## STRENGTH

# STructure and REaction Nuclei: towards a Global THeory



## TNPI2017 - XVI Conference on Theoretical Nuclear Physics in Italy

3-5 October 2017

Cortona Europe/Rome timezone



## **STRENGTH**

Started in 2014 with the aim to combine the diverse and complementary expertise of the main Italian theoretical groups working in the fields of nuclear structure and reaction dynamics with hadronic probes in order to better confront the new challenges arising from the Radioactive Ion Beam Facilities



Sede	Responsabile	FTE
MI	Enrico Vigezzi	2.5
PD	Lorenzo Fortunato	5.2
PI	Angela Bonaccorso	1.0
NA	Angela Gargano	7.2
CT	Edoardo Lanza	2.0
LNS	Maria Colonna	2.8
		20.7

\* anno di riferimento 2018

# Ric.	Ass. senior	Non strutturati
26	2	7

## 1. Development and application of models for nuclear structure studies

- Shell model
- Density functional theory and its extensions
- Microscopic and algebraic cluster models

All based on the use of effective interactions (microscopic or phenomenological) to account for the reduction in the number of degrees of freedom explicitly considered, namely the dimension of the basis spaces or the form of many-body wave functions

- 1. Construction of effective interactions
- 2. Assessment and extensions of the models
- 3. Calculations of bulk/spectroscopic properties, reaction observables and comparison with experiment

The complementary nature of these approaches may be of help to acquire a more comprehensive understanding of the studied phenomena. *Key questions,* as the role of the various components of nuclear force or the interplay of single-particle and collective modes, can be tackled thus providing insights on different aspects of the nuclear problem



## 2. Dynamics of nuclear excitations and reaction mechanisms

- Heavy ion collisions from the Coulomb barrier up to the Fermi energies involving different reaction mechanisms (fusion-fission, deep-inelastic and charge equilibration, inelastic collisions leading to collective excitations) between neutron-rich systems in the framework of semi-classical or microscopic theories
- Collisions dominated by peripheral, direct mechanisms such as transfer, charge exchange and breakup direct reactions
- Determination of optical potentials for total reaction cross section calculations, elastic scattering and knockout involving light exotic nuclei

In these studies, attention is payed to the underlying structure models and the effective interactions with the aim of reaching a description as coherent as possible of both nuclear structure and reaction dynamics





## STRENGTH

Strong support to the experimentalists in the analysis of recent experimental data on exotic nuclei as well as in the proposal of new "key" experiments, in particular to the Italian project SPES @ LNL







## 1. Many-body correlations and nuclear structure properties

2. Collective modes in neutron rich nuclei

3. Direct reactions





## Many-body correlations and nuclear structure properties

#### **Shell model**

Reduced number of active nucleons in a truncated space

$$H_{\text{eff}} = \sum_{i=1}^{\mathcal{N}} h_i + \sum_{i < j=1}^{\mathcal{N}} V_{ij}$$

Excluded degrees of freedom taken into account through effective interactions and operators

- J. Bonnard, S.M. Lenzi, A.P. Zuker, PRL 116, 212501 (2016)
- Talk by L. De Angelis
- Talk by T. Fukui

Beyond the DFT Particle vibration coupling approaches

Collective vibrations & single particles as relevant building blocks *H* = *H*'<sub>sp</sub> + *H*<sub>B</sub> + *h h* = interaction between particles and vibrations

→ diagonalized or treated perturbatively

G. Colò, P. F. Bortignon, G. Bocchi, PRC 95, 034303 (2017)

F. Barranco, G. Potel, R.A. Broglia, E. Vigezzi PRL 119, 082501

(2017)

Talk by E. Vigezzi

#### **Cluster models**

Aggregates of nucleons, and in particular four-body correlated systems, as relevant building blocks

- $\alpha$ -cluster model based on group-theory G. Stellin, L. Fortunato, A. Vitturi, JPG 43 (2016) 085104
- microscopic quartet model Talk by M. Sambataro

## Hybrid configuration mixing model for odd nuclei

Many body correlations

G. Colò, P. F. Bortignon, G. Bocchi, PRC 95, 034303 (2017)



\*  $|[j' \otimes NJ]_{jm}\rangle$  basis  $\rightarrow$  nonorthogonal and overcomplete!







#### Structure and Reactions of <sup>11</sup>Be: Many-Body Basis for Single-Neutron Halo F. Barranco, G. Potel, R.A. Broglia, E. Vigezzi PRL 119, 082501 (2017)

- **Renormalized nuclear field theory**
- $p_{3/2}$ ,  $p_{1/2}$ ,  $s_{1/2}$ ,  $d_{5/2}$  single-particle states up  $E_{cut}$ =25 MeV
- Coupling to quadrupole collective vibrations of <sup>10</sup>Be
- Mixing between bound and continuum states
- $\rightarrow$  3 parameters for the 2<sup>+</sup> vibration (exp) + 4 for the bare mean field (fit)

Effects due to octupole and pair removal modes of <sup>10</sup>Be are marginal





**Diagrams describing the main self-consistent** renormalization processes of the SP energies Bold lines describe dressed particle/hole states

Many body correlations



- ✓ Renormalized nuclear field theory
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**Diagrams describing the main self-consistent renormalization processes of the SP energies** Bold lines describe dressed particle/hole states

### Why a NFT calculation? when <sup>11</sup>Be can be studied with *ab initio* approaches.



#### Better framework to clarify

- Role of the mean field
- Mechanism behind the parity inversion
- Role of the continuum states in exotic nuclei

No-core shell model with continuum - A. Calci, et al., PRL 117, 242501 (2016)

## Results



Parity inversion between the  $1p_{1/2}$  and  $2s_{1/2}$  & position/width of  $5/2^+$  resonance  $\rightarrow$  reproduced!

$$\begin{split} |\widetilde{1/2^+}\rangle &= \sqrt{0.80} |s_{1/2}\rangle + \sqrt{0.20} |(d_{5/2} \otimes 2^+)_{1/2^+}\rangle, \\ |\widetilde{1/2^-}\rangle &= \sqrt{0.84} |p_{1/2}\rangle \\ &+ \sqrt{0.16} |(p_{1/2}, p_{3/2}^{-1})_{2^+} \otimes 2^+)_{0^+}, p_{1/2}\rangle, \\ \widetilde{5/2^+}\rangle &= \sqrt{0.49} |d_{5/2}\rangle + \sqrt{0.23} |(s_{1/2} \otimes 2^+)_{5/2^+}\rangle \\ &+ \sqrt{0.28} |(d_{5/2} \otimes 2^+)_{5/2^+}\rangle. \end{split}$$

• strong coupling of  $d_{5/2}$  to  $2^+ \rightarrow s_{1/2}$  and  $d_{5/2}$  BE increasing (0.6 and 5.9 MeV)

• smaller phase space of the clothed  $1/2^-$  state with respect to the bare  $p_{1/2}$  due to the antisymmetry between the valence nucleon and those participating in 2<sup>+</sup>  $\rightarrow p_{1/2}$  BE decreasing (2.9 MeV)

## Results

The radial dependence of the many-body wave functions and the phonon admixture in single-neutron states can be probed by onenucleon transfer reactions



#### **Overall account of the experimental findings!**

renormalization of the radial dependence of the single-particle states due to the many-body processes involving the continuum states plays an important role in the absolute one-nucleon transfer differential cross sections

## Neutron skin and charge radii in sd and fp nuclei

Many body correlations

J. Bonnard, S.M. Lenzi, A.P. Zuker, PRL **116**, 212501 (2016)



For neutron-rich calcium isotopes, beyond N=28

no even-odd staggering large and unexpected increase of the size

very large charge radius for  $^{52}$ Ca, with an increase relative to  $^{48}$ Ca of  $\delta \langle r^2 \rangle ^{48,52} = 0.530(5)~{\rm fm}^2$ 





#### Many body correlations

#### 1. Try a fit of radii for Z<30

J. Duflo and A.P. Zuker, PRC 66, 051304 (2002)

$$\sqrt{\langle r_{\pi}^2 \rangle} = \rho_{\pi} = A^{1/3} \left( \rho_0 - \frac{\zeta}{2} \frac{t}{A^{4/3}} - \frac{v}{2} \left( \frac{t}{A} \right)^2 \right) e^{(g/A)}$$

$$+\lambda [z(D_{\pi}-z)/D_{\pi}^{2} \times n(D_{\nu}-n)/D_{\nu}^{2}]A^{-1/2}$$

term accounting for correlations t = (N-Z) $\rho_0, \zeta, v, g = parameters$ 



#### $\rightarrow$ <u>Suggestion</u>: p orbits are LARGER than f orbits

Effect that can be simulated in shell-model calculations by using different values for neutrons and protons and for different orbits

## 2. Semi-microscopic SM calculation for single-particle states built on $^{\rm 40}{\rm ca}$

•  $V_{\text{low-k}}$  ( $\Lambda$ =2 fm<sup>-1</sup>) from N3LO

$$\hbar\omega_{v} = \frac{41.47}{\langle r_{v}^{2} \rangle} \sum_{i} n_{i} \left( N_{i} + \frac{3}{2} \right) / N ; \ \hbar\omega_{\pi} = \frac{41.47}{\langle r_{\pi}^{2} \rangle} \sum_{i} z_{i} \left( N_{i} + \frac{3}{2} \right) / Z$$

 $\langle r_{\pi}^2 \rangle \& \langle r_{\nu}^2 \rangle$  from DZ formula and fit of the mirror energies differences (MED) for T=1/2 mirror nuclei with  $\zeta$  treated as a free parameter

A	J <sup>π</sup>	MED(MeV)	ħω <sub>υ</sub> (MeV)	$\hbar ω_{\pi}$ (MeV	) ζ(fm)	$\Delta r_{v\pi}(\text{fm})$	$r_{\pi}(\mathrm{fm})$	$r_v(fm)$
41	7/2-	7.278	10.78	10.63	0.610	0.015	3.422	3.437
	$3/2^{-}$	7.052	10.61	10.59	1.513	0.038	3.427	3.465
	$1/2^{-}$	7.129	10.61	10.59	1.482	0.037	3.428	3.465
	5/2-	7.351	10.75	10.61	0.702	0.018	3.424	3.442
	5/2-	7.338	10.75	10.61	0.725	0.018	3.427	3.442

rms radii of p orbits exceed those of the f orbits by ~0.7 fm





## Electromagnetic selection rules for $^{12}\mbox{C}$ in the 3 $\alpha$

cluster model G.Stellin, L.Fortunato, A. Vitturi, JPG 43 (2016) 085104

C particle as building block

Bijker and lachello, PRC **61** 067305 (2000)

Ground

band

0-

band





## Electromagnetic selection rules for $^{12}\text{C}$ in the 3 $\alpha$

cluster model G.Stellin, L.Fortunato, A. Vitturi, JPG 43 (2016) 085104

Many body correlations



Bijker and lachello, PRC **61** 067305 (2000)

 $3 \alpha$  particles perform *normal harmonic vibrations* about their equilibrium positions at the vertexes of an equilateral triangle, which is expected to rotate as a rigid symmetric top



#### Assuming decoupled vibrational for each mode

$$\Psi_{J,K,M}^{n_1,n_2} = \Phi_{n_1}^A(Q_1)\Phi_{n_2}^E(Q_2, Q_3)\psi_{JKM}$$

 $n_1$ ,  $n_2$  = phonon numbers in the  $A'_1$  and E'' vibrations;  $\psi_{JKM}$  = rotational wave function

## Results

#### lowest allowed electric transitions

lowest allowed magnetic transitions



## The predicted selection rules are robust signatures of $\alpha$ -cluster model



Perspectives on<sup>16</sup>O and <sup>20</sup>Ne





## **Collective modes in n-rich nuclei**

### **Pigmy dipole resonance (PDR)**

- **PDR**  $\rightarrow$  reaction rates in the astrophysical r process
- **PDR**  $\rightarrow$  neutron skin  $\rightarrow$  symmetry energy of the Equation of state(EoS) $\rightarrow$  neutron-rich nuclear matter

**E1 strength for 5**  $\leq E \leq$  **10 MeV -** observed in different mass regions, in particular in neutron-rich nuclei







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#### From HF +RPA calculations





neutrons and protons are in phase inside the nucleus and at the surface only neutrons survive (isoscalar (IS) and isovector (IV) TD have the same magnitude)  $\rightarrow$  IS/IV mixing  $\rightarrow$  PDR populated by IS and IV probes





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#### **Open questions**

- Nature of the PDR, single-particle/collective?
- Mixing among the IS and IV components
- Its evolution with respect to mass, deformation and neutron excess
- A. Bracco, F.C.L. Crespi, and E.G. Lanza, EPJA A 5, 99 (2015)
- H. Zheng, S. Burrello, M. Colonna, V. Baran, PRC 94, 014313 (2016)
- X. Roca-Maza, ... G. Colò, et al, PRC 92, 064304 (2015)
- E. Lanza et al. , work in progress

#### Strong collaboration between CT-PD, LNS-MI

## Gamma decay of pygmy states from inelastic scattering

of ions A. Bracco, F.C.L. Crespi, and E.G. Lanza, EPJA A 5, 99 (2015)

Analysis of exp PDR excitations for several ( ${}^{17}O,{}^{17}O\gamma'$ ) reactions (@LNL) with microscopic form factors from RPA transition densities to investigate isospin mixing



## Dipole response in neutron-rich nuclei with new Skyrme interactions H. Zheng, S. Burrello, M. Colonna, V. Baran, PRC 94, 014313 (2016)

How the mixed IS/IV character of the E1 response in neutron-rich depends on the symmetry energy - <sup>68</sup>Ni <sup>132</sup>Sn <sup>208</sup>Pb

- semiclassical model (no single-particle structure is included)
- SAMi-J interactions (from MI group); J=symmetry energy coefficient at saturation density



#### Coupling of isoscalar and isovector excitations confirmed: an initial IS perturbation of the system $\rightarrow$ IV response and viceversa



The same analysis can be performed for *pre-equilibrium dipole strength:* dipole oscillations in compound systems originating from reactions with strong isospin asymmetry between target and projectile

Pre-equilibrium dipole response in the charge-asymmetric reaction  $^{132}$ Sn +  $^{58}$ Ni @ E<sub>lab</sub> = 10 MeV/A



H. Zheng, S. Burrello, M. Colonna, PLB **769**, 424 (2017)





The neutron skin thickness from the measured electric dipole <sup>Collective modes</sup> polarizability in <sup>68</sup>Ni, <sup>120</sup>Sn, and <sup>208</sup>Pb X. Roca-Maza, ... G. Colò, *et al*, PRC **92**, 064304 (2015)

How to get information on the symmetry energy and its density dependence from the electric dipole polarizability  $\alpha_{\text{D}}$ 

- RPA or QRPA approaches
- EDF (Skyrmes, ...)

From Droplet model (DM)  

$$\alpha_D^{\rm DM} \approx \frac{\pi e^2}{54} \frac{A \langle r^2 \rangle}{J} \left[ 1 + \frac{5}{2} \frac{\Delta r_{np}^{\rm DM}}{I \langle r^2 \rangle^{1/2}} \right]$$

Strong correlation  $\alpha_{\rm D} J - \Delta r_{np}$ 

J=symmetry energy coefficient at saturation density

$$\Delta r_{np} = \langle r^2 \rangle_n^{1/2} - \langle r^2 \rangle_p^{1/2}.$$

high-precision measurements of  $\alpha_D$  - if J is known - may be used to constrain the neutron skin thickness  $\Delta r_{np}$ 

providing important constraints on the density dependence of the symmetry energy

#### Assessment of the validity of correlations suggested by the DM



Identification of a subset of EDFs that simultaneously reproduces the measured electric dipole polarizability in <sup>68</sup>Ni, <sup>120</sup>Sn, and <sup>208</sup>Pb



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Strong correlation between  $\alpha_{\rm D}$  of two nuclei is instrumental to predict the values of  $\alpha_{\rm D}$  in other nuclei

**Collective modes** 

> The subset of EDFs is used to estimate isovector-sensitive observables: such as the neutron skin  $(\Delta r_{np})$ , the coefficient (J), and the slope (L) of the symmetry energy at the saturation density

(a) from the su (b) from DM	bset of EDFs			
	<sup>68</sup> Ni	<sup>120</sup> Sn	<sup>208</sup> Pb	
(a)	0.15 – 0.19	0.12 - 0.16	0.13 – 0.19	
(b)	0.16 ± 0.04	0.12 ± 0.04	0.16 ± 0.03	
J and L values (in MeV)				
J		30 – 35		
L		20 - 66		

These estimates are consistent with predictions extracted in heavy ion reaction [M.Colonna *et al*, EPJA 50, 30 92014)] and suggest a fairly soft symmetry energy

Predictions of  $\Delta r_{np}$  in <sup>48</sup>Ca (0.15 – 0.18 fm) in <sup>90</sup>Zr (0.06 – 0.08 fm)

 $\Delta r_{nn}$  (in fm)





## Pigmy dipole response in deformed nuclei

E. Lanza et al., work in progress



Presence of a double-bump structure of PDR similar to the one observed in the GDR? Two peaks corresponding to oscillations of the neutron excess against the core along the symmetry axes (K=0<sup>-</sup>) and the perpendicular one (K=1<sup>-</sup>)

#### From calculations within a simple macroscopic model



The variation of the ratio for the IS case is stronger  $\rightarrow$  different population of the PDR for different probes



## **Direct reactions**

- Ion-ion charge exchange dynamics and connections to nuclear beta decay spectroscopy
- H. Lenske, I. J. Bellone, M. Colonna, J. A. Lay, to be submitted to PRC
- Talk by J. Bellone

## Optical potentials and properties of quasibound states

Talk by A. Bonaccorso
 Reaction mechanisms, transfer and fragmentation, that
 can populate resonance states of exotic nuclei



Heavy Ion Single Charge Exchange Reactions and Beta Decay Matrix Elements H. Lenske, I. J. Bellone, M. Colonna, J. A. Lay, to be submitted to PRC

• DWBA - Unified structure and reaction description

 $^{18}O+^{40}Ca \rightarrow ^{18}F+^{40}K$ 

 $T_{lab} = 15 \text{ MeV/A} @LNS$ 



 $p, \Delta$ 

**Direct reactions** 

 $n, \Delta$ 

For low momentum transfer  $\rightarrow$  factorization of the charge exchange cross section into reaction and structure parts



## To end

From 2014 until now	
papers	~280*
talks	~220
thesis (PhD, triennale, magistrale)	~25

\* many of them in collaboration with experimental groups

The STRENGTH Units have given an important contribution to the nuclear community through the organization of meetings, workshops and schools

In particular,

- GGI lectures on Frontiers in Nuclear and Hadronic Physics, Florence
- Summer school Rewriting nuclear physics textbooks, Pisa
- Incontri Nazionali di Fisica Nucleare
- SPES One Day Workshops
- International SPES Workshops



