Physics in Collision 2008, Perugia

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## D<sup>0</sup> – D<sup>0</sup> Mixing an Overview

### Jörg Marks University of Heidelberg

for the



**BABAR** Collaboration

### Introduction

- Most unexpected physics result of last years spring conferences: Evidence for D<sup>0</sup> - D<sup>0</sup> Mixing from the Belle and BaBar Collaborations CDF II was able to present evidence end of the year 2007
- > Neutral meson mixing has been already observed in the K (1956), B (1987) and  $B_s$  (2006) systems
- > Why is  $D^0$  Mixing interesting ?
  - Processes with down type quarks are involved in the mixing loop
  - Within the Standard Model mixing and CP violation in the charm sector are expected to be small
  - Depending on the measured values of the parameters it could indicate new physics

 $\succ$  Present an overview of the mixing measurements of D<sup>0</sup> mesons



## Outline

### Charm mixing phenomenology

- ✤ Mixing
- Time evolution
- Processes
- Survey of recent results of D<sup>0</sup> mixing
  - Mixing parameters (and CP violation as related to mixing)
  - Experiments
    - BABAR, Belle, CLEO, CDF
  - Techniques

Time-dependence, lifetime differences, Dalitz plot analyses

Hadronic decays

Twobody and multibody decays, quantum correlated decays

### Summary



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## **Mixing Formalism**

Neutral D<sup>0</sup> mesons are created as flavor eigenstates of the strong interaction. They can mix through weak interactions.

The time evolution is obtained by

$$i\frac{\partial}{\partial t} \begin{pmatrix} D^0(t)\\ \bar{D}^0(t) \end{pmatrix} = (M - \frac{i}{2}\Gamma) \begin{pmatrix} D^0(t)\\ \bar{D}^0(t) \end{pmatrix}$$

 $\succ$  The physical eigenstates are D<sub>1</sub> and D<sub>2</sub>:

$$egin{aligned} |D_{1,2}
angle &= p |D^0
angle \mp q |ar{D}^0
angle & D_1: \ \mathsf{CP} \ \mathsf{ever} \ |D_{1,2}(t)
angle &= e^{-i(M_{1,2}-i\Gamma_{1,2}/2)t} |D_{1,2}(t=0)
angle & D_2: \ \mathsf{CP} \ \mathsf{odd} \end{aligned}$$

 $\succ$  Define mass and lifetime differences of D<sub>1</sub> and D<sub>2</sub>:

$$x = \frac{\Delta M}{\Gamma} = \frac{M_1 - M_2}{\Gamma} \qquad y = \frac{\Delta \Gamma}{2\Gamma} = \frac{\Gamma_1 - \Gamma_2}{2\Gamma}$$

$$|D^{0}\rangle \frac{\bar{u}}{c} \xrightarrow{\bar{c}} |\bar{D}^{0}\rangle$$

 $\Gamma = \frac{\Gamma_1 + \Gamma_2}{2}$ 

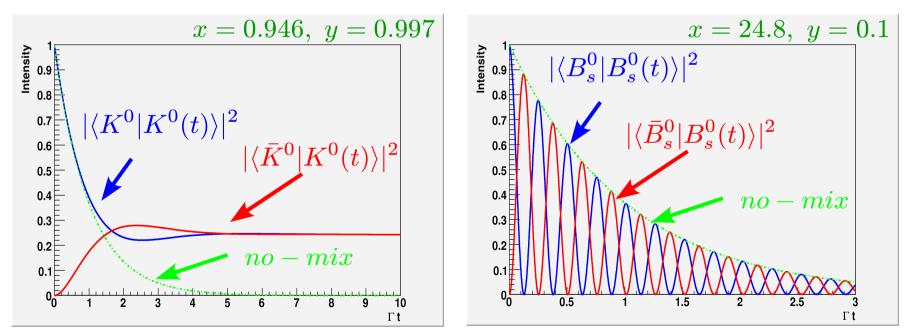
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### **Time Evolution and Mixing**

Mixing will occur if either x or y is non – zero. The time evolution of the probability to find a  $D^0(\overline{D}^0)$  after a time t is:

$$\begin{split} &I(D^{0} \to D^{0};t) \,:\, |\langle D^{0} | D^{0}(t) \rangle|^{2} = \frac{e^{-\Gamma t}}{2} [\cosh(y\Gamma t) + \cos(x\Gamma t)] \\ &I(D^{0} \to \bar{D}^{0};t) \,:\, |\langle \bar{D}^{0} | D^{0}(t) \rangle|^{2} = \frac{e^{-\Gamma t}}{2} [\cosh(y\Gamma t) - \cos(x\Gamma t)] |\frac{p}{q}|^{2} \end{split}$$





## **Charm Mixing Processes**

The box diagram contributions to charm mixing in the Standard Model are expected to be very small

♦ Lowest order short distance calculation:  $x_{box} \cong O(10^{-5})$   $y_{box} \cong O(10^{-7})$ ♦ x and y enhancement due to higher orders in OPE:  $x \sim y \cong O(10^{-3})$ 

Long distance contributions dominate
Numerical predictions lack in precision  $D^0 - \bar{D}^0 - \bar{D}^0$   $x \cong O(10^{-2})$   $y \cong O(10^{-2})$ 

### New Physics

- \* E.Golowich et al.: arXiv:0705.3650 Which new physics model can yield sizeable values for x and y
- CP violation in charm is small in SM Measurement of CPV: New Physics



# Mixing in $D^0 \to K\pi$ - Flavor Tagging

### Flavor tagging at production time

Standard technique in charm physics: use

$$Q = m(D^{0}\pi^{+}) - m(D^{0}) - m(\pi^{+}) \approx 6MeV$$

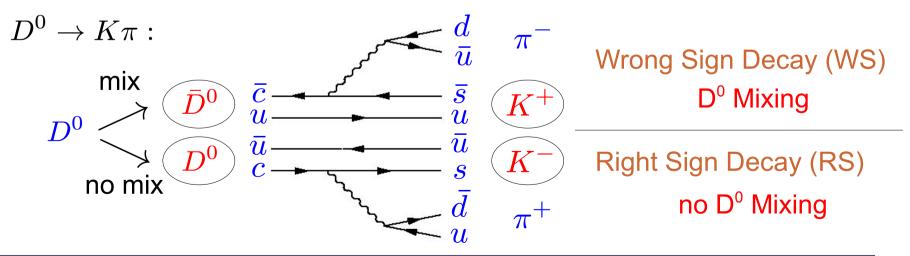
$$D^{*+} \begin{cases} c & c \\ \bar{d} & \bar{u} \\ \bar{d} & \bar{d} \end{cases} \pi^{+}$$

• Narrow peak in  $\Delta m = m(D^0\pi^+) - m(D^0)$  due to a small Q

- \* Select events around the expected  $\Delta m$  with good background suppression
- \* The charge of the low energy  $\pi$  determines the flavor of the D<sup>0</sup>

### Flavor at decay time

Use final state particle properties to tag the D<sup>0</sup> flavor at the decay time



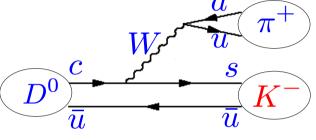


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## **Doubly Cabbibo Suppressed Decays**

The flavor tagging at decay time does not uniquely identify Mixing in hadronic D<sup>0</sup> decays

```
Cabibbo favored (CF)
decay
R \approx 1
```





Doubly Cabibbo suppressed (DCS) decay  $R_D \approx 0.3\%$ 

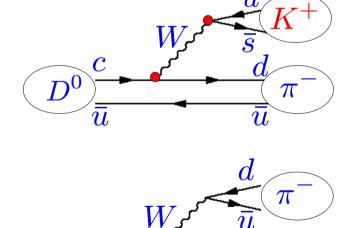
Mixed CF decay $R_Mpprox 0.006\%$ 

 $D^{\hat{0}}$ 

mixing

 $\hat{D}^{\hat{0}}$ 

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WS decays

Interference between DCS and mixed CF decay



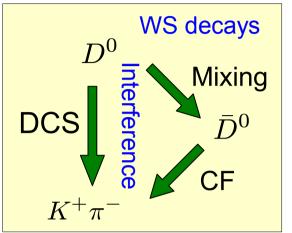
 $K^+$ 

# Time Evolution in $D^0 \to K\pi$ Decays



- DCS: exponential time distribution
- mixed decays occur with a time structure
- Time evolution of the WS decay rate

assume CP conservation and  $|x| \ll 1$  ;  $|y| \ll 1$ 



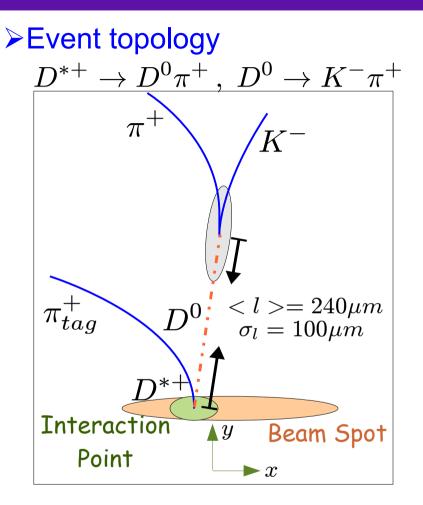
$$T_{WS}(t) \propto e^{-\Gamma t} \left( \underbrace{R_D}_{\text{D}} + \underbrace{\sqrt{R_D} y' \Gamma t}_{\text{DCS}} + \underbrace{\frac{x'^2 + y'^2}{4} (\Gamma t)^2}_{\text{Mixing}} \right) \int_{t} = \frac{x'^2 + y'^2}{2} = R_M$$
  
> Strong phase  $\delta_{\text{K}\pi}$ 

$$\begin{aligned} x' &= x \cos \delta_{K\pi} + y \sin \delta_{K\pi} \\ y' &= -x \sin \delta_{K\pi} + y \cos \delta_{K\pi} \end{aligned} \qquad y'^2 + x'^2 = x^2 + y^2 \end{aligned}$$

 $\delta_{K\pi}$  is the strong phase between CF and DCS amplitudes (  $D^0 \rightarrow K\pi$  ) phase may differ between decay modes phase may vary over phase space for multibody decays

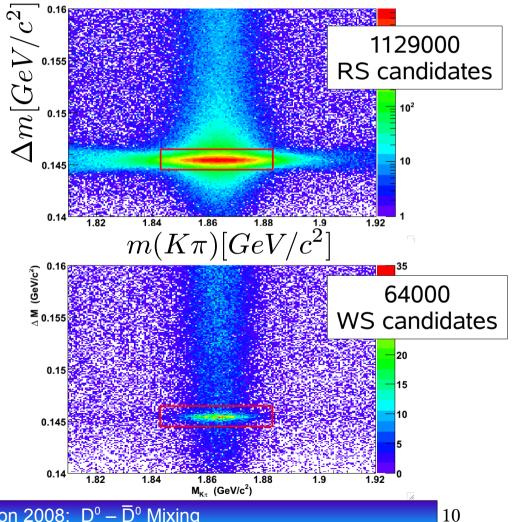


## **BABAR** – $D^0 \rightarrow K\pi$ Event Selection



Beam spot constraint vertex fit to  $\pi_{tag}, D^0$  provides  $t(D^0)$  and  $\sigma_t(D^0)$ 

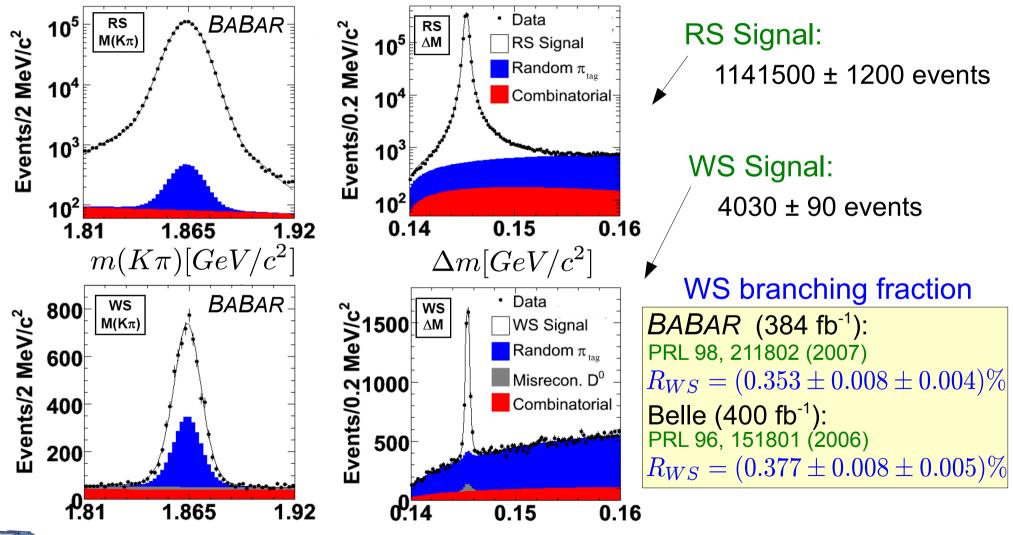
> $D^0$  selection (PID, m(K $\pi$ ), large P\*(D<sup>0</sup>)) >  $\pi^+_{tag}$  selection ( $\Delta$ m, small P\*( $\pi_{tag}$ ))





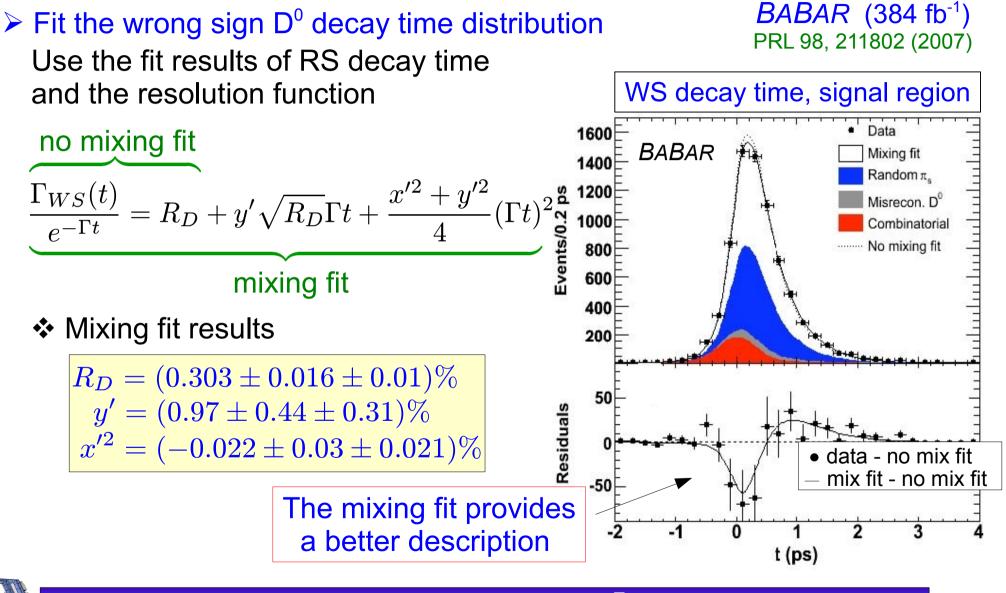
## $D^0 \rightarrow K\pi - WS$ Branching Fraction

### Determine Signal and background PDF's by unbinned maximum likelihood fit





## $D^0 \rightarrow K\pi - WS$ Decay Time Fit





Physics in Collision 2008:  $D^0 - \overline{D}^0$  Mixing

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# D<sup>0</sup> Mixing Fit - Likelihood Contours

Significance is computed from change in log likelihood The contours include systematic errors

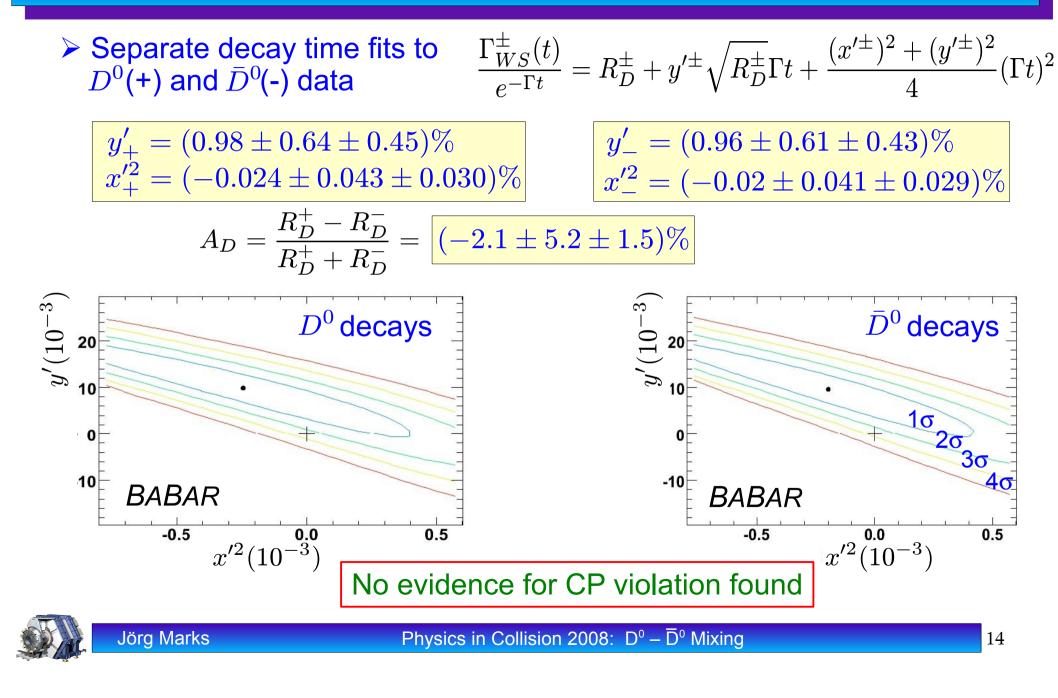
Best fit is in non physical 30 region BABAR Best fit with  $x'^2 > 0$  has 20  $-2\Delta \ln \mathcal{L} = 0.7$ 01 <sup>3</sup> 0 ζ / 10<sup>3</sup> Statistical errors only °10 Best fit to no mixing has 2σ 0  $-2\Delta \ln \mathcal{L} = 23.9 (4.5\sigma)$ <u>3</u>σ Best fit 4σ Best fit  $x'^2 > 0$ -10 0 Fit is inconsistent with 5σ No mixing no mixing at 3.9  $\sigma$ -20 -0.5 -1.0 0.0 0.5 1.0  $x^{\prime 2} / 10^{-3}$ Evidence for  $D^0 - \overline{D}^0$  Mixing



**BABAR** (384 fb<sup>-1</sup>)

PRL 98, 211802 (2007)

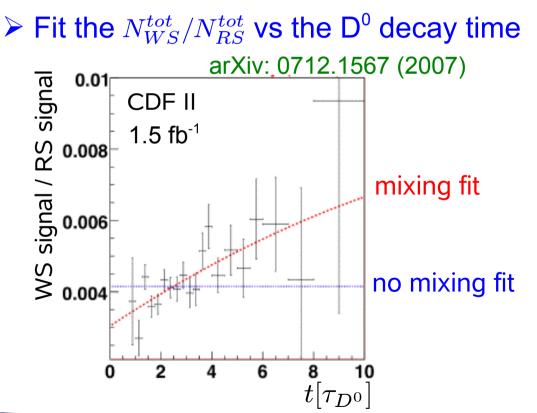
## $D^0 \rightarrow K\pi$ – Fit Results CP Violation



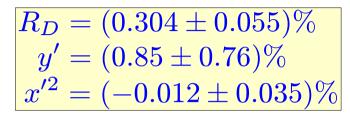
## **CDF II** – **D**<sup>0</sup> Mixing in $D^0 \to K\pi$

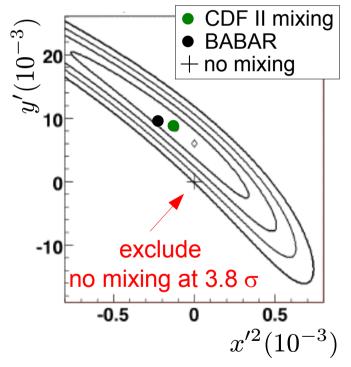
Measure the Number of WS and RS D<sup>0</sup> decays in bins of the decay time

$$N_{RS}^{tot} = (3.044 \pm 0.0023) \cdot 10^6$$
  
 $N_{WS}^{tot} = (12.7 \pm 0.3) \cdot 10^3$ 



### Mixing Parameter



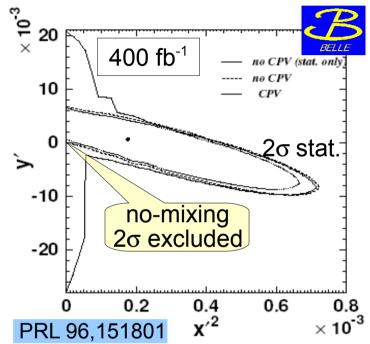


Very good agreement with BABAR



## $D^0 \rightarrow K\pi$ Results: *BABAR* Belle CDF



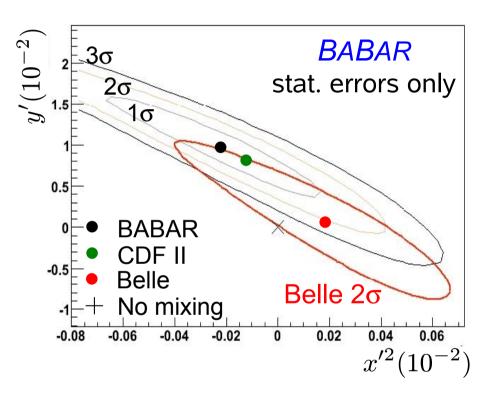


$$R_D = (0.364 \pm 0.017)\%$$
  

$$y' = (0.06^{+0.40}_{-0.39})\%$$
  

$$x'^2 = (0.018^{+0.021}_{-0.23})\%$$

 $\succ$  Compare  $D^0 \rightarrow K\pi$  results



All 3 mixing parameter measurements agree at the  $2\sigma$  level



## First Measurement of $\delta_{K\pi}$ by CLEO-c

### Motivation

- $\clubsuit$  Need  $\delta_{\text{K}\pi}$  to compare the measurements of y and y'
- $\delta = -\delta_{\mathrm{K}\pi} \text{ is defined as the phase of the K}\pi \text{ DCS to CF amplitude}$  arXiv: 0802.2264 ratio  $\frac{|\langle K^+\pi^-|D^0\rangle}{|\langle K^+\pi^-|\bar{D}^0\rangle} = re^{-i\delta} \quad \text{with} \quad r \approx 0.06$  (sub. to PRL)
- ➢ Determination of the strong phase in quantum correlated  $D^0 \overline{D}^0$  pairs  $e^+e^- \rightarrow \psi(3770) \rightarrow \gamma^* \rightarrow D^0 \overline{D}^0 \qquad \Rightarrow C = -1$ 
  - Measure time integrated yields of correlated and uncorrelated D<sup>0</sup> decays
  - \* The ratio of correlated and uncorrelated D<sup>0</sup> decay rates depends on the mixing parameters and  $\delta_{K\pi}$

 $\rightarrow\,$  Extract x²,y, r² and cos(  $\delta_{K\pi})$  from time integrated yields

External branching fraction are used and including external mixing parameter measurements improves the 
δ<sub>Kπ</sub> extraction



CLEO-c

## Results of the $\delta_{K\pi}$ Measurement

> Extract the strong phase  $\delta_{K\pi}$  in a fit to 281pb<sup>-1</sup> of CLEO-c data (external branching fraction measurements are used)  $x \sin(\delta_{K\pi})$  can not be determined in this fit, therefore set  $x \sin(\delta_{K\pi}) = 0$ 

 $cos(\delta_{K\pi}): 1.03^{+0.31}_{-0.17} \pm 0.06$ 

### Including in addition external measurements of mixing parameters improves the fit.

 $x \sin(\delta_{K\pi})$  can now be determined

$$cos(\delta_{K\pi}): \qquad 1.10 \pm 0.35 \pm 0.07$$
  
x sin( $\delta_{K\pi}$ ): (4.4<sup>+2.7</sup><sub>-1.8</sub> ± 0.29) · 10<sup>-3</sup>  
 $\delta_{K\pi}: \qquad (22^{+11+9}_{-12-11})^{\circ}$ 

#### external input parameters

Parameter	Average
y	$0.00662 \pm 0.00211$
x	$0.00811 \pm 0.00334$
$r^2$	$0.00339 \pm 0.00012$
y'	$0.0034 \pm 0.0030$
$x^{\prime 2}$	$0.00006 \pm 0.00018$

Established a new technique using time independent measurements of mixing parameters and the strong phase.



## Measurement of y<sub>CP</sub> - Introduction

 $\succ$  Decay time of D<sup>0</sup>'s is exponential with modifications due to mixing

 $\tau^{\pm} = \frac{\tau^{0}}{1 + |q/p|(y\cos\phi_{f} \mp x\sin\phi_{f})} \qquad \tau^{\pm}: \text{ lifetime of } \mathsf{D}^{0} \ (\overline{\mathsf{D}}^{0}) \to \mathsf{CP+ eigenstates} \\ \tau^{0}: \text{ lifetime of } \mathsf{D}^{0} \to \mathsf{CP} \text{ mixed (CF)}$ 

A lifetime difference between CP+ and CP mixed states gives access to mixing

$$y_{CP} = \frac{\tau^{0}}{\tau} - 1 \quad \text{or} \quad y_{CP} = \frac{\tau(K^{-}\pi^{+})}{\tau(K^{-}K^{+})} - 1 = \frac{\tau(K^{-}\pi^{+})}{\tau(\pi^{-}\pi^{+})} - 1$$
$$y_{CP} \neq 0 \quad \Rightarrow \ \mathsf{D}^{0} - \overline{\mathsf{D}}^{0} \text{ mixing}$$

Test of CP violation

$$\Delta Y = \frac{\tau^0 A_\tau}{\tau} \qquad \text{with} \qquad A_\tau = \frac{\tau^+ - \tau^-}{\tau^+ + \tau^-} = -A_\Gamma$$

 $\begin{array}{ll} \Delta Y \neq 0 & \Rightarrow & \begin{array}{l} \mathsf{CP} \text{ violation in } \mathsf{D}^0 \cdot \overline{\mathsf{D}}^0 \text{ mixing} \\ \\ \mathsf{CP} \text{ violation in interf. between mixing and decay} \\ y_{CP} = y & \begin{array}{l} \text{in the limit of } \mathsf{CP} \text{ conservation} \end{array} \end{array}$ 



## Belle - Results for y<sub>CP</sub>

 $\begin{array}{c} \succ \text{ Lifetime ratio measurements of CP+ and} \\ \text{ CP mixed D}^0 \text{ decays by BELLE} \\ \text{ provide evidence for D}^0 \text{ -}\overline{D}^0 \text{ mixing } \end{array} \right. \begin{array}{c} \overset{\text{Channe}}{\overset{\overset{\text{Channe}}{\overset{\overset{\text{Channe}}{\overset{\overset{\text{Channe}}{\overset{\overset{\text{Channe}}{\overset{\overset{\overset{\tilde{}$ 

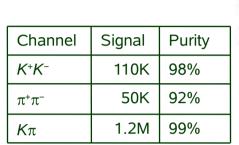
 $y_{CP} = (13.1 \pm 3.2 \pm 2.5) \cdot 10^{-3}$ 

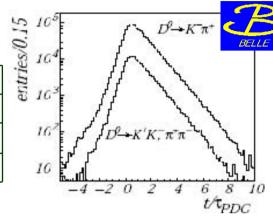
> Evidence for  $D^0 - \overline{D}^0$  Mixing

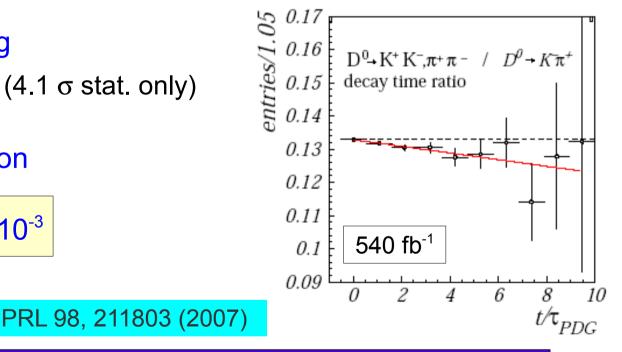
\* exclude no-mixing at 3.2  $\sigma$  (4.1  $\sigma$  stat. only)

➢ No Evidence for CP violation

 $A_{\Gamma} = (0.01 \pm 0.3 \pm 0.15) \cdot 10^{-3}$ 







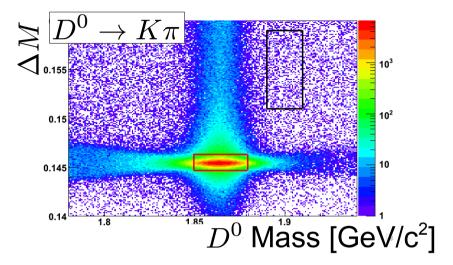


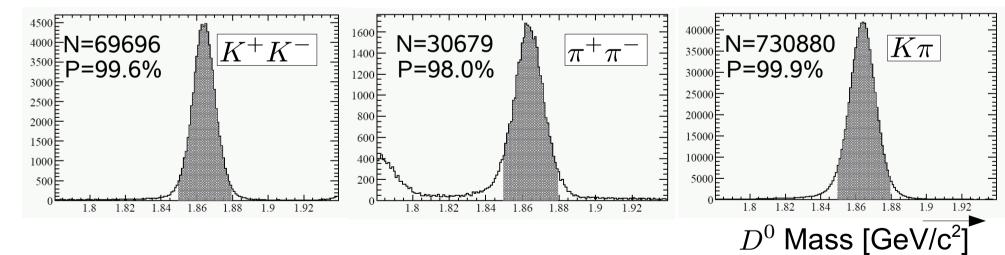
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## **BABAR - Lifetime Measurements (1)**

### Event selection from 384 fb<sup>-1</sup>

- ♦ Require  $D^{*+} → D^0 π_s^+$  tag identify  $D^0$  flavour by π<sub>s</sub> charge
- Clean signal samples with high purity P

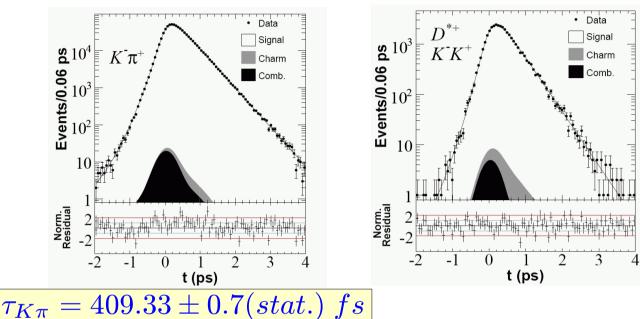


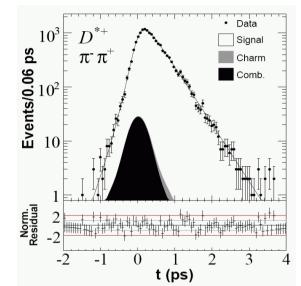




# **BABAR - Lifetime Measurements (2)**

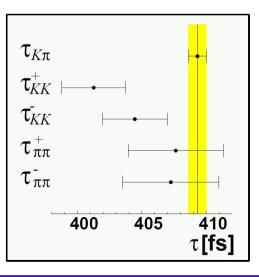
### Determine D<sup>0</sup> lifetimes from unbinned max. likelihood fit to all 5 samples





### Summary of the lifetime measurements

- Most of the measurement systematics of the signal cancel in the ratio
- Systematics of the backgrounds to the different modes do not cancel





## **BABAR - Results for y<sub>CP</sub>**

> Determine  $y_{CP}$  and  $\Delta Y$  from  $\tau_{K\pi}$ ,  $\tau_{K^+K^-}^{\pm}$ ,  $\tau_{\pi^+\pi^-}^{\pm}$  measurements

Tagged D <sup>0</sup>	arXiv: 0712.2249 (sub. to PRD-RC)		
	$y_{CP}$	$\Delta Y$	
$K^-K^+$	$(1.60\pm0.46\pm0.17)\%$	$(-0.40 \pm 0.44 \pm 0.14)$	.)%
$\pi^{-}\pi^{+}$	$(0.46\pm 0.65\pm 0.25)\%$	$(0.05 \pm 0.64 \pm 0.32)$	2)%
<b>combined</b>	$(1.24\pm0.39\pm0.13)\%$	$(-0.26 \pm 0.36 \pm 0.08)$	s)%

- Evidence for  $D^0 \overline{D}^0$  Mixing at the 3  $\sigma$  level
- No CP violation found

 $y_{CP} = (1.03 \pm 0.33 \pm 0.19)\%$ 

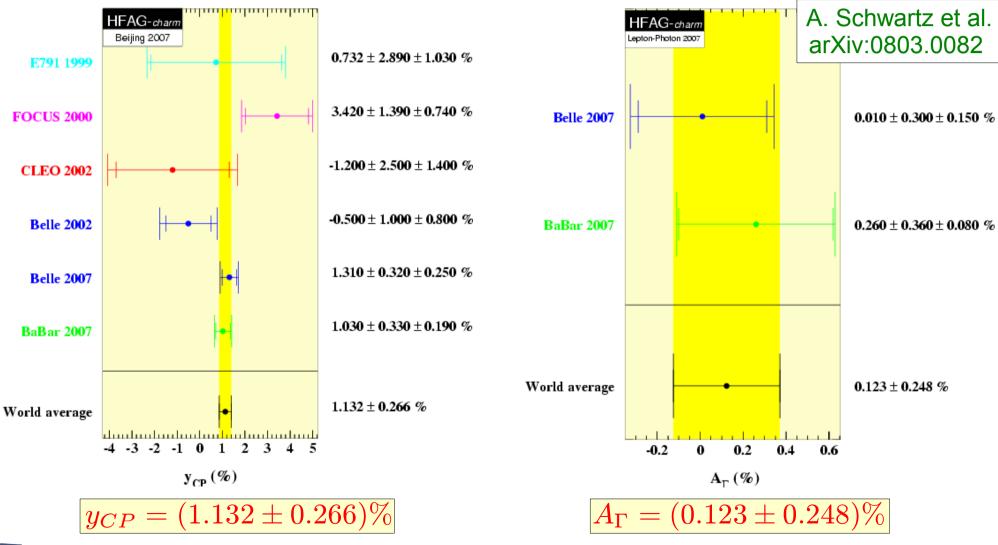
> Combined results with an untagged  $D^0$  sample (91 fb<sup>-1</sup>)

PRL 91, 221801 (2003)



### Experimental Results - y<sub>CP</sub>

### 





# Belle – t Dependent Dalitz Analysis (1)

### $\blacktriangleright$ Dalitz plot of $D^0 \to K^0_s \pi^+ \pi^-$

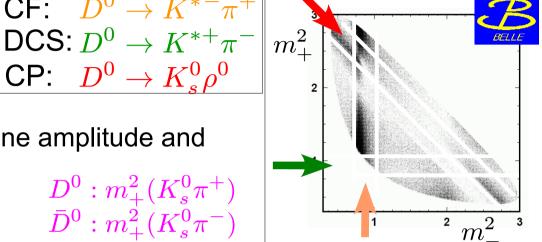
- Different quasi 2 body amplitudes contribute and interfere
- Dalitz analysis allows to determine relative phases of 18 modes  $D^{0}: m_{+}^{2}(K_{s}^{0}\pi^{+})$   $= \frac{1}{2} \underbrace{A(m_{-}^{2}, m_{+}^{2})}_{\langle f | \bar{D}^{0} \rangle} [e^{-i (\lambda)t} + e^{-i (\lambda)t}]$   $+ \frac{1}{2} \frac{q}{p} \bar{A}(m_{-}^{2}, m_{+}^{2}) [e^{-i (\lambda)t} + e^{-i (\lambda)t}]$
- Time dependence

$$\langle K_s^0 \pi^+ \pi^- | D^0(t) \rangle =$$

decay amplitude

CP: 
$$D^0 \rightarrow K^0_s \rho^0$$
  
rmine amplitude and

CF:  $D^0 \rightarrow K^{*-}\pi^+$ 



$$\lambda_{1,2} = f(x,y)$$

The decay rates contain functions of x and y

 $\blacktriangleright$  Perform unbinned max. likelihood fit in the signal region to  $(m_{\perp}^2, m_{\perp}^2, t)$ 

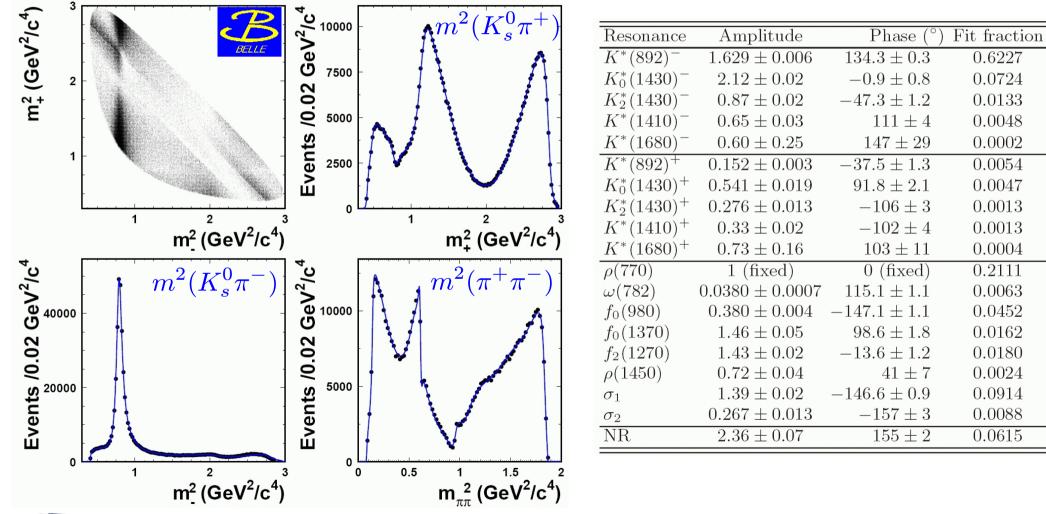
 $\Rightarrow$  extract relative amplitudes and relative phases

 $\Rightarrow$  x, y and  $\tau_{D^0}$ 



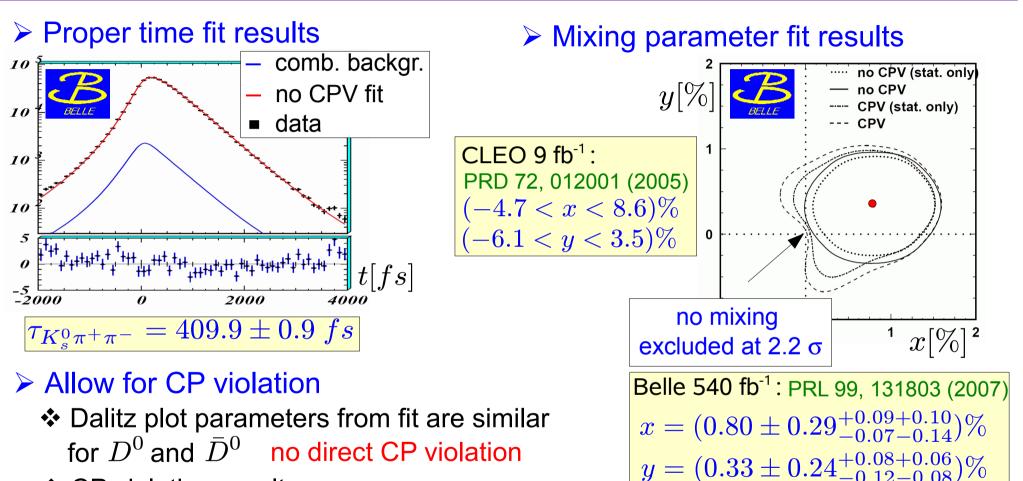
# Belle – t Dependent Dalitz Analysis (2)

### Select 534410 ± 830 events in the signal region with 95 % purity in 540 fb<sup>-1</sup>





## Belle – t Dep. Dalitz Analysis Results



✤ CP violation results :

$$|q/p| = 0.86^{+0.30+0.06}_{-0.29-0.03} \pm 0.08$$
  
arg (q/p)[°] = -14^{+16+5+2}\_{-18-3-4}

no CP violation



**BABAR** – 
$$D^0 \rightarrow K^+ \pi^- \pi^0$$
 Dalitz Analysis

### Analyse time dependence of Wrong Sign events in quasi 2 body decays

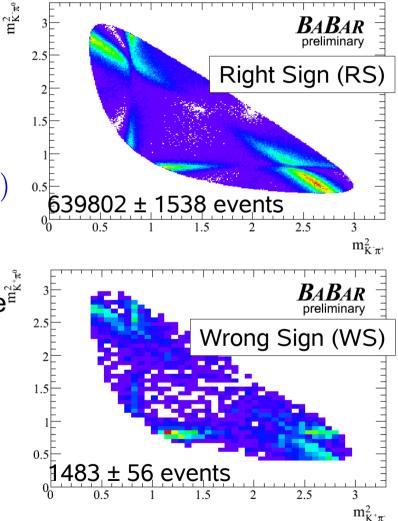
- \* 2 types of WS decays (as in  $D^0 \rightarrow K\pi$ )
  - DCS:  $D^0 \to K^+ \pi^- \pi^0$
  - Mixing followed by CF decay: mixing  $D^0 \to \bar{D}^0 \to K^+ \pi^- \pi^0$
  - Interference:

$$\Gamma_{K\pi\pi^{0}} = f(m_{K\pi}^{2}, m_{K\pi^{0}}^{2}, t, x, y, \delta)$$

- Determine DCS and CF Dalitz amplitudes and phases in a fit
- Extract x and y from a fit to the time dependence of the relative WS decay rate:

$$y'' = y \cos(\delta_{K\pi\pi^0}) - x \sin(\delta_{K\pi\pi^0})$$
$$x'' = x \cos(\delta_{K\pi\pi^0}) + y \sin(\delta_{K\pi\pi^0})$$

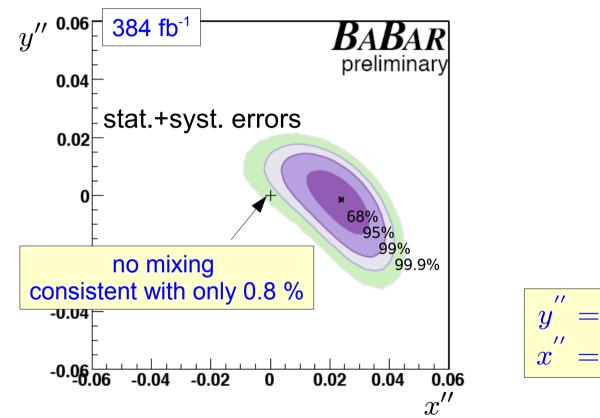
 $\delta_{K\pi\pi^0}$  : strong phase difference (  $eq \delta_{K\pi}$  )





**BABAR** – 
$$D^0 \rightarrow K^+ \pi^- \pi^0$$
 Results

### Mixing parameter fit results



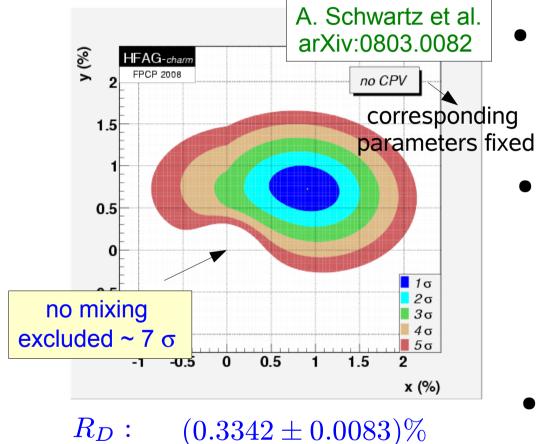
$$y^{''}_{} = (-0.14 \pm 0.60 \pm 0.40)\% \ x^{''}_{} = (2.39 \pm 0.61 \pm 0.32)\%$$



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## D<sup>o</sup> Mixing - Combined Results

### World average mixing parameters are provided by the HFAG charm group



- $\delta:$   $0.36 \pm 0.20 \ rad$
- $\delta_{K\pi\pi^0}: \ 0.55 \pm 0.45 \ rad$

• Experimental data indicates  $D^0 \rightarrow \bar{D}^0$ mixing  $y = (0.73 \pm 0.18)\%$ 

 $x = (0.91 \pm 0.26)\%$ 

• y measured from D<sup>0</sup> lifetime differences

 $y_{CP} = (1.132 \pm 0.266)\% > 0$ 

$$au(|D_1
angle) < au(|D_2
angle)$$
  
CP even state CP odd state

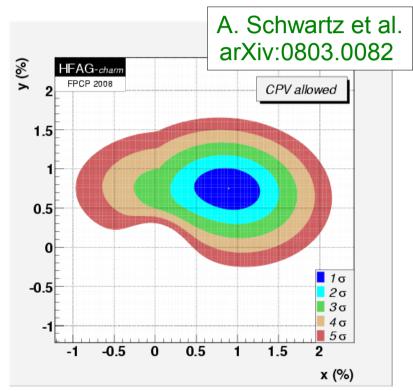
• x determined from  $D^0 \to K^0_s \pi^+ \pi^$ x > 0

 $M_1(\ket{D_1}) \; > \; M_2(\ket{D_2})$ 

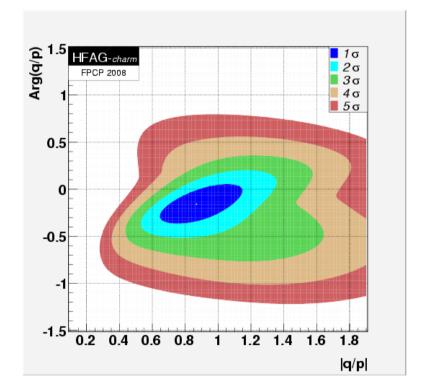
# D<sup>0</sup> Mixing & CPV - Combined Results

### Global fit of mixing parameters allowing for CP violation

Parameters are almost identical to the CP conserving case



 $A_D = (-2.0 \pm 2.5) \%$  $|q/p| = 0.87 \pm 0.17$  $\phi = (-0.16 \pm 0.14) \, rad$ 

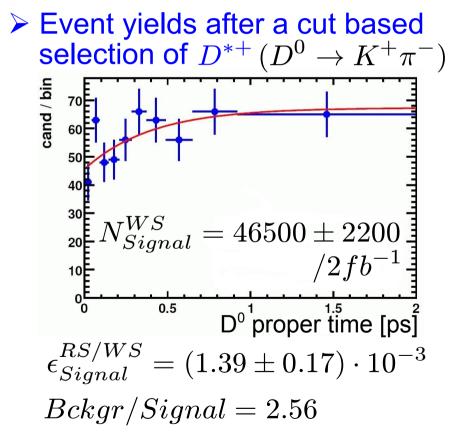


Consistent with no CP violation

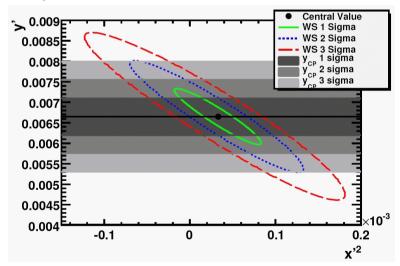


# Towards D<sup>0</sup> Mixing at LHCb

- $\succ$  MC study of D<sup>0</sup> Mixing in  $D^{*+} \rightarrow \pi_s^+ D^0(K^+\pi^-, K^+K^-, \pi^+\pi^-)$ 
  - Full detector simulation including trigger of minimum bias
     bb and signal events
     Encode bigher level trigger stream for D\*
  - Special higher level trigger stream for D\*



Extract y<sub>CP</sub> and (x'<sup>2</sup>, y') from toy MC Statistical error by a factor 5 smaller compared to BABAR



Signal extraction, systematic errors and .... a lot more to be done



### Summary

- Experimental Evidence of D<sup>0</sup> Mixing from 3 Experiments
- Measured values of the mixing parameters x ≈ y ≈ 1% are compatible with Standard Model
- > World averages of the mixing parameters exclude No D<sup>0</sup> Mixing at  $\sim 7\sigma$
- > No Evidence for CP Violation in D<sup>0</sup> Mixing

Looking forward seeing new and updated results on D<sup>0</sup> Mixing at the summer conferences



