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in collaboration with:

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About this *exploratory* work:

- ullet Aim 1: explore the possible effects of $ec{B}$ on v_2 at RHIC and LHC energies
- Aim 2: evaluate which are the most significant parameters to focus on
- Aim 3: find constraints on the properties of the medium
- Method: ideal 3D+1 MHD simulations with ECHO-QGP using Glauber i c
- We focus on: impact parameter, σ (σ_{χ}), $T_{f.o.}$
- Strengths: dynamical evolution of the magnetic field coupled with the fluid
- Weaknesses: no resistivity, no charge distinction in produced particles, no hadronic rescattering

What is ECHO-QGP

ECHO-QGP derives from the Eulerian Conservative High-Order astrophysical code for general relativistic magnetohydrodynamics, developed by L. Del Zanna.

(Del Zanna, Zanotti, Bucciantini, and Londrillo, A&A 473 (2007))

A collaboration lead by F. Becattini adapted ECHO-QGP to run second order dissipative hydrodynamical simulations of heavy ion collisions, including the computation of particle spectra following the Cooper-Frye prescription.

Del Zanna, Chandra, Inghirami, Rolando, Beraudo, De Pace, Pagliara, Drago, and Becattini, Eur. Phys. J. C 73 (2013)

Floerchinger, Wiedemann, Beraudo, Del Zanna, Inghirami, Rolando, PLB 735 (2014)

Becattini, Inghirami, Rolando, Beraudo, Del Zanna, De Pace, Nardi, Pagliara, Chandra, Eur. Phys. J. C 75 (2015)

Inghirami, Del Zanna, Beraudo, Haddadi, Becattini, Bleicher, Eur. J. Phys. C 76 (2016)

Website: http://theory.fi.infn.it/echoqgp/

The fundamental equations

Energy and momentum conservation: $d_{\mu}T^{\mu\nu}=0$

Baryonic number conservation: $d_{\mu}N^{\mu} \stackrel{\cdot}{=} 0$

Second law of thermodynamics: $d_{\mu}s^{\mu} \geq 0$

Maxwell equations: $d_{\mu}F^{\mu\nu}=-J^{\nu}\quad (d_{\mu}J^{\mu}=0) \qquad d_{\mu}F^{\star\mu\nu}=0$

The fundamental assumptions

- We neglect all dissipative effects
- We neglect polarization and magnetization effects
- We assume infinite electrical conductivity

The ideal RHMD energy-momentum tensor

Polarization and magnetization neglected

$$\begin{split} T_f^{\mu\nu} &= F^\mu{}_\lambda F^{\nu\lambda} - \tfrac{1}{4} (F^{\lambda\kappa} F_{\lambda\kappa}) g^{\mu\nu} \\ \text{from Maxwell equations: } d_\mu T_{\scriptscriptstyle F}^{\mu\nu} &= J_\mu \, F^{\mu\nu} \end{split}$$

Dissipative effects neglected:

Eckart frame = Landau frame \Rightarrow single fluid u^{μ} $(u_{\mu}u^{\mu}=-1)$

Infinite electrical conductivity

Ohm's law: $J^{\mu} = \rho_{\rm e} u^{\mu} + j^{\mu}; \quad j^{\mu} = \sigma^{\mu\nu} e_{\nu} \Rightarrow e^{\mu} = 0$

Energy-momentum tensor $T^{\mu u}$

$$T^{\mu\nu} = T_m^{\mu\nu} + T_f^{\mu\nu}$$

Matter: $T_m^{\mu\nu} = (e+p)u^{\mu}u^{\nu} + pg^{\mu\nu}$

Electromagnetic field: $T_f^{\mu\nu}=b^2u^\mu u^\nu+\frac{1}{2}b^2g^{\mu\nu}-b^\mu b^\nu$

The energy momentum tensor components

Lorentz transformations from the laboratory to the comoving frame:

$$\begin{array}{l} e^{\mu}=(\gamma v_k E^k, \gamma E^i + \gamma \varepsilon^{ijk} v_j B_k) \\ b^{\mu}=(\gamma v_k B^k, \gamma B^i - \gamma \varepsilon^{ijk} v_j E_k) \text{ where:} \\ \varepsilon_{ijk} \text{ is the Levi-Civita pseudo-tensor of the spatial three-metric} \\ \gamma=\text{Lorentz factor, } g_{ij}=\operatorname{diag}(1,1,1) \text{ or } g_{ij}=\operatorname{diag}(1,1,\tau^2)) \\ e \text{ and } p \text{ are measured in the } comoving \textit{ fluid frame,} \\ \vec{E} \text{ and } \vec{B} \text{ are measured in the } laboratory \textit{ frame} \end{array}$$

Components of the energy-momentum tensor

Energy density
$$\mathcal{E}\equiv -T_0^0=(e+p)\gamma^2-p+\frac{1}{2}(E_kE^k+B_kB^k)$$
 Momentum density $S_i\equiv T_i^0=(e+p)\gamma^2v_i+\varepsilon_{ijk}E^jB^k$ Stresses $T_j^i=(e+p)\gamma^2v^iv_j+(p+\frac{1}{2}(E_kE^k+B_kB^k))\delta_j^i-E^iE_j-B^iB_j$

The evolution equations

Ideal Ohm'law in the laboratory frame

$$e^{\mu} = 0 \Rightarrow E_i = -\varepsilon_{ijk}v^jB^k$$

The evolution equations in conservative form

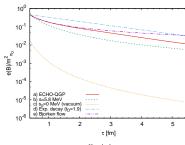
$$\partial_0 \mathbf{U} + \partial_i \mathbf{F}^i = \mathbf{S}$$

where

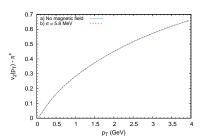
$$\mathbf{U} = |g|^{\frac{1}{2}} \left(\begin{array}{c} \gamma n \\ S_j \equiv T_j^0 \\ \mathcal{E} \equiv -T_0^0 \\ B^j \end{array} \right), \ \mathbf{F}^i = |g|^{\frac{1}{2}} \left(\begin{array}{c} \gamma n v^i \\ T_j^i \\ S^i \equiv -T_0^i \\ v^i B^j - B^i v^j \end{array} \right), \ \mathbf{S} = |g|^{\frac{1}{2}} \left(\begin{array}{c} 0 \\ \frac{1}{2} T^{ik} \partial_j g_{ik} \\ -\frac{1}{2} T^{ik} \partial_0 g_{ik} \\ 0 \end{array} \right)$$

Time evolution of the magnetic field at the center of the grid

Eur. J. Phys. C 76 (2016) 2D+1 simulation of Au+Au collision at $\sqrt{s}_{\mathrm{NN}}=200\,\mathrm{AGeV}$

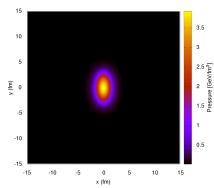


Magnetic field at x=y=0



Elliptic flow of positive pions

New 3D+1 simulations: initial conditions for pressure



Thermal pressure at $\tau=0.4\,\mathrm{fm/c}$, Au+Au collision at $\sqrt{s}_\mathrm{NN}=200\,\mathrm{AGeV}$ impact parameter b=12 fm.

3D+1 simulation in Milne coordinates Geometrical Glauber initial conditions. Almost all parameters as in:

Pang et al. - Phys. Rev. C 93, 044919

Parameter	RHIC	LHC
lon	Au 197	Pb 208
$\sqrt{s}_{\mathrm{NN}} \; (AGeV)$	200	2760
$ au_0 \; ({ m fm/c})$	0.4	0.2
$T_{f.o.}$ (MeV)	154	154
$\epsilon_0 \; ({\rm GeV/fm^3})$	55	413.9
$\sigma_{in.}$ (mb)	42	64
$\alpha_{bin.coll.}$	0.05	0.05
η_{flat}	5.9	7.0
σ_{η}	0.4	0.6

Initial conditions for \vec{B} : basic formula for point charge

Li, Sheng and Wang, Phys. Rev. C 94, 044903 (2016)

$$B_{\phi}(t, \mathbf{x}) = \frac{Q}{4\pi} \cdot \frac{v\gamma x_{T}}{\Delta^{3/2}} \left(1 + \frac{\sigma v\gamma}{2} \sqrt{\Delta} \right) e^{A},$$

$$B_{r}(t, \mathbf{x}) = -\sigma_{\chi} \frac{Q}{8\pi} \cdot \frac{v\gamma^{2} x_{T}}{\Delta^{3/2}} \cdot \left[\gamma (vt - z) + A\sqrt{\Delta} \right] e^{A},$$

$$B_{z}(t, \mathbf{x}) = \sigma_{\chi} \frac{Q}{8\pi} \cdot \frac{v\gamma}{\Delta^{3/2}}.$$

$$\left[\gamma^{2} (vt - z)^{2} \left(1 + \frac{\sigma v\gamma}{2} \sqrt{\Delta} \right) + \Delta \left(1 - \frac{\sigma v\gamma}{2} \sqrt{\Delta} \right) \right] e^{A}$$

where: σ is the electric conductivity, σ_{χ} the chiral magnetic conductivity,

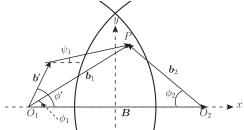
$$\Delta \equiv \gamma^2 (vt - z)^2 + x_T^2$$
, $A \equiv (\sigma v \gamma / 2) [\gamma (vt - z) - \sqrt{\Delta}]$

Our initial conditions: formula for two colliding nuclei

The nuclei freely propagate into a medium with finite conductivity, before and after the collision. For each of them (uniformly charged disk approximation):

$$B_Z(x_-,b_1) = \int 2\sqrt{R_A^2 - b'^2} \rho B(x_-,|b_1 - b'|) (-\sin\psi_1 \hat{\boldsymbol{x}} + \cos\psi_1 \hat{\boldsymbol{y}}) d^2b \quad (1)$$

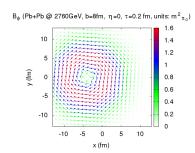
A similar expression holds for the other nucleus and the total magnetic field is the sum of the two.



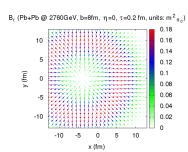
Tuchin - Phys. Rev. C 88 (2013)

Orientation of the magnetic field

Magnetic field of a lead ion at LHC energy.

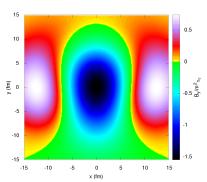


Magnetic field of <code>classic</code> origin, at $au=0.2\,\mathrm{fm/c},\;\eta=0$, <code>b=8 fm,</code> $\sigma=5.8\,\mathrm{MeV}$

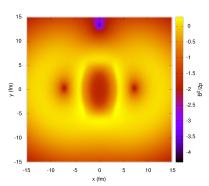


Magnetic field of *chiral* origin, at $\tau = 0.2\,\mathrm{fm/c},\; \eta = 0,\; \mathrm{b=8}\;\mathrm{fm},\\ \sigma_\chi = 1.5\,\mathrm{MeV}\\ (\nabla\!\cdot\!\vec{B} = 0\colon B_z \neq 0\;\mathrm{not\;plotted}\;!)$

3D+1 simulation of Au+Au collision at $\sqrt{s}_{\rm NN}=200\,{\rm AGeV}$ Conductivities of the medium ($\tau\leq\tau_0$): $\sigma=5.8\,{\rm MeV},\,\sigma_\chi=1.5\,{\rm MeV}$

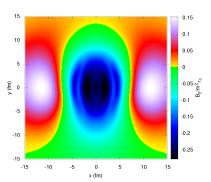


 B_u at $au=0.4\,\mathrm{fm/c}$ and $\eta=0$

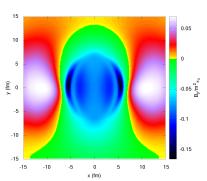


Magnetic/thermal pressure ratio

Magnetic field at later times

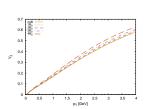


RHIC energy, b=12 fm, $\tau = 2\,\mathrm{fm/c}$

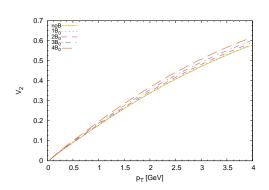


RHIC energy, b=12 fm, $\tau = 4\,\mathrm{fm/c}$

Importance of the initial B magnitude

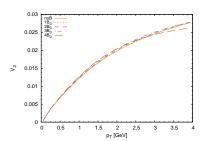


RHIC energy, b=12 fm

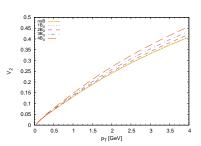


LHC energy, b=12 fm

v2 at different impact parameters

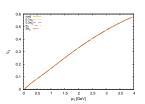


RHIC energy, b=2 fm

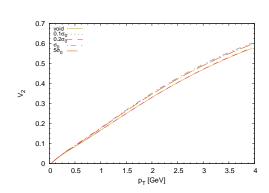


RHIC energy, b=8 fm

Impact of the initial conductivity



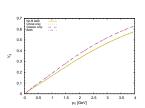
RHIC energy, b=12 fm



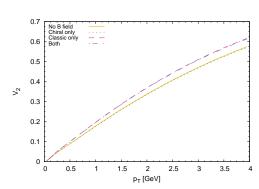
RHIC energy, b=12 fm, $B_{in.}=3B_0$ Preliminary results, to be checked!

Separate effects of classic/chiral contribution

The magnetic field of chiral origin seems to play only a minor role (we are neglecting the dynamical evolution of axial currents).



RHIC energy, b=12 fm, $B_{in} = 4B_0$



LHC energy, b=12 fm, $B_{in} = 4B_0$

Final comments

- ullet The impact of $ec{B}$ on v_2 seems to be limited both at RHIC and LHC
- However, the many uncertainties in the pre-equilibrium phase might have led to an underestimate of the initial $ec{B}$ field
- In this case, the magnetic field might produce an enhancement of v_2 in peripheral collisions
- But probably resistivity and viscosity strongly suppress this effect
- And hadronic rescattering might make measurements more difficult
- Moreover, assuming an initial null velocity field is a rough. approximation
- Anyway, the basic MHD assumption $e^{\mu} = 0$ is not realistic: arXiv:1803 06695
- Moreover, we have seen in the talk by N.Tanji that $\mathbf{E} \cdot \mathbf{B} \neq 0$
- Eventually, taking into account EM fields in the Cooper-Frye (arXiv:1705.07842) prescription requires to go beyond ideal MHD

Future perspectives

- Ongoing collaboration (also with M. Kaminski) to include resistivity and dynamical evolution of axial charges (formalism almost completed by Y. Hirono, however numerical implementation might be challenging)
- Event by event simulations coupled with UrQMD (hadronic rescattering, resonances decay)
- Use of the γ correlator or the brand new $R_{\Psi_m}(\Delta S)$ (see R. Lacey's talk)
- Comparisons with \vec{B} estimates based on $\Lambda \bar{\Lambda}$ polarization splitting (see M. Lisa's talk)
- Connections with lattice QCD results (see M. D'Elia's talk)