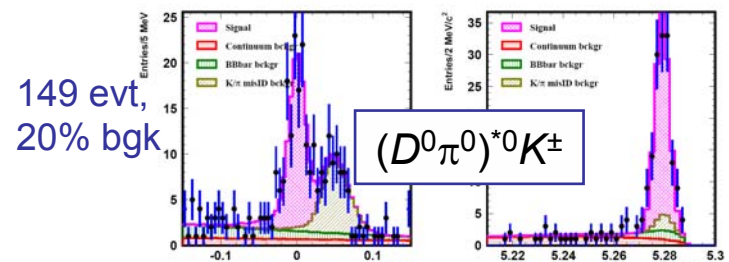
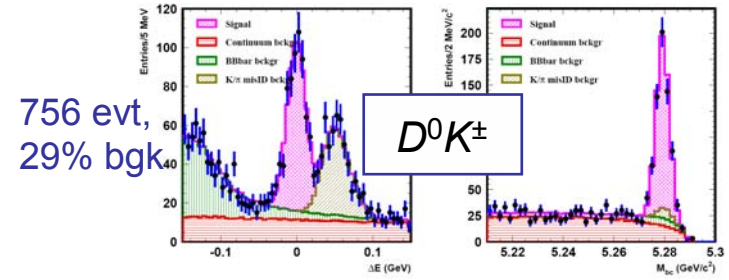
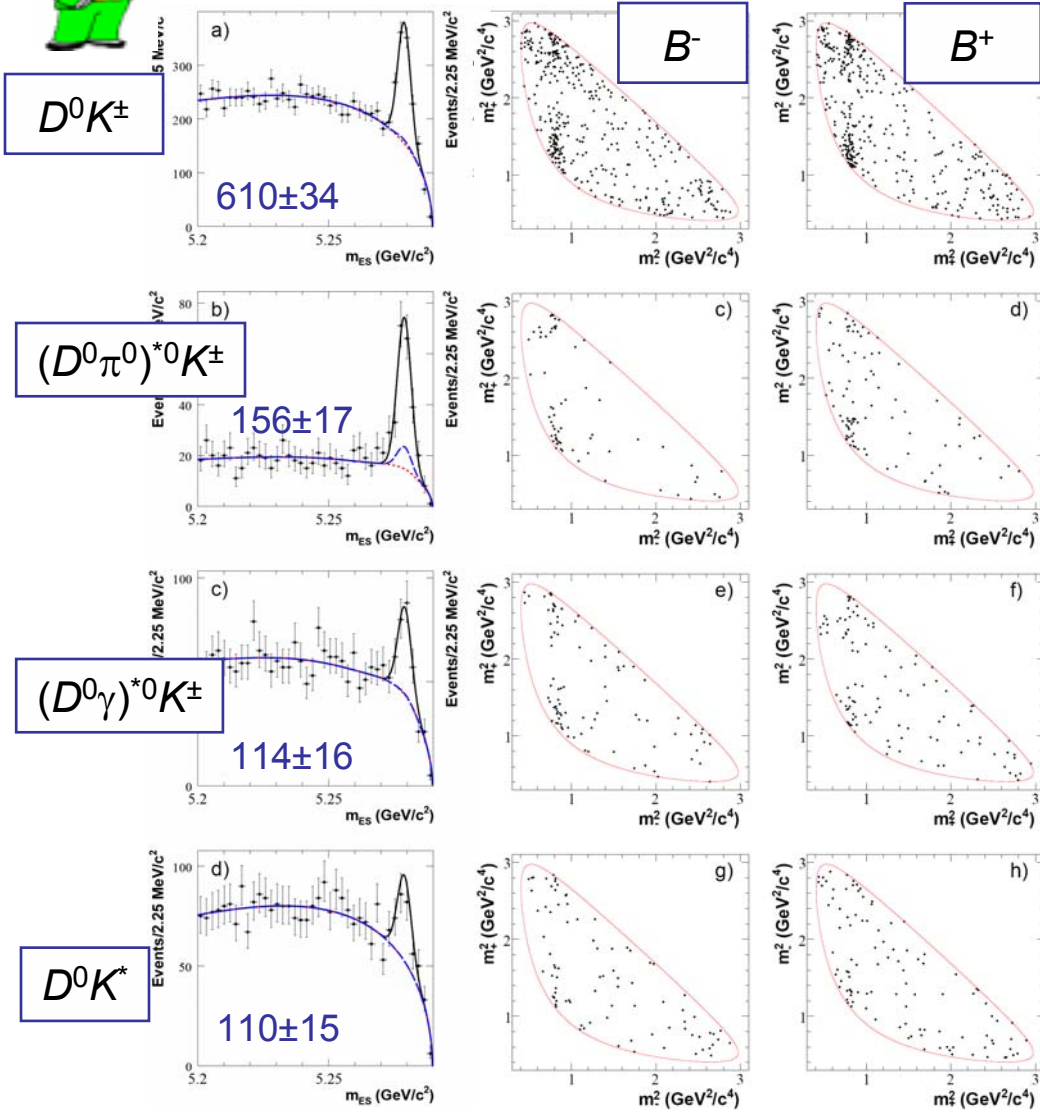
parameterization

$a_0(980)^0, \phi(1020),$   
 $f_0(1370), f_2(1270),$   
 $a_0(980)^\pm, a_0(1450)^0,$   
 $a_0(1450)^\pm$



# $D \rightarrow K_S \pi \pi$ Selected samples

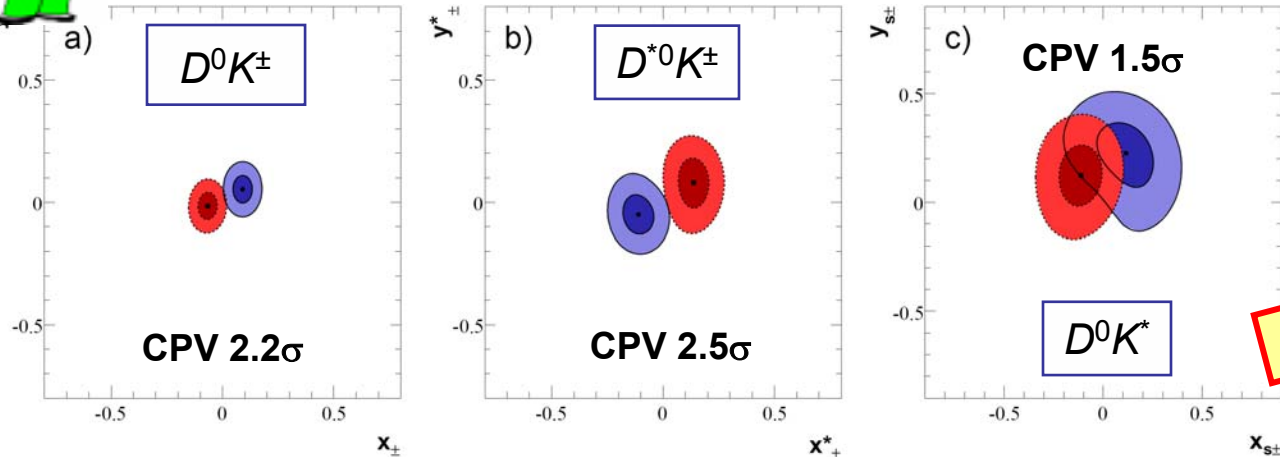
( $D \rightarrow KKK$  from BABAR not shown)



arXiv:0802.4052 383M BB accepted by PRD

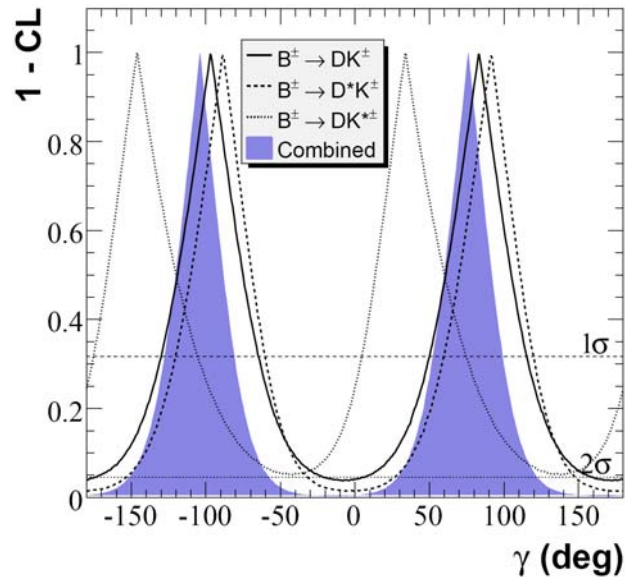
arXiv:0803.3375v1 657M BB

# BABAR Dalitz results



$d(B^+, B^-) = 2r_b |\sin\gamma|$  :  
size of direct CPV

**3σ evidence for direct CPV**



$$r_B(DK) = 0.086 \pm 0.035$$

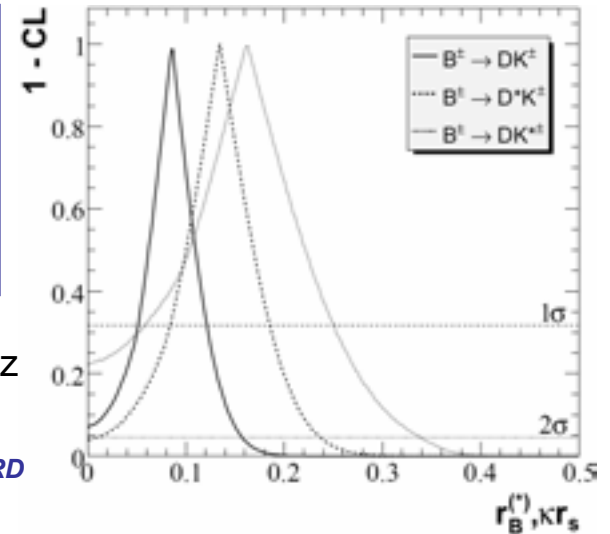
$$r_B(D^*K) = 0.135 \pm 0.051$$

$$kr_s(DK^*) = 0.163^{+0.088}_{-0.105}$$

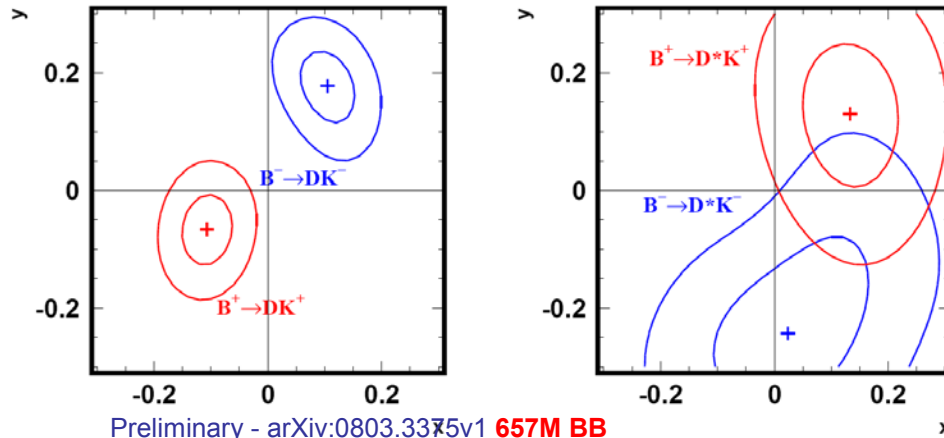
$$\gamma = (76^{+23}_{-24})^\circ$$

includes  $5^\circ$  exp. and  $5^\circ$  Dalitz

arXiv:0802.4052 **383M BB** accepted by PRD



# BELLE Dalitz results



**3.5  $\sigma$  evidence for direct CPV**

Preliminary - arXiv:0803.3375v1 **657M BB**

Parameter	1 $\sigma$ interval	2 $\sigma$ interval	Systematic error	Model uncertainty
$\phi_3$	$76^\circ \begin{smallmatrix} +12^\circ \\ -13^\circ \end{smallmatrix}$	$49^\circ < \phi_3 < 99^\circ$	$4^\circ$	$9^\circ$
$r_{DK}$	$0.16 \pm 0.04$	$0.08 < r_{DK} < 0.24$	0.01	0.05
$r_{D^*K}$	$0.21 \pm 0.08$	$0.05 < r_{D^*K} < 0.39$	0.02	0.05
$\delta_{DK}$	$136^\circ \begin{smallmatrix} +14^\circ \\ -16^\circ \end{smallmatrix}$	$100^\circ < \delta_{DK} < 163^\circ$	$4^\circ$	$23^\circ$
$\delta_{D^*K}$	$343^\circ \begin{smallmatrix} +20^\circ \\ -22^\circ \end{smallmatrix}$	$293^\circ < \delta_{DK} < 389^\circ$	$4^\circ$	$23^\circ$

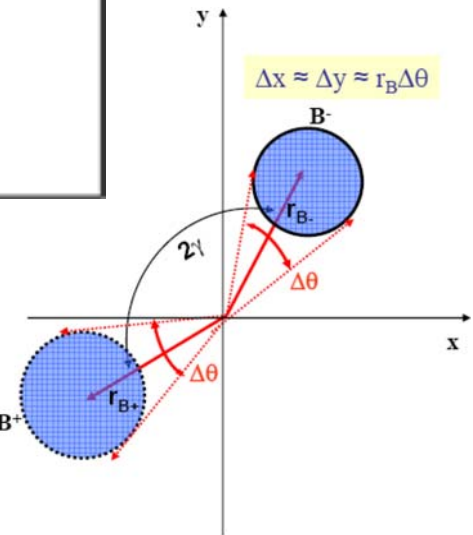
- Comparison BABAR/BELLE

- BELLE uncertainties are significantly smaller than BABAR ones
- despite the (x,y) observables have comparable errors
- this is the “ $r_B$ ” effect

$$\gamma = (76_{-23}^{+22} \pm 5 \pm 5)^\circ$$

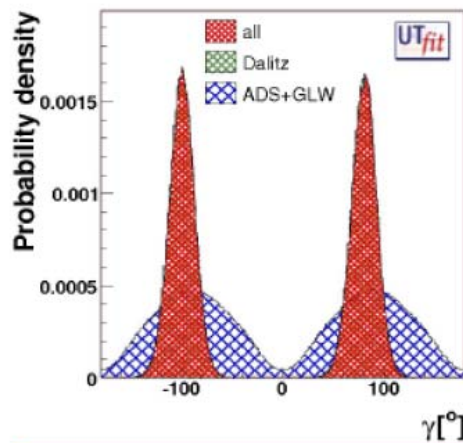
$$r_B(DK) = 0.086 \pm 0.035$$

$$r_B(D^*K) = 0.135 \pm 0.051_{B^+}$$

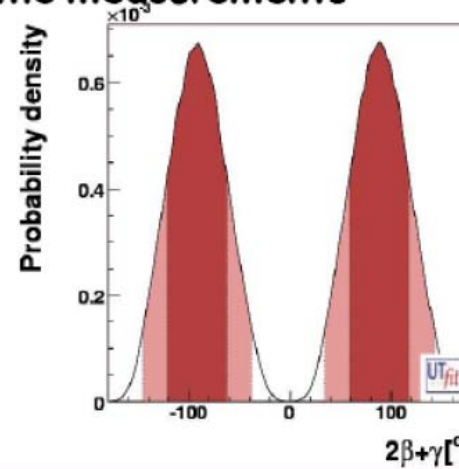


# Combined constraints on $\gamma$

Babar + Belle, from the combination of all the measurements

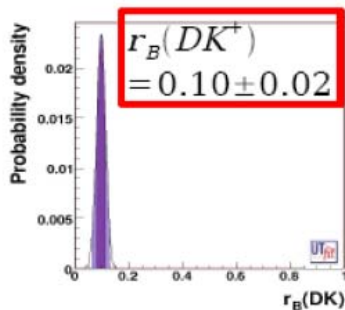


**WORLD AVERAGE  
(all new  
measurements  
here presented  
are included)**

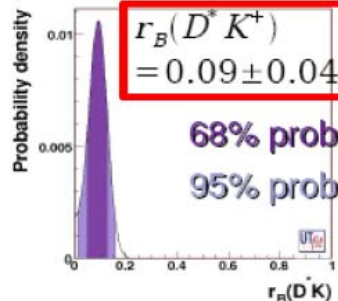


$$\gamma/\phi_3 = (80 \pm 13)^\circ \pmod{180^\circ}$$

$$2\beta + \gamma = (88 \pm 29)^\circ \pmod{180^\circ}$$

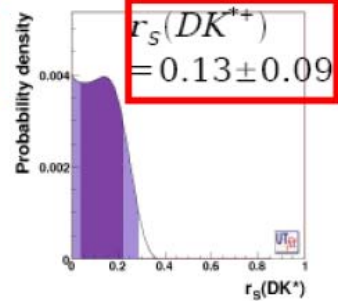


$$r_B(DK^+) = 0.10 \pm 0.02$$

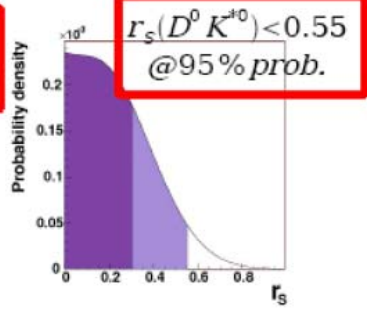


$$r_B(D^*K^+) = 0.09 \pm 0.04$$

68% prob  
95% prob



$$r_S(DK^{*+}) = 0.13 \pm 0.09$$



$$r_S(D^0 K^{*0}) < 0.55 \text{ @95\% prob.}$$



# Conclusion

- Remarkable success of B factories
  - succeeded beyond expectation, with eg, measurement of  $\gamma$
- BABAR has now finished its data taking
  - leaving BELLE alone in the “race”...
  - but still many analyses to do or update on the full data sample
- CKM UT is constrained by measurements based on both by CP conserving and CP violating
  - the picture is consistent with the SM !
- Measurement of semileptonic decays become more precise as the experimental techniques are improving and the theoretical computation of parameters.
- The measurement of  $\beta$  is a precision measurement, reaching accuracy of SM calculations
- The angle  $\alpha$  will ultimately be limited by penguin pollution
  - still more new channels being added
- The measurement of  $\gamma$  is reaching the  $13^\circ$  precision

# 2001... and now

