

D-brane Instanton Effects in String Theory



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Veneziano amplitude at 50

$$A(s, t, u) = \frac{\sqrt{\beta}}{\pi} \left[B(1-\alpha(t), 1-\alpha(s)) + B(1-\alpha(t), 1-\alpha(u)) + B(1-\alpha(s), 1-\alpha(u)) \right] \quad (3)$$

where we have introduced the Euler β -function $B(x, y) = \frac{\Gamma(x)\Gamma(y)}{\Gamma(x+y)}$.



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- Yet physics is non-perturbative
 - QCD, SYM  Veneziano-Yankielowicz
- String theory beyond perturbation theory: dualities & branes
- Focus on brane instantons

Instantons in string theory

- Instantons, saddle points of euclidan theory, a useful object in non-perturbative physics

BPST; 't Hooft

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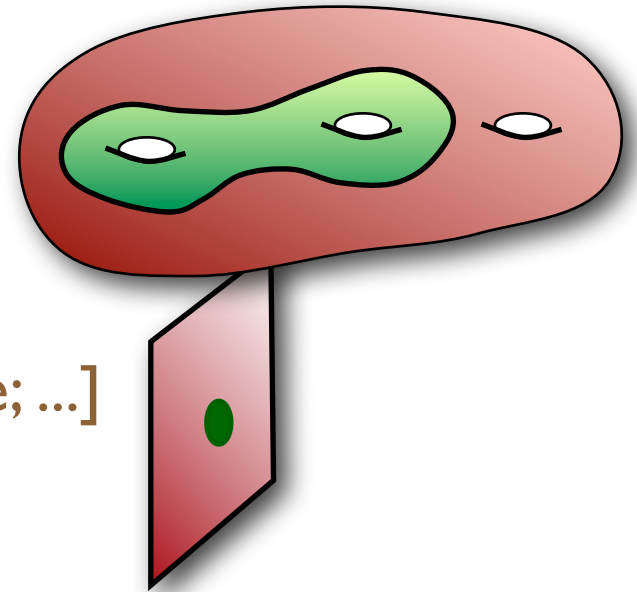
- In string theory, extended objects wrapped on extra dimensions

Worksheet instantons: pert in g_s

Brane instantons: non-pert in g_s

[Becker's, Strominger; Witten; Harvey, Moore; ...]

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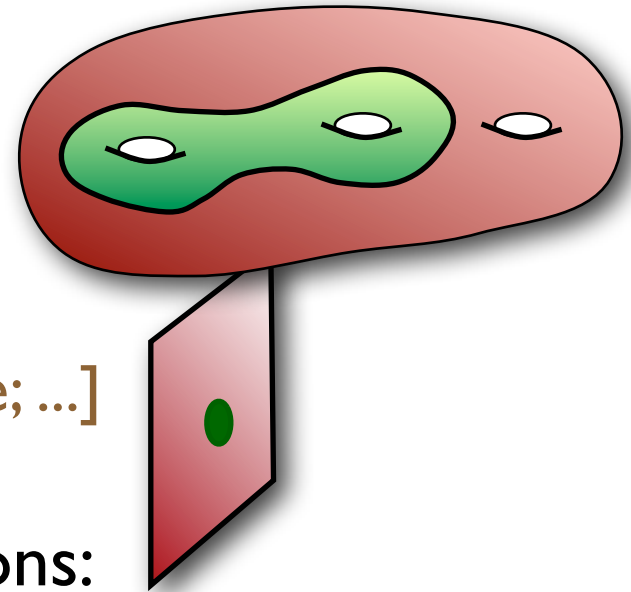
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A unified story Witten '95



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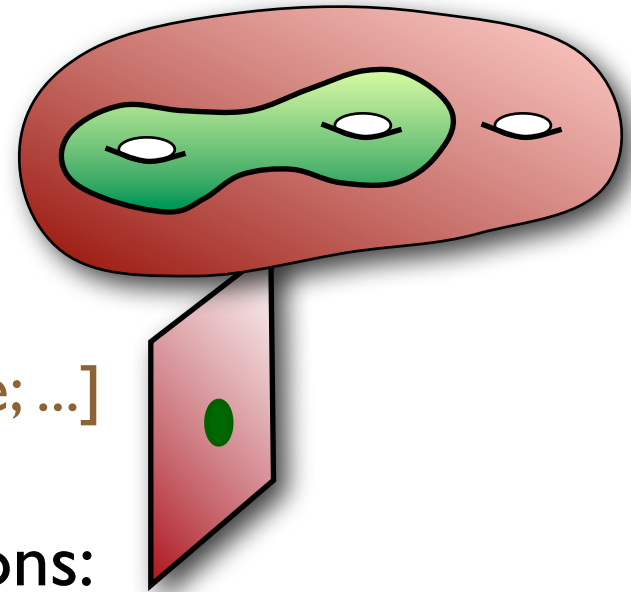
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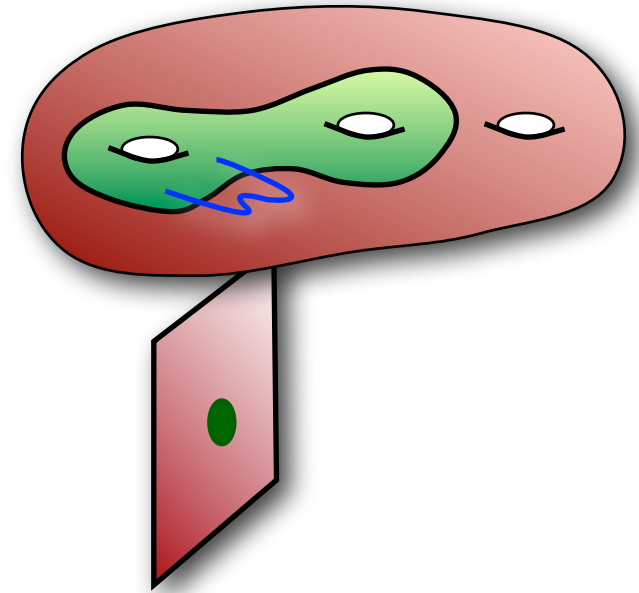
- Focus on D-brane instantons, exploit open string description

Polchinski '95



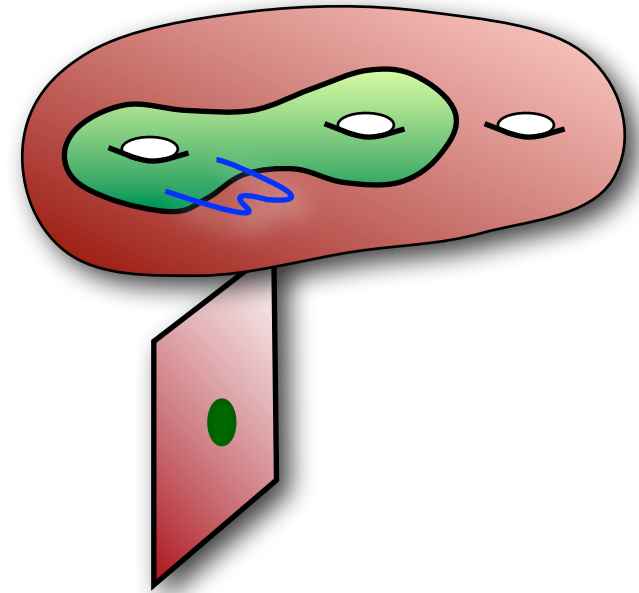
D-brane instantons

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D-brane instantons

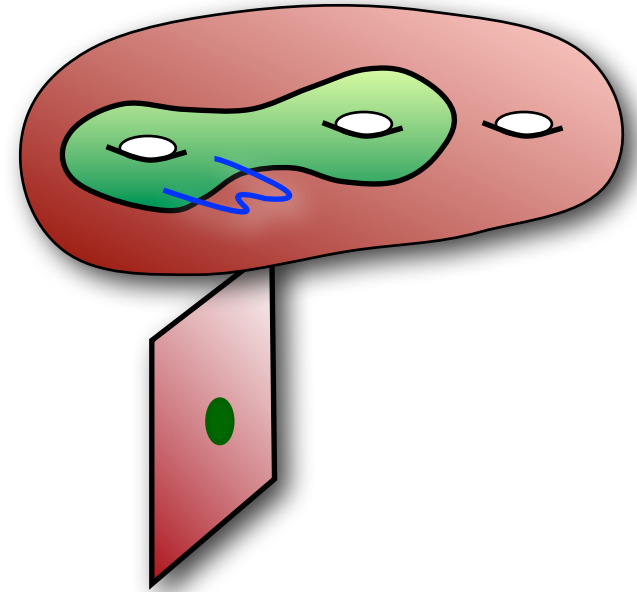
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 - neutral fermionic: type of 4d terms
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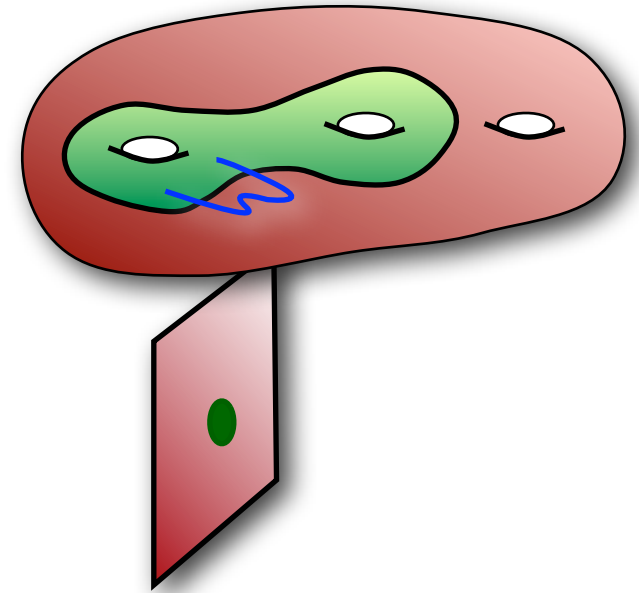
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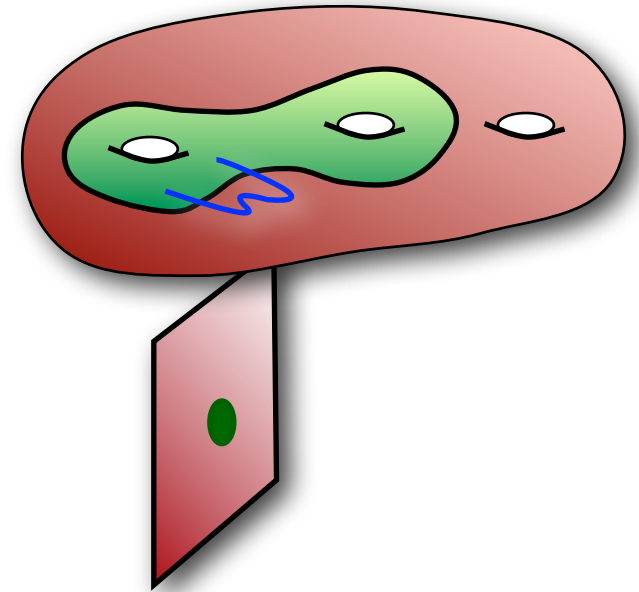
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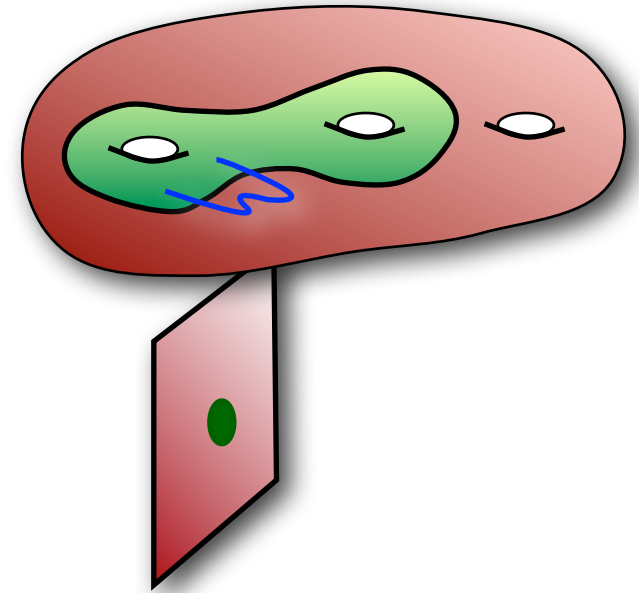
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- Tons of applications



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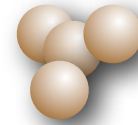
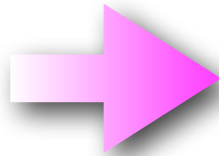
Particle loop in S^1 compactification = Tower of instantons in “T-dual”



underlies many recent proposals e.g. WGC for instantons

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Particle loop in S^1 compactification = Tower of instantons in “T-dual”



- M-th on $T^2 \Rightarrow$ 10d type IIB R^4 terms
Green, Gutperle, Vanhove
- M5-brane on $T^2 \Rightarrow$ D3-brane R^2 terms
Bachas, Bain, Green
- M-th on $CY_3 \times S^1 \Rightarrow$ A-model topological string
Gopakumar, Vafa
- M-th on $CY_3 \times S^1 / Z_2 \Rightarrow$ unoriented A-model
Piazzalunga, AU
- IIB on conifold $\times S^1 \Rightarrow$ D2-brane instantons on conifold
Ooguri, Vafa
- 5d QFT on $S^1 \Rightarrow$ Seiberg Witten
Nekrasov
- 4d QFT on $S^1 \Rightarrow$ Wall-crossing
Gaiotto, Moore, Neitzke
- M-th on $CY_3 \times T^2 \Rightarrow$ (p,q) string instantons
Collinucci, Soler, AU
- HW on $K3 \times S^1 \Rightarrow$ D7-brane R^4 terms
Petersson, Soler, AU
- ...

Applications: Pheno. Moduli

- Parameters in the compact geometry are 4d moduli fields

Phenomenological disaster!

5th forces, cosmological problems,...

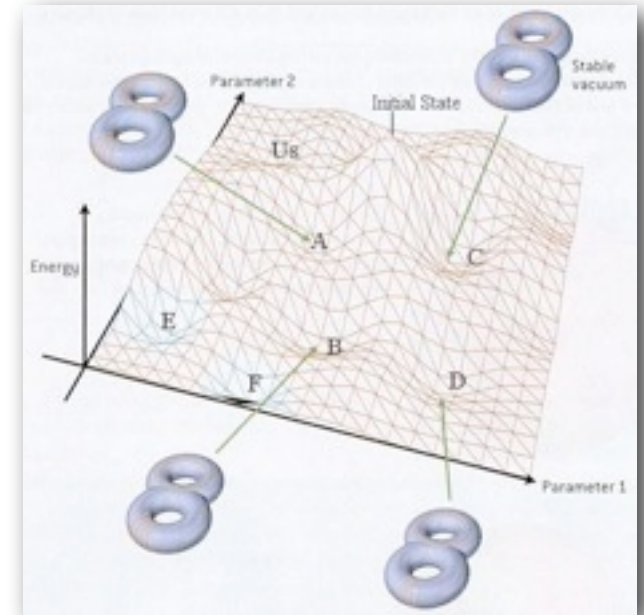
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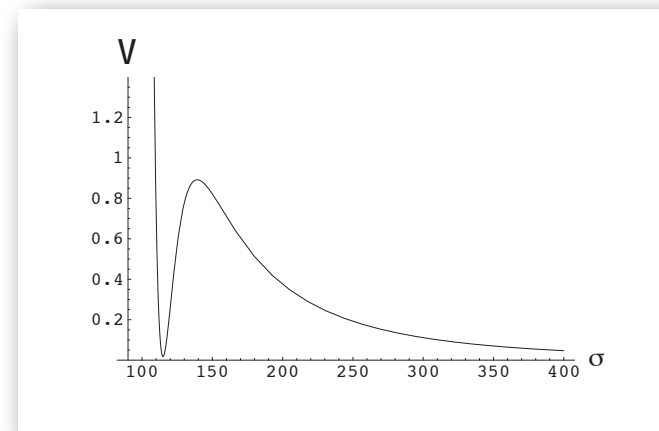
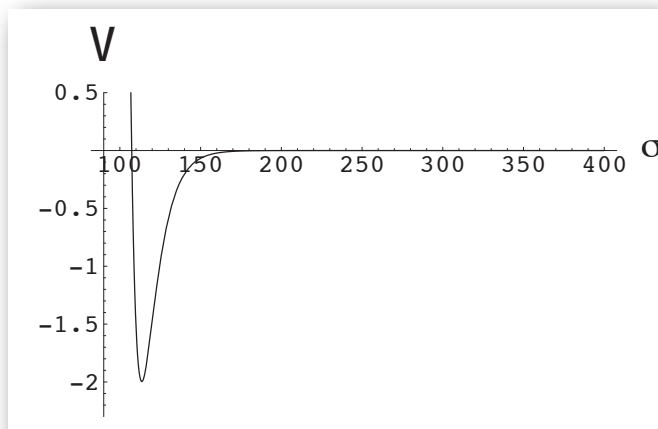
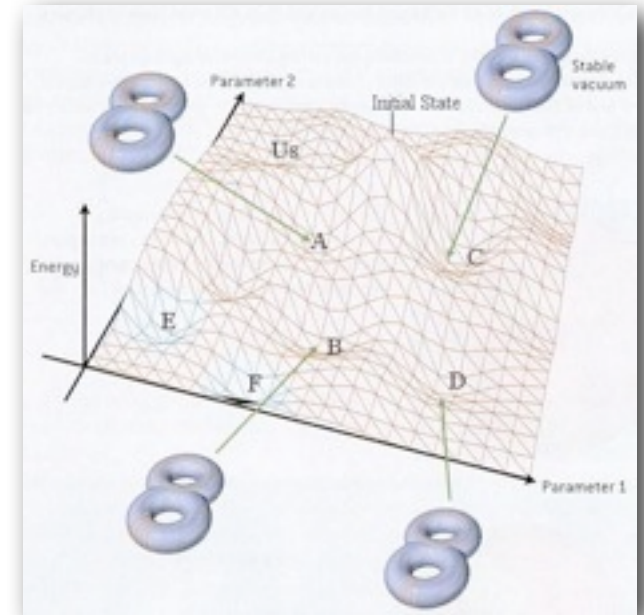
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- Contemplate instanton effects

KKLT; Large volume [Quevedo et al], ...

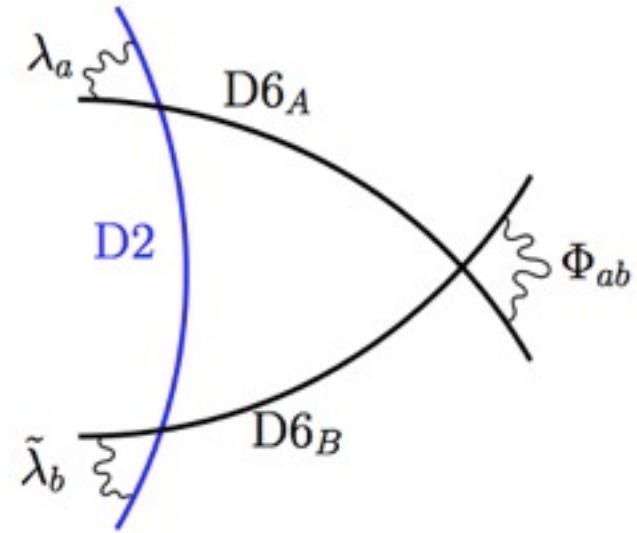


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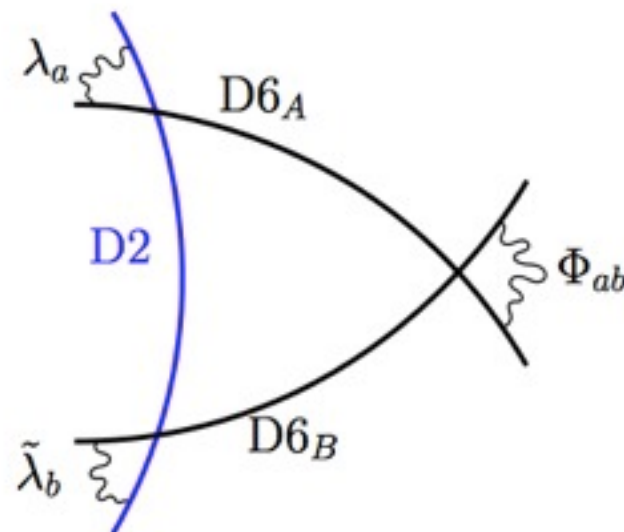


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- Integration over instanton fermion zero modes leads to insertions of charged 4d fields

$$W_{\text{inst}} = \Phi_1 \dots \Phi_n e^{-U}$$

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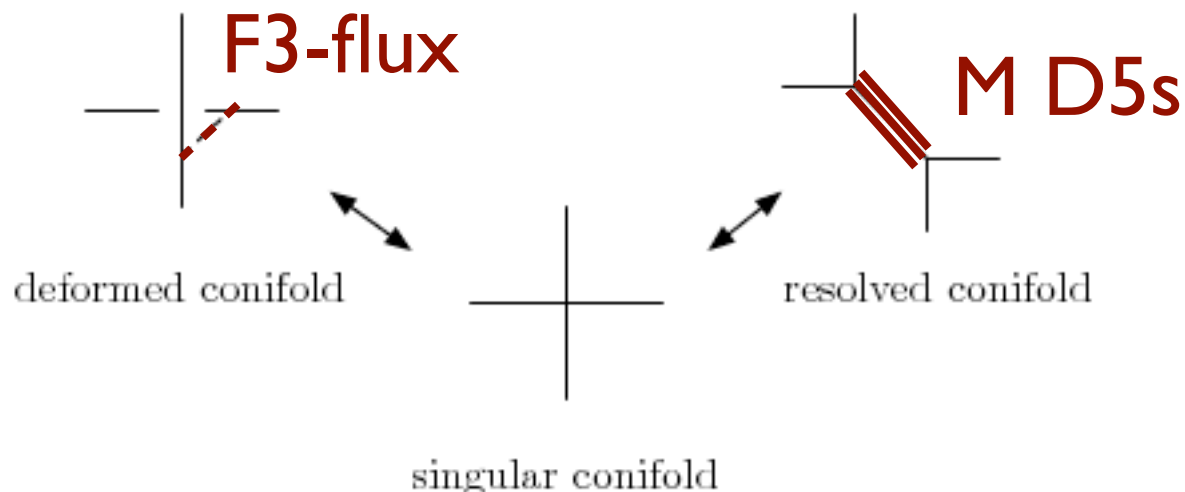
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Non-perturbative SYM condensate in terms of dual deformed geometry

e.g. Klebanov, Strassler



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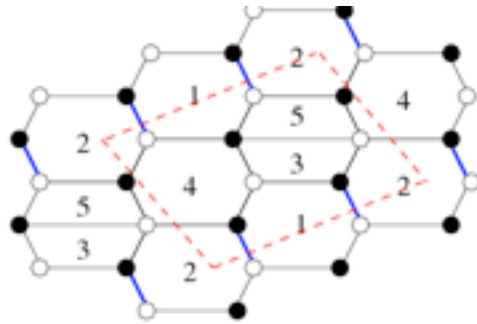
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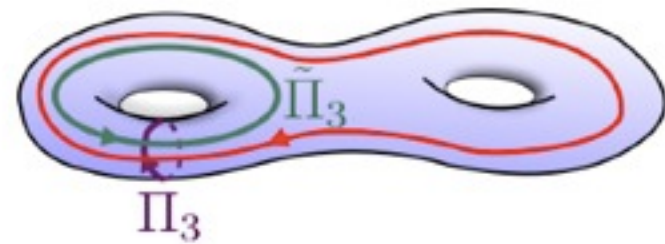
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- Fairly explicit in systems of D3 at CY3 toric singus

Brane tiling



Mirror



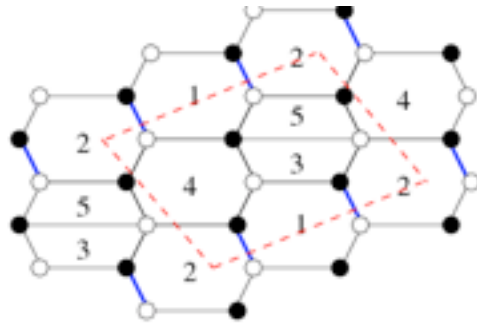
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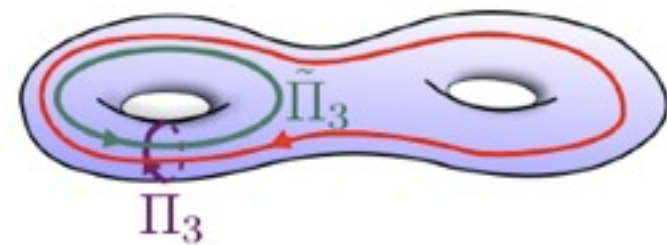
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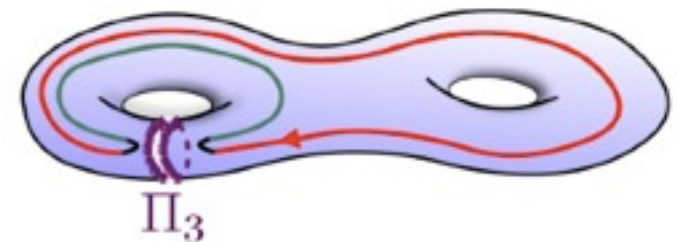
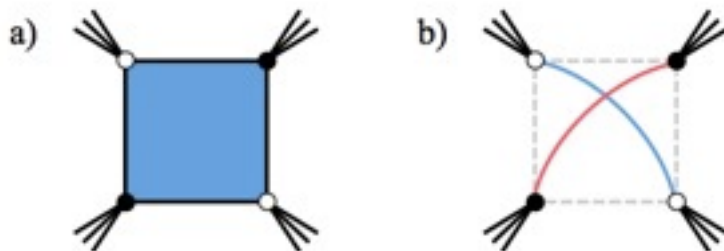
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Instantons + backreaction



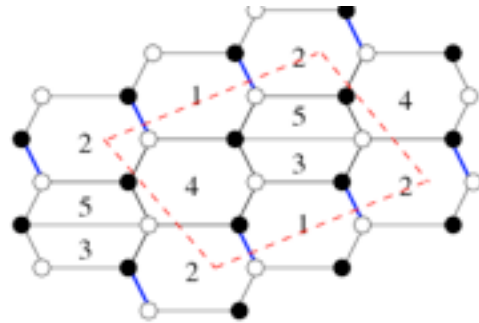
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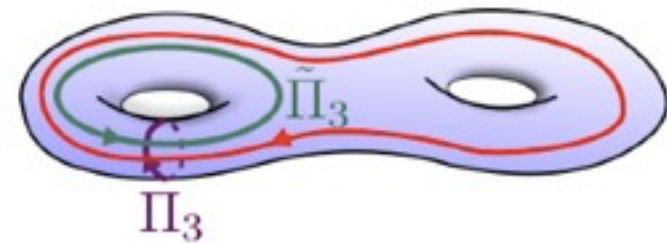
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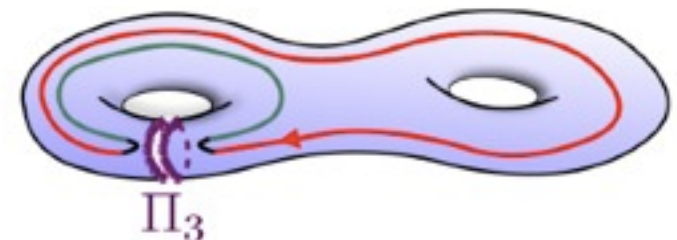
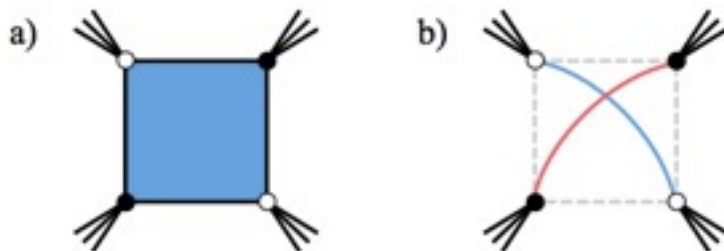
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Result in geometries associated to higher-genus bipartite graphs

introduced by Arkani-Hamed et al; Franco et al

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