

# B-anomalies related to leptons and LFV: new directions in model building

May 10<sup>th</sup> 2018

BEAUTY 2018  
La Biodola, Isola d' Elba

Ferruccio Feruglio  
Universita' di Padova

Based on:

- F.F., P. Paradisi and A. Pattori 1606.00524 and 1705.00929 [FPP]
- C. Cornella, F.F., P. Paradisi, 1803.00945

# Hints of violation of LFU in semileptonic B decays

## NC $b \rightarrow s$ [1-loop in SM]

[LHCb, 1705.05802  
SM at 2.4-2.5 $\sigma$ ]

$$R_{K^*}^{\mu/e} = \frac{\mathcal{B}(B \rightarrow K^* \mu \bar{\mu})_{\text{exp}}}{\mathcal{B}(B \rightarrow K^* e \bar{e})_{\text{exp}}} \bigg|_{q^2 \in [1.1, 6] \text{ GeV}} = 0.69 \pm_{-0.07}^{+0.11} (\text{stat}) \pm 0.05 (\text{syst})$$

$$R_K^{\mu/e} = \frac{\mathcal{B}(B \rightarrow K \mu \bar{\mu})_{\text{exp}}}{\mathcal{B}(B \rightarrow K e \bar{e})_{\text{exp}}} \bigg|_{q^2 \in [1, 6] \text{ GeV}} = 0.745_{-0.074}^{+0.090} \pm 0.036 ,$$

[LHCb, 1406.6482  
SM at 2.6 $\sigma$ ]

- allowing NP, global fits to  $b \rightarrow s$  transitions are consistent.
- solutions have a pull  $\sim 4$ -5 $\sigma$  w.r.t. the SM and prefer NP in muon channel.

## CC $b \rightarrow c$ [tree-level in SM]

[P.Owen, F. Simonetto]

$$R_{D^*}^{\tau/\ell} = \frac{\mathcal{B}(B \rightarrow D^* \tau \bar{\nu})_{\text{exp}} / \mathcal{B}(B \rightarrow D^* \tau \bar{\nu})_{\text{SM}}}{\mathcal{B}(B \rightarrow D^* \ell \bar{\nu})_{\text{exp}} / \mathcal{B}(B \rightarrow D^* \ell \bar{\nu})_{\text{SM}}} = 1.23 \pm 0.07 ,$$

$$R_D^{\tau/\ell} = \frac{\mathcal{B}(B \rightarrow D \tau \bar{\nu})_{\text{exp}} / \mathcal{B}(B \rightarrow D \tau \bar{\nu})_{\text{SM}}}{\mathcal{B}(B \rightarrow D \ell \bar{\nu})_{\text{exp}} / \mathcal{B}(B \rightarrow D \ell \bar{\nu})_{\text{SM}}} = 1.34 \pm 0.17 ,$$

[HFAG averages  
of Babar, Belle and  
LHCb, 1612.07233  
SM at 3.9 $\sigma$ ]

- theoretical uncertainties largely drop in these ratios and  $R \approx 1$  is expected

[Bordone, Isidori, Pattori, 1605.07633]

$$R_{J/\Psi}^{\text{exp}} = \frac{\mathcal{B}(B_c \rightarrow J/\Psi \tau \bar{\nu})}{\mathcal{B}(B_c \rightarrow J/\Psi \ell \bar{\nu})} = 0.71(17)(18)$$

[LHCb 2017]

# general context and implications

in the SM [ $m_\nu = 0$  and  $U_{PMNS} = 1$  in this talk]

1. no (measurable) LFV in charged lepton transitions
2. LFUV controlled by  $m_e$ ,  $m_\mu$ ,  $m_\tau$

1. Very well verified, e.g.

$\text{BR}(\mu^+ \rightarrow e^+ \gamma)$	$4.2 \times 10^{-13}$	[MEG]
$\text{BR}(\mu^+ \rightarrow e^+ e^+ e^-)$	$1.0 \times 10^{-12}$	[SINDRUM]



$$\Lambda > 10^5 \text{ TeV}$$

$$\Lambda > 10^2 \text{ TeV}$$

2. Well verified in a large energy range, at per mille level

leptonic tau/muon decays  $E \approx 1 \text{ GeV}$

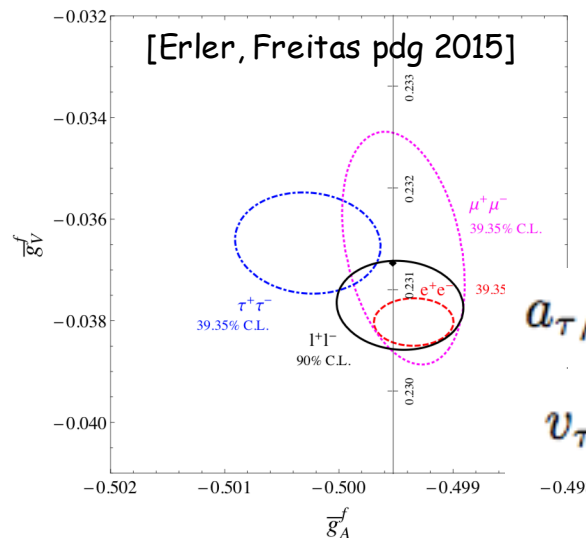
Z couplings to charged leptons  $E \approx 100 \text{ GeV}$

$$R_\tau^{\tau/e} = 1.0060 \pm 0.0030$$

$$R_\tau^{\tau/\mu} = 1.0022 \pm 0.0030$$

but also in many leptonic and semileptonic light pseudoscalar decays

[A.Pich, 1310.7922]



$$a_\tau/a_e = 1.0019 (15)$$

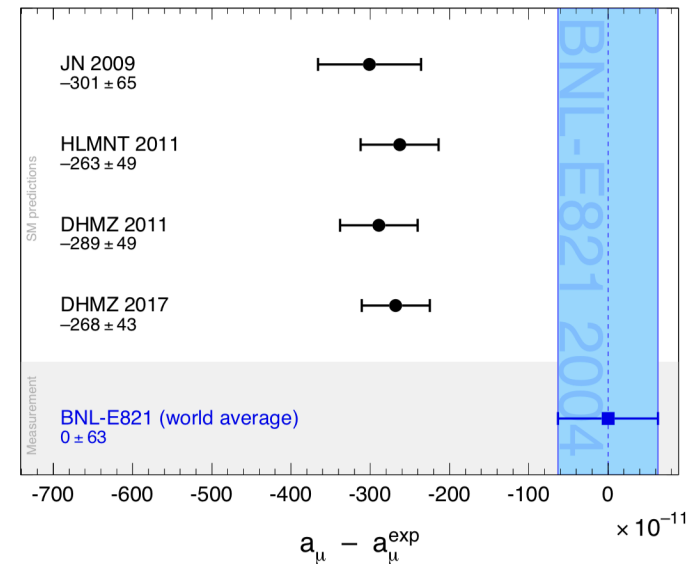
$$v_\tau/v_e = 0.959 (29)$$



the muon ( $g-2$ ):  
a long-standing exception ?

[waiting to be confirm by  
Fermilab Muon ( $g-2$ )]

[Hoecker, Marciano, pdg 2017]



any violations  
of 1. and/or 2.  $\rightarrow$  physics  
beyond the SM

LFV in charged leptons and LFUV are  
closely related in most SM extensions,  
though this is not a strict rule.

back to  $R_{D,D^*}$   $R_{K,K^*}$

can they be made compatible with the existing tests of LFV and LFUV?

any specific LFV/LFUV process to especially monitor?

we need a concrete framework to answer that. Here

- define a benchmark scenario

- discuss deviations from the benchmark

# Benchmark framework: assumptions

1. NP above the electroweak scale

$$\mathcal{L}^{NP} = \frac{1}{\Lambda^2} \sum_i C_i O_i + \dots,$$

$$L_{NP}^0(\Lambda)$$

0  $m_\tau m_b$   $m_W \approx m_Z \approx m_H \approx m_t$   $\Lambda$  Energy

2. NP mainly affects the third generation

couplings to lighter generations  
[e.g. muons, c-quark, ....]



misalignment between mass  
and interaction bases

6 sub-leading operators

$$\mathcal{L}_{NP}^0(\Lambda) = \frac{1}{\Lambda^2} (C_1 \bar{q}'_{3L} \gamma^\mu q'_{3L} \bar{\ell}'_{3L} \gamma_\mu \ell'_{3L} + C_3 \bar{q}'_{3L} \gamma^\mu \tau^a q'_{3L} \bar{\ell}'_{3L} \gamma_\mu \tau^a \ell'_{3L}) + \dots$$

(V-A) pattern in NC  
supported by global fits

not the only possibility:

- V lepton current ( $O_9$  operator) by itself provides a good fit
- right quark helicities disfavored after  $R_{K^*}$  measurement
- scalar operators are constrained by B leptonic decays-
- tensor operator at  $\Lambda$  gives rise to scalar operators at low-scale

Hiller and Schmaltz 1408.1627;

Altmannshofer, Stangl and Straub, 1704.05435;

Celis, Fuentes Martin, Vicente and Virto, 1704.05672;

Capdevila, Crivellin, Descotes-Genon, Matias and Virto, 1704.05340;

D'Amico, Nardecchia, Panci, Sannino, Strumia, Torre and Urbano, 1704.05438;

Ciuchini, Coutinho, Fedele, Franco, Paul, Silvestrini and Valli 1704.05447;

G. Hiller and I. Nisandzic, 1704.05444 [hep-ph].

# Benchmark framework: assumptions

1. NP above the electroweak scale

$$\mathcal{L}^{NP} = \frac{1}{\Lambda^2} \sum_i C_i O_i + \dots,$$

$$L_{NP}^0(\Lambda)$$

0  $m_\tau m_b$   $m_W \approx m_Z \approx m_H \approx m_t$   $\Lambda$  Energy

2. NP mainly affects the third generation

couplings to lighter generations  
[e.g. muons, c-quark, ....]



misalignment between mass  
and interaction bases

6 sub-leading operators

$$L_{NP}^0(\Lambda) = \frac{1}{\Lambda^2} (C_1 \bar{q}'_{3L} \gamma^\mu q'_{3L} \bar{\ell}'_{3L} \gamma_\mu \ell'_{3L} + C_3 \bar{q}'_{3L} \gamma^\mu \tau^a q'_{3L} \bar{\ell}'_{3L} \gamma_\mu \tau^a \ell'_{3L}) + \dots$$

(V-A) pattern in NC  
supported by global fits



$g_{VL}$

Olcyr Sumensari



$C_9^{NP} = -C_{10}^{NP}$

Nazila Mahmoudi

not the only possibility:

- V lepton current ( $O_9$  operator) by itself provides a good fit
- right quark helicities disfavored after  $R_{K^*}$  measurement
- scalar operators are constrained by B leptonic decays-
- tensor operator at  $\Lambda$  gives rise to scalar operators at low-scale



# $\mathcal{L}_{NP}^0(\Lambda)$ can address both NC and CC anomalies

$$\mathcal{L}_{NP}^0(\Lambda) = \frac{\lambda_{kl}^e}{\Lambda^2} [(C_1 + C_3) \lambda_{ij}^u \bar{u}_{Li} \gamma^\mu u_{Lj} \bar{\nu}_{Lk} \gamma_\mu \nu_{Ll} + (C_1 - C_3) \lambda_{ij}^u \bar{u}_{Li} \gamma^\mu u_{Lj} \bar{e}_{Lk} \gamma_\mu e_{Ll} + (C_1 - C_3) \lambda_{ij}^d \bar{d}_{Li} \gamma^\mu d_{Lj} \bar{\nu}_{Lk} \gamma_\mu \nu_{Ll} + (C_1 + C_3) \lambda_{ij}^d \bar{d}_{Li} \gamma^\mu d_{Lj} \bar{e}_{Lk} \gamma_\mu e_{Ll} + 2C_3 (\lambda_{ij}^{ud} \bar{u}_{Li} \gamma^\mu d_{Lj} \bar{e}_{Lk} \gamma_\mu \nu_{Ll} + h.c.)] .$$

mixing among generation  
encoded in matrices  $\lambda^{e,d,u}$

$$\lambda^u = V_{CKM}^+ \lambda^d V_{CKM}$$

$$\lambda^{d,e} \approx \begin{pmatrix} 0 & 0 & 0 \\ 0 & \vartheta_{d,e}^2 & \vartheta_{d,e} \\ 0 & \vartheta_{d,e} & 1 \end{pmatrix}$$

[Calibbi, Crivellin, Ota, 1506.02661]

4 parameters

$$\frac{C_1}{\Lambda^2}, \frac{C_3}{\Lambda^2}, \vartheta_d, \vartheta_e$$

$-\vartheta_d$

both  $R_{K^{(*)}}$  and  $R_{D^{(*)}}$  can be explained

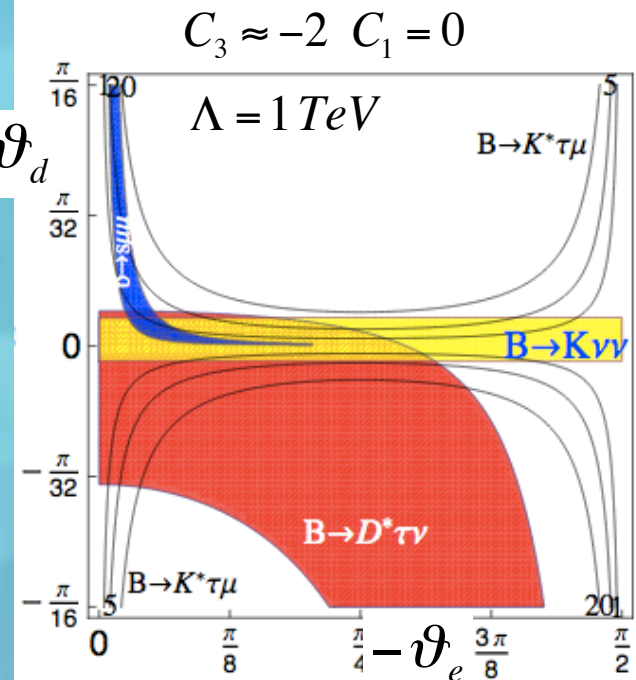
$$\Lambda \approx 1 \text{ TeV}$$

$$C_3, C_1 = O(1)$$

$$\vartheta_d = O(0.01) \approx V_{cb}$$

$$\vartheta_e = O(0.3) \approx U_{ij}^{PMNS}$$

$(\vartheta_d \times \vartheta_e^2)$  provides the  
needed suppression of  
 $R_{K^{(*)}}$  compared to  $R_{D^{(*)}}$



# Constraints (tree-level)

$R_K^{\mu/e} \quad R_{K^*}^{\mu/e}$	$(C_1 + C_3) \vartheta_d \vartheta_e^2$		
$R_D^{\tau/\ell} \quad R_{D^*}^{\tau/\ell}$	$C_3$		
process	parameters	size	exp. bound
$R_{B_s \mu \mu} = \frac{\mathcal{B}(B_s \rightarrow \mu \bar{\mu})_{\text{exp}}}{\mathcal{B}(B_s \rightarrow \mu \bar{\mu})_{\text{SM}}}$	$(C_1 + C_3) \vartheta_d \vartheta_e^2$	$O(0.1)$	$\mathcal{B}(B_s \rightarrow \mu \bar{\mu})_{\text{exp}} = 2.8_{-0.6}^{+0.7} \times 10^{-9}$ $\mathcal{B}(B_s \rightarrow \mu \bar{\mu})_{\text{SM}} = 3.65(23) \times 10^{-9}$
$R_{B\tau\nu}^{\tau/\mu} = \frac{\mathcal{B}(B \rightarrow \tau \nu)_{\text{exp}} / \mathcal{B}(B \rightarrow \tau \nu)_{\text{SM}}}{\mathcal{B}(B \rightarrow \mu \nu)_{\text{exp}} / \mathcal{B}(B \rightarrow \mu \nu)_{\text{SM}}}$	$C_3$	$O(0.1)$	Belle II ?
$R_{K^{(*)}}^{\nu\nu} = \frac{\mathcal{B}(B \rightarrow K^{(*)} \nu \bar{\nu})}{\mathcal{B}(B \rightarrow K^{(*)} \nu \bar{\nu})_{\text{SM}}}$	$(C_1 - C_3) \vartheta_d$	$O(1)$	$R_{K^*}^{\nu\nu} < 4.4 \quad R_K^{\nu\nu} < 4.3$
$\mathcal{B}(B \rightarrow K \tau \mu)$ $\mathcal{B}(B \rightarrow \tau^\pm \mu^\mp) \approx \mathcal{B}(B \rightarrow K \tau^\pm \mu^\mp),$ $\mathcal{B}(B \rightarrow K^* \tau^\pm \mu^\mp) \approx 2 \times \mathcal{B}(B \rightarrow K \tau^\pm \mu^\mp)$	[Glashow, Guadagnoli, Lane 1411.0565] $ (C_1 + C_3) \vartheta_d \vartheta_e ^2$	$O(10^{-6 \div 7})$	$\mathcal{B}(B \rightarrow K \tau \mu) \leq 4.8 \times 10^{-5}$
$\mu^+ \mu^-$ and $\tau^+ \tau^-$ Production at LHC	$(C_1 + C_3)$		[Greljo, Marzocca 1704.09015] Admir Greljo talk



$$L_{NP}(m_b) = L_{NP}^0(\Lambda) + \text{quantum corrections}$$

How can quantum corrections  $\sim \alpha/4\pi \sim 10^{-3}$  be relevant?



they generate terms that are absent in  $L_{NP}^0(\Lambda)$  and new processes are affected

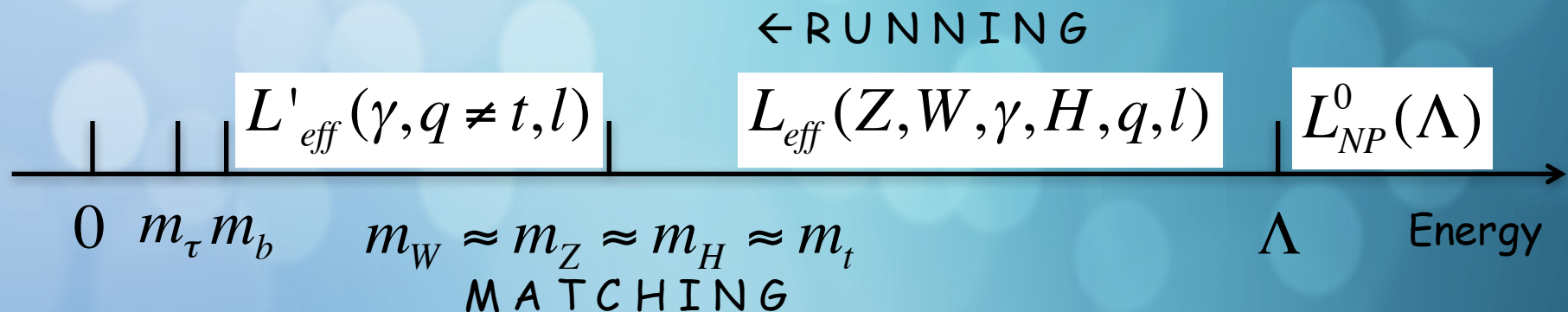


their order of magnitude is similar to accuracy in EWPT and in other tests of LFU

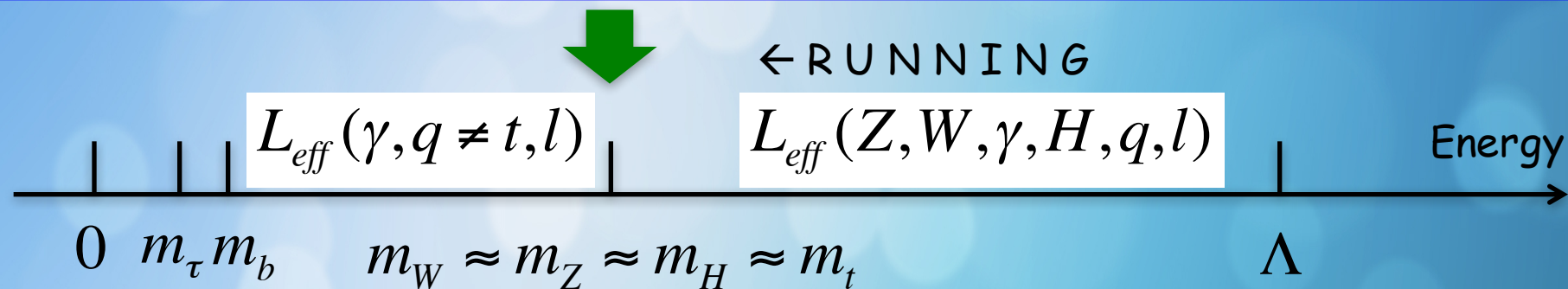


they are enhanced by logs:  $\log(\Lambda^2/m_W^2) \sim 5-7$

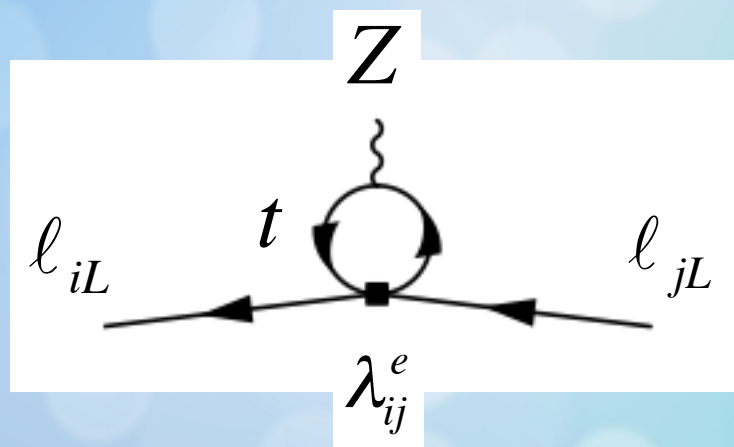
in the present framework - (V-A) semileptonic operators - corrections are dominated by electroweak interactions. They can be estimated by a well-known running and matching procedure. Here, Leading Log effects only



# 1<sup>st</sup>: the electroweak scale



## 1. modifications of the W,Z couplings to fermions by non-universal terms



$$\frac{a_\tau}{a_e} \approx 1 - 0.004 \frac{(C_1 - 0.8 C_3)}{\Lambda^2(\text{TeV}^2)}$$

$$\frac{v_\tau}{v_e} \approx 1 - 0.05 \frac{(C_1 - 0.8 C_3)}{\Lambda^2(\text{TeV}^2)}$$

$$a_\tau/a_e = 1.0019 \text{ (15)}$$

$$v_\tau/v_e = 0.959 \text{ (29)}$$

$$N_\nu \approx 3 + 0.008 \frac{(C_1 + 0.8 C_3)}{\Lambda^2(\text{TeV}^2)}$$

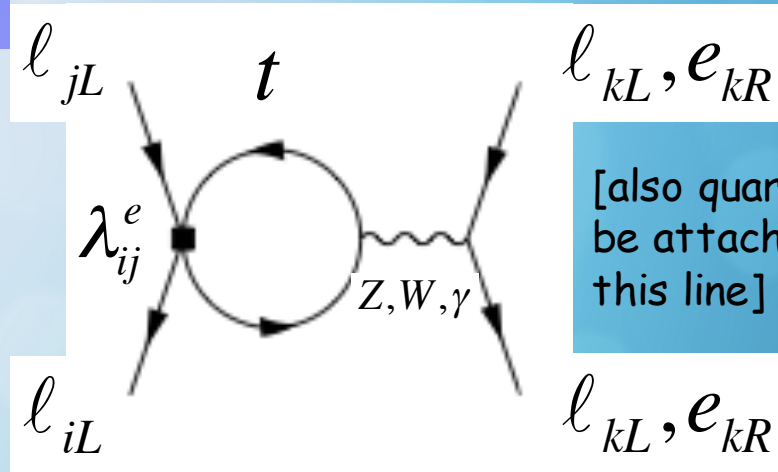
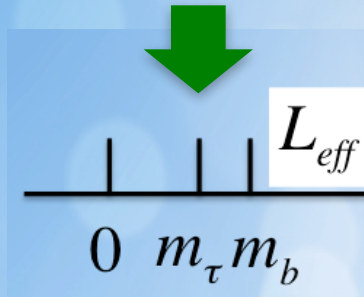
$$N_\nu = 2.9840 \pm 0.0082$$

$$\mathcal{B}(Z \rightarrow \mu^\pm \tau^\mp) \approx 10^{-7}$$

$$\mathcal{B}(Z \rightarrow \mu^\pm \tau^\mp)_{\text{exp}} \leq 1.2 \times 10^{-5}$$

## 2. generation of a purely leptonic effective Lagrangian at the scale $\leq m_b$

2<sup>nd</sup>:  $m_\tau$



$$R_\tau^{\tau/e} = \frac{\mathcal{B}(\tau \rightarrow \mu \nu \bar{\nu})_{\text{exp}} / \mathcal{B}(\tau \rightarrow \mu \nu \bar{\nu})_{\text{SM}}}{\mathcal{B}(\mu \rightarrow e \nu \bar{\nu})_{\text{exp}} / \mathcal{B}(\mu \rightarrow e \nu \bar{\nu})_{\text{SM}}}$$

$$R_\tau^{\tau/\mu} = \frac{\mathcal{B}(\tau \rightarrow e \nu \bar{\nu})_{\text{exp}} / \mathcal{B}(\tau \rightarrow e \nu \bar{\nu})_{\text{SM}}}{\mathcal{B}(\mu \rightarrow e \nu \bar{\nu})_{\text{exp}} / \mathcal{B}(\mu \rightarrow e \nu \bar{\nu})_{\text{SM}}}$$

$$\approx 1 + \frac{0.008 C_3}{\Lambda^2 (\text{TeV}^2)}$$

$$R_\tau^{\tau/e} = 1.0060 \pm 0.0030$$

$$R_\tau^{\tau/\mu} = 1.0022 \pm 0.0030$$

[A.Pich, 1310.7922]

$$\mathcal{B}(\tau \rightarrow 3\mu)$$

$$\approx 5 \times 10^{-8} \frac{(C_1 - C_3)^2}{\Lambda^4 (\text{TeV}^4)} \left( \frac{\vartheta_e}{0.3} \right)^2$$

Lusiani talk

$$\mathcal{B}(\tau \rightarrow 3\mu) \leq 1.2 \times 10^{-8}$$

[HFAG, 1412.7515]

$$\mathcal{B}(\tau \rightarrow \mu \rho)$$

$$\approx 5 \times 10^{-8} \frac{(C_1 - 1.3 C_3)^2}{\Lambda^4 (\text{TeV}^4)} \left( \frac{\vartheta_e}{0.3} \right)^2$$

$$\mathcal{B}(\tau \rightarrow \mu \rho) \leq 1.5 \times 10^{-8}$$

$$\mathcal{B}(\tau \rightarrow \mu \pi)$$

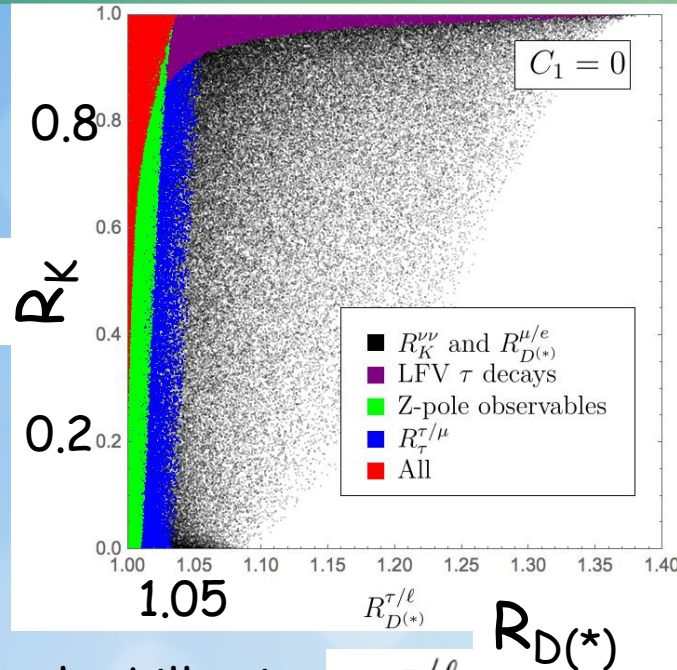
$$\approx 8 \times 10^{-8} \frac{(C_1 - C_3)^2}{\Lambda^4 (\text{TeV}^4)} \left( \frac{\vartheta_e}{0.3} \right)^2$$

$$\mathcal{B}(\tau \rightarrow \mu \pi) \leq 2.7 \times 10^{-8}$$

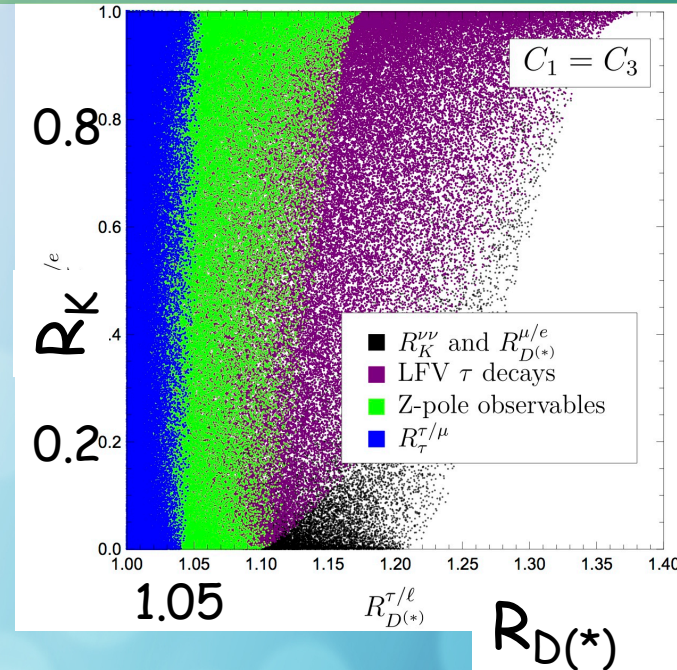
[HFAG, 1412.7515]



# Putting everything together



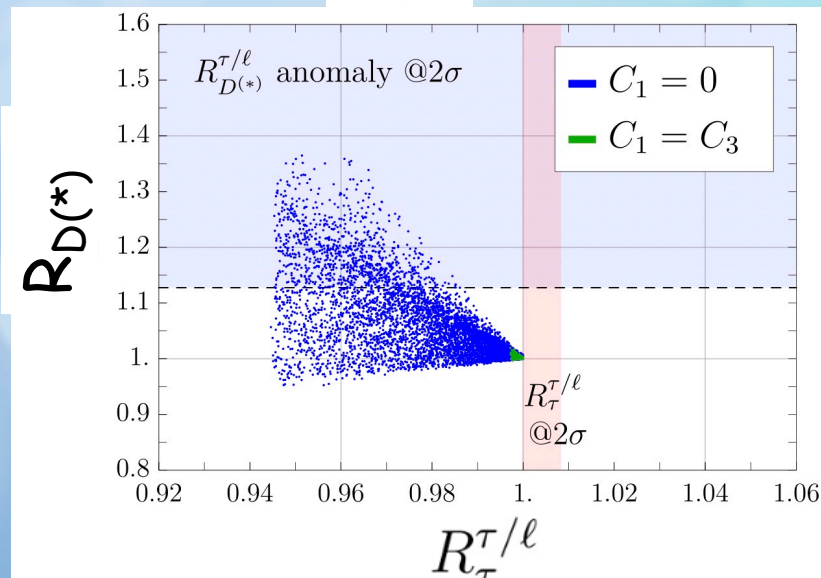
the killer is  $R_\tau^{\tau/\ell}$  !  $R_{D^{(*)}}$



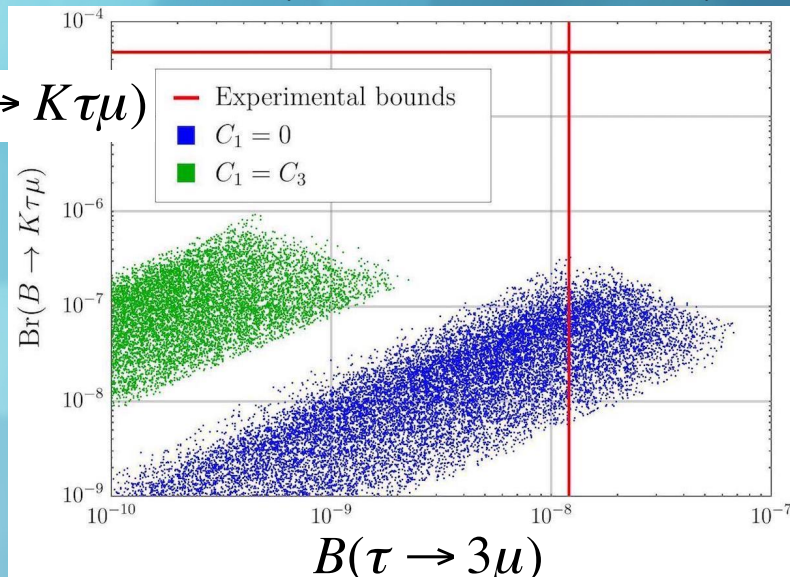
$$\left| \frac{C_{1,3}}{\Lambda^2} \right| \leq 4 \text{ TeV}^{-2}$$

$$|\vartheta_{d,e}| \leq 0.5$$

LFV better probed in tau decays



$$B(B \rightarrow K\tau\mu)$$



# A more general setup

C. Cornella, F.F., P. Paradisi, 1803.00945

$$\mathcal{L}_{\text{NP}}^0 = \frac{1}{\Lambda^2} (C_1 [Q_{lq}^{(1)}]_{3333} + C_3 [Q_{lq}^{(3)}]_{3333} + C_4 [Q_{ld}]_{3333} + C_5 [Q_{ed}]_{3333} + C_6 [Q_{qe}]_{3333})$$

$$[Q_{lq}^{(1)}]_{3333} = (\bar{\ell}'_{3L} \gamma^\mu \ell'_{3L}) (\bar{q}'_{3L} \gamma^\mu q'_{3L})$$

$$[Q_{lq}^{(3)}]_{3333} = (\bar{\ell}'_{3L} \gamma^\mu \tau^a \ell'_{3L}) (\bar{q}'_{3L} \gamma^\mu \tau^a q'_{3L})$$

$$[Q_{ld}]_{3333} = (\bar{\ell}'_{3L} \gamma^\mu \ell'_{3L}) (\bar{d}'_{3R} \gamma^\mu d'_{3R})$$

$$[Q_{ed}]_{3333} = (\bar{e}'_{3R} \gamma^\mu e'_{3R}) (\bar{d}'_{3R} \gamma^\mu d'_{3R})$$

$$[Q_{qe}]_{3333} = (\bar{q}'_{3L} \gamma^\mu q'_{3L}) (\bar{e}'_{3R} \gamma^\mu e'_{3R})$$

most general set of (current)<sup>2</sup>  
SU(2)×U(1) - invariant  
semileptonic operators  
involving the 3<sup>rd</sup> generation

the main effects are 1.  
and 2., as before

an example

$$C_1 + C_3 = C_6$$

$$C_4 = C_5 = 0.$$



$$O^9 = \frac{e^2}{16\pi^2} (\bar{s}_L \gamma_\mu b_L) (\bar{e}_i \gamma^\mu e_i)$$

we find

$$\frac{v_\tau}{v_e} = 1 - \frac{0.05 \lambda_{33}^e}{\Lambda^2} (2 C_1 + 0.2 C_3 + 0.02 (2 C_1 + C_3))$$

$$\frac{a_\tau}{a_e} = 1 + 0.007 \lambda_{33}^e \frac{C_3}{\Lambda^2}$$

directly correlated to

$$R_{\tau/\ell}^\tau$$

and

$$R_{D^{(*)}}$$

forces  $\delta R_{D^{(*)}}^{\tau/\ell}$  to be  $\lesssim 0.02$ .



# Discussion

cancellation/suppression of log effects by contributions of additional operators and/or finite correction terms not captured by this approach

different flavour pattern in  $O_{lq}^{(1,3)}$  can help in softening the bounds, e.g. in recent UV complete models with the vector LQ  $U_1=(3,1,+2/3)$

[Buttazzo, Greljo, Isidori, Marzocca, 1706.07808, Di Luzio, Greljo, Nardecchia 1708.08450, Bordone, Cornella, Fuentes-Martin, Isidori 1712.01368, Barbieri, Tesi 1712.06844,...]

couplings to 2<sup>nd</sup> lepton generation not dominated by mixing to 3<sup>rd</sup> one

$$R_D^{\tau/\ell} \quad R_{D^*}^{\tau/\ell}$$

alone can be explained in present framework

$$\text{e.g. } \vartheta_d \approx 1, \vartheta_e \ll \alpha_{em}, \Lambda \approx 5 \text{ TeV}$$



loop effects decouple as  $v^2/\Lambda^2$

$$R_K^{\mu/e} \quad R_{K^*}^{\mu/e}$$

alone can be explained in present framework

$$\text{e.g. } \vartheta_d \approx 1, \vartheta_e \approx 1, \Lambda \approx 30 \text{ TeV}$$



loop effects decouple as  $v^2/\Lambda^2$



# Discussion

cancellation/suppression of log effects by contributions of additional operators and/or finite correction terms not captured by this approach

vector LQ  $U_1=(3,1,+2/3)$

- $O_{lq}^{(1,3)}$  operators with  $C_1=+C_3$  if  $g_{ql}^L \neq 0$   $g_{ql}^R = 0$
- automatically free from p-decay
- realizes the minimal lepton-quark unification within the Pati-Salam SU(4)
- $m_U \geq 100$  TeV unless flavour pattern is cleverly arranged

$$R_D^{\tau/\ell} \quad R_{D^*}^{\tau/\ell}$$

alone can be explained in present framework

$$\text{e.g. } \vartheta_d \approx 1, \vartheta_e \ll \alpha_{em}, \Lambda \approx 5 \text{ TeV}$$



loop effects decouple as  $v^2/\Lambda^2$

$$R_K^{\mu/e} \quad R_{K^*}^{\mu/e}$$

alone can be explained in present framework

$$\text{e.g. } \vartheta_d \approx 1, \vartheta_e \approx 1, \Lambda \approx 30 \text{ TeV}$$



loop effects decouple as  $v^2/\Lambda^2$

# Discussion

cancellation/suppression of log effects by contributions of additional operators and/or finite correction terms not captured by this approach

different flavour pattern in  $O_{lq}^{(1,3)}$  can help in softening the bounds, e.g. in recent UV complete models with the vector LQ  $U_1=(3,1,+2/3)$

[Buttazzo, Greljo, Isidori, Marzocca, 1706.07808, Di Luzio, Greljo, Nardecchia 1708.08450, Bordone, Cornella, Fuentes-Martin, Isidori 1712.01368, Barbieri, Tesi 1712.06844,...]

couplings to 2<sup>nd</sup> lepton generation not dominated by mixing to 3<sup>rd</sup> one

$$R_D^{\tau/\ell} \quad R_{D^*}^{\tau/\ell}$$

alone can be explained in present framework

$$\text{e.g. } \vartheta_d \approx 1, \vartheta_e \ll \alpha_{em}, \Lambda \approx 5 \text{ TeV}$$



loop effects decouple as  $v^2/\Lambda^2$

$$R_K^{\mu/e} \quad R_{K^*}^{\mu/e}$$

alone can be explained in present framework

$$\text{e.g. } \vartheta_d \approx 1, \vartheta_e \approx 1, \Lambda \approx 30 \text{ TeV}$$



loop effects decouple as  $v^2/\Lambda^2$

# any relation to the muon (g-2) ?

among all possible 1-particle extensions of the SM a special property enjoyed by scalar LQ that couples to quarks of BOTH chiralities

$$S_1 = (\bar{3}, 1, +1/3)$$

[not automatically p-decay free]

$$R_2 = (3, 2, +7/6)$$

contributions to dipole transitions can be chirally enhanced

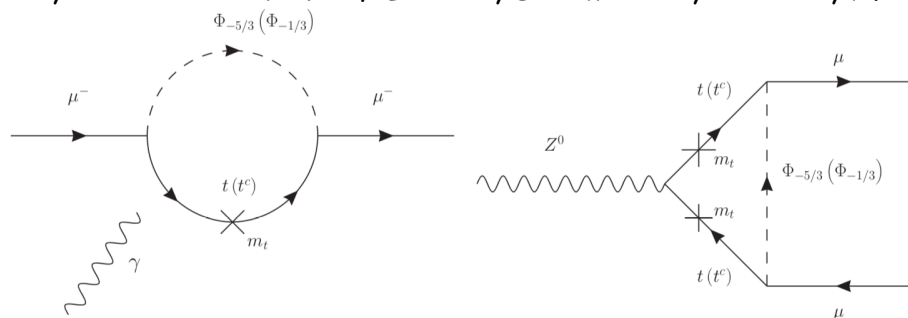
$\delta a_\ell$	$\Gamma(\ell \rightarrow \ell' \gamma)$
$\frac{1}{16\pi^2} \frac{m_\ell m_{top}}{M_{LQ}^2} g_{t\ell}^L g_{t\ell}^R$	$\frac{\alpha_{em}}{256\pi^4} \frac{m_\ell^3 m_{top}^2}{M_{LQ}^4}  g_{t\ell}^{L(R)} g_{t\ell'}^{R(L)} ^2$

[Djouadi, Kohler, Spira, Tutas, 1990  
Chakraverty, Choudhury, Datta 0102180  
Cheung 0102238  
Biggio, Bordone 1411.6799]

$\delta a_\mu$  of correct size for  $M_{LQ} \approx 1$  TeV in a weak coupling regime

1-to-1 correlation to (chirally enhanced) deviations in Z-coupling to leptons

Bauer, Neubert 1511.01900; Leskow, D' Ambrosio, Crivellin, Muller 1612.06858<sup>2</sup>



$$\delta BR(Z \rightarrow \ell^+ \ell^-) \approx \frac{1}{16\pi^2} \frac{m_{top}^2}{M_{LQ}^2} |g_{t\ell}^L|^2$$



many models addressing B-anomalies include  $S_1$  or  $R_2$  in their spectrum

[NC anomaly requires special care:  
no contribution to  $b \rightarrow s \ell^+ \ell^-$  from tree-level  $S_1$  exchange;  
 $C_9 = +C_{10}$  from  $R_2$  exchange]

Bauer, Neubert 1511.01900  
Chen, Nomura, Okada 1607.04857  
Caio, Gargalionis, Schmidt, Vokas 1704.05849  
Becirevic, Sumensari, 1704.05835  
Chauhan, Kindra, Narang, 1706.04598  
Crivellin, Muller, Ota, 1703.09226  
...

$S_1$   
 $R_2 + S_3$   
 $S_1$   
 $R_2$   
 $R_2$   
 $S_1 + S_3$

if LQ couples mainly to top and 2<sup>nd</sup> lepton generation

$$\delta a_\mu \approx +3 \times 10^{-9}$$



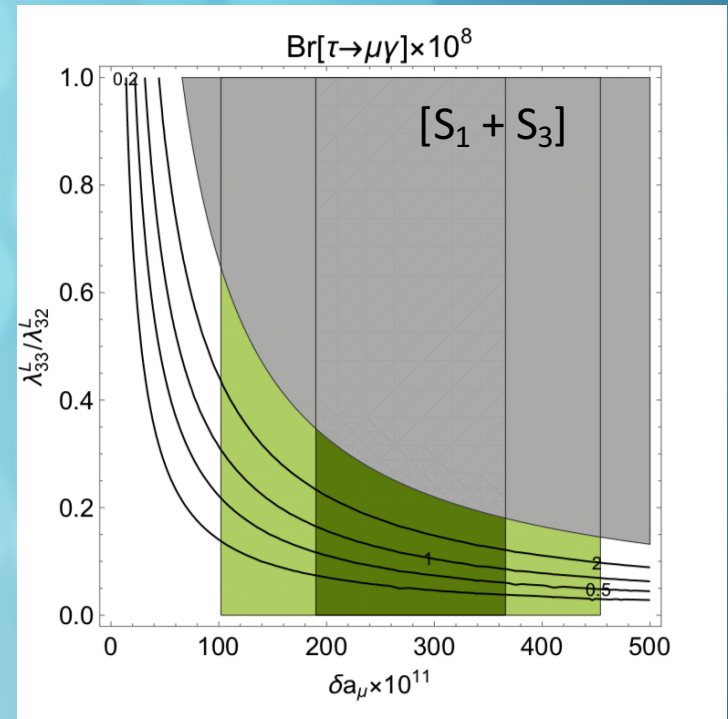
$$\delta BR(Z \rightarrow \mu^+ \mu^-) \approx 10^{-4}$$

If LQ couples also to top and 3<sup>rd</sup> lepton generation



$$\frac{BR(\tau \rightarrow \mu \gamma)}{(\delta a_\mu)^2} \geq \frac{9 \times 10^{-7}}{(+3 \times 10^{-9})^2} \left( \frac{g_{33}^L}{g_{32}^L} \right)^2$$

$$BR(Z \rightarrow \tau^\pm \mu^\mp) \approx \frac{10^{-8} (g_{33}^L g_{32}^L)^2}{M_{LQ}^4 (TeV)}$$



[Crivellin, Muller, Ota, 1703.09226]

# conclusion

■ simultaneous explanation of  $R_{K^{(*)}}$  and  $R_{D^{(*)}}$  anomalies appealing it calls for a “low” New Physics scale  $\Lambda \approx 1$  TeV, at least in simplest scheme

■ in this context the inclusion of quantum corrections  $\approx O(v^2/\Lambda^2)$  is crucial to assess the viability of proposed solutions

■ in the reference case discussed here (NP in 3<sup>rd</sup> generation V-A currents) purely leptonic LFUV/LFV transitions are generated and strong constraints arise

$$\frac{a_\tau}{a_e}$$

$$\frac{v_\tau}{v_e}$$

watch  $\tau \rightarrow 3\mu$

$$R_{\tau/e}^{\tau} = \frac{\mathcal{B}(\tau \rightarrow \mu\nu\bar{\nu})_{\text{exp}}/\mathcal{B}(\tau \rightarrow \mu\nu\bar{\nu})_{\text{SM}}}{\mathcal{B}(\mu \rightarrow e\nu\bar{\nu})_{\text{exp}}/\mathcal{B}(\mu \rightarrow e\nu\bar{\nu})_{\text{SM}}}$$
$$R_{\tau/\mu}^{\tau} = \frac{\mathcal{B}(\tau \rightarrow e\nu\bar{\nu})_{\text{exp}}/\mathcal{B}(\tau \rightarrow e\nu\bar{\nu})_{\text{SM}}}{\mathcal{B}(\mu \rightarrow e\nu\bar{\nu})_{\text{exp}}/\mathcal{B}(\mu \rightarrow e\nu\bar{\nu})_{\text{SM}}}$$

■ Bounds from EWPT and/or tau physics can be softened by

- more elaborate flavor patterns in NP and/or
- some conspiracy by UV physics

Back-up slides



# Global Fit

- $B \rightarrow K^{(*)} \ell^+ \ell^-$

$$\mathcal{O}_9 = \frac{\alpha}{4\pi} (\bar{s}_L \gamma_\mu b_L) (\bar{\ell} \gamma_\mu \ell)$$

$$\mathcal{O}_{10} = \frac{\alpha}{4\pi} (\bar{s}_L \gamma_\mu b_L) (\bar{\ell} \gamma_\mu \gamma_5 \ell)$$

$$\mathcal{O}'_9 = \frac{\alpha}{4\pi} (\bar{s}_R \gamma_\mu b_R) (\bar{\ell} \gamma_\mu \ell)$$

$$\mathcal{O}'_{10} = \frac{\alpha}{4\pi} (\bar{s}_R \gamma_\mu b_R) (\bar{\ell} \gamma_\mu \gamma_5 \ell)$$

$$\mathcal{O}_{7\gamma} = \frac{e}{4\pi^2} m_b (\bar{s}_L \sigma^{\mu\nu} b_R) F_{\mu\nu}$$

$$\mathcal{O}'_{7\gamma} = \frac{e}{4\pi^2} m_b (\bar{s}_R \sigma^{\mu\nu} b_L) F_{\mu\nu}$$



$$\left. \begin{array}{l} \triangleright C_9^{NP} \neq 0 \\ \triangleright C_9^{NP} = -C_{10}^{NP} \neq 0 \end{array} \right\} \text{good fits of: } \begin{array}{l} \triangleright R_K \\ \triangleright P'_5 \text{ (et al.)} \end{array} \quad \begin{array}{l} \text{S. Descotes-Genon, L. Hofer,} \\ \text{J. Matias, J. Virto (2015)} \end{array}$$



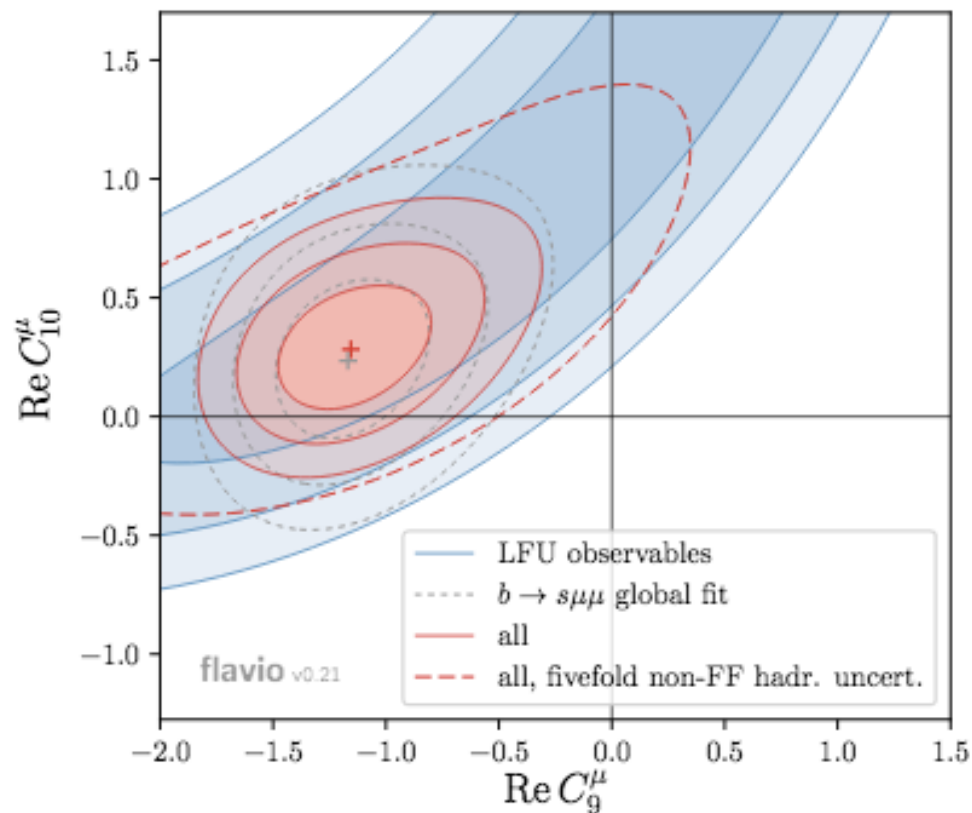
$$(\bar{s}_L \gamma_\mu b_L) (\bar{\ell}_L \gamma_\mu \ell_L) \Rightarrow \text{left-handed current}$$

# Global Fit

Coeff.	best fit	$1\sigma$	$2\sigma$	pull
$C_9^\mu$	-1.59	[-2.15, -1.13]	[-2.90, -0.73]	4.2 $\sigma$
$C_{10}^\mu$	+1.23	[+0.90, +1.60]	[+0.60, +2.04]	4.3 $\sigma$
$C_9^e$	+1.58	[+1.17, +2.03]	[+0.79, +2.53]	4.4 $\sigma$
$C_{10}^e$	-1.30	[-1.68, -0.95]	[-2.12, -0.64]	4.4 $\sigma$
$C_9^\mu = -C_{10}^\mu$	-0.64	[-0.81, -0.48]	[-1.00, -0.32]	4.2 $\sigma$
$C_9^e = -C_{10}^e$	+0.78	[+0.56, +1.02]	[+0.37, +1.31]	4.3 $\sigma$
$C_9^{\prime\mu}$	-0.00	[-0.26, +0.25]	[-0.52, +0.51]	0.0 $\sigma$
$C_{10}^{\prime\mu}$	+0.02	[-0.22, +0.26]	[-0.45, +0.49]	0.1 $\sigma$
$C_9^{\prime e}$	+0.01	[-0.27, +0.31]	[-0.55, +0.62]	0.0 $\sigma$
$C_{10}^{\prime e}$	-0.03	[-0.28, +0.22]	[-0.55, +0.46]	0.1 $\sigma$

TABLE I. Best-fit values and pulls for scenarios with NP in one individual Wilson coefficient.

[Altmannshofer, Stangl and Straub, 1704.05435]



`All' includes  $R_K, R_{K^*}$ , angular variables in  $B \rightarrow K^* \mu^+ \mu^-$ , differential BR in  $B \rightarrow K^* \mu^+ \mu^-$ ,  $B \rightarrow \phi \mu^+ \mu^-$

# Global Fit

$$[R_K]_{[1,6]} \simeq 1.00(1) + 0.230(\mathcal{C}_{9\mu-e}^{\text{NP}} + \mathcal{C}'_{9\mu-e}) - 0.233(2)(\mathcal{C}_{10\mu-e}^{\text{NP}} + \mathcal{C}'_{10\mu-e}),$$

$$[R_{K^*}]_{[0.045,1.1]} \simeq 0.92(2) + 0.07(2)\mathcal{C}_{9\mu-e}^{\text{NP}} - 0.10(2)\mathcal{C}'_{9\mu-e} - 0.11(2)\mathcal{C}_{10\mu-e}^{\text{NP}} + 0.11(2)\mathcal{C}'_{10\mu-e} + 0.55(6)\mathcal{C}_7^{\text{NP}},$$

$$[R_{K^*}]_{[1.1,6]} \simeq 1.00(1) + 0.20(1)\mathcal{C}_{9\mu-e}^{\text{NP}} - 0.19(1)\mathcal{C}'_{9\mu-e} - 0.27(1)\mathcal{C}_{10\mu-e}^{\text{NP}} + 0.21(1)\mathcal{C}'_{10\mu-e}.$$

[Celis, Fuentes Martin, Vicente and Virto, 1704.05672]



# Dimension six operators

Semileptonic operators:	Leptonic operators:
$[O_{\ell q}^{(1)}]_{prst} = (\bar{\ell}'_{pL} \gamma_\mu \ell'_{rL}) (\bar{q}'_{sL} \gamma^\mu q'_{tL})$ $[O_{\ell q}^{(3)}]_{prst} = (\bar{\ell}'_{pL} \gamma_\mu \tau^a \ell'_{rL}) (\bar{q}'_{sL} \gamma^\mu \tau^a q'_{tL})$ $[O_{\ell u}]_{prst} = (\bar{\ell}'_{pL} \gamma_\mu \ell'_{rL}) (\bar{u}'_{sR} \gamma^\mu u'_{tR})$ $[O_{\ell d}]_{prst} = (\bar{\ell}'_{pL} \gamma_\mu \ell'_{rL}) (\bar{d}'_{sR} \gamma^\mu d'_{tR})$ $[O_{qe}]_{prst} = (\bar{q}'_{pL} \gamma_\mu q'_{rL}) (\bar{e}'_{sR} \gamma^\mu e'_{tR})$	$[O_{\ell\ell}]_{prst} = (\bar{\ell}'_{pL} \gamma_\mu \ell'_{rL}) (\bar{\ell}'_{sL} \gamma^\mu \ell'_{tL})$ $[O_{\ell e}]_{prst} = (\bar{\ell}'_{pL} \gamma_\mu \ell'_{rL}) (\bar{e}'_{sR} \gamma^\mu e'_{tR})$
Vector operators:	Hadronic operators:
$[O_{H\ell}^{(1)}]_{pr} = (\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi) (\bar{\ell}'_{pL} \gamma_\mu \ell'_{rL})$ $[O_{H\ell}^{(3)}]_{pr} = (\varphi^\dagger i \overleftrightarrow{D}_\mu^a \varphi) (\bar{\ell}'_{pL} \gamma_\mu \tau^a \ell'_{rL})$ $[O_{Hq}^{(1)}]_{pr} = (\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi) (\bar{q}'_{pL} \gamma_\mu q'_{rL})$ $[O_{Hq}^{(3)}]_{pr} = (\varphi^\dagger i \overleftrightarrow{D}_\mu^a \varphi) (\bar{q}'_{pL} \gamma_\mu \tau^a q'_{rL})$	$[O_{qq}^{(1)}]_{prst} = (\bar{q}'_{pL} \gamma_\mu q'_{rL}) (\bar{q}'_{sL} \gamma^\mu q'_{tL})$ $[O_{qq}^{(3)}]_{prst} = (\bar{q}'_{pL} \gamma_\mu \tau^a q'_{rL}) (\bar{q}'_{sL} \gamma^\mu \tau^a q'_{tL})$ $[O_{qu}^{(1)}]_{prst} = (\bar{q}'_{pL} \gamma_\mu q'_{rL}) (\bar{u}'_{sR} \gamma^\mu u'_{tR})$ $[O_{qd}^{(1)}]_{prst} = (\bar{q}'_{pL} \gamma_\mu q'_{rL}) (\bar{d}'_{sR} \gamma^\mu d'_{tR})$

**Table 1:** Minimal set of gauge-invariant operators involved in the RGE flow considered in this paper. Fields are in the interaction basis to maintain explicit  $SU(2) \times U(1)$  gauge invariance. Our notation and conventions are as in [26].

# Effective Lagrangian - ew scale

$$g_{fL,R} = g_{fL,R}^{SM} + \Delta g_{fL,R} \qquad g_{\ell,q} = g_{\ell,q}^{SM} + \Delta g_{\ell,q}$$

$$\Delta g_{\nu L}^{ij} = \frac{v^2}{\Lambda^2} \frac{L}{16\pi^2} \left( \frac{1}{3} g_1^2 C_1 - g_2^2 C_3 + 3y_t^2 \lambda_{33}^u (C_1 + C_3) \right) \lambda_{ij}^e$$

$$\Delta g_{eL}^{ij} = \frac{v^2}{\Lambda^2} \frac{L}{16\pi^2} \left( \frac{1}{3} g_1^2 C_1 + g_2^2 C_3 + 3y_t^2 \lambda_{33}^u (C_1 - C_3) \right) \lambda_{ij}^e$$

$$\Delta g_{uL}^{ij} = -\frac{v^2}{\Lambda^2} \frac{L}{16\pi^2} \frac{1}{3} (g_1^2 C_1 + g_2^2 C_3) \lambda_{ij}^u$$

$$\Delta g_{dL}^{ij} = -\frac{v^2}{\Lambda^2} \frac{L}{16\pi^2} \frac{1}{3} (g_1^2 C_1 - g_2^2 C_3) \lambda_{ij}^d$$

$$\Delta g_{fR}^{ij} = 0 \quad (f = \nu, e, u, d)$$

$$\Delta g_{\ell}^{ij} = \frac{v^2}{\Lambda^2} \frac{L}{16\pi^2} (-2g_2^2 C_3 + 6y_t^2 \lambda_{33}^u C_3) \lambda_{ij}^e$$

$$\Delta g_q^{ij} = -\frac{v^2}{\Lambda^2} \frac{L}{16\pi^2} \frac{2}{3} g_2^2 C_3 \lambda_{ij}^{ud} \quad .$$

$$L = \log \frac{\Lambda}{\mu}$$

# Effective Lagrangian - ew scale

$$\mathcal{L}_{eff}^{EW} = \mathcal{L}'_{SM} + \mathcal{L}_{NP}^0 + \frac{1}{16\pi^2\Lambda^2} \log \frac{\Lambda}{m_{EW}} \sum_i \xi_i Q_i$$

$Q_i$	$\xi_i$
$(\bar{\nu}_{iL}\gamma_\mu\nu_{jL}) (\bar{\nu}_{kL}\gamma^\mu\nu_{nL})$	$\lambda_{ij}^e \delta_{kn} [-6y_t^2\lambda_{33}^u(C_1 + C_3)]$
$(\bar{\nu}_{iL}\gamma_\mu\nu_{jL}) (\bar{e}_{kL}\gamma^\mu e_{nL})$	$\lambda_{ij}^e \delta_{kn} [\frac{4}{3}e^2(C_1 + 3C_3) - 12(-\frac{1}{2} + s_\theta^2)y_t^2\lambda_{33}^u(C_1 + C_3)]$ $+\delta_{ij} \lambda_{kn}^e [-6y_t^2\lambda_{33}^u(C_1 - C_3)]$
$(\bar{\nu}_{iL}\gamma_\mu\nu_{jL}) (\bar{e}_{kR}\gamma^\mu e_{nR})$	$\lambda_{ij}^e \delta_{kn} [\frac{4}{3}e^2(C_1 + 3C_3) - 12s_\theta^2 y_t^2\lambda_{33}^u(C_1 + C_3)]$
$(\bar{e}_{iL}\gamma_\mu e_{jL}) (\bar{e}_{kL}\gamma^\mu e_{nL})$	$\lambda_{ij}^e \delta_{kn} [\frac{4}{3}e^2(C_1 - 3C_3) - 12(-\frac{1}{2} + s_\theta^2)y_t^2\lambda_{33}^u(C_1 - C_3)]$
$(\bar{e}_{iL}\gamma_\mu e_{jL}) (\bar{e}_{kR}\gamma^\mu e_{nR})$	$\lambda_{ij}^e \delta_{kn} [\frac{4}{3}e^2(C_1 - 3C_3) - 12s_\theta^2 y_t^2\lambda_{33}^u(C_1 - C_3)]$
$(\bar{\nu}_{iL}\gamma_\mu e_{jL}) (\bar{e}_{kL}\gamma^\mu\nu_{nL})$	$(\lambda_{ij}^e \delta_{kn} + \delta_{ij} \lambda_{kn}^e) [-12 y_t^2\lambda_{33}^u C_3]$

**Table 2:** Operators  $Q_i$  and coefficients  $\xi_i$  for the purely leptonic part of the effective Lagrangian  $\mathcal{L}_{eff}^{EW}$ . We set  $\sin^2 \theta_W \equiv s_\theta^2$ .



# Effective Lagrangian at low energy

$$\delta\mathcal{L}_{eff}^{QED} = \frac{1}{16\pi^2\Lambda^2} \log \frac{m_{EW}}{\mu} \sum_i \delta\xi_i Q_i$$

$Q_i$	$\delta\xi_i$
$(\bar{\nu}_{iL}\gamma_\mu\nu_{jL}) (\bar{\nu}_{kL}\gamma^\mu\nu_{nL})$	0
$(\bar{\nu}_{iL}\gamma_\mu\nu_{jL}) (\bar{e}_k\gamma^\mu e_n)$	$\lambda_{ij}^e \delta_{kn} \cdot \frac{4}{3}e^2 \left[ (C_1 + 3C_3) - 2(C_1 + C_3)(\hat{\lambda}_{33}^u \log \frac{m_t}{\mu} + \hat{\lambda}_{22}^u \log \frac{m_c}{\mu}) \right. \\ \left. + (C_1 - C_3)\hat{\lambda}_{33}^d \log \frac{m_b}{\mu} \right]$
$(\bar{e}_{iL}\gamma_\mu e_{jL}) (\bar{e}_k\gamma^\mu e_n)$	$\lambda_{ij}^e \delta_{kn} \cdot \frac{4}{3}e^2 \left[ (C_1 - 3C_3) - 2(C_1 - C_3)(\hat{\lambda}_{33}^u \log \frac{m_t}{\mu} + \hat{\lambda}_{22}^u \log \frac{m_c}{\mu}) \right. \\ \left. + (C_1 + C_3)\hat{\lambda}_{33}^d \log \frac{m_b}{\mu} \right]$

**Table 6:** Operators  $Q_i$  and coefficients  $\delta\xi_i$  for the purely leptonic part of the effective Lagrangian  $\delta\mathcal{L}_{eff}^{QED}$ . We set  $\hat{\lambda}_{ii}^{u,d} = \lambda_{ii}^{u,d} / \log \frac{m_{EW}}{\mu}$ .

# tree-level mediators of $O_{lq}^{(1,3)}$

Field	Spin	Quantum Numbers	Operator	$C_1$	$C_3$
$A_\mu$	1	$(1, 1, 0)$	$\bar{q}'_L \gamma^\mu q'_L \bar{\ell}'_L \gamma_\mu \ell'_L$	-1	0
$A_\mu^a$	1	$(1, 3, 0)$	$\bar{q}'_L \gamma^\mu \tau^a q'_L \bar{\ell}'_L \gamma_\mu \tau^a \ell'_L$	0	-1
$U_\mu$	1	$(3, 1, +2/3)$	$\bar{q}'_L \gamma^\mu \ell'_L \bar{\ell}'_L \gamma_\mu q'_L$	$-\frac{1}{2}$	$-\frac{1}{2}$
$U_\mu^a$	1	$(3, 3, +2/3)$	$\bar{q}'_L \gamma^\mu \tau^a \ell'_L \bar{\ell}'_L \gamma_\mu \tau^a q'_L$	$-\frac{3}{2}$	$+\frac{1}{2}$
$S$	0	$(3, 1, -1/3)$	$\bar{q}'_L i\sigma^2 \ell'^c_L \overline{i\sigma^2 \ell'^c_L} q'_L$	$+\frac{1}{4}$	$-\frac{1}{4}$
$S^a$	0	$(3, 3, -1/3)$	$\bar{q}'_L \tau^a i\sigma^2 \ell'^c_L \overline{i\sigma^2 \ell'^c_L} \tau^a q'_L$	$+\frac{3}{4}$	$+\frac{1}{4}$

**Table 11:** Spin zero and spin one mediators contributing, at tree-level, to the Lagrangian  $\mathcal{L}_{NP}^0(\Lambda)$  of eq. (7). Also shown are the operators they give rise to and the contribution to the coefficients  $C_1$  and  $C_3$  of the Lagrangian  $\mathcal{L}_{NP}^0(\Lambda)$ , when a single fermion generation is involved.

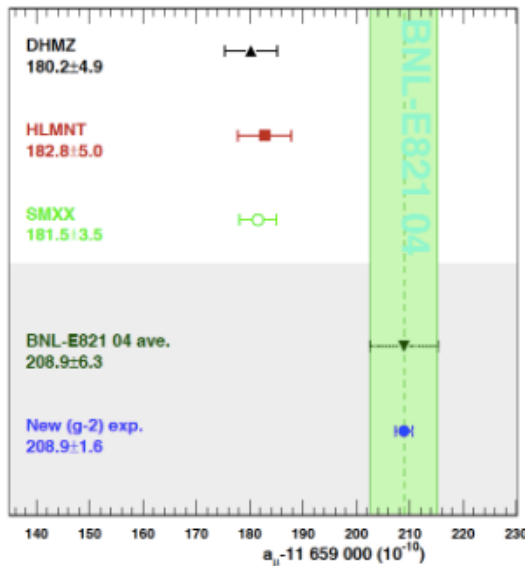
- no conclusive NP signal from individual measurements
- significant discrepancy from the SM predictions comes from average and/or global fits

other hints of LFU violation

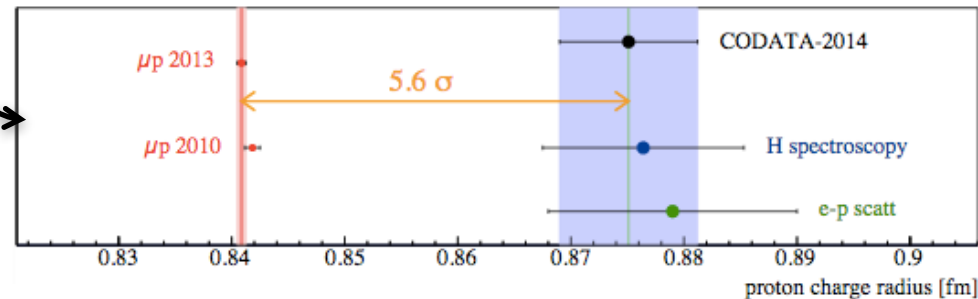
e-μ universality

muon (g-2)

T. Blum et al. (arXiv:1311.2198)



proton radius



[arXiv:1706.00696]

$\tau$ -e and  $\tau$ -μ universality

W leptonic decays

$$\frac{2\mathcal{B}(W^+ \rightarrow \tau^+ \nu_\tau)}{\mathcal{B}(W^+ \rightarrow e^+ \nu_e) + \mathcal{B}(W^+ \rightarrow \mu^+ \nu_\mu)} = 1.067 \pm 0.029 .$$