



# Review of **New** Strange Quark Results XXVII Physics In Collision Conference

**Kloe  
NA48  
KTeV  
ISRA+**

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**University of Virginia**

**June 27, 2008**

**64 years** after  
first observation  
In 1944 of a  
charged kaon in a  
cloud chamber by  
Le Prince-Ringuet,  
strange quark  
physics is still vital  
and going strong

- I. CP/CPT Violation**
- II. Lepton Flavor Violation/NP**
- III.  $e, \mu$  universality in  $K_{l3}, K_{l2}$**
- IV.  $V_{us}$**
- V. ChPT**
- VI. Quantum Coherence**
- VII. Cusp Measurements**

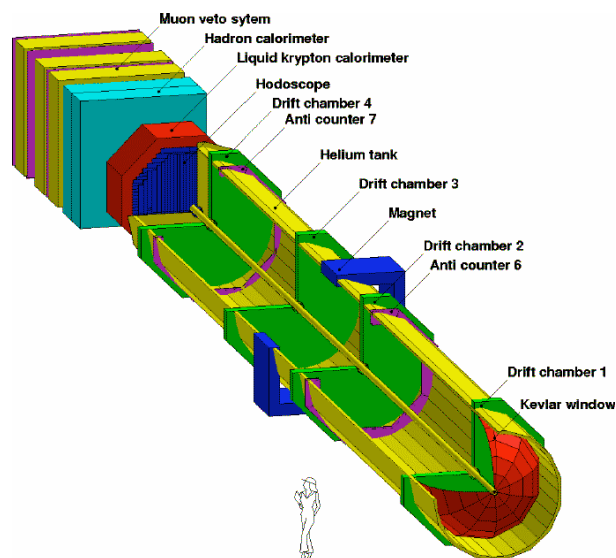
} Not covered for  
lack of time

**New Physics anywhere?**

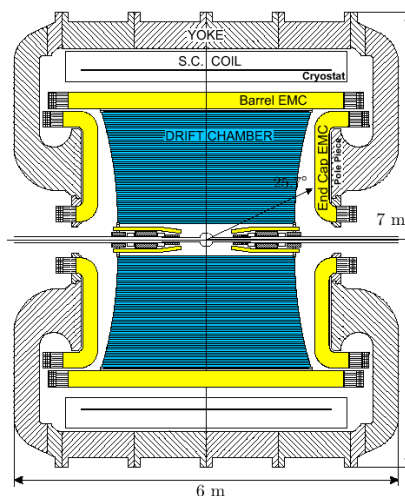


# Four Active Kaon Collaborations

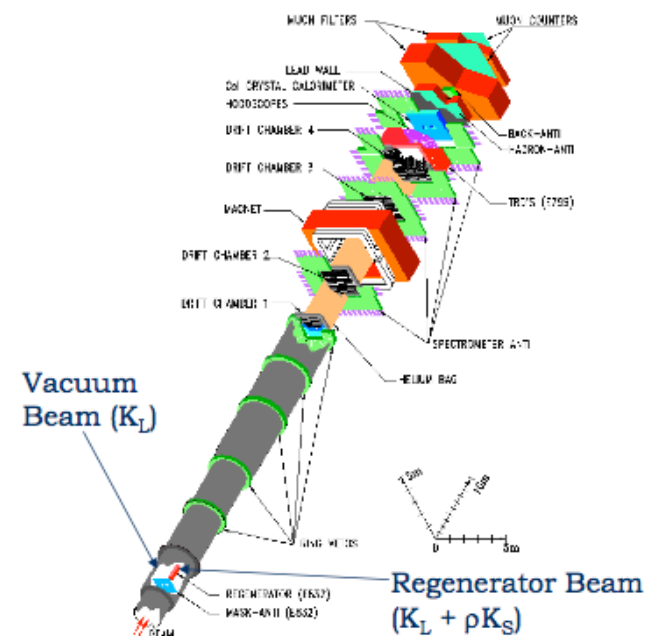
## Charged and Neutral Kaon Decays\*



**NA48/2**  
**Future NA62**



**KLOE**  
**Future KLOE II**



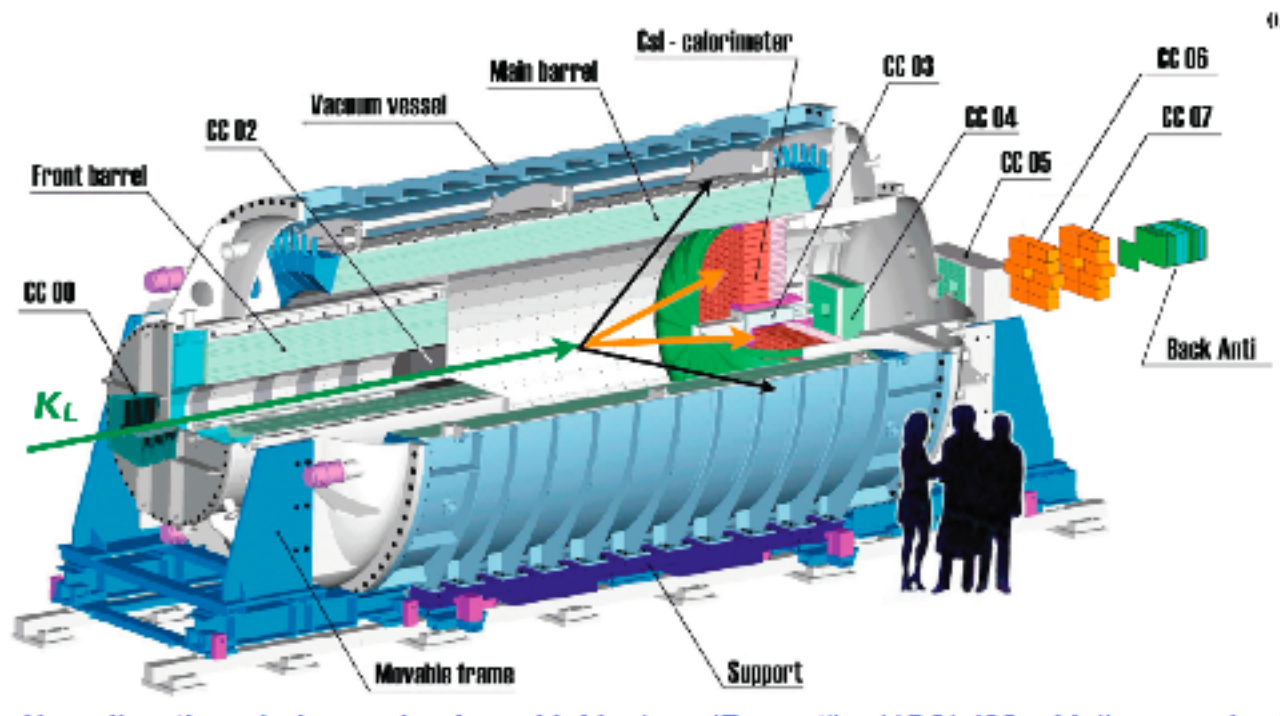
**KTeV**  
**Project x??**

\* Apologies to the Hyperon advocates



## KEK E391a

### First Dedicated $K_L \rightarrow \pi^0 \nu \nu$ Experiment



### Future E14 at J-PARC



# I. New Results on CP/CPT Violation (and associated parameters)

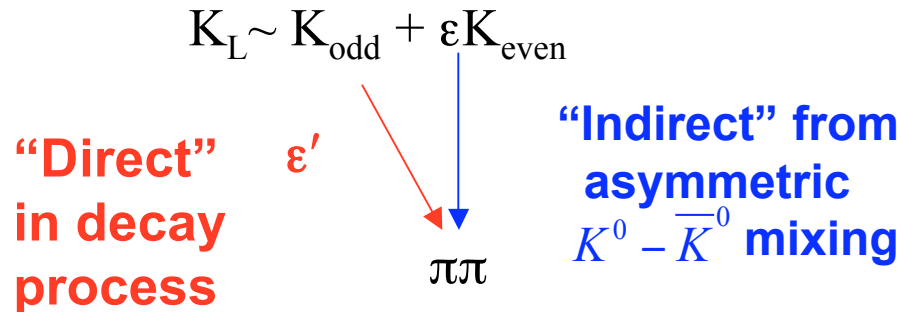
**KTeV: Epsilon Prime**

**E391a:  $K_L \rightarrow \pi^0 \nu \nu$**



## Final KTeV Measurement of $\varepsilon'/\varepsilon$ (1996, 1997 and 1999 Data Sets)

**KTeV**



To distinguish between direct and indirect CP violation, compare  $K_{L,S} \rightarrow \pi^+\pi^-, \pi^0\pi^0$ :

$$\text{Re}(\varepsilon'/\varepsilon) \approx \frac{1}{6} \left[ \frac{\Gamma(K_L \rightarrow \pi^+\pi^-)}{\Gamma(K_L \rightarrow \pi^0\pi^0)} \frac{\Gamma(K_S \rightarrow \pi^+\pi^-)}{\Gamma(K_S \rightarrow \pi^0\pi^0)} - 1 \right]$$

$\varepsilon'/\varepsilon \neq 0 \longrightarrow$  direct CP violation

$$K^0 \rightarrow \pi^+\pi^- \neq \bar{K}^0 \rightarrow \pi^+\pi^-$$



## Backgrounds and event yields

**KTeV**

Main classes of background:

- **Misidentified kaon decays**
- **For  $K \rightarrow \pi^+ \pi^-$ :  $K_L \rightarrow \pi e \nu$ ,  $K_L \rightarrow \pi \mu \nu$**
- **For  $K \rightarrow \pi^0 \pi^0$ :  $K_L \rightarrow \pi^0 \pi^0 \pi^0$**
- **Scattered  $K \rightarrow \pi \pi$  events**
- **From regenerator and final collimator**
- **Backgrounds are simulated with MC, normalized to data sidebands, and subtracted**
- **Background level is  $\sim 0.1\%$  for charged mode and  $\sim 1\%$  for neutral mode.**

After background subtraction:		
	$K_L$	“ $K_S$ ”
	Vacuum Beam	Reg. Beam
$K \rightarrow \pi^+ \pi^-$	25,107,242	43,674,208
$K \rightarrow \pi^0 \pi^0$	5,968,198	10,180,175



# Systematic Uncertainties in $\text{Re}(\epsilon'/\epsilon)$

**KTeV**

Source	Error on $\text{Re}(\epsilon'/\epsilon)$ ( $\times 10^{-4}$ )		
	$K \rightarrow \pi^+ \pi^-$	$K \rightarrow \pi^0 \pi^0$	
Trigger	0.23	0.20	—
Csl cluster reconstruction	—	0.75	→
Track reconstruction	0.22	—	
Selection efficiency	0.23	0.34	
Apertures	0.30	0.48	
Acceptance	0.57	0.48	
Backgrounds	0.20	1.07	
MC statistics	0.20	0.25	—
Total	0.81	1.55	—
Fitting	0.31		—
Total	1.78		—

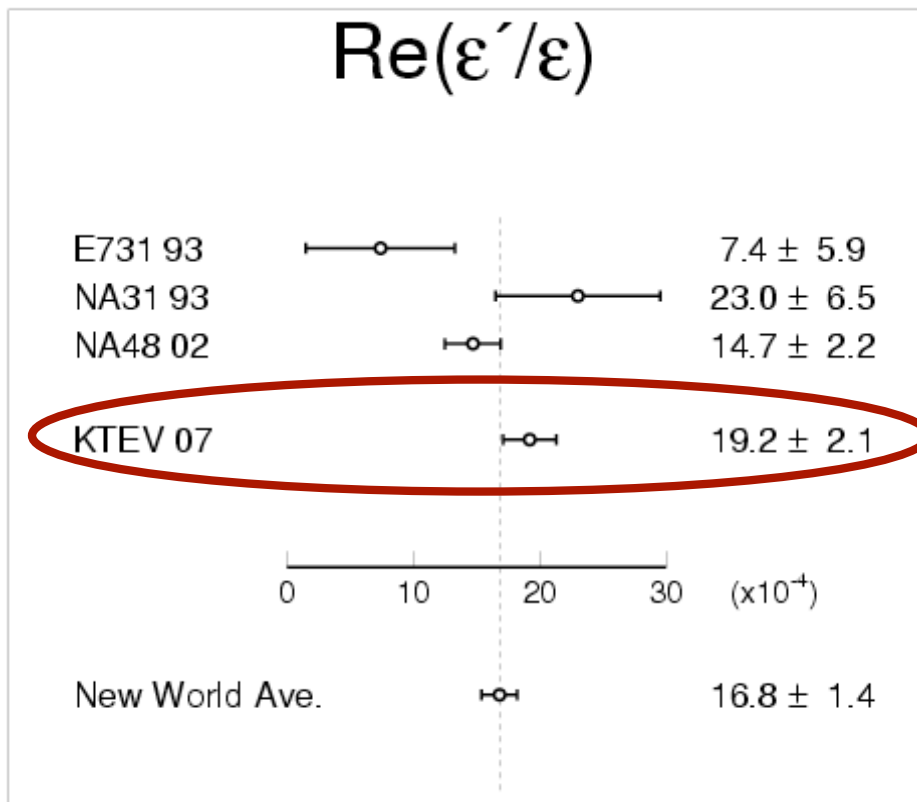
Reduced  
from 1.47



## New KTeV Result:

$$\begin{aligned}\text{Re}(\epsilon'/\epsilon) &= [19.2 \pm 1.1(\text{stat}) \pm 1.8(\text{syst})] \times 10^{-4} \\ &= (19.2 \pm 2.1) \times 10^{-4}\end{aligned}$$

**KTeV**



**World average:**

$$\begin{aligned}\text{Re}(\epsilon'/\epsilon) &= (16.8 \pm 1.4) \times 10^{-4} \\ &\text{(confidence level} = 13\%) \end{aligned}$$

$$(\text{KTeV 2003: } \text{Re}(\epsilon'/\epsilon) = [20.7 \pm 1.5(\text{stat}) \pm 2.4(\text{syst})] \times 10^{-4})$$

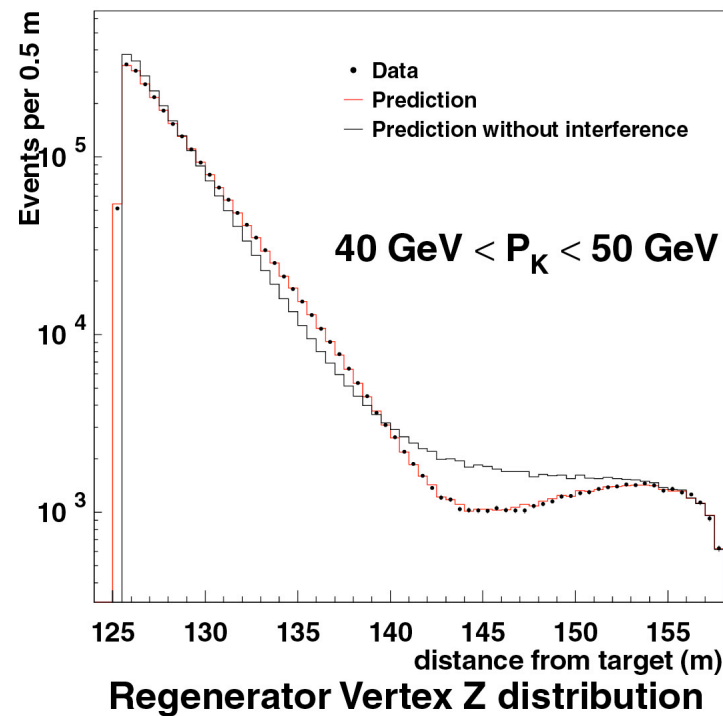
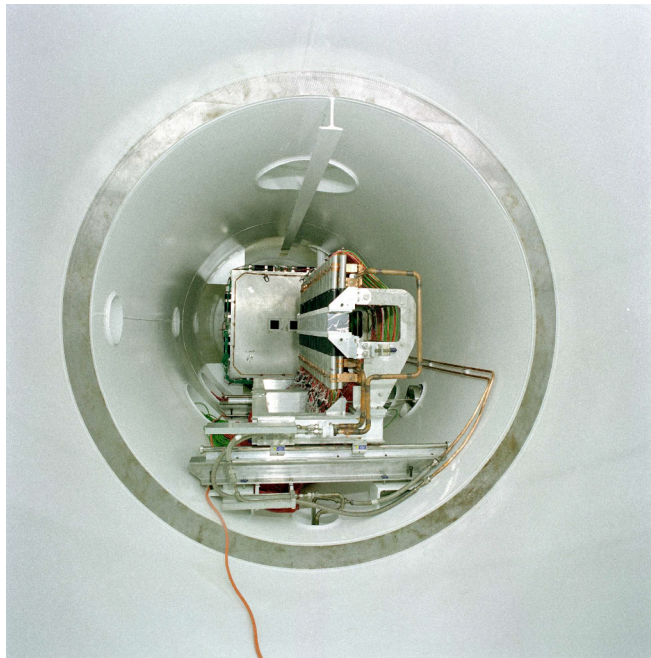




## Other Neutral Kaon Decay Parameters

**KTeV**

### $K_L - K_S$ Interference Downstream of Regenerator



$$R_{\pi\pi} \propto |\eta|^2 e^{-\Gamma_L t} + |\rho|^2 e^{-\Gamma_S t} + 2|\eta||\rho| e^{-(\Gamma_S + \Gamma_L)t/2} \cos(\Delta m t + \Phi_\rho - \Phi_\eta)$$



## Fitting Strategy for $\pi$ Decay Distribution

KTeV

- In contrast with  $\text{Re}(\epsilon'/\epsilon)$  fit, in which a single  $\sim 50$  m  $\pi$  bin is considered, the regenerator beam data is fitter in 2 m  $\pi$  bins.
- Float  $\Delta m = m_L - m_S$ ,  $\tau_S$ ,  $\phi_\epsilon$ ,  $\text{Re}(\epsilon'/\epsilon)$ ,  $\text{Im}(\epsilon'/\epsilon)$  with no CPT assumption.
- CPT constraint ( $\phi_\epsilon = \phi_{SW}$  and  $\text{Im}(\epsilon'/\epsilon) = 0$ ) then applied *a posteriori* to find best values  $\tau_S$ ,  $\Delta m$ .

$$\eta_{+-} = \frac{A(K_L \rightarrow \pi^+ \pi^-)}{A(K_S \rightarrow \pi^+ \pi^-)} = \epsilon + \epsilon'$$

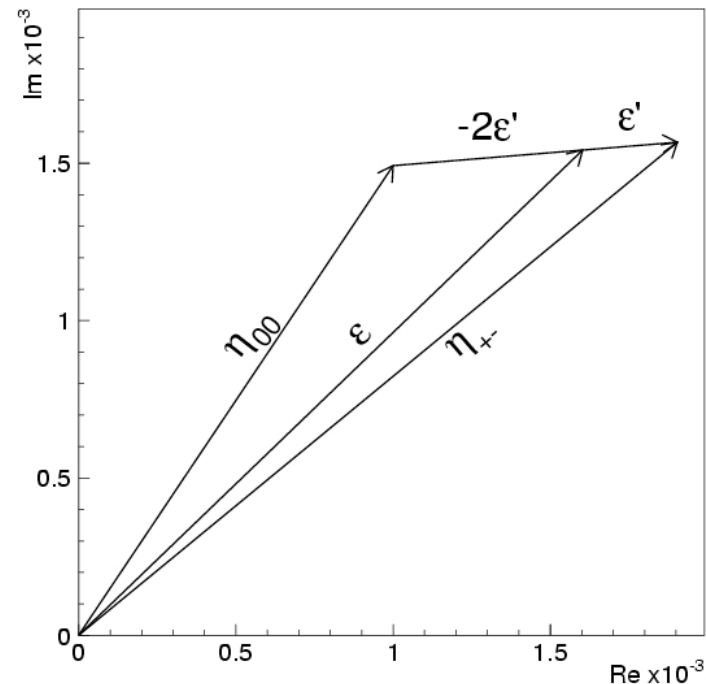
$$\eta_{00} = \frac{A(K_L \rightarrow \pi^0 \pi^0)}{A(K_S \rightarrow \pi^0 \pi^0)} = \epsilon - 2\epsilon'$$

$$\phi_{SW} = \tan^{-1} \left( \frac{2\Delta m}{\Delta \Gamma} \right)$$

$$\phi_{+-} \approx \phi_\epsilon + \text{Im}(\epsilon'/\epsilon)$$

$$\phi_{00} \approx \phi_\epsilon - 2 \text{Im}(\epsilon'/\epsilon)$$

$$\Delta \phi \equiv \phi_{00} - \phi_{+-} \approx -3 \text{Im}(\epsilon'/\epsilon)$$

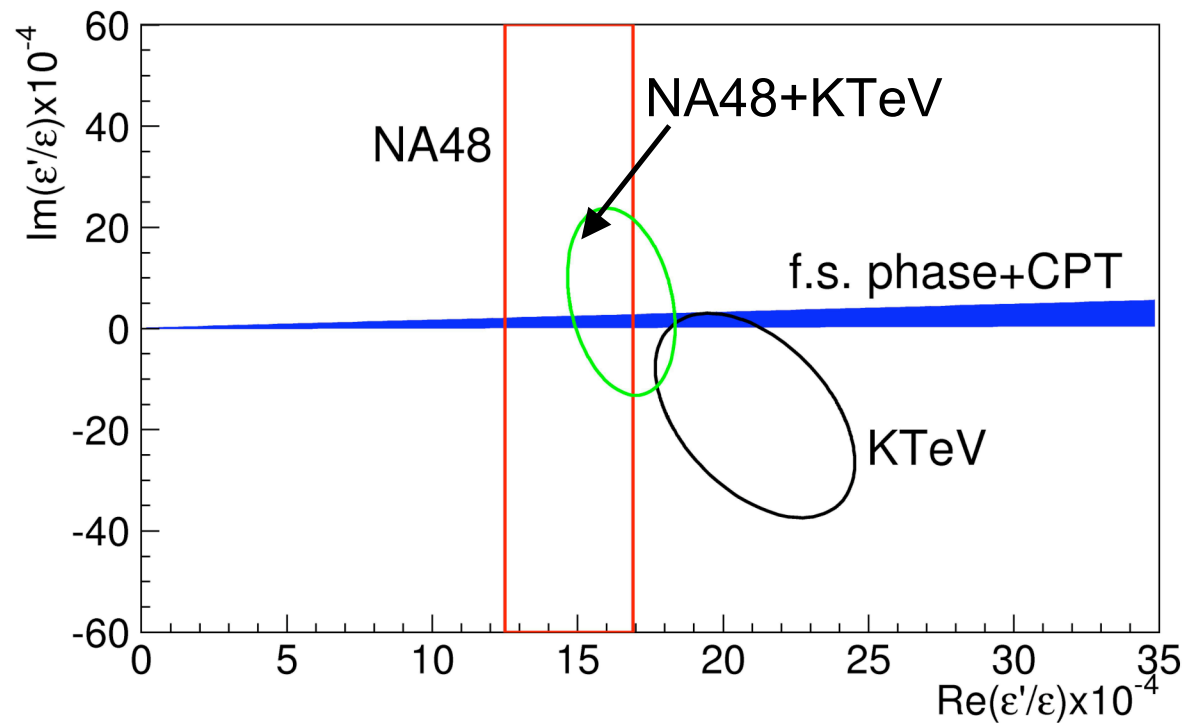




## Z Distribution Fit Results

**KTeV**

$$\begin{aligned}\phi_\varepsilon &= (43.86 \pm 0.63)^\circ \\ \phi_\varepsilon - \phi_{\text{SW}} &= (0.40 \pm 0.56)^\circ \\ \Delta\phi &= (0.30 \pm 0.35)^\circ\end{aligned}$$

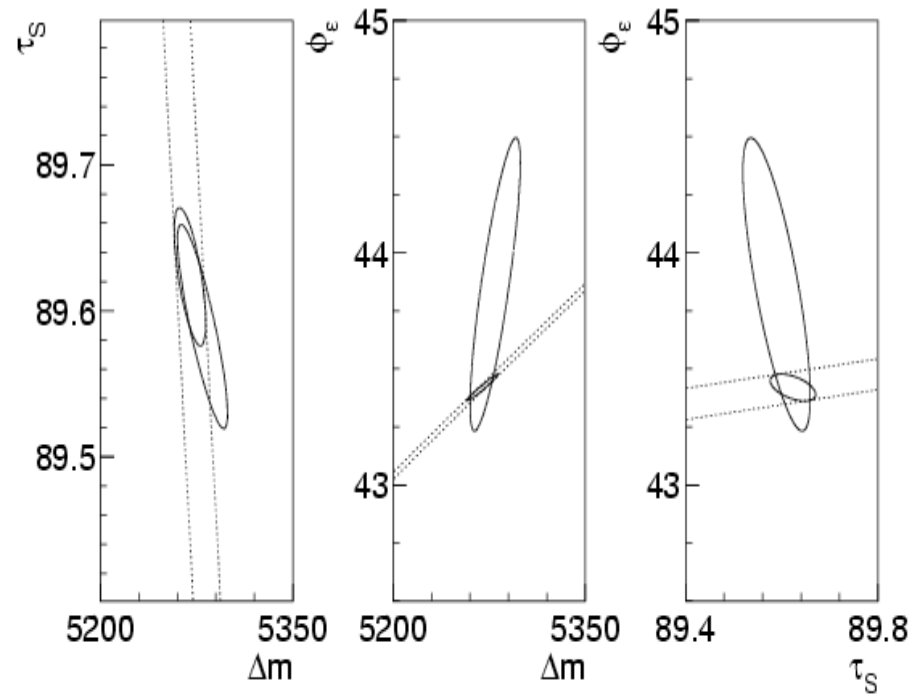


**All results consistent with CPT symmetry**



## Z Distribution Fit Results (cont)

KTeV



**No CPT constraint:**

$$\Delta m = (5279.7 \pm 19.5) \times 10^6 \hbar s^{-1}$$

$$\tau_S = (89.589 \pm 0.070) \times 10^{-12} \text{ s}$$

**CPT constraint applied:**

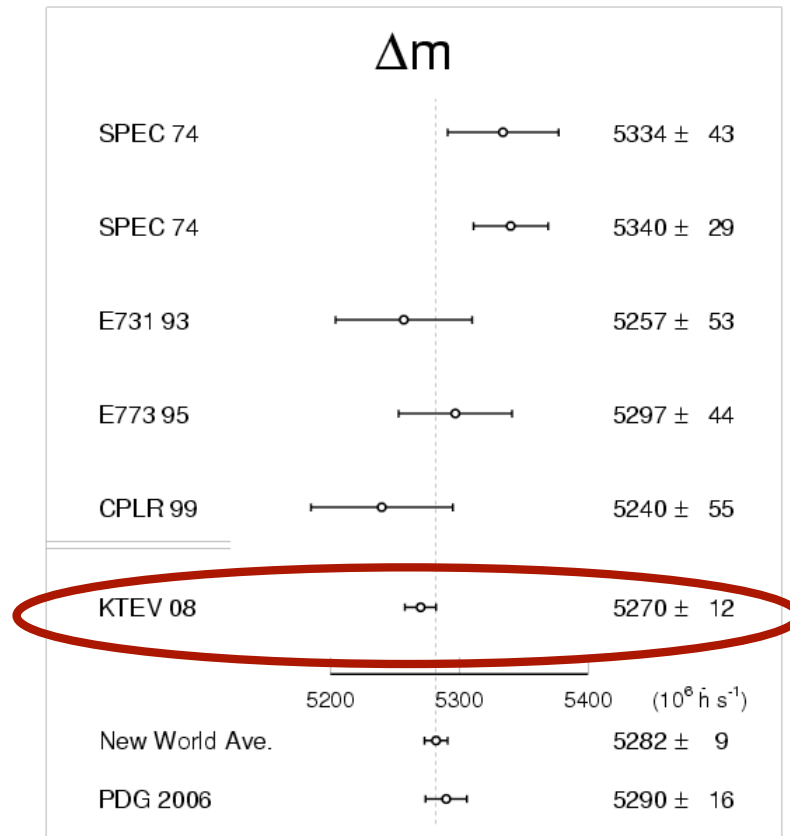
$$\Delta m = (5269.9 \pm 12.3) \times 10^6 \hbar s^{-1}$$

$$\tau_S = (89.623 \pm 0.047) \times 10^{-12} \text{ s}$$



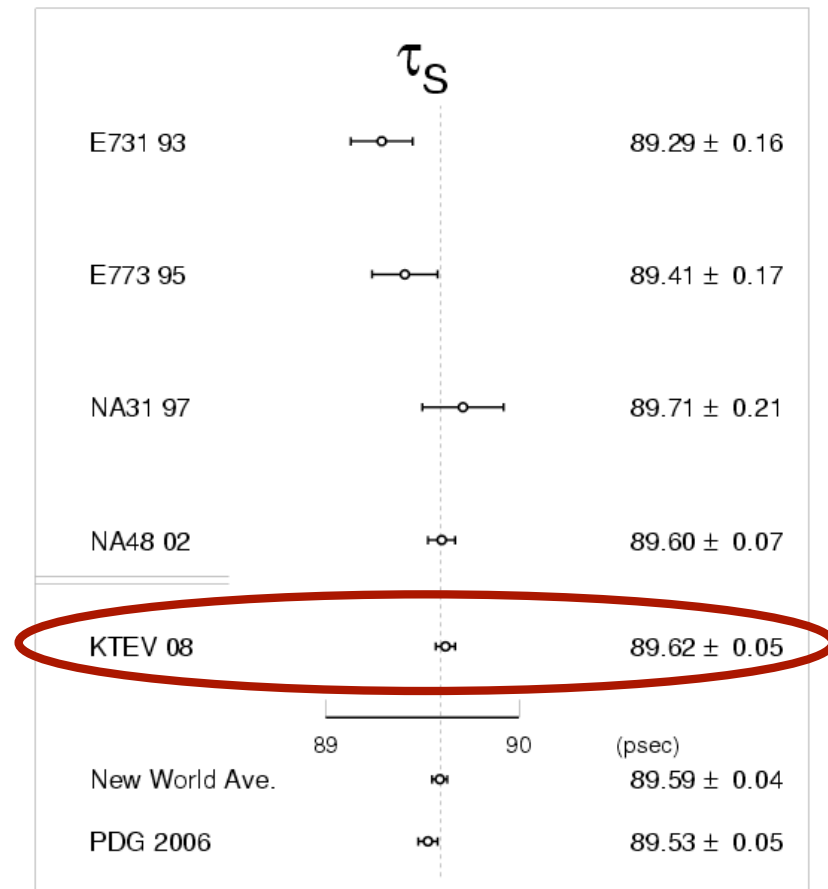
## $\Delta m$ and $\tau_S$

**KTeV**



KTeV 2003:  $\Delta m = (5261 \pm 13) \times 10^6 \hbar s^{-1}$

6/27/08



KTeV 2003:  $\tau_S = (89.65 \pm 0.07) \times 10^{-12} s$

B. Cux

13



## Summary of KTeV Results from Total Data (Preliminary)

KTeV

$$\frac{\text{Rate}(K^0 \rightarrow \pi^+\pi^-) - \text{Rate}(\bar{K}^0 \rightarrow \pi^+\pi^-)}{\text{Rate}(K^0 \rightarrow \pi^+\pi^-) + \text{Rate}(\bar{K}^0 \rightarrow \pi^+\pi^-)} = (5.5 \pm 0.5) \times 10^{-5}$$

- $\text{Re}(\epsilon'/\epsilon) = (19.2 \pm 2.1) \times 10^{-4}$
  - $\Delta m = (5269.9 \pm 12.3) \times 10^6 \hbar\text{s}^{-1}$
  - $\tau_S = (89.623 \pm 0.047) \times 10^{-12} \text{ s}$
  - $\phi_\epsilon = (43.86 \pm 0.63)^\circ$
  - $\phi_\epsilon - \phi_{\text{SW}} = (0.40 \pm 0.56)^\circ$
  - $\Delta\phi = (0.30 \pm 0.35)^\circ$
- } Assuming CPT
- } No CPT assumption

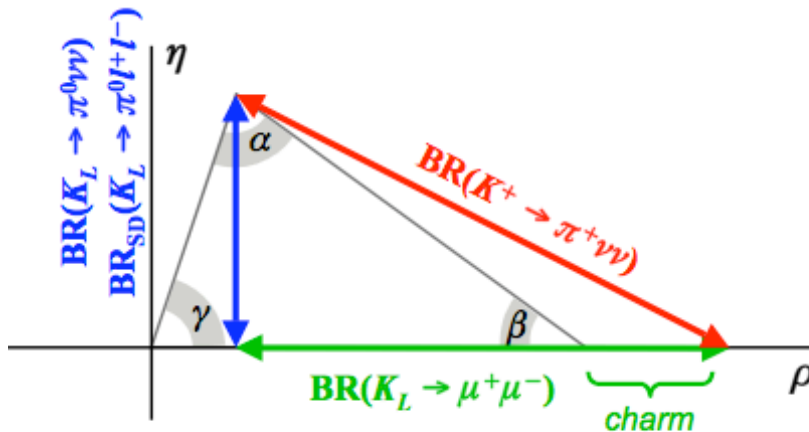
Phases  $\phi_{+-}$ ,  $\phi_{00}$  dominate uncertainty in unitarity fit in PDG  
Future lattice calculations may allow precise tests of the SMI.  
All measurements consistent with CPT symmetry



# Importance of $K_L \rightarrow \pi^0 \nu \nu$

E391a

One of a number of **Golden Decays**  
Measures  $\eta$  (height of CKM Triangle) directly



	$\Gamma_{SD}/\Gamma$	Irreducible theory err. (amp)	SM BR
$K_L \rightarrow \pi^0 \nu \nu$	>99%	1%	$3 \times 10^{-11}$
$K^+ \rightarrow \pi^+ \nu \nu$	88%	3%	$8 \times 10^{-11}$
$K_L \rightarrow \pi^0 e^+ e^-$	38%	15%	$3.5 \times 10^{-11}$
$K_L \rightarrow \pi^0 \mu^+ \mu^-$	28%	30%	$1.5 \times 10^{-11}$

FCNC processes  
dominated by Z-penguin  
and box diagrams

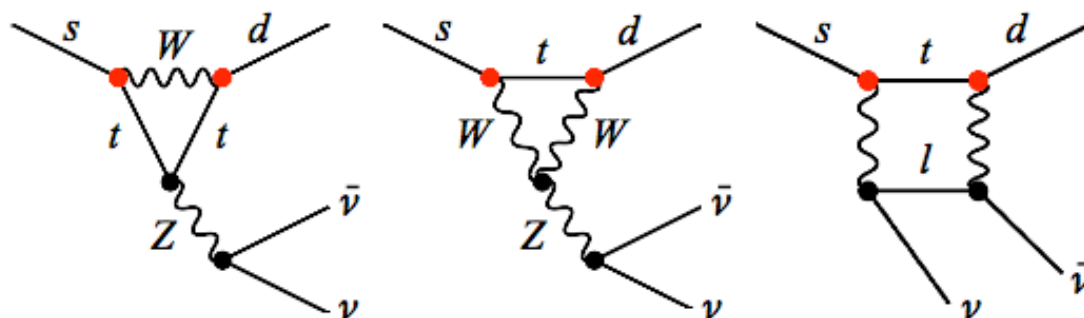
Give direct information on  
CKM matrix elements:

- No LD contributions from processes with intermediate  $\gamma$ s
- Hadronic matrix elements can be obtained from BRs for leading  $K$  decays
- $K_L \rightarrow \pi^0 \nu \nu$  is nearly pure direct CP violating



# Theoretical Framework for $K_L \rightarrow \pi^0 \nu \bar{\nu}$

E391a



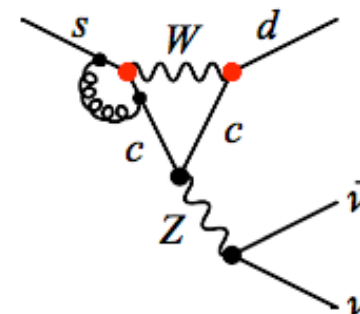
$$\begin{aligned}\lambda &= V_{us} \\ \lambda_c &= V_{cs}^* V_{cd} \\ \lambda_t &= V_{ts}^* V_{td}\end{aligned}$$

$$x_q \equiv m_q^2/m_W^2$$

Loop functions favor top contribution

$$\begin{aligned}\text{BR}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) &= \kappa_+ \left[ \left( \frac{\text{Im } \lambda_t}{\lambda^5} X(x_t) \right)^2 + \left( \frac{\text{Re } \lambda_t}{\lambda^5} X(x_t) + \frac{\text{Re } \lambda_c}{\lambda} P_c(X) \right)^2 \right] \\ \text{BR}(K_L \rightarrow \pi^0 \nu \bar{\nu}) &= \kappa_L \left( \frac{\text{Im } \lambda_t}{\lambda^5} X(x_t) \right)^2 \leftarrow \mathcal{CP}\end{aligned}$$

QCD corrections for charm diagrams contribute to uncertainty



Hadronic matrix element obtained from  $\text{BR}(K_{e3})$  via isospin rotation

$$\kappa_+ = r_{K^+} + \frac{3\alpha^2 \text{BR}(K^- \rightarrow \pi^0 e^+ \nu)}{2\pi^2 \sin^4 \theta_W} \lambda^8$$





# $K_L \rightarrow \pi^0 \nu \nu$ searches

**E391a  
KTEV**

## Essential signature: “ $2\gamma$ + nothing”

All other decays have 2 extra  $\gamma$  or 2 tracks except  $K_L \rightarrow \gamma\gamma$   
(not a big problem since  $p_{\perp} = 0$ ,  $\phi_{12} = 180^\circ$ )

## Main backgrounds:

$K_L \rightarrow \pi^0 \pi^0$  with 2 lost  $\gamma$   $\rightarrow$  Hermetic veto, including beam exit

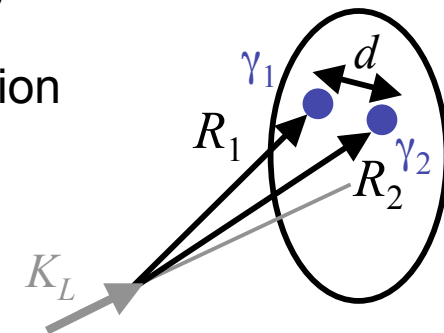
$n + \text{gas} \rightarrow X\pi^0, X\eta$   $\rightarrow$  High vacuum decay region

$M(\gamma\gamma) = m_{\pi^0}$  is the only sharp kinematic constraint

Generally used to reconstruct vertex position

Additional topological constraints advantageous:

- Small beam cross section
- Measurement of photon directions
- Microbunched beam for TOF constraints



$$m_{\pi^0}^2 = 2E_1 E_2 (1 - \cos \theta)$$

$$R_1 \approx R_2 \equiv R = \frac{d\sqrt{E_1 E_2}}{m_{\pi^0}}$$

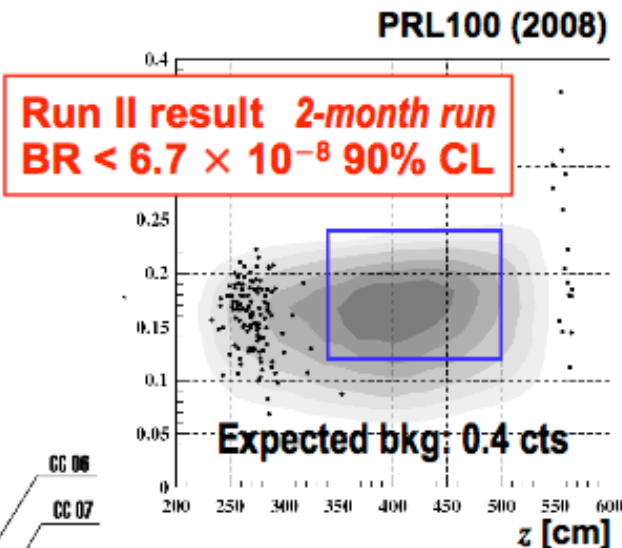
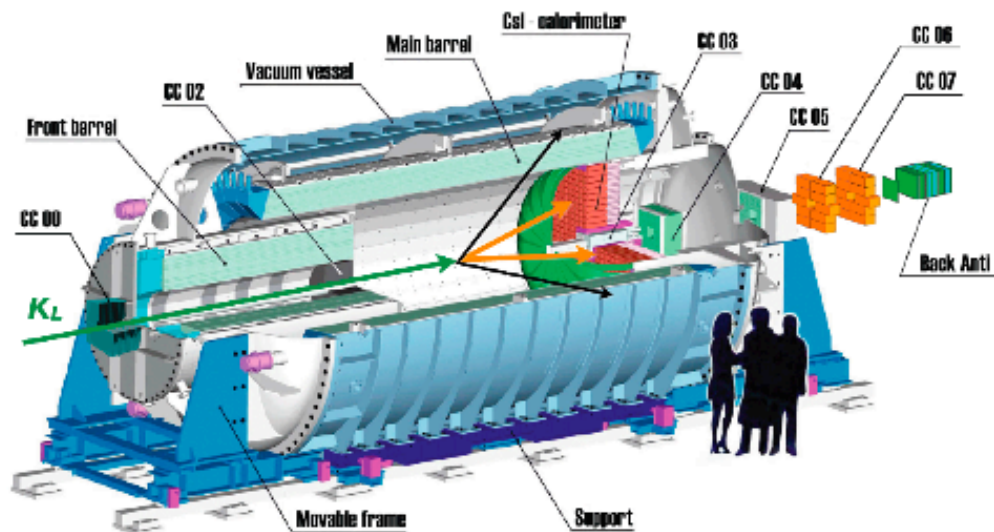
**Veto system performance & experiment design are paramount**



# KEK 391a New Result for $BR(K_L \rightarrow \pi^0 \nu \nu)$

**E391a**

Neutral secondary beam from KEK PS  
Pb and Be filters to screen  $\gamma, n$   
Peak  $K_L$  momentum 2 GeV at detector  
Collimated to "pencil beam"  
Geometric constraint for  $\pi^0$  vertexing  
Halo suppressed to  $10^{-4}$  at  $r = 4$  cm



**Forward photon veto**  
Pure CsI crystals  
 $7 \times 7 \times 30 \text{ cm}^3$

**Vacuum decay volume**  
 $10^{-7}$  mbar



## Summary of All Results for upper limits for $\text{BR}(K_L \rightarrow \pi^0 \nu \nu)$

**E391a**

$$\text{E391}^* < 6.7 \times 10^{-8}$$

$$\text{KTeV}^{**} < 5.9 \times 10^{-7}$$

$$\text{KTeV} < 1.6 \times 10^{-6}$$

### SM Prediction

Mescia, Smith '07

Update at <http://www.lnf.infn.it/wg/vus>

$$\text{BR}(K_L \rightarrow \pi^0 \nu \nu) = 2.76 \pm 0.40 \times 10^{-11}$$

- \* Will be upgraded by addition of CsI from KTeV and moved to J-Parc as E-14
- \*\* Required a Dalitz pair from one of the  $\pi^0$  photons



## II. Lepton Flavor Violation/NP

**KTeV:  $K_L \rightarrow \pi^0 \mu e$**   
 **$K_L \rightarrow \pi^0 \pi^0 \mu e$**   
 **$\pi^0 \rightarrow \mu e$**

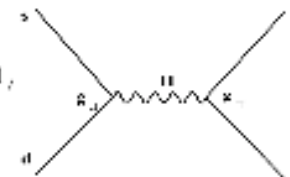


## Lepton Flavor Violation in K Decays In KTeV

KTeV

**Searches motivation: tests for tree-level LFV amplitudes possible in Technicolor, SUSY, ...**

**E.g., horizontal bosons in extended TC:**  $M_H \approx 85 \text{ TeV} \left[ \frac{10^{-11}}{B(K^+ \rightarrow \pi^+ \mu^+ e)} \right]^{1/2}$



- Look for two charged tracks in detector:
  - One muon
    - Track must match hits in the muon hodoscopes
  - One electron
    - Track momentum = cluster energy in CsI
    - TRD info is consistent with an electron
- Allows searches for:
  - $K_L \rightarrow \pi^0 \mu e$
  - $K_L \rightarrow \pi^0 \pi^0 \mu e$
  - $\pi^0 \rightarrow \mu e$



**LFV:  $K_L \rightarrow \pi^0 \mu e$**

**KTeV**

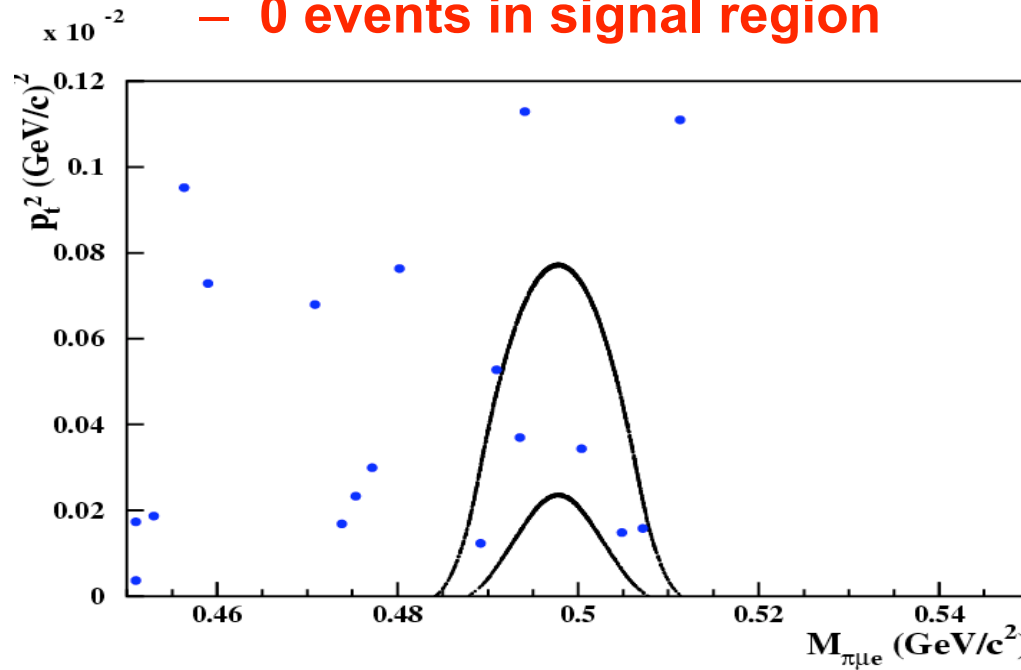
- **Highest background out of our trio of LFV decays**
  - **Ke3/Ke4 +  $\pi$  decay or  $\pi$  punch through to muon hodoscopes = fake signal**
    - **Make tight cut on accidental activity in detector**
    - **Apply cut on calculated  $|p_\nu|$  assuming Ke4 decay**
      - **Real Ke4 events produce positive values**
      - **Other events produce negative ( non-physical ) values**
- **Sum of MC background estimates:**
  - 4.21 +/- 0.53 in control region**
    - **contains 99% of signal**
  - 0.66 +/- 0.23 in signal region**
    - **contains 95% of signal**



## LFV: $K_L \rightarrow \pi^0 \mu e$

KTeV

- 1997 plus 1999 Data after all cuts:
  - 5 events in control region
  - 0 events in signal region



Resulting limit:  $\text{Br}(K_L \rightarrow \pi^0 \mu e) < 7.56 \times 10^{-11}$  (90% C.L.)

Factor of 83 lower than previous limit



**LFV:  $K_L \rightarrow \pi^0 \pi^0 \mu e$**

**KTeV**

- **Extend  $K_L \rightarrow \pi^0 \mu e$  search**
- **Attempt to reconstruct 2<sup>nd</sup>  $\pi^0$** 
  - **Slashes backgrounds**
  - **Offset by relaxing cuts to improve sensitivity**
    - **Remove tight cuts on accidental activity**
    - **Remove cuts on TRD information for electron track**
- **Largest background from  $K_L \rightarrow \pi^0 \pi^0 \pi^0$** 
  - **Need a bad electron cluster in Csl combined with an accidental muon in the muon hodoscope**
  - **Apply VERY loose TRD cut on muon track**





## LFV: $K_L \rightarrow \pi^0 \pi^0 \mu e$

KTeV

- Expect 0.44 +/- 0.23 events in signal region
- Observe no events in signal region
- Resulting limit:  $Br(K_L \rightarrow \pi^0 \pi^0 \mu e) < 1.7 \times 10^{-10}$  (90% CL)
  - First reported limit on this decay mode

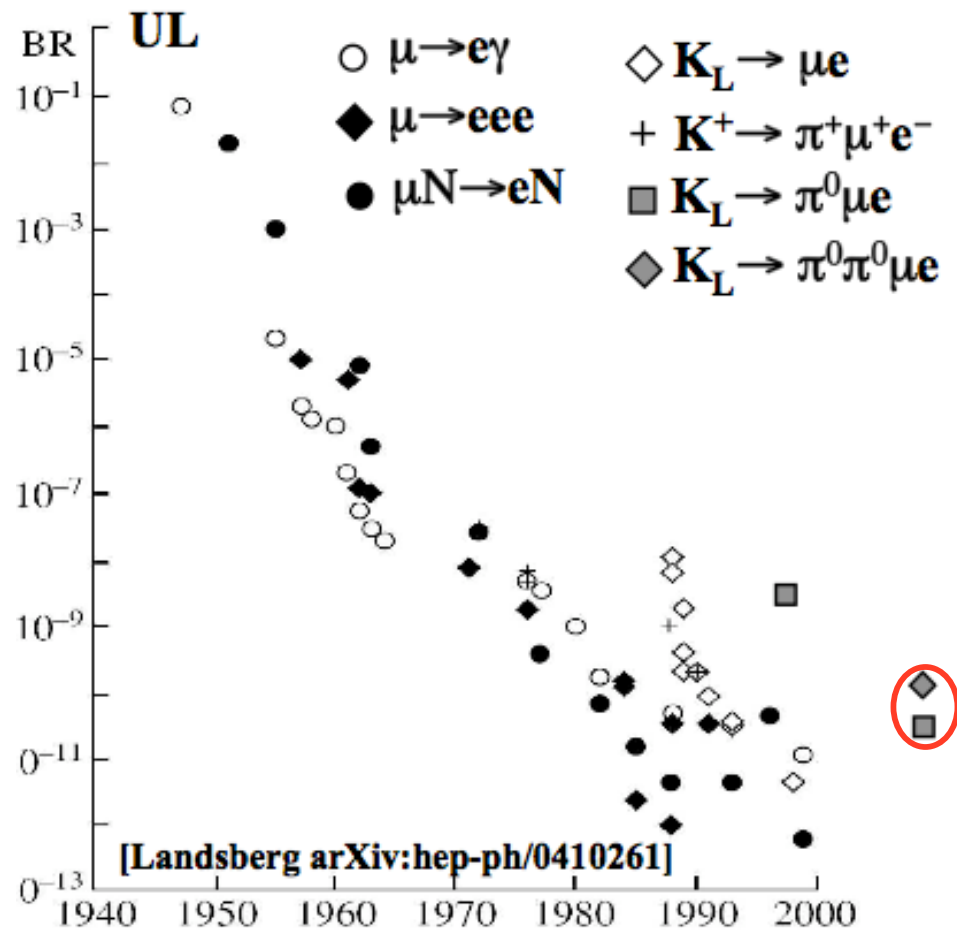
## LFV: $\pi^0 \rightarrow \mu e$

- Analysis can be extended by placing an extra constraint:
  - $M_{\mu e}$  reconstructs near  $M_{\pi^0}$
- Resulting limit:  $Br(\pi^0 \rightarrow \mu e) < 3.59 \times 10^{-10}$  (90% CL)
- Limit 10x(2x) lower than previous best limit on  $\pi^0 \rightarrow \mu^- e^+ (\mu^+ e^-)$
- Equally sensitive to both charge modes



# Lepton Flavor Violation Summary

KTeV





### III. NP and Lepton Flavor Universality

**KLOE**  
**NA48**  
**KTeV**  
**ISRA+**



## NP and Lepton Universality in K Decays

KLOE  
NA48  
KTeV  
ISR+

In SM, electron and muon differs only by mass and coupling to Higgs

Can measure ratio of coupling constants, seeking deviations from prediction in processes well determined in SM, like:

$$R_{e\mu} = \Gamma(K_{e3})/\Gamma(K_{\mu3}) \rightarrow G_F^e/G_F^\mu,$$

Test of lepton universality for weak vector currents

$$R_{K\pi} = \Gamma(K \rightarrow \mu\nu)/\Gamma(\pi \rightarrow \mu\nu),$$

Test for  $H^+$  exchange (scalar) or presence of right-handed currents

$$R_K = \Gamma(K \rightarrow e\nu)/\Gamma(K \rightarrow \mu\nu)$$

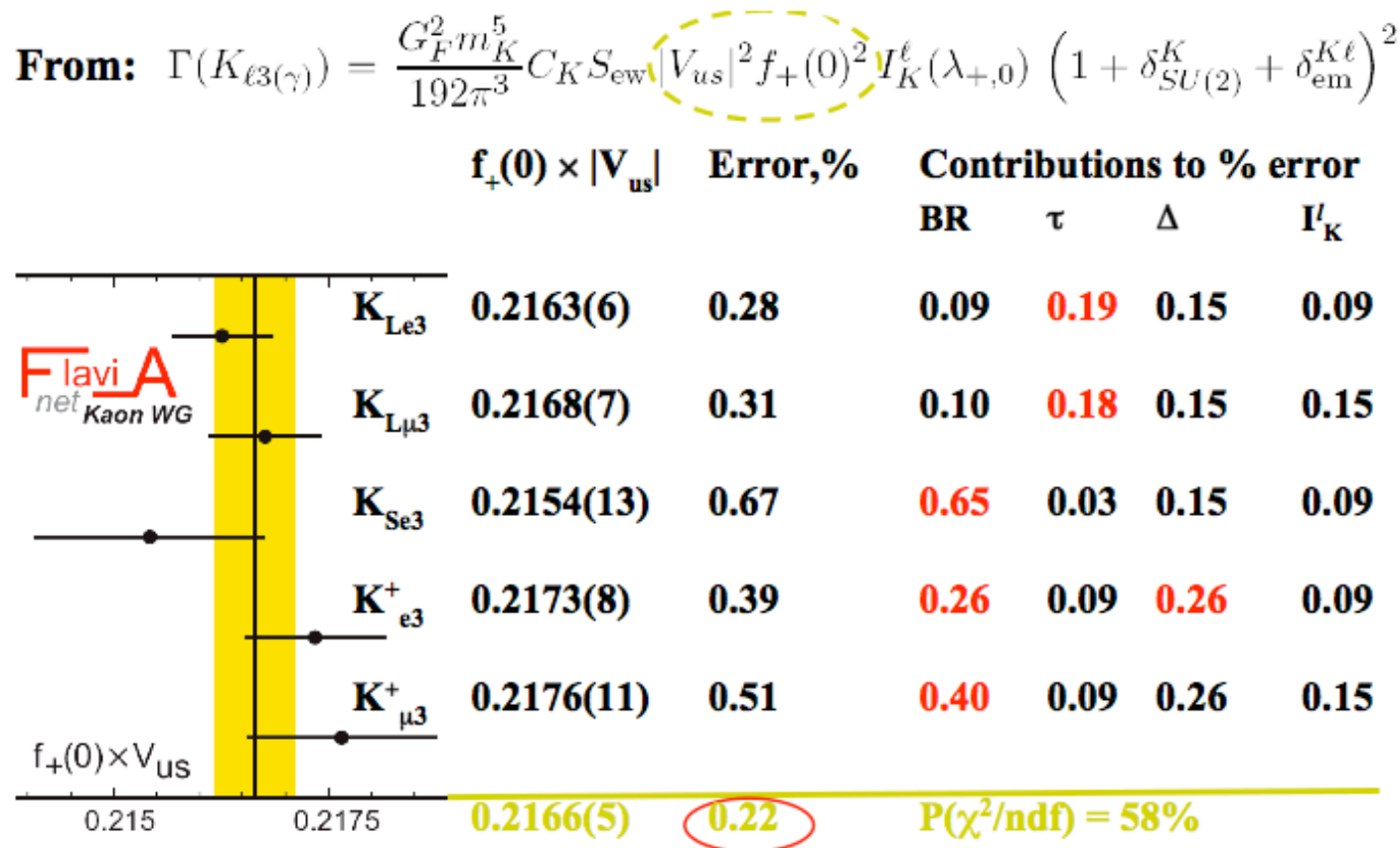
Test for LFV due to effective pseudoscalar weak currents



# NP from $K_{l3}$ Branching Ratios

KLOE  
NA48  
KTeV  
ISTRA+

World data for  $K_{l3}$  BR are in good shape due to Kloe, NA48, KTeV and ISTRA+





## NP Results in $R_{e\mu}$ from $K_{l3}$

KLOE  
NA48  
KTeV  
ISR+

$$\frac{\Gamma_{\mu 3}}{\Gamma_{e 3}} \cdot \frac{I_{e 3} (1 + \delta_{e 3})}{I_{\mu 3} (1 + \delta_{\mu 3})} = \frac{[|V_{us}| f_+(0)]_{\mu 3, \text{obs}}^2}{[|V_{us}| f_+(0)]_{e 3, \text{obs}}^2} = \frac{g_{\mu}^2}{g_e^2}$$

**Result:  $e/\mu$  universality satisfied:**

$K_L$	$g_{\mu}^2/g_e^2 = 1.0049(61)$	cfr with $g_{\mu}^2/g_e^2 = 1.054(15)$ [PDG04]
$K^+$	$g_{\mu}^2/g_e^2 = 1.0029(86)$	cfr with $g_{\mu}^2/g_e^2 = 1.019(13)$ [PDG04]
<b>Avg</b>	$g_{\mu}^2/g_e^2 = 1.0043(52)$	

**Compare with test sharing the same theoretical scenario,  $\tau \rightarrow l\nu\nu$  decays:**

$$\tau \rightarrow l\nu\nu \quad g_{\mu}^2/g_e^2 = 0.9998(40) \text{ [PDG07]}$$

**Precision from K's comparable with that from  $\tau$ 's**



## NP effects in $K_{l2}$ vs $\pi_{l2}$ Decays

**KLOE**

**In two Higgs doublet models (MSSM, too), exchange of  $H^+$  provides an additional scalar current, which might contribute sizeably wrt to SM:**

$$\frac{\Gamma(\mathbf{K} \rightarrow \ell \nu)}{\Gamma_{SM}(\mathbf{K} \rightarrow \ell \nu)} \cong \left| 1 - \frac{m_{K^+}^2}{M_{H^+}^2} \left( 1 - \frac{m_d}{m_s} \right) \frac{\tan^2 \beta}{1 + \epsilon_0 \tan \beta} \right| \quad [\text{Hou PRD48 (1992) 2342, Isidori-Paradisi}]$$

**NP effect is suppressed for  $\pi_{l2}$  wrt  $K_{l2}$ , so NP might appear in  $K_{l2} / \pi_{l2}$ , predicted in the SM to be:**

$$\frac{\Gamma(K_{\ell 2}^{\pm}(\gamma))}{\Gamma(\pi_{\ell 2}^{\pm}(\gamma))} = \left| \frac{V_{us}}{V_{ud}} \right|^2 \frac{f_K^2 m_K}{f_\pi^2 m_\pi} \left( \frac{1 - m_\ell^2/m_K^2}{1 - m_\ell^2/m_\pi^2} \right)^2 \times (1 + \delta_{em})$$

**NP test from comparing  $V_{us}/V_{ud}$  from  $M \rightarrow \ell \nu$  with  $V_{us}(K_{l3})/V_{ud}(0^+ \rightarrow 0^+)$ :**

$$\left| \frac{V_{us}(K_{\ell 2})}{V_{us}(K_{\ell 3})} \times \frac{V_{ud}(0^+ \rightarrow 0^+)}{V_{ud}(\pi_{\ell 2})} \right| \stackrel{?}{=} \left| 1 - \frac{m_{K^+}^2}{M_{H^+}^2} \left( 1 - \frac{m_d}{m_s} \right) \frac{\tan^2 \beta}{1 + \epsilon_0 \tan \beta} \right|$$

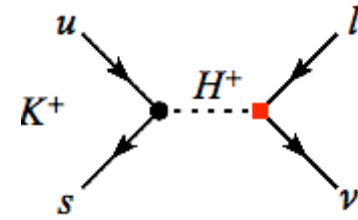


## NP Results for $R_{K\pi} = \Gamma(K \rightarrow \mu\nu)/\Gamma(\pi \rightarrow \mu\nu)$

**KLOE**

**Result is:**

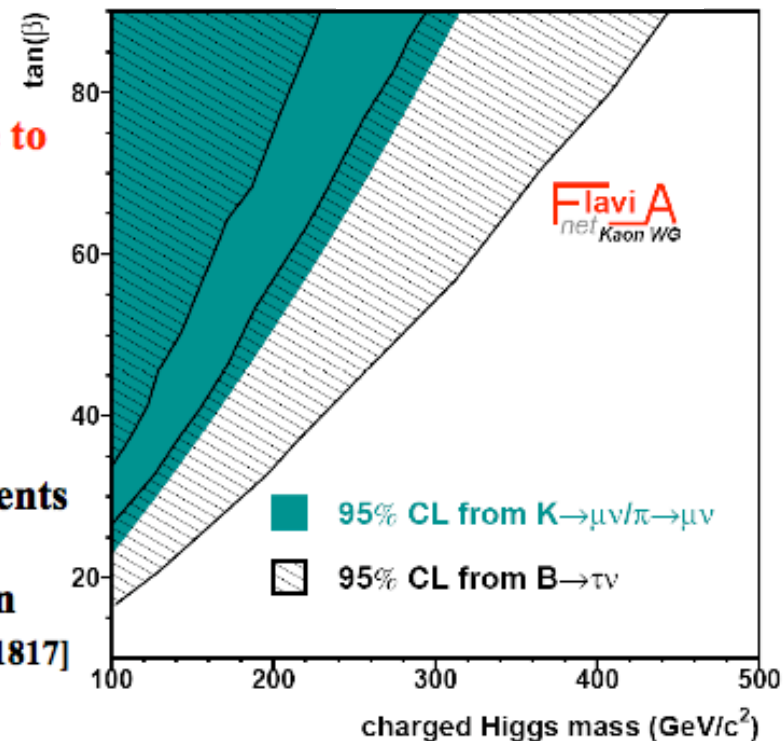
$$\left| \frac{V_{us}(K_{\ell 2})}{V_{us}(K_{\ell 3})} \times \frac{V_{ud}(0^+ \rightarrow 0^+)}{V_{ud}(\pi_{\ell 2})} \right| = 1.0018(57)$$



**NP sensitivity from  $K \rightarrow \mu\nu$  comparable to that from  $\text{BR}(B \rightarrow \tau\nu) = 1.42(44) \times 10^{-4}$  [Babar-Belle average]**

**Error dominated by theoretical uncertainties in form factors**

**NP induced by weak right-handed currents can be also tested (there, complement lattice information with Callan-Treiman scalar ff constraint) [FlaviaNet arXiv:0801.1817]**







**NP in  $R_K = \Gamma(Ke2)/\Gamma(K\mu2)$**

**KLOE  
NA48  
NA62**

**SM prediction w 0.04% precision, benefits of cancellation of hadronic uncertainties (no  $f_K$ ):  $R_K = 2.477(1) \times 10^{-5}$  [Cirigliano Rosell arXiv:0707:4464]**

**Helicity suppression can boost NP [Masiero-Paradisi-Petronzio PRD74 (2006) 011701]**

**In R-parity MSSM, LFV can give 1% deviations from SM:**

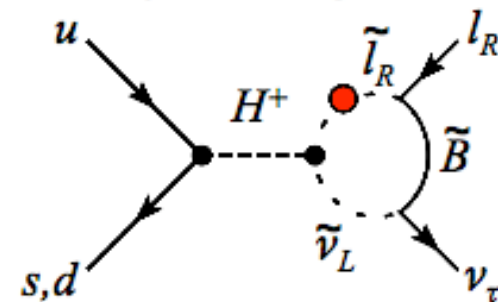
$$R_K^{LFV} \simeq R_K^{SM} \left[ 1 + \left( \frac{m_K^4}{M_H^4} \right) \left( \frac{m_\tau^2}{m_e^2} \right) |\Delta_R^{31}|^2 \tan^6 \beta \right]$$

**NP dominated by contribution of  $e\nu_\tau$  final state, with effective coupling**

$$lH^\pm \nu_\tau \rightarrow \frac{g_2}{\sqrt{2}} \frac{m_\tau}{M_W} \Delta_{13}, \text{ from loop } R\text{-parity violating MSSM}$$

**Present exp. accuracy on  $R_K$  @ 6%**

**New measurement of  $R_K$  can be very interesting, if error is pushed @1% or better**





## NP Results for $R_K = \Gamma(K \rightarrow e\nu)/\Gamma(K \rightarrow \mu\nu)$

Kloe  
NA48  
NA62

### KLOE

- preliminary result with 2001—5 data:  $R_K = 2.55 (5)_{\text{stat}} (5)_{\text{syst}} 10^{-5}$ , from  $\sim 8000$  Ke2 candidates (3% accuracy), perspectives to reach 1% error after analysis completion

### NA48/2

- preliminary result with 2003 data:  $R_K = 2.416 (43)_{\text{stat}} (24)_{\text{syst}} 10^{-5}$ , from  $\sim 4000$  Ke2 candidates, statistical error dominating (2% accuracy)
- preliminary result with 2004 data:  $R_K = 2.455 (45)_{\text{stat}} (41)_{\text{syst}} 10^{-5}$ , from  $\sim 4000$  Ke2 candidates from special minimum bias run (3% accuracy)

### NA62 (ex NA48)

- collected  $\sim 100,000$  Ke2 events in dedicated 2007 run, aims at breaking the 1% precision wall, possibly reaching  $< \sim 0.5\%$

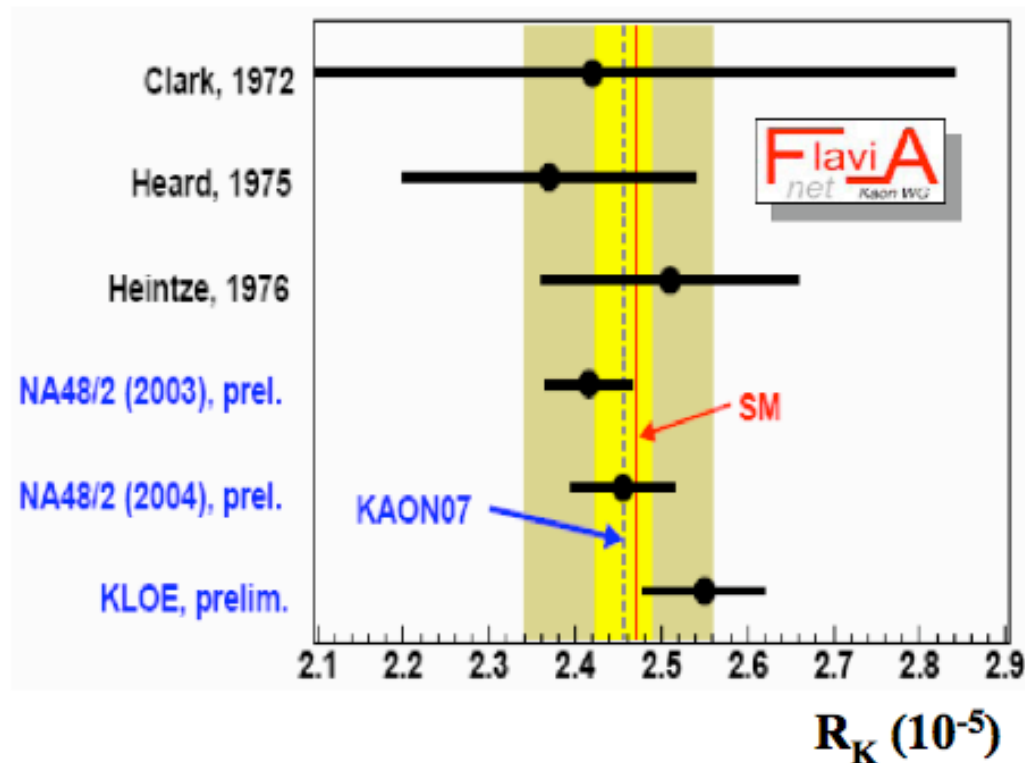


## Summary of $R_K$ measurements

KLOE  
NA48  
NA62

Recent (preliminary) results improved greatly with respect to 2006 PDG

World average,  $R_K = 2.457(32) \times 10^{-5}$ , agrees with SM





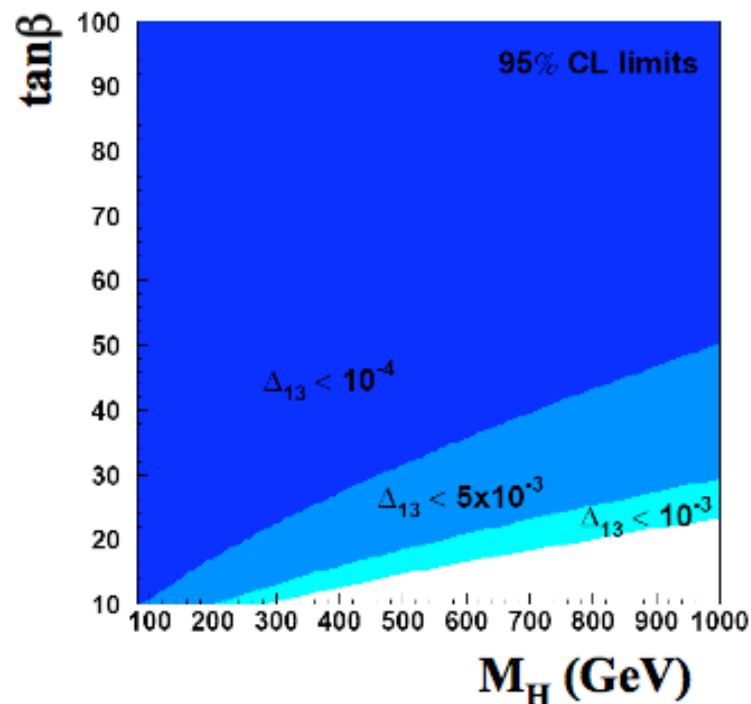
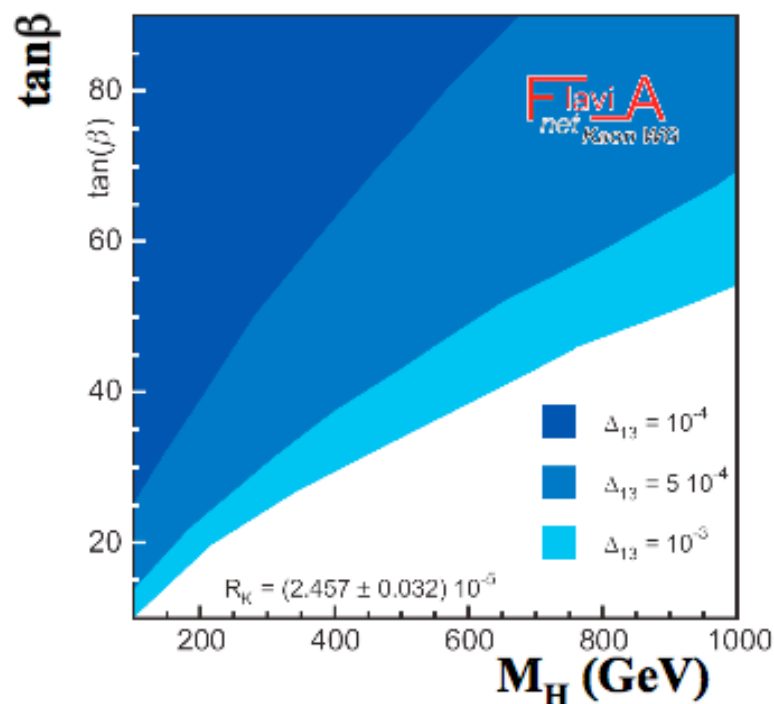
## $R_K$ Exclusion Regions for Higgs

Kloe  
NA48  
NA62

Sensitivity shown as 95%-CL excluded regions in the  $\tan\beta$  -  $M_H$  plane, for fixed values of the 1-3 slepton-mass matrix element,  $\Delta_{13} = 10^{-3}, 0.5 \times 10^{-3}, 10^{-4}$

Present world avg:  $R_K = 2.457(32) \times 10^{-5}$

Perspective: same  $R_K$ ,  $\delta R_K = 0.3\%$





## IV. CKM Unitarity

**KLOE  
KTeV  
NA48**

In 2004 it was realized that the PDG branching ratios that had been used for decades to calculate  $V_{us}$  and the first row unitarity of the CKM matrix were flawed. A large effort by these three experiments was mounted to remeasure the various K branching ratios and form factors and by the Flavia group to bring together the information to redo  $V_{us}$ .

**The saga continues**



## Quantities for CKM Unitarity Check

KLOE  
KTeV  
NA48  
ISTRA+

$$|V_{us}| \times f_+(0)$$

$$\Gamma(K_{\ell 3}(\gamma)) = \frac{G_F^2 m_K^5}{192\pi^3} C_K S_{\text{ew}} |V_{us}|^2 f_+(0)^2 I_K^\ell(\lambda_{+,0}) \left(1 + \delta_{SU(2)}^K + \delta_{\text{em}}^{K\ell}\right)^2$$

$$|V_{us}|/|V_{ud}| \times f_K/f_\pi.$$

$$\frac{\Gamma(K_{\ell 2}^\pm(\gamma))}{\Gamma(\pi_{\ell 2}^\pm(\gamma))} = \left| \frac{V_{us}}{V_{ud}} \right|^2 \frac{f_K^2 m_K}{f_\pi^2 m_\pi} \left( \frac{1 - m_\ell^2/m_K^2}{1 - m_\ell^2/m_\pi^2} \right)^2 \times (1 + \delta_{\text{em}})$$

Obtained from global fits and averages of dominant  $K_L$ ,  $K_S$ , and  $K^\pm$  BRs and lifetime and parameterization of the  $K \rightarrow \pi$  interaction form factor



## Determination of $|V_{us}| \times f_+(0)$

KLOE  
KTeV  
NA48  
ISTRA+

$$\Gamma(K_{l3(\gamma)}) = \frac{C_K^2 G_F^2 M_K^5}{192\pi^3} S_{EW} |V_{us}|^2 |f_+^{K^0\pi^-}(0)|^2 I_{K\ell}(\lambda_{+,0}) (1 + \delta_{SU(2)}^K + \delta_{em}^{K\ell})^2$$

with  $K = K^+, K^0$ ;  $\ell = e, \mu$  and  $C_K^2 = 1/2$  for  $K^+$ , 1 for  $K^0$

### Inputs from theory:

- $S_{EW}$  Universal short distance EW correction (1.0232)
- $\delta_{SU(2)}^K$  Form factor correction for strong SU(2) breaking
- $\delta_{em}^{K\ell}$  Long distance EM effects
- $f_+^{K^0\pi^-}(0)$  Form factor at zero momentum transfer ( $t=0$ )

### Inputs from experiment:

- $\Gamma(K_{l3(\gamma)})$  **Branching ratios** properly inclusive of radiative effects; **lifetimes**
- $I_{K\ell}(\lambda)$  Phase space integral:  $\lambda$ 's parameterize form factor dependence on  $t$ :
  - $K_{e3}$ : only  $\lambda_+$
  - $K_{\mu 3}$ : need  $\lambda_+$  and  $\lambda_0$



B. Cox

6/27/08

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## $K_L$ leading branching ratios and $\tau_L$

**KLOE**  
**KTeV**  
**NA48**

**18 input measurements:**

**5 KTeV** ratios

**NA48**  $K_{e3}/2\text{tr}$  and  $\Gamma(3\pi^0)$

**4 KLOE** BRs

**KLOE, NA48**  $\pi^+\pi^-/K_{l3}$

**KLOE, NA48**  $\gamma\gamma/3\pi^0$

**PDG** ETAFIT for  $\pi^+\pi^-/\pi^0\pi^0$

**KLOE**  $\tau_L$  from  $3\pi^0$

**Vosburgh '72**  $\tau_L$

Parameter	Value	$S$
$\text{BR}(K_{e3})$	0.4056(7)	1.1
$\text{BR}(K_{\mu3})$	0.2705(7)	1.1
$\text{BR}(3\pi^0)$	0.1951(9)	1.2
$\text{BR}(\pi^+\pi^-\pi^0)$	0.1254(6)	1.1
$\text{BR}(\pi^+\pi^-)$	$1.997(7) \times 10^{-3}$	1.1
$\text{BR}(2\pi^0)$	$8.64(4) \times 10^{-4}$	1.3
$\text{BR}(\gamma\gamma)$	$5.47(4) \times 10^{-4}$	1.1
$\tau_L$	51.17(20) ns	1.1

**8 free parameters, 1 constraint:  $\Sigma\text{BR}=1$**

Main differences wrt PDG06:

- For KLOE and KTeV, use values obtained before applying constraints.
- Make use of preliminary  $\text{BR}(3\pi^0)$  and new  $\text{BR}(\pi^+\pi^-)/\text{BR}(K_{e3})$  from NA48
- Fit parameter  $\text{BR}(\pi^+\pi^-)$  is understood to be inclusive of the DE component.





## $K_S$ leading branching ratios and $\tau_S$

KLOE  
KTeV  
NA48

4 input measurements:

KLOE  $BR(K_{e3})/BR(\pi^+\pi^-)$

KLOE  $BR(\pi^+\pi^-)/BR(\pi^0\pi^0)$

Universal lepton coupling

NA48  $BR(K_{e3})$

$\tau_S$ : non CPT-constrained fit value, dominated  
by 2002 NA48 and 2003 KTeV measurements

4 free parameters:  $K_S\pi\pi$ ,  $K_S\pi^0\pi^0$ ,  $K_Se3$ ,  $K_S\mu3$ , 1 constraint:  $\Sigma BR=1$

- KLOE meas. completely determine the leading BR values.
- NA48  $K_{e3}$  input improve the  $BR(K_{e3})$  accuracy of about 10%.
- $BR(K_Se3)/BR(K_L e3)$  from NA48 not included (need of a  $K_L$  and  $K_S$  combined fit)
- Combined fit would be useful in properly account for preliminary NA48  $\Gamma(K_L \rightarrow 3\pi^0)$  and PDG ETAFIT, used in the  $K_L$  fit.



## $K^\pm$ leading branching ratios and $\tau^\pm$

**KLOE**  
**NA48**  
**ISTRA+**

### 26 input measurements:

5 older  $\tau$  values in PDG

2 KLOE  $\tau$

KLOE BR( $\mu\nu$ )

KLOE  $Ke3$ ,  $K\mu3$ , and  $K\pi2$  BRs

ISTRA+  $K_{e3}/\pi\pi^0$

NA48/2  $K_{e3}/\pi\pi^0$ ,  $K_{\mu3}/\pi\pi^0$

E865  $K_{e3}/K_{\text{dal}}$

3 old  $\pi\pi^0/\mu\nu$

2 old  $Ke3/2$  body

3  $K\mu3/Ke3$  (2 old)

2 old + 1 KLOE results on  $3\pi$

7 free parameters,

1 constraint:  $\Sigma\text{BR}=1$

Parameter	Value	$S$
BR( $K_{\mu2}$ )	63.57(11)%	1.1
BR( $\pi\pi^0$ )	20.64(8)%	1.1
BR( $\pi\pi\pi$ )	5.595(31)%	1.0
BR( $K_{e3}$ )	5.078(26)%	1.2
BR( $K_{\mu3}$ )	3.365(27)%	1.7
BR( $\pi\pi^0\pi^0$ )	1.750(26)%	1.1
$\tau_\pm$	12.384(19) ns	1.7

Don't use the 6 BR meas. from Chiang;

- no implementation of radiative corrections
- 6 BR constrained to sum to unit.
- the correlation matrix not available.

What about discarding many other old meas.?

- no recent meas. involving BR( $\pi\pi\pi$ )
- fit instable if only recent are used.



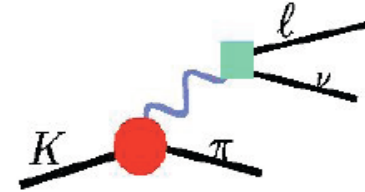
## Parameterization of $K_{\ell 3}$ form factors

KLOE  
KTeV  
NA48  
ISTRA+

- Hadronic  $K \rightarrow \pi$  matrix element is described by two form factors  $f_+(t)$  and  $f_0(t)$  defined by:

$$\langle \pi^-(k) | \bar{s} \gamma^\mu u | K^0(p) \rangle = (p+k)^\mu f_+(t) + (p-k)^\mu f_-(t)$$

$$f_-(t) = \frac{m_K^2 - m_\pi^2}{t} (f_0(t) - f_+(t))$$



- Experimental or theoretical inputs to define  $t$ -dependence of  $f_{+,0}(t)$ .
- $f_-(t)$  term negligible for  $K_{e3}$ .

• **Taylor expansion:**

$$\tilde{f}_{+,0}(t) \equiv \frac{f_{+,0}(t)}{f_{+,0}(0)} = 1 + \lambda'_{+,0} \frac{t}{m_\pi^2} + \frac{1}{2} \lambda''_{+,0} \left( \frac{t}{m_\pi^2} \right)^2 + \dots$$

$\lambda'$  and  $\lambda''$  are strongly correlated:  $-95\%$  for  $f_+(t)$ , and  $-99.96\%$  for  $f_0(t)$

• **Pole parameterization:**

$$\tilde{f}_{+,0}(t) = \frac{M_{V,S}^2}{M_{V,S}^2 - t}$$

- Dispersive approach plus  $K\pi$  scattering data for both  $f_+(t)$  and  $f_0(t)$**



## Vector form factor from $K_{e3}$

KLOE  
KTeV  
NA48  
ISTRA+

### Quadratic expansion

- Measurements from ISTRA+, KLOE, KTeV, NA48 with  $K_L e3$  and  $K^- e3$  decays.
- **Good fit quality:  $\chi^2/\text{ndf}=5.3/6(51\%)$  for all data;  $\chi^2/\text{ndf}=4.7/4(32\%)$  for  $K_L$  only**
- **The significance of the quadratic term is  $4.2\sigma$  from all data and  $3.5\sigma$  from  $K_L$  only.**
- **Using all data or  $K_L$  only changes the space phase integrals  $I^0_{e3}$  and  $I^\pm_{e3}$  by 0.07% .**
- Errors on  $I_{e3}$  are significantly smaller when  $K^-$  data are included.

Pole parameterization is in good agreement with present data:

$$\tilde{f}_+(t) = M_V^2 / (M_V^2 - t), \text{ with } M_V \sim 892 \text{ MeV} \quad \lambda' = (m_{\pi^+}/M_V)^2; \lambda'' = 2\lambda'^2$$

- KLOE, KTeV, NA48 quote value for  $M_V$  for pole fit to  $K_L e3$  data ( $\chi^2/\text{ndf}=1.8/2$ )
- The values for  $\lambda'_+$  and  $\lambda''_+$  from pole expansion are in agreement with quadratic fit results.
- **Using quadratic averages or pole fit results changes  $I^0_{e3}$  by 0.03% .**

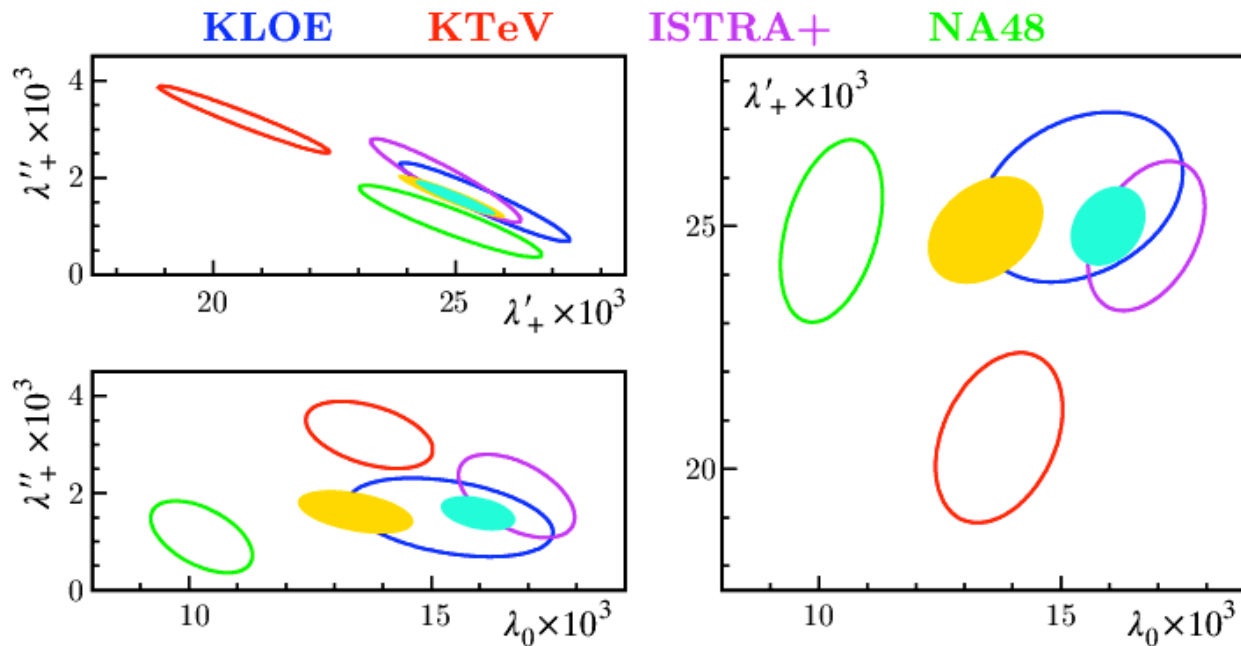
Dispersive parameterization show improvements for  $f_+(t)$ , with good analytical and unitarity properties and a correct threshold behavior, (e.g. Passemar arXiv:0709.1235[hep-ph])  
Dispersive results for  $\lambda_+$  and  $\lambda_0$  are in agreement with pole parameterization.



## Vector and scalar form factor from $K_{\mu 3}$

KLOE  
KTeV  
NA48  
ISTRA+

- $\lambda_+' , \lambda_+''$  and  $\lambda_0$  measured for  $K_{\mu 3}$  from ISTRA+, KLOE, KTeV, and NA48.
- **new NA48 results are difficult to accommodate** in the  $[\lambda_+' , \lambda_+'' , \lambda_0]$  space.
- Fit probability varies from  $1 \times 10^{-6}$  (with NA48) to 22.3% (without NA48).



$1\sigma$  contour  
for all the  
experimental  
results.

Fit  
with NA48

Fit  
without  
NA48

- Because of correlation, is not possible measure  $\lambda_0''$  at any plausible level of stat.
- Neglecting a quadratic term in the param. of scalar FF implies:  $\lambda_0' \rightarrow \lambda_0' + 3.5\lambda_0''$



## Vector and scalar form factor from $K_{\ell 3}$

KLOE  
KTeV  
NA48  
ISTRA+

- Slope parameters  $\lambda'_+$ ,  $\lambda''_+$  and  $\lambda_0$  from ISTRA+, KLOE, KTeV, and NA48.

	$K_L$ and $K^-$	$K_L$ only
Measurements	16	11
$\chi^2/\text{ndf}$	54/13 ( $7 \times 10^{-7}$ )	33/8 ( $8 \times 10^{-5}$ )
$\lambda'_+ \times 10^3$	$24.9 \pm 1.1$ ( $S = 1.4$ )	$24.0 \pm 1.5$ ( $S = 1.5$ )
$\lambda''_+ \times 10^3$	$1.6 \pm 0.5$ ( $S = 1.3$ )	$2.0 \pm 0.6$ ( $S = 1.6$ )
$\lambda_0 \times 10^3$	$13.4 \pm 1.2$ ( $S = 1.9$ )	$11.7 \pm 1.2$ ( $S = 1.7$ )
$\rho(\lambda'_+, \lambda''_+)$	-0.94	-0.97
$\rho(\lambda'_+, \lambda_0)$	+0.33	+0.72
$\rho(\lambda''_+, \lambda_0)$	-0.44	-0.70
$I(K_{e3}^0)$	0.15457(29)	0.1544(4)
$I(K_{e3}^\pm)$	0.15892(30)	0.1587(4)
$I(K_{\mu 3}^0)$	0.10212(31)	0.1016(4)
$I(K_{\mu 3}^\pm)$	0.10507(32)	0.1046(4)
$\rho(I_{e3}, I_{\mu 3})$	+0.63	+0.89

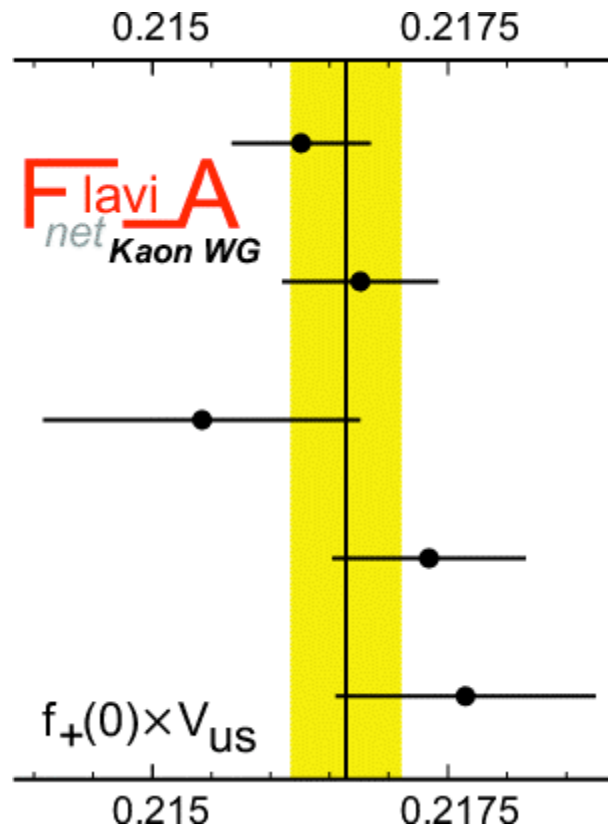
Averages of quadratic fit results for  $Ke3$  and  $K\mu 3$  slopes.

Space integral  
used for the  $|V_{us}|f_+(0)$   
determination

- Adding  $K\mu 3$  data to the fit doesn't cause significant changes to  $I_{e3}^0$  and  $I_{e3}^\pm$ .
- NA48:  $\Delta[I(K\mu 3)] = 0.6\%$ , but  $Ke3+K\mu 3$  average gives  $\Delta[V_{us}f_+(0)] = -0.08\%$ .**



## Determination of $|V_{us}| \times f_+(0)$



		% err	Approx. contribution to % err from:			
			BR	$\tau$	$\delta$	$I_{K^*}$
$K_L e3$	0.2163(6)	0.28	0.09	0.19	0.15	0.09
$K_L \mu3$	0.2168(7)	0.31	0.10	0.18	0.15	0.15
$K_S e3$	0.2154(13)	0.67	0.65	0.03	0.15	0.09
$K^\pm e3$	0.2173(8)	0.39	0.26	0.09	0.26	0.09
$K^\pm \mu3$	0.2176(11)	0.51	0.40	0.09	0.26	0.15

**Average:  $|V_{us}| f_+(0) = 0.2166(5)$      $\chi^2/\text{ndf} = 2.74/4$  (60%)**



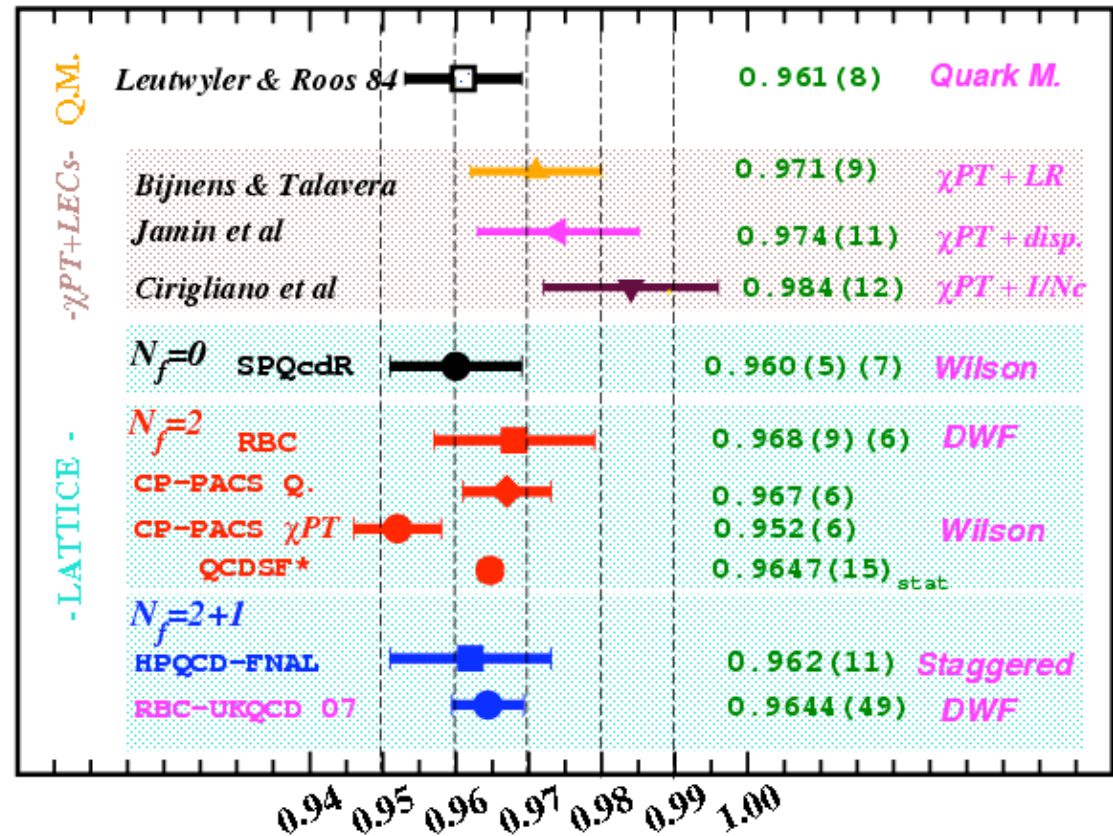
## Theoretical estimate of $f_+(0)$

KLOE  
KTeV  
NA48  
ISTRA+

Leutwyler & Roos estimate  
still widely used:

$$f_+(0) = 0.961(8).$$

Lattice evaluations generally  
agree well with this value;  
use RBC-UKQCD07 value:  
 $f_+(0) = 0.9644(49)$  (0.5%  
accuracy, total err.).



Kl3:  $|V_{us}| f_+(0) = 0.2166(5)$  and  $f_+(0) = 0.964(5)$ , obtain  $|V_{us}| = 0.2246(12)$





## $V_{us}/V_{ud}$ determination from $BR(K_{\mu 2})$

KLOE  
NA48  
ISTRA+

$$\frac{\Gamma(K_{\mu 2(\gamma)})}{\Gamma(\pi_{\mu 2(\gamma)})} = \frac{|V_{us}|^2}{|V_{ud}|^2} \times \frac{f_K}{f_\pi} \times \frac{M_K(1-m_\mu^2/M_K^2)^2}{m_\pi(1-m_\mu^2/m_\pi^2)^2} \times (1+\alpha(C_K-C_\pi))$$

### Inputs from experiment

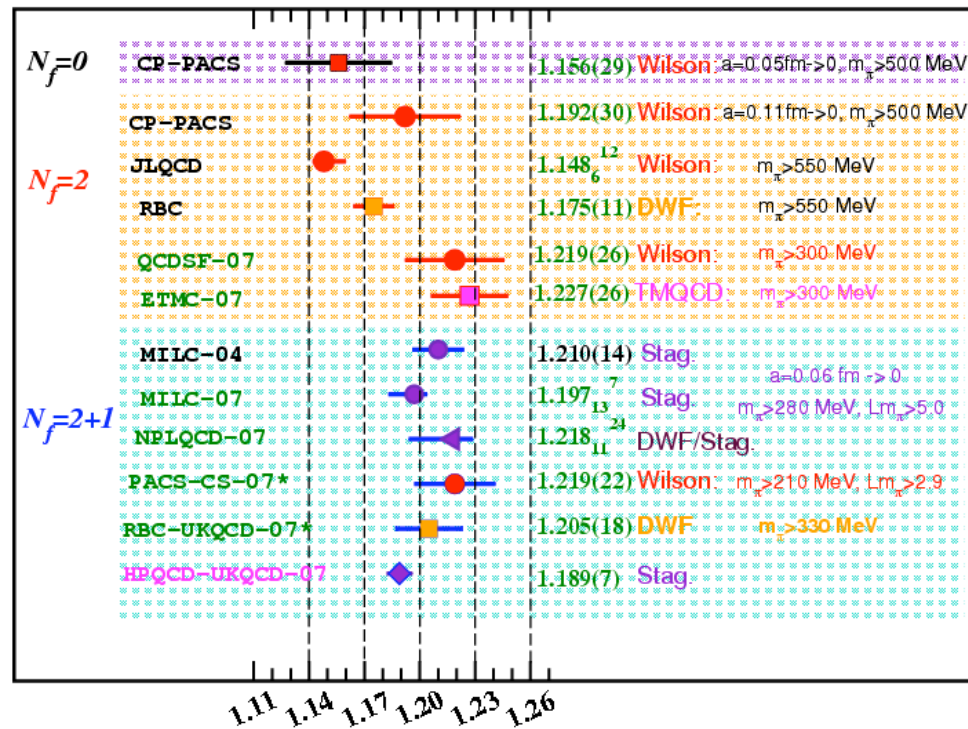
$\Gamma(\pi, K_{l2(\gamma)})$  BR properly includes  
radiative effects; lifetimes

### Inputs from theory

$C_{K,\pi}$  Rad. includes EW corr.

$f_K/f_\pi$  Not protected by the Ademollo-Gatto theorem:  
Lattice calculation of  $f_K/f_\pi$   
and radiative corrections  
benefit of cancellations.

- Use HPQCD-UKQCD07  
value:  $f_K/f_\pi = 1.189(7)$ .



K12:  $|V_{us}|/|V_{ud}| f_K/f_\pi = 0.2760(6)$  and  $f_K/f_\pi = 1.189(7)$ , obtain  $|V_{us}|/|V_{ud}| = 0.2321(15)$



## $V_{ud}$ , $V_{us}$ and $V_{us}/V_{ud}$

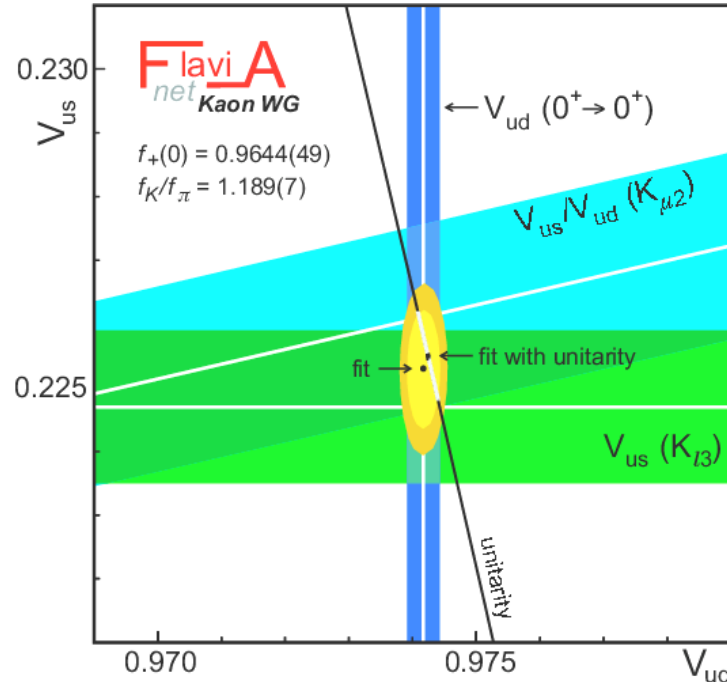
KLOE  
KTeV  
NA48  
ISTRA+

$|V_{us}| = 0.2246(12)$ ,  $|V_{us}|/|V_{ud}| = 0.2321(15)$   
 $V_{ud} = 0.97418(26)$  from nuc.  $\beta$  decay:  
 [Hardy-Towner, nucl-th 0710.3181]

### Fit (no CKM unitarity constraint)

$V_{ud} = 0.97417(26)$ ;  $V_{us} = 0.2253(9)$   
 $\chi^2/\text{ndf} = 0.65/1$  (41%)

Unitarity:  $1 - V_{ud}^2 - V_{us}^2 = 0.0002(6)$



- The test on the unitarity of CKM can be also interpreted as a **test of the universality of lepton and quark gauge coupling**:

$$G_{\text{CKM}} \equiv G_{\mu} [ |V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 ]^{1/2}$$

$$= (1.1662 \pm 0.0004) \times 10^{-5} \text{ GeV}^{-2}$$

$$G_{\mu} = (1.166371 \pm 0.000007) \times 10^{-5} \text{ GeV}^{-2}$$

### Fit (with CKM unitarity constraint)

$V_{us} = 0.2255(7)$   $\chi^2/\text{ndf} = 0.8/2$  (67%)



## $V_{us}$ Summary

KLOE  
KTeV  
NA48  
ISTRA+

- Dominant  $K_S$ ,  $K_L$ , and  $K^\pm$  BRs, and lifetime known with very good accuracy.
- Dispersive approach for form factors.
- Constant improvements from lattice calculations of  $f_+(0)$  and  $f_K/f_\pi$ :  
Callan-Treiman relation allows checks from measurements;  
syst errors often not quoted, problem when averaging different evaluations.
- $|V_{us}| f_+(0)$  at 0.2% level.
- $|V_{us}|$  measured with 0.4% accuracy (with  $f_+(0) = 0.9644(49)$ )  
Dominant contribution to uncertainty on  $|V_{us}|$  still from  $f_+(0)$ .  
CKM unitarity test satisfied at  $0.3\sigma$  level  
test of lepton-quark universality
- Comparing  $|V_{us}|$  values from  $K\mu 2$  and  $Kl 3$ , exclude large region in the  $(m_{H^\pm}, \tan\beta)$  plane, complementary to results from  $B \rightarrow \tau \nu$  decays.
- Test of Lepton Universality with  $Kl 3$  decays with 0.5% accuracy.



## V. New Results contributing to ChPT

**KLOE**  
**KTeV**  
**NA48**



## V. New Kaon Results on ChPT

Kloe  
KTeV  
NA48/2

**NA48/2** recent results in charged Kaon decays

- $K^\pm \rightarrow \pi^\pm e^+ e^-$  BR and Form Factors (preliminary)
- $K^\pm \rightarrow \pi^\pm \gamma \gamma$  BR and kinematics (preliminary)
- $K^\pm \rightarrow \pi^\pm e^+ e^- \gamma$  Branching Ratio (final)

**KTeV** “recent” results in neutral Kaon decays

- $K_L \rightarrow \pi^0 e^+ e^-$  BR (99 data to be added)
- $K_L \rightarrow \pi^0 \gamma \gamma$  BR and kinematics (final)
- $K_L \rightarrow \pi^0 e^+ e^- \gamma$  Branching Ratio (final)

**KLOE** recent results in neutral Kaon decays

- $K_S \rightarrow \gamma \gamma$  Branching Ratio (final)
- $K_S \rightarrow e^+ e^-$  Direct Search, Upper Limit (final)
- $K_L \rightarrow \pi e \nu \gamma$  Branching Ratio (final)



**KTeV**  
**NA48**

**NA48/2:  $K^{\pm} \rightarrow \pi^{\pm} e^{+} e^{-}$**

**KTeV:  $K_L \rightarrow \pi^0 e^{+} e^{-}$**



# $K^\pm \rightarrow \pi^\pm \gamma^* \rightarrow \pi^\pm e^+ e^-$ Theoretical Framework

NA48/2

- ✓ suppressed FCNC processes
- ✓ one-photon exchange
- ✓ useful test for ChPT

$$d\Gamma_{\pi ee}/dz \sim P(z) \cdot |W(z)|^2$$

$z=(M_{ee}/M_K)^2$ ,  $P(z)$  phase space factor

## Form-factor models:

- (1) polynomial:  $W(z) = G_F M_K^2 \cdot f_0 \cdot (1 + \delta z)$
- (2) ChPT  $O(p^6)$ :  $W(z) = G_F M_K^2 \cdot (a_+ + b_+ z) + W^{\pi\pi}(z)$
- (3) Dubna ChPT:  $W(z) = W(M_a, M_\rho, z)$

(2) D'Ambrosio et al. JHEP 8 (1998) 4      (3) Dubnickova et al. hep-ph/0611175

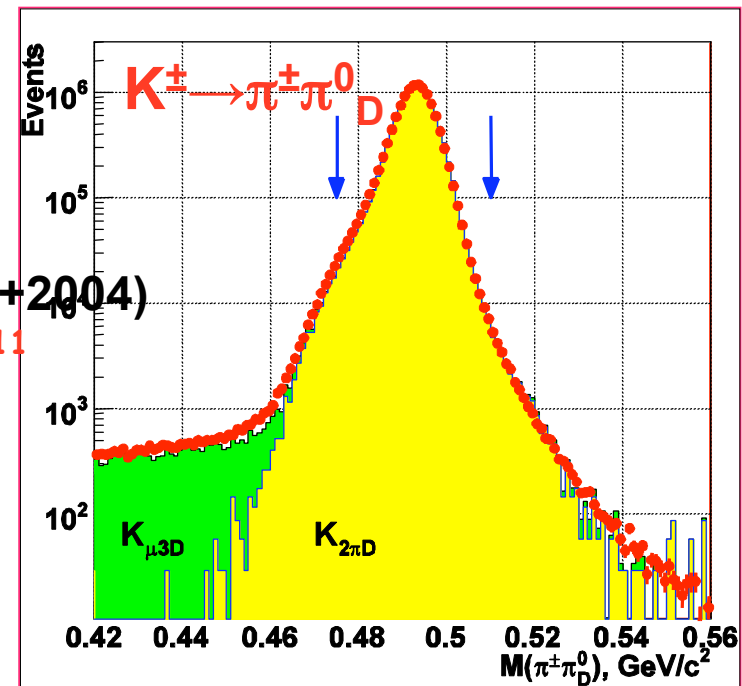
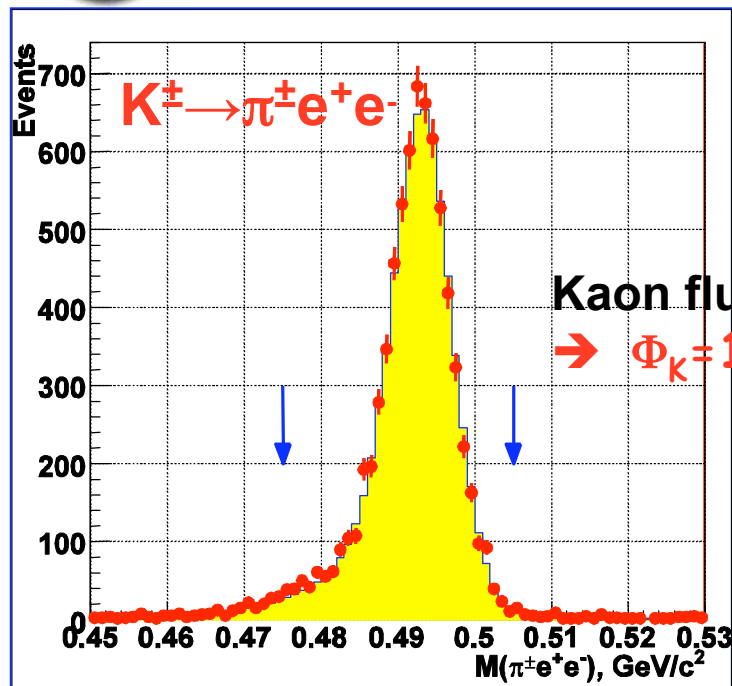
$(f_0, \delta)$  or  $(a_+, b_+)$  or  $(M_a, M_\rho)$  determine a model-dependent BR

- Parameters of models and BR in full kinematical range
- Model-independent BR ( $z > 0.08$ ) in visible kinematical range



# Data $K^\pm \rightarrow \pi^\pm \gamma^* \rightarrow \pi^\pm e^+ e^-$

NA48/2



7146 events ( $M_{ee} > 140$  MeV) (BG 0.6%)

$12.23 \times 10^6$  events (BG 0.15%)

- The BR is measured normalizing to  $K^\pm \rightarrow \pi^\pm \pi^0_D \rightarrow \pi^\pm e^+ e^- \gamma$   
 $\rightarrow$  particle ID efficiencies cancel at first order
- common selection criteria for signal and normalization channel  
 $\rightarrow$  3 track vertex, electron (pion) ID with  $E/p > 0.95$  ( $< 0.85$ )
- $K^\pm \rightarrow \pi^\pm \pi^0_D$  BG suppressed using a kinematical cut  $M_{ee} > 140$  MeV





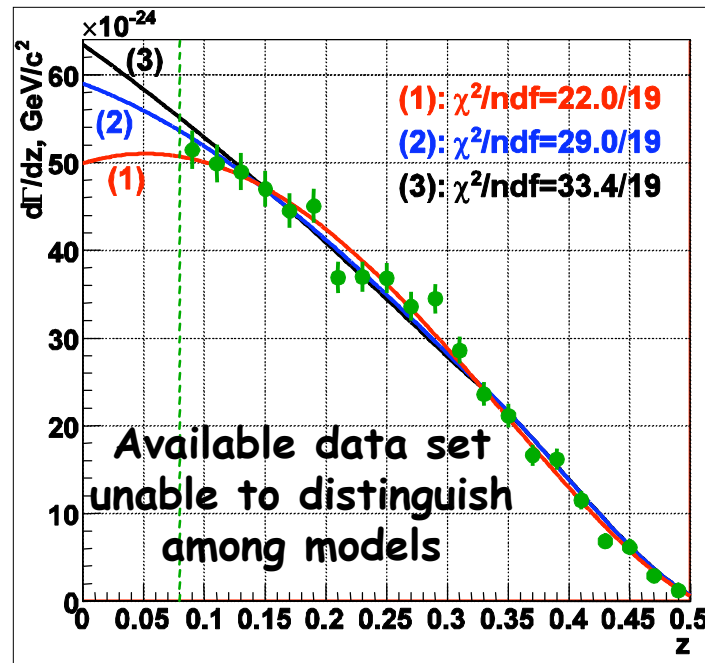
## Fit results (preliminary)

**NA48/2**

polynomial:  $W(z) = G_F M_K^2 \cdot f_0 \cdot (1 + \delta z)$

ChPT  $O(p^6)$ :  $W(z) = G_F M_K^2 \cdot (a_+ + b_+ z) + W_{\pi\pi}(z)$

Dubna ChPT:  $W(z) = W(M_a, M_\rho z)$



{	(1)	$\delta = 2.35 \pm 0.18$ $f_0 = 0.532 \pm 0.016$ $(\delta, f_0) = -0.963$
	(2)	$a_+ = -0.579 \pm 0.016$ $b_+ = -0.798 \pm 0.067$ $(a_+, b_+) = -0.913$
	(3)	$M_a = (0.965 \pm 0.033) \text{ GeV}$ $M_\rho = (0.711 \pm 0.013) \text{ GeV}$ $(M_a, M_\rho) = 0.998$

Model-Independent BR computed  
by integrating  $dG/dz$

$$\text{BR}_{\text{MI}}(z > 0.08) = (2.26 \pm 0.08) \times 10^{-7}$$

$$\begin{aligned} \text{BR1} &= (3.02 \pm 0.04_{\text{stat}}) \times 10^{-7} \\ \text{BR2} &= (3.11 \pm 0.04_{\text{stat}}) \times 10^{-7} \\ \text{BR3} &= (3.15 \pm 0.04_{\text{stat}}) \times 10^{-7} \end{aligned}$$

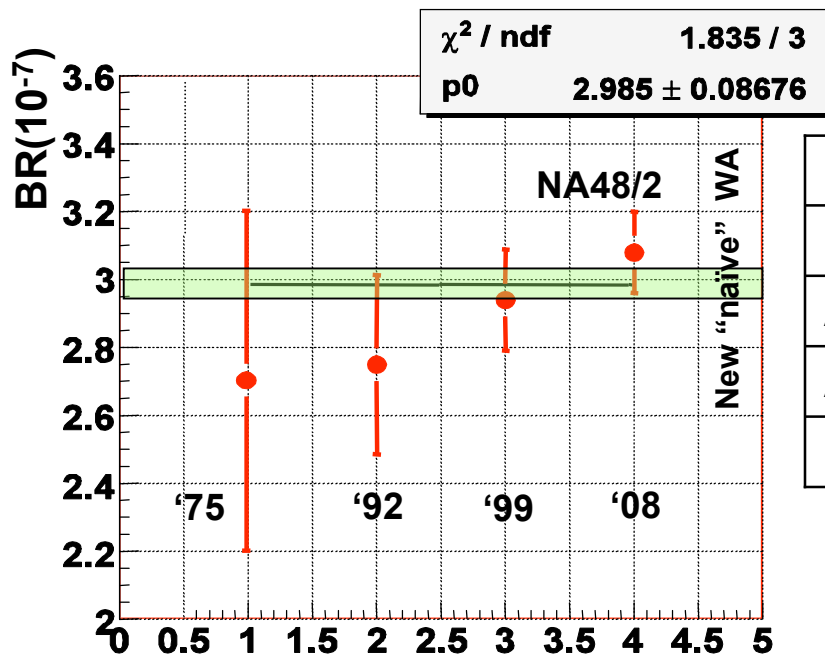


## Results – BR in full kinematic range

**NA48/2**

$$\text{BR} = (3.08 \pm 0.04_{\text{stat}} \pm 0.04_{\text{syst}} \pm 0.08_{\text{ext}} \pm 0.07_{\text{model}}) \times 10^{-7} = (3.08 \pm 0.12) \times 10^{-7}$$

Including the uncertainty due to the model dependence (preliminary)



Measurement	BR $\times 10^7$
Bloch et al., PL 56 (1975) B201	2.70 $\pm$ 0.50
Alliegro et al., PRL 68 (1992) 278	2.75 $\pm$ 0.26
Appel et al. [E865], PRL 83 (1999) 4482	2.94 $\pm$ 0.15
<b>NA48/2 preliminary (2008)</b>	<b>3.08<math>\pm</math>0.12</b>

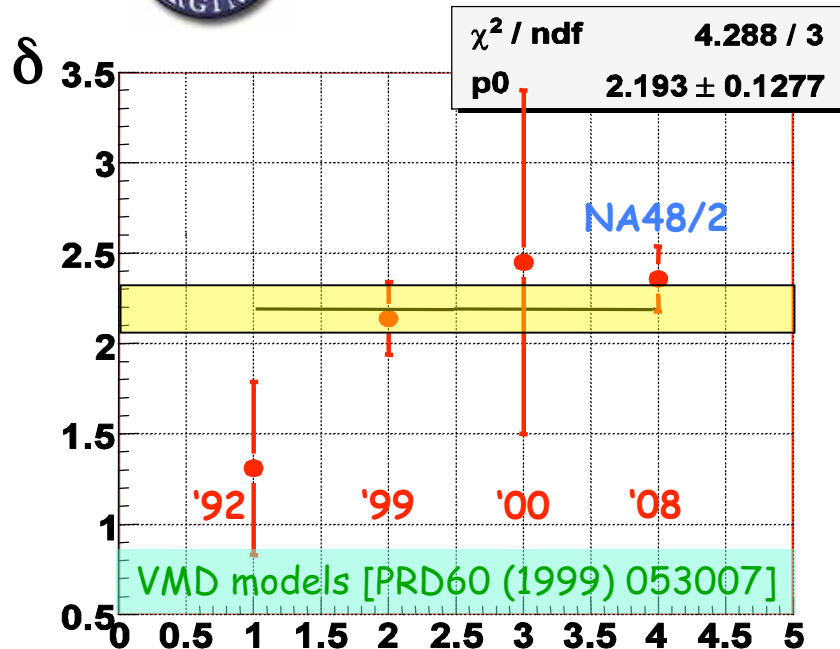
First measurement of CPV parameter  
(correlated  $K^+/K^-$  uncertainties excluded)

$$\Delta(K_{\pi ee}^\pm) = (\text{BR}^+ - \text{BR}^-) / (\text{BR}^+ + \text{BR}^-) \\ = (-2.1 \pm 1.5_{\text{stat}} \pm 0.3_{\text{syst}})\%$$



## Results – FF slope $\delta$

**NA48/2**



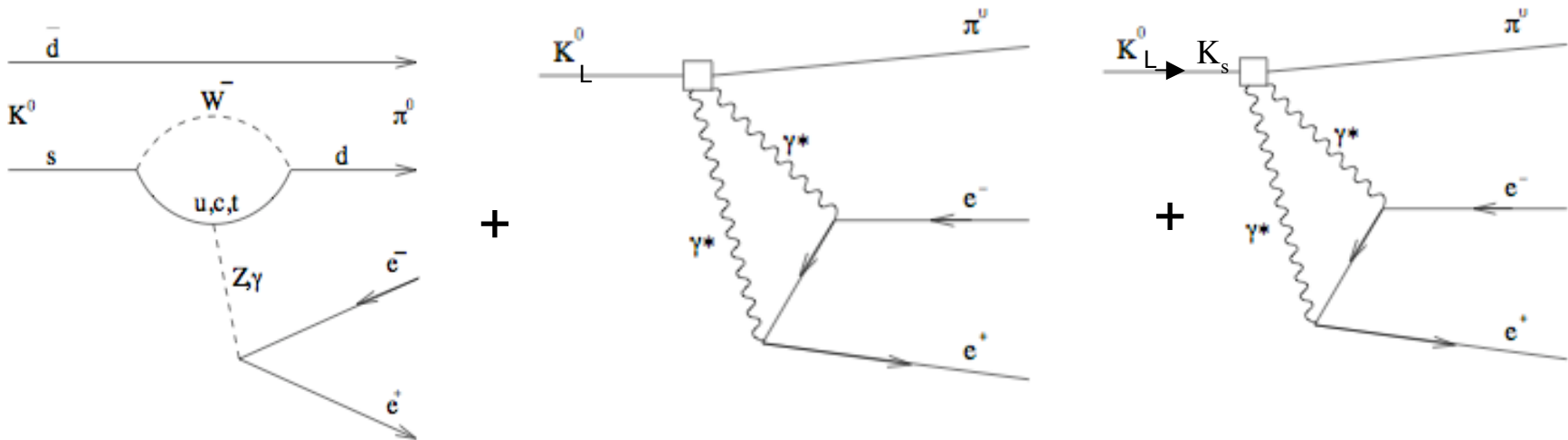
- NA48/2 measurement of  $\delta$   
 good precision  
 compatible with earlier results
- Contradiction of the data to VMD  
 further confirmed
- NA48/2 values of  $(f_0, a_+, b_+)$   
 in agreement with BNL E865

Measurement	Process	Result
Alliegro et al., PRL 68 (1992) 278	$K^+ \rightarrow \pi^+ e^+ e^-$	$1.31 \pm 0.48$
Appel et al. [E865], PRL 83 (1999) 4482	$K^+ \rightarrow \pi^+ e^+ e^-$	$2.14 \pm 0.20$
Ma et al. [E865], PRL 84 (2000) 2580	$K^+ \rightarrow \pi^+ \mu^+ \mu^-$	$2.45^{+1.30}_{-0.95}$
<b>NA48/2 preliminary (2008)</b>	$K^\pm \rightarrow \pi^\pm e^+ e^-$	<b><math>2.35 \pm 0.18</math></b>



# $K_L \rightarrow \pi^0 \gamma^* \rightarrow \pi^0 e^+ e^-$ Theoretical Framework

**KTeV**



**Direct CPV penguin**

**$2.8-6.5 \times 10^{-12}$**

**CP Conserving  $\sim O(P^6)$**

**$1-3 \times 10^{-12}$**

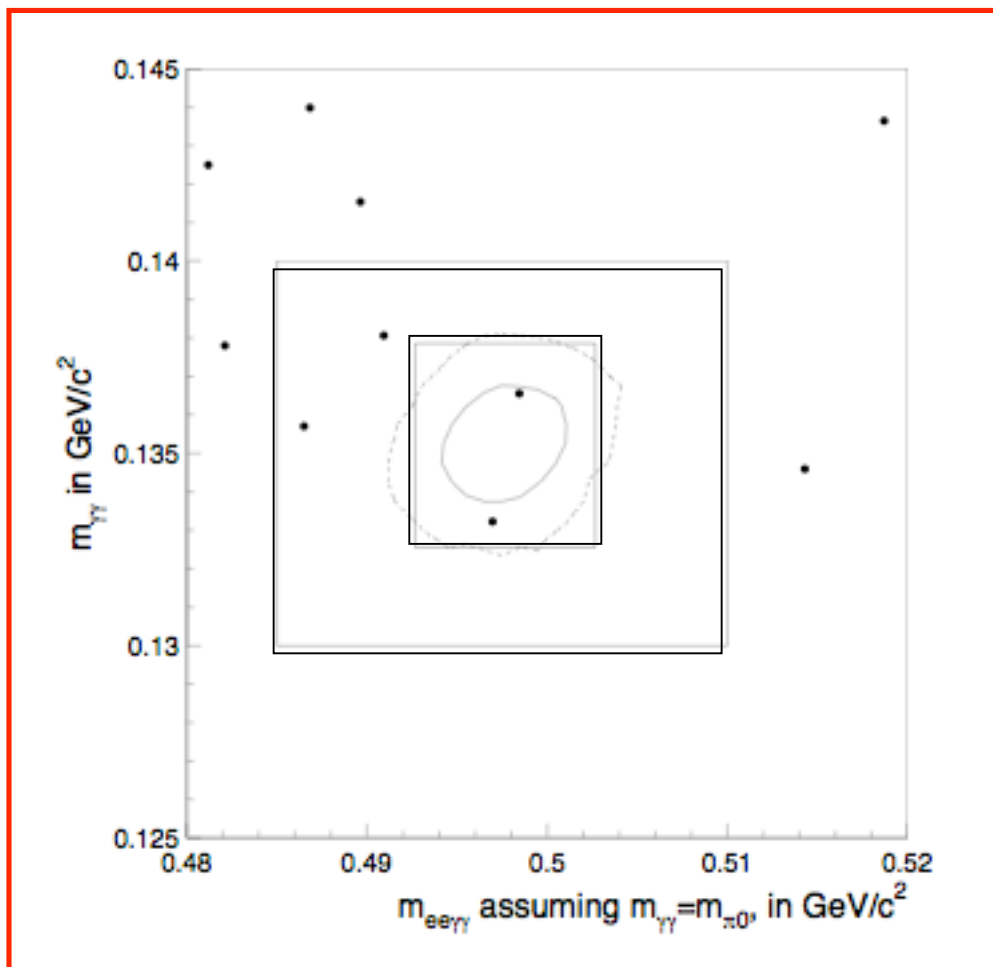
**Indirect CPV**

**$\epsilon \times (1-3) \times 10^{-12}$**



## Results: $K_L \rightarrow \pi^0 e^+ e^-$ Search

**KTeV**



**Two events observed in  
signal region**

**Total expected  
background from  
 $K_L \rightarrow \pi^0 \pi^0_D$   
 $1.06 \pm 0.41$  events**

$$\text{BR}(K_L \rightarrow \pi^0 e^+ e^-) < 5.1 \times 10^{-10}$$

**Only 1997 data  
1999 data analysis  
in progress**



**KTeV  
NA48**

**NA48/2  $K^{\pm} \rightarrow \pi^{\pm} \gamma \gamma$**

**$K^{\pm} \rightarrow \pi^{\pm} \gamma \gamma^{*} \rightarrow \pi^{\pm} \gamma e^{+} e^{-}$**

**KTeV:  $K_L \rightarrow \pi^0 \gamma \gamma$**

**$K_L \rightarrow \pi^0 \gamma \gamma^{*} \rightarrow \pi^0 \gamma e^{+} e^{-}$**



# $K^\pm \rightarrow \pi^\pm \gamma\gamma$ Theoretical Framework

NA48/2

$$\frac{\partial^2 \Gamma}{\partial y \partial z} = \frac{m_{K^+}}{(8\pi)^3} \left[ z^2 (|A|^2 + |C|^2) + \underbrace{\left( y^2 - \frac{1}{4} \lambda(1, r_\pi^2, z) \right)^2}_{\text{relevant only at low } m_\gamma} (|B|^2 + |D|^2) \right]$$

$$z = \frac{(q_1 + q_2)^2}{m_{K^+}^2} = \frac{m_{\gamma\gamma}^2}{m_{K^+}^2} \quad y = \frac{p \cdot (q_1 - q_2)}{m_{K^+}^2}$$

$O(p^4)$

$A(z) \rightarrow$  loop diagrams contribution

$C(z) \rightarrow$  Wess-Zumino-Witten functional (10%)

$B=D=0$

[G. Ecker, A. Pich and E. de Rafael, Nucl., Phys. B303 (1988), 665]

$O(p^6)$

unitarity corrections effects can increase the BR by 30-40 %

[G. D'Ambrosio and J. Portoles, Nucl., Phys. B386 (1996), 403]

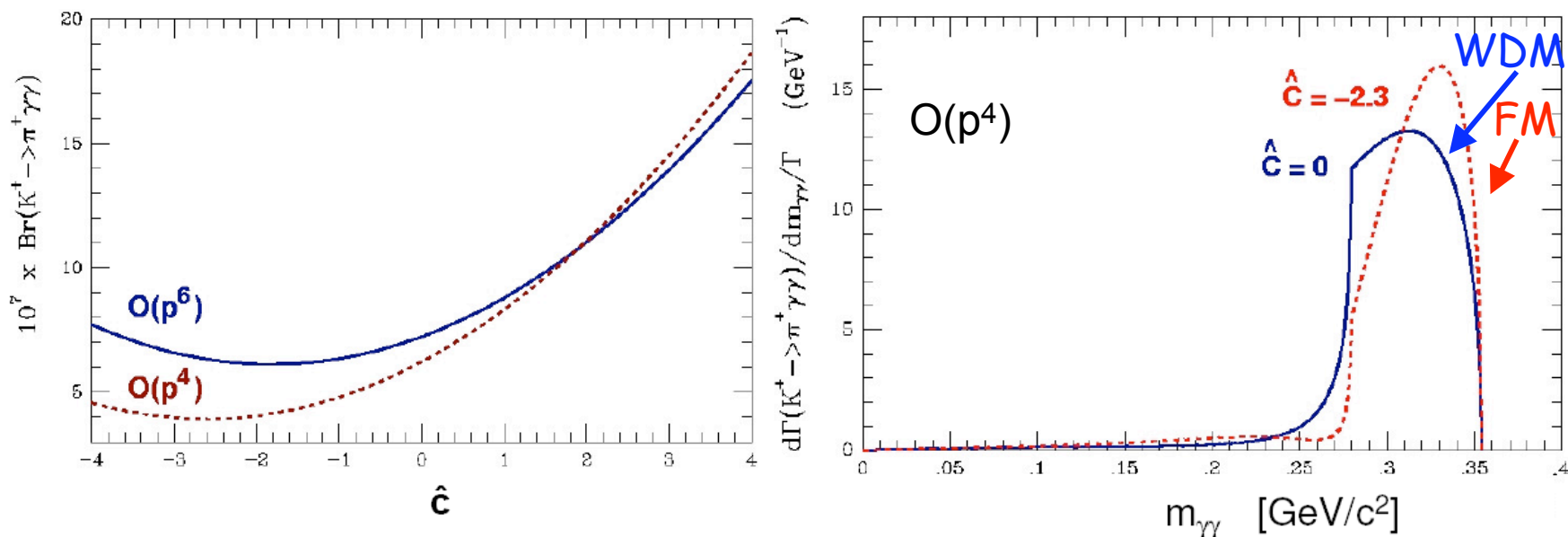


# $M_{\gamma\gamma}$ Spectrum from $K^\pm \rightarrow \pi^\pm \gamma\gamma$ dependence on $\hat{c}$

NA48/2

- Both decay spectrum and rate strongly depend on the single  $\hat{c}$  parameter
- The  $M_{\gamma\gamma}$  spectrum has a pronounced cusp-like behaviour at  $2\pi$  threshold.

$$\Gamma(K^\pm \rightarrow \pi^\pm \gamma\gamma) = \Gamma_{loop} + \Gamma_{WZW} \begin{cases} \Gamma_{loop} = (2.80 + 0.87 \cdot \hat{c} + 0.17 \cdot \hat{c}^2) \times 10^{-23} \text{ GeV} \\ \Gamma_{WZW} = 0.26 \times 10^{-23} \text{ GeV} \end{cases}$$



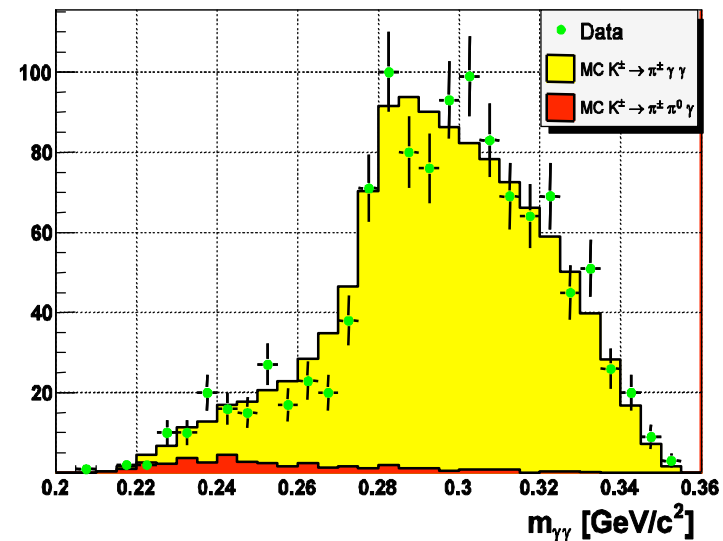
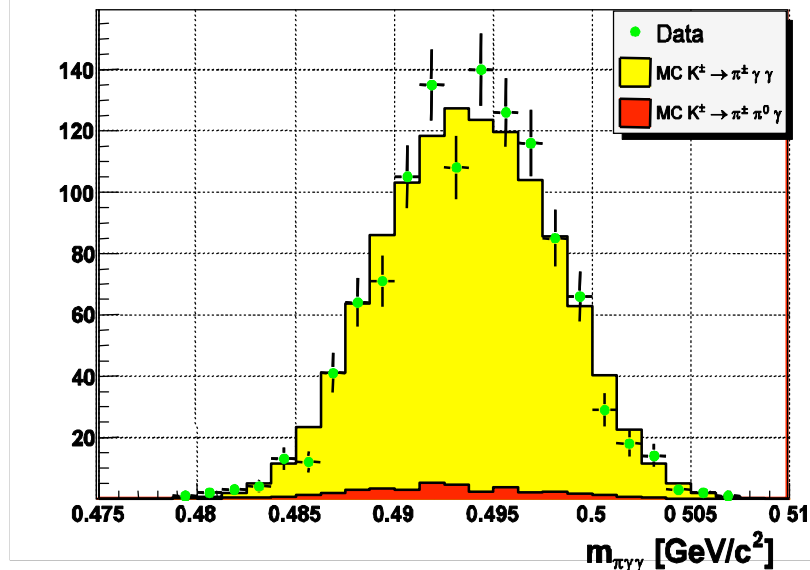
[G. D'Ambrosio and J. Portoles, Nucl., Phys. B386 (1996), 403]





# $K^\pm \rightarrow \pi^\pm \gamma\gamma$ data preliminary

NA48/2



**1164 events** in 40% of the full data  
**~40 times** larger wrt to world sample  
**3.3% BG** mainly from  $\pi\pi\gamma$ (IB)

The only previous measurement (E787),  
 based on 31 events (5 BG events)

$$BR = (1.10 \pm 0.32) \cdot 10^{-6} ; \hat{c} = 1.8 \pm 0.6$$

$$BR_{(O(p6), \hat{c}=2)} = (1.07 \pm 0.04_{\text{stat}} \pm 0.08_{\text{sys}}) \cdot 10^{-6}$$

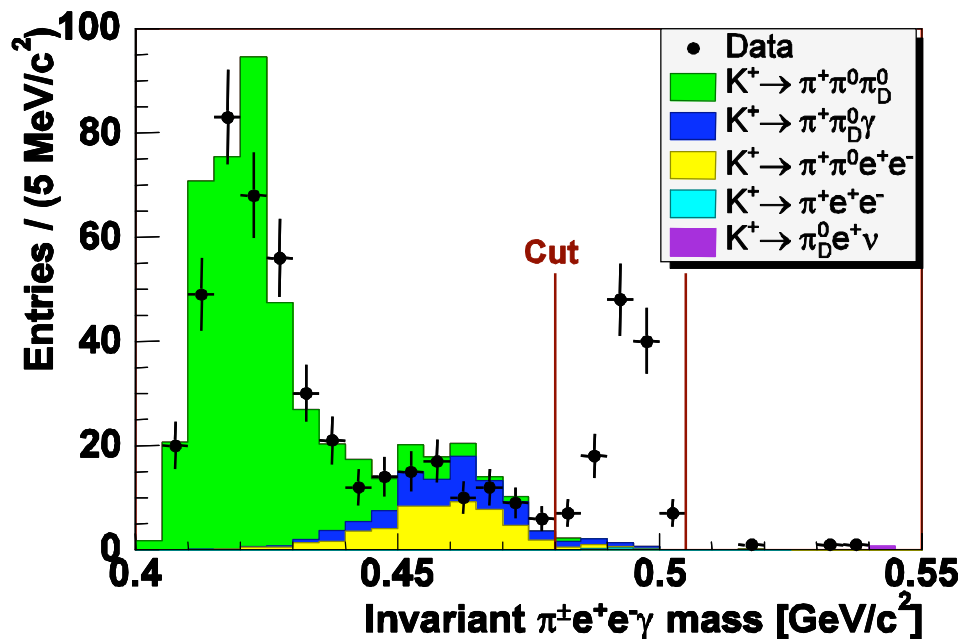
- MC  $O(p^6)$  and  $\hat{c}=2$  comparison data shape follows ChPT prediction
- Model independent measurement and extraction of  $\hat{c}$  is ongoing



# $K^\pm \rightarrow \pi^\pm e^+ e^- \gamma$ - first observation

NA48/2

120 candidate events (6.1% BG)

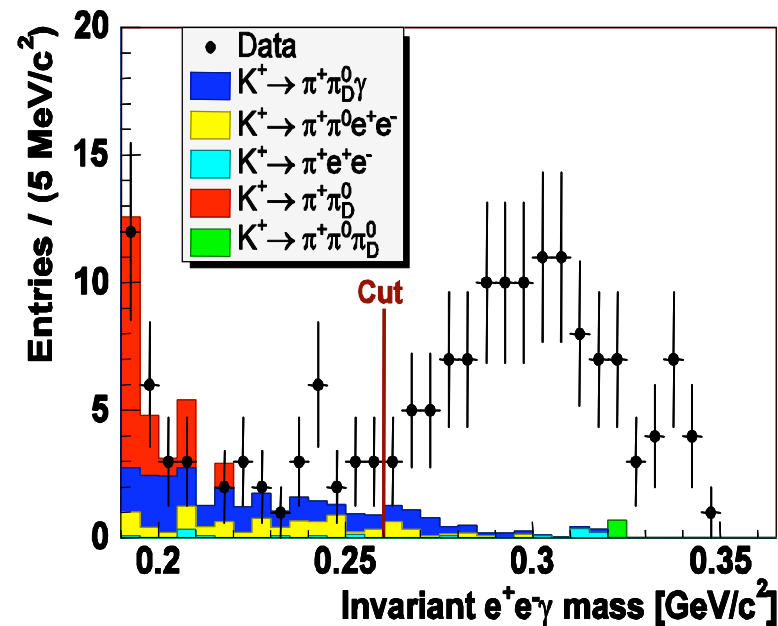


Model-independent BR ( $M_{\text{gee}} > 260 \text{ MeV}/c^2$ )

$$\text{BR}(\pi^\pm e^+ e^- \gamma) = (1.19 \pm 0.12_{\text{stat}} \pm 0.04_{\text{sys}}) \cdot 10^{-8}$$

[final result published, PLB659 (2008) 493]

never observed before!!



Shape analysis [ChPT  $O(p^6)$  model, F. Gabbiani, PRD59 (1999) 094022]:

$$\hat{c} = 0.90 \pm 0.45$$



## $K_L \rightarrow \pi^0 \gamma \gamma + K_L \rightarrow \pi^0 e e \gamma$ Theoretical Framework

KTeV

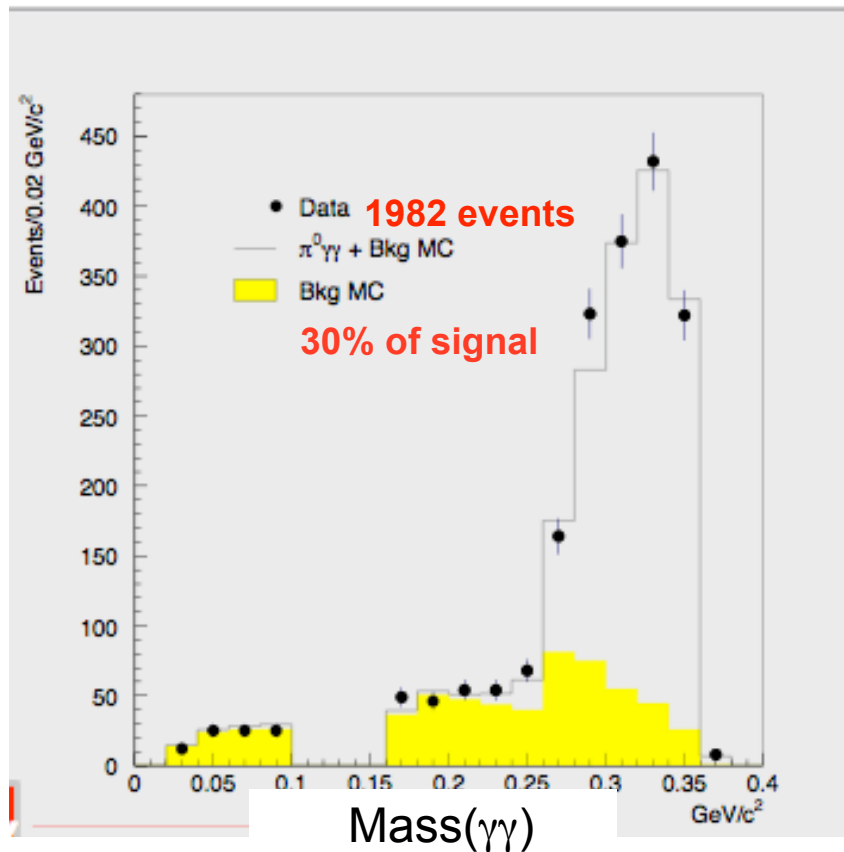
- Tests of ChPT
  - No free parameters in branching ratio to  $O(p^4)$
  - $O(p^6)$  terms include Vector Meson exchange terms  
(strength of which is described by  $A_V$ )
  - $O(p^6)$  terms increase branching ratios by factor of 2-3
- $A_V$  determines CP conserving part of  $K_L \rightarrow \pi^0 l^+ l^-$ 
  - CP conserving part is from  $K_L \rightarrow \pi^0 \gamma^* \gamma^*$
- Indirect CP violating part of  $K_L \rightarrow \pi^0 l^+ l^-$  determined by  $\text{Br}(K_S \rightarrow \pi^0 l^+ l^-)$



# $K_L \rightarrow \pi^0 \gamma \gamma$ Data

**KTeV**

Physical Review D77, No.11(June1, 2008)



- Selection requirements:
  - Require 4 photon clusters in CsI, each with an energy  $> 2.0$  GeV
  - Require energy center to be in vacuum beam hole in CsI
    - Rejects events from mixed  $K_L$ - $K_S$  regenerator beam
  - Two photons must reconstruct to within  $3 \text{ MeV}/c^2$  of the  $\pi^0$  mass, while the other two must not.
- Normalize with  $K_L \rightarrow \pi^0 \pi^0$ 
  - Same final state

**KTeV:  $\text{Br}(K_L \rightarrow \pi^0 \gamma \gamma) = (1.29 \pm 0.03_{\text{stat}} \pm 0.05_{\text{syst}}) \times 10^{-6}$**

**NA48:  $\text{Br}(K_L \rightarrow \pi^0 \gamma \gamma) = (1.36 \pm 0.03_{\text{stat}} \pm 0.03_{\text{syst}} \pm 0.03_{\text{norm}}) \times 10^{-6}$**



# $K_L \rightarrow \pi^0 e^+ e^- \gamma$ Data

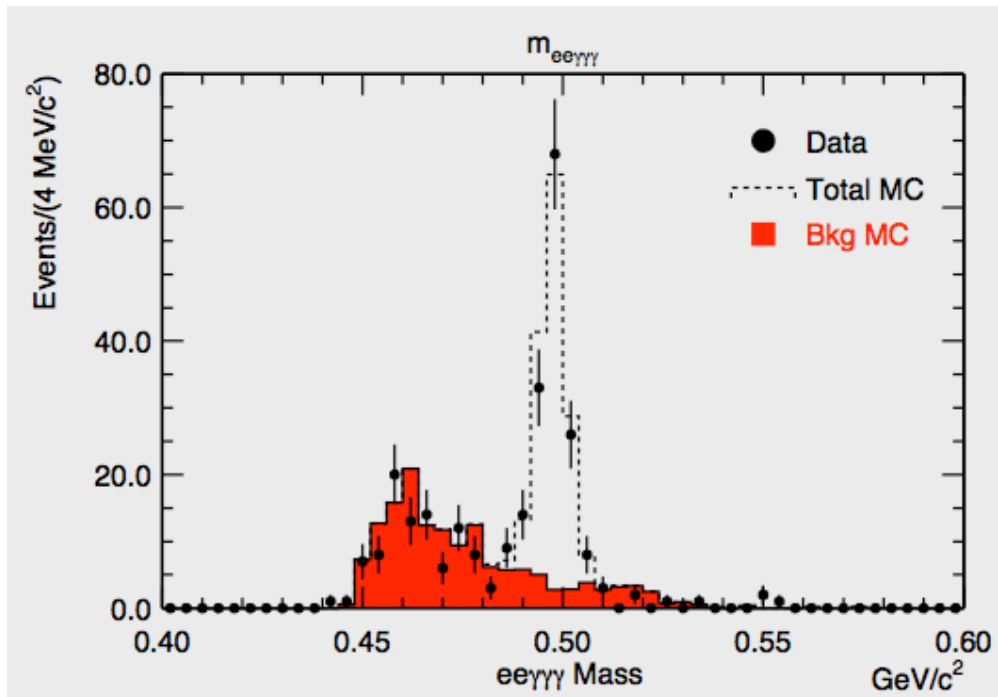
**KTeV**

139 events  
(Bkg: 14.4  $\pm$  2.5 events)

## Selection requirements...

- Require 2 tracks and 3 neutral CsI clusters
- Two neutral clusters must combine to an invariant mass near the  $\pi^0$  mass
- Neutral decay vertex used to compute:

- $M_{ee\gamma}, M_{ee\gamma\gamma}$
- Mass resolution with neutral vertex is better than charged vertex since  $e^+$  and  $e^-$  tracks are very close
- None of the 3 possible  $ee\gamma$  solutions reconstruct to a  $\pi^0$ .
- Normalize using  $K_L \rightarrow \pi^0 \pi^0_D$



$$\text{Br}(K_L \rightarrow \pi^0 e^+ e^- \gamma) = (1.62 \pm 0.14_{\text{stat}} \pm 0.09_{\text{syst}}) \times 10^{-8}$$

CHPT 0(p<sup>6</sup>) predicts  $1.51 \times 10^{-8}$



## Extracting $A_V$

KTeV

- $K_L \rightarrow \pi^0 \gamma \gamma$
- Maximum likelihood fit to the two Dalitz parameters:
  - $Z_{\text{Dalitz}} = m_{34}^2 / M_K^2$
  - $Y_{\text{Dalitz}} = (E_{\gamma 3} - E_{\gamma 4}) / M_K$
- $K_L \rightarrow \pi^0 e e \gamma$
- Maximum likelihood fit to the three Dalitz parameters:
  - $Z_{\text{Dalitz}} = M_{ee\gamma}^2 / M_K^2$
  - $Y_{\text{Dalitz}} = (E_{\gamma} - E_{ee}) / M_K$
  - $Q_{\text{Dalitz}} = M_{ee}^2 / M_K^2$

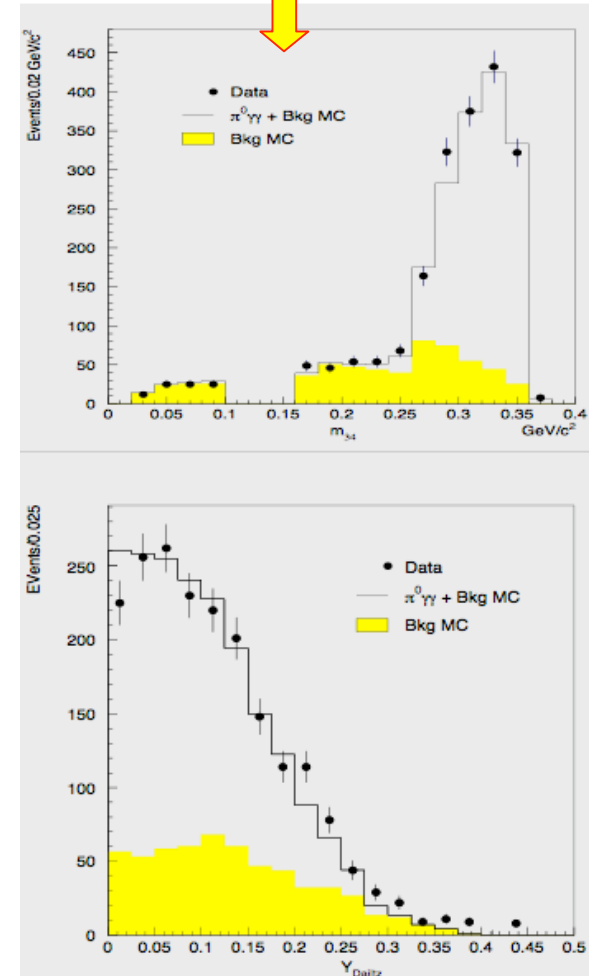
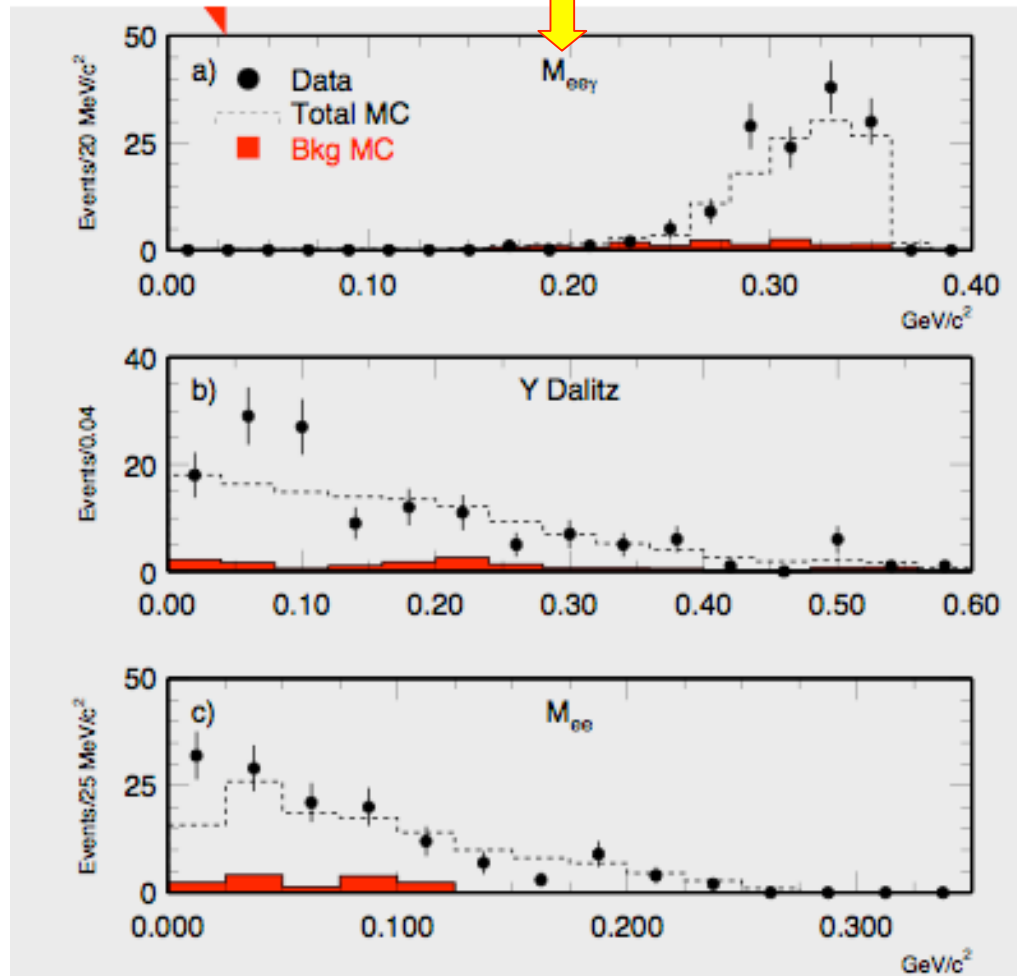


# Data + Best Fit

**KTeV**

$$K_L \rightarrow \pi^0 e e \gamma$$

$$K_L \rightarrow \pi^0 \gamma \gamma$$



6/27/08

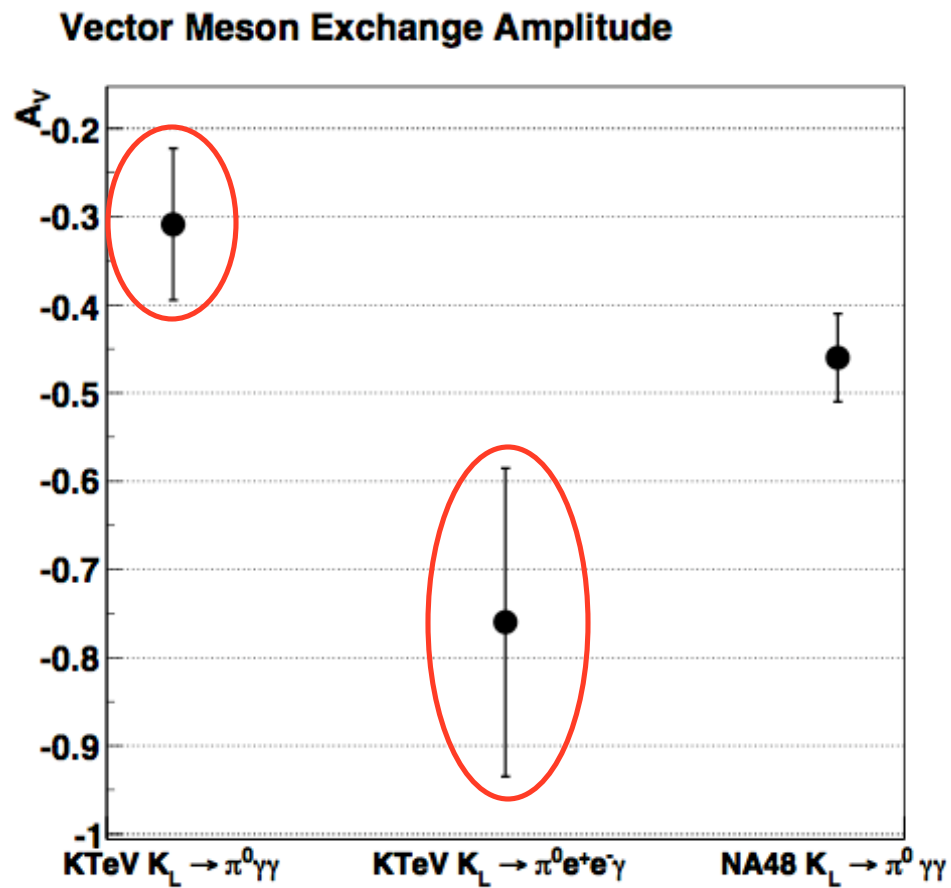
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## Results for $A_V$

KTeV



- Values imply that  $K_L \rightarrow \pi^0 l^+ l^-$  is indeed dominated by CPV terms





**KLOE**

**KLOE: Measurement of  $\text{BR}(K_S \rightarrow \gamma\gamma)$   
Search for  $K_S \rightarrow e^+e^-$   
Measurement of  $\text{BR}(K_L \rightarrow \pi e \nu \gamma)$**



## Motivation to study $K_S \rightarrow \gamma\gamma$

**KLOE**

- Important probe of ChPT
- Decay amplitude evaluated at leading order,  $O(p^4)$   
 $BR(K_S \rightarrow \gamma\gamma) = 2.1 \times 10^{-6}$   
D'Ambrosio and Espriu, Phys.Lett.B 175(1986) 237  
Kambor and Holstein, Phys.Rev.D 49(1994) 2346
- No full  $O(p^6)$  calculation exists
- Experimental value of the BR changed along the years,
  - improving in precision
- Most recent measurement by NA48/1  
 $BR(K_S \rightarrow \gamma\gamma) = (2.78 \pm 0.06 \pm 0.04) \times 10^{-6}$
- Differs from ChPT  $O(p^4)$  by 30% possible large  $O(p^6)$  contribution

In **NA48**, the  $K_L \rightarrow \gamma\gamma$  background is a relevant component of the fit

In **KLOE**, the background from  $K_L$  is reduced to zero (tagging)



# $K_S \rightarrow \gamma\gamma$ Analysis Strategy

**KLOE**

Main background  $\rightarrow K_S \rightarrow 2\pi^0$   
with 2 photons lost in the beam-pipe  
and/or colliding into QCAL

$\rightarrow$  veto these photons using  
a cut on arrival time

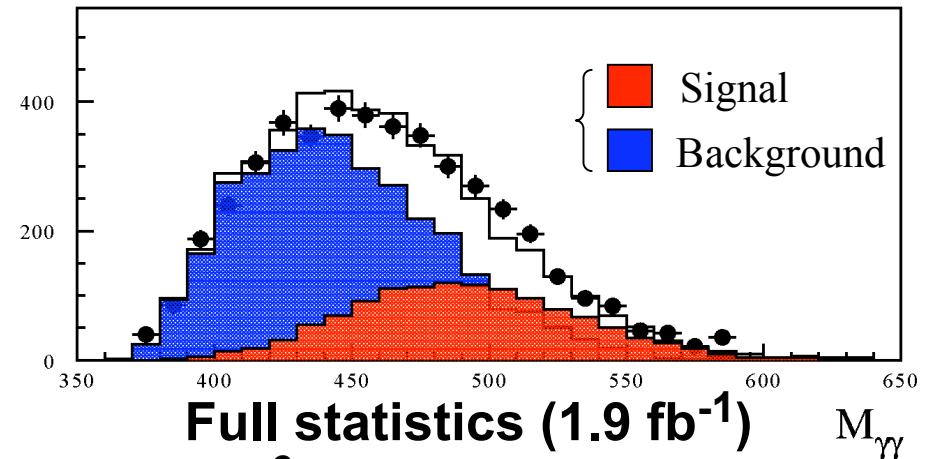
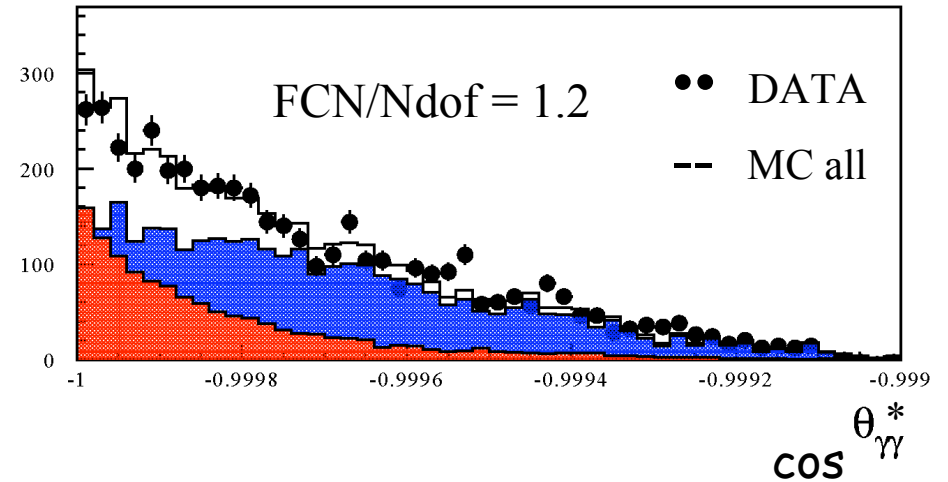
$$\Delta T = |T_{\text{QCAL}} - R_{\text{QCAL}}/c| < 5 \text{ ns}$$

$\rightarrow$  Background reduction to 70 %

Determine signal events by fitting  
 $M_{\gamma\gamma}$  and  $\cos \theta_{\gamma\gamma}^*$  in the  $K_S$  cms

$$N_{\text{sig}} = 711 \pm 35$$

(4.9% stat. error)



700 x 10<sup>6</sup>  $K_S$  events after  $K_L$  tag

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## Result: $\text{BR}(\text{K}_S \rightarrow \gamma\gamma)$

**KLOE**

now published: [JHEP05 (2008) 05]

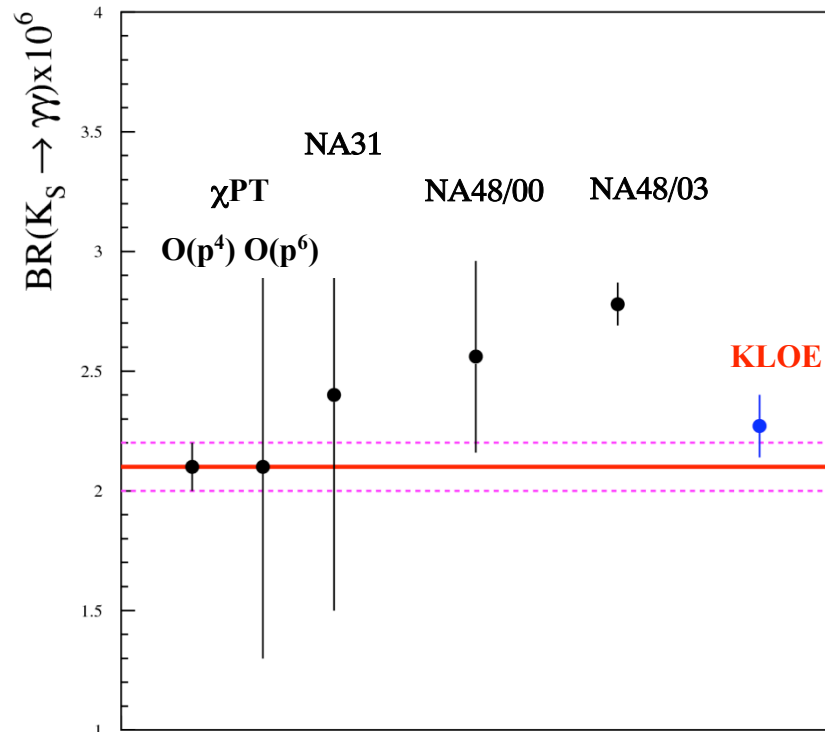
NA48 Coll., Phys. Lett. B551 (2003) 7

NA48 Coll., Phys. Lett. B493 (2000) 29

NA31 Coll., Phys. Lett. B351 (1995) 579

There is a  $3\sigma$  discrepancy between  
KLOE and NA48 results

- The **NA48** measurement implies the existence of a sizeable  $\text{O}(p^6)$  counterterm in ChPT
- The **KLOE** result makes this
- contribution practically negligible



$$\text{BR}(\text{K}_S \rightarrow \gamma\gamma) = (2.26 \pm 0.12_{\text{stat}} \pm 0.06_{\text{sys}}) \cdot 10^{-6}$$



## Search for FCNC in $K_S \rightarrow e^+e^-$

**KLOE**

Exotic mediators could produce  
tree level FCNC processes

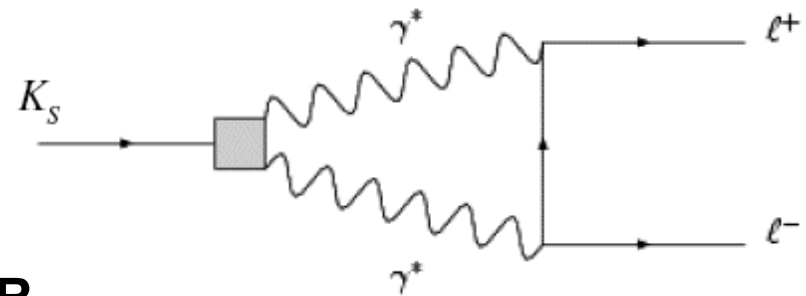
- Precise SM ChPT,  $O(p^4)$  prediction:

$$BR(K_S \rightarrow e^+e^-) = 1.6 \times 10^{-15}$$

[Ecker and Pich, Nucl. Phys. B366, 189, 1991]

- Most precise measurement by CPLEAR

$$BR(K_S \rightarrow e^+e^-) < 1.4 \times 10^{-7} \text{ (90\% C.L.)}$$



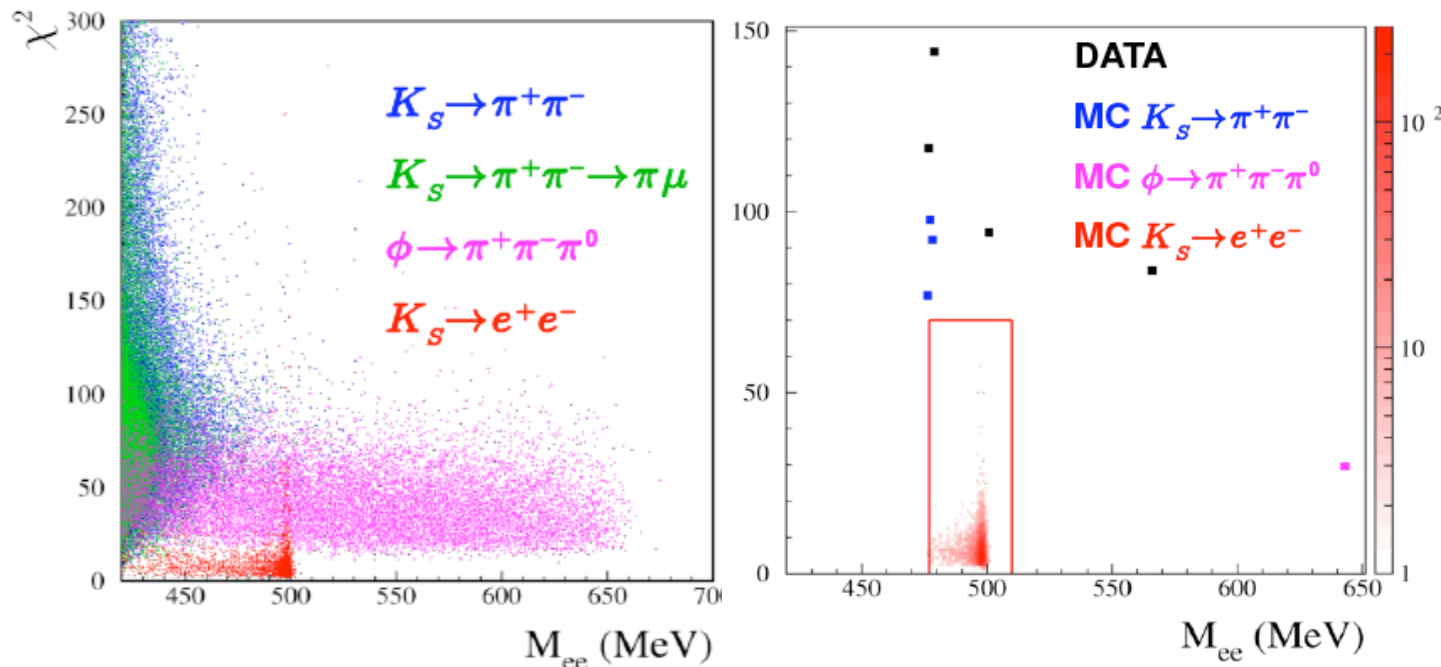
In KLOE è direct search of this decay using a pure  $K_S$  beam  
After preselection: 1.1 M evts in Data sample

- Signal identification using a  $\chi^2$  variable based on time of particles, E/p and cluster position
- Background rejection by kinematic cuts
- Signal box defined in the plane  $\chi^2$  vs  $M_{inv}$  ( $e^+e^-$  hypothesis))



## Result: Upper Limit for $K_S \rightarrow e^+e^-$

KLOE



**NO** events found in the signal box

Upper Limit evaluated normalizing to the number of  $K_S \rightarrow \pi^+\pi^-$  events

$$\text{BR}(K_S \rightarrow e^+e^-) < 9.3 \times 10^{-9} \text{ (90\% C.L.)}$$

Previous result improved by more than one order of magnitude



$K_L \rightarrow \pi e \nu \gamma$

**KLOE**

$$R \equiv \frac{\Gamma(K_{e3\gamma}^0; E_\gamma^* > 30 \text{ MeV}, \theta_\gamma^* > 20^\circ)}{\Gamma(K_{e3}^0)}$$

$$\frac{d\Gamma}{dE_\gamma^*} \simeq \frac{d\Gamma_{\text{IB}}}{dE_\gamma^*} + \langle X \rangle f(E_\gamma^*)$$

A 2-dimensional fit in  $(E_\gamma^*, \theta_\gamma^*)$   
allow to measure both  $R$  and  $\langle X \rangle$

$$R = (924 \pm 23 \pm 16) \times 10^{-5}$$

$$\langle X \rangle = -2.3 \pm 1.3 \pm 1.4$$

$$R = (944 \pm 14) \times 10^{-5}$$

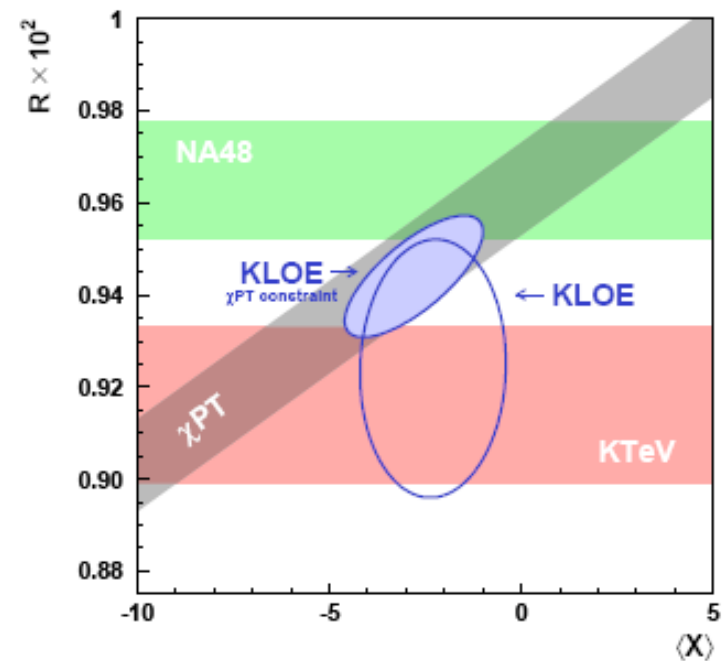
$$\langle X \rangle = -2.8 \pm 1.8$$

arXiv:0710.3993

With ChPT  
constraint

Largely dominated by IB, negligible DE  
Interference IB-DE small (1%)

→ test of ChPT  $O(p^6)$



NA48 Coll., Phys.Lett. B605 (2005) 247  
KTeV Coll., Phys. Rev. D71 (2005) 012001



## ChPT Summary

The **NA48/2**, **KLOE** and **KTeV** experiments have obtained important new experimental inputs to the Chiral Perturbation Theory, the effective theory of strong interaction at low energy

- **KTeV**                      neutral kaon sector
  - Precise study of  $K_L \rightarrow \pi^\pm \gamma \gamma$  decay (final)
  - Precise study of  $K_L \rightarrow \pi^\pm \gamma e^+ e^-$  decay (final)
- **NA48/2**                  charged kaon sector
  - Precise study of the  $K^\pm \rightarrow \pi^\pm e^+ e^-$  decay (preliminary)
  - Precise study of the  $K^\pm \rightarrow \pi^\pm \gamma \gamma$  decay (preliminary)
  - First observation of the  $K^\pm \rightarrow \pi^\pm \gamma e^+ e^-$  decay (final)
- **KLOE**                      neutral kaon sector
  - Measurement of  $K_S \rightarrow \gamma \gamma$  decay (final)
  - Upper limit for  $K_S \rightarrow e^+ e^-$  decay (final)
  - Measurement of decay (final)





## Conclusions

- No new physics evidence
- Final  $\varepsilon'/\varepsilon$  prime result from KTeV:  
(high precision; can someone calculate this?)
- No breaks in e, $\mu$  universality
- First row CKM unitarity is better and better satisfied
- Many new results bearing on ChPT
- Many more new results to come

**Do we have a flavor problem? Where are all these new particles?**

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