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Light and heavy hadron production in heavy-ion collisions from a coalescence model

In collaboration with: S. Plumari, V. Greco,
F. Scardina, S.K. Das

Outline

- ❑ **Hadronization:**
 - Fragmentation
 - Coalescence model
 - *p, π, k, Λ spectra and baryon/meson ratio*
- ❑ **Heavy Quarks:**
 - Λ_c and D mesons spectra for RHIC and LHC energies
 - Λ_c/D^0 ratio
- ❑ **Conclusions**

Quark Gluon Plasma

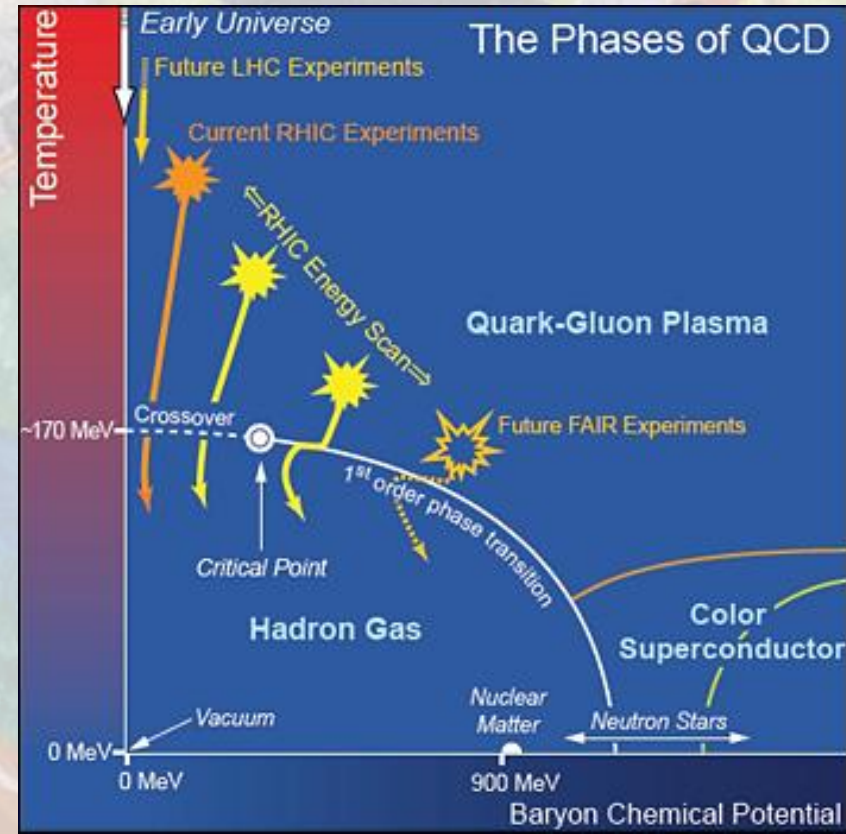
- Nuclear matter: Critical Energy and Temperature in the transition between confined and deconfined phase

$$\varepsilon_c \approx 0.7 \text{ GeV} / \text{fm}^3$$

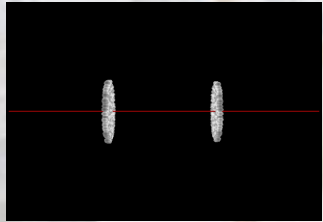
$$T_c \cong 165 \text{ MeV} \approx 10^{12} \text{ K}$$

- If $T > T_c$ colour charges are deconfined in a Quark Gluon Plasma (QGP)
- Different value of T and ρ for deconfinement

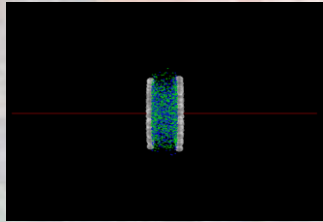
→ Phase Diagram



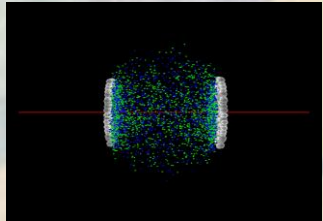
Ultra-relativistic heavy ion collisions



Initial Stage



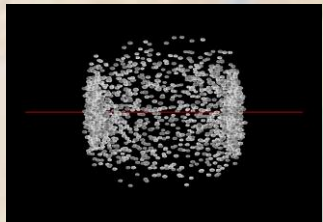
Pre-equilibrium stage



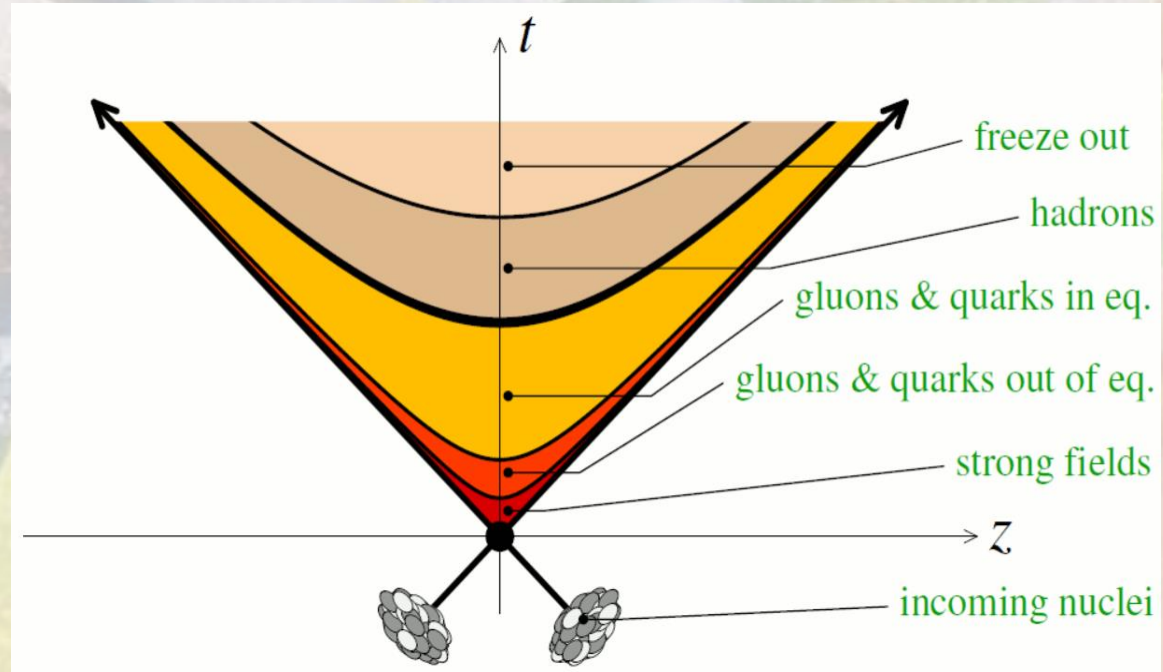
Expansion

QGP

Hadronization



Chemical and kinetic freeze-out



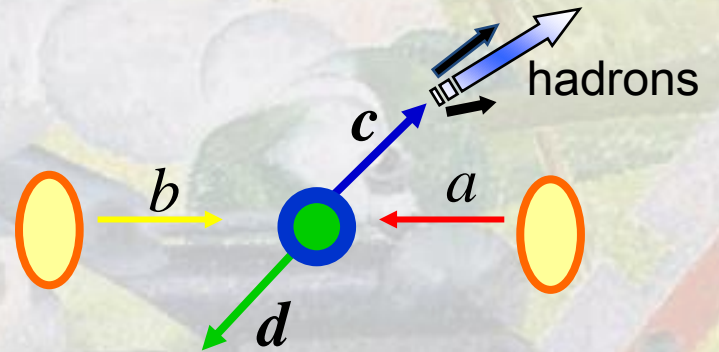
Hadronization

$$\frac{dN_h}{d^2p_h} = \sum_f \int dz \frac{dN_f}{d^2p_f} D_{f \rightarrow h}(z)$$

Fragmentation function

We use the AKK fragmentation function

S. Albino, B.A. Kniehl, G. Kramer, NPB 803 (2008)



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Proton to pion ratio Enhancement:

In vacuum from fragmentation functions the ratio is small

$$\frac{D_{c \rightarrow p}(z)}{D_{c \rightarrow \pi}(z)} < 0.25$$

Elliptic flow splitting:

For $p_T > 2$ GeV Both hydro and fragmentation predicts similar v_2 for pions and protons

Another hadronization mechanism is by coalescence

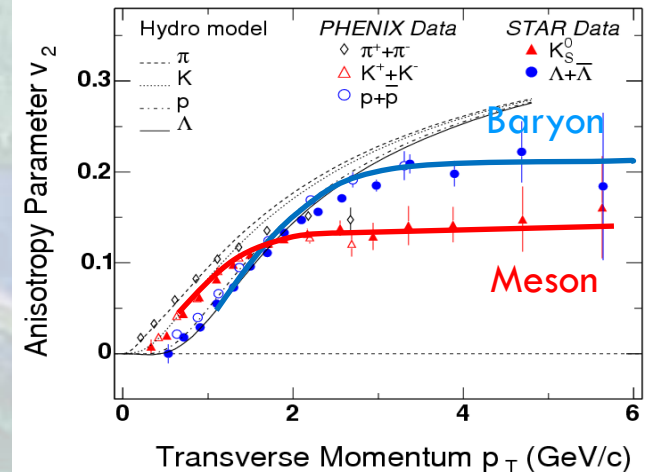
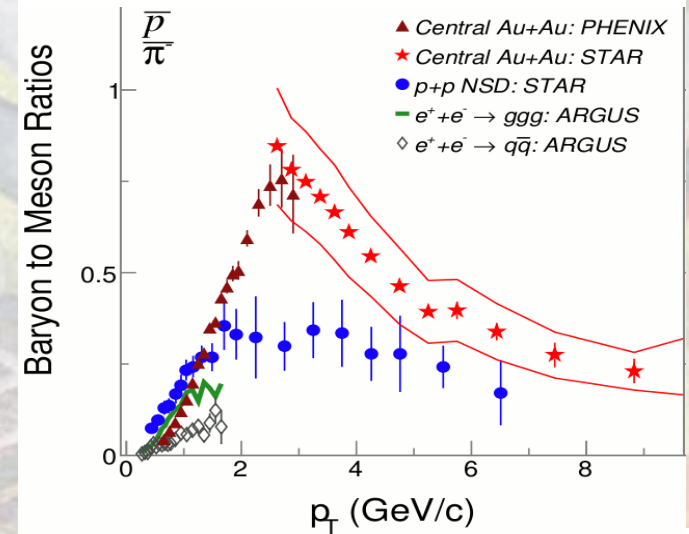
V. Greco, C.M. Ko, P. Levai PRL 90, 202302 (2003).

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R.J. Fries, B. Muller, C. Nonaka, S.A. Bass PRL 90, 202303 (2003).

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R. J. Fries, V. Greco, P. Sorensen
Ann.Rev.Nucl.Part.Sci. 58 (2008) 177

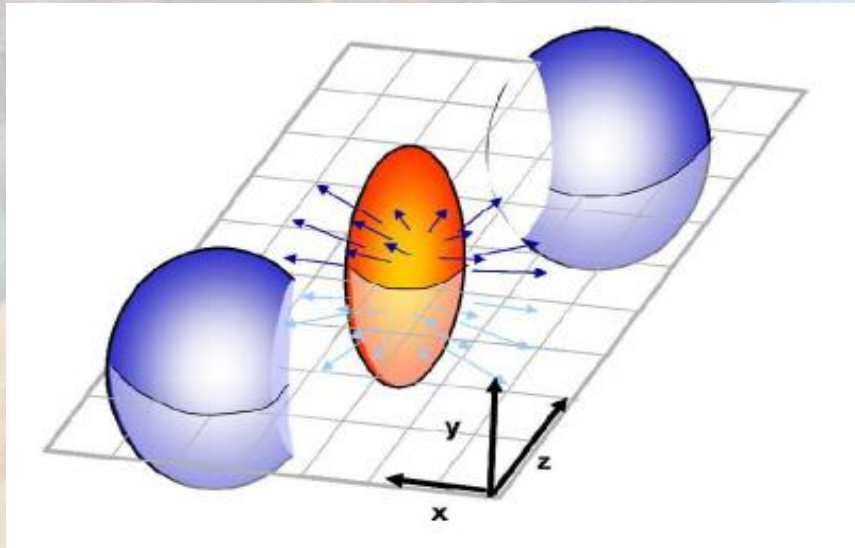


Elliptic Flow

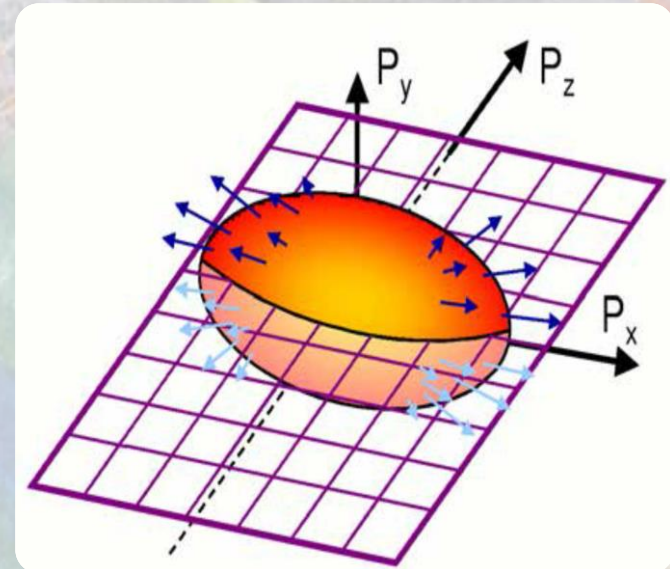
Fourier expansion of the azimuthal distribution

$$f(\varphi, p_T) = 1 + 2 \sum_{n=1}^{\infty} v_n(p_T) \cos n\varphi$$

$n=2$ Elliptic flow



Coordinate space: initial anisotropy



Momentum space: final anisotropy

Free streaming $v_2=0$

Hadronization

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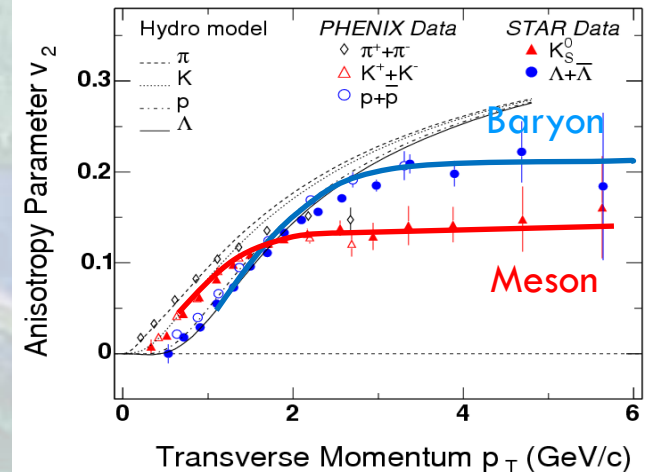
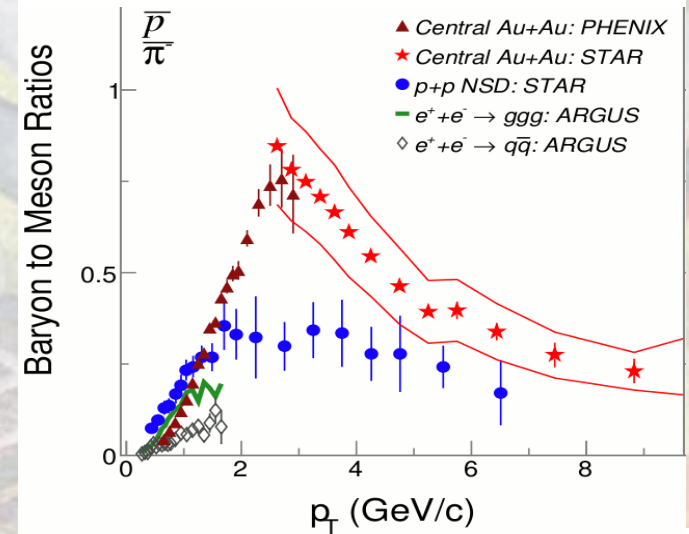
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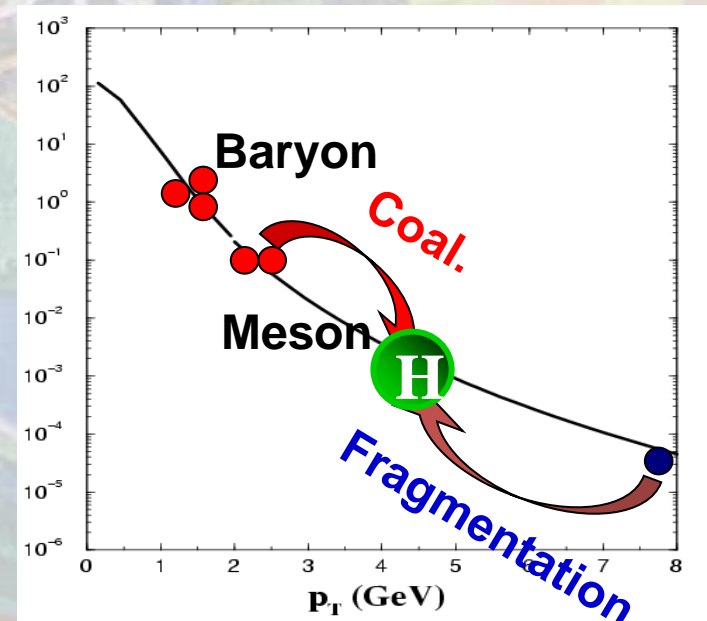
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Hadronization: Coalescence

Statistical factor
colour-spin-isospin

Parton Distribution
function

Hadron Wigner
function

$$\frac{dN_{Hadron}}{d^2p_T} = g_H \int \prod_{i=1}^n p_i \cdot d\sigma_i \frac{d^3p_i}{(2\pi)^3} f_q(x_i, p_i) f_W(x_1, \dots, x_n; p_1, \dots, p_n) \delta\left(p_T - \sum_i p_{iT}\right)$$

Constraints from experiments

- Thermal Distribution ($p_T < 2$ GeV)

$$\frac{dN_q}{d^2r_T d^2p_T} = \frac{g_q m_T}{(2\pi)^3} \exp\left(-\frac{\gamma_T(m_T - p_T \cdot \beta_T)}{T}\right)$$

- Collective flow $\beta_T = \beta_0 \frac{r}{R}$

- Minijet Distribution ($p_T > 2$ GeV)

- Fireball radius+radial flow constraints
 dN_{ch}/dy and dE_T/dy

$$f_{Meson} = \frac{9\pi}{2} \Theta(\sigma_x^2 - x_{r1}^2) \Theta(\sigma_p^2 - p_{r1}^2 + \Delta m_{12}^2)$$

$$f_{Baryon} = \frac{9\pi}{2} \Theta\left(\sigma_x^2 - \frac{1}{2} x_{r1}^2\right) \Theta(\sigma_p^2 - p_{r1}^2 + \Delta m_{12}^2) \\ \times \frac{9\pi}{2} \Theta(\sigma_x^2 - x_{r2}^2) \Theta(\sigma_p^2 - p_{r2}^2 + \Delta m_{123}^2)$$

$$\sigma_x = 1/\sigma_p \quad \text{Only one free parameter in } f_W$$

V. Greco, C.M. Ko, P. Levai PRC 68, 034904 (2003)

V. Minissale, F. Scardina, V. Greco PRC 92, 054904 (2015)

Fireball

Central Collision 0-10% impact parameter $b=2.5$ fm

From Experiment

RHIC \rightarrow LHC

$dE_T/dy \sim 740 \text{ GeV} \rightarrow 2100 \text{ GeV}$

$dN_{ch}/dy \approx 670 \rightarrow 1600$

$T_c \sim 160 \text{ MeV}$

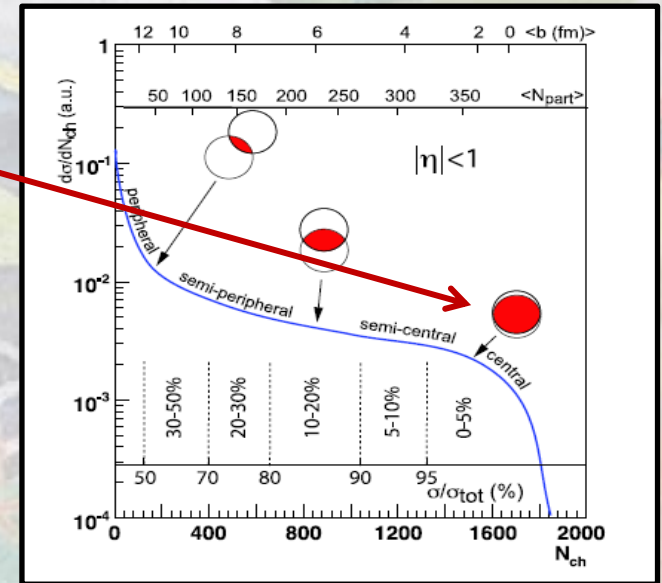
Lifetime and Volume implied

$\tau \sim 4.5 \text{ fm}/c \rightarrow 8 \text{ fm}/c$

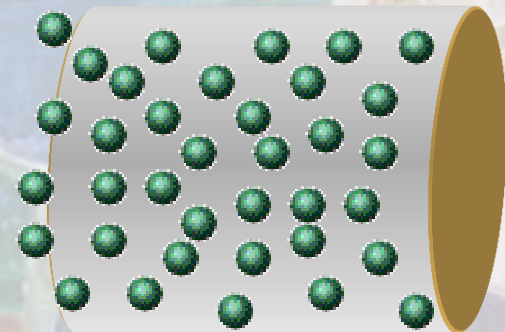
$\beta_0 = 0.37 \rightarrow 0.63$

$V \sim 1100 \text{ fm}^3 \rightarrow 2500 \text{ fm}^3$

In agreement with HBT



$|\Delta y| \leq 0.5$



Resonance decay

□ $\pi (I = 1, J = 0)$

mesons

Resonances:

- $k^* (I = 1, J = 1/2) \rightarrow k\pi$
- $\rho (I = 1, J = 1) \rightarrow \pi\pi$
- $\Delta (I = 3/2, J = 3/2) \rightarrow N\pi$

□ $k^\pm (I = 0, J = 1/2)$

Resonances:

- $k^* (I = 1, J = 1/2) \rightarrow k\pi$

Main hadronic channels including the ground states and the first excited states have been taken into account

Statistical factor

$$\frac{[(2J + 1)(2I + 1)]_{H^*}}{[(2J + 1)(2I + 1)]_H} \left(\frac{m_{H^*}}{m_H} \right)^{3/2} e^{-(E_{H^*} - E_H)/T}$$

□ $p (I = 1/2, J = 1/2)$

baryons

Resonances:

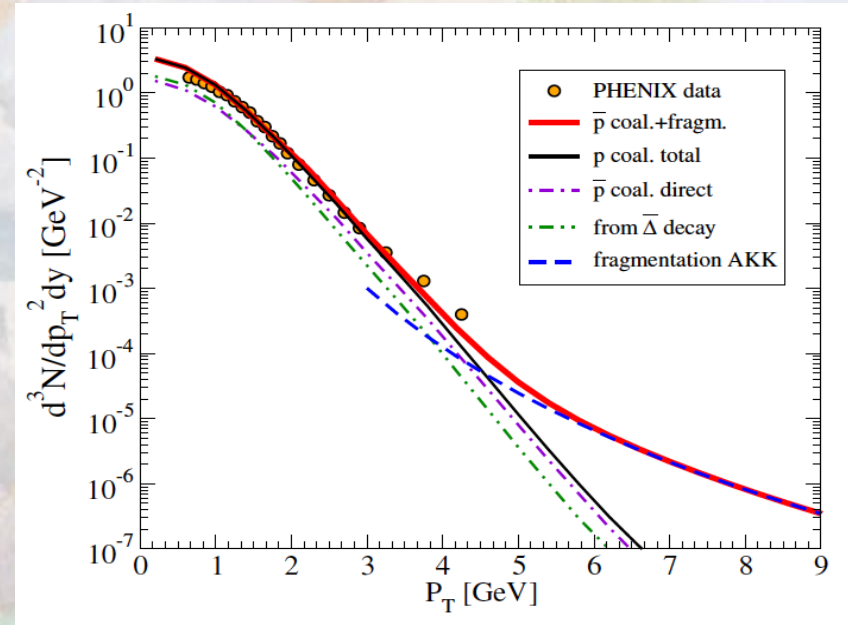
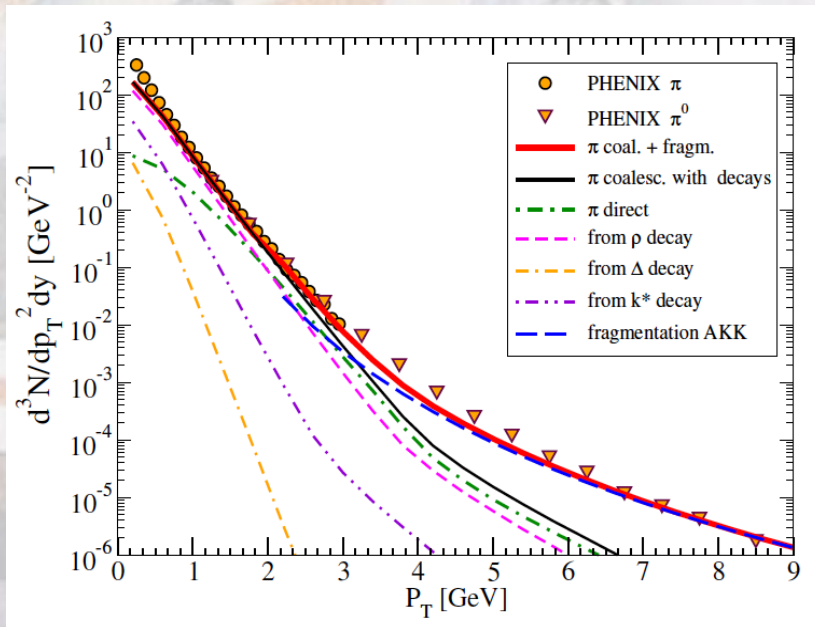
- $\Delta (I = 3/2, J = 3/2) \rightarrow N\pi$

□ $\Lambda (1116) (I = 0, J = 1/2)$

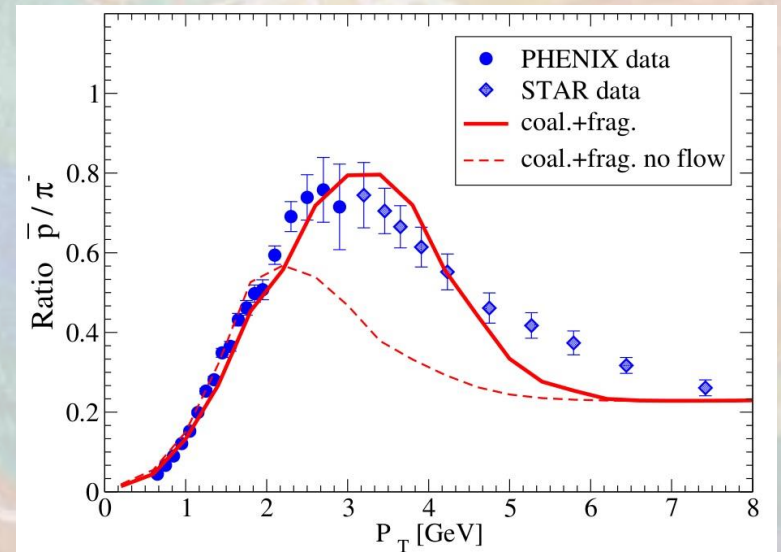
Resonances:

- $\Sigma^0(1193) (I = 1, J = 1/2) \rightarrow \Lambda\gamma$
- $\Lambda (1405) (I = 0, J = 1/2) \rightarrow \Sigma\pi$
- $\Sigma^0(1385) (I = 1, J = 3/2) \rightarrow \Lambda\pi$ with B. R. = 88%
- $\rightarrow \Sigma\pi$ with B. R. = 11,7%

RHIC: spectra and baryon/meson

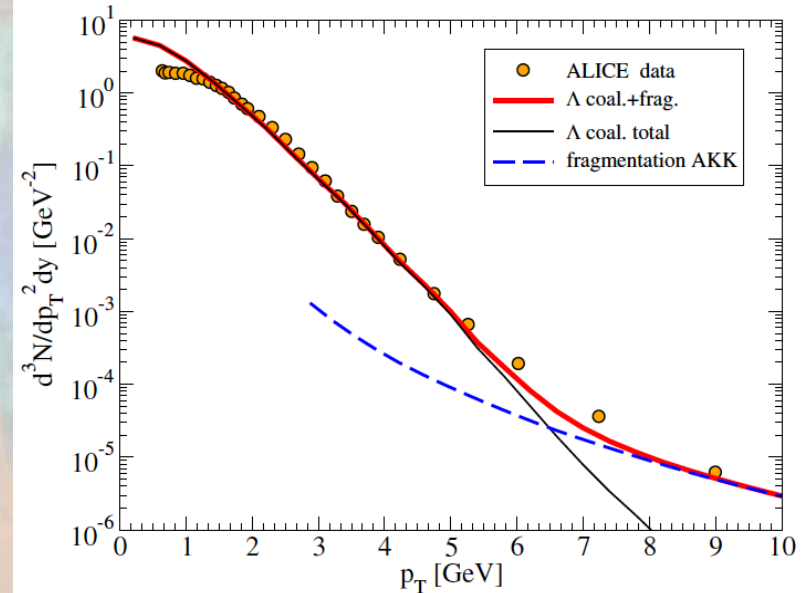
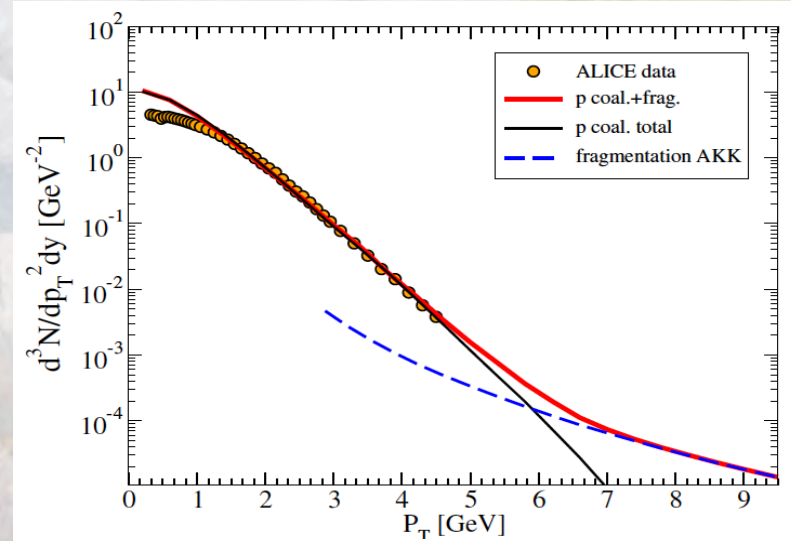
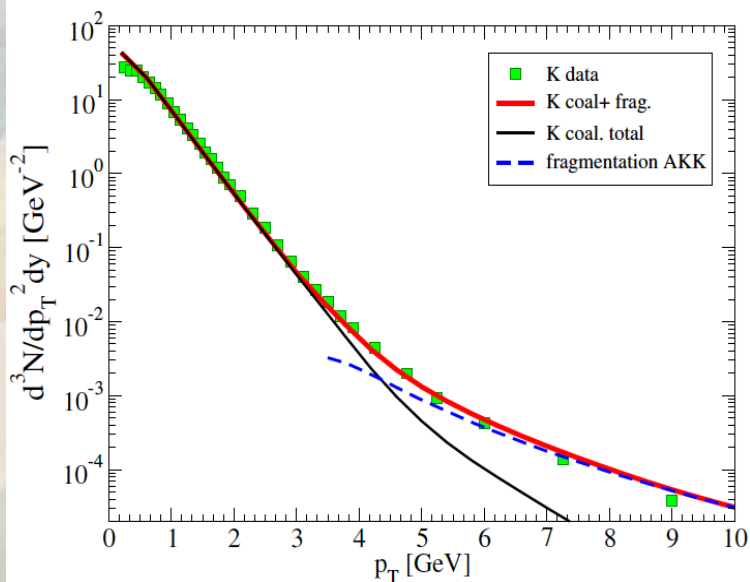
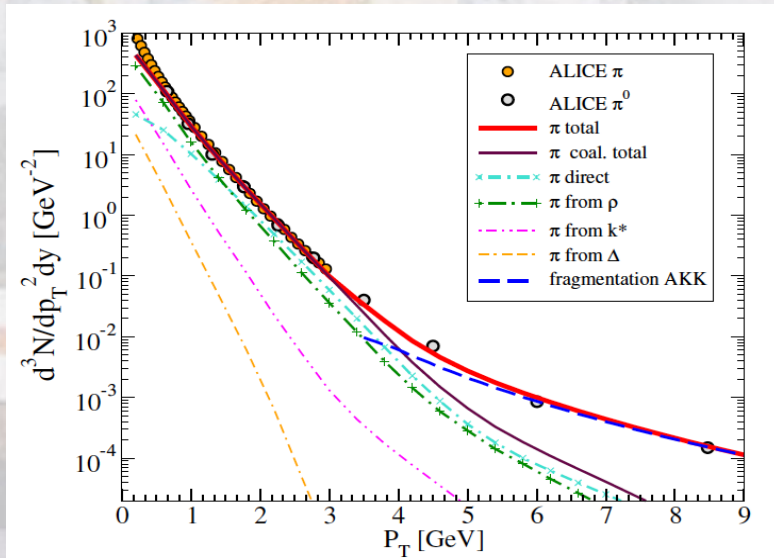


- ❑ Resonances improve the description at low p_T
- ❑ Height and p_T position of the peak well described
- ❑ Lack of fragmentation at $p_T \approx 5$ GeV (seen in pp with AKK)
- ❑ Without radial flow ... (similar to pp collisions but not exactly)



LHC: spectra π , p , k , Λ

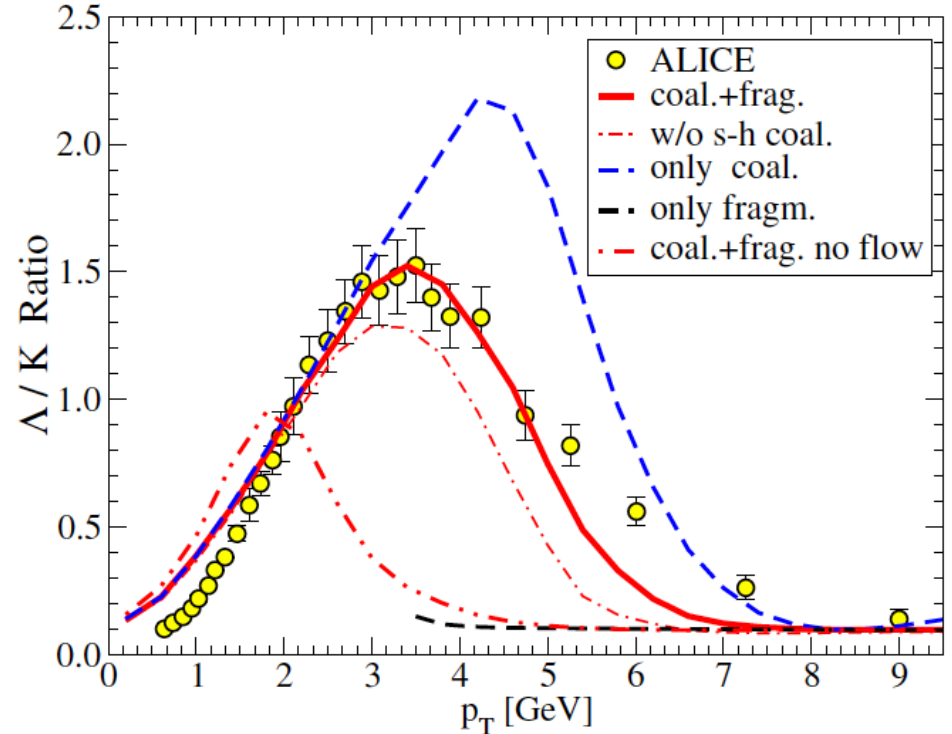
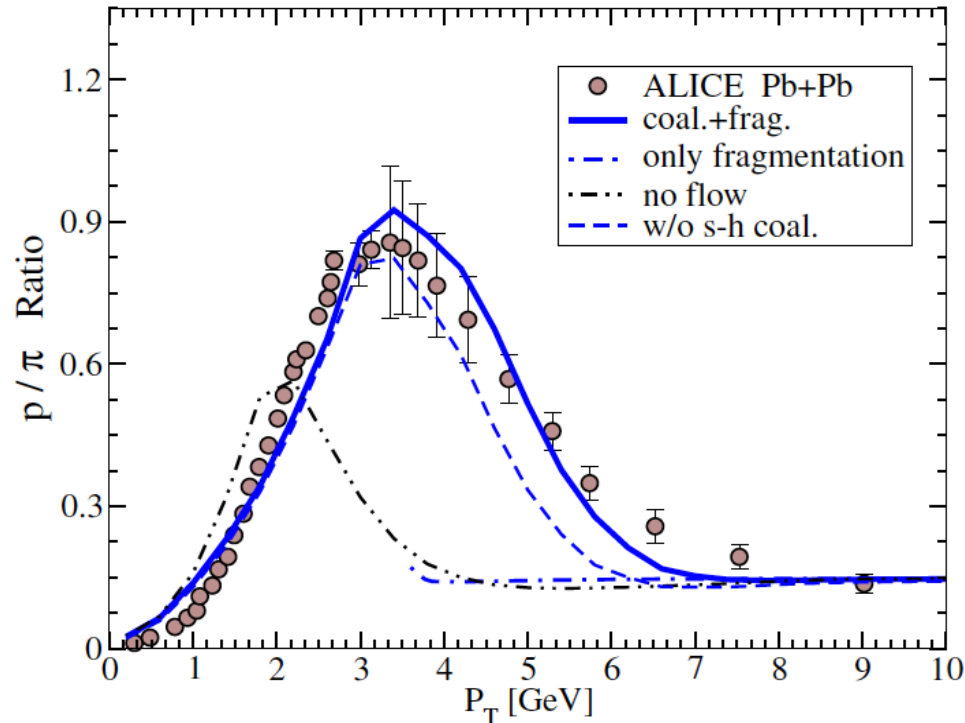
wave function widths σ_p of baryon and mesons are the same at RHIC and LHC!



LHC: baryon/meson

wave function widths σ_p of baryon and mesons are the same at RHIC and LHC!

V. Minissale, F. Scardina, V. Greco PRC 92, 054904 (2015)



- ✓ Height and p_T position of the peak well described.
- ✓ Soft-minijet coalesc. contribution around and above the peak
- ✓ Lack of fragmentation at $p_T \approx 6$ GeV (seen also in pp with AKK)
- ✓ in-medium fragmentation as a quark recombination of shower partons taking into account also the gluon splitting into quark pairs that recombine

→ Rainer J. Fries, Kyongchol Han, and Che Ming Ko, Nucl. Phys. **A956**, 601 (2016).

Heavy flavour Hadronization: Fragmentation

$$\frac{dN_h}{d^2p_h} = \sum_f \int dz \frac{dN_f}{d^2p_f} D_{f \rightarrow h}(z)$$

The distribution function is evaluated at the Fixed-Order plus Next-to-Leading-Log (FONLL)

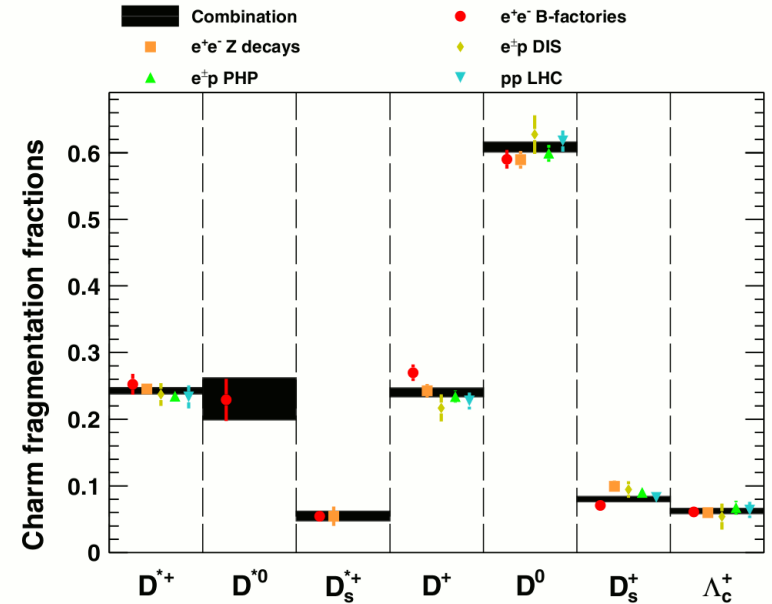
M. Cacciari, P. Nason, R. Vogt, PRL 95 (2005) 122001

We use the Peterson fragmentation function

C. Peterson, D. Schaller, I. Schmitt, P.M. Zerwas PRD 27 (1983) 105

$$D_{f \rightarrow h}(z) \propto \frac{1}{z \left[1 - \frac{1}{z} - \frac{\epsilon}{1-z} \right]^2}$$

The parameter ϵ for D meson hadronization fixed by pp collisions data. For baryons we fix it in accordance with e^+e^- collisions as done in S.K. Das et al, PRD94 (2016) no.11, 114039. Measurement in $e^\pm p$, pp and e^+e^- are in agreement within uncertainties: fragmentation at most independent of the specific production process



M. Lisovsky, et al. EPJ C76 (2016) no.7, 397

$$\left(\frac{\Lambda_c^+}{D^0} \right)_{e^+e^-} \simeq 0.1 \left(\frac{D_s^+}{D^0} \right)_{e^+e^-} \simeq 0.13$$

3 and 2 times smaller respect to the one expected from thermal models

A. Andronic et al., Phys. Lett. B571, 36 (2003)

I. Kuznetsova, J. Rafelski, EPJ C51, 113 (2007)

Hadronization: Coalescence

Statistical factor
colour-spin-isospin

Parton Distribution
function

Hadron Wigner
function

$$\frac{dN_{Hadron}}{d^2p_T} = g_H \int \prod_{i=1}^n p_i \cdot d\sigma_i \frac{d^3p_i}{(2\pi)^3} f_q(x_i, p_i) f_W(x_1, \dots, x_n; p_1, \dots, p_n) \delta\left(p_T - \sum_i p_{iT}\right)$$

charm distribution function at mid-rapidity from parton simulations solving Boltzmann transport eq. that give good description of both R_{AA} and $v_2(p_T)$ from RHIC to LHC energies.

• The width parameters σ in $f_W(\dots)$ fixed by the root-mean-square charge radius as predicted by quark models

C.-W. Hwang, EPJ C23, 585 (2002).

C. Albertus et al., NPA 740, 333 (2004)

$$\langle r^2 \rangle_{D^+} = 0.184 fm^2; \langle r^2 \rangle_{D_s^+} = 0.124 fm^2; \\ \langle r^2 \rangle_{\Lambda_c^+} = 0.152 fm^2$$

• Normalization in $f_W(\dots)$ fixed by requiring that $P_{coal}=1$ for $p=0$

Heavy flavour: Resonance decay

In our calculations we take into account main hadronic channels, including the ground states and the first excited states for D and Λ_c

MESONS

- $D^+ (l=1/2, J=0)$
- $D^0 (l=1/2, J=0)$
- $D_s^+ (l=0, J=0)$

Resonances

- $D^{*+} (l=1/2, J=1) \rightarrow D^0 \pi^+ \text{ B.R. } 68\%$
 $\rightarrow D^+ X \text{ B.R. } 32\%$
- $D^{*0} (l=1/2, J=1) \rightarrow D^0 \pi^0 \text{ B.R. } 62\%$
 $\rightarrow D^0 \gamma \text{ B.R. } 38\%$
- $D_s^{*+} (l=0, J=1) \rightarrow D_s^+ X \text{ B.R. } 100\%$
- $D_{s0}^{*+} (l=0, J=0) \rightarrow D_s^+ X \text{ B.R. } 100\%$

Statistical factor

$$\frac{[(2J+1)(2I+1)]_{H^*}}{[(2J+1)(2I+1)]_H} \left(\frac{m_{H^*}}{m_H} \right)^{3/2} e^{-(E_{H^*}-E_H)/T}$$

BARYONS

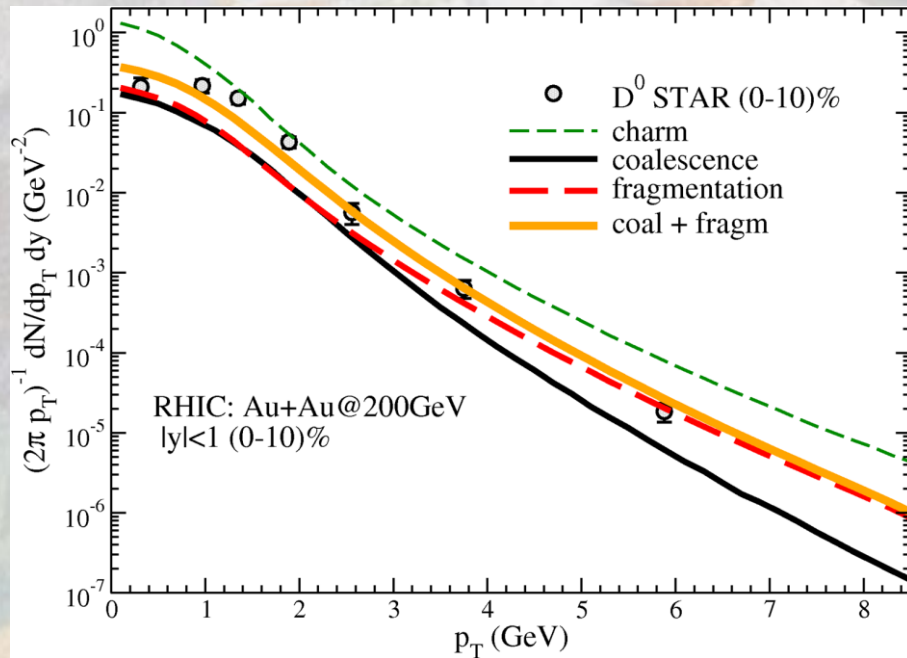
- $\Lambda_c^+ (l=0, J=1/2)$

Resonances

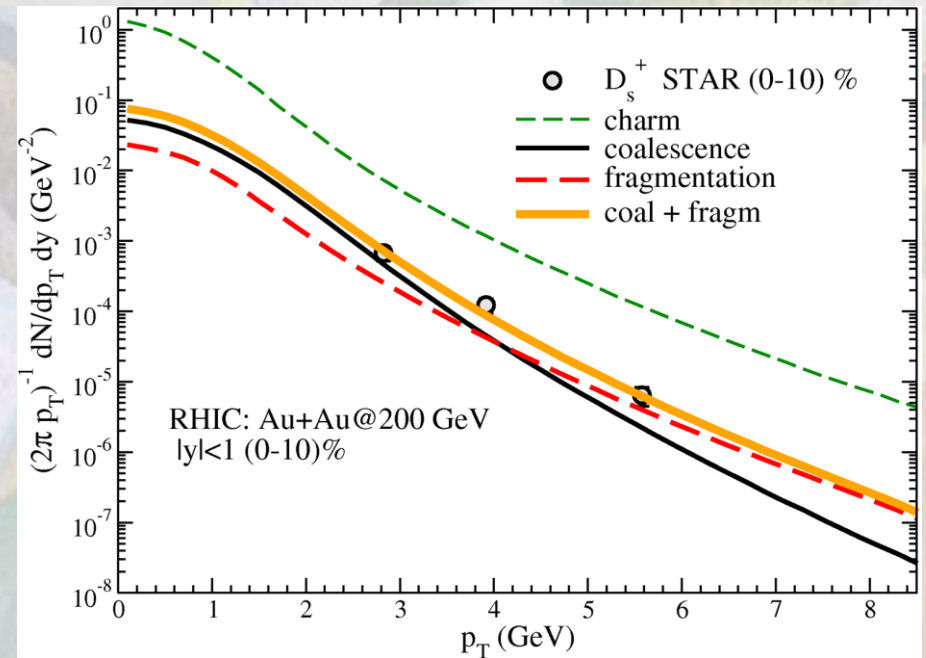
- $\Lambda_c^+(2595) (l=0, J=1/2) \rightarrow \Lambda_c^+ \text{ B.R. } 100\%$
- $\Lambda_c^+(2625) (l=0, J=3/2) \rightarrow \Lambda_c^+ \text{ B.R. } 100\%$
- $\Sigma_c^+(2455) (l=1, J=1/2) \rightarrow \Lambda_c^+ \pi \text{ B.R. } 100\%$
- $\Sigma_c^+(2520) (l=1, J=3/2) \rightarrow \Lambda_c^+ \pi \text{ B.R. } 100\%$

RHIC: results

Data from STAR Coll. PRL **113** (2014) no.14, 142301



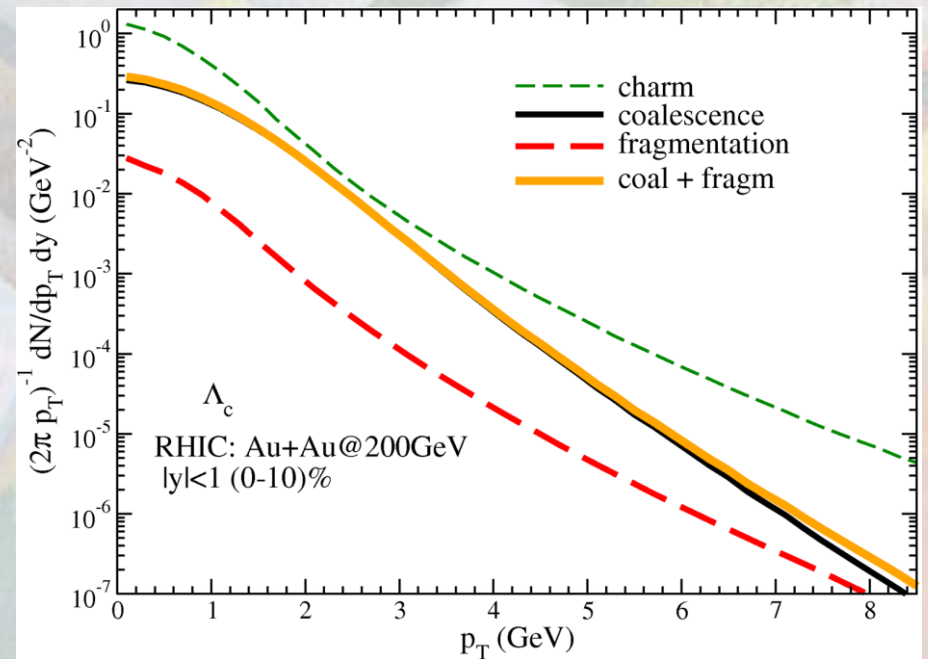
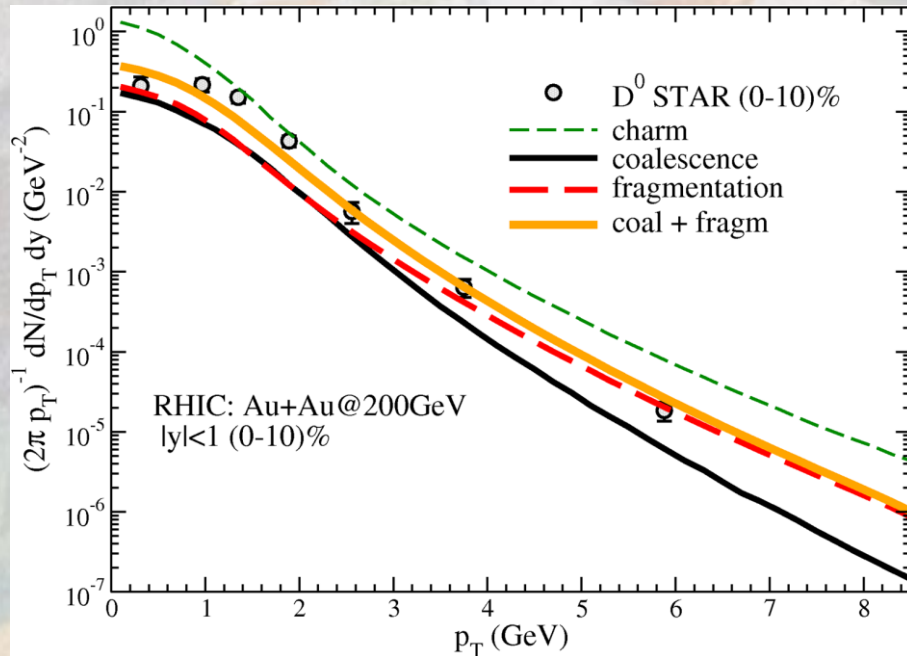
Data from STAR Coll., arXiv:1704.04364 [nucl-ex].



- For D^0 coalescence and fragmentation comparable at 2 GeV
- fragmentation fraction for D_s^+ are small and less than about 8% of produced total heavy hadrons

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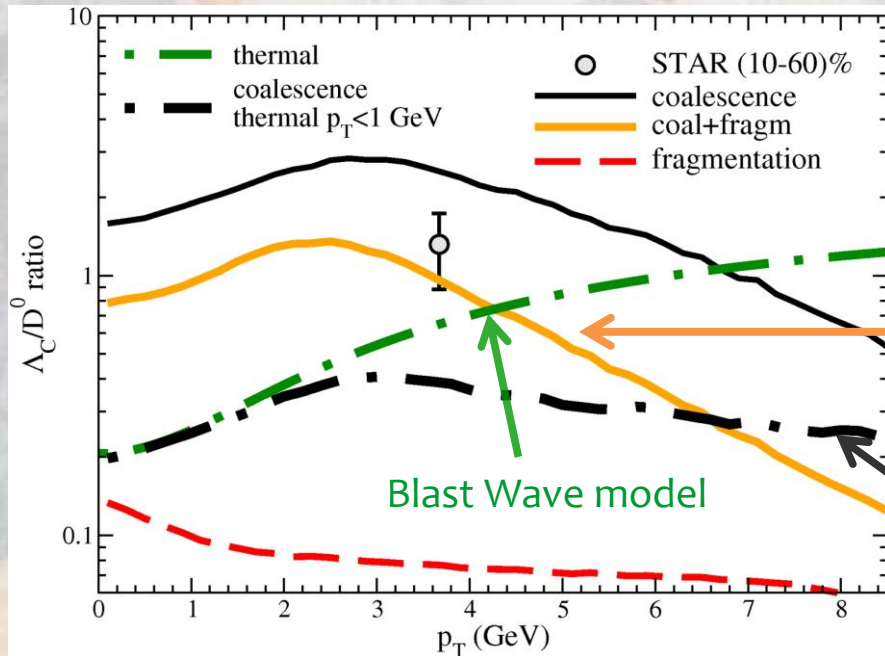
Data from STAR Coll. PRL **113** (2014) no.14, 142301



- For D^0 coalescence and fragmentation comparable at 2 GeV
- fragmentation fraction for D_s^+ are small and less than about 8% of produced total heavy hadrons
- Λ_c^+ fragmentation is even more smaller, coalescence gives the dominant contribution

RHIC: Baryon/meson

Data from STAR Coll., arXiv:1704.04364 [nucl-ex].



• Compared to light baryon/meson ratio the Λ_c/D^0 ratio has a larger width (flatter)

• Similar to the one predicted in Y. Oh, C.M. Ko, S.H. Lee, S. Yasui PRC 79,044905 (2009)

Coal with wave function width σ_p of D^0 and Λ_c changed to have $\Lambda_c/D^0 = \text{thermal ratio at } p_T \rightarrow 0$

Some more calculations on Λ_c/D can be found in:

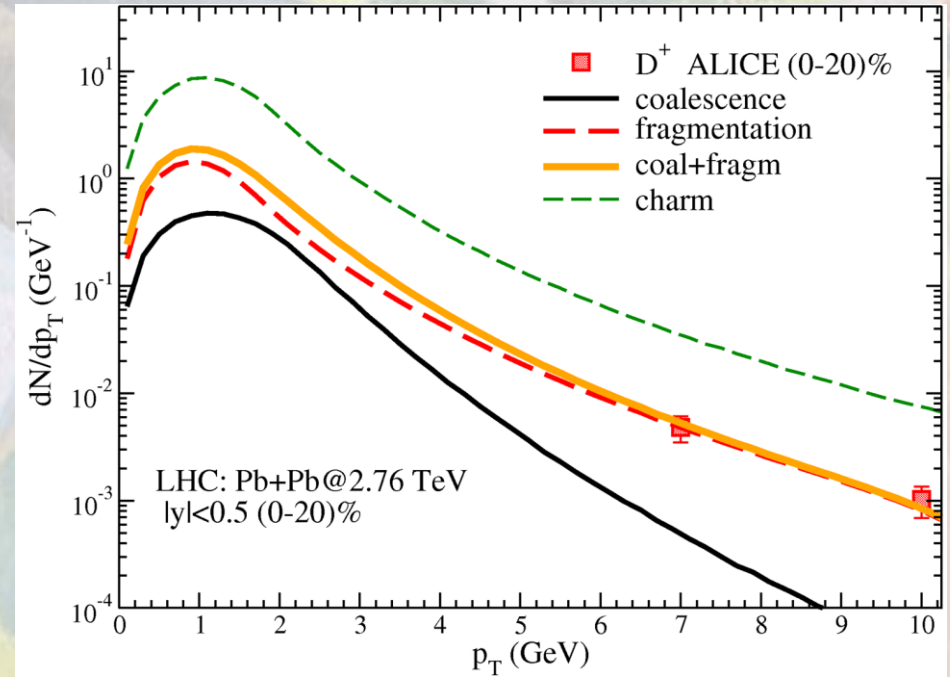
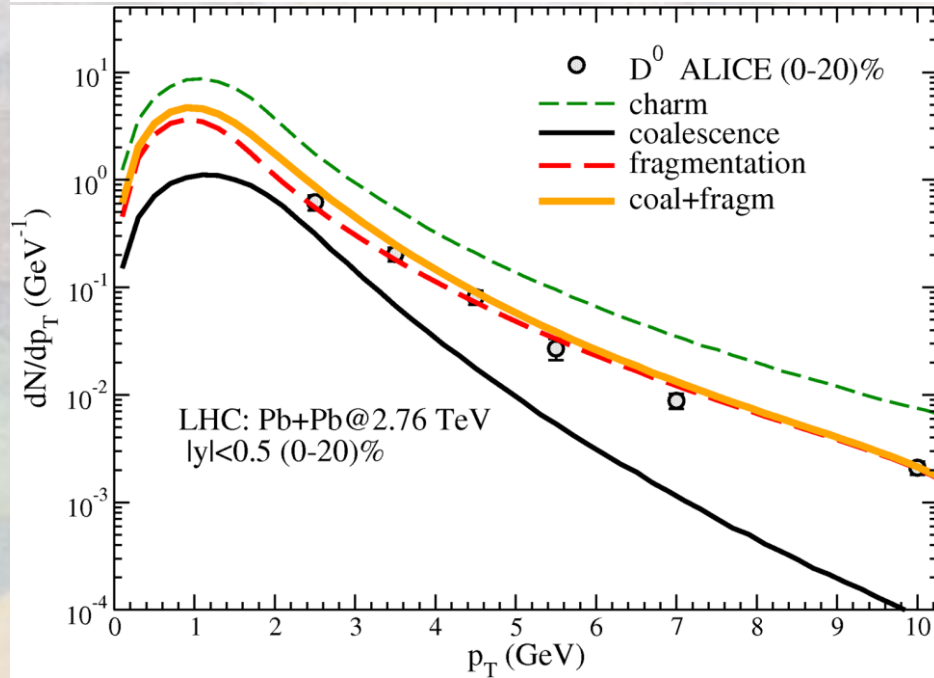
S. Ghosh, S. K. Das, V. Greco, S. Sarkar, J. Alam, PRD90 (2014) no.5, 054018.

S. K. Das, J. M. Torres-Rincon, L. Tolos, V. Minissale, F. Scardina, V. Greco, PRD94 (2016) no.11,114039.

LHC: results

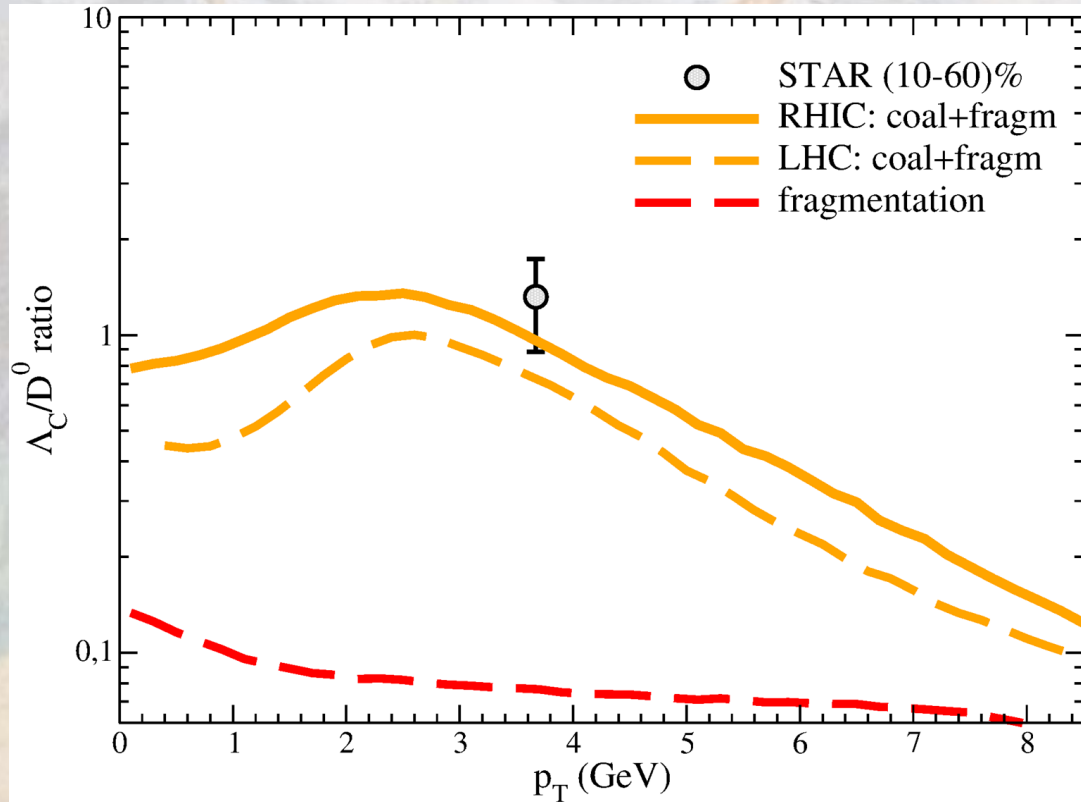
wave function widths σ_p of baryon and mesons are the same at RHIC and LHC!

Data from ALICE Coll. JHEP 1209 (2012) 112



LHC: results

wave function widths σ_p of baryon and mesons are the same at RHIC and LHC!



The Λ_c/D^0 ratio is smaller at LHC energies: fragmentation play a role at intermediate p_T

Conclusions

- ❖ **Good agreement with RHIC and LHC data:**
 - p, π, k, Λ spectra
 - baryon/meson ratio
- ❖ **Heavy Quarks:**
 - Good agreement with experimental data of D^0, D^+, D_s^+ mesons spectra
 - Λ_c production at intermediate p_T dominant role of coalescence mechanism
 - $\Lambda_c/D^0 \sim 1.5$ for $p_T \sim 3$ GeV with Coal.+fragm. model
- ❖ **Extension to study Λ_b and B^0 spectra and their ratio**

The background is a vibrant, abstract painting in a cubist style. It features a variety of geometric shapes and colors including greens, yellows, oranges, blues, and greys. In the upper left, there are stylized white clouds. Below them, a satellite dish is visible on a hill. To the right, there are hints of buildings and more foliage. The overall composition is dynamic and layered.

Backup Slides

Elliptic Flow – Quark Number Scaling

Fourier expansion of the azimuthal distribution

$$f(\varphi, p_T) = 1 + 2 \sum_{n=1}^{\infty} v_n(p_T) \cos n\varphi$$

$n=2$ Elliptic flow

momentum anisotropy in the transverse plane

Assumption

coalescence brings to

$$\begin{aligned} v_{2,M}(p_T) &\approx 2v_{2,q}(p_T/2) \\ v_{2,B}(p_T) &\approx 3v_{2,q}(p_T/3) \end{aligned}$$

Partonic
elliptic flow

Hadronic
elliptic flow

- one dimensional
- Dirac delta for Wigner function
- isotropic radial flow
- not including resonance effect

Baryon to meson ratio

With a partonic thermal distribution

$$f_{th} \approx A e^{-p/T}$$

for a two-quark hadron with coalescence

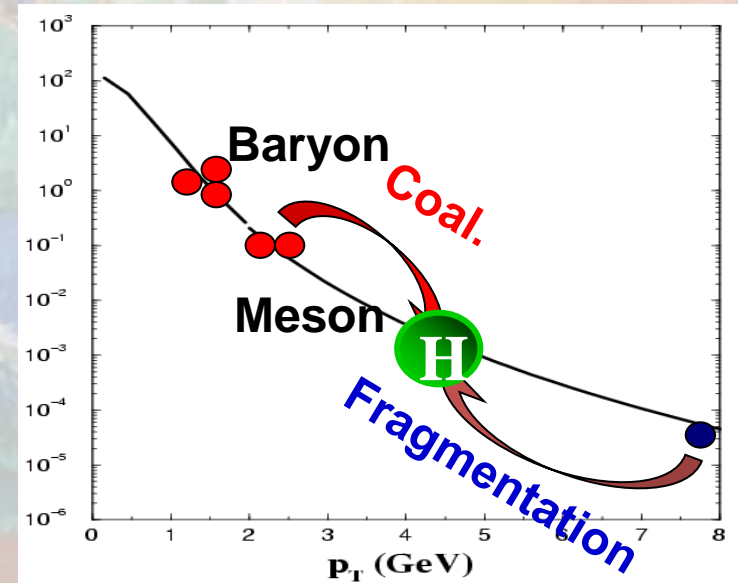
$$e^{-p_1/T} e^{-p_2/T} \Rightarrow e^{-xP/T} e^{-(1-x)P/T} = e^{-P/T}$$

final Hadron momentum

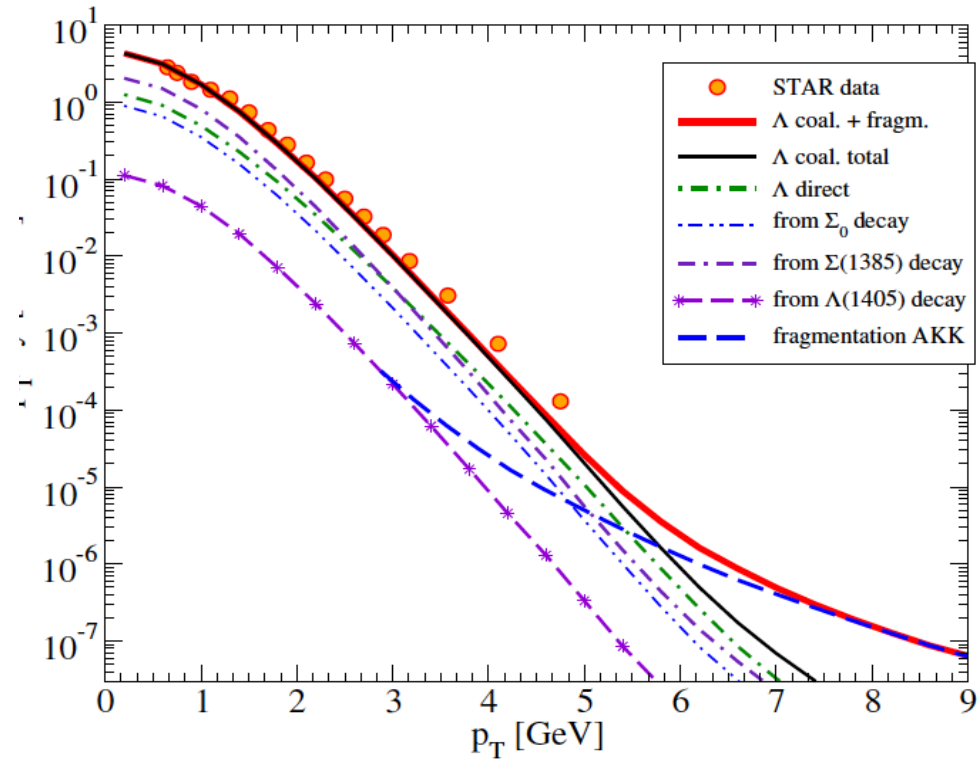
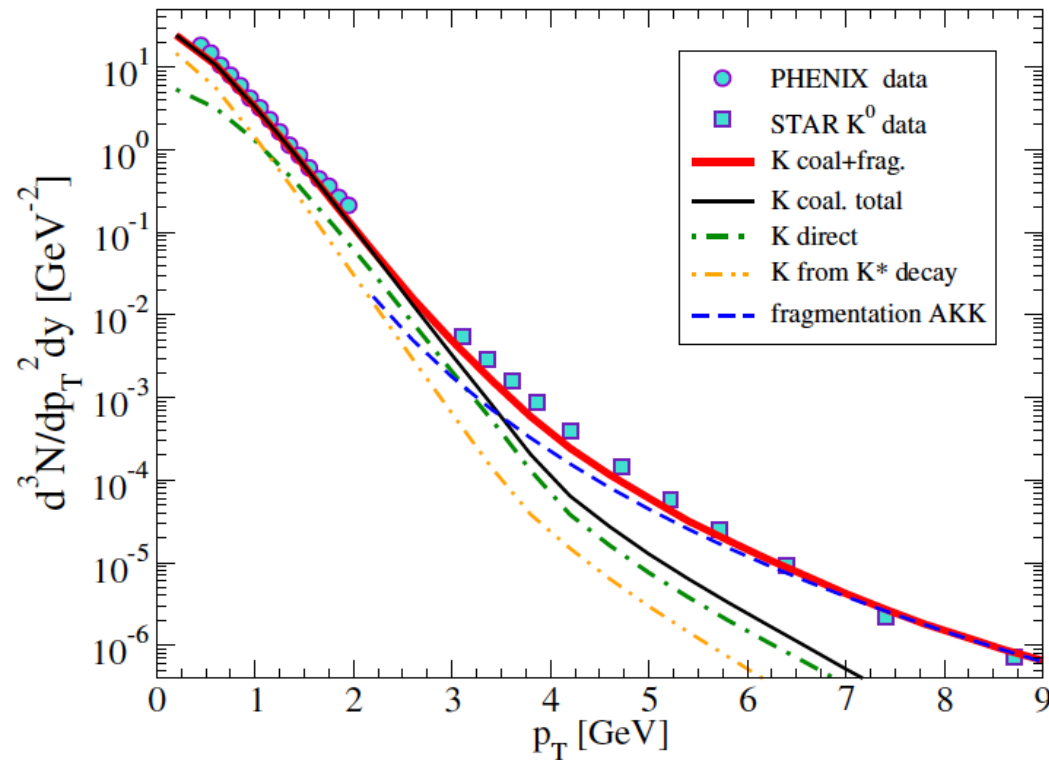
n-quark case

$$\prod_n e^{-p_n/T} \rightarrow e^{-n \frac{P}{nT}} \propto e^{-\frac{P}{T}}$$

Baryon/Meson Ratio = 1

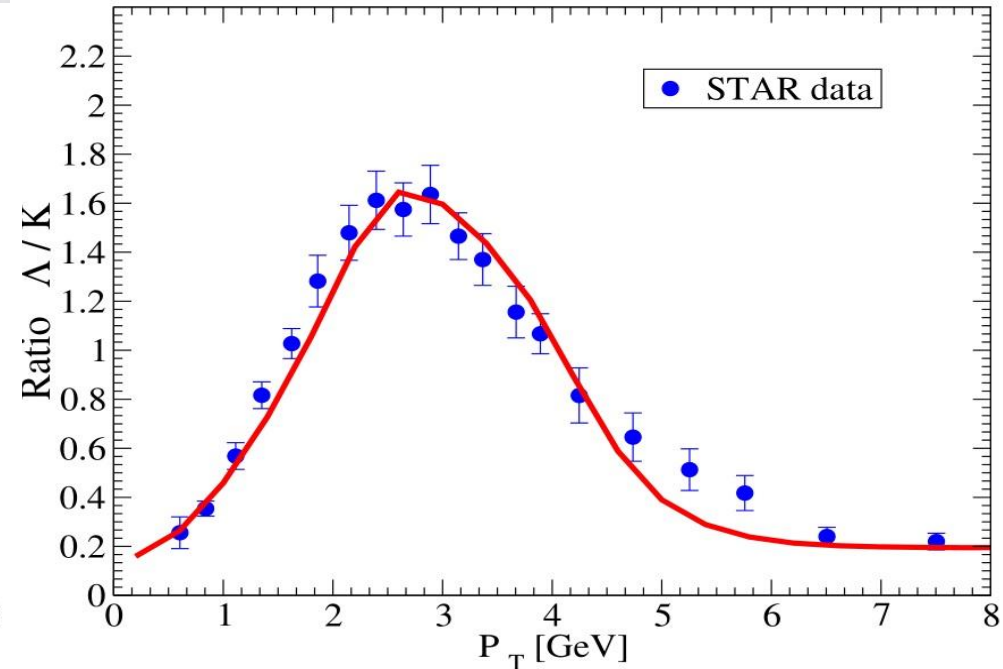
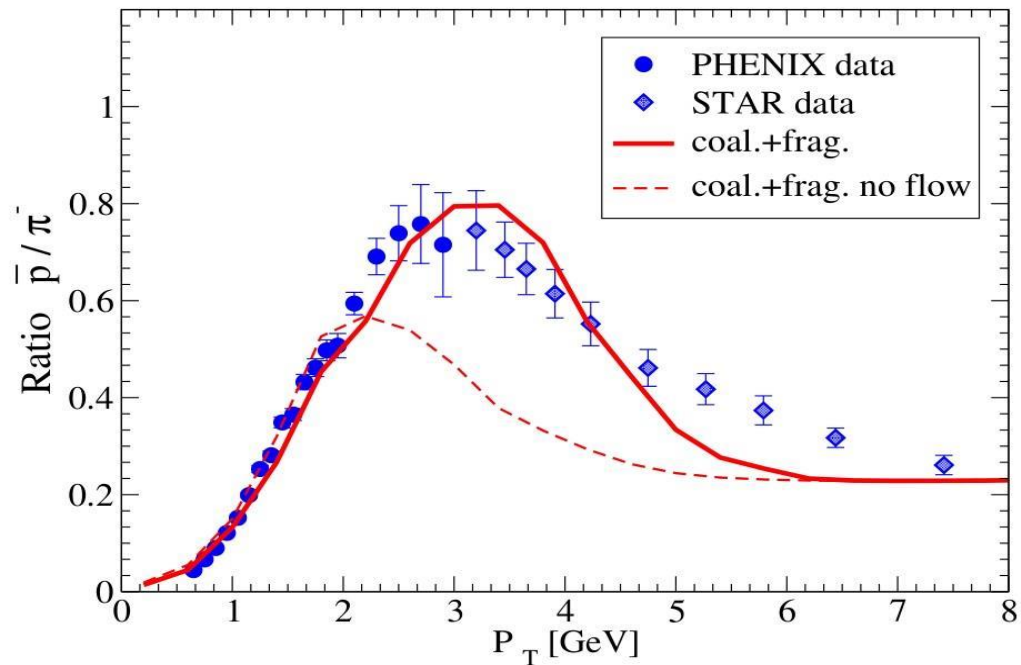


Kaon and Lambda at RHIC



- ❖ For Kaon some lack of yield at $p_T \simeq 4\text{GeV}$ where the fragmentation is starting to be dominant
- ❖ For Λ there are several hadronic states that have a significant contribution

Baryon to meson ratio at RHIC



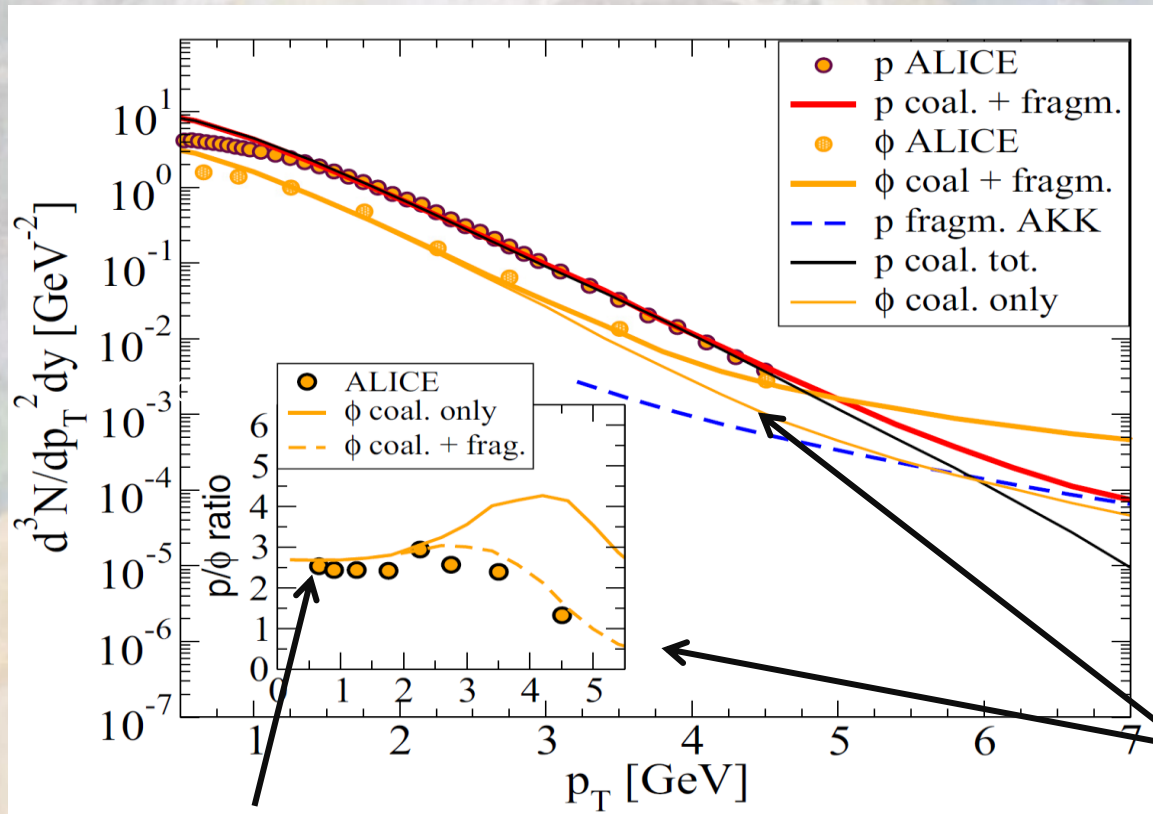
- ✓ coalescence naturally predict a baryon/meson enhancement in the region $p_T \approx 2-4\text{GeV}$ with respect to pp collisions
- ✓ Lack of baryon yield in the region $p_T \approx 5-7\text{GeV}$

LHC: ϕ meson

Discussed question for long time:

ϕ meson behaviour \rightarrow meson-like or mass effect

Coalescence predicts a similar slope for ϕ and p.

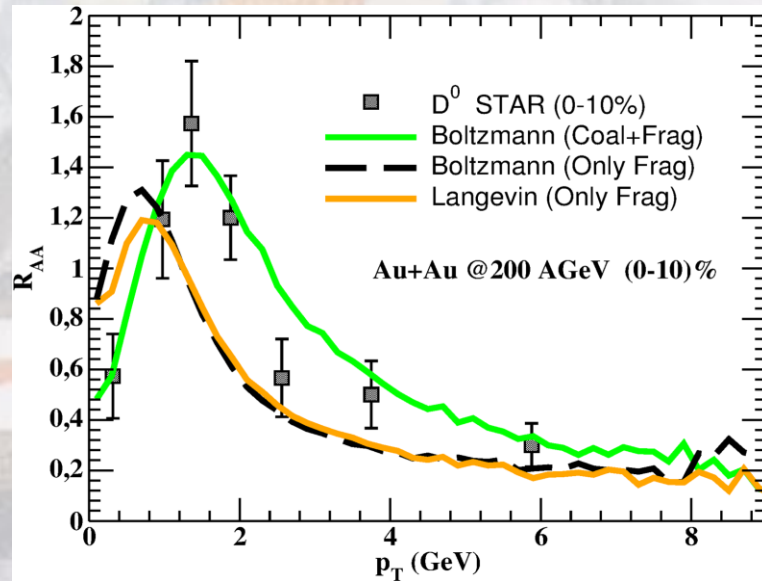


Proton is a combination of 3 quarks flowing each with a mass of about 330 MeV and ϕ is composed by 2 quarks flowing each with a mass of about 550 MeV

Missing fragmentation
Contribution usually
half of the yield at $p_T \approx 4$ GeV

Soft part same
slope ϕ and p

Data from STAR Coll. , PRL 113, 142301 (2014)



- In 0-10% coalescence implies an increase of the R_{AA} for $p_T > 1$ GeV.
- The impact of coalescence decreases with p_T and fragmentation is dominant at high p_T .
- In 0-80% the $v_2(p_T)$ due to only coalescence increase a factor 2 compared to the $v_2(p_T)$ charm.
- In 0-80% coalescence+fragmentation give a good description of exp. data.

Data from STAR Coll. PRL 118, 212301 (2017)

