### $b ightarrow s \ell \ell$ : angular analyses and studies with muons

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**RWTH Aachen** 

on behalf of the LHCb collaboration Beauty 2018 (7-11 May 2018)







### Why rare $b \rightarrow s \ell \ell$ decays?

NB: this talk covers  $b \rightarrow s\mu\mu$  decays at LHCb, for  $b \rightarrow see$  decays (including LFU results) see Albert Puig's talk (up next!)

- b → sℓℓ transitions are forbidden at tree level → suppressed decays in the SM maybe be more sensitive to new physics (NP) effects.
- Virtual new physics particles  $\rightarrow$  high mass reach.



### Use of effective theories in $b \rightarrow s\ell\ell$ SM predictions

- The heavy physics in b→sℓℓ decays can be integrated out to give effective couplings, parameterised by the Wilson Coefficients (C<sub>i</sub>).
- $b \rightarrow s\ell\ell$  transitions are most sensitive to the coefficients  $C_{9/10}$



### Measuring $b \rightarrow s \ell \ell$ transitions

• Angular analyses and branching fraction measurements



### $B^0 \rightarrow K^{*0} [\rightarrow K^+ \pi^-] \mu^+ \mu^-$ angular analysis $[C_7, C_9, C_{10}]$

Angular decay fully described by the dilepton mass ( $q^2$ ) and the angles  $\cos(\theta_l)$   $\cos(\theta_k)$  and  $\phi$ :



3D fit to all three angles (in  $q^2$  bins), exploiting the correlations between the  $S_i$ ,  $F_L$  and  $A_{FB}$  terms to obtain their respective values (+ swave - see back-up).

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## $B^0 \rightarrow \overline{K^{*0}} [\rightarrow K^+ \pi^-] \mu^+ \mu^-$ angular analysis: Results





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## $B^0 \rightarrow K^{*0} [\rightarrow K^+ \pi^-] \mu^+ \mu^-$ angular analysis: Results

Generally very good agreement with the Standard Model



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### $B^0 \rightarrow K^{*0} [\rightarrow K^+ \pi^-] \mu^+ \mu^-$ angular analysis: Results

### Reduce form factor dependence

Can construct ratios of angular observables where form-factors cancel at leading order:  $P'_5 = S_5 / \sqrt{F_L(1 - F_L)}$  $P'_5$  plot: Bins 4/5 = local SM tension of 2.8 and 3.0 $\sigma$ . Global tension= 3.4 $\sigma$ , assuming tension due to shift in Wilson coeff.  $\mathcal{R}e(C_9)$  (LHCb only)



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 $B^0 \to K^{*0} [\to K^+\pi^-] \mu^+\mu^-$  branching fraction



### Performance comparison: $B^0 \rightarrow K^{*0} \mu^+ \mu^-$





### $B^0_s o \phi[ o K^+K^-]\mu^+\mu^-$ [ $\mathcal{C}_7, \mathcal{C}_9, \mathcal{C}_{10}$ ]

Equivalent process of  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$  for  $B_s^0 \overset{c}{\to}$  mesons.

Angular variables consistent with the SM.  $P_5'$  cannot be measured as  $B_s^0 \to \phi \mu^+ \mu^-$  not self-tagging.

In bin  $1 < q^2 < 6$ GeV/ $c^2$  the data is  $3.3\sigma$ from the SM prediction.





![](_page_11_Picture_2.jpeg)

### $b \rightarrow s \ell \ell$ transitions in baryons

- Baryon sector still relatively unexplored compared to mesons
- Measurements can complement those from meson sector

![](_page_12_Picture_3.jpeg)

### The decays $\Lambda_b^0 \to \Lambda^0 \mu^+ \mu^-$ and $\Lambda_b^0 \to p K \mu^+ \mu^-$

![](_page_13_Figure_1.jpeg)

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## CPV in $\Lambda^0_b \to p K \mu^+ \mu^-$

Baryon production asymmetries not well known: use  $\Delta A_{cp}$  and triple products

 $a_{CP}^{\hat{T}-odd}$  = (1.2  $\pm$  5.0(stat)  $\pm$  0.7(syst)) imes 10<sup>-2</sup> ightarrow no significant CPV

• Measure  $\Delta A_{CP} = A_{CP}(\Lambda_b^0 \to pK^-\mu^+\mu^-) - A_{CP}(\Lambda_b^0 \to J/\psi pK^-)$ 

 $\Delta A_{CP} = (-3.5 \pm 5.0 \text{ (stat)} \pm 0.2 \text{ (syst)}) \times 10^{-2} \rightarrow \text{no significant CPV}$ Beauty 2018 (7-11 May 2018)
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### Global fits

- Global fits performed by theorists to a range of results from  $b \to s \ell \ell$  measurements
- Will also discuss interpretations of global fits

### Global fits

- Sub-divide between 'clean' observables (LFU measurements see next talk) and 'dirty' observables (e.g. angular analyses)
- Just LFU ightarrow  $\sim$  4  $\sigma$  deviations
- Combining all measurements  $\rightarrow$  over 5  $\sigma$  deviations

Non-exhaustive list of global fit examples: arXiv:1704.05438, arXiv:1703.09189, arXiv:1603.00865, arXiv:1702.02234

one example of a global fit, many others out there (!)						
Coeff.	best fit	$1\sigma$	$2\sigma$	pull		
$C_9^{\mu}$	-1.56	[-2.12, -1.10]	[-2.87, -0.7]	1] 4.1σ		
$C_{10}^{\mu}$	+1.20	[+0.88, +1.57]	[+0.58, +2.0]	$0] 4.2\sigma$		
$C_9^e$	+1.54	[+1.13, +1.98]	[+0.76, +2.4]	8] $4.3\sigma$		
$C_{10}^{e}$	-1.27	$[-1.65,\ -0.92]$	[-2.08, -0.6]	1] $4.3\sigma$		
$C_{9}^{\mu} = -C_{10}^{\mu}$	-0.63	[-0.80, -0.47]	[-0.98, -0.3]	2] $4.2\sigma$		
$C_{9}^{e} = -C_{10}^{e}$	+0.76	[+0.55, +1.00]	[+0.36, +1.2]	7] 4.3 $\sigma$		
$C_9^e = C_{10}^e$	-1.91	[-2.30, -1.51]	[-2.71, -1.1]	0] 3.9 $\sigma$		

Pull assuming 1D variation only and just LFU measurements -> increased tension when including angular analyses

![](_page_16_Figure_7.jpeg)

arXiv:1704.05435

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### What could be causing this anomaly?

![](_page_17_Figure_1.jpeg)

![](_page_17_Picture_2.jpeg)

- Due to the difficulty of modelling Charmonium resonances, the J/ψ and ψ(2S) are generally removed from data when looking at just the short-distance contributions.
- Vector resonances producing dimuon pairs could mimic a contribution to *C*<sub>9</sub> allowing *C*<sub>9</sub> to be expressed as

$$C_{\rm 9eff}=C_9+Y(q^2)$$

• Possible that the deficiency in muons could be due to destructive interference from such Charmonium resonances.

# Data driven measurements of short and long distance interference

![](_page_19_Figure_1.jpeg)

- Data driven approach  $\rightarrow$  fit to unbinned data in  $q^2$  for the data  $B^+$   $\rightarrow K^+ \mu^+ \mu^-$
- Express Y(q<sup>2</sup>) in terms of the sum of the magnitude and phases of the vector meson resonances (ρ, ω, φ, J/ψ, ψ(2S), ψ(X)) → model these contributions as a sum of Breit Wigners with individual width and phase.

![](_page_19_Picture_6.jpeg)

# Data driven measurements of short and long distance interference

![](_page_20_Figure_1.jpeg)

- Four solutions fit data well reflecting the unknown sign of the  $J/\psi$  and  $\psi(2S)$  phases (NB resolution dominants these resonances widths)
- The phases that are measured suggest a small contribution to the short-distance component in the dimuon mass regions far from the J/ $\psi$  and  $\psi(2S)$  masses, given the assumptions made in model.

![](_page_20_Picture_6.jpeg)

### $b \rightarrow d\ell\ell$ transitions

 The increased data collected at the LHCb detector means that the Cabibbo-suppressed b→dℓℓ modes are becoming more of interest

![](_page_21_Picture_2.jpeg)

### Why $b \rightarrow d\ell\ell$ transitions?

- Combining b → sℓℓ with their Cabibbo-suppressed partner allows a measurement of V<sub>td</sub>/V<sub>ts</sub> and thus a test of Minimal Flavour Violation.
- Expect branching fractions to be  $\sim$  25 times smaller than s quark partner

![](_page_22_Figure_3.jpeg)

![](_page_22_Picture_6.jpeg)

### Examples of $b \rightarrow d\ell \ell$ transitions

![](_page_23_Figure_1.jpeg)

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### Conclusions and outlook

- Number of anomalies in  $b \to s\ell\ell$  transitions, consistent with a deficit in the muon channel
- Could be theoretical limitations or new physics
- More data necessary to further qualify this, as well as development in theory
- Advent of Belle 2 and further runs at the LHC will yield interesting results

![](_page_24_Figure_5.jpeg)

![](_page_24_Picture_8.jpeg)

## **Back-up slides**

![](_page_25_Picture_1.jpeg)

# Data driven measurements of short and long distance interference

Following the notation of Ref. [40], the *CP*-averaged differential decay rate of  $B^+ \rightarrow K^+ \mu^+ \mu^-$  decays as a function of the dimuon mass squared,  $q^2 \equiv m_{\mu\mu}^2$ , is given by

$$\frac{\mathrm{d}\Gamma}{\mathrm{d}q^2} = \frac{G_F^2 \alpha^2 |V_{tb} V_{ts}^*|^2}{128\pi^5} |\mathbf{k}| \beta \left\{ \frac{2}{3} |\mathbf{k}|^2 \beta^2 \left| \mathcal{C}_{10} f_+(q^2) \right|^2 + \frac{4m_\mu^2 (m_B^2 - m_K^2)^2}{q^2 m_B^2} \left| \mathcal{C}_{10} f_0(q^2) \right|^2 + |\mathbf{k}|^2 \left[ 1 - \frac{1}{3} \beta^2 \right] \left| \mathcal{C}_9 f_+(q^2) + 2\mathcal{C}_7 \frac{m_b + m_s}{m_B + m_K} f_T(q^2) \right|^2 \right\}, \tag{1}$$

where  $|\mathbf{k}|$  is the kaon momentum in the  $B^+$  meson rest frame. The parameters  $f_{0,+,T}$  denote the scalar, vector and tensor  $B \to K$  form factors.

 $\mathcal{C}_9^{\text{eff}} = \mathcal{C}_9 + Y(q^2),$  Insert term into eq. above

where the term  $Y(q^2)$  describes the sum of resonant and continuum hadronic states appearing in the dimuon mass spectrum. In this analysis  $Y(q^2)$  is replaced by the sum of vector meson resonances j such that If n\*pi/2 term disappears in eq.1

assumes no continuum 
$$C_9^{\text{eff}} = C_9 + \sum_j \eta_j e^{\frac{i \delta_j}{2}} A_j^{\text{res}}(q^2),$$
 (3)

where  $\eta_j$  is the magnitude of the resonance amplitude and  $\delta_j$  its phase relative to  $C_9$ .

## CPV in $\Lambda^0_b \to p K \mu^+ \mu^-$

Baryon production asymmetries not well known: use  $\Delta A_{cp}$  and triple products Sensitivity of methods may differ depending on strong phase interference

 $\hat{T}_{even}, \hat{T}_{odd}$  amplitudes  $a_{CP}^{\hat{T}-odd} \propto \cos(\delta_{even} - \delta_{odd})\sin(\phi_{even} - \phi_{odd})$ not sensitive if  $\delta_{even} - \delta_{odd} = \pi/2$  or  $3\pi/2$ 

### A<sub>1</sub>, A<sub>2</sub> amplitudes

$$\mathcal{A}_{CP} \propto sin(\delta_1 - \delta_2)sin(\phi_1 - \phi_2)$$

not sensitive if  $\delta_1 - \delta_2 = 0$  or  $\pi$ 

- $\delta$  = strong phase,  $\phi$  = weak phase
  - Measure  $\Delta A_{CP} = A_{CP}(\Lambda_b^0 \to pK^-\mu^+\mu^-) A_{CP}(\Lambda_b^0 \to J/\psi \, pK^-)$
  - $\Delta A_{CP}$  = ( -3.5 ± 5.0 (stat) ± 0.2 (syst)) ×10<sup>-2</sup> → no significant CPV

![](_page_27_Picture_12.jpeg)

### $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ : S-wave pollution

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- S wave:  $K^+\pi^-$  doesn't come from  $K^{*0}$  (P-wave) but from spin 0 configuration
- Introduces additional terms in decay amplitude

$$\frac{1}{\mathrm{d}(\Gamma+\bar{\Gamma})/\mathrm{d}q^2} \frac{\mathrm{d}^3(\Gamma+\bar{\Gamma})}{\mathrm{d}\vec{\Omega}} \bigg|_{\mathrm{S}+\mathrm{P}} = (1-F_{\mathrm{S}}) \frac{1}{\mathrm{d}(\Gamma+\bar{\Gamma})/\mathrm{d}q^2} \frac{\mathrm{d}^3(\Gamma+\bar{\Gamma})}{\mathrm{d}\vec{\Omega}} \bigg|_{\mathrm{P}} + \frac{3}{16\pi} F_{\mathrm{S}} \sin^2 \theta_{\ell} + \text{S-P interference}$$

$$\frac{1}{\mathrm{d}(\Gamma+\bar{\Gamma})/\mathrm{d}q^2} \frac{\mathrm{d}(\Gamma+\bar{\Gamma})}{\mathrm{d}\cos\theta_l \,\mathrm{d}\cos\theta_K \,\mathrm{d}\phi}\Big|_{\mathrm{S+P}} = (1-F_S) \frac{1}{\mathrm{d}(\Gamma+\bar{\Gamma})/\mathrm{d}q^2} \frac{\mathrm{d}(\Gamma+\bar{\Gamma})}{\mathrm{d}\cos\theta_l \,\mathrm{d}\cos\theta_K \,\mathrm{d}\phi}\Big|_{\mathrm{P}} \\ + \frac{3}{16\pi} \Big[F_S \sin^2\theta_l + S_{S1} \sin^2\theta_l \cos\theta_K \\ + S_{S2} \sin2\theta_l \sin\theta_K \cos\phi \\ + S_{S3} \sin\theta_l \sin\theta_K \cos\phi \\ + S_{S4} \sin\theta_l \sin\theta_K \sin\phi \\ + S_{S5} \sin2\theta_l \sin\theta_K \sin\phi \Big].$$

- To determine *F<sub>s</sub>* more precisely, exploit difference in *m<sub>K<sup>+</sup>π<sup>-</sup></sub>* mass shape between P-, S-wave and fit simultaneously to *m<sub>K<sup>+</sup>π<sup>-</sup></sub>*
- $m_{K^+\pi^-}$  line shape in S-wave: LASS model (Nucl. Phys. B296 (1988) 493), P-wave, Breit-Wigner Beauty 2018 (7-11 May 2018) Eluned Smith

### Analysis statistically dominated (and still will be in Run 2)

Source	$F_{\rm L}$	$S_3 - S_9$	$A_3 - A_9$	$P_1 - P_8'$
Acceptance stat. uncertainty	< 0.01	< 0.01	< 0.01	< 0.01
Acceptance polynomial order	< 0.01	< 0.02	< 0.02	< 0.04
Data-simulation differences	0.01 - 0.02	< 0.01	< 0.01	< 0.01
Acceptance variation with $q^2$	< 0.01	< 0.01	< 0.01	< 0.01
$m(K^+\pi^-)$ model	< 0.01	< 0.01	< 0.01	< 0.03
Background model	< 0.01	< 0.01	< 0.01	< 0.02
Peaking backgrounds	< 0.01	< 0.01	< 0.01	< 0.01
$m(K^+\pi^-\mu^+\mu^-)$ model	< 0.01	< 0.01	< 0.01	< 0.02
Det. and prod. asymmetries	-	_	< 0.01	< 0.02

### $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ : J terms

Definition of  $J_i$  terms in decay rate (the complex amplitudes are the terms which are sensitive to the Wilson coefficients):

$$\begin{split} J_1^s &= \frac{(2+\beta_{\mu}^2)}{4} \Big[ |A_{\perp}^L|^2 + |A_{\parallel}^L|^2 + (L \to R) \Big] + \frac{4m_{\mu}^2}{q^2} \Re e(A_{\perp}^L A_{\perp}^{R*} + A_{\parallel}^L A_{\parallel}^{R*}) \\ J_1^c &= |A_0^L|^2 + |A_0^R|^2 + \frac{4m_{\mu}^2}{q^2} \big[ |A_t|^2 + 2\Re e(A_0^L A_0^{R*}) \big] \\ J_2^s &= \frac{\beta_{\mu}^2}{4} \Big[ |A_{\perp}^L|^2 + |A_{\parallel}^L|^2 + (L \to R) \Big] \\ J_2^s &= -\beta_{\mu}^2 \Big[ |A_{0}^L|^2 + (L \to R) \Big] \\ J_3 &= \frac{\beta_{\mu}^2}{2} \Big[ |A_{\perp}^L|^2 - |A_{\parallel}^L|^2 + (L \to R) \Big] \\ J_4 &= \frac{\beta_{\mu}^2}{\sqrt{2}} \Big[ \Re e(A_{0}^L A_{\parallel}^{L*}) - (L \to R) \Big] \\ J_5 &= \sqrt{2}\beta_{\mu} \Big[ \Re e(A_{\perp}^L A_{\perp}^{L*}) - (L \to R) \Big] \\ J_7 &= \sqrt{2}\beta_{\mu} \Big[ \Re e(A_{0}^L A_{\perp}^{L*}) - (L \to R) \Big] \\ J_8 &= \frac{\beta_{\mu}^2}{\sqrt{2}} \Big[ \Im m(A_{0}^L A_{\perp}^{L*}) + (L \to R) \Big] \\ J_9 &= \beta_{\mu}^2 \Big[ \Im m(A_{\perp}^L A_{\perp}^{L*}) + (L \to R) \Big] \end{split}$$

with  $\beta_{\mu}^2 = (1 - 4m(\mu)^2/q^2)$ . The angular distribution therefore depends on 7  $q^2$  dependent complex amplitudes  $(A_0^{L,R}, A_{\parallel}^{L,R}, A_{\perp}^{L,R} \text{ and } A_t)$  corresponding to different polarisation states of the  $B \to K^*V^*$  decay.

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### The LHCb detector

The LHCb detector is a single arm spectrometer which covers the forward region at LHC.

![](_page_31_Figure_2.jpeg)

 $\Delta p/p \sim 0.4\%$  at 5 GeV,  $\sigma_{IP} = 20 \ \mu m$  for high  $p_T$  tracks.  $\pi/K$  separation:  $\epsilon_K \sim 90\%$ , 5%  $\pi \rightarrow K$  mis-id.  $\pi/\mu$  separation:  $\epsilon_\mu \sim 97\%$ , 1-3%  $\pi \rightarrow K$  mis-id.

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![](_page_31_Picture_7.jpeg)

- The excellent agreement with theory of flavour measurements places stringent constraints on the mass scale,  $\Lambda$ , of new physics  $\rightarrow$  if new physics is assumed to have a generic flavour structure of  $\mathcal{O}(1) \rightarrow \Lambda$  as high as 10<sup>4</sup> TeV (Ann.Rev.Nucl.Part.Sci.60:355, 2010)
- The MFV hypothesis offers solution to this flavour problem: Assume NP flavour structure = SM flavour structure
- Comparing the CKM elements obtained via loop and tree level processes tests the MFV hypothesis.

![](_page_32_Picture_7.jpeg)