Equation of state of dense nuclear matter and neutron star structure from nuclear chiral interactions

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Cortona

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- A study of infinite hadronic matter with modern chiral interactions...

motivations:

1) Strongly correlated to the physics of hypernuclei

2) Determination of symmetry energy

3) Study of astrophysical systems: neutron stars, supernovae and mergers

Hadronic matter

- System of $A = N + Z + Y$ hadrons in a volume V
- Thermodynamical limit: $A \to +\infty$ and $V \to +\infty$ with $\frac{A}{V} = \rho = const.$
- Asymmetry between number of N and number of $Z \Rightarrow \beta = \frac{N-Z}{N+Z}$, strangeness fraction $y = Y/A$

How to study it?

- Relativistic mean field (Hartree) $\Rightarrow \mathcal{L}$ (QFT) $\Rightarrow$ Eulero-Lagrange equations solved in mean field approximation.
- Relativistic mean field (Hartree-Fock) $\Rightarrow \mathcal{L}$ (QFT) $\Rightarrow$ Eulero-Lagrange equations solved in mean field approximation.
- Skyrme models $\Rightarrow$ effective nuclear interaction
- Ab initio approaches $\Rightarrow$ Brueckner-Hartree-Fock, Quantum-Monte-Carlo, Self-consistent Green function $\Rightarrow$ start from microscopic potentials explicitly including many-body forces.

The Brueckner-Hartree-Fock approach

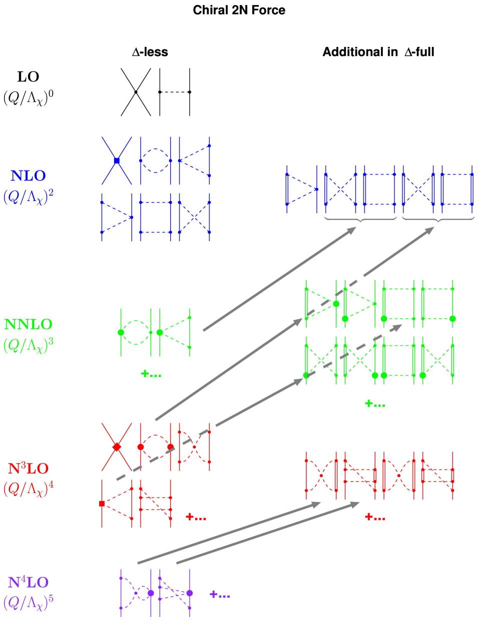
- Starting point: the Bethe-Goldstone equation

$$G(\omega)_{B_1B_2,B_3B_4} = V_{B_1B_2,B_3B_4} + \sum_{B_iB_j} V_{B_1B_2,B_iB_j} \times \frac{Q_{B_iB_j}}{\omega - E_{B_i} - E_{B_j} + i\eta} G(\omega)_{B_iB_j,B_3B_4}$$

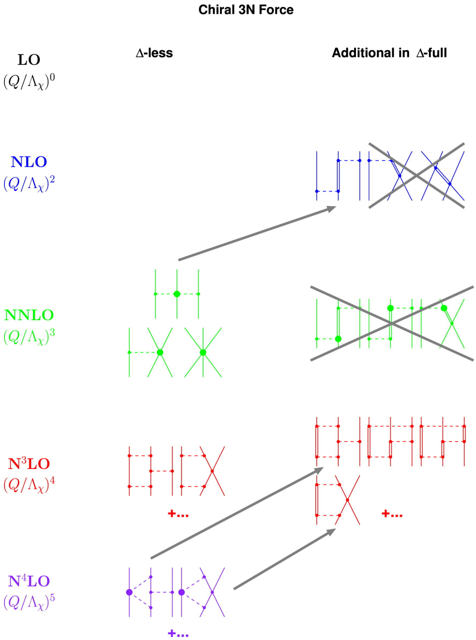
$$U_{B_i}(k) = \sum_{B_j} \sum_{\vec{k'}} n_{B_j}(|\vec{k'}|) \times \langle \vec{k}\vec{k'} | G(E_{B_i}(\vec{k}) + E_{B_j}(\vec{k'}))_{B_iB_j,B_iB_j} | \vec{k}\vec{k'} \rangle_{\mathcal{A}}$$

$$E_{B_i}(k) = M_{B_i} + \frac{\hbar^2 k^2}{2M_{B_i}} + U_{B_i}(k)$$

$$\epsilon_{BHF} = \frac{1}{V} \sum_{B_i} \sum_{k \le k_{F_i}} \left[M_{B_i} + \frac{\hbar^2 k^2}{2M_{B_i}} + \frac{1}{2} U_{B_i}(k) \right]$$


Chiral 2N Force
Δ-less
Additional in Δ-full
LO
$(Q/\Lambda_\chi)^0$
NLO
$(Q/\Lambda_\chi)^2$
NNLO
$(Q/\Lambda_\chi)^3$
+...
+...
N^{3}LO
$(Q/\Lambda_\chi)^4$
+...
+...
N^{4}LO
$(Q/\Lambda_\chi)^5$
+...

NNN chiral forces



- NN potentials: non local N3LO (Idaho-2003), minimal local N3LOΔ (M. Piarulli-2014)
- N3LO (Idaho-2003) $\Rightarrow$ in $\mathcal{L}$ included N, π
- N3LOΔ (M. Piarulli-2014) $\Rightarrow$ in $\mathcal{L}_{eff}$ included N, π and Δ
- NNN potential: N2LO and N2LOΔ

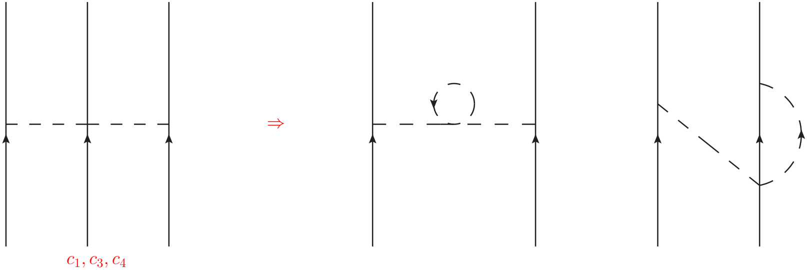
- BHF calculations with NNN forces ⇒ very challenging

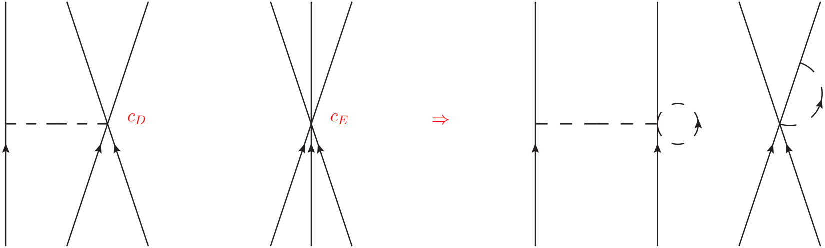
⇓

- NNN force is reduced to a NN density dependent one
- In p-space:

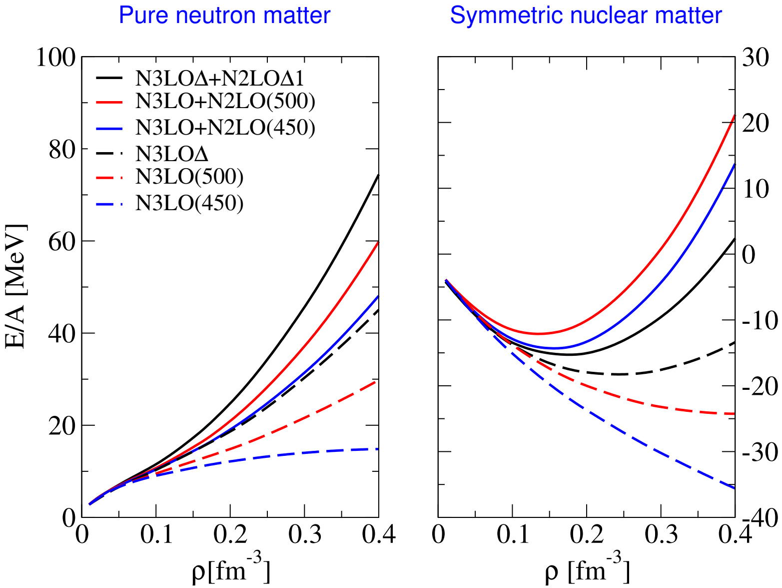
$$W_{eff}(1,2) = Tr_{\sigma_3\tau_3} \int dp_3 \sum_{cyc} W(1,2,3)\, n(3)(1 - P_{13} - P_{23})$$

Momentum space average of N2LO TBF (J. W. Holt et al. 2010)





E/A nuclear matter N3LO+N2LO



Logoteta et al. Phys. Rev. C 94, 064001 (2016)

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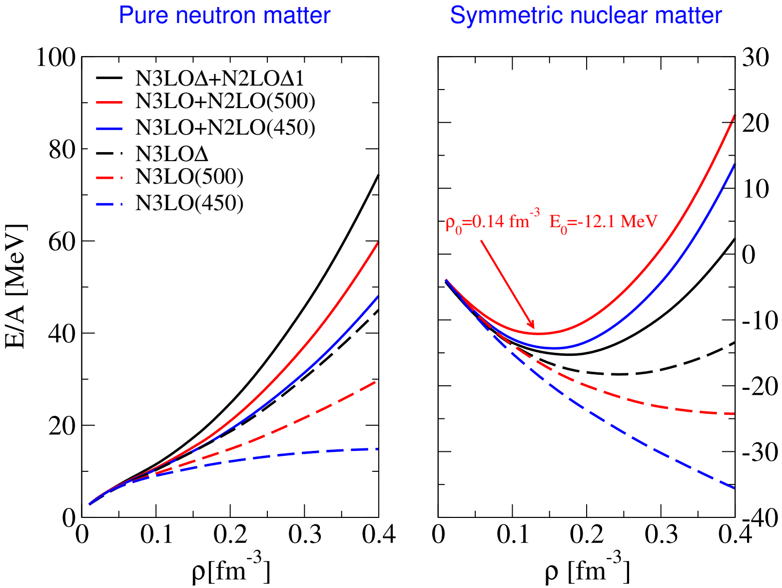

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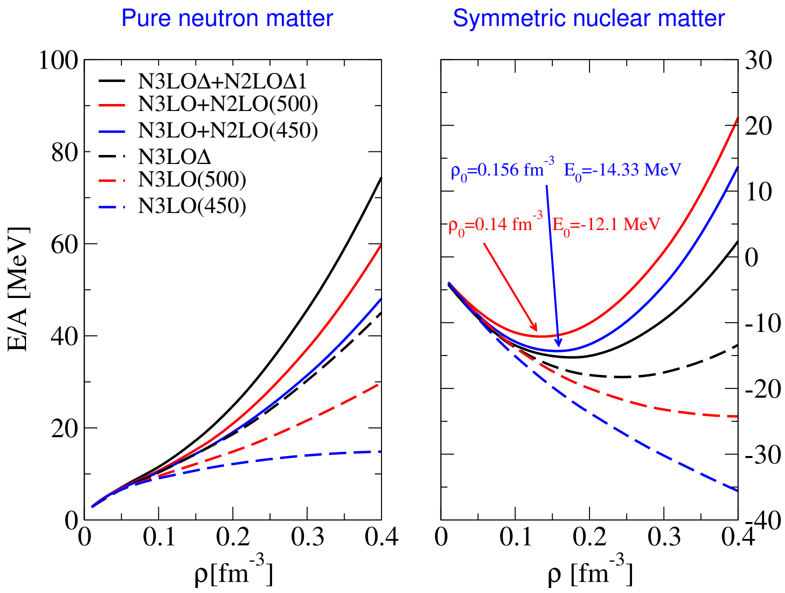

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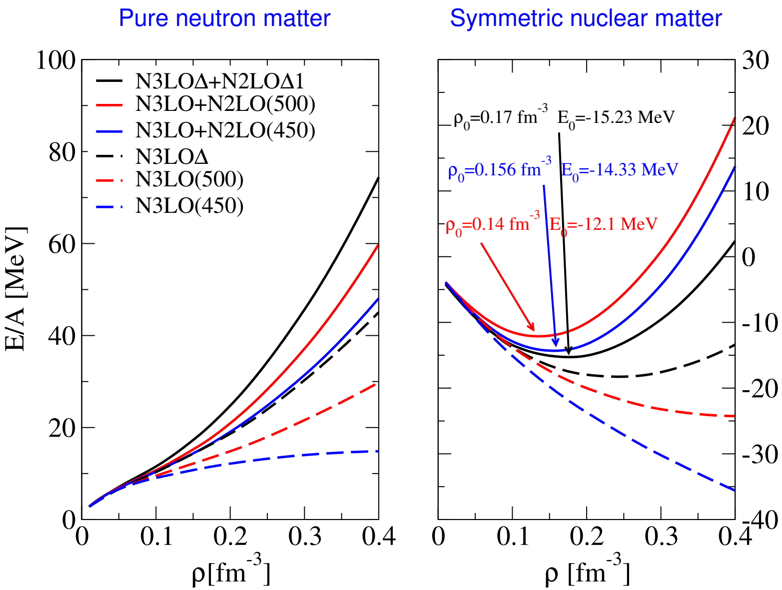

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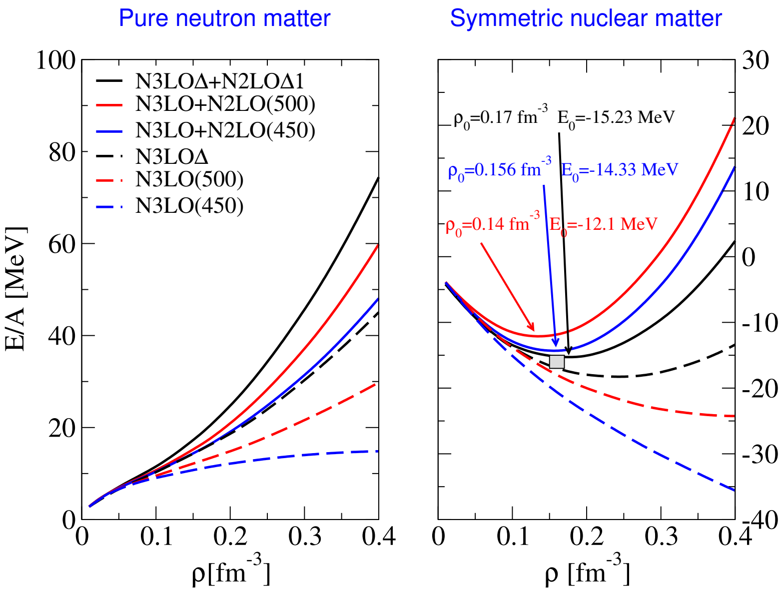

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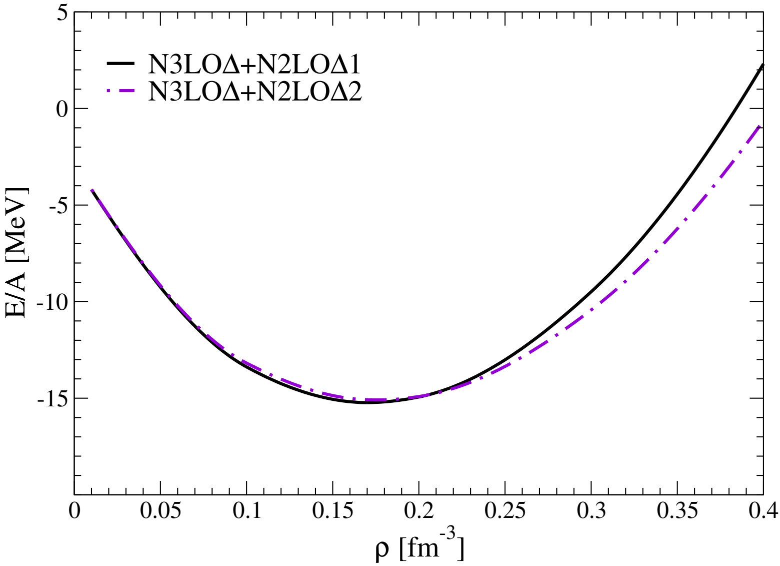
Symmetric nuclear matter: comparision between N2LOΔ1 and N2LOΔ2



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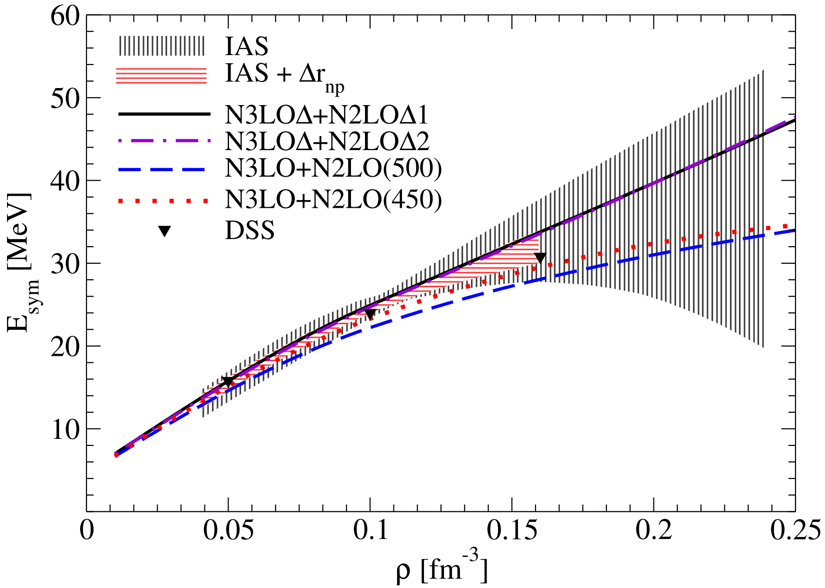
Symmetry energy N3LO+N2LO



Logoteta et al. Phys. Rev. C 94, 064001 (2016)

- Asymmetric matter $\Rightarrow$ parabolic approximation:

$$E/A(\beta,\rho) = (E/A(\rho))_{snm} + (E/A(\rho))_{sym}\beta^2 \qquad \beta = \frac{\rho_n - \rho_p}{\rho_n + \rho_p}$$

$$\mu_i = \frac{\partial(\rho E/A(\beta,\rho))}{\partial \rho_i} \qquad \rho = \rho_n + \rho_p$$

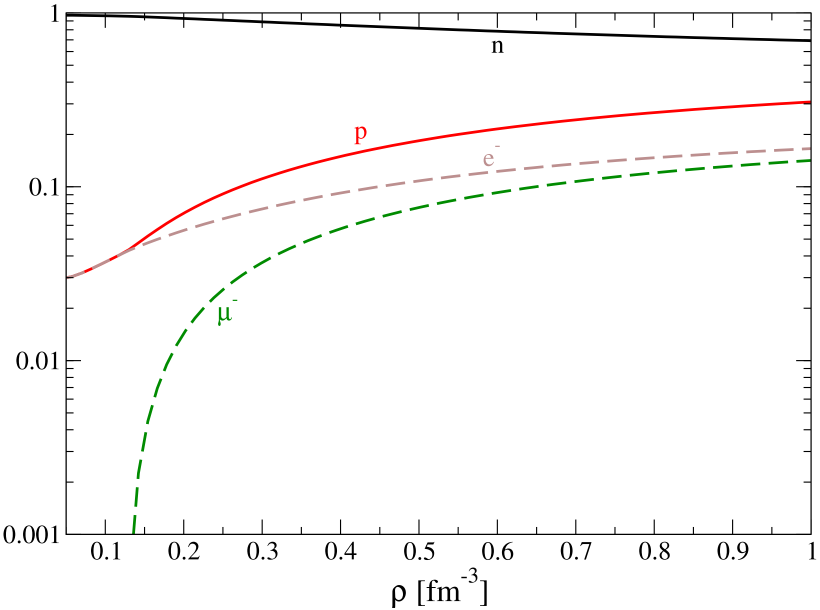
- Chemical equilibrium:

$$\mu_n - \mu_p = \mu_e \qquad \mu_e = \mu_\mu .$$

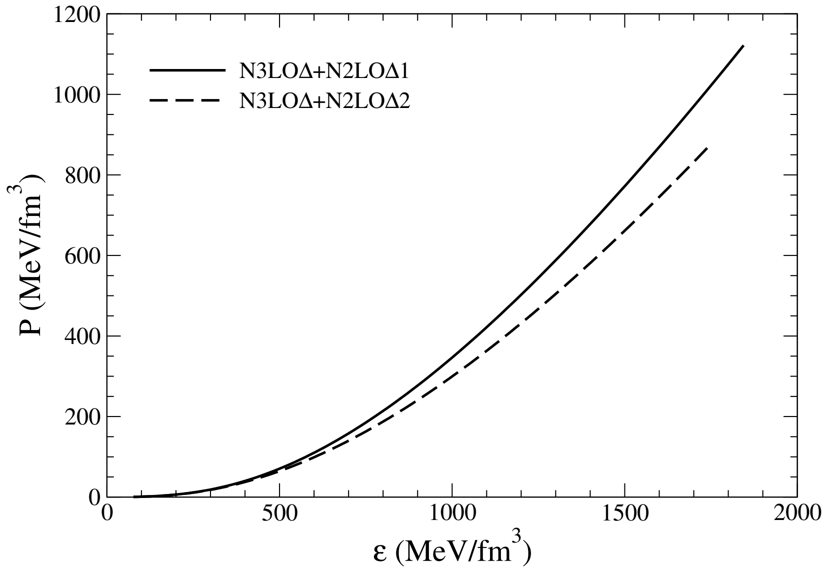
- Charge neutrality:

$$n_p - n_\mu - n_e = 0\,.$$

Particle fractions in $\beta-$stable matter N3LOΔ+N2LOΔ



EOS $\beta-$stable matter N3LOΔ+N2LOΔ



Submitted to A&A

- For a fixed equation of state (EOS): $P = P(\rho)$ and $P = P(n_B)$

$\Downarrow$

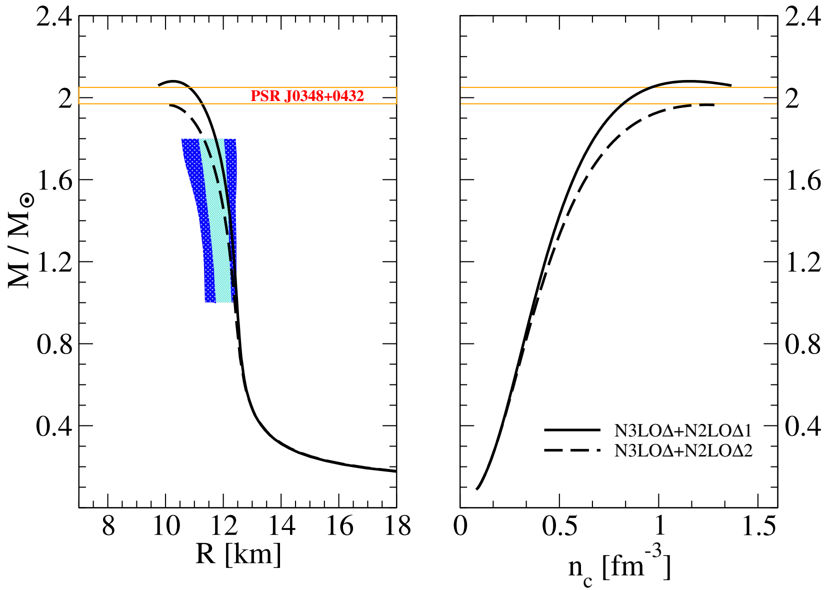
Neutron stars structure $\Rightarrow$ TOV equations

Equations of hydrostatic equilibrium in general relativity of Tolman-Oppenheimer-Volkoff (TOV):

$$\frac{dP}{dr} = -\frac{G\rho m}{r^2}\left(1 + \frac{P}{\rho c^2}\right)\left(1 + \frac{4\pi P r^3}{mc^2}\right)\left(1 - \frac{2Gm}{rc^2}\right)^{-1},$$

$$\frac{dm(r)}{dr} = 4\pi r^2 \rho \, .$$

Neutron stars based on N3LOΔ+N2LOΔ



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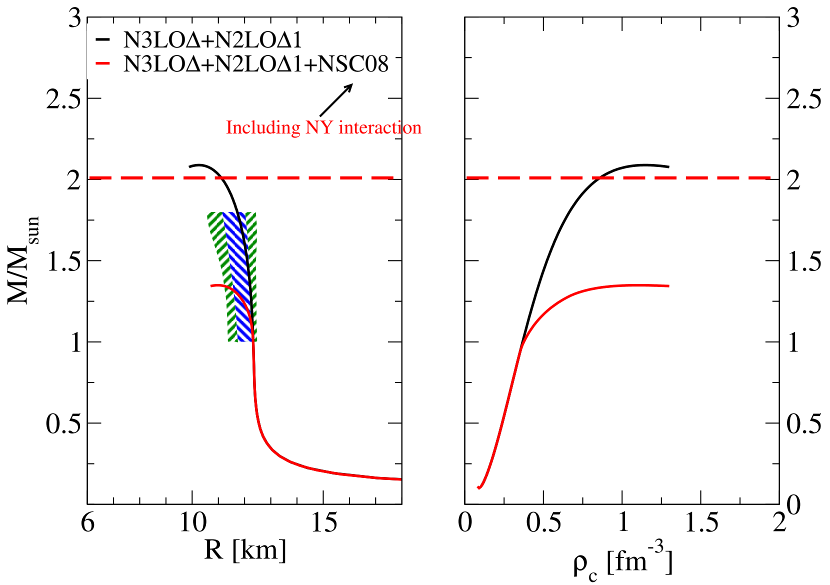
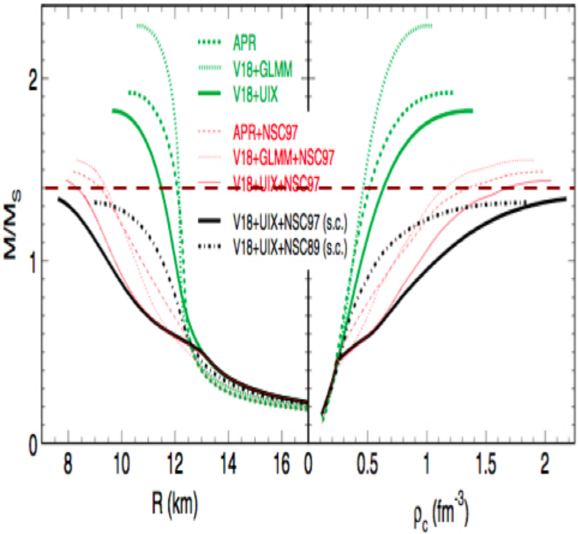
Neutron stars based on N3LOΔ+N2LOΔ+NY



The problem of the maximum mass of neutron stars with microscopic approaches

H.-J. Schulze et al. Phys. Rev. C 73, 058801 (2006)



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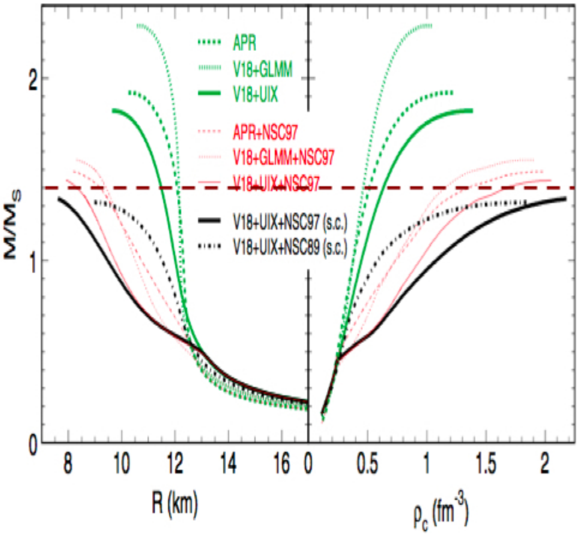

- $n + n \to n + \Lambda$
- $n + n \to p + \Sigma^-$
- $p + e^- \to \Lambda + \nu_{e^-}$
- $n + e^- \to \Sigma^- + \nu_{e^-}$

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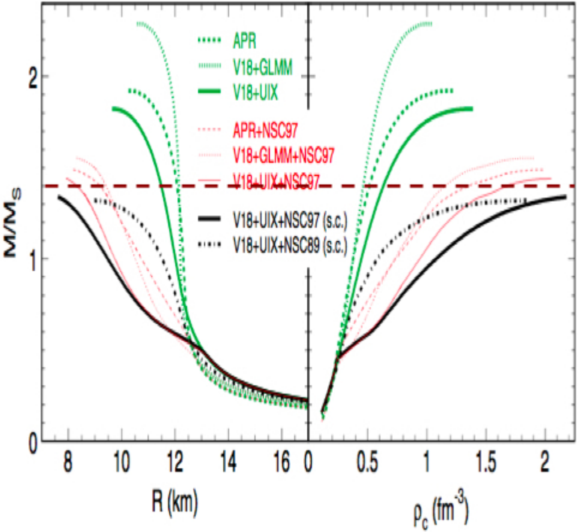
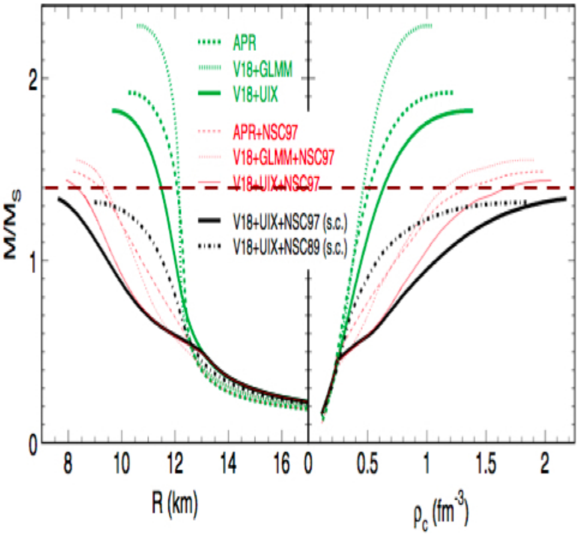


- $n + n \rightarrow n + \Lambda$
- $n + n \rightarrow p + \Sigma^-$
- $p + e^- \rightarrow \Lambda + \nu_{e^-}$
- $n + e^- \rightarrow \Sigma^- + \nu_{e^-}$
- Appearance of Hyperons ⇒ Fermi pressure relieves
- $M_{max} < 1.44\ M_\odot$

H.-J. Schulze et al. Phys. Rev. C 73, 058801 (2006)



- Recent measurements:
- $M_{PRS}^{J1903+0327} = 1.67\ M_\odot$
- $M_{PRS}^{J1614-2230} = 1.97\ M_\odot$
- $M_{PRS}^{J0348+0432} = 2.01\ M_\odot$

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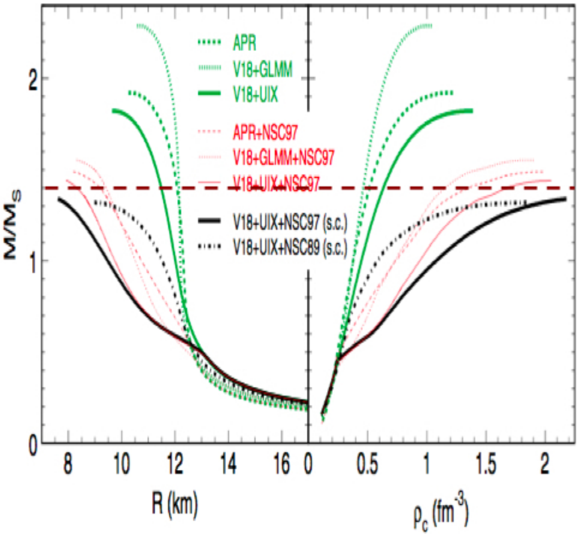

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DRAMMATIC SCENARIO!!

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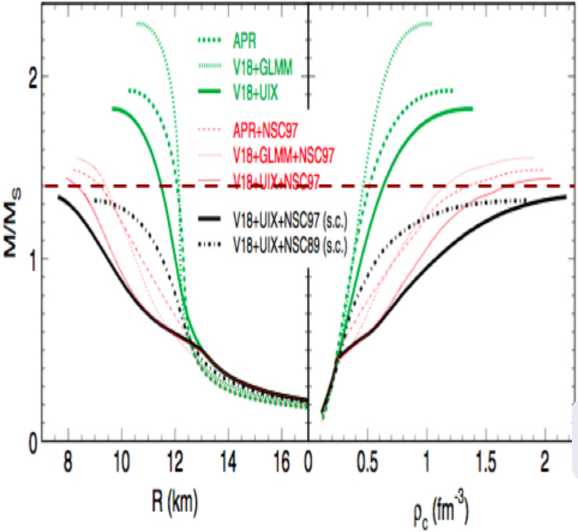

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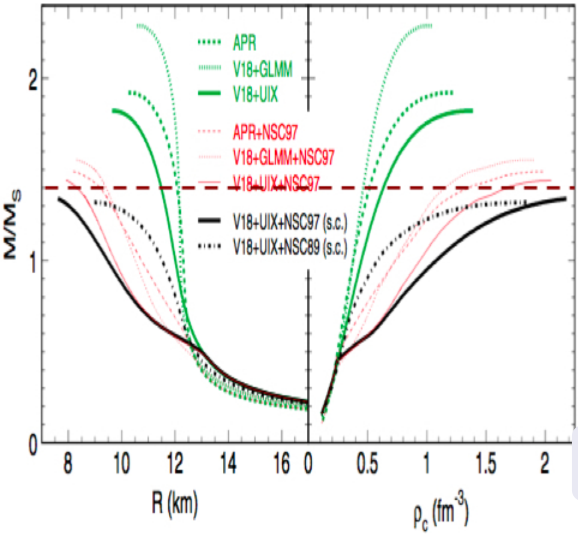
DRAMMATIC SCENARIO!!

NNY, NYY and YYY may help??

H.-J. Schulze et al. Phys. Rev. C 73, 058801 (2006)



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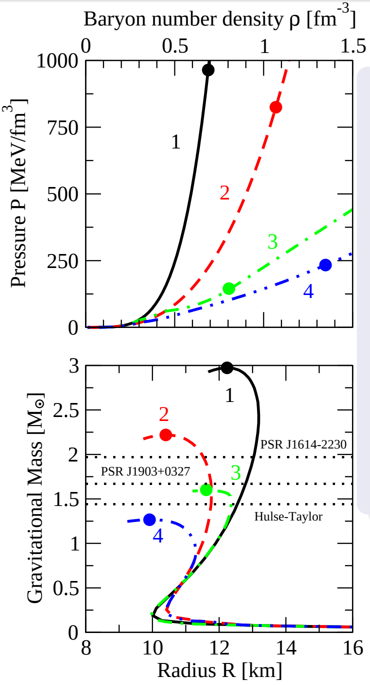
DRAMMATIC SCENARIO!!

We focused on the NNY interactions

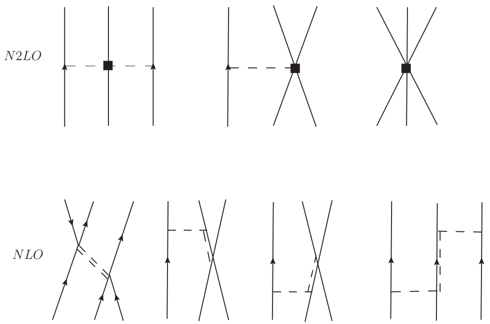


γ_{NN}	x	γ_{YN}	M_{max}
	0	-	1.27 (2.22)
	1/3	1.49	1.33
2	2/3	1.69	1.38
	1	1.77	1.41
	0	-	1.29 (2.46)
	1/3	1.84	1.38
2.5	2/3	2.08	1.44
	1	2.19	1.48
	0	-	1.34 (2.72)
	1/3	2.23	1.45
3	2/3	2.49	1.50
	1	2.62	1.54
	0	-	1.38 (2.97)
	1/3	2.63	1.51
3.5	2/3	2.91	1.56
	1	3.05	1.60

$$1.27\ M_\odot < M_{max} < 1.6\ M_\odot$$

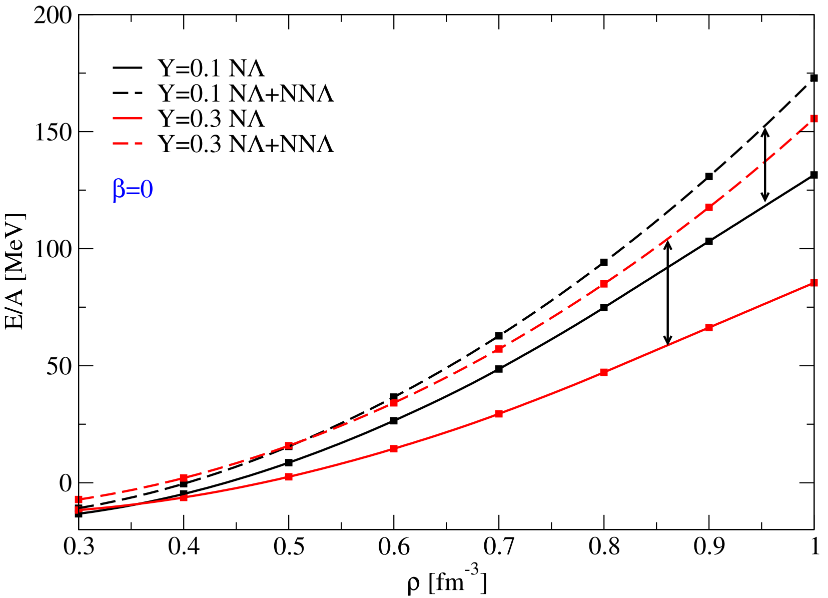
I. Vidana, D. Logoteta, C. Providencia, A. Polls, I. Bombaci EPL 94, 11002 (2011)

NNΛ force from ChPT

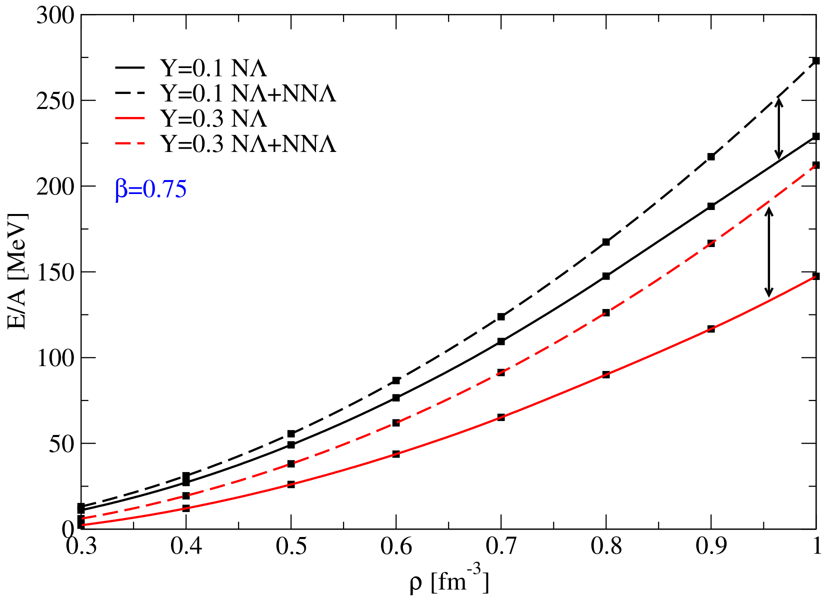


- Following Petschauer (2013)
- Baryonic three-body forces from chiral effective field theory
- Nonvanishing leading order contributions at order NLO and N2LO
- Same strategy used for nuclear matter
- Effective NΛ interaction from bare NNΛ force
- Low energy constants estimated from decuplet saturation

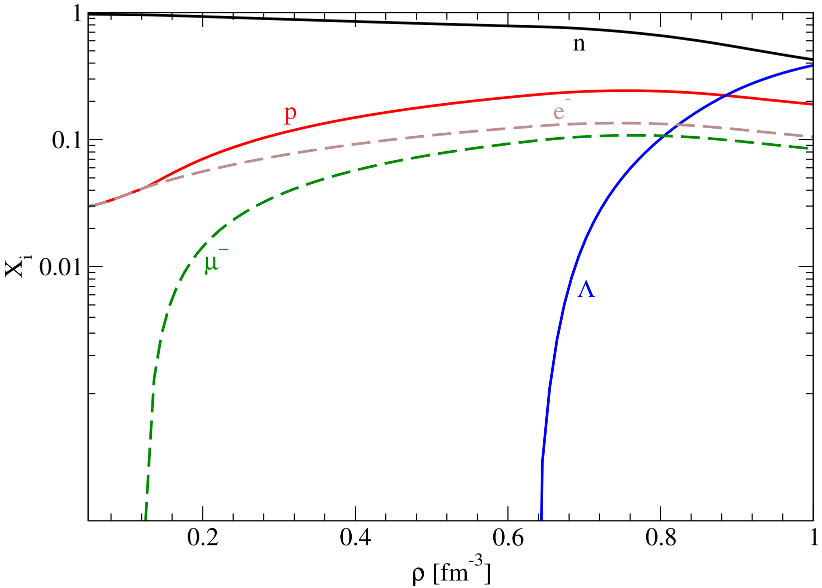
Effect of hyperonic three-body force NNΛ



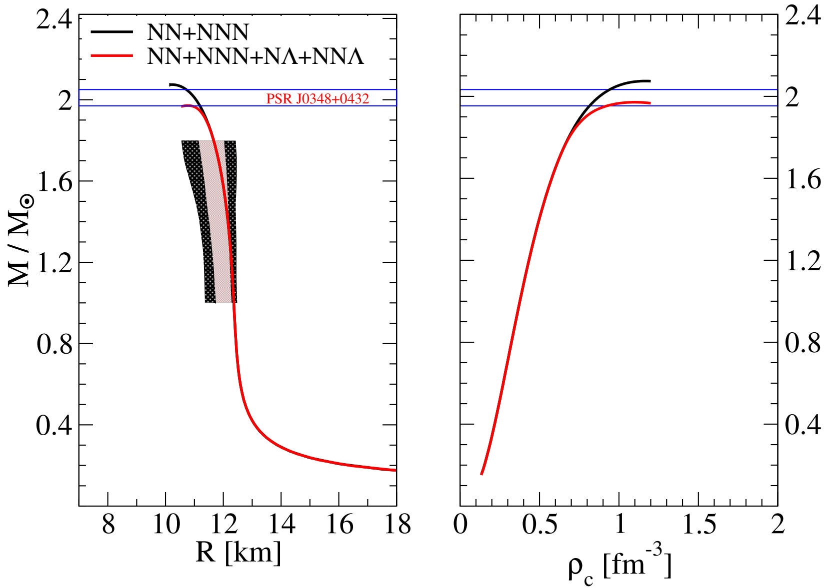
Effect of hyperonic three-body force NNΛ



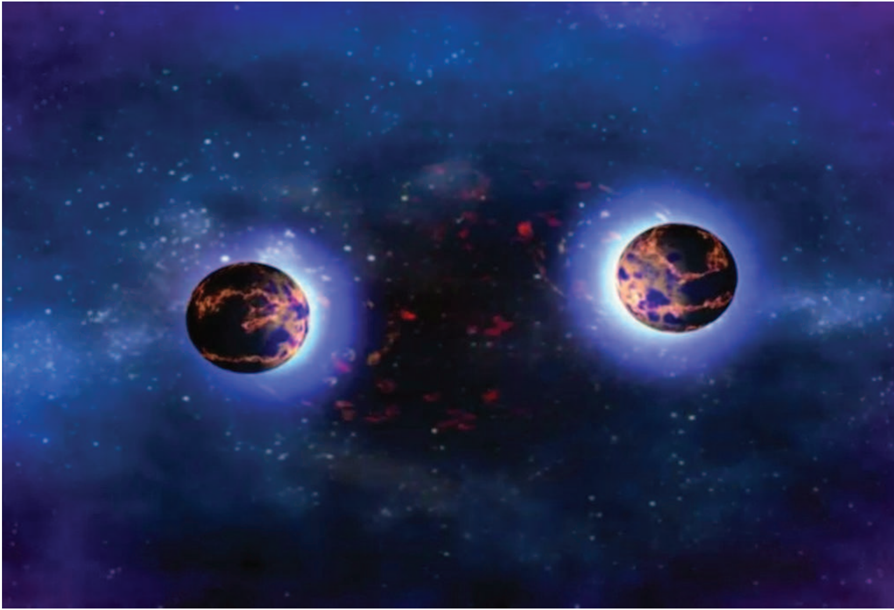
Effect of hyperonic three-body force NNΛ on $\beta-$stable composition



Neutron stars based on N3LOΔ+N2LOΔ+NΛ+NNΛ



Neutron stars merge



Supernova explosions

Conclusions

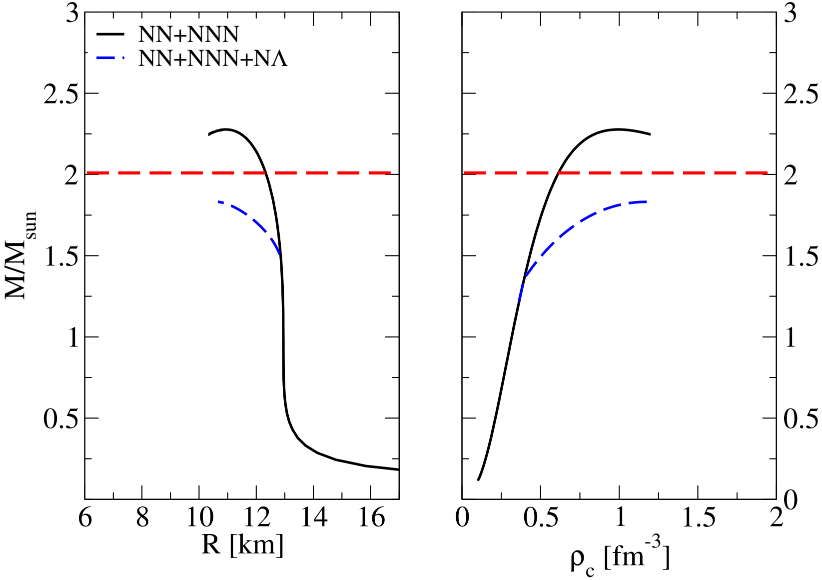
- A reasonable description of nuclear matter based on ChEFT is possible
- A full study of β-stable hyperonic matter based on NY, NNY chiral is under development.
- ...but...how work chiral NY and NNY interactions in hypernuclei?

$$\Downarrow$$

- Problem of maximum mass of neutron stars with hyperons.
- More experimental effort is required to improve the quality of NY, YY and NNY interactions!!!

Thank you!

A simplified model of neutrons and Λ's matter...



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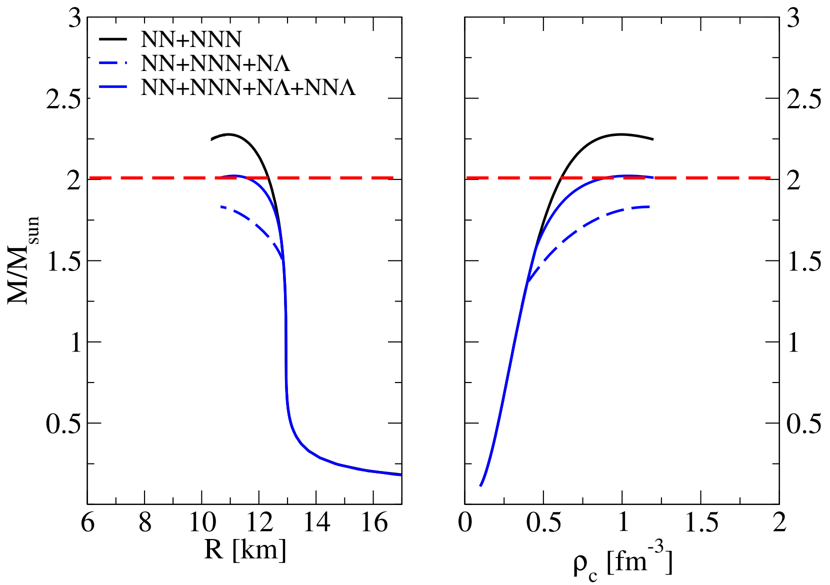
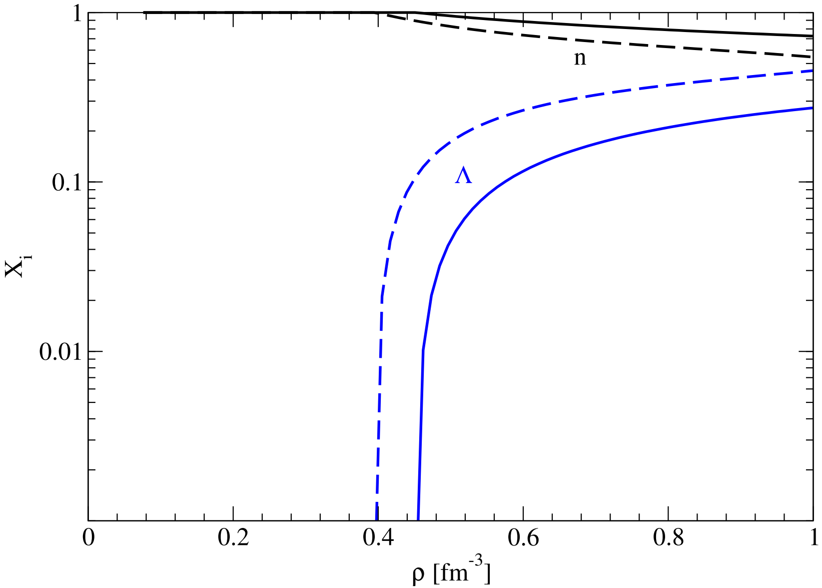


Particle fractions for neutrons and Λ's matter



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